

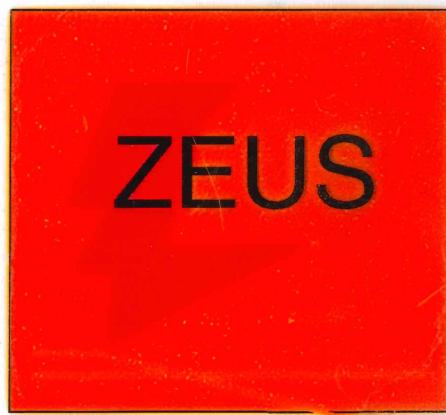
Dedicated to the memory of Bjoern Wiik

# ep Cross Sections and Proton Structure Functions at HERA

Bruno Stella

(Roma III Univ. and INFN )

on behalf of



Les Rencontres de Physique de la Vallée d'Aoste  
RESULTS AND PERSPECTIVES IN PARTICLE PHYSICS

LaThuile, 2 March 1999

# Selected results on $e^+p$ , $e^-p$ DIS

Introduction  
 $F_2(x, Q^2)$

'94 - '97 :

The longitudinal structure function  $F_L$

Charm contribution to  $F_2$  ( $F^c$ )

Gluon density in the proton

High  $Q^2$  Neutral Currents interactions

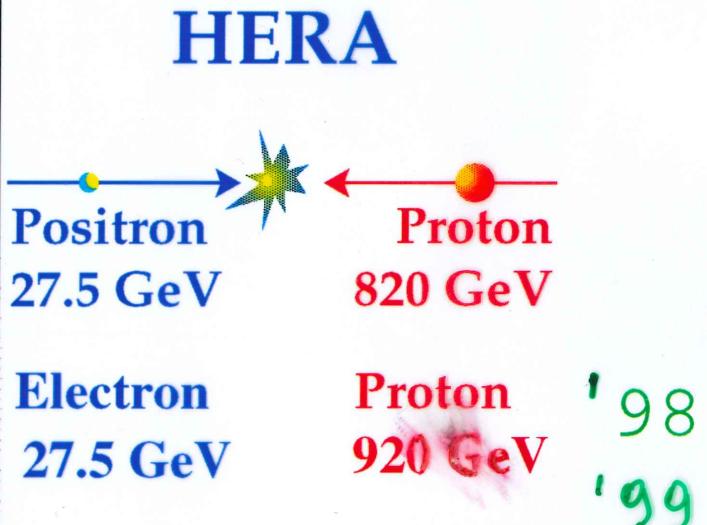
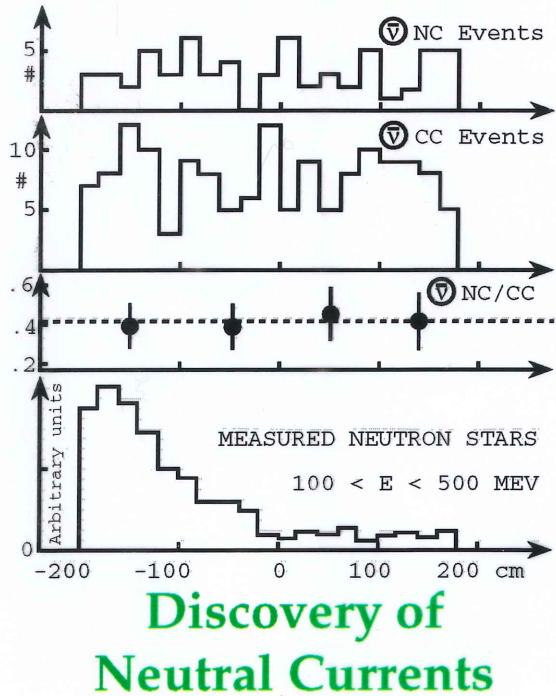
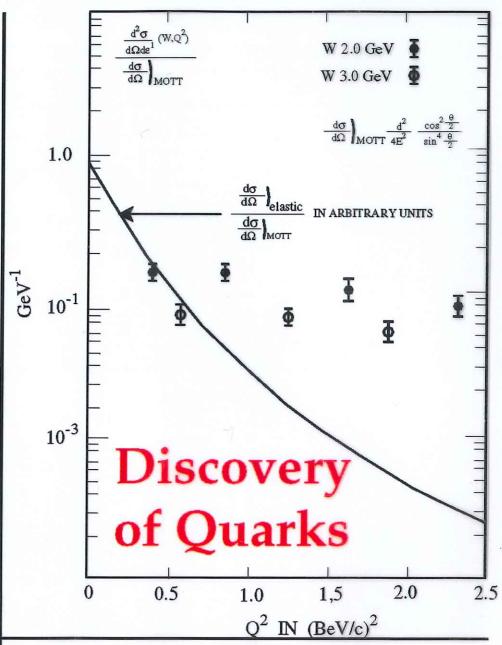
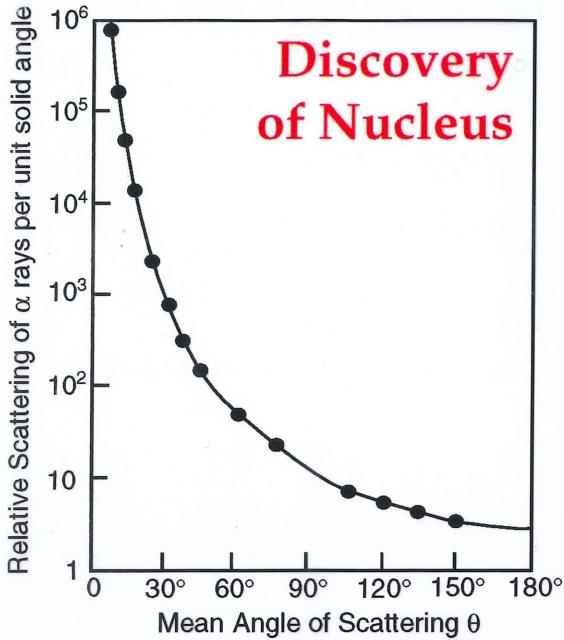
High  $Q^2$  Charged Currents interactions

Running '98 – '99

Future of HERA

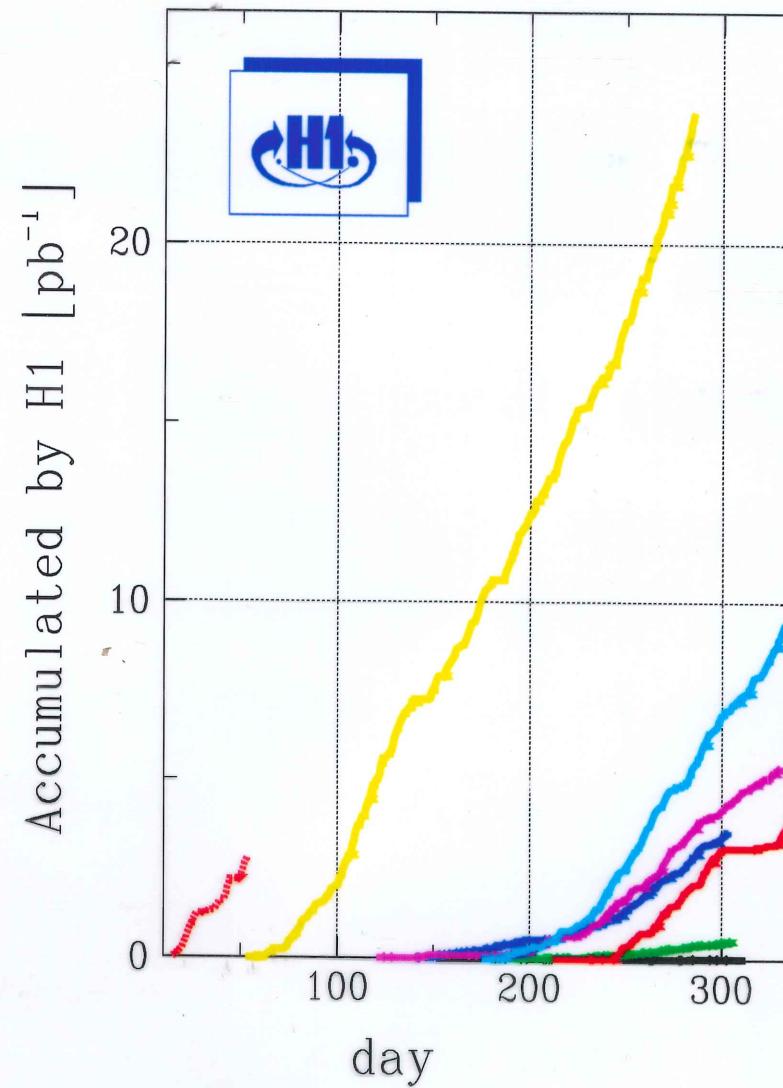
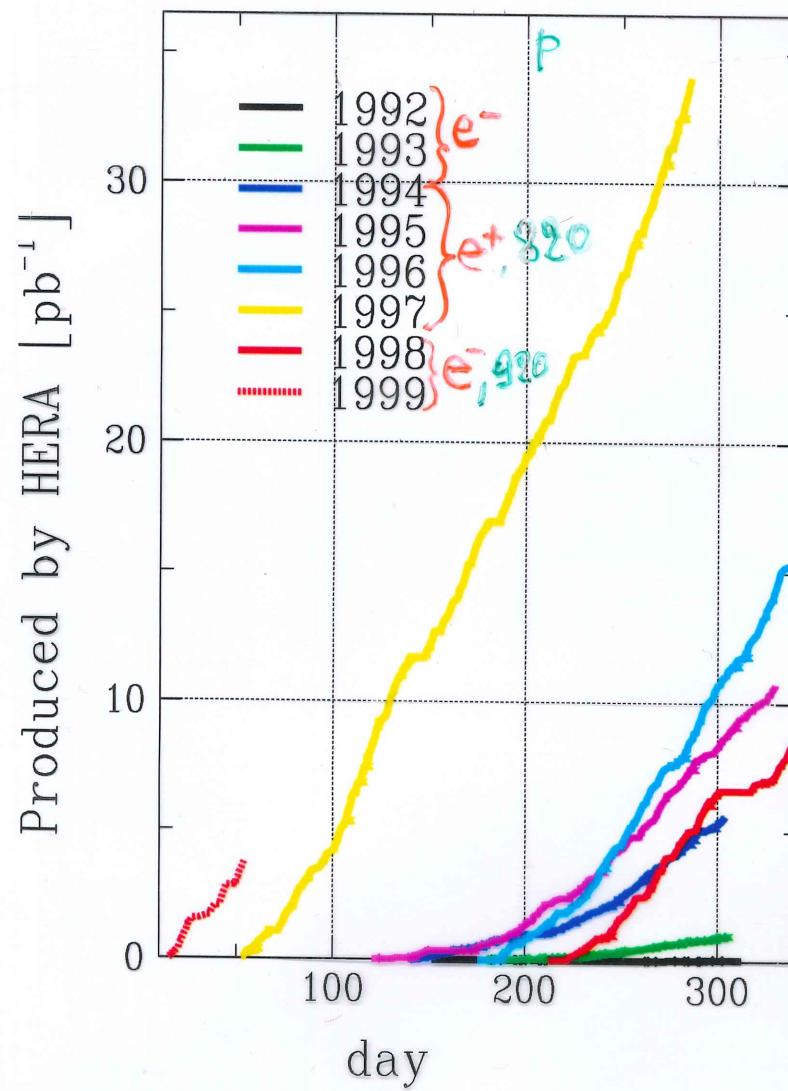
# D.I.Scovery Potential

- Historical Perspective



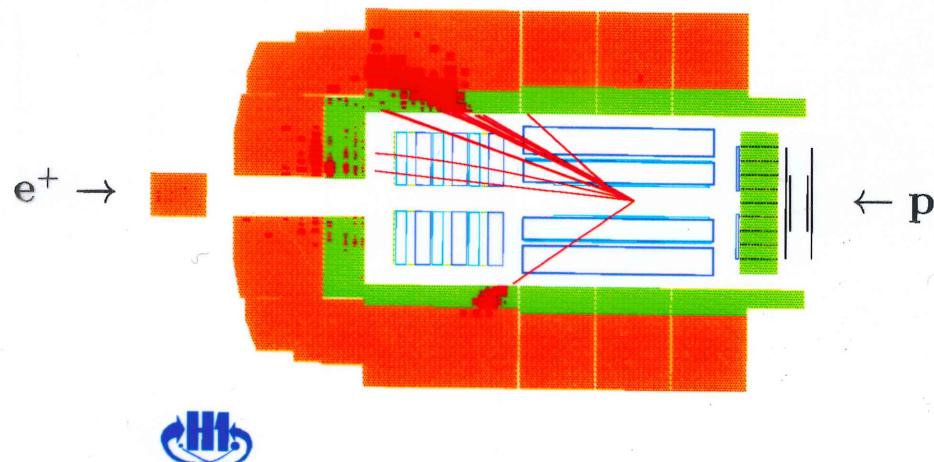
Geiger and Marsden; Proc. Roy. Soc. Lxxxi P. 495 (1909)  
 Friedman, Kendall, Taylor; Rev. Mod. Phys. 63(3) (1991)

# INTEGRATED LUMINOSITY



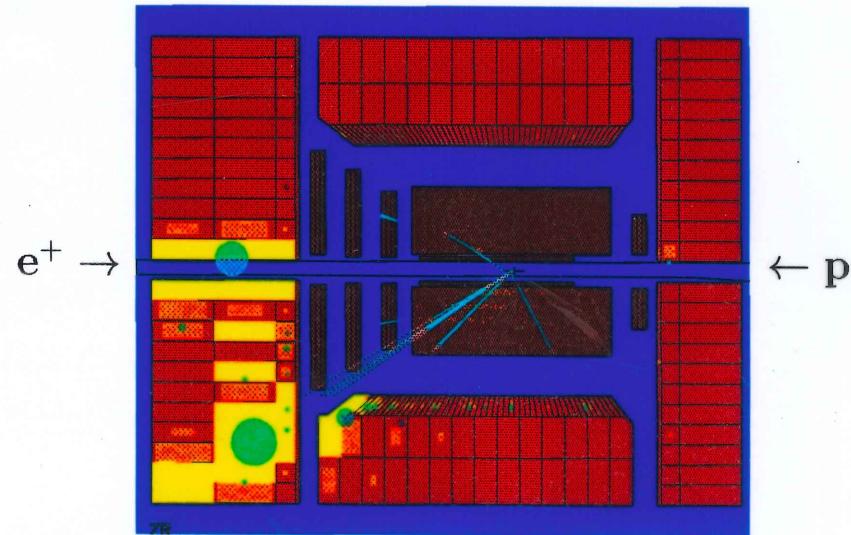
## H1 Detector

Neutral Current Event:  $e^+ p \rightarrow e^+ X$   
 $Q^2 = 17000 \text{ GeV}^2, x = 0.43, E'_e = 170 \text{ GeV}$



## ZEUS Detector

Charged Current Event:  $e^+ p \rightarrow \bar{\nu} X$   
 $Q^2 = 17200 \text{ GeV}^2, x = 0.34, p_t = 86 \text{ GeV}$



## Liquid Argon Calorimeter

44000 Cells

$\sigma_{\theta_e} = 2.5 \text{ mrad}$

$\sigma/\sqrt{E} (\text{e}) = 12 \%$

$\sigma/\sqrt{E} (\text{had}) = 50 \%$

$\Delta E/E (\text{syst}) = 3 \%$

## Uranium-Scintillator Calorimeter

6000 Cells, each read out by 2 PMTs

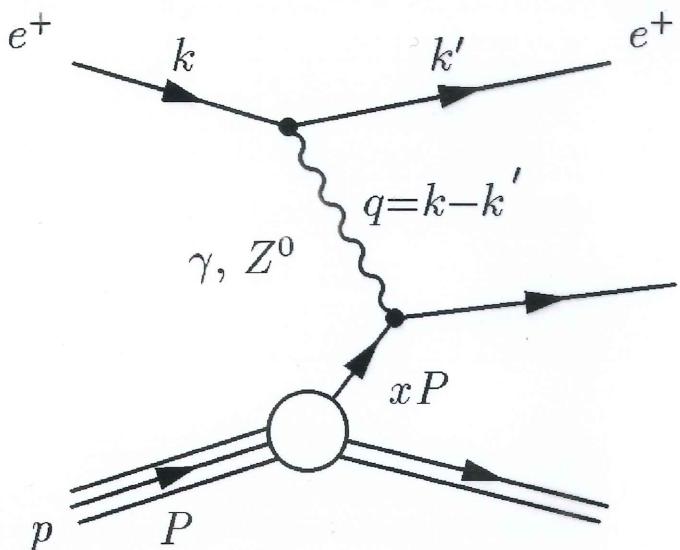
$\sigma_{\theta_e} = 5 \text{ mrad}$

$\sigma/\sqrt{E} (\text{e}) = 18 \%$

$\sigma/\sqrt{E} (\text{had}) = 35 \%$

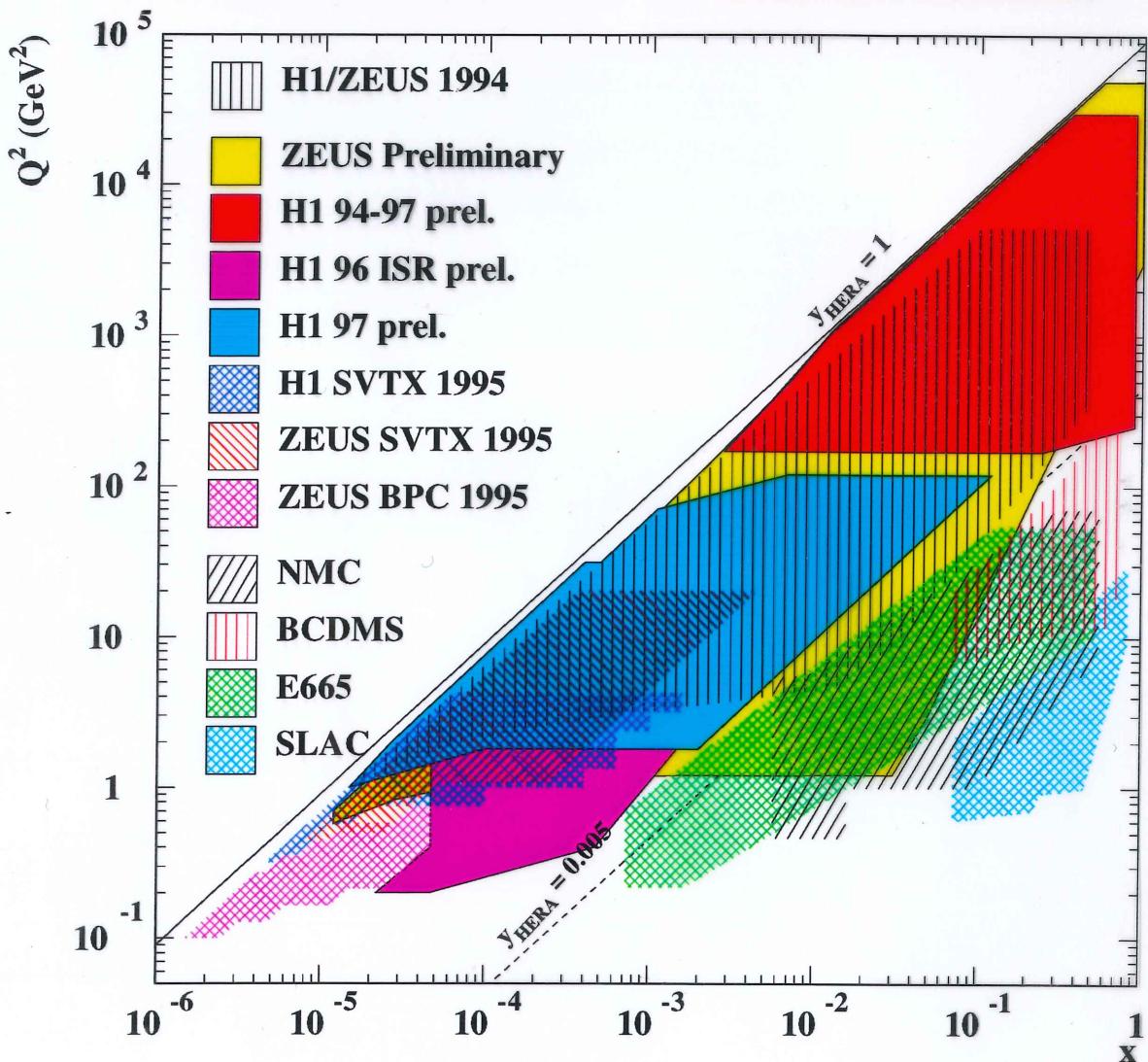
$\Delta E/E (\text{syst}) = 3 \%$

## DIS Kinematics



- $Q^2 = -q^2 = -(k - k')^2$   
4-momentum transfer squared
- $x = Q^2 / (2P \cdot q)$   
parton momentum fraction
- $y = (P \cdot q) / (P \cdot k)$   
inelasticity
- $s = (k + P)^2$   
total energy squared
- $W^2 = (P + q)^2$   
hadronic mass squared
- $Q^2 \approx sxy$       Quasi-two body kin.: only 2 indep. var.

# HERA Kinematic Range



$Q^2 \rightarrow 0$  :

transition to  $\gamma p$

$Q^2 \rightarrow s$  :

electro-weak unification, substructure

$y \rightarrow 1$  :

sensitivity to  $F_L$

$y \rightarrow 0.005$  :

overlap with fixed target experiments

$x \rightarrow 1$  :

probe valence quarks at high  $Q^2$

Probe proton structure  
down to  $\boxed{1/1000} r_p$   
 $(Q^2 > 40.000 \text{ GeV}^2)$

and at very high number  
of partons for very short time  
(very high  $1/x$ )

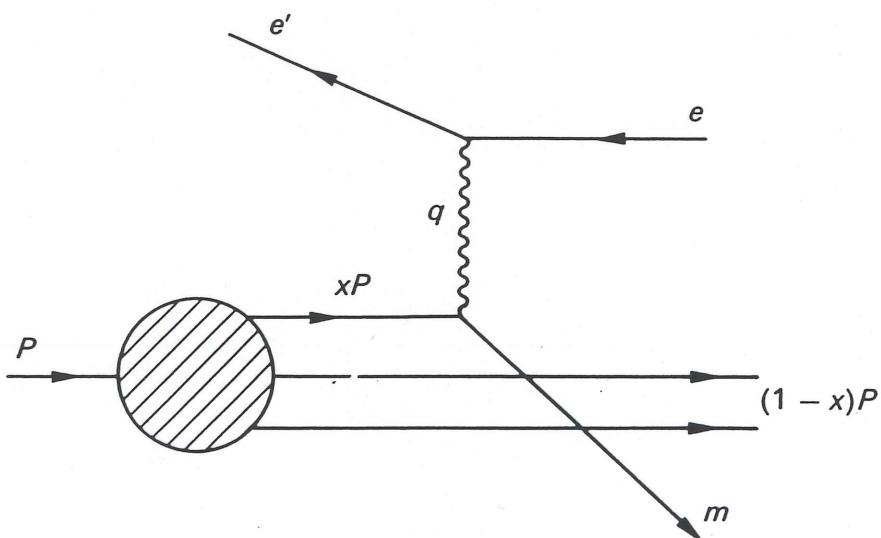
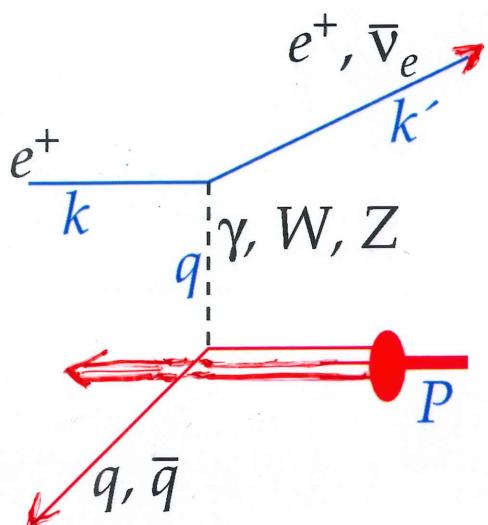


Figure 8.9 The parton model of a deep-inelastic collision.

F<sub>2</sub><sup>NC</sup>

# NC

## Formalism



$$Q^2 = -q^2 \quad x = \frac{Q^2}{2P \cdot q}$$

$$y = \frac{P \cdot q}{P \cdot k} \quad W^2 = (P + q)^2$$

$$Q^2 = sxy$$

$$\frac{d^2\sigma(l^\pm N)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \cdot [Y_+ F_2^{lN}(x, Q^2) - Y_- x F_3^{lN}(x, Q^2) - y^2 F_L^{lN}(x, Q^2)] \quad (1+\delta_r)$$

where  $Y_\pm = 1 \pm (1 - y)^2$

- Contribution from  $F_L^{lN}$  important only at large  $y$
- Contribution from  $x F_3^{lN}$  is negligible for  $Q^2 \ll M_Z^2$
- Either  $F_L^{lN}$  and  $x F_3^{lN}$  treated as QCD corrections
- Or reduced cross section:

$$\tilde{\sigma}(e^+ p) \equiv \frac{xQ^4}{2\pi\alpha^2} \frac{1}{Y_+} \frac{d^2\sigma(e^+ p)}{dx dQ^2} = F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2)$$

In QPM (QCD DIS scheme),

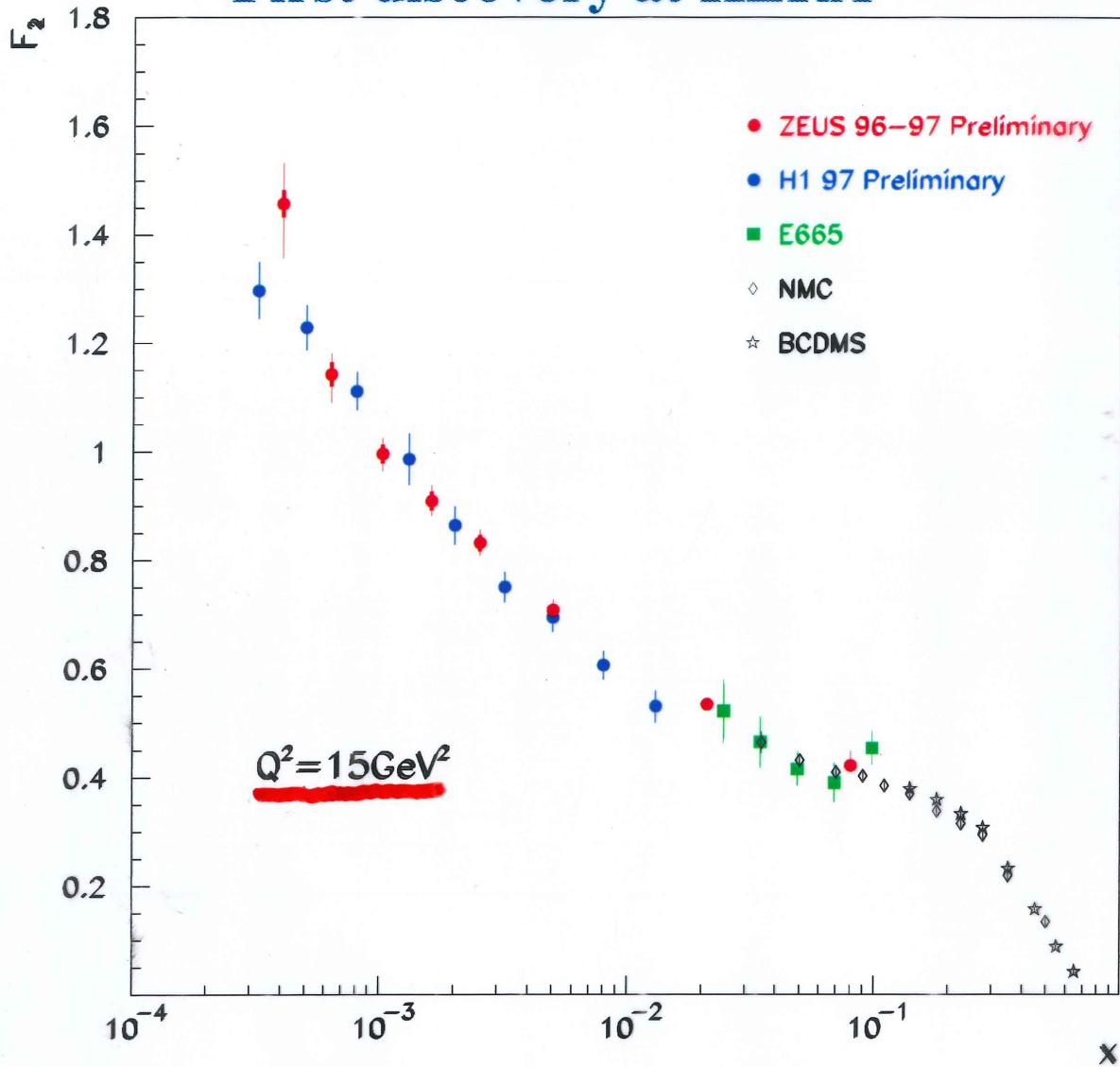
$$F_2^{lN}(x, Q^2) = \sum_i e_i^2 x [q_i(Q^2) + \bar{q}_i(Q^2)]$$

# Measurement of Kinematics

- measure:  $E'_e, E_h, \theta_e, \theta_h$  **2 needed**
- calculate:  $x, Q^2$
- Electron Method (H1):
  - $x, Q^2$  from  $E_e, \theta_e$
  - good  $Q^2$  resolution in full range
  - $\delta x/x = 1/y \cdot \delta E'_e/E'_e$   
poor x resolution at low y
  - sensitive to QED radiation
- $\Sigma$  Method (H1):
  - include hadronic information
  - good x resolution also at low y
  - independent of QED initial state radiation
- Double Angle Method (ZEUS):
  - $x, Q^2$  from  $\theta_e, \theta_h$
  - independent of energy scale  $\Rightarrow$  use for calibration
  - sensitive to QED radiation

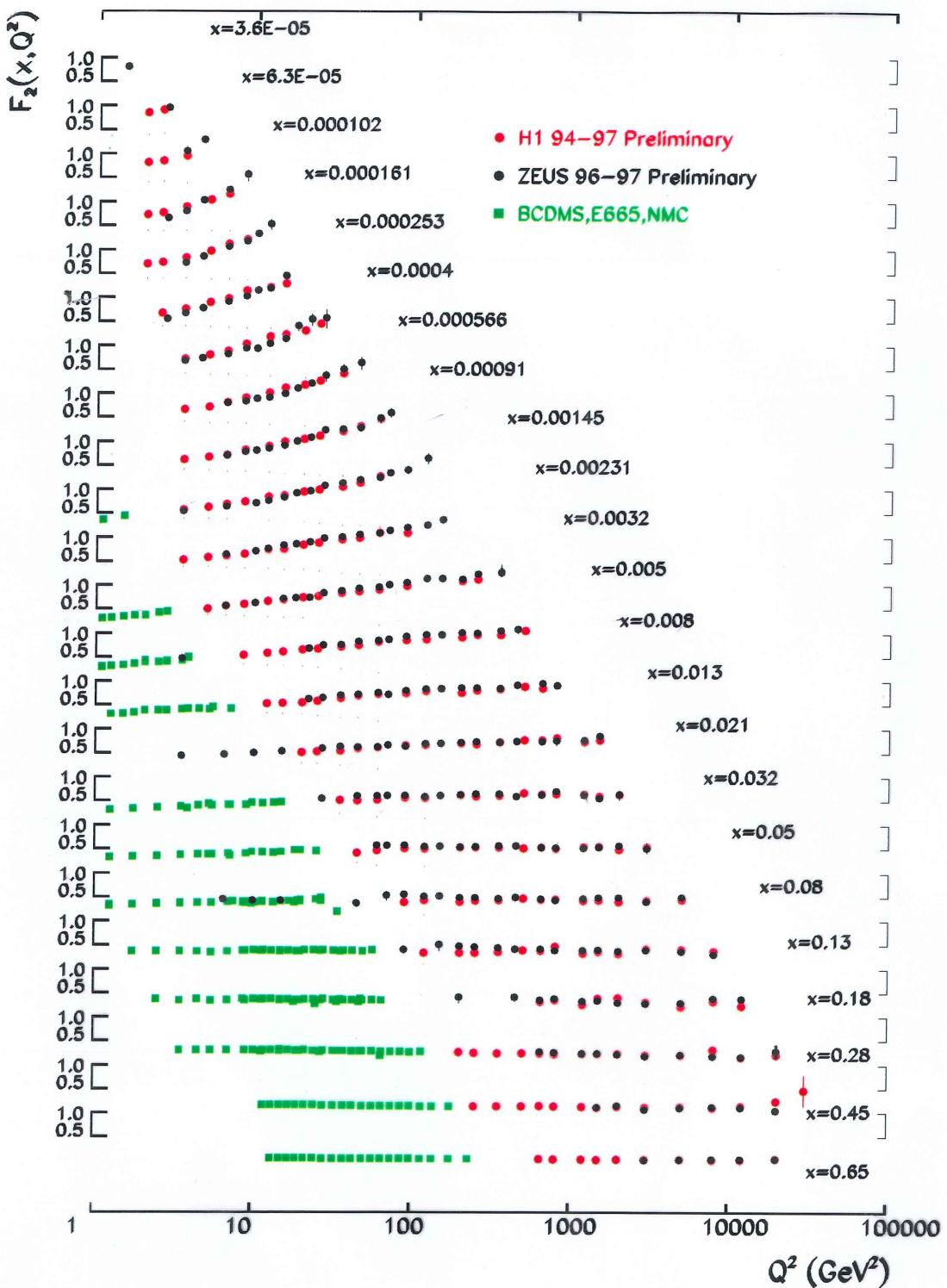
## $F_2(x)$ by ZEUS + H1 at medium $Q^2$

### First discovery at HERA



- H1 and ZEUS **agree** well
- **Precision** improved by a factor 2
- **Fixed target:** high  $x$  : valence quark structure
- **HERA:** low  $x$  : strong rise of  $F_2 \sim x^{-\lambda}$  (6?)

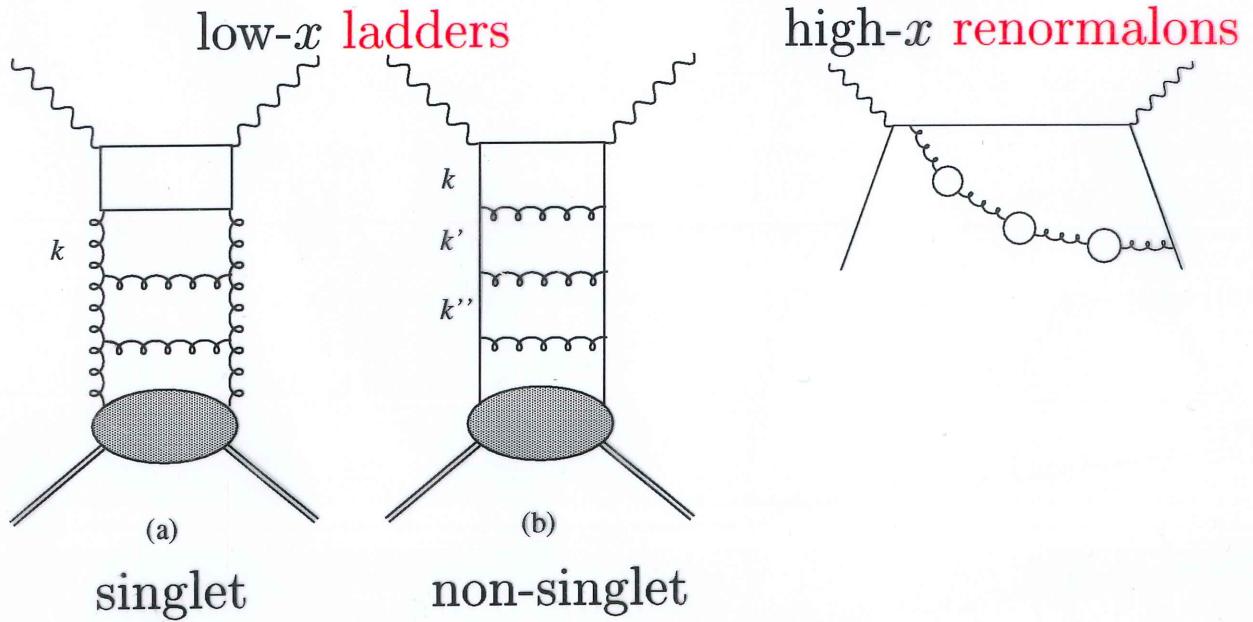
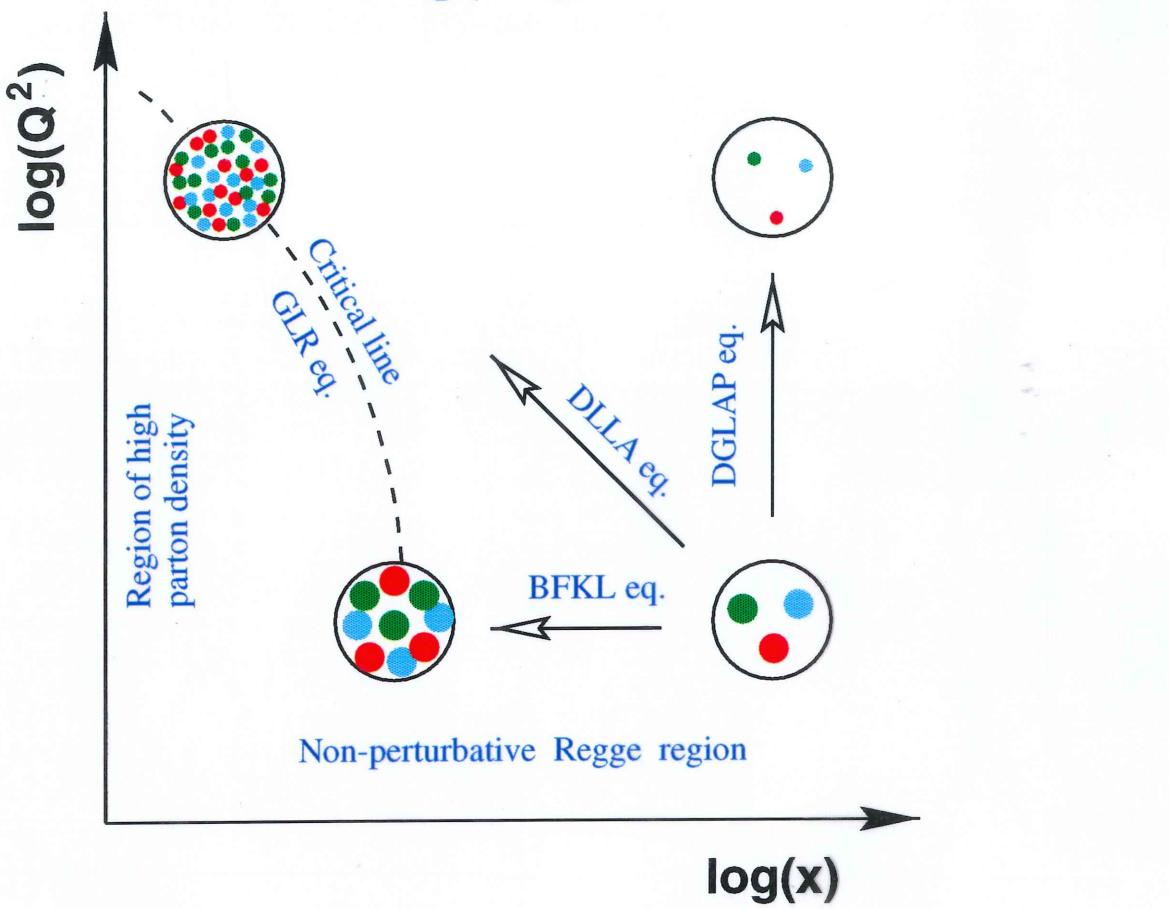
# $F_2$ vs $Q^2$



# Low- $x$ Road Map

- Theoretical Expectations

- High Gluon Density Regime
- Importance of NLO BFKL ?  
evolution in  $\log(1/x)$



## DGLAP Equations

- NLO  $\overline{\text{MS}}$ :

$$F_2(x, Q^2) = \sum_{i=1}^{n_f} [e_i^2 C_q \otimes x(q_i + \bar{q}_i) + C_g \otimes xg]$$

- describe evolution of parton densities  
 $q^{NS}(x, Q^2)$ ,  $q^{SI}(x, Q^2)$ ,  $x g(x, Q^2)$

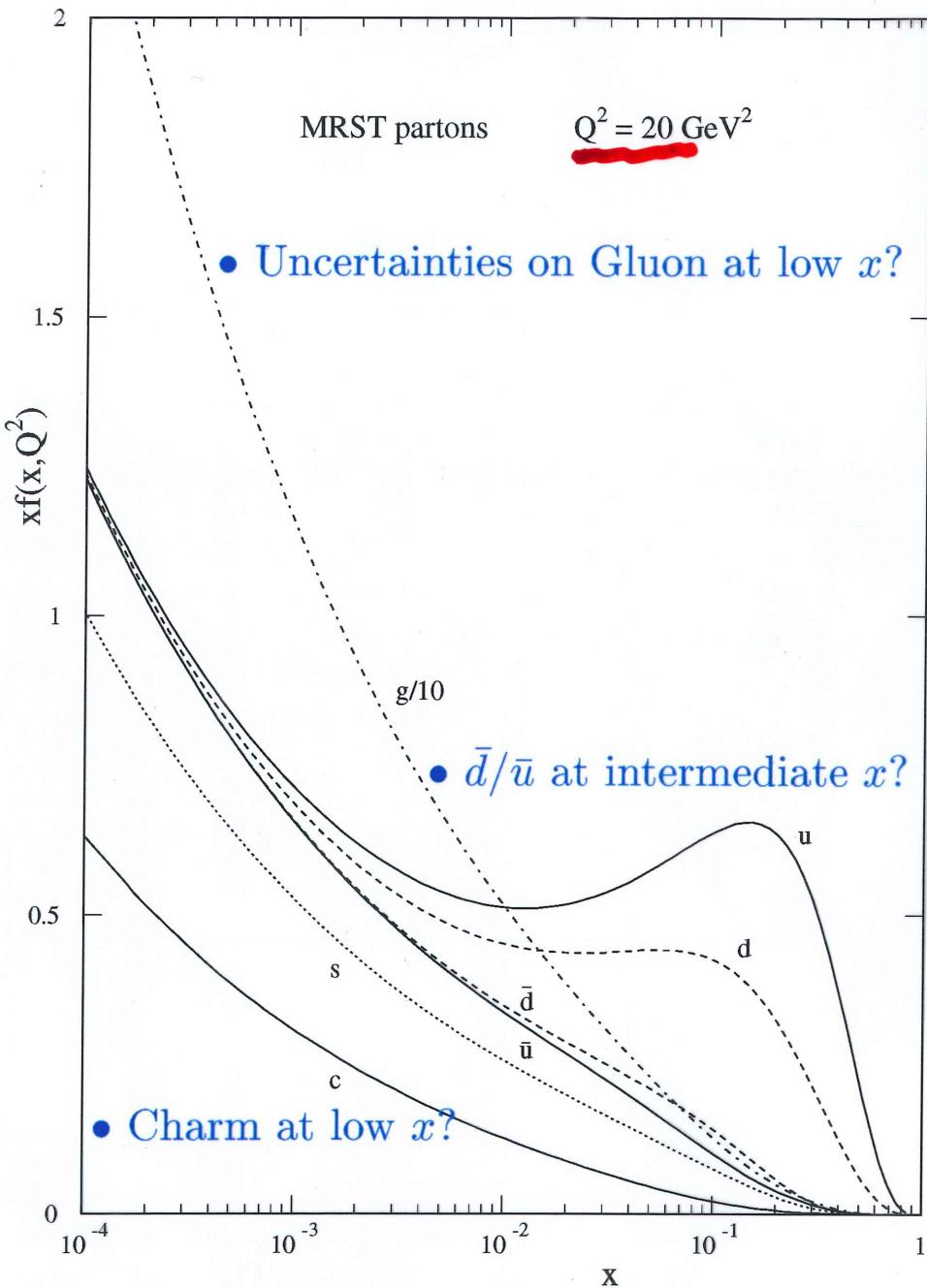
$$\frac{\partial}{\partial \ln Q^2} \begin{pmatrix} q^{NS} \\ q^{SI} \\ xg \end{pmatrix} = \frac{\alpha_s}{2\pi} \begin{pmatrix} q^{NS} \\ q^{SI} \\ xg \end{pmatrix} \otimes \begin{pmatrix} P_{qq}^{NS} \\ P_{qg}^{NS} \\ P_{gq}^{NS} \\ P_{gg}^{NS} \end{pmatrix}$$

- Coefficient and Splitting Functions  
 $C_i$  and  $P_{ij}$  known to NLO
- $q(x) \otimes P = \int_x^1 dz/z \ q(x/z) \ P(z)$   
 convolution over momentum splitting
- $Q^2$  depend. predicted by QCD
- $x$  depend. parametrized at  $Q_0^2$  + fitted

# Proton Structure

## MRST

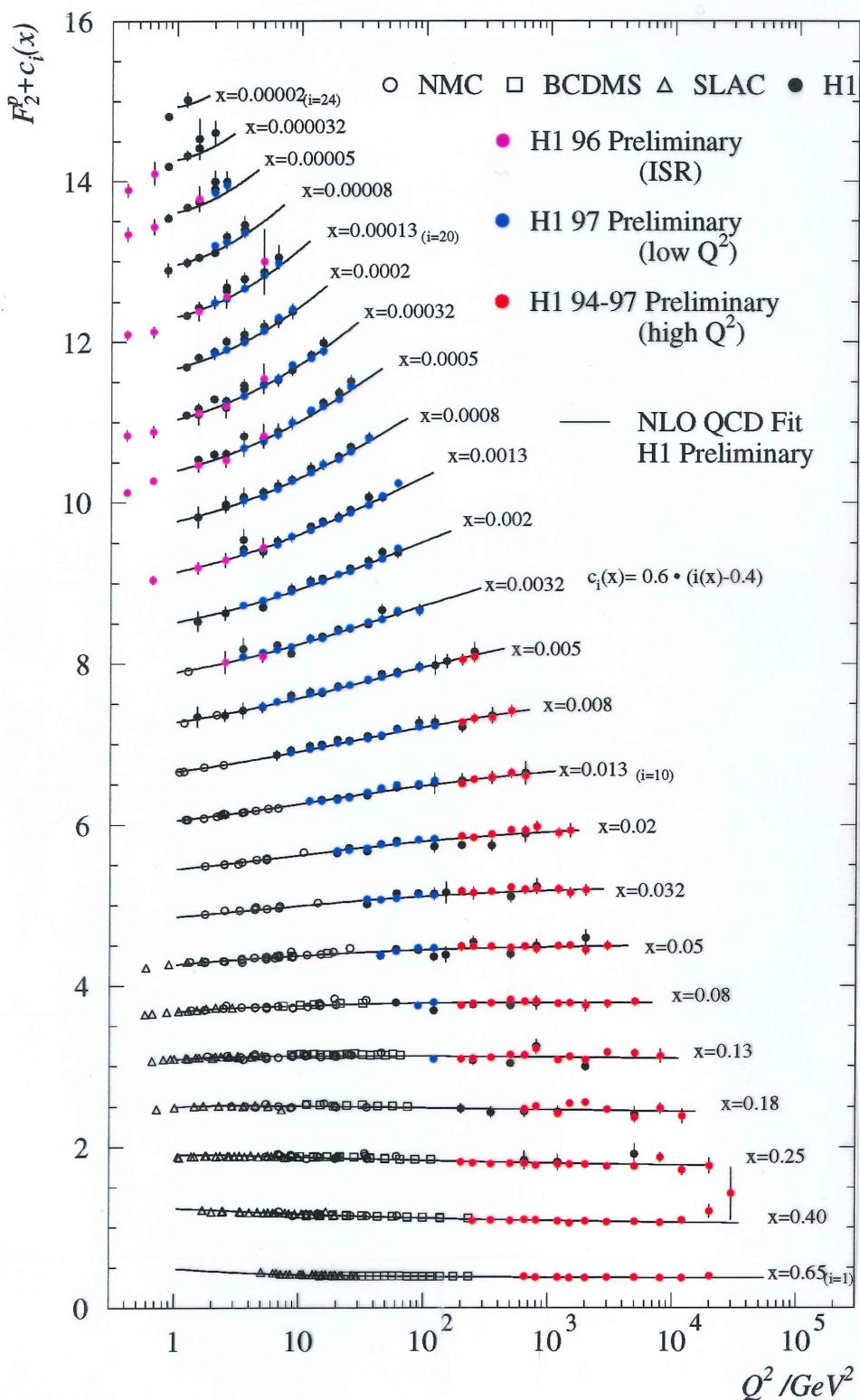
- Output Parton Distributions



• Uncertainties at Large  $x$  - HT?  $d/u$ ?

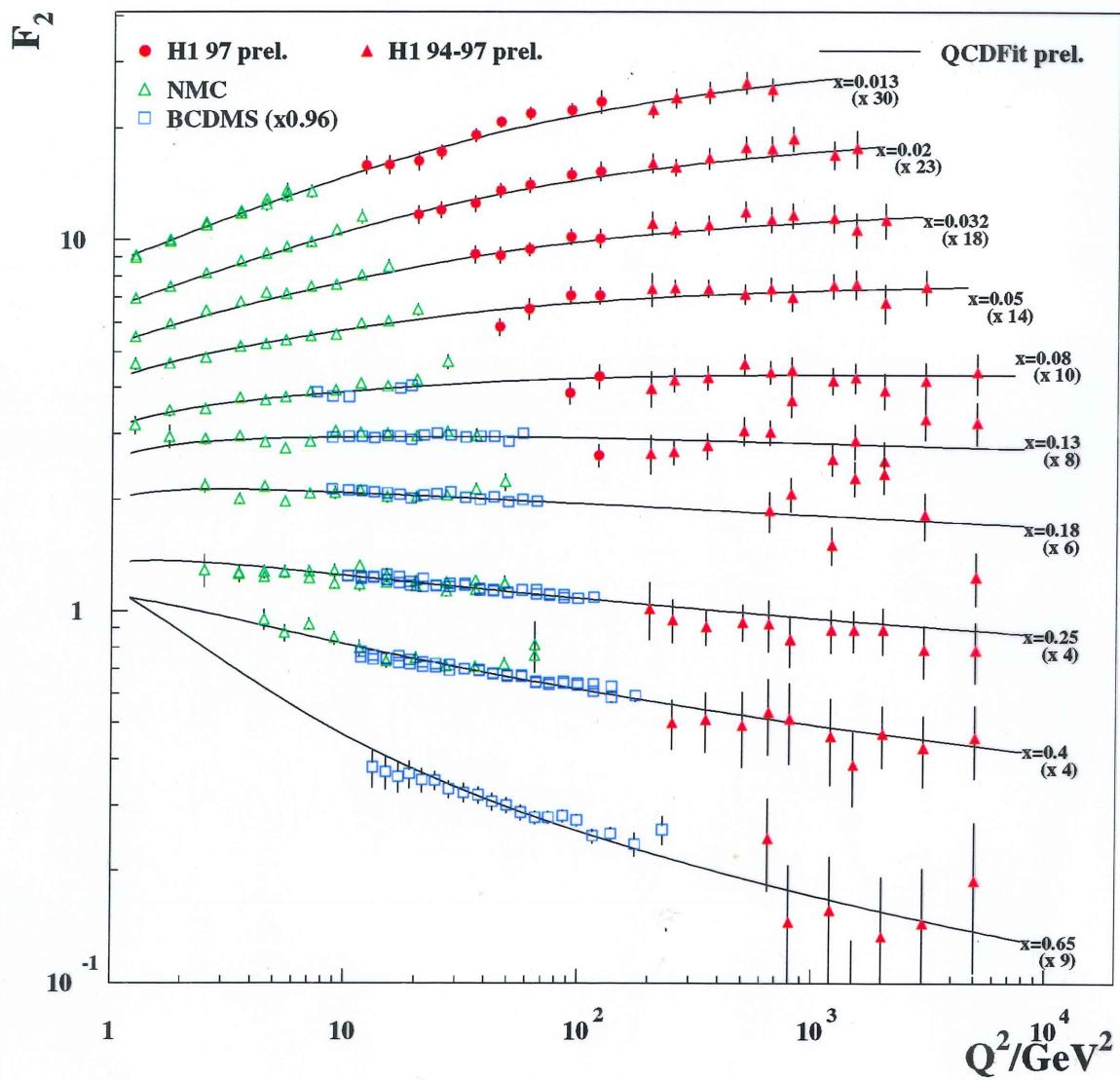
► New Cross Section Data at Highest  $Q^2$

# $F_2$ and perturbative QCD



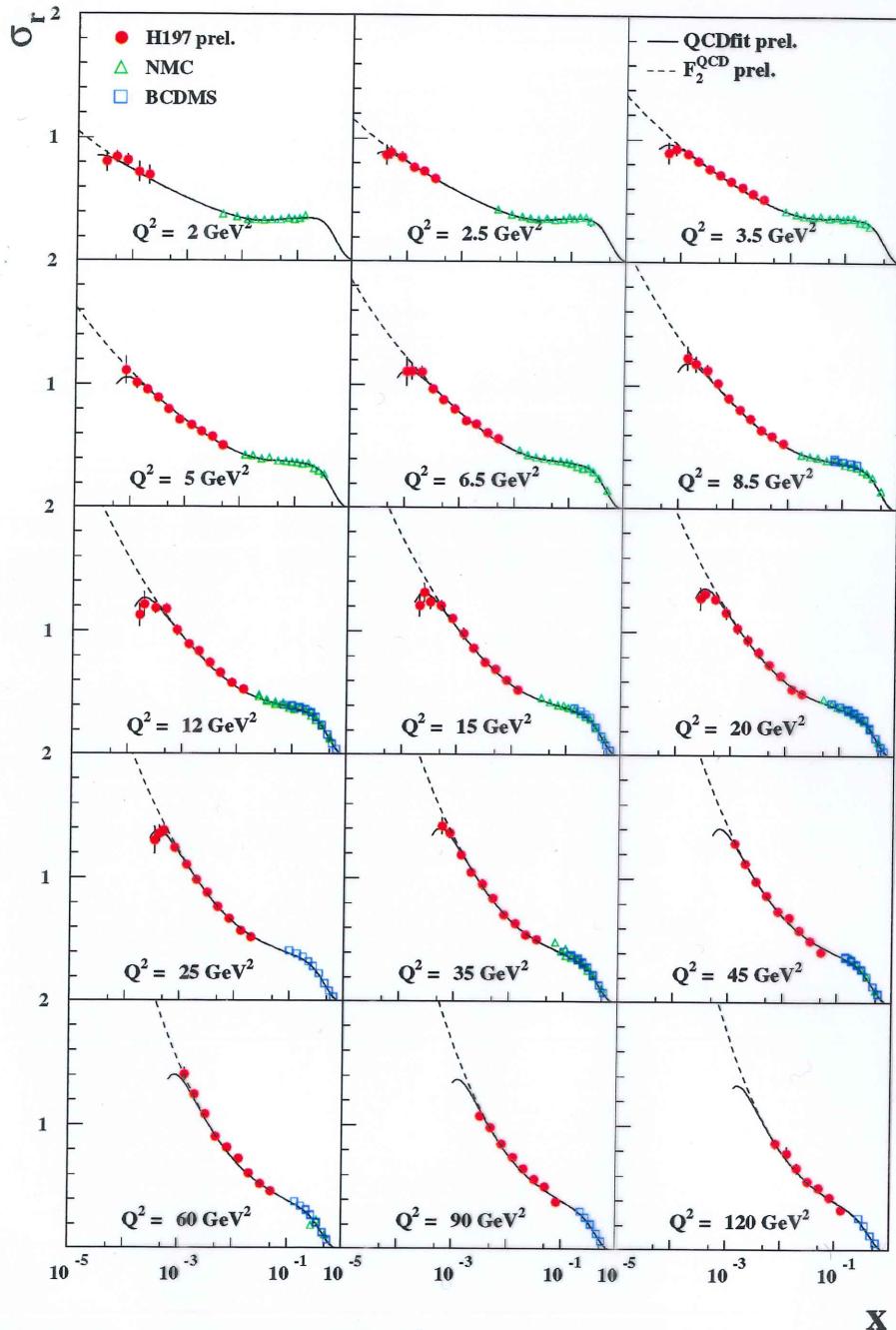
- Good description of the data by the NLO DGLAP fit over more than 4 orders of magnitude in  $x$  and  $Q^2$

## Scaling at $x \sim 0.1$



- HERA and fixed target experiments agree well
- Scaling at  $x \sim 0.1$  observed up to  $5000 \text{ GeV}^2$

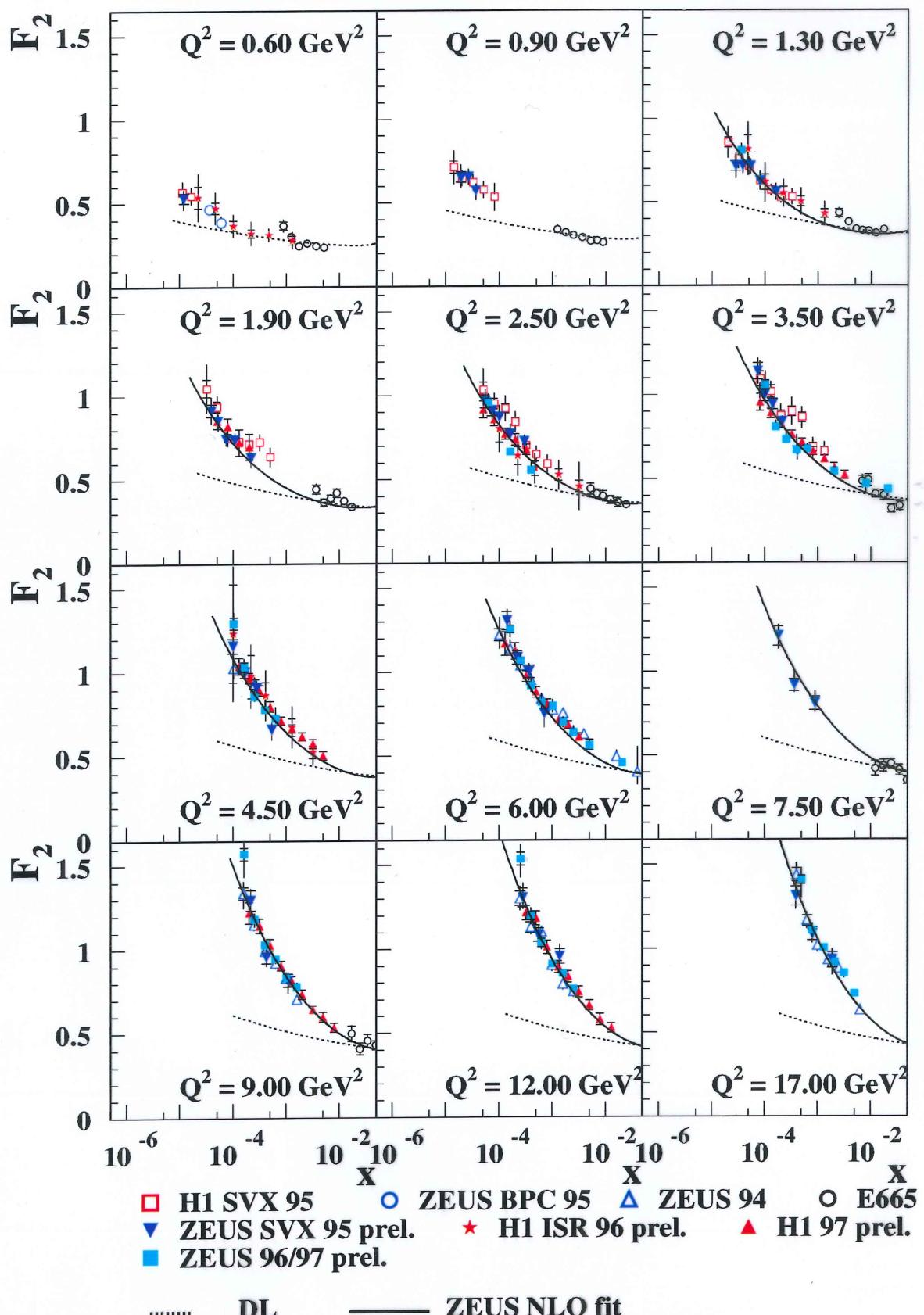
## QCD fit to $\sigma_r(x)$



- NLO DGLAP works down to  $Q^2 \sim 2 \text{ GeV}^2$
- $F_2(x) \sim x^{-\lambda}$ : steepness increases with  $Q^2$
- low  $x$ :  $F_2(x)$  deviates from  $\sigma_r \Rightarrow$  extract  $F_L$

# Transition Region

## HERA 1995-1997 preliminary



- New datasets using different methods give consistent results

$F_L$

$F^{\text{Charm}}$

gluon  $g(x, Q^2)$

## $F_L$ Extraction

- Reduced cross section:

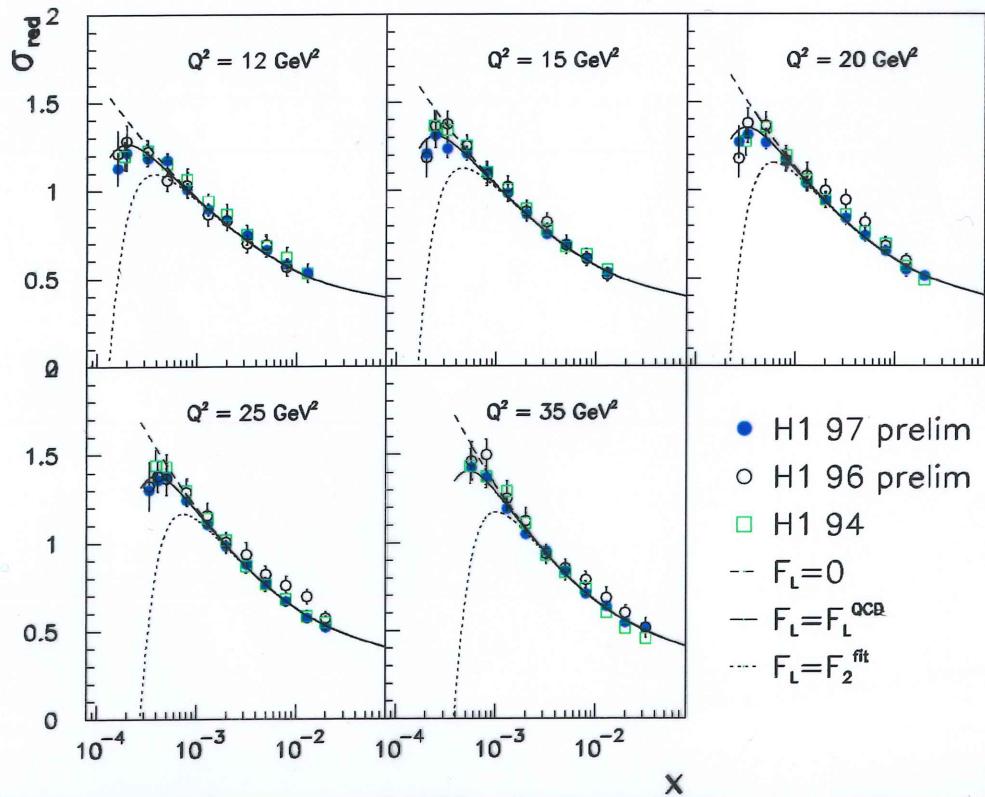
$$\sigma_r = \frac{1}{\kappa} \frac{d^2\sigma}{dxdQ^2} = F_2 - \frac{y^2}{Y_+} F_L$$

with  $\kappa = \frac{2\pi\alpha^2 Y_+}{Q^4 x}$  and  $Y_+ = 1 + (1 - y)^2$

- H1:**

- QCD fit to  $F_2$   
where  $F_L$  is negligible:  $y < 0.35$
- extrapolate to high  $y$
- subtract measured reduced cross section:

$$F_L = \frac{Y_+}{y^2} (F_2^{fit} - \frac{1}{\kappa} \frac{d^2\sigma^{exp}}{dxdQ^2})$$



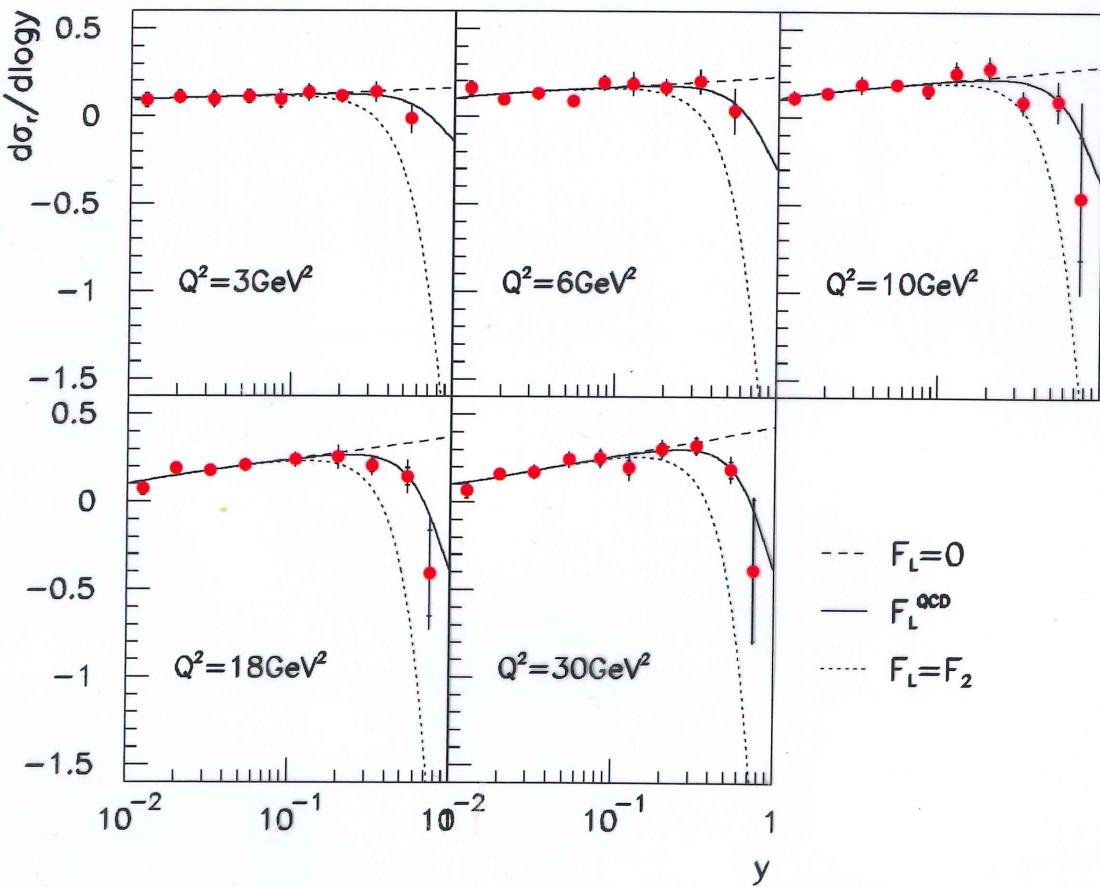
## $F_L$ from $\partial\sigma_r/\partial \ln y$

- Derive reduced cross section at fixed  $Q^2$ :

$$\frac{\partial\sigma_r}{\partial \ln y} = -\frac{\partial F_2}{\partial \ln x} - F_L \cdot 2y^2 \cdot \frac{2-y}{Y_+^2} + \frac{\partial F_L}{\partial \ln x} \cdot \frac{y^2}{Y_+}$$

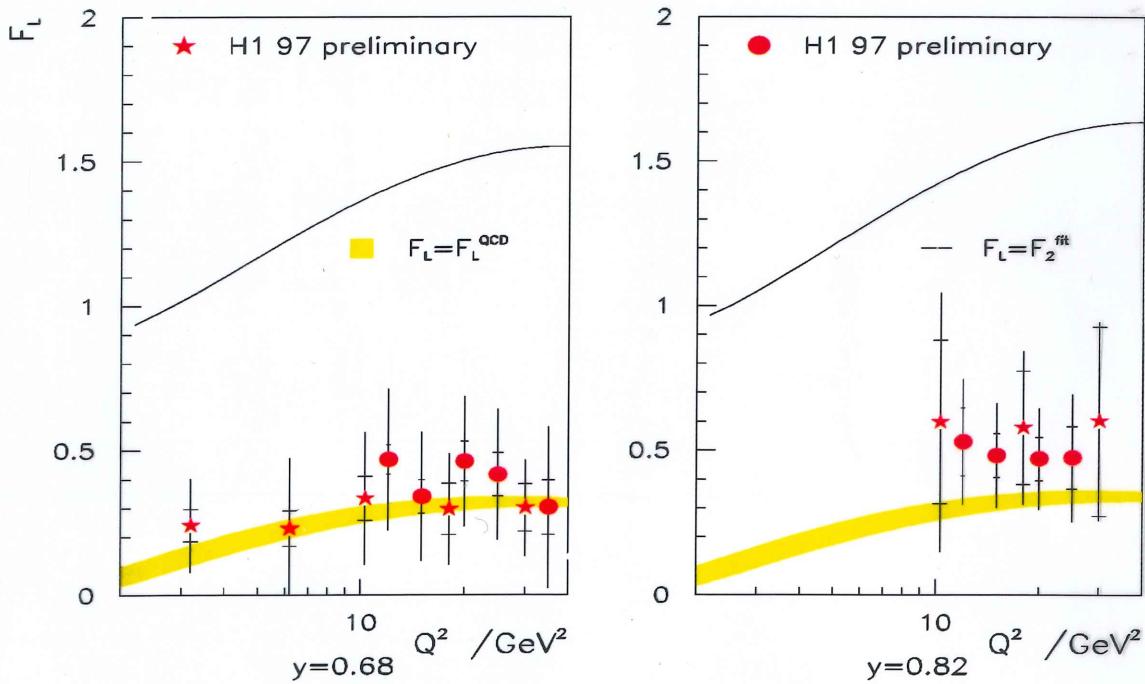
- Assume  $\partial F_2/\partial \ln y = A \ln y + B$   
checked with QCD fit and put to error
- Straight line fit to  $\partial\sigma/\partial \ln y$  in  $Q^2$  bins at  $y < 0.2$
- Access lower  $Q^2$  than with subtraction method

H1 preliminary



## $F_L$ Determination

- Two methods to determine  $F_L$ : subtraction (●) and derivative (★) method
- Methods use different aspects of  $F_2$  and  $F_L$  behaviour
- Systematic errors at same  $y$  correlated



- $F_L$  determination from both methods consistent
- $F_L$  agrees with QCD prediction but
- **Direct**  $F_L$  measurement not assuming QCD still important: vary beam energies !

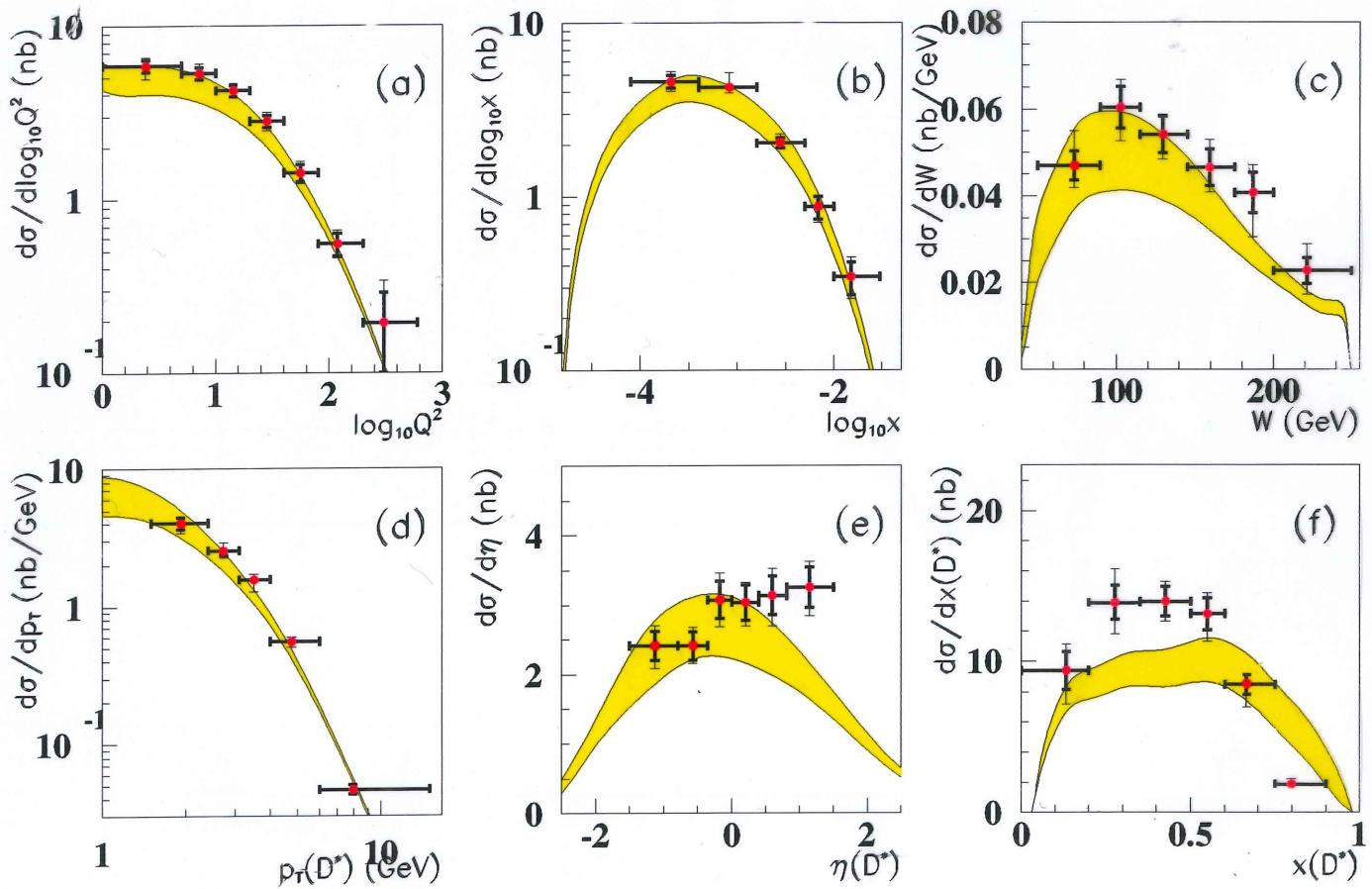
# Charm in DIS

New ► "Precision" results from HERA

For  $1 < Q^2 < 600 \text{ GeV}^2$ ,  $0.02 < y < 0.7$ ,

$1.5 < p_T(D^*) < 15 \text{ GeV}$ ,  $|\eta(D^*)| < 1.5$

$$\Rightarrow \sigma(ep \rightarrow eD^*X) = 8.55 \pm 0.31^{+0.30}_{-0.50} \text{ nb}$$



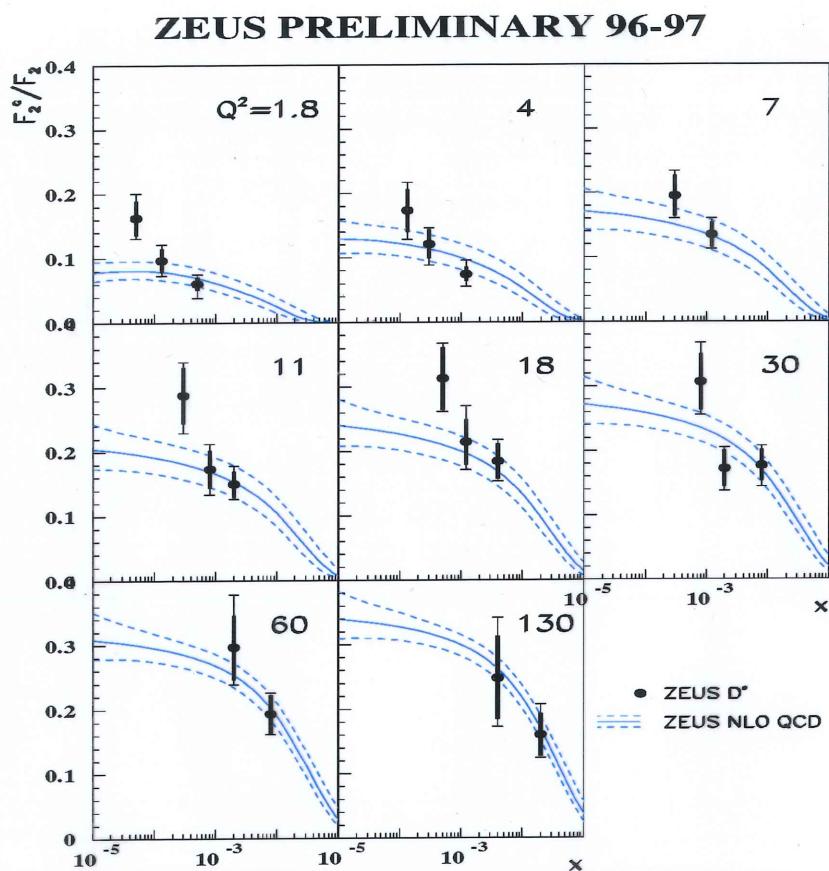
⇒ agreement with "massive" NLO pQCD BGF  
band:  $m_c$  uncertainty (1.2-1.6 GeV)  
 $f(c \rightarrow D^{*+}) = 0.222 \pm 0.014 \pm 0.014^\dagger$

<sup>†</sup>B. W. Harris and J. Smith, hep-ph/9706334

<sup>†</sup>OPAL Collab., Eur. Phys. J C1(1998)439

# Charm in the Proton

$$\frac{d^2\sigma_{c\bar{c}X}}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} [1 + (1 - y)^2] F_2^c(x, Q^2)$$



Charm  
 $F_2^c$   
 $\underline{F_2}$

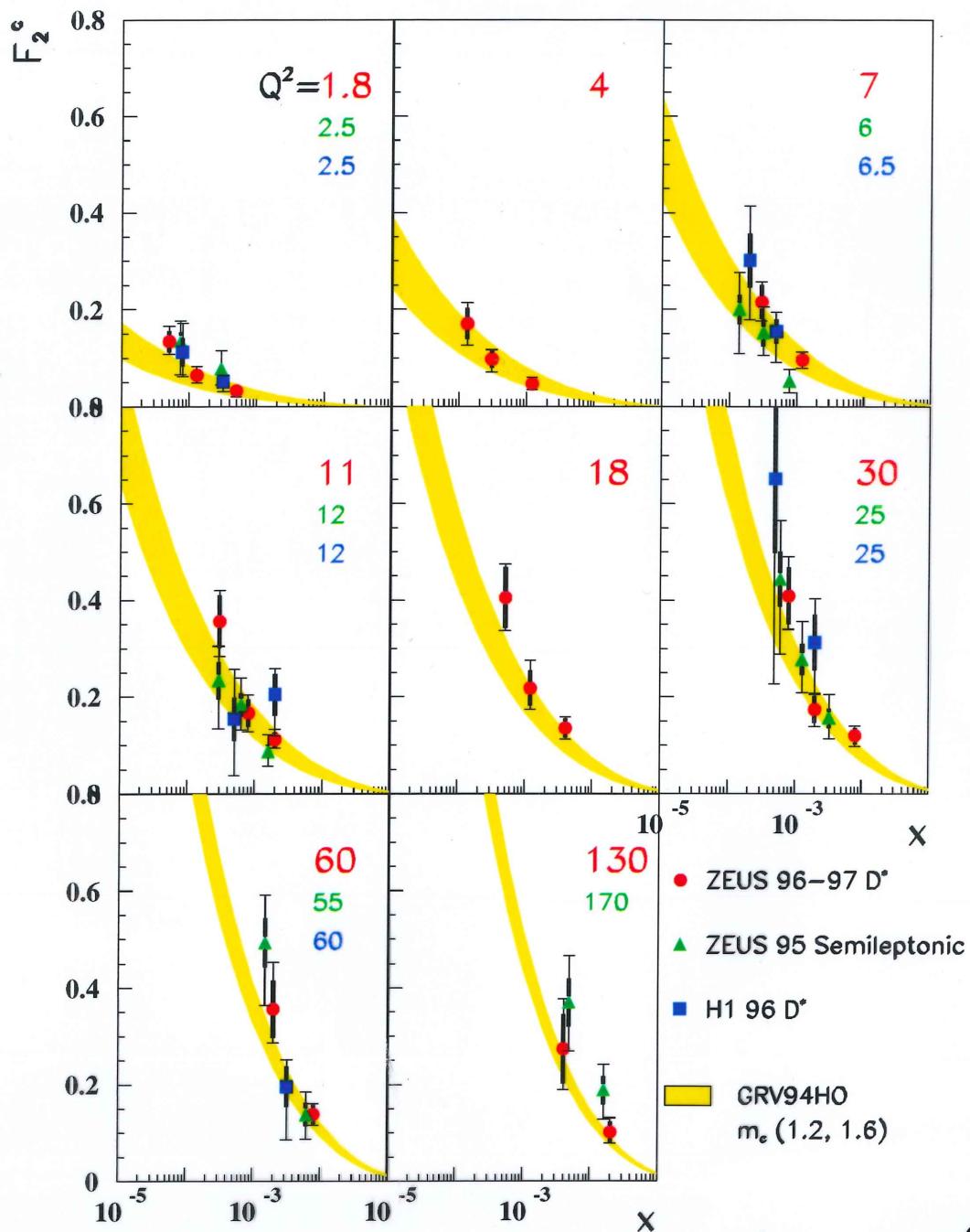
- Charm content of the proton grows from 10 to 25 % between  $Q^2 = 1.8$  and  $130 \text{ GeV}^2$

$$F_2^c$$

$$\frac{d^2\sigma_{c\bar{c}X}}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} [1 + (1-y)^2 F_2^c(x, Q^2) - y^2 F_L^c(x, Q^2)]$$

Extraction of  $F_2^c$  is made possible by the large acceptance in  $\{\eta, p_T\}$  of  $D^*$

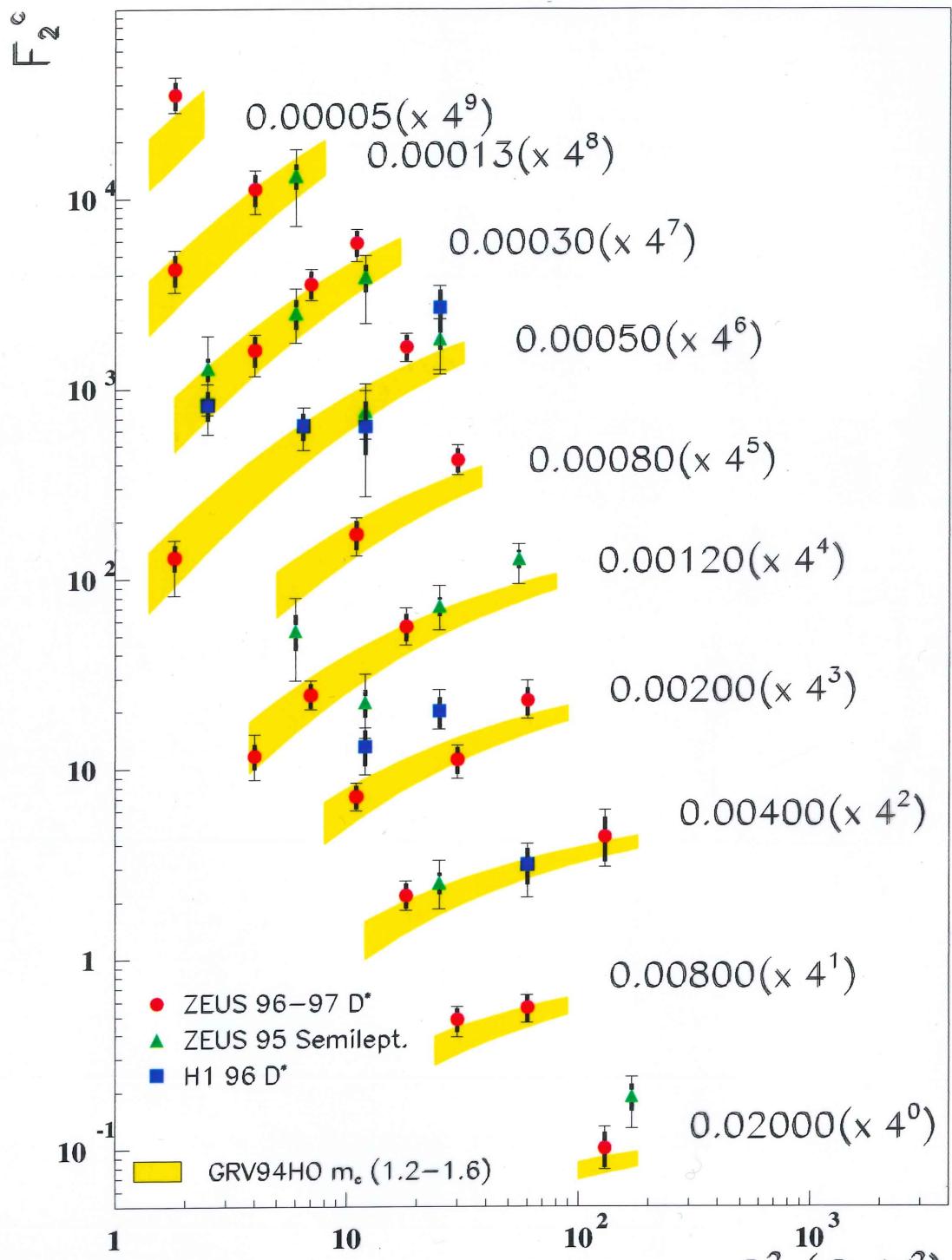
### HERA 95-97 PRELIMINARY



- Precision  $\approx 15 - 20\%$  (much better than earlier m.)

# $F_2^C$ Scaling Violations

HERA PRELIMINARY 95-97

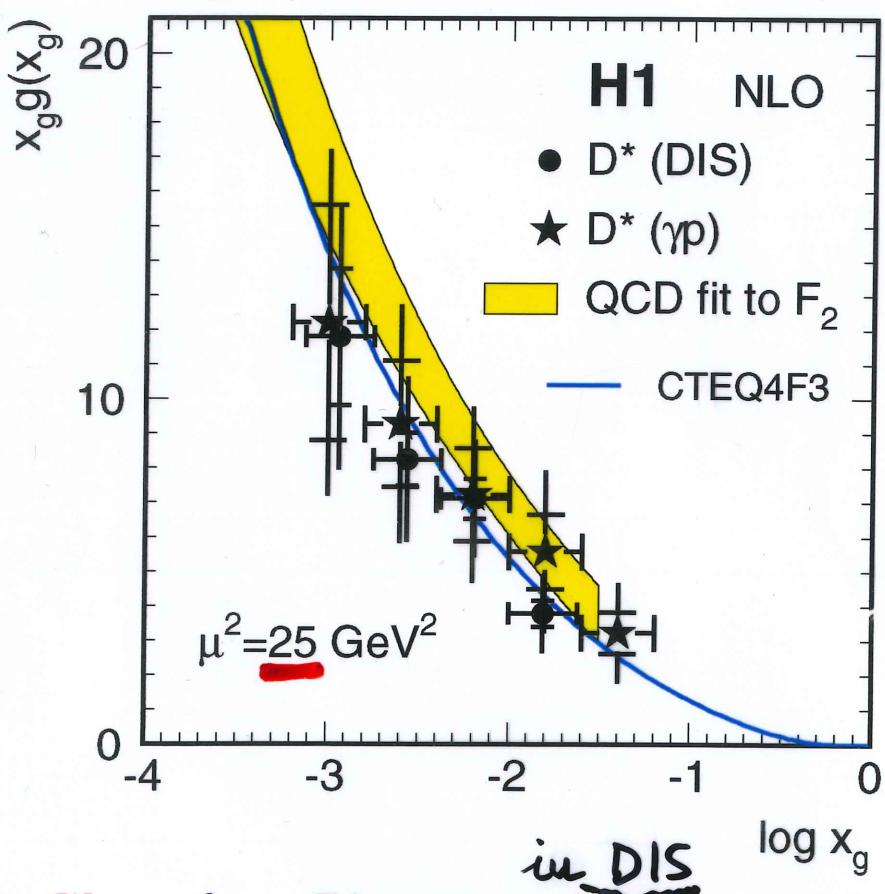


► Large scaling violations

ZEUS semileptonic and H1  $D^*$  plotted at closest  $x$  values

# Gluon Density from Charm

- Measure  $x_g$  from scattered  $e$  and  $p_t$  and  $(E - p_z)$  of  $D^*$
- Cut  $p_t$  and  $\eta$  of  $D^*$  in MC (no extrapolation!)
- Iteratively unfold true  $x_g$  using
  - NLO Heavy Quark DIS QCD Monte Carlo
  - Peterson fragmentation

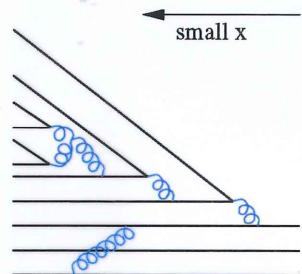
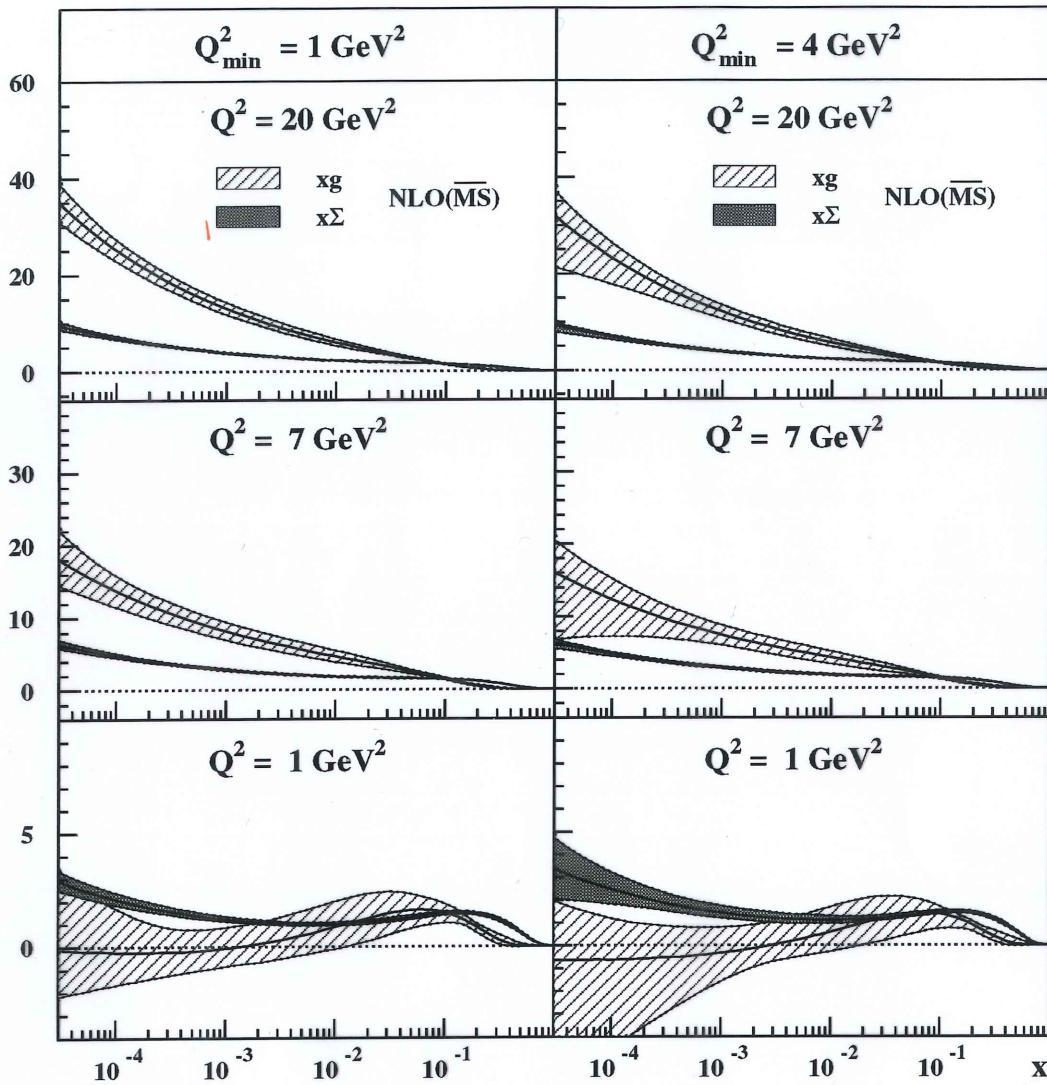


- **Gluon** from  $D^*$  cross section agrees with
- **Gluon** from  $D^*$  photoproduction and
- **Gluon** from QCD fit to inclusive cross section
- **Same** gluon + boson-gluon fusion generate cross sections

# The transition region

Comparison of  $xg$  and  $x\Sigma$  resulting from QCD fit including  $F_2$  down to  $Q_{min}^2 = 1 \text{ GeV}^2$ :

**ZEUS 1995**



Different behavior of gluon and  $q\bar{q}$  sea distributions at  $Q^2 \approx 1 \text{ GeV}^2$ :

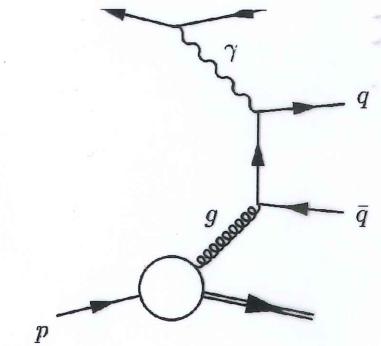
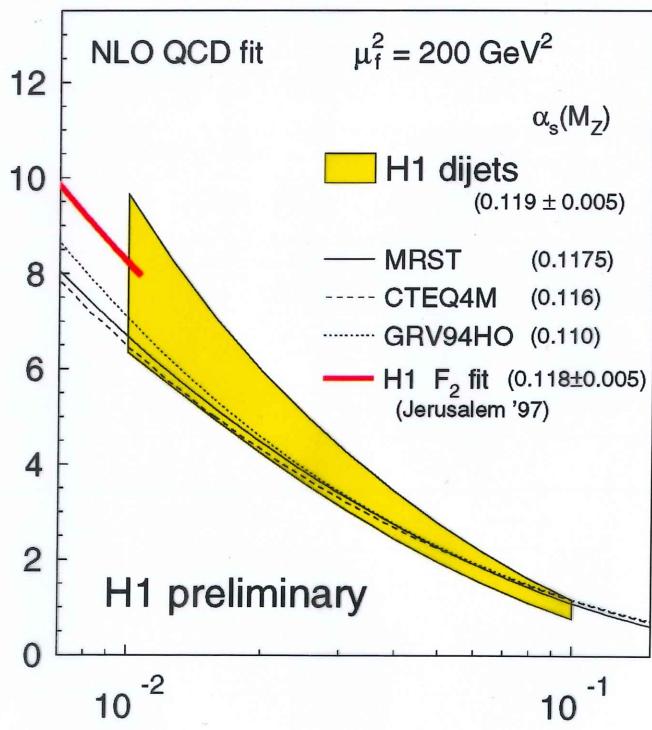
- at high  $Q^2$  gluon drives sea;
- at low  $Q^2$  sea drives gluon.

Also found by MRST, while in GRV94 sea and gluon both singular at  $Q^2 \approx 1 \text{ GeV}^2$ .

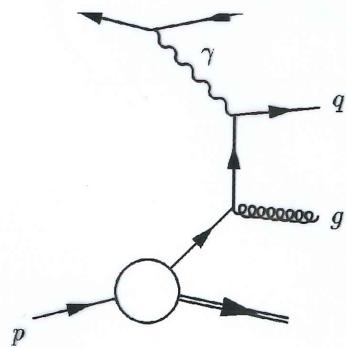
# The Gluon from Di-Jets

- Similar to  $c\bar{c}$ , but  $M_{jj} \gg M_{c\bar{c}} \Rightarrow$  get gluon at higher  $x$
- more stat. but also more backgr. than g from charm
- Data:  $200 \leq Q^2 \leq 5000 \text{ GeV}^2$

**fit:**  $\frac{d^2\sigma}{dQ^2dx}$  and  $\frac{d^2\sigma_{dijet}}{dQ^2d\xi}$  with  $\xi = x(1 + \frac{M_{jj}^2}{Q^2})$



Boson-Gluon-Fusion



QCD-Compton

- consistent with gluon from scaling violations and charm
- more direct in  $x_g$  than gluon from scaling violations

HIGH

$Q^2$

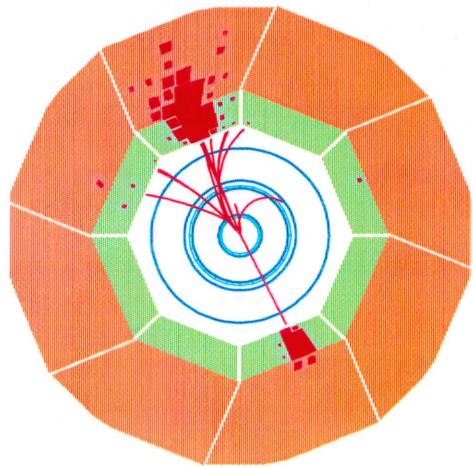
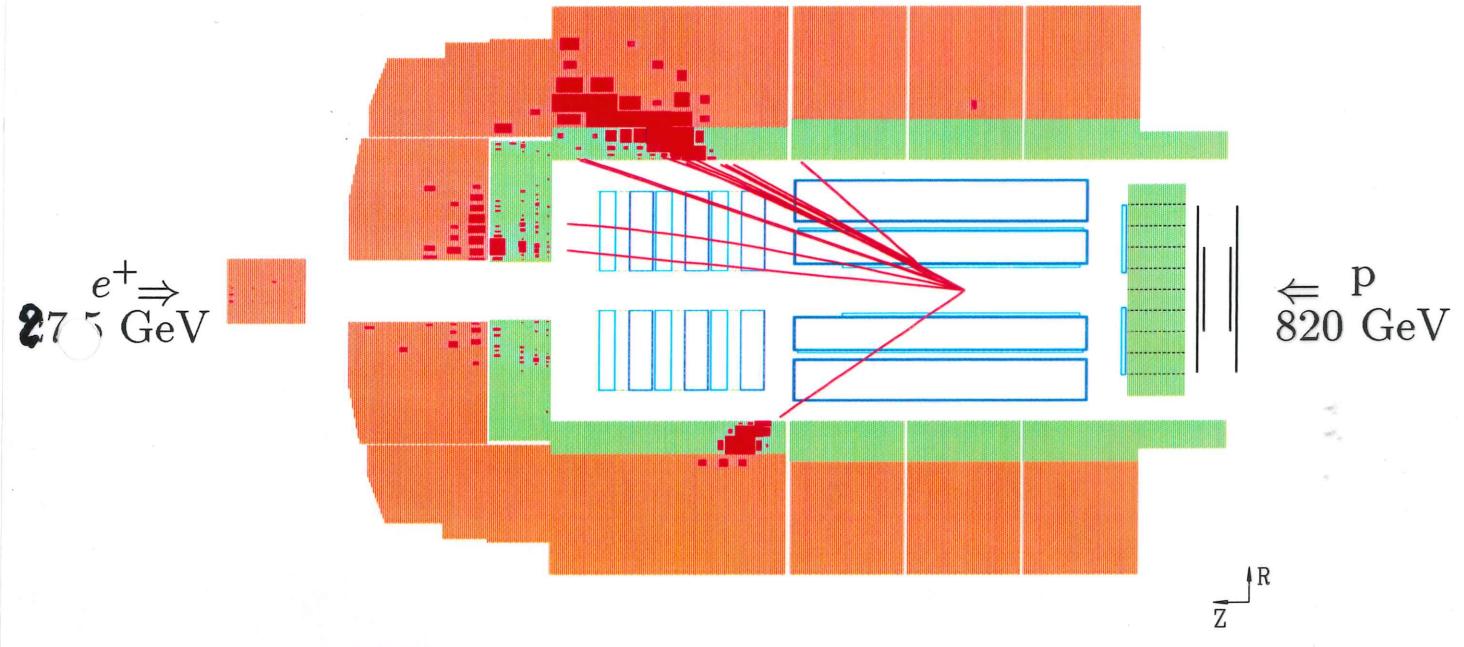
NC  
Neut. Currents

interactions

First look to  $F_3$  effect

# NC DIS Event

$$Q^2 = 16950 \text{ GeV}^2, \quad y = 0.44, \quad M = 196 \text{ GeV}$$



## Liquid Argon Calorimeter:

44000 Cells

$$\sigma(E)/E(em) \simeq 12\%/\sqrt{E/\text{GeV}} \oplus 1\%$$

$$\sigma(E)/E(had) \simeq 50\%/\sqrt{E/\text{GeV}} \oplus 2\%$$

$$\Delta E/E_{em} = 1 - 3\%$$

$$\Delta E/E_{had} = 4\%$$

$$\Delta\theta_e = 2 - 5 \text{ mrad}$$

## measured quantities:

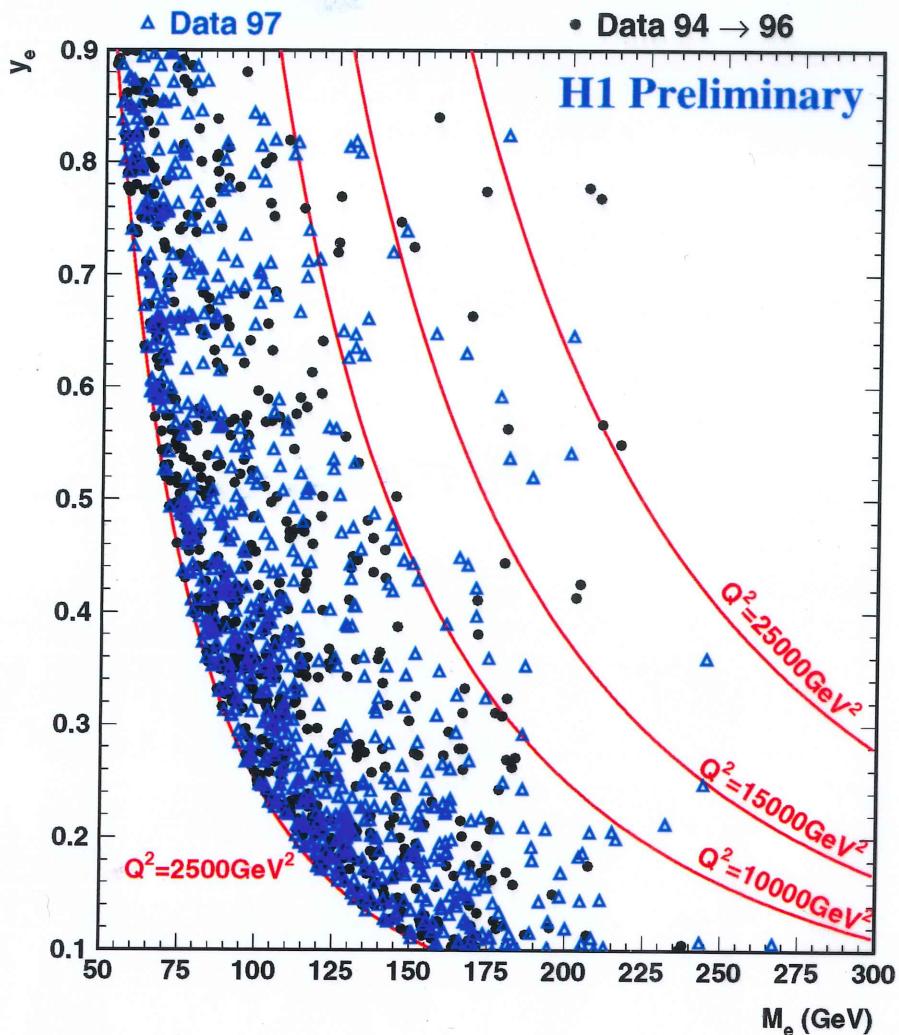
$e^+$ : energy  $E$

polar angle  $\theta$

hadrons:  $\Sigma = \sum_{hadrons} (E_h - p_{z,h})$

$$\tan \gamma/2 = \Sigma/p_{t,h}$$

# H1 High $Q^2$ Events



$$Q_e^2 > 15000 \text{ GeV}^2$$

$$\text{Obs.} = 22 \Leftrightarrow \text{Exp.} = 14.7 \pm 2.1$$

- accumulation of events in mass window?

$$M_e = 200 \pm 12.5 \text{ GeV}$$

$$\begin{aligned} \text{Obs} &= 8 \text{ for 94-97} \Leftrightarrow \text{Exp} = 3.01 \pm 0.54 \\ (\text{Obs} &= 7 \text{ for 94-96} \Leftrightarrow \text{Exp} = 0.95 \pm 0.18) \end{aligned}$$

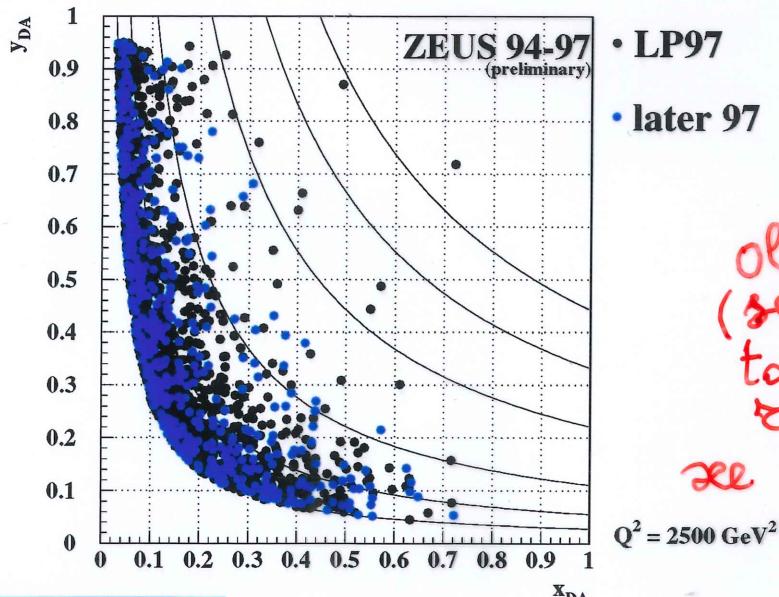
- compatible, but less significant with '97 data

► Cross Section  
Measurements

# ZEUS High Q<sup>2</sup> Events

## Neutral Current

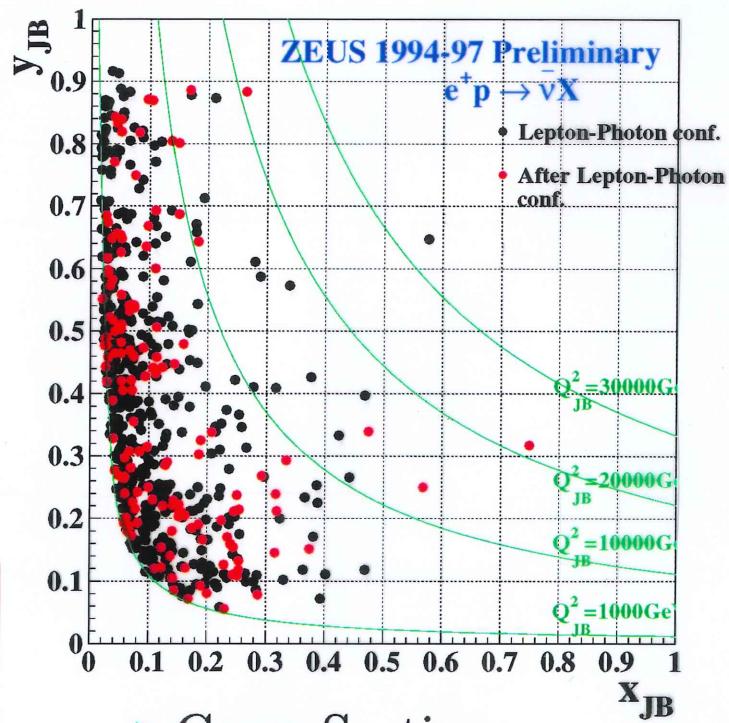
No new high  $Q^2$   
 $> 20,000 \text{ GeV}^2$   
 events after LP97



$Q^2_{min}$	$N_{obs}$	$N_{exp}$
10000	66	$60 \pm 4$
15000	20	$17 \pm 2$
35000	2	$0.29 \pm 0.02$

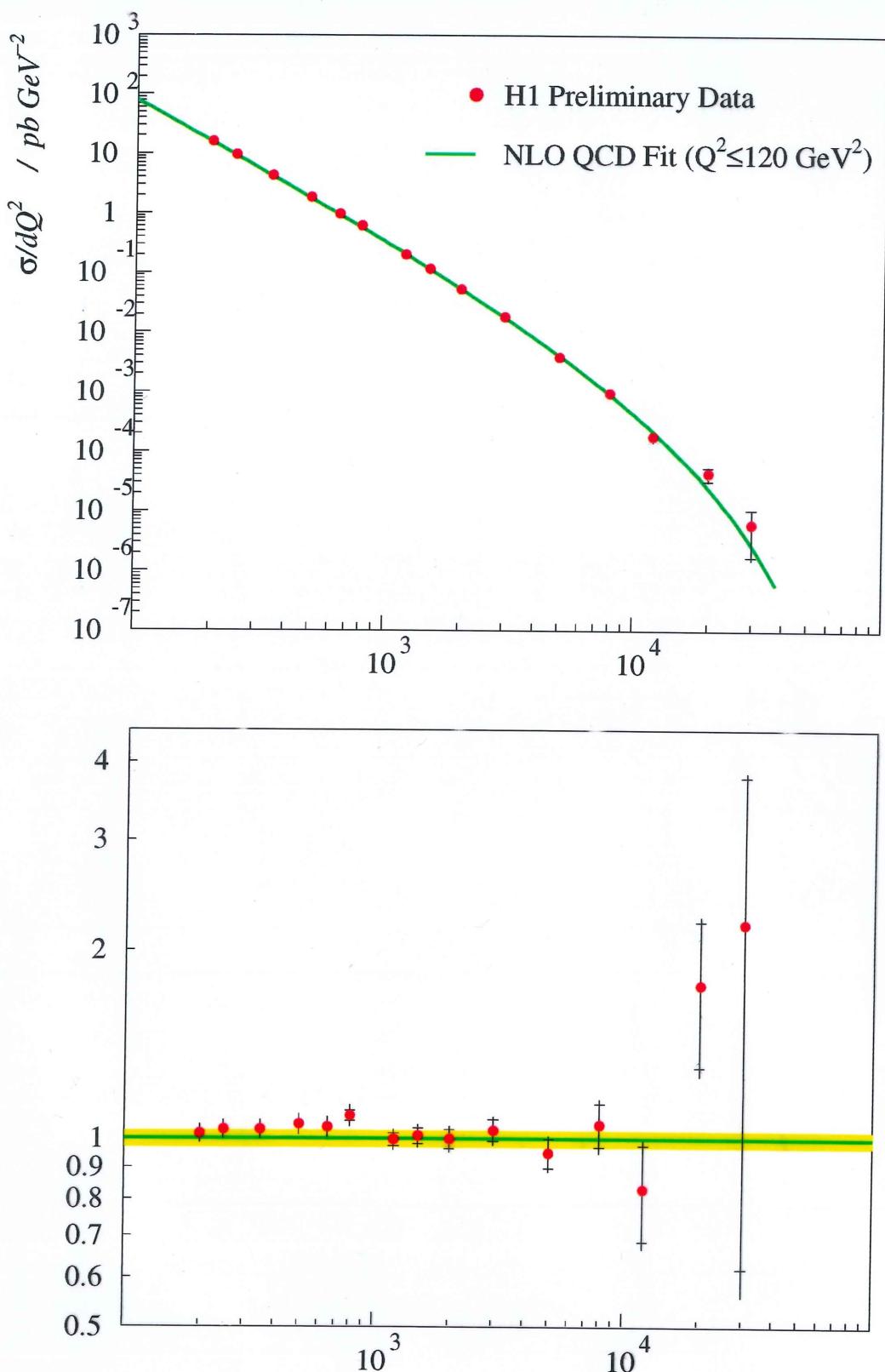
## Charged Current

Two new high  $Q^2$   
 $> 20,000 \text{ GeV}^2$   
 events after LP97



$Q^2_{min}$	$N_{obs}$	$N_{exp}$
10000	22	$17^{+5.7}_{-5.2}$
15000	8	$3.9^{+1.9}_{-1.6}$
30000	1	$0.06^{+0.08}_{-0.04}$

$$d\sigma^{NC}/dQ^2$$

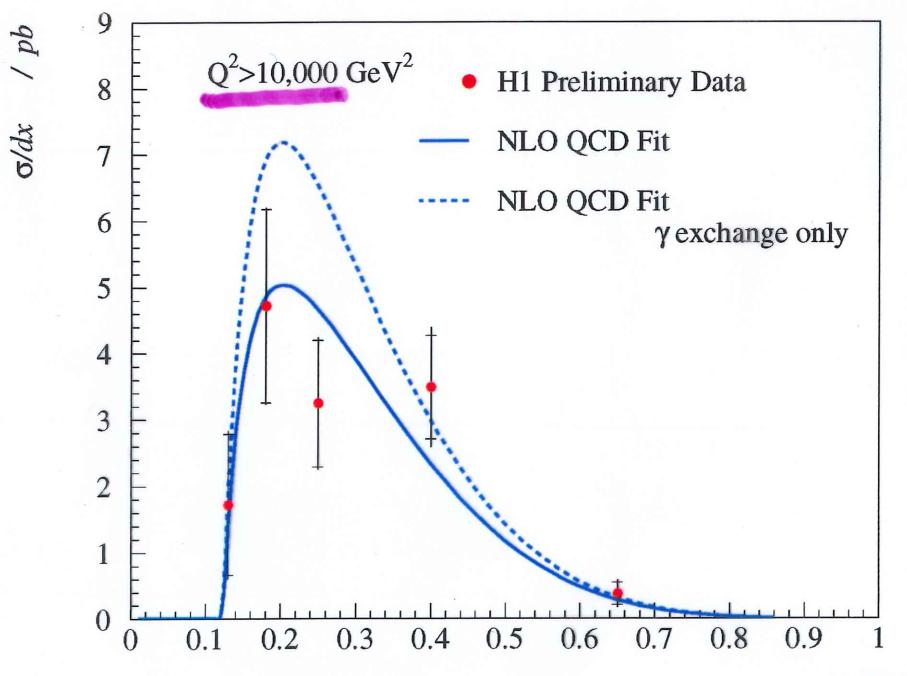
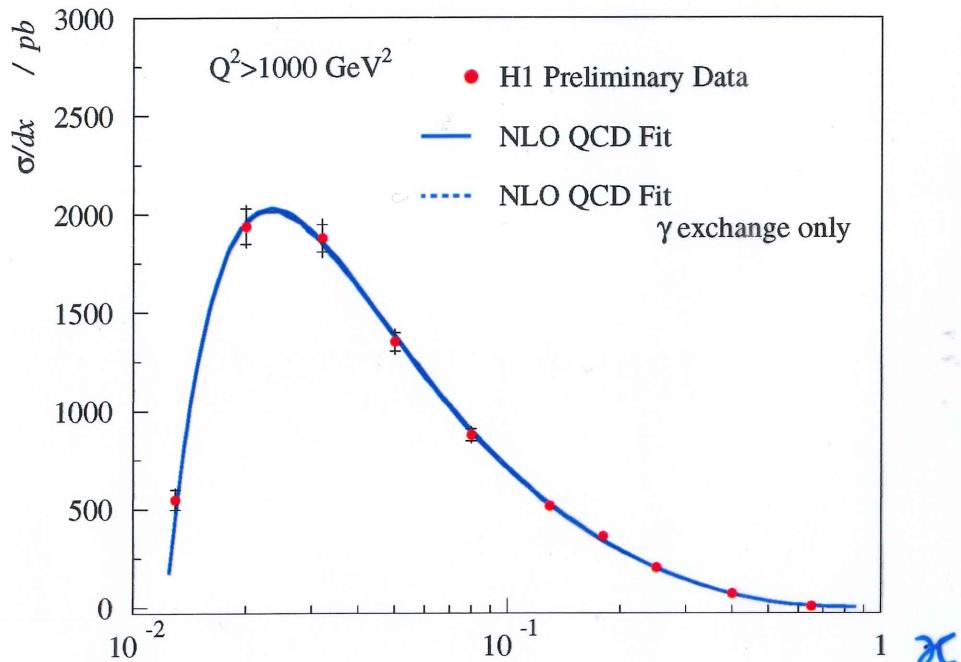


Good agreement with Standard Model  
up to  $Q^2 \simeq 10,000 \text{ GeV}^2$

H1 and ZEUS precision sufficient to constrain PDFs  
→ Benchmark for Standard Model

# Sensitivity to $Z$

$$\sigma(eq \rightarrow eq) \propto \left| \begin{array}{c} \text{Diagram 1: } e \xrightarrow{Q_e} e + \gamma \xrightarrow{Q_q} q \\ \text{Diagram 2: } e \xrightarrow{(v_e, a_e)} e + Z \xrightarrow{(v_q, a_q)} q \end{array} \right|^2$$



Sensitivity through propagator

CHARGED  
CURRENTS  
INTERACTIONS  
AND  
W PROPAGATOR  
AT HIGH  $Q^2$

# Charged Current Cross-Sections

---

Cross Section for  $e^+ p \rightarrow \bar{\nu} X$  :

$$\frac{d^2\sigma}{dxdQ^2} = \frac{G_F^2}{2\pi} \frac{1}{(1 + Q^2/M_W^2)^2} (\bar{u} + \bar{c} + (1 - y)^2(d + s))$$

- Propagator dependence  $\Rightarrow$  W mass determination
  - H1 (94-97):  $81.2 \pm 3.3 \pm 4.3$  GeV
  - ZEUS (94-97):  $78.6^{+2.5+3.3}_{-2.4-3.0}$  GeV
- parton densities  $\Rightarrow$  sensitivity to  $d$ -quark density
- helicity dependence  $\Rightarrow$  V-A coupling
- QED radiative Corrections ( $< 10\%$ ) applied

Reduced Charged Current Cross-Section:

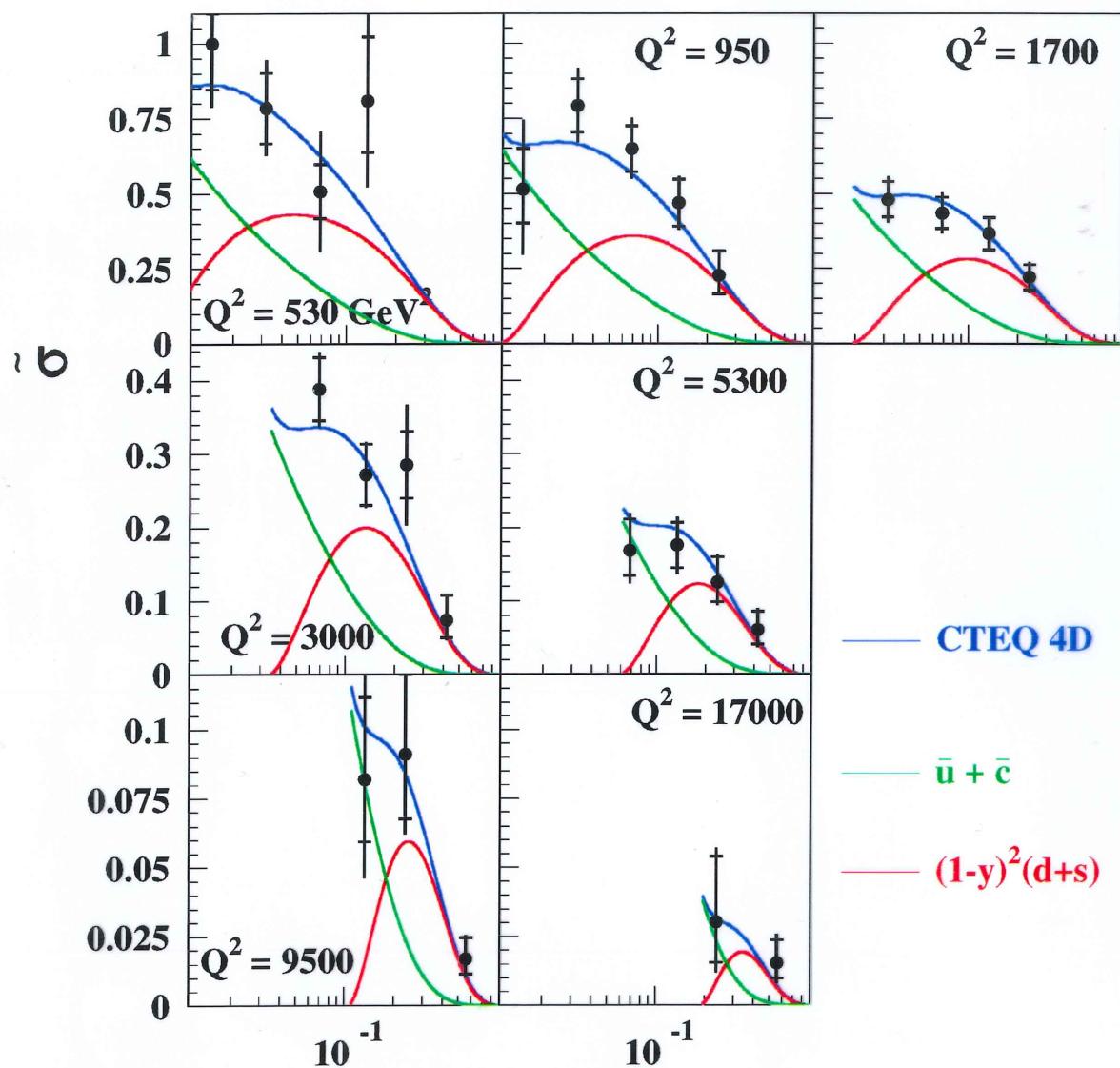
$$\begin{aligned}\sigma_{CC} &\equiv x \cdot \frac{2\pi}{G_F^2} (1 + Q^2/M_W^2)^2 \frac{d^2\sigma}{dxdQ^2} \\ &= x \cdot (\bar{u} + \bar{c} + (1 - y)^2(d + s)) \text{ in QPM}\end{aligned}$$

- definition in analogy to the Reduced Neutral Current Cross-Section
- different relation to the parton densities:  
supression of the valence quark contribution at high  $y$  due to the helicity factor

$$d^2\sigma^{CC}/dxdQ^2$$

$$\frac{d^2\sigma_{e+p}}{dx dQ^2} \simeq \frac{G_F^2}{2\pi} \frac{1}{(1+Q^2/M_W^2)^2} [\bar{u} + \bar{c} + (1-y)^2(d+s)]$$

**ZEUS CC Preliminary 1994-97**

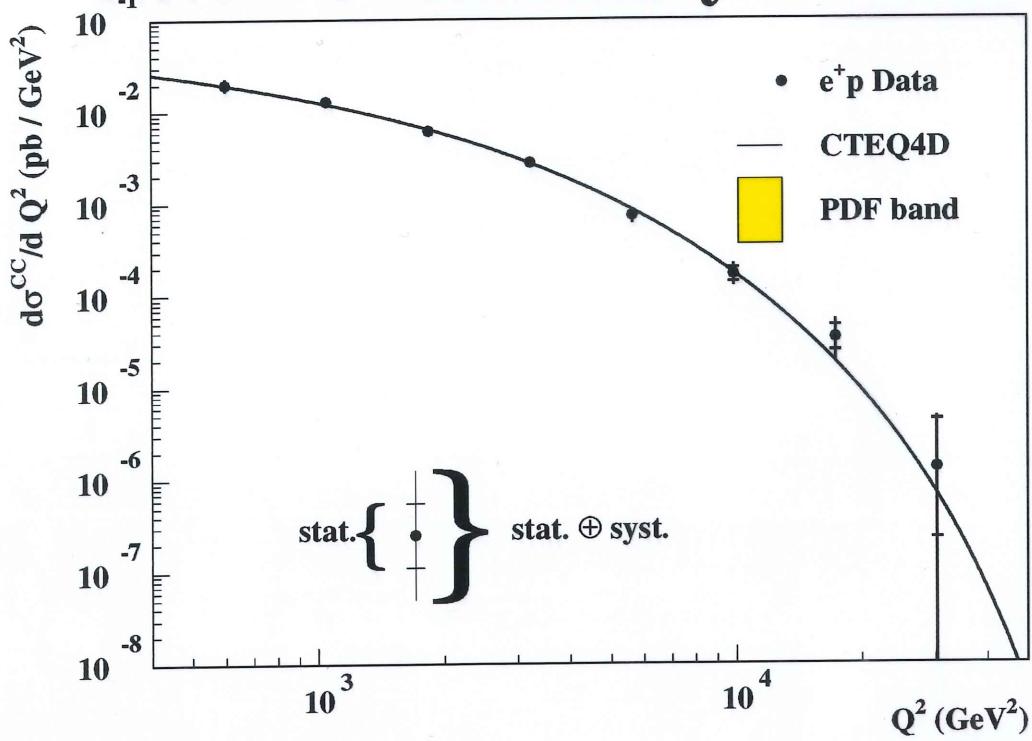


Good agreement with Standard Model

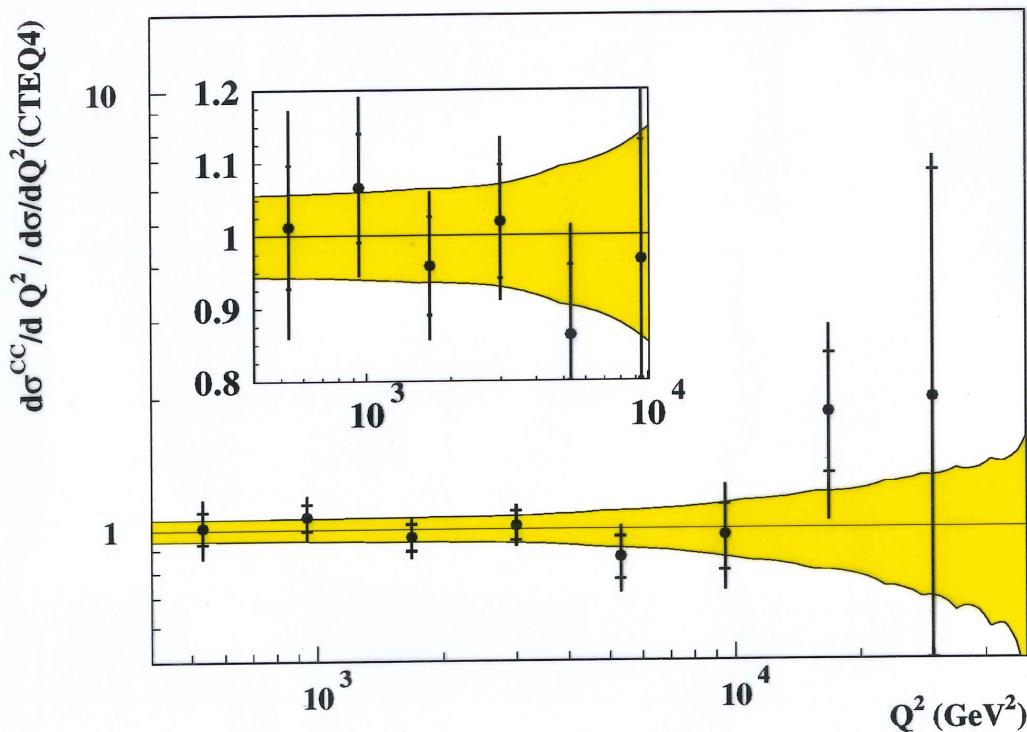
Sensitivity to  $d$  and sea

$$d\sigma^{CC}/dQ^2$$

## ZEUS Preliminary 1994-97

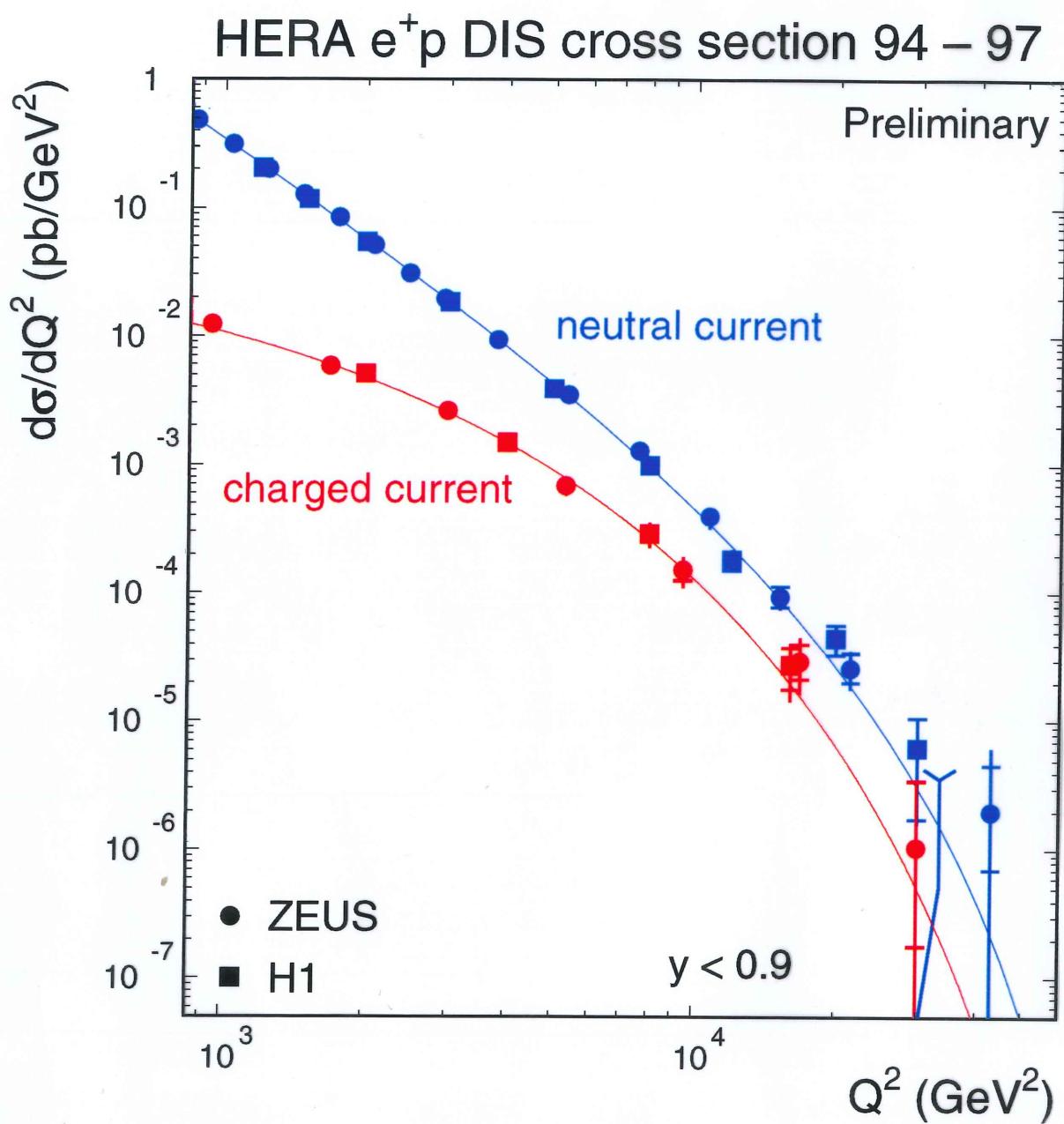


Test of  
EW  
propaga-  
tor



Good agreement with Standard Model  
up to  $Q^2 \simeq 10,000$  GeV<sup>2</sup>

# High $Q^2$ Cross Sections



RUNNING

'98 , '99

WITH

$e^-$  (27.5 GeV)

AND

p (920 GeV)

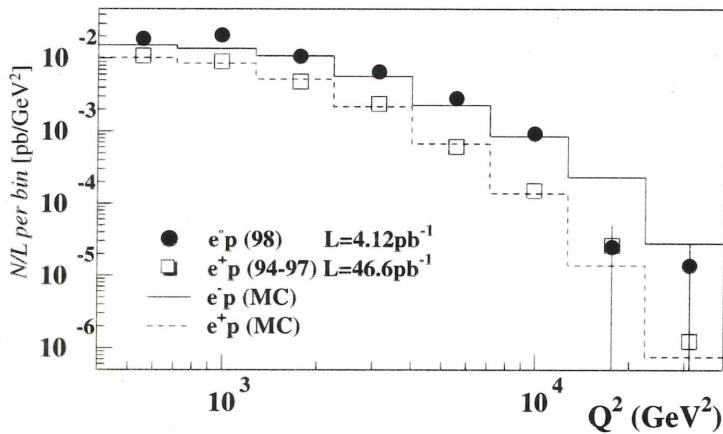
# Running in 1998

(A Different Machine!)

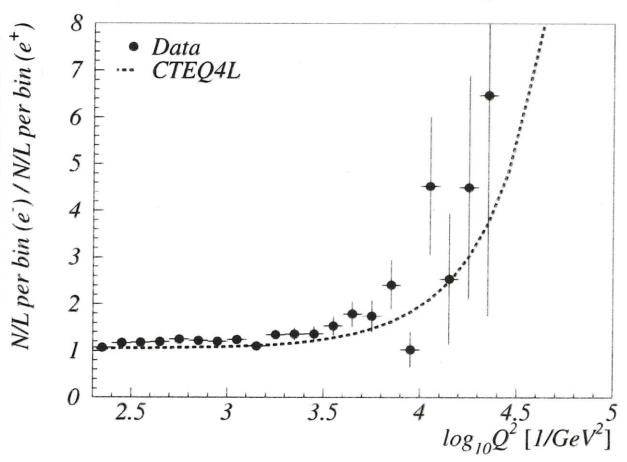
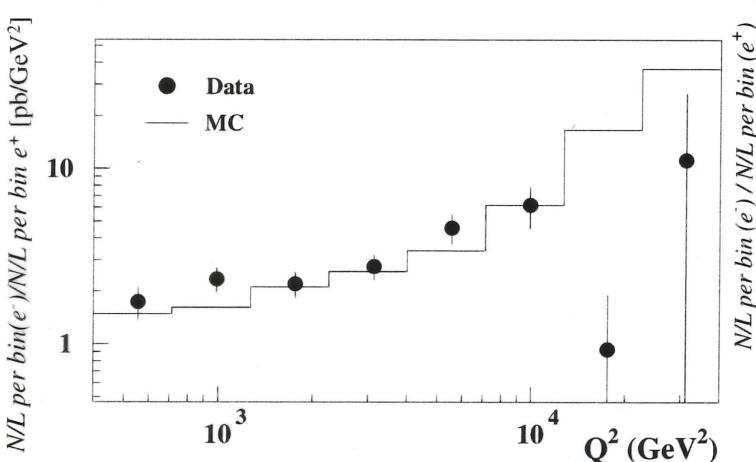
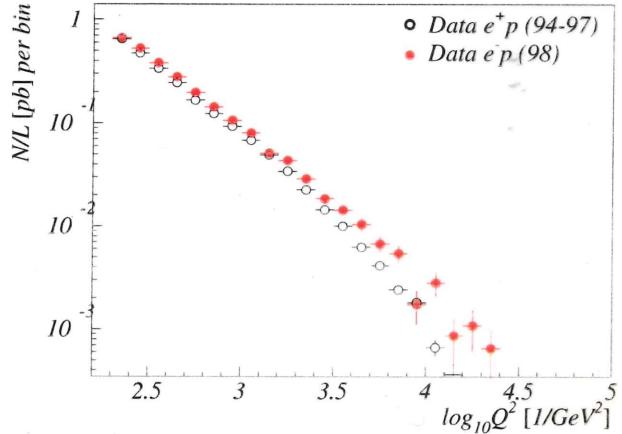
- *Electrons on Protons*
- *Proton Energy = 920 GeV*

*ZEUS (in progress)*

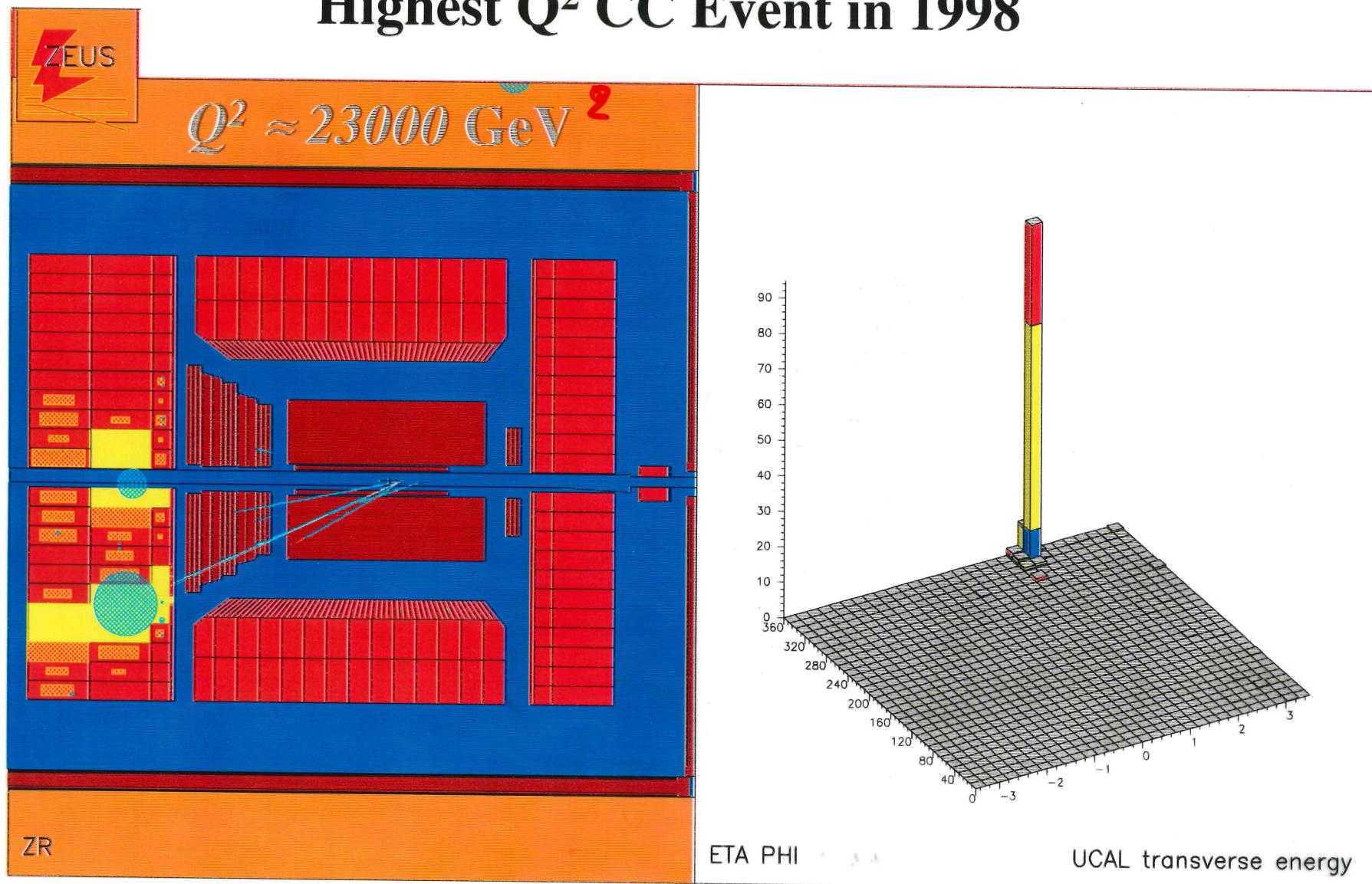
*Charged Currents*



*Neutral Currents*



# Highest $Q^2$ CC Event in 1998



# H1 (in progress)

E. Ei sen

PRC 13.1.1999

## e<sup>-</sup> / e<sup>+</sup> Comparison

e<sup>-</sup> beams have an easier time to find a matching parton in the proton

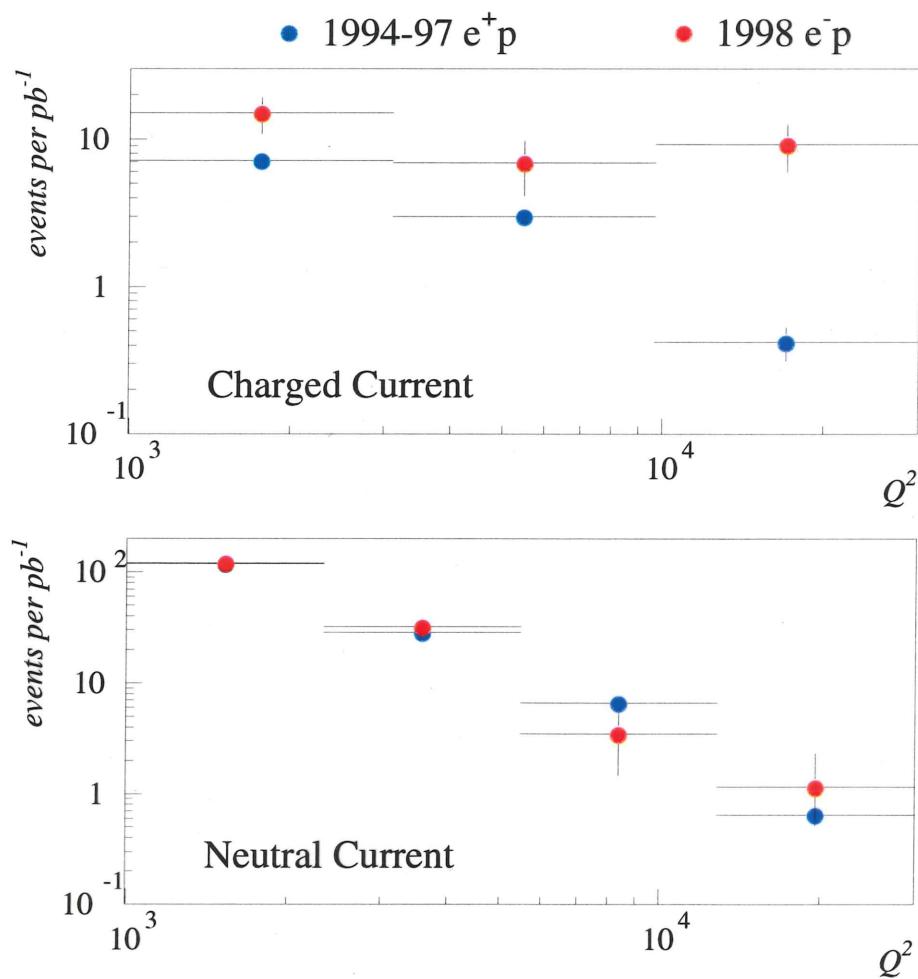
- Standard Model Cross sections for  $Q^2 > 10000 \text{ GeV}^2$

NC

$$\frac{\sigma(e^- p \rightarrow e^- X)_{920 \text{ GeV}}}{\sigma(e^+ p \rightarrow e^+ X)_{820 \text{ GeV}}} = 2.3$$

CC

$$\frac{\sigma(e^- p \rightarrow \nu X)_{920 \text{ GeV}}}{\sigma(e^+ p \rightarrow \nu X)_{820 \text{ GeV}}} = 11.0$$





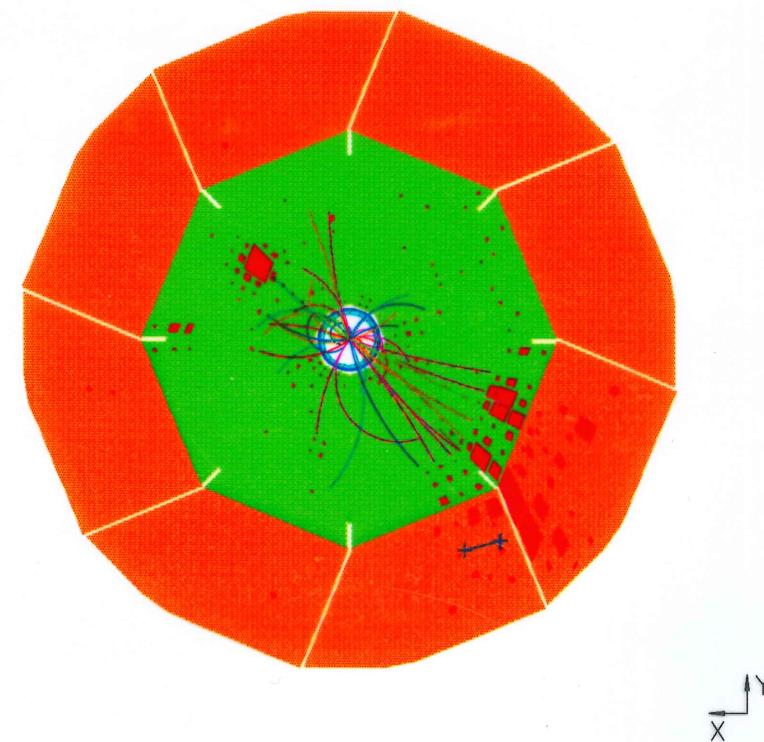
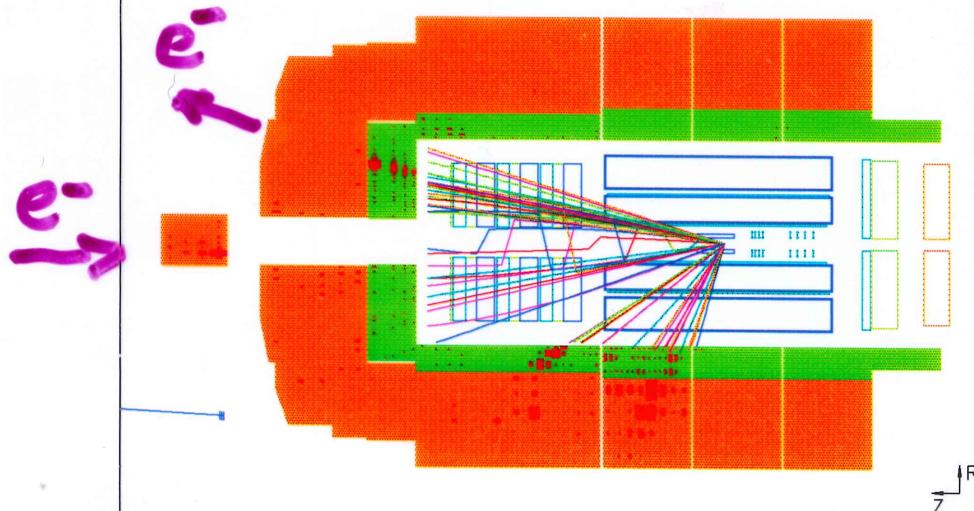
Run 229365 Event 96751 Class: 4 5 6 7 8 11 19 22 26 28 29 Date 16/02/1999

H1 Event Display 1.17/03  
DSN=/data\_98/data/CDST1.C98.PRESEL.DST, INDEX

E = -27.6 x 820.0 GeV B=11.6 kG

AST (DMIS) = 0 D 0 0 0  
RST (DMIS) = C0 D 0 0 0

$$Q^2 \approx 41.000 \text{ GeV}^2$$



# FUTURE

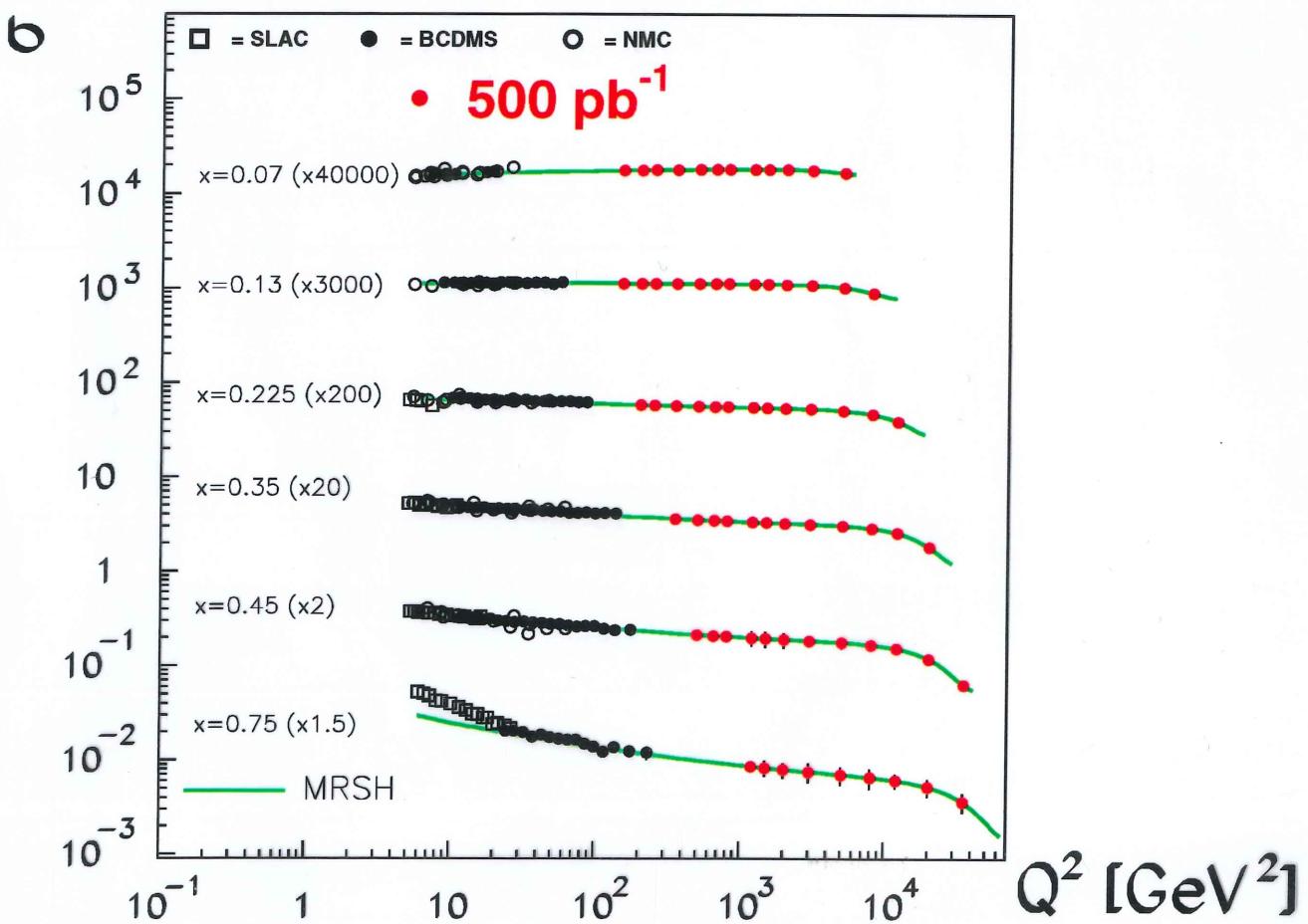
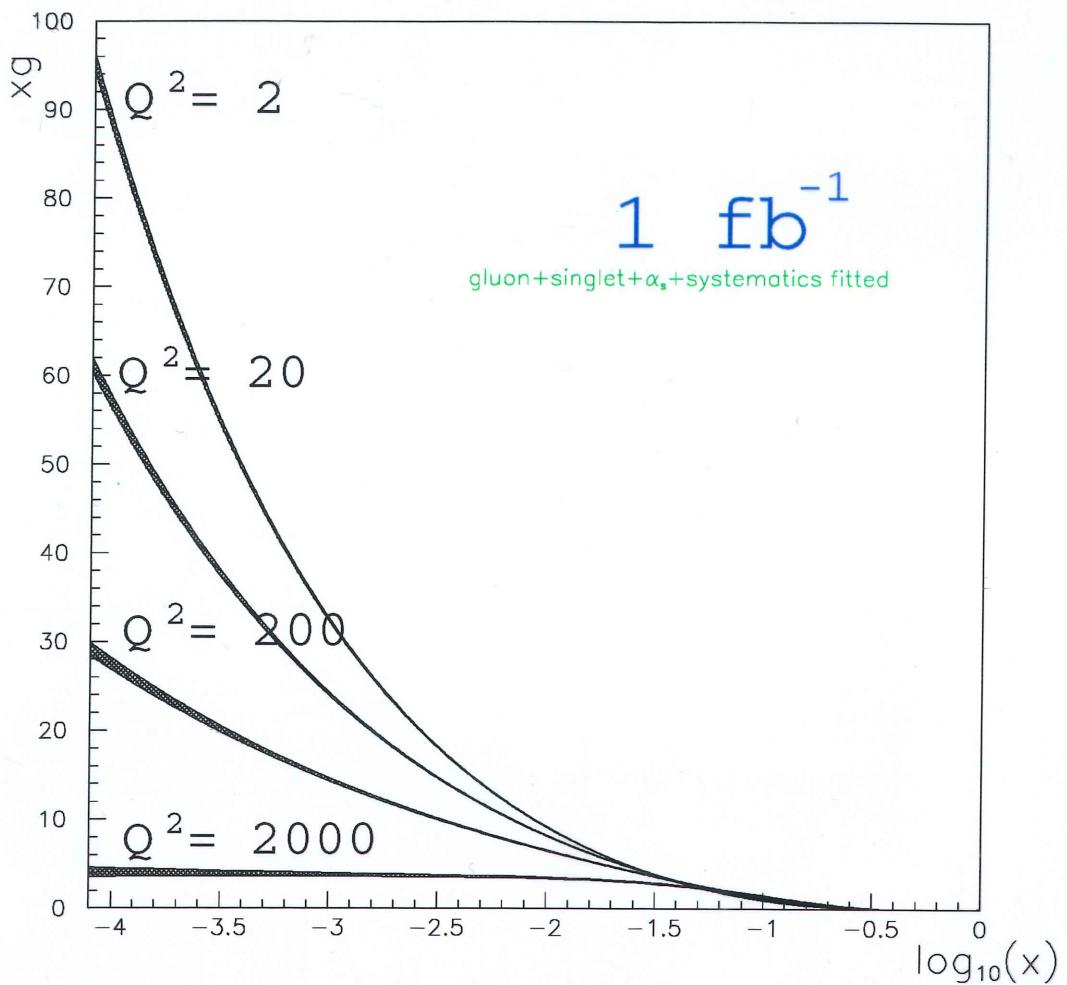
2000 - 2001

Luminosity upgrade ( $\times\sim 5$ )

$$\mathcal{L} \approx 100 \text{ pb}^{-1}/\text{year}$$

Electron polarization

- New phenomena
- Rare effects
- Electroweak physics
- Precise systematics



# SUMMARY

- Proton being probed down to  $\sim 1.5/1000$  of  $r_p$
- 5 order of magnitudes in  $Q^2$  and  $x$  measured.
- Experimental agreement between H1, ZEUS, fixed target.
- NLO QCD fits, with DGLAP evolution, good in the range  $1 < Q^2 < 10^4 \text{ GeV}^2$
- Gluon density measurement confirmed in 4 different ways; at various  $Q^2$
- $F^C$  contribution sizable and rising with  $Q^2$
- $F_L$  different from zero.
- $Z_0$  contribution observed.
- Very high  $Q^2$ : a little more than expected .
- CC agree with SM. Test of W propagator at high  $Q^2$ : a novel aspect.
- Recent exper. interest for very low  $Q^2$  physics; transition region between perturbative and non pert. physics studied.
- '98 - '99  $e^-$  runs will provide  $e^-$  data comparable in statistics with previous  $e^+$  ones.
- Future: luminosity upgrade 2000-2001;  $500 \text{ pb}^{-1}$  possible;  
--> new physics; precise systematics.

Thanks to our friend Bjoern Wiik !