

The final H1+ZEUS combined inclusive data and HERAPDF2.0

Eur.Phys.J.C75 (2015) 12, 580 [[arxiv:1506.06042](https://arxiv.org/abs/1506.06042)]

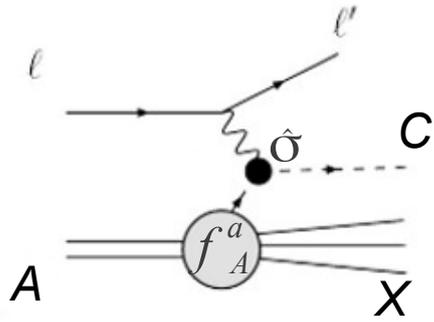
Volodymyr Myronenko
DESY

on behalf of
H1 and ZEUS collaborations

Rencontres de Moriond
La Thuile, Italy 2016

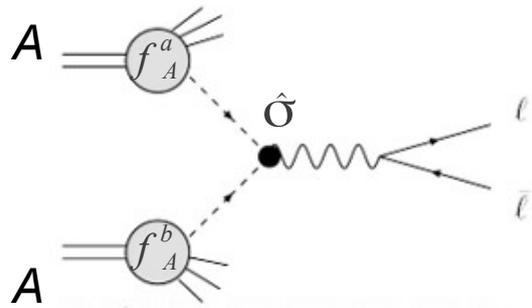


PDFs for the precision measurements



◆ Factorisation theorem: PDFs + hard-scattering cross section

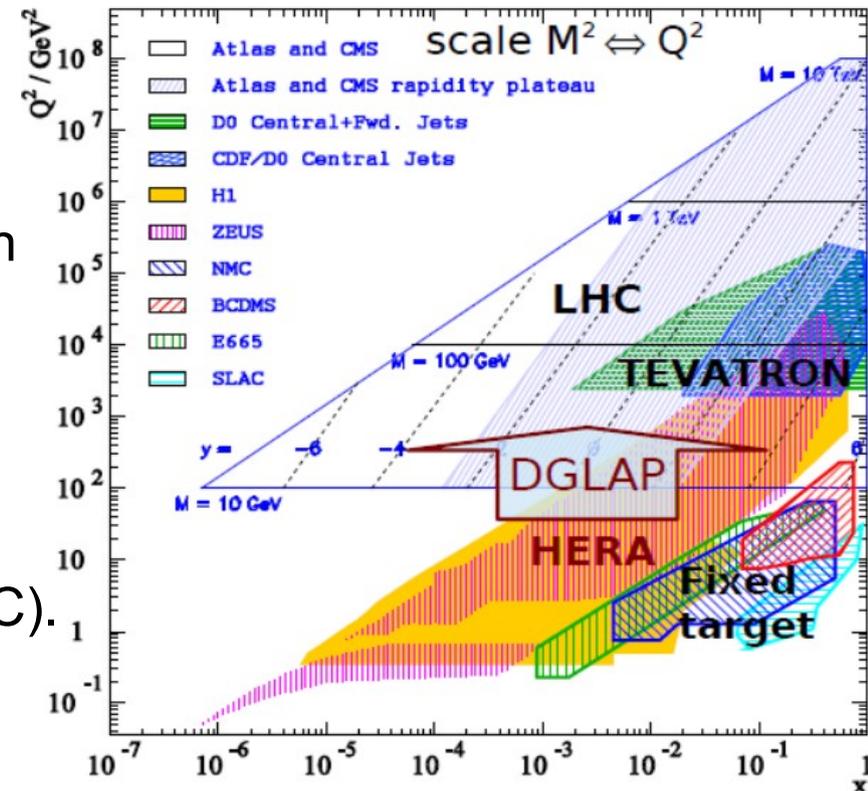
$$\sigma_{A \rightarrow C}^i(q, p) = \sum_a \int_x^1 d\xi f_A^a(\xi, \mu) \hat{\sigma}_{a \rightarrow C}^i(q, \xi p, \mu, \alpha_s)$$



◆ PDFs are **universal** => essential for precision measurements.

◆ HERA data is a core of every PDF determination

- ◆ Covers wide kinematic range
- ◆ Probes linear combination of quarks.
- ◆ Sensitive to the quark flavor decomposition (CC).
- ◆ Information on the gluon content of proton

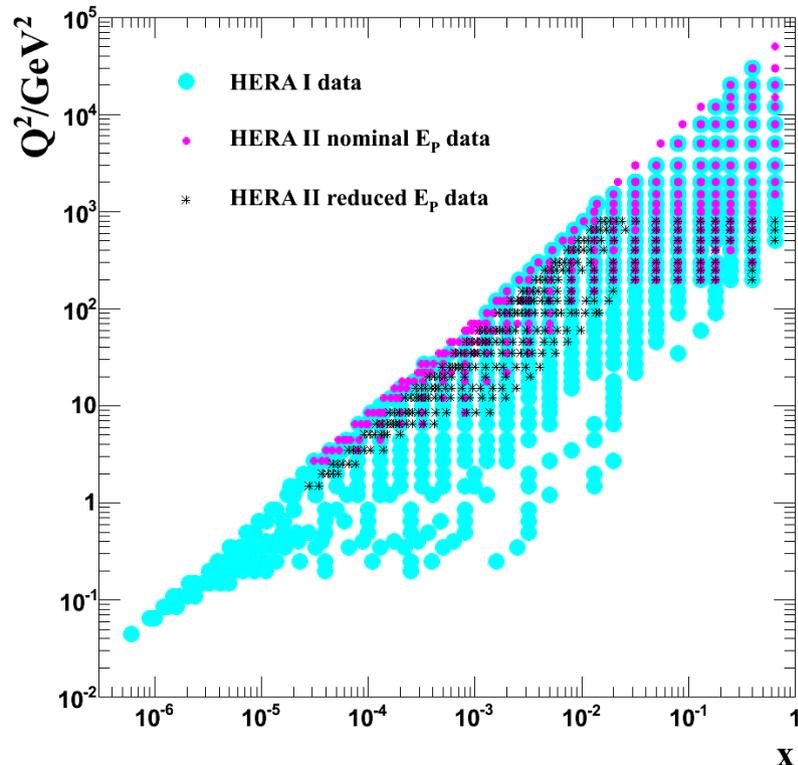


Full HERA data combination

HERAPDF1.0

HERAPDF1.5

HERAPDF2.0



Data Set		x_{Bj} Grid		Q^2 [GeV ²] Grid		\mathcal{L} pb ⁻¹	e^+/e^-	\sqrt{s} GeV
		from	to	from	to			
HERA I $E_p = 820$ GeV and $E_p = 920$ GeV data sets								
H1 svx-mb	95-00	0.000005	0.02	0.2	12	2.1	e^+p	301, 319
H1 low Q^2	96-00	0.0002	0.1	12	150	22	e^+p	301, 319
H1 NC	94-97	0.0032	0.65	150	30000	35.6	e^+p	301
H1 CC	94-97	0.013	0.40	300	15000	35.6	e^+p	301
H1 NC	98-99	0.0032	0.65	150	30000	16.4	e^-p	319
H1 CC	98-99	0.013	0.40	300	15000	16.4	e^-p	319
H1 NC HY	98-99	0.0013	0.01	100	800	16.4	e^-p	319
H1 NC	99-00	0.0013	0.65	100	30000	65.2	e^+p	319
H1 CC	99-00	0.013	0.40	300	15000	65.2	e^+p	319
ZEUS BPC	95	0.000002	0.00006	0.11	0.65	1.65	e^+p	300
ZEUS BPT	97	0.0000006	0.001	0.045	0.65	3.9	e^+p	300
ZEUS SVX	95	0.000012	0.0019	0.6	17	0.2	e^+p	300
ZEUS NC	96-97	0.00006	0.65	2.7	30000	30.0	e^+p	300
ZEUS CC	94-97	0.015	0.42	280	17000	47.7	e^+p	300
ZEUS NC	98-99	0.005	0.65	200	30000	15.9	e^-p	318
ZEUS CC	98-99	0.015	0.42	280	30000	16.4	e^-p	318
ZEUS NC	99-00	0.005	0.65	200	30000	63.2	e^+p	318
ZEUS CC	99-00	0.008	0.42	280	17000	60.9	e^+p	318
HERA II $E_p = 920$ GeV data sets								
H1 NC ^{1.5p}	03-07	0.0008	0.65	60	30000	182	e^+p	319
H1 CC ^{1.5p}	03-07	0.008	0.40	300	15000	182	e^+p	319
H1 NC ^{1.5p}	03-07	0.0008	0.65	60	50000	151.7	e^-p	319
H1 CC ^{1.5p}	03-07	0.008	0.40	300	30000	151.7	e^-p	319
H1 NC med Q^2 ^{*y.5}	03-07	0.0000986	0.005	8.5	90	97.6	e^+p	319
H1 NC low Q^2 ^{*y.5}	03-07	0.000029	0.00032	2.5	12	5.9	e^+p	319
ZEUS NC	06-07	0.005	0.65	200	30000	135.5	e^+p	318
ZEUS CC ^{1.5p}	06-07	0.0078	0.42	280	30000	132	e^+p	318
ZEUS NC ^{1.5}	05-06	0.005	0.65	200	30000	169.9	e^-p	318
ZEUS CC ^{1.5}	04-06	0.015	0.65	280	30000	175	e^-p	318
ZEUS NC nominal ^{*y}	06-07	0.000092	0.008343	7	110	44.5	e^+p	318
ZEUS NC satellite ^{*y}	06-07	0.000071	0.008343	5	110	44.5	e^+p	318
HERA II $E_p = 575$ GeV data sets								
H1 NC high Q^2	07	0.00065	0.65	35	800	5.4	e^+p	252
H1 NC low Q^2	07	0.0000279	0.0148	1.5	90	5.9	e^+p	252
ZEUS NC nominal	07	0.000147	0.013349	7	110	7.1	e^+p	251
ZEUS NC satellite	07	0.000125	0.013349	5	110	7.1	e^+p	251
HERA II $E_p = 460$ GeV data sets								
H1 NC high Q^2	07	0.00081	0.65	35	800	11.8	e^+p	225
H1 NC low Q^2	07	0.0000348	0.0148	1.5	90	12.2	e^+p	225
ZEUS NC nominal	07	0.000184	0.016686	7	110	13.9	e^+p	225
ZEUS NC satellite	07	0.000143	0.016686	5	110	13.9	e^+p	225

Full HERA I data

HERA II data HER

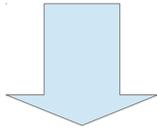
HERA II data LER

◆ All inclusive DIS results are final and published!

Combining measurements

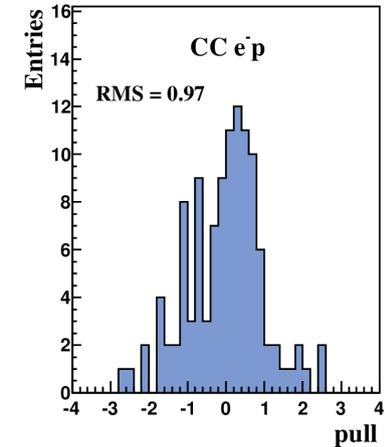
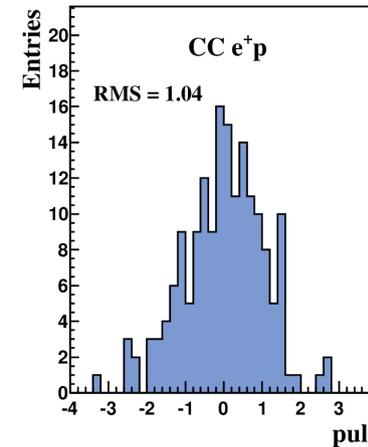
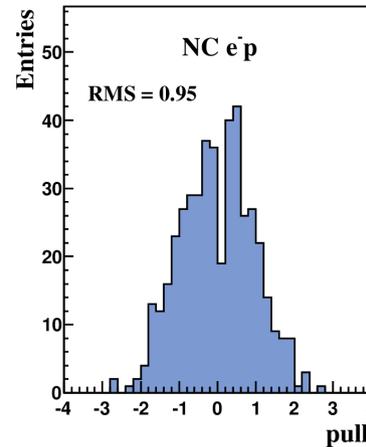
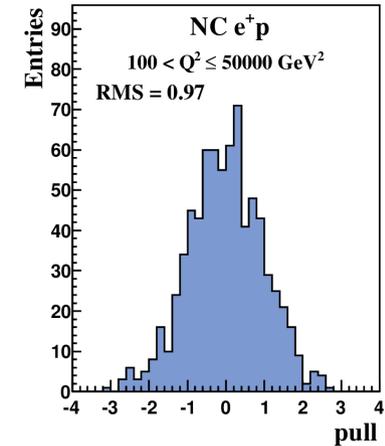
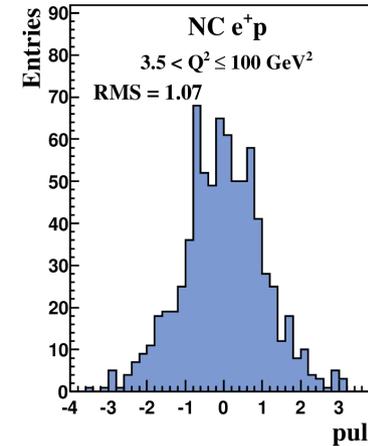
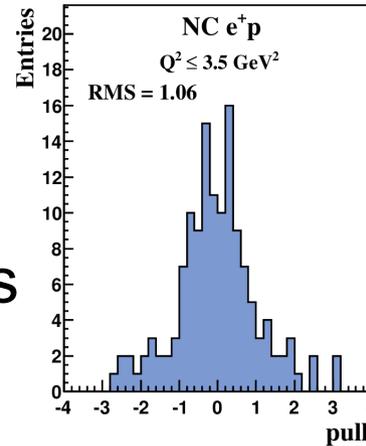
H1 and ZEUS

2927 original measurements



1307 averaged measurements

$$p^{i,k} = \frac{\mu^{i,k} - \mu^{i,ave} (1 - \sum_j \gamma_j^{i,k} b_{j,ave})}{\sqrt{\Delta_{i,k}^2 - \Delta_{i,ave}^2}}$$



Consistant data sets: **total $\chi^2/\text{ndf} = 1685/1620$.**

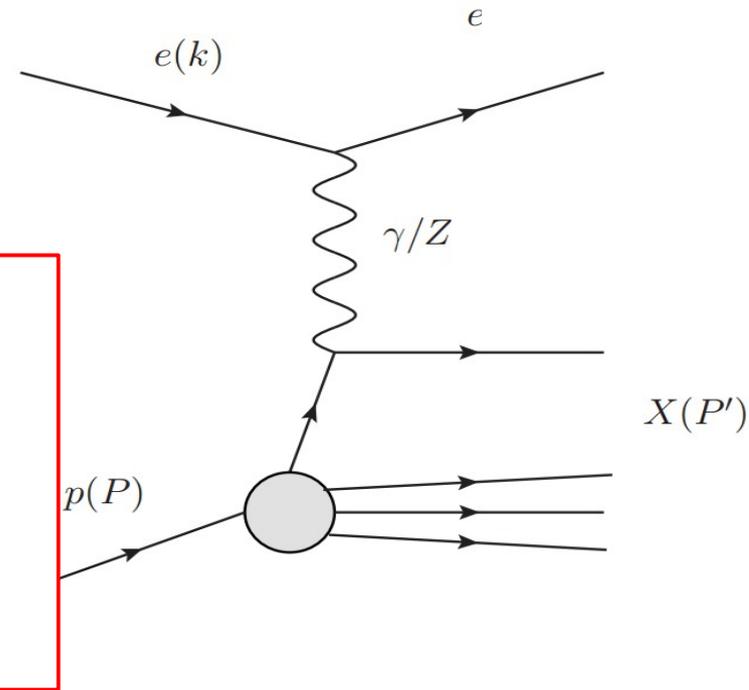
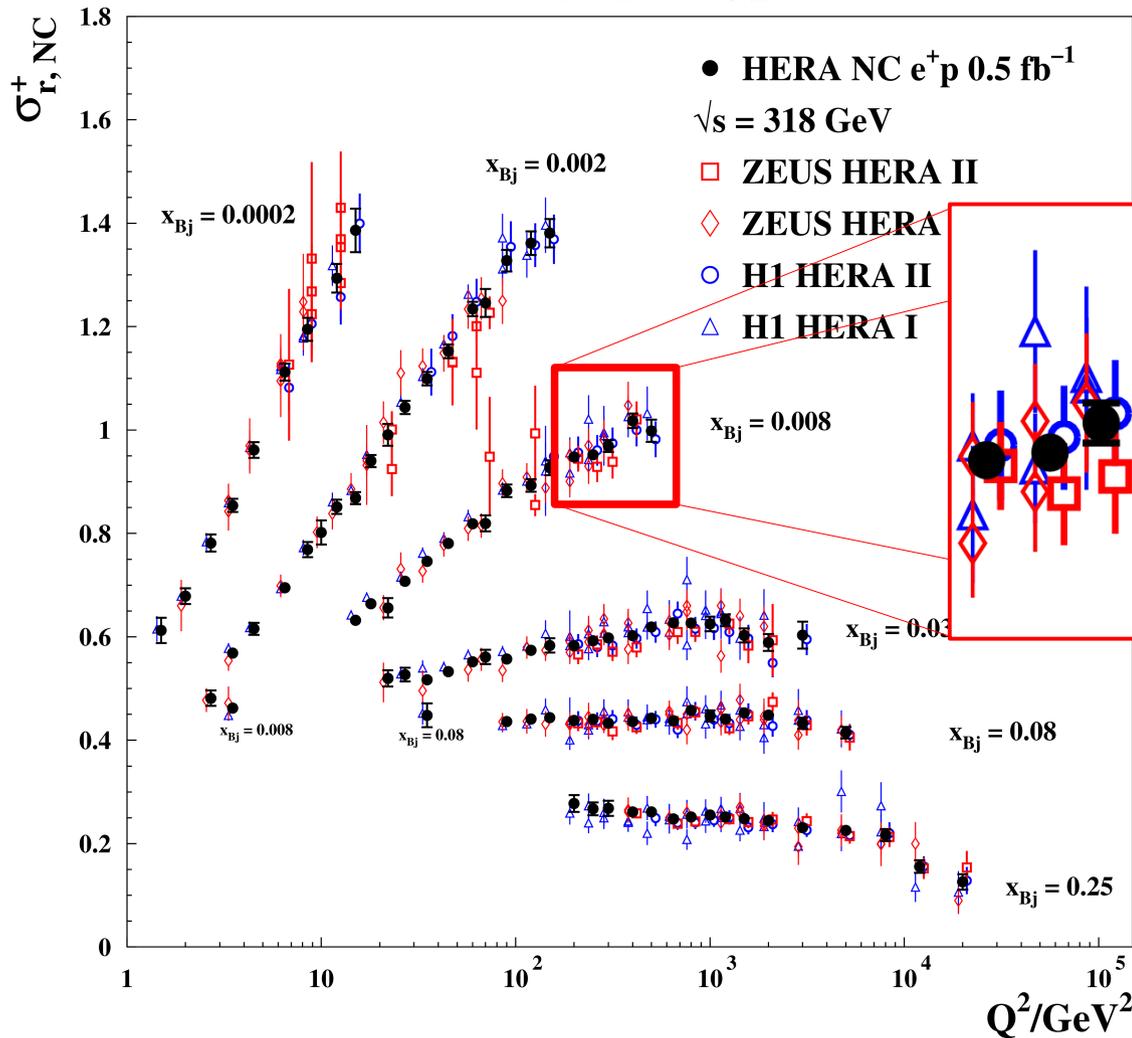
◆ Correlations of systematic uncertainties considered.

◆ Procedural uncertainties $\sim 1\%$.

Combined reduced cross-sections

$$\sigma_{r,NC}^{\pm} = \frac{Q^4 x}{2\pi\alpha^2 Y_{\pm}} \frac{d^2 \sigma_{NC}^{e^{\pm}p}}{dx dQ^2} = \tilde{F}_2^{\mp} \frac{Y}{Y_{\pm}} x \tilde{F}_3 - \frac{y^2}{Y_{\pm}} \tilde{F}_L \quad Y_{\pm} = 1 \pm (1-y)^2$$

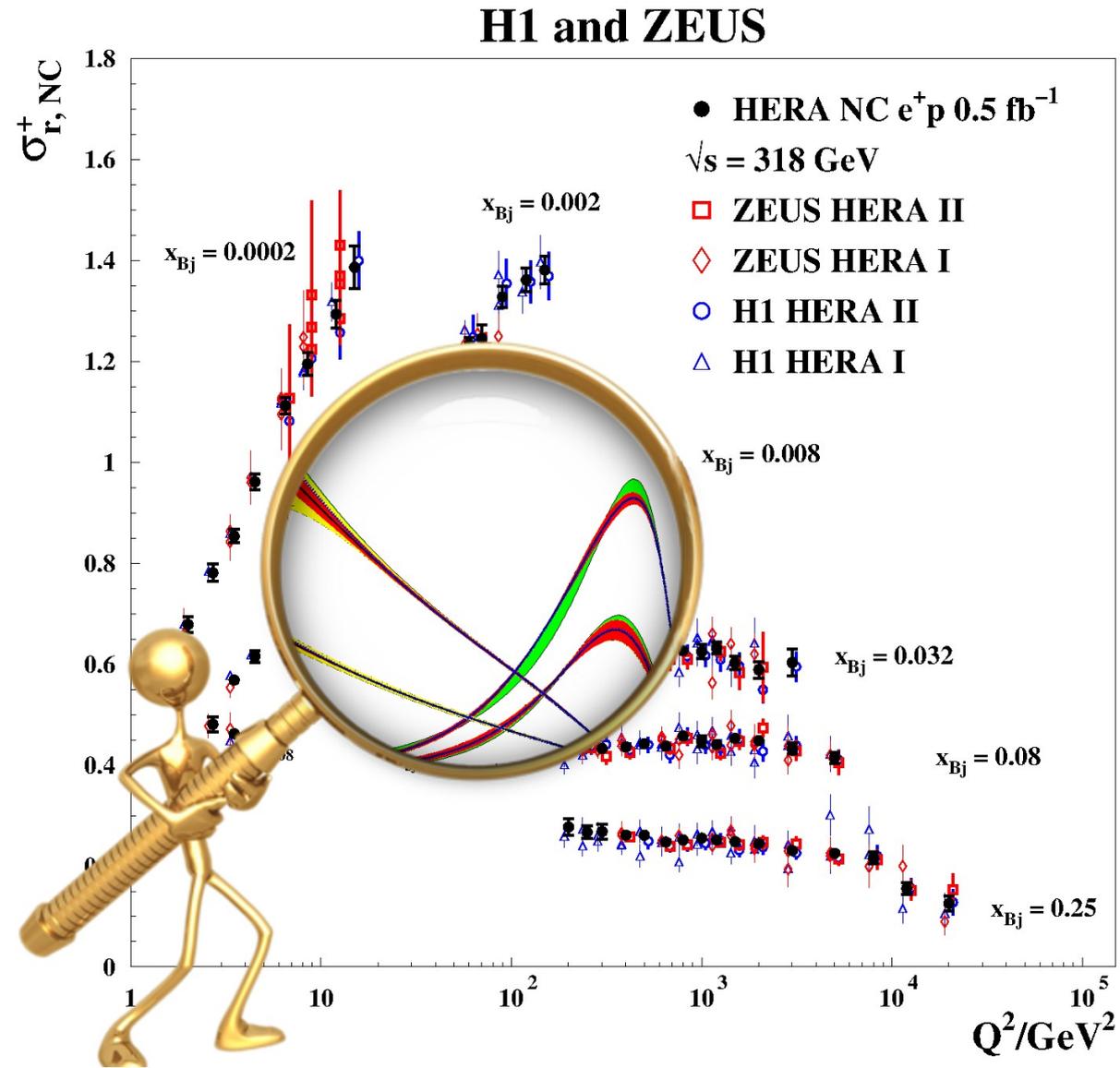
H1 and ZEUS



◆ Up to ~6 measurements averaged.

◆ High precision achieved.

Extraction of PDFs from inclusive data



HERAPDF2.0: settings for QCD fit

- ◆ The fit is performed using the **HERA data only**.
- ◆ QCD fits are performed using **HERAFitter package** www.herafitter.org
- ◆ PDFs (**14p**) are parametrised at $Q_0^2 = 1.9 \text{ GeV}^2$



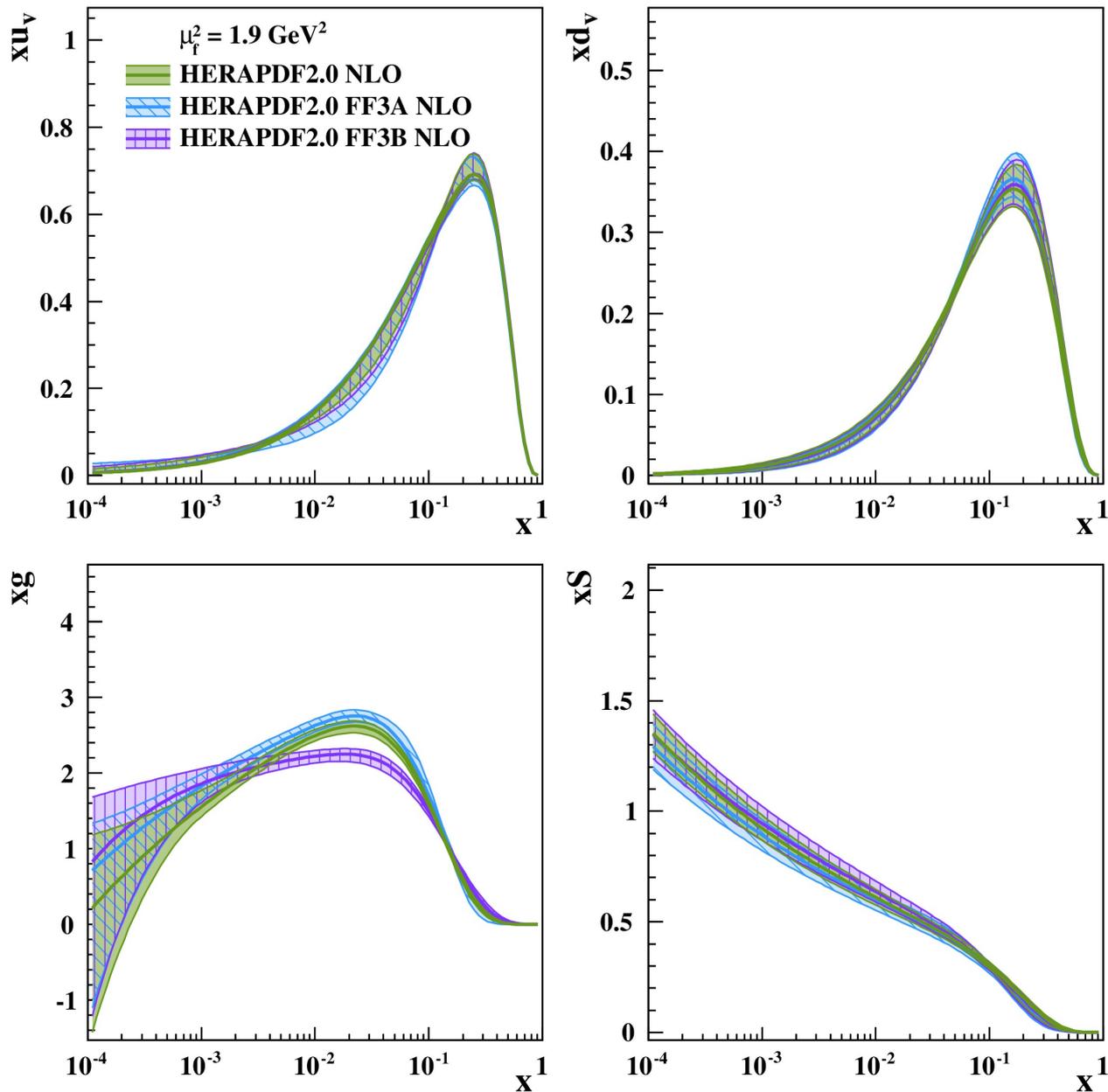
$$xf(x) = Ax^B(1-x)^C(1+Dx+Ex^2)$$

$$xg(x), xu_v(x), xd_v(x), x\bar{U}(x), x\bar{D}(x)$$

- ◆ PDF evolution is performed using **DGLAP** equations
- ◆ Heavy flavour coefficients are obtained within **GM VFNS (RT OPT)**

HERAPDF2.0 and variants

H1 and ZEUS



◆ Data above:

◆ $Q_{\min}^2 = 3.5 \text{ GeV}^2$

◆ $Q_{\min}^2 = 10 \text{ GeV}^2$

◆ Orders of calculation:

◆ LO

◆ NLO

◆ NNLO

◆ HF schemes:

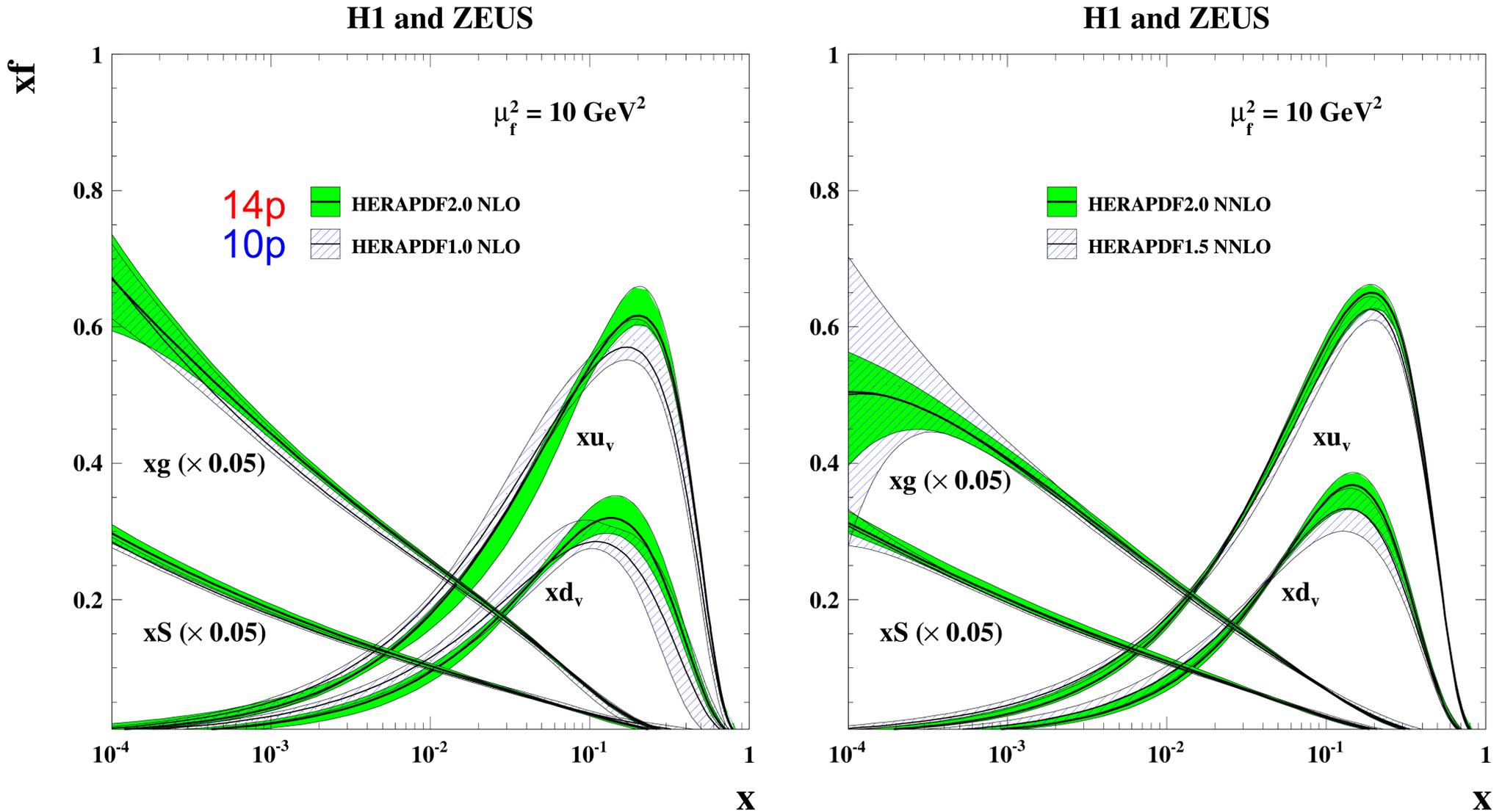
◆ GM VFNS (RTOPT)

◆ FF3A / FF3B

◆ Various α_s as input

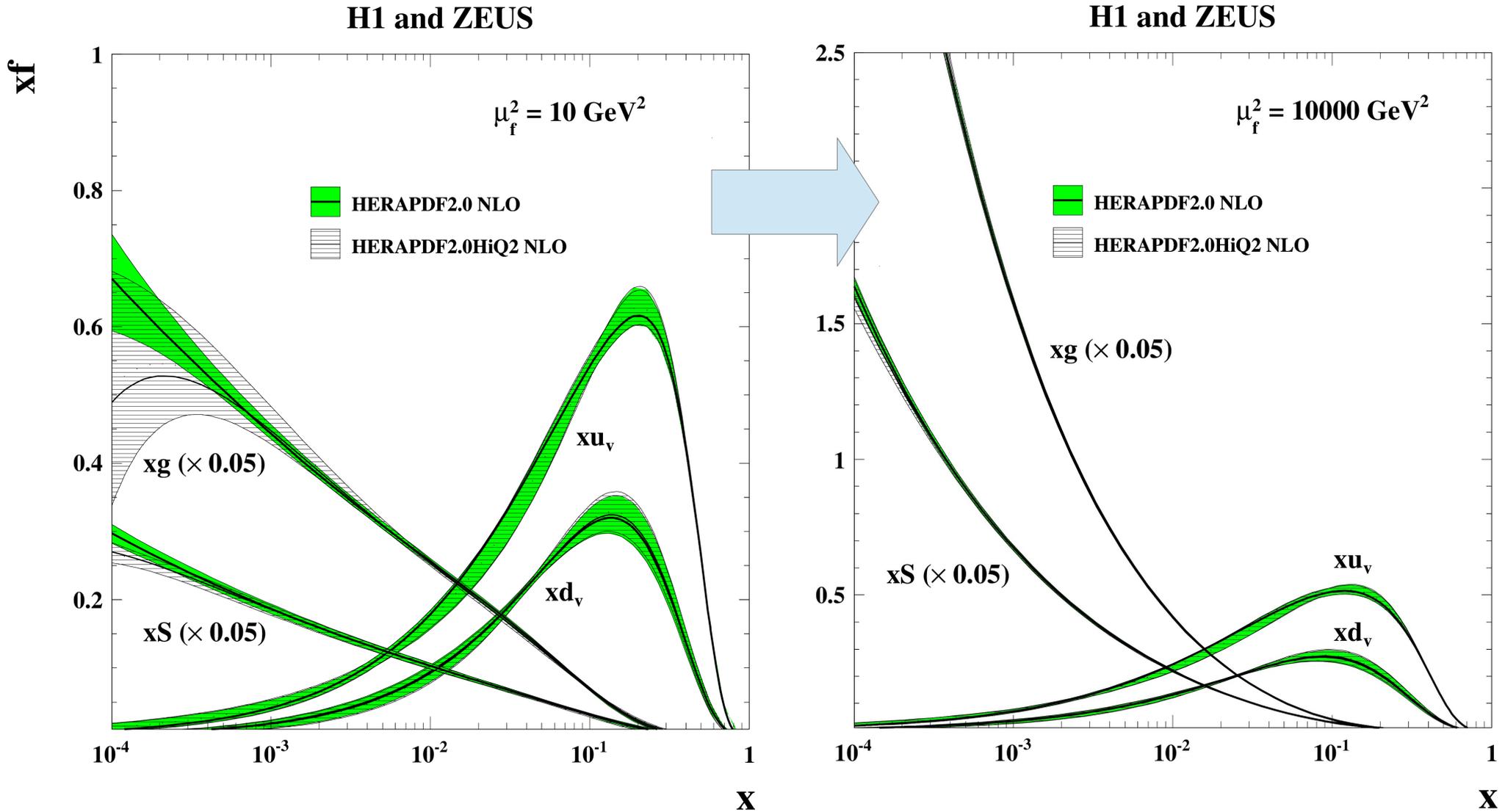
◆ Various gluon parametrisations.

HERAPDF1.0 vs HERAPDF2.0



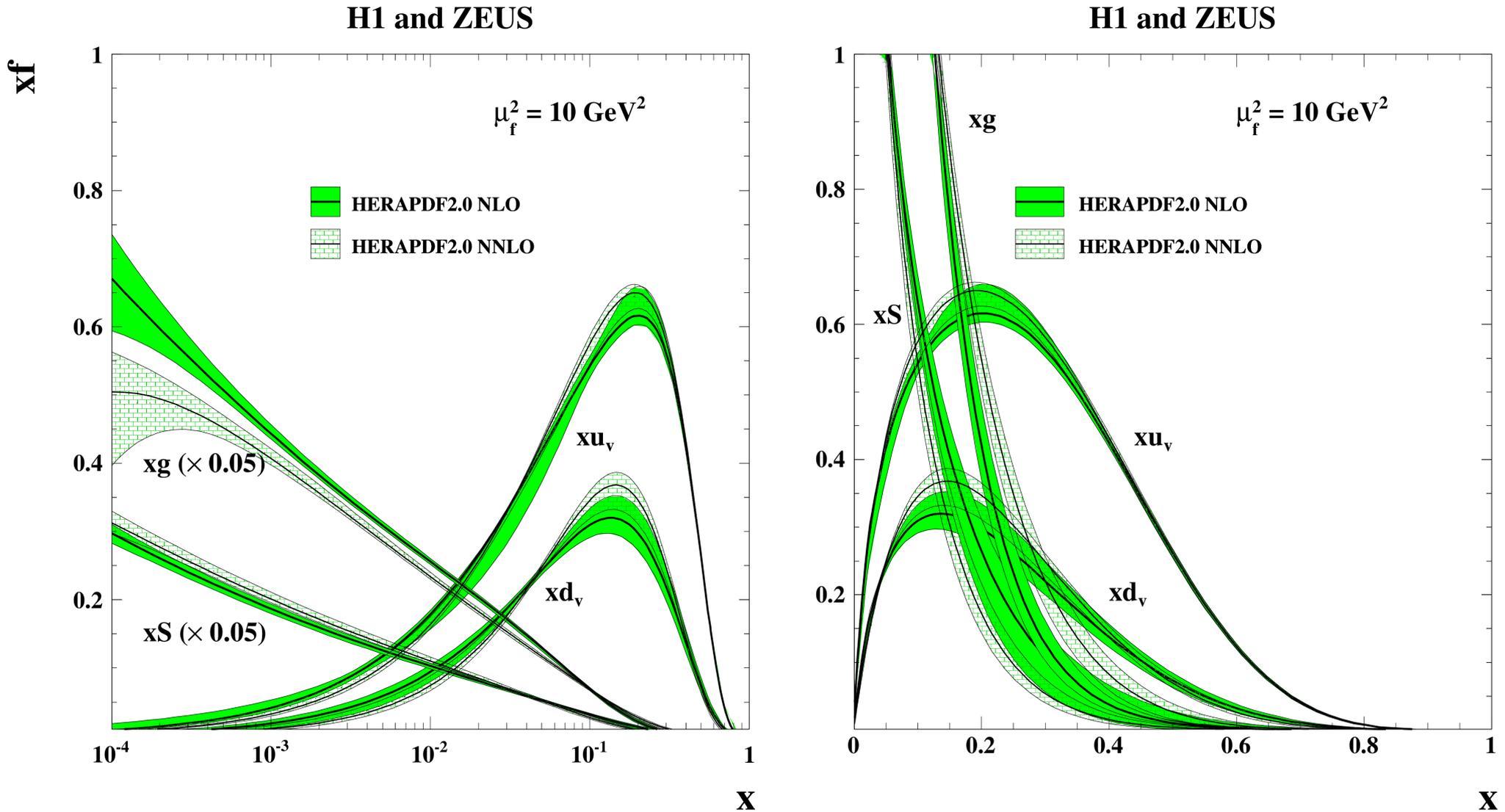
- ◆ Valence are more peaked and precise at HERAPDF2.0 (new data).
- ◆ Smaller uncertainties at high x .

HERAPDF2.0 vs HERAPDF2.0HiQ2



- Larger uncertainty for HERAPDF2.0HiQ2 gluon at low x .
- PDFs very alike at higher scales \Rightarrow similar predictions at LHC domain.

HERAPDF2.0: NLO vs NNLO fits



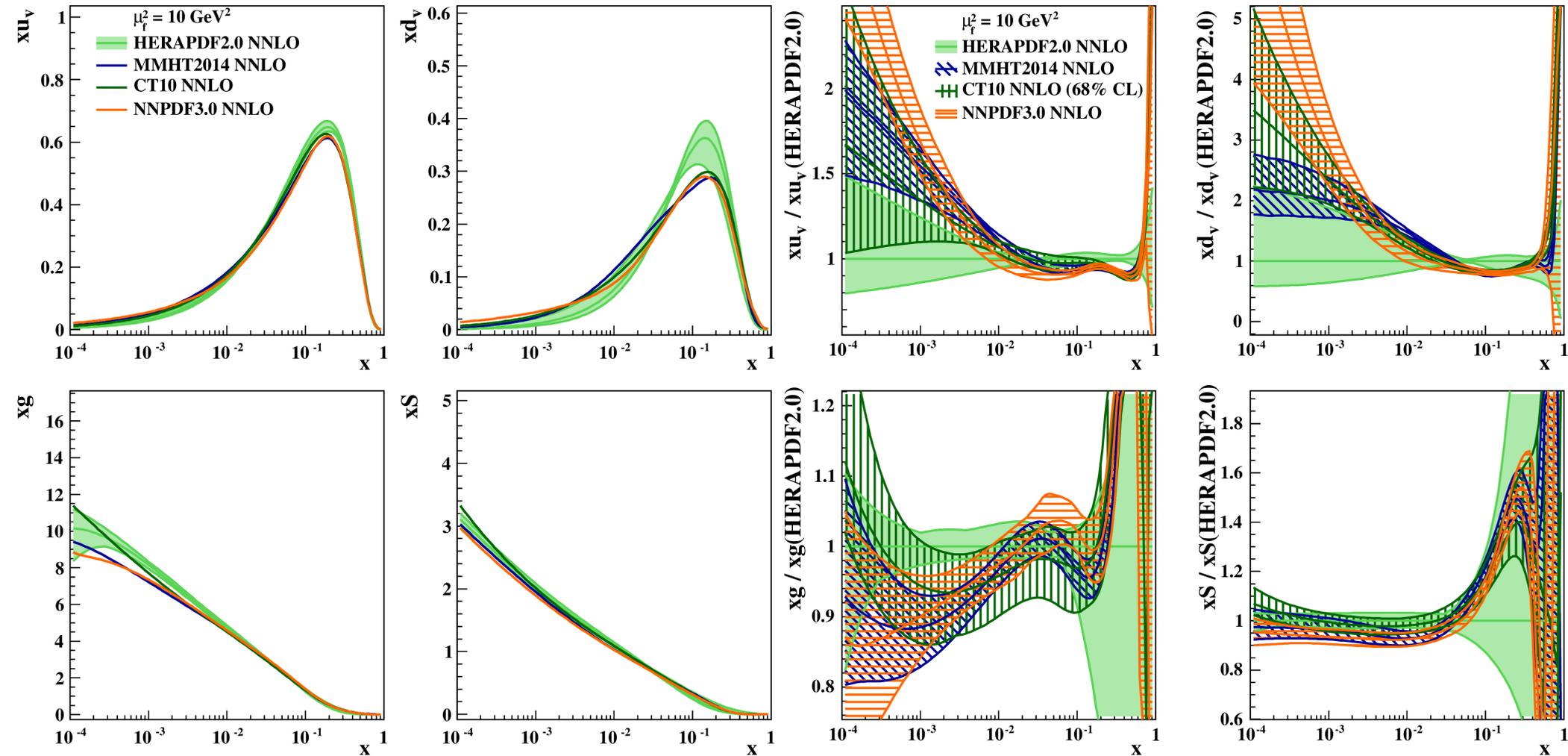
◆ Valence distributions look similar.

◆ Gluons are a bit shifted.

HERAPDF2.0 vs other PDFs

H1 and ZEUS

H1 and ZEUS



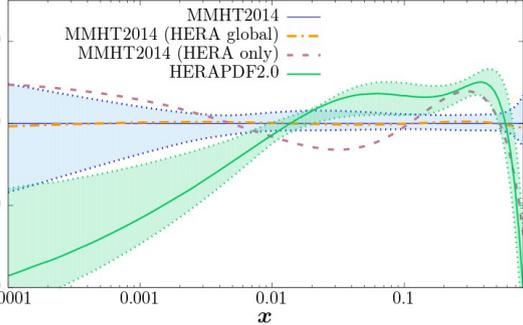
◆ The largest difference - xu_v at $x \approx 0.4$ (2.5σ).

◆ Various gluon behaviours at low x .

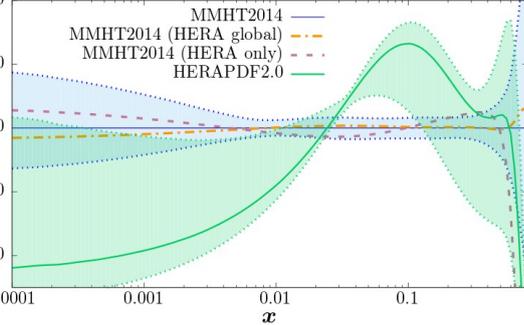


HERA data in global fits

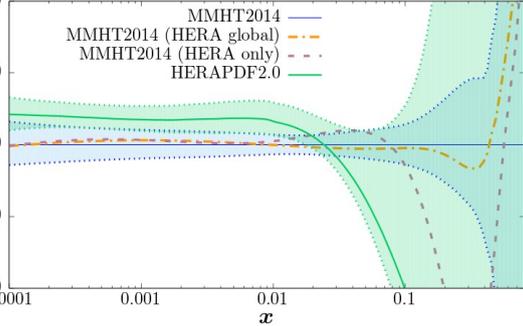
Up valence (NNLO), percentage difference at $Q^2 = 10 \text{ GeV}^2$



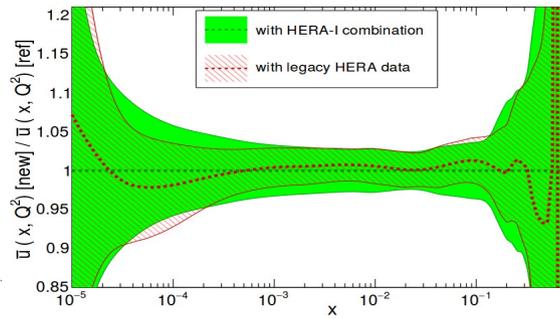
Down valence (NNLO), percentage difference at $Q^2 = 10 \text{ GeV}^2$



Light sea (NNLO), percentage difference at $Q^2 = 10 \text{ GeV}^2$

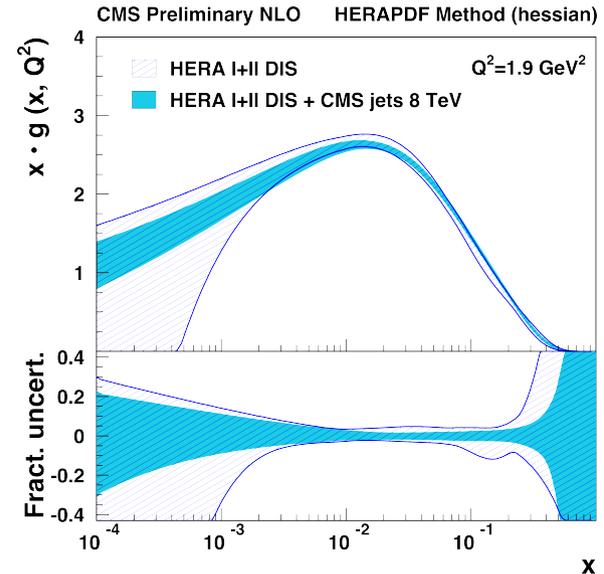
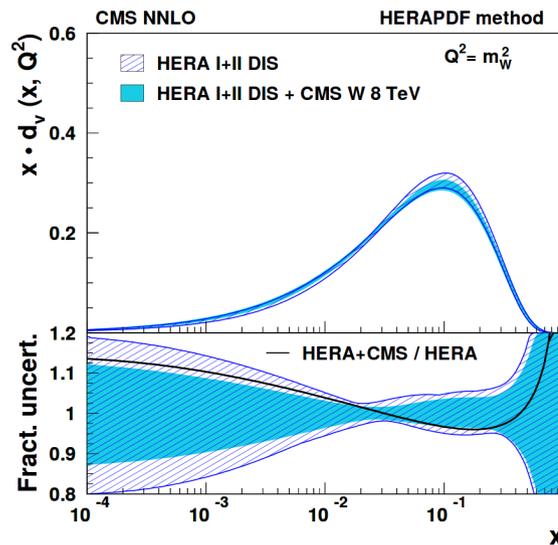
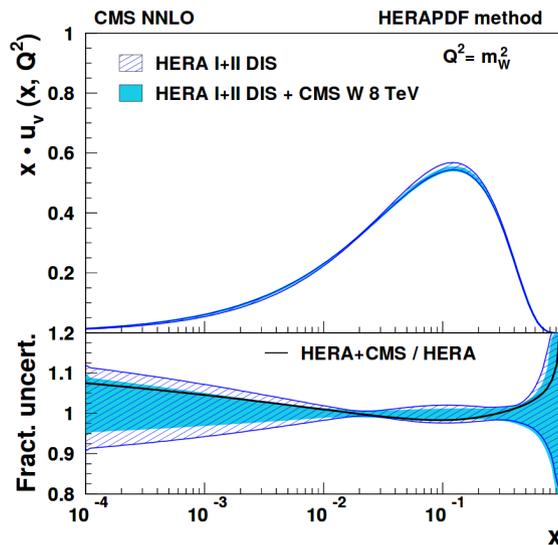


NNPDF3.0 NNLO Global, $Q^2=10^2 \text{ GeV}^2$



◆ Precision improvement of few percent at moderate x .

◆ No tensions within global fits from HERA data.



Summary

◆ Final combination of HERA I+II data is performed.

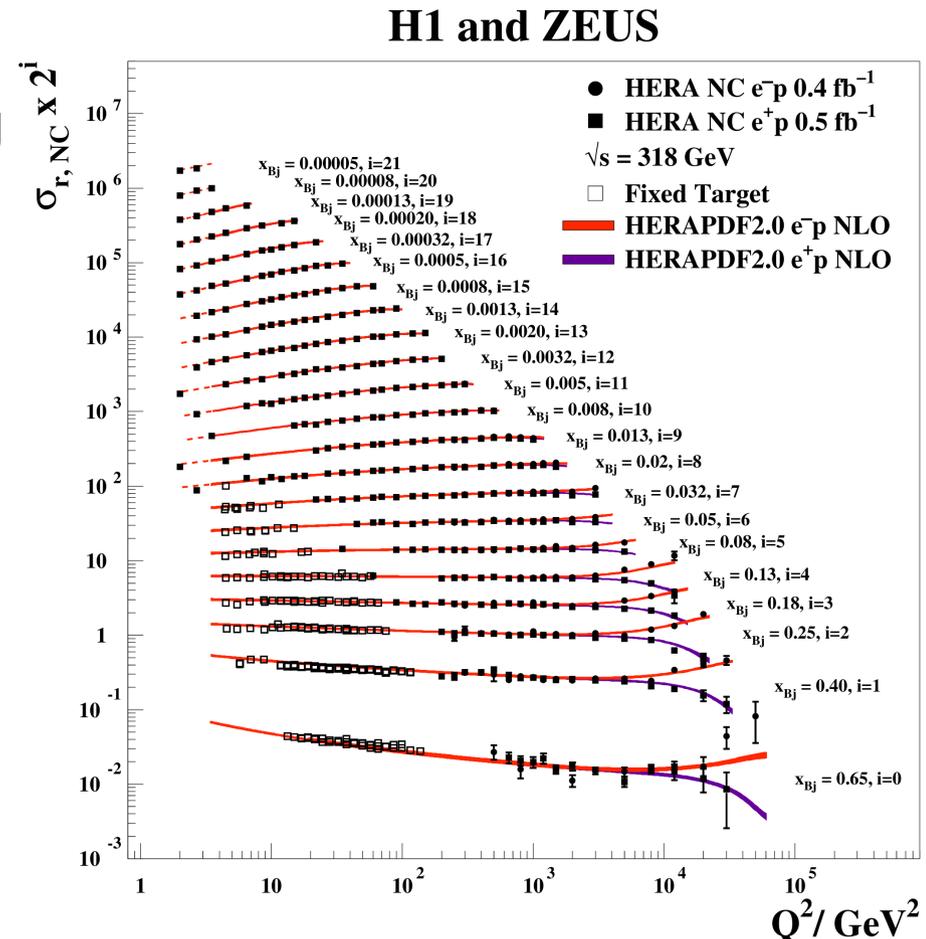
◆ Significant reduction of uncertainties is achieved.

◆ HERAPDF2.0 fits are performed using combined HERA I+II data.

◆ PDFs are publicly available in many variations.

◆ Adding new HERA II data improves PDFs precision.

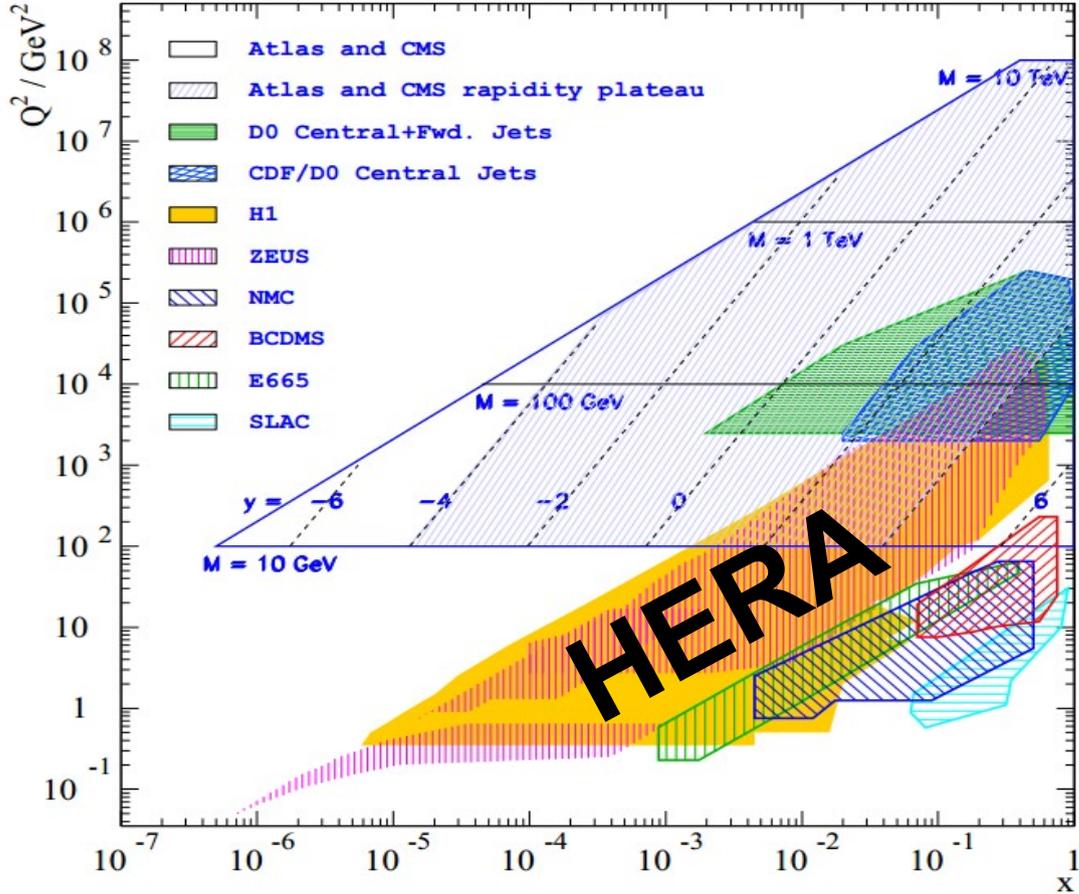
Eur.Phys.J.C75 (2015) 12, 580 [[arxiv:1506.06042](https://arxiv.org/abs/1506.06042)]



Backup

not necessarily useful...

HERA collider



$$Q^2 = -q^2 = -(k - k')^2$$

$$x_{Bj} = \frac{Q^2}{2pq} \quad y = \frac{pq}{pk}$$

$$s = (p + k)^2 \quad Q^2 = xys$$

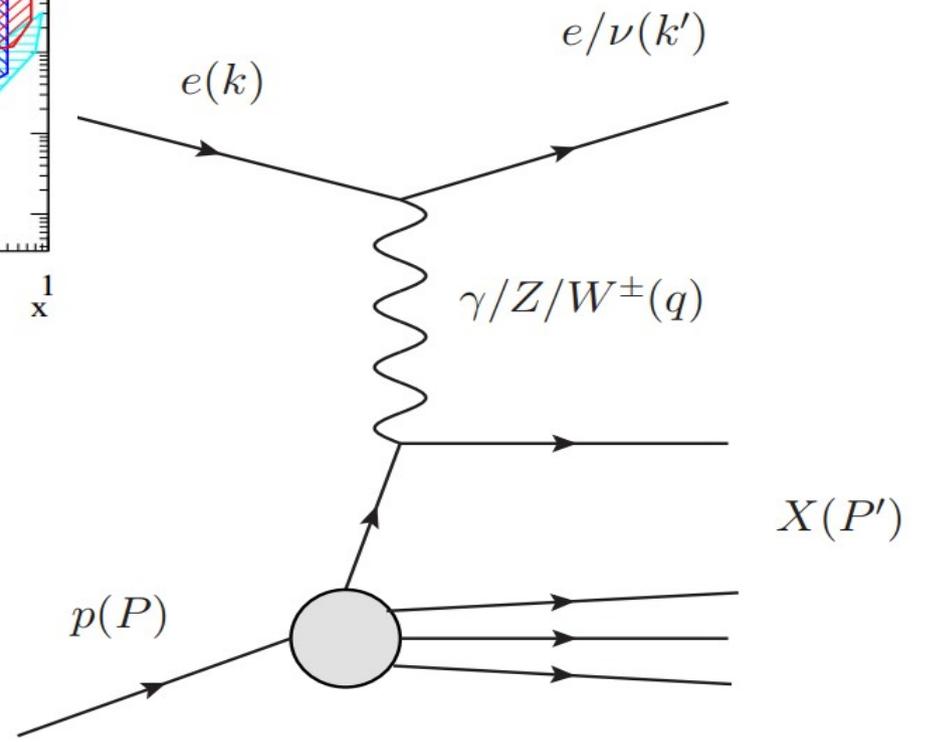
$$E_p = 920 (460, 575) \text{ GeV}$$

$$E_e = 27.5 \text{ GeV}$$

$$\sqrt{s} = 318 (225, 252) \text{ GeV}$$

Experimental achievements:

$\sim 0.5 \text{ fb}^{-1}$ DIS data from each experiment



HERAPDF2.0: settings for QCD fit

◆ QCD fits are performed using **HERAFitter** package

◆ PDFs (**14p**) are parametrised at $Q_0^2 = 1.9 \text{ GeV}^2$

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g},$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2),$$

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x),$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$$

◆ A_{u_v}, A_{d_v}, A_g are constrained by **QCD sum rules**

◆ $x\bar{u} \xrightarrow{x \rightarrow 0} x\bar{d}$ ◆ $A_{\bar{U}}, A_{\bar{D}}$ are constrained via $x\bar{s} = f_s x\bar{D}$

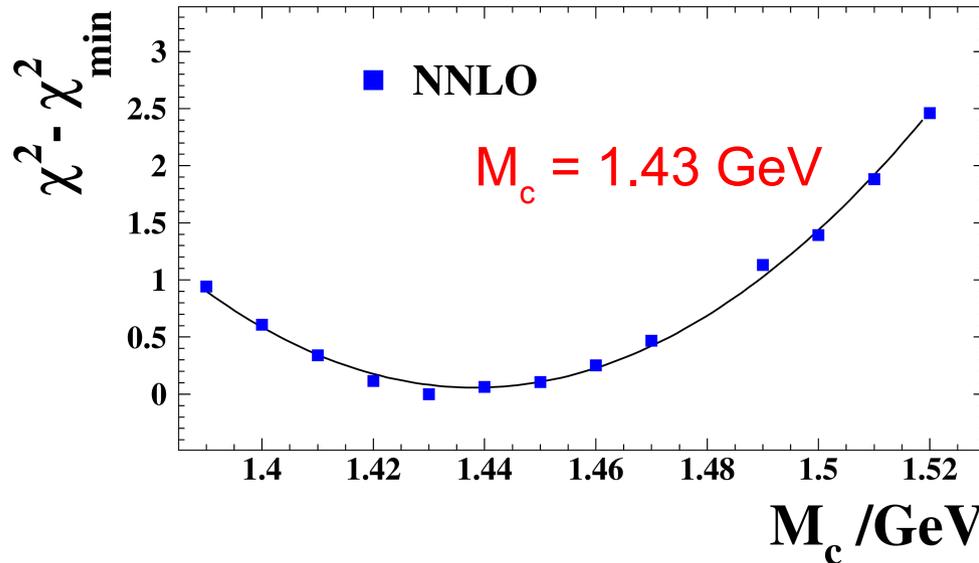
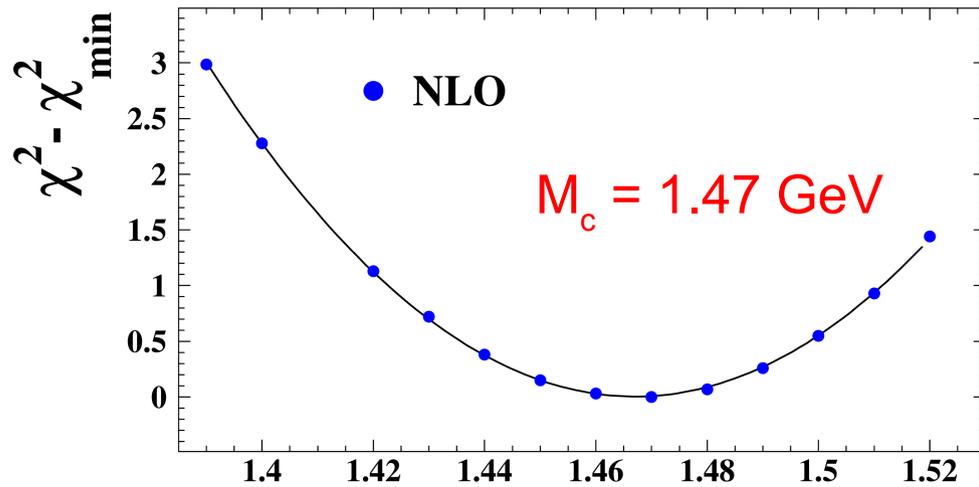
◆ PDF evolution is performed using **DGLAP** equations

◆ Heavy flavour coefficients are obtained within **GM VFNS (RT OPT)**

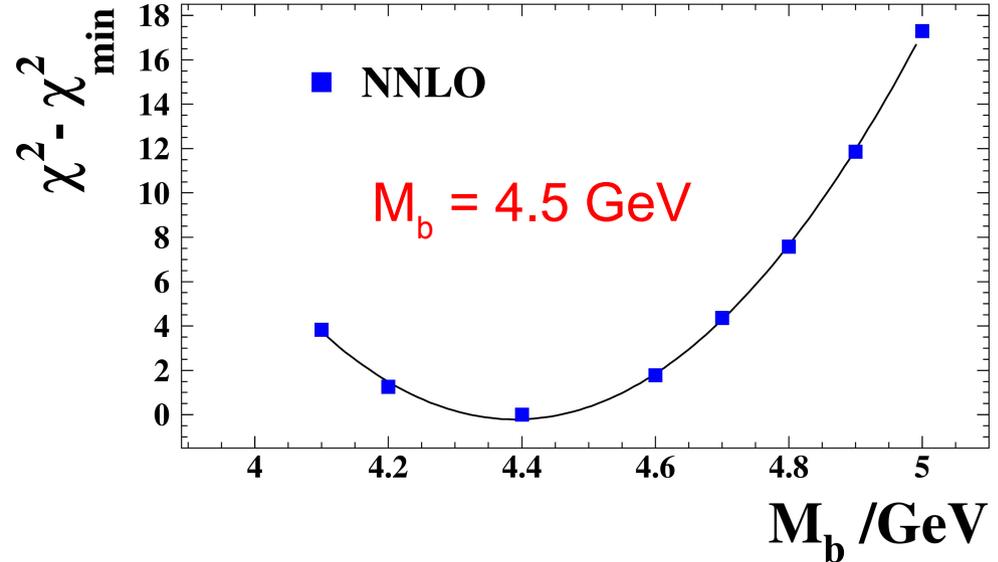
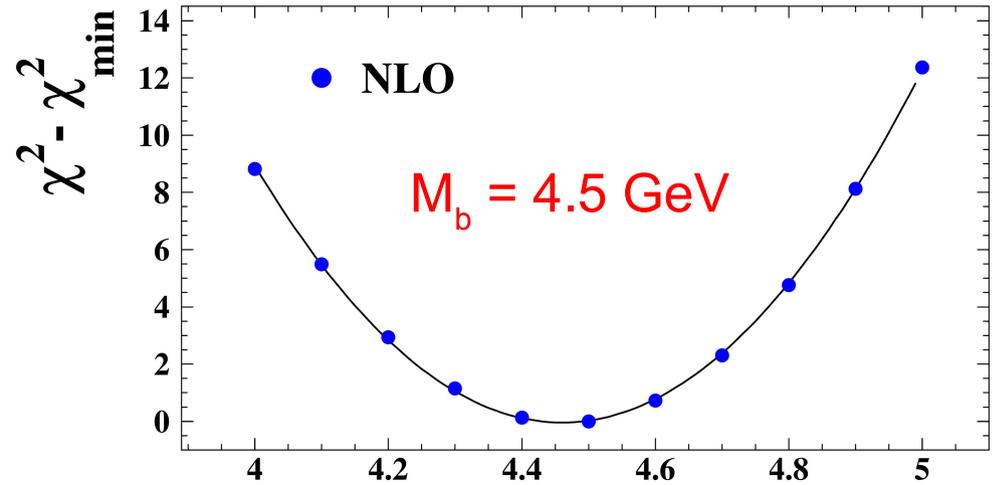
$$\chi^2 = \sum_i \frac{[\mu_i - m_i (1 - \sum_j \gamma_j^i b_j)]^2}{\delta_{i,uncor}^2 m_i^2 + \delta_{i,stat}^2 \mu_i m_i (1 - \sum_j \gamma_j^i b_j)} + \sum_j b_j^2 + \sum_i \ln \frac{\delta_{i,uncor}^2 m_i^2 + \delta_{i,stat}^2 \mu_i m_i}{\delta_{i,uncor}^2 \mu_i^2 + \delta_{i,stat}^2 \mu_i^2}$$

Charm and beauty mass parameters

H1 and ZEUS



H1 and ZEUS

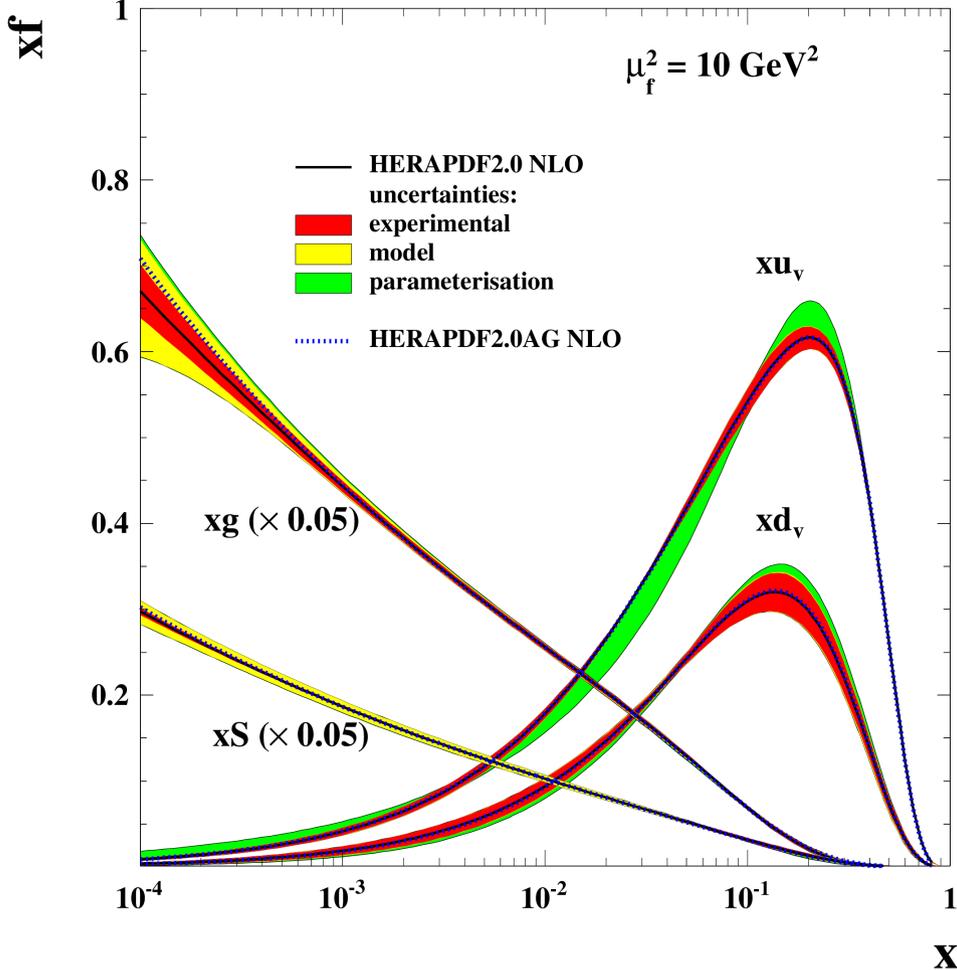


➡ M_c / M_b determined from inclusive data + charm / beauty data.

Method from the HERA charm combination (*Eur. Phys. J. C73 (2013) 2311*)

HERAPDF2.0: errors estimation

H1 and ZEUS



Parametrisation uncertainties:

- The largest deviation taken.

Full systematic correlation treatment.

Experimental uncertainties:

- Hessian method used: full second-derivative matrix calculated
- Conventional $\Delta\chi^2 = 1 \Rightarrow 68\% \text{ CL}$

Model uncertainties:

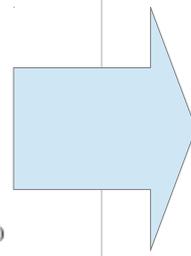
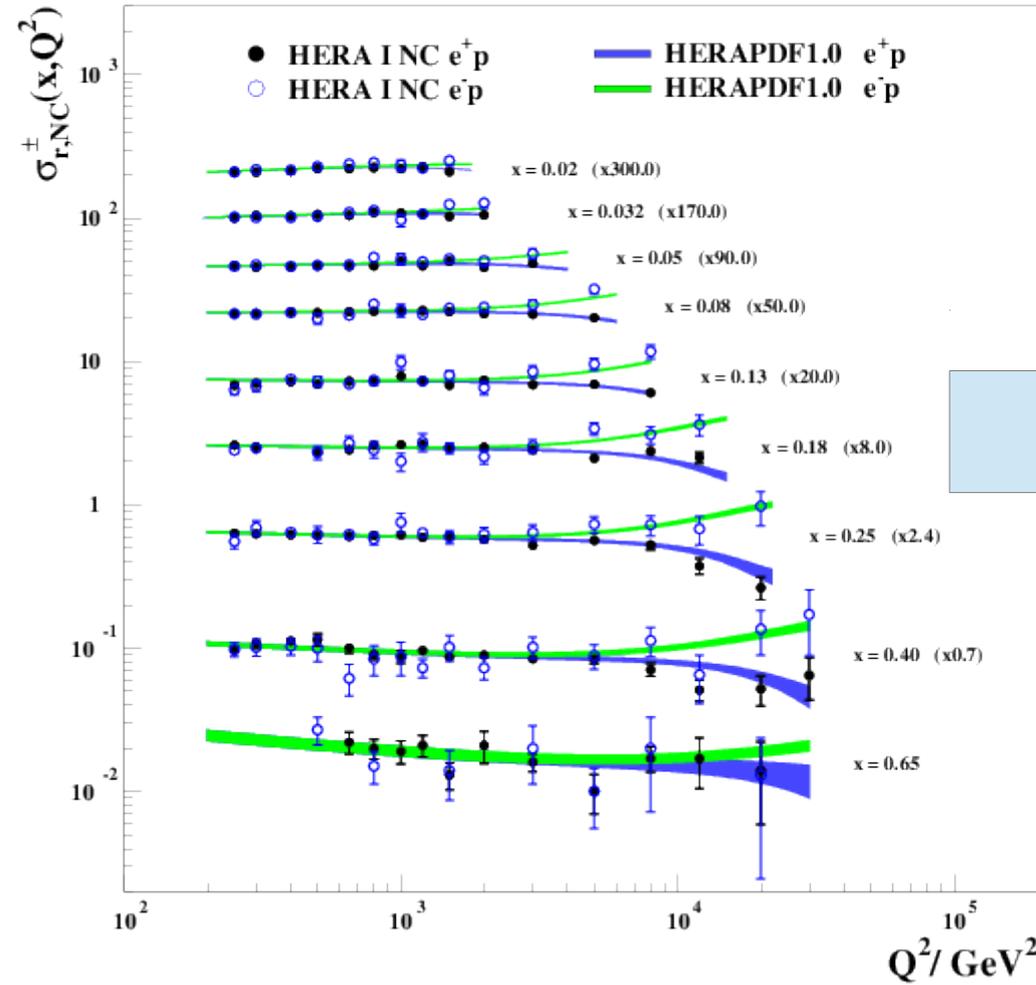
- All variations are added in quadratures, separately positive and negative.

Variation	Standard Value	Lower Limit	Upper Limit
Q_{\min}^2 [GeV ²]	3.5	2.5	5.0
Q_{\min}^2 [GeV ²] HiQ2	10.0	7.5	12.5
M_c (NLO) [GeV]	1.47	1.41	1.53
M_c (NNLO) [GeV]	1.43	1.37	1.49
M_b [GeV]	4.5	4.25	4.75
f_s	0.4	0.3	0.5
μ_{f_0} [GeV]	1.9	1.6	2.2

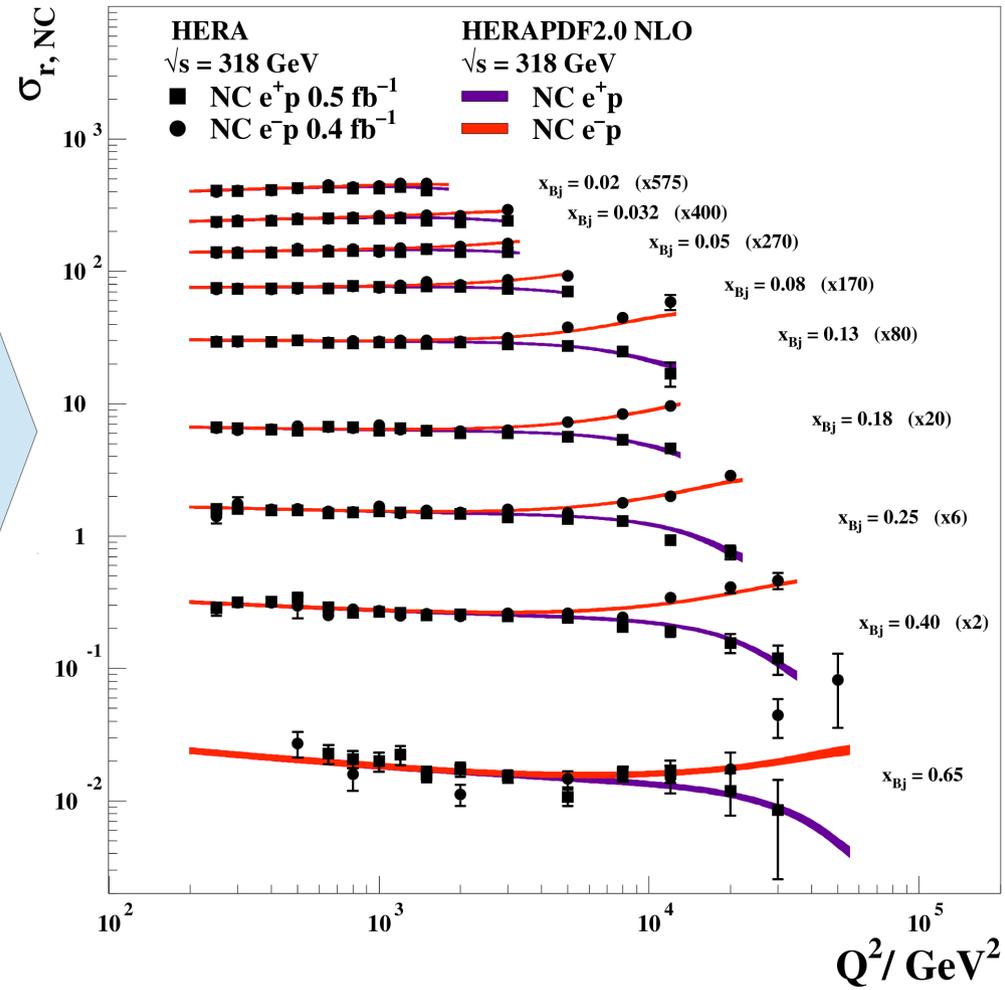
Adding D and E parameters to each PDF

EW effects: HERAPDF 1.0 vs 2.0

H1 and ZEUS



H1 and ZEUS

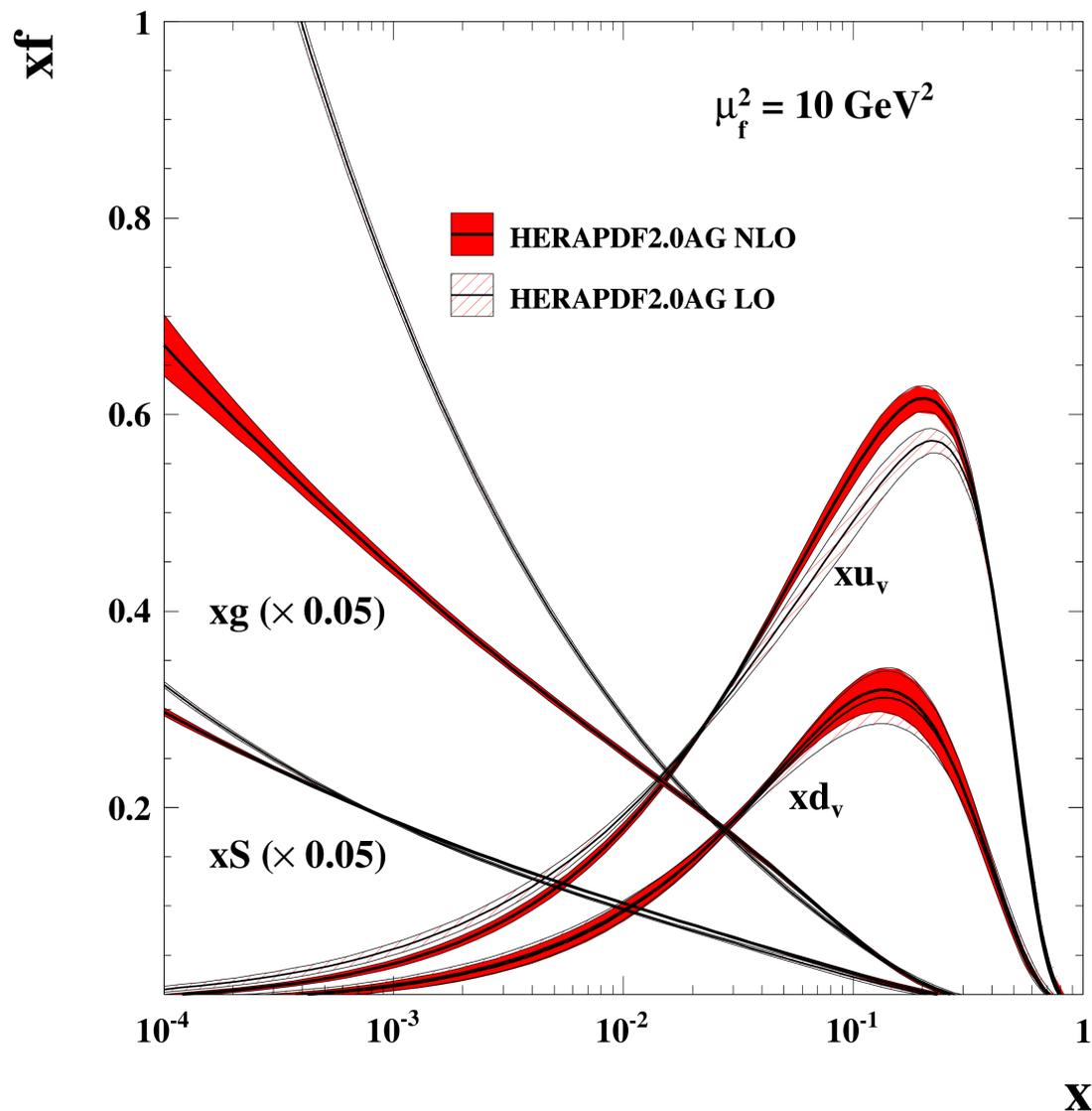


Great precision!

$$\sigma_{r,NC}^{\pm} = \frac{Q^4 x_{Bj}}{2\pi\alpha^2 Y_+} \frac{d^2 \sigma_{NC}^{e^{\pm}p}}{dx_{Bj} dQ^2} = \tilde{F}_2 \left(\frac{Y_-}{Y_+} x \tilde{F}_3 \right) - \frac{y^2}{Y_+} \tilde{F}_L$$

HERAPDF2.0 at LO

H1 and ZEUS



◆ Parton densities @LO are presented.

◆ Essential for parton showers simulation in LO+PS Monte Carlo event generators

HERAPDF2.0: Q^2_{\min} dependence

◆ $Q^2_{\min} = 3.5 \text{ GeV}^2$
HERAPDF2.0

NLO $\frac{\chi^2}{ndf} = \frac{1357}{1131}$

NNLO $\frac{\chi^2}{ndf} = \frac{1363}{1131}$

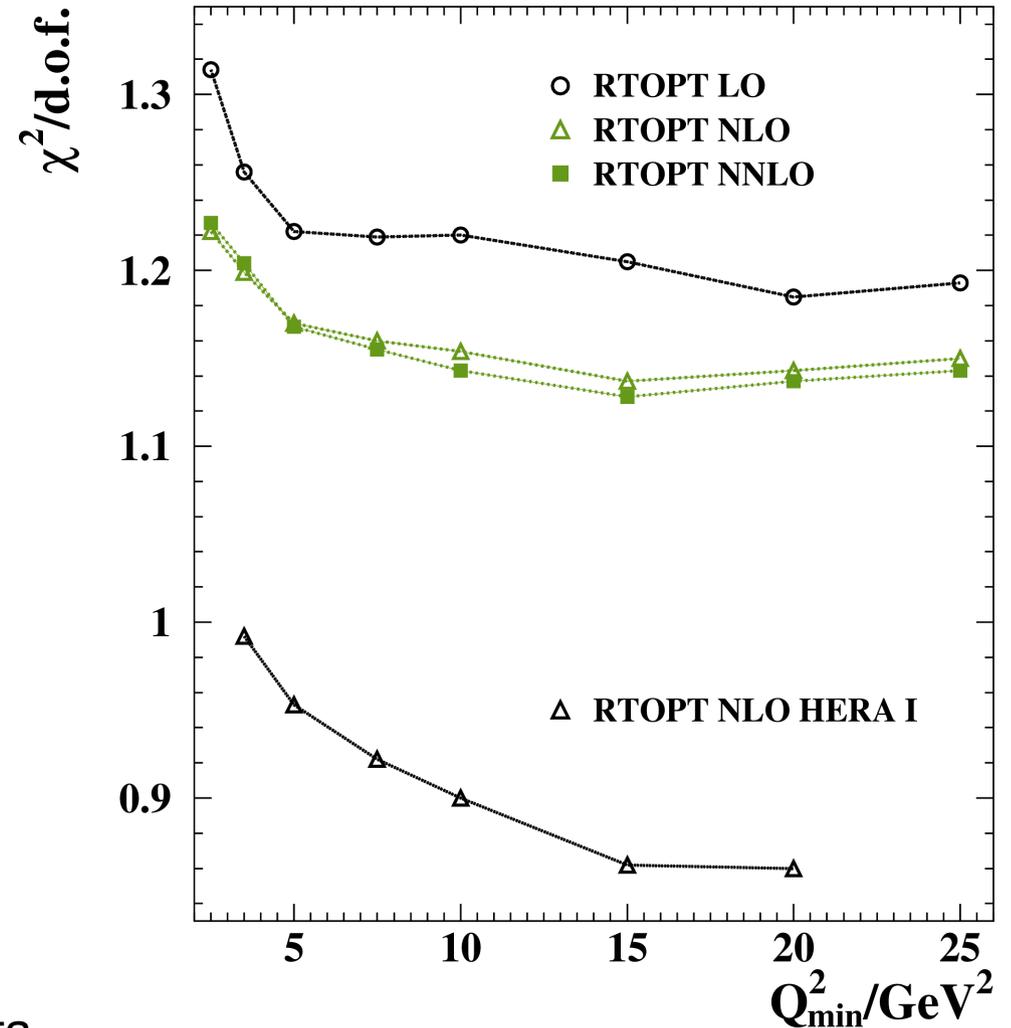
◆ $Q^2_{\min} = 10 \text{ GeV}^2$
HERAPDF2.0HiQ2

NLO $\frac{\chi^2}{ndf} = \frac{1156}{1002}$

NNLO $\frac{\chi^2}{ndf} = \frac{1146}{1002}$

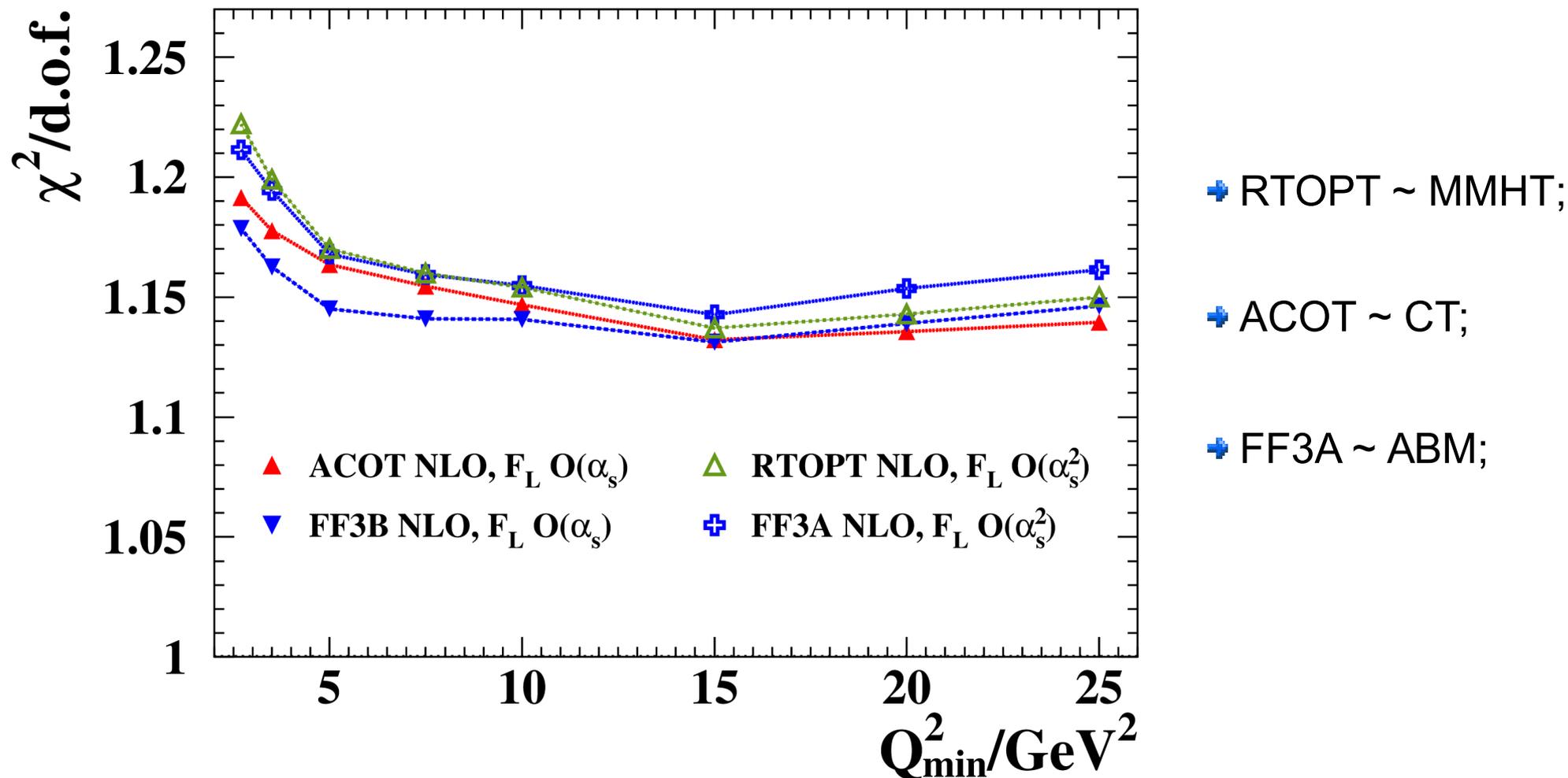
◆ Small tension between low and high Q^2 data.

H1 and ZEUS



HERAPDF2.0: dependence on F_L order

H1 and ZEUS



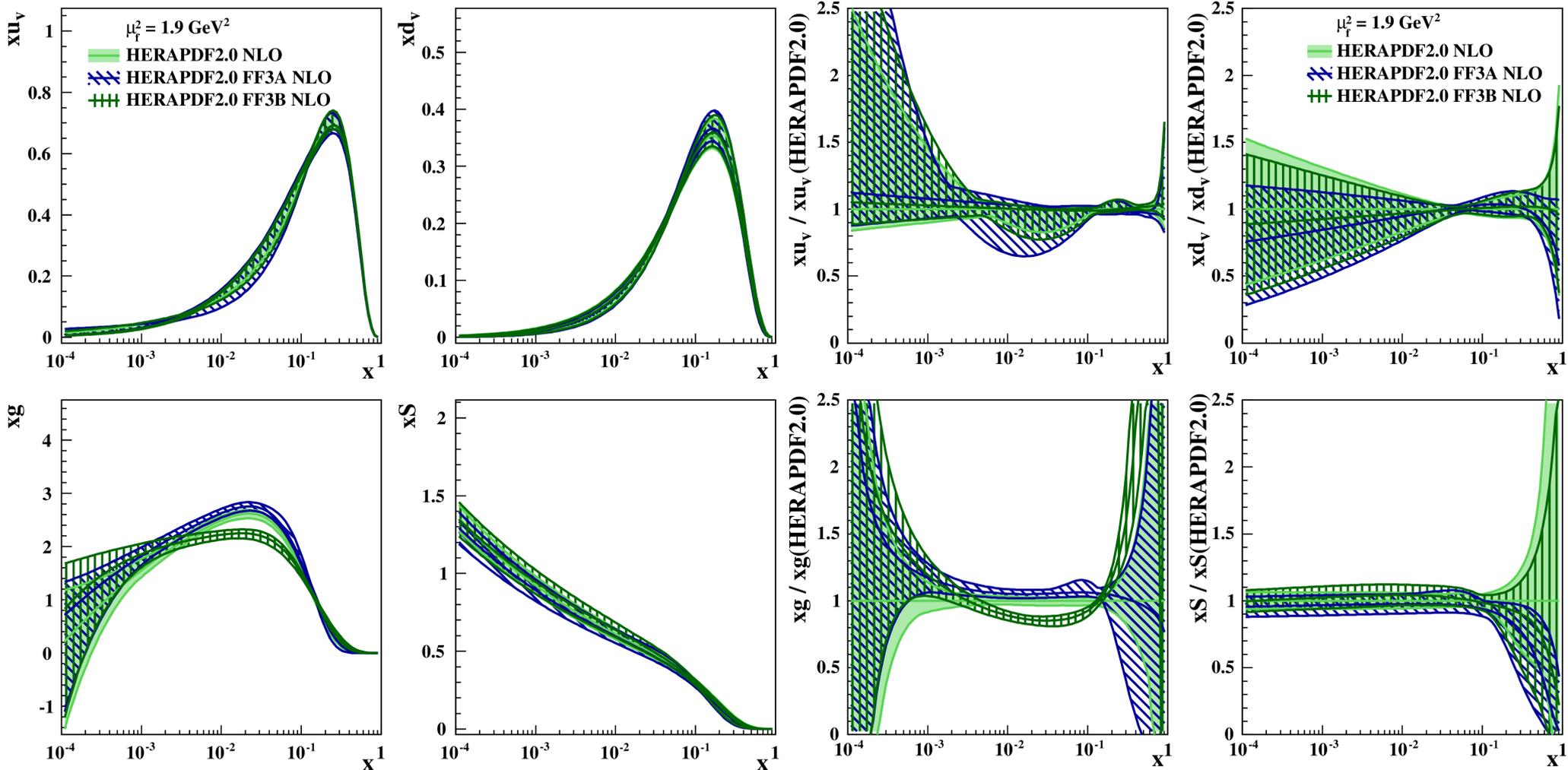
◆ Treating of F_L to the same order in α_s as F_2 gives better results at NLO.

◆ Almost independent of HF scheme.

HERAPDF2.0 FF3A and FF3B

H1 and ZEUS

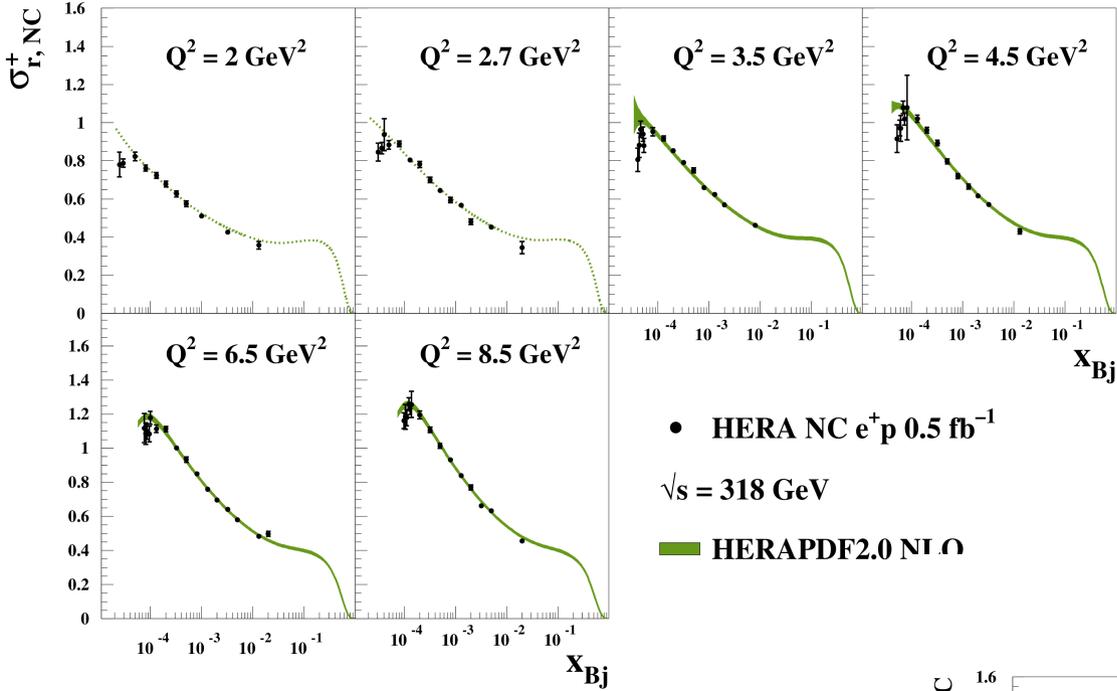
H1 and ZEUS



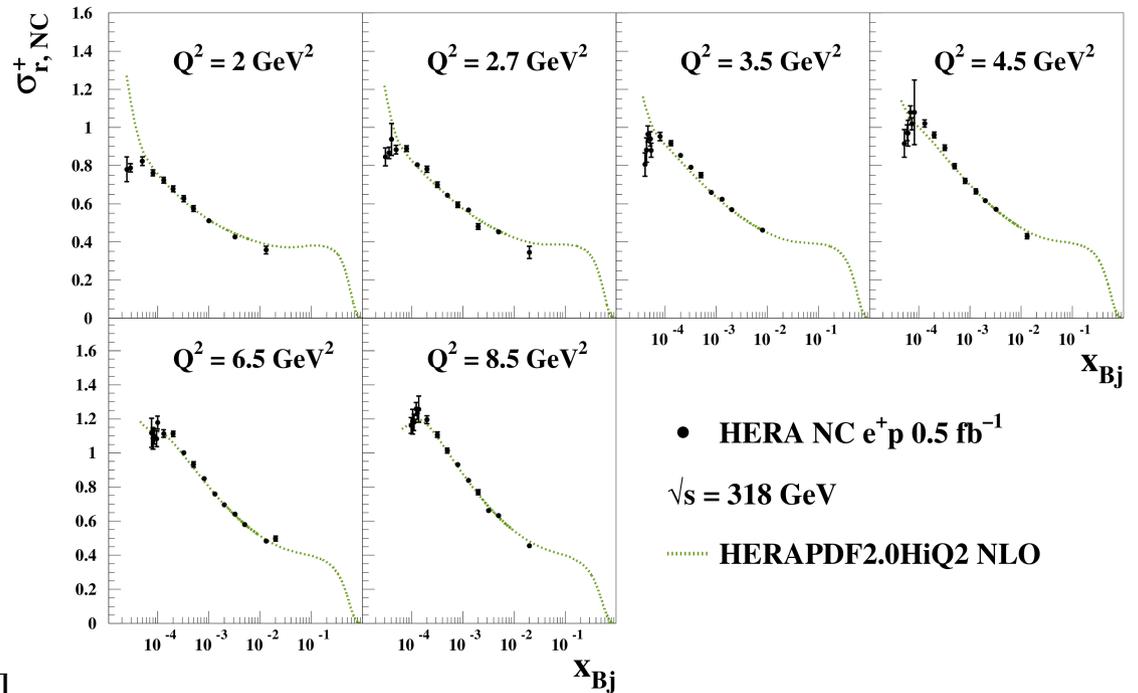
Deferences in gluons between RTOPT and FF → different F_L orders in α_s .

NLO: NC low Q^2 , x

H1 and ZEUS

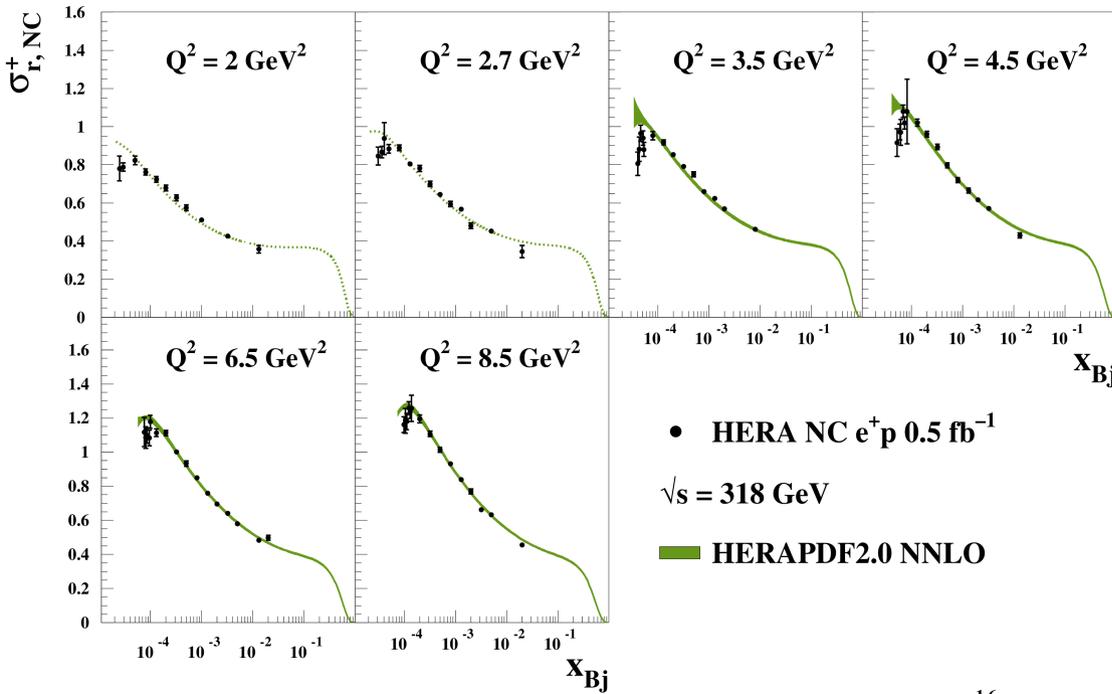


H1 and ZEUS

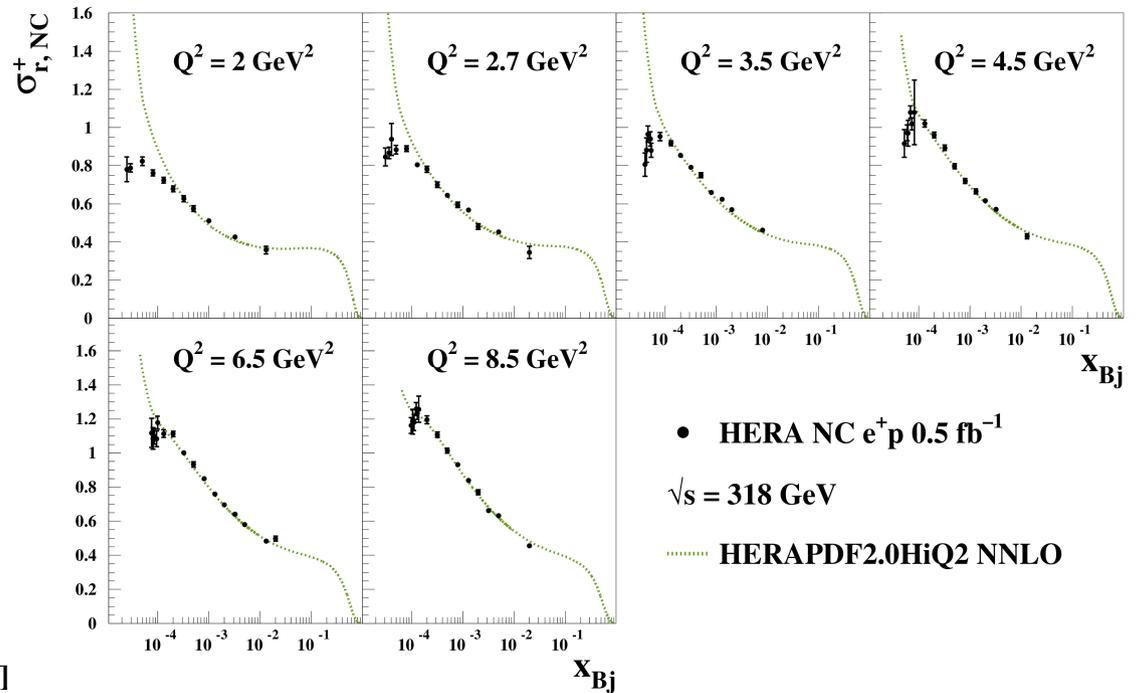


NNLO: NC low Q^2 , x

H1 and ZEUS



H1 and ZEUS



Helicity effects in CC interactions

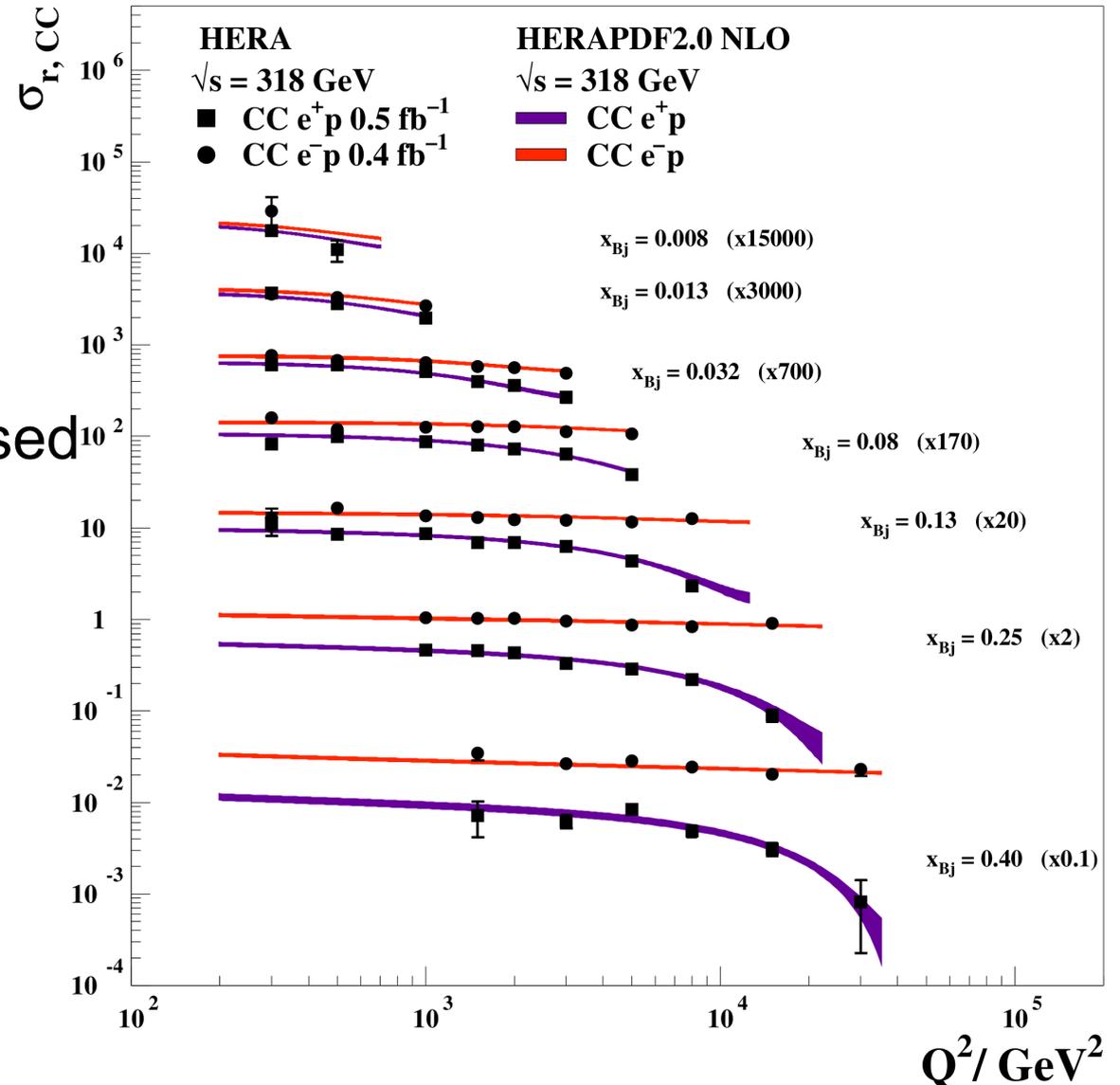
$$\sigma_{r,CC}^+ \approx x \bar{U} + (1-y)^2 x D$$

$$\sigma_{r,CC}^- \approx x U + (1-y)^2 x \bar{D}$$

◆ e^+p : d_v quarks are suppressed at high Q^2 .

◆ e^-p : helicity factor applies only to sea quarks.

H1 and ZEUS

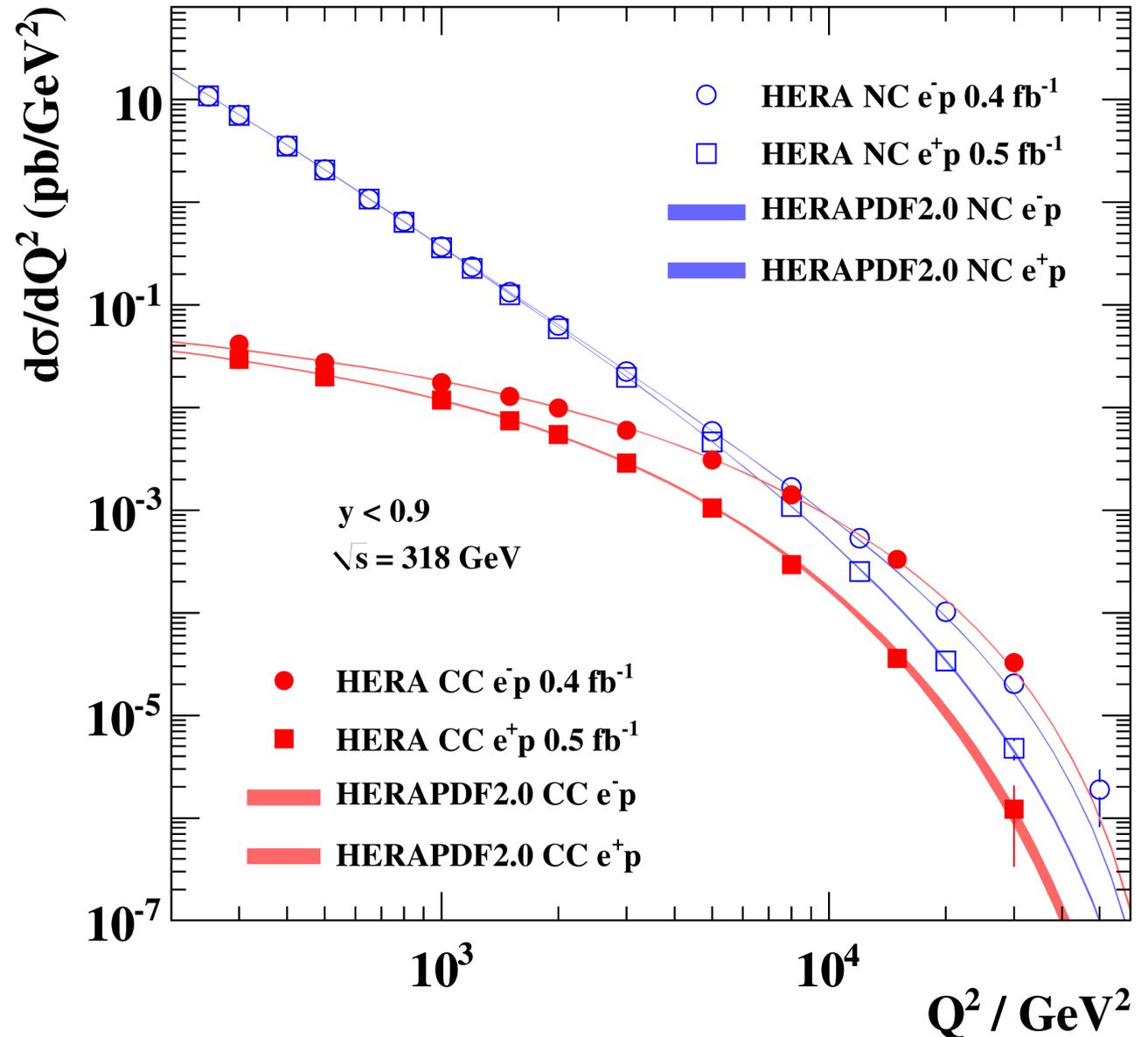


Electroweak unification

H1 and ZEUS

Virtual photon exchange is dominant for low Q^2 NC reactions.

At high scales CC and NC become similar in magnitude.

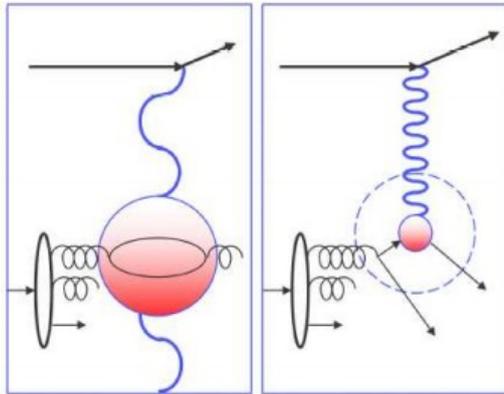


Scaling violation

◆ NLO and NNLO predictions are similar

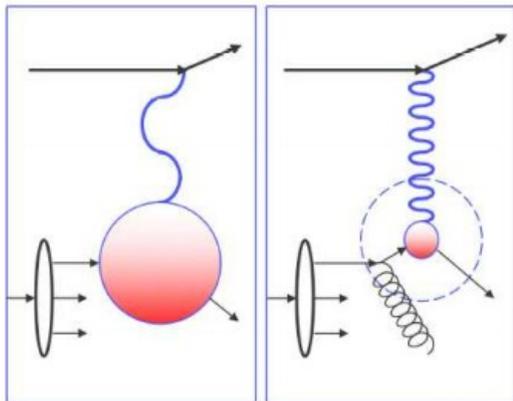
H1 and ZEUS

Small x : Gluons, sea quarks

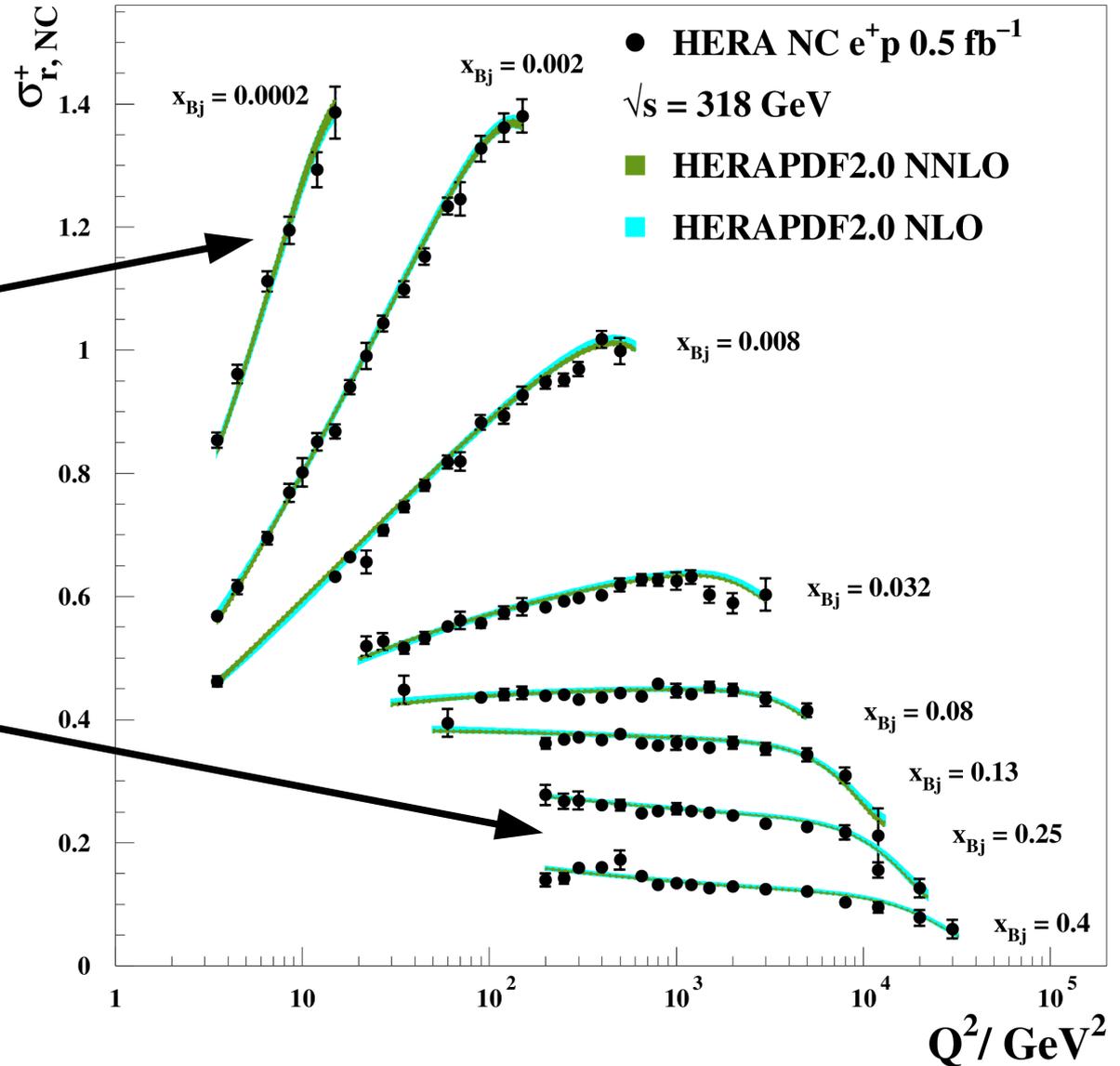


$Q^2 \uparrow \Rightarrow F_2 \uparrow$ for fixed x

Large x : valence quarks



$Q^2 \uparrow \Rightarrow F_2 \downarrow$ for fixed x



FF3A and FF3B

◆ FF3A

- ◆ Three flavour running of α_s ;
- ◆ F_L calculated to $O(\alpha_s^2)$;
- ◆ Pole masses for charm and beauty.

◆ FF3B

- ◆ Variable-flavour running of α_s ;
- ◆ F_L calculated to $O(\alpha_s)$;
- ◆ \overline{MS} running masses for charm and beauty.