



# Electroweak and new physics fits to HERA DIS data



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On behalf of H1 and ZEUS Collaborations



- Inclusive data combination and HERAPDF2.0
- Electroweak physics at HERA
- Beyond Standard Model analysis using the simultaneous fit of BSM parameter and PDFs

# HERA — world only $e^\pm p$ collider

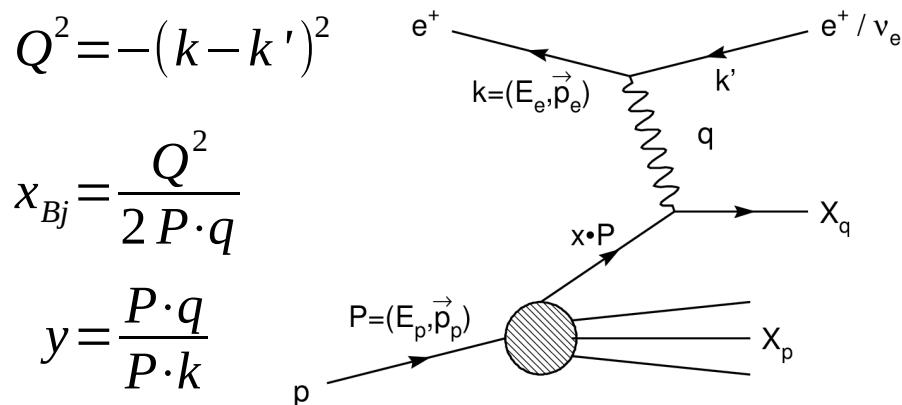
HERA data provides unique opportunity to study the structure of the proton.

operated during 1992 - 2007,  
2003 - 2007 — polarised lepton beams

→ important for the EW  
measurements

$e^\pm$  energy 27.5 GeV;  
 $p$  energies 920, 820, 575 and 460 GeV.

Kinematics of the  $e^\pm p$  collisions:



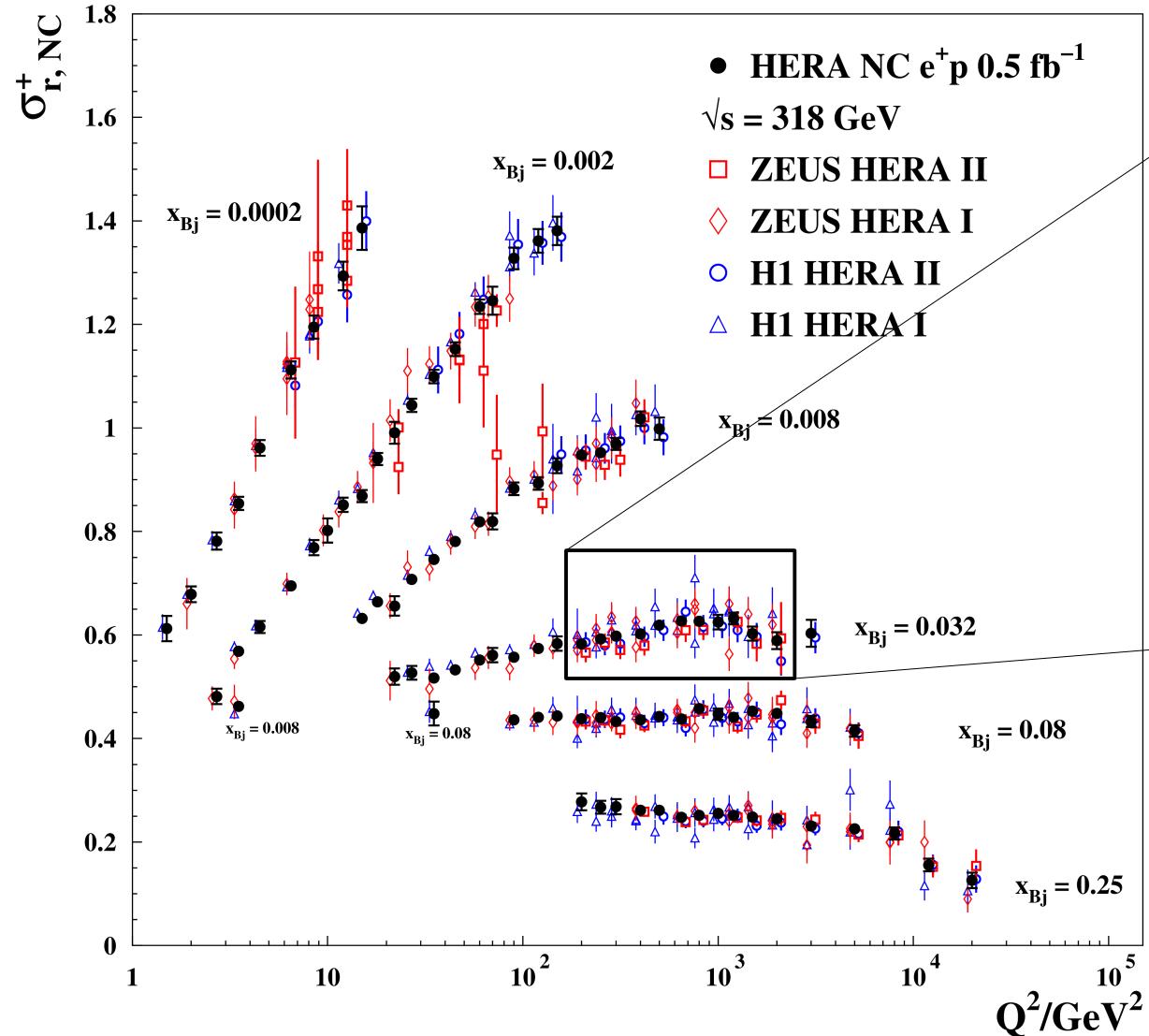
H1 and ZEUS — two collider experiments at HERA :

~ 0.5  $\text{fb}^{-1}$  of luminosity recorded by each experiment.

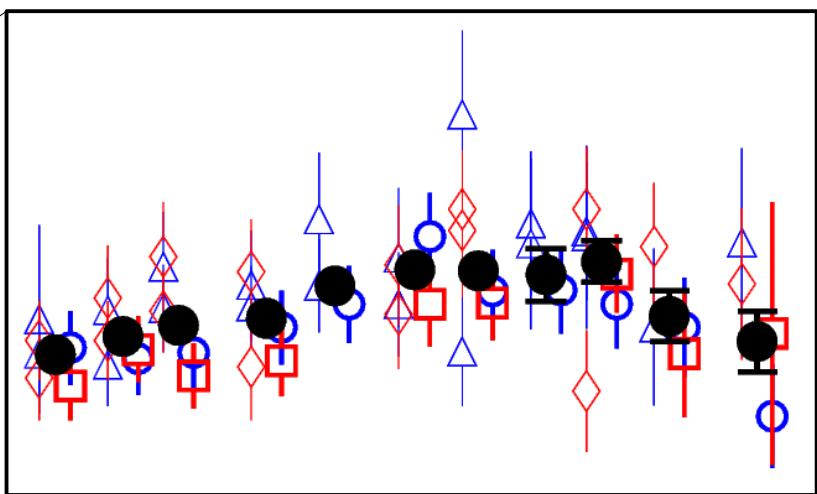
# Combined Inclusive DIS

H1 and ZEUS have presented the combination of inclusive DIS measurements,  
but for zero beams polarisation.

## H1 and ZEUS



- 2927 data points combined to 1307

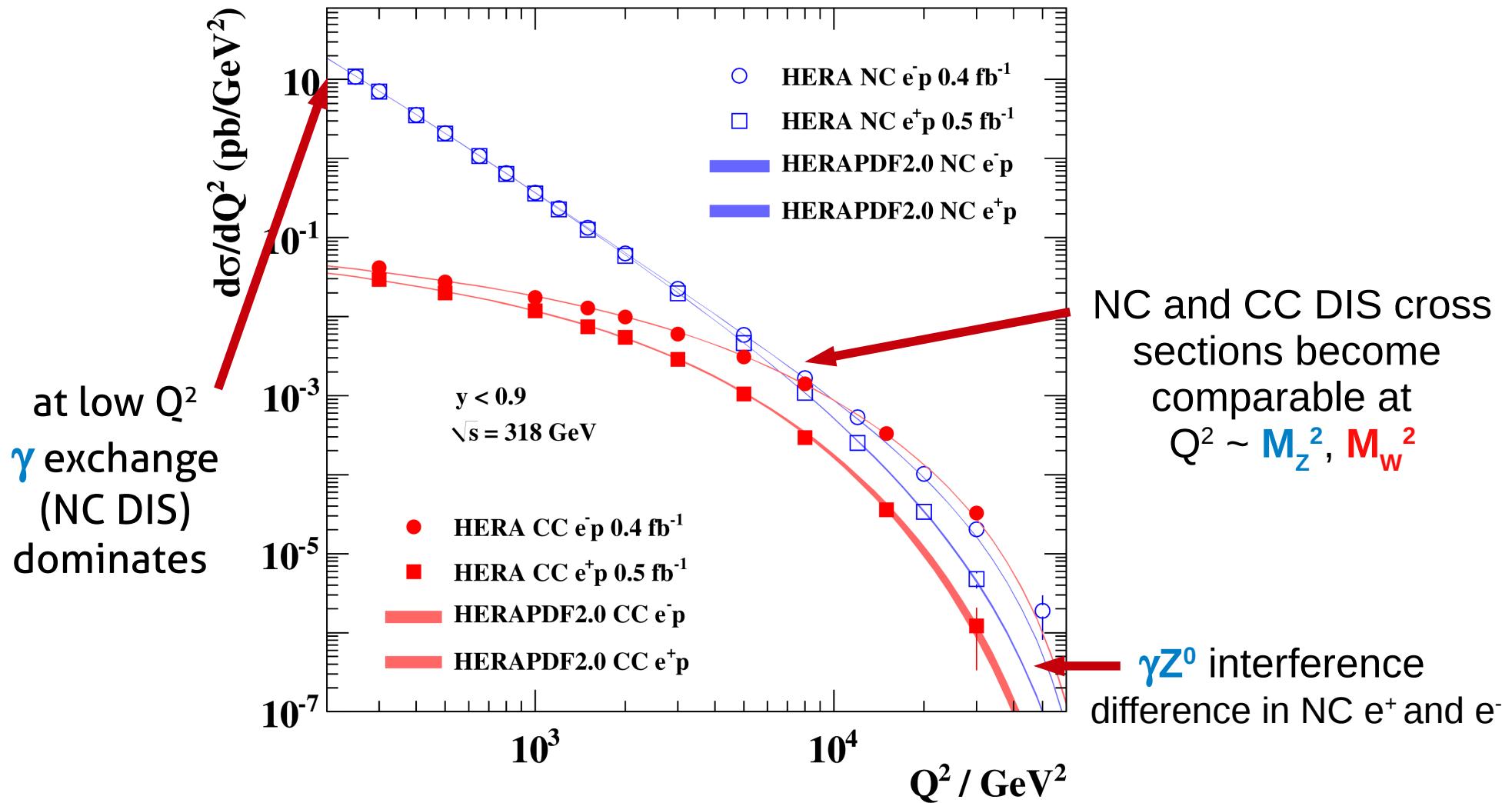


- up to 8 data points combined to 1
- data consistent between two experiments and data taking periods:

$$\chi^2 / \text{ndf} = 1685 / 1620$$

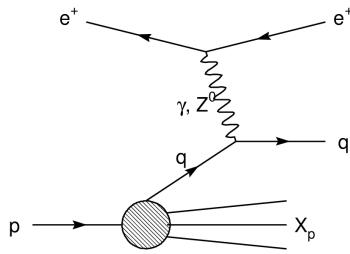
# Combined Inclusive DIS

H1 and ZEUS



Effects of electroweak unification clearly seen.

# QCD analysis of combined DIS data



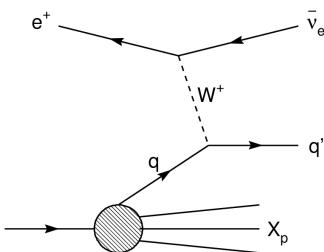
**Neutral Current:**

$$\frac{d^2 \sigma_{\text{NC}}^{e \mp p}}{dx_{Bj} dQ^2} = \frac{2\pi\alpha^2}{x_{Bj} Q^4} \cdot (Y_+ \cdot F_2 \pm Y_- \cdot x \cdot F_3 - y^2 \cdot F_L)$$

$$Y_{\pm} = 1 \pm (1-y)^2$$

$$F_2 = \frac{4}{9}(xU + x\bar{U}) + \frac{1}{9}(xD + x\bar{D})$$

$$x \cdot F_3 \sim x u_v + x d_v$$



Similar equation for **CC** DIS.

**Parton Density Functions** parametrization at starting scale  $Q^2 = 1.9 \text{ GeV}^2$ :

$$x g(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g}$$

■ fixed or calculated by sum-rules

$$x u_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + D_{u_v} x + E_{u_v} x^2)$$

■ set equal

$$x d_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}}$$

- Evolve to any  $Q^2$  with DGLAP at NLO.

$$x \bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x)$$

- Use Thorne-Roberts GMVFN scheme

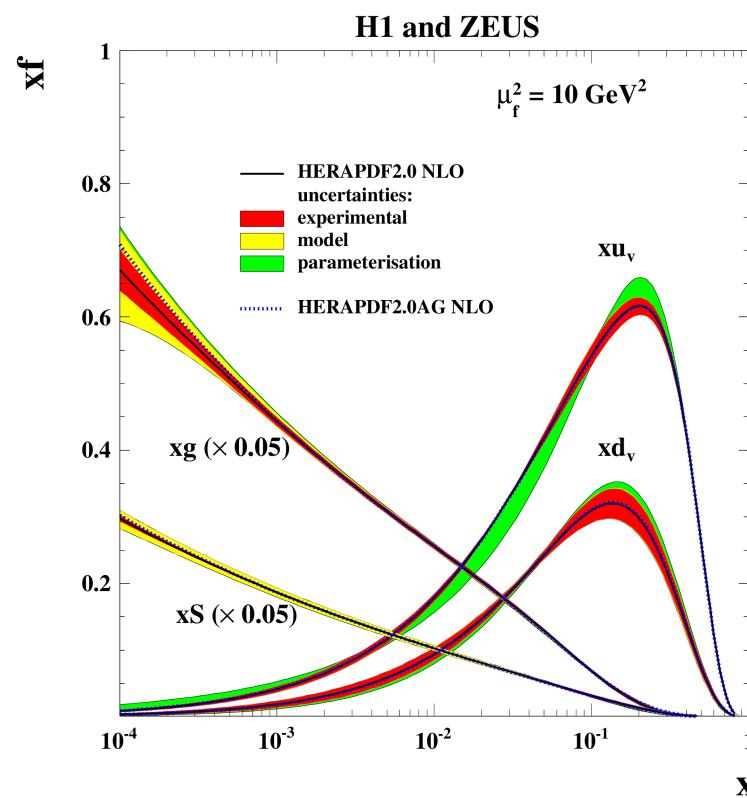
for Heavy quarks.

$$x \bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}$$

# QCD analysis of combined DIS data

Eur. Phys. J. C 75 (2015) 580  
arXiv:1506.06042

PDFs set **HERAPDF2.0** :



**Combination of measurements of inclusive deep inelastic  $e^\pm p$  scattering cross sections and QCD analysis of HERA data**

This paper is dedicated to the memory of Professor Guido Altarelli who sadly passed away as it went to press. The results which it presents are founded on the principles and the formalism which he developed in his pioneering theoretical work on Quantum Chromodynamics in deep-inelastic lepton-nucleon scattering nearly four decades ago

H1 and ZEUS Collaborations

# Polarised DIS

[Phys. Rev. D 93 \(2016\) 092002](#)  
[arXiv:1603.09628](#)

In NC DIS polarisation affects  $\gamma Z^0$  interference and  $Z^0$  exchange:

$$P_e = \frac{N_R - N_L}{N_R + N_L}$$

$$F_2^\mp = F_2^y - (v_e \mp P_e a_e) \chi_Z F_2^{yz} + \\ + (v_e^2 + a_e^2 \mp 2 P_e v_e a_e) \chi_Z^2 F_2^z$$

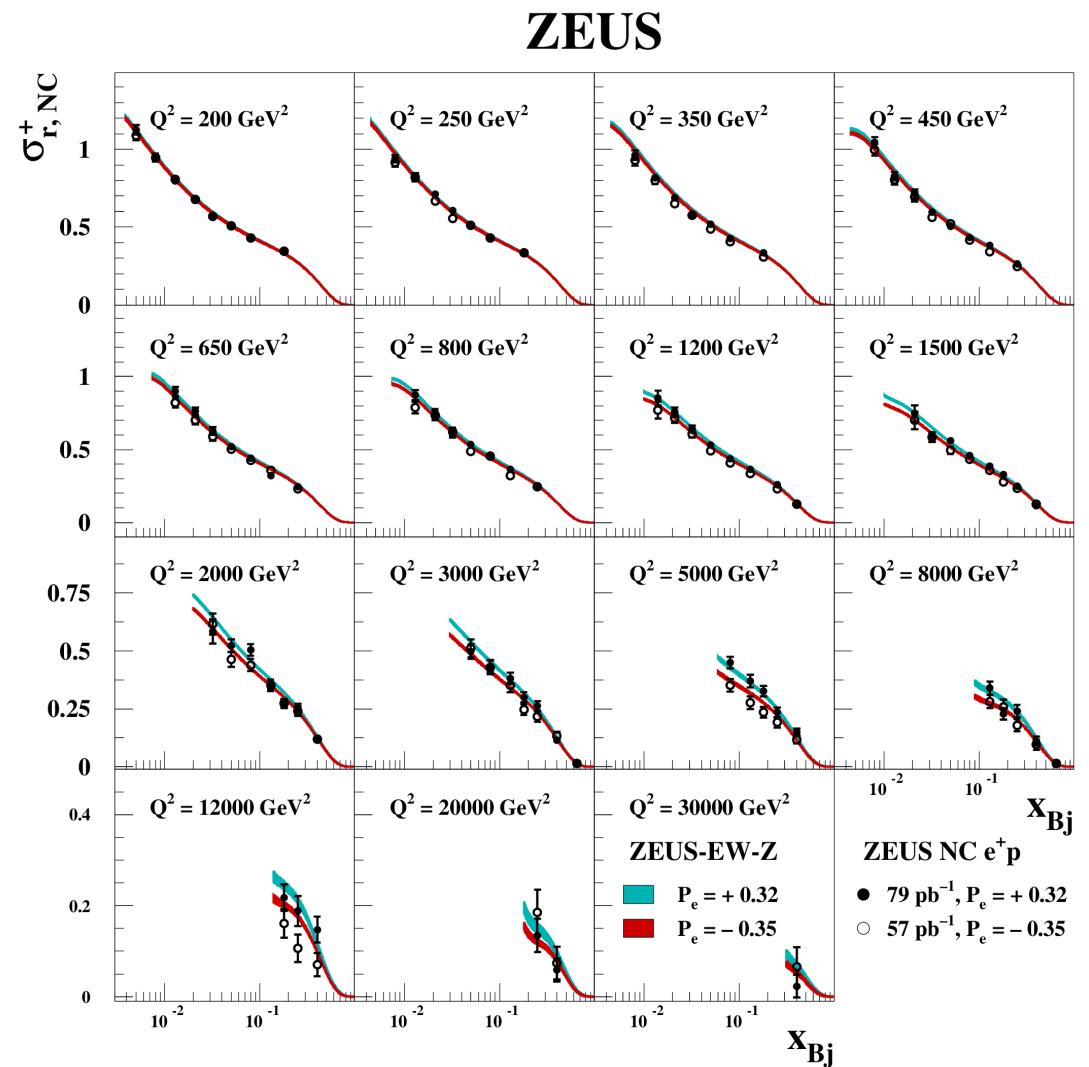
$$xF_3^\mp = -(a_e \mp P_e v_e) \chi_Z x F_3^{yz} + \\ + (2 v_e a_e \mp P_e (v_e^2 + a_e^2)) \chi_Z^2 x F_3^z$$

$$v_e = -\frac{1}{2} + 2 \sin^2(\Theta_W) \quad a_e = -\frac{1}{2}$$

In the on-shell scheme:

$$\sin^2(\Theta_W) = 1 - \frac{M_W^2}{M_Z^2}$$

$$\chi_Z = \frac{1}{\sin^2(2\Theta_W)} \frac{Q^2}{M_Z^2 + Q^2} \frac{1}{1 - \Delta R}$$



# Polarised DIS

In CC DIS polarisation scales the whole cross section:

$$\frac{d^2\sigma_{CC}^{e-p}}{dx_{Bj} dQ^2} = (1 - P_e) \frac{G_F^2 M_W^4}{2\pi x_{Bj} (Q^2 + M_W^2)^2} \times \\ \times x [(u + c) + (1 - y)^2 (\bar{d} + \bar{s} + \bar{b})]$$

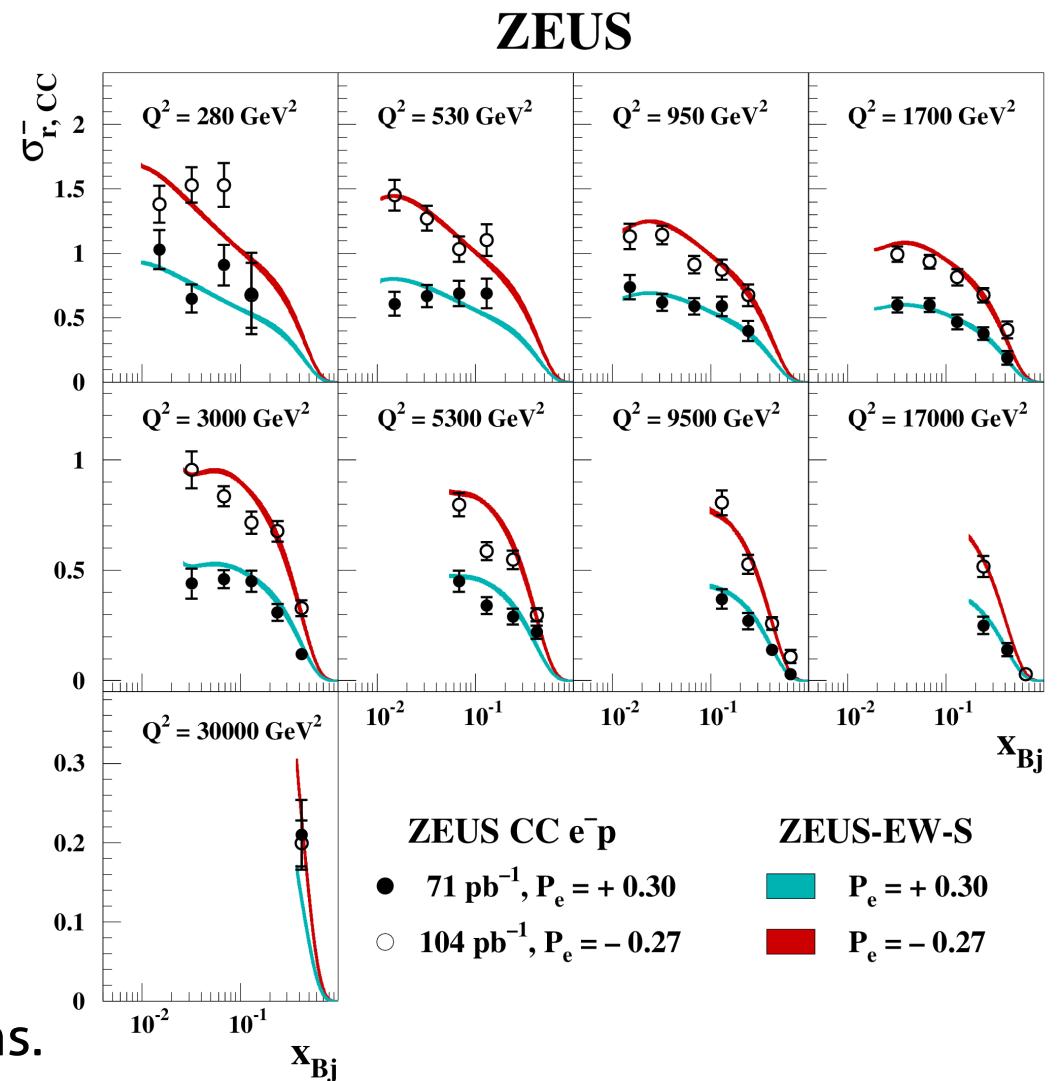
$$\frac{d^2\sigma_{CC}^{e+p}}{dx_{Bj} dQ^2} = (1 + P_e) \frac{G_F^2 M_W^4}{2\pi x_{Bj} (Q^2 + M_W^2)^2} \times \\ \times x [(\bar{u} + \bar{c}) + (1 - y)^2 (d + s + b)]$$

In the on-shell scheme:

$$M_W = \frac{A_0}{\sin^2(\Theta_W) \sqrt{1 - \Delta R}}$$

$$G_F = \frac{\pi \alpha_0}{\sqrt{2} \sin^2(\Theta_W) M_W^2} \frac{1}{1 - \Delta R}$$

$\Delta R$  — radiative corrections.



# ZEUS QCD + EW fits

[Phys. Rev. D 93 \(2016\) 092002](#)

[arXiv:1603.09628](#)

Used uncombined datasets:

→ Same as in the data combination:

- All HERA I data from H1 and ZEUS, unpolarised
- Reduced  $E_p$  data from H1 and ZEUS
- HERA II data from H1, unpolarised

→ Different from the data combination:

- HERA II data from ZEUS, **polarised**

Data from  $Q^2 = 3.5 \text{ GeV}^2$

PDFs fits:

→ Closely follow HERAPDF2.0

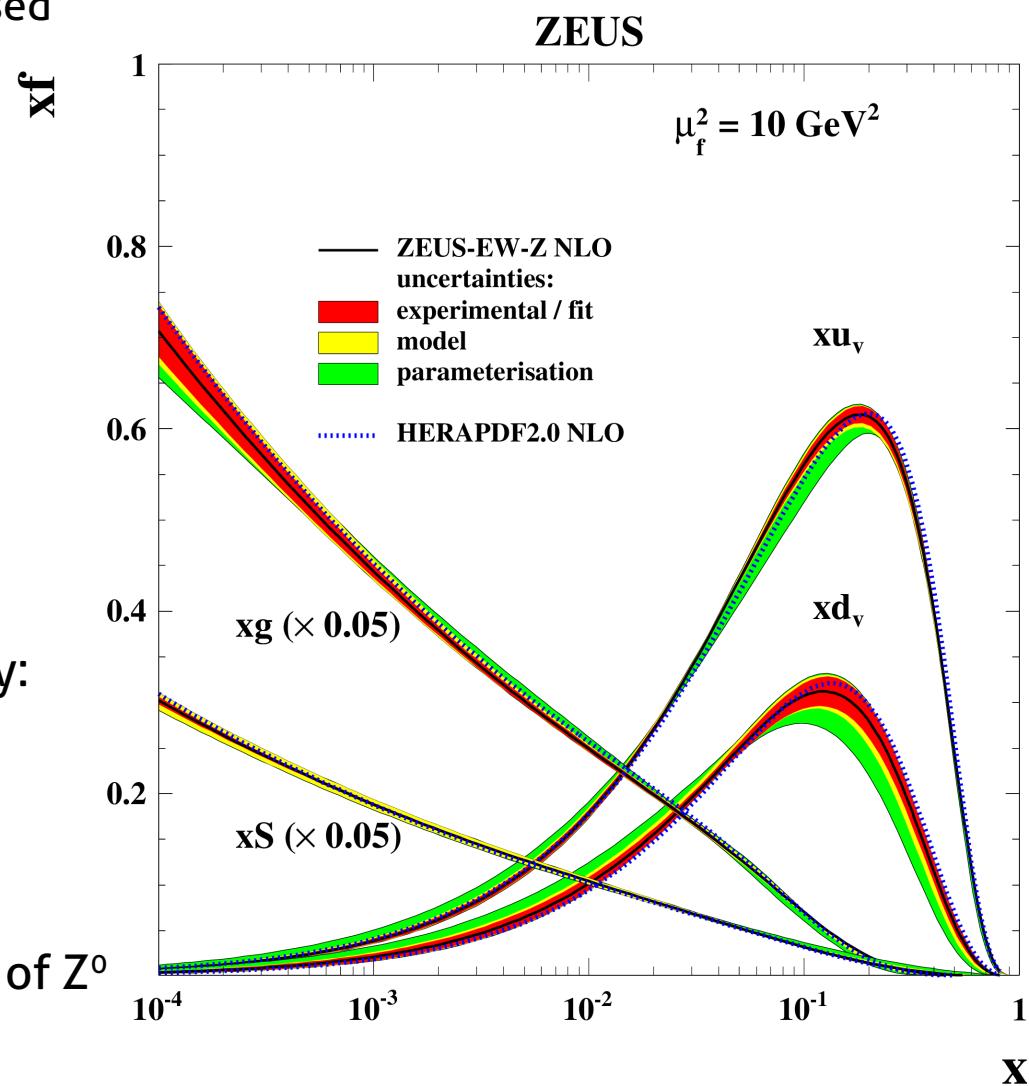
→ One parameter less for better fit stability:

$$x \bar{U}(x) = A_{\bar{U}} x^{B_u} (1-x)^{C_u}$$

→  $\Delta R$  calculated with EPRC code:

[desy.de/~hspiesb/eprc.html](http://desy.de/~hspiesb/eprc.html)

→ Simultaneous PDFs fits with 4 couplings of  $Z^0$  to quarks, or  $\sin^2(\Theta_w)$  and  $M_w$



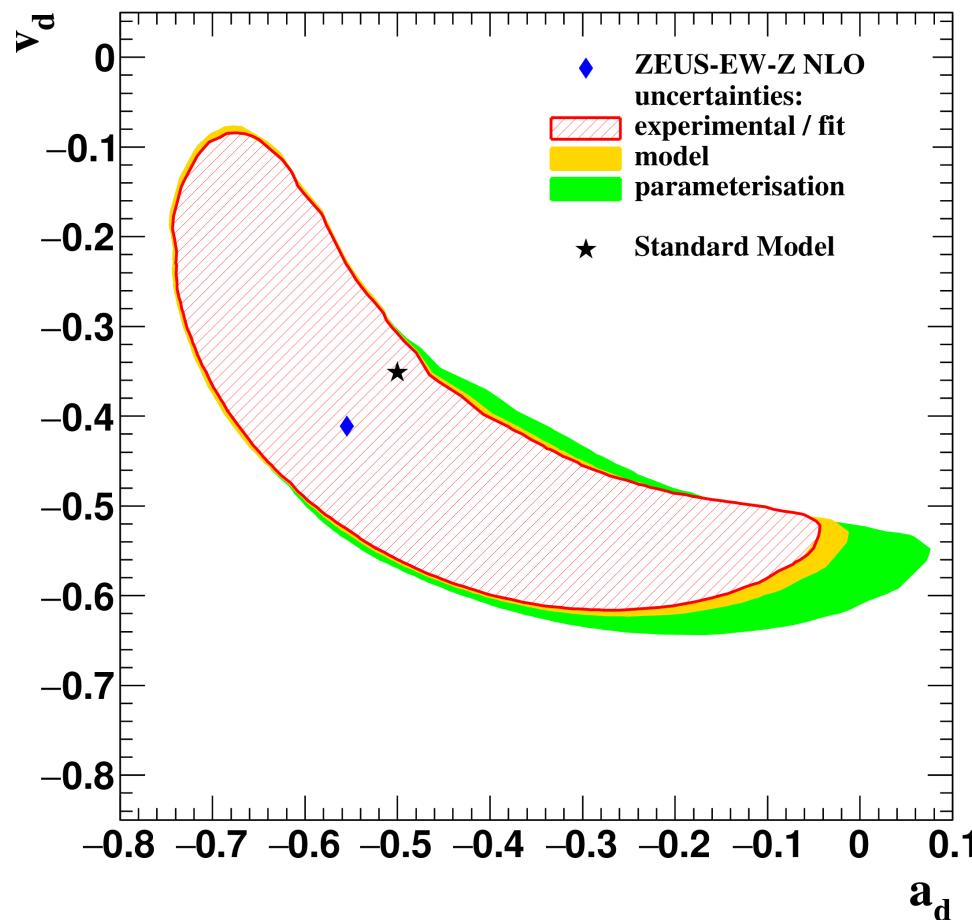
# ZEUS light quark couplings

In quark parton model:

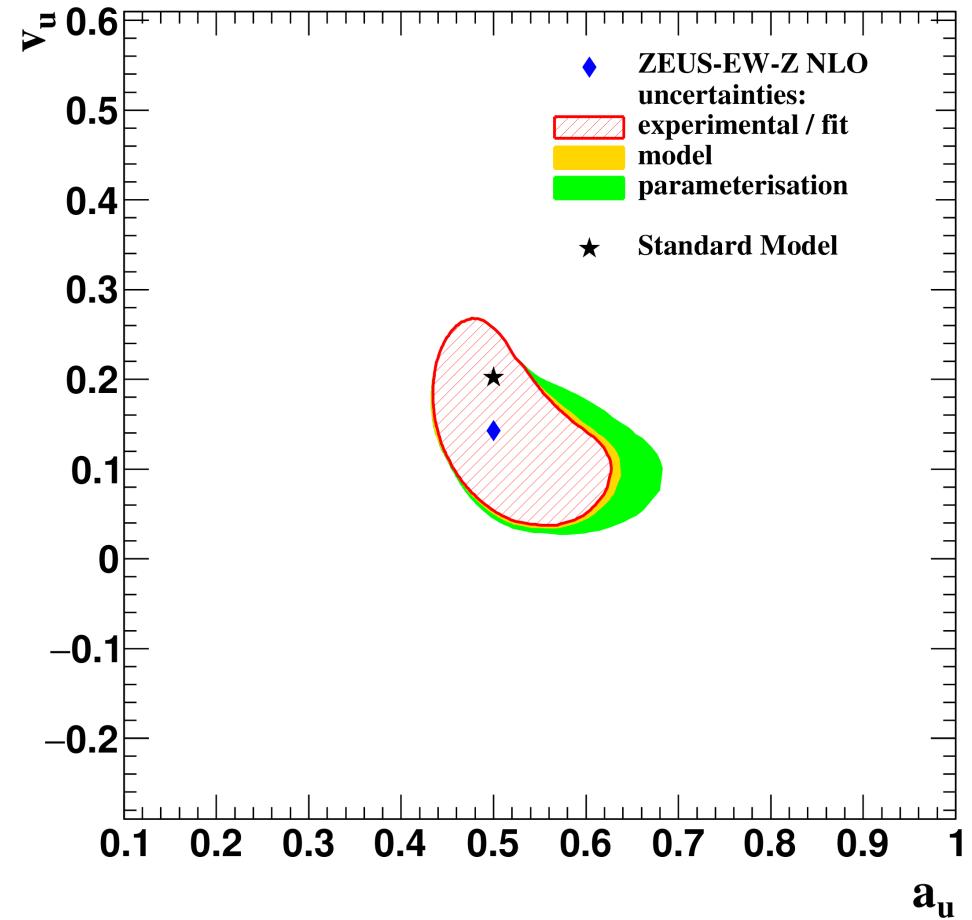
$$[F_2^y, F_2^{yz}, F_2^z] = \sum_q [e_q^2, 2e_q v_q, v_q^2 + a_q^2] x(q + \bar{q})$$

$$[xF_3^{yz}, xF_3^z] = \sum_q [e_q a_q, v_q a_q] 2x(q - \bar{q})$$

ZEUS

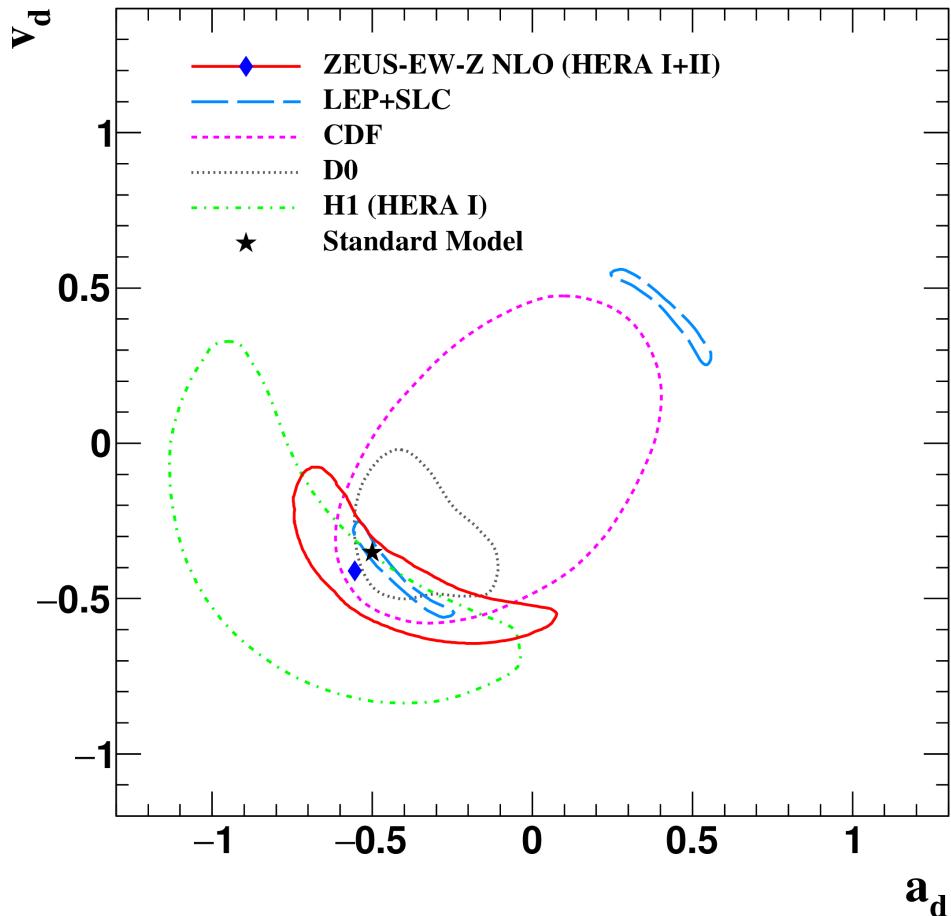


ZEUS



# Comparison to other measurements

ZEUS



$$a_d = -0.56^{+0.34}_{-0.14} \text{ (exp/fit)}^{+0.11}_{-0.05} \text{ (mod)}^{+0.20}_{-0.00} \text{ (param)}$$

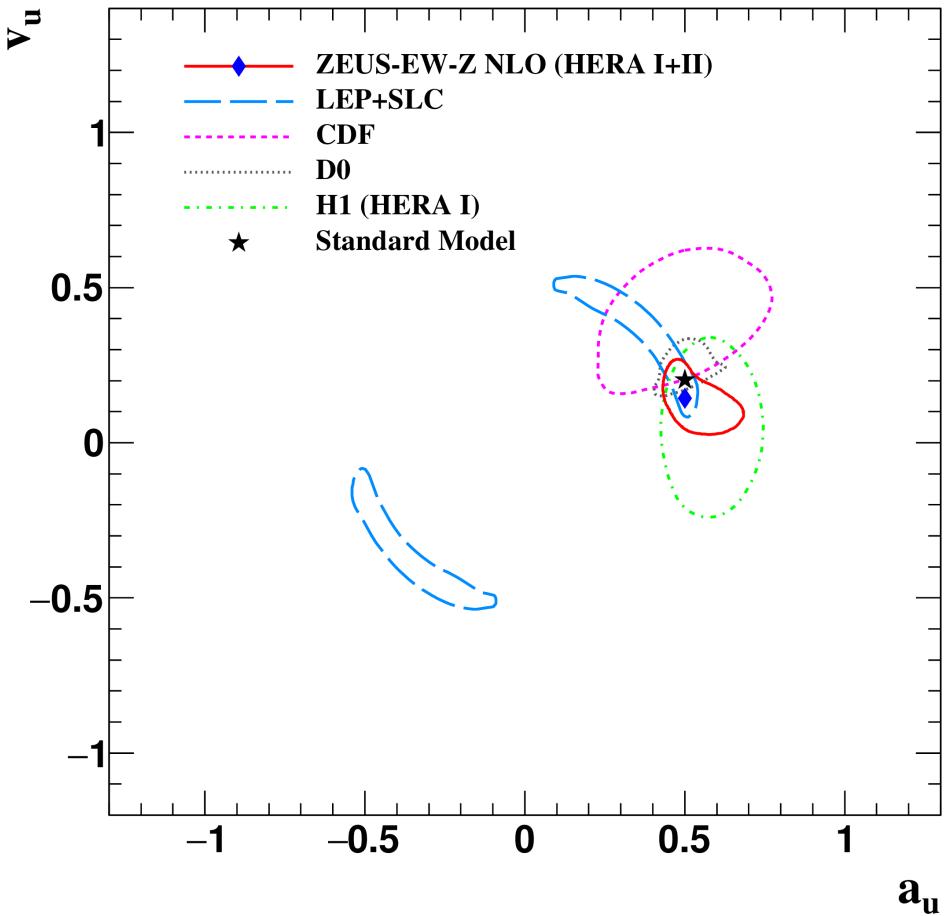
$$v_d = -0.41^{+0.24}_{-0.16} \text{ (exp/fit)}^{+0.04}_{-0.07} \text{ (mod)}^{+0.00}_{-0.08} \text{ (param)}$$

**a<sub>d</sub>**

SM

-0.50

ZEUS



$$a_u = 0.50^{+0.09}_{-0.05} \text{ (exp/fit)}^{+0.04}_{-0.02} \text{ (mod)}^{+0.08}_{-0.01} \text{ (param)}$$

$$v_u = 0.14^{+0.08}_{-0.08} \text{ (exp/fit)}^{+0.01}_{-0.00} \text{ (mod)}^{+0.03}_{-0.01} \text{ (param)}$$

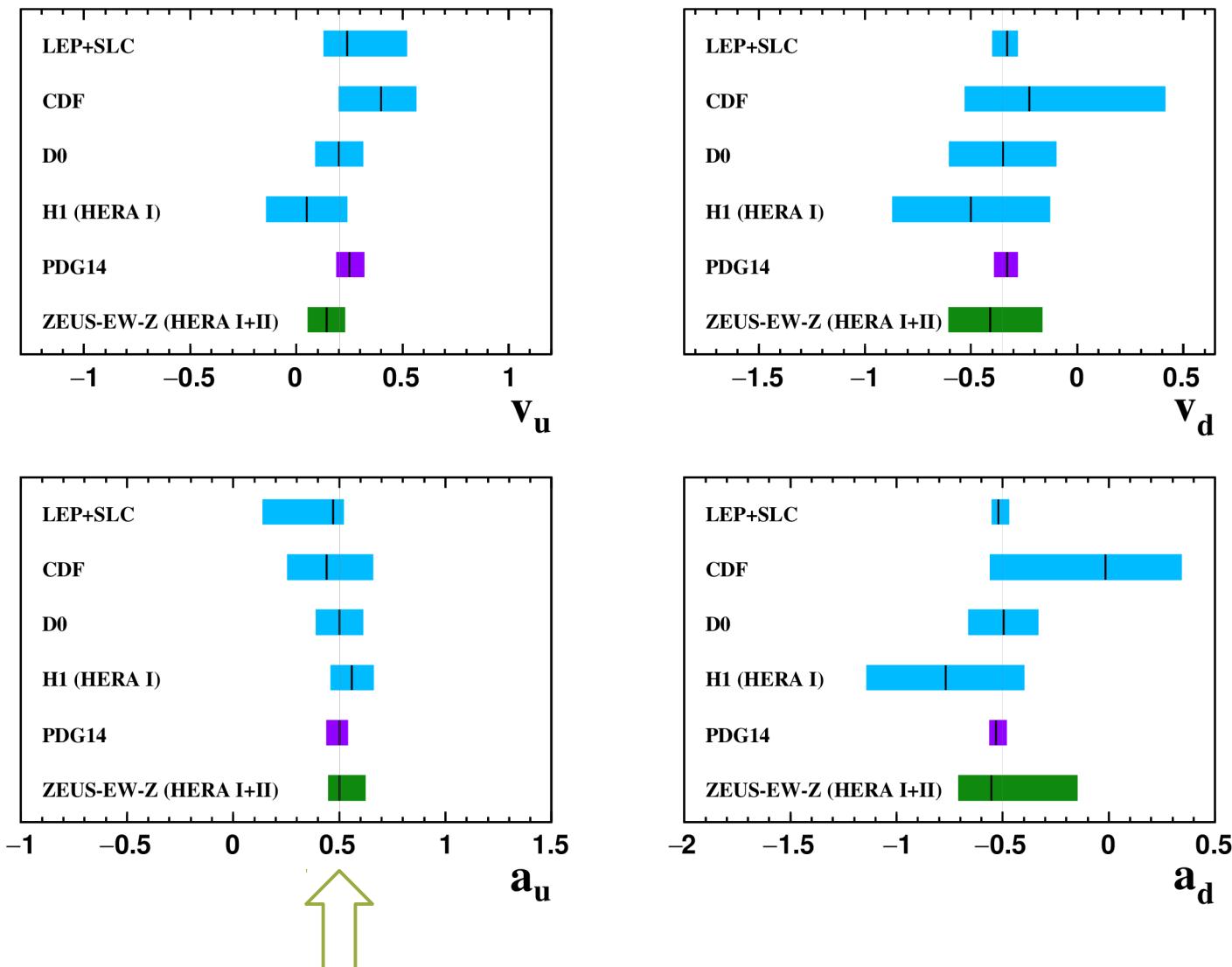
**a<sub>u</sub>**

SM

0.50

# Comparison to other measurements

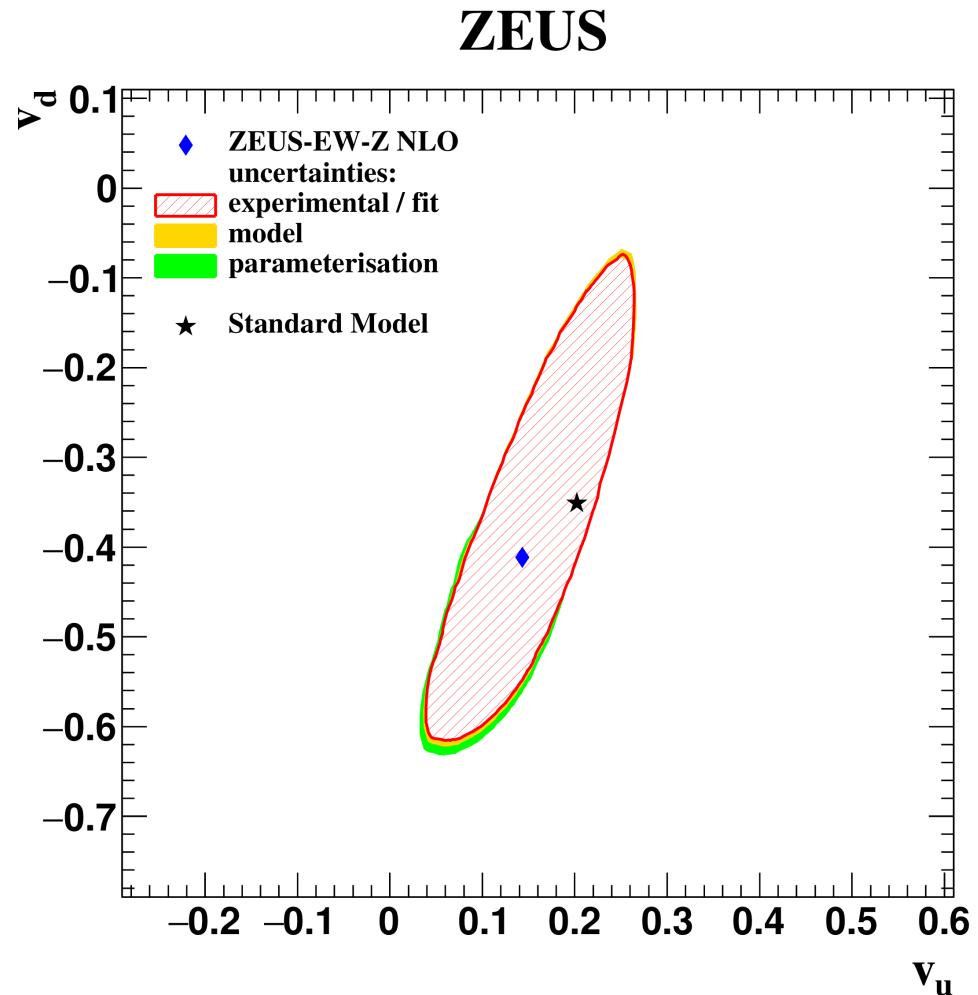
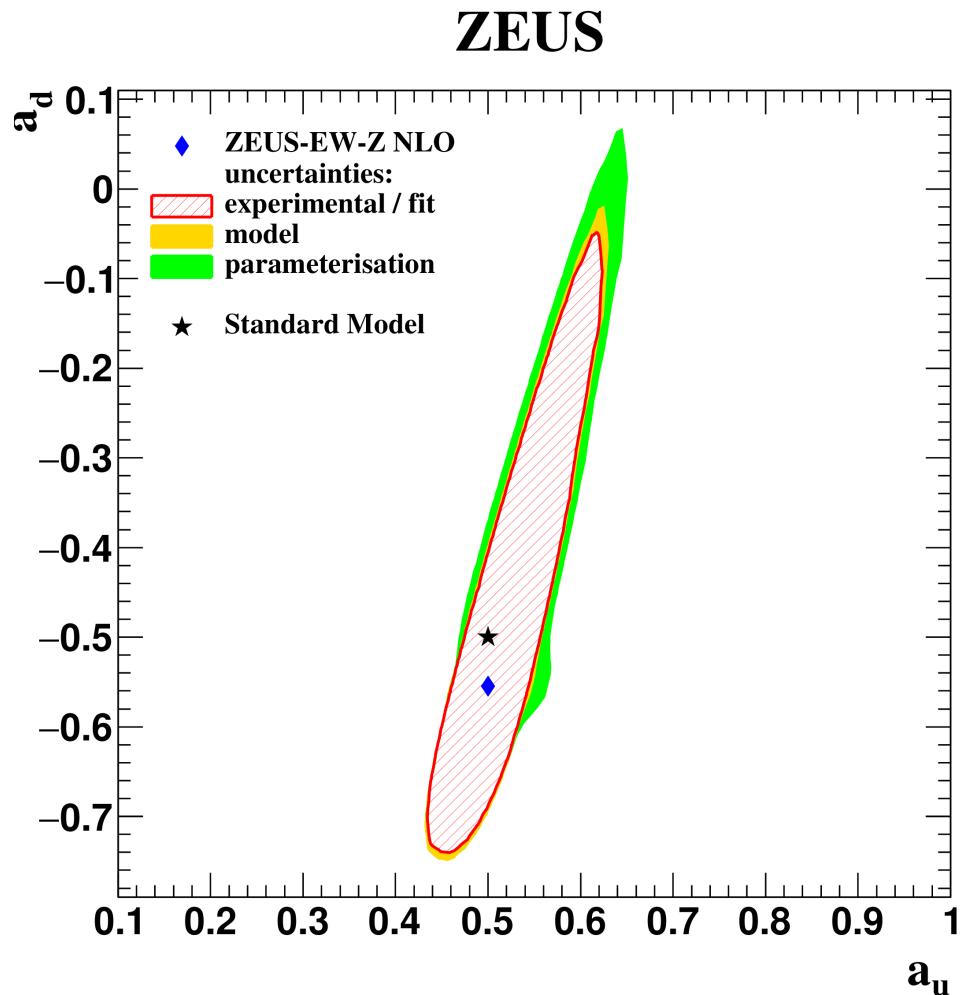
ZEUS



Remarkable sensitivity to **u-type** quark couplings

# Correlations

Fit shows high correlation of axial-vector and vector couplings between quark types:

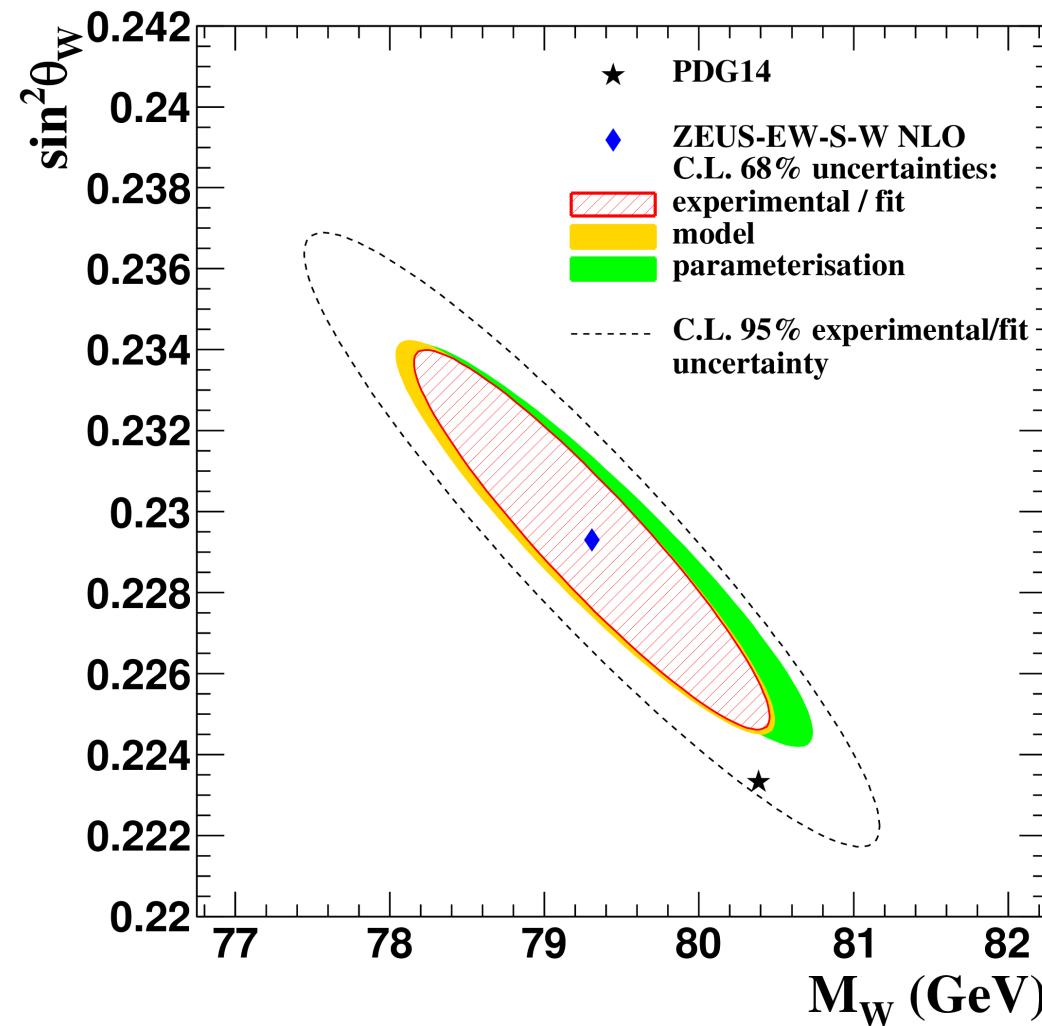


Their correlations to PDF parameters are small.

# $M_W$ and $\sin^2(\Theta_W)$

Simultaneous extraction of  $M_W$  and  $\sin^2(\Theta_W)$ :

ZEUS



$$\sigma_{\text{NC}}(\alpha, \sin^2(\Theta_W), M_Z)$$

$$\sigma_{\text{CC}}(G_F(\alpha, \sin^2(\Theta_W), M_W), M_W)$$

$$M_W = 79.30 \pm 0.76 {}^{+0.38}_{-0.08} {}^{+0.48}_{-0.10} {}^{(exp/fit)} {}^{(mod)} {}^{(param)}$$

$$\sin^2(\Theta_W) = 0.2293 \pm 0.0031 {}^{+0.005}_{-0.001} {}^{+0.003}_{-0.001} {}^{(exp/fit)} {}^{(mod)} {}^{(param)}$$

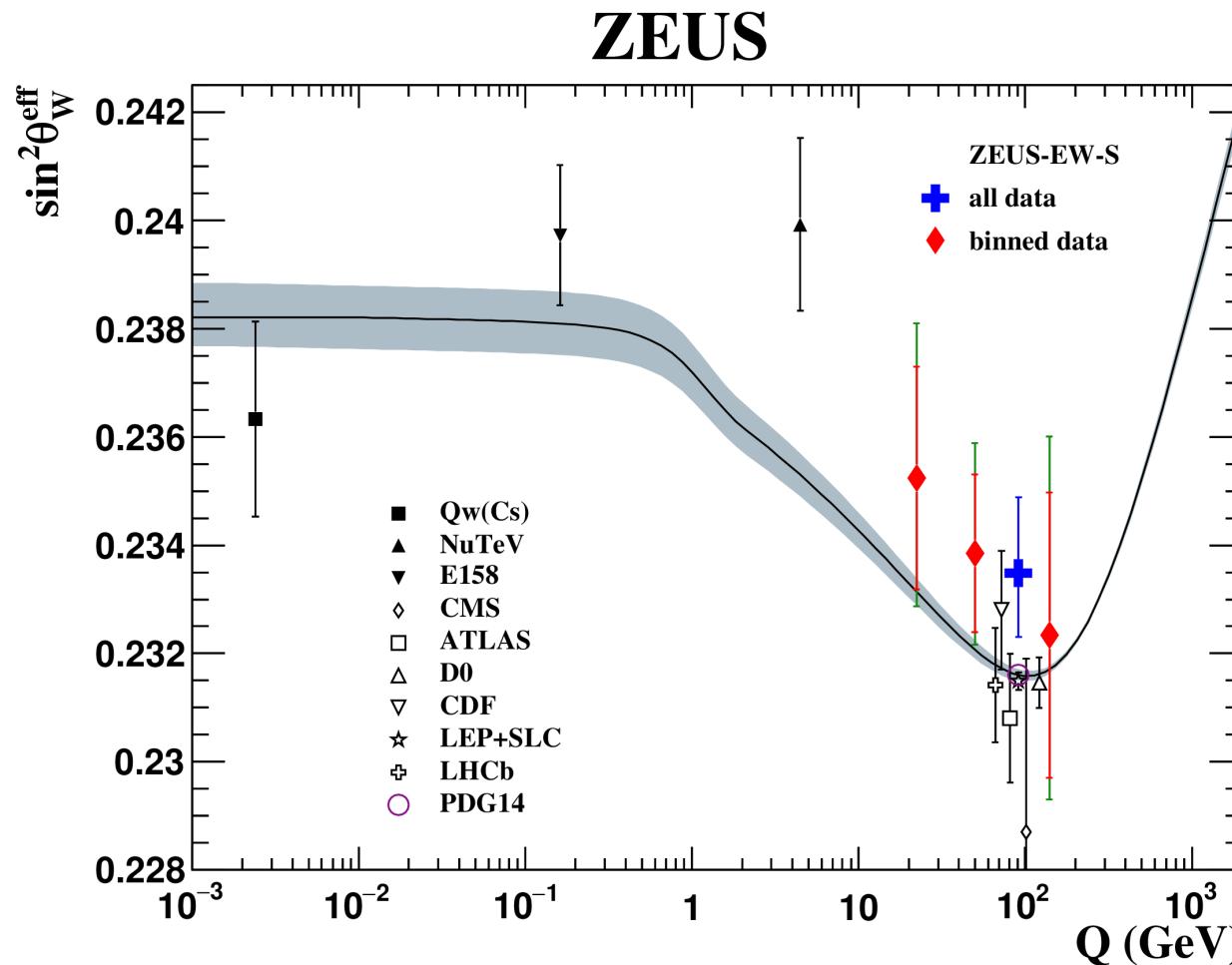
Good agreement with world average:

$$M_W^{\text{DPG14}} = 80.385 \pm 0.015$$

$$\sin^2(\Theta_W)^{\text{PDG14 on-shell}} = 0.22333 \pm 0.00011$$

# Effective $\sin^2(\Theta_W)$

On-shell measurements for the whole data and for three bins in  $Q^2$  translated to effective  $\sin^2(\Theta_W)$ :



First observation of  $\sin^2(\Theta_W)^{\text{eff}}$  running from one experiment.

# H1 QCD + EW fits

H1prelim-16-041

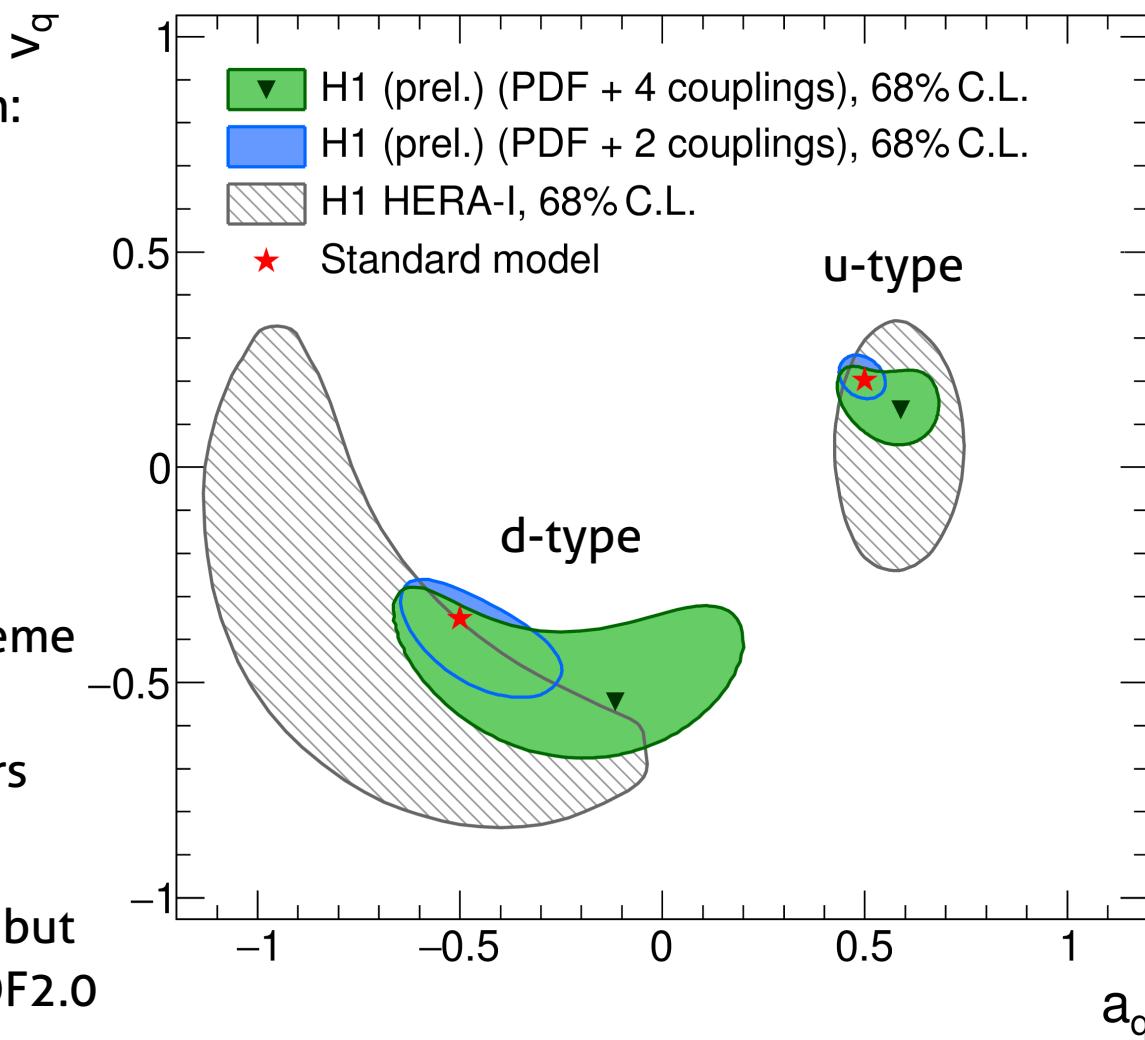
Used uncombined datasets:

- Same as in the data combination:
  - All HERA I data from H1, unpolarised
  - Reduced  $E_p$  data from H1
- Different from the data combination:
  - HERA II data from H1, **polarised**

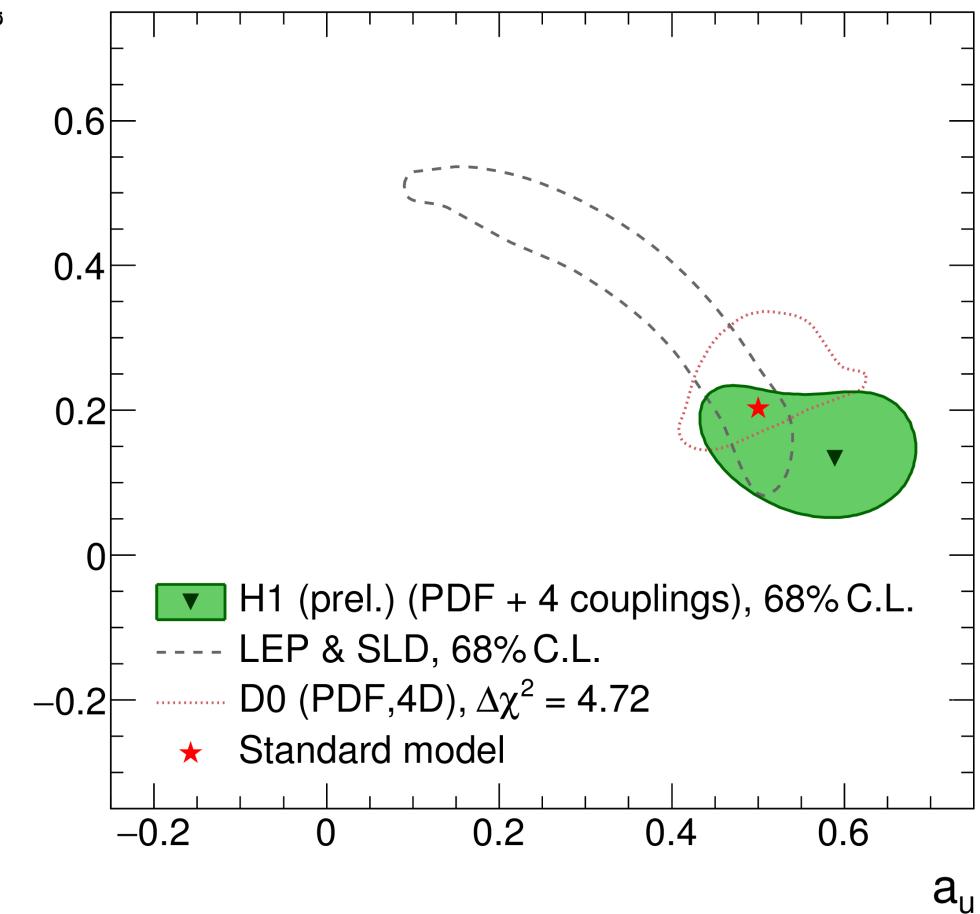
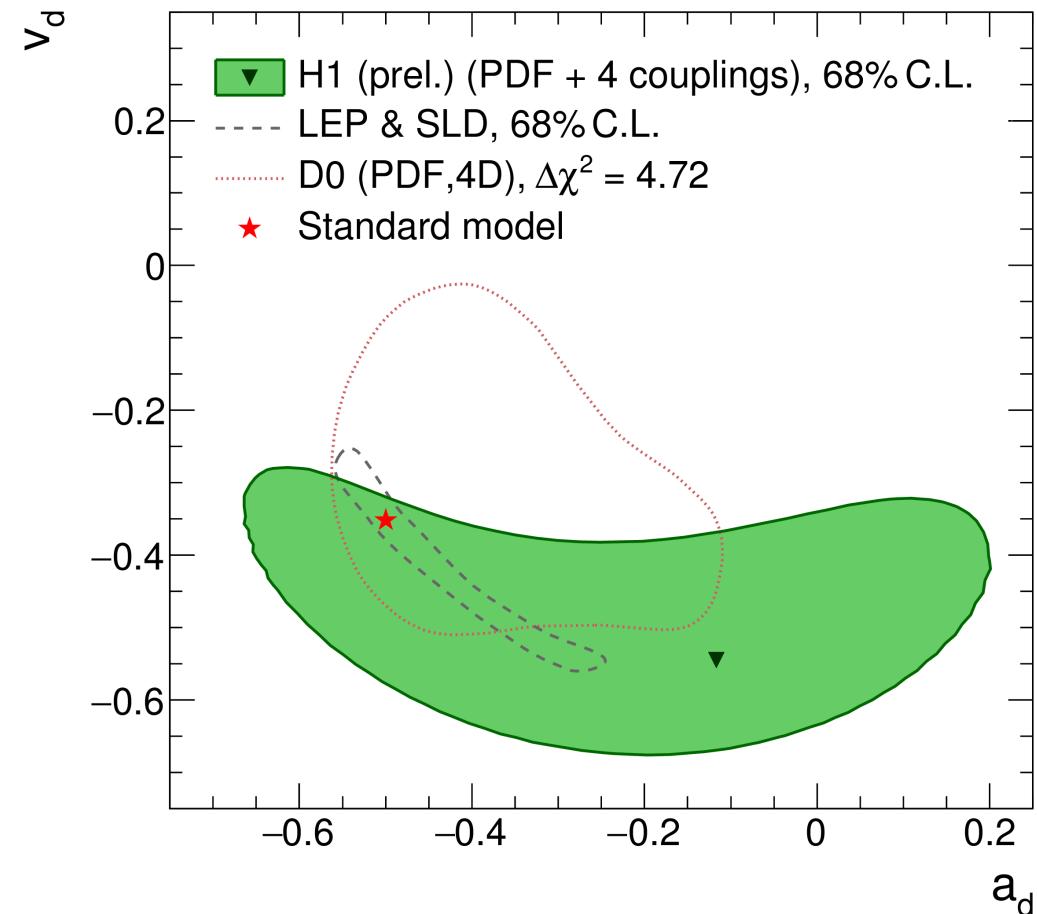
Data from  $Q^2 = 12 \text{ GeV}^2$

PDFs fits:

- Basics similar to ZEUS approach
- DGLAP evolution at NNLO
- Calculations strictly in on-shell scheme
- Polarisation values fitted within uncertainties as 4 additional parameters
- New C++ fitter and Alpos code used
- Different (log-normal)  $\chi^2$  definition, but results similar to using  $\chi^2$  from HERAPDF2.0

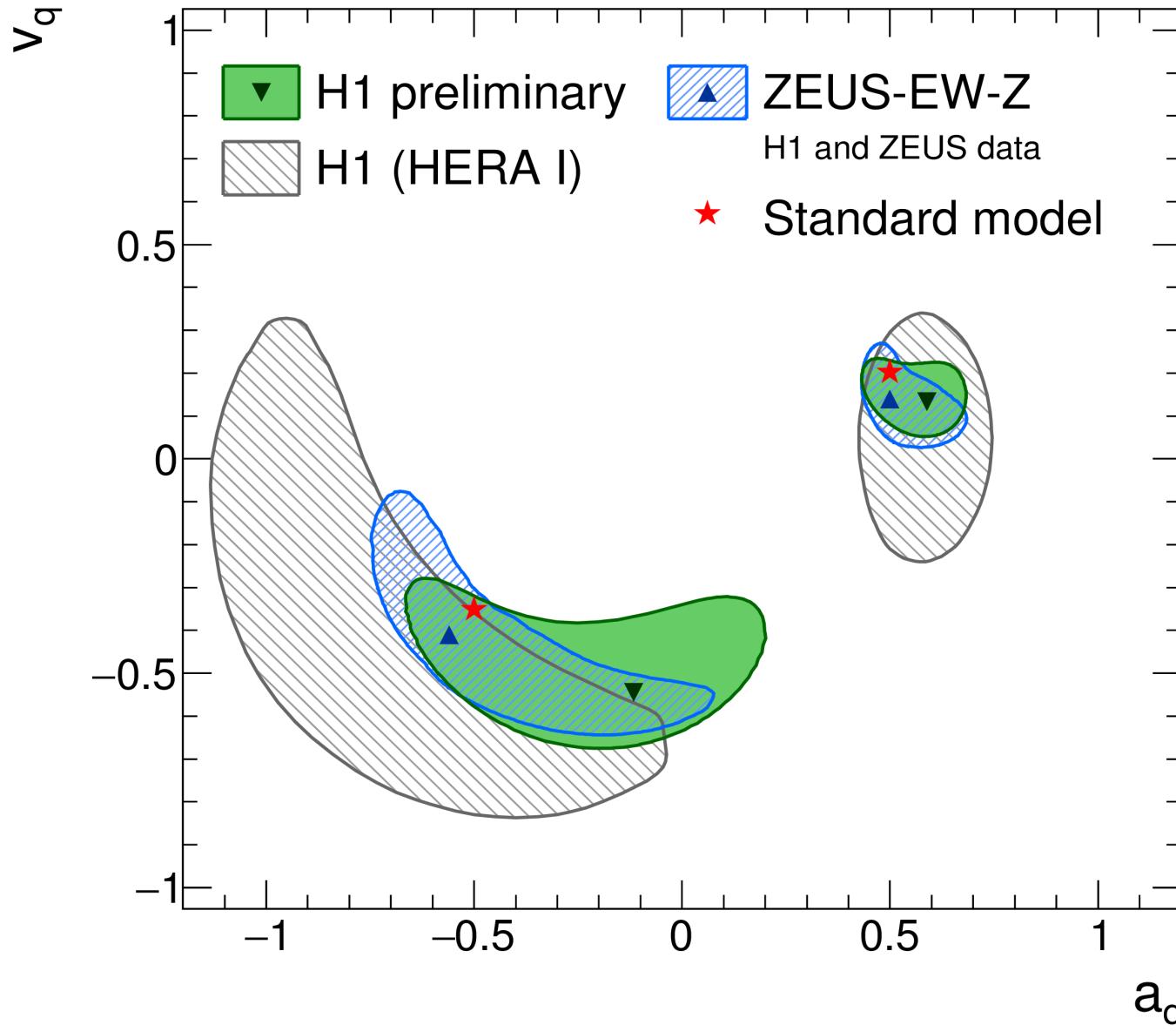


# Comparison to other measurements



Comparable precision for **u-type** quark couplings

# Comparison to ZEUS result

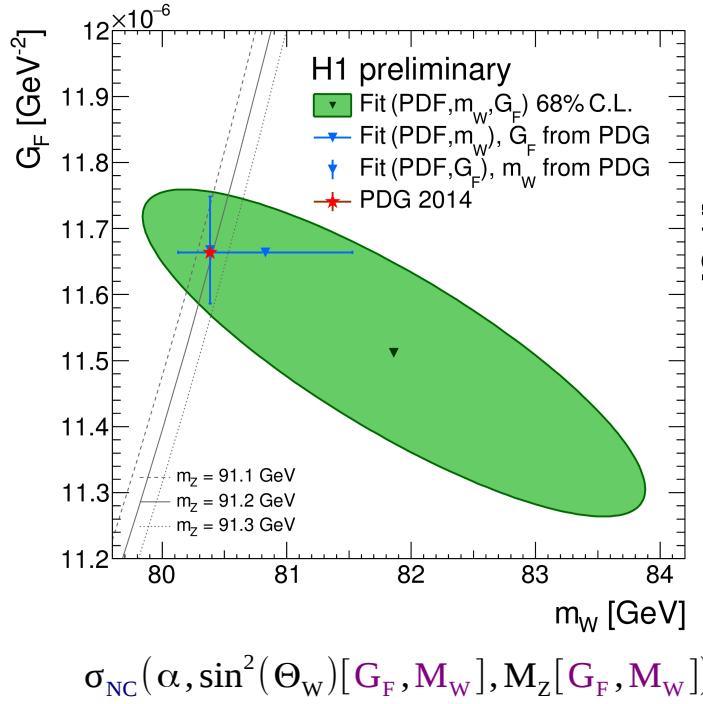
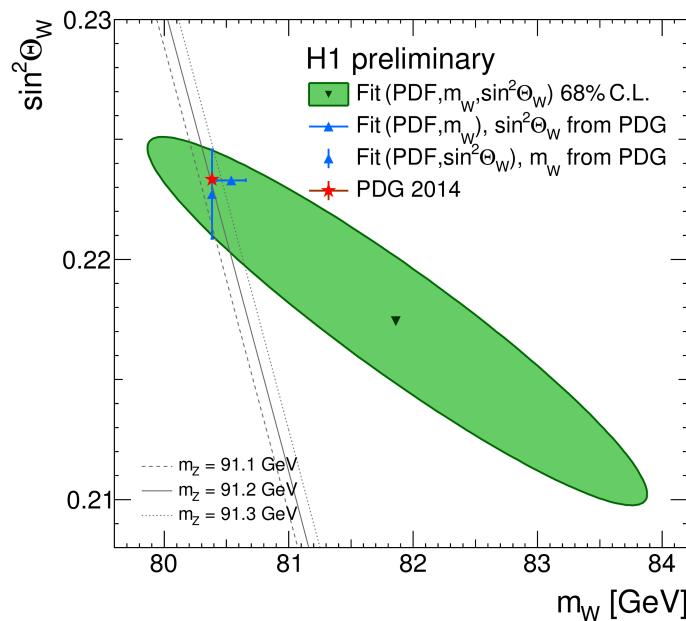


# $M_W$ and $\sin^2(\Theta_W)$ , $G_F$ , $M_Z$

Simultaneous extraction of pairs of parameters:

$$\sigma_{NC}(\alpha, \sin^2(\Theta_W), M_Z[\sin^2(\Theta_W), M_W])$$

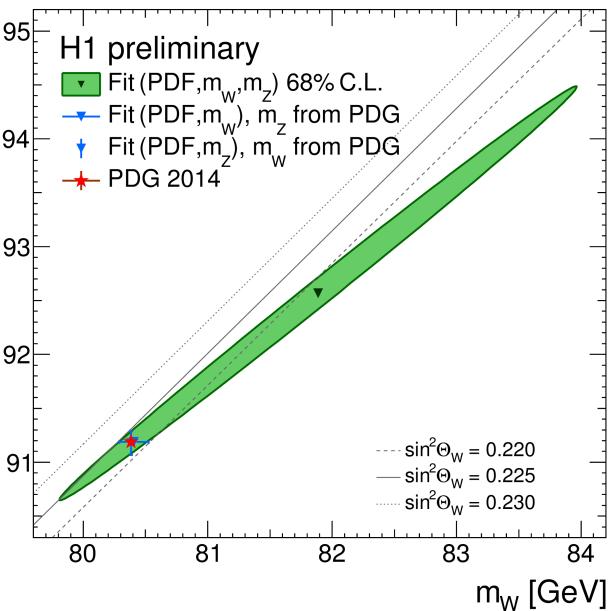
$$\sigma_{CC}(G_F[\alpha, \sin^2(\Theta_W), M_W], M_W)$$



$$\sigma_{CC}(G_F, M_W)$$

$$\sigma_{NC}(\alpha, \sin^2(\Theta_W)[M_Z, M_W], M_Z)$$

$$\sigma_{CC}(G_F[\alpha, M_Z, M_W], M_W)$$



Determined mass of W boson using external mass of  $Z^0$ :

$$\sigma_{NC}(\alpha, \sin^2(\Theta_W)[M_Z, M_W], M_Z)$$

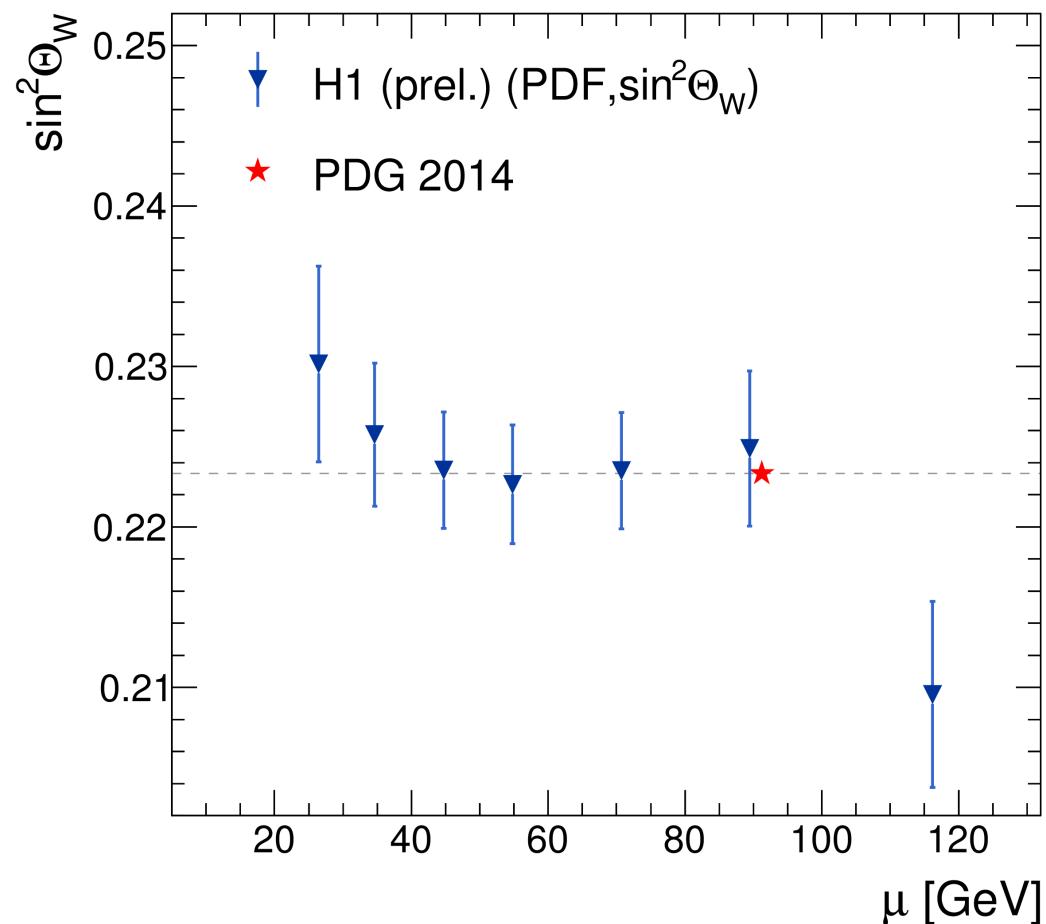
$$\sigma_{CC}(G_F[\alpha, M_Z, M_W], M_W)$$

$$m_W = 80.407 \pm 0.118_{(\text{exp}, \text{pdf})} \pm 0.005_{(m_z, m_t, m_h)}$$

Result consistent with PDG2014:  $M_W^{PDG14} = 80.385 \pm 0.015$

# On-shell $\sin^2(\Theta_W)$

On-shell measurement for seven bins in  $Q^2$ :



$$\sin^2(\Theta_W) = 0.2252 \pm 0.0011_{\text{(exp/fit)}}^{+0.0003} {}_{\text{(mod)}}^{-0.0001} {}_{\text{(param)}}^{-0.0001}$$

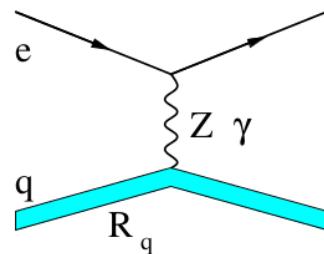
Good agreement with world average:

$$\sin^2(\Theta_W)^{\text{PDG 14 on-shell}} = 0.22333 \pm 0.00011$$

Unique measurement of  $\sin^2(\Theta_W)$  at different scales.

# BSM physics - quark form factor

One of the possible parameterisations of deviations from SM – spatial distribution or substructure of electrons and/or quarks:



$$\frac{d\sigma}{dQ^2} = \frac{d\sigma^{SM}}{dQ^2} \left(1 - \frac{R_e^2}{6} Q^2\right)^2 \left(1 - \frac{R_q^2}{6} Q^2\right)^2$$

$R_e$ ,  $R_q$  – root mean square radii of the electroweak charge distributions in the electron and quark.

Same dependence expected for NC and CC  $e^+p$  and  $e^-p$ .

We assume  $R_e^2 = 0$  and consider both, positive and negative values of  $R_q^2$

HERA data is a core of any PDF extraction, and thus simultaneous fit, PDF+BSM, is necessary for any BSM analysis. For  $R_q^2$  such fit provide:

$$R_q^2 \text{ Data} = -[0.14 \cdot 10^{-16} \text{ cm}]^2$$

in agreement with SM expectation of  $R_q^{\text{Data}} = 0$ .

# Frequentist approach

Monte Carlo replicas of the whole data set were generated as:

$$\mu^i = [m_0^i + \delta_{tot.uncor.}^i \cdot r_{tot.uncor.}^i \cdot \mu_0^i] \cdot (1 + \sum_j \gamma^j \cdot r_{sys.sh.}^j)$$

$r^i, r^j$  – Gaussian random numbers.

**Previous  
method**  $R_q$ -only

$R_q^2$  parameter fitted  
with PDFs **fixed to SM PDFs**.

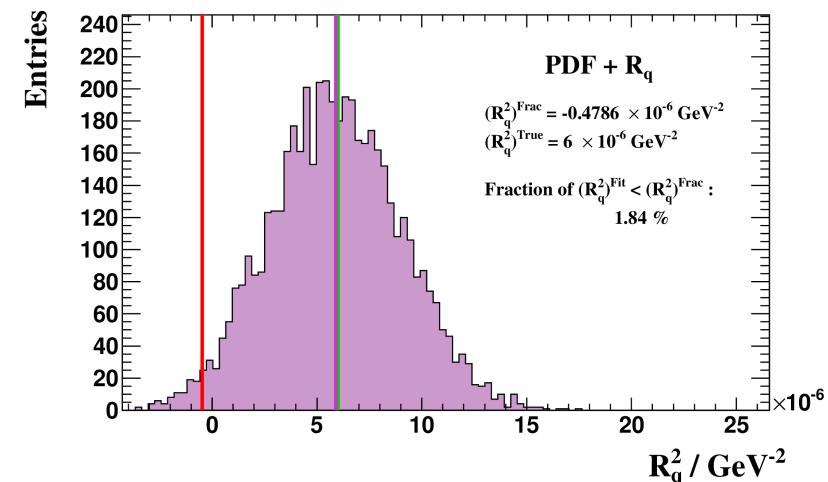
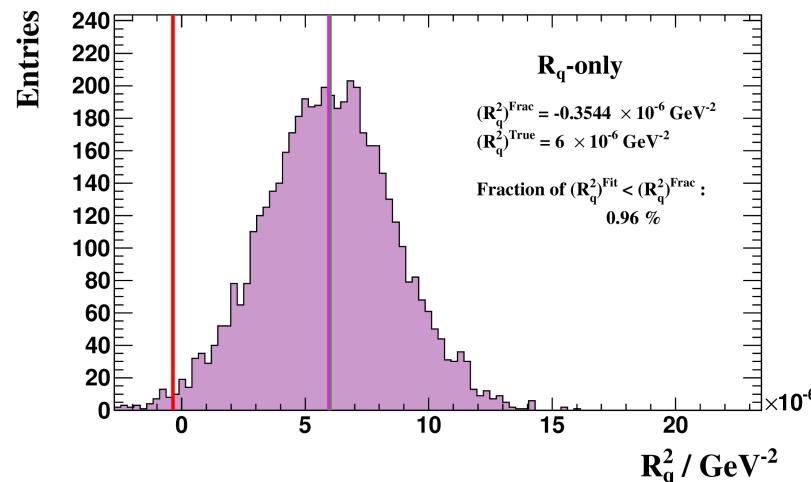
And **two different** procedures were tested:

**New  
method**

PDF+ $R_q$

$R_q^2$  parameter fitted  
**simultaneously** with PDFs.

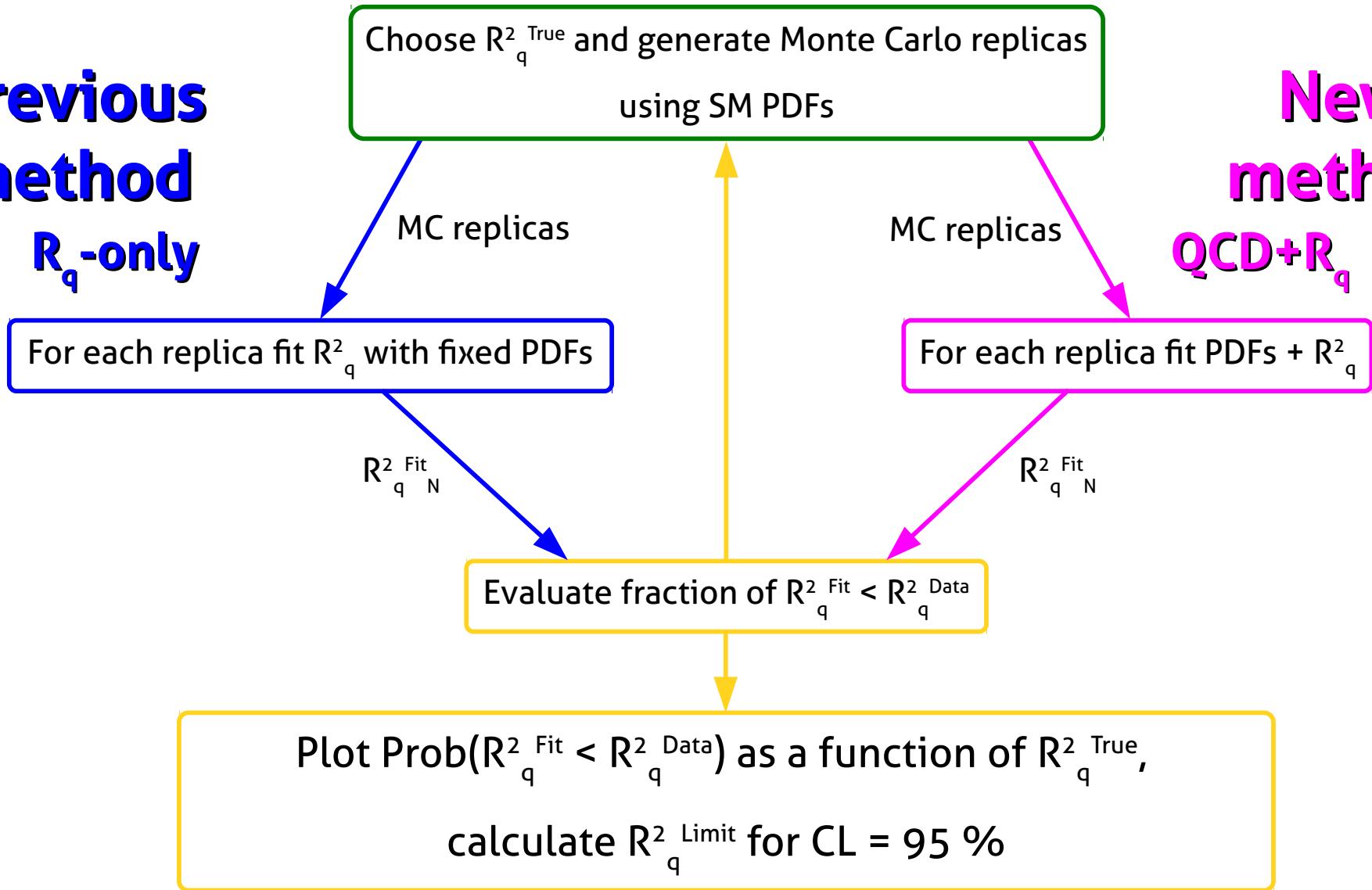
For example, for  $R_q^{True} = 0.48 \cdot 10^{-16}$  cm:



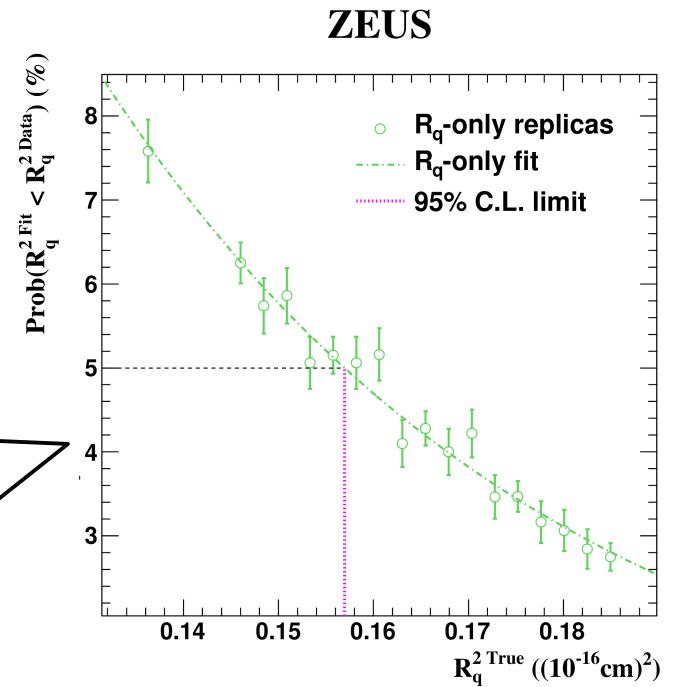
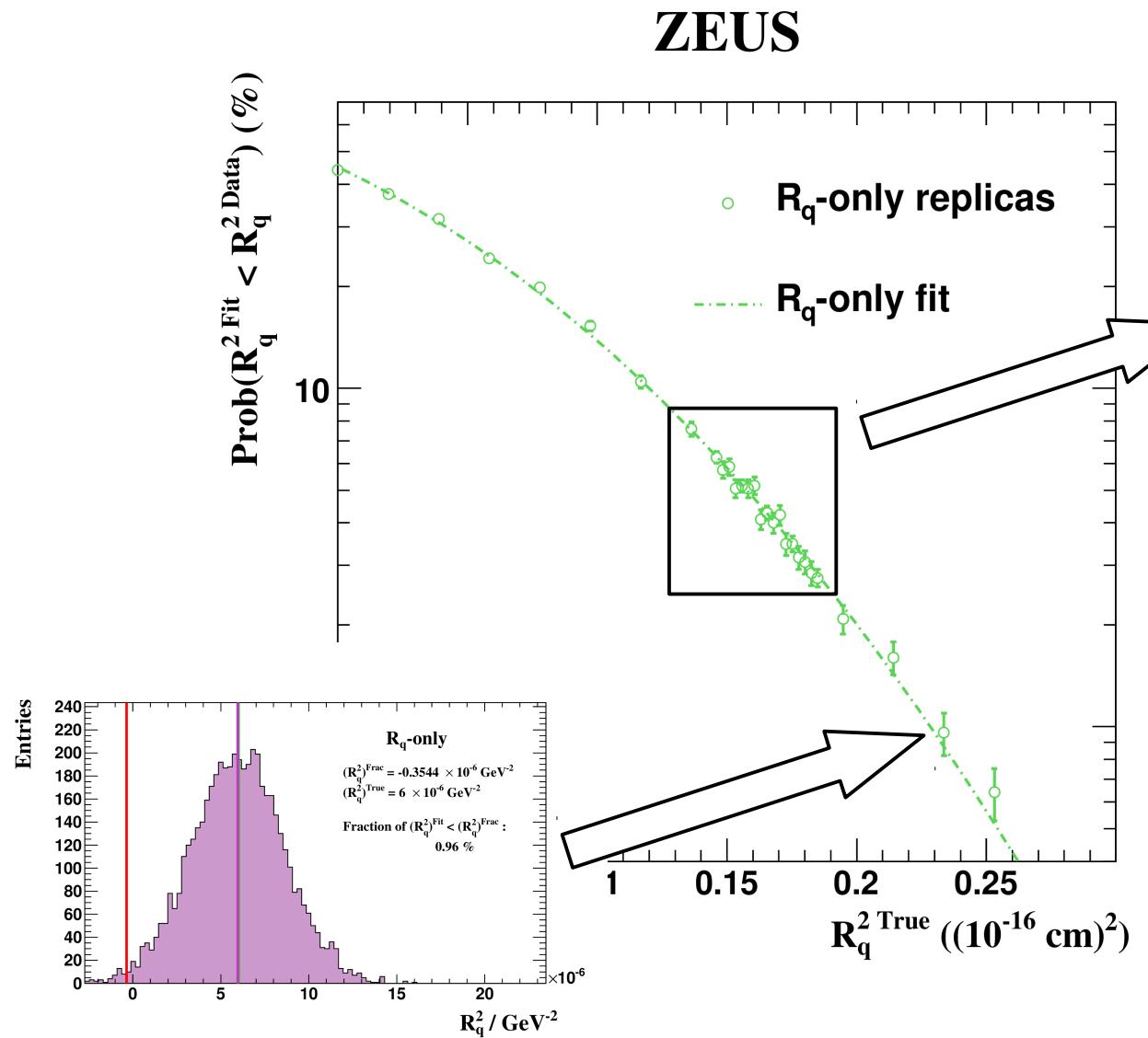
# Analysis flowchart

**Previous  
method**  
 **$R_q$ -only**

**New  
method**  
**QCD+ $R_q$**



# $R_q$ -only



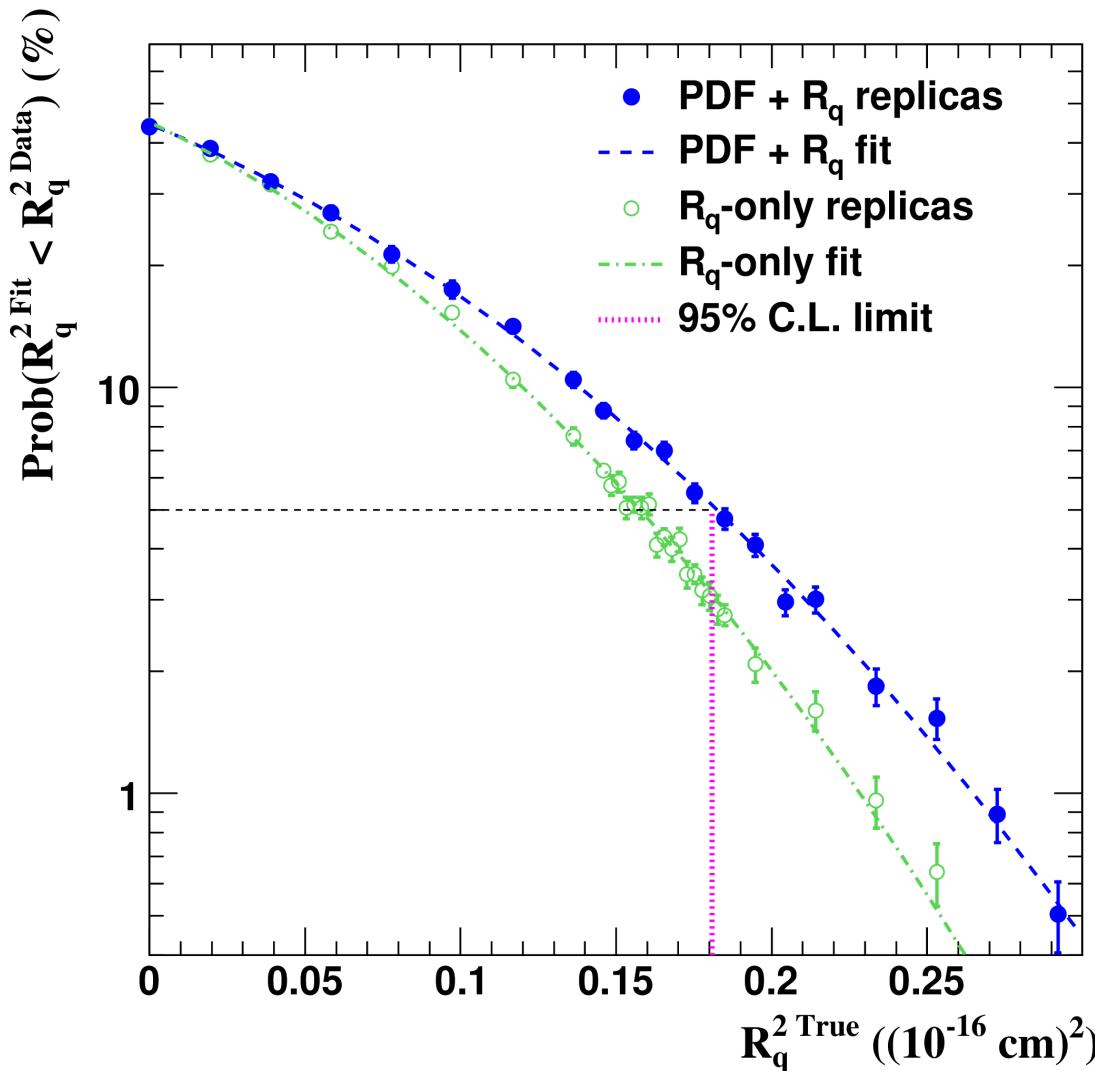
Fractions close to 5% fitted with:

$$f(x) = 5 \cdot \exp((x - A) \cdot B)$$

$$R_q^{\text{Limit}} = 0.40 \cdot 10^{-16} \text{ cm}$$

QCD+ $R_q$ 

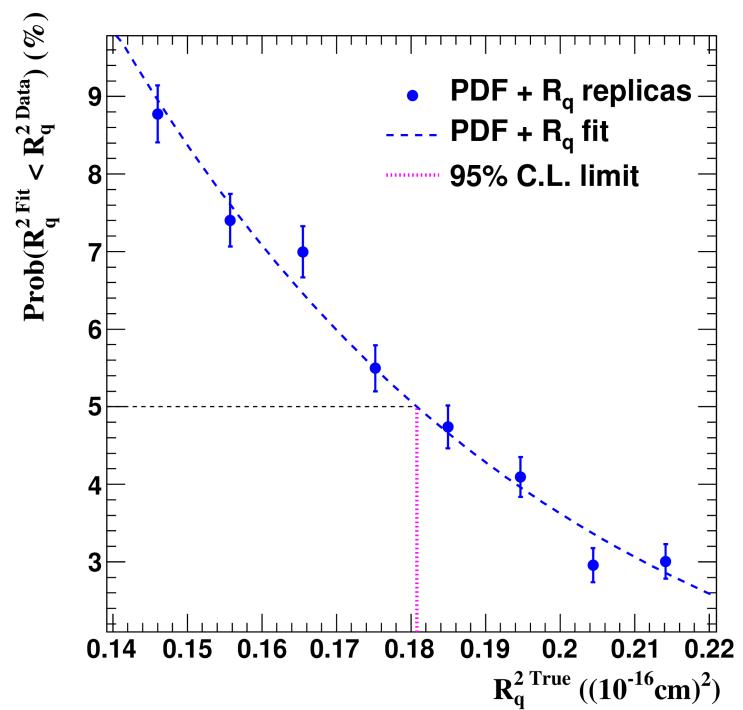
ZEUS



Fractions close to 5% fitted with:

$$f(x) = 5 \cdot \exp((x - A) \cdot B)$$

ZEUS

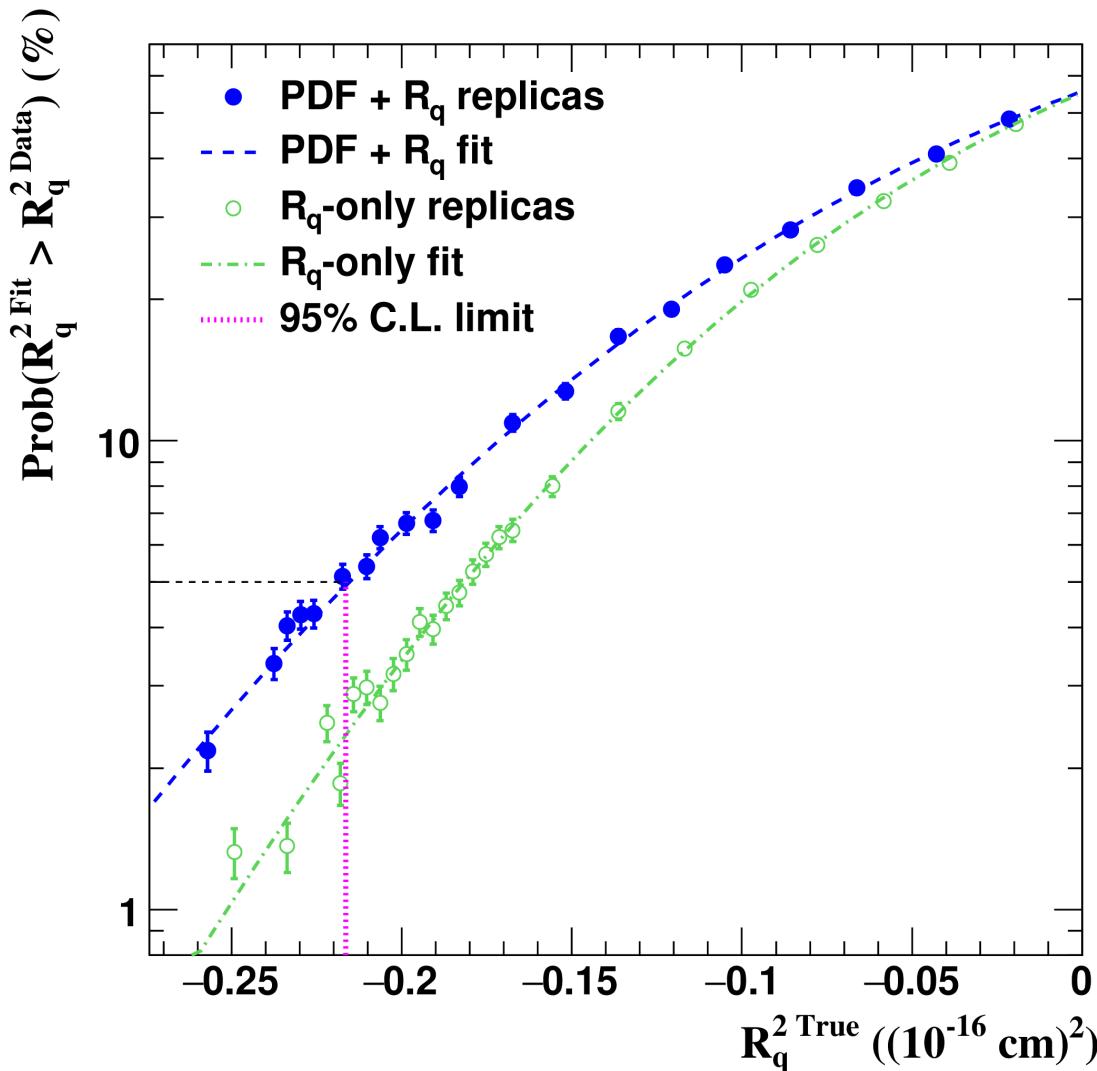


$$R_q^{\text{Limit}} = 0.43 \cdot 10^{-16} \text{ cm}$$

# Negative $R_q^2$ limit:

**QCD+ $R_q$**

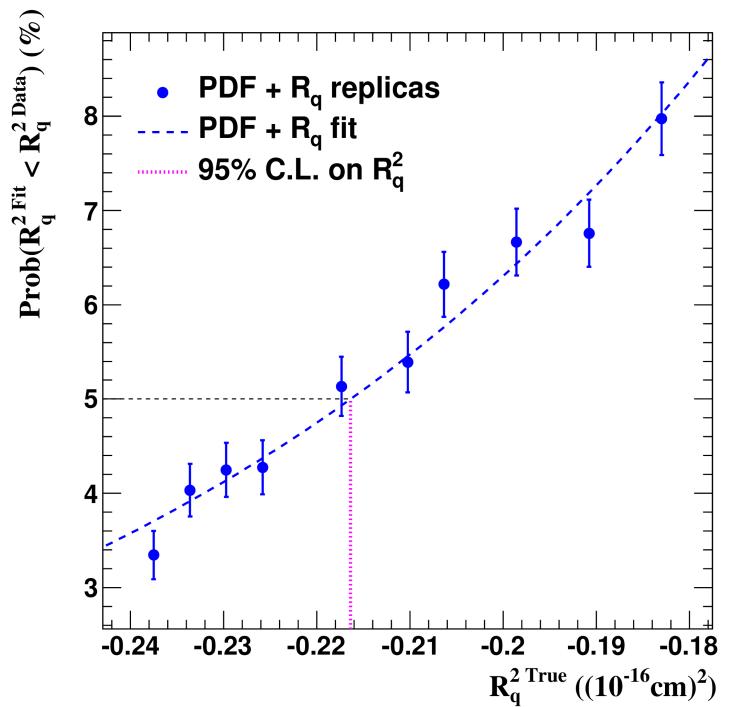
**ZEUS**



Fractions close to 5% fitted with:

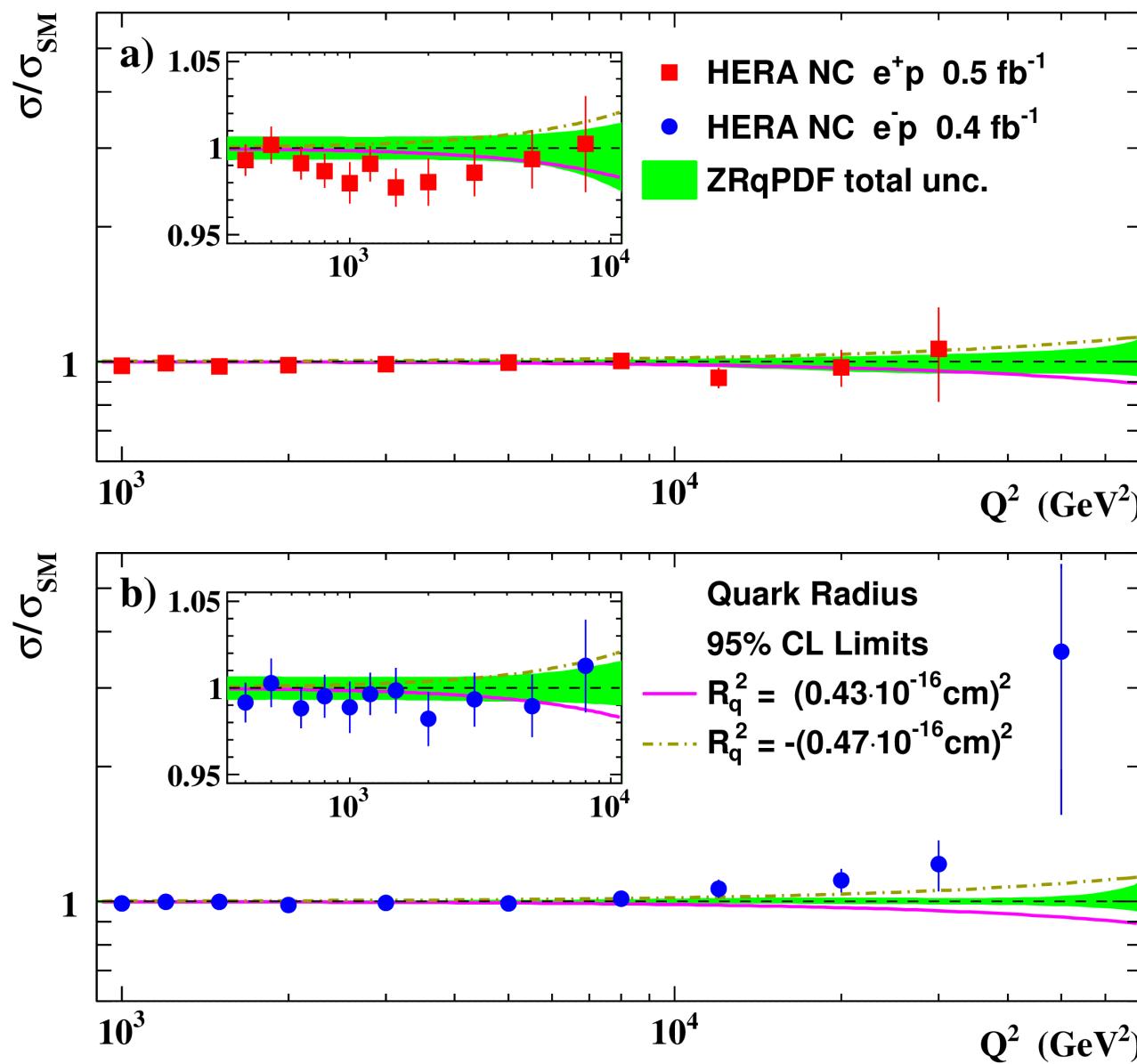
$$f(x) = 5 \cdot \exp((x - A) \cdot B)$$

**ZEUS**



$$R_q^2 \text{ Limit} = -[0.47 \cdot 10^{-16} \text{ cm}]^2$$

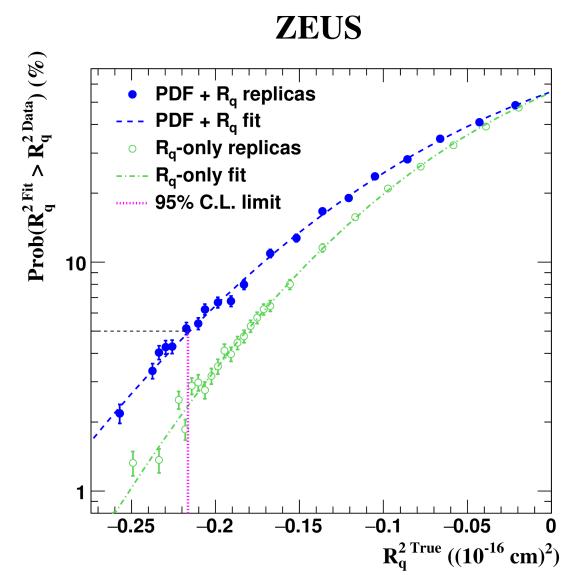
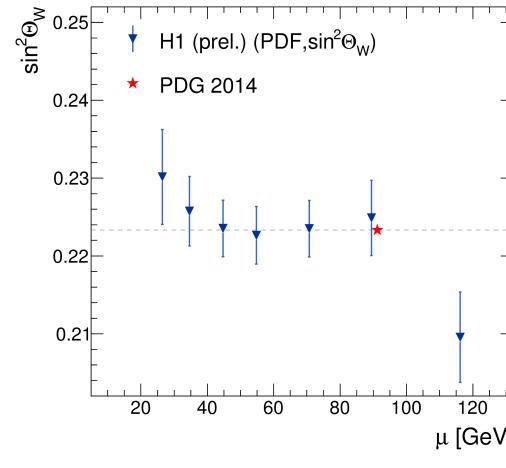
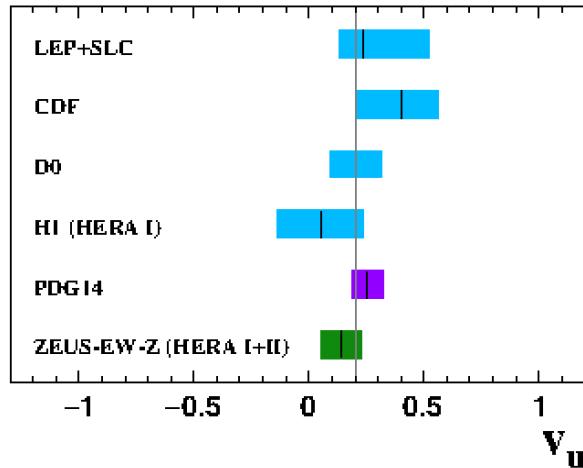
# ZEUS



Comparison of  $R_q^2$  exclusion limits to HERA NC ep DIS data.

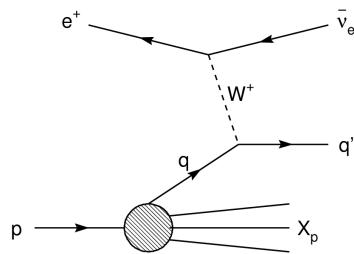
# Summary

- HERA polarised inclusive data allows to determine electroweak parameters simultaneously with PDFs
- Couplings of u-type quarks among the most accurate in the world
- Unique observations of  $\sin^2(\Theta_W)$  and  $\sin^2(\Theta_W)^{\text{eff}}$  running from one experiment
- First BSM limits based on the new approach: simultaneous fit of PDF and BSM contribution; it shows that limits obtained with “previous” method  $\sim 10\text{-}20\%$  too strong.



# Backup

## QCD analysis of combined DIS data



Charged Current :

$$\frac{d^2 \sigma_{CC}^{e\mp p}}{dx dQ^2} = \frac{G_F^2}{4\pi x} \cdot \kappa^2 \cdot (Y_+ \cdot W_2^\mp \pm Y_- \cdot x \cdot W_3^\mp - y^2 \cdot W_L^\mp)$$

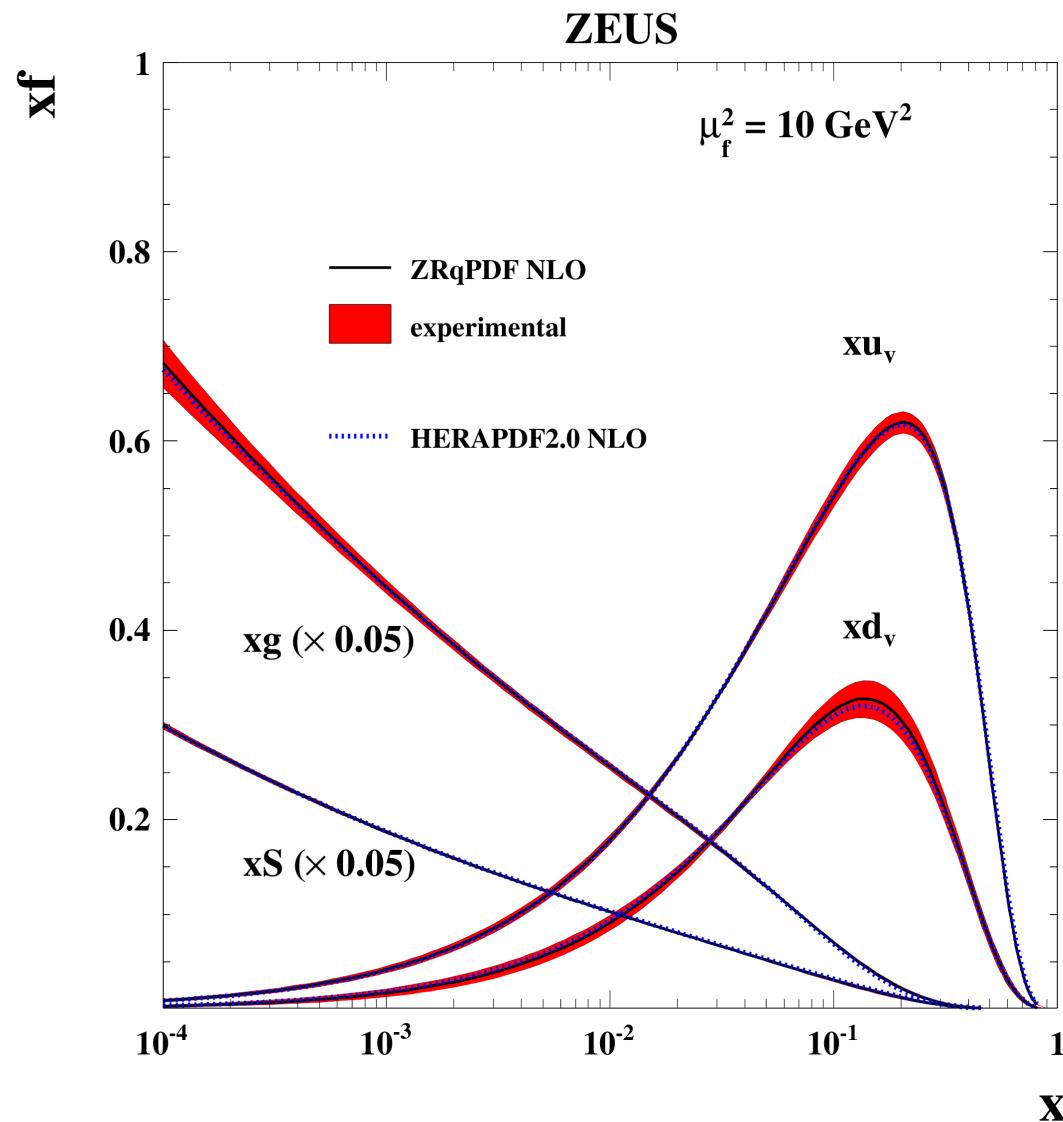
$$\kappa = \frac{M_W^2}{M_W^2 + Q^2}$$

$$W_2^- = x(U + \bar{D}) \quad W_2^+ = x(D + \bar{U})$$

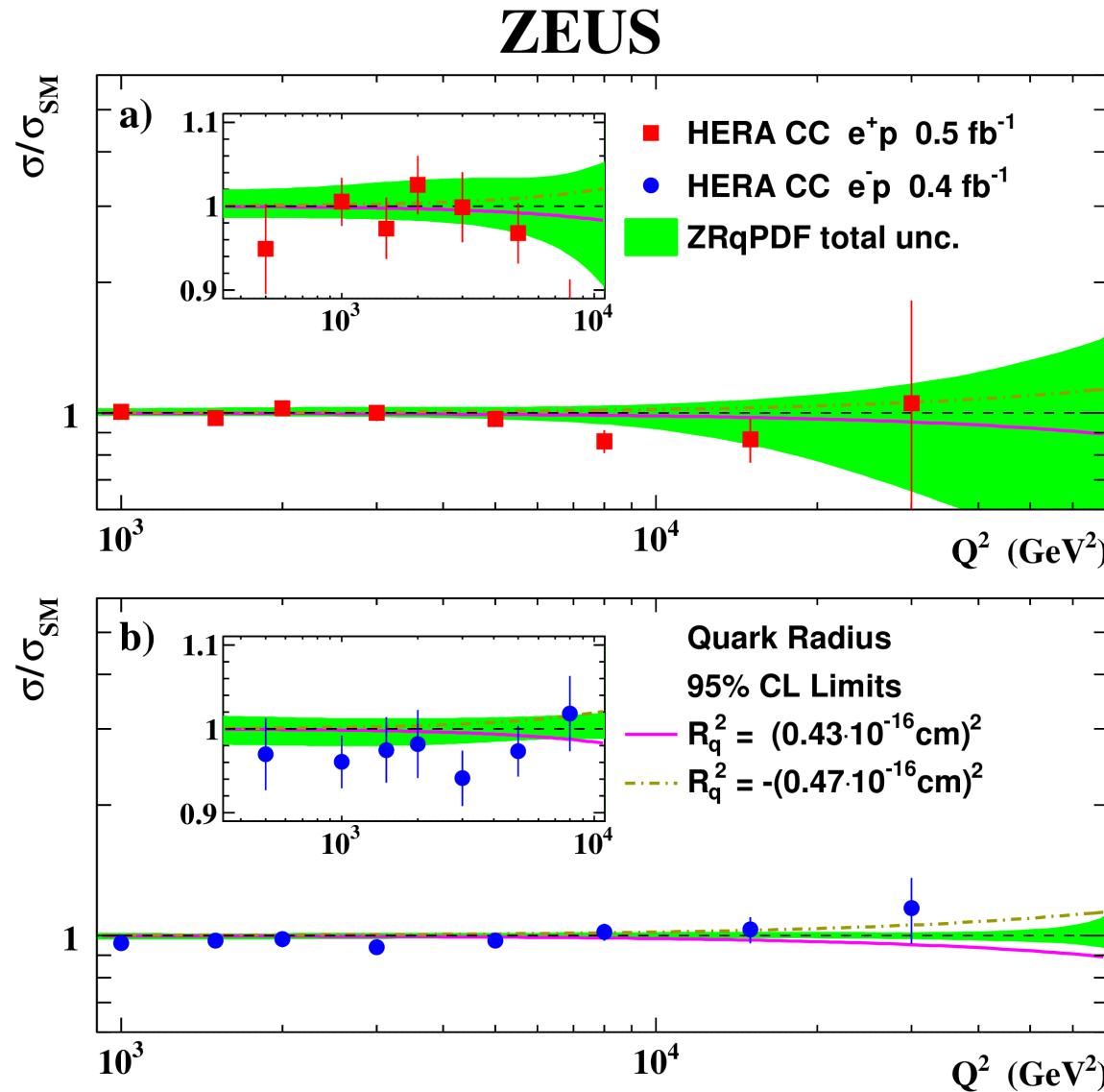
$$xW_3^- = x(U - \bar{D}) \quad xW_3^+ = x(D - \bar{U})$$

# BSM QCD analysis of combined DIS data

ZRqPDF set compared to HERAPDF2.0:



# Quark form factor and CC DIS data



Comparison of  $R_q^2$  exclusion limits to HERA CC ep DIS data.