



# Measurement of Multijet Production in $ep$ Collisions at High $Q^2$ and Determination of the Strong Coupling $\alpha_s$

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DESY

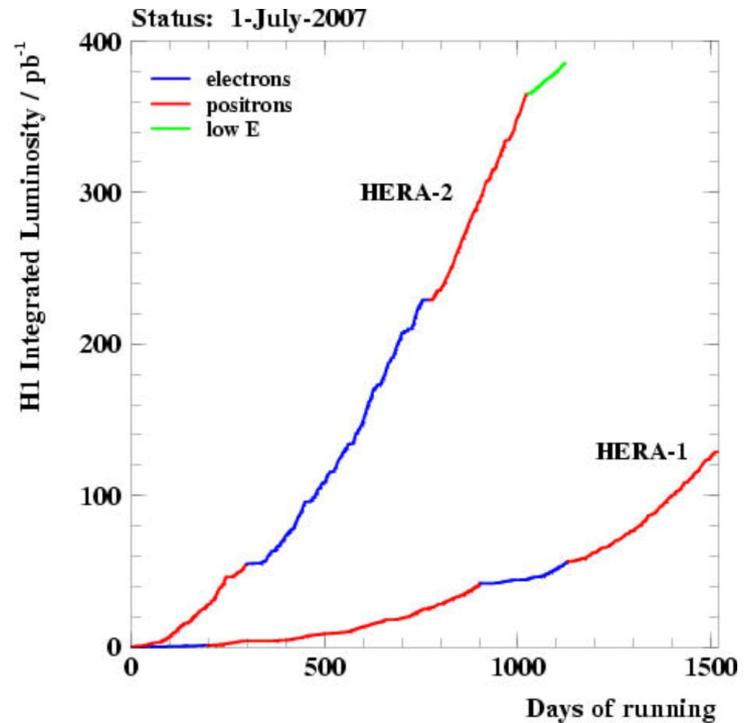
on behalf of the  collaboration

DIS 2015, Dallas, Texas, April 27 – May 1



# Introduction

HERA was the worlds only  $e^\pm p$  collider



$e^\pm(27.5 \text{ GeV}), p(460-920 \text{ GeV})$

centre of mass energy:

$$\sqrt{s} = 225-318 \text{ GeV}$$

Two collider experiments: **H1** and **ZEUS**

$\sim 0.5 \text{ fb}^{-1}$  of luminosity recorded by each experiment

Two running periods:

1994-2000: **HERA I data**

2003-2007: **HERA II data**

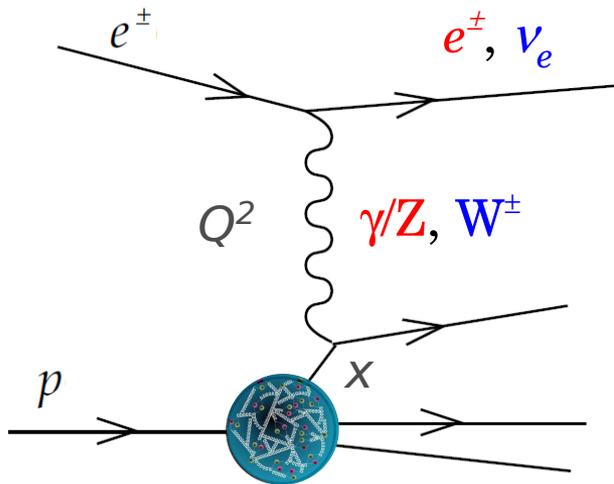
# Deep Inelastic Scattering (DIS)

## Deep Inelastic Scattering (DIS) at HERA

→ provides unique opportunity to study the structure of the proton

Neutral Current (NC):  $ep \rightarrow eX$

Charged Current (CC):  $ep \rightarrow \nu X$



### Kinematics:

$Q^2$  - virtuality of exchanged boson

$x$  - Bjorken scaling variable

$y$  - inelasticity

$Q^2 = sxy$  ( $\sqrt{s}$  centre-of-mass energy)

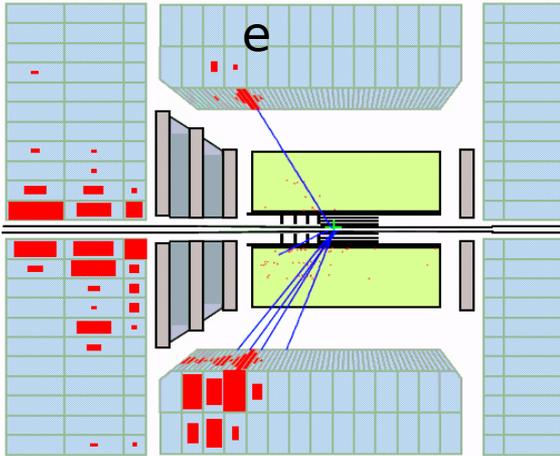
Cross section: a convolution of the PDFs and perturbatively calculable hard-scattering coefficients

$$\sigma = \hat{\sigma} \otimes \text{PDF}$$

# ep Scattering at HERA

DIS Neutral and Charged Current cross sections:

## Neutral Currents



$$\frac{d^2\sigma_{NC}^{e^\pm p}}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[ Y_+ \tilde{F}_2^\pm \mp Y_- x \tilde{F}_3^\pm - y^2 \tilde{F}_L^\pm \right]$$

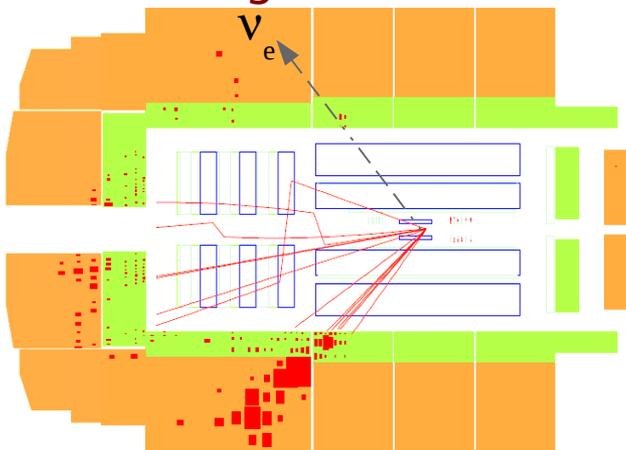
dominant contribution  $\uparrow$   
 important at high  $Q^2$   $\uparrow$   
 sizable at high  $y$   $\uparrow$

$$Y_\pm = 1 \pm (1-y)^2$$

LO:  $F_2 \approx x \sum e_q^2 (q + \bar{q})$  (in NLO ( $\alpha_s g$ ) appears)

$$xF_3 \approx x \sum 2e_q a_q (q - \bar{q})$$

## Charged Currents



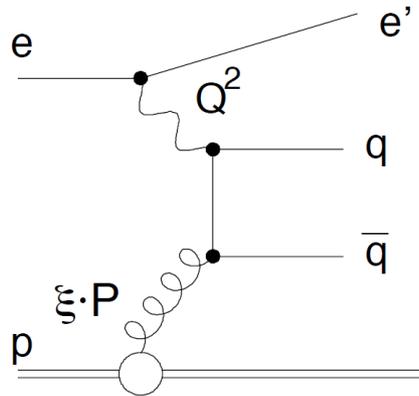
In LO  $e^+/e^-$  charged current cross sections are sensitive to different quark densities:

$$e^+ : \quad \tilde{\sigma}_{CC}^{e^+ p} = x[\bar{u} + \bar{c}] + (1-y)^2 x[d + s]$$

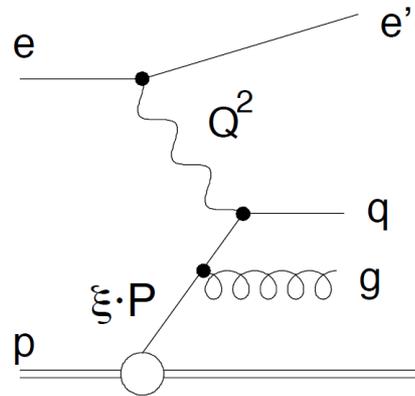
$$e^- : \quad \tilde{\sigma}_{CC}^{e^- p} = x[u + c] + (1-y)^2 x[\bar{d} + \bar{s}]$$

# Jet production in NC DIS

Jet production in leading order pQCD:

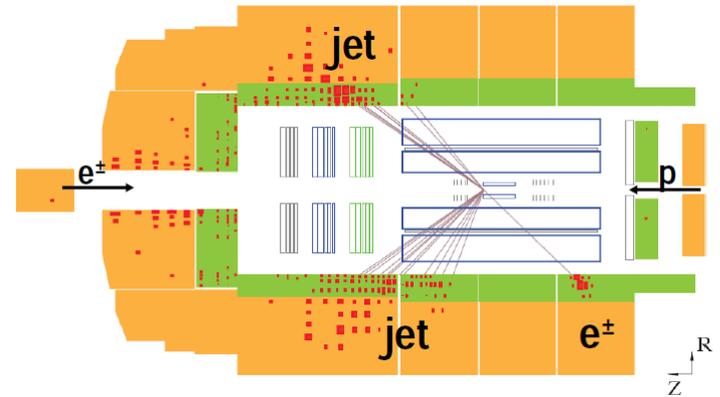


**boson-gluon fusion**



**QCD Compton scattering**

proton's longitudinal momentum fraction  $\xi = x(1 + M_{12}^2/Q^2)$

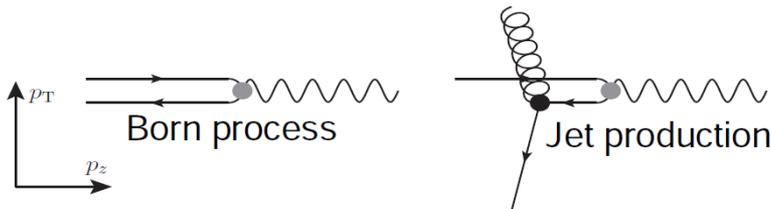


Jet reconstruction:

$k_t$  and anti- $k_t$  algorithms

H1 measurements performed in *Breit frame*

→ virtual boson collides head on with a parton from the proton



**Inclusive jets:**

measure transverse momentum  $P_T^{\text{jet}}$

**Dijet and trijets:**

average of two/three leading jets

$$\langle P_T \rangle_2 = \frac{1}{2} (P_T^{\text{jet1}} + P_T^{\text{jet2}})$$

# Multijet Production at High $Q^2$

Simultaneous measurement ( $351 \text{ pb}^{-1}$ ) of:

→ **inclusive jet, dijet and trijet cross sections**

and

→ **normalized inclusive jet, dijet and trijet cross sections**

normalization w.r.t. inclusive NC DIS (partial cancellation of experimental uncertainties)

	<b>Extended analysis phase space</b>	<b>Measurement phase space for jet cross sections</b>
NC DIS phase space	$100 < Q^2 < 40\,000 \text{ GeV}^2$ $0.08 < y < 0.7$	$150 < Q^2 < 15\,000 \text{ GeV}^2$ $0.2 < y < 0.7$
Jet polar angular range	$-1.5 < \eta_{\text{lab}}^{\text{jet}} < 2.75$	$-1.0 < \eta_{\text{lab}}^{\text{jet}} < 2.5$
Inclusive jets	$P_{\text{T}}^{\text{jet}} > 3 \text{ GeV}$	$7 < P_{\text{T}}^{\text{jet}} < 50 \text{ GeV}$
Dijets and trijets	$3 < P_{\text{T}}^{\text{jet}} < 50 \text{ GeV}$	$5 < P_{\text{T}}^{\text{jet}} < 50 \text{ GeV}$ $M_{12} > 16 \text{ GeV}$

*Note: the extended phase space is used to quantify migration effect in this way improving the precision of the measurement*

# Multijets at High $Q^2$ : Measurement Procedure

Jet cross sections obtained using a regularised unfolding procedure

## Multidimensional Regularised Unfolding:

4 double-differential measurements unfolded simultaneously

→ NC DIS, inclusive jet, dijet and trijet

## Using TUnfold tool

- statistical correlations considered
- enlarged phase space for migrations
- up to 7 observables are considered for migrations

## Migration Matrix

$\epsilon \rightarrow$	$\epsilon_E, \beta_1, \beta_2, \beta_3$	$\epsilon_1$	$\epsilon_2$	$\epsilon_3$
Detector level	Reconstructed Trijet events which are not generated as Trijet event <b>B<sub>3</sub></b>			Trijet $Q^2, <p_T>_3, y,$ Trijet-cuts <b>J<sub>3</sub></b>
	Reconstructed Dijet events which are not generated as Dijet event <b>B<sub>2</sub></b>		Dijet $Q^2, <p_T>_2, y,$ Dijet-cuts <b>J<sub>2</sub></b>	
	Reconstructed jets without match to generator level <b>B<sub>1</sub></b>	Incl. Jet $p_T^{\text{jet}}, Q^2, y, \eta$ <b>J<sub>1</sub></b>		
	NC DIS <b>E</b> $Q^2, y$			
	Hadron level			

# Multijets at High $Q^2$ : Uncertainties

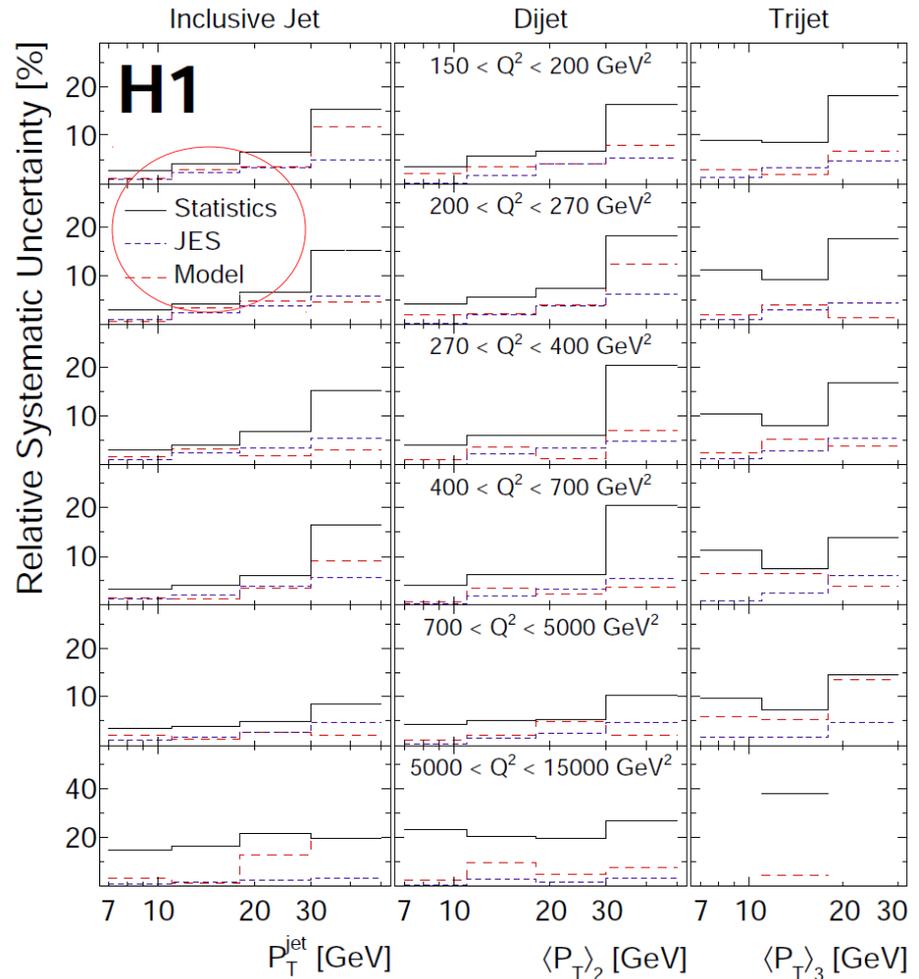
## Main experimental uncertainties of the measurement:

→ improved electron calibration and the energy flow algorithm

- Hadronic Final State (HFS):
  - jet energy scale and
  - energy of HFS
  - 1% (up to 4% for trijets)
- model uncertainty
  - taking into account differences in migration matrices between data and theory (Django, Rapgap)

$$\delta^{\text{Model}} = \pm \sqrt{\frac{1}{2} \left( \max(\delta_{d,R}^{\text{Model}}, \delta_{p,R}^{\text{Model}})^2 + \max(\delta_{d,D}^{\text{Model}}, \delta_{p,D}^{\text{Model}})^2 \right)}$$

- E of scattered electron (0.5 – 2%) and identification (0.5 – 2%)
- luminosity (2.5%)
- etc



# Multijets at High $Q^2$ : Cross Sections

Theory (NLO) calculations:

**NLOJet++** corrected for hadronisation and electroweak effects

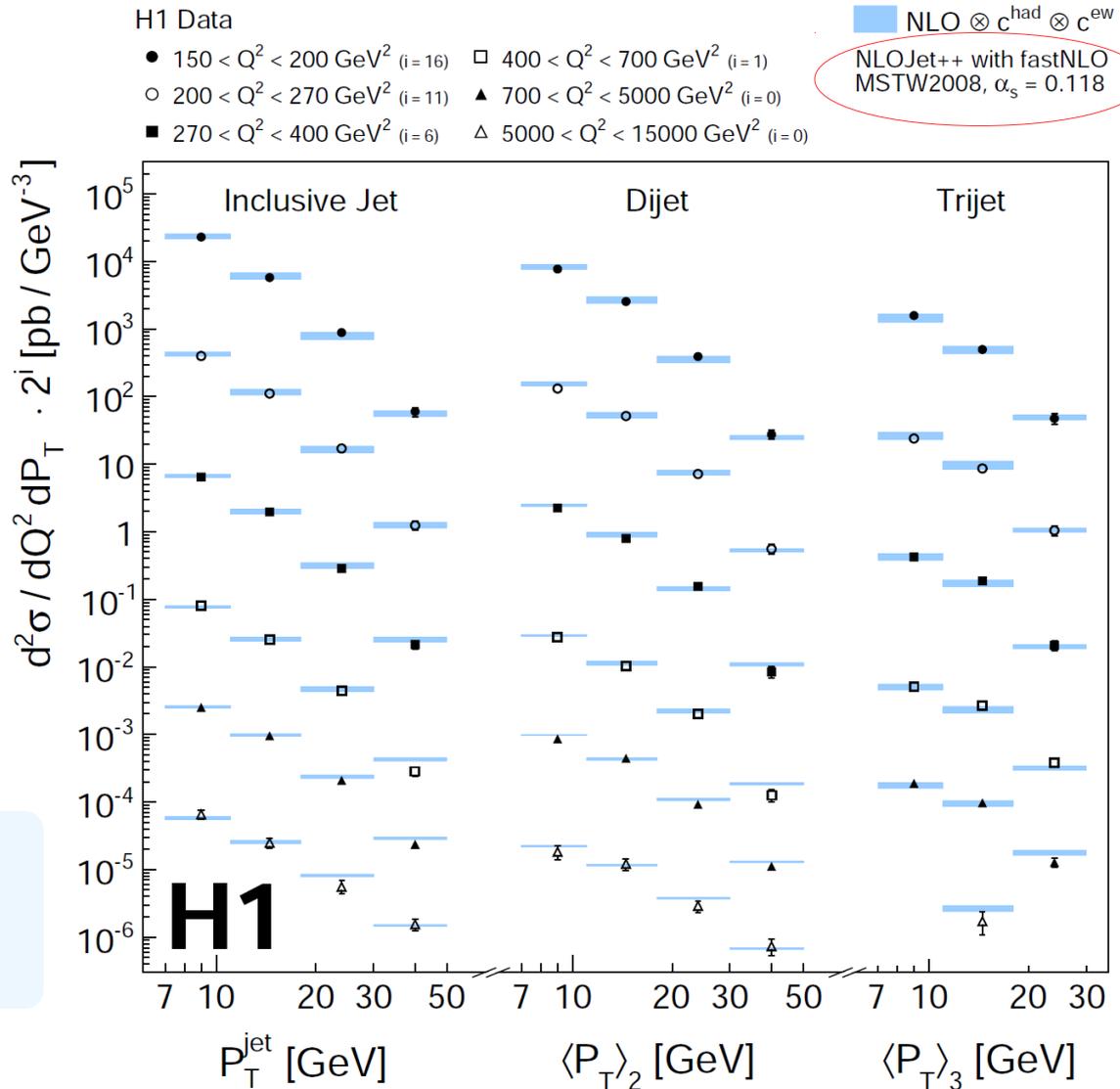
scale choice:

$$\mu_f = Q^2$$

$$\mu_r = (Q^2 + P_T)/2$$

Theory uncertainty obtained by varying scales by factor 2

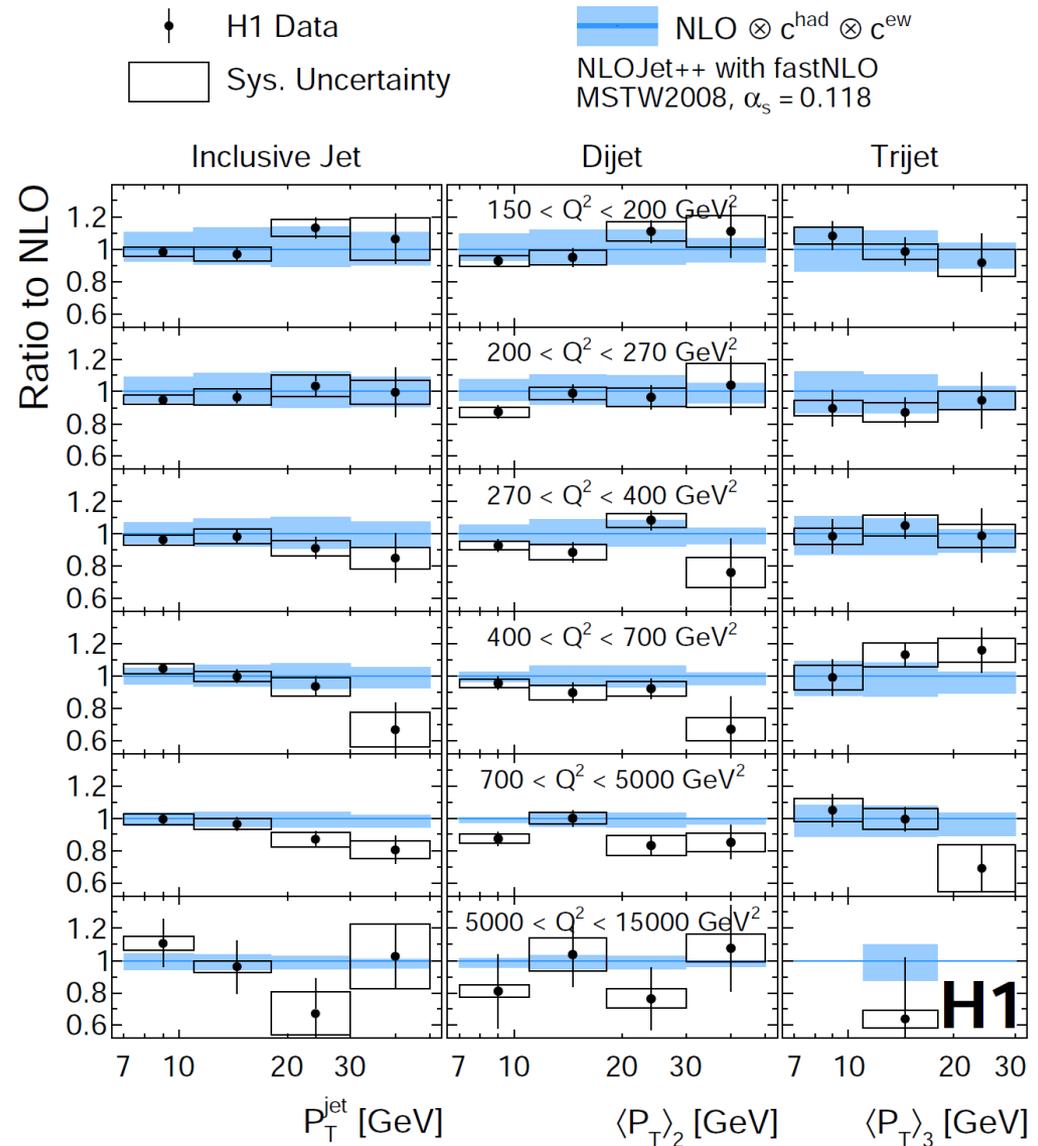
→ good description of the measured double-differential jet cross sections



# Multijets at High $Q^2$ : Cross Sections

Ratio of jet cross sections to NLO predictions as function of  $Q^2$  and  $P_T$

→ precision of the jet data is better than that of the theory calculations

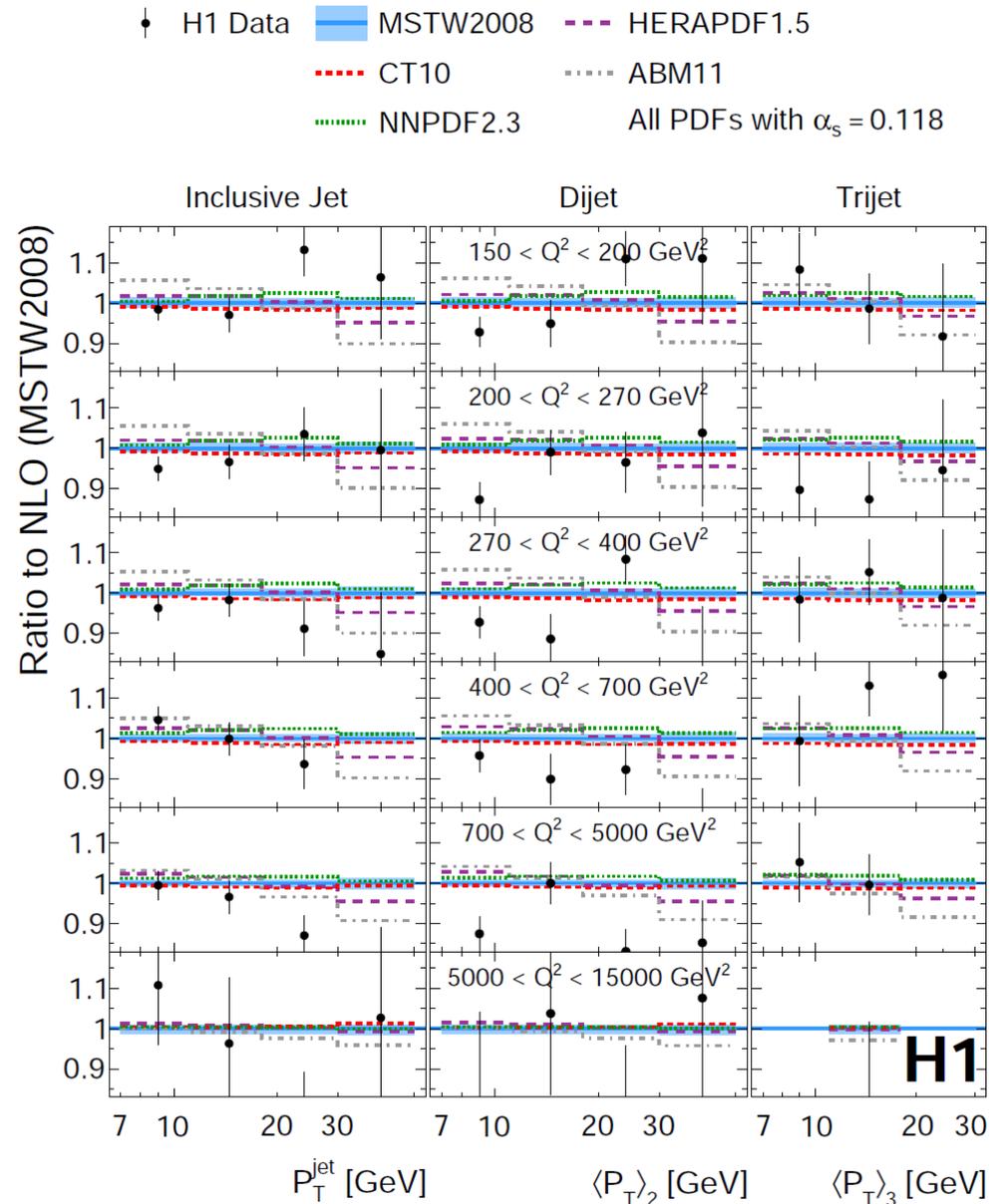


# Multijets at High $Q^2$ : Cross Sections

Ratio of NLO predictions with **various PDF** sets to MSTW2008 as function of  $Q^2$  and  $P_T$

→ small differences observed between predictions for different choices of PDF sets

(compared to the theory uncertainty from scale variations)

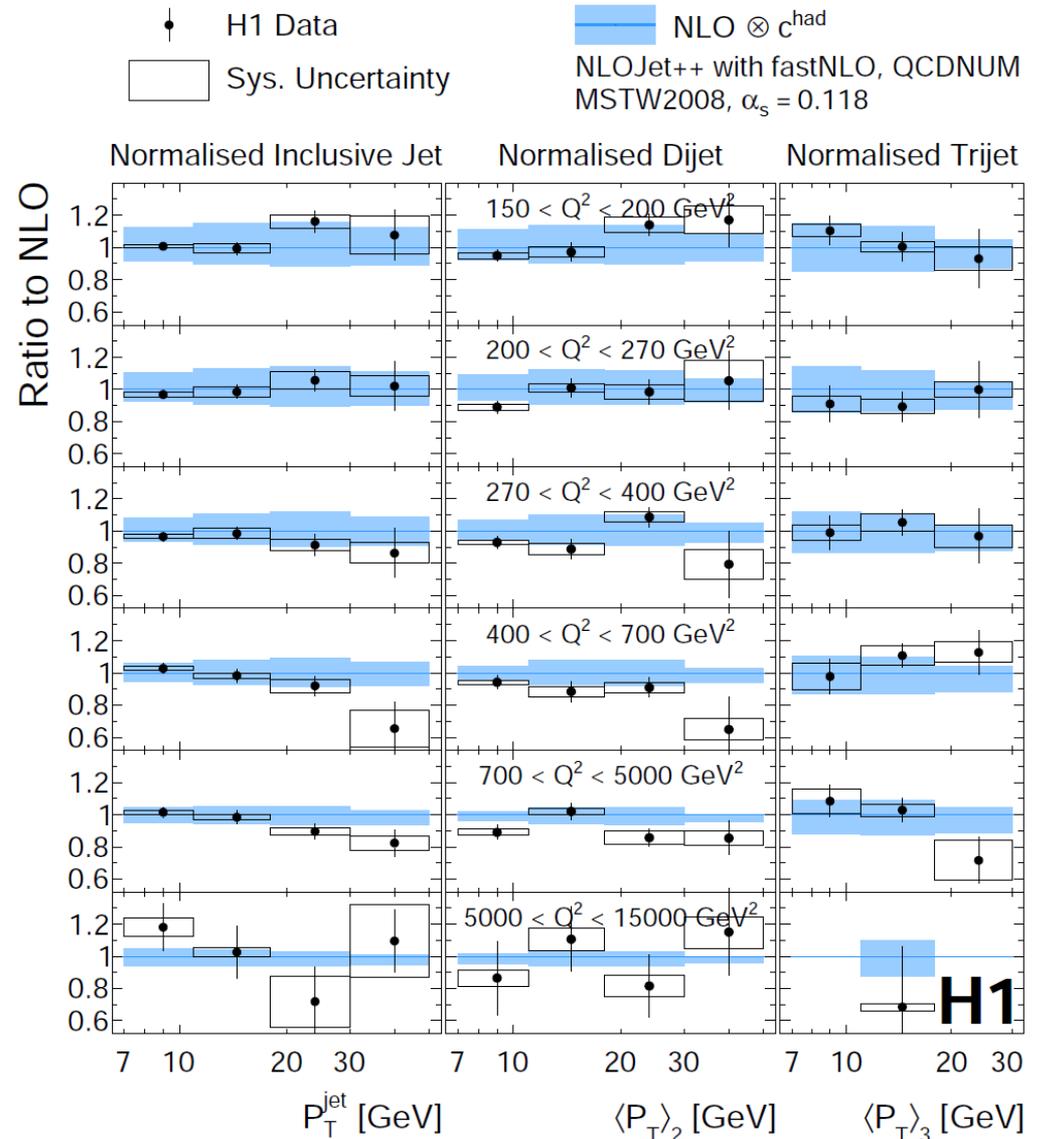


# Multijets at High $Q^2$ : Normalised Cross Sections

Ratio of normalised jet cross sections to NLO predictions as function of  $Q^2$  and  $P_T$

→ experimental systematic uncertainties are reduced

→ precision of the jet data is better than that of the theory calculations



# Extraction of Strong Coupling Constant $\alpha_s$

Iterative  $\chi^2$  minimisation procedure is used to extract  $\alpha_s$

→ fit theory (t) to data (m) taking statistical correlations into account:

$$\chi^2 = \vec{p}^T V^{-1} \vec{p} + \sum_k^{N_{\text{sys}}} \varepsilon_k^2 \quad \text{with} \quad p_i = \log m_i - \log t_i - \sum_k^{N_{\text{sys}}} E_{i,k}$$

$\alpha_s(M_Z)$  and  $\varepsilon$  are free parameters in the fit

Uncertainties  $\delta$  of  $m$  are considered as **log-normal** distributed with:

$$E_{i,k} = \sqrt{f_k^C} \left( \frac{\delta_{m,i}^{k,+} - \delta_{m,i}^{k,-}}{2} \varepsilon_k + \frac{\delta_{m,i}^{k,+} + \delta_{m,i}^{k,-}}{2} \varepsilon_k^2 \right)$$

nuisance parameters  $\varepsilon_k$  for each source of systematic uncertainty  $k$  are free parameters

→ **consistent treatment of all measurement uncertainties**

# Extraction of Strong Coupling Constant $\alpha_s$ : Results

Jet cross sections are directly sensitive to  $\alpha_s$

The best experimental precision on  $\alpha_s$  is obtained from a fit to normalised multijet cross sections:

$$\begin{aligned}\alpha_s(M_Z)|_{k_T} &= 0.1165 \text{ (8)}_{\text{exp}} \text{ (5)}_{\text{PDF}} \text{ (7)}_{\text{PDFset}} \text{ (3)}_{\text{PDF}(\alpha_s)} \text{ (8)}_{\text{had}} \text{ (36)}_{\mu_r} \\ &= 0.1165 \text{ (8)}_{\text{exp}} \text{ (38)}_{\text{pdf,theo}} .\end{aligned}$$

Experimental uncertainty significantly smaller than theoretical one

→ higher order calculations mandatory

→ value consistent with value extracted using anti- $k_t$  jets

The most precise value of  $\alpha_s(M_Z)$  from jet cross sections

→ can be used in PDF fit together with inclusive data

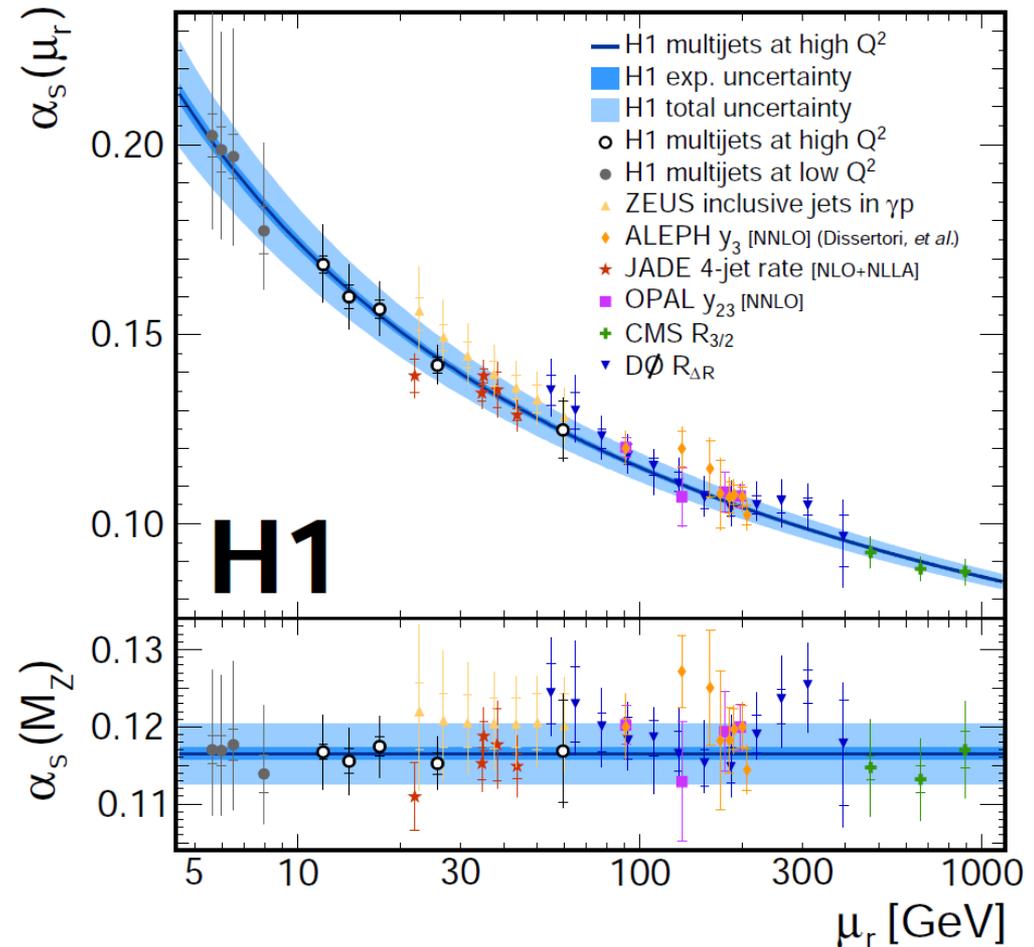
# Extraction of Strong Coupling Constant $\alpha_s$ : Results

Determination of  $\alpha_s$  at various scales (running)

- H1 multijet cross sections with superior precision
- consistency with other jet data
- agreement with the theory prediction over more than two orders of magnitude
- better than recent CMS results on inclusive jet measurements

[arXiv:1410.6765](https://arxiv.org/abs/1410.6765)

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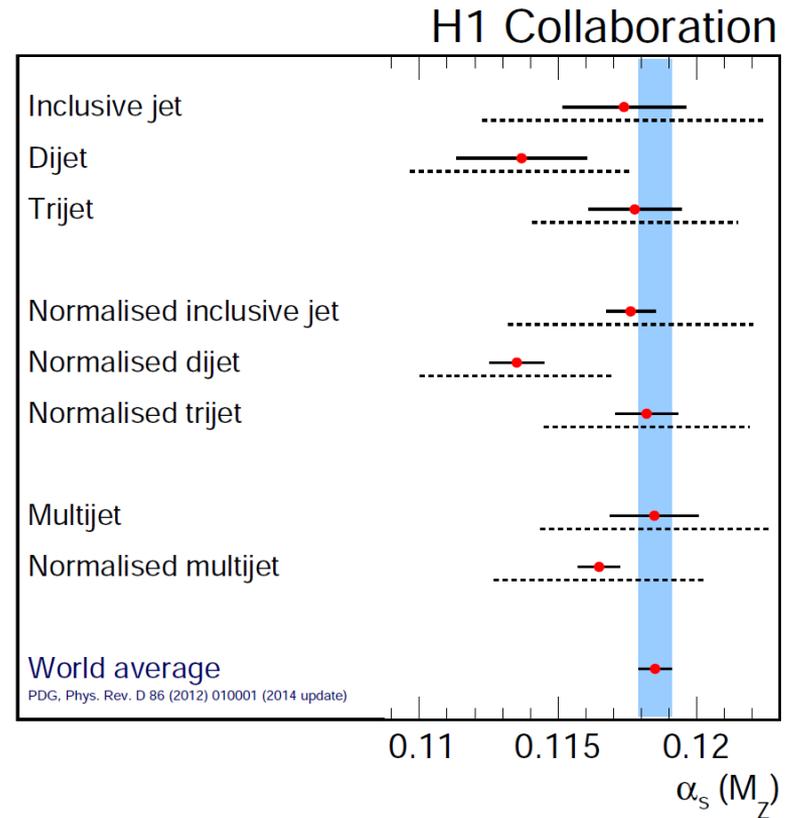
# Extraction of Strong Coupling Constant $\alpha_s$ : Results

Comparison of  $\alpha_s$  values extracted from different jet measurements

(separately and simultaneously)

→ compared to the world average value of  $\alpha_s(M_Z)$

→ values consistent within total uncertainties



→ value of  $\alpha_s(M_Z)$  from dijet cross sections is smaller than from inclusive jet or trijets

*(most likely attributed to higher order contributions in phase space regions which are different in the dijet and the inclusive jet measurement)*

# Summary

New QCD results from H1 were presented

## Multijet (inclusive, dijet and trijet) cross sections in DIS

→ final results with superior experimental precision  
(supersede previously published H1 measurements)

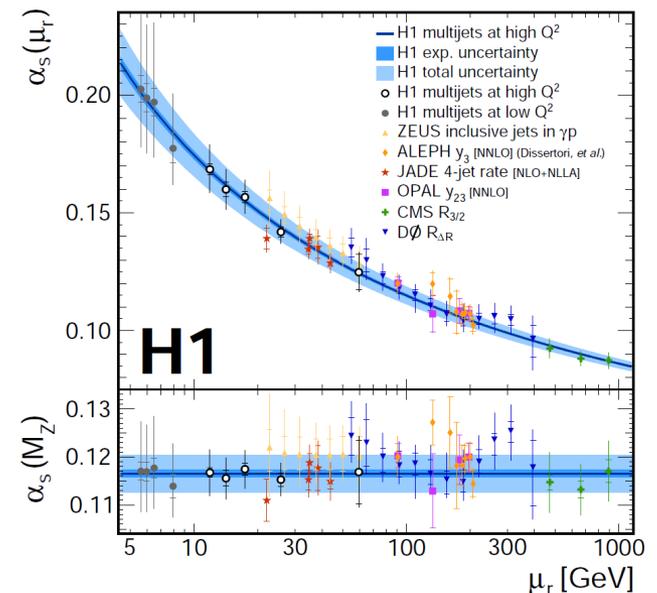
used to **determine the strong coupling constant  $\alpha_s$**

→ obtained value is consistent with the world average

→ most precise value from jet cross sections!

THANK YOU

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H1

# Back-up slides