

Precision QCD (jets and α_s) measurements at HERA

Jacek Turnau IFJ PAN

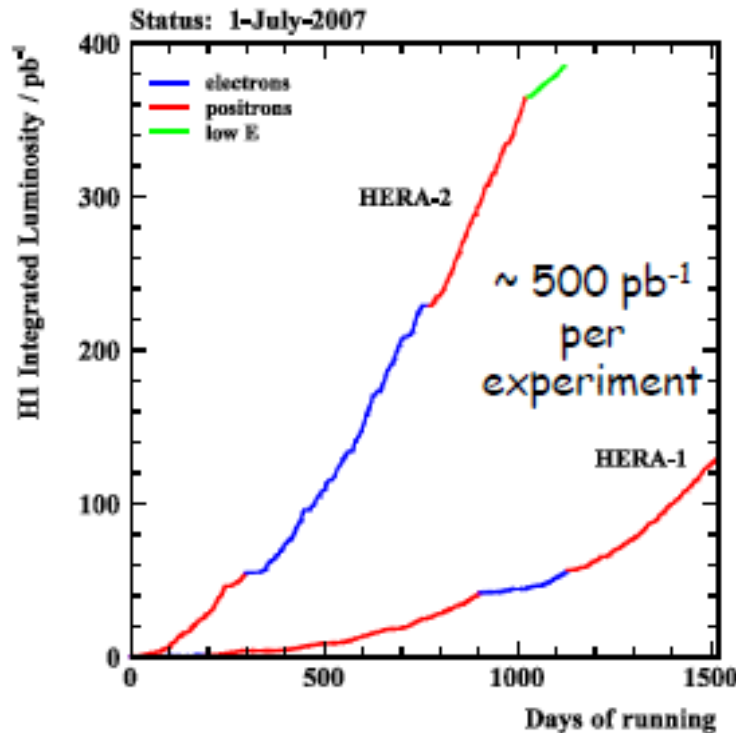
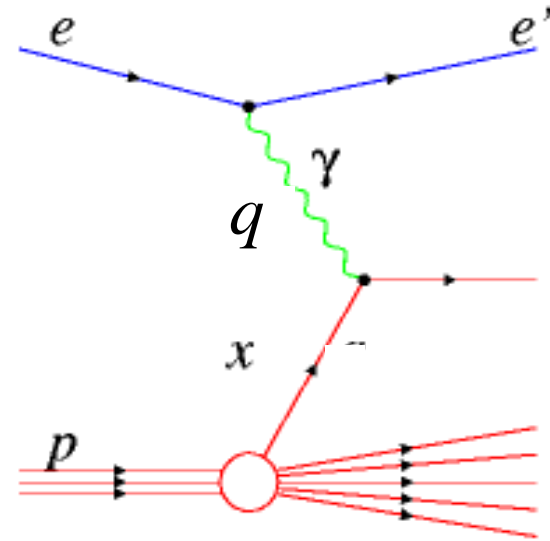
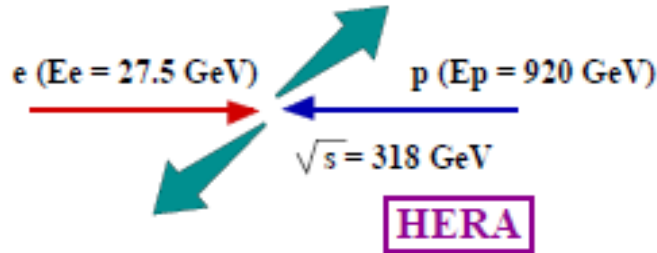


On behalf of H1 and ZEUS Collaborations



- Jet measurements at HERA
- Multijet measurement in DIS – unfolding
- Jet measurement in photoproduction
- Extraction of α_s : H1 and ZEUS methods
- Comparison of the extracted values of α_s
- Summary

ep – scattering at HERA



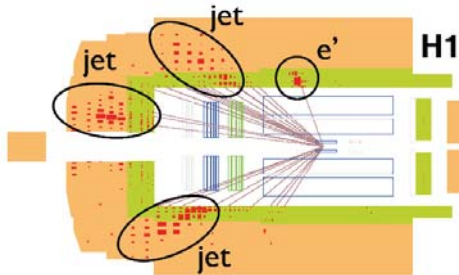
$Q^2 = -q^2$ exchanged boson virtuality
 x Bjorken scaling variable

Two kinematic regimes:

- $Q^2 \approx 0 \text{ GeV}^2$: Photoproduction
- $Q^2 > 1 \text{ GeV}^2$: DIS

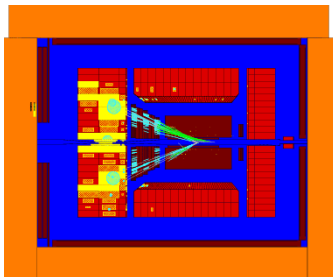
Precision jet measurements at HERA

□ Data sets 300 – 500 pb⁻¹ → High statistics → small statistical uncertainties even at high Q² and high jet transverse momentum



H1 DIS multijets:
≈ 104000 events

$150 < Q^2 < 15000 \text{ GeV}^2$
 $0.2 < y < 0.7$
 $-1 < \eta_{\text{lab}} < 2.5$
 $5(7) < p_T < 50 \text{ GeV}$



ZEUS photoproduction
≈ 450000 events

• $Q^2 < 1 \text{ GeV}^2$
• $0.2 < y_{\text{JB}} < 0.85$
• $E_T > 17 \text{ GeV}$
• $-1 < \eta^{\text{jet}} < 2.5$

□ Excellent control of systematic uncertainties

- Electron measurement : 0.5 – 1% scale uncertainty
- **Jet energy scale : 1% !** (effect on jet cross section 3-10 %)

Jets: key to precise determination of α_s

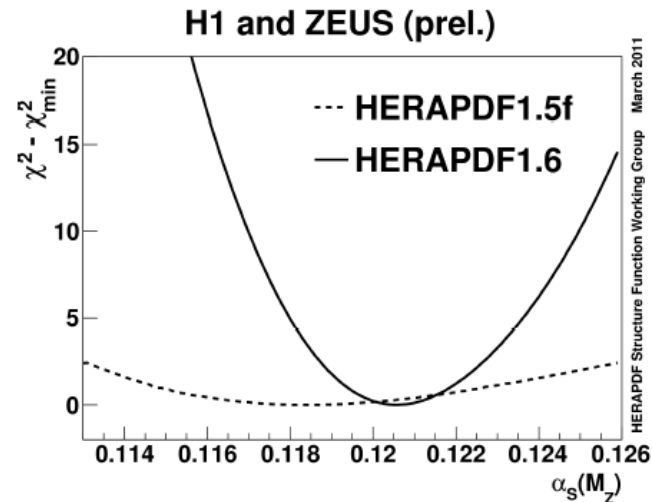
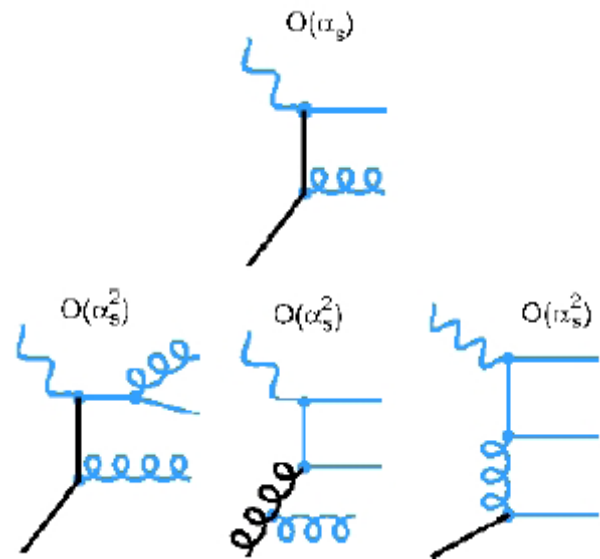
Breit frame inclusive jet cross section proportional to α_s in LO. Its inclusion to global QCD fit (HERAPDF1.5 \rightarrow 1.6) increases immensely sensitivity to $\alpha_s(M_Z)$

BGF: strong correlation α_s – gluon density



Due to high statistics of events with $Q^2 > 1000$ GeV and increased sensitivity to QCDC (valence quark distributions) gluon – α_s correlation diminished

Trijets: α_s^2 term in LO diminishes experimental uncertainty in extraction of $\alpha_s(M_Z)$



Multijet measurements - unfolding

- ❑ Detector resolution introduces migrations between jet samples
- ❑ Correlations between samples ex definitione: inclusive dijet (trijet) is a subsample of inclusive jet (dijet)...

m - measured distribution at the detector level

x - true particle level

A – detector response 

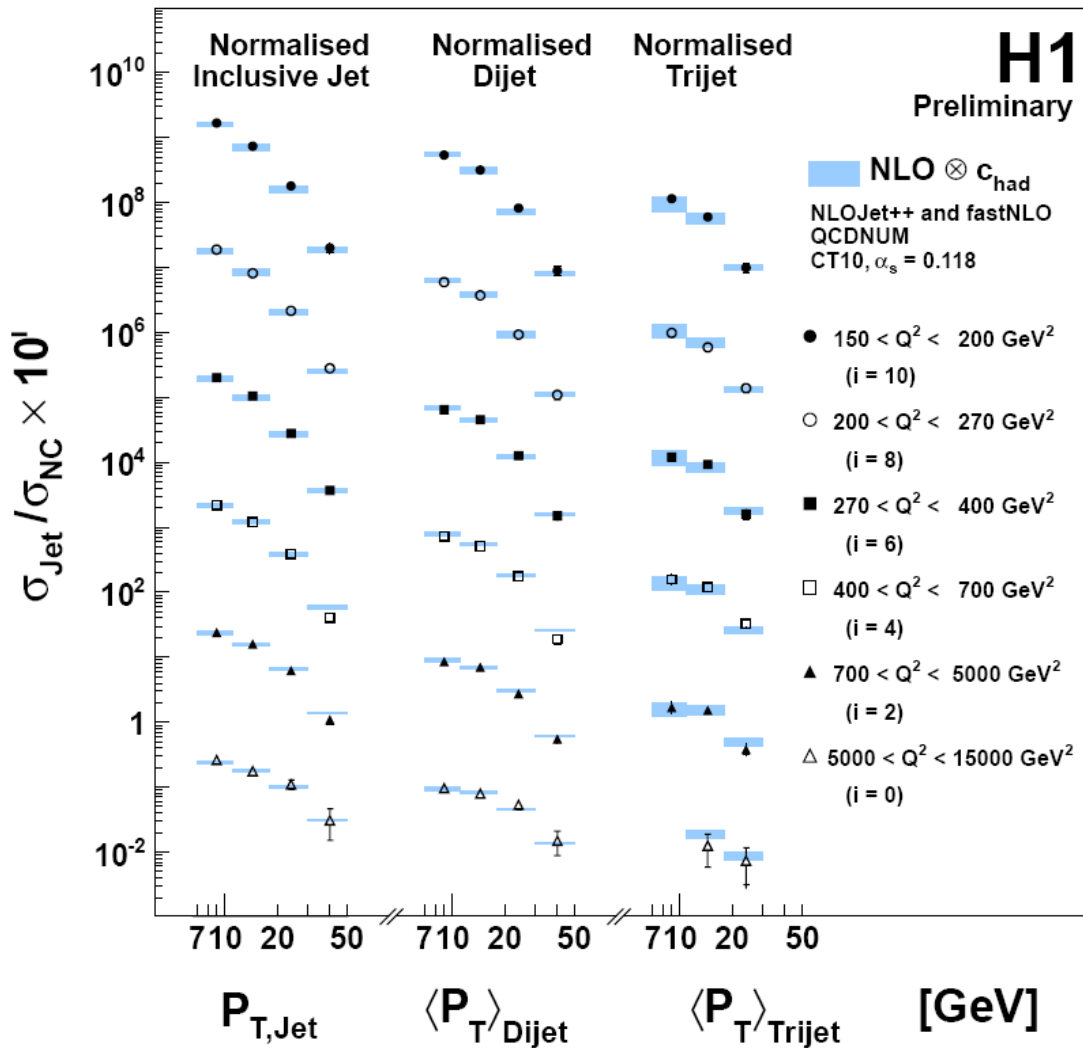
Unfolding solves equation $\mathbf{m} = \mathbf{A} \cdot \mathbf{x}$

Method: TUnfold, regularized unfolding Root application (S. Schmitt, arXiv:1205.6201)

			Trijet $Q^2, \langle p_T \rangle_3, y,$ Trijet-cuts	ϵ_{J3}
			Dijet $Q^2, \langle p_T \rangle_2, y,$ Dijet-cuts	ϵ_{J2}
		Incl. Jet $p_T, Q^2, y, (\eta)$		ϵ_J
DIS- Events (Q^2, y)	Reconstructed jets without match to generator level	Reconstructed Dijet events which are not generated as Dijet event	Reconstructed Trijet events which are not generated as Trijet event	ϵ_E $-\beta_1$ $-\beta_2$ $-\beta_3$
	Detector level			

600 X 2200 bins

Normalized multijet cross sections



H1-Prel-12-031

NLO Calculation:

PDF: CT10, $\alpha_s = 0.118$

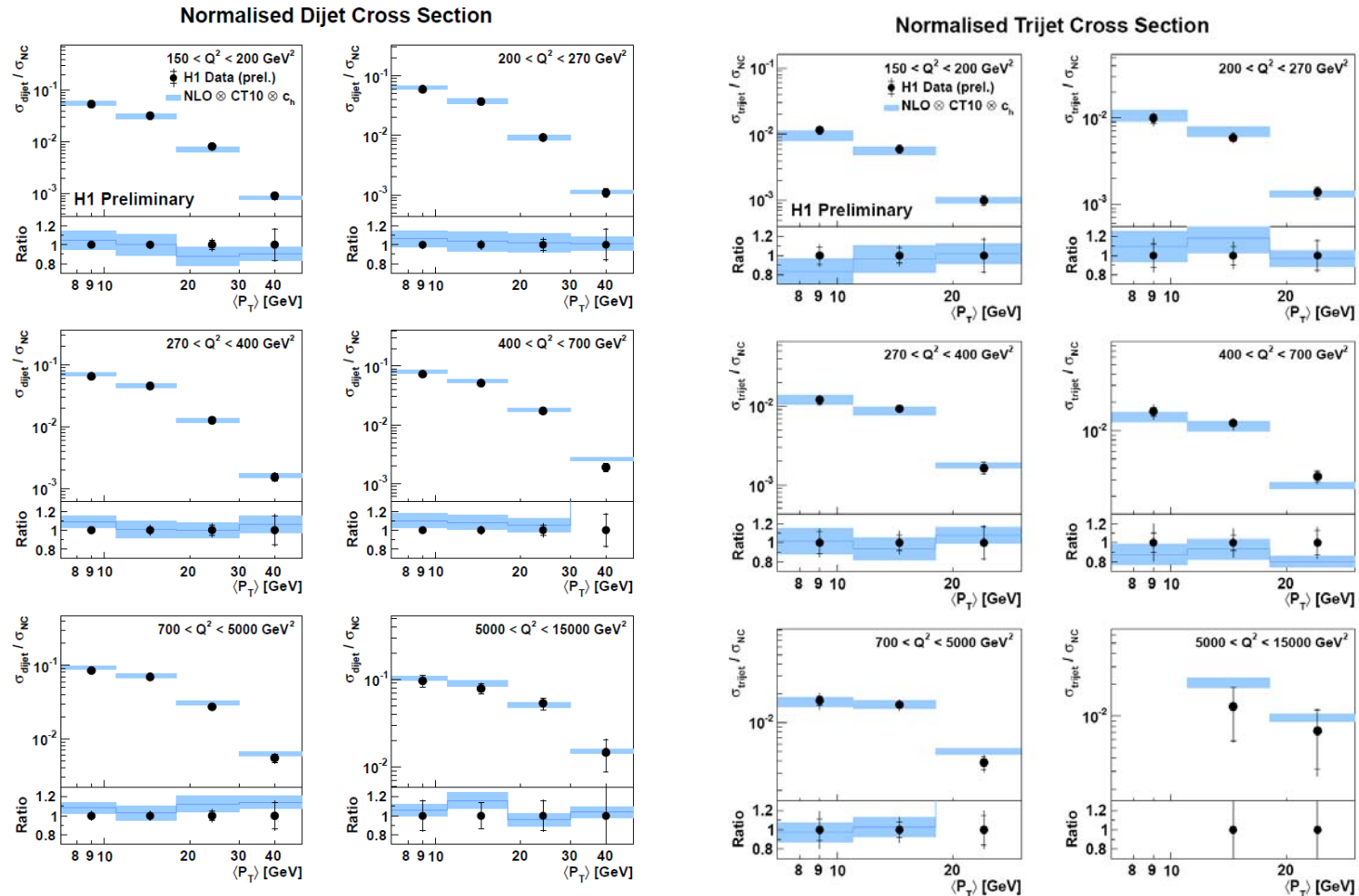
NLOJet++

FastNLO QCDNUM

Corrected for hadronisation

- **Trijets for the first time**
- **Small experimental errors**
- **Very good NLO and LO (trijets) description of the data**

Normalized dijet and trijet cross sections



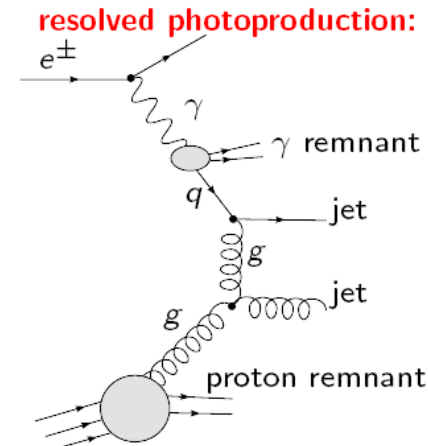
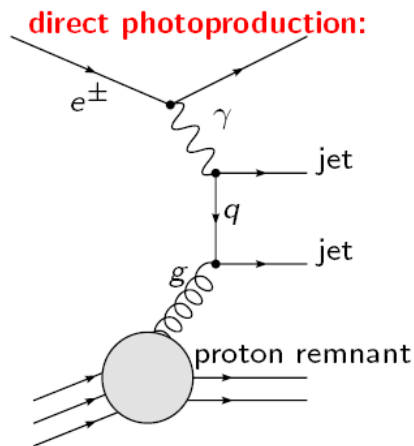
Except for highest Q^2 bins experimental uncertainty much smaller than theoretical

Jets in photoproduction ($Q^2 \approx 0$)

- Large cross section \rightarrow large statistics of jets with very high transverse momentum
- Single hard scale : jet p_T

Excellent for extraction of α_s

But...



Multiple parton interactions and significant spread between photon structure functions (γPDF) - possible source of ambiguities

Inclusive jet measurement in photoproduction

DESY-12-045 (March 2012) [Nucl. Phys. B864 \(2012\), pp. 1-37](#)

Phase space

- $Q^2 < 1 \text{ GeV}^2$
- $0.2 < y_{JB} < 0.85$
- $E_T > 17 \text{ GeV}$
- $-1 < \eta^{\text{jet}} < 2.5$

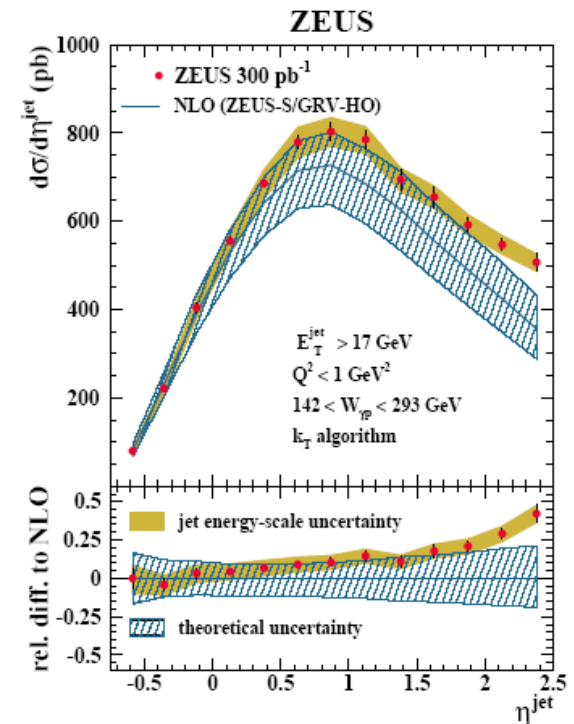
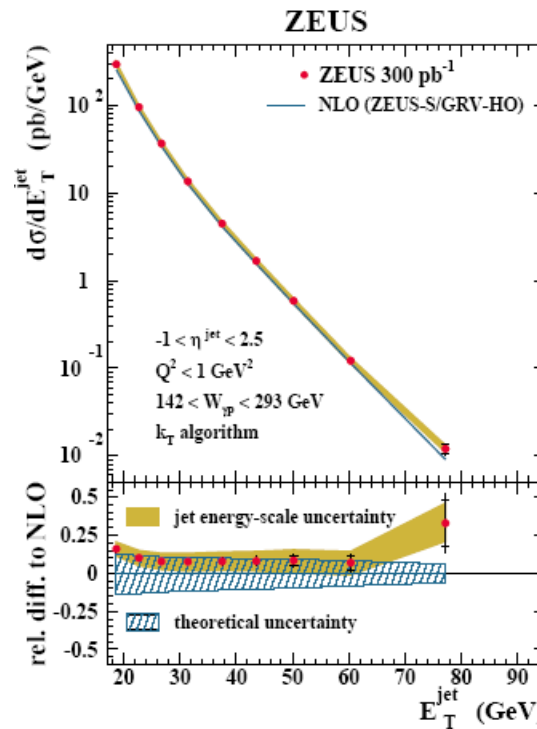
NLO QCD

Klasen, Kleinwort, Kramer

pPDF: ZEUS-S

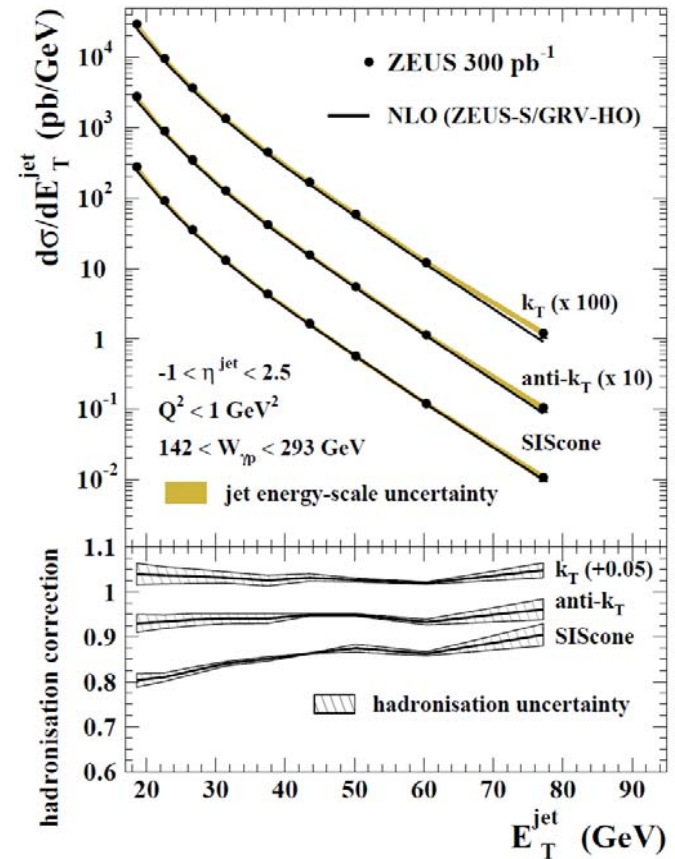
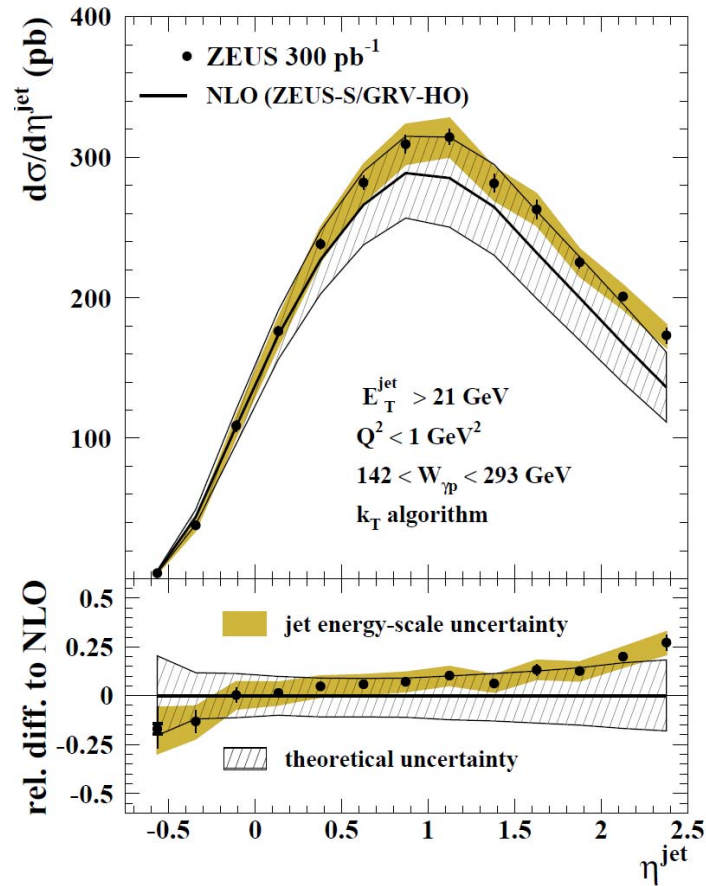
γ PDF: GRV-HO

$\mu_r = \mu_f = E_T^{\text{jet}}$



- experimental uncertainty smaller than theoretical
- good description by NLO calculation except for $\eta^{\text{jet}} > 2.0$
- MI and/or γ PDF possible source of discrepancies

Inclusive jet measurement in photoproduction



- Good description in the whole η^{jet} range after raising threshold to $E_T > 21 \text{ GeV}$
- Stringent test of jet algorithms

Determination of $\alpha_s(M_Z)$

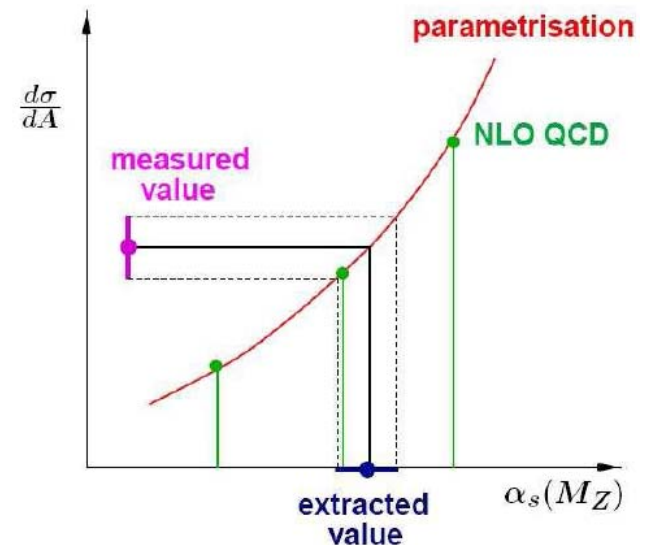
H1: Hessian method: Minimise $\chi^2(\alpha_s)$

$$\chi^2 = \sum_{i=1}^N \frac{[d_i - t_i(1 - \sum_k \epsilon_k \Delta_{ik})]^2}{\sigma_{i,\text{stat}}^2 + \sigma_{i,\text{uncorr}}^2} + \sum_k \epsilon_k^2$$

- Keep PDF (CT10) fixed and fit α_s
- Theoretical uncertainty obtained by offset method : repeat fit with μ_r and μ_f varied by factor $\frac{1}{2}$ and 2

ZEUS:

- Parametrise theory using NLO calculations with PDF sets obtained for different α_s .
- Measured value and its uncertainty is projected on the parametrization
- Theory uncertainty by band method (more sophisticated version of offset method \rightarrow 30-50% smaller uncertainty)
- ZEUS method unlike H1 takes into account α_s – PDF (gluon) correlation



Extracted $\alpha_s(M_Z)$

$$\sigma^{\text{jet}} \rightarrow \sigma^{\text{parton}} \rightarrow \alpha_s(M_Z)$$

Normalized multijets (k-factor < 1.3)

$\alpha_s = 0.1163 \pm 0.0011$ (exp)	Measurement of jet cross section	} theory
± 0.0014 (PDF)	Dependence on proton PDF	
± 0.0008 (had)	Hadron \rightarrow parton level	
± 0.0045 (scale)	μ_r and μ_f dependence	

Theory uncertainty dominated by scale and \gg experimental uncertainty

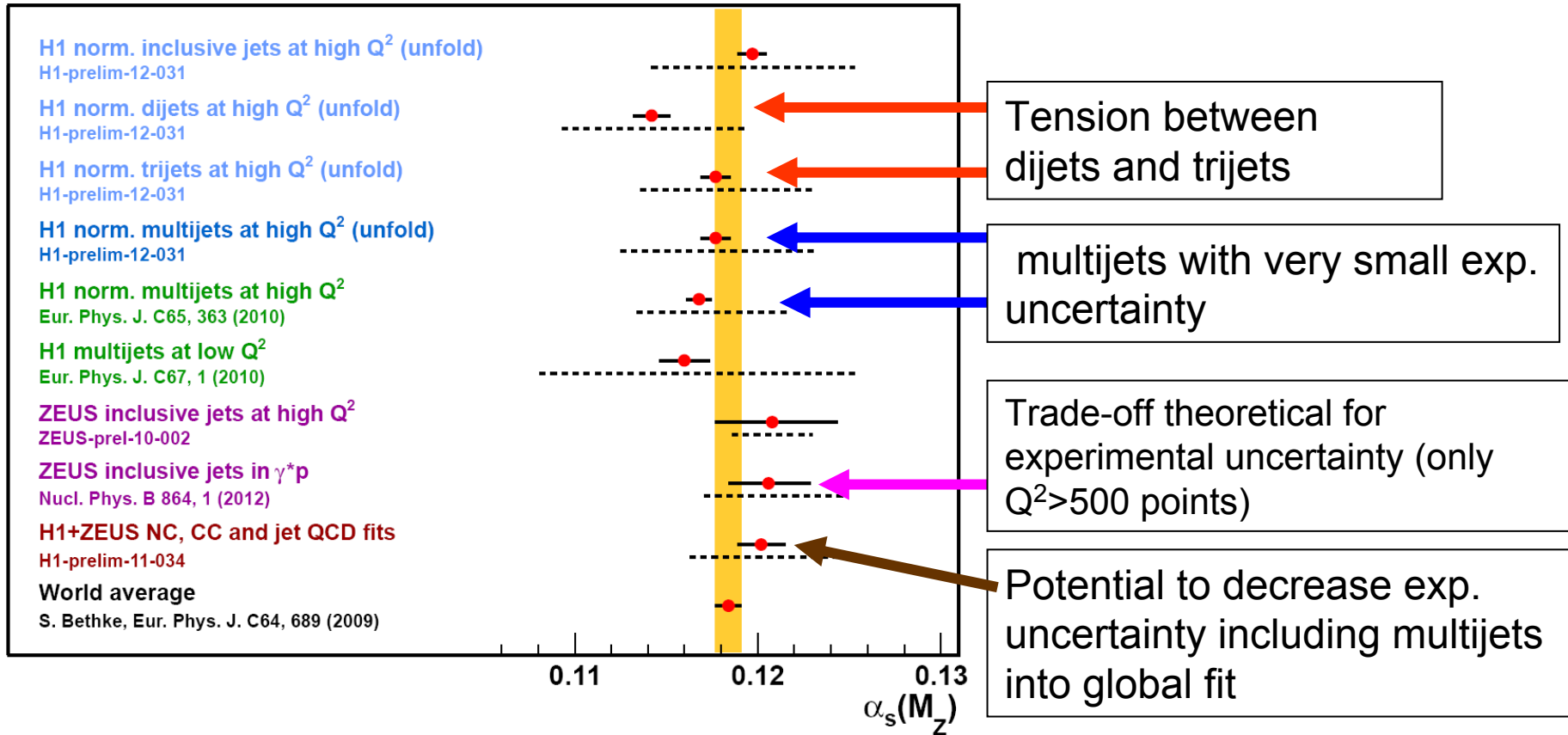
Photoproduction inclusive jets $E_T > 21$ GeV

$$\alpha_s = 0.1206 \pm 0.002 \text{ (exp)}$$
$$\pm 0.004 \text{ (theory)}$$

γ PDF and scale contribute equally to theory uncertainty

Comparison of extracted $\alpha_s(M_Z)$ values

Uncertainties: exp. ——— theo. - - - - -



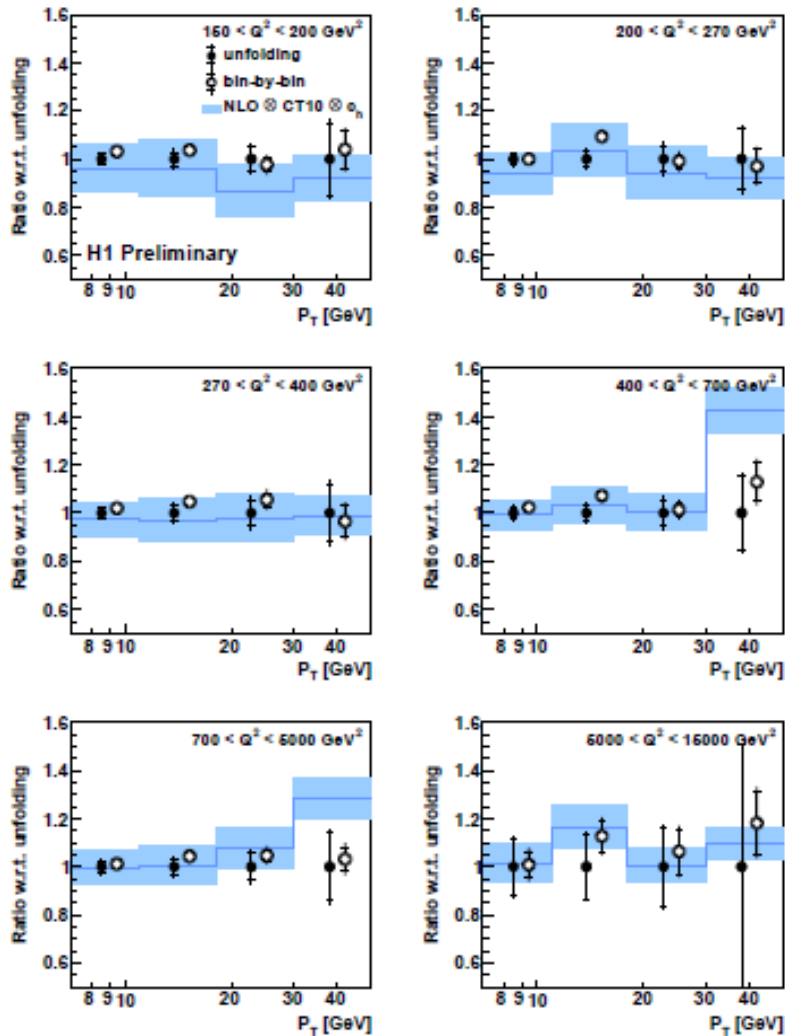
Experimental uncertainty much smaller than theoretical, dominated by missing NNLO
 All results compatible with world average within uncertainties

Summary

- ❑ Recent precision jet measurements at high Q^2 (H1) and in photoproduction (ZEUS)
- ❑ Inclusive jet, dijet and trijet measurements at high Q^2 using multidimensional unfolding, very small experimental uncertainties, good description of the data by NLO (jet, dijet) and LO (trijet) calculation
- ❑ Inclusive jet measurement in photoproduction, good description of the data by NLO calculation for $E_T > 21$ GeV
- ❑ **In general, the data are more precise than QCD predictions**
- ❑ **Extracted values of α_s are consistent with world average and their experimental uncertainties are much smaller than theoretical**
- ❑ In the inclusive multijet measurement, theoretical α_s uncertainty is dominated by missing NNLO terms of the perturbative expansion
- ❑ In the inclusive photoproduction jet measurement terms beyond NLO and γPDF contribute similarly to theoretical α_s uncertainty

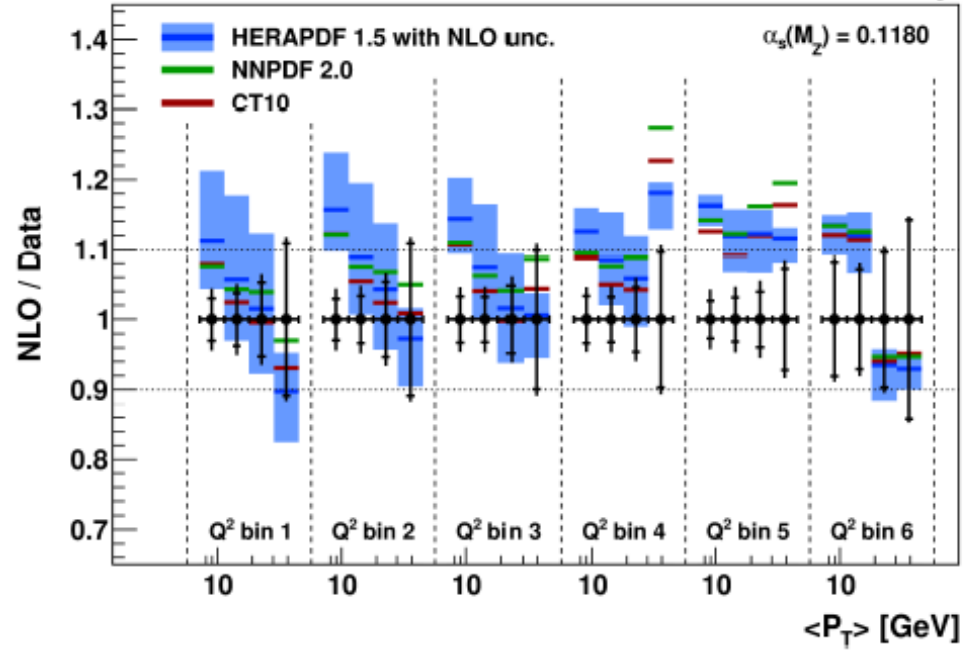
Backup slides

Normalised Inclusive Jet Cross Section

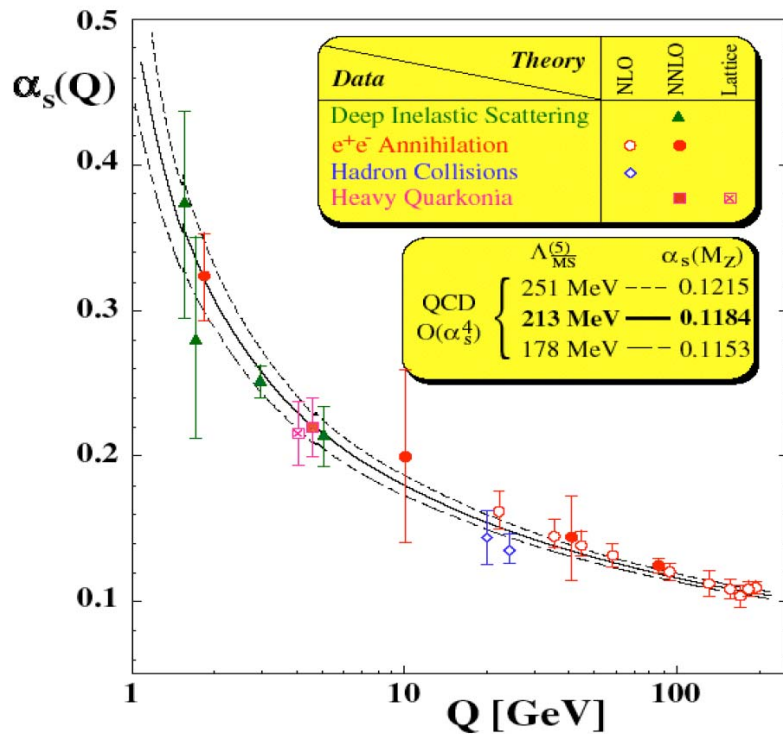


4 – 6%
Dijet

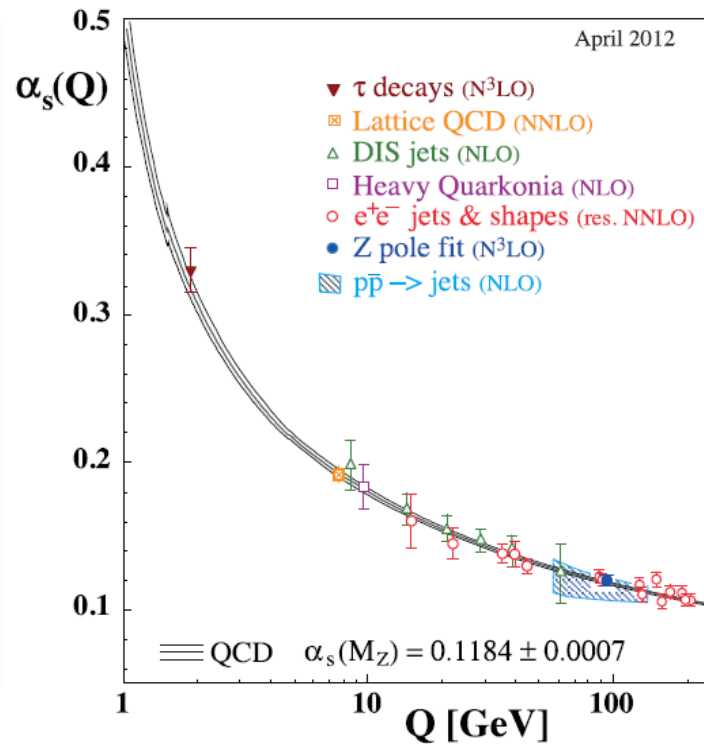
H1 Preliminary



$\alpha_s(M_Z)$ – fundamental constant



Copied from slide of prof. Frank Wilczek Nobel Lecture **2004**

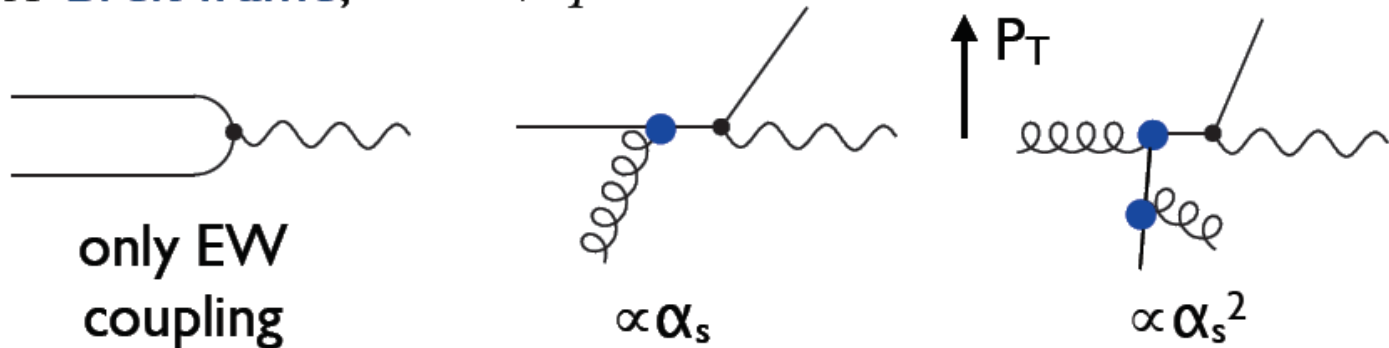


Running α_s compilation from **2012 PDG QCD review**

$\alpha_s(M_Z)$ is a fundamental constant of the nature, it is not possible to exaggerate in efforts to increase the accuracy of the measurements

Jet production in DIS

Boost to Breit frame, $2xP + q = 0$



- In Breit frame only hard QCD processes generate considerable p_T
- Inclusive jets, dijets, trijets...: at least one, two three.. jet above certain threshold in p_T
- n-jet production in LO proportional to α_s^{n-1}