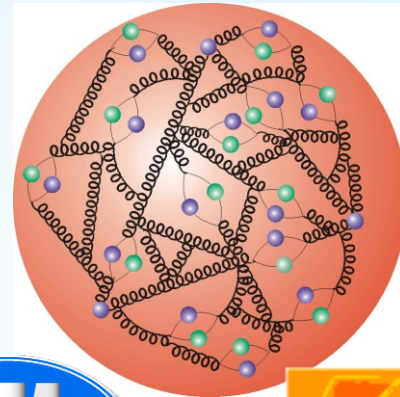
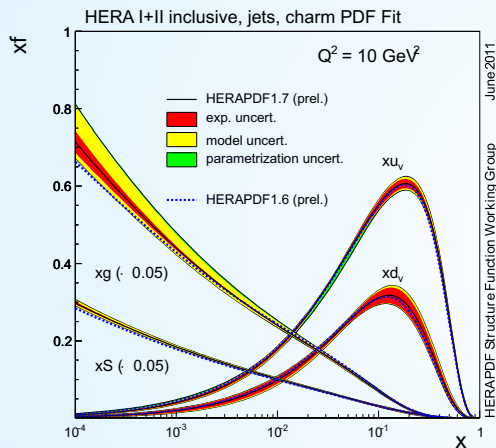


Precision Measurements of the Proton Structure

Functions at HERA



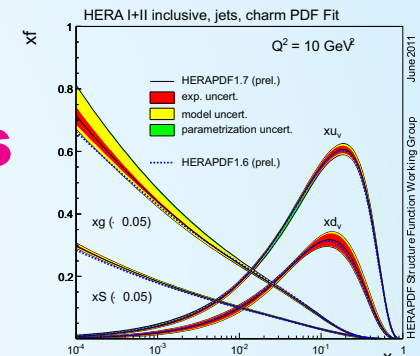
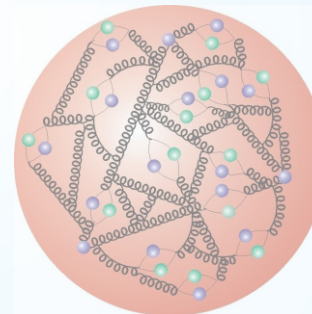
Bonn 26.3.2012

I.Abt, MPI München



Content

- **Protonic Facts**
- **Cross Sections and Structure Functions**
 - **Measurements**
 - **Parton Distribution Functions**
- **Predictions**
 - **charm and glue**
- **Proton Structure ?**
 - **Photon Structure ?**
- **Proton Size and Shape**
- **Summary & Outlook**



Before I start

Multiple Apologies

I really know very little about the proton:

- **mass = 1 GeV = $1.67 \cdot 10^{-27}$ kg**
- **3 valence quarks**
- **charge = +1**
- **spin = $1/2 \rightarrow$ Spin**
- **radius \approx 1 fm; shape?**
- **lifetime » age of the universe**
- **afflicted by QCD**

I have no real
explanation for
any of this!



And I am sorry, if I should disturb you doing
your Email or reading your favorite newspaper.



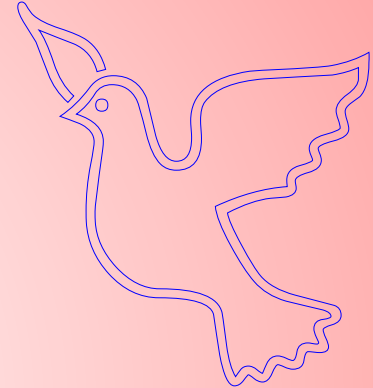
DISCLAIMER

**I will not try to be complete
on any subject.**

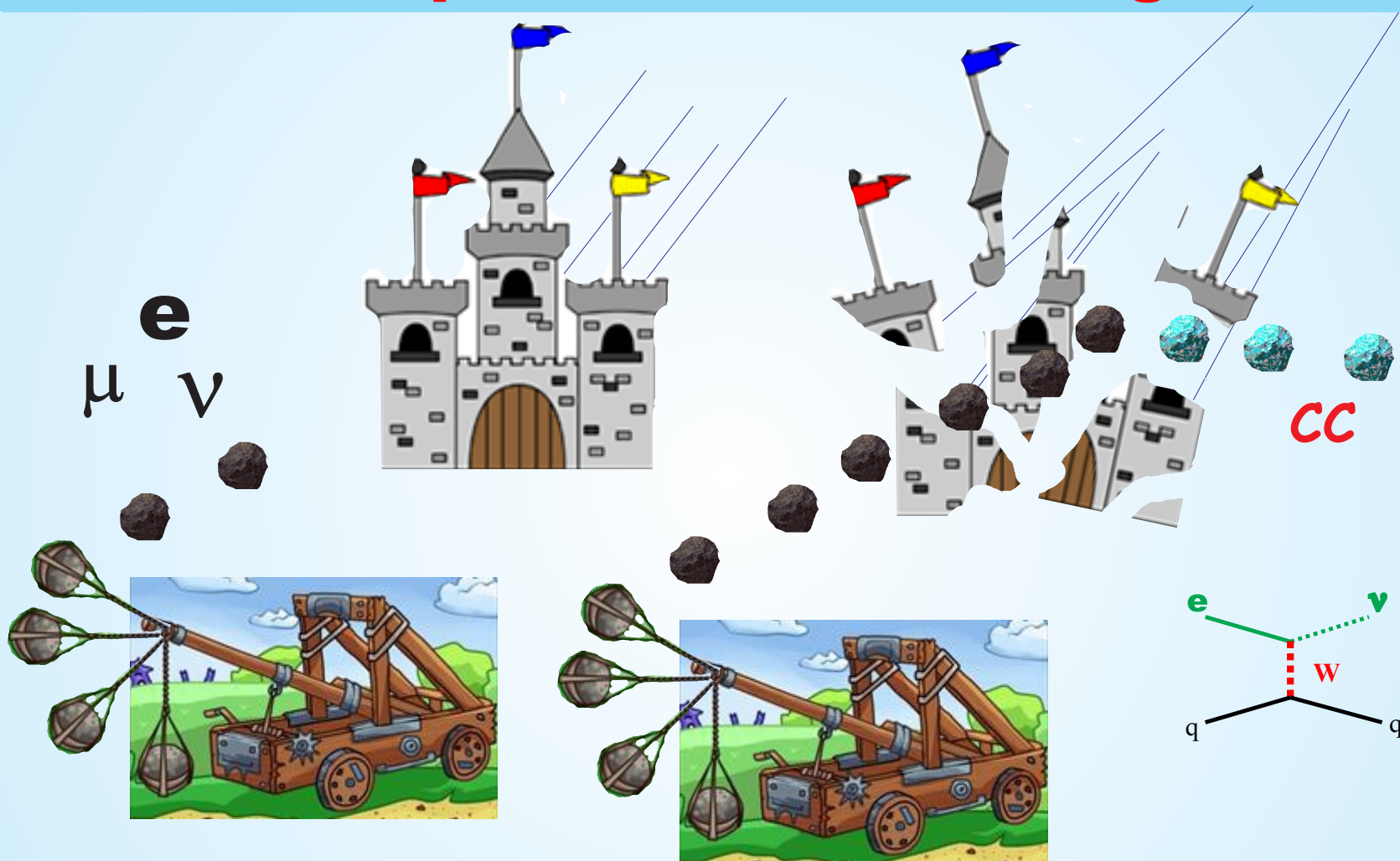
**I have selected what I saw fit
to make my point.**

**Any opinion is only mine and is
in no way supported by either
ZEUS or H1 or probably anybody else.**

**Nevertheless I am proud to represent
H1 and ZEUS.**



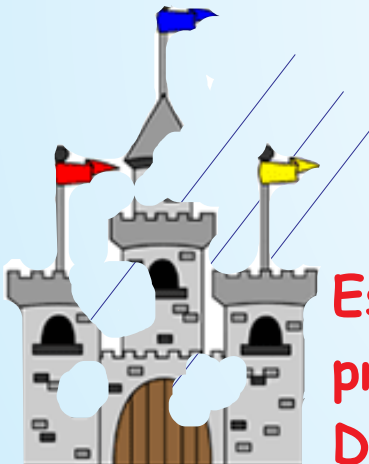
Deep Inelastic Scattering



Deep Inelastic Scattering

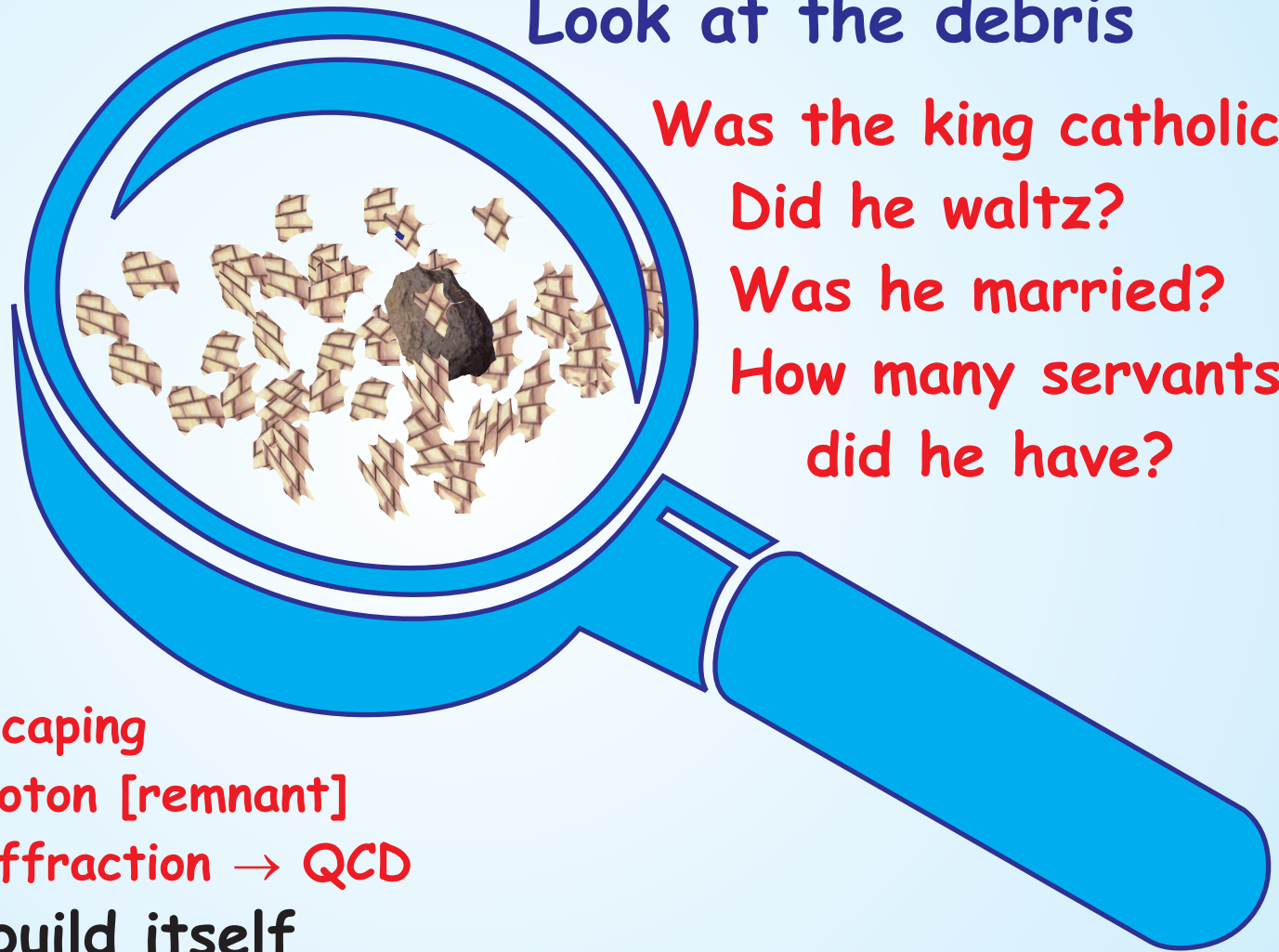
Look at the debris

Was the king catholic?
Did he waltz?
Was he married?
How many servants
did he have?



Escaping
proton [remnant]
Diffraction \rightarrow QCD

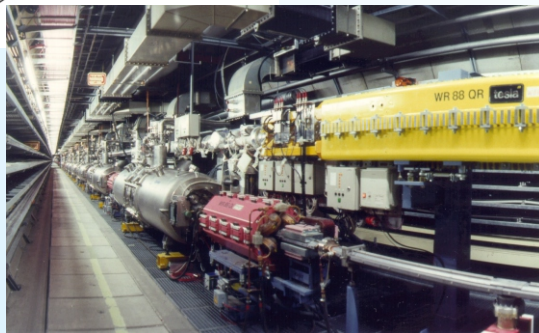
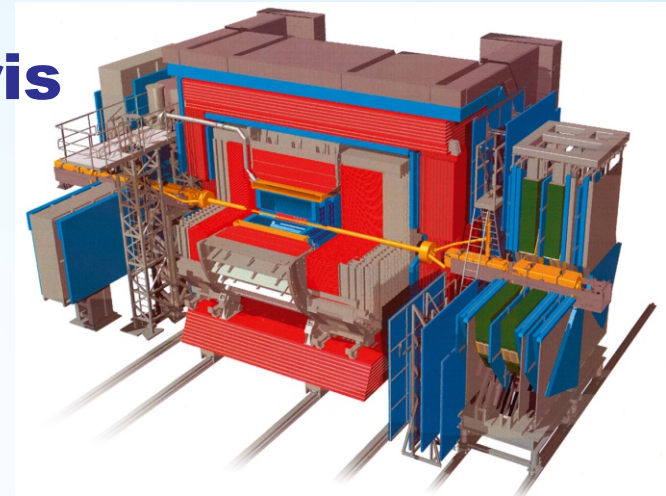
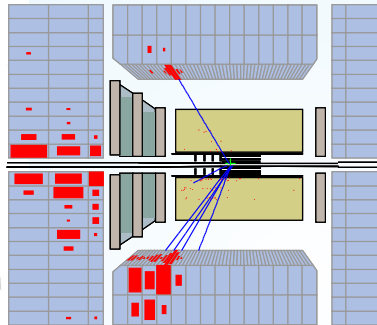
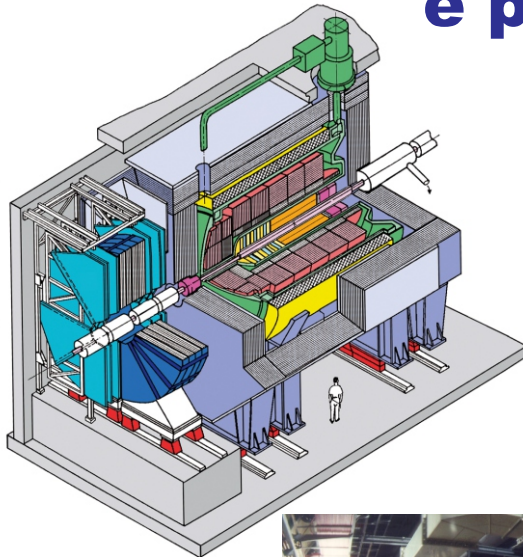
This can rebuild itself



The Microscope

That is what we measure!

$e p \rightarrow e (\nu) \text{ debris}$



We sort events,
classify, count,
plot and interpret.



**kinematic
variables**

Kinematics

Virtuality $Q^2 = -(k - k')^2$

Spatial resolution of probe

$$\lambda \sim 1/\sqrt{Q^2}$$

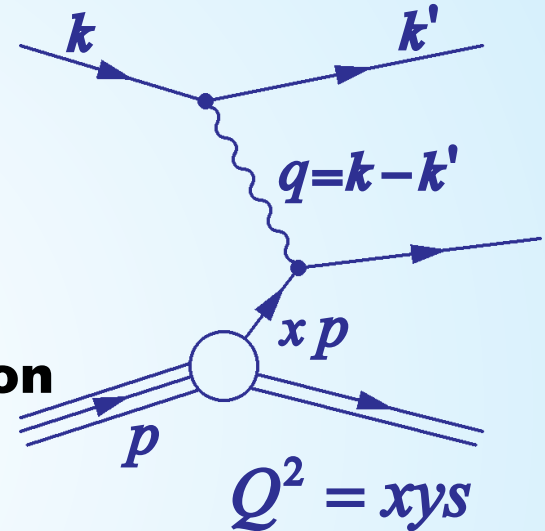
Bjorken scaling variable:

$$x = Q^2 / 2pq$$

Momentum fraction of struck parton

Inelasticity: $y = pk / pq$

Energy transfer to proton (in p rest frame)



$$Q^2 = xys$$

Reconstruction

$$y_e = 1 - \frac{E'_e(1 - \cos \theta_e)}{2E_e}$$

$$Q_e^2 = \frac{E_e'^2 \sin^2 \theta_e}{1 - y_e}$$

$$x_e = \frac{Q_e^2}{4E_p E_e y_e}$$

Factorisation

Decompose cross section:

$$\sigma(ep \rightarrow e + H + X) = \sum_{j,j'=q,\bar{q},g} f_{j/p}(x, Q) \otimes \hat{\sigma}_{jj'}(x, Q, z) \otimes F_{H/j'}(z, Q)$$

**parton
distribution
functions**

PDF

**partonic
cross section**

hadronisation

NC $V^* = \gamma^*, Z^*$

Born $V^* q \rightarrow q$

boson-gluon-fusion $V^* g \rightarrow q\bar{q}$

QCD-Compton-scattering $V^* q \rightarrow qg$

CC W^*

$V^* q \rightarrow q'$

lowest-order QCD

Structure Functions

$e^\pm p$

tree level

$$\sigma_{r,NC}^\pm = \frac{d^2 \sigma_{NC}^{e^\pm p}}{dx dQ^2} \cdot \frac{Q^4 x}{2\pi\alpha^2 Y_+} = \tilde{F}_2 \mp \frac{Y_-}{Y_+} x\tilde{F}_3 - \frac{y^2}{Y_+} \tilde{F}_L$$

$$\tilde{F}_2 = F_2 - \kappa_Z v_e \cdot F_2^{\gamma Z} + \kappa_Z^2 (v_e^2 + a_e^2) \cdot F_2^Z$$

$$\tilde{F}_L = F_L - \kappa_Z v_e \cdot F_L^{\gamma Z} + \kappa_Z^2 (v_e^2 + a_e^2) \cdot F_L^Z$$

$$x\tilde{F}_3 = \kappa_Z a_e \cdot xF_3^{\gamma Z} - \kappa_Z^2 \cdot 2v_e a_e \cdot xF_3^Z$$

$$Y_\pm = 1 \pm (1-y)^2$$

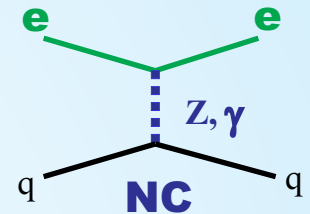
v_e vector

a_e axial-vector

eZ weak couplings

$$\kappa_Z(Q^2) = Q^2 / [(Q^2 + M_Z^2)(4 \sin^2 \theta_W \cos^2 \theta_W)]$$

(2)



QPM $\tilde{F}_L = 0$

$$(F_2, F_2^{\gamma Z}, F_2^Z) = [(e_u^2, 2e_u v_u, v_u^2 + a_u^2)(xU + x\bar{U}) + (e_d^2, 2e_d v_d, v_d^2 + a_d^2)(xD + x\bar{D})]$$

$$(xF_3^{\gamma Z}, xF_3^Z) = 2[(e_u a_u, v_u a_u)(xU - x\bar{U}) + (e_d a_d, v_d a_d)(xD - x\bar{D})]$$

$$xU = xu + xc$$

$$x\bar{U} = x\bar{u} + x\bar{c}$$

$$xD = xd + xs$$

$$x\bar{D} = x\bar{d} + x\bar{s}$$

sea quarks = anti-quarks

valence quark distributions

$$xu_v = xU - x\bar{U}$$

$$xd_v = xD - x\bar{D}$$

Structure Functions

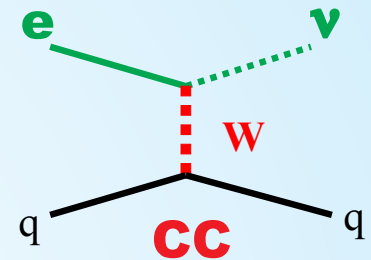
$e^\pm p$

tree level

$$\sigma_{r,CC}^\pm = \frac{Y_+}{2} W_2^\pm \mp \frac{Y_-}{2} x W_3^\pm - \frac{y^2}{2} W_L^\pm$$

QPM $W_L^\pm = 0$

CC is unfortunately
a bit more difficult.



$$W_2^+ = x\bar{U} + xD$$

$$xW_3^+ = xD - x\bar{U}$$

$$W_2^- = xU + x\bar{D}$$

$$xW_3^- = xU - x$$

$$\sigma_{r,CC}^+ = x\bar{U} + (1-y)^2 xD$$

$$\sigma_{r,CC}^- = xU + (1-y)^2 x\bar{D}$$

NC and **CC** yield **valence and sea quark distribution**.

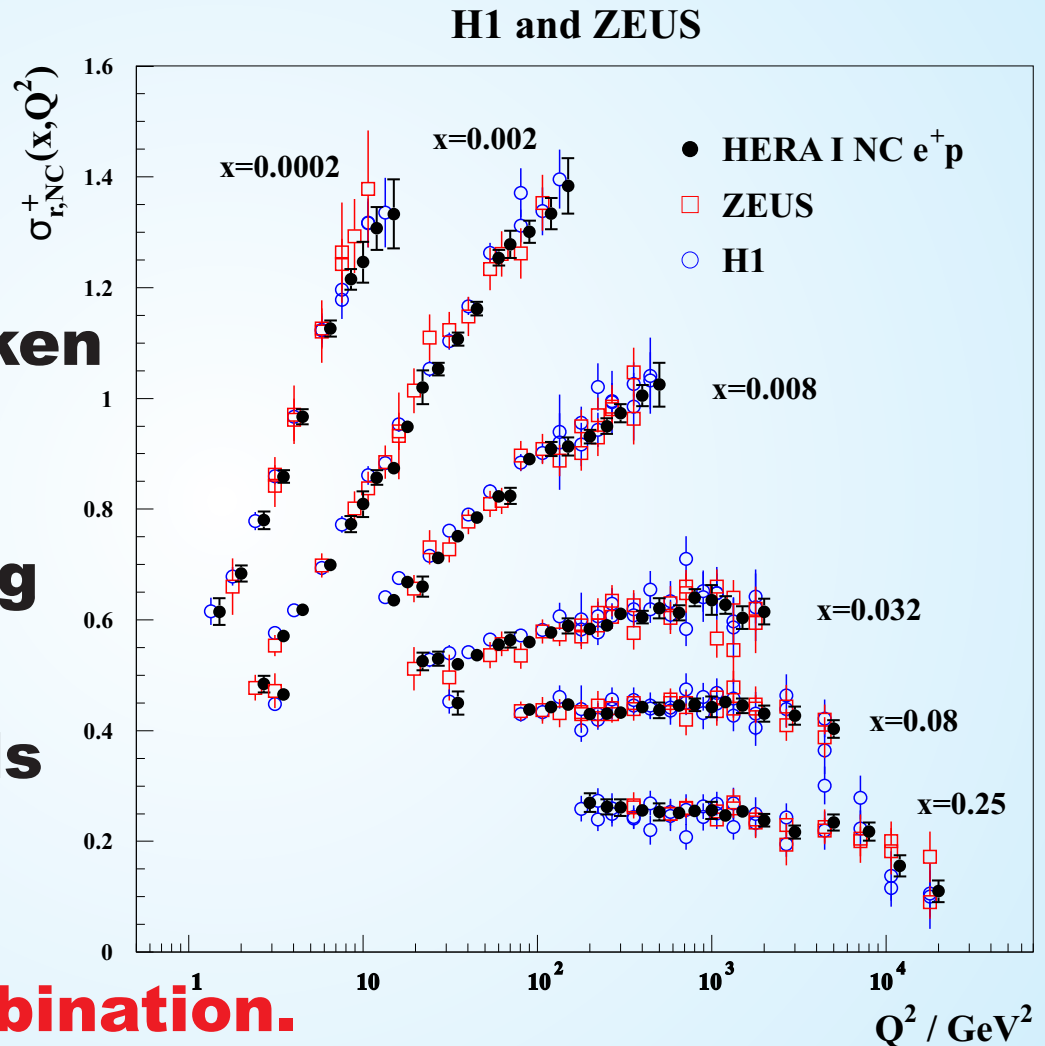
QCD analysis [DGLAP] yields gluon distribution.

Advent of Precision

**2010:
H1 and ZEUS
publish combined
results on data taken
1993 to 2000.**

**10 years of fighting
to understand
detectors, methods
and systematics.**

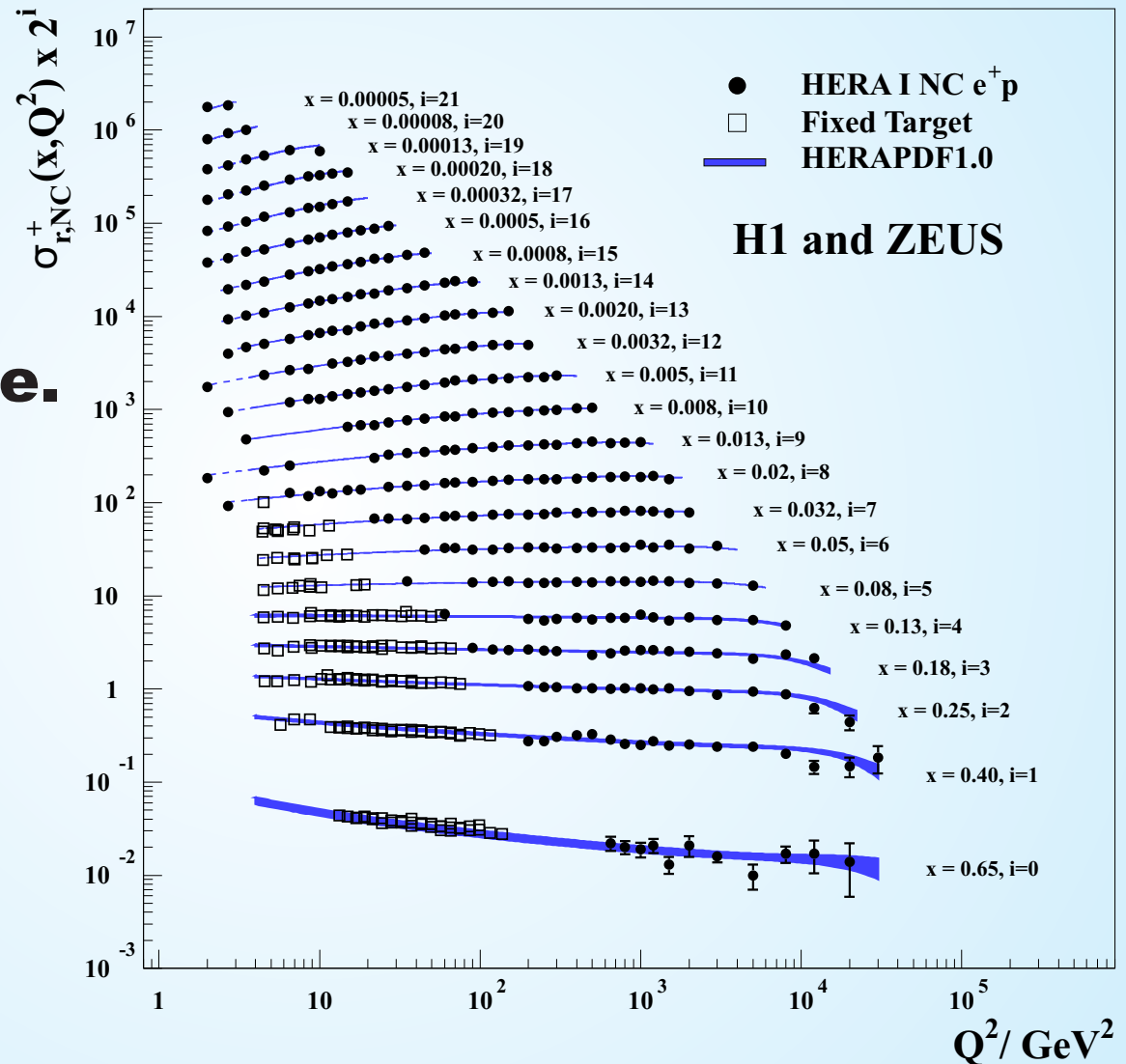
The power of combination.



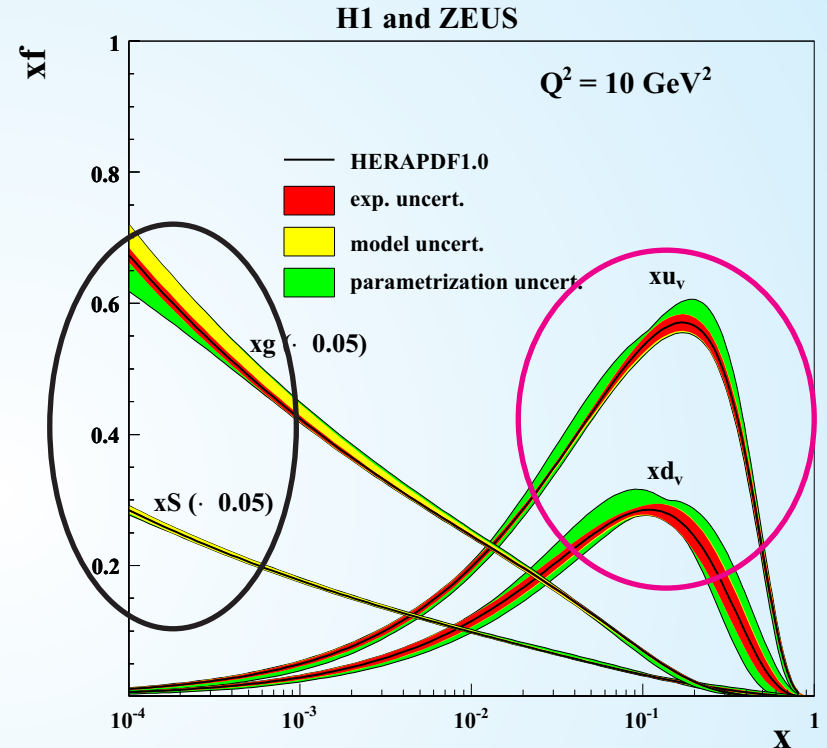
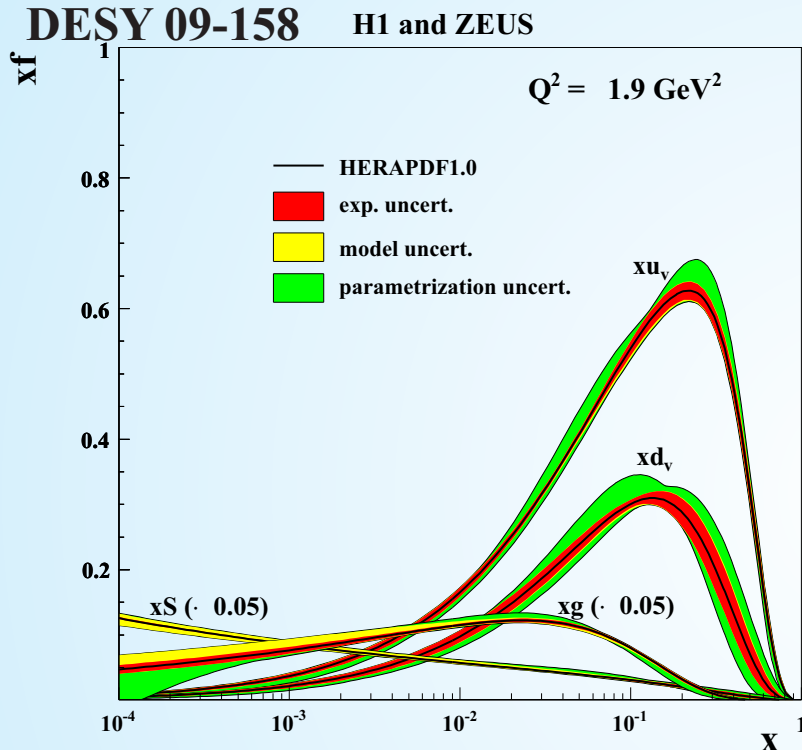
Reduced Cross Section

Cross section data over a very large kinematic range.

HERA data were used as only input to fit HERAPDF 1.0



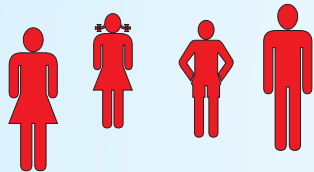
HERAPDF1.0



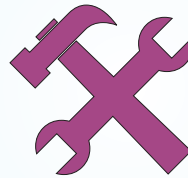
**The proton pdfs reveal the valence quarks
plus glue and sea evolving with Q^2 .
Inclusive DIS data alone can do this.**

The PDF Community

CTEQ JR
HERA MSTW
NNPDF ABKM



SF:We 12.00



Schemes

Parametrisations

systematic
uncertainties

[HERA]fitter

DATA

PDF

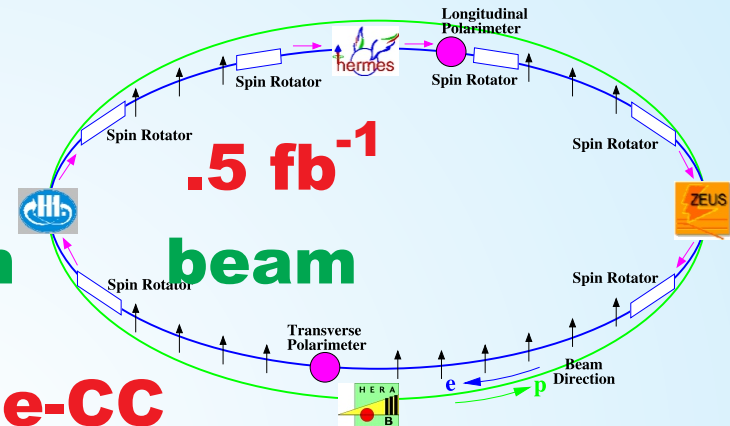
Prediction

Consistency between fit and “→” for prediction
is essential.

High Statistics Data

HERA II 2003-2007

**ZEUS and H1 both got to \approx
polarised electron/positron**



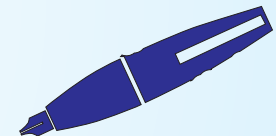
e+ NC e-NC e+CC e-CC



prel. published



preliminary



Everything high Q^2 to be published soon.

In addition:

F_{2c} F_{2b} F_L

F_{2diff}

Diffraction

jets

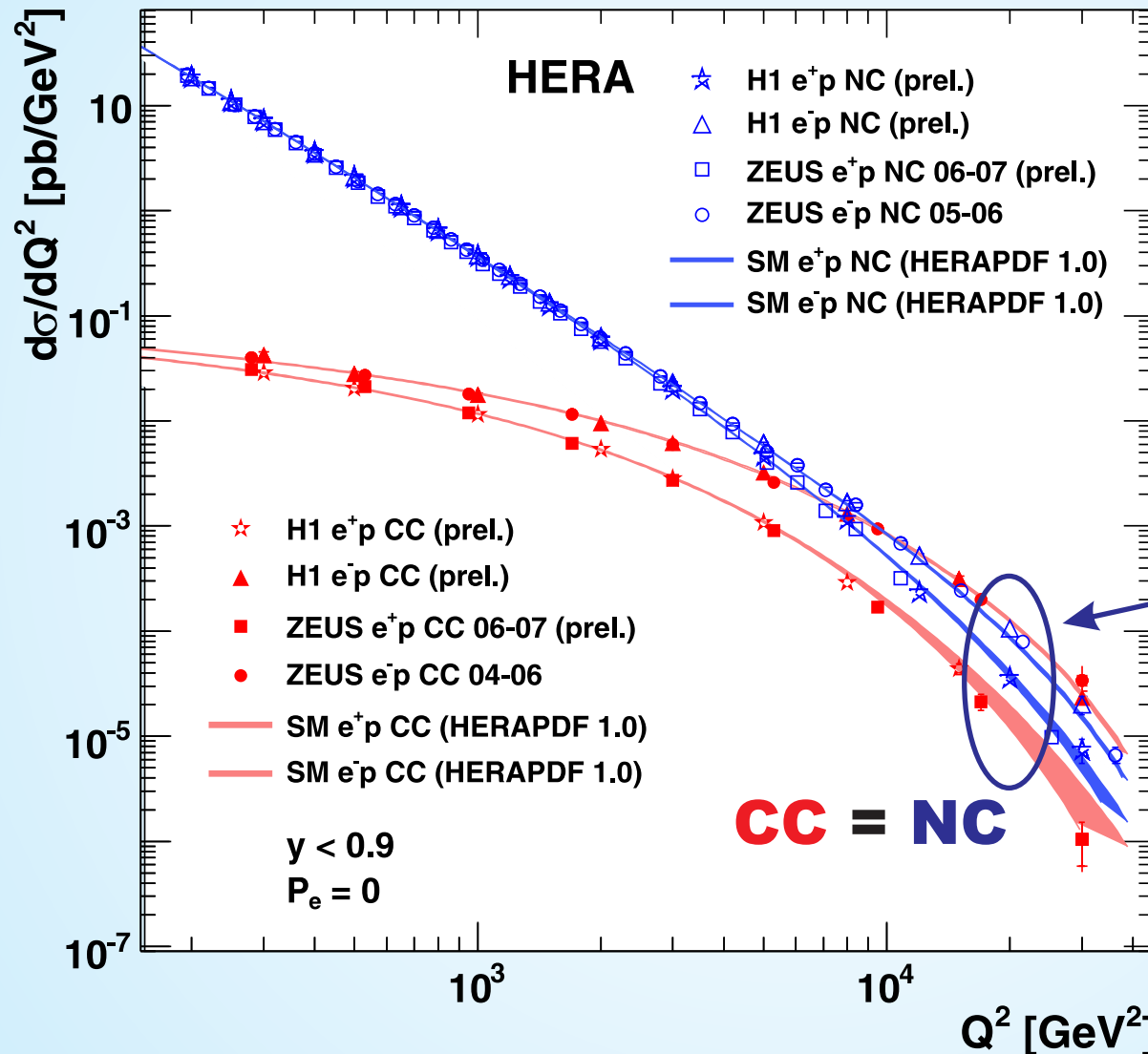
HFS

QCD

P:K. Daum

Mo 14.55

A Taste of Precision



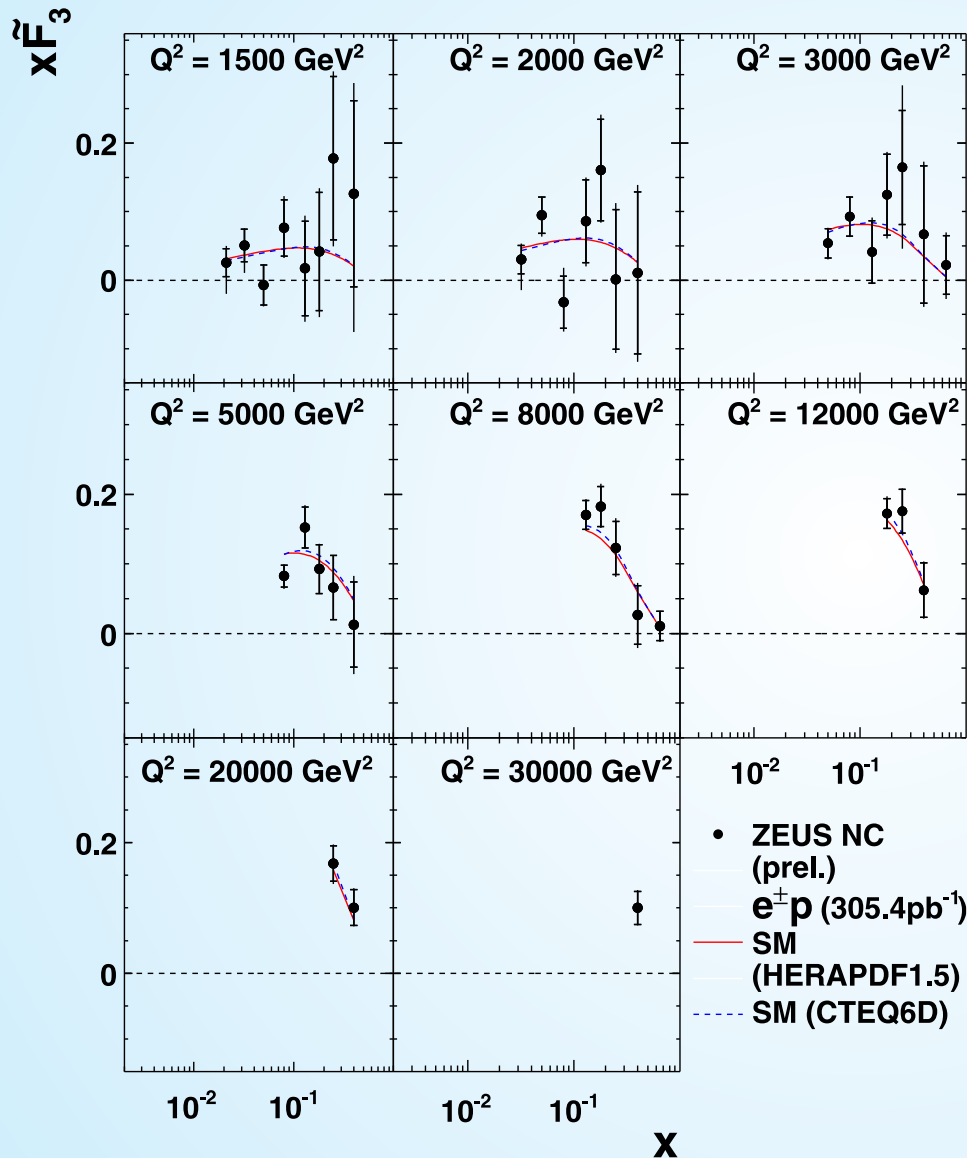
high Q^2

NC

CC

$x F_3$
difference
between
positron
and electron
data

A Taste of Precision



ZEUS

NC

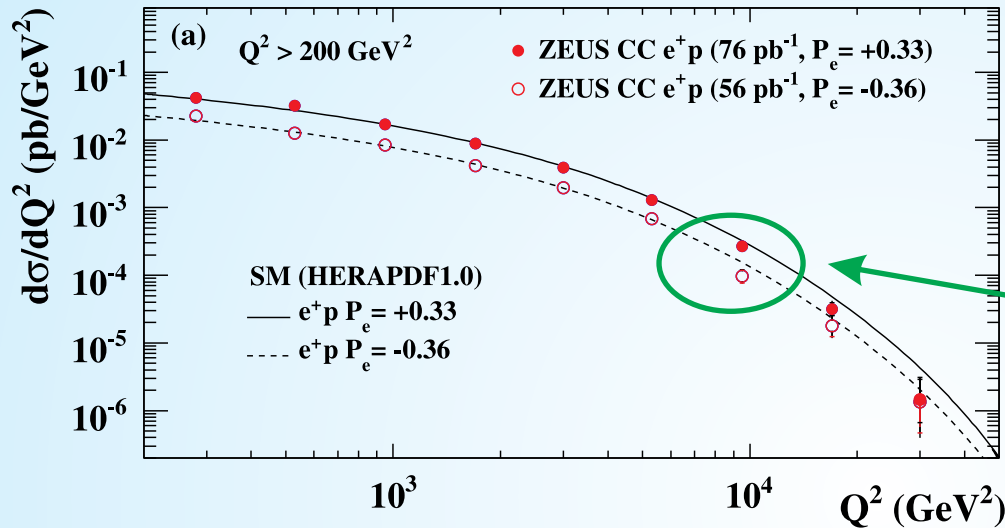
positron and
electron data

SF: We 9.00

ZEUS-prel-11-003

$$x\tilde{F}_3 = \frac{Y_+}{2Y_-} (\sigma_{r,\text{NC}}^- - \sigma_{r,\text{NC}}^+)$$

A Taste of Precision



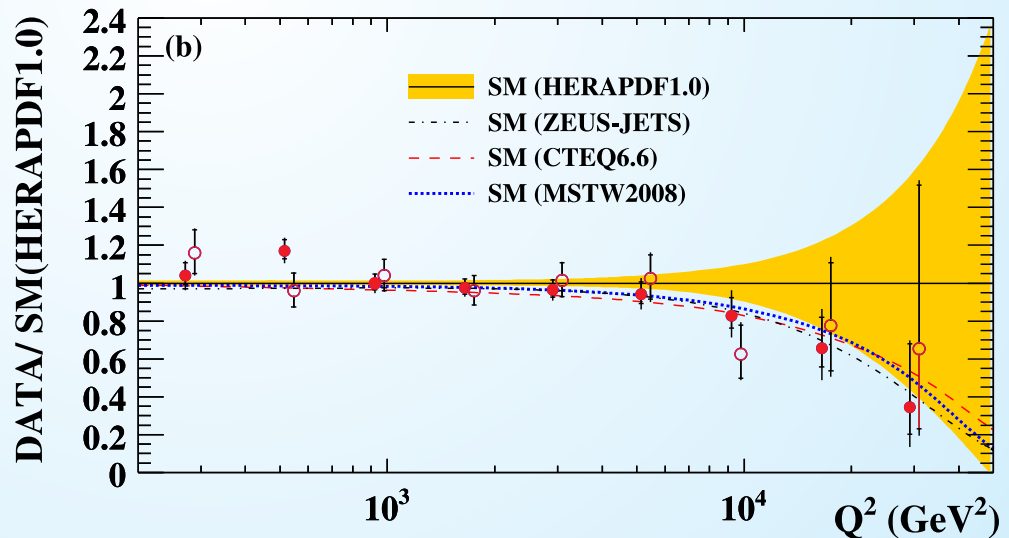
ZEUS

CC

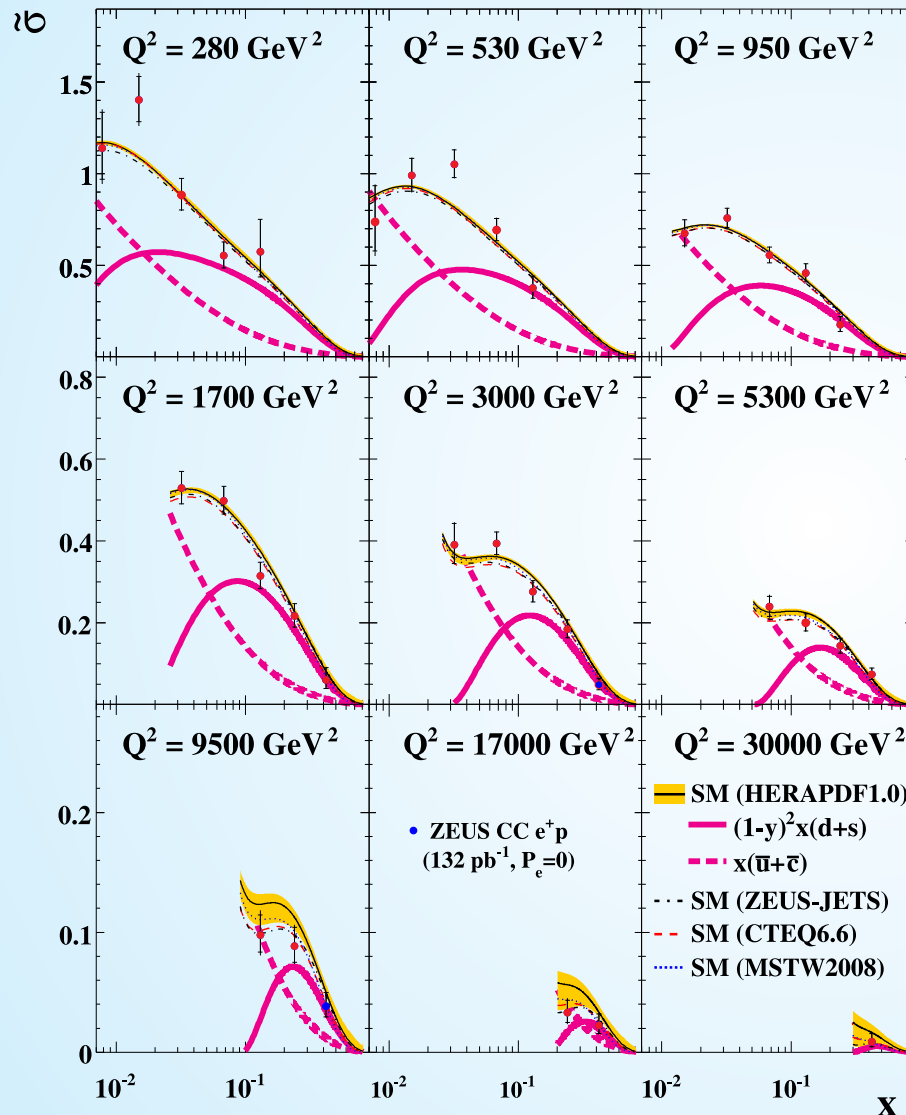
**polarised
positron data**

DESY 10-129

**Beautiful
input
for fits**



A Taste of Precision



ZEUS

DESY-10-129

CC

positron data

$$\sigma_{r,CC}^+ = x\bar{U} + (1-y)^2 xD$$

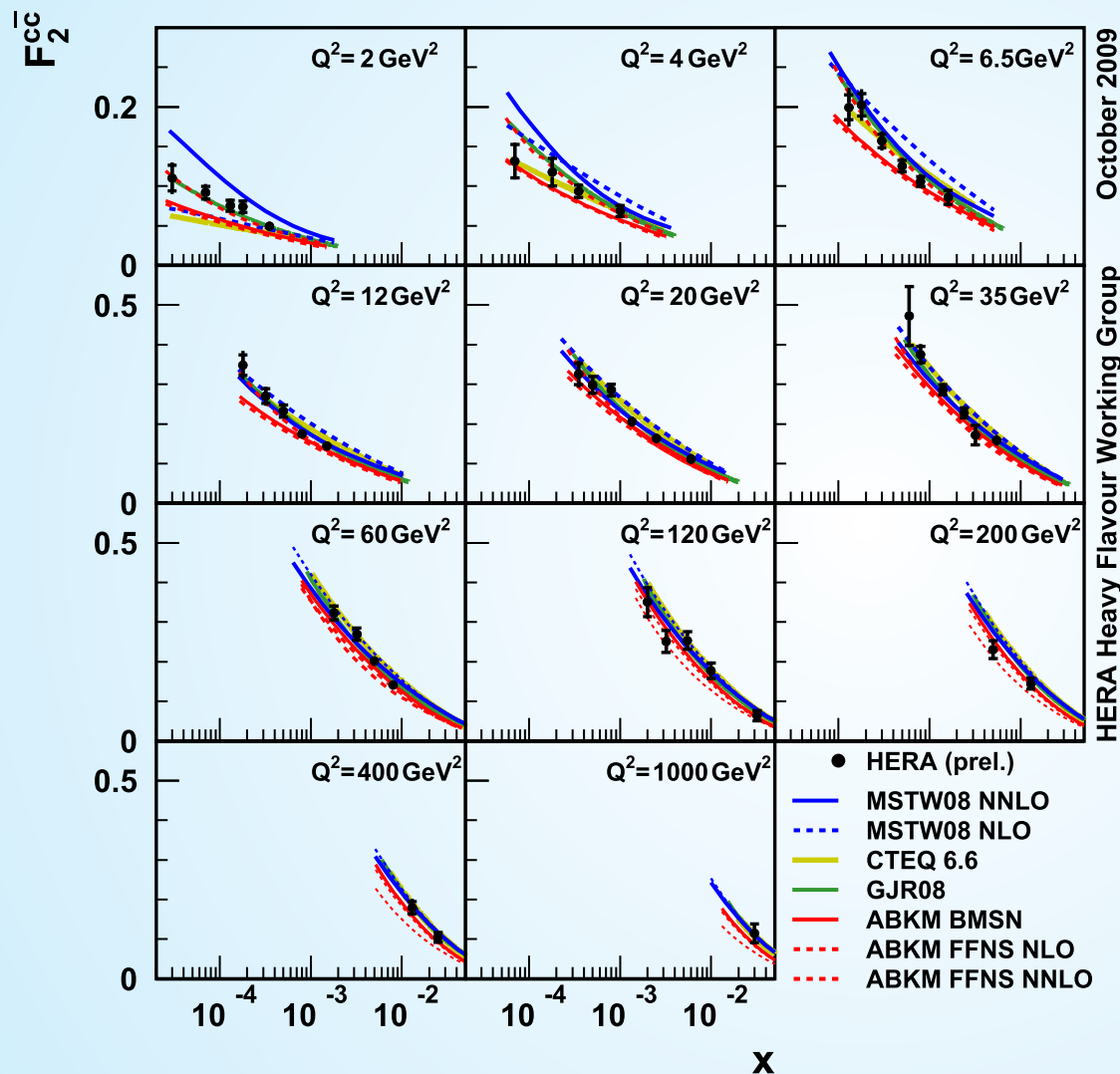
$$xD = xd + xs$$

$$x\bar{U} = x\bar{u} + \boxed{x\bar{c}}$$

**a hint of
charm**



Charm Structure Function



$$xU = xu + xc$$

a handle
on charm



NC :

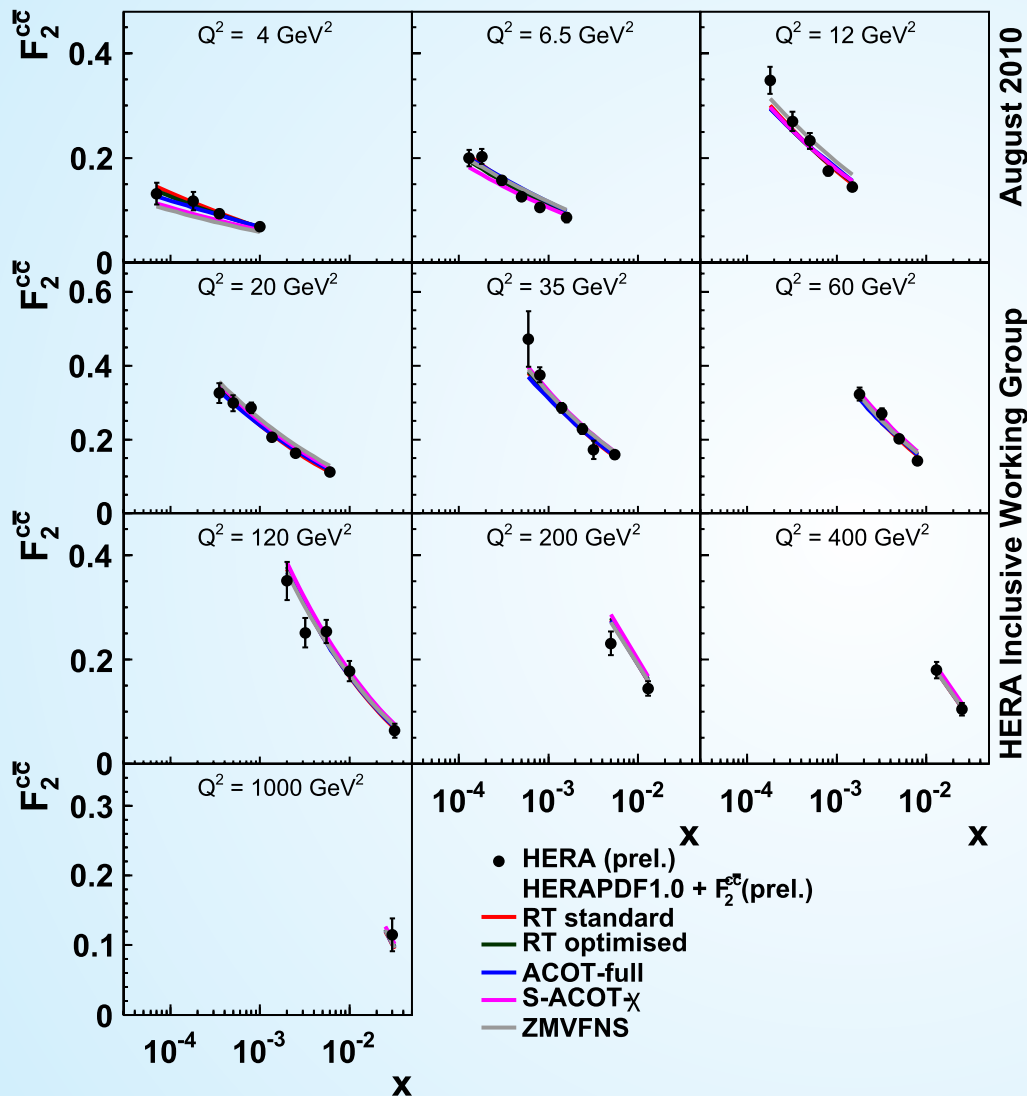
produce all
kinds of
D mesons

[tagged somehow]



H1prel-09-0171
ZEUS-prel-09-015

Charm Structure Function



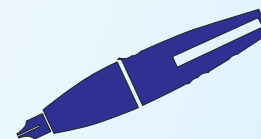
August 2010

HERA Inclusive Working Group

$$xU = xu + xc$$

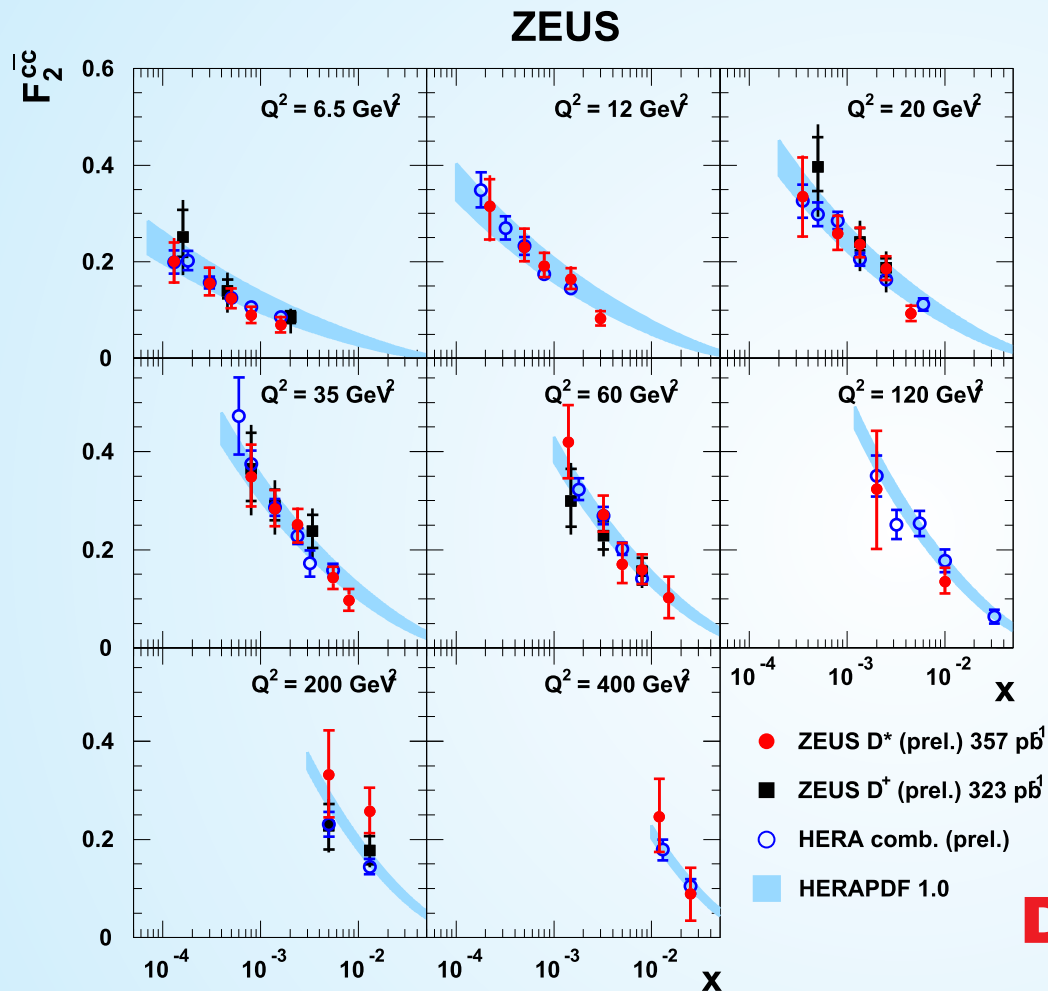
HERAPDF1.0
plus preliminary
charm data

charm mass scan



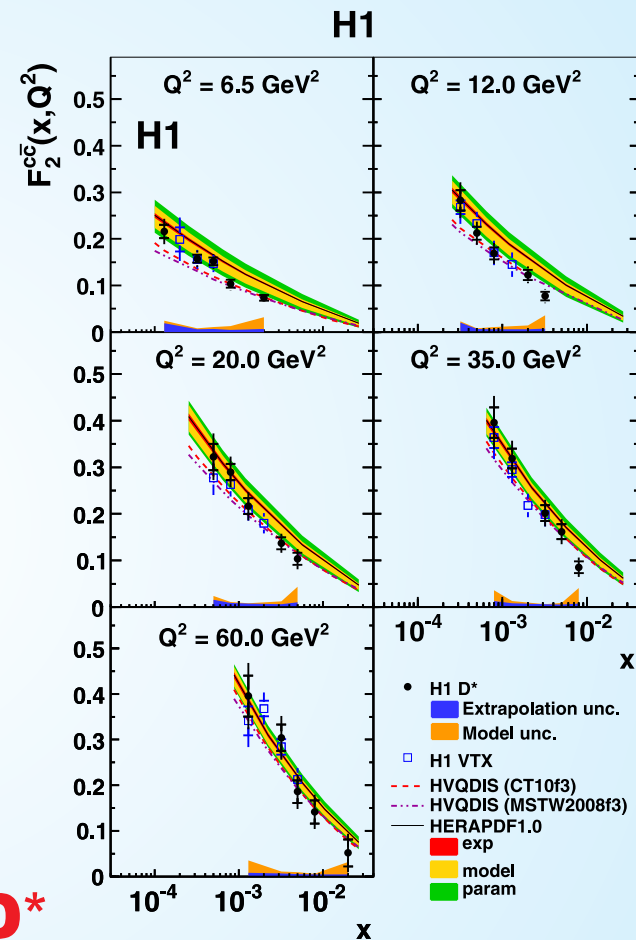
H1prel-10-143
ZEUS-prel-10-019

Charm Structure Function



ZEUS-prel-11-012

HFL: Thursday 11.00 + 11.18 Z-prel-12-002



D^*

H1 DESY 11-066

HFL: Thursday 11.36

HERAPDF Family

recommended
version →

NAME	NC and CC DIS	NC, lower E(p_beam)	Jets	Charm	Docu	Grids	Data comparison	Date
HERAPDF1.7 NLO	HERAI + partial HERAI	H1+ZEUS	H1 and ZEUS(1)	H1+ZEUS	Figures	N.A.		June 2011
HERAPDF1.6 NLO	HERAI + partial HERAI	---	H1 and ZEUS(1)	---	Writeup and figures	N.A.		March 2011
HERAPDF 1.5 NNLO	HERAI + partial HERAI	---	---	---	Figures	LHAPDF beta 5.8.6		March 2011
HERAPDF 1.5 NLO	HERAI + partial HERAI	---	---	---	Figures	LHAPDF beta 5.8.6		July 2010
Charm mass scan	HERAI	---	---	H1+ZEUS	Writeup and figures	---		August 2010
HERAPDF1.0 NNLO	HERAI	---	---	---	ICHEP2010 writeup and figures	Docu for LHAPDF		April 2010
	HERAI	H1+ZEUS	---	---	Writeup and figures	N.A.		April 2010
	HERAI	---	---	H1+ZEUS	DIS2010 writeup and figures	N.A.		April 2010
HERAPDF1.0 NLO PUBLISHED	HERAI	---	---	---	Paper HERAPDF1.0 page	LHAPDF	Benchmarking HERAPDF1.0	Nov. 2009

More and more data are being added.

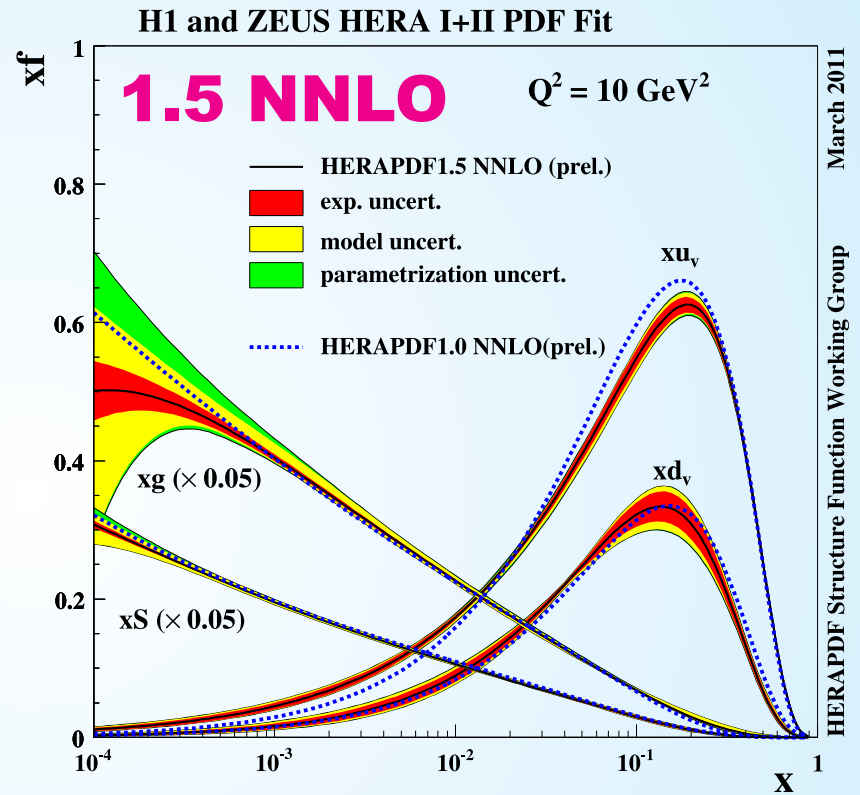
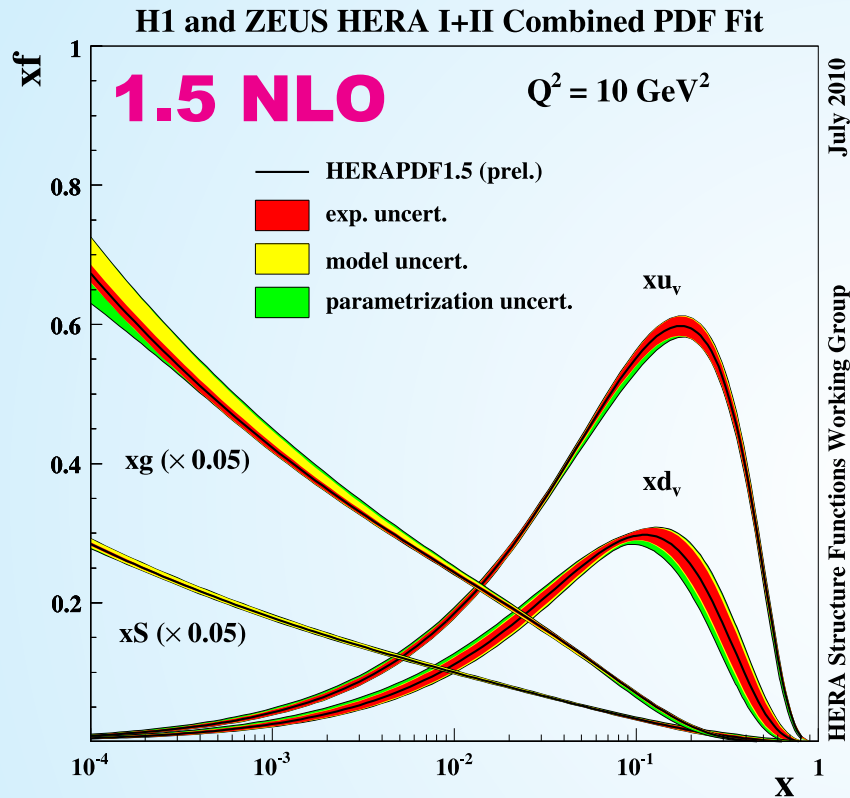
A major release will come as soon as all inclusive data published.

SF: Tu 10.05

H1prel-11-143

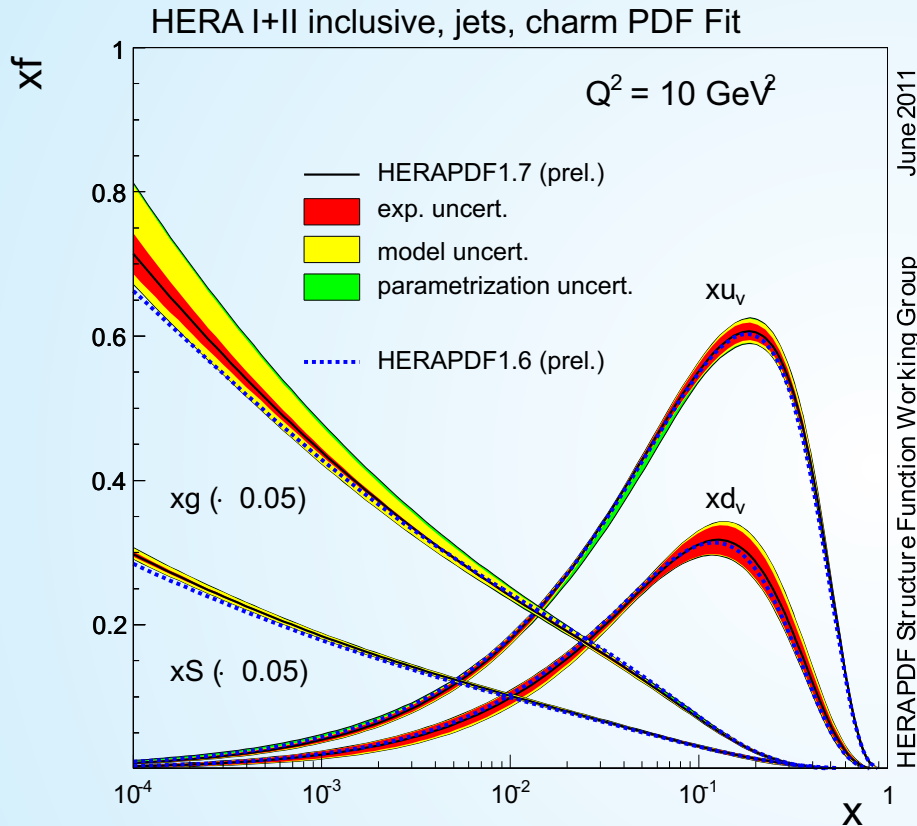
ZEUS-prel-11-010

HERAPDF Family



HERAPDF 1.5 NLO and 1.5 NNLO are the family members recommended for general use.

HERAPDF Family



H1prel-11-143
ZEUS-prel-11-010

SF: Tu 10.05

HERAPDF 1.7
is the newest
member based
on inclusive,
low E_p , jets and
charm data.

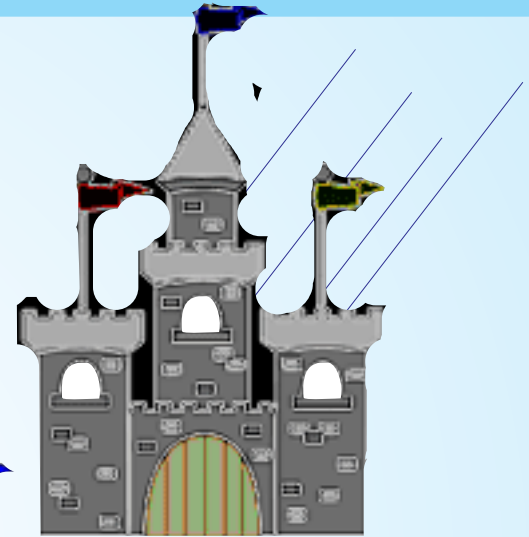
**steeper low-x gluon
than ever before:**

low E_p data

$m_c: 1.4 \rightarrow 1.5 \text{ GeV}$
RT optimal scheme

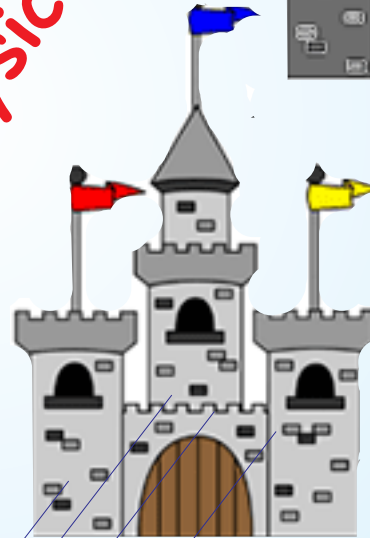
Castle Castle Interactions

proton
proton
collisions

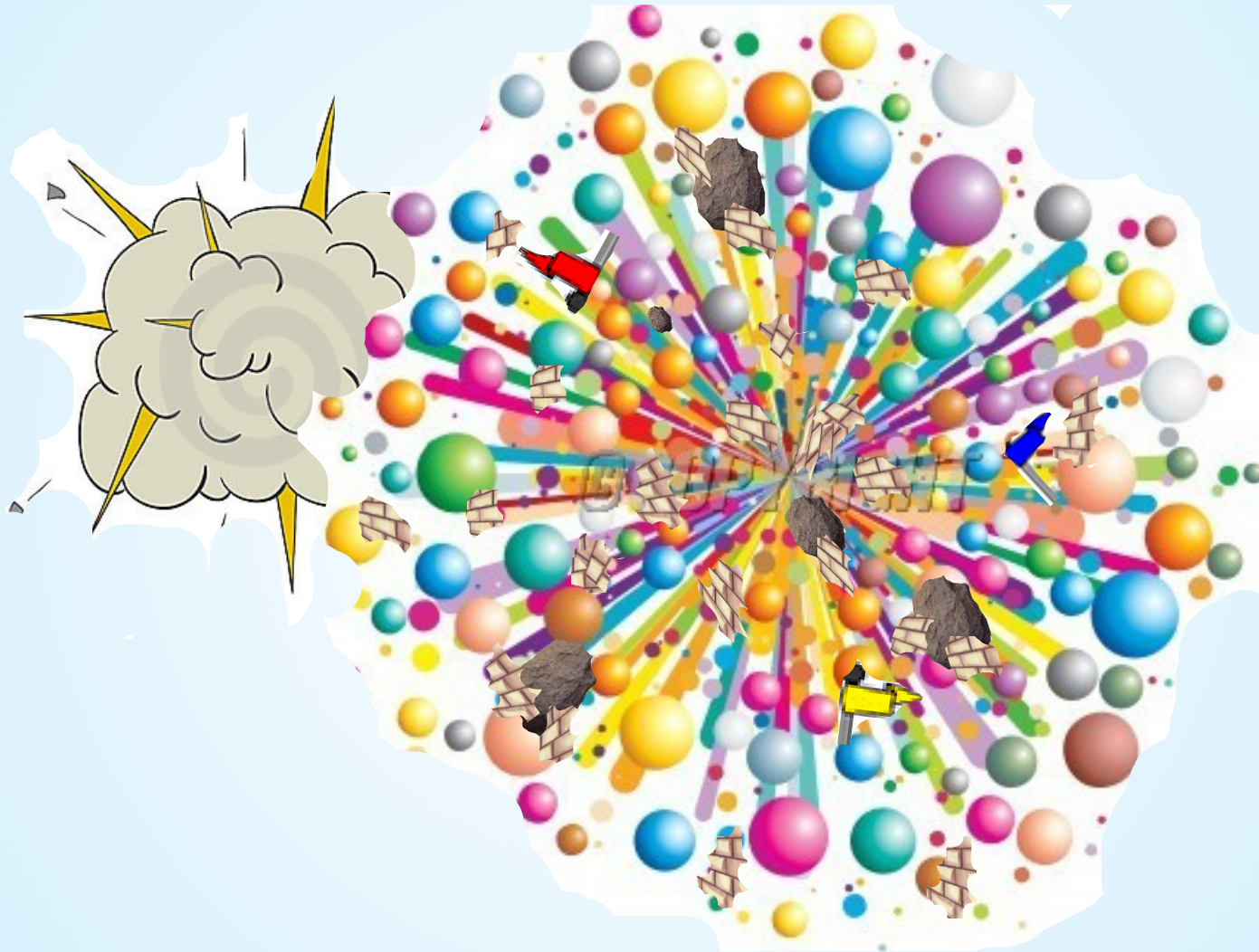


collider physics

antiproton
proton
collisions

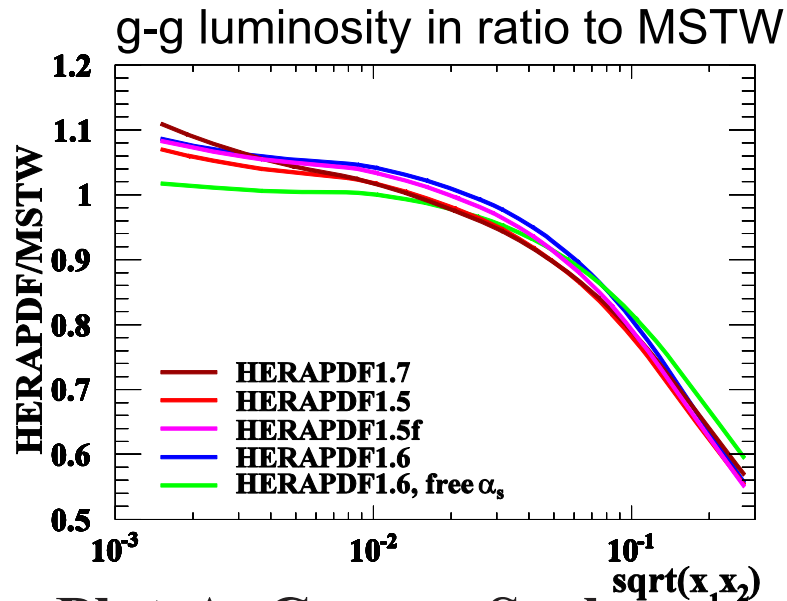


Beautiful Destruction

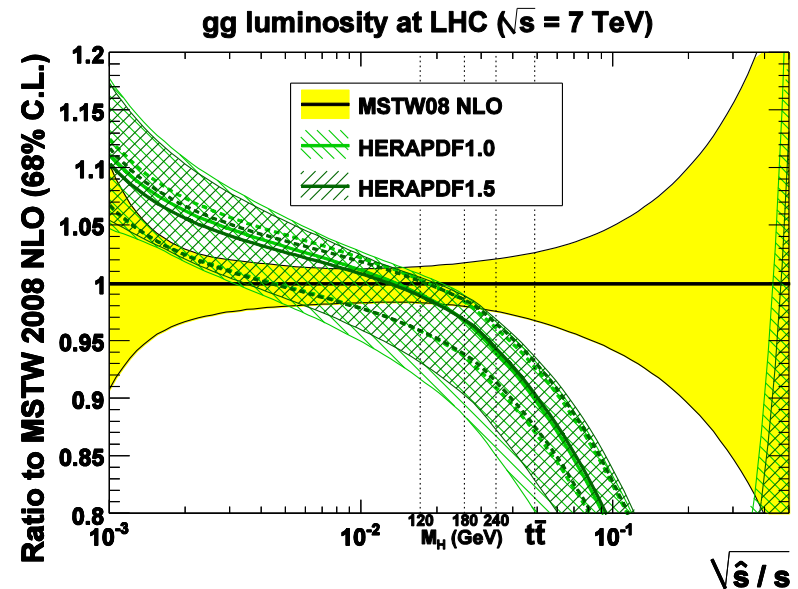


HERAPDF Predictions

LHC needs PDFs to predict SM distributions



Plot: A. Cooper-Sarkar



Plot: G. Watt

No reliable PDFs

⇒ no reliable searches



HERAPDF used by ATLAS and CMS

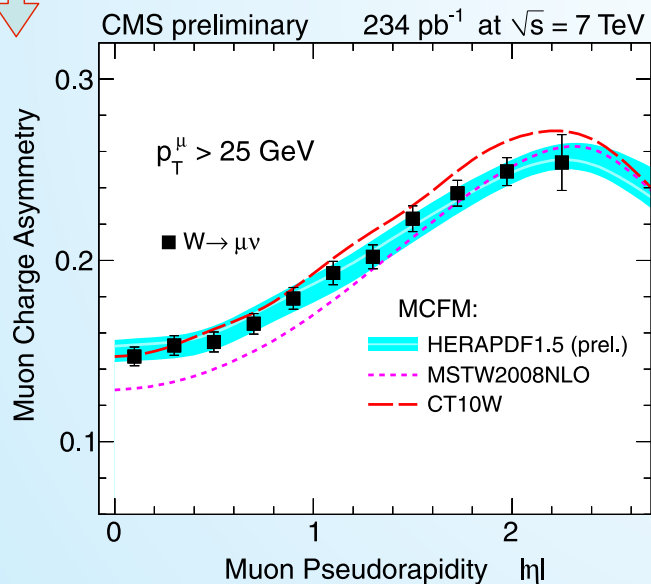
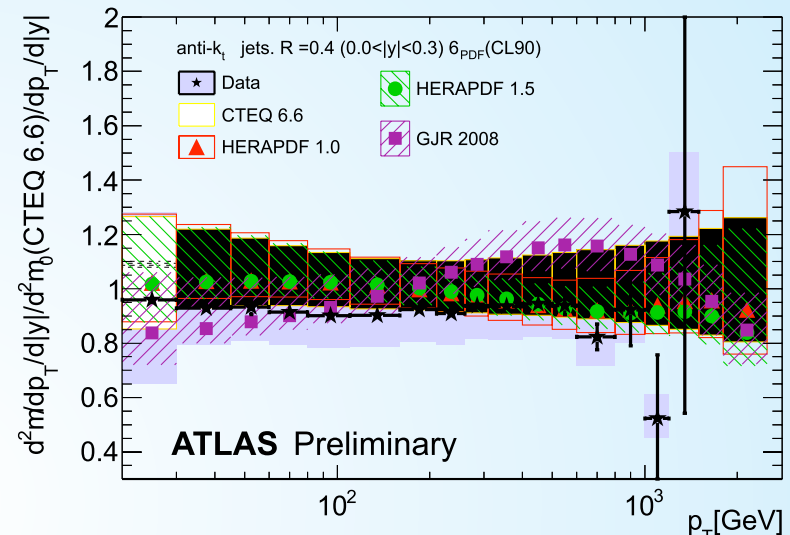
Jet production measurement:

sensitive to gluon distribution, $\alpha_S(M_Z)$

W muon charge asymmetry:

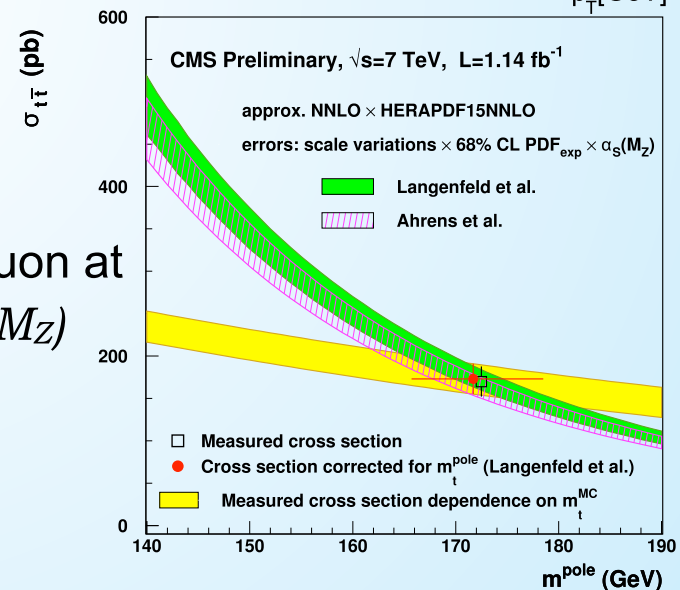
sensitive to difference between u and d

$$A_W = \frac{W^+ - W^-}{W^+ + W^-} \approx \frac{u_v - d_v}{u_v + d_v + 2u_{\text{sea}}}$$



Top pair production:

sensitive to gluon at high x , $\alpha_S(M_Z)$

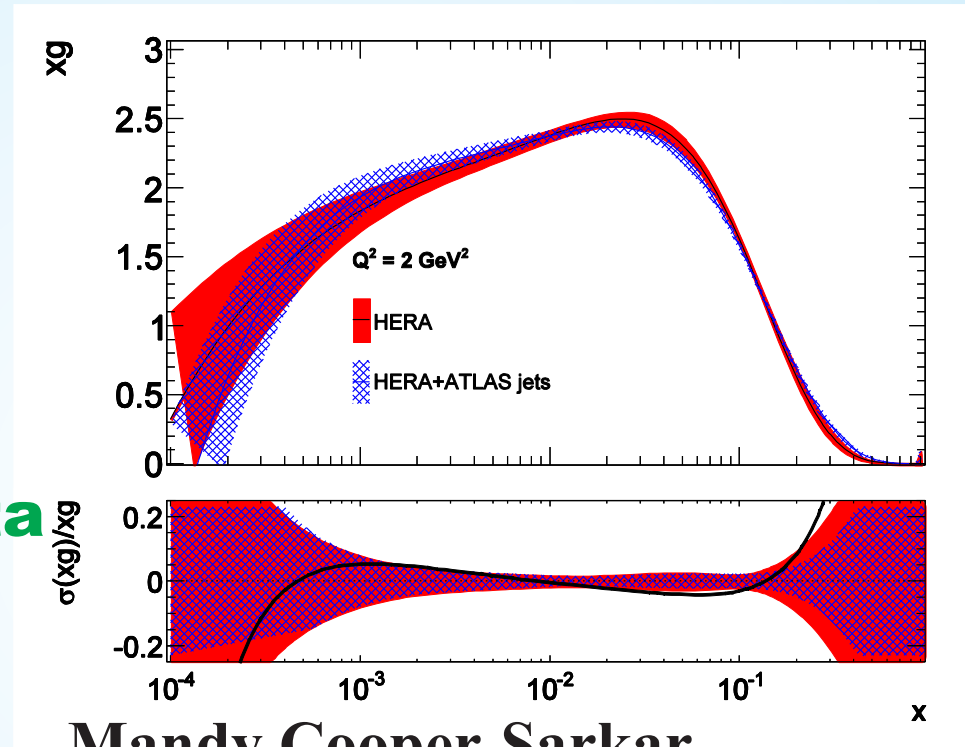
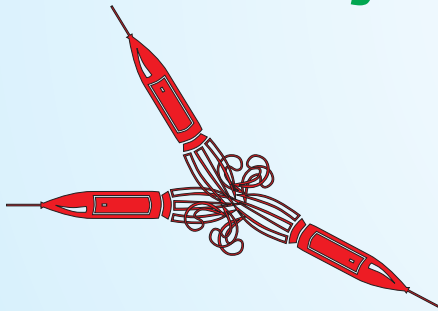


LHC can contribute



HERAPDF 1.5f

plus ATLAS jet data



Mandy Cooper-Sarkar

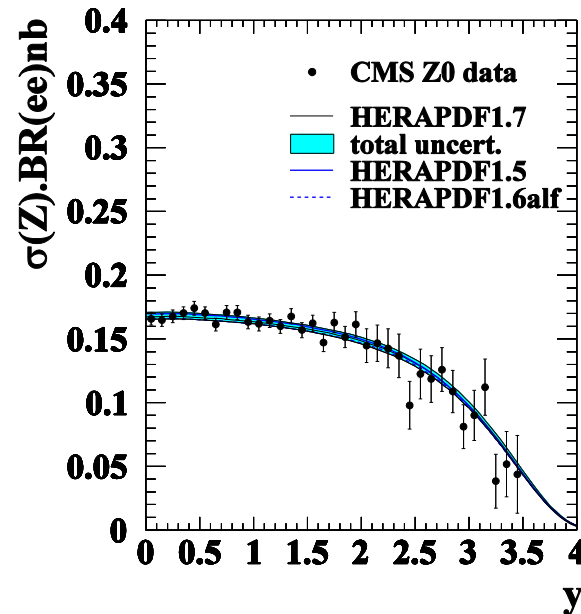
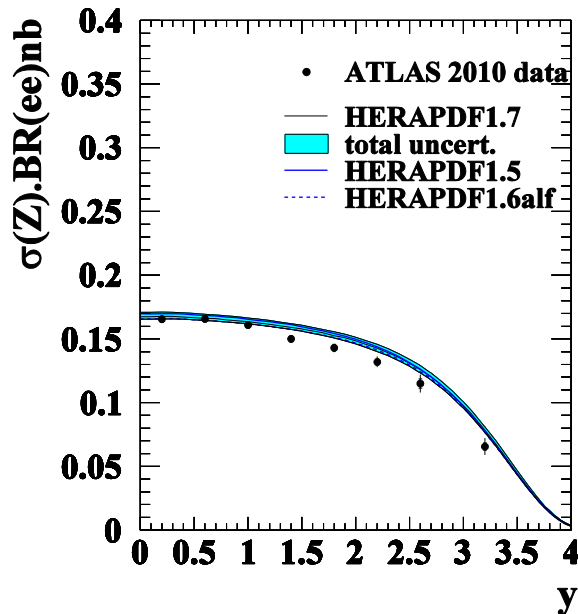
Work done on published ATLAS data

ATLAS jets would like high-x gluon to be harder.

HERA also still has jet data. DESY 12-045 HFS: Tu 17.50

HERAPDF Predictions

Z^0 production at the LHC



Private communication from Mandy Cooper-Sarkar

HERAPDF 1.7 is doing quite well.

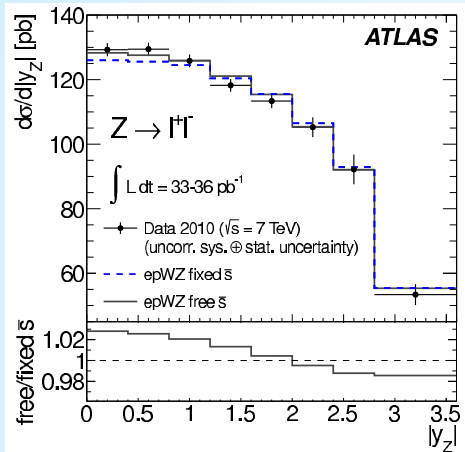
The differences to HERAPDF1.5/1.6 are small.

The strange sea is so far restricted in HERAPDF.

LHC can contribute

Strangeness

3



strange quark would need
CC analysis of Ds at HERA
 mission impossible

**ATLAS measures rapidity
 distribution of Z^0 production**

Fit $r_s = 0.5(s + \bar{s})/\bar{d}$ $x\bar{s}(x) = A_s x^{B_{\bar{d}}}(1-x)^{C_s}$

HERAFitter

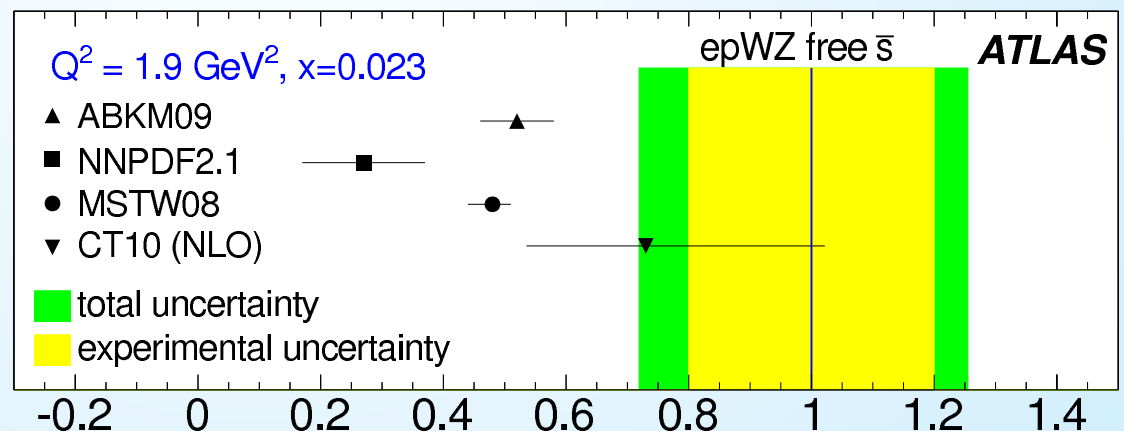
arxiv:1203.4051

$$r_s = 1.00 \pm 0.20_{\text{exp}}$$

$$\pm 0.07_{\text{mod}}^{+0.10}_{-0.15} \text{par}^{+0.06}_{-0.07} \alpha_s$$

$$\pm 0.08_{\text{th.}}$$

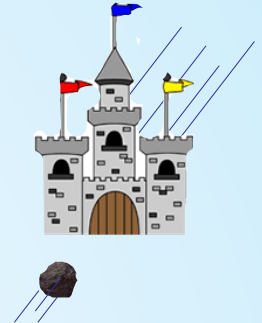
SF: Tu 9.40



Longitudinal Structure Function

FL is a high y phenomenon:

$$\sigma_r(x, Q^2) = F_2(x, Q^2) - \frac{y^2}{1 + (1 - y)^2} F_L(x, Q^2)$$



Need cross section for varying y at fixed x and Q^2

$$Q^2 = xys \Rightarrow \text{need to change } s$$

$$E_p = 920 \text{ GeV} \quad E_p = 575 \text{ GeV} \quad E_p = 460 \text{ GeV}$$

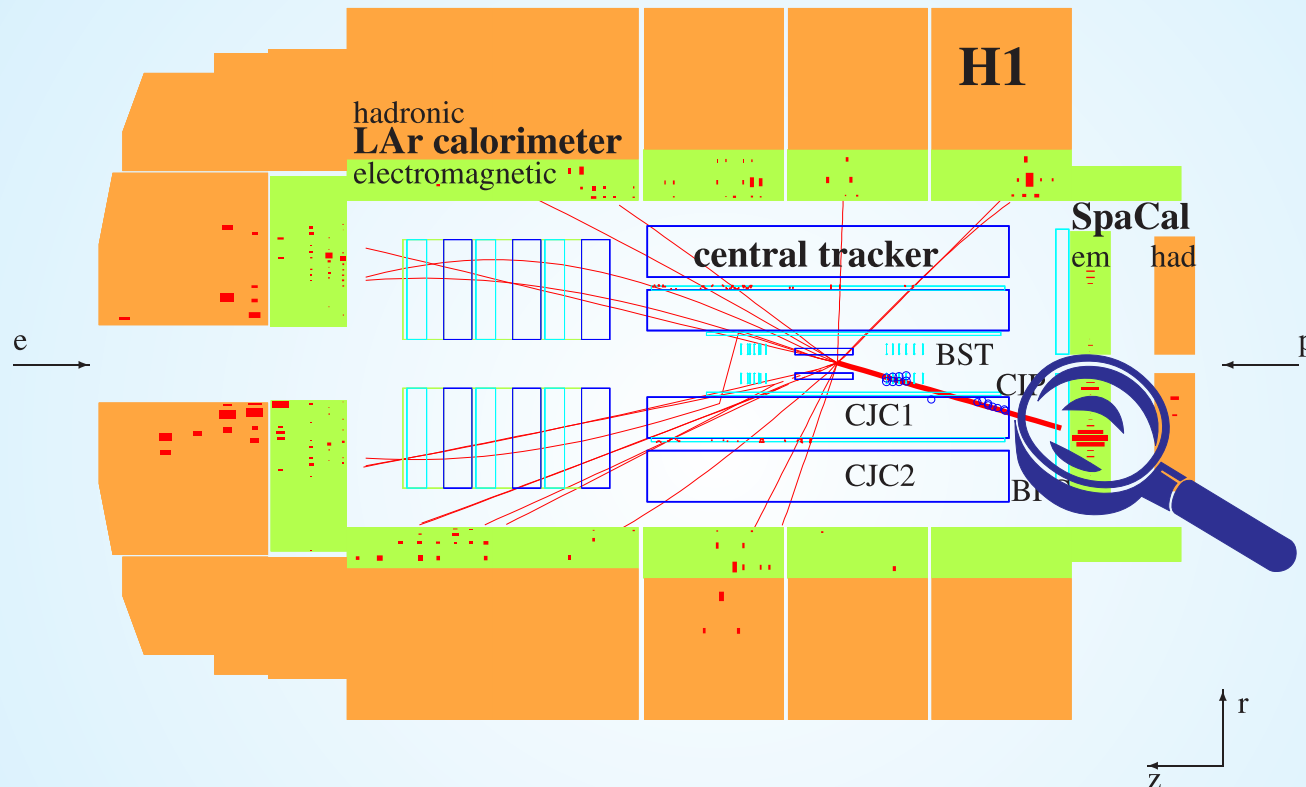
Low Q^2 and high $y \Rightarrow$ low energy of scattered electron



This is a challenge!

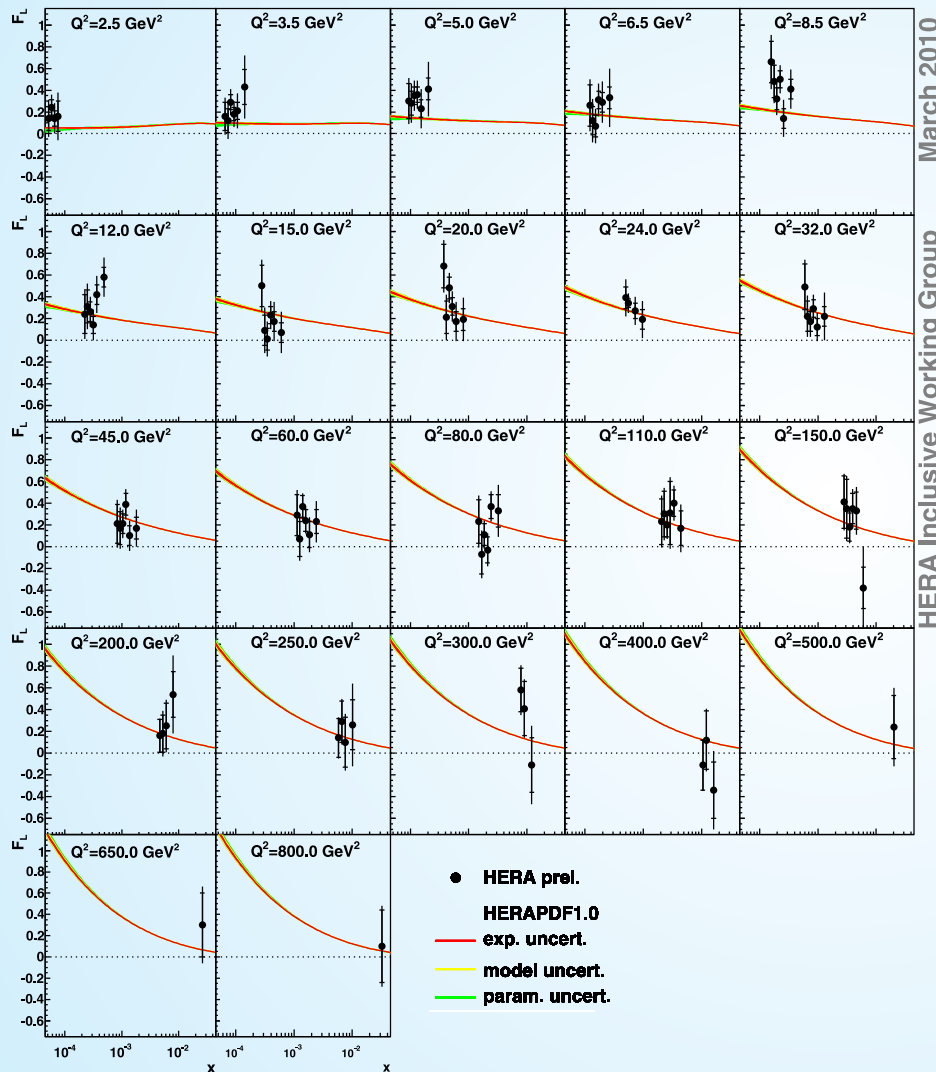
Direct access to glue!

Longitudinal Structure Function



**Events down to electron energies of 3.4 GeV
for ZEUS 6.0 GeV**

Longitudinal Structure Function

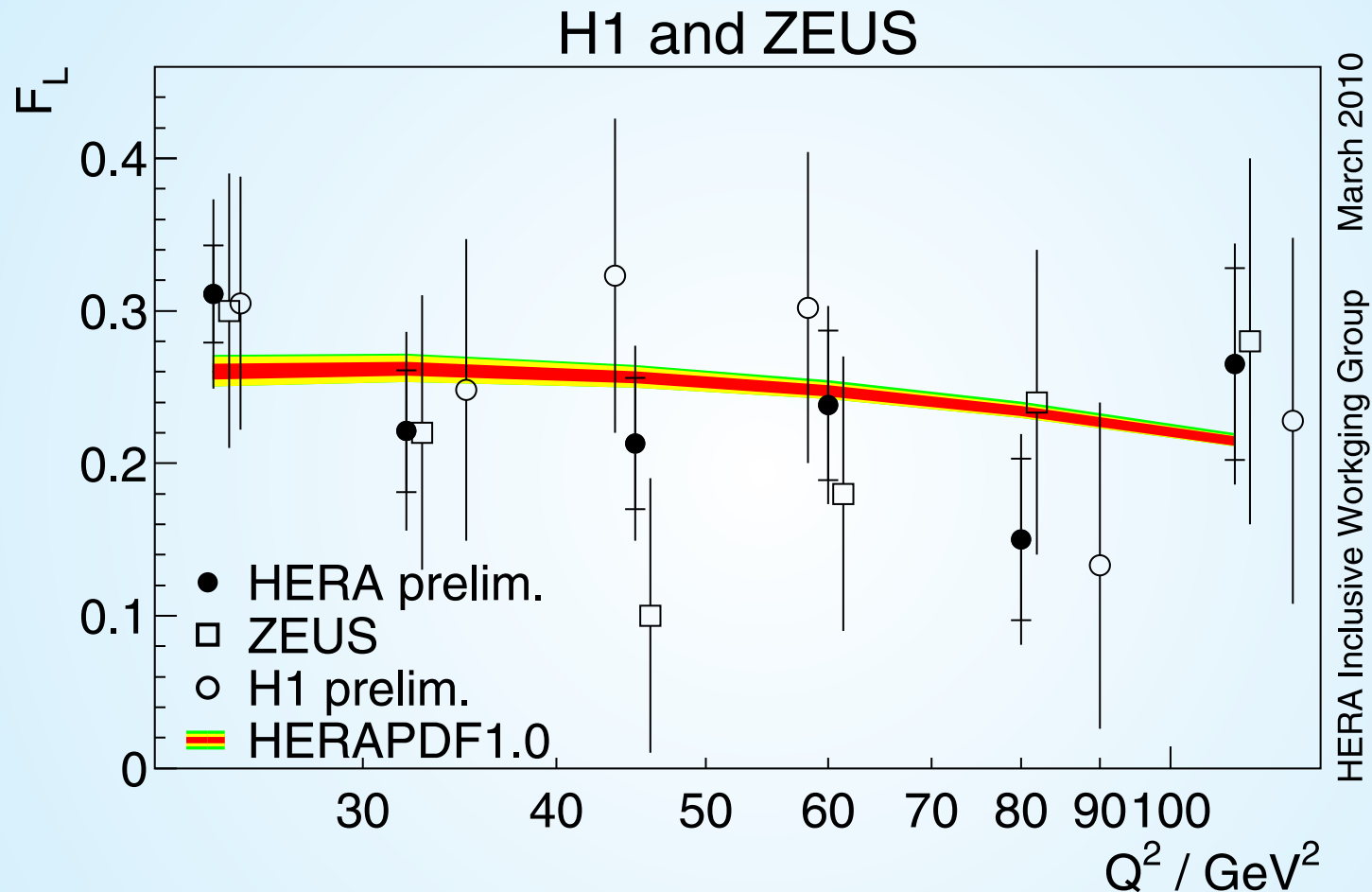


**H1 and ZEUS
combined**

**wide range
of Q^2 and down
to $x \approx 0.00003$**

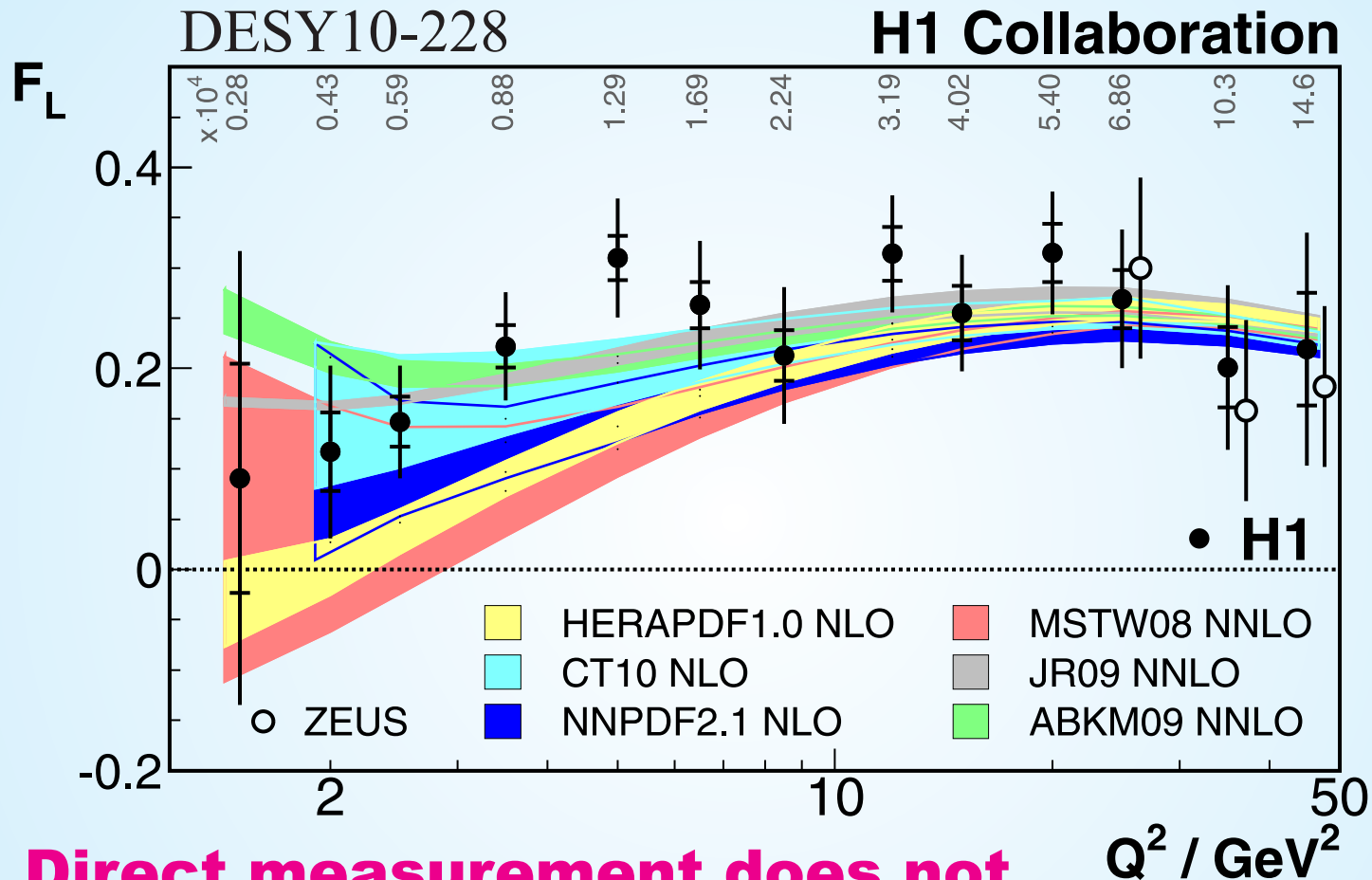
**Fixed Target
could only access
high x region,
where F_L is small.**

Longitudinal Structure Function



It is not zero.

Longitudinal Structure Function



Direct measurement does not contradict PDF predictions.

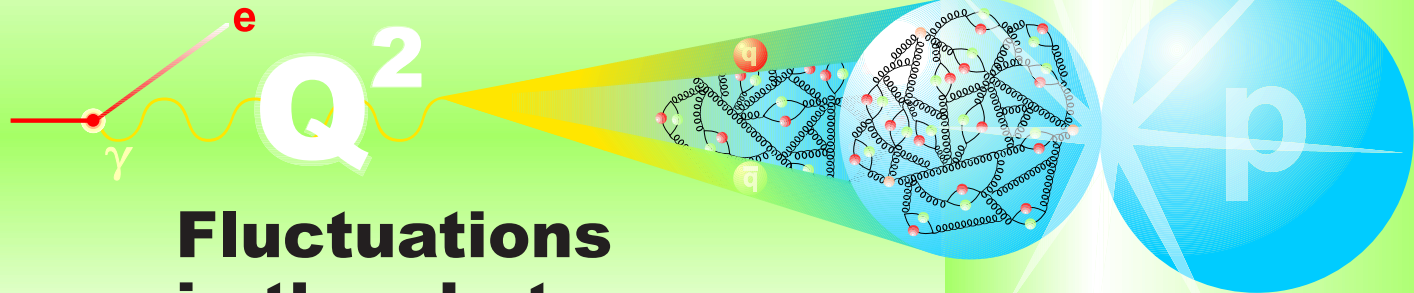
But there is something else.

Low x Partons in the Proton ?

Heisenberg is strictly against it !

That x is a fraction of the proton momentum is only an interpretation.

DESY: B.Liebaug



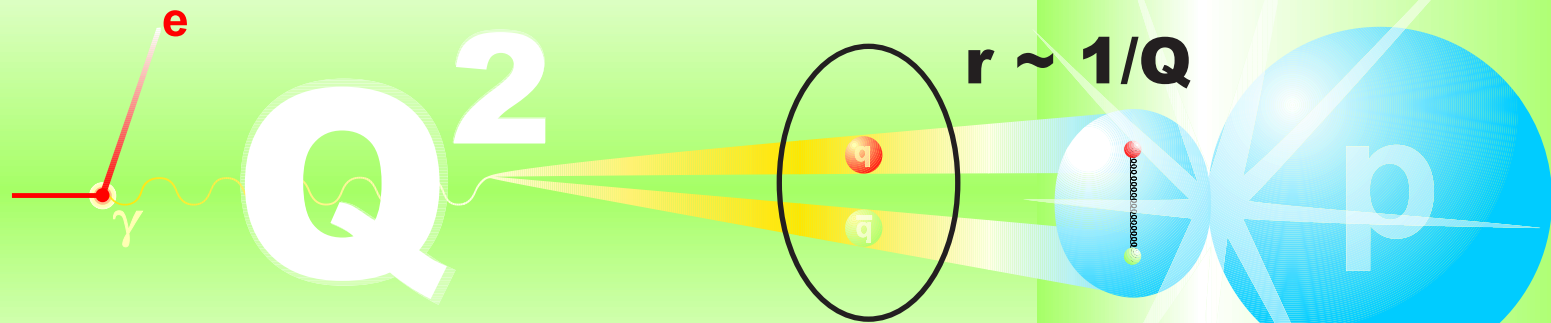
**Fluctuations
in the photon can grow.
For low Q^2 they live long and prosper.**

**Its a parton distribution, but not necessarily
in the proton. Has the parametrisation a meaning?**

Color Dipole Model

Coherence length: l [fm] $\approx 0.1/x$

DESY: B.Liebaug



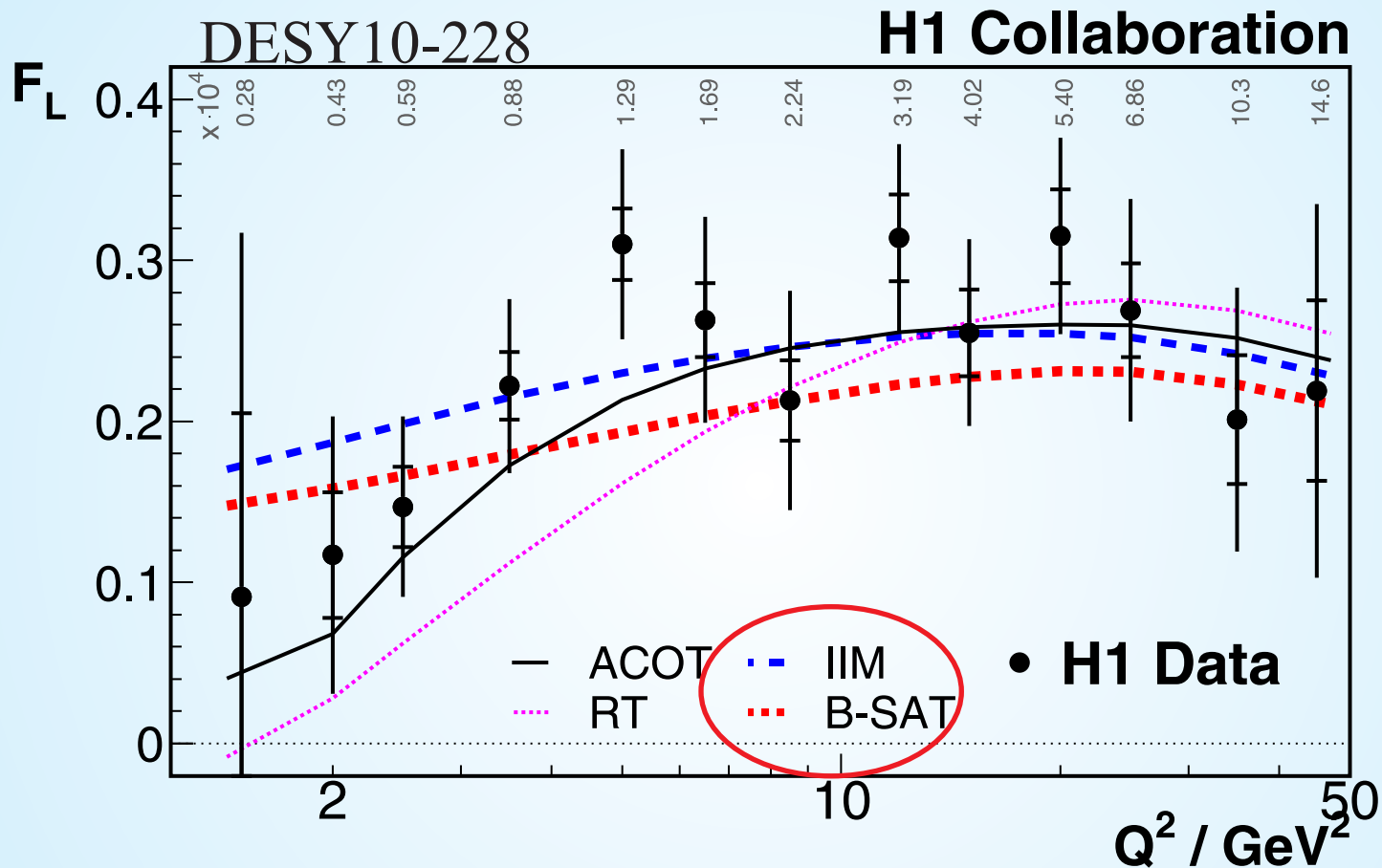
**For high Q^2 only a color dipole forms.
No time for more.**

The fluctuation might forget where it came from.

**Do I get the same PDFs for neutrino - nucleon or
nucleon nucleon scattering? Is factorisation holding?**

SF: Tu 16.30

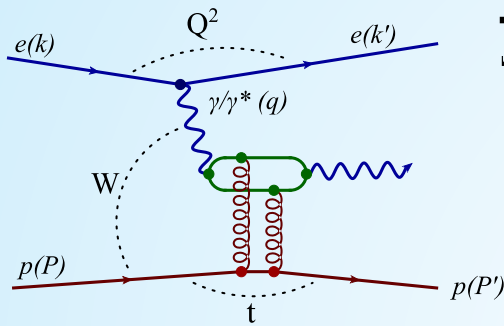
Longitudinal Structure Function



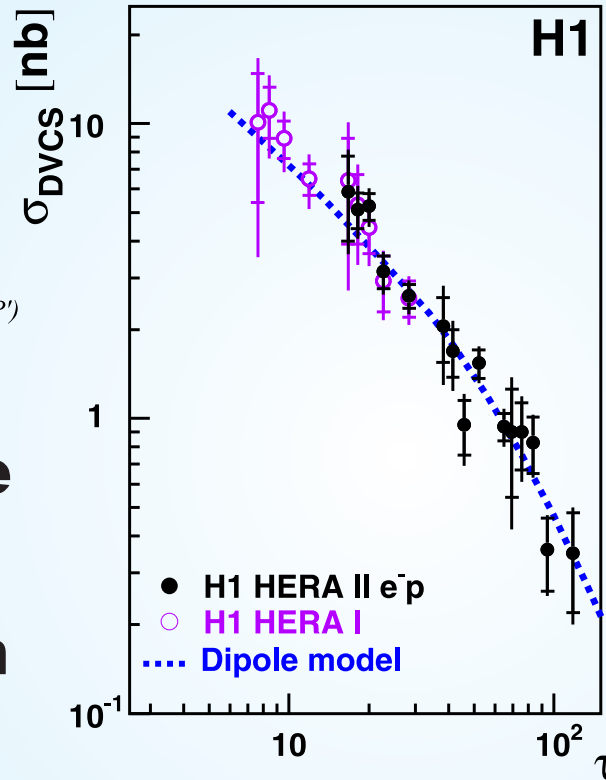
Color dipole models also describe the data.

SF: Tu 16.45

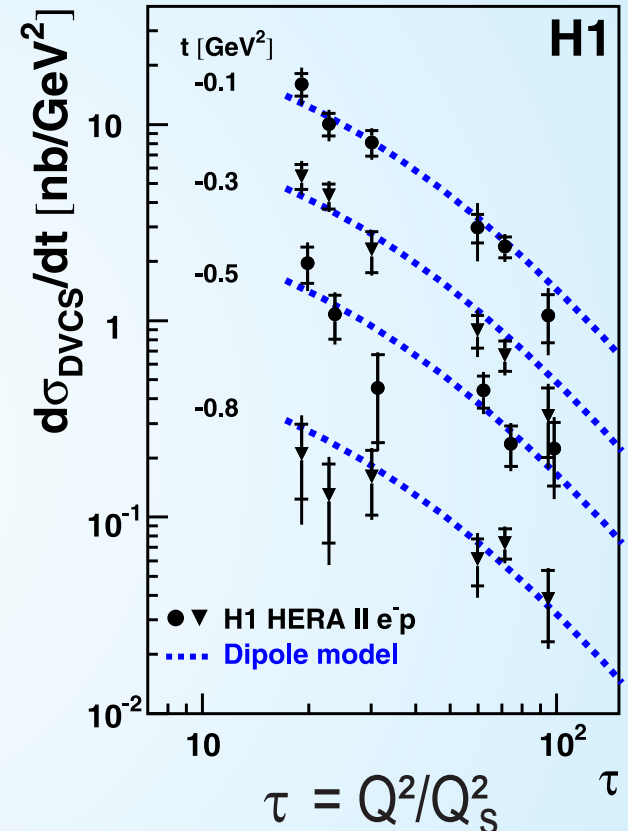
Deeply Virtual Compton Scattering



**t-dependence
of the
cross section
is also of
interest.**



DESY07-142



The dipole model does well.

Deeply Virtual Compton Scattering

**Generalised parton distribution functions
are used for two gluons.**

**Interpretation in longitudinal momentum space
and transverse position space**

$$d\sigma/dt \sim \exp(-b|t|)$$

$$b = 5.45 \pm 0.19 \pm 0.34 \text{ /GeV}^2$$

DESY07-142

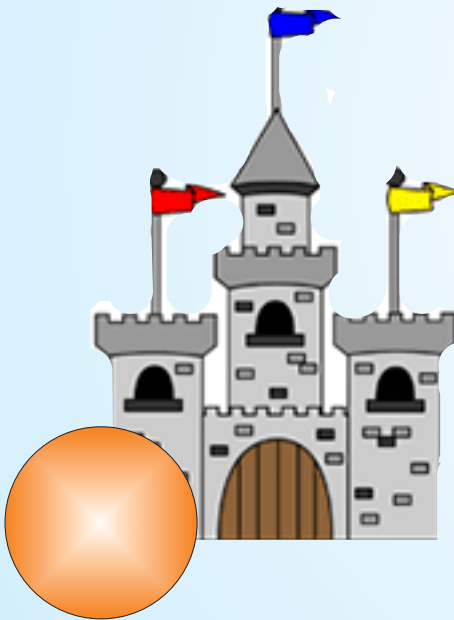
average impact parameter

$$0.65 \pm 0.02 \text{ fm}$$

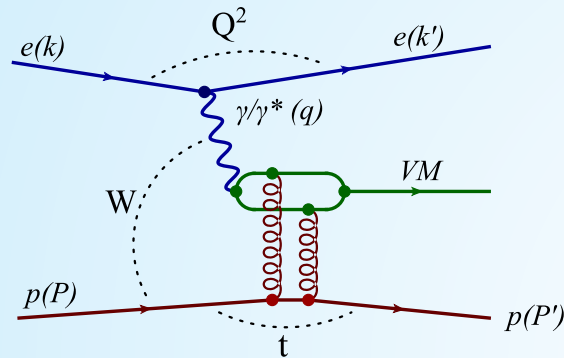
$$x=0.0012$$

**transverse expansion of partons
-- in the proton?**

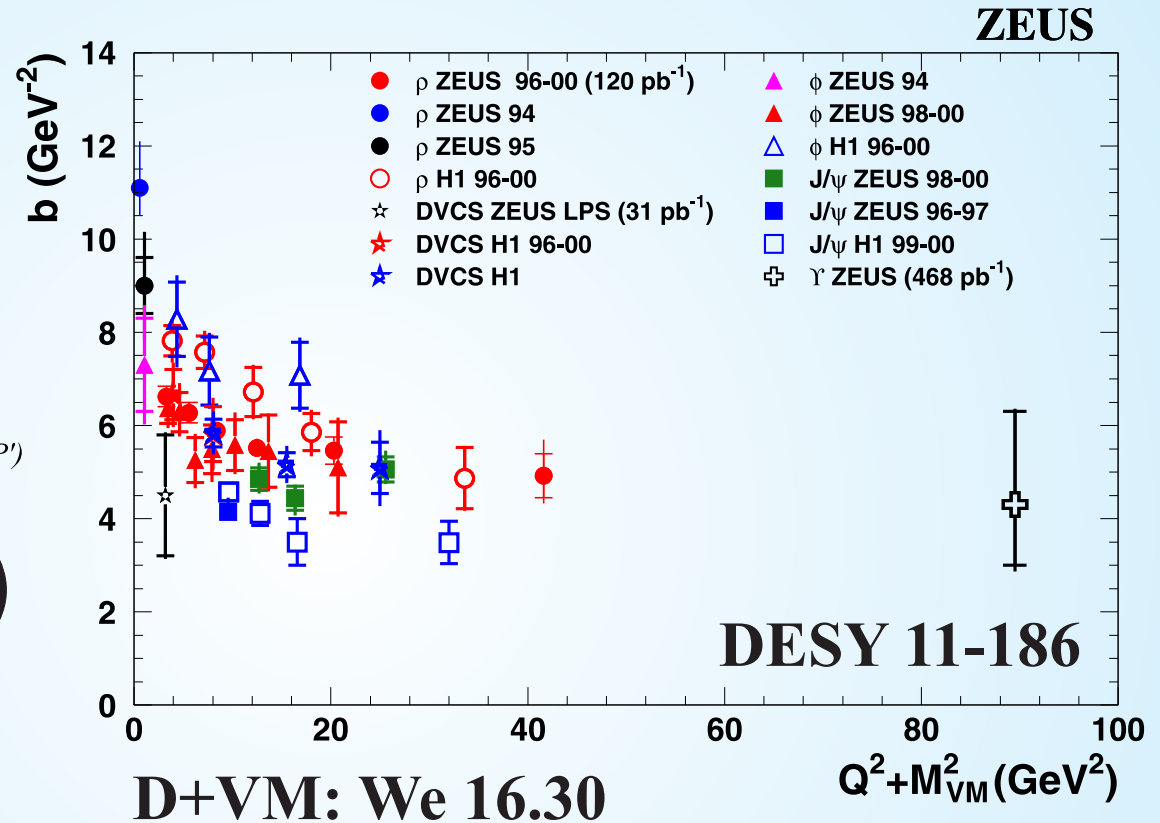
D+VM: We 14.00



t-Slopes for Vector Meson Production



$$d\sigma/dt \sim \exp(-b|t|)$$



Should be analysed with respect to proton size.

More data: D+VM We 15.05, 15.25, 15.45

Proton Size and Dynamics

rms charge radius

electron: 0.8786 ± 0.0069 fm

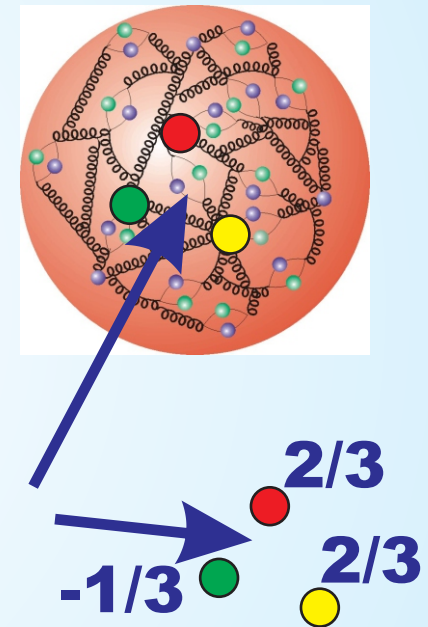
muon: 0.84184 ± 0.00067 fm

rms glue/sea radius

DVCS : 0.65 ± 0.02 fm

What a misleading picture....

dipole moment: $< 0.54 \cdot 10^{-23}$ ecm



Can we measure a dynamic system while averaging over time. Heisenberg again....

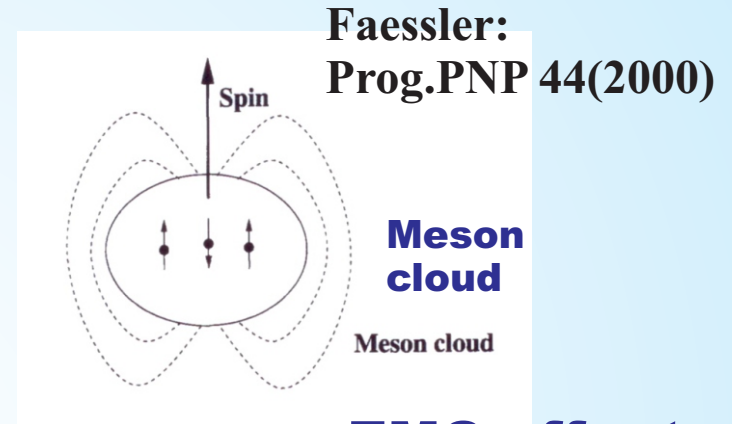
Proton Shape

magnetic moment

$$\mu_p/\mu_N = 2.792847356 \pm 0.000000023$$

$p \rightarrow \Delta$ excitations

[also used for GZK cutoff]



EMC effect



**There has to be some cloud,
otherwise they cannot interact.**

**Can we see the
proton behind the
strong field?**

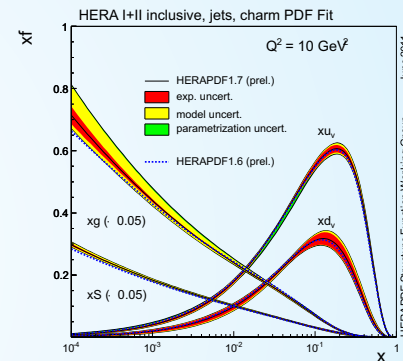
Summary

The proton still holds a lot of secrets.

Proton PDFs are getting measured with high precision, HERA was a success.

This allows for effective predictions and thus searches.

The interpretation of proton PDFs is not trivial.



There is more to the proton than PDFs.

There are many questions about size, shape and the spatial distribution of quarks and glue.

It might take more than pQCD to understand the proton.

Outlook

**HERA data will be used to the last bite.
LHC and new fixed target experiment
will join in and we will have perfect
PDFs.**

**Different communities will join and
we will have a 3d picture of the
valence, sea and glue structure of the proton.**



**We open the door
and look inside.**

That is my vision.

