

# Perturbative and non-perturbative diffraction at HERA



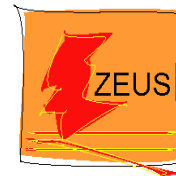
Marcella Capua  
Calabria University and INFN



On behalf of the



and



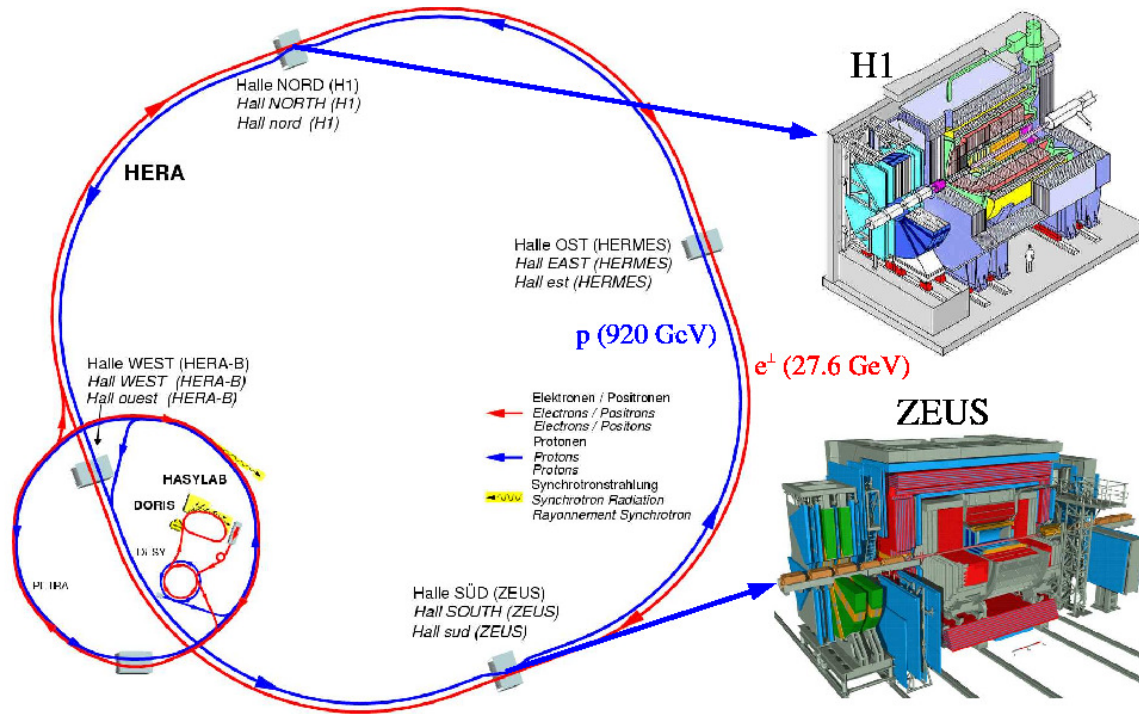
Collaborations

Physics in Collisions 2010

Karlsruhe, Germany, September 1-4 2010

# HERA colliding experiments

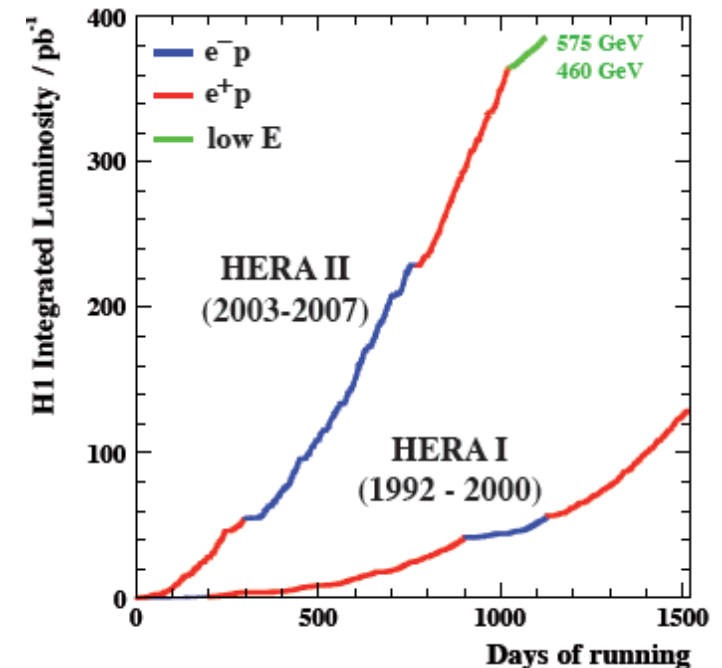
27.5 GeV leptons on 920 GeV protons



Detectors not originally designed for diffractive physics. Forward instrumentation added:

- ZEUS LPS for HERA I only
- H1 FPS for HERA I and II
- H1 VFPS for HERA II

HERA I + HERA II  $\sim 0.5 \text{ fb}^{-1}$



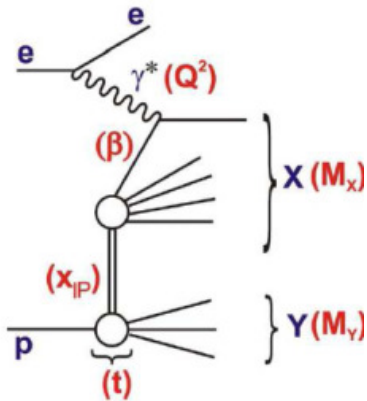
Lots of results achieved in diffraction at HERA:

- ✓ Inclusive diffraction
  - ✓ Exclusive diffraction
  - ✓ Leading Baryons
- and many analyses ongoing



# Kinematic variables

## Standard DIS variables



$W$  =  $\gamma^*$ -proton centre of mass energy

$Q^2$  =  $\gamma^*$  4-momentum squared

$x$  = fraction of proton's momentum carried by struck quark  $\approx Q^2/W^2$

## Diffractive variables

$t$  = squared 4-momentum transfer at proton vertex =  $(p-p')^2$

$x_{IP}$  = fraction of the  $p$  mom carried by the  $IP$   $x_{IP} = \frac{q \cdot (p - p')}{q \cdot p} \approx \frac{Q^2 + M_X^2}{Q^2 + W^2}$

$\beta$  = fraction of the  $IP$  mom carried by the struck quark  $\beta = \frac{Q^2}{2q \cdot (p - p')} \approx \frac{Q^2}{Q^2 + M_X^2} = \frac{x}{x_{IP}}$

reduced cross section

diffractive structure function

$$\frac{d^4 \sigma}{d\beta dQ^2 dx_{IP} dt} = \frac{4\pi\alpha^2}{\beta Q^4} \left[ 1 - y + \frac{y^2}{2} \right] \sigma_r^{D(4)}(\beta, Q^2, x_{IP}, t) \quad \sigma_r^{D(4)}(\beta, Q^2, x_{IP}, t) = F_2^{D(4)} - \frac{y^2}{2(1-y+y^2/2)} F_L^{D(4)}$$

$F_2^{D(3)}$  integrated over  $t$  needed for LRG comparisons

# Selection methods

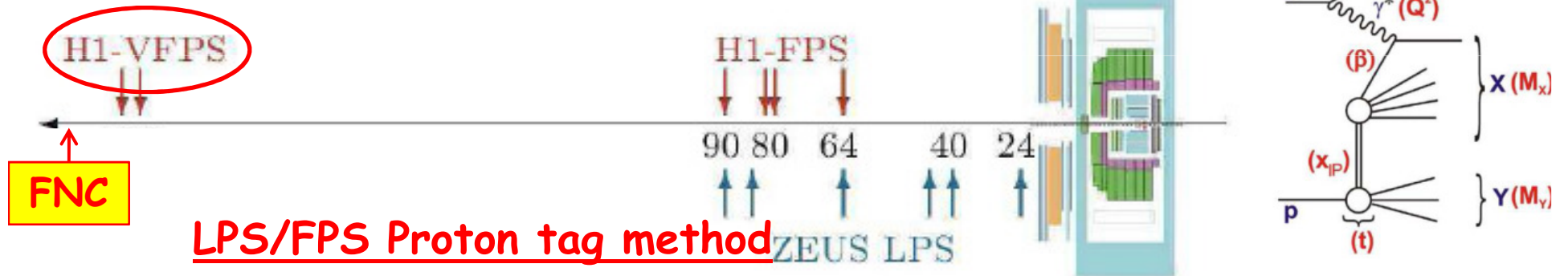
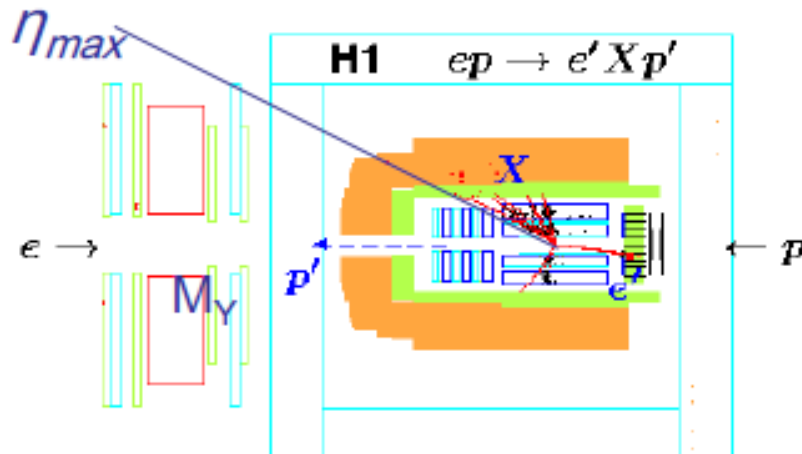
## LRG method

Large rapidity gap method (H1 and ZEUS):

→ No activity in the forward direction

High statistics, p-diss (~20%)

Measurements integrated over  $t$



## LPS/FPS Proton tag method

Dedicated detectors:

ZEUS-LPS for HERA I only

H1-FPS for HERA I and II

H1-VFPS for HERA II

Low statistics but no p-diss bkg and  $M_y = m_p$

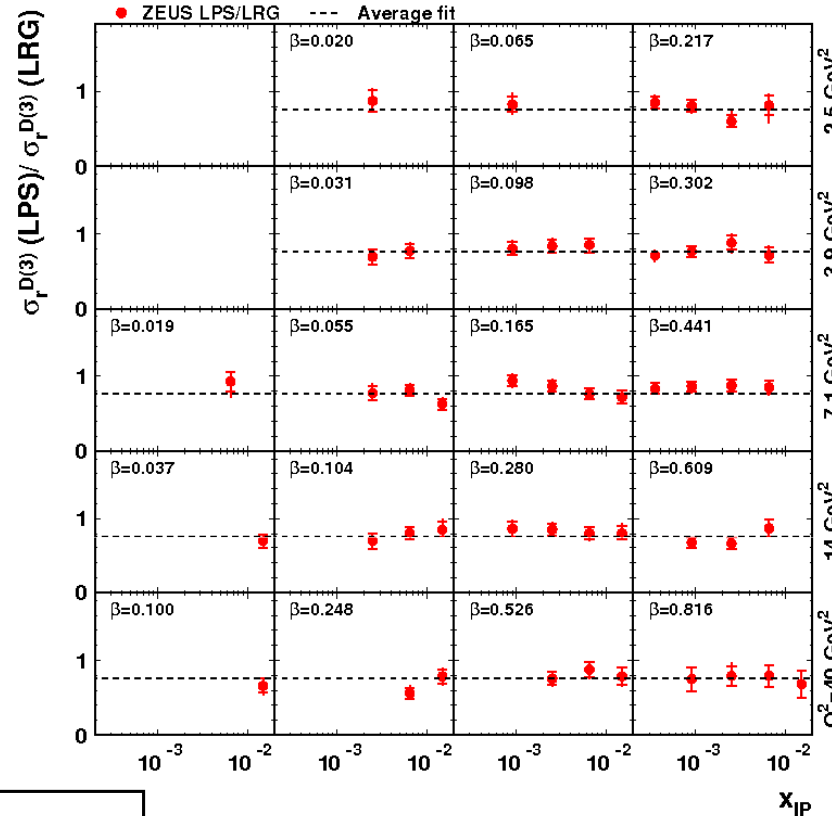
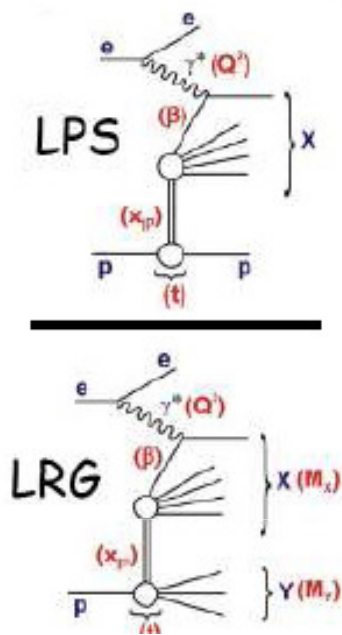
Measurements of  $x_{IP}$  and  $t$

Methods comparison



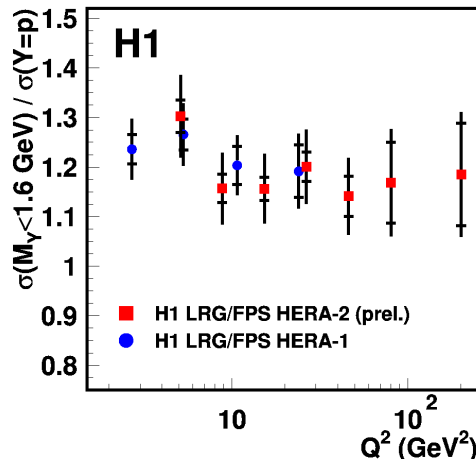
# Comparison between methods

## ZEUS



ZEUS estimate of p-diss fraction about 20%

No significant dependence on  $\beta$ ,  $Q^2$  and  $x_{IP}$



Same conclusions from H1  
 Combining FPS HERA I and HERA II  
 data p-diss contribution about 20%  
 (H1prelim-09-012)

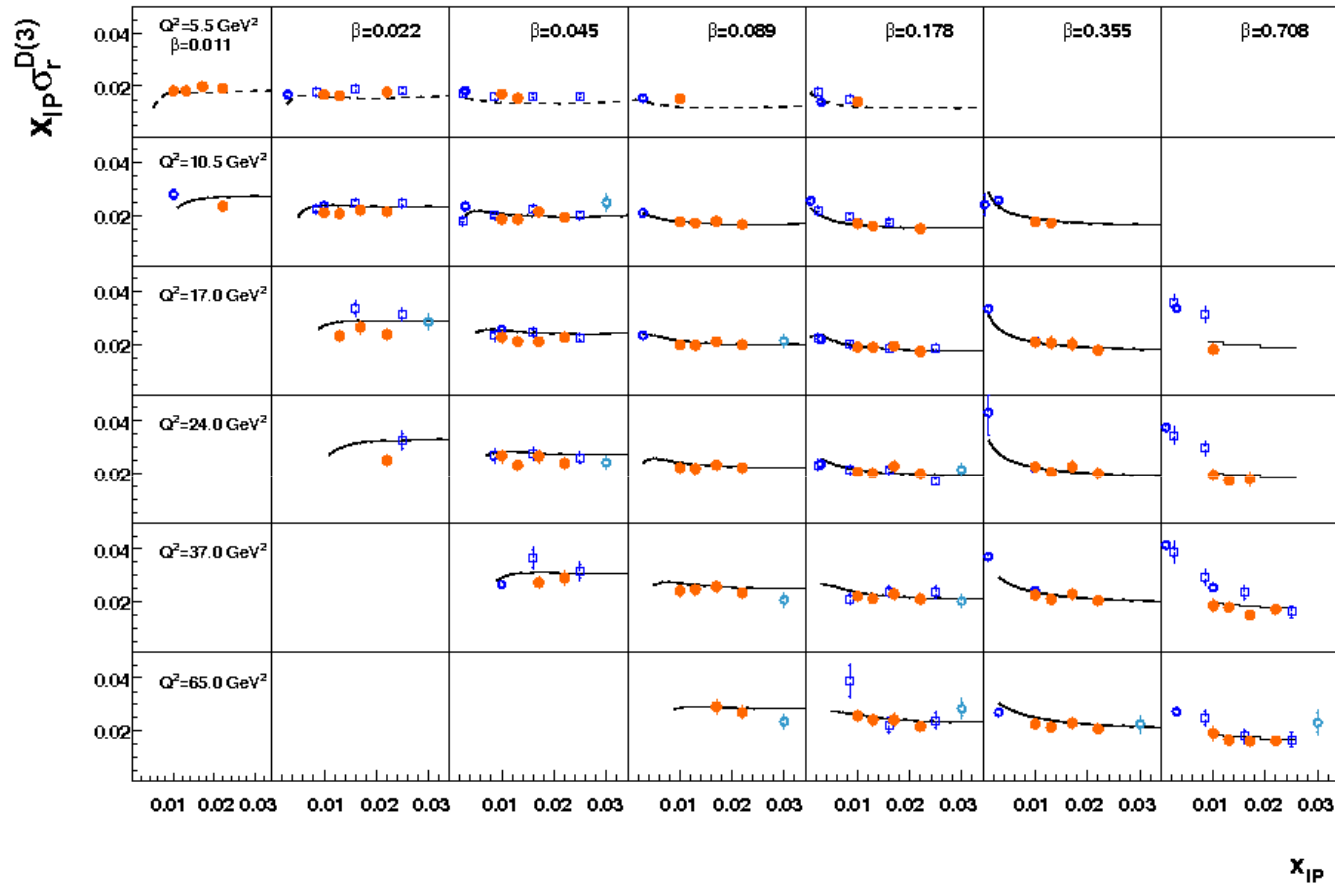
New measurements from H1!



# First results from H1 VFPS

H1 PRELIMINARY

- H1 VFPS Preliminary
- H1 FPS Preliminary
- H1 LRG Preliminary x 0.81
- H1 LRG Published x 0.81
- H1 2006 DPDF Fit B x 0.81
- - - H1 2006 DPDF Fit B x 0.81 (extrapol.)



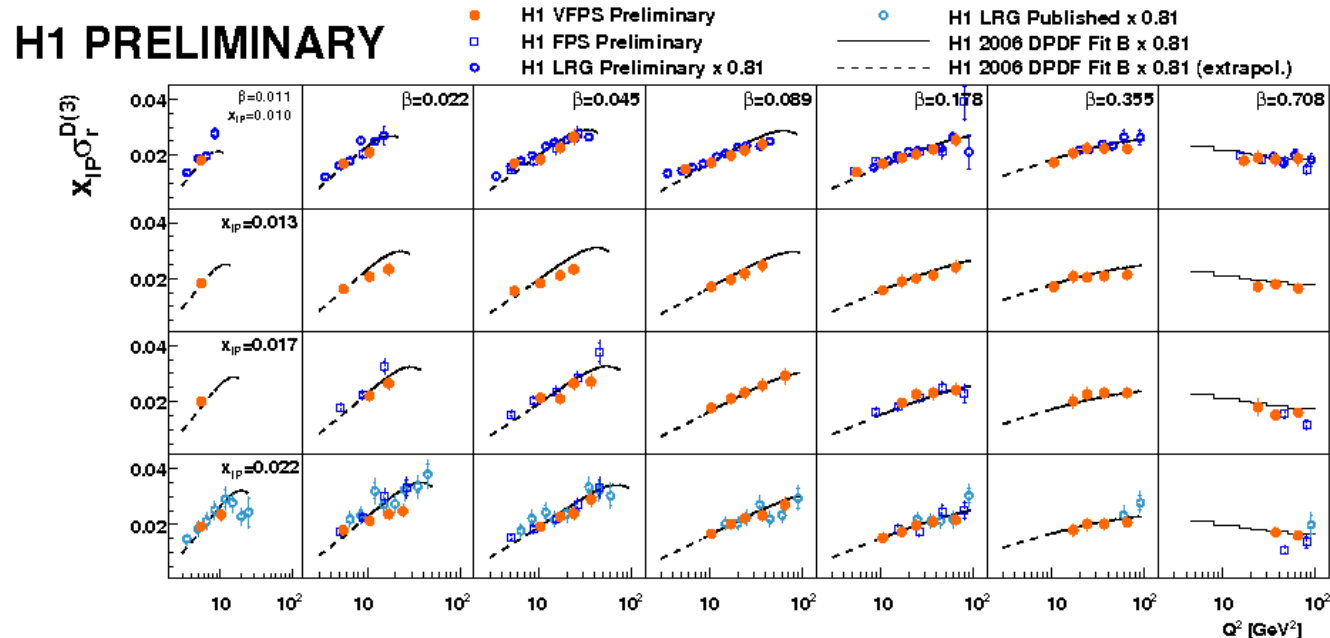
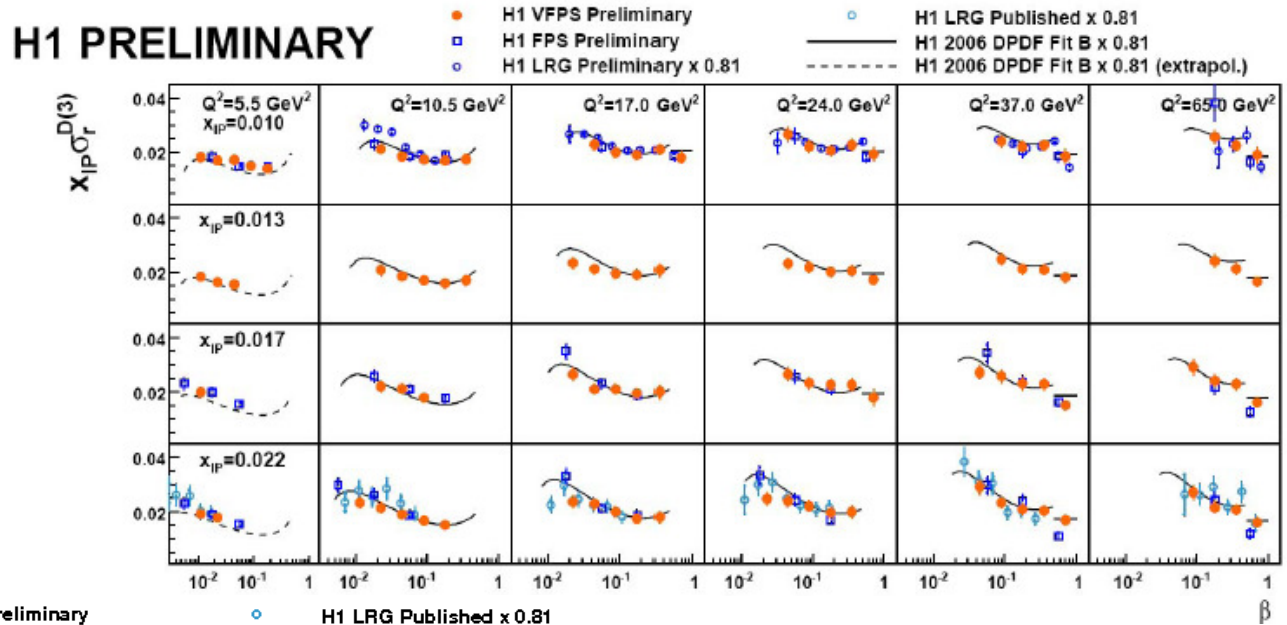
New results released!

- VFPS:**  
(H1-prelim-10-14)  
 $5 < Q^2 < 100 \text{ GeV}^2$   
 $95 \text{ pb}^{-1}$
- FPS:**  
(H1-prelim-10-12)  
 $5 < Q^2 < 200 \text{ GeV}^2$   
 $157 \text{ pb}^{-1}$
- LRG:**  
(H1-prelim-10-11)  
 $Q^2 > 3.5 \text{ GeV}^2$   
 $370 \text{ pb}^{-1}$

**VFPS:** Covers complementary  $x_{IP}$  range w.r.t. LRG analysis, 20 times higher statistics than HERA I data, VFPS normalisation uncertainty 5%, low background contamination < 2%

All the measurements in agreement with H1 2006 DPDF fit B

# First results from H1 VFPS



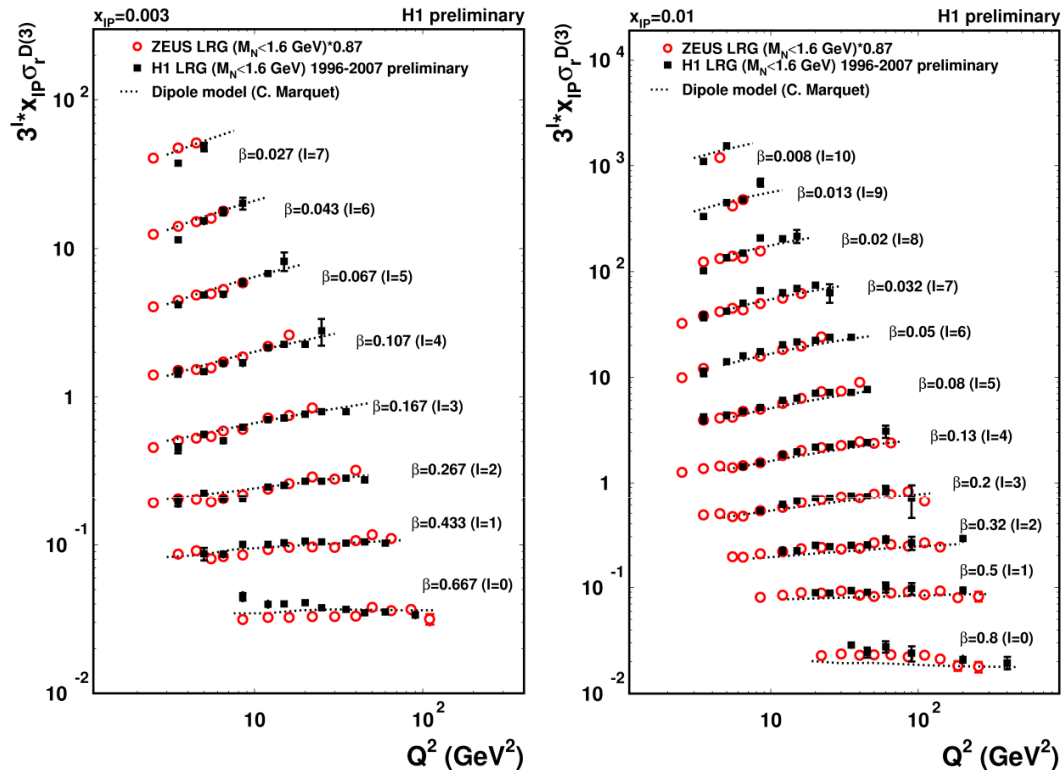
Positive scaling  
violations visible:  
a lot of gluons in DDIS

All the measurements in agreement with H1 2006 DPDF fit B

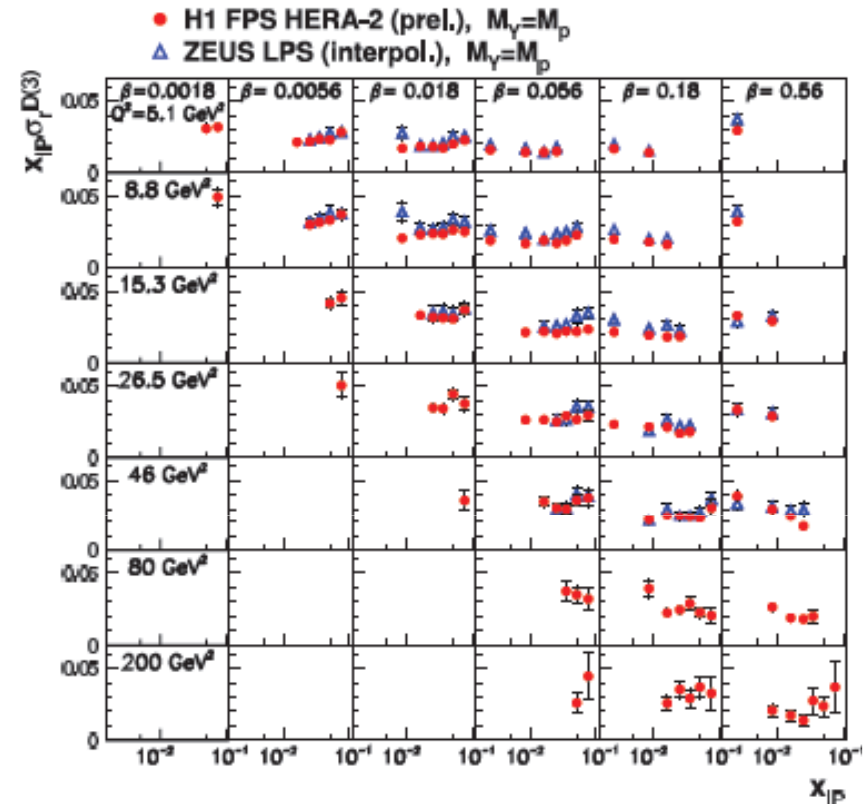


# Comparison between experiments

## LRG



## LPS/FPS



ZEUS LRG  $62 \text{ pb}^{-1}$  pub. (High stat precision)  
 Compared with new prel H1 LRG  $370 \text{ pb}^{-1}$   
 13% difference in overall normalisation  
 compatible within uncertainties

Good agreement, 15%  
 difference in overall  
 normalisation compatible  
 within uncertainties

Both H1 and ZEUS inclusive data used to extract DPDFs

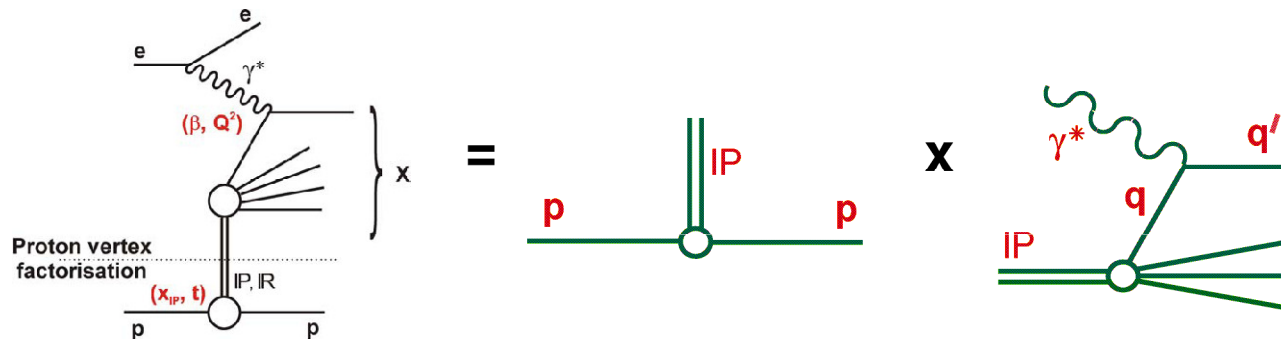


# Diffractive PDFs

QCD collinear factorization theorem proved also for DDIS (Collins 1998):

$$\sigma(\gamma^* p \rightarrow Xp) \approx f_i(z, Q^2, x_{IP}, t) \otimes \hat{\sigma}_{\gamma^* i}(z, Q^2)$$

variables describing proton vertex ( $x_{IP}, t$ ) factorize from those at photon vertex ( $\beta, Q^2$ ) to good approximation



$$\sigma(\gamma^* p \rightarrow Xp) \approx \underbrace{f_{IP}(x_{IP}, t)}_{\text{Regge motivated pomeron flux}} \times \underbrace{f_i(z, Q^2)}_{\text{DPDFs}} \otimes \hat{\sigma}_{\gamma^* i}(z, Q^2)$$

Regge motivated pomeron flux:  $f_{IP}(x_{IP}, t) = \frac{e^{Bt}}{x_{IP}^{2\alpha(t)-1}}$

$$\alpha_{IP}(t) = \alpha_{IP}(0) + \alpha'_{IP} t$$

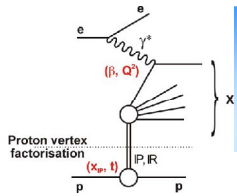
DPDFs:

Universal partonic distribution function, obey evolution equations, apply when vacuum quantum numbers are exchanged

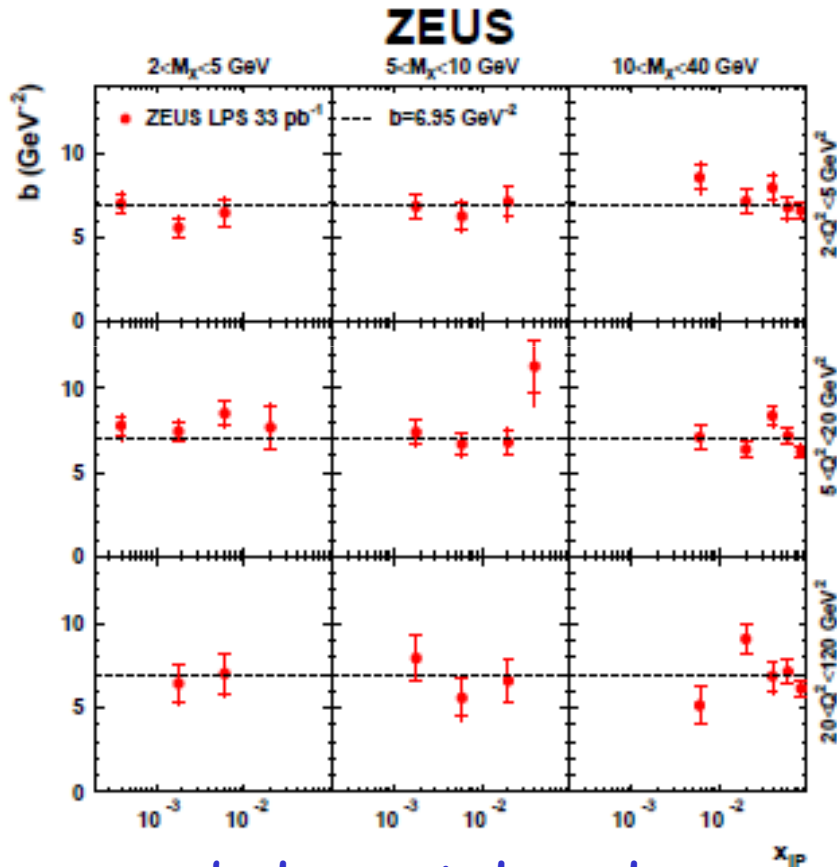
B and  $\alpha(t)$  extracted from HERA data

$z$  is a generalisation of  $\beta$ : fraction of the  $IP$  mom carried by the struck parton

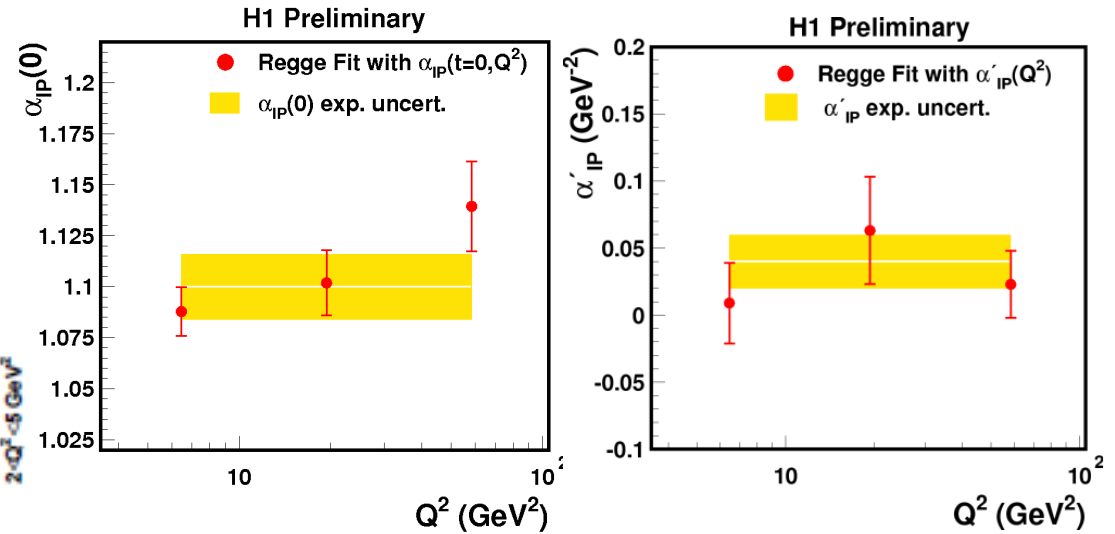
# Proton vertex factorization: $f_{IP}(x_{IP}, t)$



$$\frac{d\sigma}{dt} \propto e^{-bt}$$



**b does not depend  
on  $\beta$ ,  $Q^2$  at fixed  $x_{IP}$ :  
consistent with factorization**



**Regge fit results:**

**ZEUS:**

$$\alpha_{IP}(0) = 1.11 \pm 0.02(\text{stat.}) \pm 0.02(\text{syst.}) \pm 0.02(\text{mod})$$

$$\alpha'_{IP} = -0.01 \pm 0.06(\text{exp.})^{+0.04}_{-0.08}(\text{syst.}) \pm 0.04(\text{mod.}) \text{ GeV}^{-2}$$

$$b = 7.1 \pm 0.7(\text{stat.})^{+1.4}_{-0.7}(\text{syst}) \text{ GeV}^{-2}$$

**H1-FPS:**

$$\alpha_{IP}(0) = 1.10 \pm 0.02(\text{exp.}) \pm 0.02(\text{mod.})$$

$$\alpha'_{IP} = 0.04 \pm 0.02(\text{exp.}) \pm 0.03(\text{mod.}) \text{ GeV}^{-2}$$

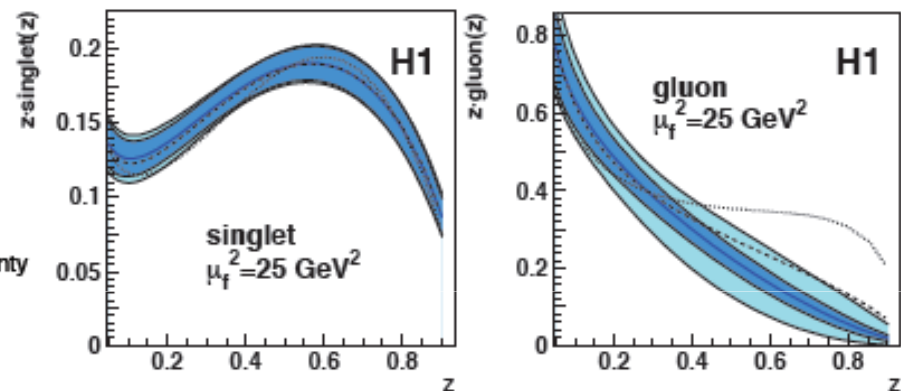
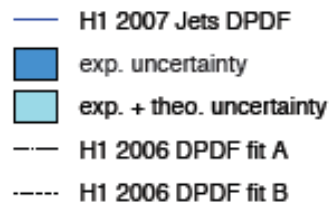
$$b = 5.7 \pm 0.3(\text{exp.}) \pm 0.6(\text{mod.}) \text{ GeV}^{-2}$$

**DL:**  $\alpha_{IP}(t) = 1.08 + 0.25t$

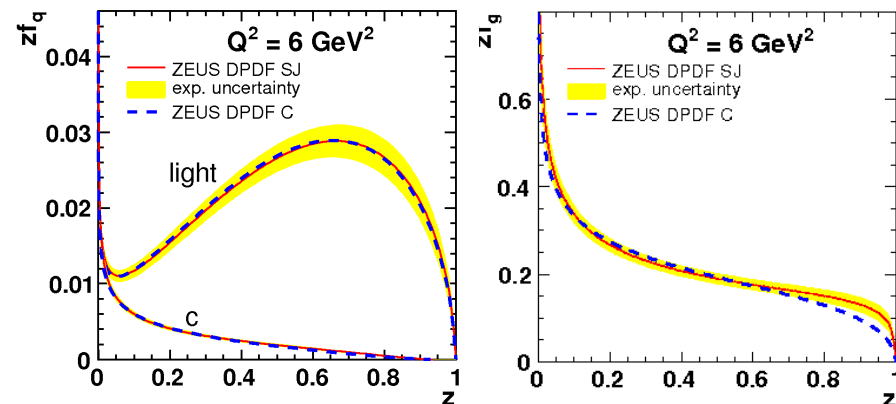
# HERA Diffractive Parton densities

The vertex factorisation allow to extract DPFs fitting  $\beta, Q^2$  dependance at fixed  $x_{IP}$  from a fit to the HERA data (inclusive+jets): evolution in  $Q^2$  with DGLAP equations, parameterise  $q$  and  $g$  densities at initial scale  $Q_0^2$

Combining inclusive and dijet data constrains  $g$  and  $q$  densities with comparable precision for all  $z$



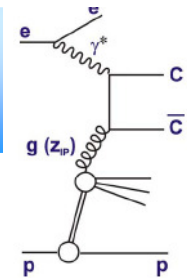
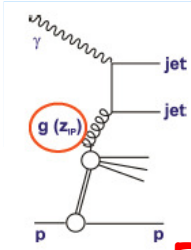
Reasonable agreement ZEUS and H1  
A final data set of inclusive data is now available from H1 and ZEUS: plan to extract HERA DPDFs from the H1+ZEUS combined (reduction of exp. uncertainties)



H1: EPJ C48 (2006) and JHEP 710 (2007).

ZEUS: NPB 816 (2009) and EPJ C52 (2007)

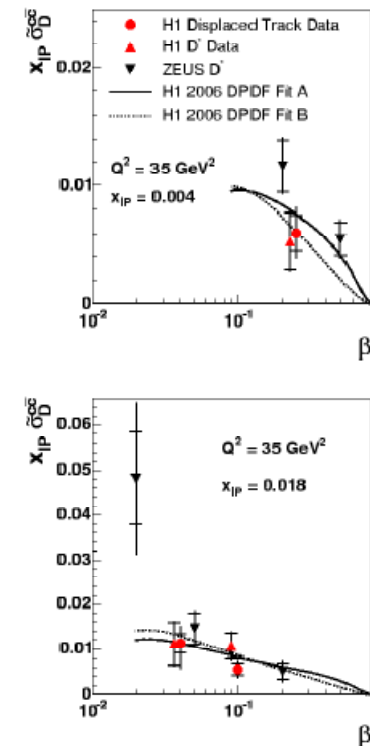
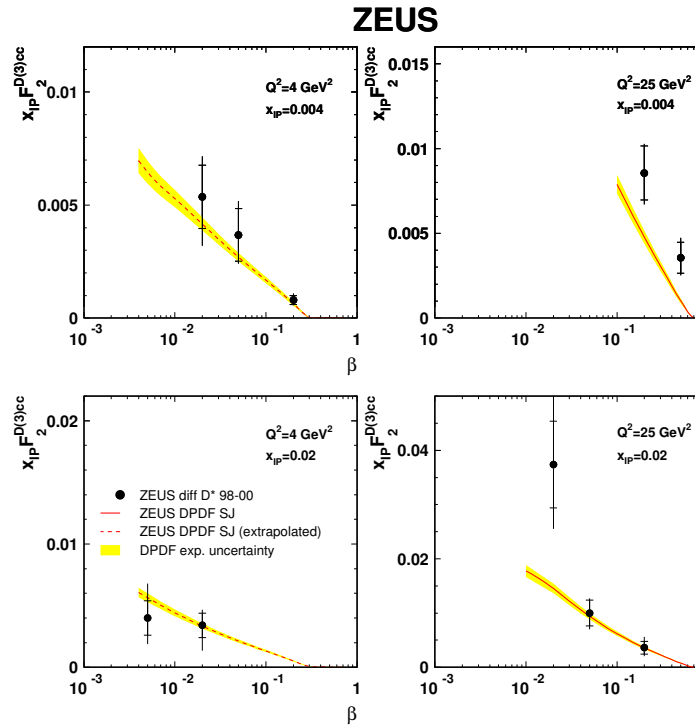
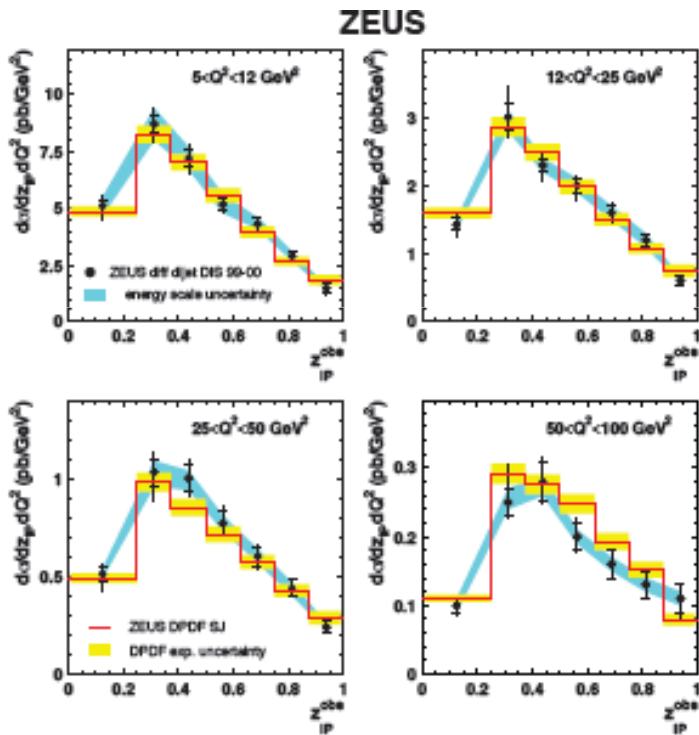
# Several QCD factorisation tests...



Final states with a hard scale, sensitive to gluons are a good test!

## Dijets in DIS

## Charm in DIS



ZEUS DPDF SJ and H1 Fit describe well the diffractive Dijets and charm production data (although still statistically limited)

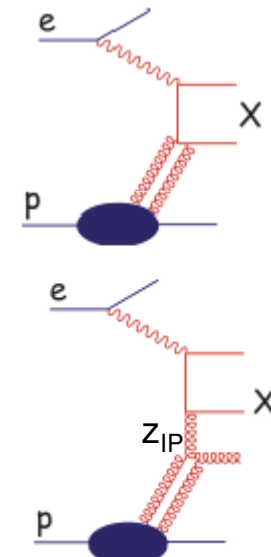
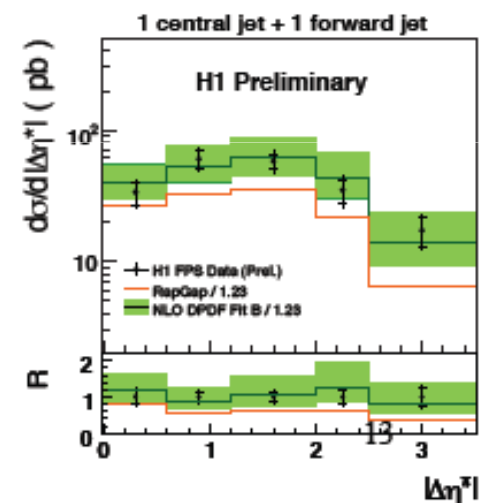
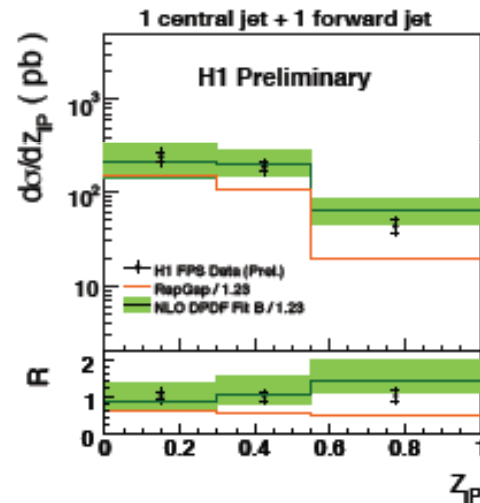
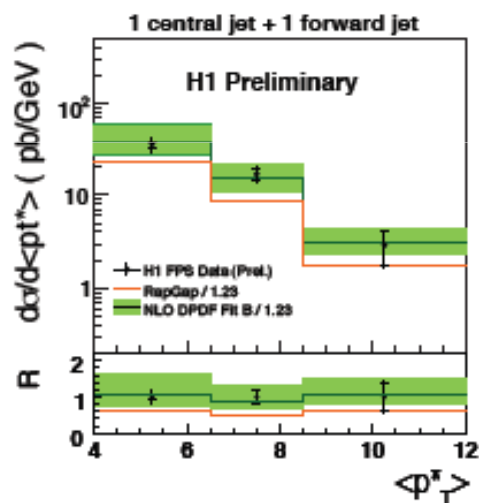
The factorization holds in DDIS!

# Forward jets in DDIS

1 central jet + 1 forward jet + FPS proton

New H1 results on DDIS using FPS in a wider  $x_{IP}$  and  $\eta_{jet}$  range

No evidence for effects beyond NLO DGLAP (pQCD contributions breaking DGLAP  $p_T$  ordering at low  $x \rightarrow$  BFKL)

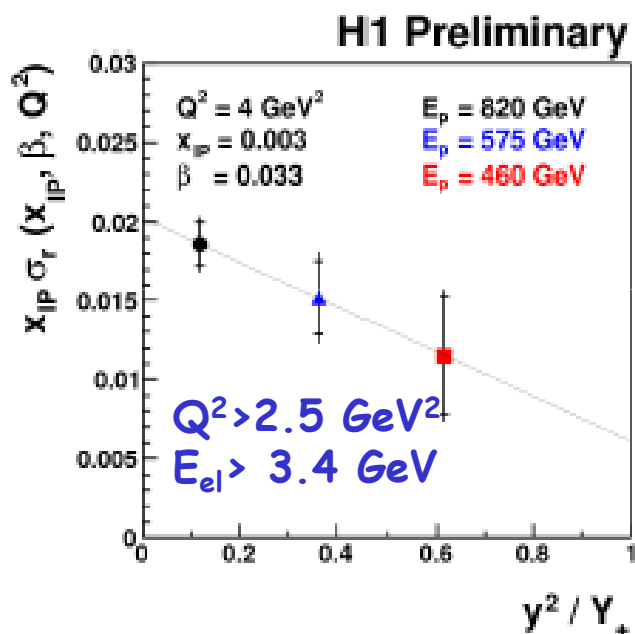


(H1 prelim-10-013)

# New $F_L^D$ measurements at low $Q^2$

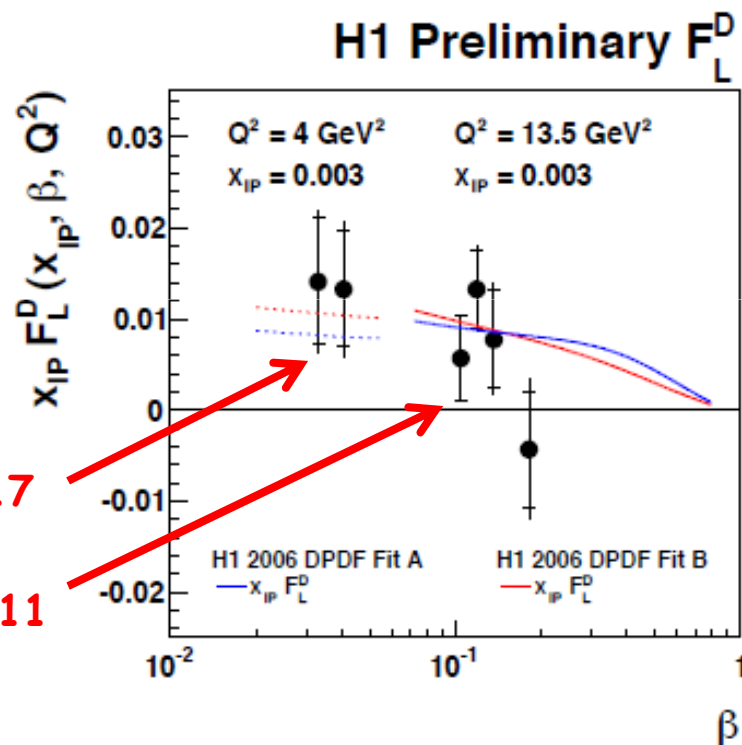
At fixed  $\beta, Q^2$  and  $x_{IP}$   $F_L^D$  can be extract with a linear fit

$$\sigma_r^{D(3)}(\beta, Q^2, x_{IP}) = F_2^{D(3)}(\beta, Q^2, x_{IP}) - \frac{y^2}{Y^+} F_L^{D(3)}$$



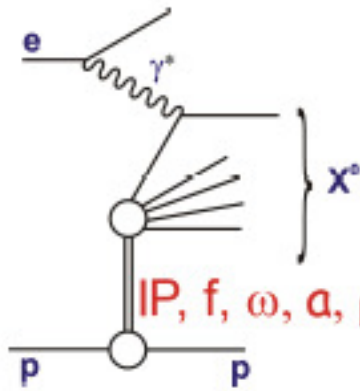
H1 prelim-10-017

H1 prelim-09-011

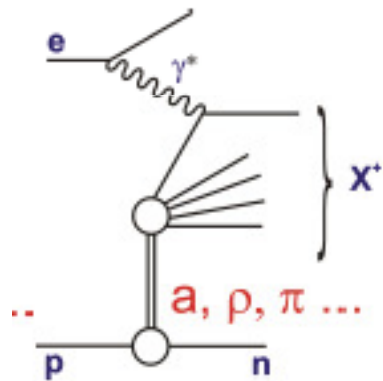


- $F_L^D$  probes directly the diffractive gluon density
- Measurements are consistent with NLO QCD fits

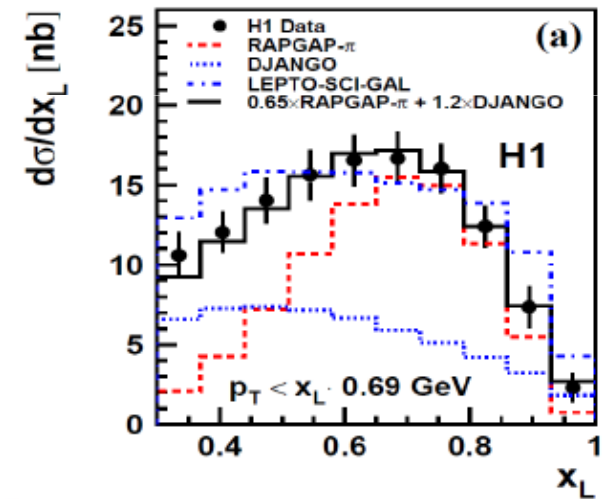
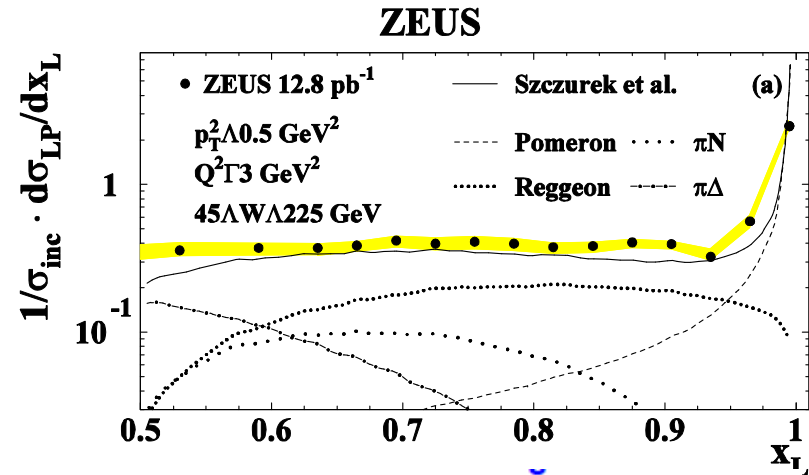
# Leading Baryon



LP produced via exchange IP, IR,  $\pi^0$ . IR exchange dominates at medium  $x_L$



LN produced via charged exchange reactions  $\pi^+$ ,  $\rho^+$ ,  $a_2$ . Dominated at large  $x_L$  by  $\pi^+$  exchange and at low  $x_L$  by standard baryon fragmentation

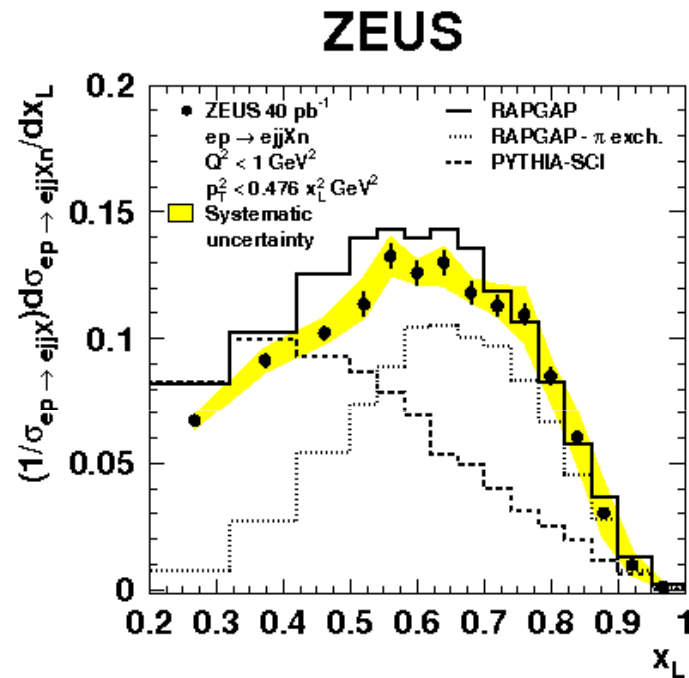


$x_L = 1 - x_{IP}$   
fraction of the p mom carried by the LB

- ZEUS: LP DESY 08-176 [JHEP06\(2009\)074](#)
- LN DESY 09-139 [Nucl. Ph. B 827 \(2010\) 1-33](#)
- LN DESY 07-011 [Nucl. Ph. B 776 \(2007\) 1-37](#)
- H1: LN DESY-09-185
- LN H1-prelim 10-113



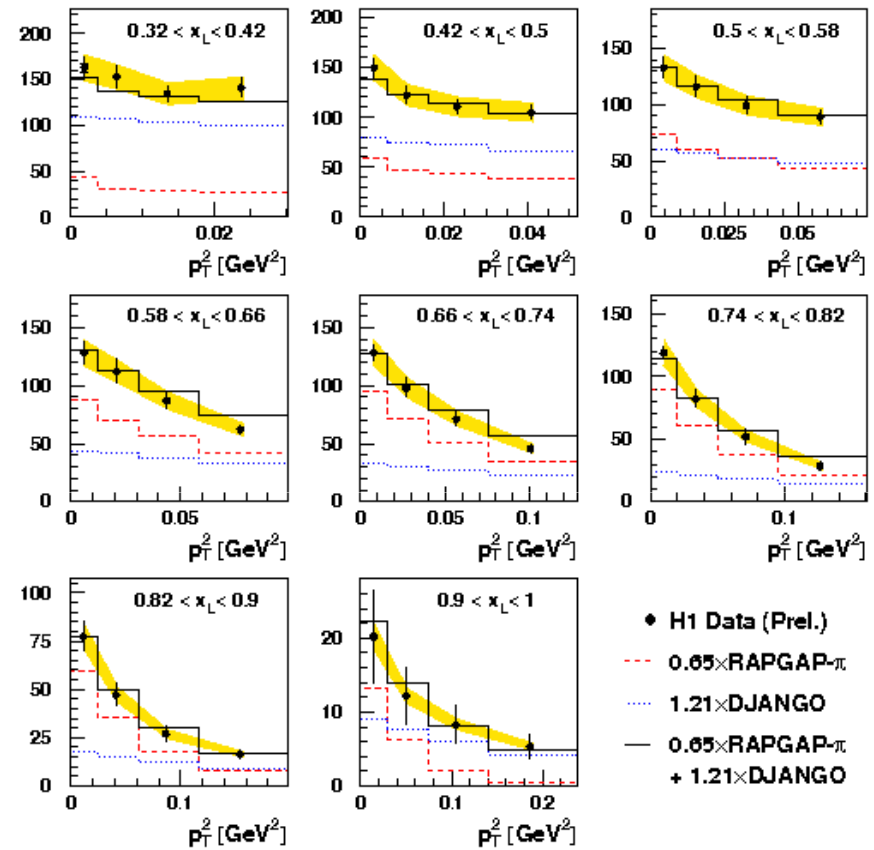
# LN $x_L$ and $p_T$ distributions



ZEUS pub-09-139  
LN+Dijets PHP

$d^2\sigma/(dx_L dp_T^2)$  [nb/GeV<sup>2</sup>]

H1 Preliminary



H1 prelim-10-113  
6 < Q<sup>2</sup> < 100 GeV<sup>2</sup>

MC mix of  $\pi$ -exchange and standard fragmentation gives a good description of  $x_L$  and  $p_T$  dependences for inclusive neutrons and dijets+neutrons

# LN structure function

$$\sigma_r^{LN(3)}(\beta, Q^2, x_L) = F_2^{LN(3)}(\beta, Q^2, x_L) - \frac{y^2}{Y^+} F_L^{LN(3)}$$

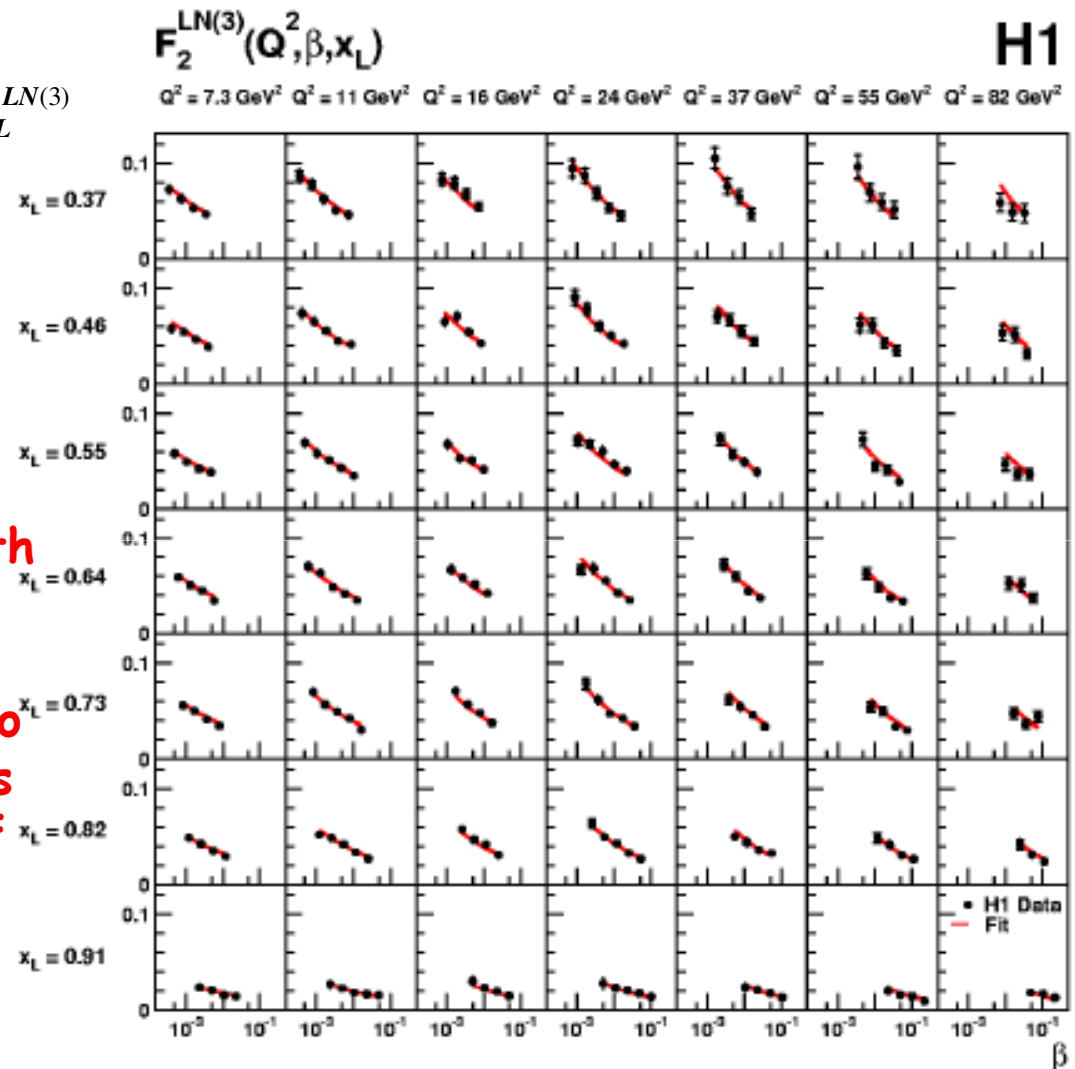
Assuming p vertex factorisation:

$$F_2^{LN(3)}(\beta, Q^2, x_L) = f(x_L) \cdot F_2^{LN(3)}(\beta, Q^2)$$

Fitting  $F_2^{LN}$  with  $\sim \beta^{-\lambda}$  :

$\lambda$  independent to  $x_L$  (consistent with vertex factorisation)

- $\lambda$  increases with  $Q^2$  from 0.23 to 0.3 (similar of proton  $F_2$ ) which is consistent with the hypothesis of limiting fragmentation



# Pion structure function

Assuming proton vertex factorisation and the dominance of  $\pi^+$ -exchange at high  $x_L$  we estimate pion structure function from  $F_2^{LN(3)}$  at  $0.68 < x_L < 0.77$

$$F_2^\pi(\beta, Q^2) = F_2^{LN(3)}(\beta, Q^2, x_L) / \Gamma_\pi(x_L)$$

$$\Gamma_\pi = \int f_{\pi/p}(x_L = 0.73, t) dt \approx 0.13$$

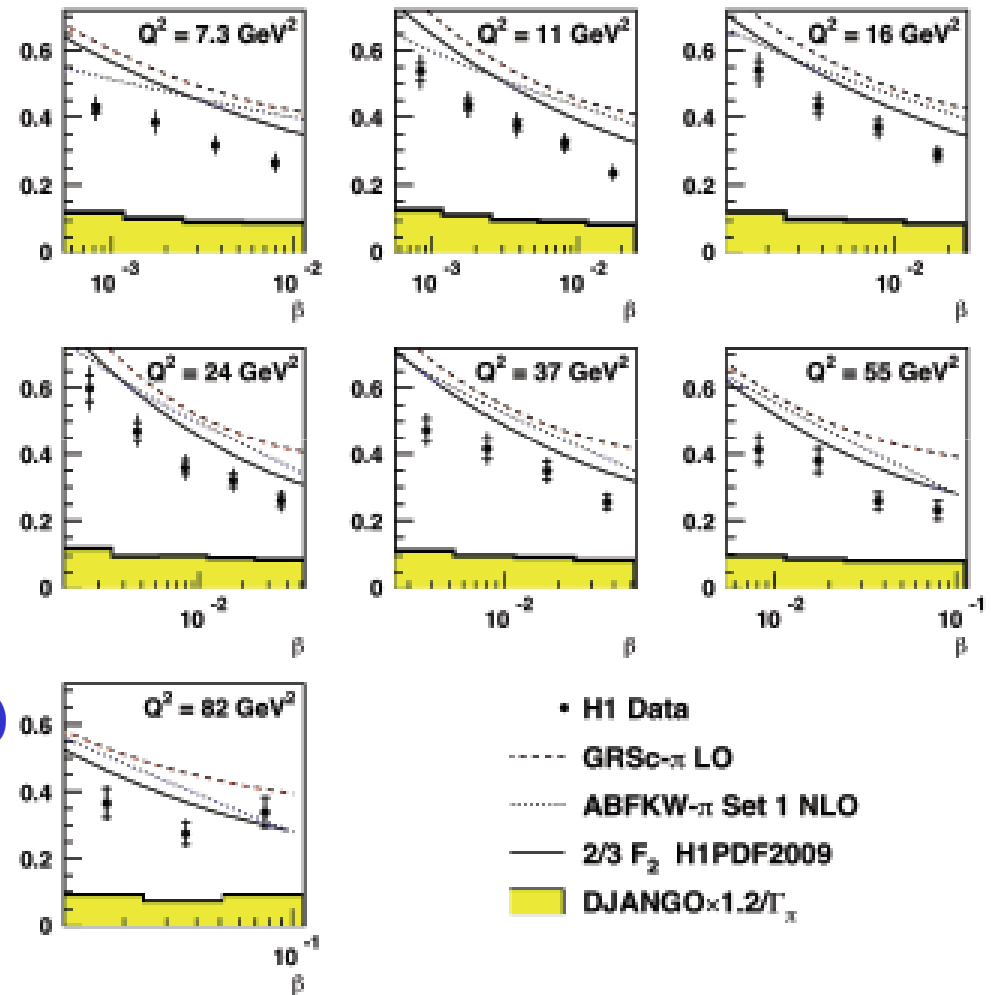
Pion flux parameterisation uncertainty  $\sim 30\%$

Contribution of neutrons from fragmentation (estimated by DJANGO) is  $\sim 25-30\%$  and  $\beta, Q^2$  independent

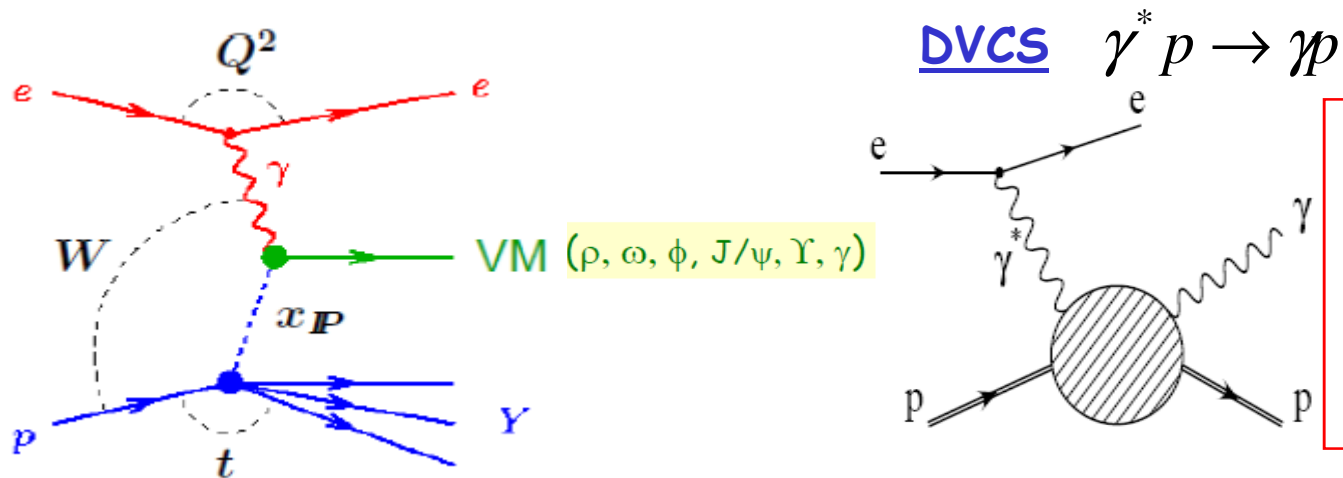
Contribution from  $\rho$  or other bkg negligible in this  $x_L$  bin

$$F_2^{LN(3)}(x_L = 0.73) / \Gamma_\pi, \Gamma_\pi = 0.13$$

H1



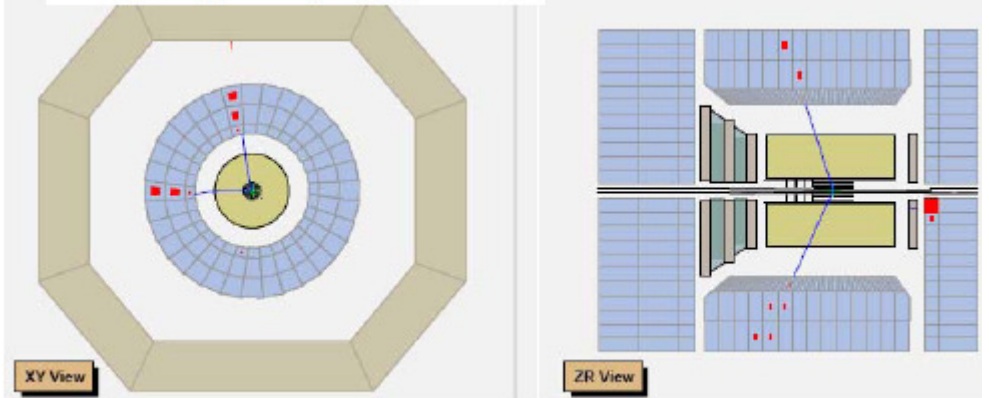
# Exclusive diffraction



VM ( $\rho, \omega, \phi, J/\psi, \Upsilon, \gamma$ )

- ✓ Fully calculable in QCD
- ✓ Gives access to GPDs
- ✓ no uncertainty due to VM wave function

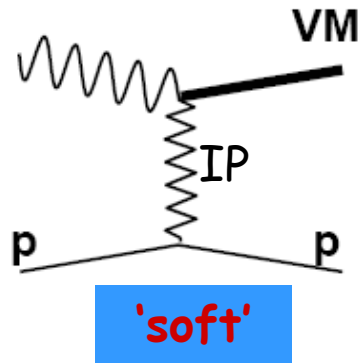
ZEUS:  $ep \rightarrow e' + p^0 + p, \rho \rightarrow \pi^+ \pi^-$



Signature:  
VM decay particle and  
nothing else in the main  
detector!

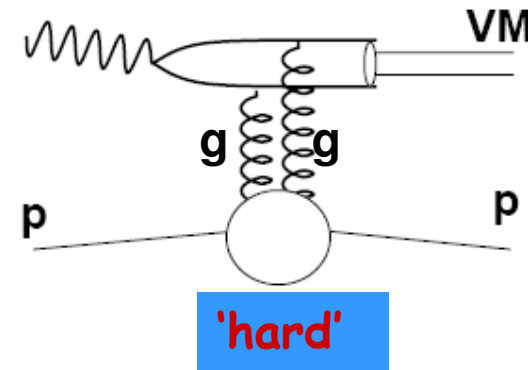
$W$  and  $t$  cross section dependence for VM and DVCS  
to investigate the transition from soft to hard at HERA

# Soft and hard diffraction



Pomeron trajectory:

$$\alpha(t) = \alpha(0) + \alpha' t$$



2-gluon exchange  
(pQCD) at LO

Gluon density in the proton

$$\left\{ \begin{array}{l} \sigma \propto [x g(x, \mu^2)]^2 \\ \mu^2 \propto (Q^2 + M_V^2) \end{array} \right.$$

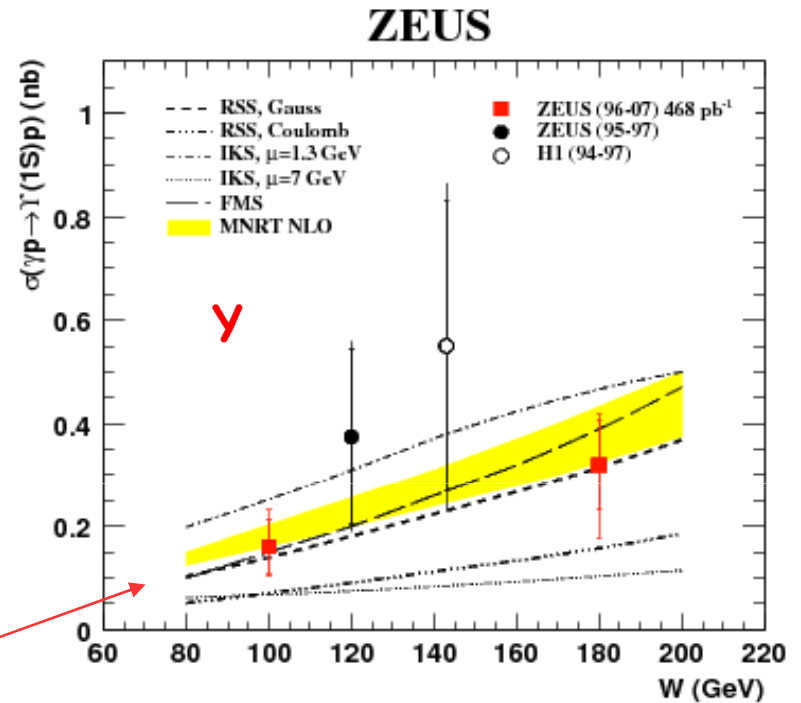
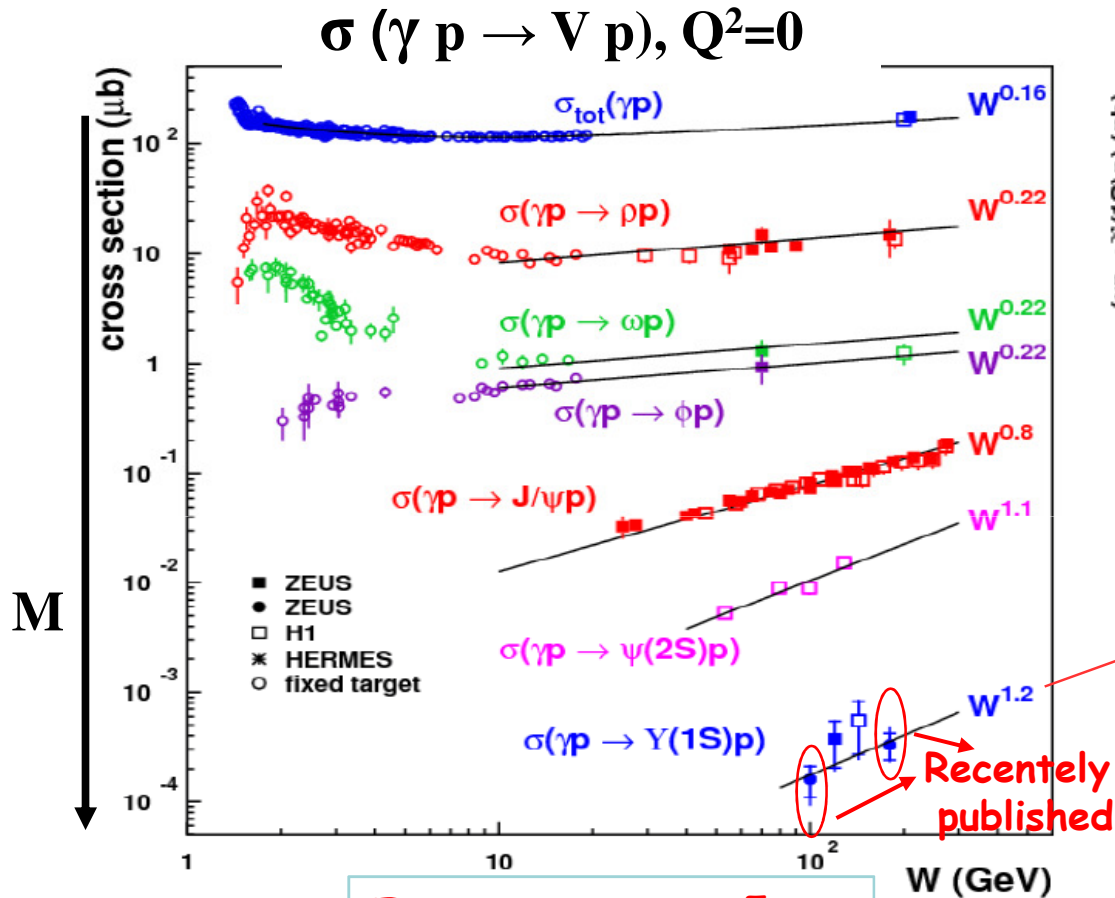
Fast increase of cross section proportional to probability of finding 2 gluons in the proton

$\sigma(W) \propto W^\delta$  ➡  $\delta$  Expected to increase from soft ( $\sim 0.2$ , "soft Pomeron") to hard ( $\sim 1.$ , "hard Pomeron")

$\frac{d\sigma}{dt} \propto e^{-b|t|}$  ➡  $b$  expected to decrease from soft ( $\sim 10 \text{ GeV}^{-2}$ ) to hard ( $\sim 4-5 \text{ GeV}^{-2}$ )

# VM photoproduction: $W$ -dependence

Phys. Lett. B 680 (2009) 4-12



$Y:$   
 $\delta = 1.2 \pm 0.8$

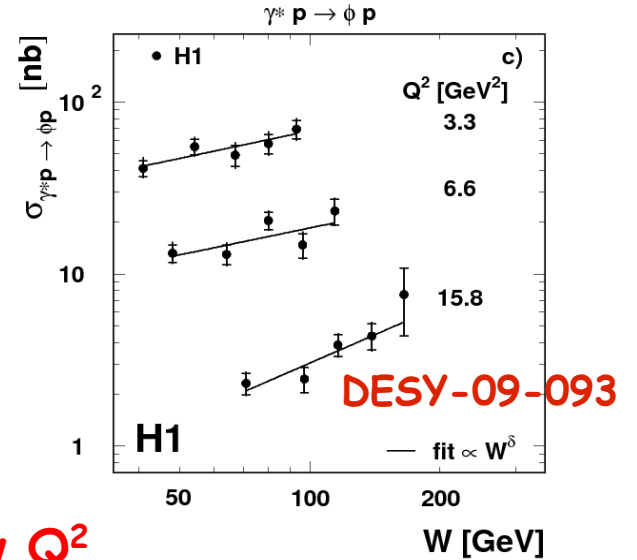
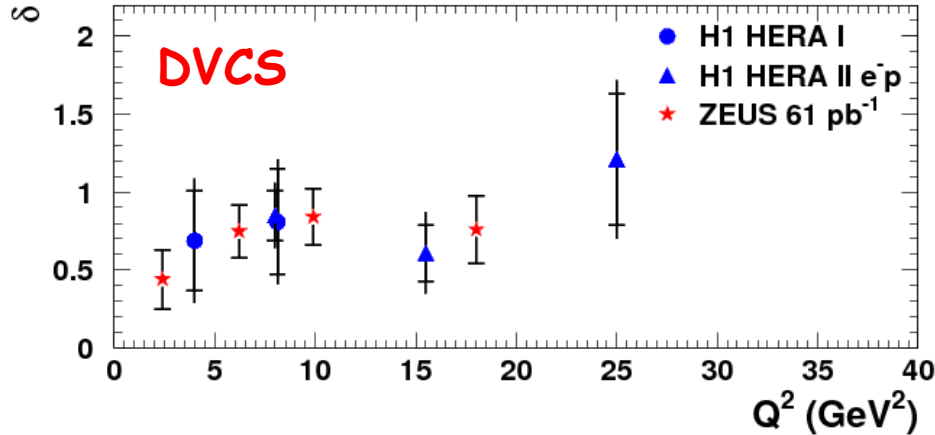
Consistent comparison with pQCD models  
 Sensitive to VM wave function (Gaussian-like light-cone WF favoured)

As the VM mass increases, the process gets harder: large  $M_V$  supplies a scale for hard processes  $\rightarrow$  apply pQCD models

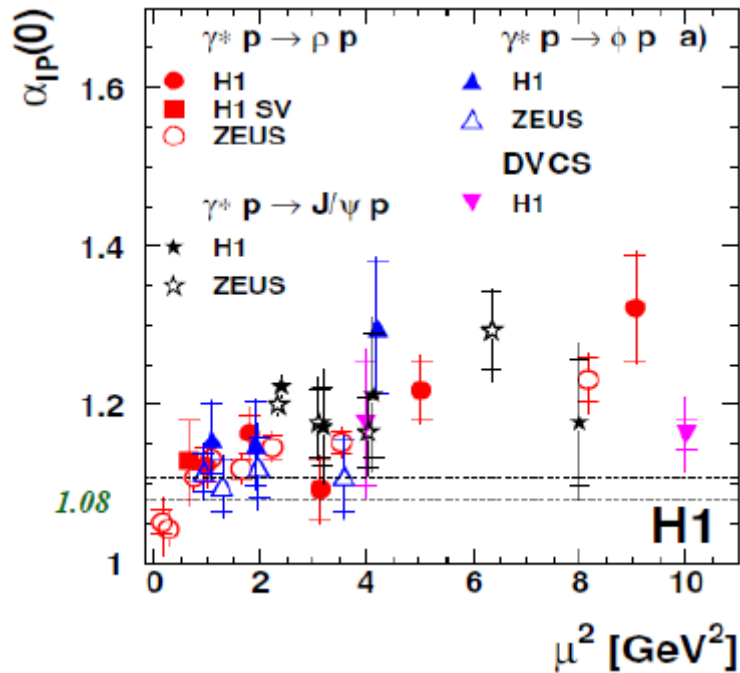
# W-dependence in DIS

ZEUS: JHEP05(2009)108  
 H1: Phys.Lett.B659:796-806,2008

Fit:  $\sigma \sim W^\delta$



DVCS W dependence shows a hard regime even at low  $Q^2$

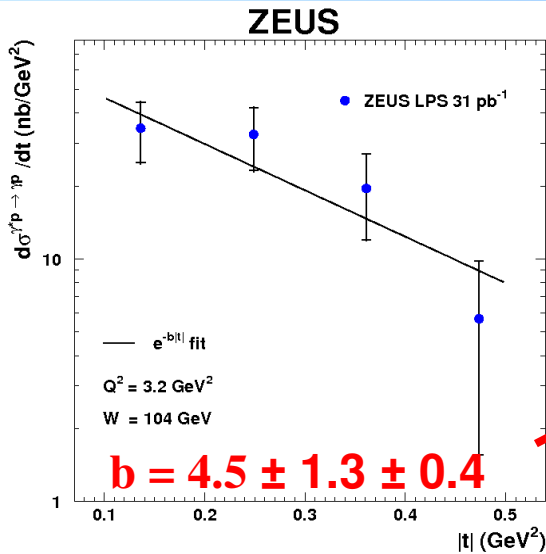


$$\begin{cases} \sigma(W) \propto W^\delta \\ \delta(t) = 4(\alpha_{IP}(t) - 1) \end{cases} \rightarrow \begin{cases} \alpha_{IP}(0) = 1 + \delta/4 + \alpha'_{IP} / \langle |t| \rangle \\ \mu^2 = (Q^2 + M^2)/4 \end{cases}$$

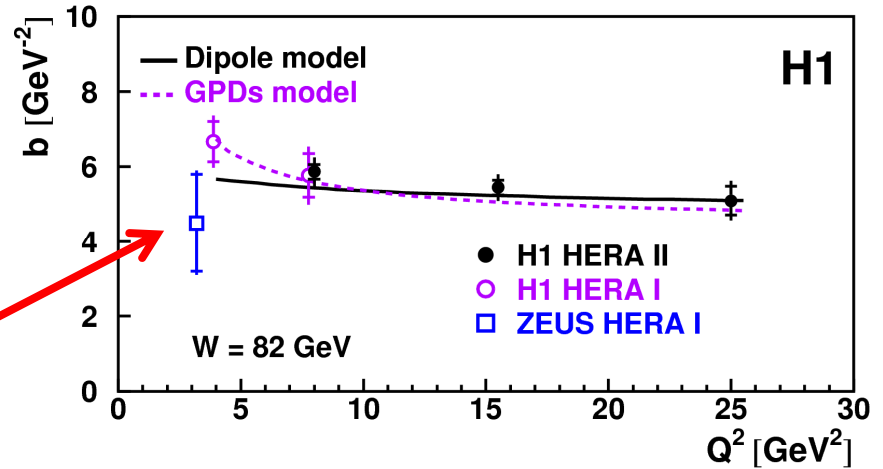
Common hardening of  $\alpha_{IP}(0)$  with  $\mu^2$

$\delta$  increases with  $\mu^2$   
 (from soft to hard)

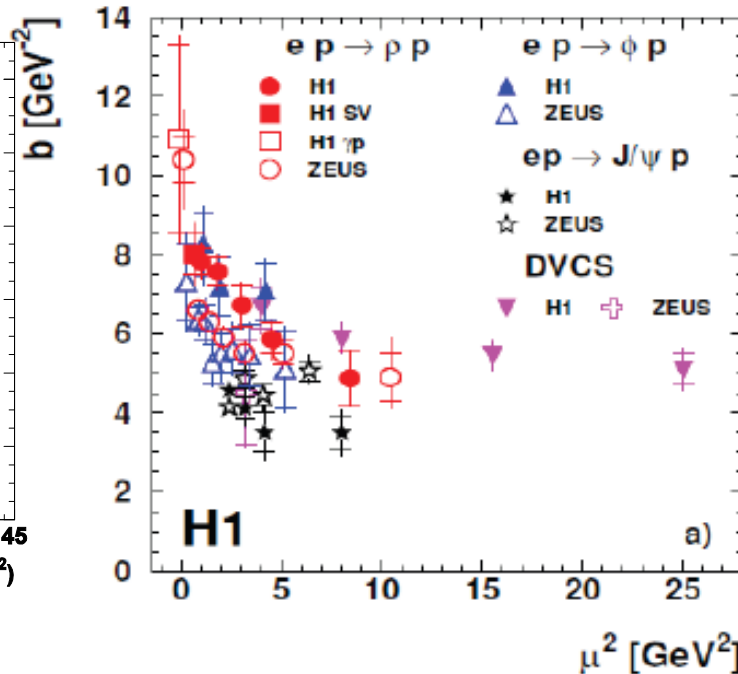
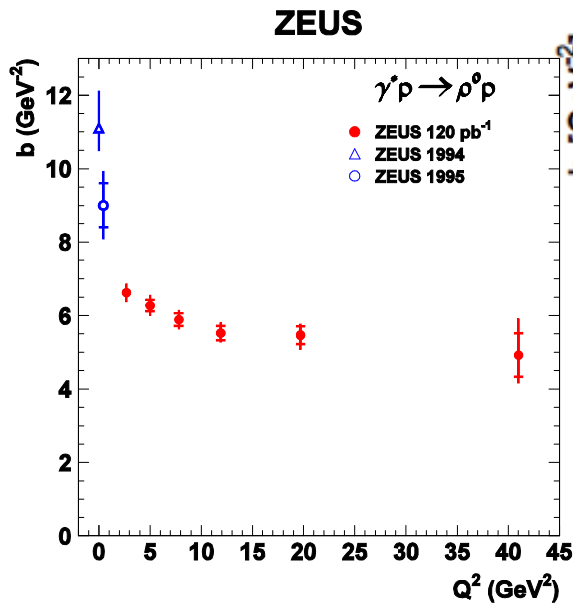
# t dependence



DVCS



Same slope for all VM vs  $\mu^2$



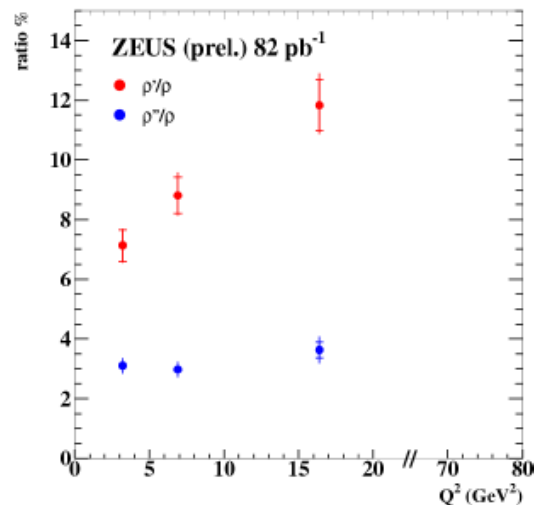
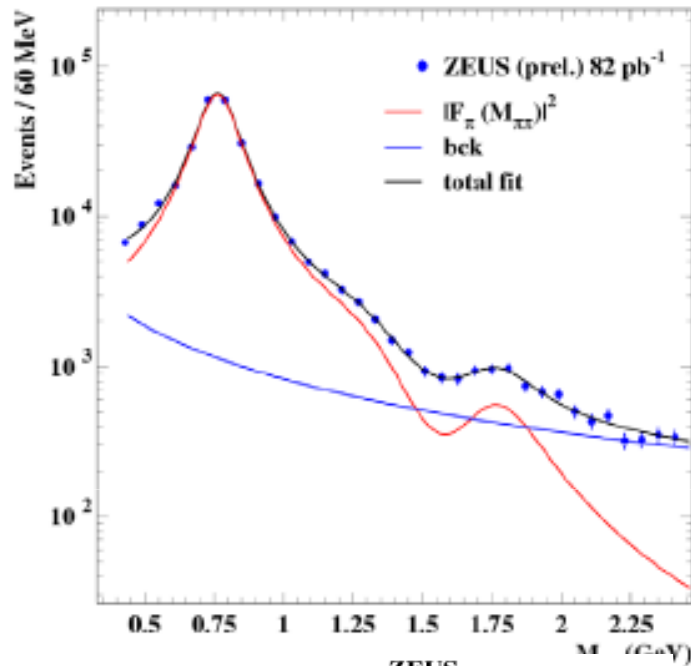
- $b$  characterize the size of interaction, large dipole for light VM, the size became smaller with scale

- $b$  decreases with  $\mu^2$  (from soft to hard)



# Two pion electroproduction

ZEUS-prel-10-012 Two pion mass  $0.4 < M_{\pi\pi} < 2.4 \text{ GeV}$  -  $2 < Q^2 < 80 \text{ GeV}^2$



Fit with 3 resonances:  $\rho, \rho', \rho''$

$$\bullet \frac{dN(M_{\pi\pi})}{dM_{\pi\pi}} = N \left[ |F_{\pi}(M_{\pi\pi})|^2 + \frac{B}{M_{\pi\pi}^n} \right]$$

$$\bullet F_{\pi}(M_{\pi\pi}) = \frac{BW(\rho) + \beta BW(\rho') + \gamma BW(\rho'')}{1 + \beta + \gamma}$$

Parameter	ZEUS (prel.)	PDG
$M_{\rho}$ (GeV)	$772 \pm 2^{+2}_{-1}$	$775.49 \pm 0.34$
$\Gamma_{\rho}$	$155 \pm 5 \pm 2$	$149.4 \pm 1.0$
$\beta$	$-0.27 \pm 0.02 \pm 0.02$	
$M_{\rho'}$ (GeV)	$1360 \pm 20^{+20}_{-30}$	$1465 \pm 25$
$\Gamma_{\rho'}$	$460 \pm 30^{+40}_{-45}$	$400 \pm 60$
$\gamma$	$0.10 \pm 0.02^{+0.02}_{-0.01}$	
$M_{\rho''}$ (GeV)	$1770 \pm 20^{+15}_{-20}$	$1720 \pm 20$
$\Gamma_{\rho''}$	$310 \pm 30^{+25}_{-35}$	$250 \pm 100$

$Q^2$  dependence:

$\rho'/\rho$  increases with  $Q^2$

(consistent with pQCD expectation: Martin, Ryskin, Teubner Phys.Rev. D56, 3007, 1997)

$\rho''/\rho$  flat with  $Q^2$

# Summary

A lot of data analysed and new measurements are coming:

- New inclusive measurements presented (first H1 measurements with VFPS)
- NLO predictions using HERA DPDFs agree very well with the data (see charm, dijet, forward jet, etc.) fact holds at HERA
- Combinations of H1 and ZEUS final results underway
  
- Precise measurements of LN ( $x_L$  and  $P_T^2$ ) presented in PHP with jets and in DIS
- Pion structure function estimated from  $F_2^{LN}$
  
- New exclusive measurements presented (two pion production)
- VM measurements allow the study the transition from the soft to the hard regime

HERA represents a powerful 'instrument' to understand diffraction in perturbative regime and to complete the mapping of the proton structure

# Backup

# ZEUS diffractive QCD fits

Regge factorization assumption  $\rightarrow$   $F_{2/L}^{D(4)}(x_{IP}, t, Q^2, \beta)$   
DGLAP evolution equations  $= f(x_{IP}, t)F_{2/L}^{IP}(Q^2, \beta) + f(x_{IR}, t)F_{2/L}^{IR}(Q^2, \beta)$   
(QCDNUM)

Heavy quarks contribution treated  
within TR-VFNS scheme (H1 FFNS)

DPDFs (q and g) parametrized

at the starting scale  $Q_0^2 = 1.8 \text{ GeV}^2$  as:  $z f_{d,u,s}(z, Q_0^2) = A_q z^{B_q} (1-z)^{C_q}$   
 $z f_g(z, Q_0^2) = A_g z^{B_g} (1-z)^{C_g}$

Fit C (constant) gluon parameters:  $B_g = C_g = 0$  ( $\sim$ H1 FitB)

Fit S (standard) gluon parameters:  $B_g, C_g$  fitted

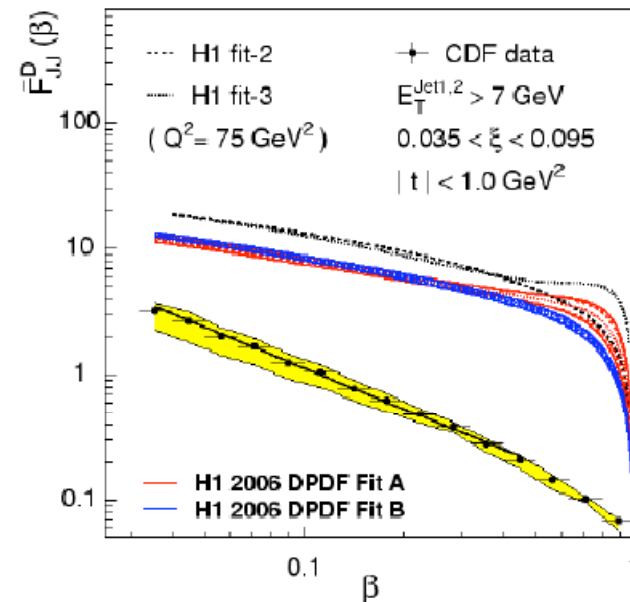
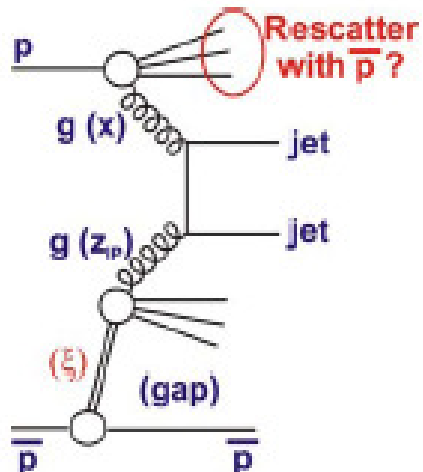
Fit SJ (standard+dijet) gluon parameters:  $B_g, C_g$  fitted

$Q_{\min}^2 > 5 \text{ GeV}^2$  (H1:  $Q_{\min}^2 > 8.5 \text{ GeV}^2$ )

# Diffraction Dijet Photoproduction

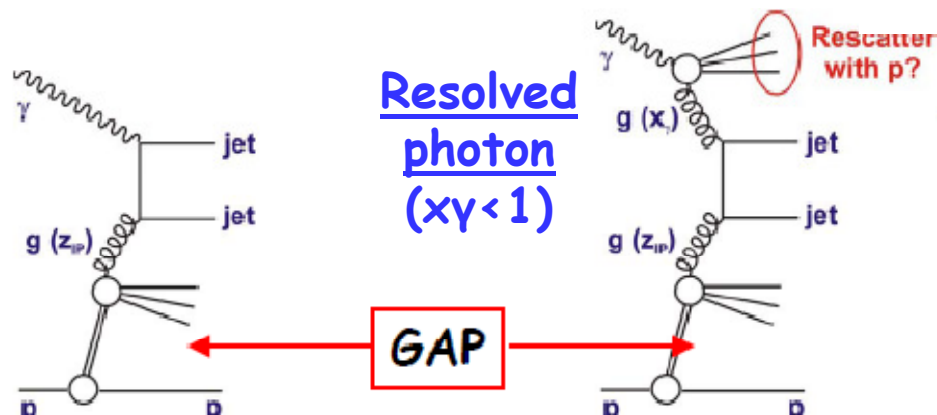
**TEVATRON**

Rapidity Gap Survival probability  $S^2 \sim 0.1$ :  
Multi-Pomeron exchange absorptive effect, etc...



'Direct' photon  
( $x_\gamma \rightarrow 1$ )

" $S^2 = 1$ "



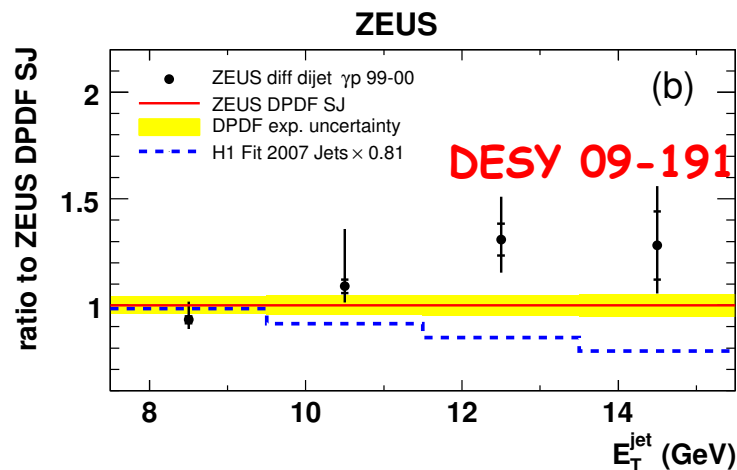
Resolved photon  
( $x_\gamma < 1$ )

**GAP**

**HERA**

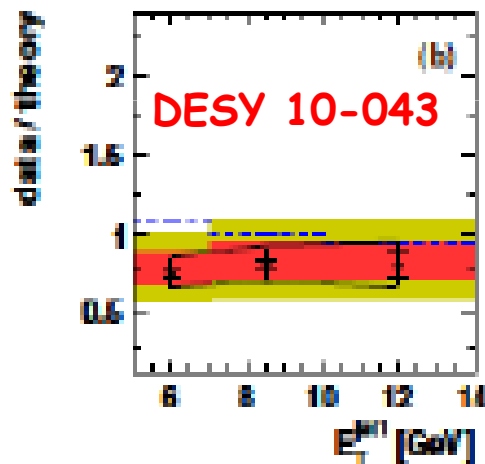
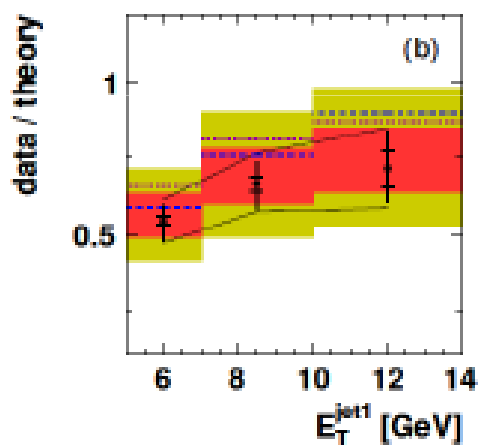
The strong suppression observed at Tevatron can be studied also at HERA using dijet cross sections in resolved dijet PHP

# Diffractive Dijet Photoproduction



ZEUS:  $E_T^{\text{jet1}} > 7.5$  GeV

Good description with no evidence for suppression on any variable



H1:  $E_T^{\text{jet1}} > 5$  GeV

$\sigma(\text{data})/\sigma(\text{theory}) \sim 0.6 \pm 0.2$

Results compatible ( $\sim 2\sigma$ ) with ZEUS

Results also compared with a refined gap survival model (KKMR) hep-ph/0911.3716

H1 data / theory

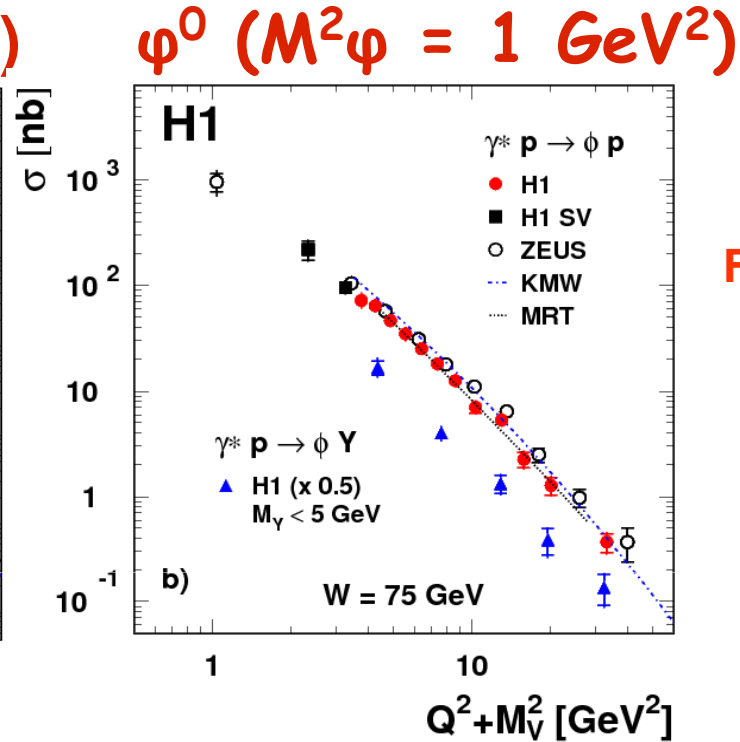
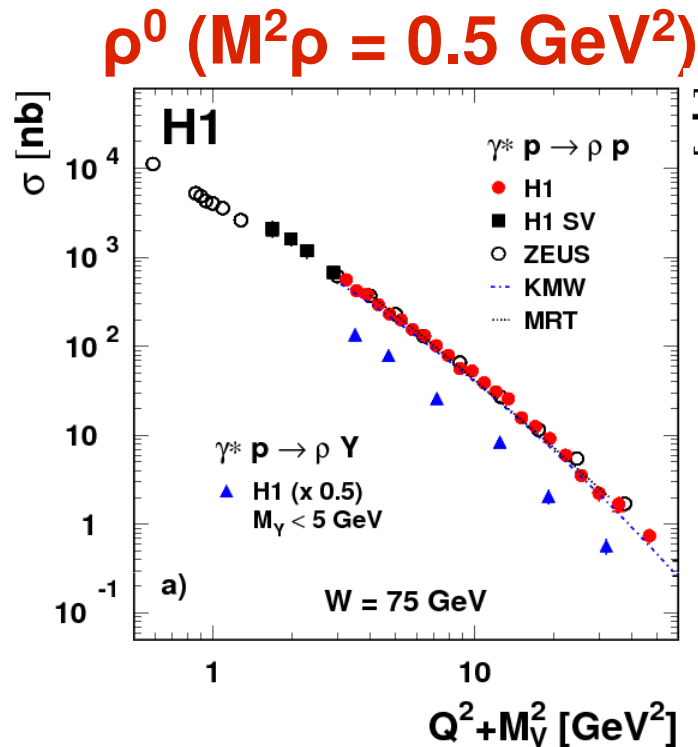
- NLO H1 2006 Fit B  $\times (1+\delta_{\text{gap}})$
- data correlated uncertainty
- - - NLO H1 2007 Fit Jets  $\times (1+\delta_{\text{gap}})$
- - - NLO ZEUS SJ  $\times 1.23 \times (1+\delta_{\text{gap}})$

H1 data / theory

- NLO H1 2006 Fit B, KKMR suppressed  $\times (1+\delta_{\text{gap}})$  [hep-ph/0911.3716]
- data correlated uncertainty
- - - NLO H1 2006 Fit B, resolved  $\times 0.34 \times (1+\delta_{\text{gap}})$

# Q<sup>2</sup>-dependence

DESY-09-093



$$\sigma \propto (Q^2 + M^2)^{-n}$$

Fit to whole  $Q^2$  range  
gives bad  $\chi^2/df$

## Good H1/ZEUS agreement

- $Q^2 \geq 0 \text{ GeV}^2$ ,  $n \approx 2.00 \pm 0.01$ ,  $\chi^2/ndf \sim 10$  ( $n \neq \text{const}$ )
- $Q^2 \geq 10 \text{ GeV}^2$ ,  $n \approx 2.50 \pm 0.02$ ,  $\chi^2/ndf \sim 1.5$

- high precision for elastic  $\rho, \phi$  cross sections

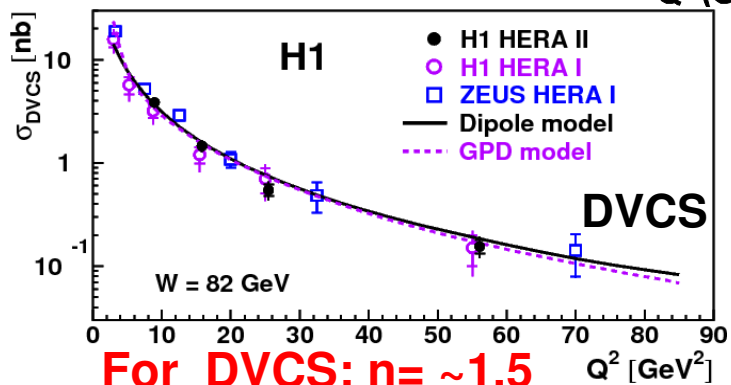
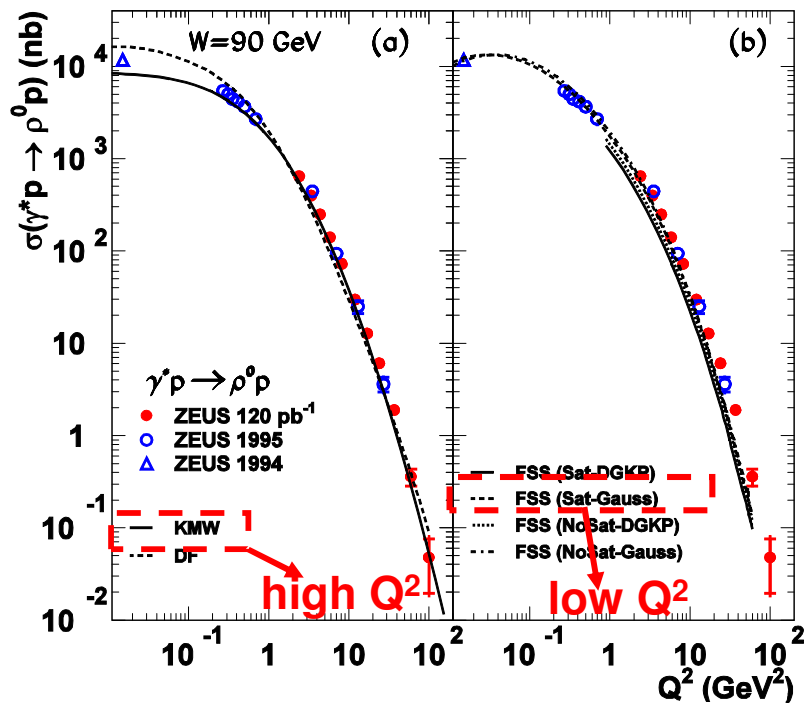
- good agreement between H1/ZEUS

- Steep decrease of  $\sigma$  with increasing  $Q^2 + M^2$

- similar for p-dissociation

# Q<sup>2</sup>-dependence

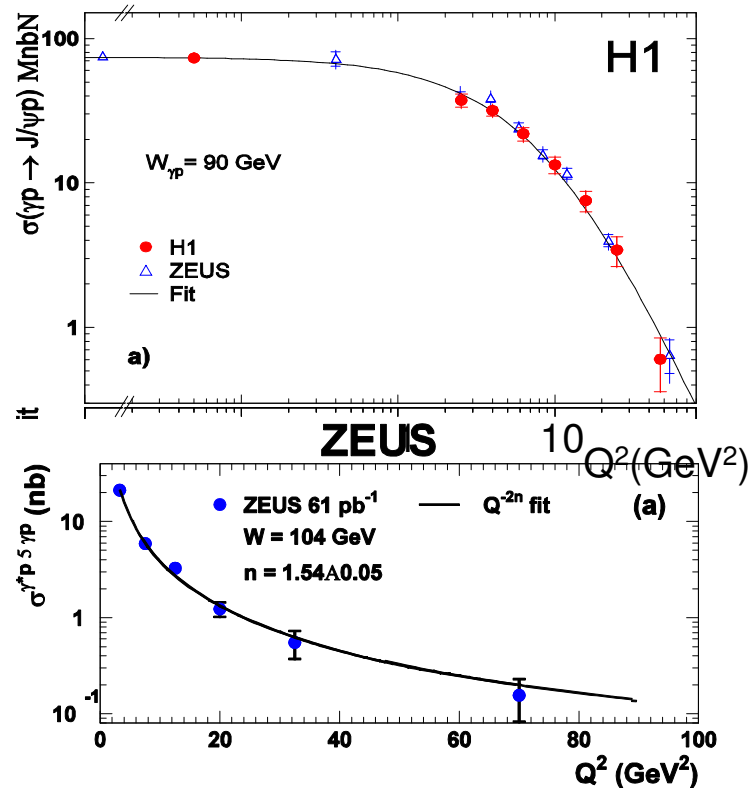
**ZEUS**



Fit to whole Q<sup>2</sup> range  
gives bad  $\chi^2/\text{df}$  ( $\sim 70$ )



n increasing with Q<sup>2</sup> appears to  
be favored



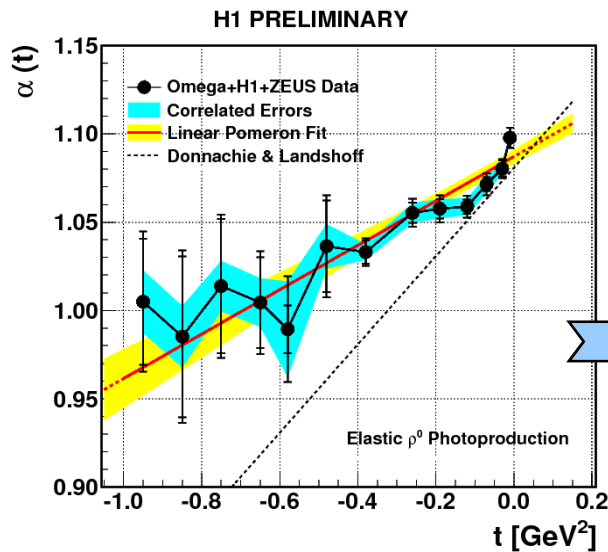


# Pomeron trajectory in ep collisions

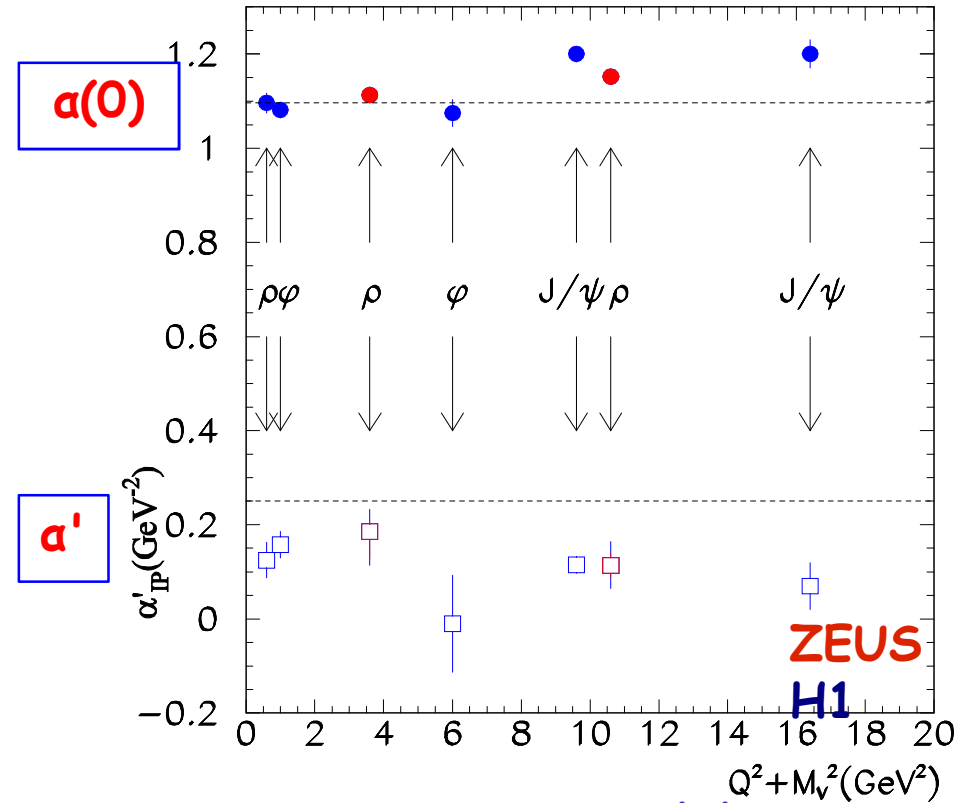
From SOFT to HARD.....

$$\alpha(t) = \alpha(0) + \alpha' t$$

In electron-proton interactions:  
As the scale gets harder the intercept grows up to 1.2  
The Pomeron slope is around  $\sim 0.1$



H1-prelim-09-016



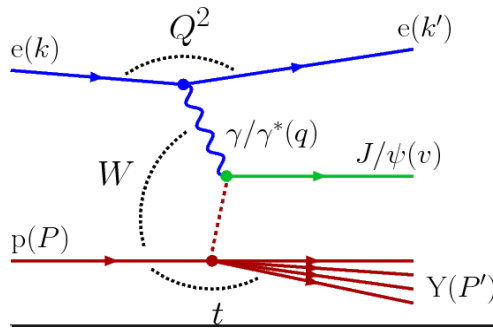
$\rho$  (light VM); elastic production (low  $|t|$ ):

$$\alpha(0) = 1.087 \pm 0.003 \pm 0.003$$

$$\alpha' = 0.126 \pm 0.013 \pm 0.012 \text{ GeV}^{-2}$$

$$\alpha_{IP}(t) = 1.08 + 0.25t \quad \text{measured in hh scattering}$$

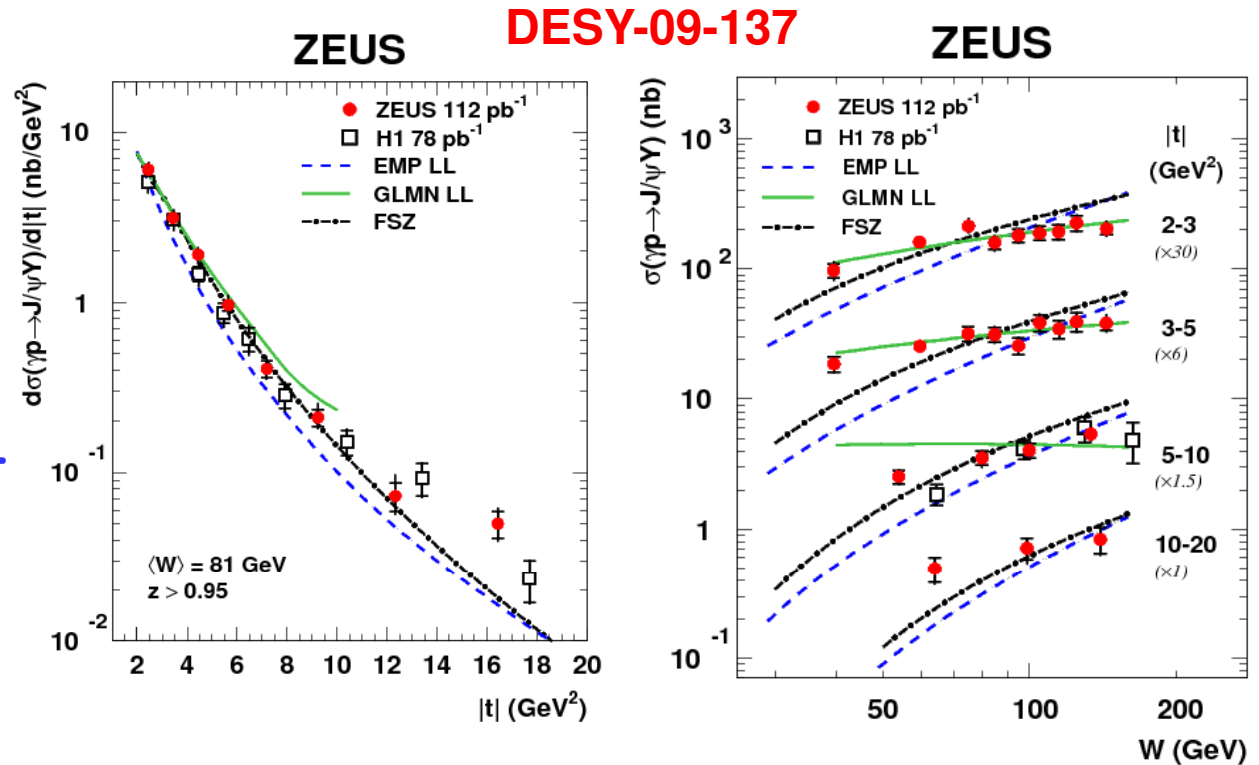
# High $|t|$ measurement of $J/\psi$



- Hard scale provided by  $t$
- $t$  dependence no longer exponential

Fit:  $\frac{d\sigma}{d|t|} \sim t^n$

$n = -1.9 \pm 0.1, 2 < |t| < 4 \text{ GeV}^2$   
 $n = -3.0 \pm 0.1, 4 < |t| < 16 \text{ GeV}^2$



- $\sigma$  vs  $W$  in  $t$  ranges: data rise with  $W$  for all  $t$
- EMP (BFKL) below data
- GLMN (DGLAP) fails at  $|t| > 5 \text{ GeV}^2$
- FSZ ( $W$  dependence of  $\sigma$  depends on the gluon distribution): describes data up to  $|t| = 12 \text{ GeV}^2$
- None of the models describes the data over the full  $t$ -range