

# Precision Measurement of $F_2$ with H1

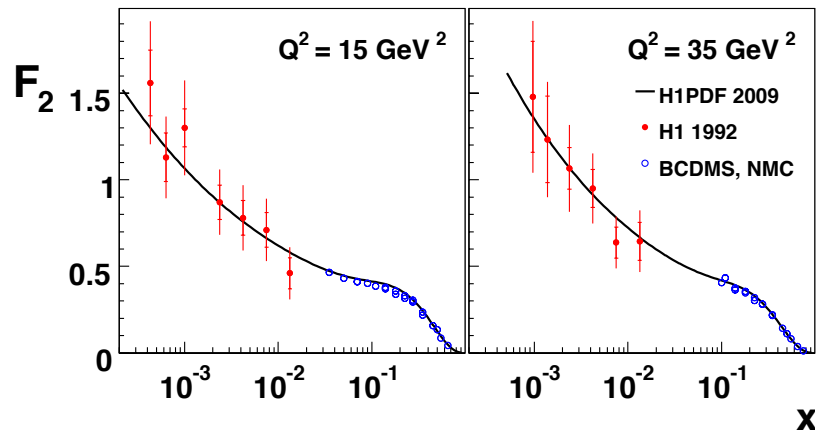
Towards today  
The Measurement  
Results  
QCD Analysis

Max Klein  
for the H1 Collaboration

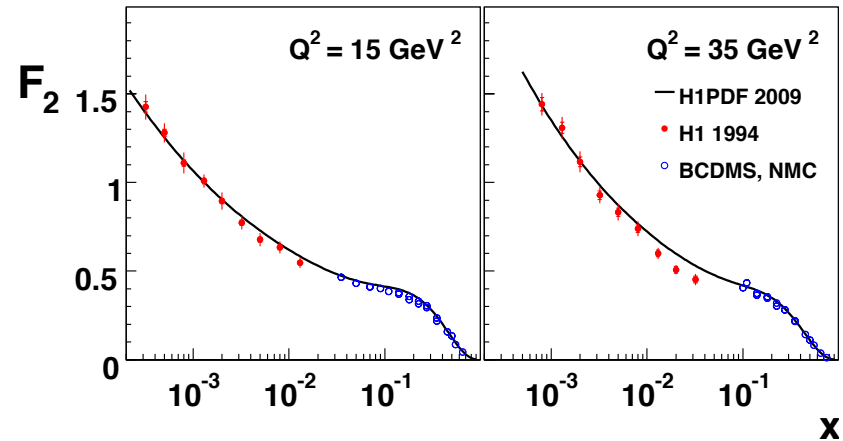


# As $F_2$ developed..

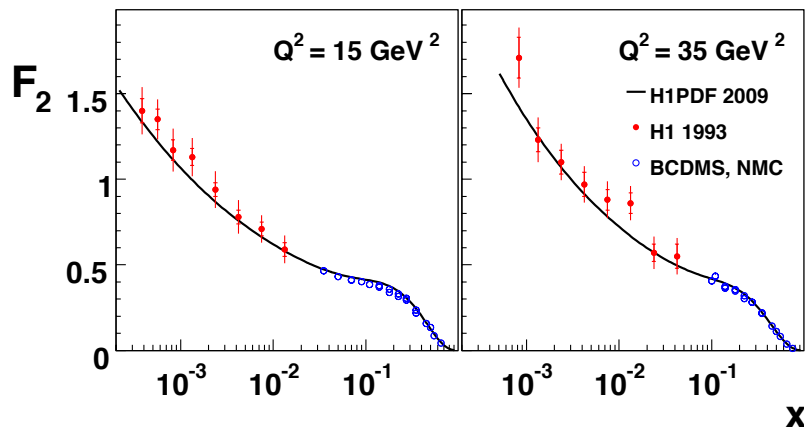
1992 [data] – discovery of the rise



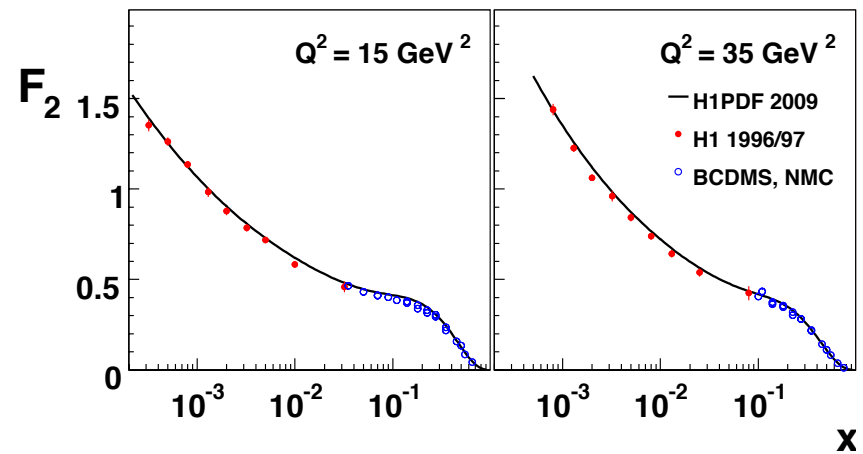
1994 – the last BEMC result 3%



1993 – a first measurement



1996/7 – first accurate SPACAL 2%



BCDMS: final publication 15 years after the experiment proposal 1974

## Systematic errors

	e	m
$E_e$ 2% and $\pm 2\%$ smearing	5-15%	3-6%
$\delta$ 5 mrad	4-12%	4-8%
$y_{JB}$ fragmentation [ $D^+$ , PS vs HERWIG], 7% energy scale, $(y_{JB} - y_{Gen})/y_{Gen}$ , thresholds	-	10-25%
$Z_{vtx}$ statistics, satellite bunch, comparison of methods I, II		7%
BPC, tracker cut, EBDI/ECRA, cluster-hit		6%
strucuse fct. $D^+/D^0$ (lowest x).		5-10%
radiative corrections (MC statistics for I) $Z_{vtx}$ , $E - p_z$ in MC	8%	2%
bin centre correction ( $\alpha \sqrt{E, \delta} \rightarrow x, Q^2$ )	5%	2%
	17-23%	18-29%

• statistics: 950 events

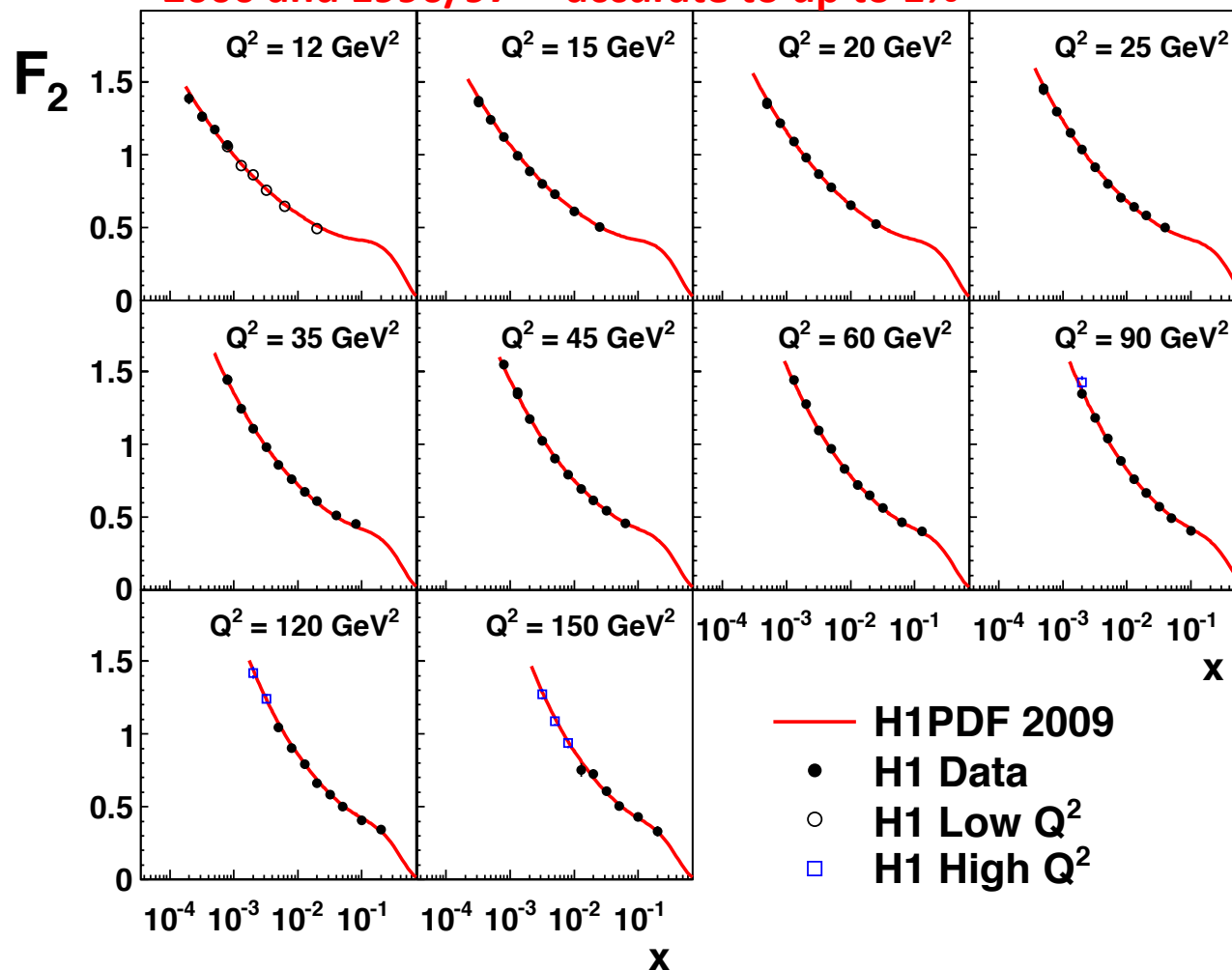
• scale error: lumi 7% TOP, trigger  $\rightarrow$  9%

## $\sigma_r$ Errors in 2009

Spacal	
Double angle calibration: 0.2% up to 1% at 2 GeV	
BST /CJC/ BDC	0.2mrad
Low y	$E_h$ : 2% at 0.01 LAR: 15% of its noise
z vertex	0.3%
eID: BDC	max 1% 0.5%
Iteration	--
RC to alpha in MC	0.3%
Negligible	
	-----
	1.3-3%
$\sim 10^6$	
+ Lumi 1.2%	trigger --

# The present measurement

2000 and 1996/97 – accurate to up to 1% H1 Collaboration

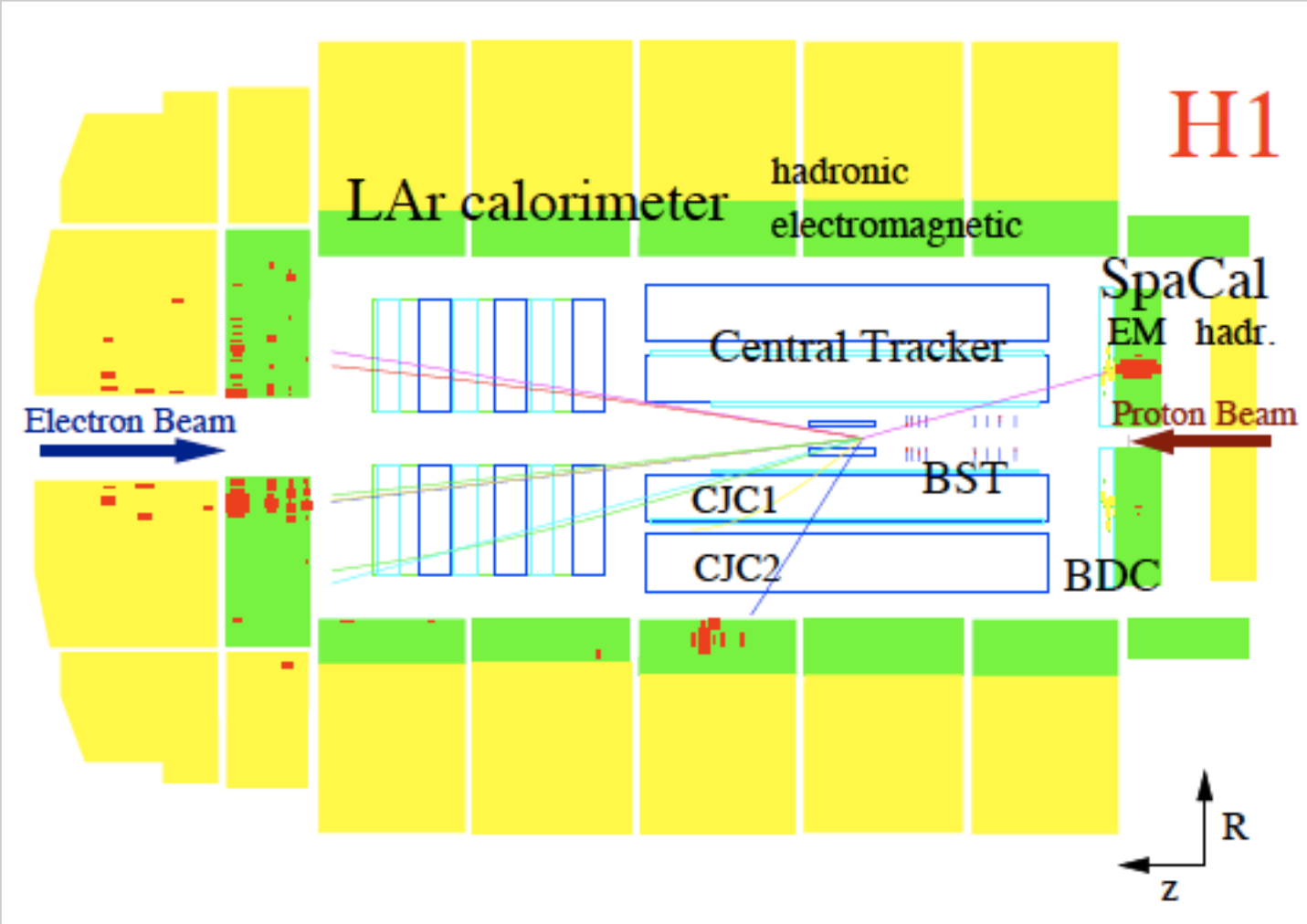


$$F_2 = \frac{\sigma_r}{1 - f(y) \frac{R}{1+R}}$$

R taken from own QCD fit. Very small effect as  $y < 0.6$

Important input to the combined H1/ZEUS data. At  $Q^2 \sim 30 \text{ GeV}^2$  the accuracy further reduced (1.3  $\rightarrow$  1.1%) and the amount of systematic uncertainties from 75 to 55%.

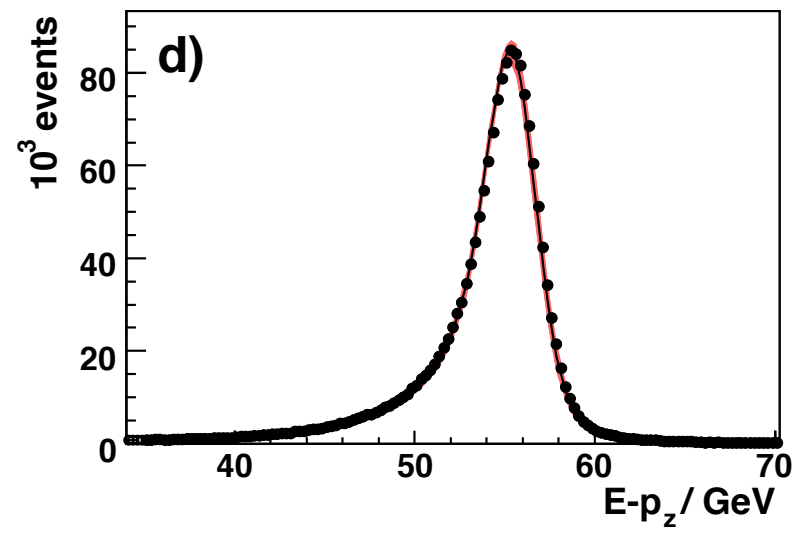
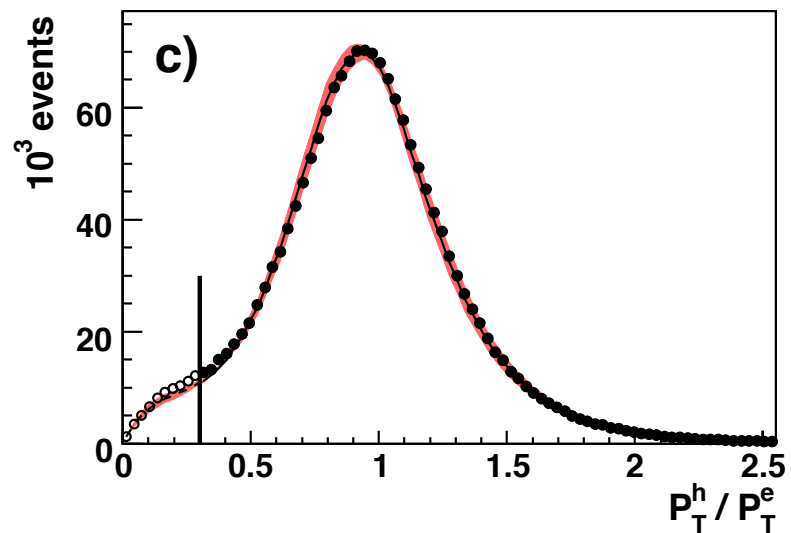
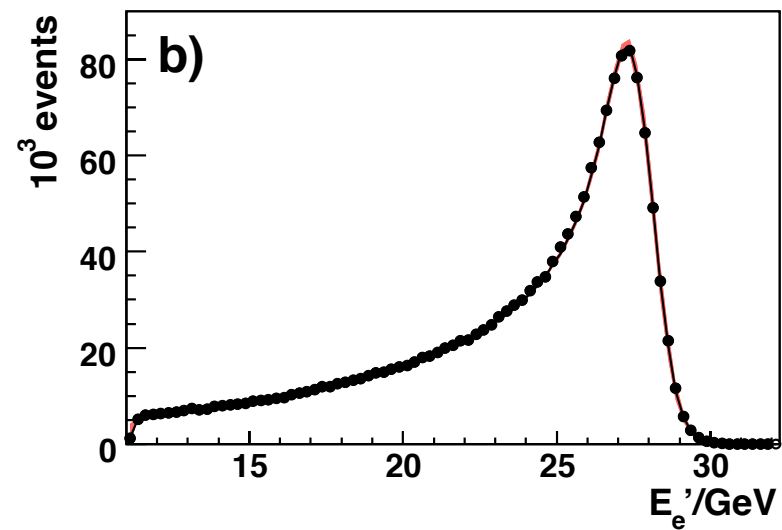
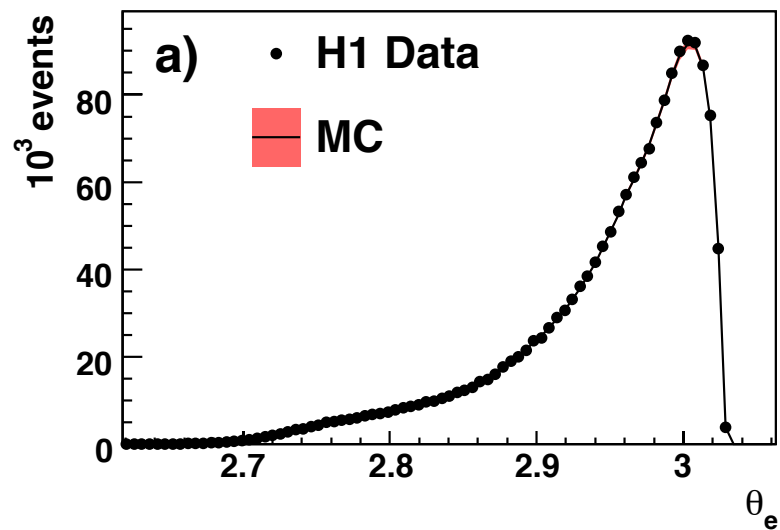
# DIS Event in the H1 Detector



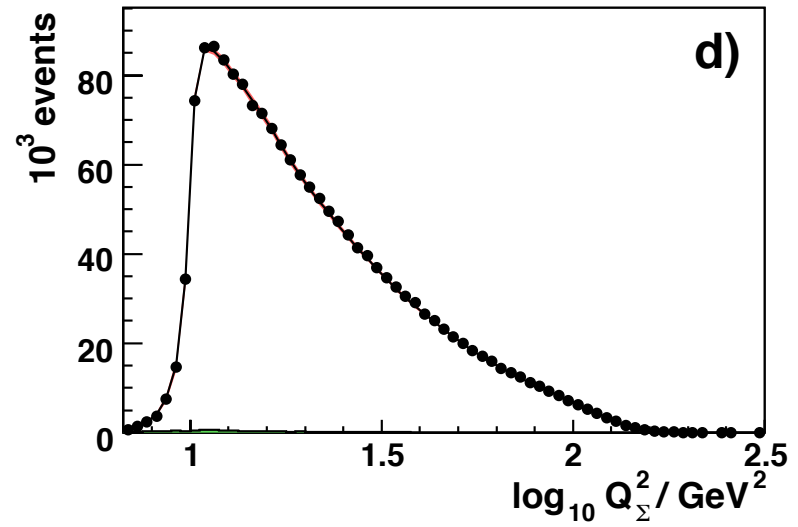
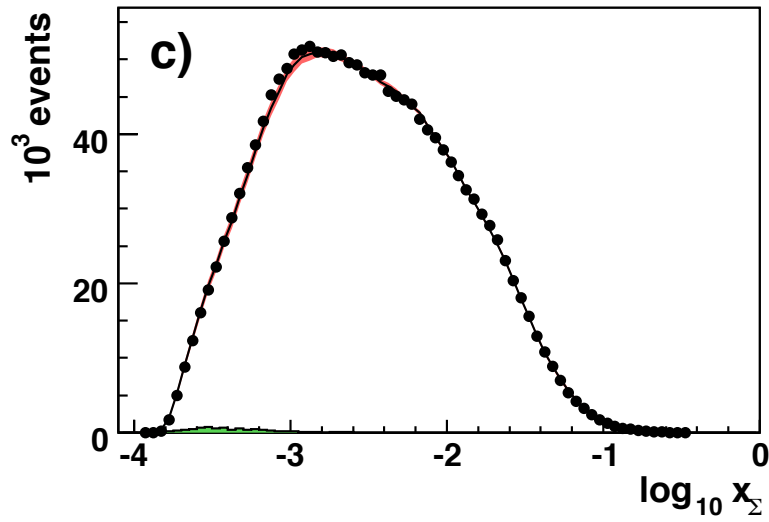
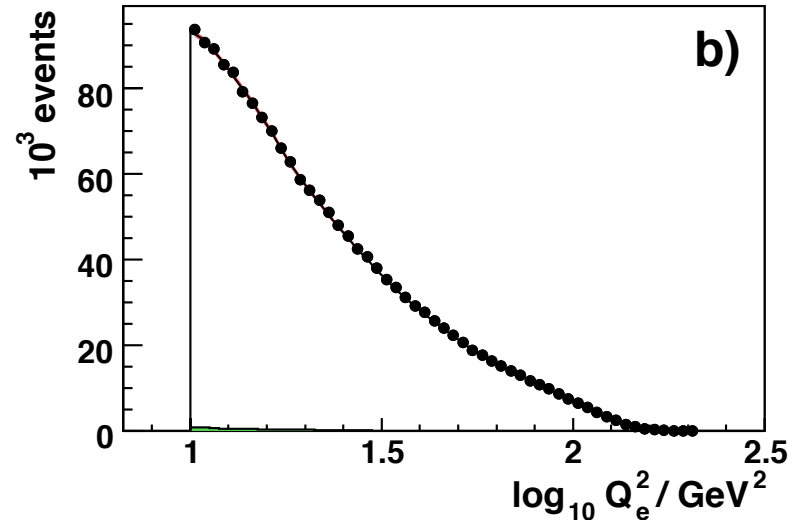
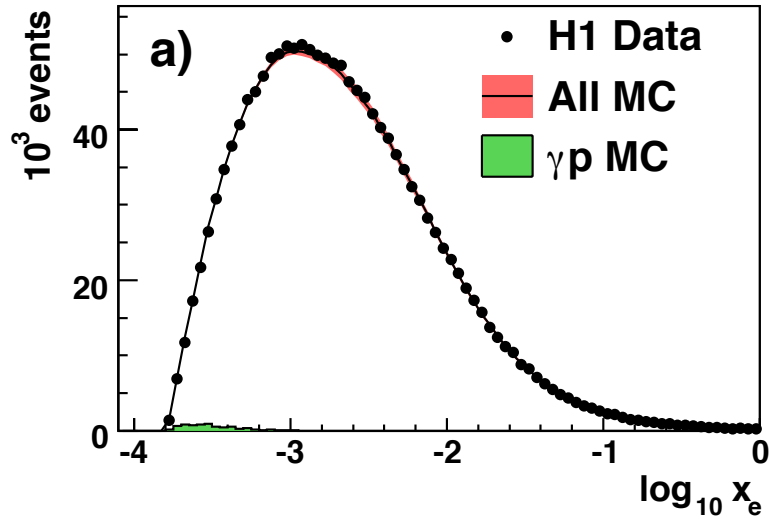
## Event Selection

Description	Requirement	
Kinematic Range	$Q_e^2 > 10 \text{ GeV}^2$	Low $Q^2$ – next talk $F_L$ a separate task
Scattered positron energy	$E'_e > 11 \text{ GeV}$	
SpaCal cluster radius	$R_{\text{log}} < 4 \text{ cm}$	3 electron ID and validation cuts
Energy in hadronic SpaCal section	$E_h/E'_e < 0.15$	
BDC validation	$\geq 4$ linked hits, BDC-SpaCal radial match $< 2.5 \text{ cm}$	
Radial cluster position	$r_{\text{Spac}} < 73 \text{ cm}$	DIS: vertex and e/h pt balance
Vertex $z$ position	$ z_{\text{vtx}}  < 35 \text{ cm}$	
Transverse momentum balance	$P_T^h / P_T^e > 0.3$	
Longitudinal momentum balance	$E - P_z > 35 \text{ GeV}$	h.o. QED radiation anti-cuts
QED Compton Rejection	Topological veto	

# Control Plots



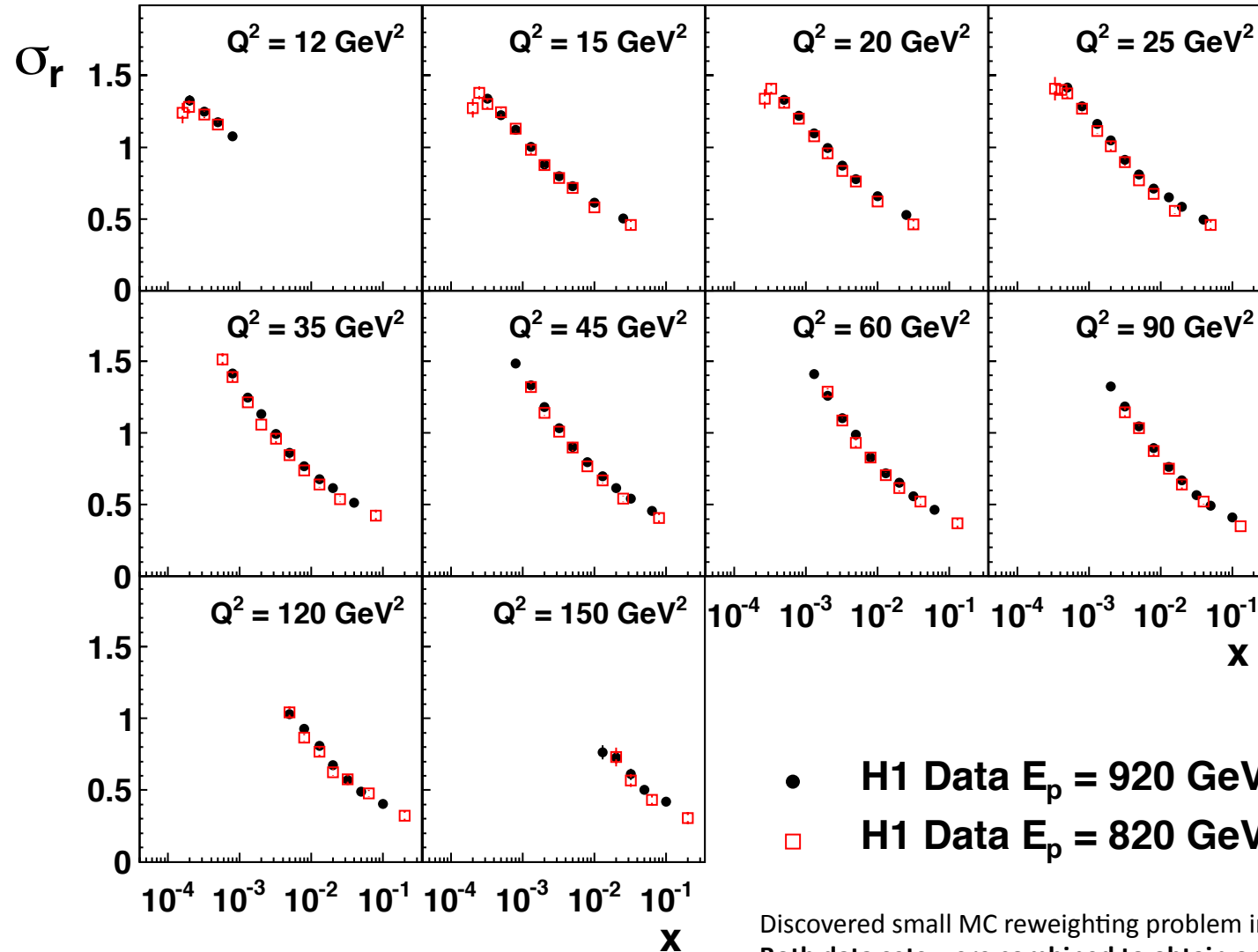
## Control Plots ( e and $\Sigma$ )





# Comparison of 820 (96/97) and 920 (2000) Data

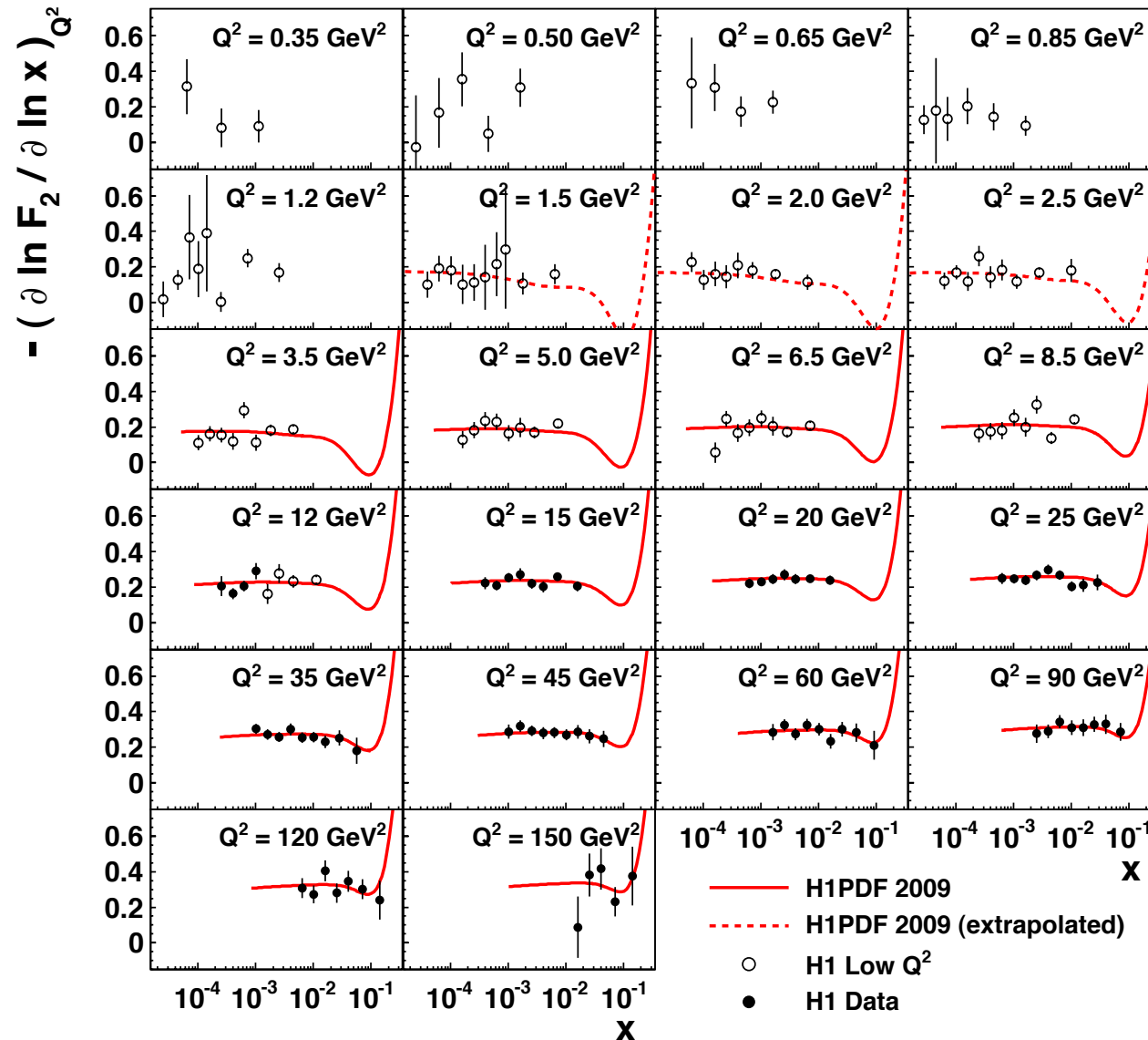
H1 Collaboration



Discovered small MC reweighting problem in 820 GeV data  
Both data sets were combined to obtain one set of H1 data

# x Dependence

H1 Collaboration



Not excluded that “the rise” is a “two-dimensional phenomenon”, i.e. for  $F_2 \sim x^{-\lambda}$ ,  $\lambda = \lambda(x, Q^2)$

H1 previously:  
Phys.Lett.B520:183,2001

$$F_2(x, Q^2) = c(Q^2)x^{-\lambda(Q^2)}$$

$$\lambda(Q^2) = a \cdot \ln(Q^2 / \Lambda^2)$$

$$\Lambda = 292 \pm 20(st) \pm 51(sy) MeV$$

$$Q^2 \geq 3.5 GeV^2, x \leq 0.01$$

# H1pdf2009

## Parameterisations

$$\begin{aligned}
 xg(x) &= A_g x^{B_g} (1-x)^{C_g} [1 + D_g x], \\
 xu_v(x) &= A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}}, \\
 xd_v(x) &= A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}}, \\
 x\bar{U}(x) &= A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}}, \\
 x\bar{D}(x) &= A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.
 \end{aligned}$$

## Fit results

$xP$	$A_P$	$B_P$	$C_P$	$D_P$
$xg$	5.66*	0.243	18.76	34.0
$xu_v$	5.15*	0.784	3.25	–
$xd_v$	3.29*	0.784*	4.77	–
$x\bar{U}$	0.105*	–0.177	2.42	–
$x\bar{D}$	0.152	–0.177*	3.42	–

## Parameter assumptions

$$B_{u_v} = B_{d_v}$$

$$B_{\bar{U}} = B_{\bar{D}}$$

$$A_{\bar{U}} = A_{\bar{D}} \cdot (1 - f_s)$$

$$A_{u_v}, A_{d_v}, A_g : \quad \begin{array}{l} \text{Quark counting and} \\ \text{Momentum sum rules} \end{array}$$

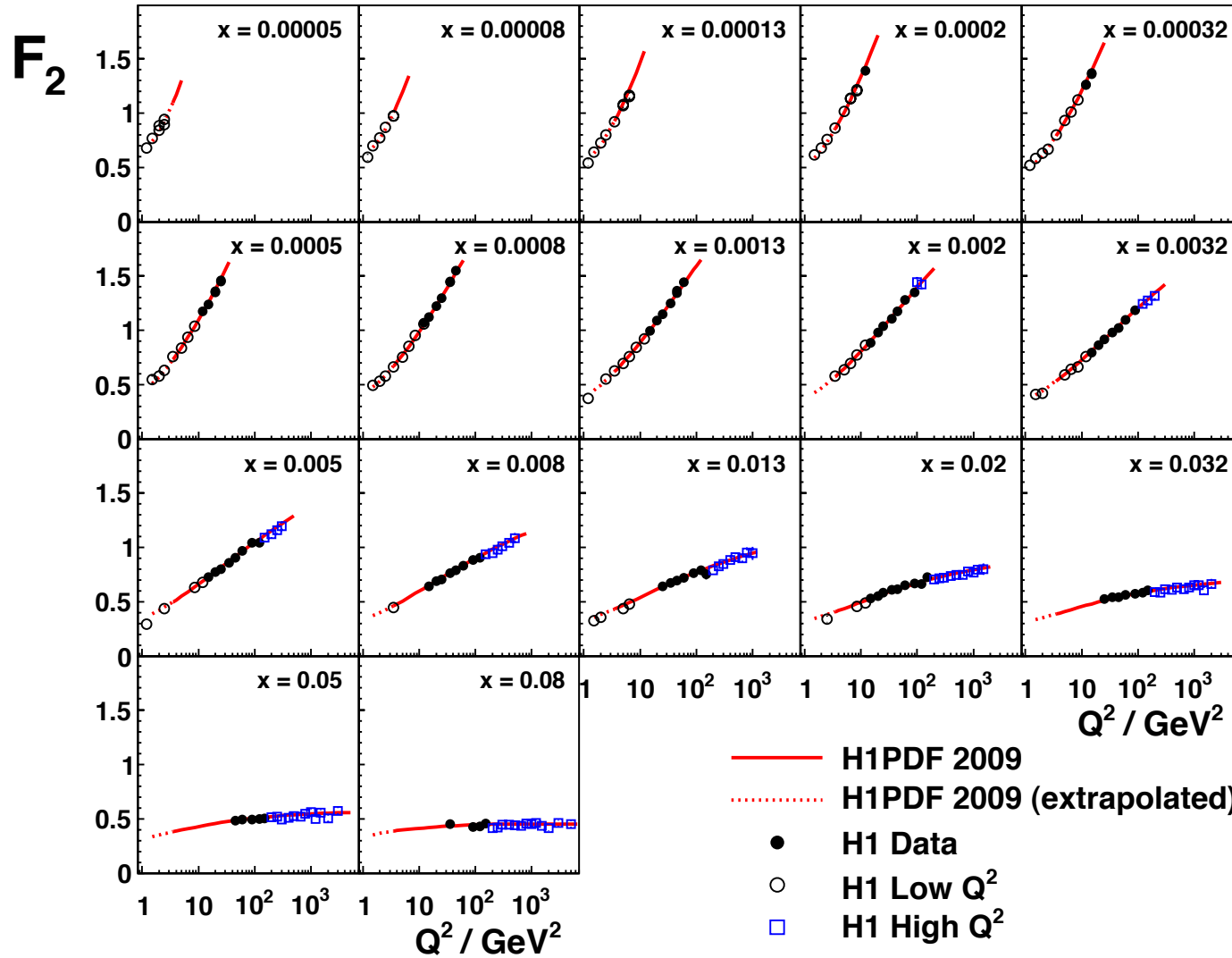
$$Q_0^2 = 1.9 \text{ GeV}^2$$

NLO, QCDNUM, VFNS

Data set	Data points	$\chi_{\text{unc}}^2$
Low $Q^2$	58	55.9
Medium $Q^2$	99	81.5
$e^+p$ NC high $Q^2$ , 94 – 97	130	92.6
$e^+p$ CC high $Q^2$ , 94 – 97	25	21.2
$e^-p$ NC high $Q^2$ , 98 – 99	139	112.1
$e^-p$ CC high $Q^2$ , 98 – 99	28	17.3
$e^+p$ NC high $Q^2$ , 99 – 00	147	137.4
$e^+p$ CC high $Q^2$ , 99 – 00	28	31.1

# $Q^2$ Dependence – $F_2$

H1 Collaboration

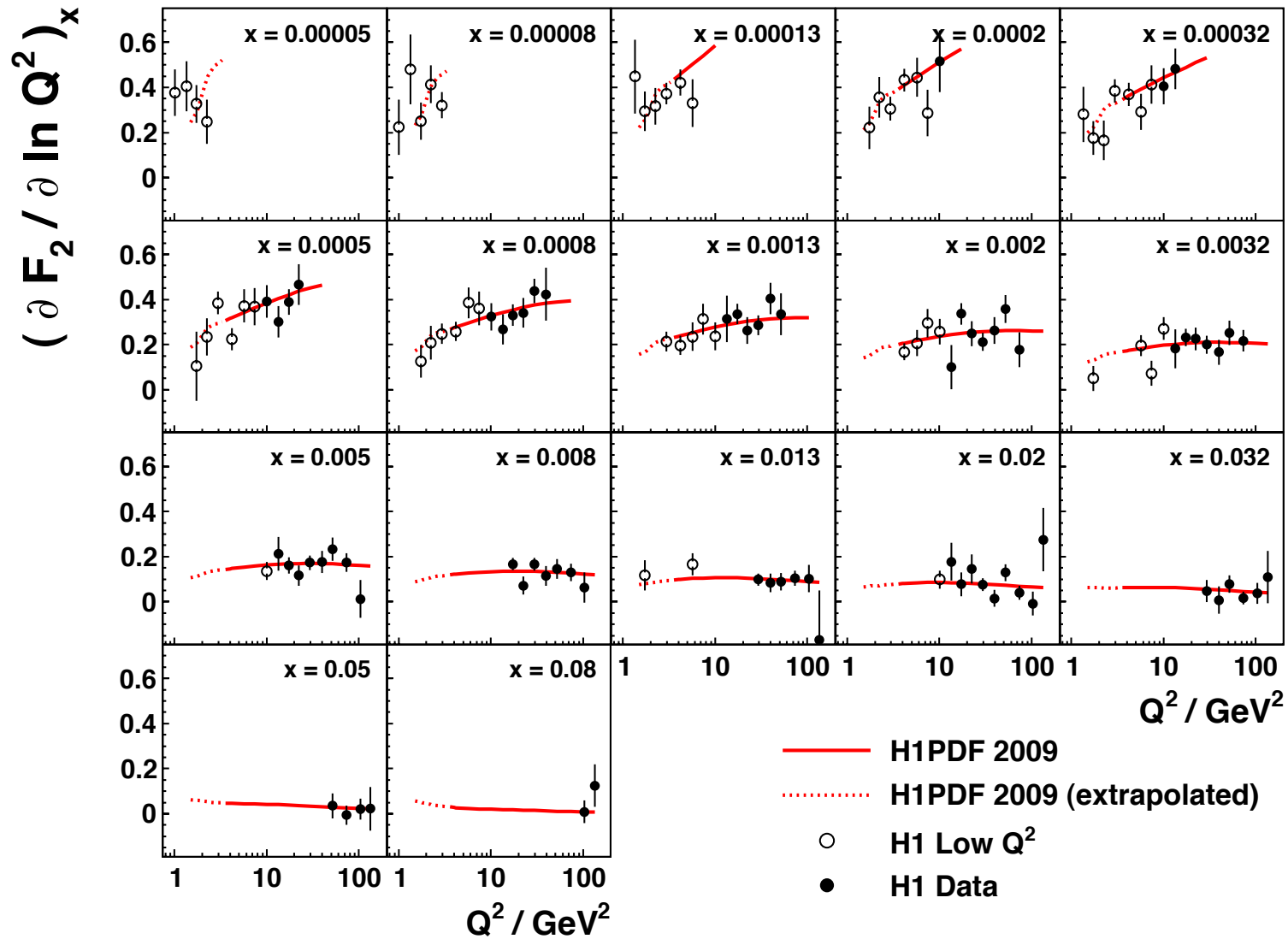


Data are consistent with other H1 data at lower and at larger  $Q^2$

cf S.Glazov: Low  $Q^2$  Talk

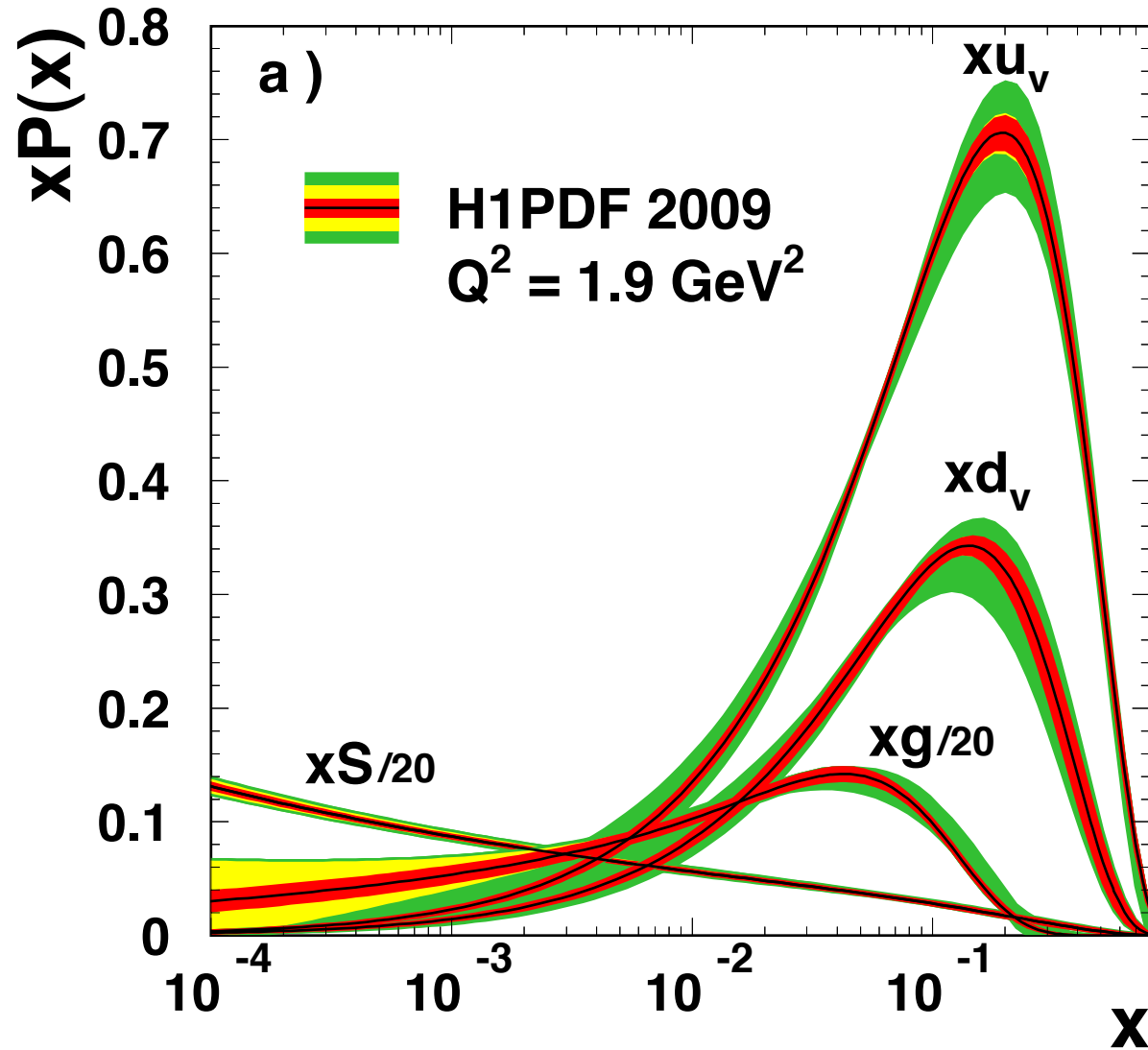
# Q<sup>2</sup> Dependence – dF<sub>2</sub>/dlnQ<sup>2</sup>

H1 Collaboration



Q<sup>2</sup> dependence well described by NLO QCD fit to the H1 data and its extrapolation

## Partons at the Initial Scale



Red: experimental

Yellow: exp+model:

- $m_c, m_b, f_s$
- $Q^2_{\min} = 2.25 - 5 \text{ GeV}^2$
- $Q^2_0 = 1.9 - 1.5 \text{ GeV}^2$

Green: +parameterisation

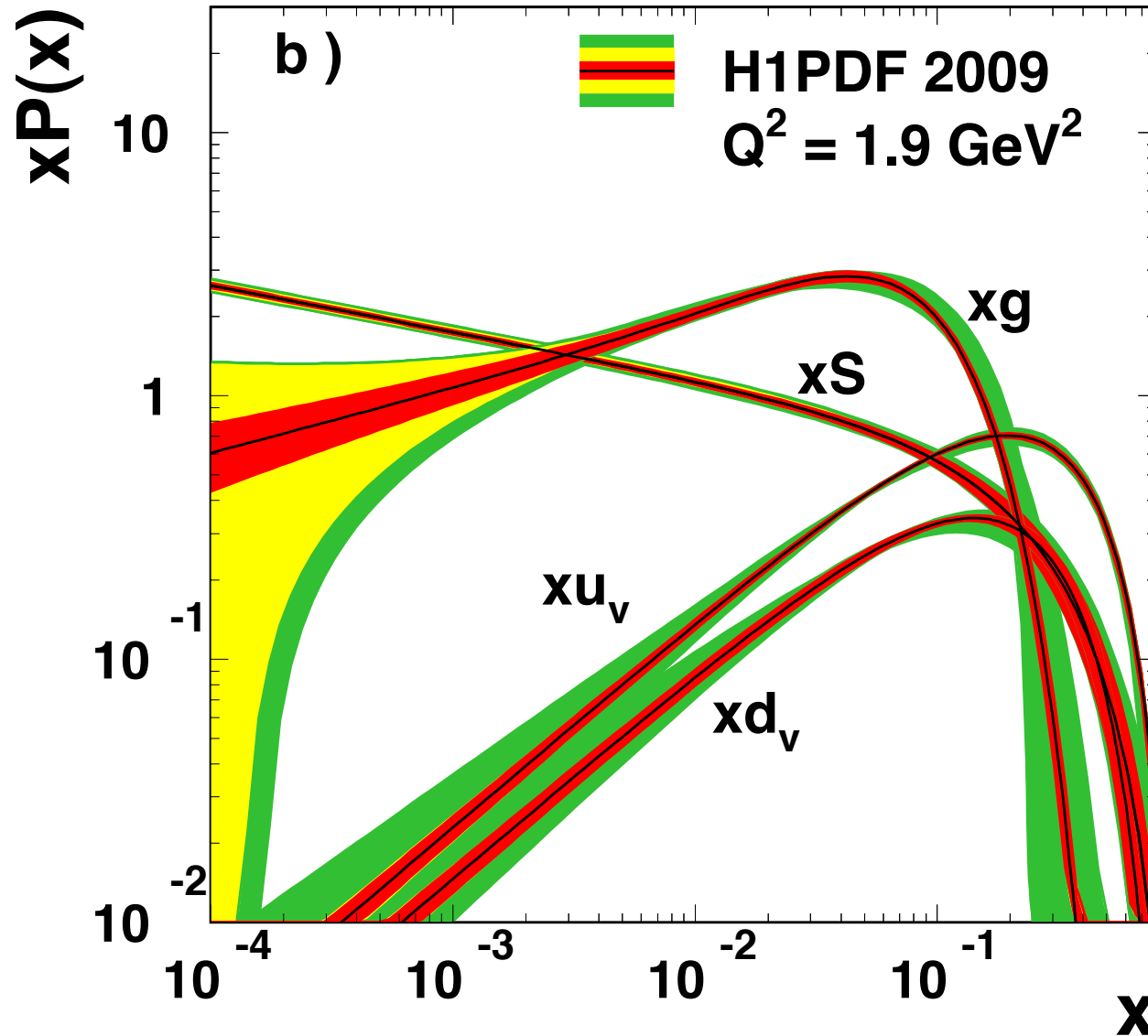
$$P(x) = Ax^B(1-x)^C[1+Ex+Dx^2..]$$

For error bands require:

- D, E if  $\chi^2 < \chi^2_0 + 3$
- $F_2$  and  $F_L > 0$
- allow for non-canonical (vN) valence/sea quark ratios at large x

.. A first attempt to quantify parameterisation uncertainty.

## Partons at the Initial Scale



**Large uncertainty of gluon at low  $x$**

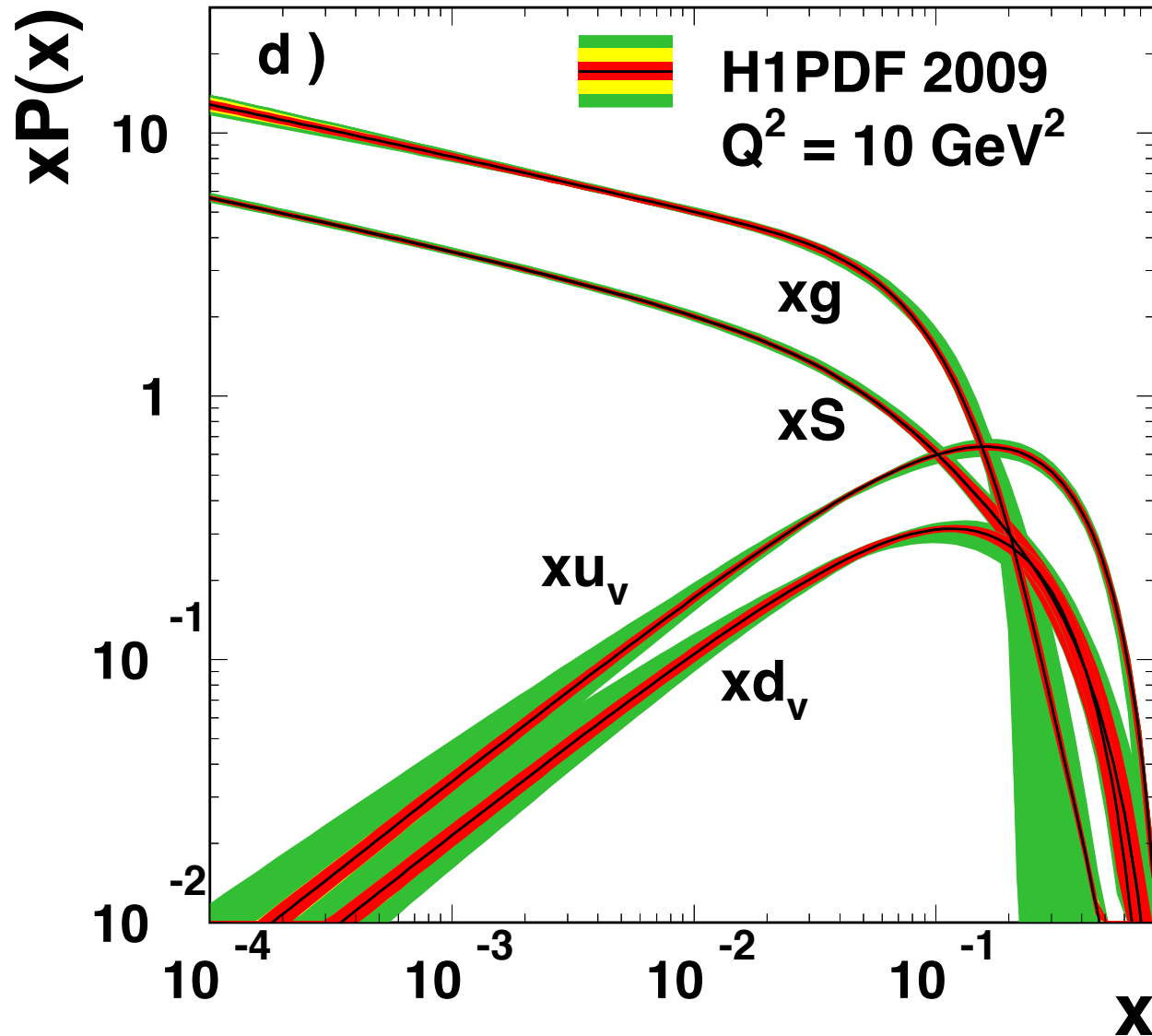
-further reduced with low energy and  $F_L$  data (cf Talks of J.Grebenyuk and V.Radescu)

- $Q_0^2$  variation mimics parameterisation uncertainty (yellow ~ green)

**Large uncertainty of gluon also at large  $x$**

Note that this fit describes the Tevatron jet data well.

## Evolution drives Gluon and Sea to large values at low $x$



Valence quarks remain rather unaffected as non-singlet quantities. Some constraints on valence quarks at low  $x$  may be expected from  $W^\pm$  asymmetry data at the LHC. At high  $x$   $d_v$  remains uncertain.



## Summary

Recent data have been presented on the reduced cross section at  $y < 0.6$ ,  $12 \leq Q^2 \leq 150 \text{ GeV}^2$

These represent the most accurate data on the proton structure function  $F_2$  obtained so far.

The evolution of the measurements of  $F_2$  over the past almost 20 years has been consistent and lead to a reduction of the uncertainties from initially  $\sim 20\%$  to nearly 1% now.

The data have been used in the combination with the ZEUS data and while dominating the combination in the here covered region of phase space they are still improved by the average.

The partial derivative of  $F_2(x, Q^2)$  wrt.  $\ln(x)$  is about constant at low  $x$  in the DIS region of  $Q^2$ .

A refined NLO QCD fit was made with a minimum number of parameters on the chosen initial parton distributions,  $xg$ ,  $xu_v$ ,  $xd_v$ , and the total up and down anti-quark distributions.

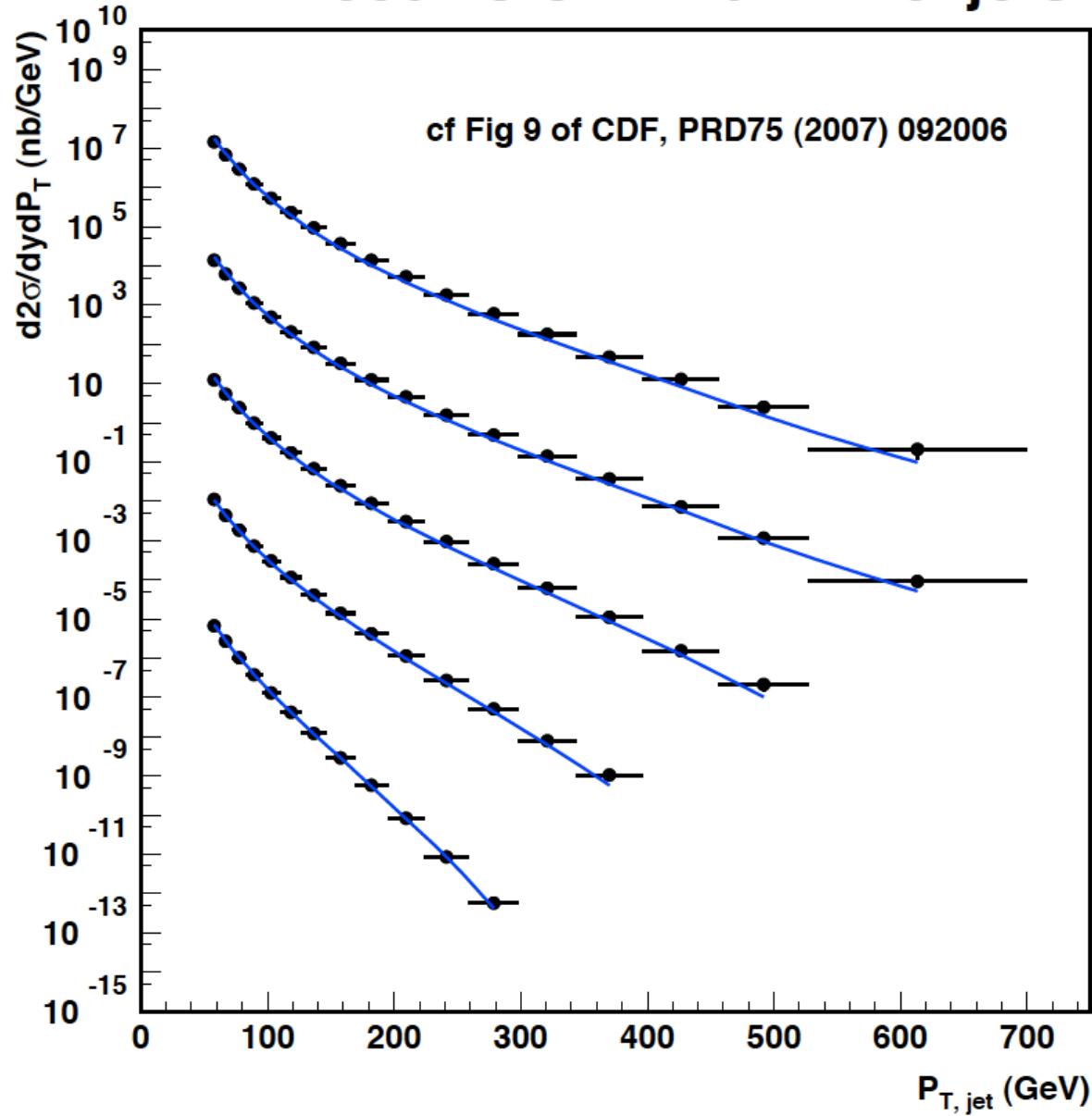
The  $\ln Q^2$  derivative is described by NLO QCD and in accord with a rising gluon density at low  $x$ .

The fit method attempts to quantify the uncertainty due to the parameterisations of the pdf's in a way, which has been adopted in the HERAPDF1.0 subsequent fit.

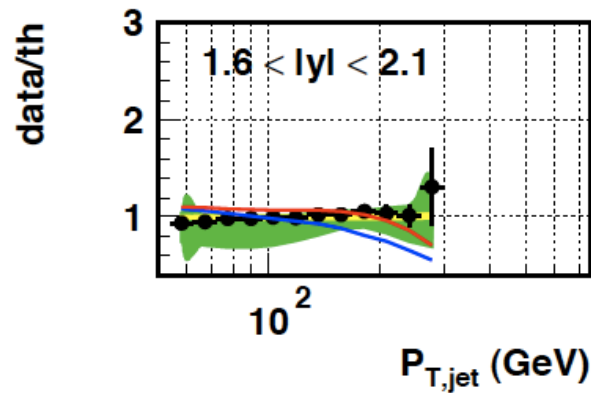
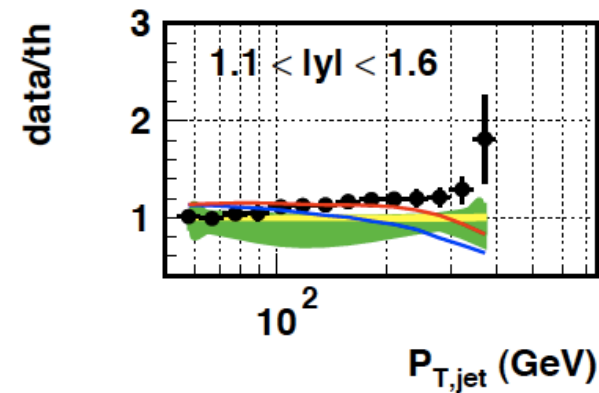
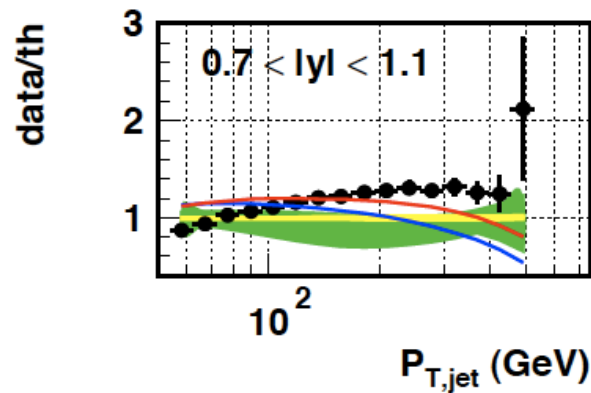
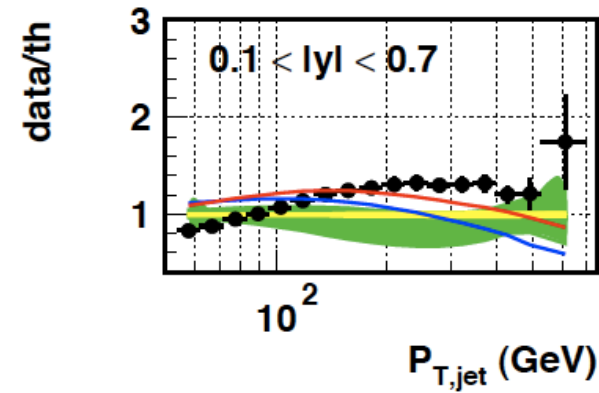
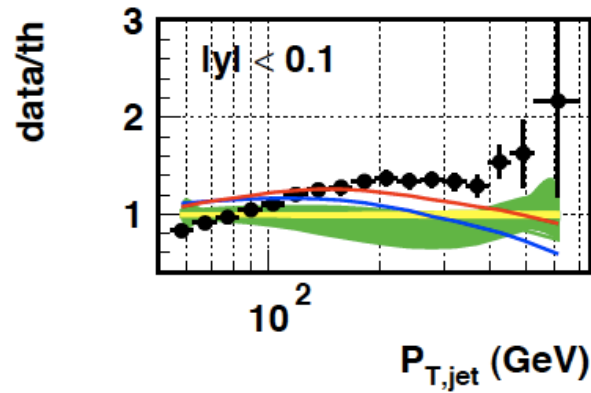
Overall there is very good agreement with NLO QCD, yet much is still to be learned on the structure of the proton and its inherent parton dynamics [cf further talks and the future..].

**Backup**

# H1 PDF2009 vs CDF RunII inc. jets



# H1PDF2009 vs CDF RunII inc. jets



• CDF RunII, KT D=0.7  
(raw data points)

■ H1pdf2009 (model + param)

— H1pdf2k / H1pdf2009

— ZEUS-Jets / H1pdf2009

## Consistency of 96/97 and 2000 data

**Table 5** Shifts in the central values of the systematic uncertainties determined for the combination of the 1996/1997 data at  $E_p = 820$  GeV and the 2000 data at  $E_p = 920$  GeV. The value for each shift is given in units of the original uncertainty. Note that for the two data sets some of the correlated systematic error sources were defined differently

Systematic source	Shift	
	1996/1997	2000
$E'_e$ scale	0.72	0.50
$E'_e$ linearity	–	–0.39
Polar angle $\theta_e$	–0.46	0.09
LAr hadronic scale	–0.86	–0.13
LAr noise	–0.22	0.04
SpaCal hadronic scale	–	0.35
$\gamma p$ background	0.11	–0.11
Luminosity	0.64	–0.46