

# Precise measurement of DIS at low $Q^2$ and phenomenological fits

Alexey Petrukhin, DESY/ITEP  
(on behalf of the H1 Collaboration)



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# Content

- Deep Inelastic Scattering
- DIS cross section at low  $Q^2$
- Rise of  $F_2$  at low  $x$
- Model comparisons
- Conclusions

Submitted to EPJ:

H1 Collaboration. DESY-08-171, Apr 2009. 90pp.

arXiv:0904.0929 [hep-ex]

# NC cross section and structure functions

NC Reduced cross section:  $\sigma_r(x, Q^2)$

$$\frac{d^2 \sigma_{NC}(e^\pm p)}{dx dQ^2} = \frac{2\pi \alpha^2}{x Q^4} Y_+ \left[ F_2 - \frac{y^2}{Y_+} F_L \right]$$

$$Y_+ = 1 + (1-y)^2$$

$$R = \frac{F_L}{F_2 - F_L}$$

Dominant contribution

Sizeable only at high  $y$  ( $y > \sim 0.6$ )

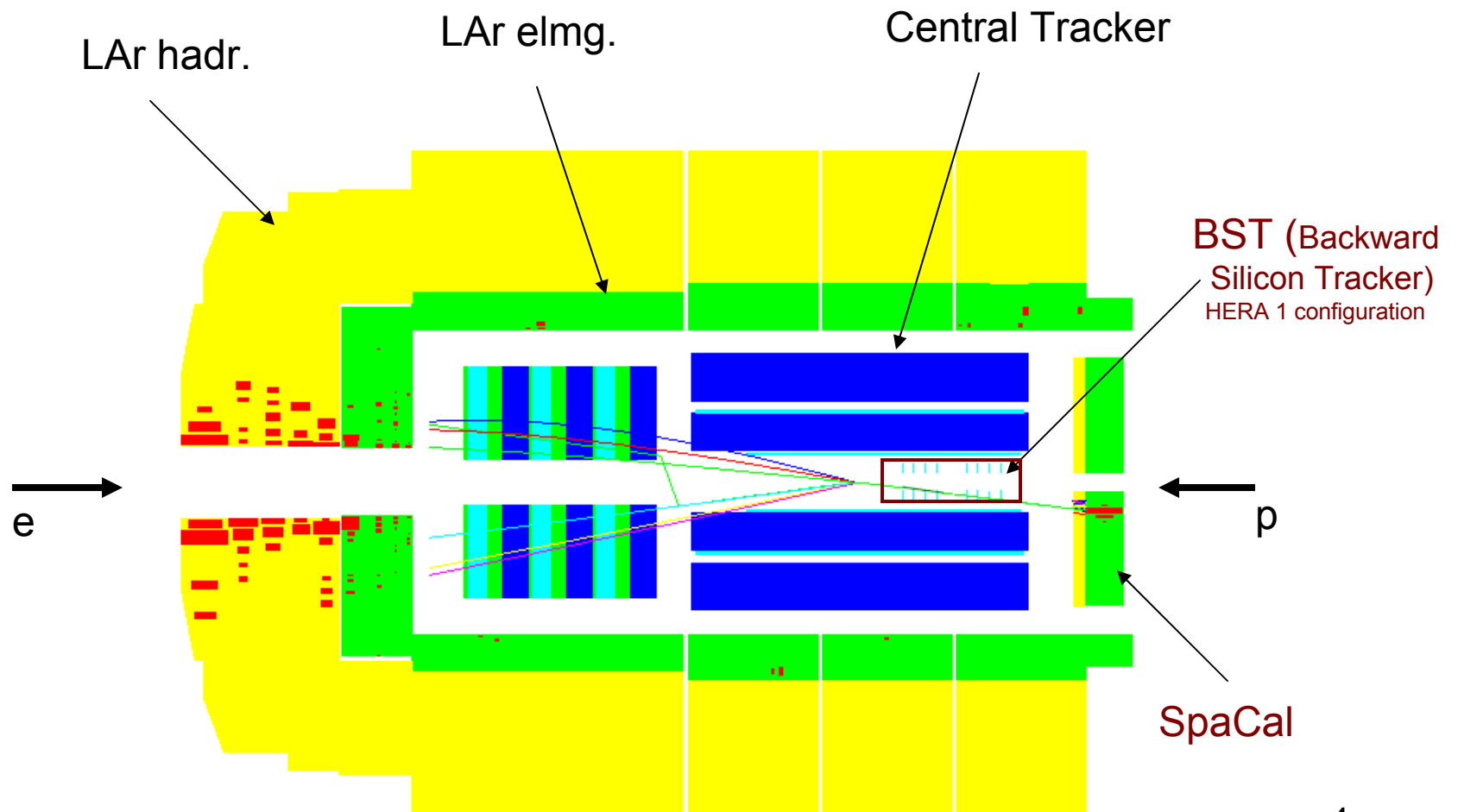
- The proton structure functions in QPM:

$$F_2(x) = \sum_i e_i^2 x [q_i(x) + \bar{q}_i(x)] - \text{sum of the (anti)quarks density distributions weighted with their electric charge squared}$$

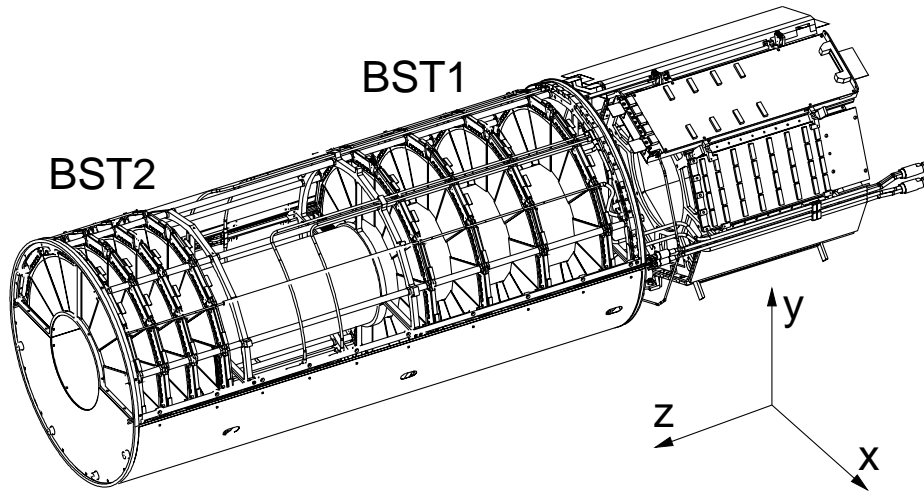
$$F_L(x) = 0$$

- In QCD:  $F_L(x, Q^2) \sim$  gluon density

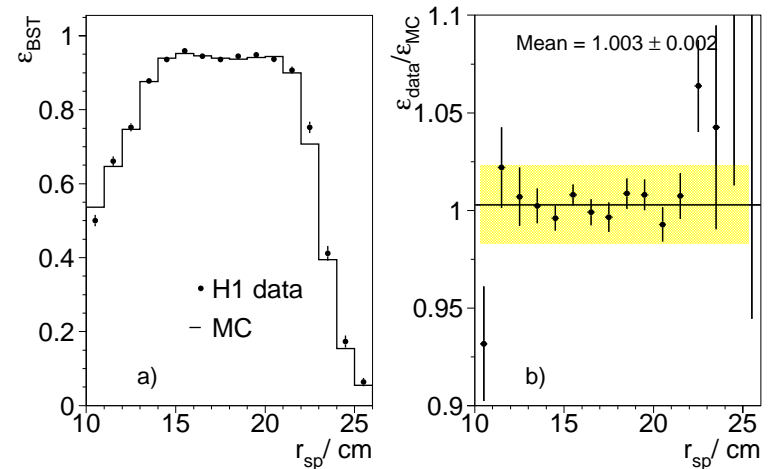
# Low $Q^2$ event in H1 detector



# Backward Silicon Tracker



- Consist of 8 planes and 16 sectors
- Acceptance:  $164^\circ < \theta_e < 178^\circ$
- Angular resolution: 0.1 mrad
- Hit resolution:  $\sim 20\mu\text{m}$
- Alignment accuracy:  $\sim 0.2$  mrad
- Track reconstruction efficiency:  $\sim 95\%$
- Used for reconstruction of vertex and  $\theta_e$

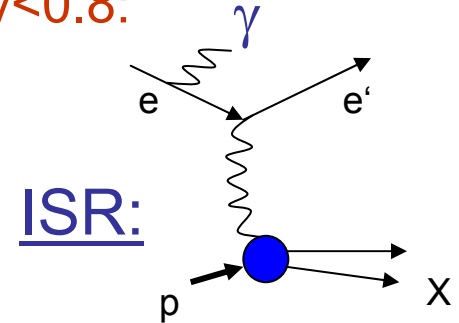


# Reconstruction of event kinematics

- ‘Electron method’- used for measurements at  $0.1 < y < 0.8$ :

$$y_e = \frac{2E_e - E'_e(1 - \cos \theta_e)}{2E_e} \equiv \frac{2E_e - \Sigma_e}{2E_e} \quad \text{where } \Sigma_e = (E - P_z)_{el}$$

$$Q_e^2 = \frac{E_e'^2 \sin^2 \theta_e}{1 - y_e} \quad \text{and} \quad x_e = \frac{Q_e^2}{4E_p E_e y_e}$$



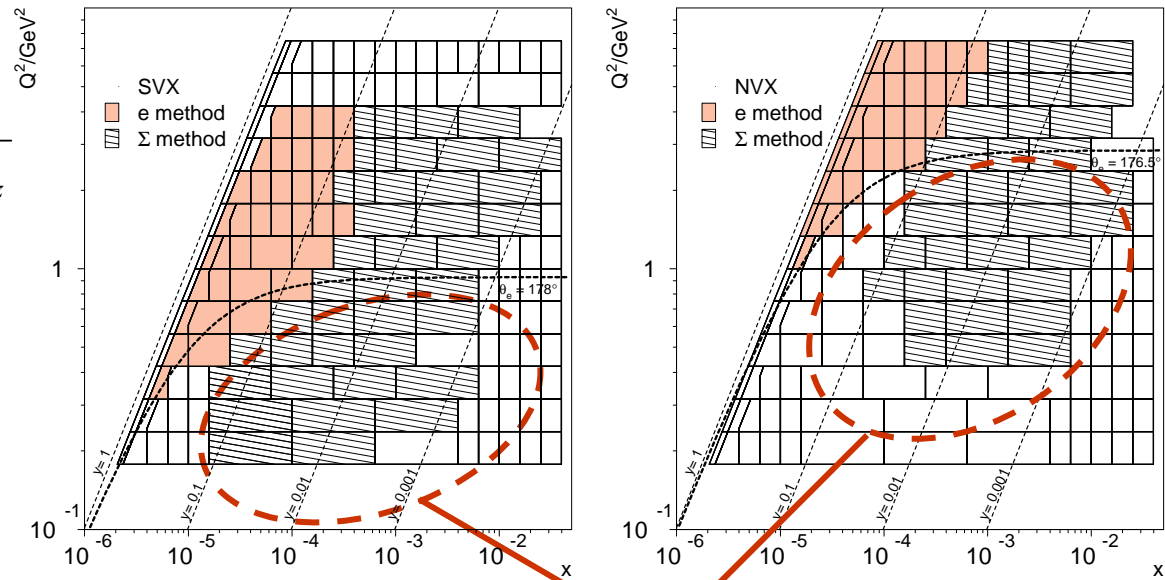
- ‘Sigma method’- used for  $0.002 < y < 0.1$  and also for low  $Q^2$  by accepting events with Initial State Radiation (ISR):

$$y_\Sigma = \frac{\Sigma_h}{\Sigma_h + E'_e(1 - \cos \theta_e)} = \frac{\Sigma_h}{E - P_z}$$

$$\Sigma_h = \sum_i (E_i^h - P_{z,i}^h)$$

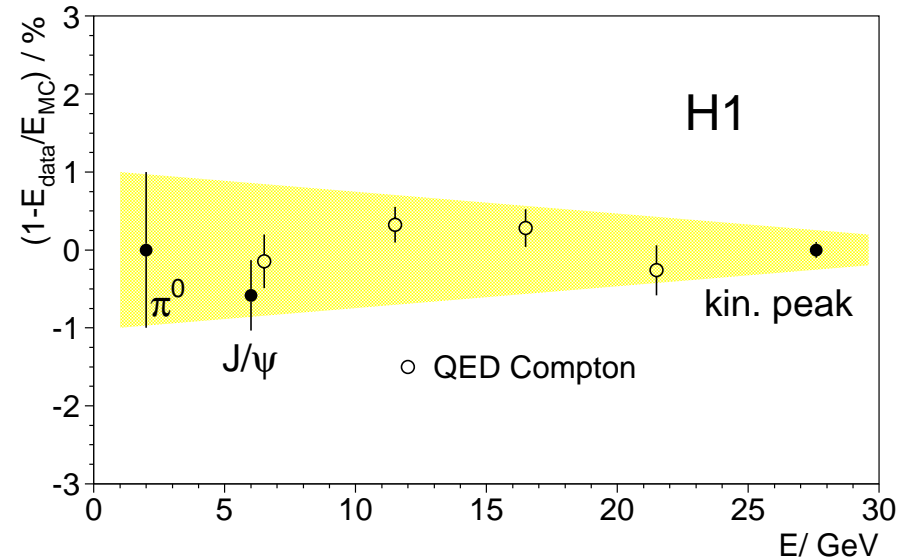
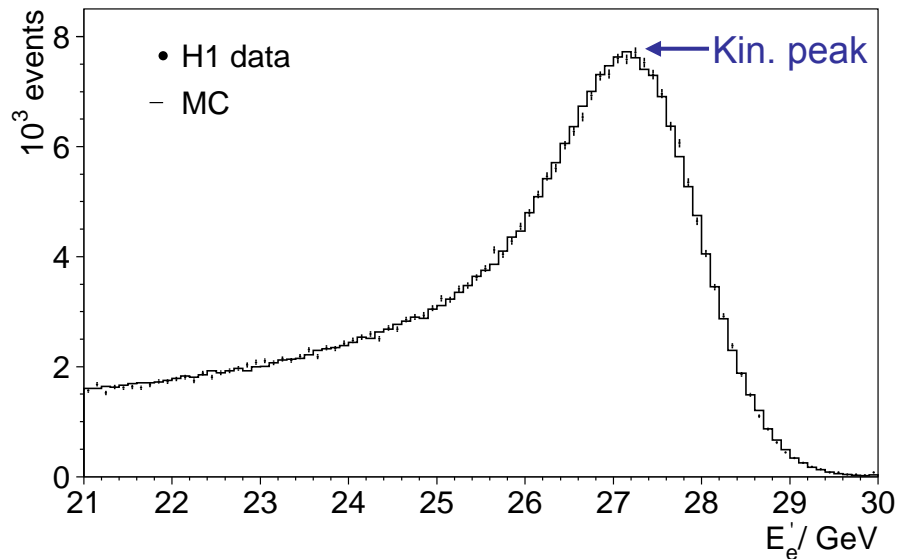
$$Q_\Sigma^2 = \frac{E_e'^2 \sin^2(\theta_e)}{1 - y_\Sigma}$$

$$x_\Sigma = \frac{Q_\Sigma^2}{2E_p y_\Sigma} \cdot \frac{1}{E - P_z}$$



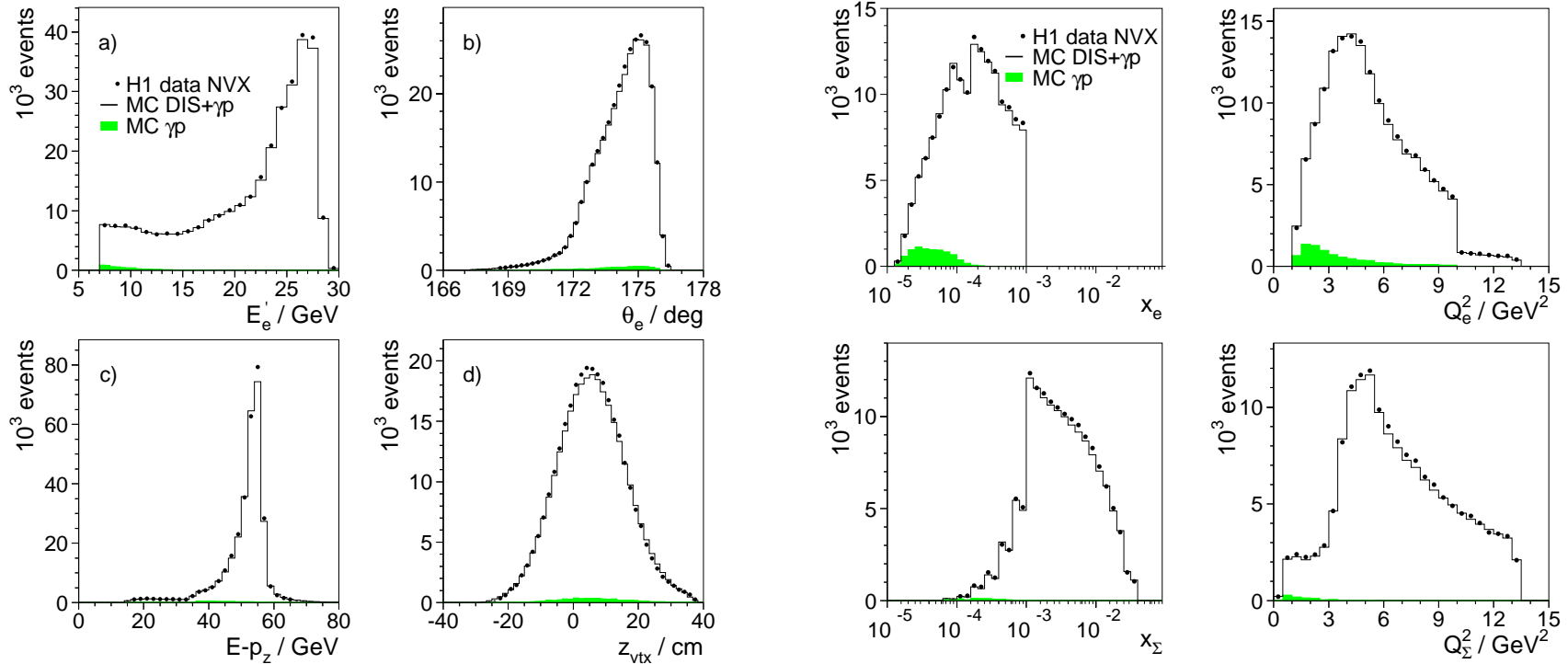
Extended by ISR

# Electron energy scale calibration



- Use multi-step calibration. Correct for the gain difference of PMTs and for non-uniformities of SpaCal
- Use  $\pi^0$  events to calibrate low energy, correct for non-linearity and check intermediate range with  $J/\psi$  and QED Compton events
- The precision of energy calibration: **0.2%** at 27.6 GeV to **1%** at 2 GeV

# Control distributions

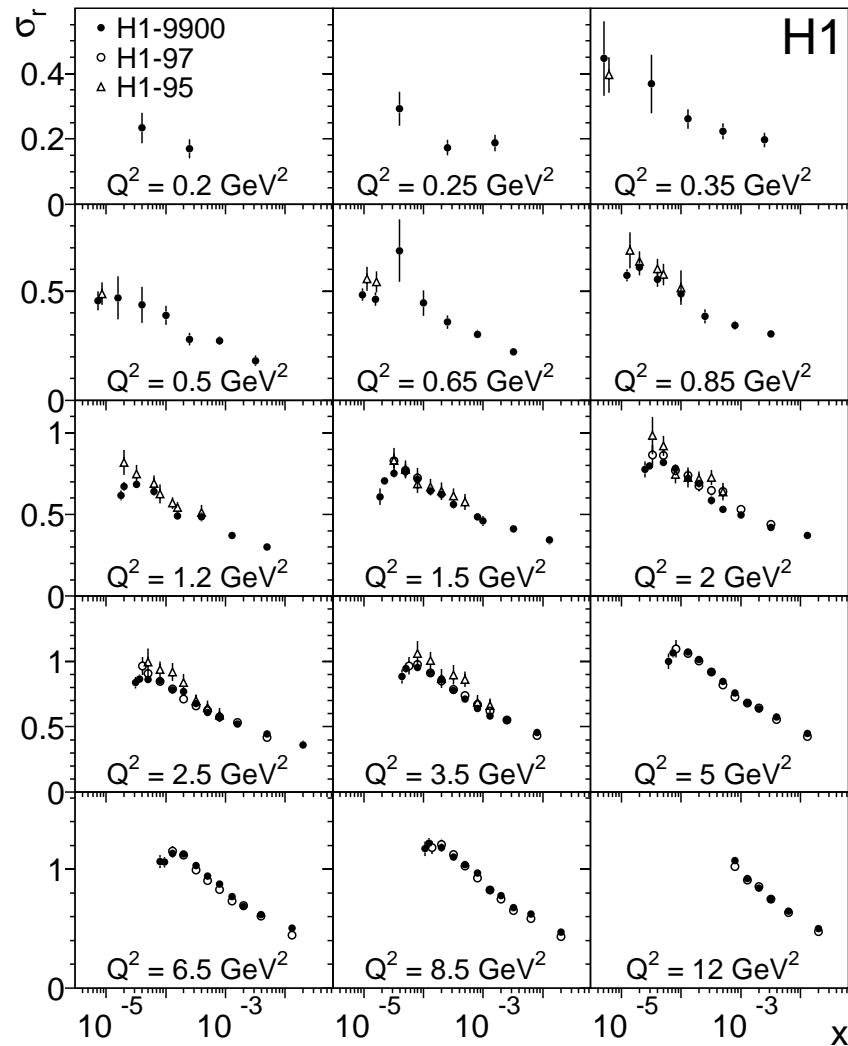


- Require a BST reconstructed vertex, SpaCal cluster and BST track matching this cluster

- Good understanding of detector acceptance and control of the  $\gamma$ p background



# $\sigma_r$ at low $Q^2$

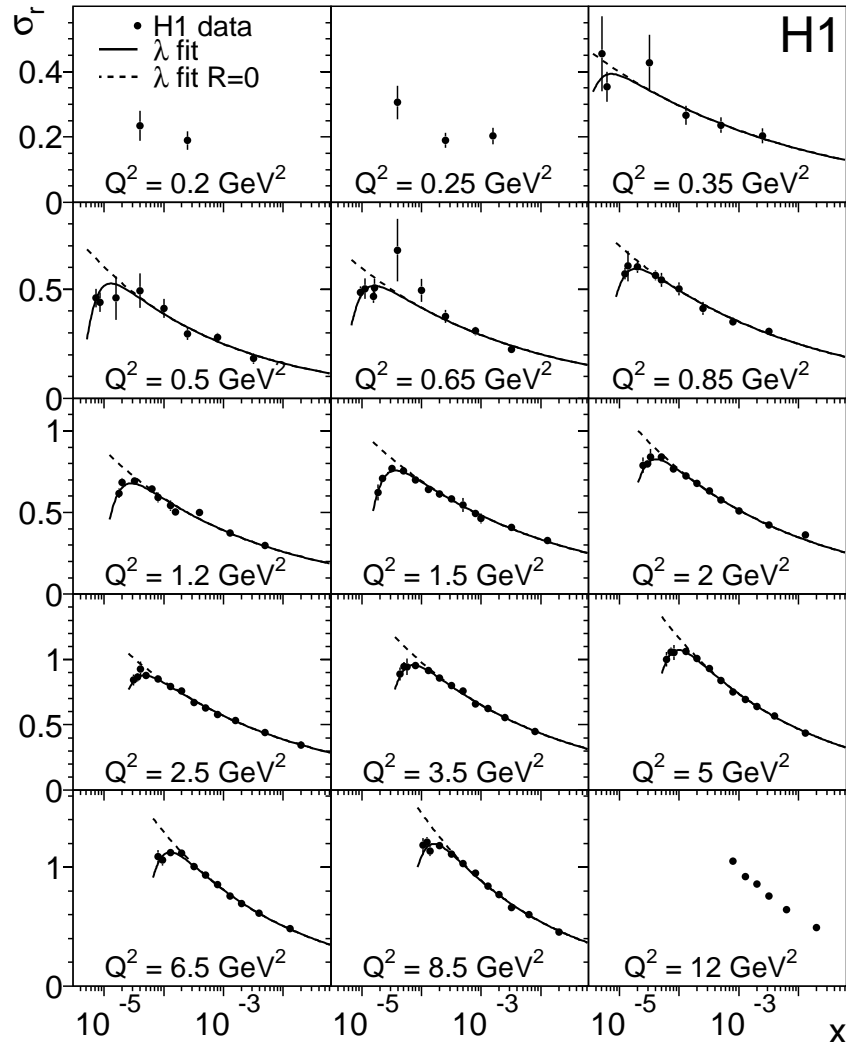


- New H1-9900 results extend H1 measurements to low  $Q^2$  and high  $x$  by using of ISR events
- Significant overlap between H1-9900 data and previously published results
- New (9900) data agree well with H1-97, these are corrected by +3.4% due to luminosity tagger acceptance change
- The 95 SVX data are consistent within 95 data normalisation uncertainty

# Combination of H1 data

- Combine 95, 97, SVX and NVX data taking into account bin-to-bin correlated systematic uncertainties
- For  $E_p=820$  GeV data, perform CME correction for  $y<0.35$ . Keep data separate for  $y\geq 0.35$
- Systematic errors assumed to be uncorrelated between the different data sets
- Good agreement between H1 data:  $\chi^2/n_{\text{dof}}=86/125$
- The precision of the combined data set is high, up to 1.5% in the central  $Q^2, x$  region of the measurement

# Combined reduced cross section $[F_2 - f(y)F_L]$



- Measured  $\sigma_r$  at low  $0.2 \leq Q^2 \leq 12 \text{ GeV}^2$  and  $5 \cdot 10^{-6} < x < 0.02$

- Rise of  $F_2$  towards low  $x$  may be described by  $F_2 = c(Q^2)x^{-\lambda(Q^2)}$  for  $x < 0.01$

- Fit  $x$ -dependences of  $\sigma_r$  in  $Q^2$  bins and extract  $c(Q^2)$ ,  $\lambda(Q^2)$  and  $R(Q^2)$ :

$$\sigma_r(Q^2, x) = c(Q^2)x^{-\lambda(Q^2)} \left[ 1 - \frac{y^2}{1 + (1-y)^2} \cdot \frac{R(Q^2)}{1 + R(Q^2)} \right]$$

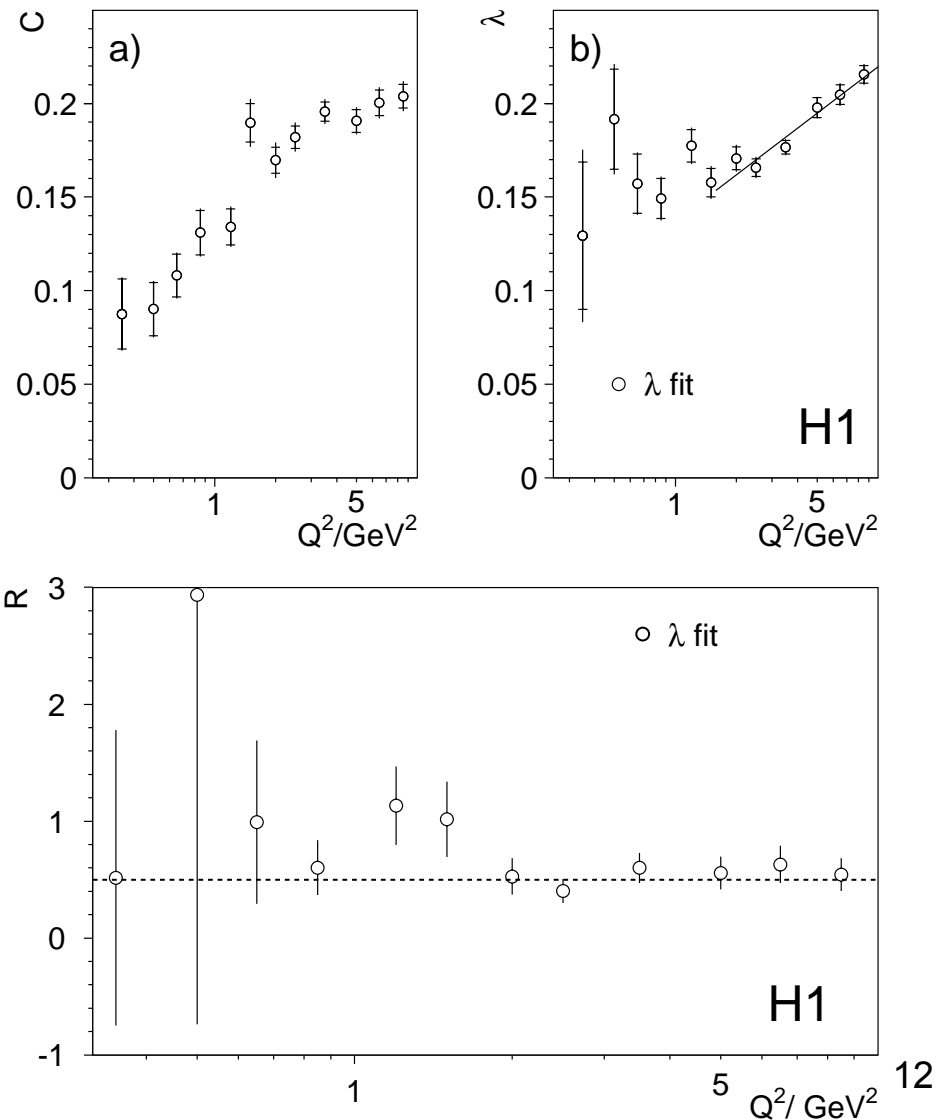
- Note: this extraction of  $R(Q^2)$  relies on the simple model used for  $F_2$

# Fit results

- $\lambda \sim \ln(Q^2/\Lambda^2)$  and  $c(Q^2) \sim \text{const.}$  for  $Q^2 > 1 \text{ GeV}^2$
- Around  $Q^2 = 1 \text{ GeV}^2$   $\lambda$  deviates from linear  $\ln(Q^2/\Lambda^2)$  dependence

H1 Collaboration, C. Adloff et al.,  
Phys.Lett. B520(2001)183 [hep-ex/0108035]

- The value of average  $R$  obtained from this model is consistent with  $R=0.5$ , higher vs direct  $F_L$  measurements



# Models

- **Fractal fit:** based on the concept of self similarity. Structure function  $F_2$  parameterised using 4 parameters  $Q_0, D_0, D_1, D_3$  with  $D_2=1.08$  :

$$F_2(Q^2, x) = D_0 Q_0^2 \left(1 + \frac{Q_0^2}{Q^2}\right)^{1-D_2} \frac{x^{-D_2+1}}{1 + D_3 - D_1 \ln x} \left( x^{-D_1 \ln \left[1 + \frac{Q_0^2}{Q^2}\right]} \left(1 + \frac{Q_0^2}{Q^2}\right)^{D_3+1} - 1 \right)$$

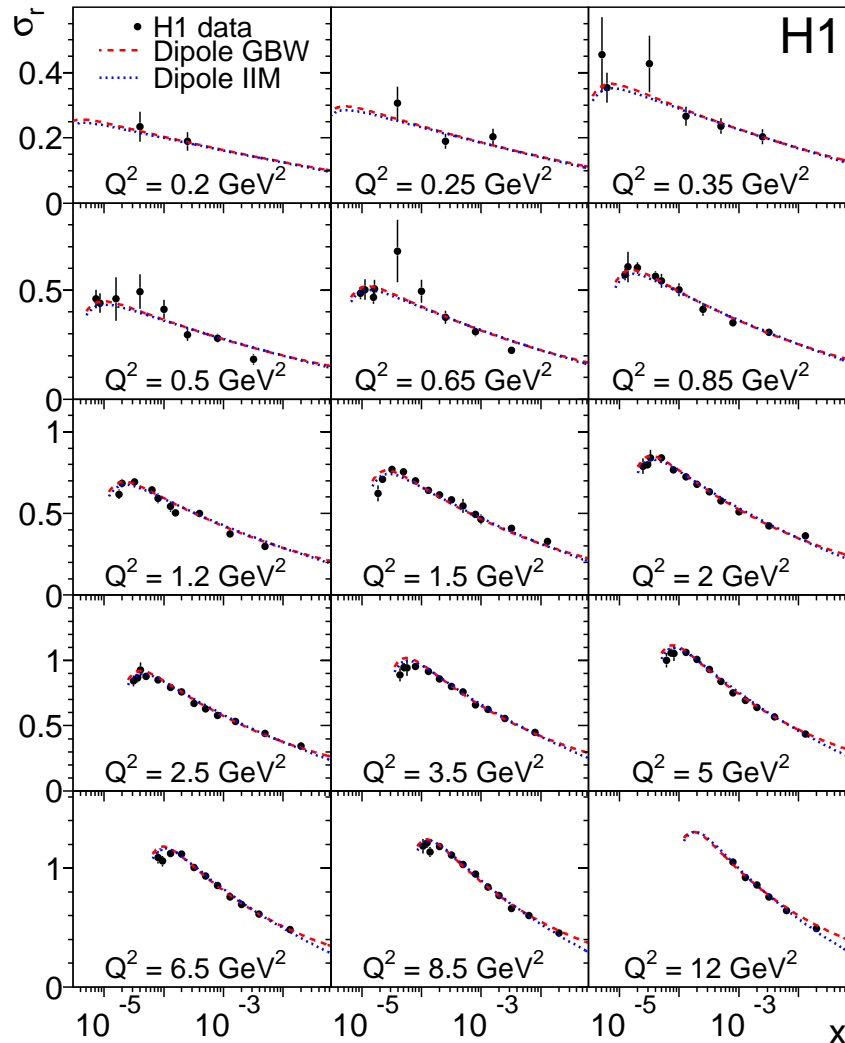
- No Fractal parameterisation for  $F_L$ , use  $F_L = \frac{R}{R+1} F_2$  with  $R$  as an additional parameter

- **Colour Dipole Model (CDM) fits:** 3 parameter fits.  $\gamma^*p$  scattering via  $\gamma^*$  splitting into dipole which scatters off the proton. In the GBW (Golec-Biernat & Wusthoff) model the dipole-proton cross section is given by

$$\hat{\sigma}(x, r) = \sigma_0 \left\{ 1 - \exp\left[-r^2 / (4r_0^2(x))\right] \right\} \quad \text{with } r_0^2(x) \sim (x/x_0)^\lambda$$

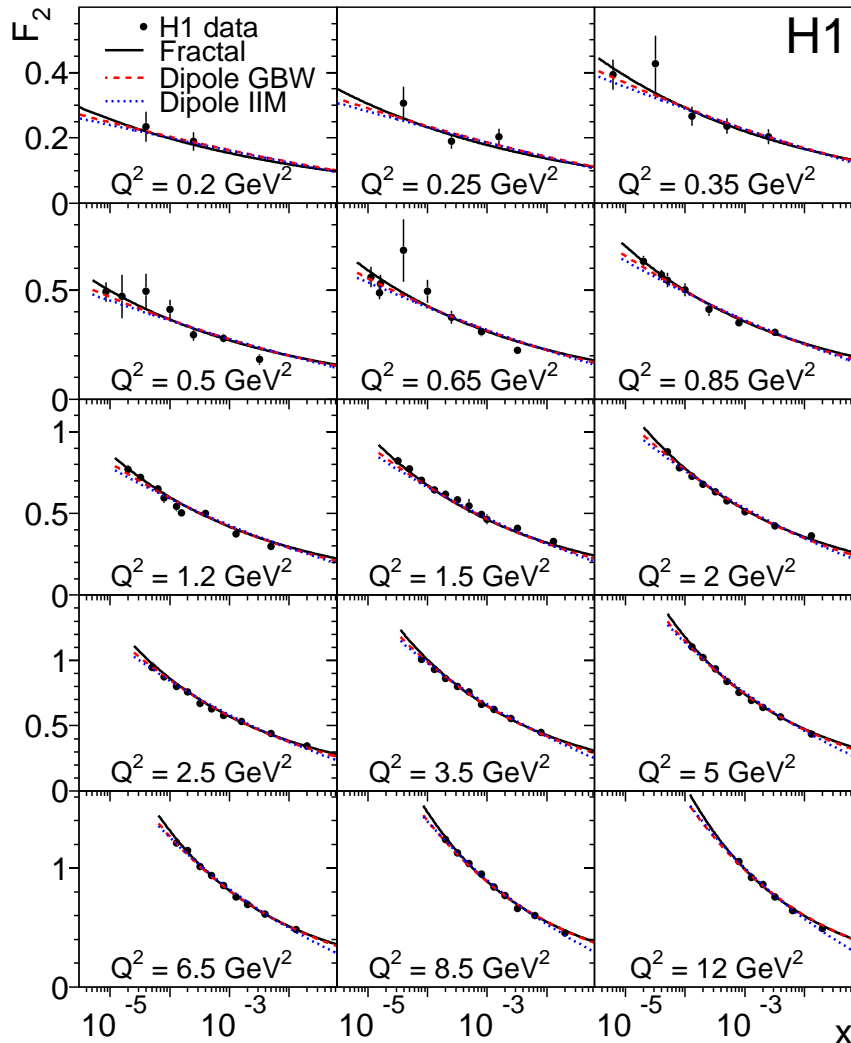
- $r$  corresponds to transverse quark-antiquark separation.  $\lambda, x_0$  and  $\sigma_0$  are parameters of the model. For  $r \gg r_0$ , **GBW** model predicts a saturation with a constant  $\hat{\sigma} \approx \sigma_0$  at  $x = x_s$
- Another Dipole fit **IIM** (Iancu, Itakura & Munier) uses different model of cross section  $\hat{\sigma}$
- These two models are considered here as representative for a much larger variety of Dipole models

# $\sigma_r$ and Dipole models



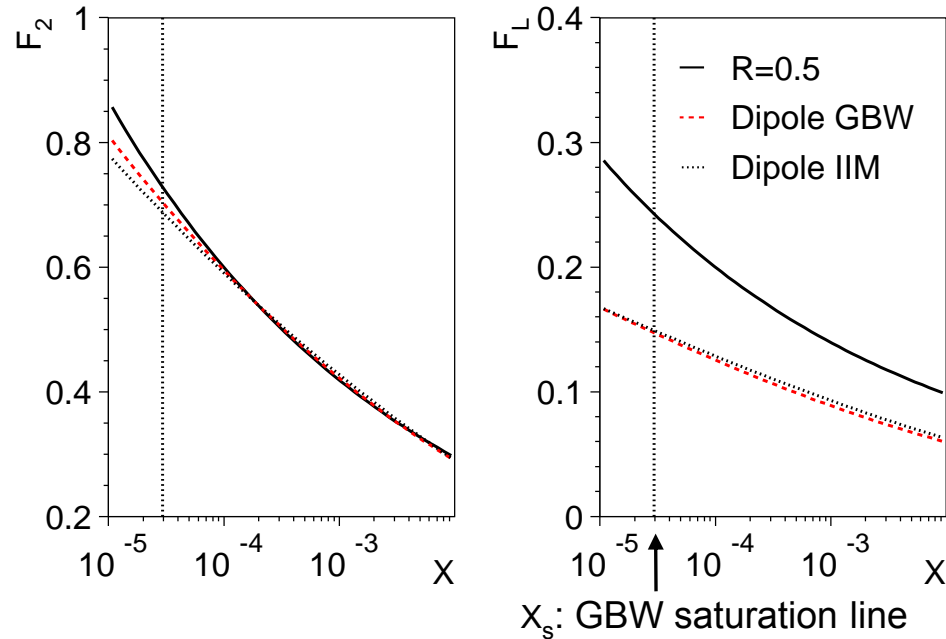
- H1 cross section data are well described by GBW & IIM Dipole fits
- GBW fit yields a  $\chi^2/n_{\text{dof}} = 183.1/(149-3)$  and IIM a  $\chi^2/n_{\text{dof}} = 178.2/(149-3)$

# $F_2$ and models



- Restrict  $F_2$  extraction to  $y < 0.6$  where effect from  $F_L$  is small
- Steeper rise of  $F_2$  from Fractal fit as compared to Dipole fits
- The Fractal fit describes data well with  $\chi^2/n_{\text{dof}} = 155.3/(149-5)$

# $F_2$ and $F_L$ from models



$$F_L = \frac{R}{1+R} \cdot F_2$$

- $F_2$  for  $Q^2=1.2 \text{ GeV}^2$  from the Fractal and Dipole fits to H1 data.  $F_L$  from Dipole fits and using  $F_2$  from Fractal fit assuming  $R=0.5$
- Good agreement between 3 models in  $F_2$  apart from lowest  $x$ . Dipole models predict softer  $F_2$  dependence for  $x < x_s$
- The  $F_L$  predictions of Dipole models are nearly half of the Fractal result
- Formally allow  $F_L$  in Dipole models to scale independently of  $F_2$

$$F_L(x, Q^2) = F_L^{Dipole}(x, Q^2)(1 + B_L)$$

- $B_L = 0.54 \pm 0.15$  (GBW) and  $B_L = 0.17 \pm 0.14$  (IIM), i.e. IIM model gives consistent description of data
- Steeper  $F_2$  in lambda and Fractal fits lead to large  $R$ . Softer  $F_2$  of IIM allows to describe data with smaller  $F_L$



# Conclusions

- The analysis of the H1 low  $x$  and  $Q^2$  data from HERA-1 is submitted for publication [[H1 Collaboration. DESY-08-171, Apr 2009. 90pp. arXiv:0904.0929 \[hep-ex\]](#)]
- A coherent data set is presented, combining data from dedicated running periods in 1995-2000
- The measurement of the reduced cross section reaches 1.5% precision
- The transition region from non-perturbative to deep inelastic behaviour is generally well described by the phenomenological models
- In the deep inelastic region, the data are used as input for the new NLO QCD analysis of H1 [H1PDF2009, cf talk of J.Kretzschmar]
- A power law parameterisation of  $F_2$  leads to  $R$ , which is about twice larger compare to Dipole models and the direct measurements of  $F_L$  [cf talk of A.Glazov]