

Scaled momentum distributions of charged particles in dijet photoproduction

ZEUS Collaboration

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Talk outline

- 1 Theoretical framework:
 - The MLLA and LPHD;
 - Physics motivation.
- 2 Physics Analysis:
 - Analysis strategy;
 - Data selection.
- 3 Results:
 - The measured ξ distributions;
 - Extraction of theoretical parameters;
 - Global comparisons.
- 4 Summary.

The MLLA + LPHD Theoretical Framework

The Modified Leading Log Approximation (MLLA)

- All orders pQCD resummation.
- Analytical description of parton evolution.
- Predicts parton multiplicity and momenta.
- MLLA describes fragmentation with 2 parameters:
 - Q_0 - A self-imposed cut-off energy scale.
 - Λ_{eff} - Absolute minimum cut-off of the theory.
- Predictions only physical with $Q_0 \geq \Lambda_{\text{eff}} > \Lambda_{\text{QCD}}$.
- Limiting spectrum defined such that, $Q_0 = \Lambda_{\text{eff}}$.
- Λ_{eff} predicted to be universal.
- We study MLLA within jets, where fragmentation is well defined.
- Assuming **Local Parton Hadron Duality** MLLA predictions are directly comparable to data.

The MLLA + LPHD Theoretical Framework

The Local Parton Hadron Duality (LPHD) Hypothesis

- Simple non-perturbative hypothesis.
- Assumes hadronisation is local and occurs at the end of the parton shower.
- Event topology is defined in the perturbative phase.
- Relates the observed hadron distributions to the calculated parton distributions via a single constant factor, κ_{ch} .

$$O(x_1, x_2, \dots)|_{\text{hadrons}} = \kappa_{\text{ch}} O(x_1, x_2, \dots, \Lambda_{\text{eff}})|_{\text{partons}}$$

What is κ_{ch} ?

- κ_{ch} is the ratio of the number of charged particles over the total number of partons produced during fragmentation.
- From isospin invariance, expect $\kappa_{\text{ch}} \approx 2/3$
- 2 free parameters in MLLA + LPHD: Λ_{eff} and κ_{ch} .

Physics Motivation

Investigating the limits of the MLLA

- Λ_{eff} and κ_{ch} have been measured using 359pb^{-1} γP data collected using the ZEUS detector.
- The measurement was performed at various energy scales and within cones of various opening angles, θ_C , around the jet axis.

Is Λ_{eff} universal?

- Λ_{eff} previously measured for ee , eP & $P\bar{P}$. Never for γP .
- Is Λ_{eff} independent of interaction type? ee , eP , $P\bar{P}$, γP .
- Is Λ_{eff} independent of E_{Jet} and θ_C , as predicted?

How to measure Λ_{eff} and κ_{ch}

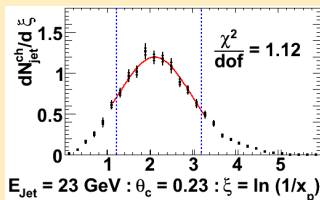
Outline of analysis

- Select dijet photoproduction events from 359pb^{-1} ZEUS data.
- Measure scaled track momentum within jets, $x_p = \frac{P_{\text{track}}}{P_{\text{Jet}}}$.
- Plot scaled momentum distributions, $\xi = \ln\left(\frac{1}{x_p}\right)$, in bins of jet energy $E_{\text{Jet}} = \frac{M_{2j}}{2}$ (the hard scale) and θ_c (the opening angle).

Fitting ξ distributions

- 2 methods:
 - Gaussian around mean;
 - MLLA + LPHD theory.
- ξ_{peak} , Λ_{eff} and κ_{ch} extracted from fits.

Sneak preview - a ξ distr.



Λ_{eff} dependence on jet opening angle, θ_c

MLLA predicts $E_{\text{Jet}} \sin(\theta_c)$ scaling

- Sequentially emitted partons are constrained to smaller angles due to enforced angular ordering.
- Scaling violations expected to occur at large θ_c as MLLA is only strictly valid in the collinear approximation.

Testing for scaling violations

- Calculate angle, θ_i , of each constituent particle from jet axis, working in the centre-of-mass frame, as θ_i not Lorentz invariant.
- Plot ξ distributions enforcing a maximum $\theta_i \leq \theta_c$ cut.
- The values of θ_c used are:
 - $\theta_c = 0.23$
 - $\theta_c = 0.28$
 - $\theta_c = 0.34$

Data Selection

Jet selection

- Jets were reconstructed using the k_T cluster algorithm in the longitudinally invariant inclusive mode.
- $E_T^{\text{Jet1}} \geq 17 \text{ GeV}$
- $E_T^{\text{Jet2}} / E_T^{\text{Jet1}} \geq 0.8$
- $0.9\pi \leq |\phi^{\text{Jet1}} - \phi^{\text{Jet2}}|$
- $|\eta^{\text{Jet1,2}}| \leq 1.0$
- $E_T^{\text{Jet3}} \leq 6 \text{ GeV}$
- $|\eta^{\text{Jet3}}| \leq 2.4$

Additional cuts

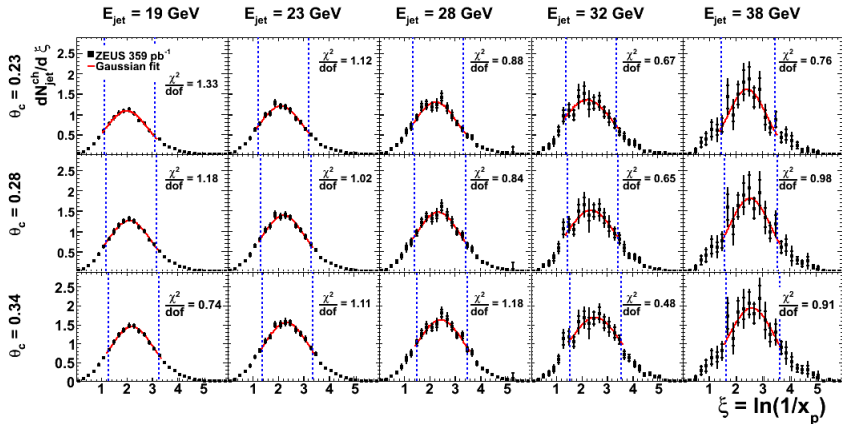
- $0.2 \leq y \leq 0.85$
- $Q^2 \leq 1 \text{ GeV}^2$
- $x_\gamma^{\text{OBS}} \geq 0.75$

Tracking cuts

- $p_T^{\text{track}} \geq 150 \text{ MeV}$
- $|\eta^{\text{track}}| \leq 1.7$
- MC Truth lifetime $\geq 0.01 \text{ ns}$

23,449 events were selected from 359 pb^{-1} of ZEUS data.

The measured ξ distributions



359 pb^{-1} ZEUS data shown in bins of E_{Jet} and θ_c

- The Gaussian fits are shown. $0.48 \leq \chi^2/\text{dof} \leq 1.33$
- Blue lines indicate fitted region, ± 1 around mean.

Determining ξ_{peak} , Λ_{eff} and κ_{ch} - 2 methods:

1 The Gaussian fit method:

- Gives peak position of ξ distribution, ξ_{peak} ;
- ξ_{peak} gives Λ_{eff} - Only valid for Leading Order (LO).

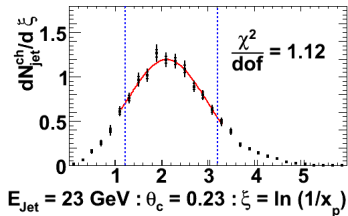
2 The MLLA+LPHD fit method:

- Gives Λ_{eff} and K (the normalisation) directly from fit;
- κ_{ch} is calculated from K ;
- Λ_{eff} has strong dependence on ambiguous fit range;
- κ_{ch} only weakly dependant on the fitting range.

The results presented here use:

- 1 The Gaussian method for ξ_{peak} and Λ_{eff} ;
- 2 The MLLA+LPHD method for κ_{ch} and to cross check Λ_{eff} .

The Gaussian fit method



Peak position, ξ_{peak}

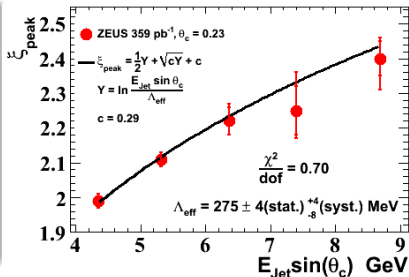
- Fit Gaussian ± 1 around mean.
- $\forall \xi$, independently measure ξ_{peak} .

$$\Lambda_{\text{eff}} = \frac{E_{\text{Jet}} \sin(\theta_c)}{e^{\left(\sqrt{0.87 + 2\xi_{\text{peak}}} - 0.54\right)^2}} \quad (@ \text{ LO})$$

Measuring Λ_{eff}

- Only use $\theta_c = 0.23$ energy points:
 - Different θ_c values are correlated;
 - MLLA loses validity at large θ_c .
- Fit equation to all 5 energy points.

$$\Lambda_{\text{eff}} = 275 \pm 4 \text{ (stat.)}_{-8}^{+4} \text{ (syst.) MeV}$$



The MLLA + LPHD fit method

Momentum distribution of partons from a gluon is given by:

- $$\bar{D}_{g\text{-Jet}}^{\text{lim}} \left(\ln \left(\frac{1}{x_p} \right), Y \right) = \frac{4C_f}{b} \Gamma(B) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} e^{-B\alpha} \left[\frac{\cosh \alpha + (1-2\zeta) \sinh \alpha}{\frac{4N_c}{b} Y \frac{\alpha}{\sinh \alpha}} \right]^{\frac{B}{2}}$$

$$\cdot I_B \left(\sqrt{\frac{16N_c}{b} Y \frac{\alpha}{\sinh \alpha} [\cosh \alpha + (1-2\zeta) \sinh \alpha]} \right) \frac{d\tau}{\pi}$$
- Valid for: $\ln \left(\frac{1}{x_p \ll 1} \right) \leq \ln \left(\frac{1}{x_p} \right) \leq \ln \left(\frac{M_{2j}}{2P_0} \right)$ $P_0 =$ Upper bound

For number of flavours, $N_f = 3$, and number of colours, $N_c = 3$

- $C_f = \frac{9}{4}$, $b = 9$, $B = 1.247$.
- I_B is the modified Bessel function of order B .
- $\alpha = \alpha_0 + i\tau$, where α_0 is determined by $\tanh \alpha_0 = 2\zeta - 1$
- $\zeta = 1 - \frac{\ln \left(\frac{1}{x_p} \right)}{Y}$ and $Y = \ln \left(\frac{E_{\text{Jet}} \sin(\theta_c)}{\Lambda_{\text{eff}}} \right)$ $\bar{D}_{q\text{-Jet}}^{\text{lim}} = \frac{1}{r} \bar{D}_{g\text{-Jet}}^{\text{lim}}$

Quarks, gluons and the next-to-MLLA predictions

Quark and gluon jet mixture

- In γP events there is a mix of quark and gluon jets.

$\bar{D}_{\text{mix}}^{\text{lim}} = \left(\epsilon_g + \frac{1-\epsilon_g}{r} \right) \bar{D}_{\text{g-Jet}}^{\text{lim}}$, where ϵ_g is the fraction of gluon jets.

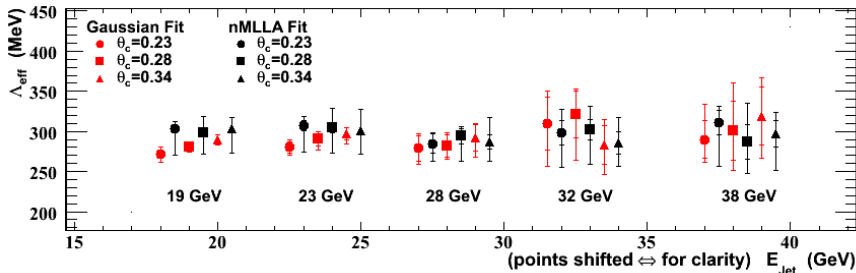
Energy (GeV)	19	23	28	32	38
ϵ_g (From PYTHIA)	0.203	0.213	0.211	0.227	0.242

The so called "next-to-MLLA" predictions

- Not actually higher order calculation, but a modification of MLLA.
- In nMLLA, $\bar{D}_{\text{mix}}^{\text{lim}} = F_{\text{nMLLA}} \left(\epsilon_g + \frac{1-\epsilon_g}{r} \right) \bar{D}_{\text{g-Jet}}^{\text{lim}}$
- Where $r = 1.6 \pm 0.2$ and $F_{\text{nMLLA}} = 1.3 \pm 0.2$ (from theory).
- When fitting to data the normalisation can be expressed as:

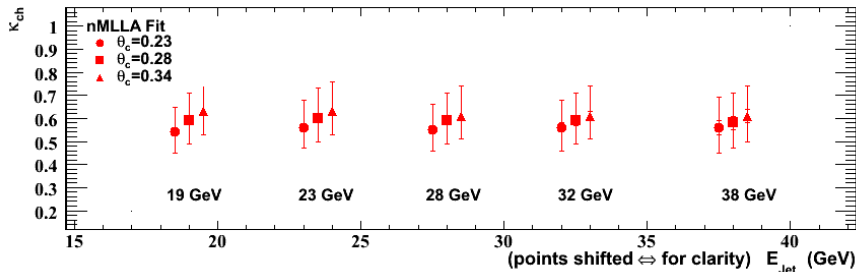
$$K = \kappa_{\text{ch}} F_{\text{nMLLA}} \left(\epsilon_g + \frac{1-\epsilon_g}{r} \right)$$

Λ_{eff} - Comparison of extraction methods



Λ_{eff} extracted from 359pb^{-1} ZEUS data via both methods

- $\forall \xi$, independently extract Λ_{eff} : Red = Gaussian. Black = nMLLA.
- Λ_{eff} has a weak dependence on θ_c , no dependence on scale.
- nMLLA, $\theta_c = 0.23$: $\Lambda_{\text{eff}} = 304 \pm 6$ (stat.) $^{+8}_{-32}$ (syst.) MeV
- Large nMLLA systematics come from ambiguous fitting range.
- nMLLA regularisation scheme \Rightarrow Parton cut-off at $p_T^{\text{rel,pl}} = \Lambda_{\text{eff}}$

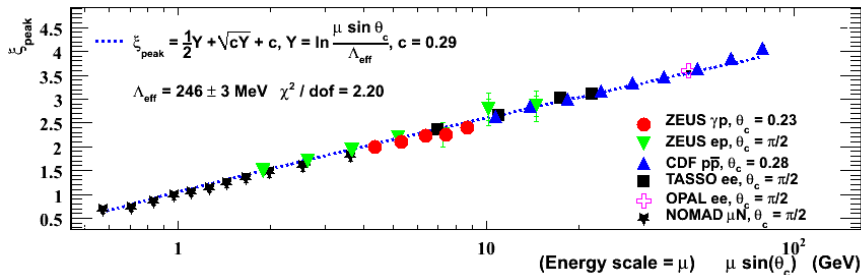
κ_{ch} 

κ_{ch} extracted from 359pb¹ ZEUS data via nMLLA method

- κ_{ch} comes from the normalisation of ξ
- κ_{ch} is insensitive to the ambiguous fitting range.
- κ_{ch} has a weak dependence on θ_c , no dependence on scale.
- Theoretical uncertainties dominate the overall uncertainty.

$$\kappa_{\text{ch}} = 0.55 \pm 0.01 \text{ (stat.)}_{-0.02}^{+0.03} \text{ (syst.)}_{-0.09}^{+0.11} \text{ (theo.)}$$

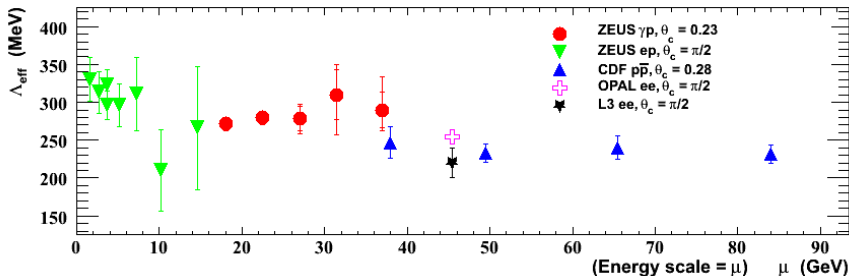
Global Comparisons - ξ_{peak}



Global fit gives $\Lambda_{\text{eff}} = 246 \pm 3 \text{ MeV}$ with $\chi^2 / \text{dof} = 2.20$

- The fit assumes that Λ_{eff} is independent of scale and θ_c .
- Both ZEUS and CDF observe a weak θ_c dependence.
- CDF also observe a weak scale dependence:
 - Λ_{eff} observed to decrease with increasing energy.
- May explain why this is inconsistent with ZEUS only fit result.

Global Comparisons - Λ_{eff}



Global results for Λ_{eff} as a function of energy scale.

- 359pb^{-1} ZEUS data fills the gap from $19 \rightarrow 38$ GeV.
- First measurement of Λ_{eff} from γp process.
- I will update this plot in a few years with LHC data to ~ 4 TeV.

Summary

Summary

- Scaled momentum distributions have been measured in dijet events in 359pb^{-1} γp ZEUS data.
- Λ_{eff} and κ_{ch} have been extracted at energy scales from $19 \rightarrow 38$ GeV.

$$\Lambda_{\text{eff}} = 275 \pm 4 \text{ (stat.)}_{-8}^{+4} \text{ (syst.) MeV}$$

$$\kappa_{\text{ch}} = 0.55 \pm 0.01 \text{ (stat.)}_{-0.02}^{+0.03} \text{ (syst.)}_{-0.09}^{+0.11} \text{ (theo.)}$$

Publication

- Pre-print on arXiv : [hep-ex/0904.3466](https://arxiv.org/abs/hep-ex/0904.3466)
- Submitted to JHEP.