

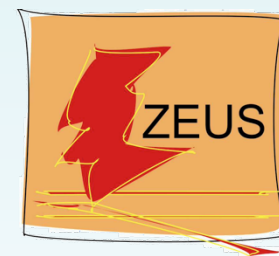
# Jet cross sections and $\alpha_s$ in DIS and photoproduction at HERA

DIS09, Madrid, 26<sup>th</sup>–30<sup>th</sup> April 2009

**Claire Gwenlan** (University of Oxford, STFC Advanced Fellow)  
on behalf of the ZEUS collaboration

## Outline

- motivation
- jet cross section measurements
- strong coupling,  $\alpha_s$



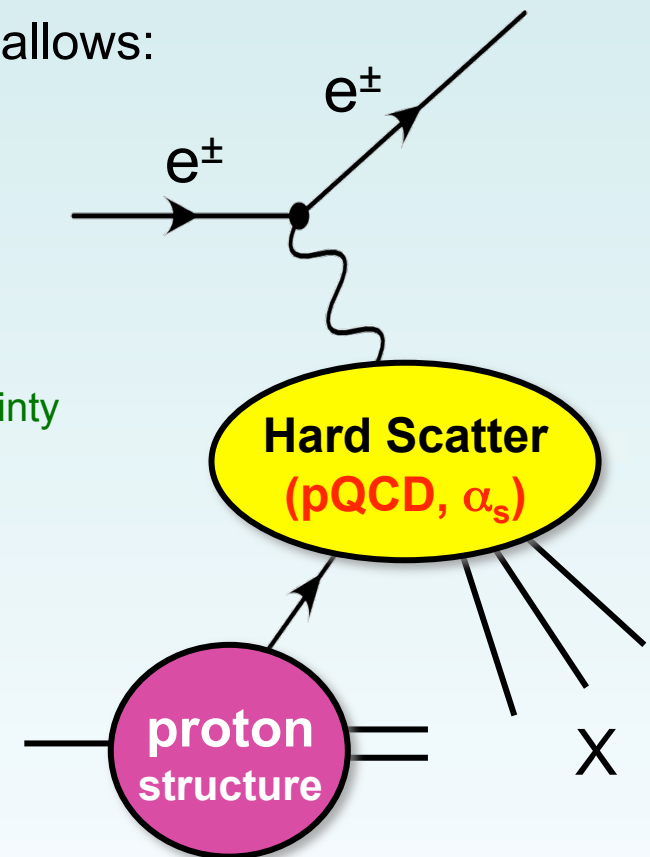
= new for DIS09

# Motivation

**HERA  $e^\pm p$  collider**:- an ideal environment for precision studies of QCD

Study of **jets** in the **Hadronic Final State** at HERA allows:

- stringent tests of our understanding of **pQCD**
  - factorisation, perturbative expansion, PDF universality
- constraints on **proton** (and photon) structure
- extractions of **QCD parameters** ( $\alpha_s, \dots$ )
  - in regions of small experimental and theoretical uncertainty



# Motivation

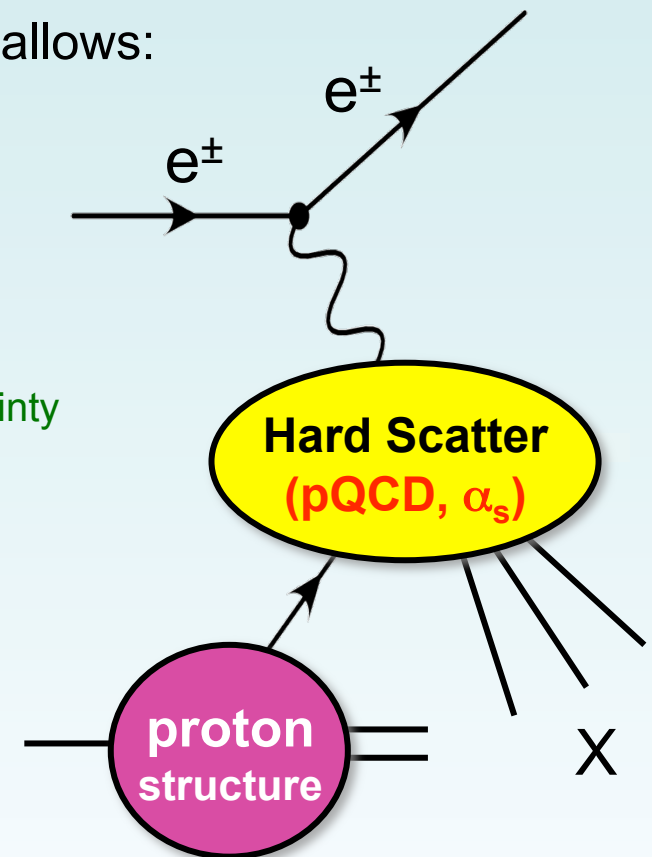
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- extractions of **QCD parameters** ( $\alpha_s$ , ...)
  - in regions of small experimental and theoretical uncertainty

**new** from ZEUS since DIS08:

- **inclusive jets in neutral current DIS**  
( $\times 2.5$  increase in statistics c.f. most recent studies)
- **two new extractions of  $\alpha_s$  from jet data**  
(NC DIS inclusive jets; **re-analysis** of published  $\gamma p$ )



# Motivation

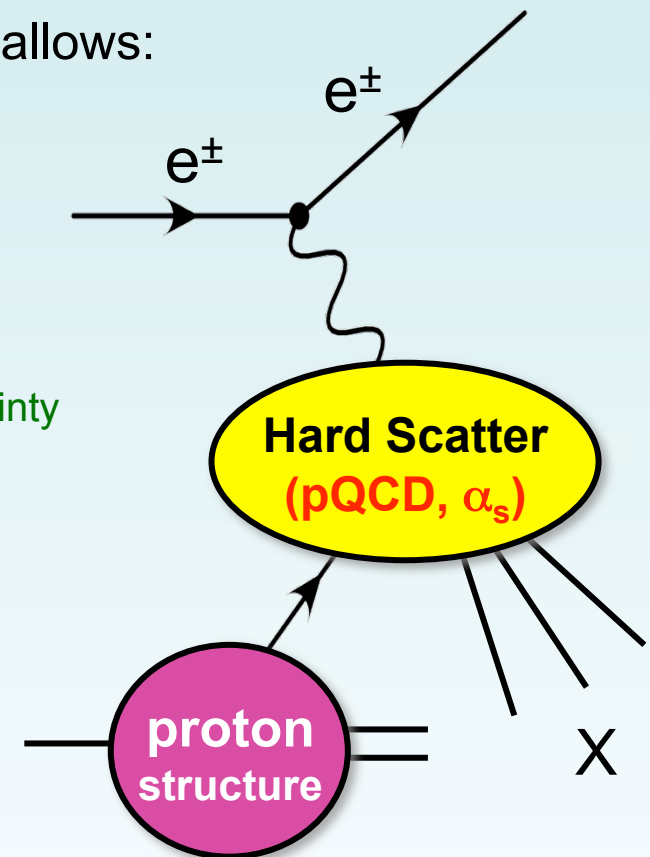
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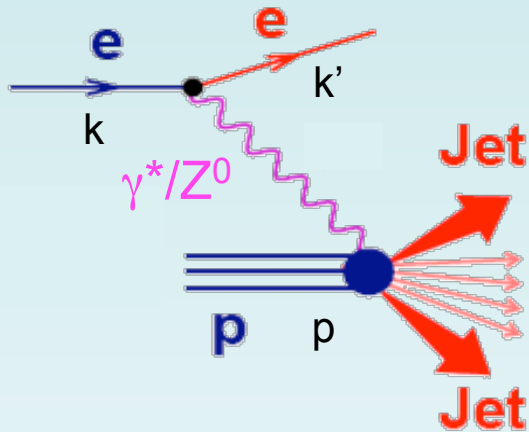
presented here:

- **jet cross sections in neutral current DIS**  
(**new inclusive jet** cross sections; **dijets**)
- **two new extractions of  $\alpha_s$  from jet data**  
(NC DIS inclusive jets; **re-analysis** of published  $\gamma p$ )



# Jet production at HERA

Neutral Current (NC):  $\gamma$  or  $Z^0$  exchange



## Kinematic Variables:

- 4-momentum transfer ('resolution'):  
 $Q^2 = -q^2 = -(k-k')^2$
  - Bjorken scaling variable:  $x = Q^2/2p.q$
  - inelasticity:  $y = p.q/p.k$
- related via:  $Q^2 = sxy$   
[where  $\sqrt{s}$  = CoM energy:  $s = (k+p)^2$ ]

Broadly, two main processes:

- Deep Inelastic Scattering (DIS):**  $Q^2 \gg 1 \text{ GeV}^2$
- Photoproduction ( $\gamma p$ ):**  $Q^2 \approx 0 \text{ GeV}^2$  ← quasi-real **photon** exchange

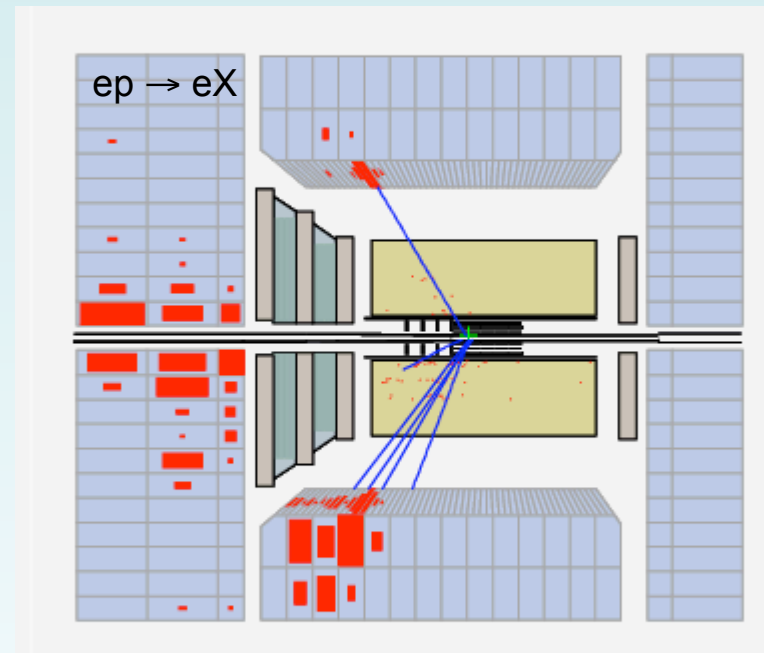
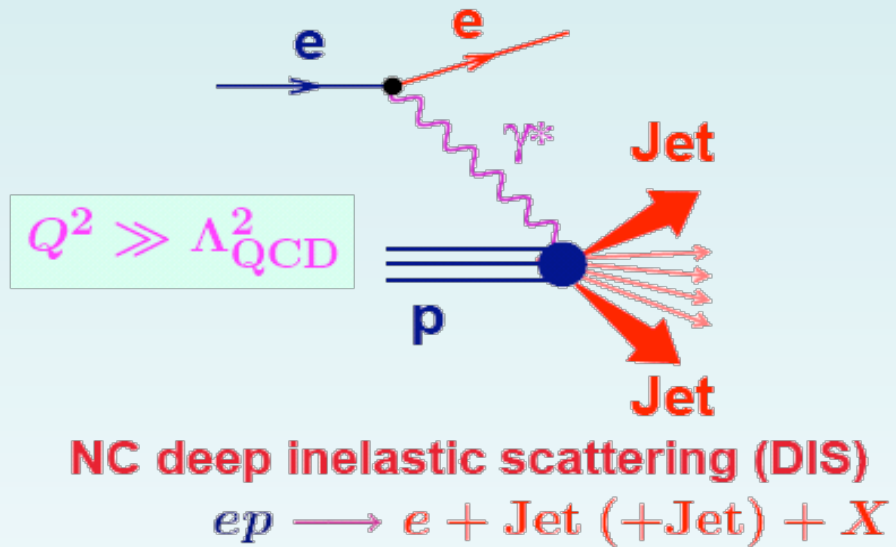
## Jet cross section (DIS):

$$\sigma = \sum_n \alpha_s^n \cdot \sum_{a=q,\bar{q},g} f_a \otimes \hat{\sigma}_a^{(n)}$$

$\hat{\sigma}_a$ : perturbatively calculable **subprocess cross section**  
 $f_a$ : **proton PDF** (long-distance, experimentally determined)

$\gamma p$ : need **photon** PDF too

# Jet cross sections in NC DIS

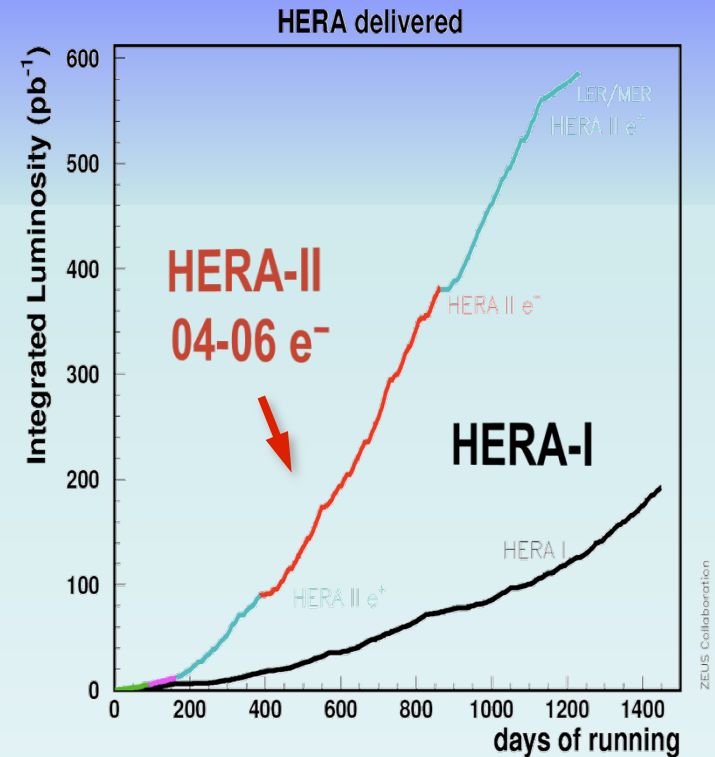
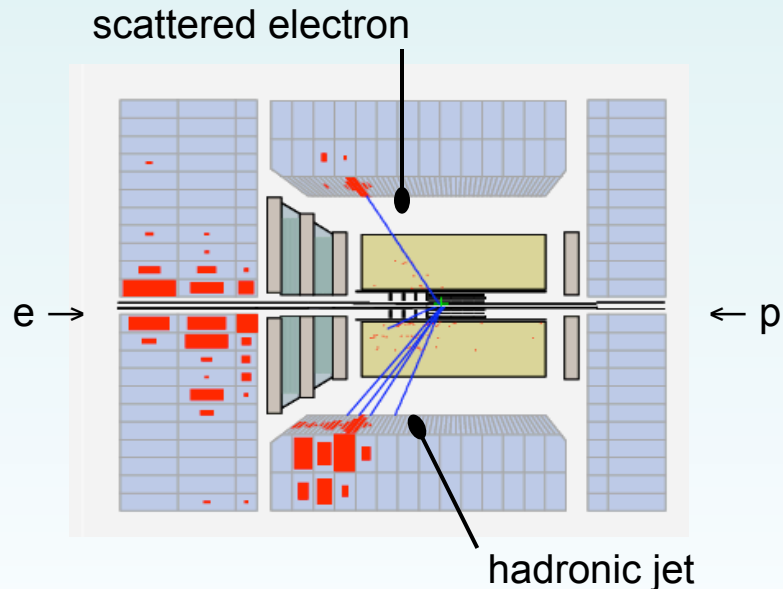


# Data selection

event samples ( $\sqrt{s} = 319 \text{ GeV}$ ):

1. **inclusive jet NC DIS analysis:**
  - HERA-II 05-06 e-p (**188 pb<sup>-1</sup>**)
2. **dijet NC DIS analysis:**
  - HERA-I 98-00 + II 04-05 e-p (**209 pb<sup>-1</sup>**)

## NC DIS event in the ZEUS detector



## phase space:

- $Q^2 > 125 \text{ GeV}^2$  dijet:  $Q^2 < 5000 \text{ GeV}^2$  ↙ no  $Z^0$
- $|\cos(\gamma_{\text{had}})| < 0.65$
- jet selection (in Breit frame; defined next):
  - inclusive:  $\geq 1$  jet with  $E_{T,\text{Breit}} > 8 \text{ GeV}$
  - dijet:  $\geq 2$  jets with  $E_{T,\text{Breit}1(2)} > 12(8) \text{ GeV}$
  - $-2 < \eta_{\text{Breit}} < 1.5$

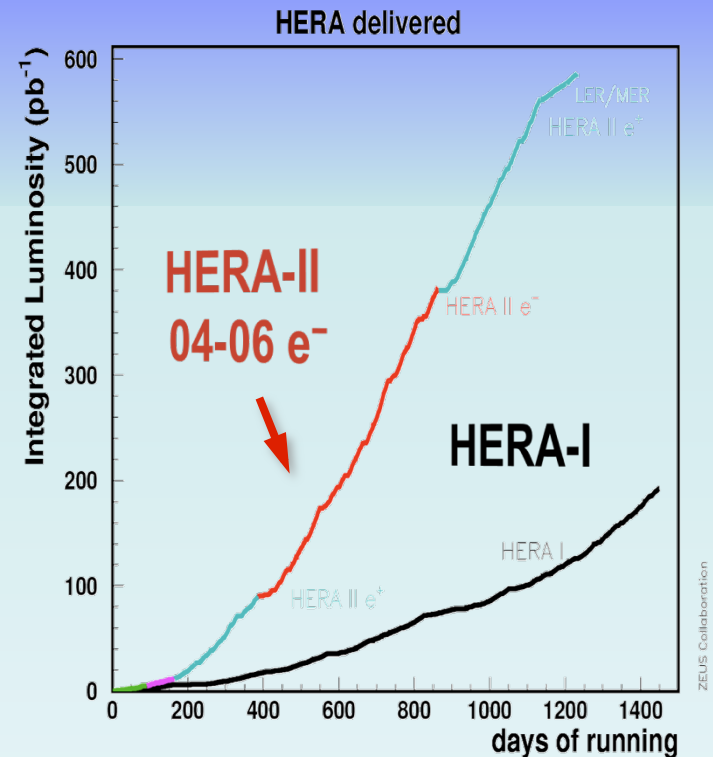
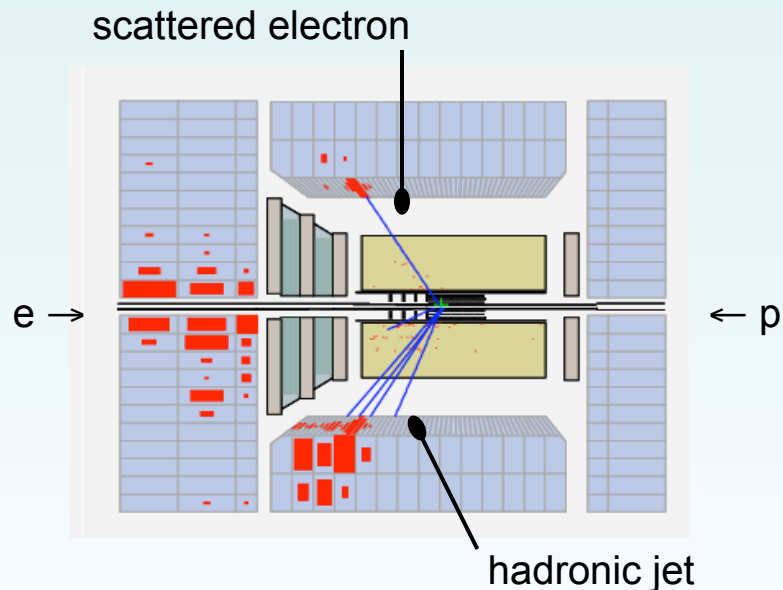
\*  $\gamma_{\text{had}} \equiv$  angle of scattered quark (in QPM)

# Data selection

event samples ( $\sqrt{s} = 319 \text{ GeV}$ ):

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  - HERA-II 05-06 e-p (**188 pb<sup>-1</sup>**)
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  - HERA-I 98-00 + II 04-05 e-p (**209 pb<sup>-1</sup>**)

## NC DIS event in the ZEUS detector



## experimental uncertainties:

- **statistical:** typically **1-5%**
- **systematic:** **jet energy scale\*** dominates (1-3%) → **5-10%** on cross sections  
[next important: **model uncertainty** for acceptance corrections (ARIADNE vs. LEPTO)]

\* from **energy balance** with scattered electron

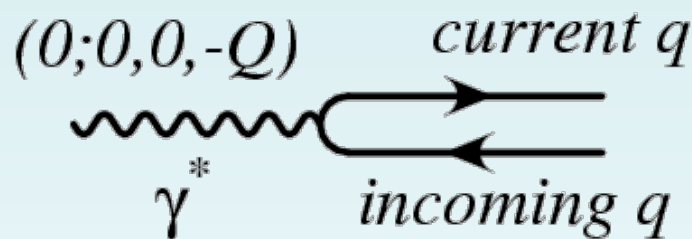


# Jet reconstruction and the Breit frame

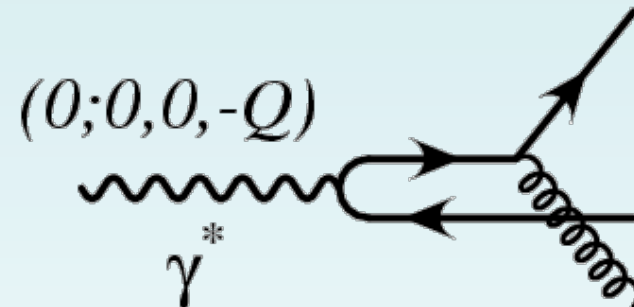
**Jet reconstruction:**  $k_T$ -algorithm in longitudinally-invariant inclusive mode ( $R=1$ )

↑  
infra-red and collinear safe jet definition

**Breit frame:**— virtual boson collides head-on with struck quark from proton



Born level



$O(\alpha_s): q\gamma^* \rightarrow qg$

requirement of **high-transverse-energy** jets in the **Breit frame**:

- Born level contribution suppressed  $\rightarrow$  struck quark back-scattered with zero- $E_T$
- lowest order (non-trivial) contributions,  $O(\alpha_s) \rightarrow$  **two high- $E_T$  jets** (well separated from p remnant)

$\rightarrow$  directly sensitive to **hard QCD sub-process** at  $O(\alpha_s)$  (and higher orders)

# NLO QCD theory

comparison of **measurements** to  $\mathcal{O}(\alpha_s^2)$  QCD calculations:



- NC DIS differential **jet** cross sections calculated at **NLO** using **DISENT**:
    - **proton PDFs**: **ZEUS-S** (global PDF fit)    dijet: **CTEQ6**
    - value of  $\alpha_s(M_Z) = 0.118$ ; calculated at two loops
    - **renormalisation scale**:  $\mu_R = E_{T,B}$  of each jet    dijet:  $\mu_R = \sqrt{Q^2 + \overline{E_{T,B}}^2}$   
[default choices; other scales also investigated]
    - **factorisation scale**:  $\mu_F = Q$     ↓ not necessary for dijet due to restricted  $Q^2$  range
    - corrections for **hadronisation** and  **$Z^0$**  effects applied
  - sources of theoretical **uncertainty** considered:
    - **terms beyond NLO**: variation of scale  $\mu_R$  by (conventional) factors of  $\{1/2, 2\}$
    - **pPDFs**: using the provided eigenvector error PDF sets (exp. sources only)
    - $\alpha_s(M_Z)$ : using two additional sets of PDFs with different  $\alpha_s(M_Z)$
    - modelling of **parton shower**: two different Monte Carlos (CDM vs. MEPS)
    - **factorisation scale**: variation of  $\mu_F$  by factors of  $\{1/2, 2\}$  → negligible
- variation of  $\mu_R$  **dominates** → typically 5–20%; other sources mostly small

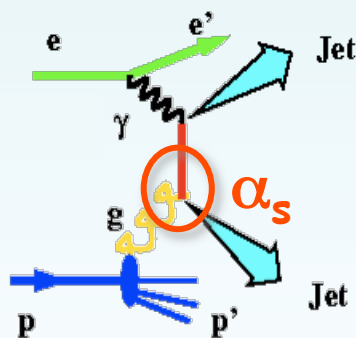
# Inclusive jets cross sections

HERA-II 05-06 (188 pb<sup>-1</sup>) : **50k events**

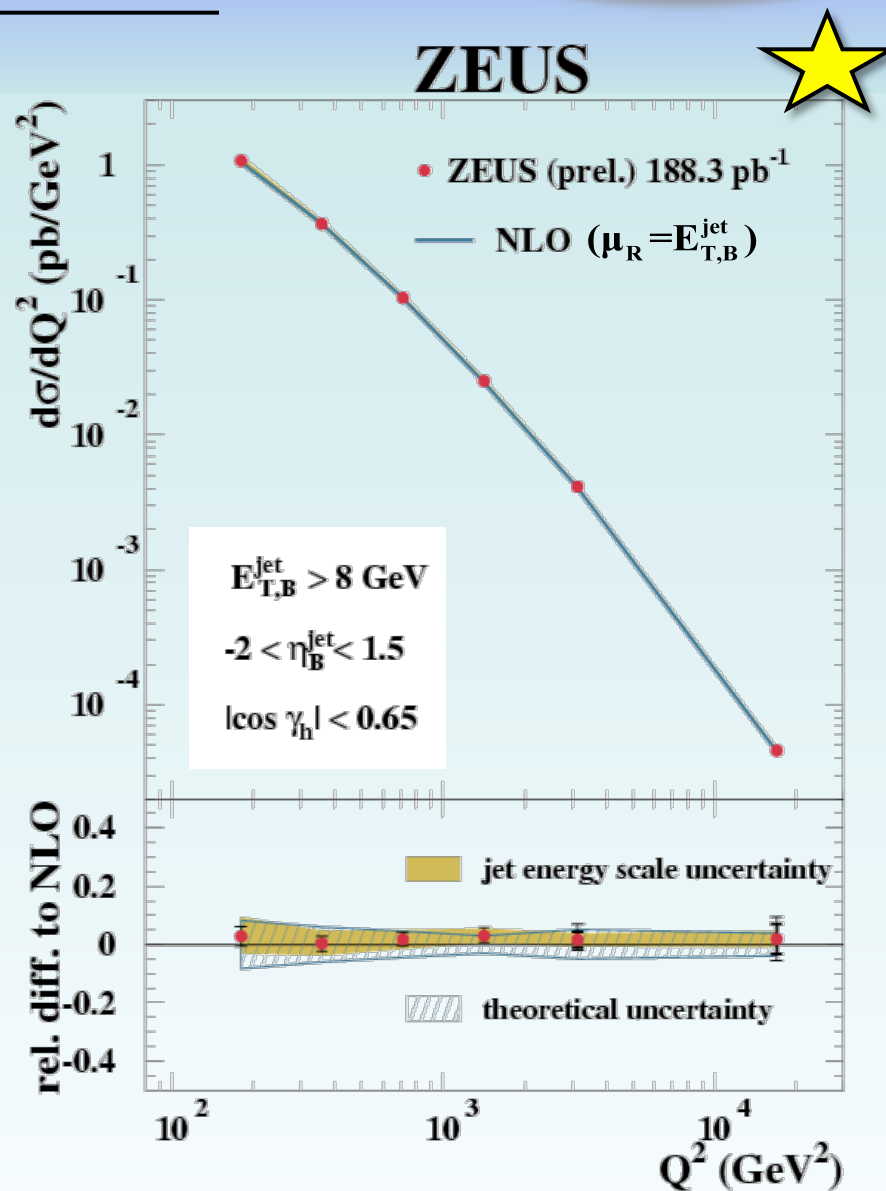
→ **×2.5** increase c.f. most precise HERA-I

**shown:-** single-differential inclusive jet NC cross section as a function of  $Q^2$ :

- **good description** of data by **NLO QCD** over **many orders of magnitude** in the cross section (for both  $\mu_R = E_{T,B}$  and  $Q$ )
- **smaller theoretical uncertainty** than dijet ... **but** still **dominates** over experimental, except at highest  $Q^2$
- also sensitive to the **strong coupling  $\alpha_s$** :

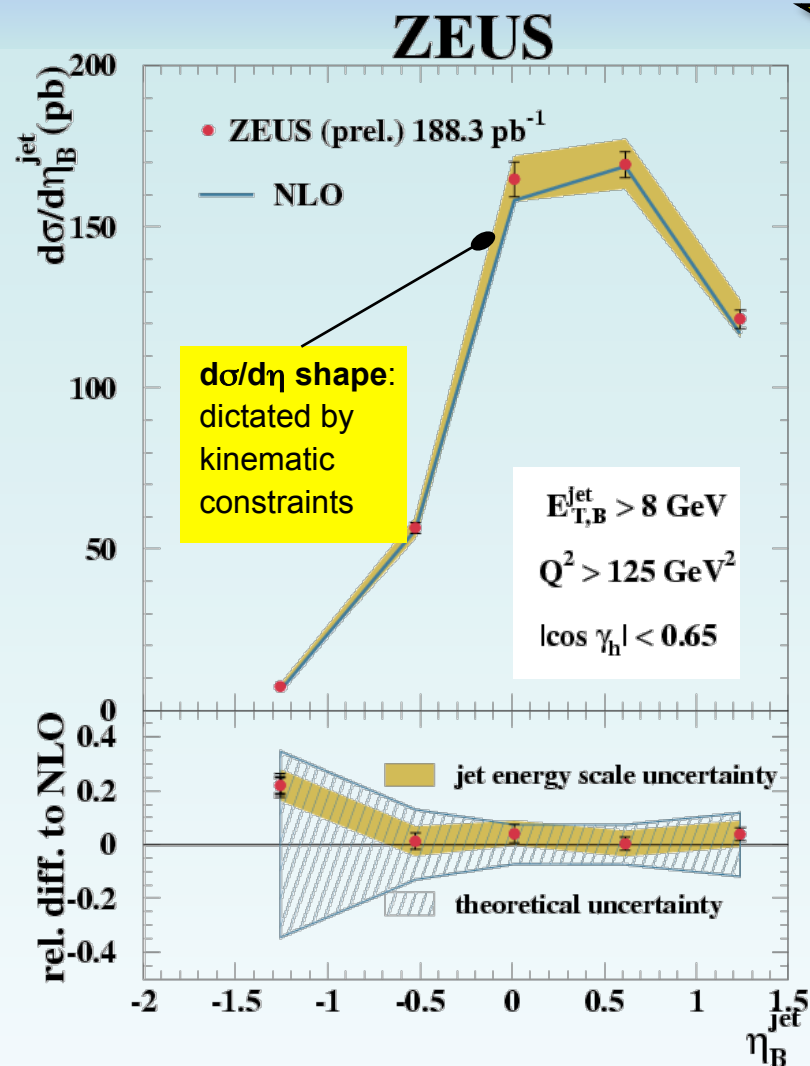
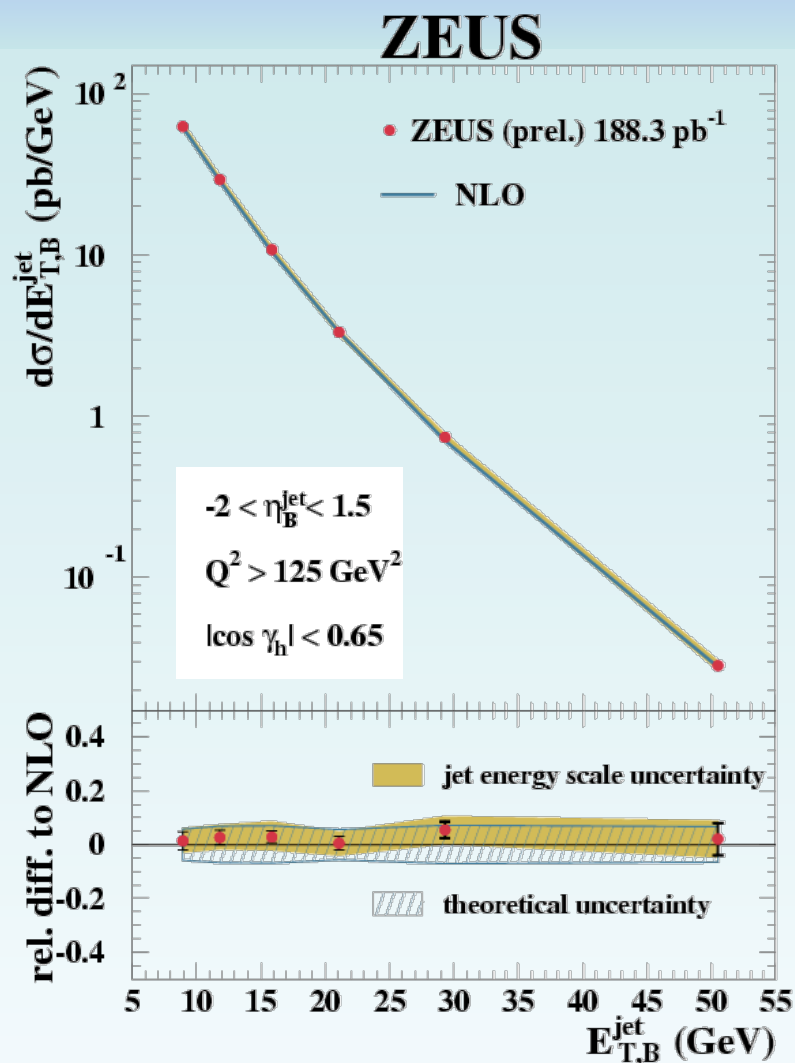


cross section for  
 $Q^2 > 500 \text{ GeV}^2$   
used to extract  
 $\alpha_s(M_Z)$  (see later)



# Inclusive jet cross sections

ZEUS-prel-09-006

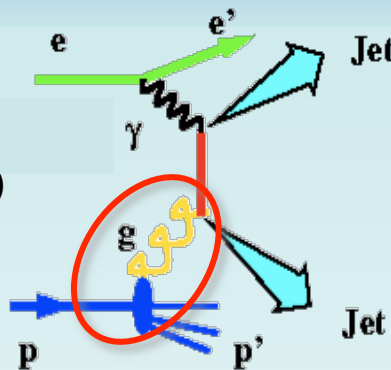


single-differential in jet observables  $E_{T,B}$  and  $\eta_B$  → good description of all data by **NLO QCD**

# HERA jet data and the gluon

## HERA jets:

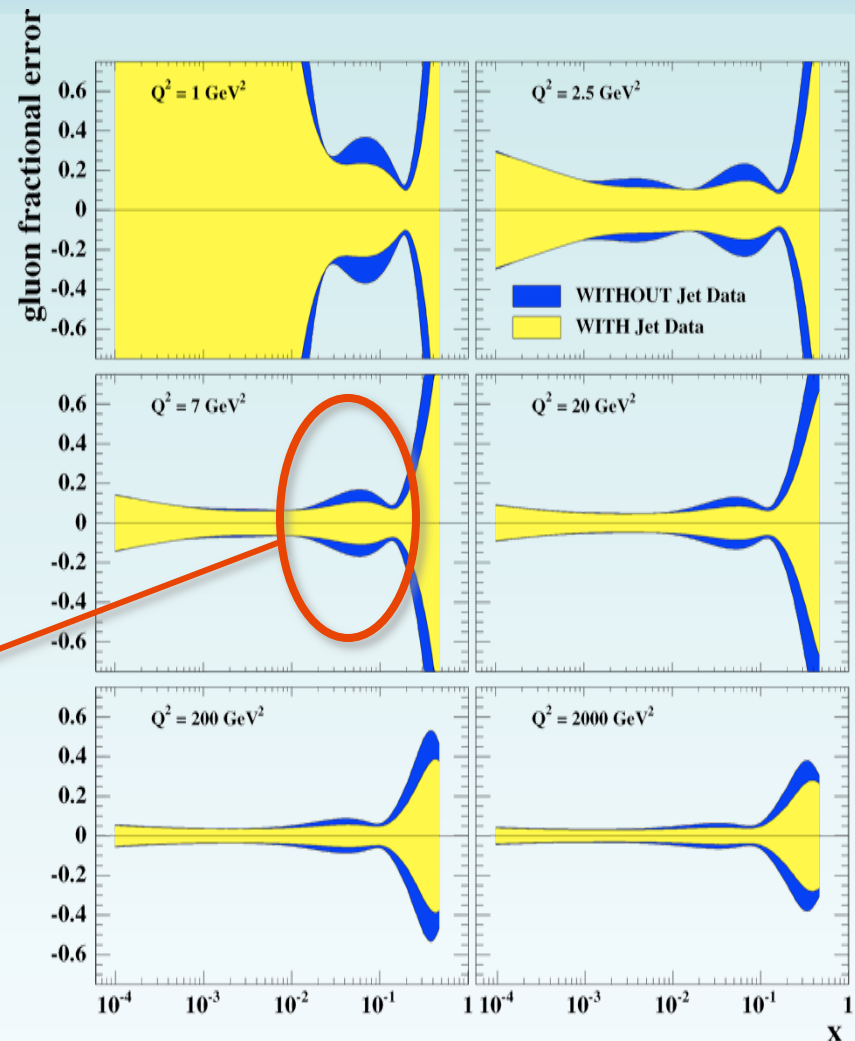
also sensitive to  
**gluon** (and **quark**)  
content of proton  
 $\gamma p$ : also to photon  
structure



- **NC DIS inclusive** and  **$\gamma p$  jet** cross sections included in a previous **ZEUS NLO QCD fit**, (together with more inclusive data) [Eur Phys J **C42** (2005) 1]
- ➔ **gluon uncerts. substantially reduced** (medium-to-high- $x$ )
- same analysis: also a precise  $\alpha_s$  determination

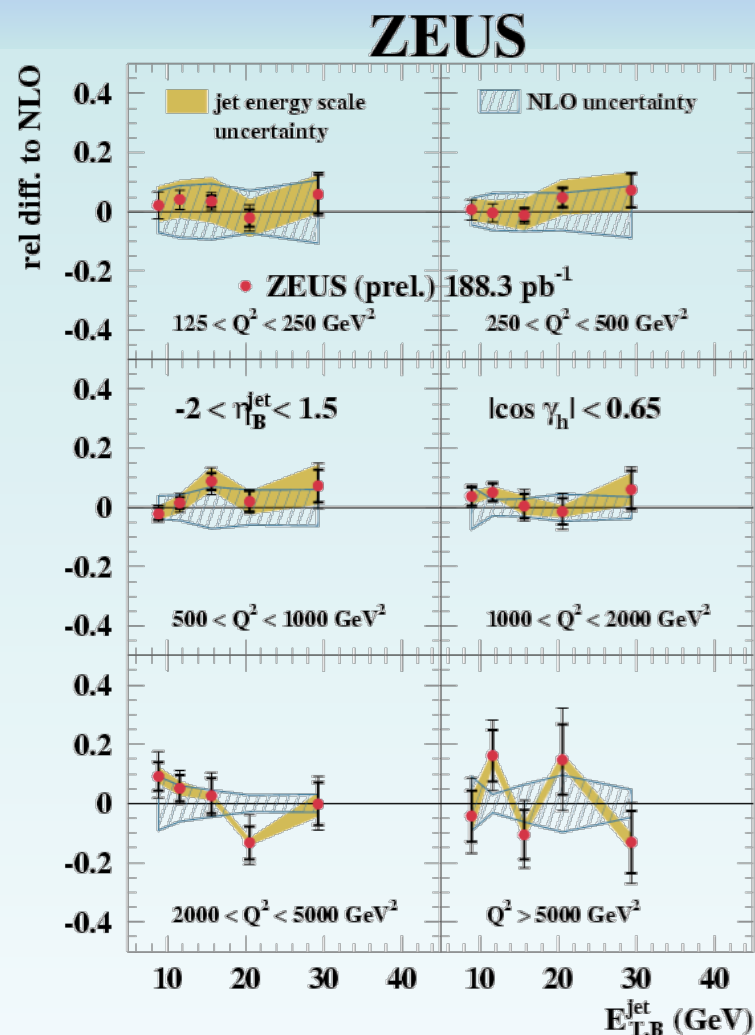
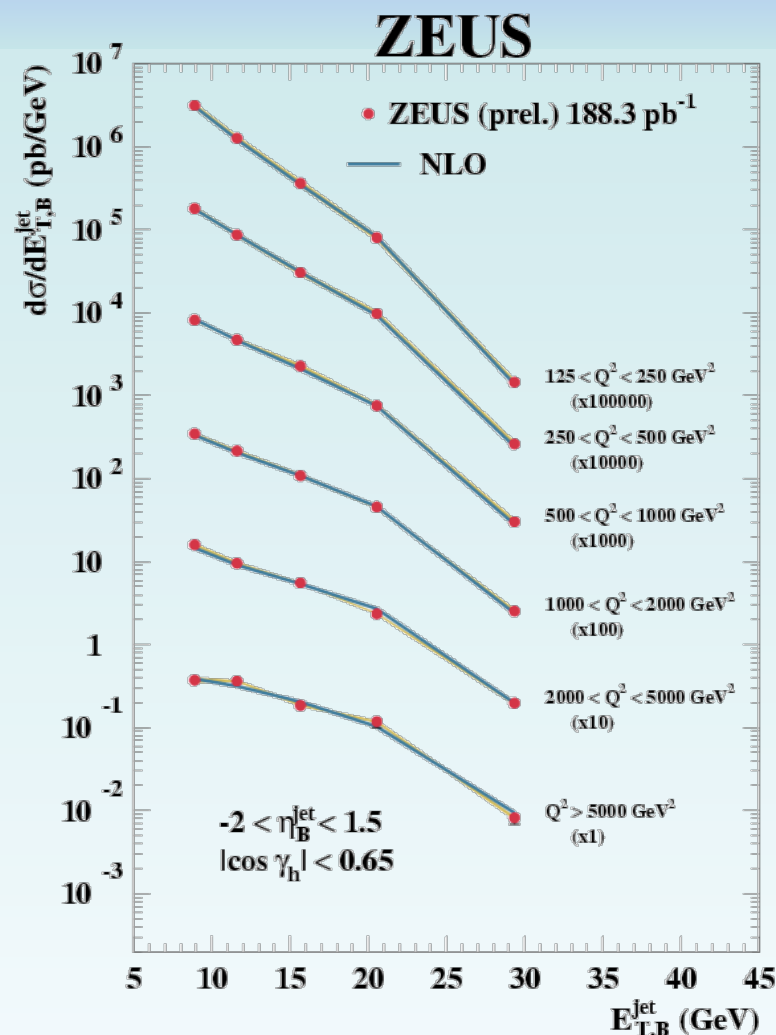
## Proof of Principle:

... jet cross sections from **only** 40 pb<sup>-1</sup> used  
➔ now have the new NC DIS inclusive jets



# Inclusive jet cross sections

ZEUS-prel-09-006



double-differential NC DIS inclusive jet cross sections, as a function of  $E_{T,B}$  in bins of  $Q^2$

→ same kinematic region as NC DIS measurement used in ZEUS QCD fit; × 4.5 increase in statistics

# Dijet cross sections

HERA-I 98-00 + HERA-II 04-05 (209 pb<sup>-1</sup>)

→ **×2.5** luminosity c.f. HERA-I alone

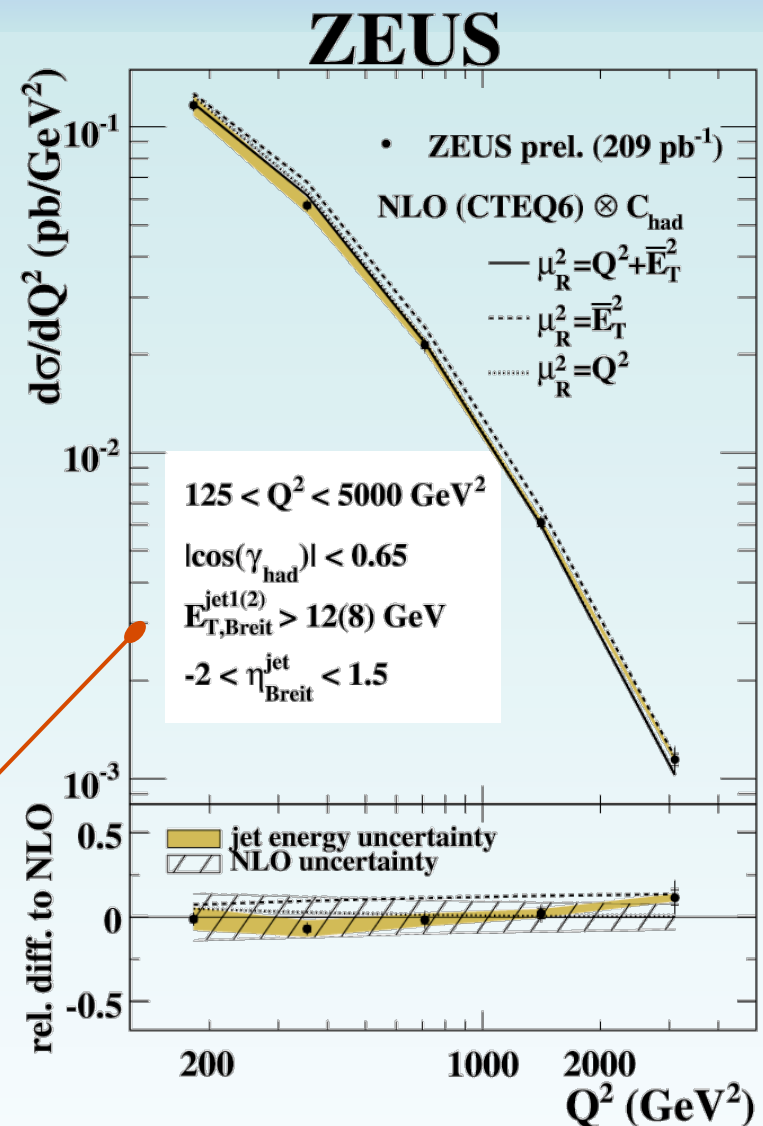
[N.B. results with full HERA-II (04-07) statistics coming soon!]

**shown:-** single-differential NC **dijet** cross section as a function of  $Q^2$ :

**Comparison to NLO QCD** (with various scale choices):

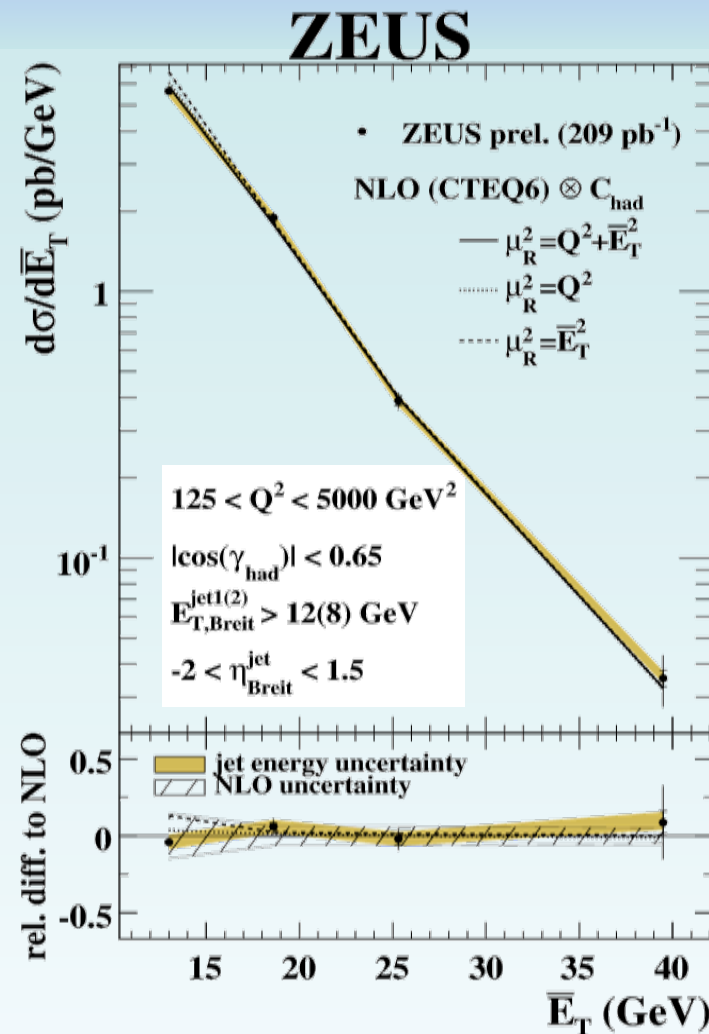
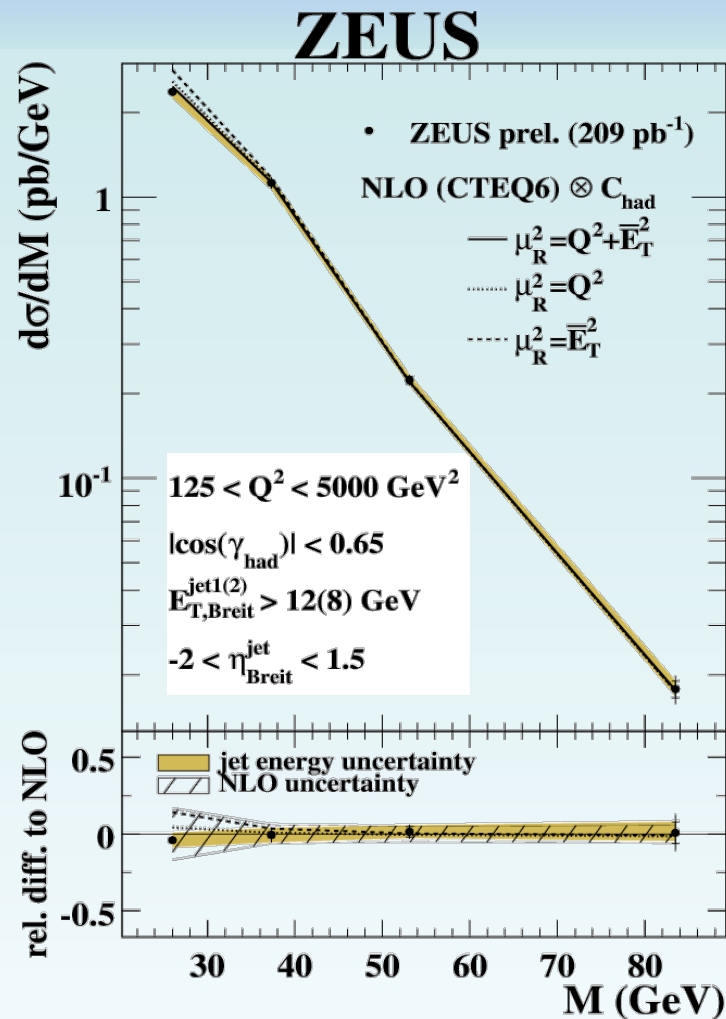
- data **well described** by **NLO QCD** across measured range
  - overall best description with  $\mu_R = \sqrt{Q^2 + \bar{E}_T^2}$  ( $Q^2$  also good)
- theoretical uncertainties **dominate**
  - $\mu_R$  scale variation (terms beyond NLO)

note asymmetric cut on jet- $E_T$  cut: → infra-red safety



# Dijet cross sections

ZEUS-prel-07-005



single-differential, as functions of  $\mathbf{M}_{jj}$ ,  $\bar{E}_T \rightarrow$  sensitive to the **matrix element** in the perturbative calculations

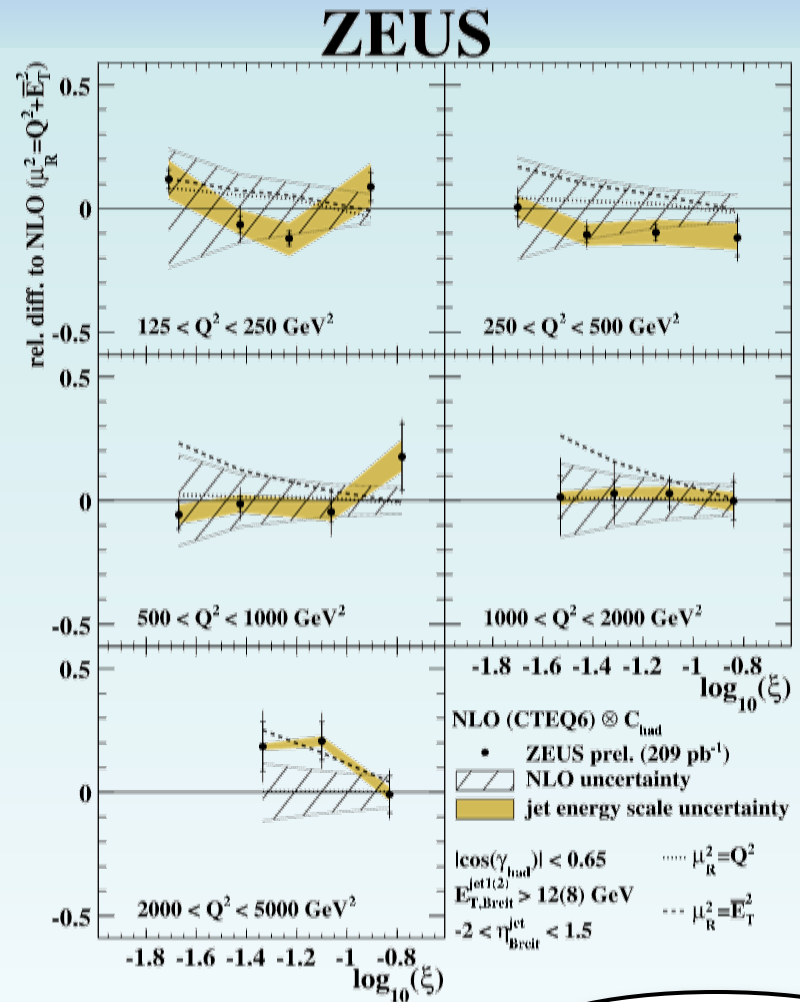
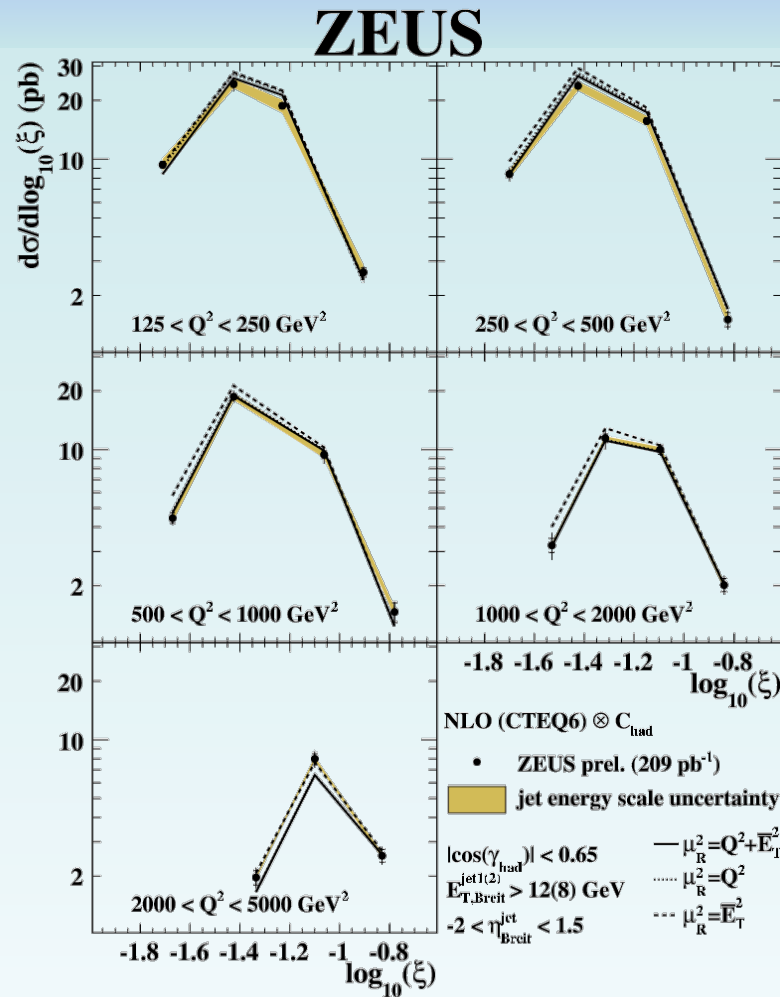
$\rightarrow$  data well described by **NLO QCD**  $\rightarrow$  validity of description of **dijet dynamics** by pQCD at  $O(\alpha_s^2)$



# Dijet cross sections

parton momentum fraction:

$$\xi = x_{Bj} (1 + M_{jj}^2 / Q^2)$$



ZEUS-prel-07-005

double-differential cross sections as a function of  $\log_{10}(\xi)$  in different  $Q^2$  bins:

→ reasonable description by **NLO QCD** → sensitivity to **scale** and **proton PDFs** (next slide)

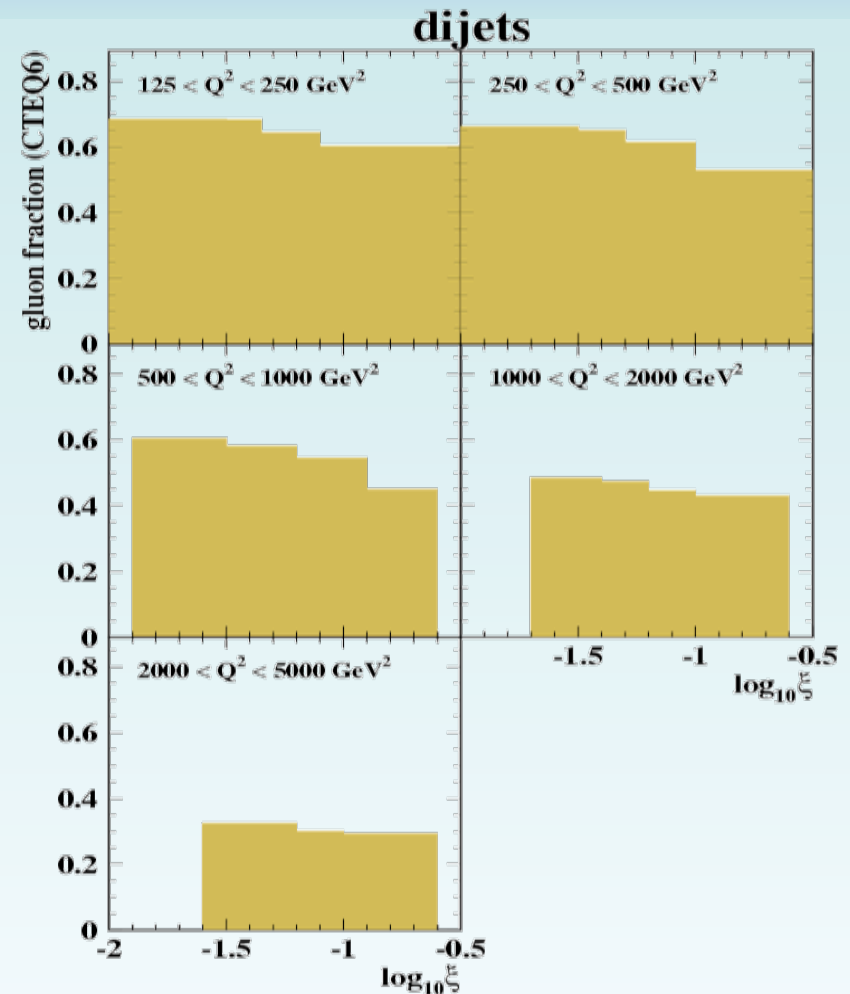
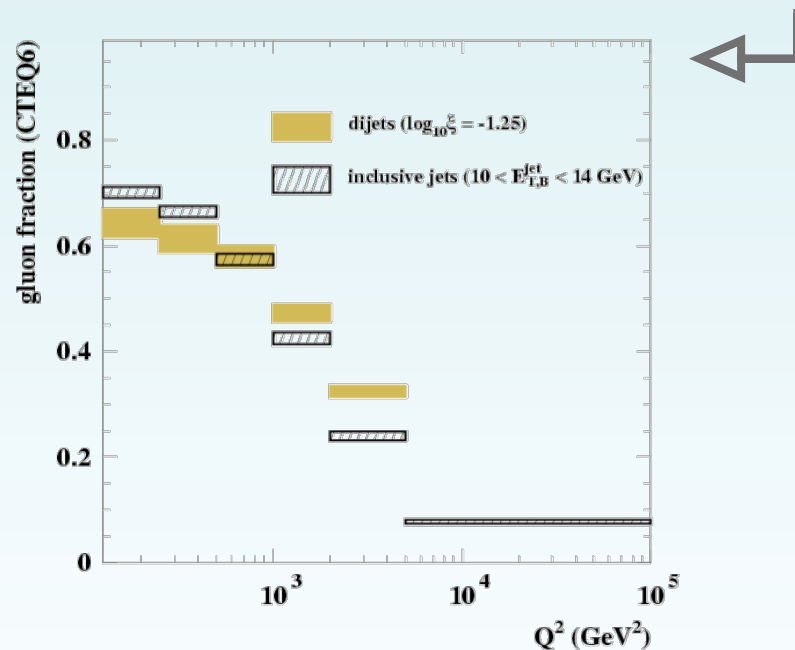
# HERA dijets and the gluon

parton momentum fraction:  
 $\xi = x_{Bj} (1 + M_{jj}^2 / Q^2)$

NC DIS **inclusive jet data** previously shown to constrain the **gluon PDF**

double-differential **dijet** NC cross sections:

- gluon** contribution **at least 30%**, even at highest  $Q^2$ ,  $\xi$  (larger contribution than for inclusive in some regions of phase space)



gluon-induced fraction of the dijet cross section

# HERA dijets and the gluon

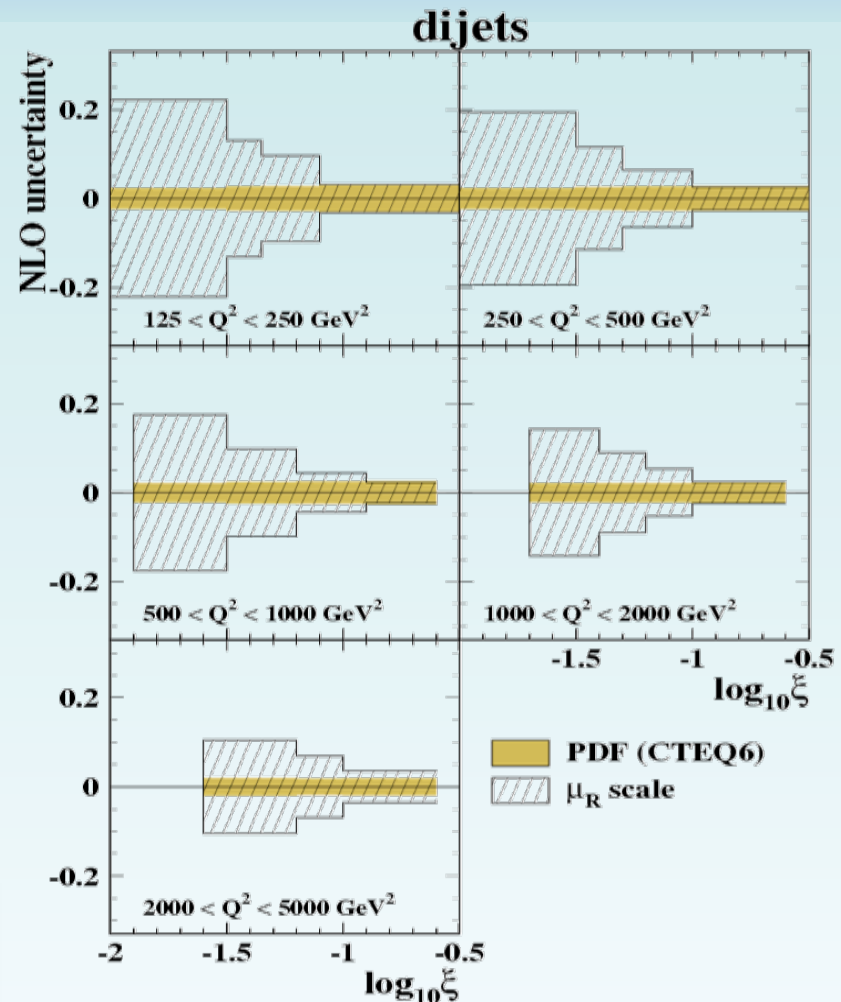
$$\xi = x_{Bj} (1 + M_{jj}^2 / Q^2)$$

NC DIS **inclusive jet data** previously shown to constrain the **gluon PDF**

double-differential dijet NC cross sections:

- **gluon** contribution **at least 30%**, even at highest  $Q^2$ ,  $\xi$  (larger contribution than for inclusive in some regions of phase space)
  - **uncertainties:**
    - $\mu_R$  scale uncertainty **decreases** at high  $Q^2$ ,  $\xi$
    - **PDF** uncertainty **approximately constant** and **non-negligible**
- potentially significant constraints on **gluon**

plus, results including rest of **HERA-II (+06-07)** data **coming soon** → further **x2** luminosity!



theoretical uncertainties from  $\mu_R$  scale + PDFs

extraction of the strong coupling  $\alpha_s$



# HERA jets and $\alpha_s$

$\alpha_s$ : a **fundamental** parameter of QCD → but **must** be determined experimentally

many **precise determinations** of  $\alpha_s$  from **HERA** (from both jet observables and NLO QCD fits)

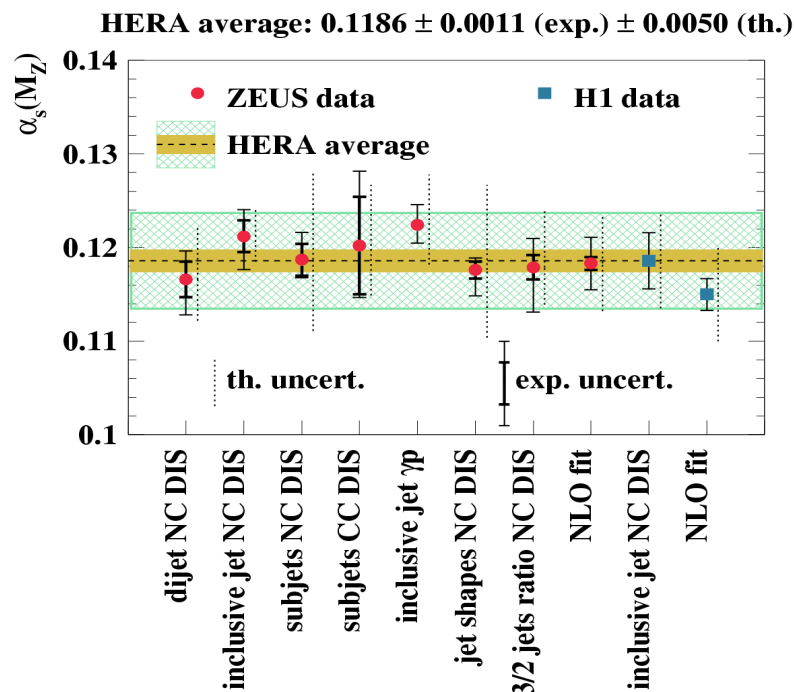
→ just some examples shown here →

**NEW** measurements from ZEUS:



since DIS08: two **new**  $\alpha_s(M_Z)$  determinations:

1. from **new** measurement of **inclusive jets** in **NC DIS** from **HERA-II**  
(cross sections shown earlier)  
→ improved statistical precision  
c.f. previous HERA-I analysis
2. from **re-analysis** of **HERA-I inclusive jet photoproduction** data  
→ reduced theoretical uncertainty c.f.  
previous determination using **same** data



# $\alpha_s$ extraction from jet observables

---

**method:** based on the  $\alpha_s$  dependence of the **perturbative QCD calculations**

pQCD calculations depend on  $\alpha_s$  via the:

- **partonic cross section**
- **proton PDFs** (implicit;  $\alpha_s$  assumed in evolution)

# $\alpha_s$ extraction from jet observables

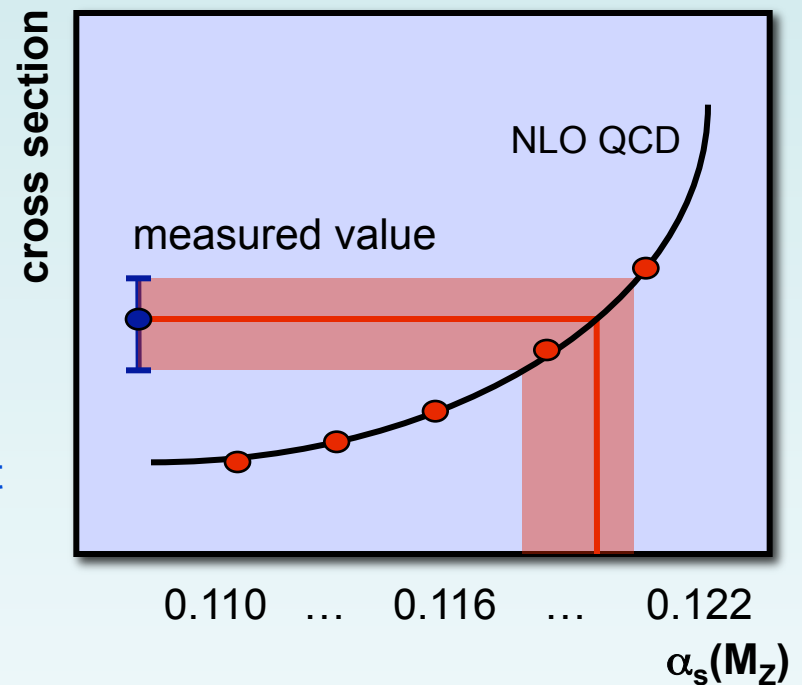
**method:** based on the  $\alpha_s$  dependence of the **perturbative QCD calculations**

pQCD calculations depend on  $\alpha_s$  via the:

- **partonic cross section**
- **proton PDFs** (implicit;  $\alpha_s$  assumed in evolution)

to take into account the correlation:

- perform **NLO** calculations using various sets of **proton PDFs** (i.e. with different assumed  $\alpha_s$ )
- as input to calc., use  $\alpha_s(M_Z)$  assumed in PDF set
- parameterise  $\alpha_s$  dependence of observable  
 $\rightarrow [d\sigma/dA(\alpha_s(M_Z))]^i = A_1^i \alpha_s(M_Z) + A_2^i \alpha_s(M_Z)^2$
- determine  $\alpha_s(M_Z)$  and its **uncertainty** from **measured observable** (using the NLO param.)



This procedure **correctly handles** the **complete  $\alpha_s$  dependence** of the **NLO calculations** (from matrix element and PDFs), while **preserving the correlation** between  $\alpha_s$  and the **PDFs**

# $\alpha_s$ from inclusive jets in NC DIS

ZEUS-prel-09-006



$\alpha_s$  from **new** ZEUS measurement of **inclusive jets** in **NC DIS** from **HERA-II** (188 pb<sup>-1</sup>)

→ extracted from the measured  $d\sigma/dQ^2$  for  $Q^2 > 500 \text{ GeV}^2$  ↓ (yields smallest  $\alpha_s$  uncert.)

$$\alpha_s(M_Z) = 0.1192 \pm 0.0009 \text{ (stat.)}_{-0.0032}^{+0.0035} \text{ (exp.)}_{-0.0021}^{+0.0020} \text{ (th.) (3.5\% total)}$$

## experimental uncertainties:

- dominated by jet energy scale: **±1.9%**

## theoretical uncertainties:

- dominated by terms beyond NLO: **±1.8%**  
(estimated using method of Jones et al. – see later)
- pPDFs (**±0.8%**), hadronisation corrections (**±0.8%**),  $\mu_F$  uncertainty (**negligible**)

↑ first HERA-II  $\alpha_s$  from ZEUS

$\alpha_s(M_Z)$  from **HERA-II** (05–06 e<sup>-</sup>p)  
**inclusive jets** in the Breit frame:  
→ very **precise determination** from  
ZEUS (comparable precision to e<sup>+</sup>e<sup>-</sup>)

c.f. equivalent from HERA-I:  $\alpha_s(M_Z) = 0.1207 \pm 0.0014 \text{ (stat.)}_{-0.0033}^{+0.0035} \text{ (exp.)}_{-0.0023}^{+0.0022} \text{ (th.) (3.7\% total)}$

→ agreement within 1%; improved statistics for HERA-II (82 pb<sup>-1</sup> → 188 pb<sup>-1</sup>)



# $\alpha_s$ from inclusive jets in $\gamma p$

---

$\alpha_s$  from re-analysis of inclusive jets in  $\gamma p$

previous publication [Phys Lett B560 (2003) 7]

**HERA-I 98-00** (82 pb<sup>-1</sup>):  $\alpha_s$  extracted from  $d\sigma/dE_T$

$$\alpha_s(M_Z) = 0.1224 \pm 0.0001 (\text{stat.})^{+0.0022}_{-0.0019} (\text{exp.})^{+0.0054}_{-0.0042} (\text{th.})$$

→ dominated by **theoretical uncertainty**

# $\alpha_s$ from inclusive jets in $\gamma p$

ZEUS-prel-08-008

$\alpha_s$  from re-analysis of inclusive jets in  $\gamma p$

previous publication [Phys Lett B560 (2003) 7]

**HERA-I 98-00** (82 pb<sup>-1</sup>):  $\alpha_s$  extracted from  $d\sigma/dE_T$

$\alpha_s(M_Z) = 0.1224 \pm 0.0001(\text{stat.})^{+0.0022}_{-0.0019}(\text{exp.})^{+0.0054}_{-0.0042}(\text{th.})$

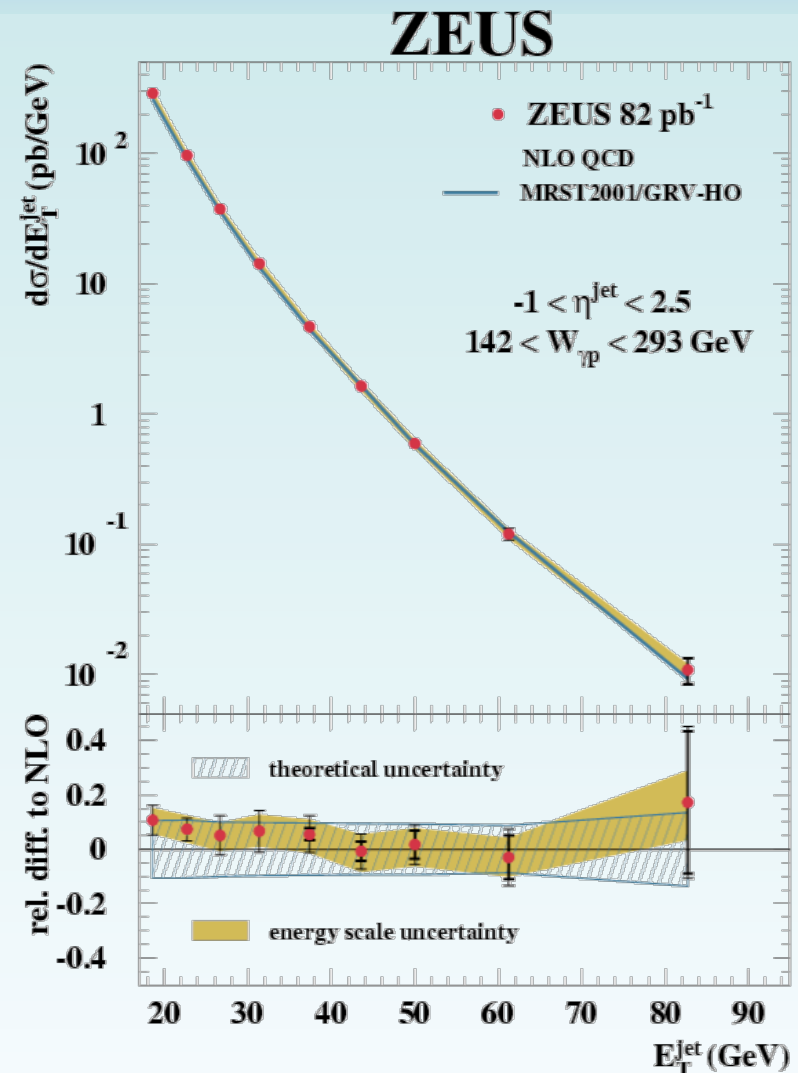
→ dominated by **theoretical uncertainty**

re-analysis (same data):

– **updated** theory; **new method** for  $\mu_R$  variation

NLO QCD prediction:

- $\mathcal{O}(\alpha_s^2)$  : Klasen, Kleinwort and Kramer
- proton PDFs: **MRST01** (previously: MRST99)
- photon PDFs: **GRV-HO**
- $\mu_R = \mu_F = E_T^{\text{jet}}$  for each jet



good description by **NLO QCD** ↑

# $\alpha_s$ from inclusive jets in $\gamma p$

ZEUS-prel-08-008

$\alpha_s$  from re-analysis of inclusive jets in  $\gamma p$

## experimental uncertainties:

- dominated by jet energy scale:  $\pm 1.5\%$

## theoretical uncertainties:

- terms beyond NLO (Jones et al.):  $\pm 2.4\%$
- proton PDF (MRST01 error sets:  $\pm 0.15\%$ );  
 $\gamma$ PDF (AFG:  $\pm 0.7\%$ ); hadronisation corrections  
(Pythia vs. Herwig:  $\pm 0.36\%$ );  $\mu_F$  (negligible)

## $\mu_R$ variation (Jones et al. method)

- extract measured  $\alpha_s$
- calculate cross sections  $\sigma_{\{1/2, 2\}}$  using extracted  $\alpha_s$  but  $\mu_R$  varied by  $\{1/2, 2\}$
- for default  $\mu_R$ , find  $\alpha_s$  values that give  $\sigma_{\{1/2, 2\}}$
- difference c.f. nominal:  $\pm \Delta\alpha_s$

$\Delta\alpha_s$  :- from uncertainty on predicted cross section  $\rightarrow$  no re-fitting of data

new value of  $\alpha_s(M_Z)$  from ZEUS:

0.0001 change to central value from use of updated PDFs

$$\alpha_s(M_Z) = 0.1223 \pm 0.0001(\text{stat.})_{-0.0021}^{+0.0023} (\text{exp.})_{-0.0030}^{+0.0029} (\text{th.}) (3.1\% \text{ total})$$

$\rightarrow$  precise  $\alpha_s$  determination from a single HERA measurement

# Summary of $\alpha_s(M_Z)$ values

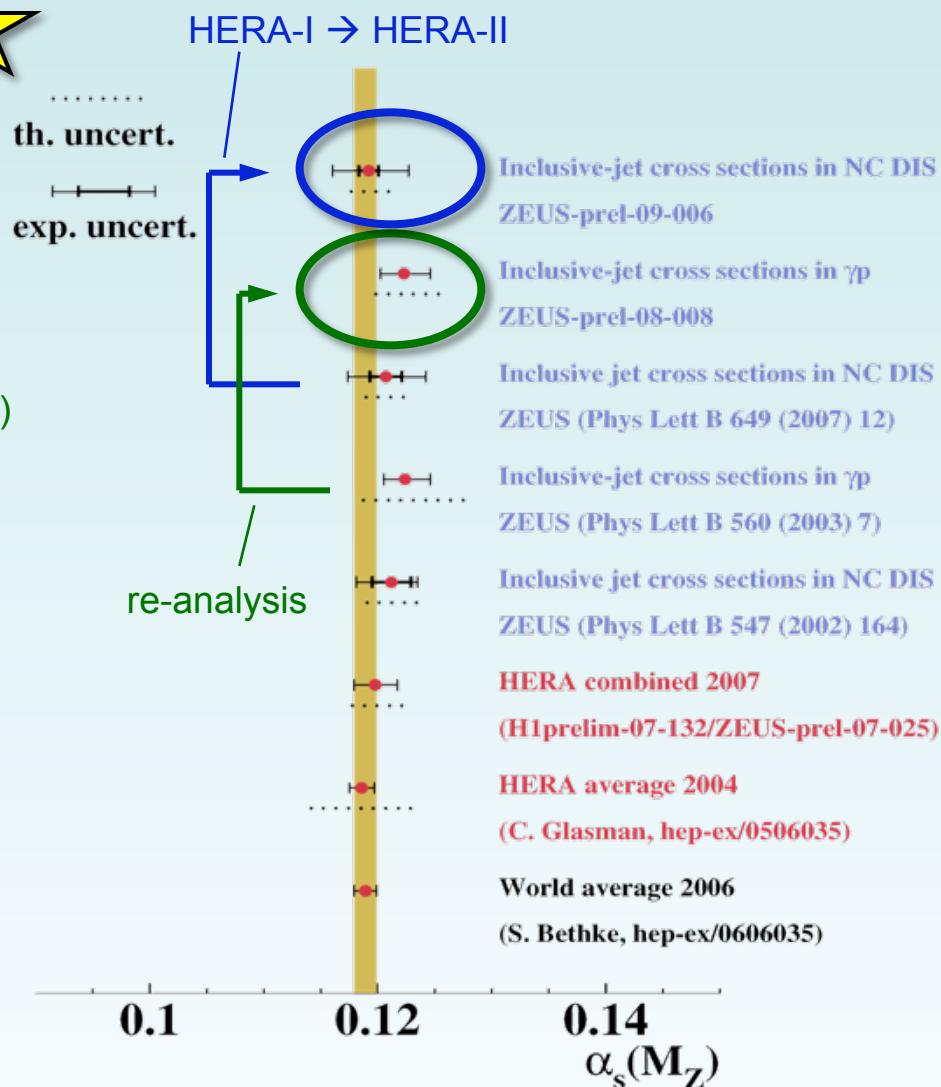
need **NNLO** to  
improve theoretical  
uncertainty

1. new **HERA-II** NC DIS incl. jets: ★  
total uncertainty **3.5%**  
c.f. HERA-I (Phys Lett B649 (2007) 12)
2. re-analysis of **HERA-I**  $\gamma p$  incl. jets:  
total uncertainty **3.1%**  
c.f. previous anal. (Phys Lett B560 (2003) 7)

↑ note the competitive precision of  
these determinations, **from single HERA  
measurements**, compared to averages:

- HERA combined 2007 (**2.7%** uncert.)  
(from H1 and ZEUS inclusive jets in NC DIS;  
currently the highest precision HERA extraction)
- LEP (**1.7%** uncert.) [S. Kluth, EPS07]

measurements **consistent** with each  
other and with **world average**



# Summary

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## » NC DIS jet cross sections from ZEUS with HERA-II data:

1. **new** measurement of **inclusive jets** from HERA-II (188 pb<sup>-1</sup>)
  2. **dijets** using combined HERA-I + II (209 pb<sup>-1</sup>)
- **inclusive** and **dijet** data well described by **NLO QCD**
  - **theoretical uncertainties** dominate ( $\mu_R$  variation; or use of different scale choices)
  - data sensitive to **proton PDFs** (and  $\alpha_s$  ↓)

## » new extractions of $\alpha_s$ from ZEUS

- **precise** determinations from new inclusive jets in **NC DIS** and re-analysis of  $\gamma p$ 
  - compatible with averages (HERA, LEP, world); total uncertainty ~ **3–3.5%**

## » future:

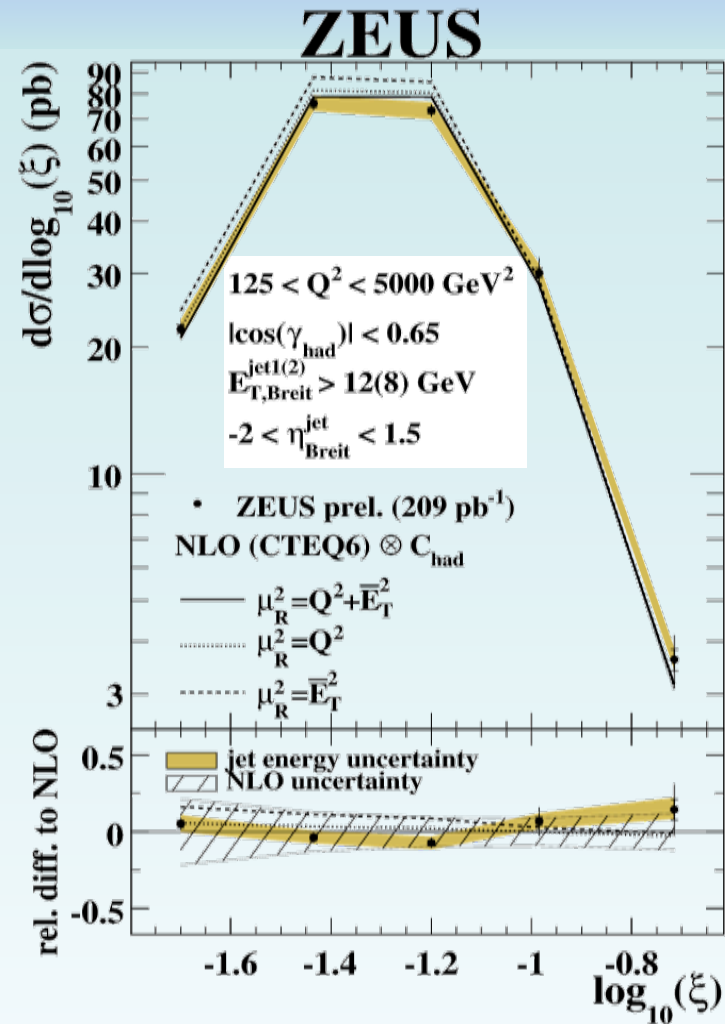
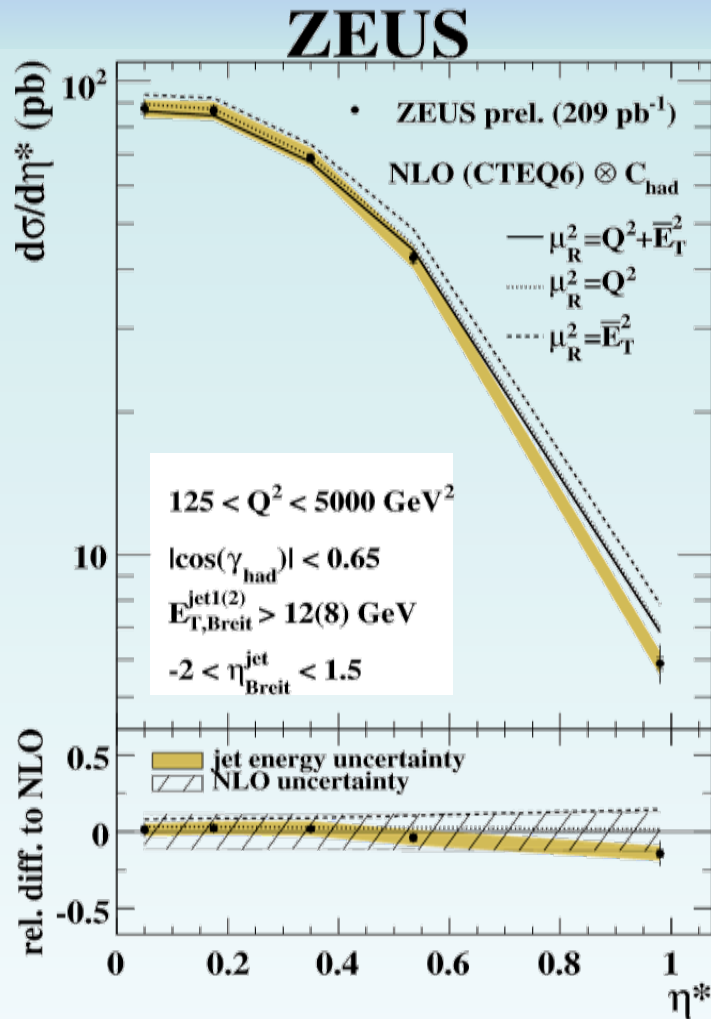
- Jets measurements with full HERA-II data (**coming soon**)
- HERA combinations → **final word on HERA  $\alpha_s$**
- updates to **QCD fits** using new jet data → **improvement to PDFs?**

extras

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# Dijet cross sections

ZEUS-prel-07-005



single-differential, as functions of  $\eta^* = \frac{1}{2} (\eta^1 + \eta^2)$  and  $\log_{10}(\xi) \rightarrow$  data well described by NLO QCD