Exclusive Vector Meson & Diffractive Jets @ HERA

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MPI@LHC
Perugia
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Outline of the talk:

Short review of low x HERA data, Dipole Picture,
Diffractive Jets in the Dipole Picture
vs Diffractive Structure Function approach
DVCS & VM in the Dipole Picture
➔ abundance of multiple interactions

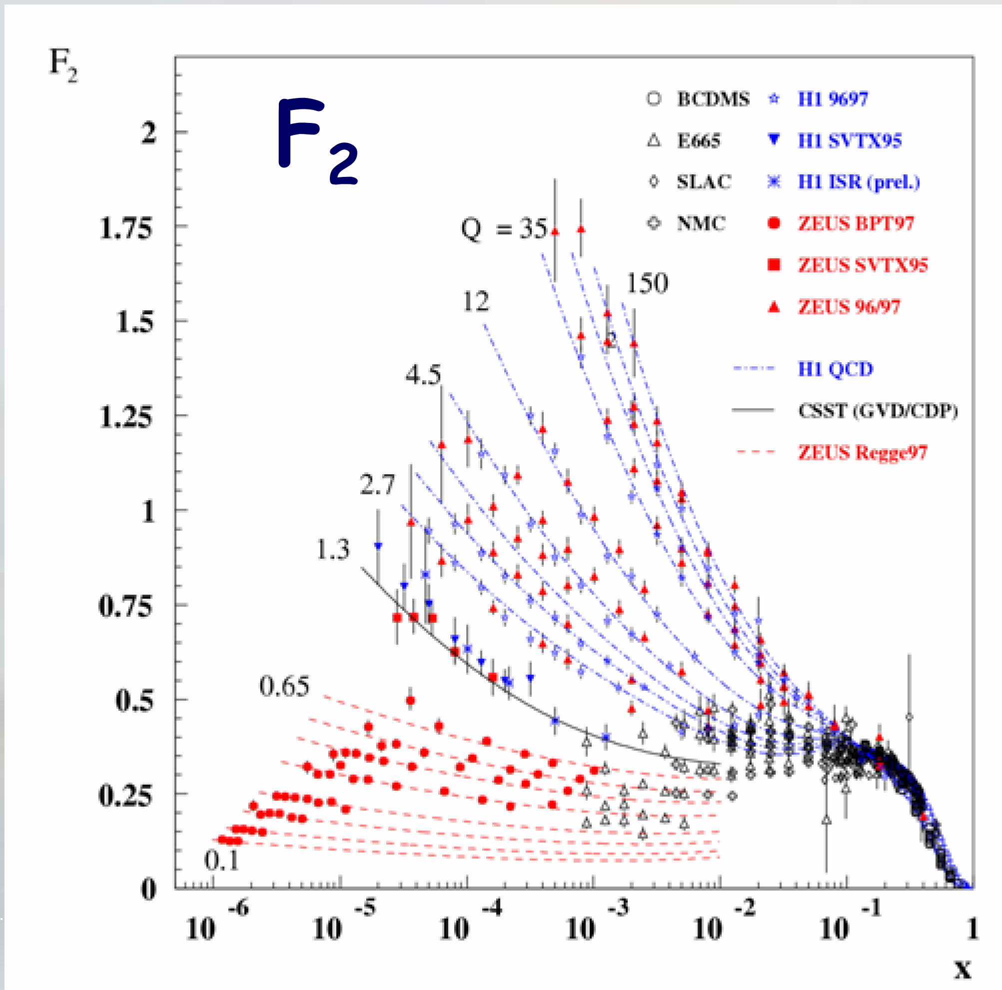
Saturation, oomph factor and all that

Why Pomeron at HERA?,
What is DAF-BFKL Pomeron
Evidence for DAF-Pomeron from HERA data

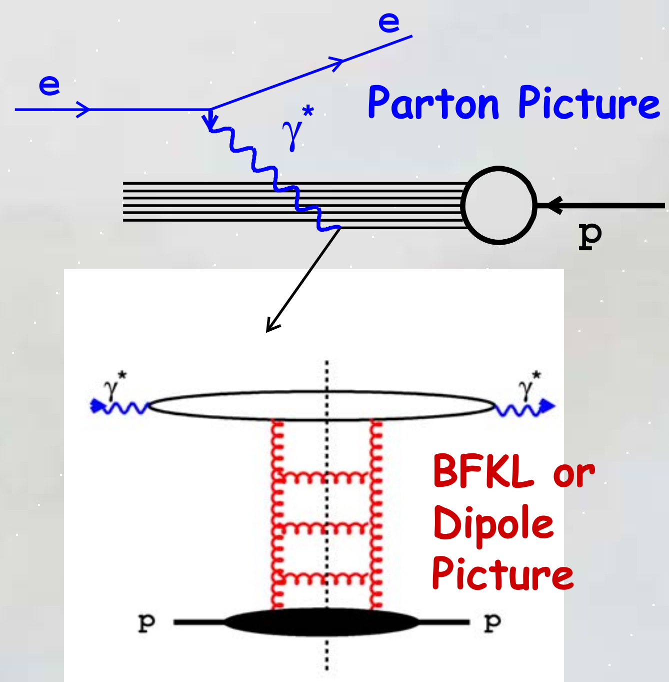
Relation with DGLAP
MRST ←→ EKR

Pomeron-Graviton Correspondence

Low-x Physics @ HERA



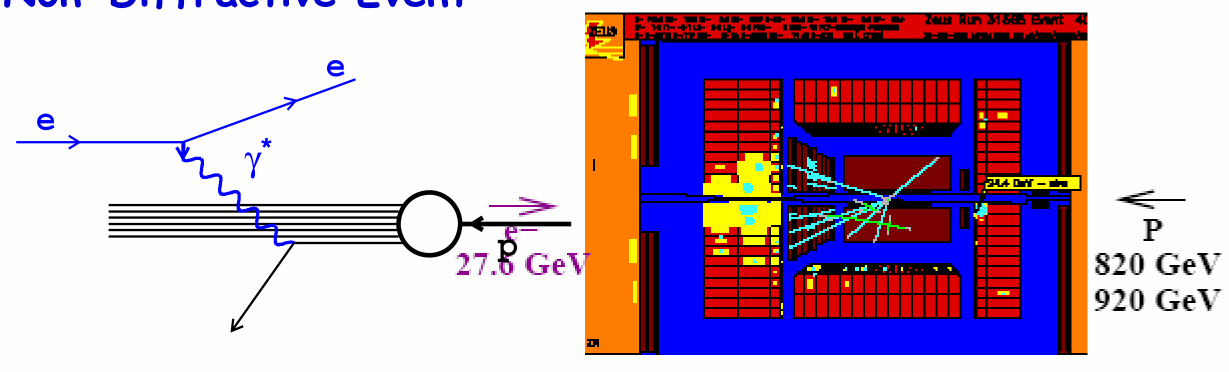
- At low x and high Q^2, steep rise in structure function

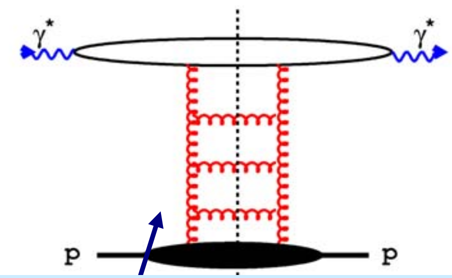


Behavior of F_2 is dominated by gluon density at small-x

Hard Diffraction – the HERA surprise

Non-Diffractive Event

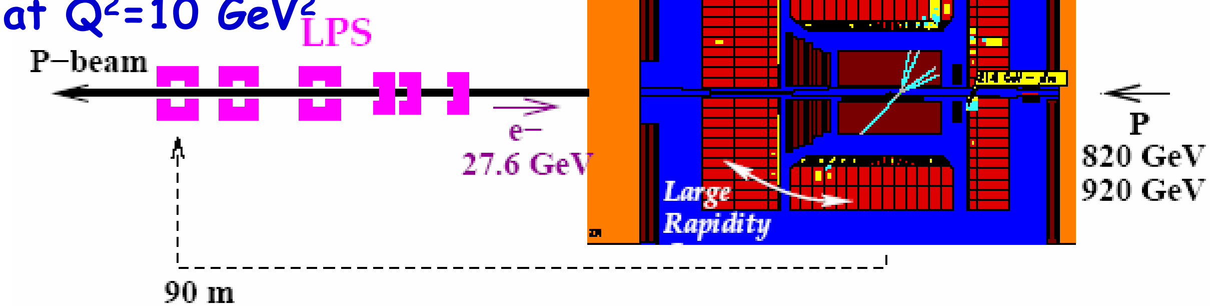


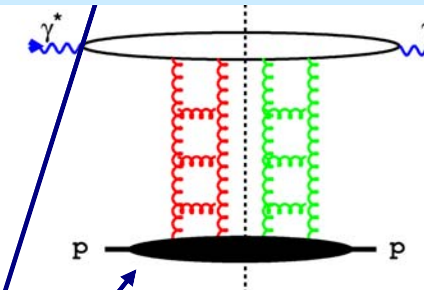


$$\tau_{qq} \approx \frac{1}{\Delta E} \approx \frac{1}{m_p x} \approx 10 - 1000 \quad \mathrm{fm}$$

Diffractive Event

expected before HERA <0.01%, seen over 10% at Q^2=10 GeV^2





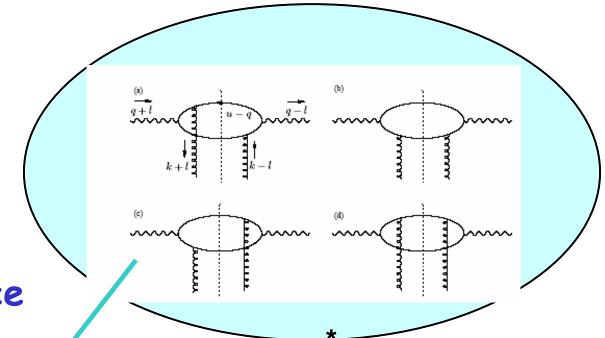
Diffraction at HERA is so large because it is a shadow of DIS (i.e. inelastic processes) ➔ dipole picture

$$\sigma_{tot}^{\gamma^* p} = \frac{1}{W^2} Im A_{el}(W^2, t = 0)$$

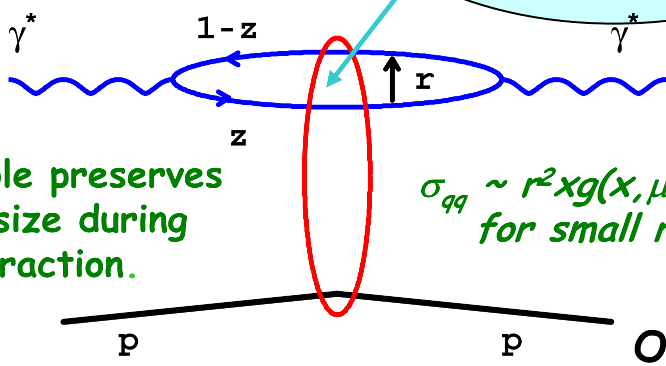
Dipole description of DIS

equivalent to Parton Picture in the perturbative region

momentum space



configuration space



dipole preserves its size during interaction.

$\sigma_{qq} \sim r^2 xg(x,\mu)$
for small r

$$\left|\Psi_T^f\right|^2 = \frac{3\alpha_{em}}{2\pi^2} e_q^2 \{[z^2 + (1-z)^2]\varepsilon^2 K_1^2(\varepsilon r) + m_q^2 K_0^2(\varepsilon r)\}$$

$$\left|\Psi_L^f\right|^2 = \frac{3\alpha_{em}}{2\pi^2} e_q^2 \{4Q^2 z^2 (1-z)^2 K_0^2(\varepsilon r)\}$$

$$\varepsilon^2 = z(1-z)Q^2 + m_q^2$$

$\varepsilon r << 1$
$Q^2 \sim 1/r^2$

Optical T

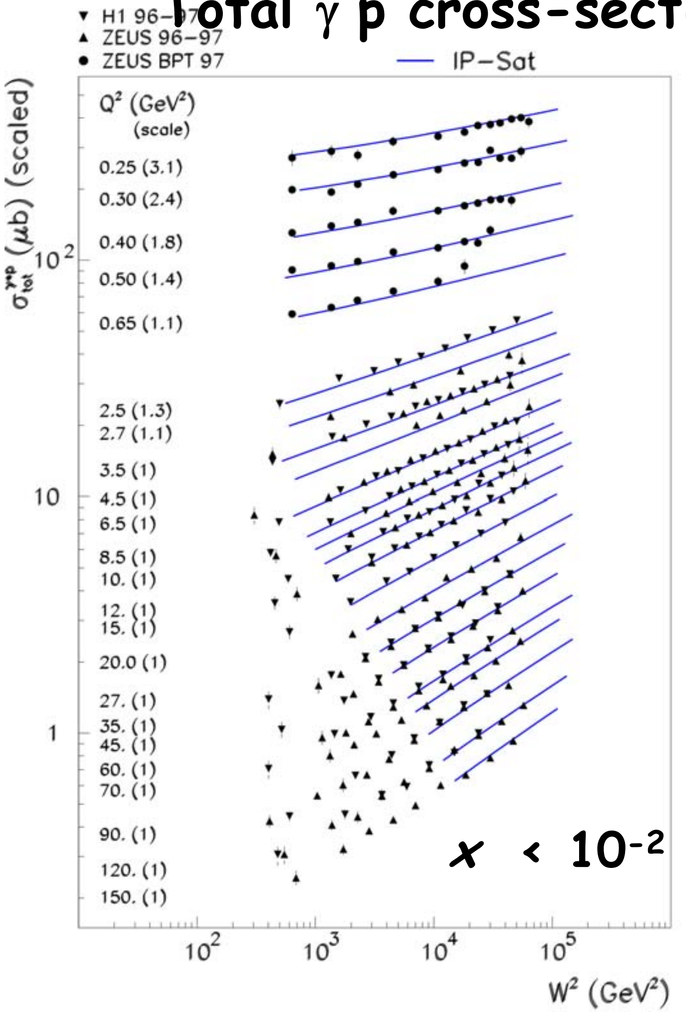
Mueller, Nikolaev, Zakharov

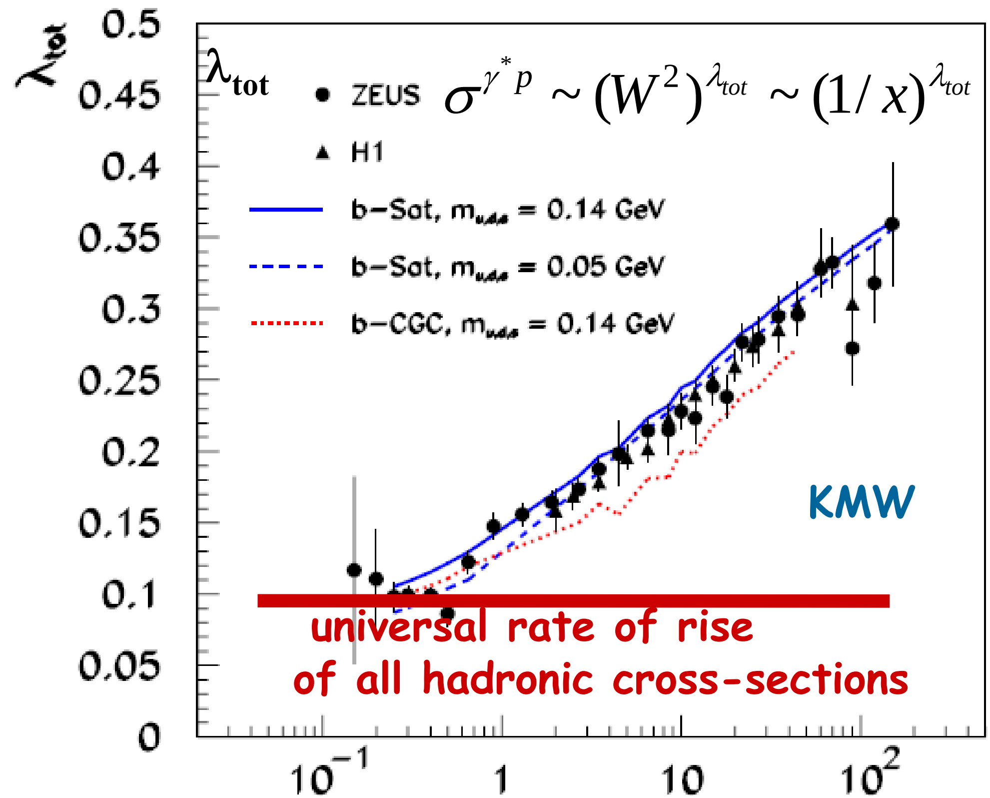
$$\sigma_{tot}^{\gamma^* p} = \int d^2\hat{\vec{r}} \int_0^1 dz \Psi^* \sigma_{q\bar{q}}(x, r^2)\Psi$$

$$\frac{d\sigma_{VM}^{\gamma^* p}}{dt}\Big|_{t=0} = \frac{1}{16\pi}\left|\int d^2\vec{r}\int_0^1 dz \Psi_{VM}^*(Q^2, z, \vec{r})\ \sigma_{q\bar{q}}(x, r^2)\Psi(Q^2, z, \vec{r})\right|^2$$

$$\frac{d\sigma_{diff}^{\gamma^* p}}{dt}\Big|_{t=0} = \frac{1}{16\pi}\int d^2\vec{r}\int_0^1 dz \Psi^* \sigma_{q\bar{q}}^2(x, r^2)\Psi$$

Total $\gamma^* p$ cross-section





$$\mu^2 = \frac{C}{r^2} + \mu_0^2$$

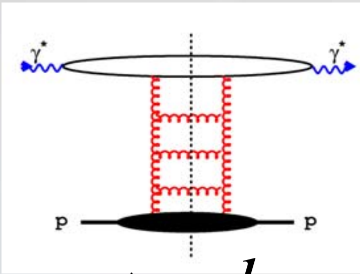
$$\frac{\mathrm{d}\sigma_{q\bar{q}}}{\mathrm{d}^2\boldsymbol{b}} = 2\left[1 - \exp\left(-\frac{\pi^2}{2N_c} r^2 \alpha_S(\mu^2) xg(x,\mu^2) T(b)\right)\right] \quad xg(x,\mu_0^2) = A_g \left(\frac{1}{x}\right)^{\lambda_g} (1-x)^{5.6}$$

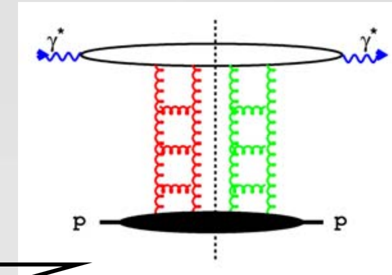
b-Sat

$$\frac{\mathrm{d}\sigma_{q\bar{q}}}{\mathrm{d}^2\boldsymbol{b}} \equiv 2\mathcal{N}(x,r,b) = 2 \times \begin{cases} \mathcal{N}_0 \left(\frac{rQ_s}{2}\right)^{2\left(\gamma_s + \frac{1}{\kappa\lambda Y}\ln\frac{2}{rQ_s}\right)} & : \quad rQ_s \le 2 \\ 1 - \mathrm{e}^{-A\ln^2(BrQ_s)} & : \quad rQ_s > 2 \end{cases}$$

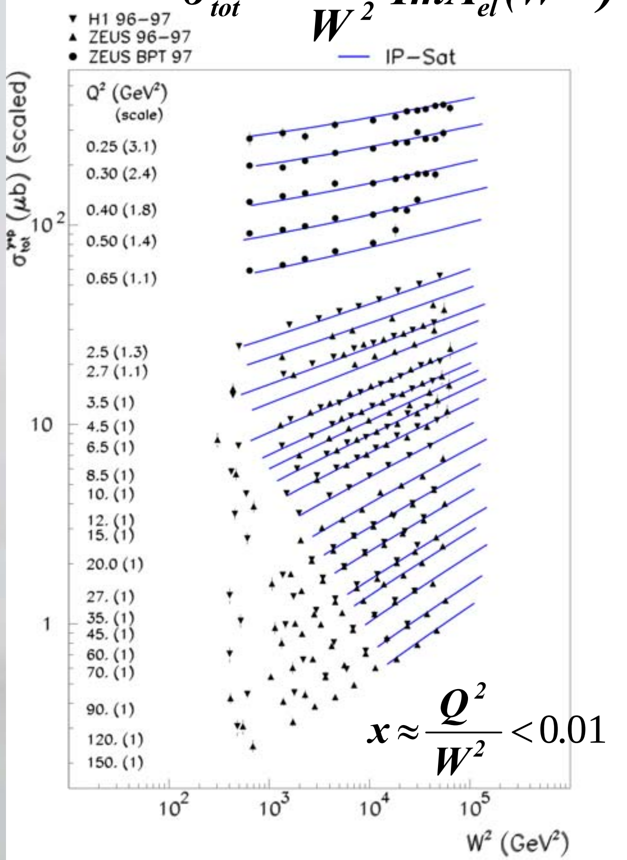
b- CGC
IIM+KMW

Low-x Physics @ HERA





$$\sigma_{tot}^{\gamma^* p} = \frac{1}{W^2} Im A_{el}(W^2)$$

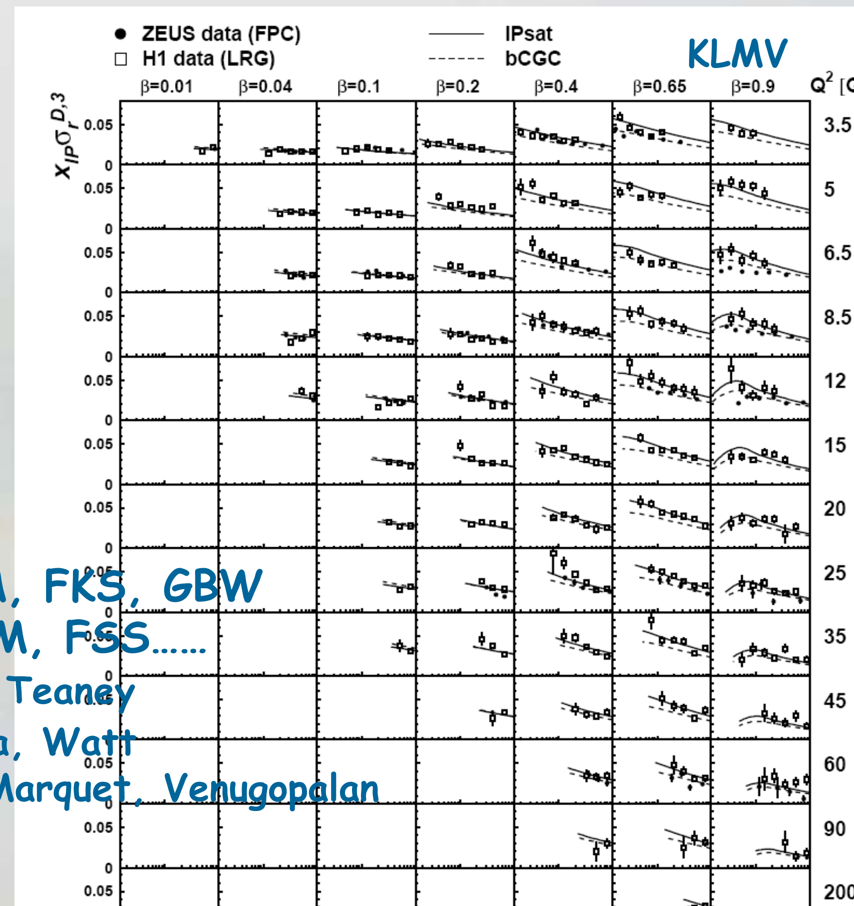


$$x \approx \frac{Q^2}{W^2} < 0.01$$

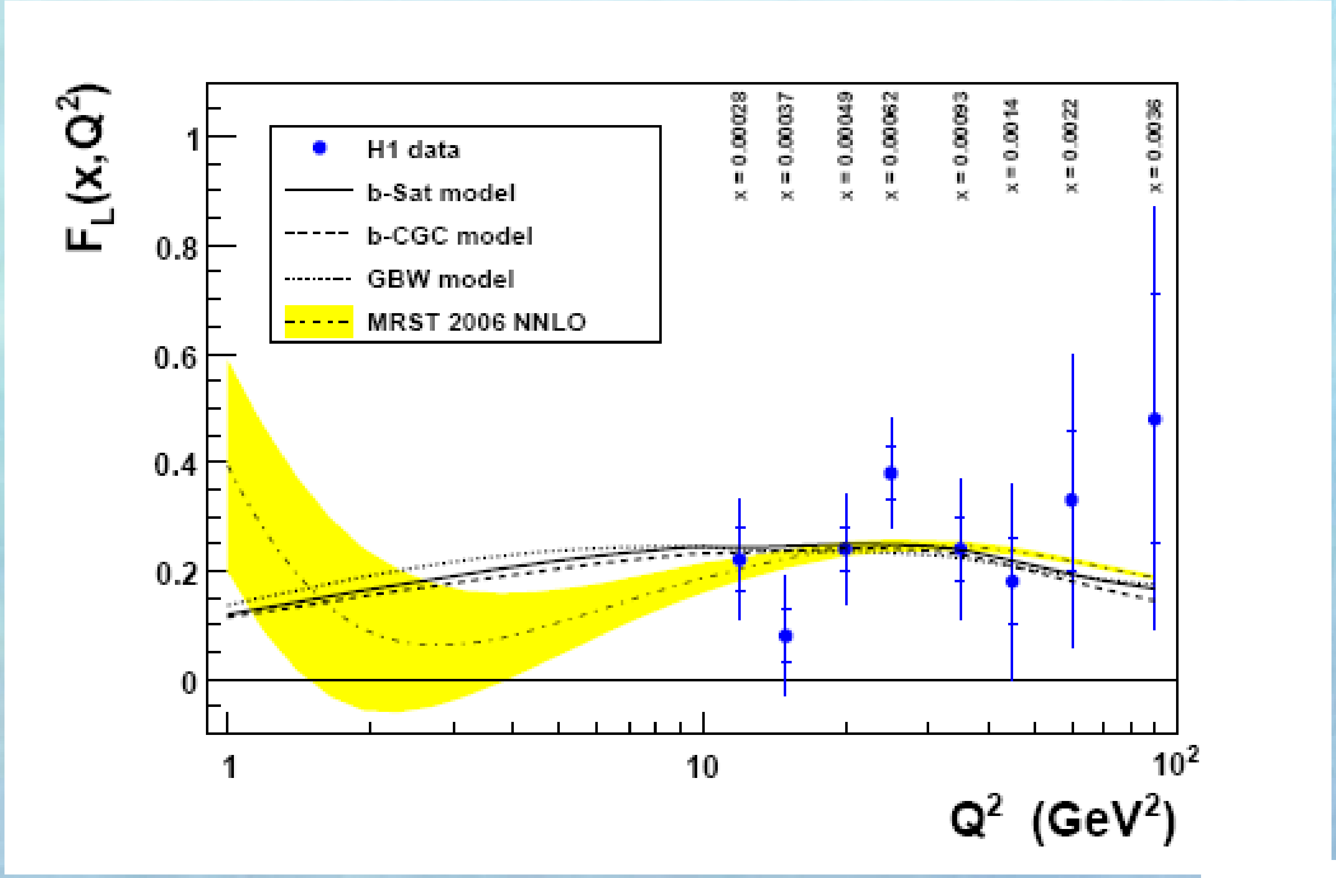
$$\sigma_{tot}^{\gamma^* P}(W,Q^2) = \frac{4\pi^2 \alpha_{em}}{Q^2} \cdot F_2(x,Q^2)$$

Diffraction at HERA is a shadow of DIS
➔
dipole picture,
equivalent to
LO p-QCD
for small
dipoles,
Q~1/r

KLMV



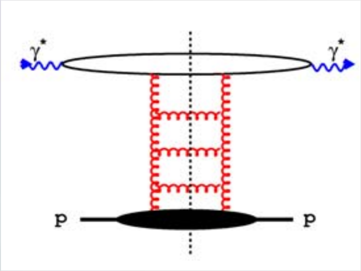
NNPZ, AM, GLM, FKS, GBW
DGKP, BGBK, IIM, FSS……
KT - Kowalski, Teaney
KMW - K, Motyka, Watt
KLMV – K, Lappi, Marquet, Venugopalan



$F_L(x,Q^2)$
H1 data
b-Sat model
b-CGC model
GBW model
MRST 2006 NNLO
x = 0.00028
x = 0.00037
x = 0.00049
x = 0.00062
x = 0.00093
x = 0.0014
x = 0.0022
x = 0.0036
1
0.8
0.6
0.4
0.2
0
1
10
10^2
Q^2 (GeV^2)

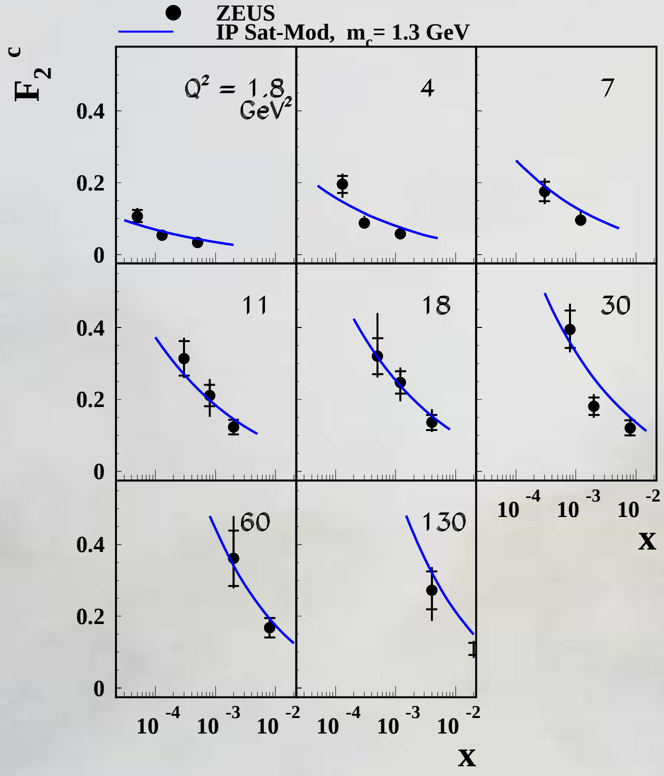
K+Watt

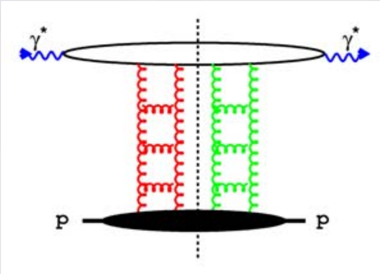
Dipole Picture-gluon density convoluted with the dipole wave functions ➔ simultaneous prediction/description of many reactions



KT

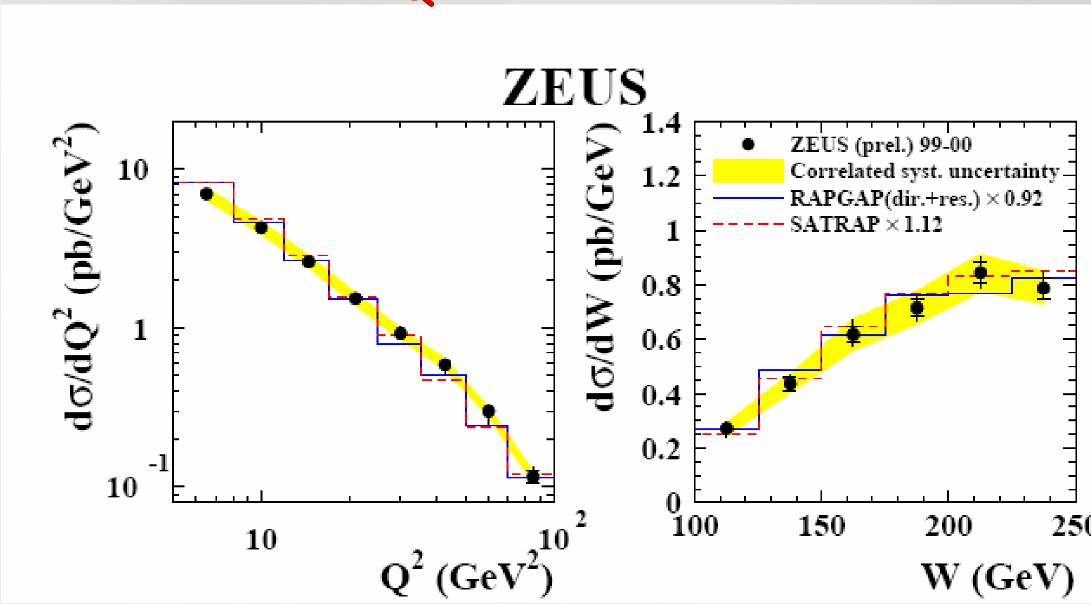
$F_2{}^c$





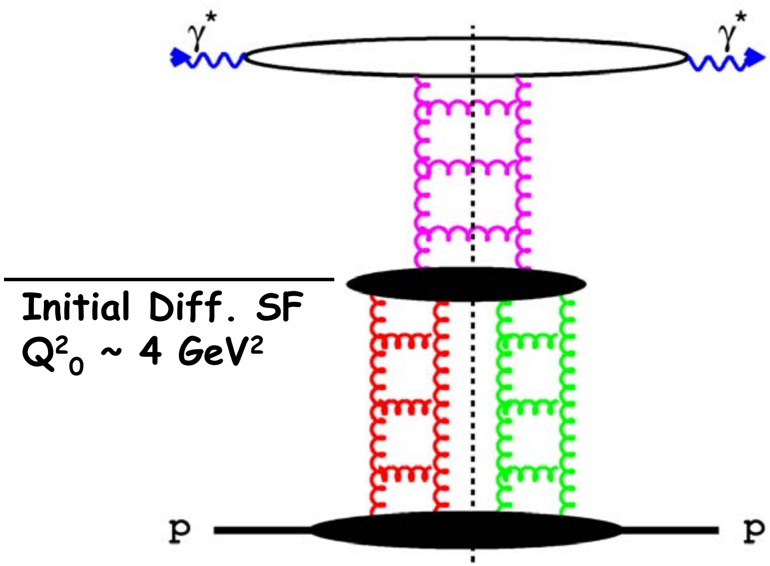
Diffractive Di-jets

Q^2 > 5 GeV^2

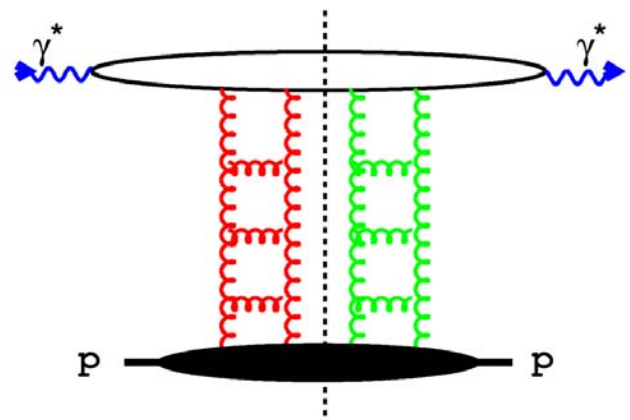


Observation of diffraction indicates that single ladder may not be sufficient
(partons produced from a single chain produce exponentially suppressed rap. gaps)

Diffractive Structure Function

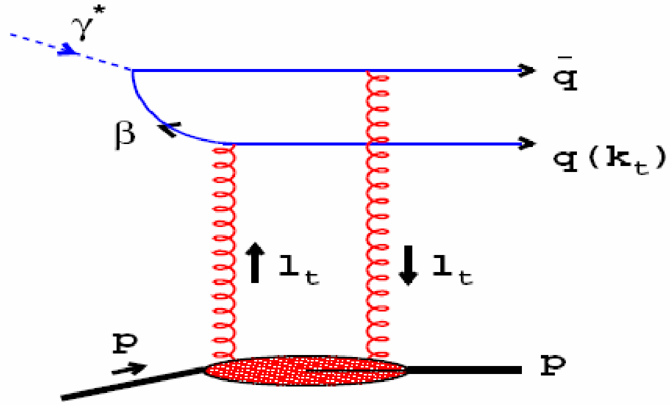


Dipole Model



Study of exclusive diffractive states
may clarify which pattern is right

Only few final states present in DiMo:
qq, qqg (aligned and as jets)
VM



Diffractive production of a $q\bar{q}$ pair

$\tilde{f}(x_{IP}, l_t^2)$ ~ *probability to find a Pomeron(2g) in p*

$= \quad Fourier\ transform\ of\ \sigma_{qq}$

$$\tilde{f}(x_{IP}, l_t^2) \quad = \quad \frac{3\,\sigma_0}{4\pi^2} R_0^2(x_{I\!P}) l_t^2 \exp(-R_0^2(x_{I\!P})\, l_t^2)$$

$$\left.\frac{d\sigma^T}{dt\, dM^2}\right|_{t=0} = \sum_f e_f^2 \frac{\pi^2 \alpha_{em}}{12\, Q^4} \frac{\beta^2}{(1-\beta)^2} \int dk_t^2 \frac{k_t^2 + m_q^2}{k_t^2 \sqrt{1 - 4\beta k^2/Q^2}} \left\{ \left[1 - \frac{2\beta k^2}{Q^2}\right] P_{I\!Pq}^T + 4 \frac{k_t^2 m_q^2}{k^4} P_{I\!Pq}^L \right\} \qquad k^2 = (k_t^2 + m_q^2)/(1-\beta)$$

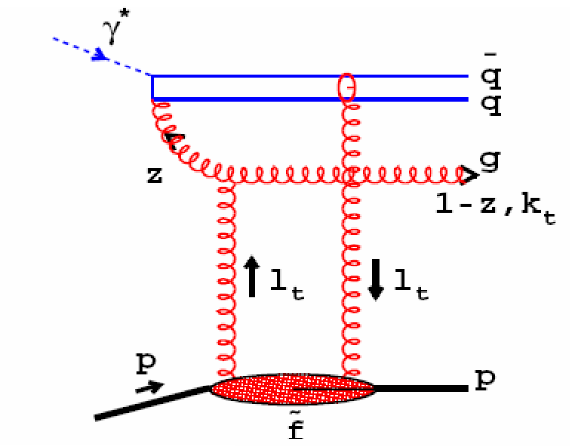
$$\left.\frac{d\sigma^L}{dt\, dM^2}\right|_{t=0} = \sum_f e_f^2 \frac{4\pi^2 \alpha_{em}}{3\, Q^6} \frac{\beta^3}{(1-\beta)} \int dk_t^2 \frac{k^2}{\sqrt{1 - 4\beta k^2/Q^2}} P_{I\!Pq}^L$$

$$P_{I\!Pq}^T(\beta, k^2) = \left| \int \frac{dl_t^2}{l_t^2} \tilde{f}(l_t^2) \left[1 - 2\beta - 2\frac{m_q^2}{k^2} + \frac{l_t^2 - (1-2\beta)k^2 + 2m_q^2}{\sqrt{(l_t^2 + k^2)^2 - 4 l_t^2 k_t^2}} \right] \right|^2$$

$$P_{I\!Pq}^L(\beta, k^2) = \left| \int \frac{dl_t^2}{l_t^2} \tilde{f}(l_t^2) \left[1 - \frac{k^2}{\sqrt{(l_t^2 + k^2)^2 - 4 l_t^2 k_t^2}} \right] \right|^2$$

~ *probability for a Pomeron(2g) to couple to a quark*

Diffractive production of a qqg state



$$\left.\frac{d\sigma}{dt\,dM^2}\right|_{t=0} = 2\sum_f e_f^2 \frac{4\pi^2\alpha_{em}}{Q^2}\frac{\beta^2}{Q^2}\int dk_t^2 \int d\phi \int dq_t^2$$

$$\frac{\alpha_s}{2\pi}\int \frac{dz}{z} P_{qg}\left(\frac{\beta}{z}\right) P_{I\!P g}\left(z, \frac{k_t^2}{1-z}\right)$$

D.C. : $Q^2 \gg q_t^2 \gg k_t^2$

$$P_{I\!P g}(z,k^2) = \frac{9}{64}\frac{1}{z}\frac{1}{(1-z)^3}\left\{\int \frac{dl_t^2}{l_t^2}\tilde{f}(x_{I\!P}, l_t^2)\right.$$

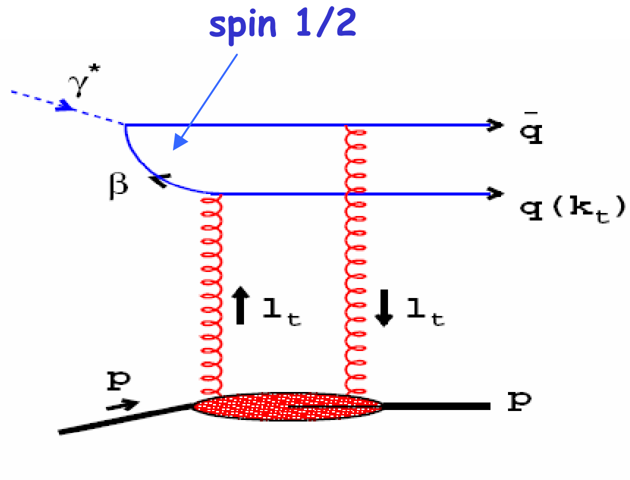
$$\left.\left[z^2+(1-z)^2+\frac{l_t^2}{k^2}-\frac{[(1-2z)k^2-l_t^2]^2+2z(1-z)k^4}{k^2\sqrt{(l_t^2+k^2)^2-4(1-z)l_t^2k^2}}\right]\right\}^2$$

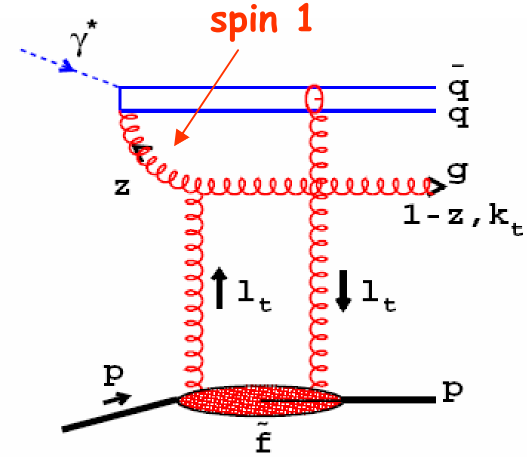
$$\boxed{\begin{aligned} z &= (Q^2+m^2)/(Q^2+M^2) \\ m^2 &= (q+\bar{q})^2+k_t^2 \end{aligned}}$$

$$P_{qg}\left(\frac{\beta}{z}\right) = \frac{1}{2}\frac{1-2\frac{q_t^2+m_q^2}{m^2}}{q_t^2+m_q^2}\left[\left(\frac{\beta}{z}\right)^2+\left(1-\frac{\beta}{z}\right)^2\right]$$

$$+\frac{4}{q_t^2+m_q^2}\frac{\beta}{z}\left(1-2\frac{\beta}{z}\right)\frac{m_q^2}{Q^2}$$

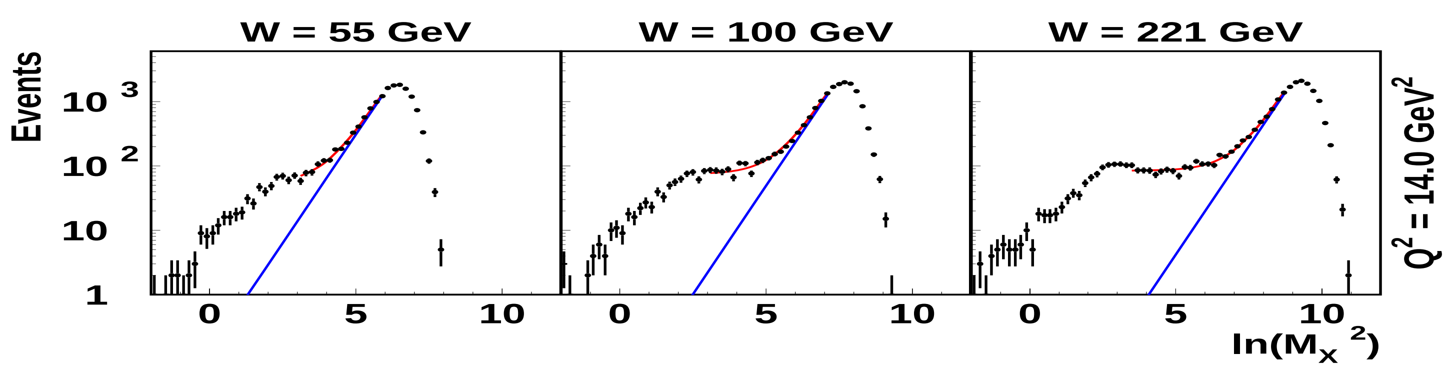
$$+\frac{2m^2}{(q_t^2+m_q^2)^2}\left(\frac{\beta}{z}\right)^2\left(1-2\frac{\beta}{z}\right)\frac{m_q^2}{Q^2}$$

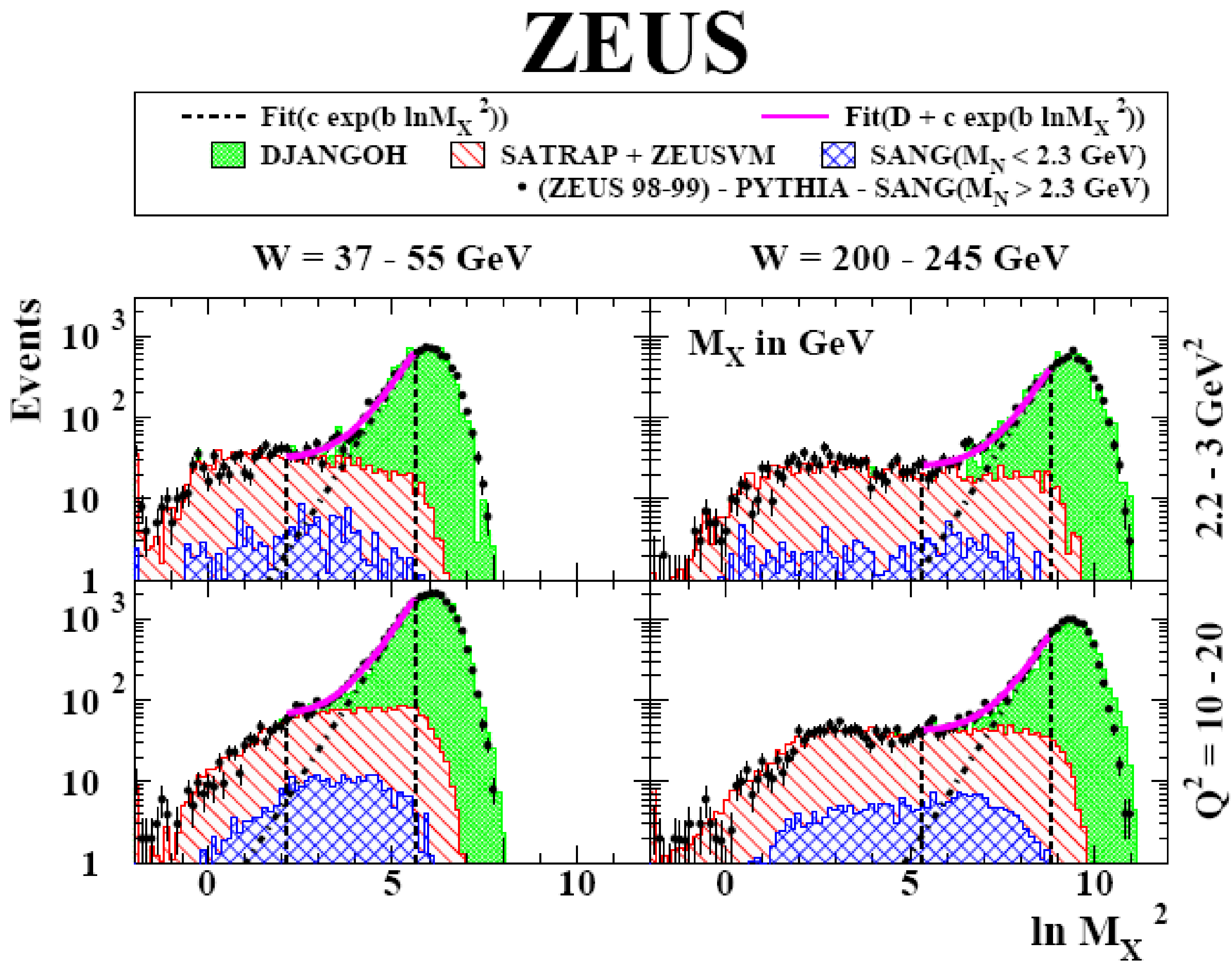




$\sigma \sim s^{\alpha-1}$ ➔ $dN/d\log M^2_X \sim$ const

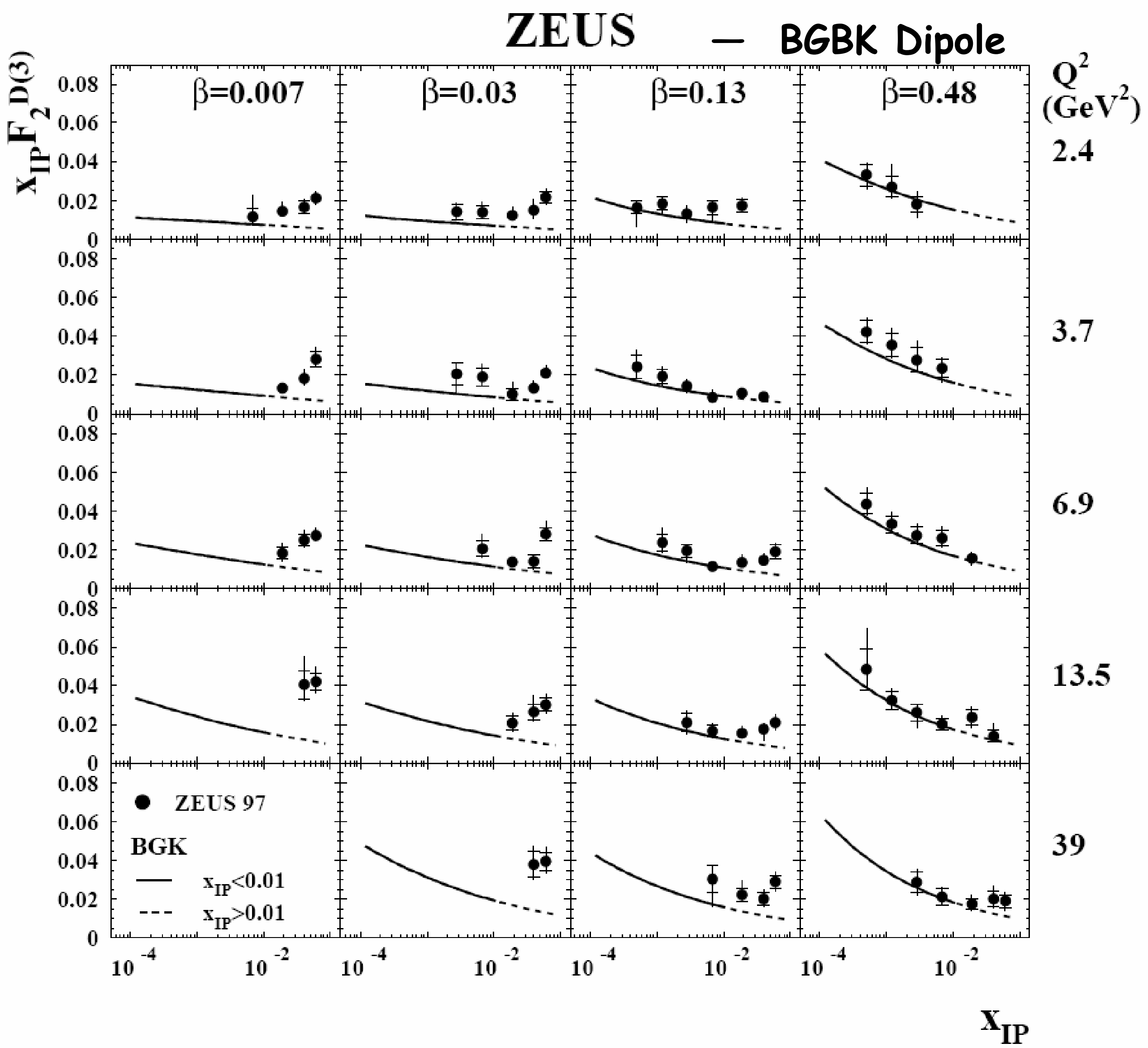
*





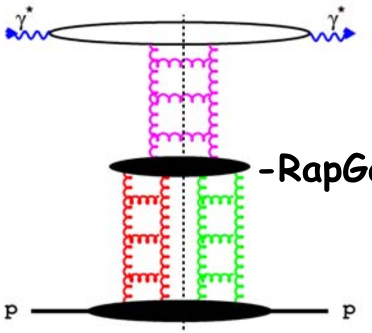
ZEUS
Fit(c exp(b lnM_X^2))
Fit(D + c exp(b lnM_X^2))
DJANGOH
SATRAP + ZEUSVM
SANG(M_N < 2.3 GeV)
• (ZEUS 98-99) - PYTHIA - SANG(M_N > 2.3 GeV)
W = 37 - 55 GeV
W = 200 - 245 GeV
Events
M_X in GeV
2.2 - 3 GeV^2
Q^2 = 10 - 20
ln M_X^2

Inclusive Diffraction
LPS

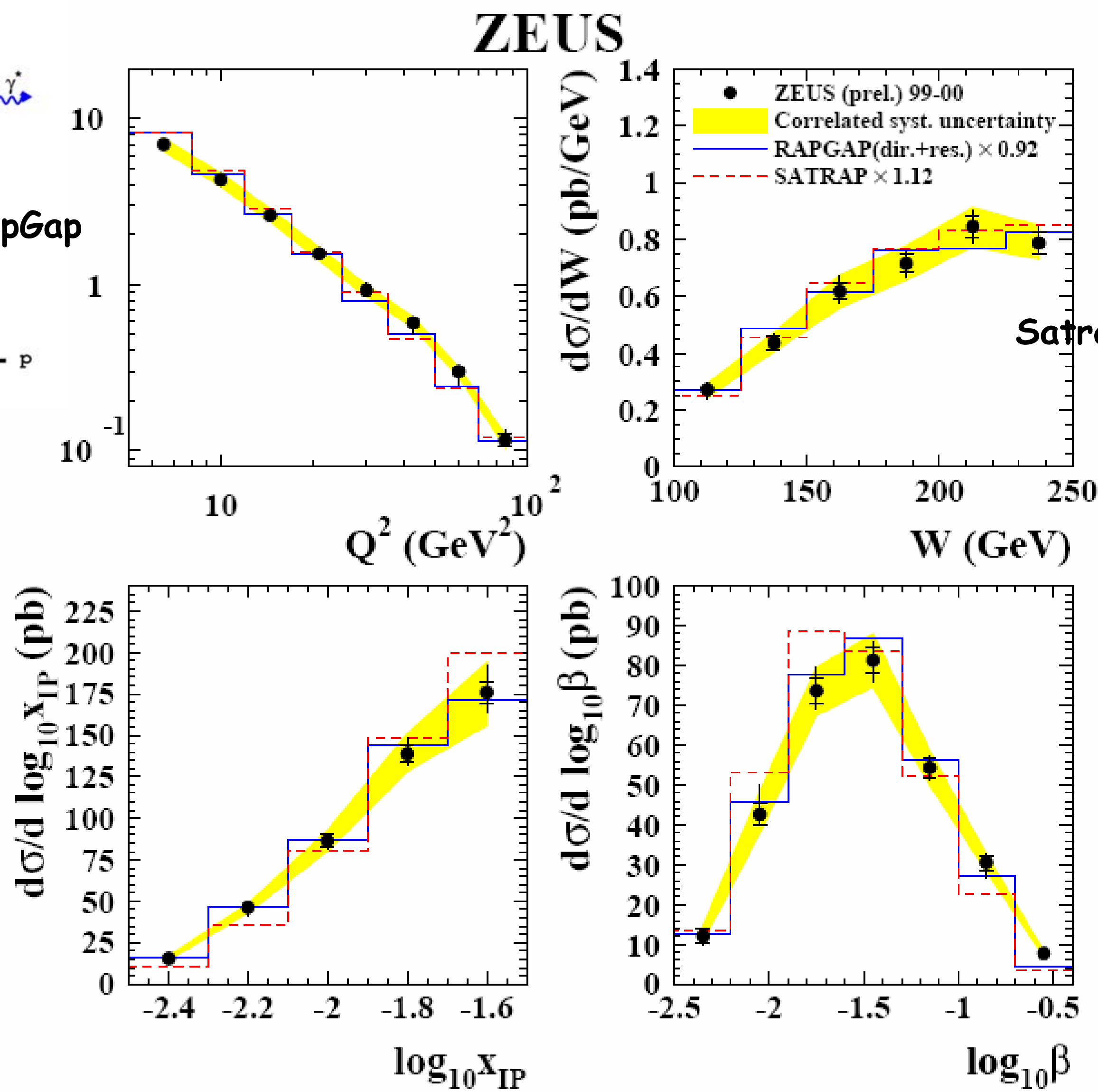


Diffractive Di-jets

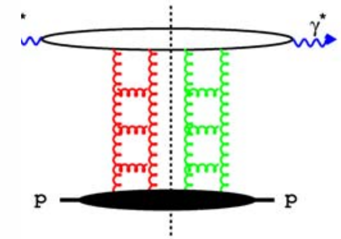
Q^2 > 5 GeV^2



-RapGap

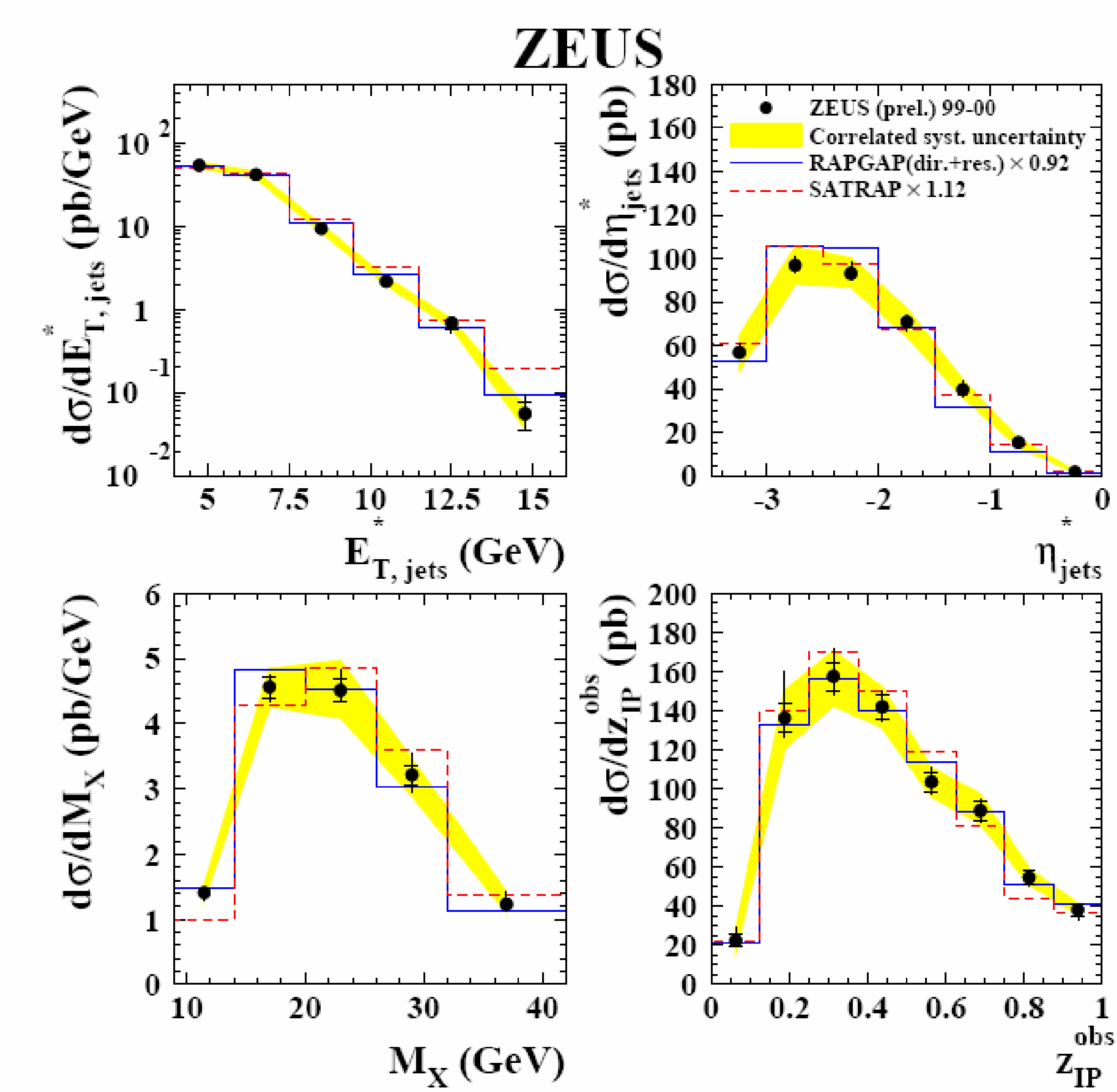


Satrap



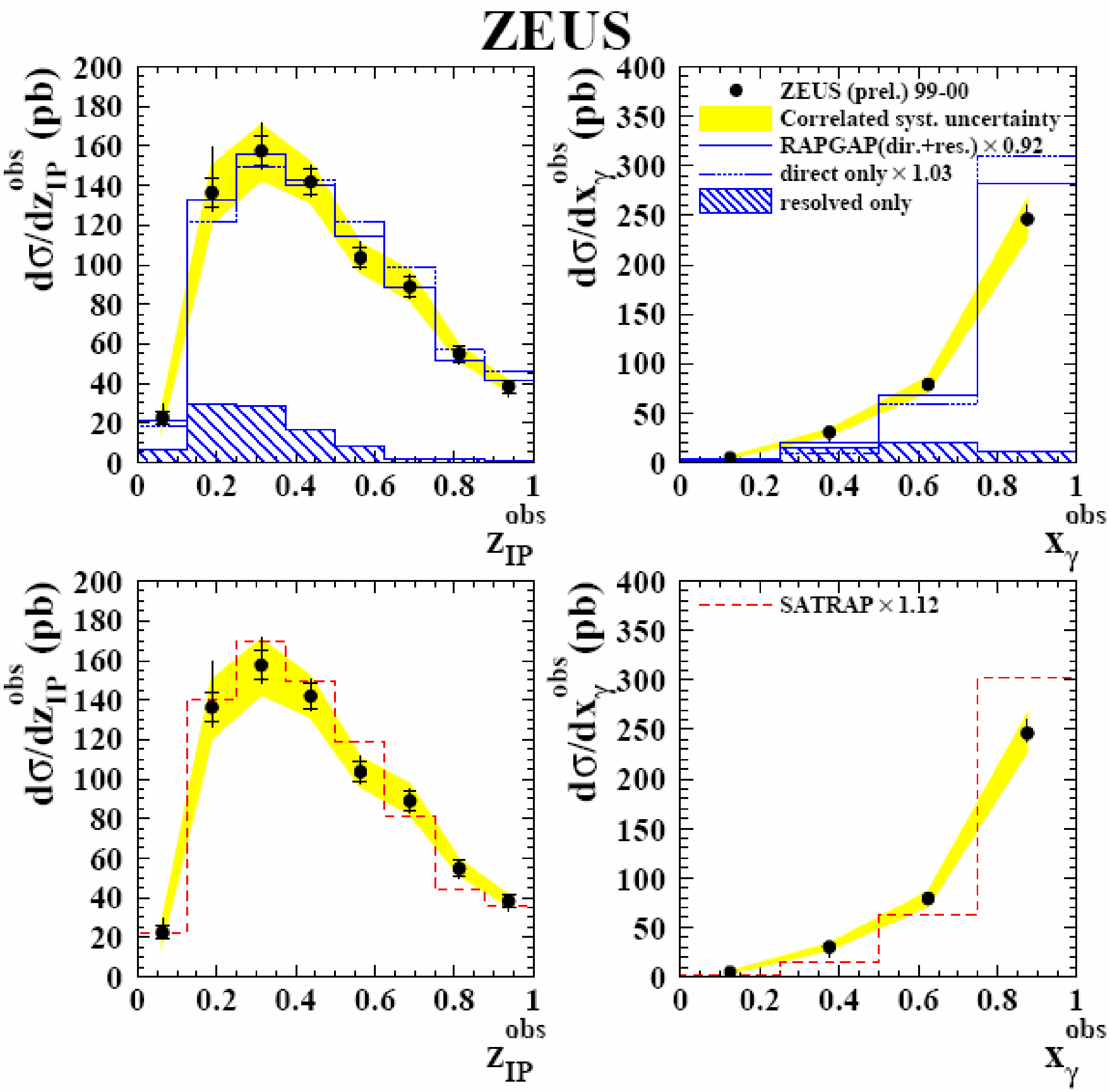
Diffractive Di-jets

$Q^2 > 5\ GeV^2$

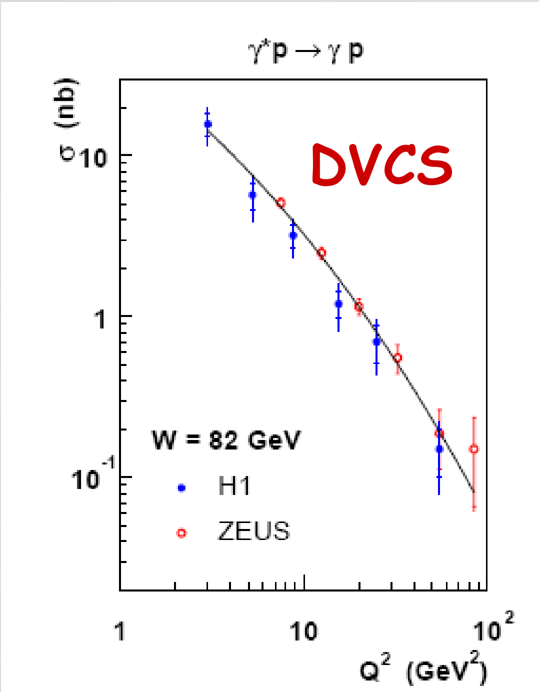


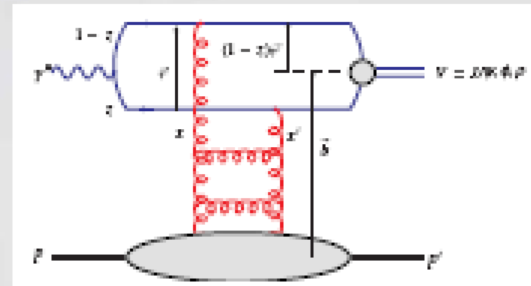
Diffractive Di-jets

$Q^2 > 5$ GeV^2



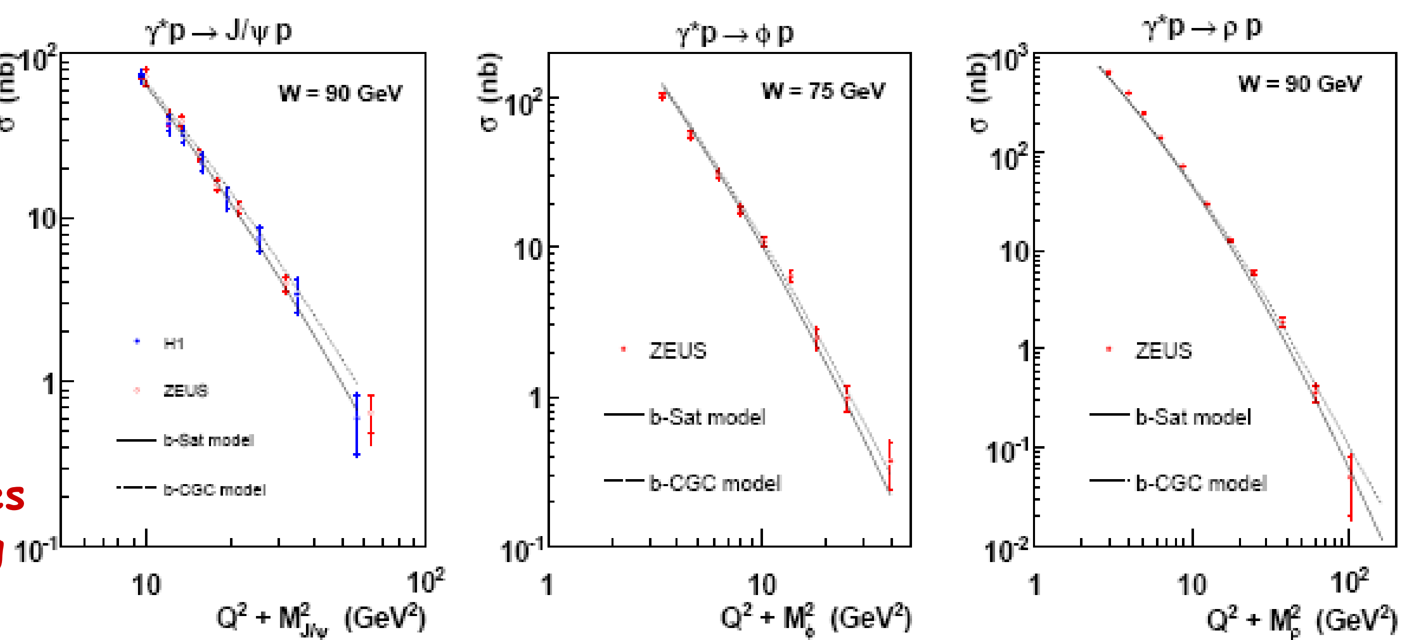
Dipole Picture-gluon density convoluted with the dipole wave functions ➔ simultaneous prediction/description of many reactions





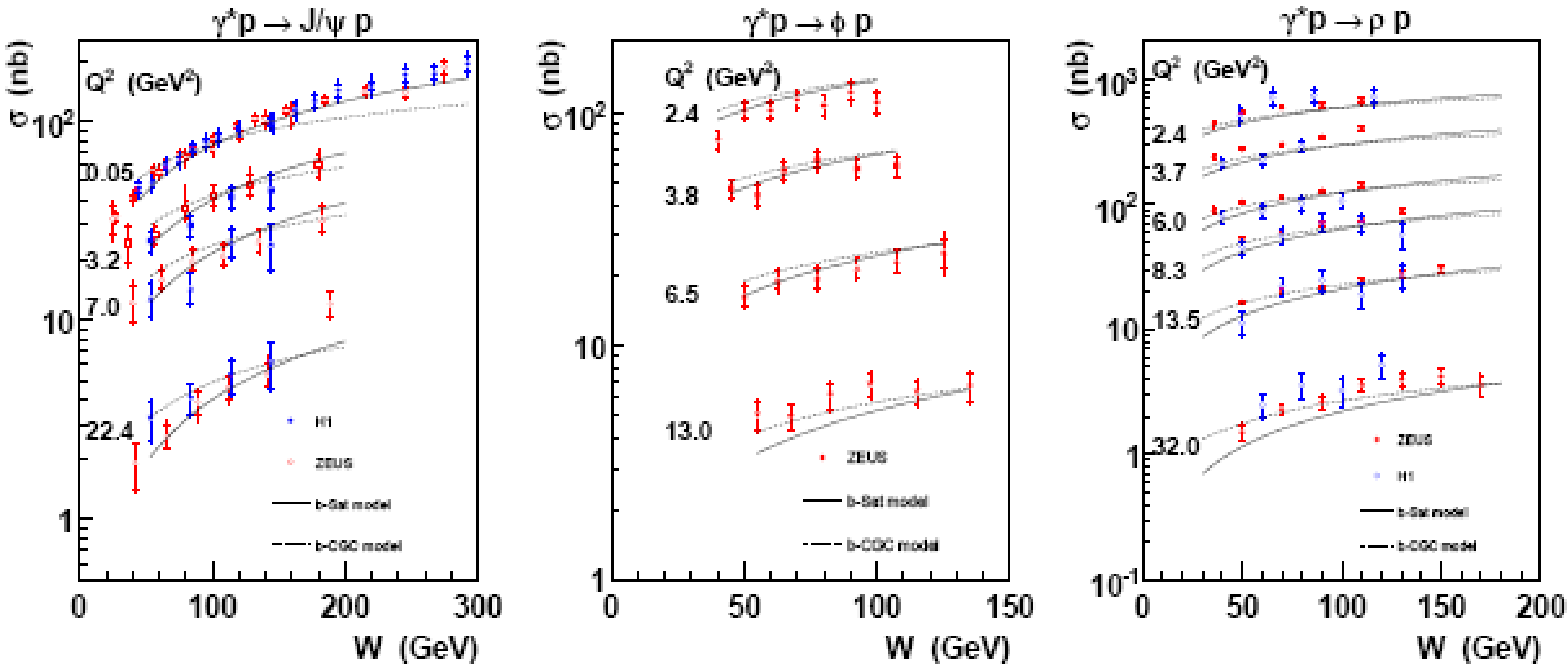
Vector Mesons

KMW

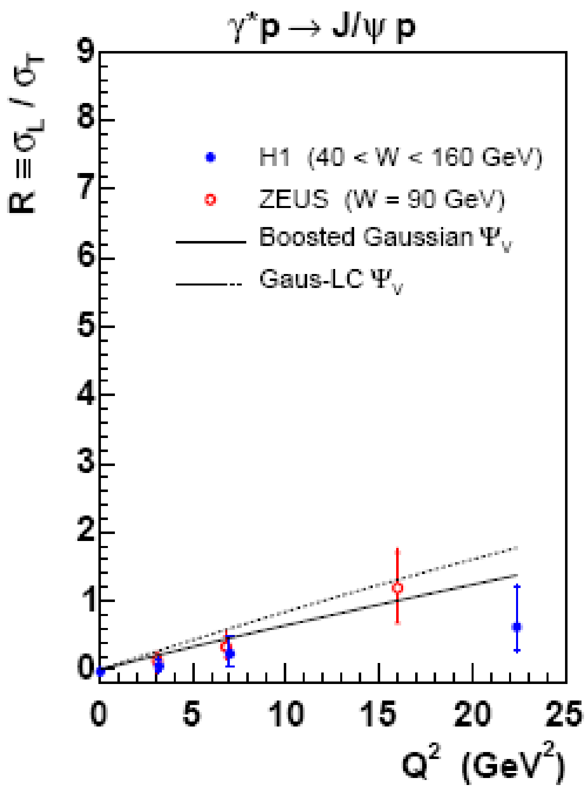


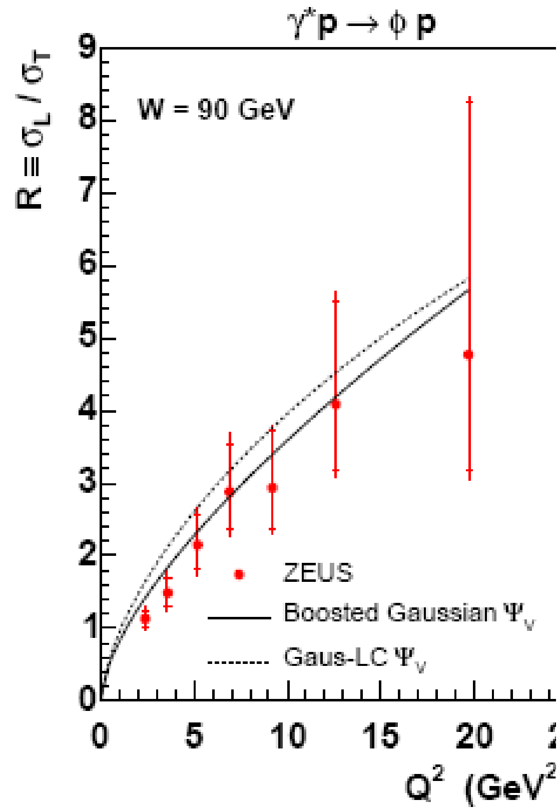
Note: educated guesses for VM wf are working very well

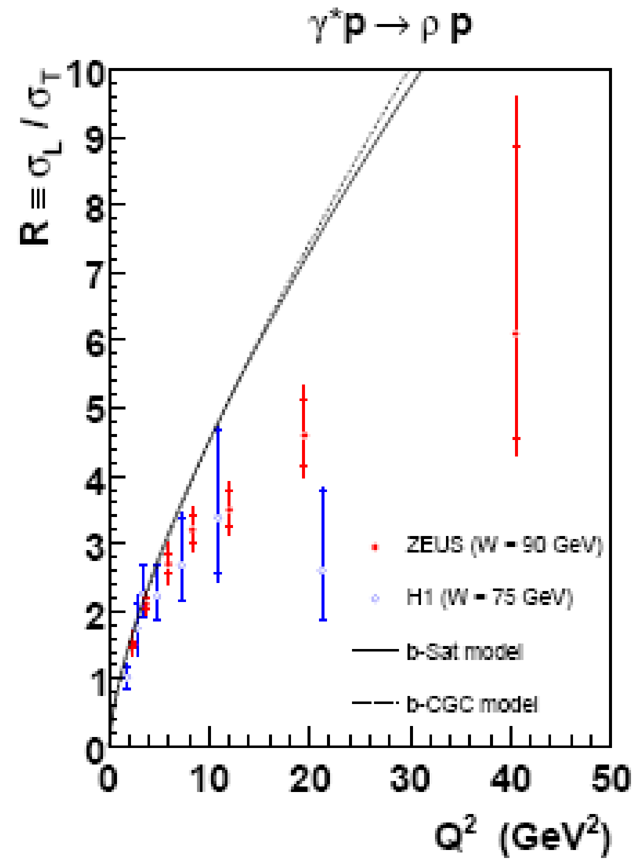
KMW


$\gamma^* p \to J/\psi\ p$
σ (nb)
Q^2 (GeV^2)
0.05
3.2
7.0
22.4
H1
ZEUS
b-Sat model
b-CGC model
W (GeV)
$\gamma^* p \to \phi\ p$
σ (nb)
Q^2 (GeV^2)
2.4
3.8
6.5
13.0
ZEUS
b-Sat model
b-CGC model
W (GeV)
$\gamma^* p \to \rho\ p$
σ (nb)
Q^2 (GeV^2)
2.4
3.7
6.0
8.3
13.5
32.0
ZEUS
H1
b-Sat model
b-CGC model
W (GeV)

KMW



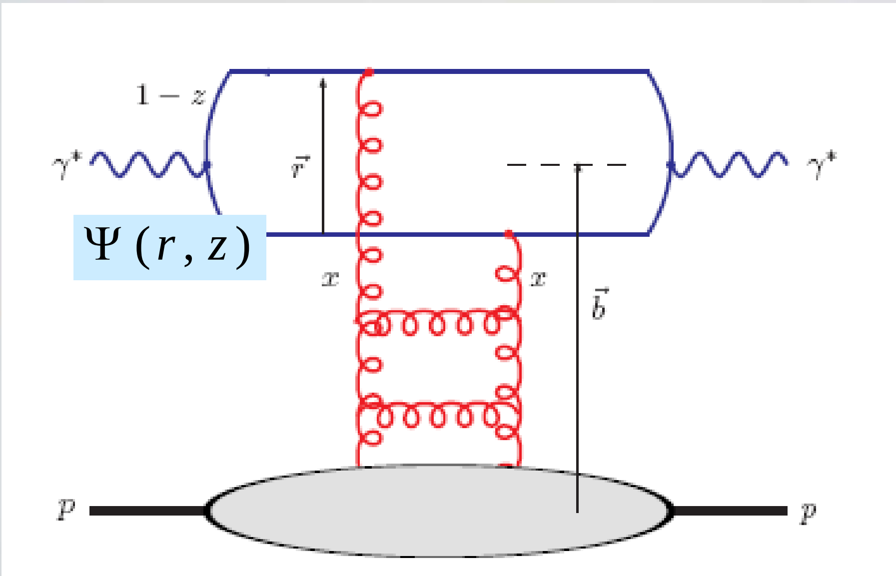


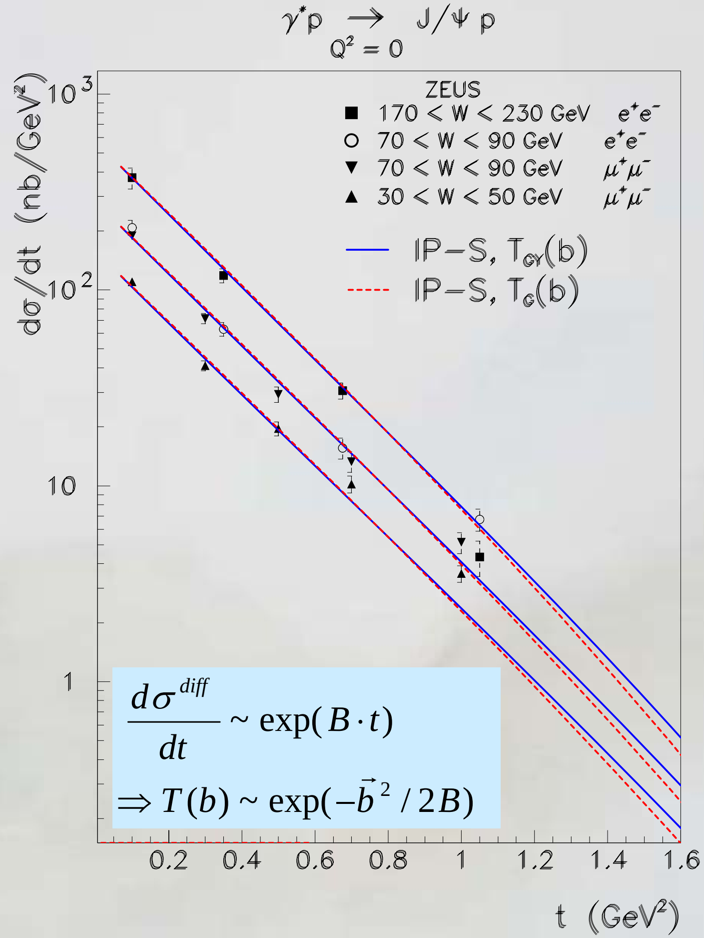


Note: educated guesses for J/Ψ and ϕ wave functions are working very well

More work to do for ρ meson wave function

Extracting Proton Vertex using Dipole Models





Can use vector meson production to extract proton profile:

$$\frac{d\sigma_{VM}^{\gamma^* p}}{dt} = \frac{1}{16\pi} \left| \int d^2\vec{r} \int d^2 b e^{-i\vec{b}\cdot\vec{\Delta}} \int_0^1 dz \Psi_{VM}^* \; 2\left\{1 - exp(-\frac{\Omega}{2})\right\} \Psi \right|^2$$

KT, KMW

$$\Omega = \frac{\pi^2}{N_C} r^2 \alpha_s(\mu^2) xg(x,\mu^2) T(b)$$

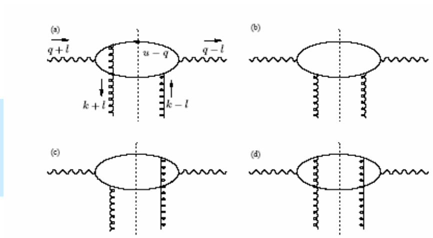
T(b)-proton shape

Description of the size of interaction region B_D

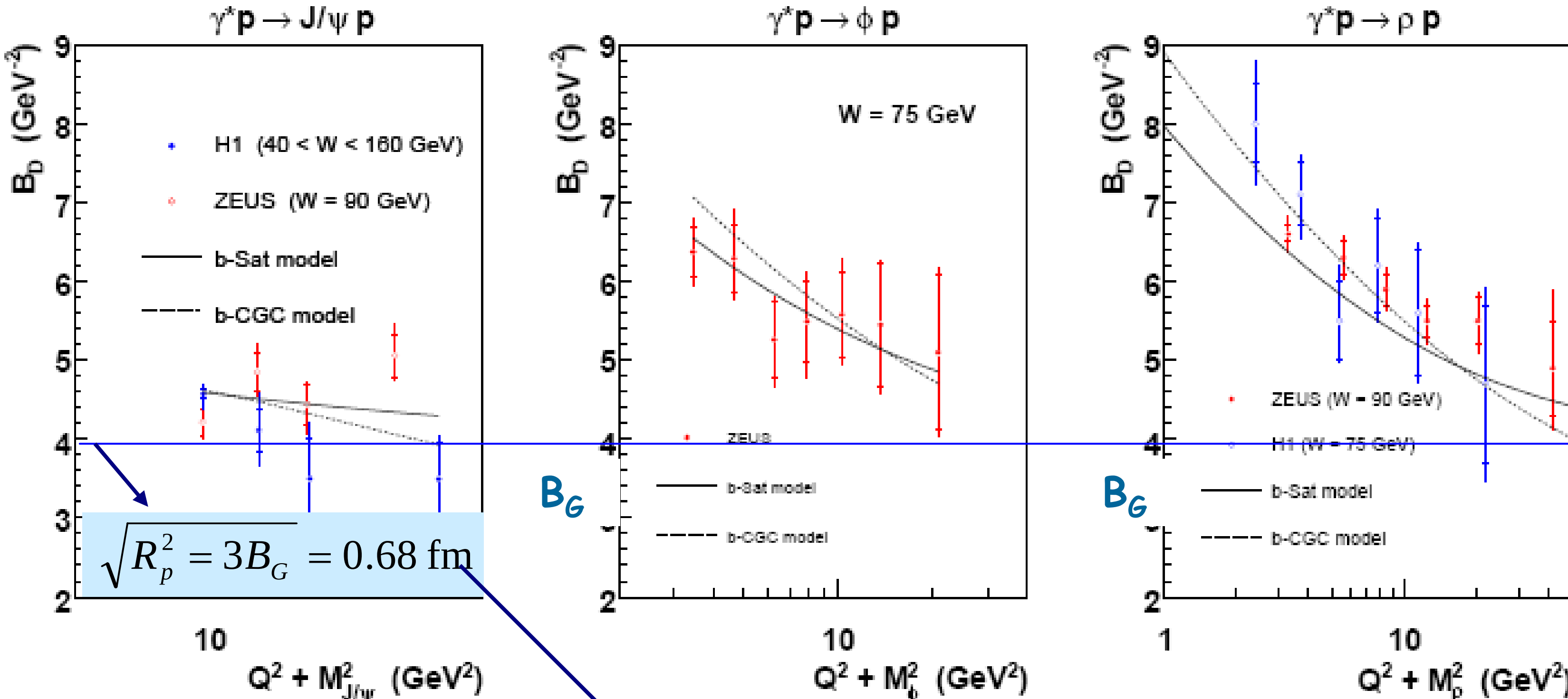
$$\frac{d\sigma^{diff}}{dt} \sim \exp(B_D \cdot t) \qquad \Rightarrow T(b) \sim \exp(-\vec{b}^2 / 2B_G)$$

Modification by Bartels, Golec-Biernat, Peters

$$e^{i\vec{b}\cdot\vec{\Delta}} \rightarrow e^{i(\vec{b}+(1-z)\vec{r})\cdot\vec{\Delta}}$$



KMW



B_G

B_G

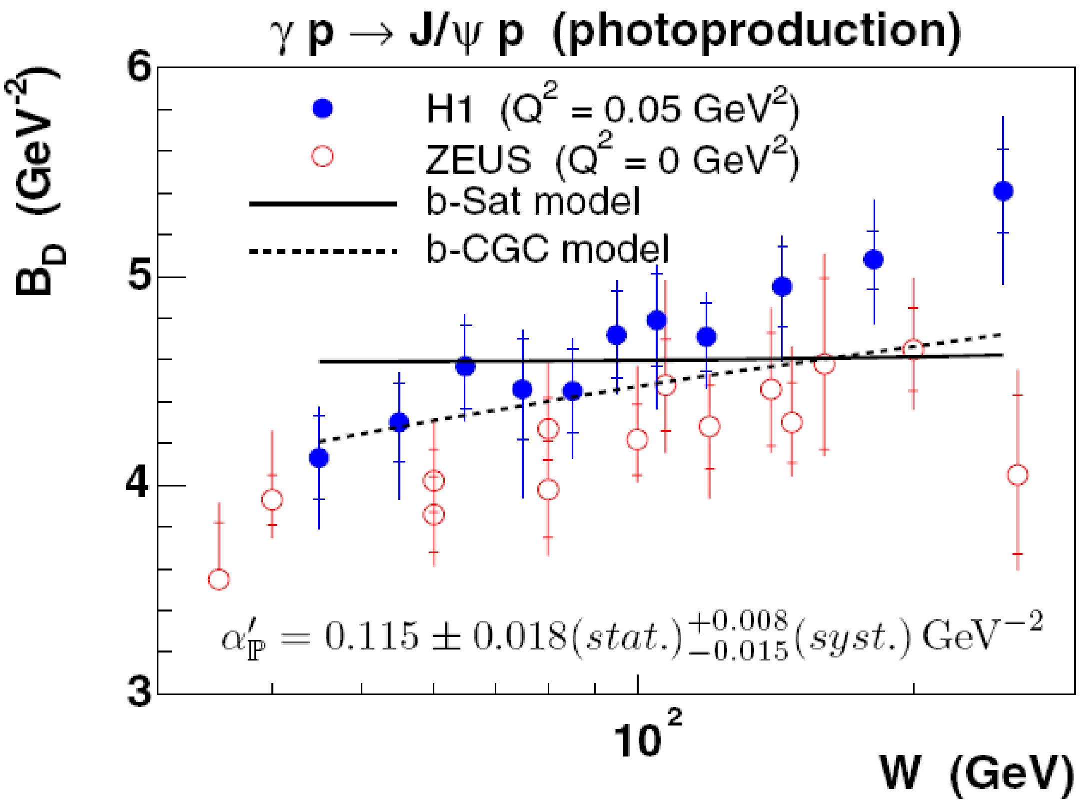
$$\sqrt{R_p^2 = 3B_G} = 0.68 \text{ fm}$$

$$R_p = 0.870 \pm 0.008 \text{ fm}$$

$$\Rightarrow B_G = 6.48 \text{ GeV}^2$$

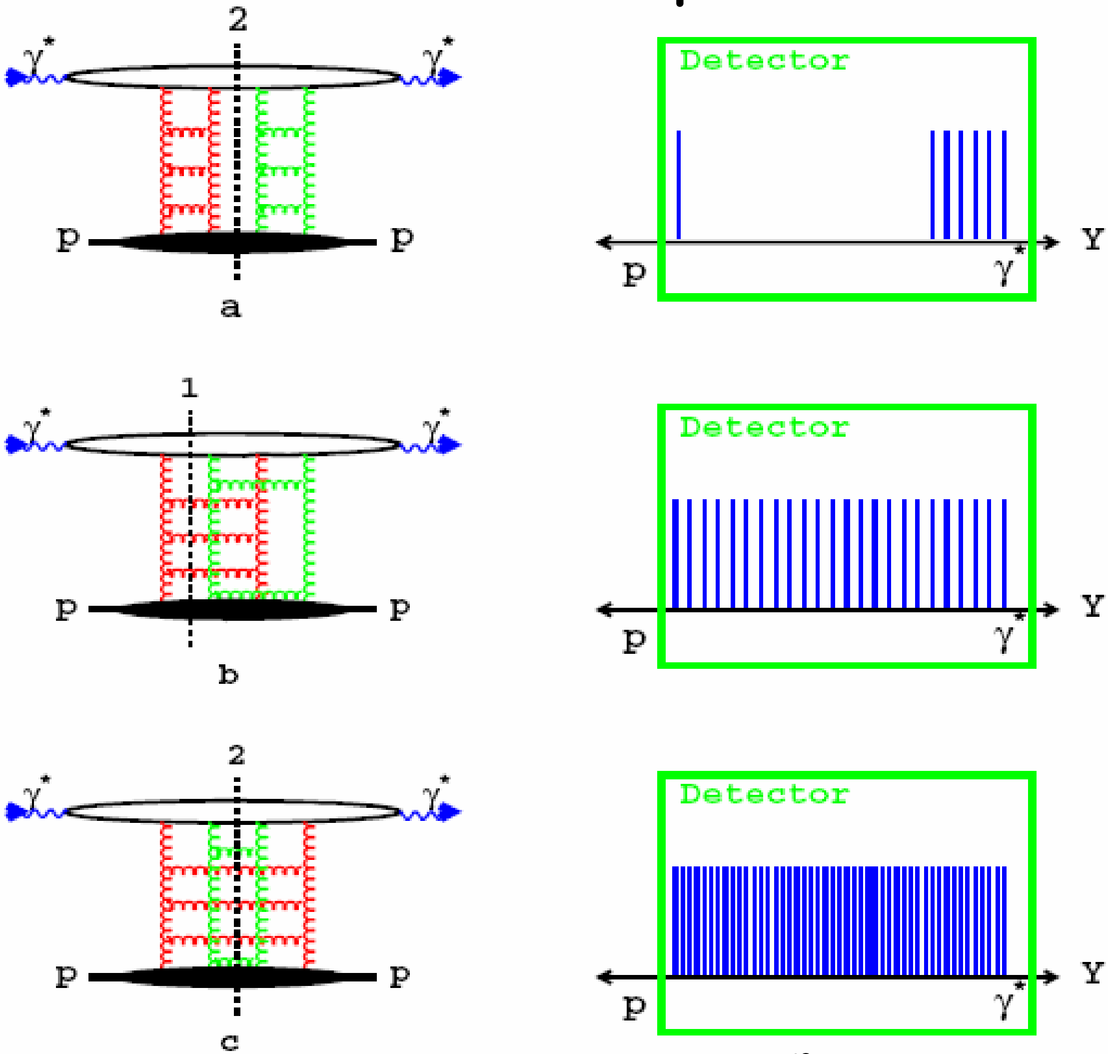
the gluonic proton radius smaller than the quark radius

measurement of α'

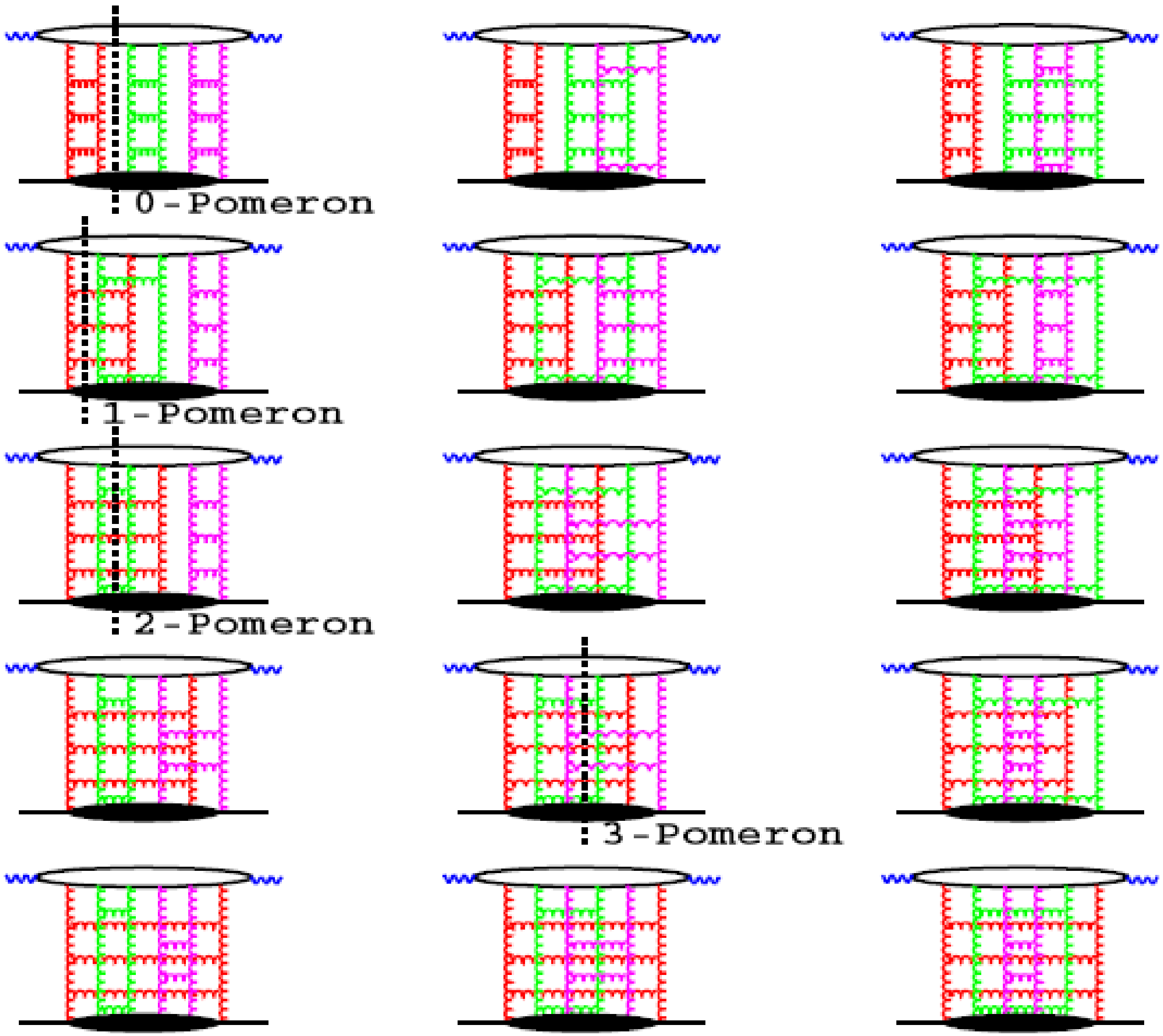


α' measurement suggests that $B_G \sim 3\ \mathrm{GeV}^{-2}$
➔ $R_P \sim 0.6$ fm

AGK rules in the Dipole Model



The cross-section for k-cut pomerons: $\sigma_k = \sum_{m=k}^{\infty} (-1)^{m-k} 2^m \frac{m!}{k!(m-k)!} F^{(m)}$

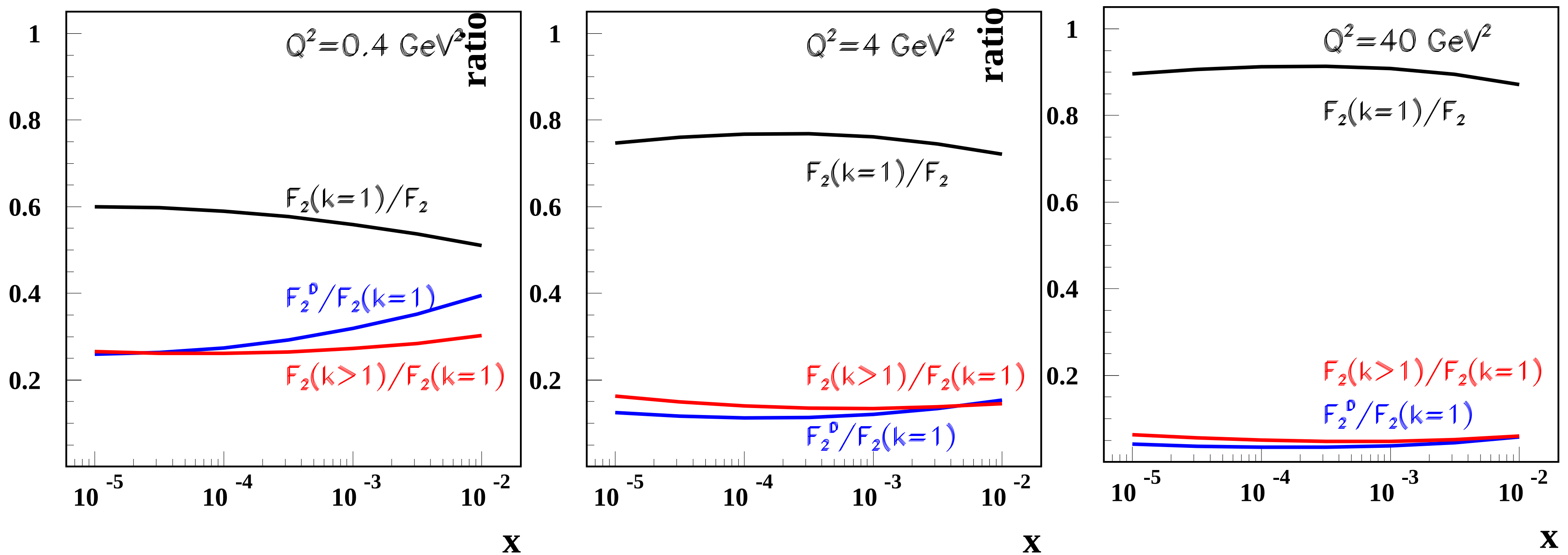


: 0 - Pomeron
: 1 - Pomeron
: 2 - Pomeron
: 3 - Pomeron

AGK rules in the Dipole Model

$$\frac{d\sigma_k}{d^2b} = \frac{\Omega^k}{k!}\exp(-\Omega)$$

$$\Omega = \frac{\pi^2}{N_C} r^2 \alpha_s(\mu^2) x g(x,\mu^2) T(b)$$



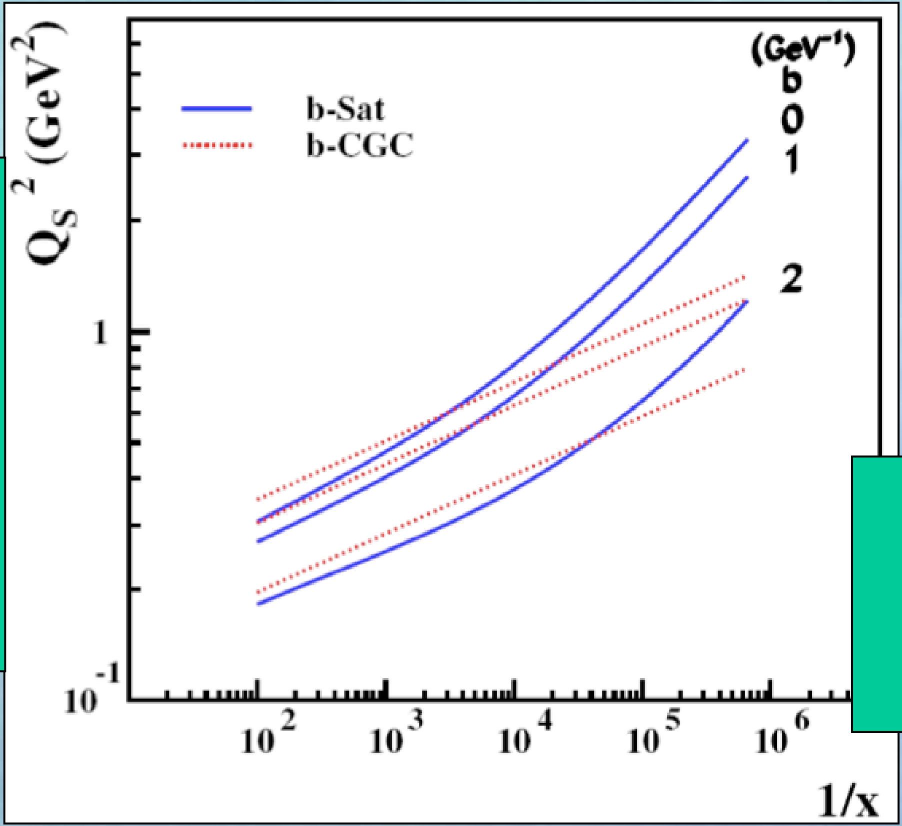
Note: AGK rules underestimate the amount of diffraction in DIS

Saturation

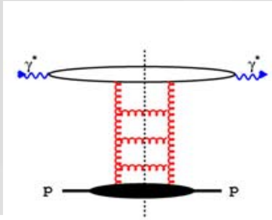
Q_S: Measure of gluon density for which a dipole, r_S, is absorbed by a proton with 1-1/e probability: $Q_S=2/r_S$

BGBK→ Saturation shapes data in a similar way as DGLAP

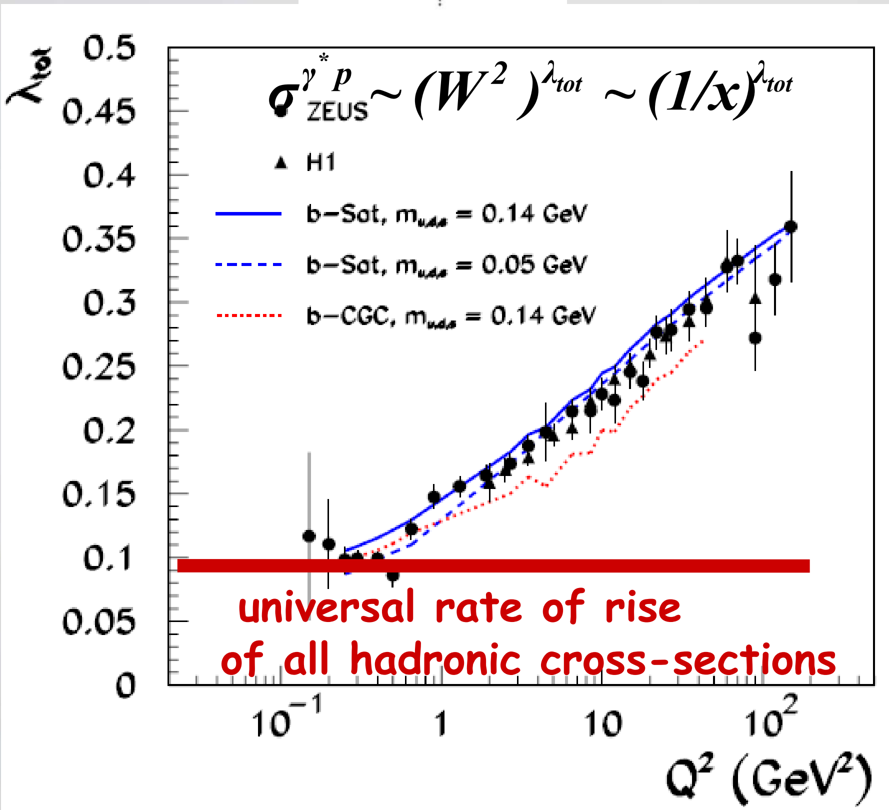
→ Difficult to distinguish at HERA

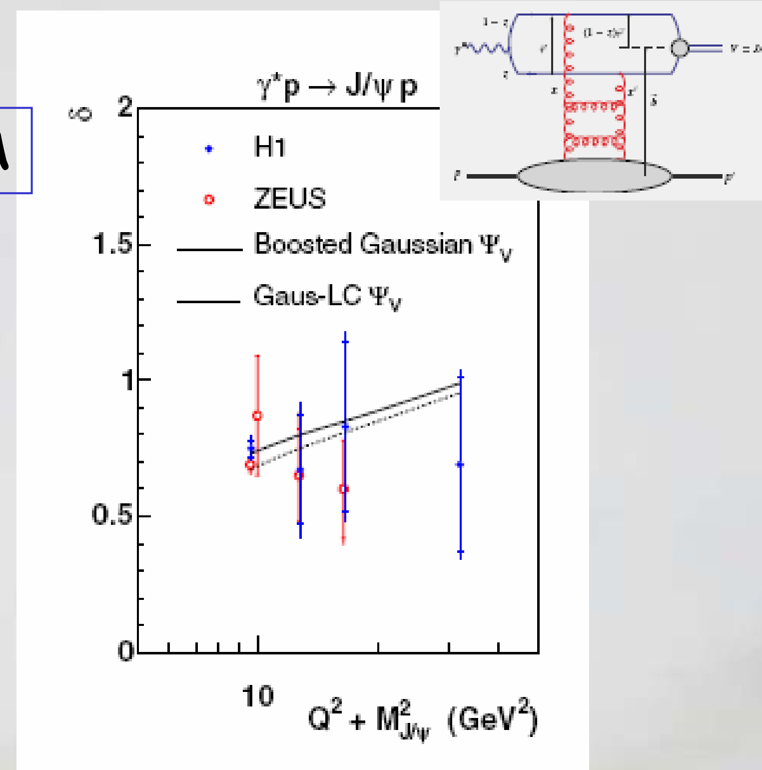


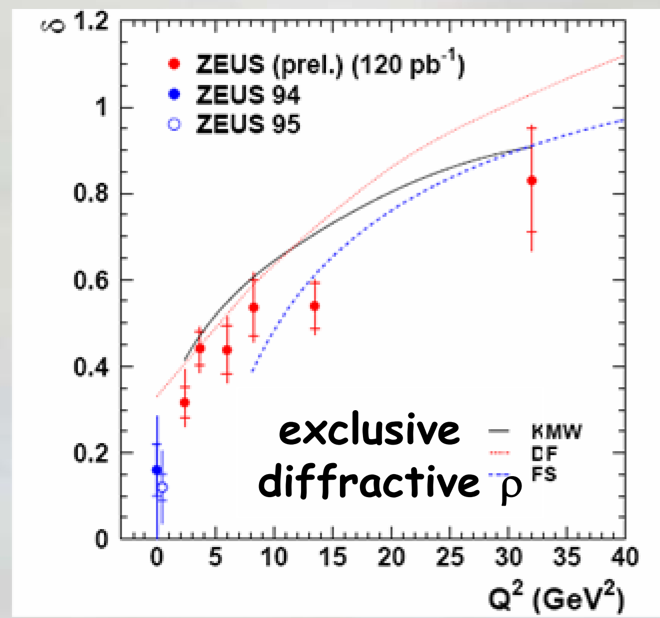
→ Oomph factor Increase saturation by going to nuclei



Discovery of HERA



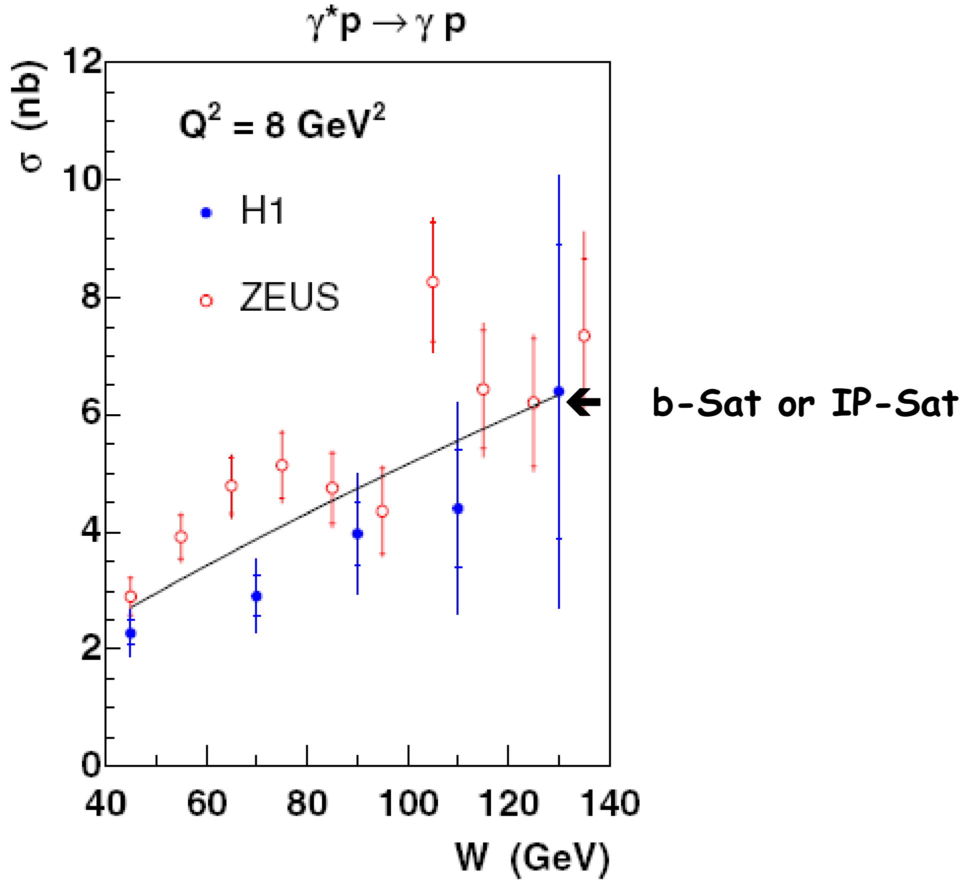




Universality of the observed intercepts

➔ Universal, "Pomeron like" QCD object
soft and hard Pomeron join together

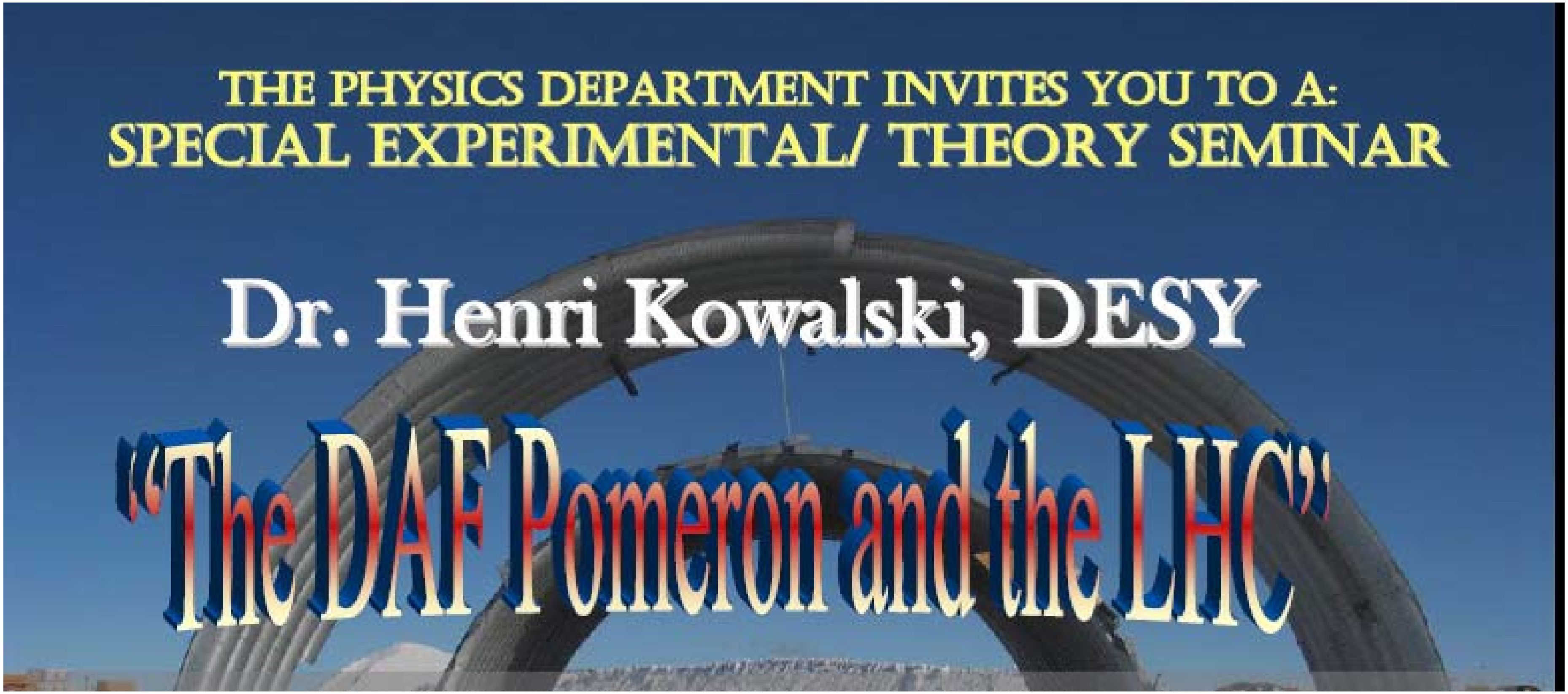
Pomeron at work
Rise of the DVCS cross-sections



At EIC (LHeC) it should be possible to reduce the errors by a large factor, O(100)
➔ detailed study of the Pomeron possible

Ongoing Investigation

First talks at Columbia & Hampton Universities, May 2008

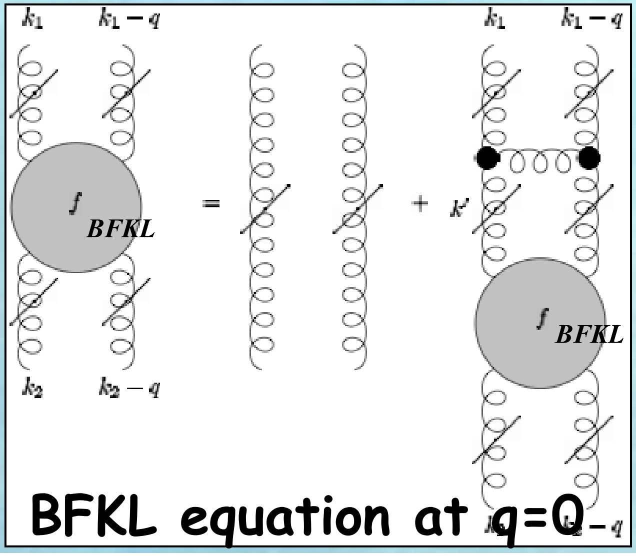


Evidence for the discrete asymptotically-free BFKL Pomeron from HERA data

J. Ellis[a], H. Kowalski[b], D.A. Ross[a,c,*]

Physics Letters B **in print**

Basics of BFKL



BFKL equation at q=0

solved by finding a complete set of eigenfunctions

$$\omega\tilde f(\omega,\mathbf{k_1},\mathbf{k_2}) = \delta^2(\mathbf{k_1}-\mathbf{k2}) + \frac{\alpha C_A}{\pi^2}\int \frac{d^2\mathbf{k}'}{(\mathbf{k_1}-\mathbf{k}')^2}\left[\tilde f(\omega,\mathbf{k}',\mathbf{k_2}) - \frac{\mathbf{k_1}^2}{\mathbf{k}'^2+(\mathbf{k}'-\mathbf{k_1})^2}\tilde f(\omega,\mathbf{k_1},\mathbf{k_2})\right]$$

Eigen-functions

$$f_\omega(k^2) = \frac{(k^2)^{i\nu}}{\sqrt{k^2}}$$

$$\omega = \bar{\alpha}_s\chi(\nu)$$

Characteristic function

$$\chi(\nu) = -2\gamma_E - \psi(1/2 + i\nu) - \psi(1/2 - i\nu)$$

ψ is the Digamma function

Green function

$$f_{BFKL}(\omega,k_1,k_2) = \int_{-\infty}^{\infty} d\nu \left(\frac{k_1^2}{k_2^2}\right)^{i\nu} \frac{1}{2\pi^2 k_1 k_2}\frac{1}{(\omega-\bar{\alpha}_s\chi(\nu))}$$

NLO BFKL with running α_s

NLO

$$\omega \equiv \chi(\alpha_s,\nu) = \bar{\alpha}_s(1-A\bar{\alpha}_s)\,\chi_0\left(\frac{1}{2}+\bar{\alpha}_s B + i\nu + \frac{\omega}{2}\right) + \bar{\alpha}_s^2\chi_1(\nu).$$

Fadin, Lipatov
G. Salam
resummation

running coupling

$$\omega = \chi\left(\alpha_s(k), \nu_\omega(k)\right).$$

$$\omega = \chi(\alpha_s(k_{\rm crit}), 0).$$

property of χ:
largest ω at $\nu=0$

Airy functions are solving BFKL eq. around $k \sim k_{crit}$

$$\left[\frac{d^2}{d\ln(k^2/k_0^2)} + \frac{\beta_0}{2\pi}\frac{\dot{\chi}(\alpha_s(k_{\rm crit}),0)}{\chi''(\alpha_s(k_{\rm crit}),0)}\ln\left(\frac{k^2}{k_0^2}\right)\right]\overline{f_\omega}(k) = 0,$$

$$f_\omega(k^2) = \frac{\overline{f_\omega}(k)}{\sqrt{k^2}},$$

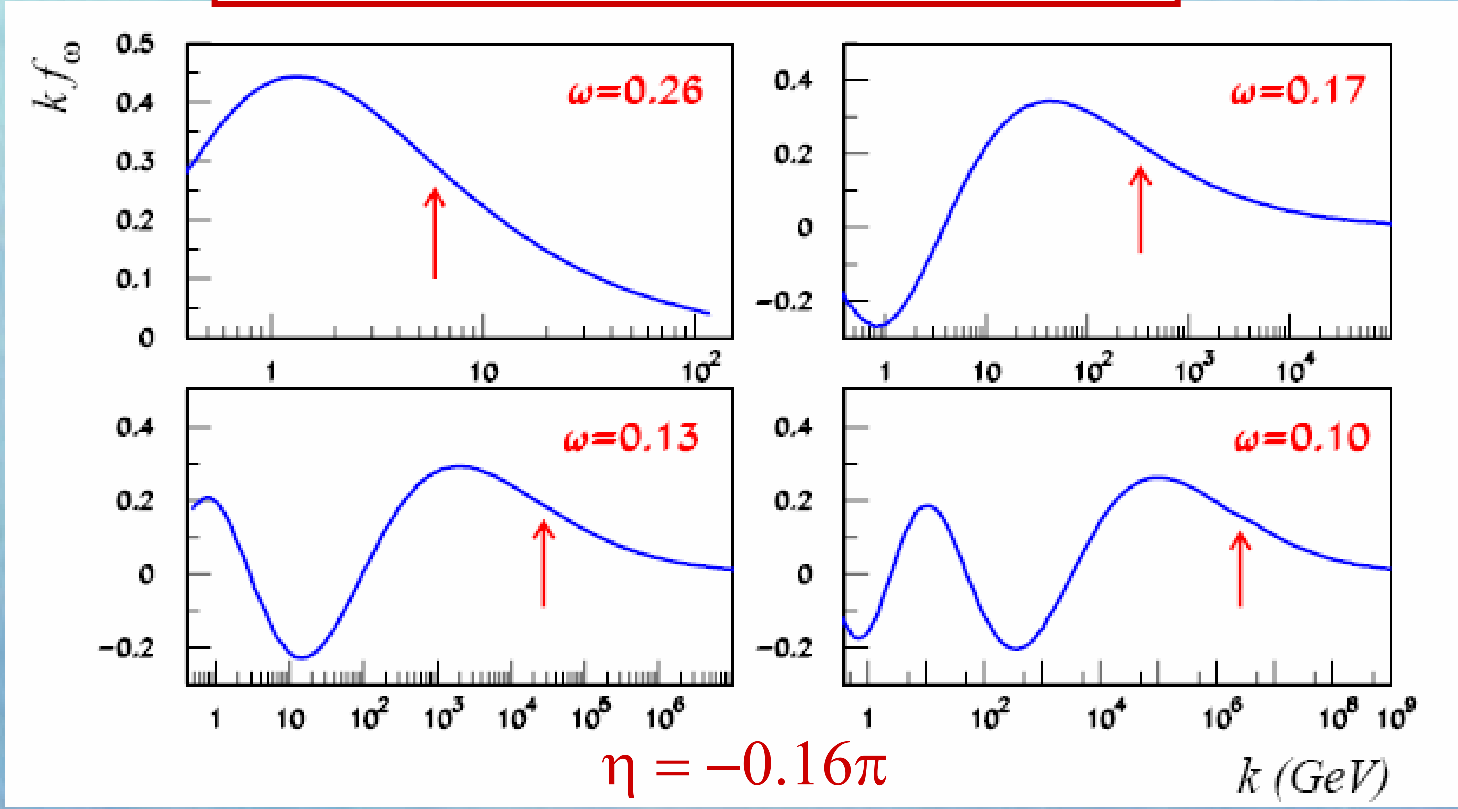
away of k_{crit}

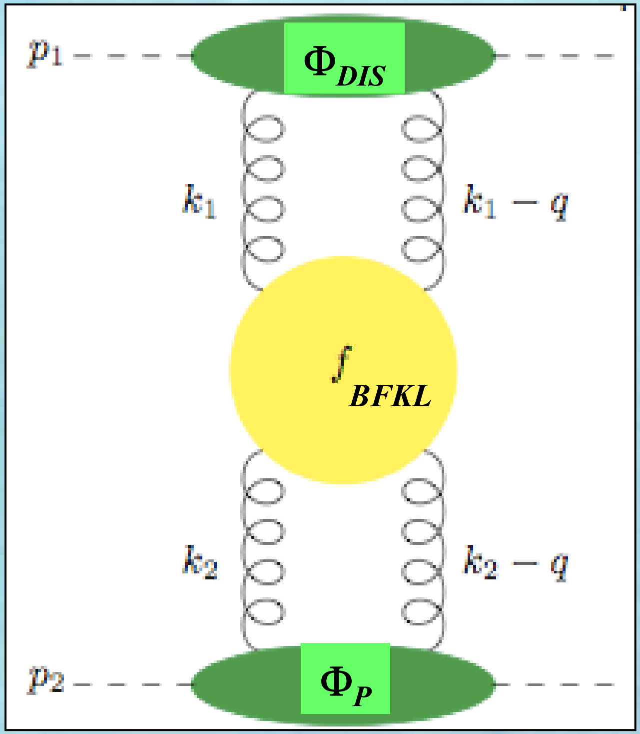
$$\boxed{\overline{f_\omega}(k) \;=\; e^{\pm i\varphi_\omega(k)},}$$

$$\varphi_\omega(k) \;=\; 2\int_k^{k_{\rm crit}} \frac{dk'}{k'}\,|\nu_\omega(k)|\,.$$

Matching the solutions at $k=k_{crit}$ determines the phase of oscil.= $\pi/4$
Lipatov 86 ➔ encode the infrared behaviour of QCD by assuming a fixed phase η at k_0

$$\boxed{\varphi_\omega(k_0) \;\equiv\; 2\int_{k_0}^{k_{\rm crit}} \frac{dk'}{k'}\,|\nu_\omega(k)| \;=\; \left(n-\frac{1}{4}\right)\pi+\eta,}$$





Structure functions in DIS

$$F_2(x, Q^2) = \int_x^1 dz \int \frac{dk}{k} \Phi_{\mathrm{DIS}}(z, Q, k) xg\left(\frac{x}{z}, k\right),$$

unintegrated gluon density

$$xg(x,k) = \sum_n \int \frac{dk'}{k'} \Phi_p(k') \left(\frac{k'x}{k}\right)^{-\omega_n} k^2 f^*_{\omega_n}(k') f_{\omega_n}(k),$$

enhancement of leading eigenfun.by $(1/x)^{\omega}$

$$xg(x,k) = \sum_n a_n x^{-\omega_n} k^{(2+\omega_n)} f_{\omega_n}(k).$$

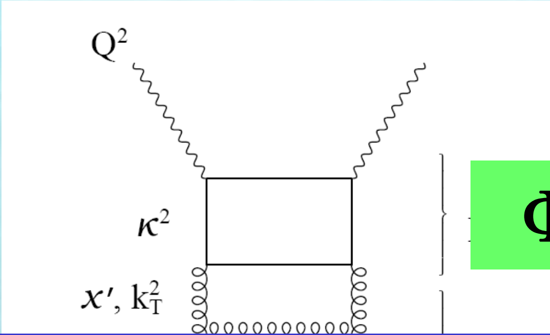
HERA
LHeC

no enhancement of leading eigenfun.

$$\Phi_p(k) = \sum_n a_n k^{(2-\omega_n)} f_{\omega_n}(k),$$

Φ_{DIS} known in QCD

Φ_P barely known



Φ_{DIS}

Kwiecinski, Martin Stasto

$$S_q(x,Q^2) = \frac{Q^2}{4\pi^2}\int\frac{dk^2}{k^4}\int_0^1 d\beta\int d^2\kappa'\alpha_S\left\{[\beta^2+(1-\beta)^2]\left(\frac{\boldsymbol{\kappa}}{D_{1q}}-\frac{\boldsymbol{\kappa}-\boldsymbol{k}}{D_{2q}}\right)^2\right.$$

$$\left. + \ [m_q^2+4Q^2\beta^2(1-\beta)^2]\left(\frac{1}{D_{1q}}-\frac{1}{D_{2q}}\right)^2\right\} f\left(\frac{x}{z},k^2\right)\Theta\left(1-\frac{x}{z}\right)$$

$\kappa' = \kappa - (1-\beta)k$ and

$$D_{1q} = \kappa^2 + \beta(1-\beta)Q^2 + m_q^2$$

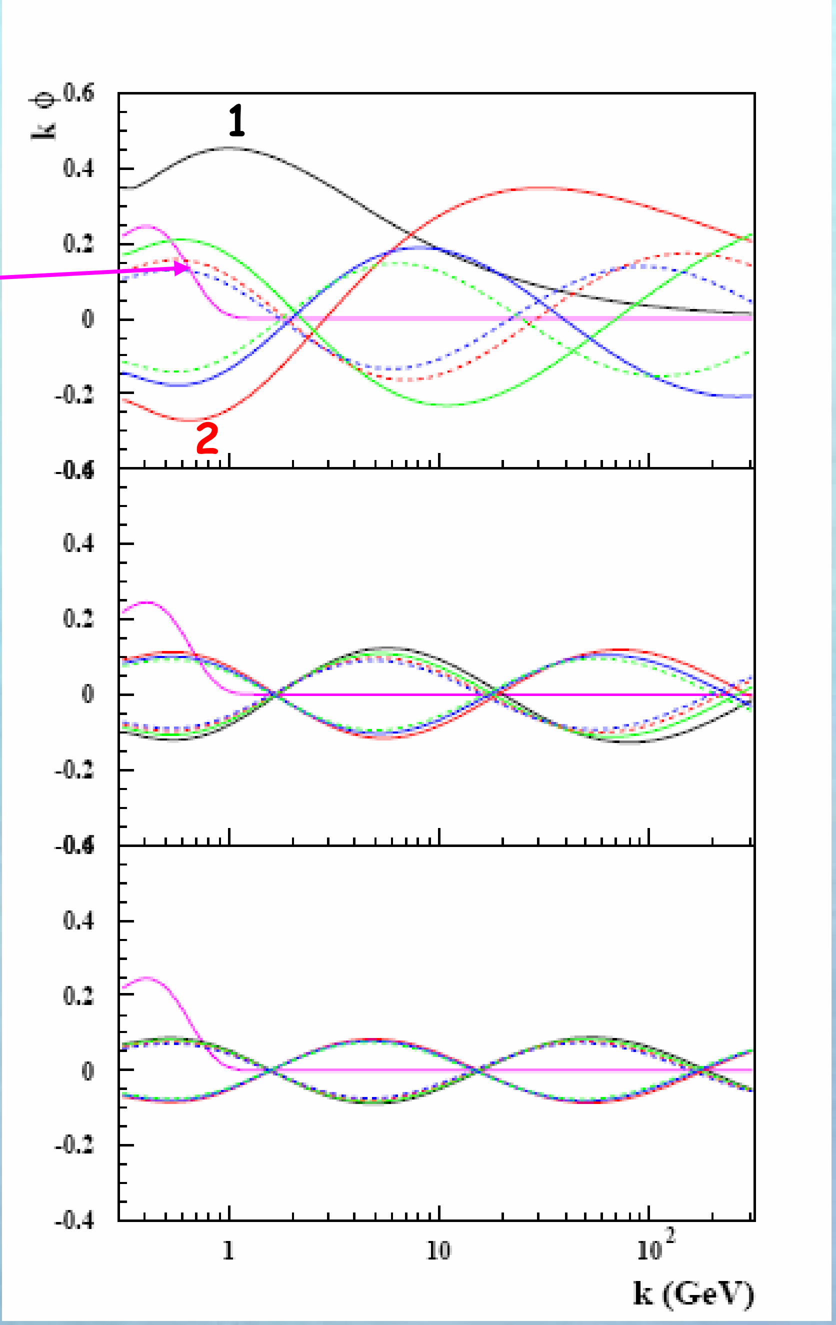
$$D_{2q} = (\boldsymbol{\kappa}-\boldsymbol{k})^2 + \beta(1-\beta)Q^2 + m_q^2$$

$$z = \left[1 + \frac{\kappa'^2+m_q^2}{\beta(1-\beta)Q^2} + \frac{k^2}{Q^2}\right]^{-1}.$$

$$F_2 = \sum_q e_q^2(S_q+V_q),$$

DAF Pomeron fit with

$\Phi_p = k^2 \exp(-bk^2)$



Eigenfunctions

1-7

8-14

15-21

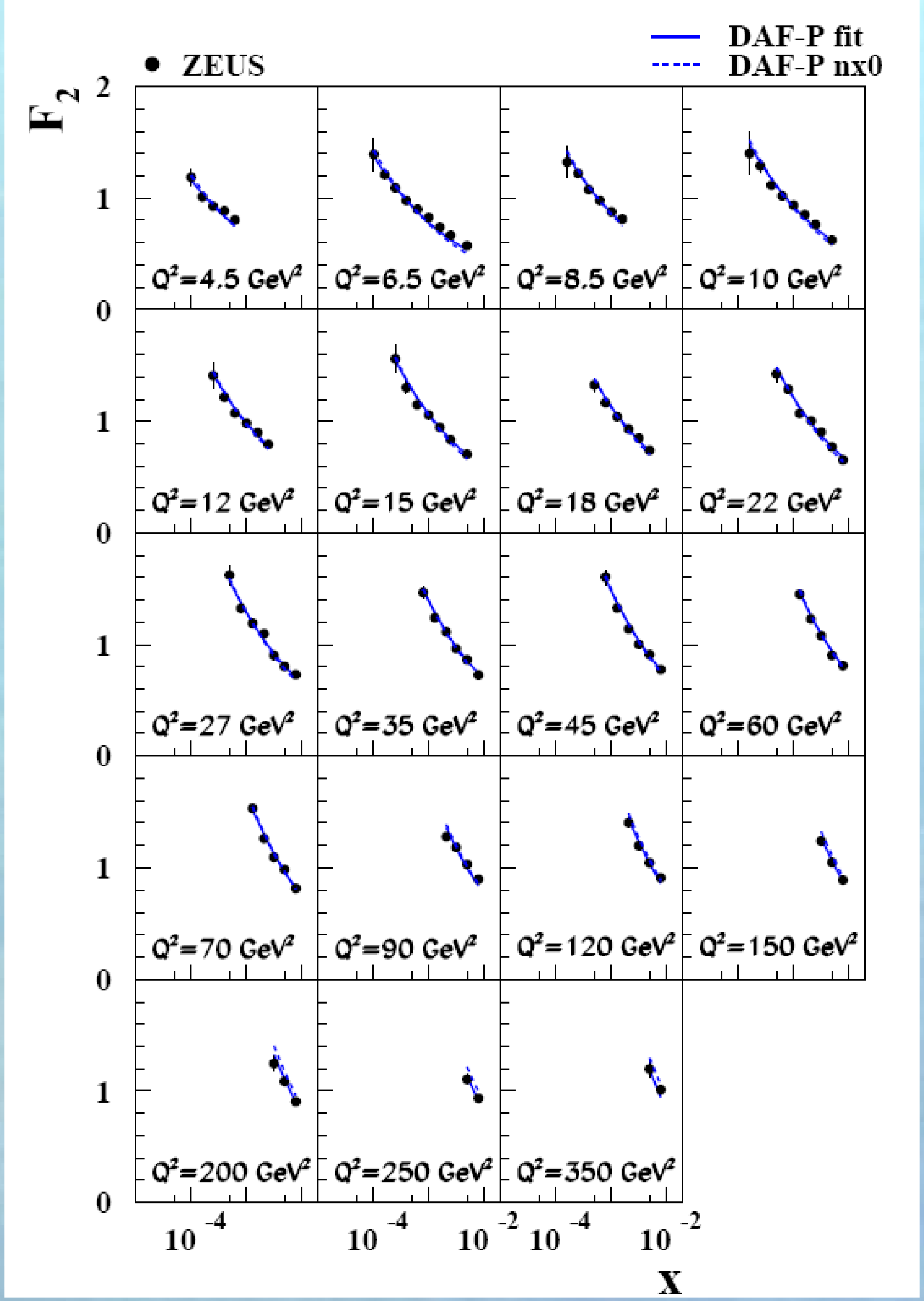
DAF Pomeron fit with

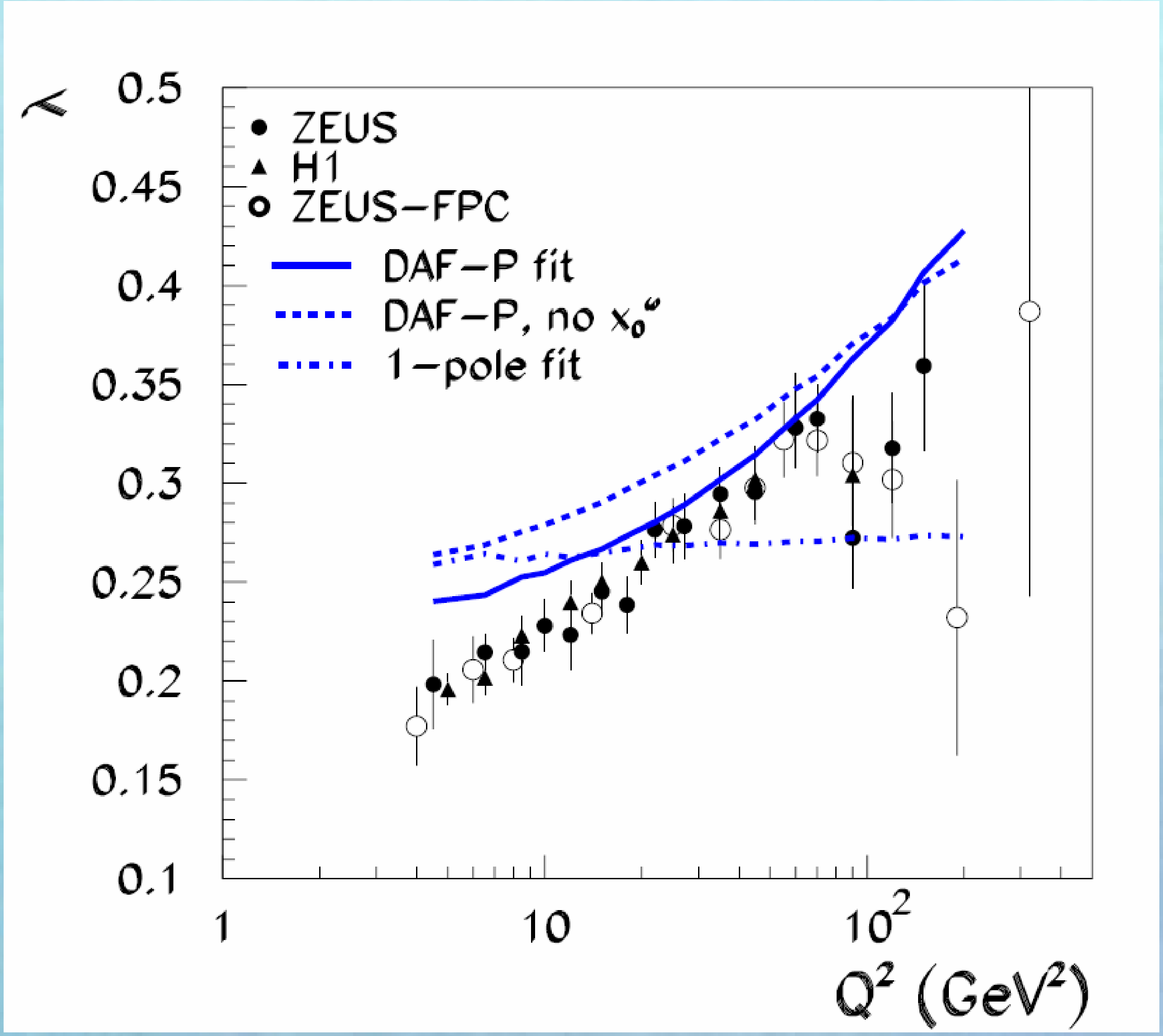
$$\Phi_p = k^2 \exp(-bk^2)*(x_0)^{\omega}$$

$\eta = -0.20*\pi$
$b = 6\ \mathrm{GeV}^{-2}$
$x_0 \sim 0.4$

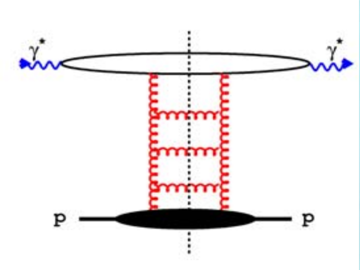
for $x < 0.001$
$\chi^2/\mathrm{ndf} = 18/30$

for $x < 0.01$
$\chi^2/\mathrm{ndf} = 115/100$

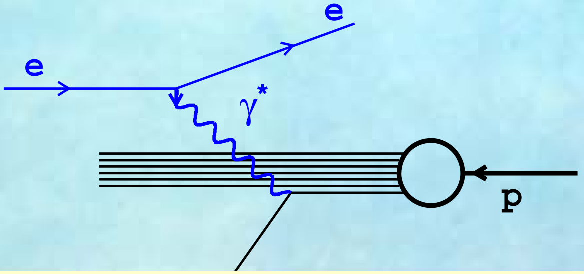




Sum of contributions with small eigenvalues can give a larger rate of rise than the leading eigenvalue !!!

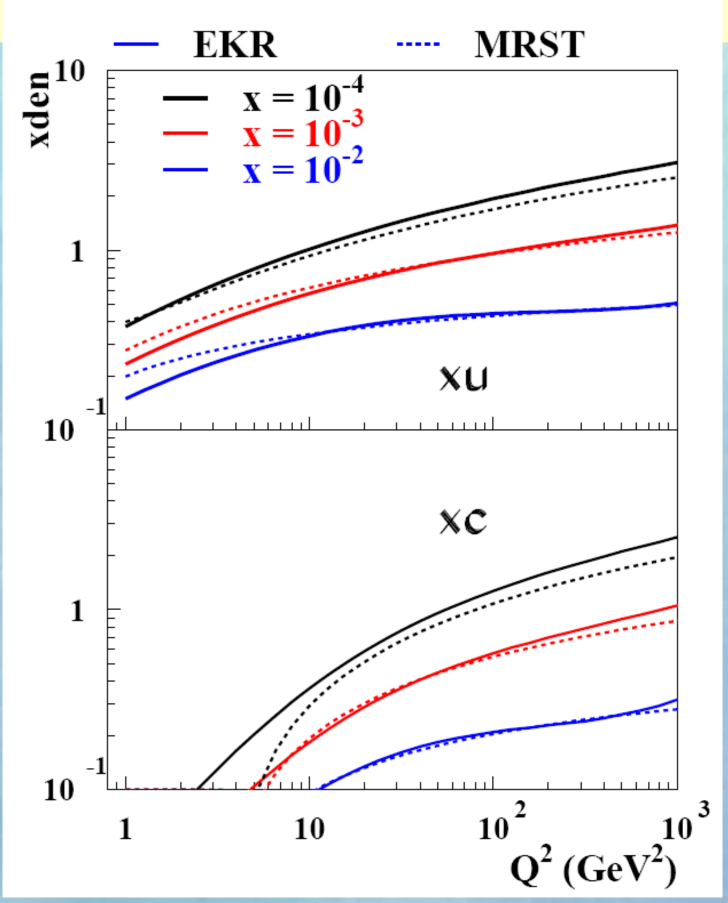


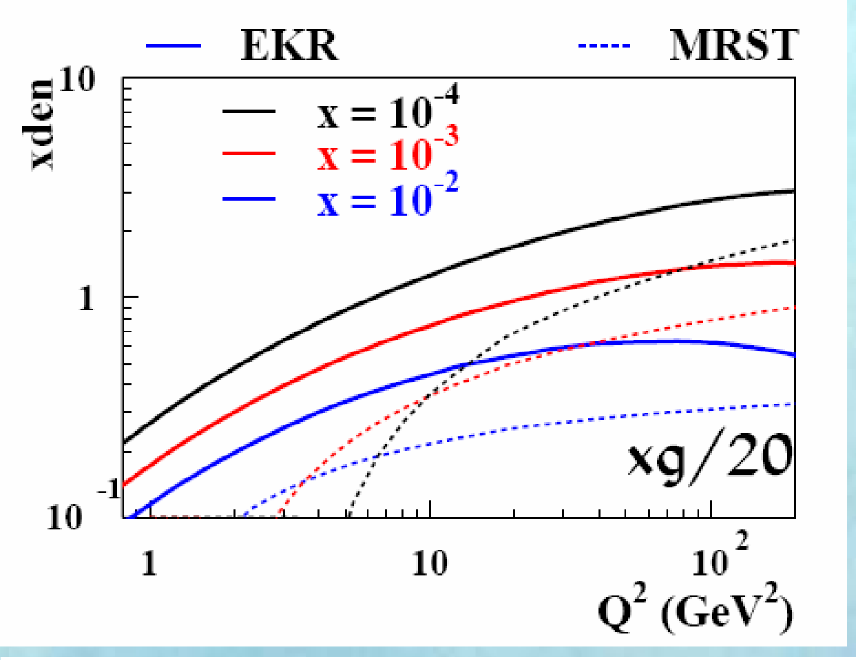
$$F_2(x,Q^2) = x\sum_q e_q^2 q(x,Q^2)$$



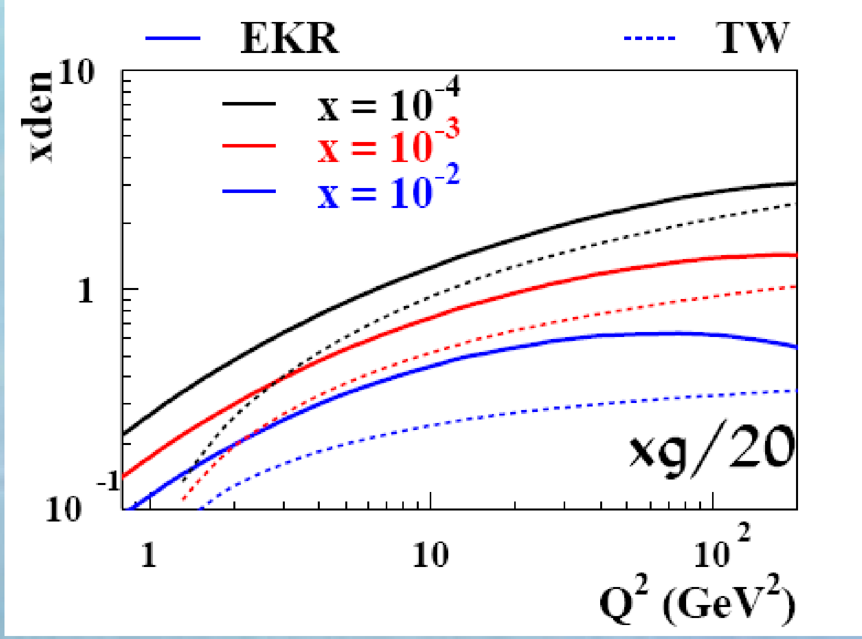
$$q(x,Q) = \int_0^Q \frac{dk}{k}\Phi_{DIS}(Q,k)\,xg(x,k)$$

$$q(x,\mu^2) = q_0(x) + \frac{\alpha_s}{\pi}\int_x^1 \frac{d\xi}{\xi} q_0(\xi)\left\{P_{qq}\left(\frac{x}{\xi}\right)\ln\mu/\kappa + \ldots\right.$$





EKR
MRST
xden
x = 10^-4
x = 10^-3
x = 10^-2
xg/20
10
1
10^-1
1
10
10^2
Q^2 (GeV^2)



EKR
TW
xden
x = 10^-4
x = 10^-3
x = 10^-2
xg/20
10
1
10^-1
1
10
10^2
Q^2 (GeV^2)

Where Do BFKL and DGLAP Meet

Lipatov, private communication

Unintegrated BFKL gluon density (LO, no running α_s)

$$xg(x,k^2) = \int d\gamma \Phi_p(\gamma) \left(\frac{k^2}{\mu^2}\right)^\gamma x^{-\bar{\alpha_s}\chi(\gamma)} = \int d\gamma \Phi_p(\gamma) \exp(F(\gamma))$$

$\gamma = ½ + i\nu$

Saddle point

$$(F(\gamma))' = (\gamma \ln(k^2/\mu^2) + \bar{\alpha_s} \ln(1/x)\chi(\gamma))' = 0$$

$$\chi(\gamma) \;=\; \frac{1}{\gamma} - 2\zeta(3)\gamma^2 + \cdots \quad \Longrightarrow \quad \gamma^2 \;=\; \frac{\bar{\alpha}\ln(1/x)}{\ln(k^2/\mu^2)}$$

$$\omega \approx \bar{\alpha_s}/\gamma = \sqrt{\frac{\bar{\alpha_s}\ln(k^2/\mu^2)}{\ln(1/x)}}$$

valid if $\bar{\alpha}(k^2)\ln(1/x) \;\ll\; 1,$

! not fulfilled for HERA or even Higgs at LHC !

equal to DLL limit of DGLAP (LO, no running α_s)

Pomeron and Gauge/String Duality

Brower, Polchinski, Strassler, and Tan, hep-th/0603115

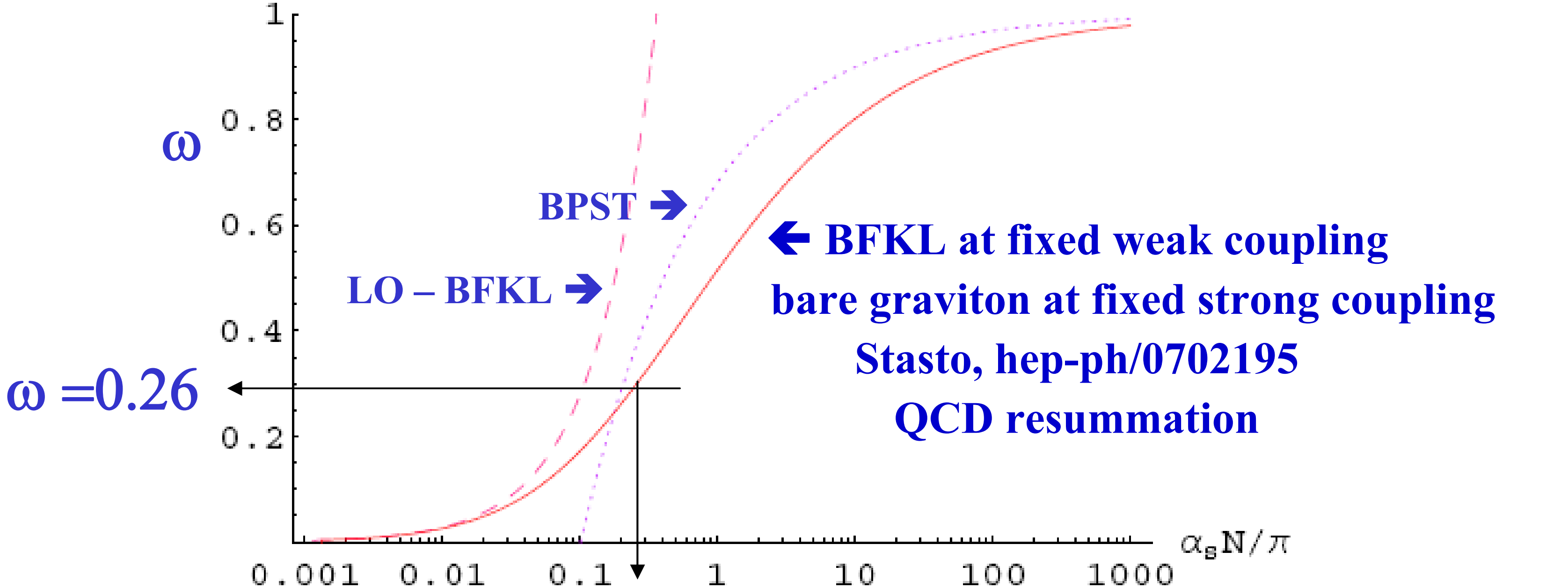
Pomeron is a coherent color-singlet object, build from gluons, with universal properties; it is a closed string propagating in ADS space, when the conformal symmetry is broken at some infrared point in the fifth dimension

$$1+\omega = 2 - \frac{2}{\sqrt{4\pi\alpha_s N}}$$

in ADS/CFT

in N=4 YM SuSy QCD

Kotikov, Lipatov, Onishchenko, Velizhanin, Phys. Lett. B 632, 754 (2006)

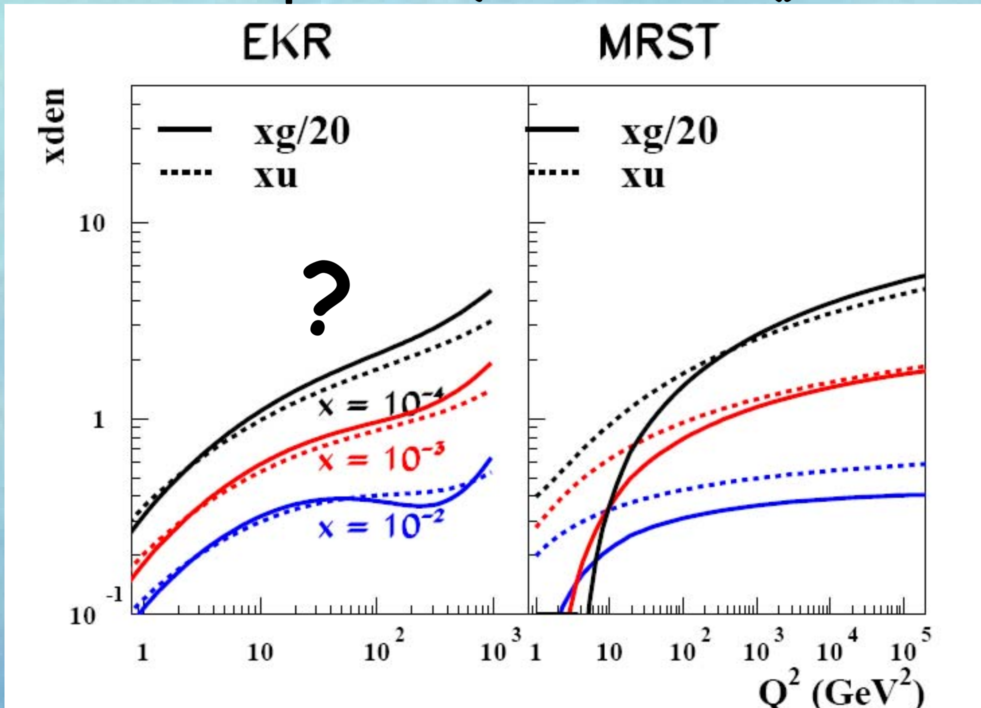


Consequences for LHC

Good knowledge of gluon density around $x \sim 10^{-2}$ and $Q^2 \sim 10000$ GeV^2 is essential for LHC physics (Higgs region)

Large effort is going into precise measurement of W and Z inclusive X-sections ➔ precise determination of sea-quark distributions
➔ precise gluon density

Is the sea-quark ←➔ gluon density relation the same in the DGLAP-like picture (MRST/CTEQ) and DAF-Pomeron?



sea-quark←➔ gluon relation can be checked by the jets with p_T around 50 GeV

Instead of Conclusions

Study of Gluon Density are very important because it is the analog of Black Body Radiation in QED

It seemed hopeless to study pure Gluon Radiation since it is never free. However, it is becoming free for a short moment in HEP reactions

HERA has shown that physics processes at low-x are completely dominated by pure Gluon Density,

Investigation of Gluon Density has a chance to become as fundamental as Black Body radiation