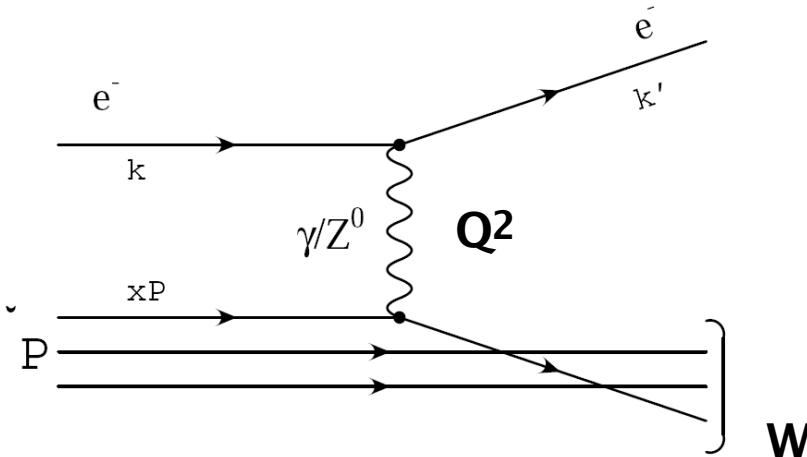




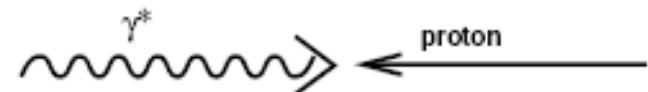
# Energy dependence of the charged multiplicity and scaled momenta in DIS

On behalf of the ZEUS Collaboration

Teresa Tymieniecka  
University of Warsaw, Poland

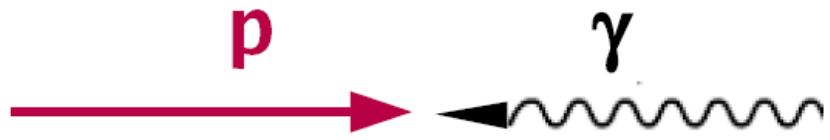


- Energy of  $\sim 300$  GeV in ep CMS
- Neutral current (NC)



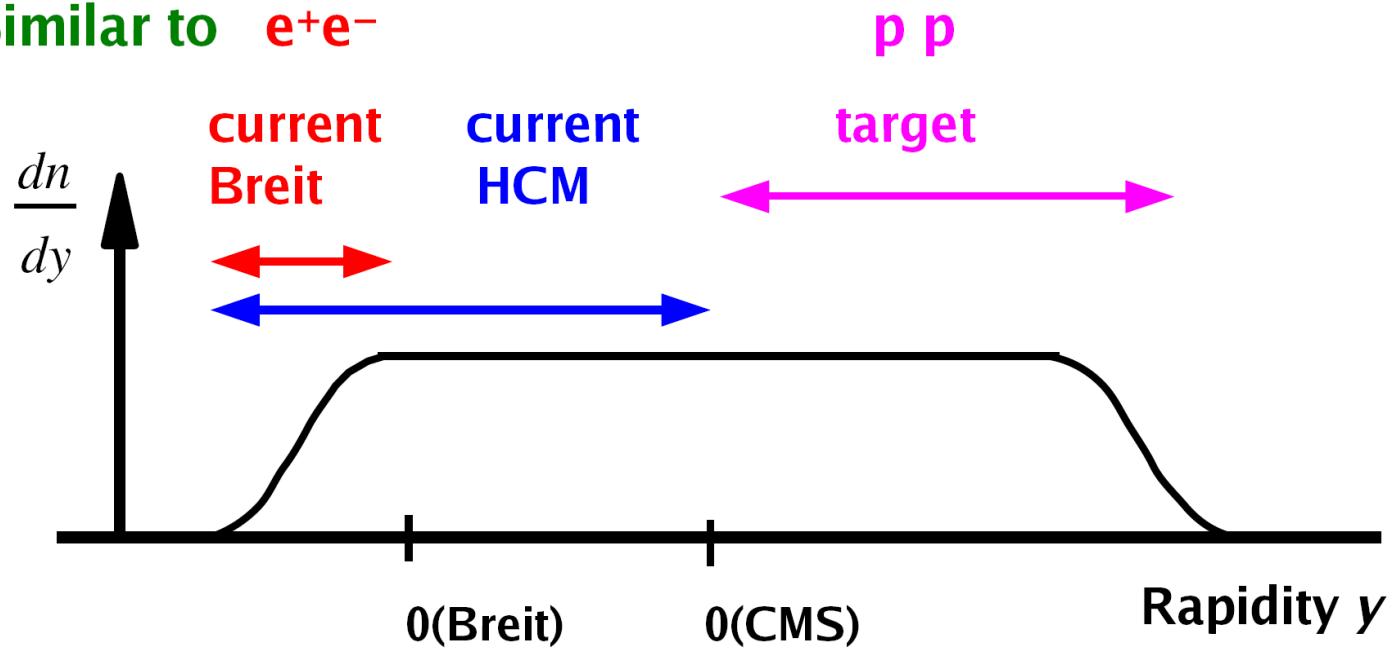
## Outline

- Motivation
- KNO scaling
- Scaled momenta compared with  $e^+e^-$  data



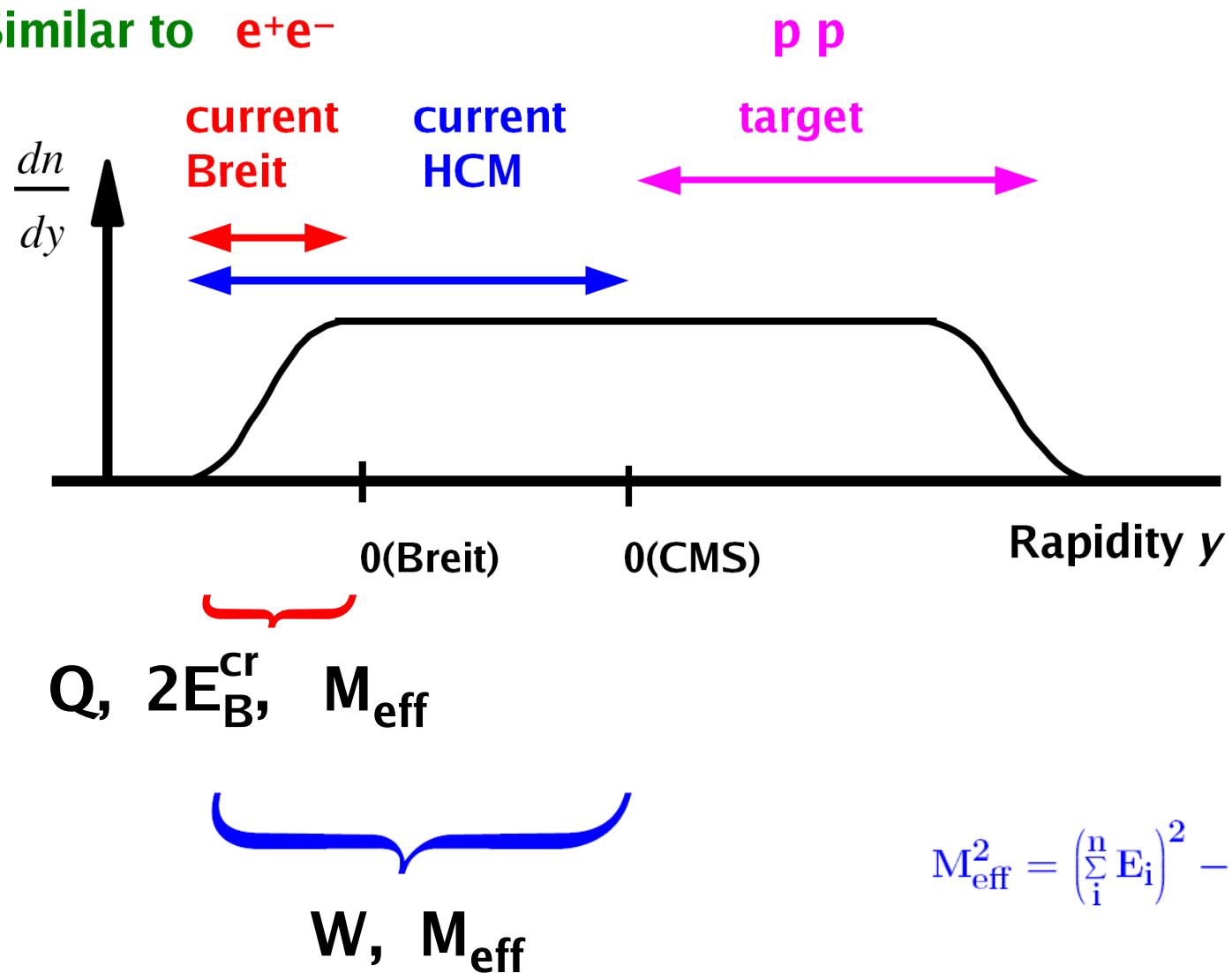
**Rapidity of particles defines their expected features,**

Similar to  $e^+e^-$





Similar to  $e^+e^-$



$$M_{\text{eff}}^2 = \left( \sum_i^n E_i \right)^2 - \left( \sum_i^n P_{Xi} \right)^2 - \left( \sum_i^n P_{Yi} \right)^2 - \left( \sum_i^n P_{Zi} \right)^2$$

# Data and motivation

Luminosity  $38.6 \text{ pb}^{-1}$  collected in 1996-7  
with  $E_{\text{proton}} = 820 \text{ GeV}$  and  $E_{e^+} = 27.5 \text{ GeV}$

NC DIS events with  $Q^2 > 25 \text{ GeV}^2$   
 $70 < W < 225 \text{ GeV}$

Comparison with  $e^+ e^-$  in previous studies in Breit frame :

- a reasonable agreement at  $Q > 8 \text{ GeV}$
- no agreement at  $Q < 8 \text{ GeV}$   
explained by the asymmetric nature of  $\gamma^* p$

Alternative energy scales to Q:

- the invariant mass of hadronic system  $M_{\text{eff}}^{\text{Breit}}$  and  $M_{\text{eff}}^{\text{HCM}}$
- the available energy in the current region  
of Breit frame  $E_B^{\text{cr}}$  or of HCM  $E_{\text{HCM}}^{\text{cr}} \approx W/2$

Published DESY-08-036

# Predictions

## Monte Carlo models

- ARIADNE 4.12** — colour dipole model
- LEPTO MEPS** — matrix element + parton shower
- fragmentation** — the Lund string model
- HERWIG** — cluster hadronisation model

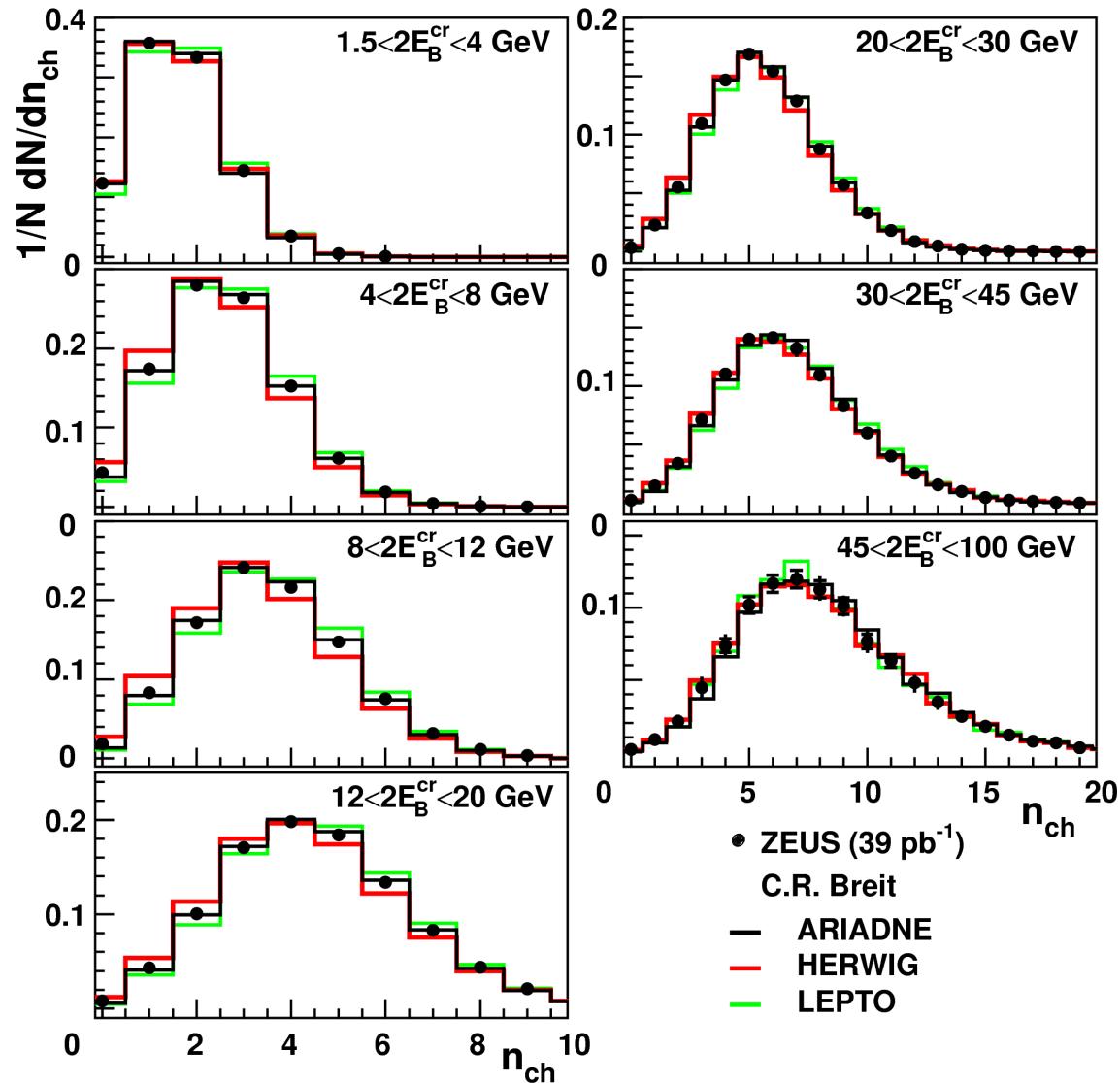
**Hadrons taken with lifetime >  $3 \cdot 10^{-10}$  s**

**Next step:**

**comparison with data for different scales**

# Multiplicity in 2 $E_B^{cr}$ bins in the Breit frame

ZEUS

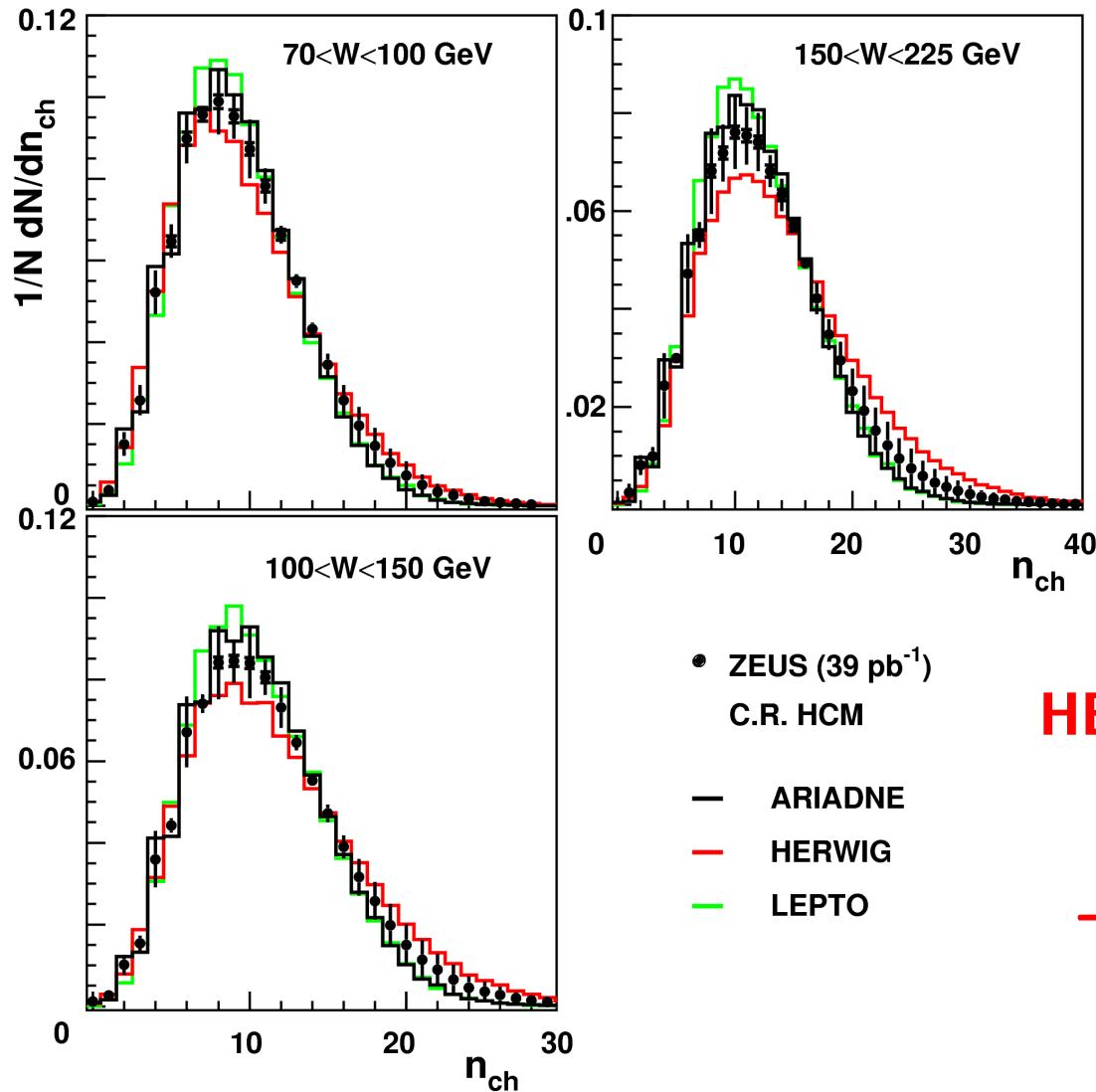


$E_B^{cr}$  — the available energy  
in the current region  
of Breit frame

All the MC models  
→ good descriptions  
but ARIADNE is the best

# Multiplicity in W bins in the HCM frame

ZEUS

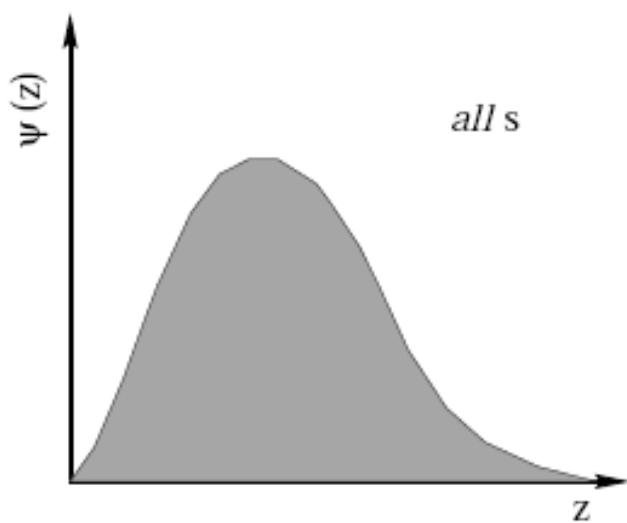
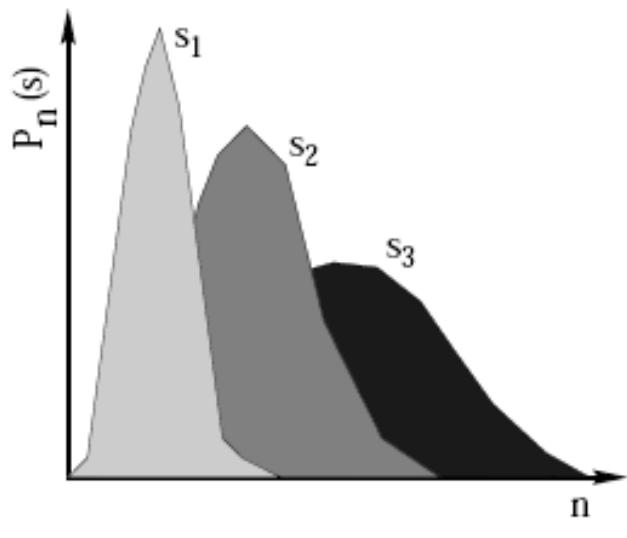


$W$  — total energy in  
 $\gamma^* p$  centre of mass

- ZEUS ( $39 \text{ pb}^{-1}$ )  
C.R. HCM
- ARIADNE
- HERWIG
- LEPTO

**HERWIG** — longer tails  
for multiplicities  
→ increase of sys. uncertainties

# KNO scaling



Z.Koba,H.B.Nielson,P.Olsen  
N.P. B40(1972)317

$P(n_{ch})$  the probability distribution  
of multiplicity  $n_{ch}$

$\langle n_{ch} \rangle$  the average multiplicity

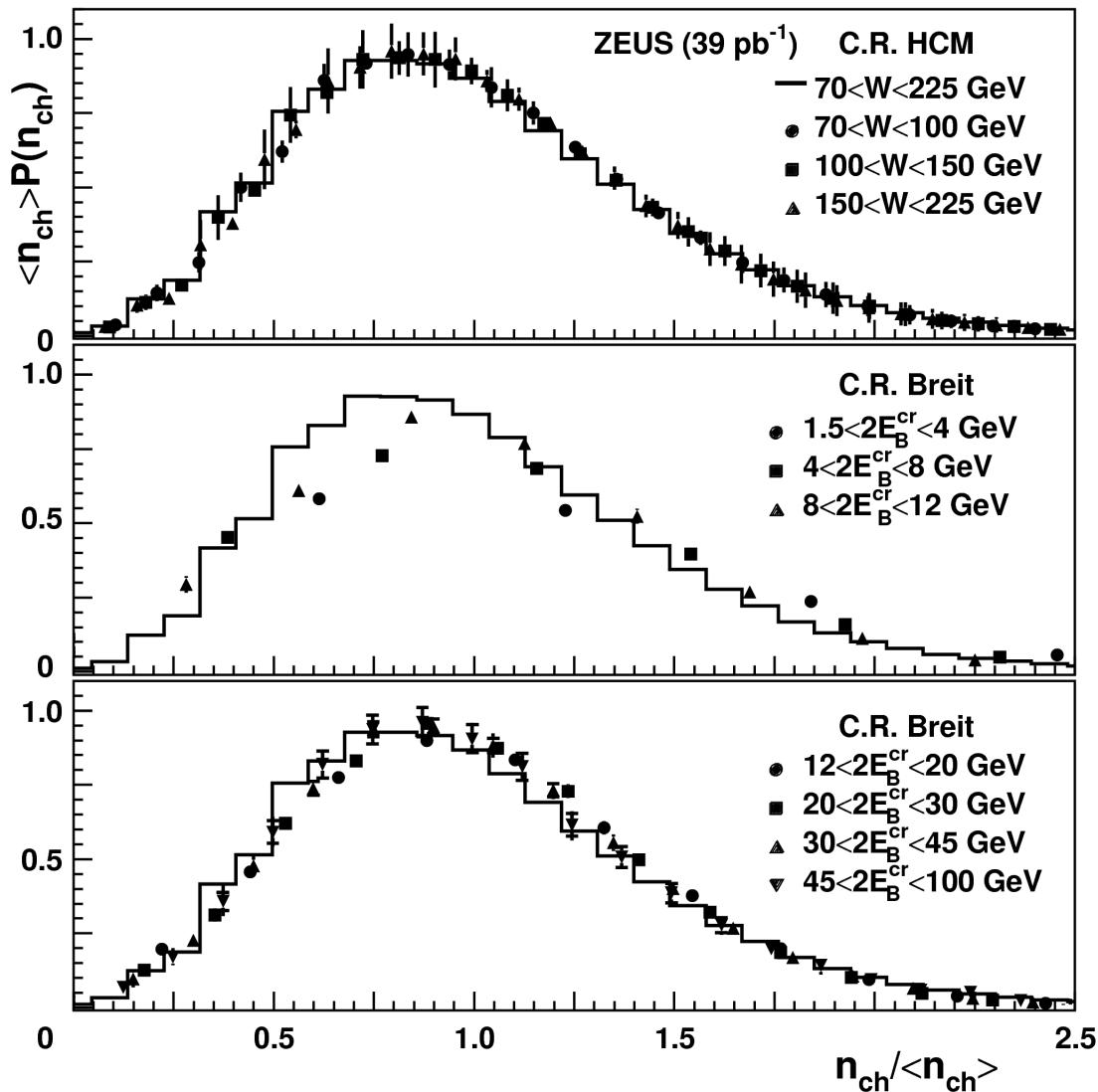
at high enough energies  $s$   
→ asymptotic behaviour

$$\langle n_{ch} \rangle P(n_{ch}) \sim n_{ch} / \langle n_{ch} \rangle$$

$$\begin{array}{ccc} \uparrow & & \uparrow \\ \psi(z) & & z \end{array}$$

# KNO scaling in W and $E_B^{cr}$ bins

ZEUS



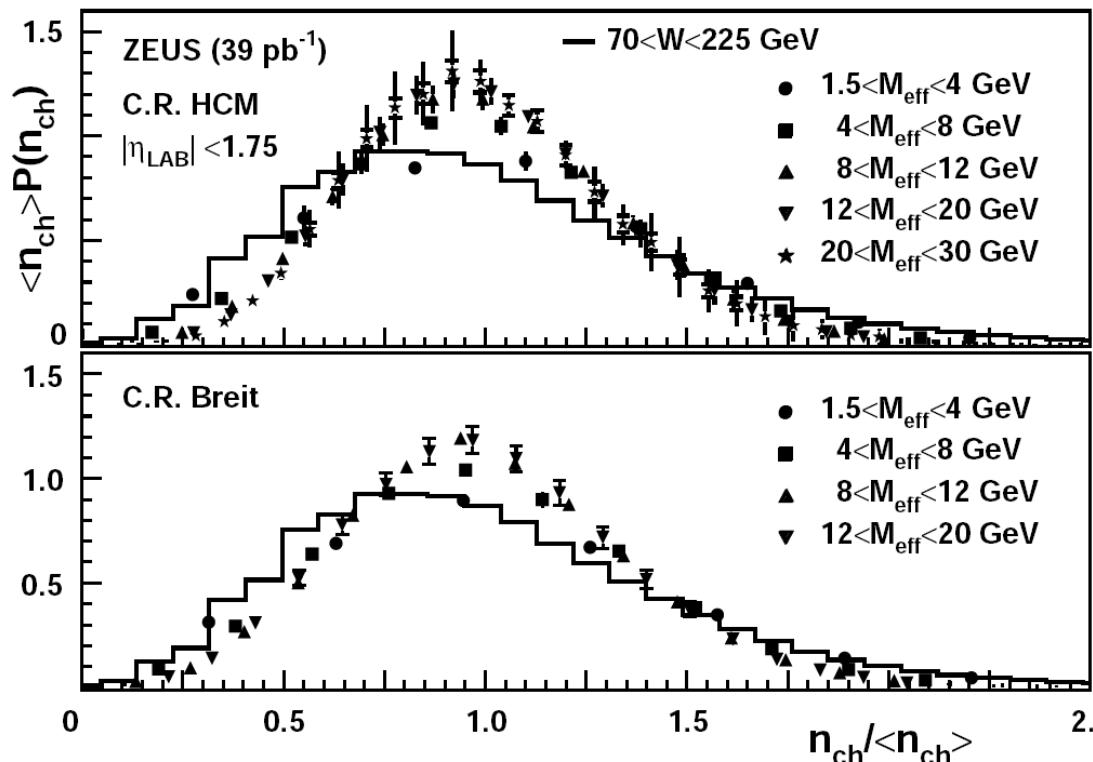
Product of  $P(n_{ch})$   $\langle n_{ch} \rangle$   
the multiplicity distribution  
and the average multiplicity

— reference distribution  
average distr.  $70 < W < 225$  GeV

bins	agreement
$2 E_B^{cr} < 12$ GeV	No
$2 E_B^{cr} > 12$ GeV	OK

# KNO scaling in $M_{\text{eff}}$ bins

ZEUS



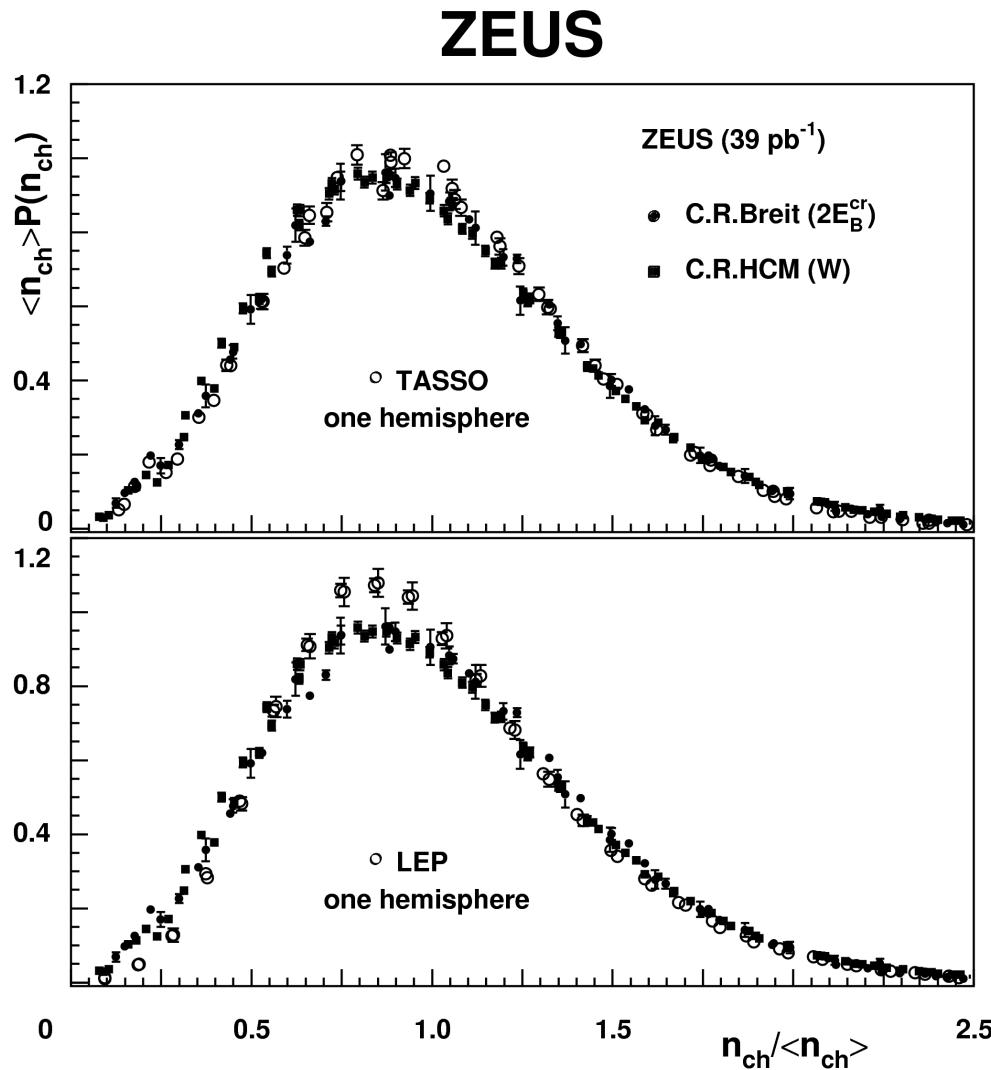
HCM frame

Breit frame

no agreement with  
the reference plot

Scaling behaviour observed for HCM and Breit  
except  $M_{\text{eff}} < 4 \text{ GeV}$

# KNO scaling (e<sup>+</sup>e<sup>-</sup> vs ep)



ep in bins

$2 E_B^{cr}$   
W

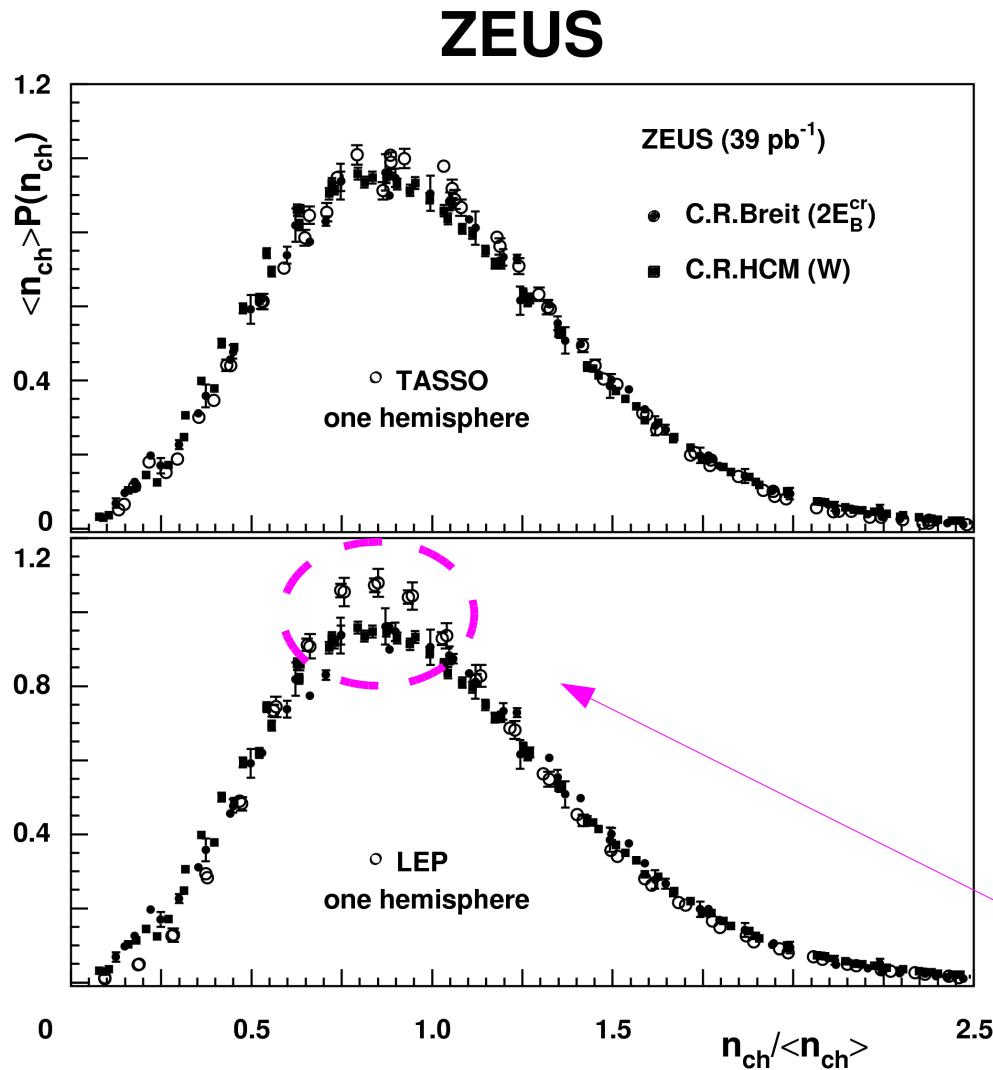
if  $2 E_B^{cr} > 12 \text{ GeV}$

e<sup>+</sup>e<sup>-</sup> data from **one hemisphere**  
LEP (DELPHI, OPAL) at  $Z^0$   
PETRA (TASSO)

acceptable agreement  
for PETRA and LEP

except LEP at peak

# KNO scaling (e<sup>+</sup>e<sup>-</sup> vs ep)



ep in bins

2 E<sub>B</sub><sup>cr</sup>  
W

if 2 E<sub>B</sub><sup>cr</sup> > 12 GeV

e<sup>+</sup>e<sup>-</sup> data from

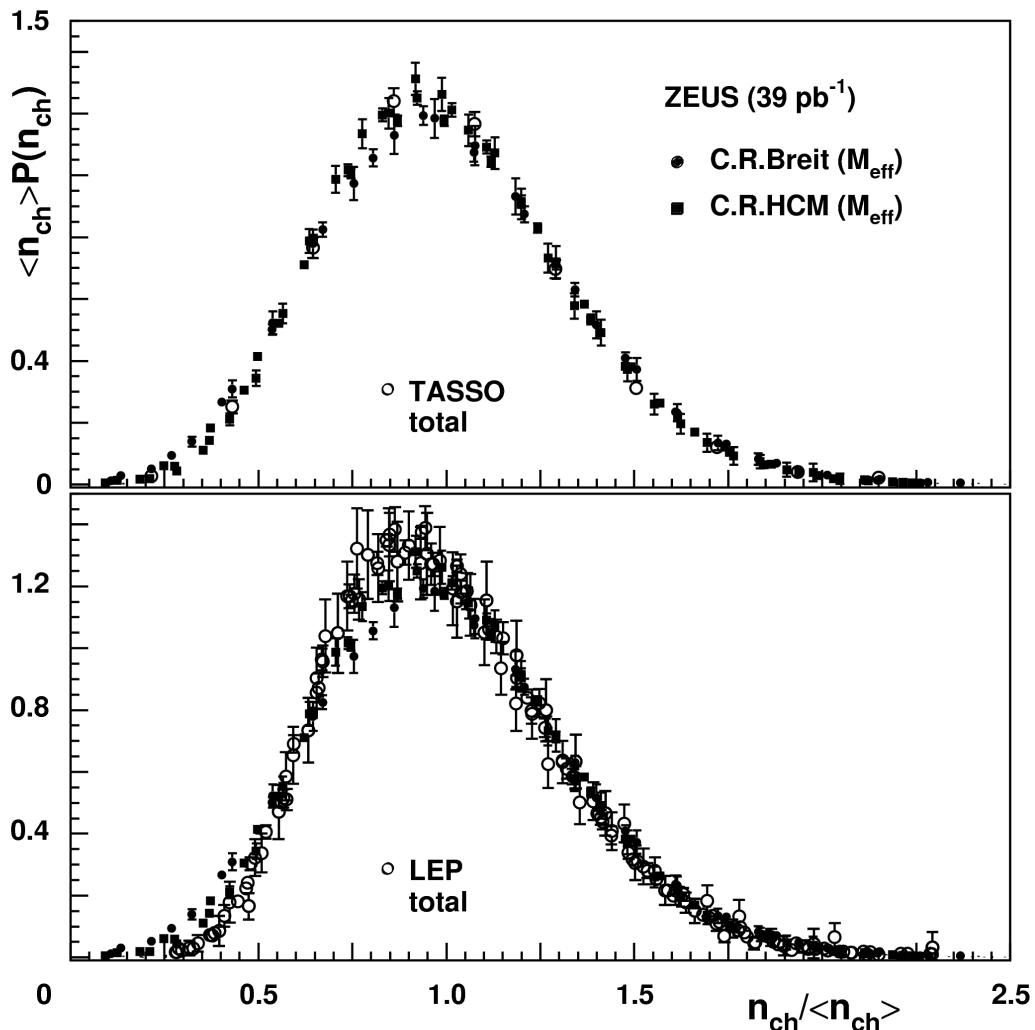
LEP (DELPHI, OPAL) at Z<sup>0</sup>  
PETRA (TASSO)

acceptable agreement  
for PETRA and LEP

except LEP at peak

# KNO scaling (e<sup>+</sup>e<sup>-</sup> vs ep in M<sub>eff</sub> bins)

ZEUS



ep with  $M_{eff} > 8$  GeV

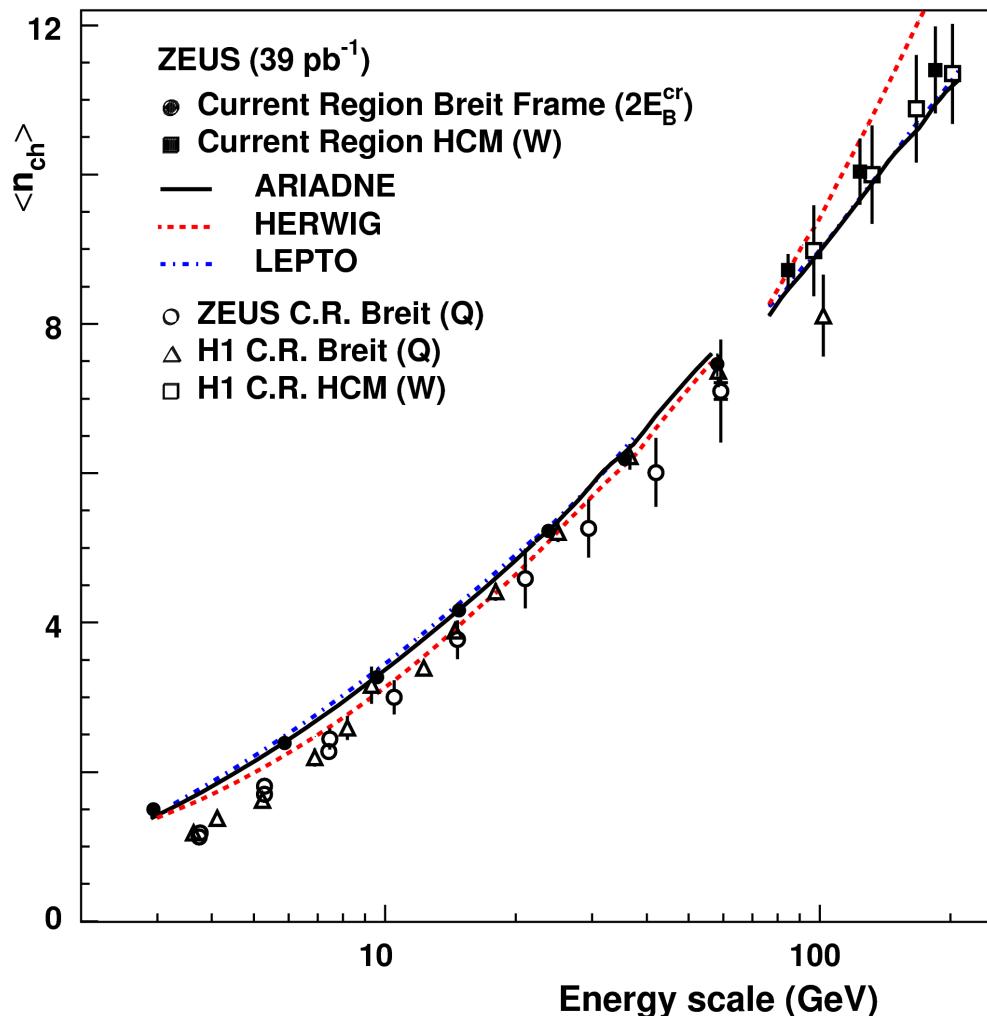
e<sup>+</sup>e<sup>-</sup> data for 2 hemispheres

- LEP  $91.2 < \sqrt{s} < 209$  GeV  
(DELPHI, OPAL, L3, ALEPH)
- PETRA (TASSO)

Good agreement

# Average multiplicity as $f(2\cdot E_B^{\text{cr}})$ and $f(W)$

ZEUS



Data are in good agreement  
with LEPTO and ARIADNE

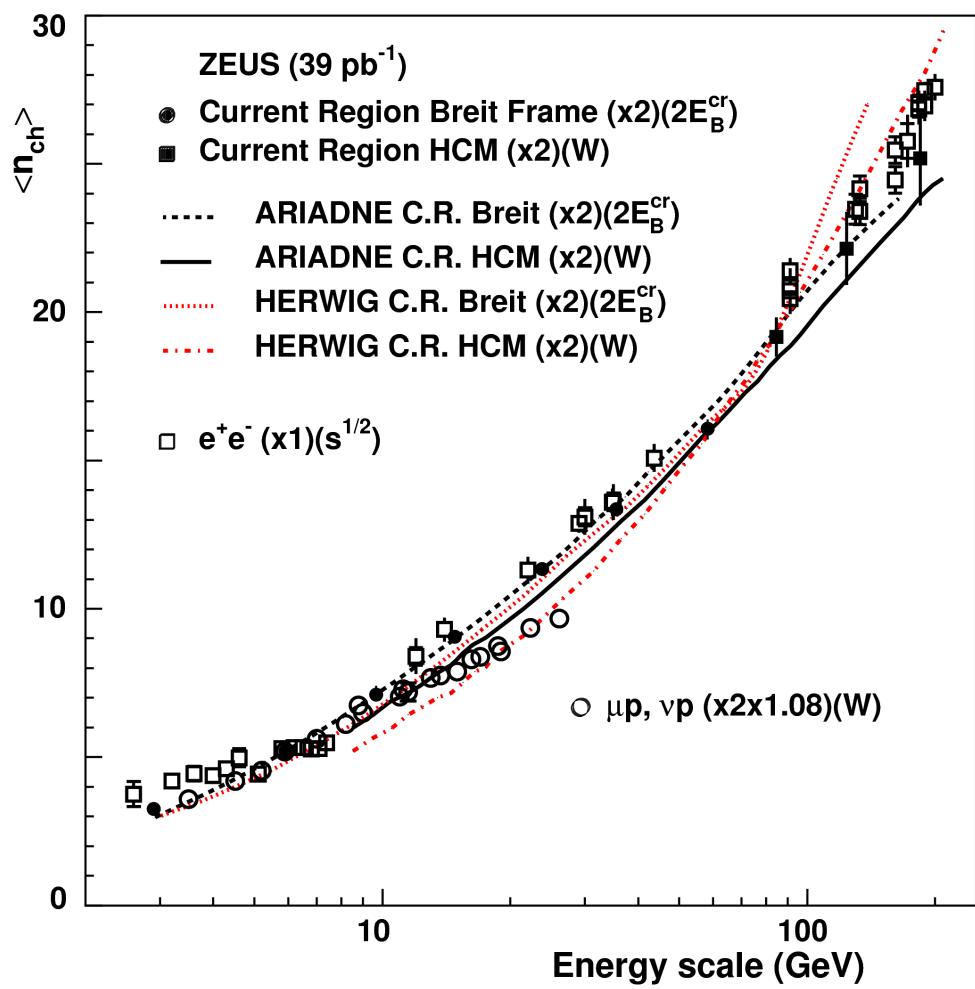
not with HERWIG

At low energy scales  
differences if  $2E_B^{\text{cr}}$  or  $Q$

At high scales  
good agreement

# Multiplicity ( $e^+e^-$ vs ep & fixed target)

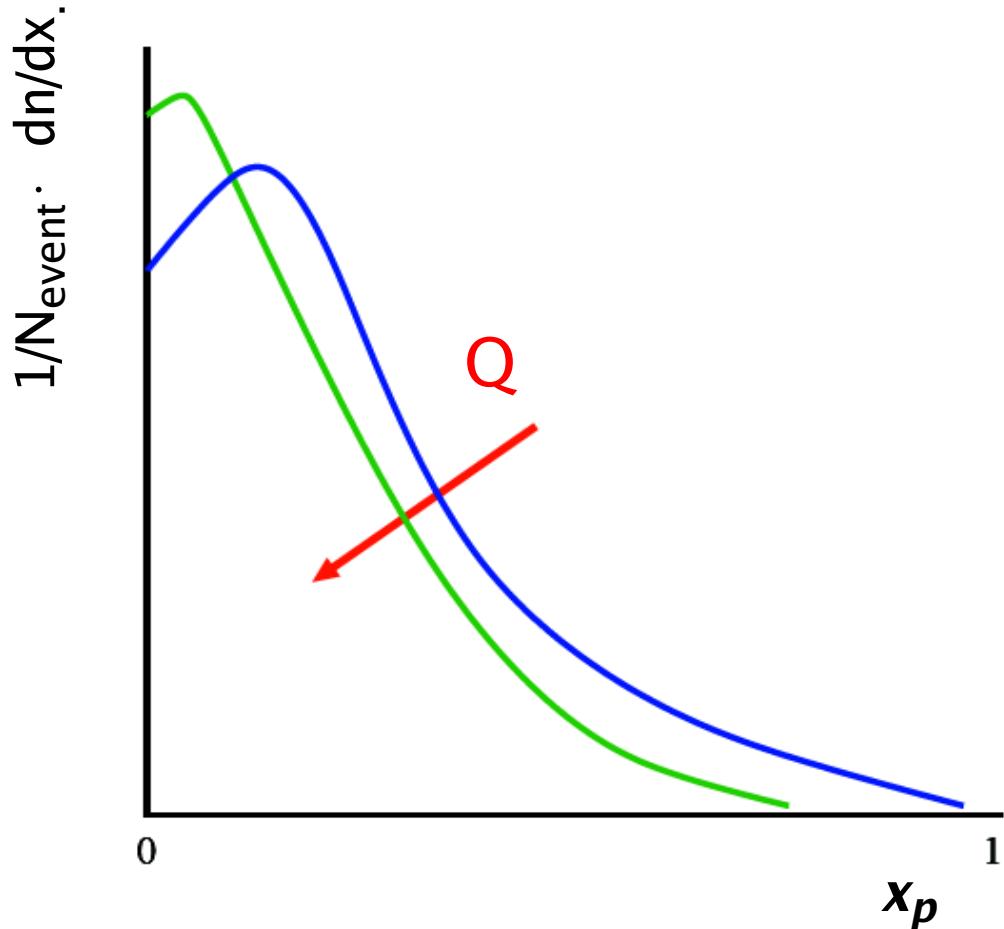
ZEUS



- At low scales  $E_B^{cr}$  gives better agreement with  $e^+e^-$  than Q
- Fixed target data deviate from the observed energy dependence above 15 GeV
- ARIADNE - the best description but data are systematically above predictions in HCM
- HERWIG deviates from data
- LEP data above ep data in HCM at scale >100 GeV

# Scaled momentum

$$x_p = \frac{(2 P_h)}{Q} = \frac{P_h}{E_{beam}}$$



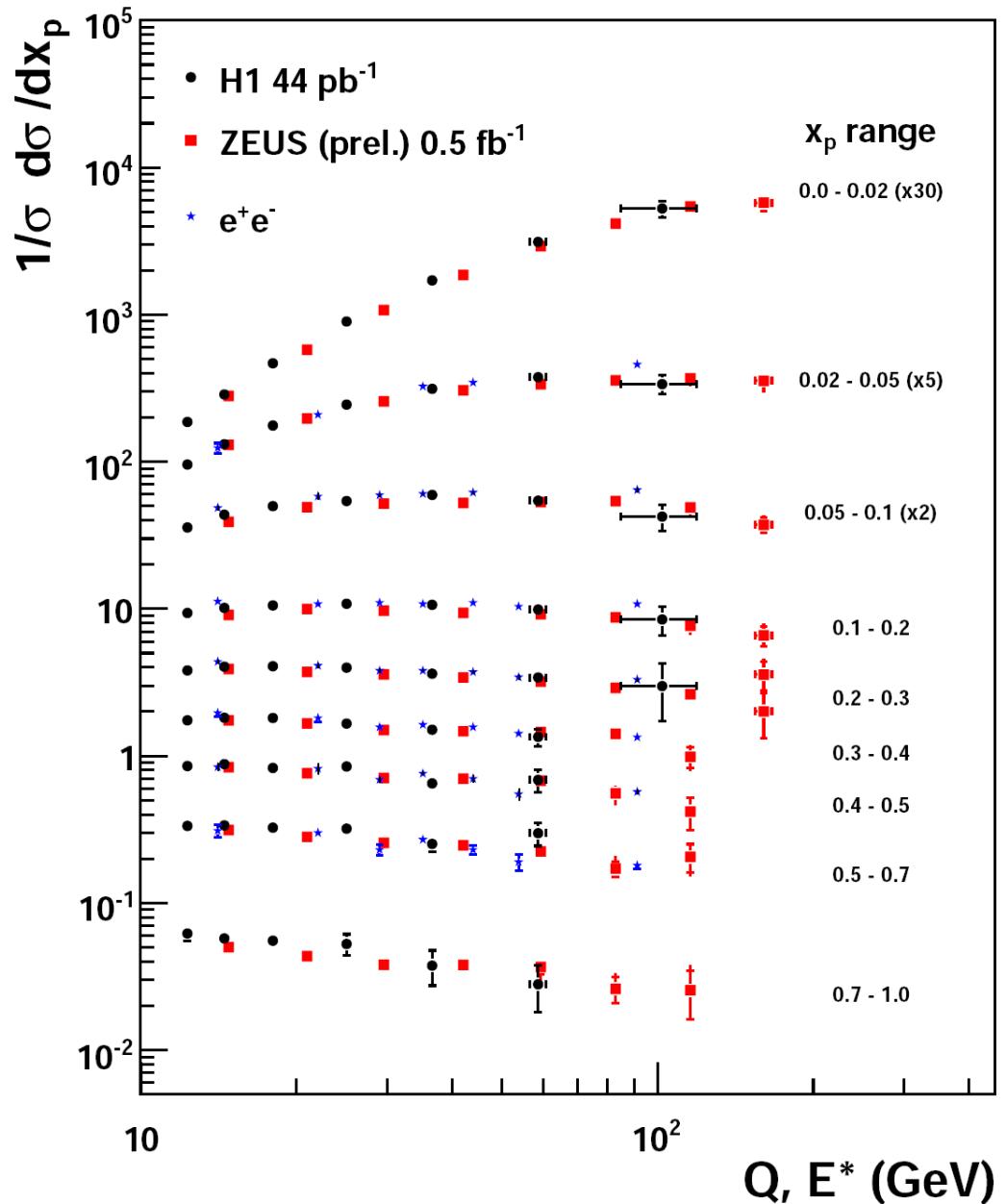
$P_h$  – momentum of charged particles in current region of the Breit frame.

With  $Q$  increasing  $dn/dx_p$  is softer,  
i.e. more particles with smaller fraction of energy  $Q/2$ .

## Comparison ep with $e^+e^-$

- supports the concept of quark fragmentation universality.
- scaling violation is observed

ZEUS data (prel),  $0.5 \text{ pb}^{-1}$ , 1996-2007  
 H1 data, Phys.Lett. B654(2007)148  
 $e^+e^-$  data from TASSO, MARK II, AMY,  
 DELPHI PL,B311(1993)408  
 $E^* = 2 E_{\text{beam}}$

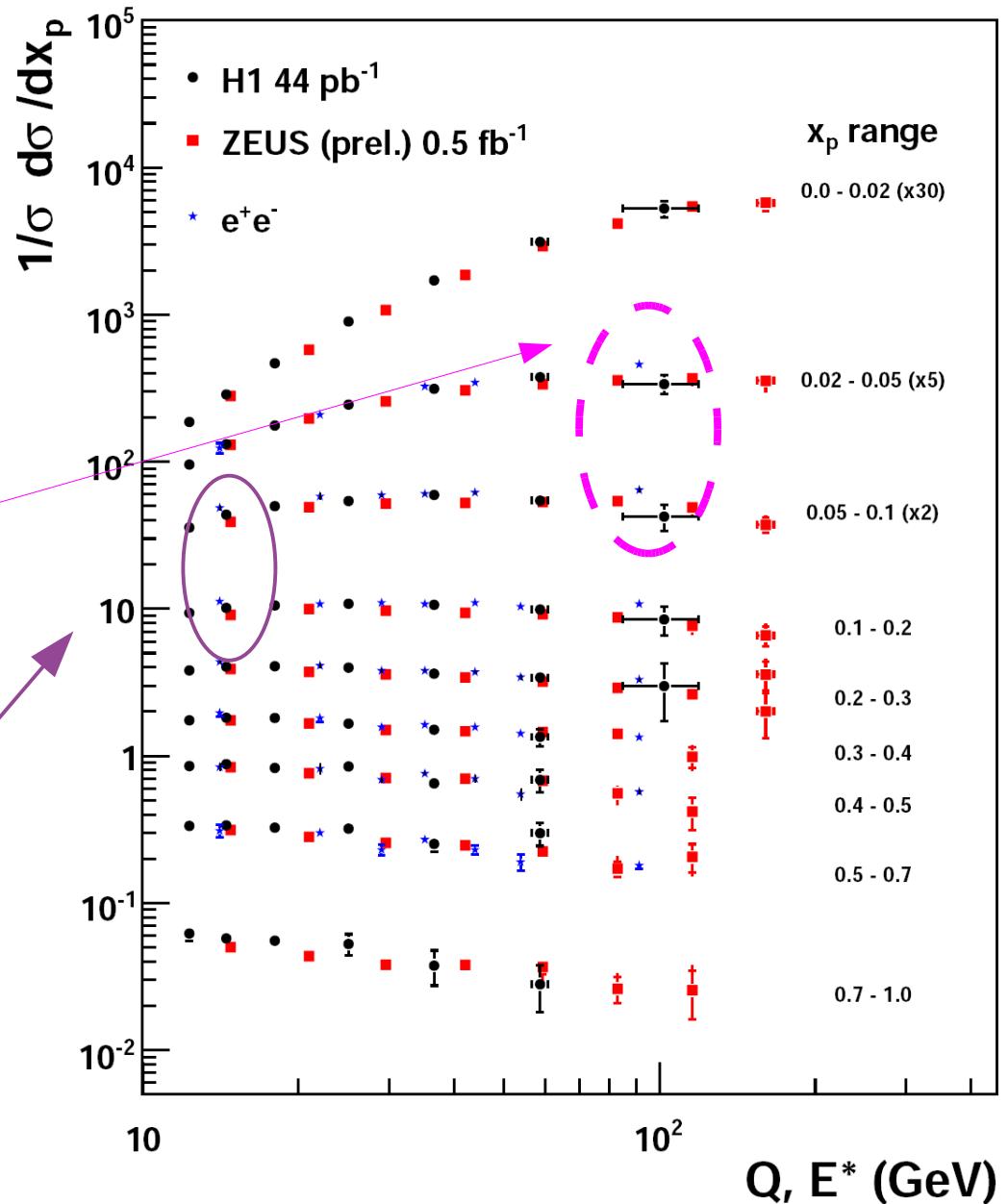


## Comparison ep with $e^+e^-$

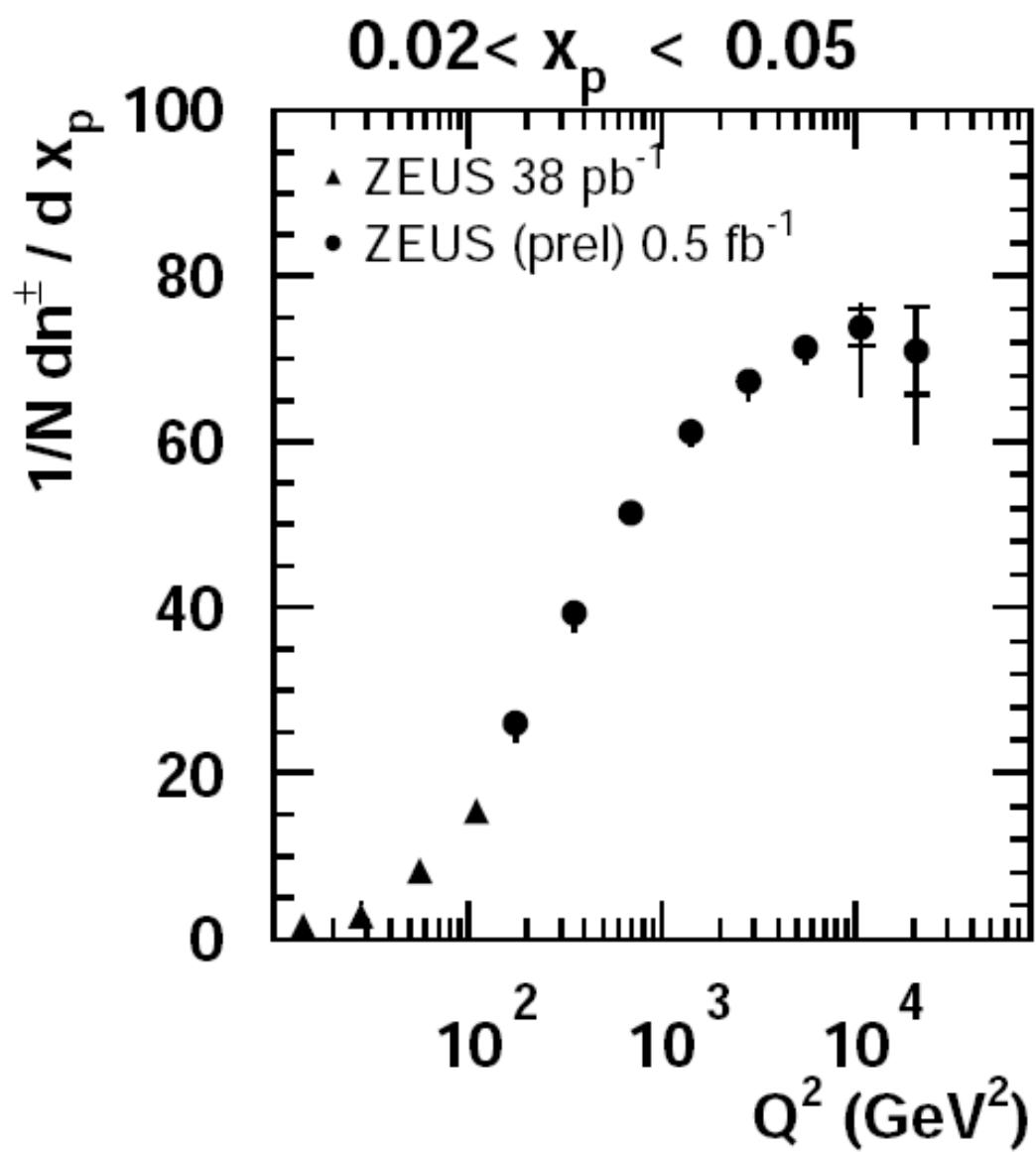
- supports the concept of quark fragmentation universality.
- scaling violation is observed

LEP (DELPHI)

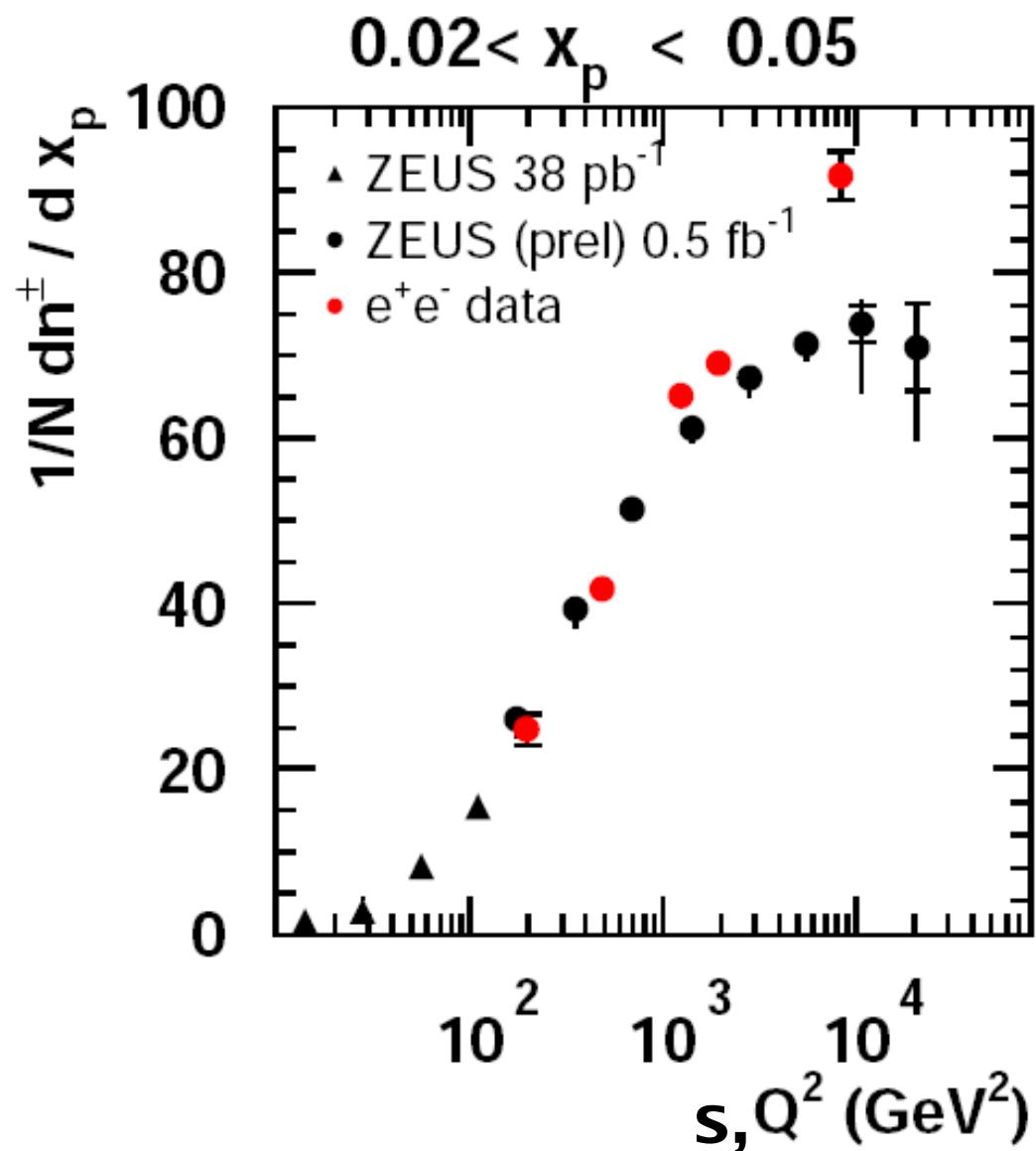
PETRA (TASSO)



# Scaled momenta in $x_p$ bins



# Scaled momenta in $x_p$ bins



$e^+e^-$  data imposed with  
 $s=4E^2_{\text{beam}}$

# Summary and conclusions

Charged hadron multiplicities are investigated in current region of Breit and HCM frames for different energy scales:  $2E_B^{cr}$ ,  $W$ ,  $M_{eff}$ ,  $Q$

- Mean charge multiplicity as a  $f(2E_B^{cr})$  agrees better with  $e^+e^-$  than as a  $f(Q)$ ,
- Usage of  $W$  and  $2E_B^{cr}$  gives a consistent comparison of  $ep$  with  $e^+e^-$  and with the previous DIS data
- KNO scaling for  $ep$  is similar to
  - one hemisphere of  $e^+e^-$  if  $W$  and  $2E_B^{cr}$  are used
  - total multiplicity if  $M_{eff}$  is used

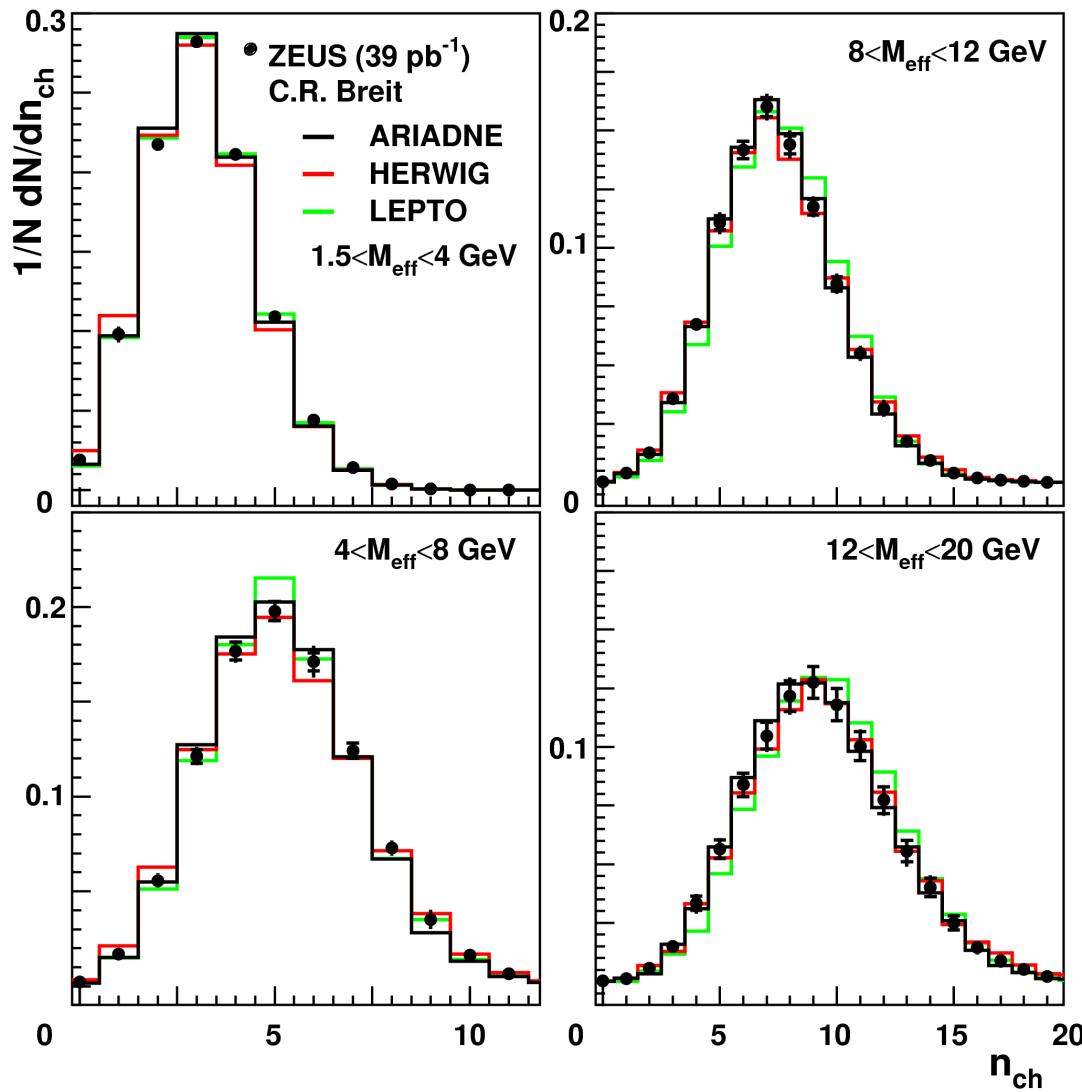
Scaled momenta in current region of  $ep$  Breit frame compared with  $e^+e^-$

- general trends are the same (the scaling violation is observed)
- some differences are seen for e.g. small  $x_p$  at LEP energies

# **Thank you for your attention.**

# Multiplicity in $M_{\text{eff}}$ bins in the Breit frame

ZEUS

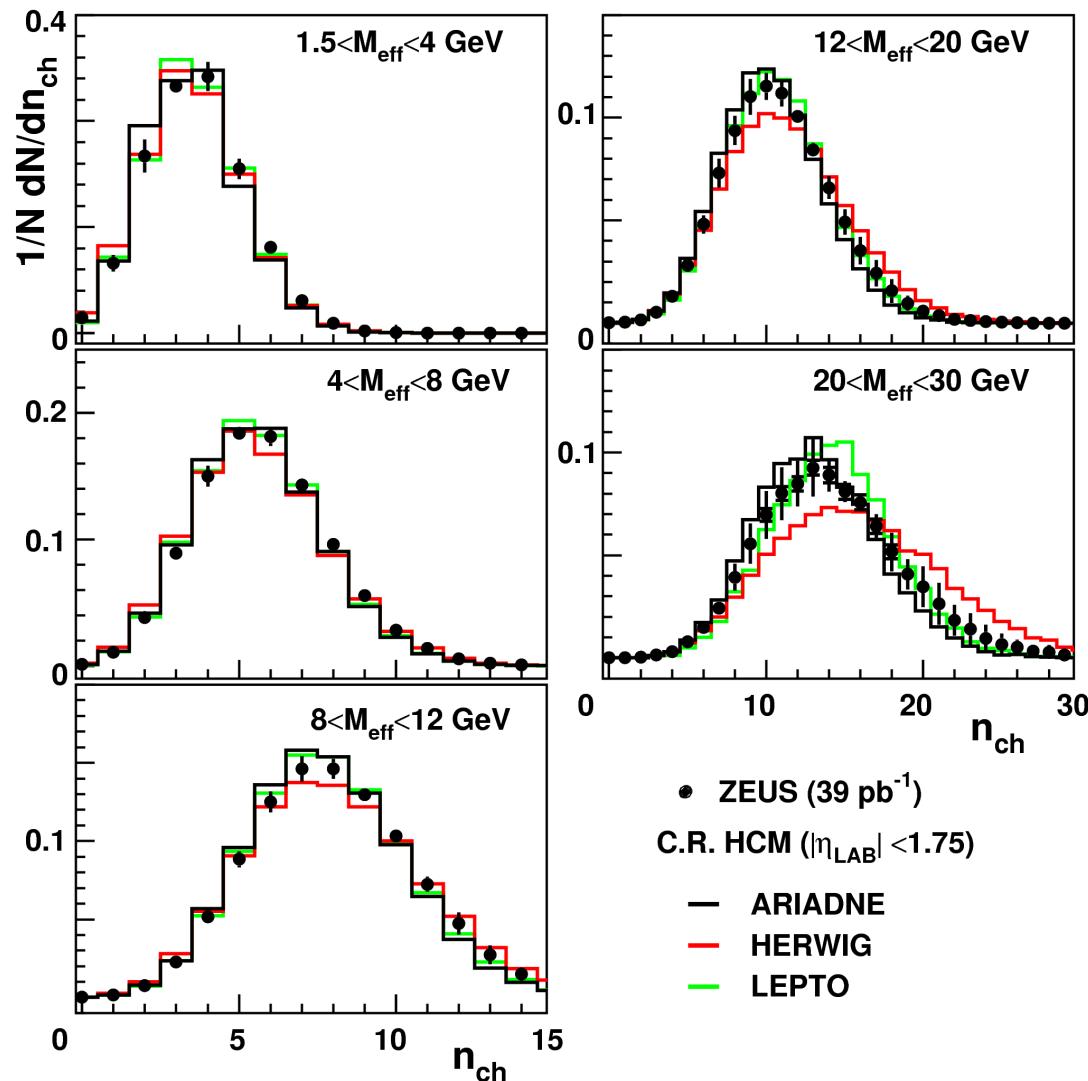


$M_{\text{eff}}$  — the invariant mass  
of hadronic system  
in the Breit frame

All the MC models  
→ good descriptions

# Multiplicity in $M_{\text{eff}}$ bins in the HCM frame

ZEUS

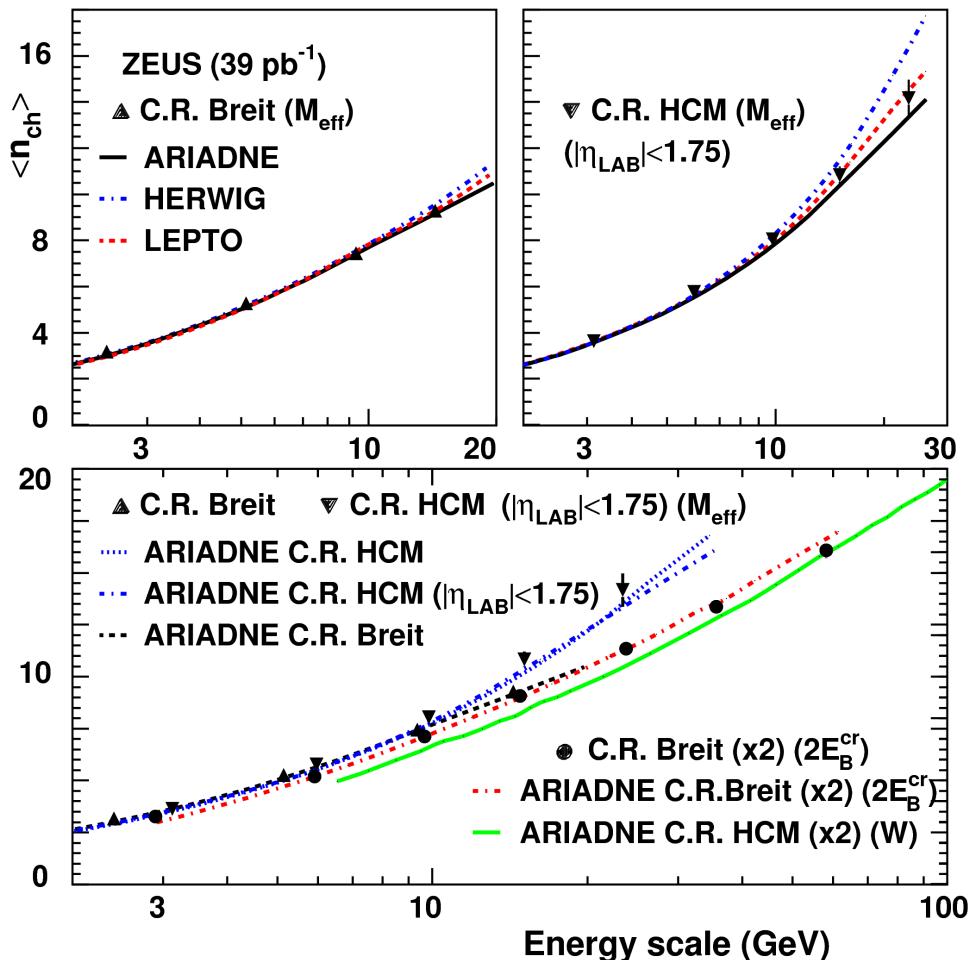


$M_{\text{eff}}$  — the invariant mass  
of hadronic system  
in  $\gamma^* p$  centre of mass

None of models gives  
a good description,  
in particular at higher  $M_{\text{eff}}$

# Average multiplicity as f ( $M_{\text{eff}}$ )

ZEUS



Data agree with  
LEPTO and ARIADNE

At energy scales  $M_{\text{eff}} < 10 \text{ GeV}$   
<math>\langle n\_{\text{ch}} \rangle</math> in Breit and HCM agree  
at higher scales  
<math>\langle n\_{\text{ch}} \rangle</math> rises faster in HCM