

α_s Determinations from Jets and Scaling Violations at HERA

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Buzios, Brazil



on behalf of the H1 and ZEUS Collaborations



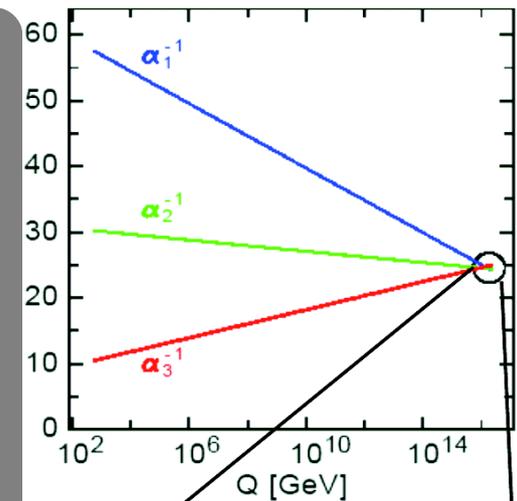
The Strong Coupling

Why is it so important to know α_s precisely?

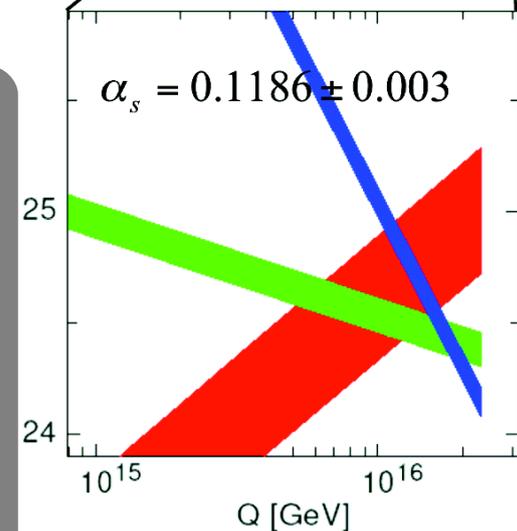
- ✗ Single free parameter of QCD
- ✗ Affects almost any cross section in high energy collisions
- ✗ Need to know QCD “background” precisely to discover new physics
- ✗ Unification of forces valid?

Features

- ✗ Asymptotic freedom
- ✗ Strong force for partons: ($10^2 \times$ EM, $10^{14} \times$ weak, $10^{40} \times$ gravitation)
- ✗ Less precisely known compared to other forces
- ✗ Cannot get hold of partons (confinement)



Unification??



hep-ph/0407067 B.Allanach ... P.Zerwas

Determinations

How to determine α_s ?

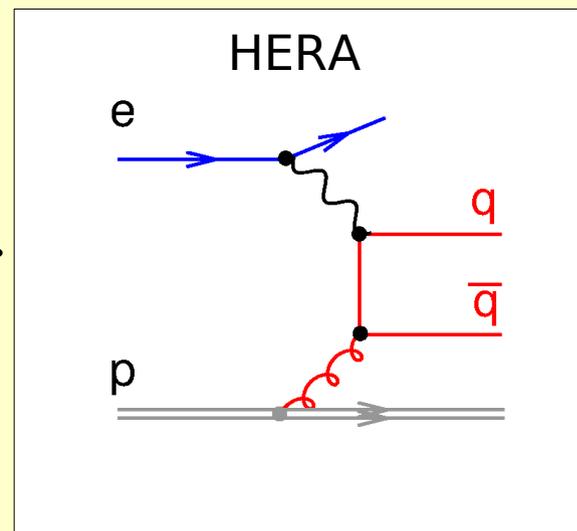
✗ Processes which involve gluon vertices

✗ electron-nucleon scattering →

✗ e^+e^- annihilation

✗ hadron-hadron collisions

✗ decays



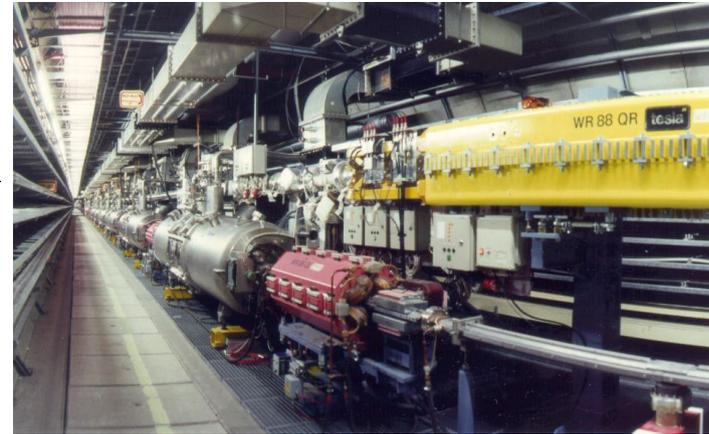
World averages

✗ 1989: $\alpha_s(m_Z) = 0.11 \pm 0.01$ only at 10%!

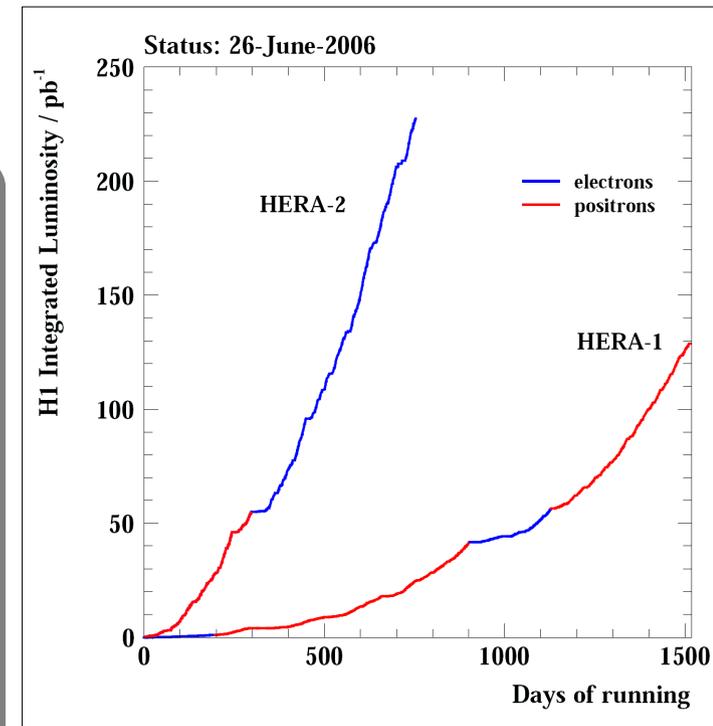
✗ Now world means from PDG and Bethke, constantly updated

✗ Making use of lots of measurements from different processes

HERA at DESY

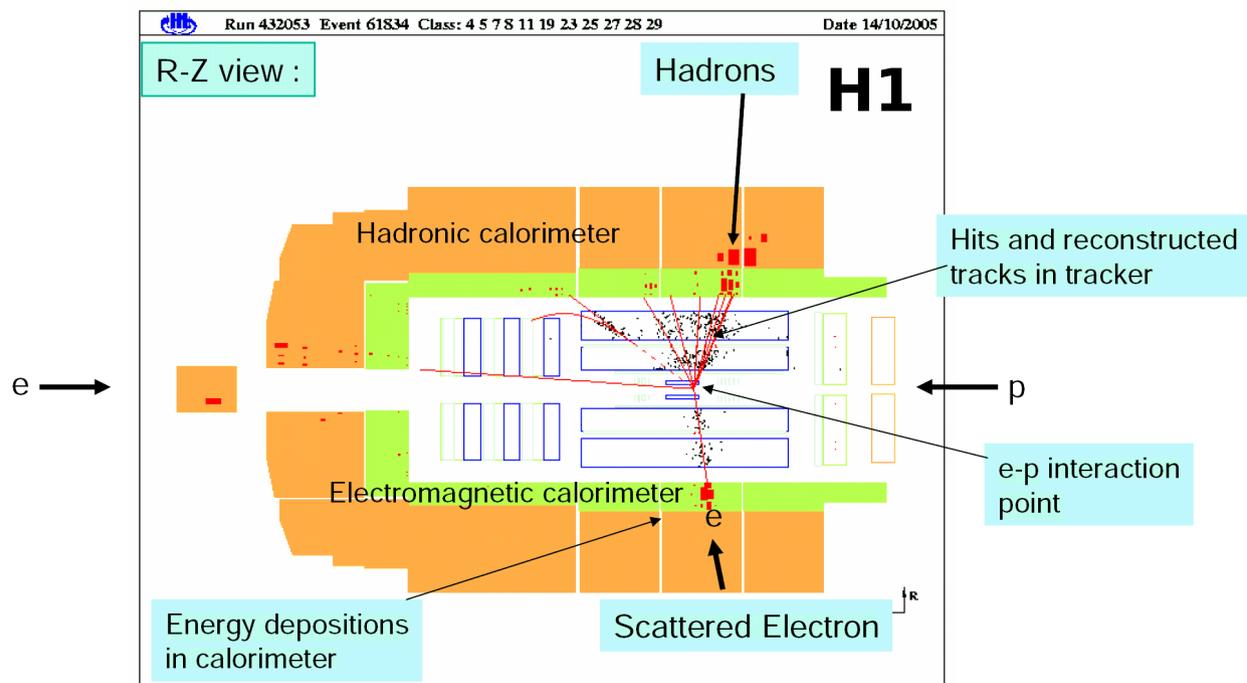
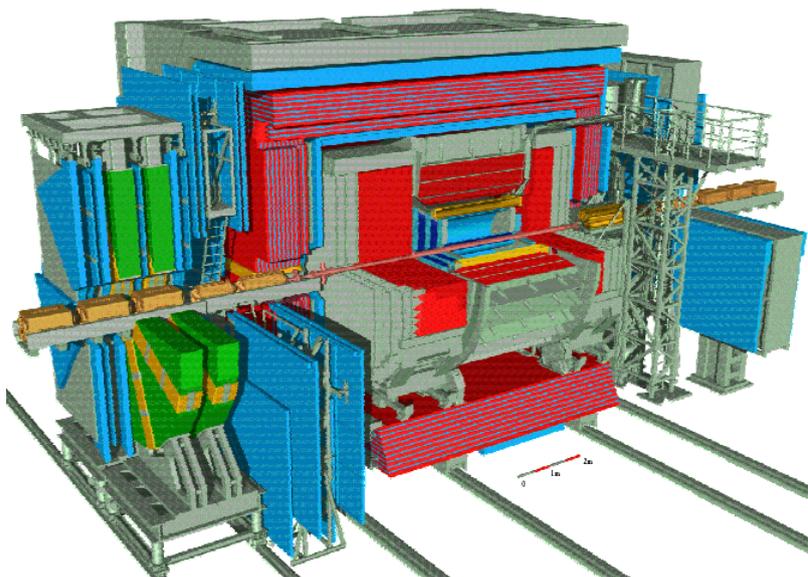


- ✘ Unique facility: separate storage rings for e^\pm and p
- ✘ 27.5 GeV electrons on 920 GeV protons
- ✘ HERA II (2002..):
 - ✘ longitudinally polarised electrons
 - ✘ inst. luminosity x5
 - ✘ 2006: best performance ever
- ✘ In the following: analyses with HERA I data



The H1 and ZEUS Experiments

ZEUS



- ✗ Two general purpose 4π detectors
- ✗ Scattered electron measured at 1% level
- ✗ Use electron to calibrate jets
- ✗ Major upgrades with HERA II:
 - ✗ More silicon detectors
 - ✗ Trigger
 - ✗

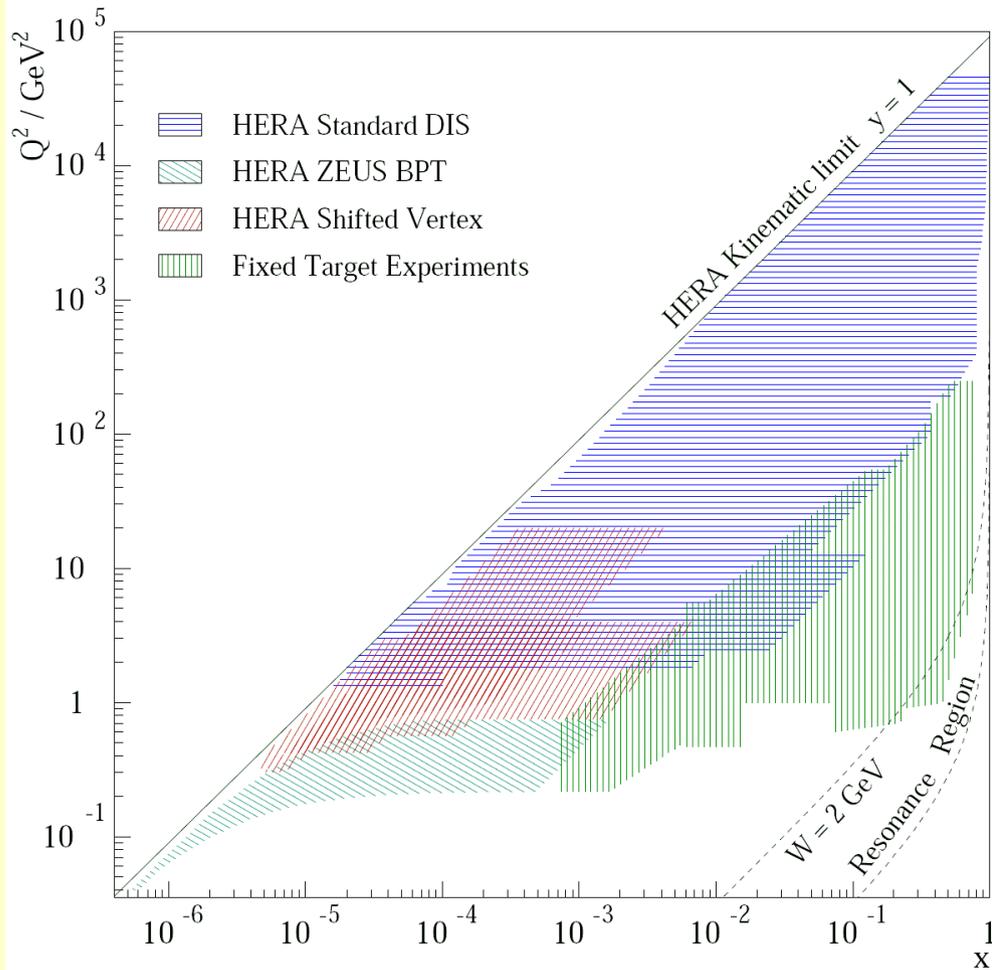
HERA's Contribution to α_s

How can HERA contribute?

- ✗ Competitive precision, enters world averages
- ✗ Complementary information:
 - ✗ Incompatible α_s from ep and $e^+e^- \Rightarrow$ QCD broken!
- ✗ Two approaches:
 - ✗ Scaling violation of F_2
 - 😊 very precise measurement and theory
 - ☹ indirect sensitivity
 - ✗ Observation of Jets
 - ☹ more difficult measurement and theory
 - 😊 direct sensitivity
 - ✗ Want both!

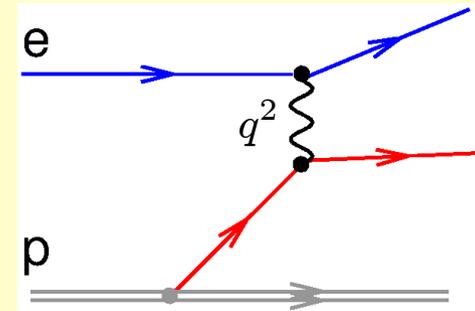
Factorisation:
$$\sigma = \left[\sum_{i=g,q,\bar{q}} \int dx f_i(x, \mu_f, \underline{\alpha}_s(\mu_f)) \hat{\sigma}_{\text{pQCD}}(x, \mu_f, \mu_r, \underline{\alpha}_s(\mu_r)) \right] (1 + \delta_{\text{had}})$$

Kinematic Coverage



X Large range in x and Q^2

Essential to establish scaling violations



Center of mass energy

$$\sqrt{s} = 31.9 \text{ GeV}$$

Four momentum transfer

$$Q^2 = -q^2$$

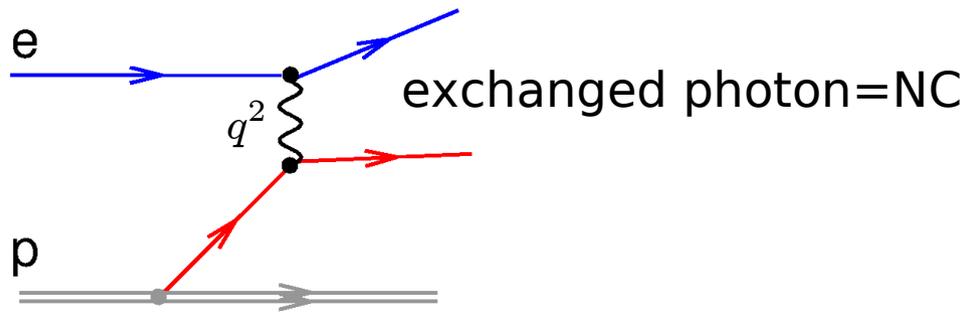
Bjorken scaling variable

$$x = \frac{Q^2}{2p \cdot q}$$

Inelasticity

$$y = \frac{Q^2}{sx}$$

Determination of F_2



$$\frac{d^2 \sigma_{NC}^{e^\pm p}}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4}$$

$$\left[\left(1 + (1-y)^2\right) \tilde{F}_2(x, Q^2) - \frac{y^2}{2} \tilde{F}_L(x, Q^2) \mp \left(y - \frac{y^2}{2}\right) x \tilde{F}_3(x, Q^2) \right]$$



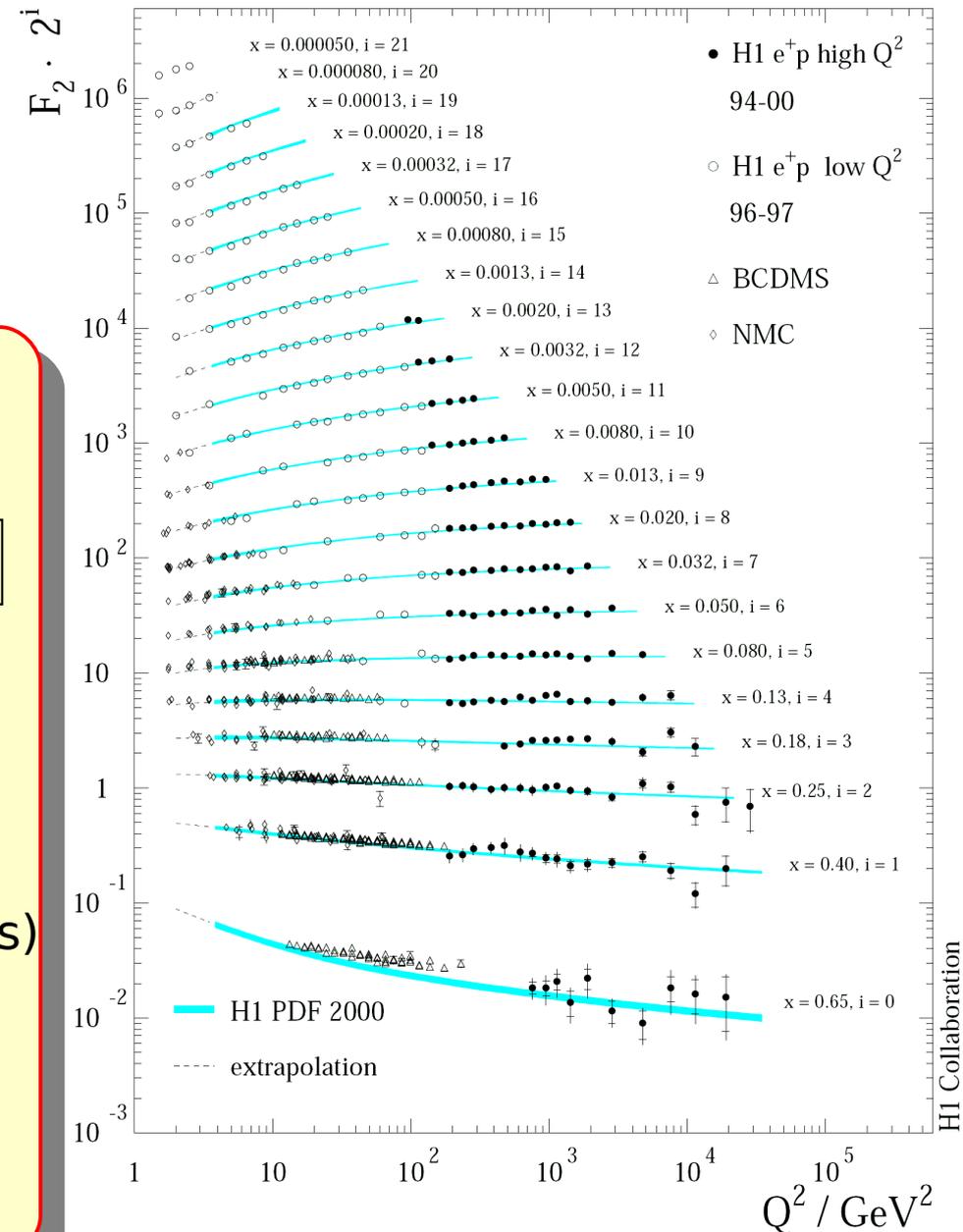
X In large part of phase space:
cross section dominated by
electromagnetic structure function F_2

X F_2 related to parton density functions(pdf's)

in QPM:

$$F_2 = x \sum_q e_q^2 (q + \bar{q})$$

does not depend on $Q^2 \Rightarrow$ scaling



α_s Extraction with F_2

✘ Higher order QCD processes introduce scaling violations

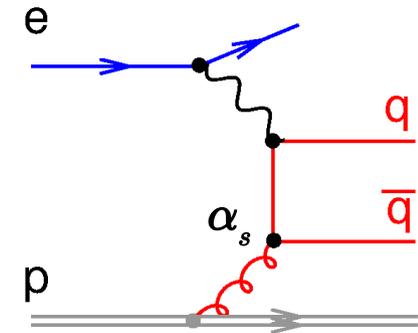
$$\frac{\partial F_2}{\partial \ln Q^2} \neq 0$$

✘ Magnitude given by gluon density and α_s

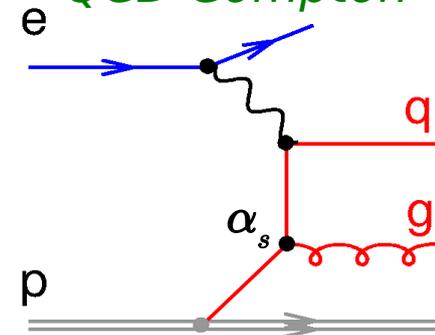
✘ Evolution of the pdfs with Q^2 by DGLAP equations

✘ In a fit, the gluon density and $\alpha_s(m_Z)$ can be simultaneously determined

Boson Gluon Fusion



QCD Compton



+ higher orders.....

α_s Extraction with F_2

✘ Structure functions data from H1 and BCDMS (high x, muon) used

✘ Determination of the pdfs: gluon, up-type, down-type

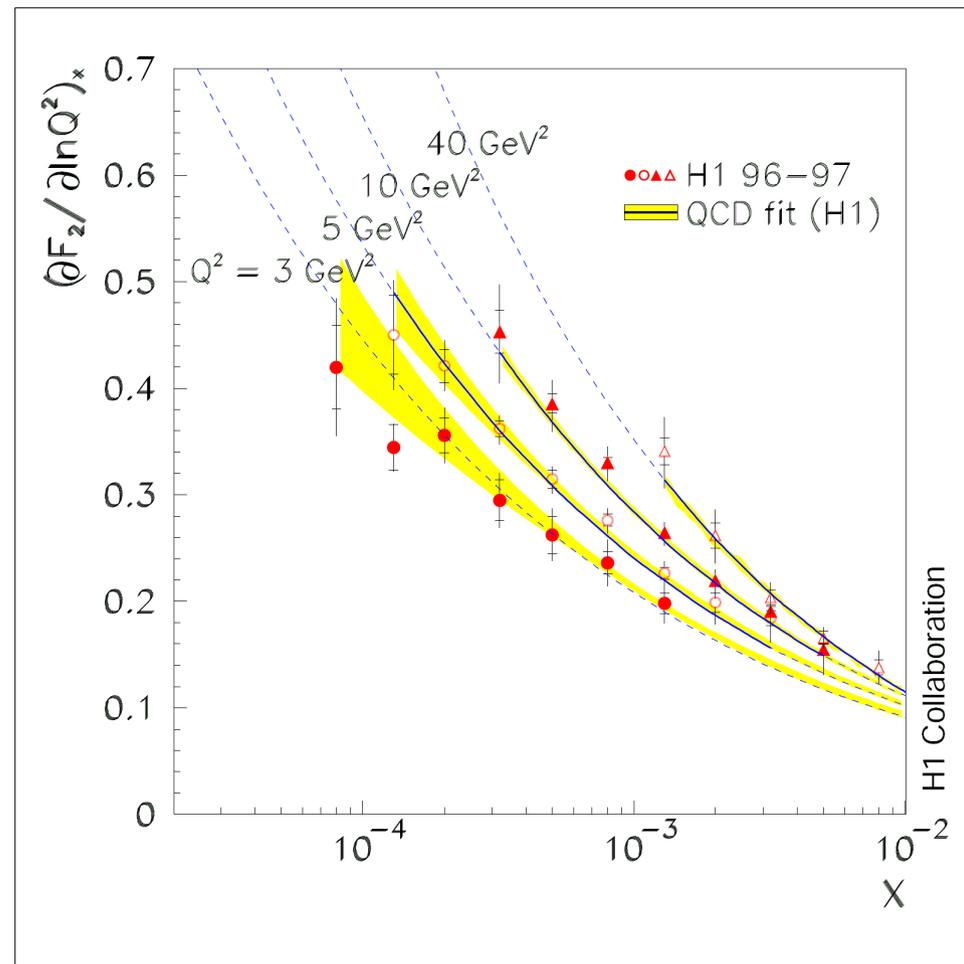
✘ Best fit:

$$\alpha_s(m_Z) = 0.1150 \pm 0.0017(\text{exp})$$

$$+0.0009$$

$$-0.0005(\text{model}) \pm 0.0050(\text{th.})$$

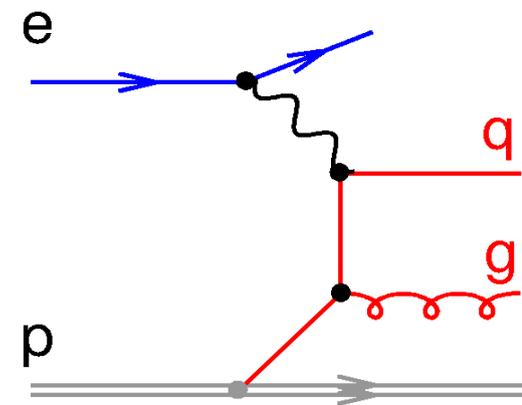
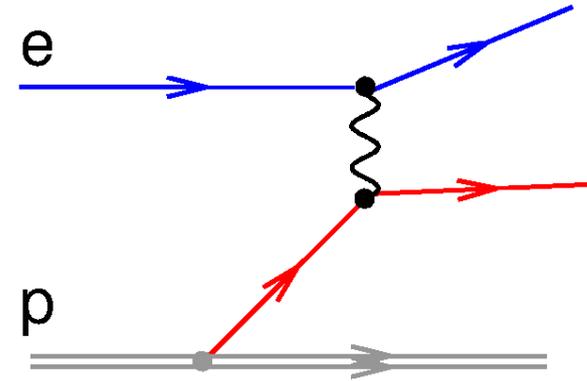
✘ Compatible with world mean, small experimental error



EPJ 21 (2001) 33

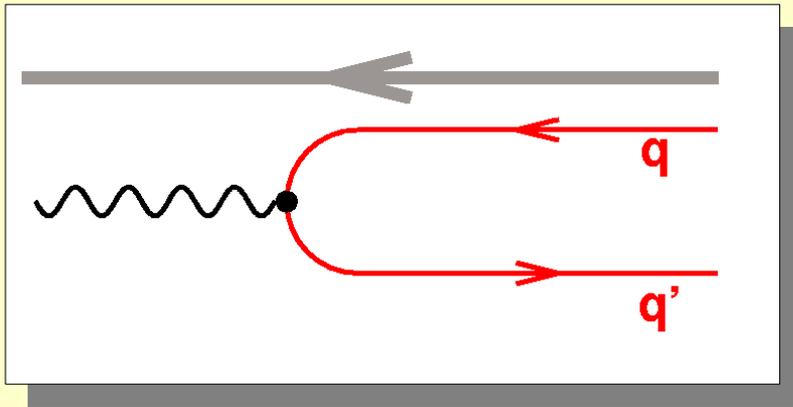
Jet Measurements

- ✗ To obtain direct sensitivity: observable which vanishes for the Born graph
- ✗ Final state with multiple partons
- ✗ Correspondence jet ↔ parton at high E_t
- ✗ No unique definition of a jet, here **incl. k_t cluster algorithm**
 - ✗ similar to e^+e^- algorithms
 - ✗ favoured by theory over cone algorithms
 - ✗ infrared and collinear safe at all orders
 - ✗ factorisable
- ✗ For DIS: the E_t of jets in the laboratory frame not QCD driven: recoil of the scattered electron!
⇒ boost to **Breit frame** of reference

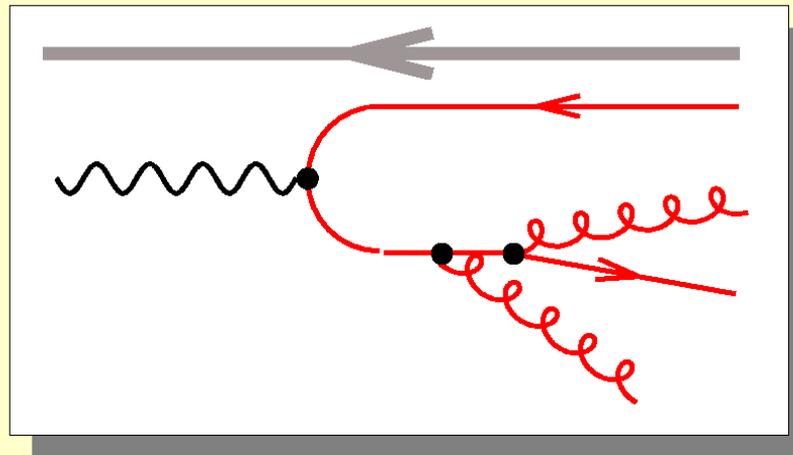


Breit Reference Frame

- ✗ Virtual photon and incoming parton: head-on
- ✗ Calculated using kinematic variables



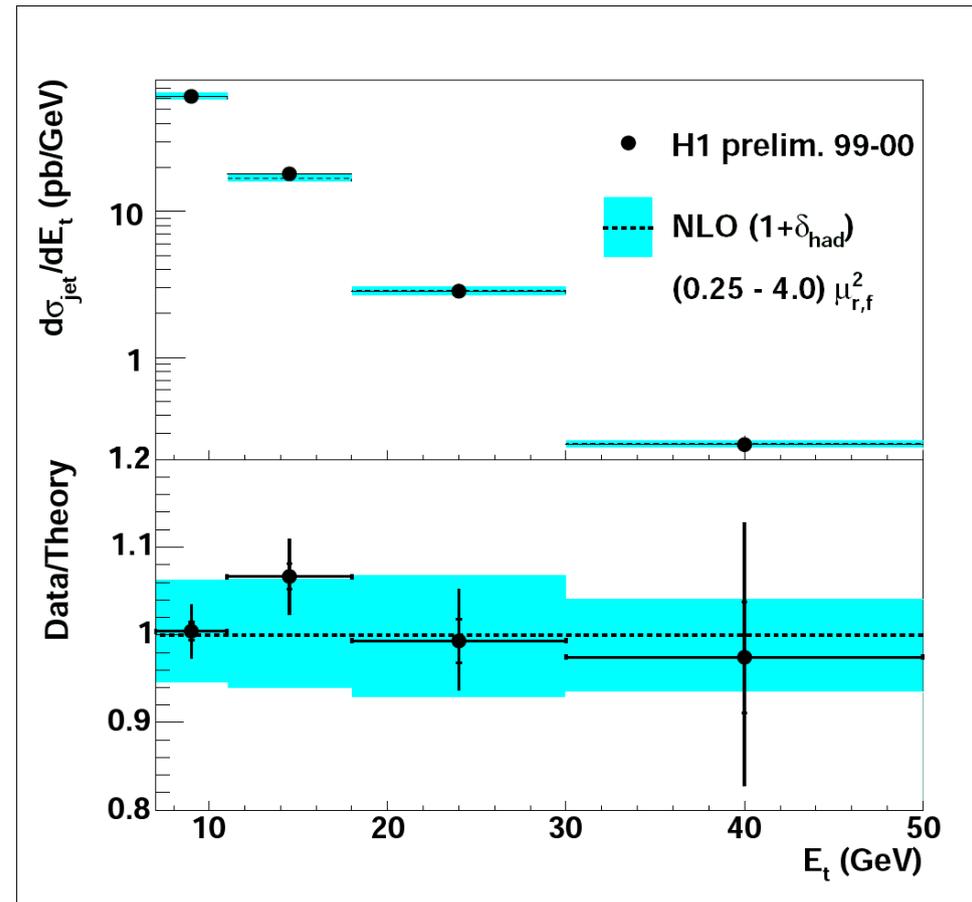
Breit frame: jet at Born level has **no** E_t
may have high E_t in lab. frame



require minimum E_t in Breit frame ->
pQCD **reliable**

Inclusive Jets at High Q^2

- ✗ “inclusive”: each jet of an event contributes to the cross section
- ✗ High Q^2 : 150 $\text{GeV}^2 \dots 5000 \text{ GeV}^2$
- ✗ Exp. error $\sim 5\%$, mainly due to hadronic energy scale
- ✗ Theory prediction:
 - ✗ NLOJET++, CTEQ5M1
 - ✗ Hadronisation corrections $< 10\%$ (obtained with MC generators)
 - ✗ $\mu_R = E_t$, $\mu_F = Q$, varied by factor 2 to estimate uncertainty
- ✗ Data well reproduced over E_t range



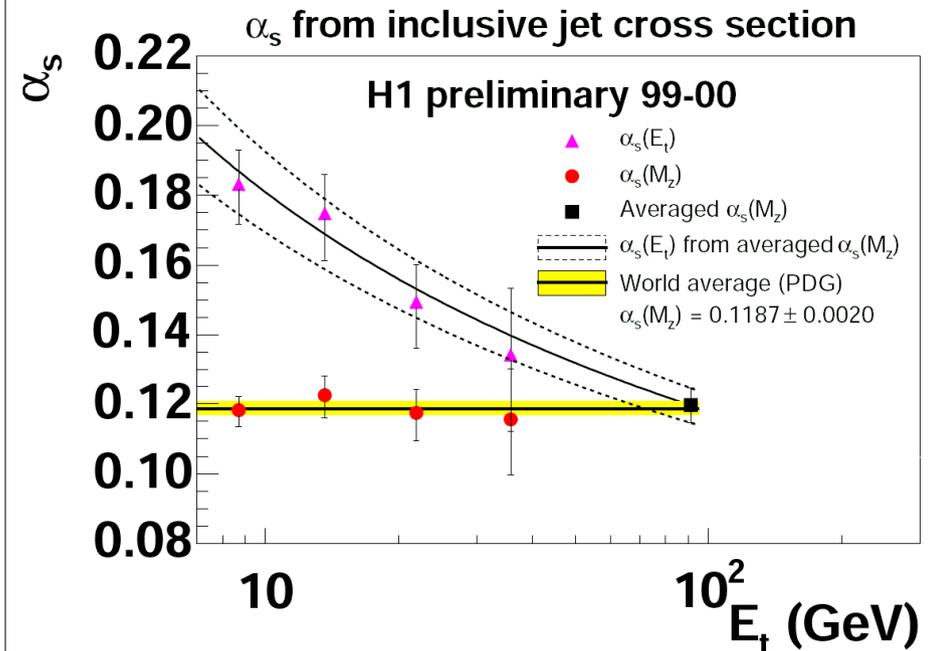
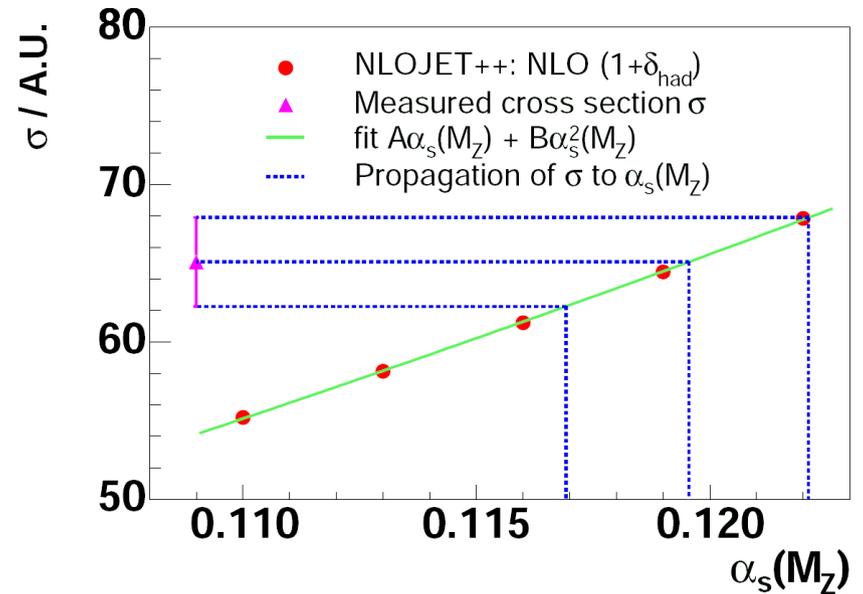
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Inclusive Jets at High Q^2

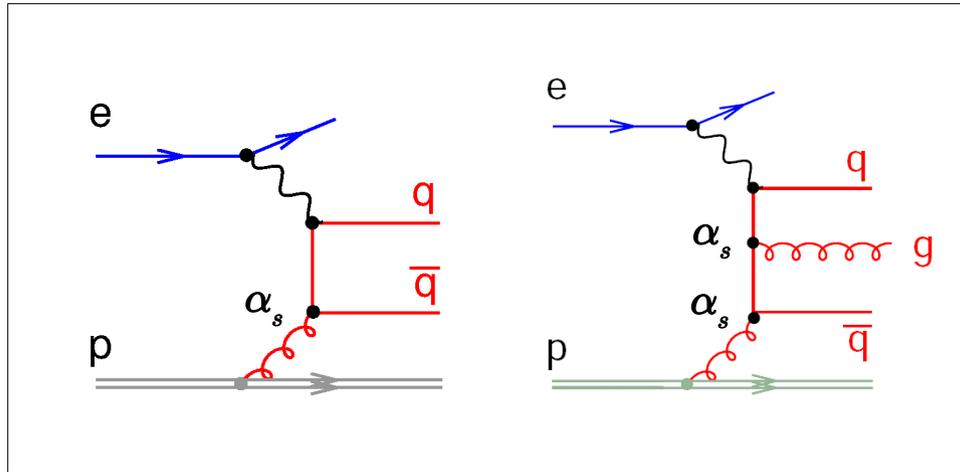
Method to extract α_s

- ✗ Calculate each cross section for some values of $\alpha_s(m_Z)$, matched with pdfs
- ✗ Interpolate between points
- ✗ Map measured cross section with error onto $\alpha_s(m_Z)$ axis
- ✗ Using **R**enormalisation **G**roup **E**quation obtain “running” $\alpha_s(E_t)$
- ✗ Average (with correlated systematics):

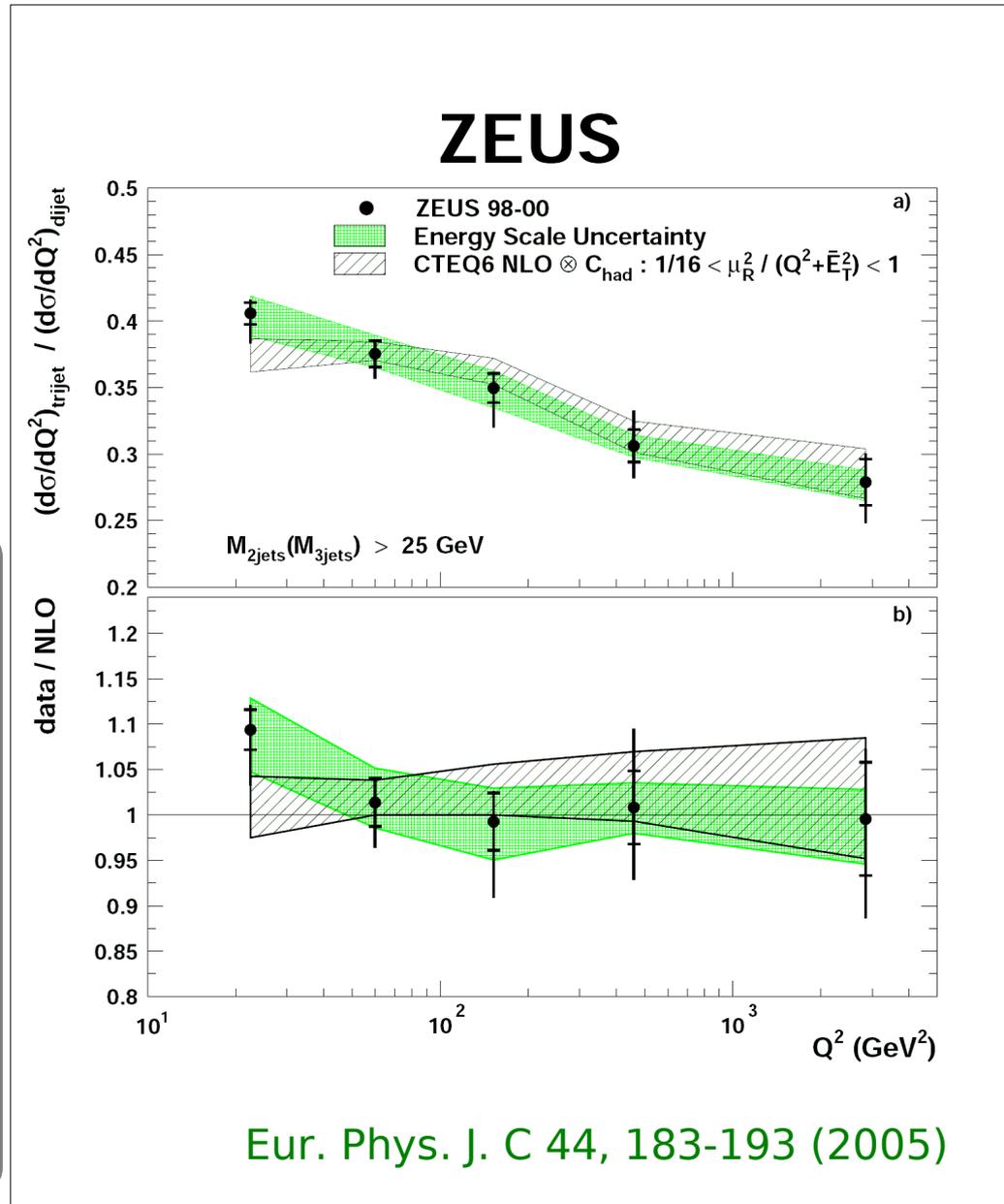
$$\alpha_s(m_Z) = 0.1197 \pm 0.0016 (\text{exp.})_{-0.0048}^{+0.0046} (\text{th.})$$
 theory error dominating
- ✗ Precision comparable with F_2 analysis, compatible within errors



Multi Jets at High Q^2



- ✗ Build a ratio 3-jet/2-jet
- ☺ Partial cancellation of uncertainties (e.g. on gluon density)
- ☹ But: less statistics, more constrained phase space
- ✗ An alternative
- ✗ Good description of Q^2 dependence by NLOJET++ and CTEQ6 pdfs



Multi Jets at High Q^2

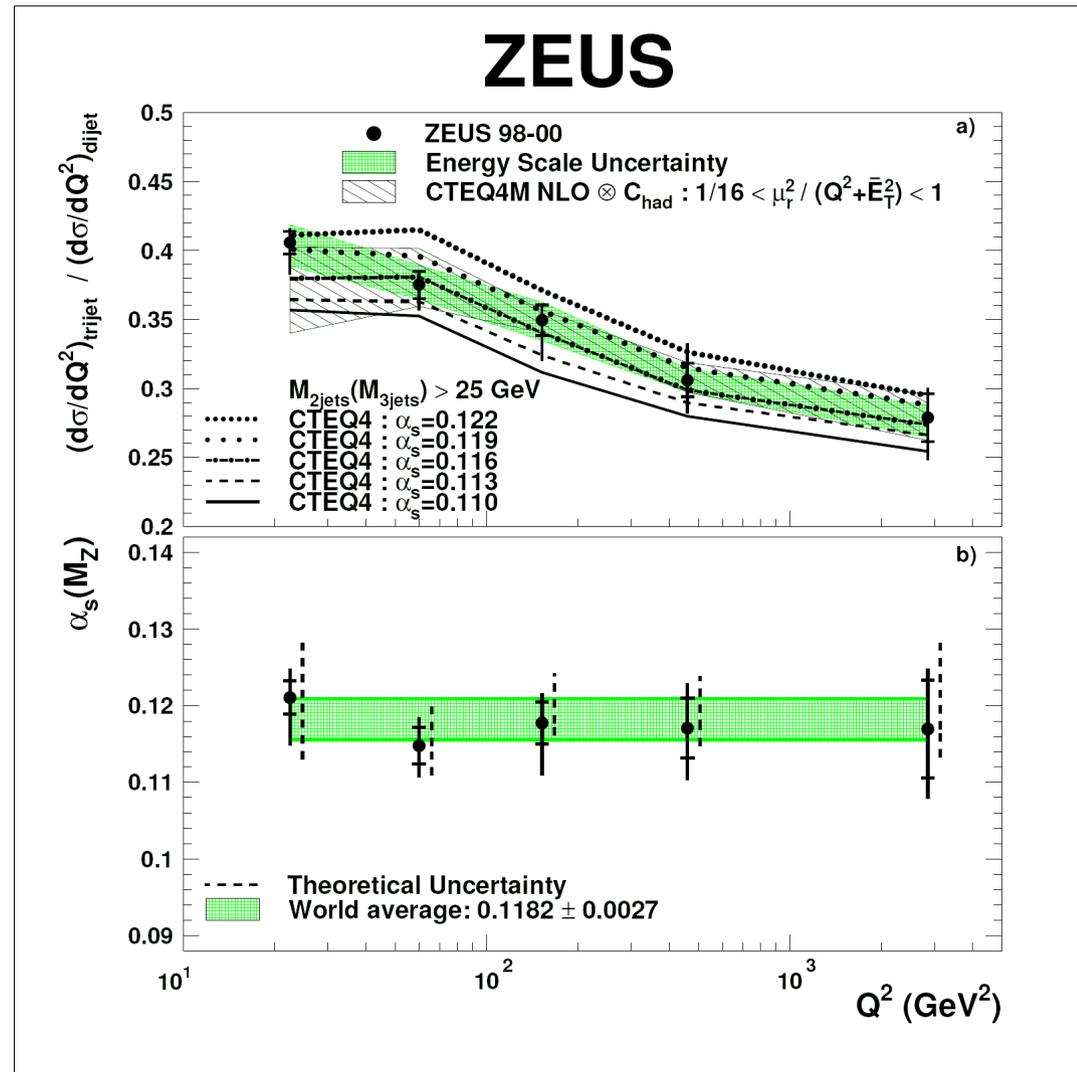
- ✗ Same method to extract $\alpha_s(m_Z)$ as for incl. jets
- ✗ Extension to lower Q^2 :
10 $\text{GeV}^2 \dots 5000 \text{ GeV}^2$ possible due to reduced theory uncertainty
- ✗ Average value consistent with the other determinations

$$\alpha_s(m_Z) = 0.1179 \pm 0.0013(\text{stat.})$$

$$+0.0028 \text{ (exp.)} +0.0064 \text{ (th.)}$$

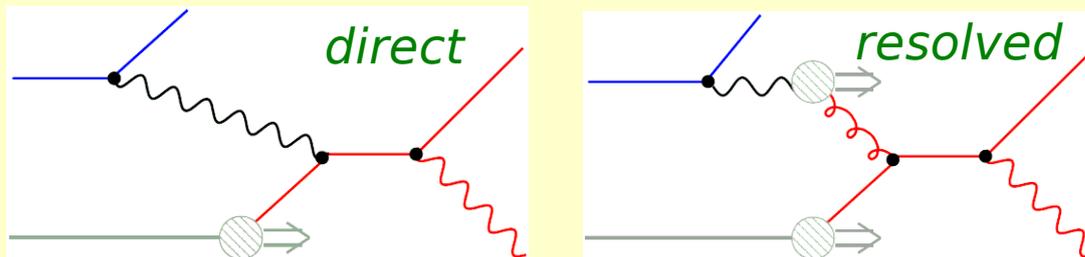
$$-0.0046 \text{ (exp.)} -0.0046 \text{ (th.)}$$

again theory largest uncertainty



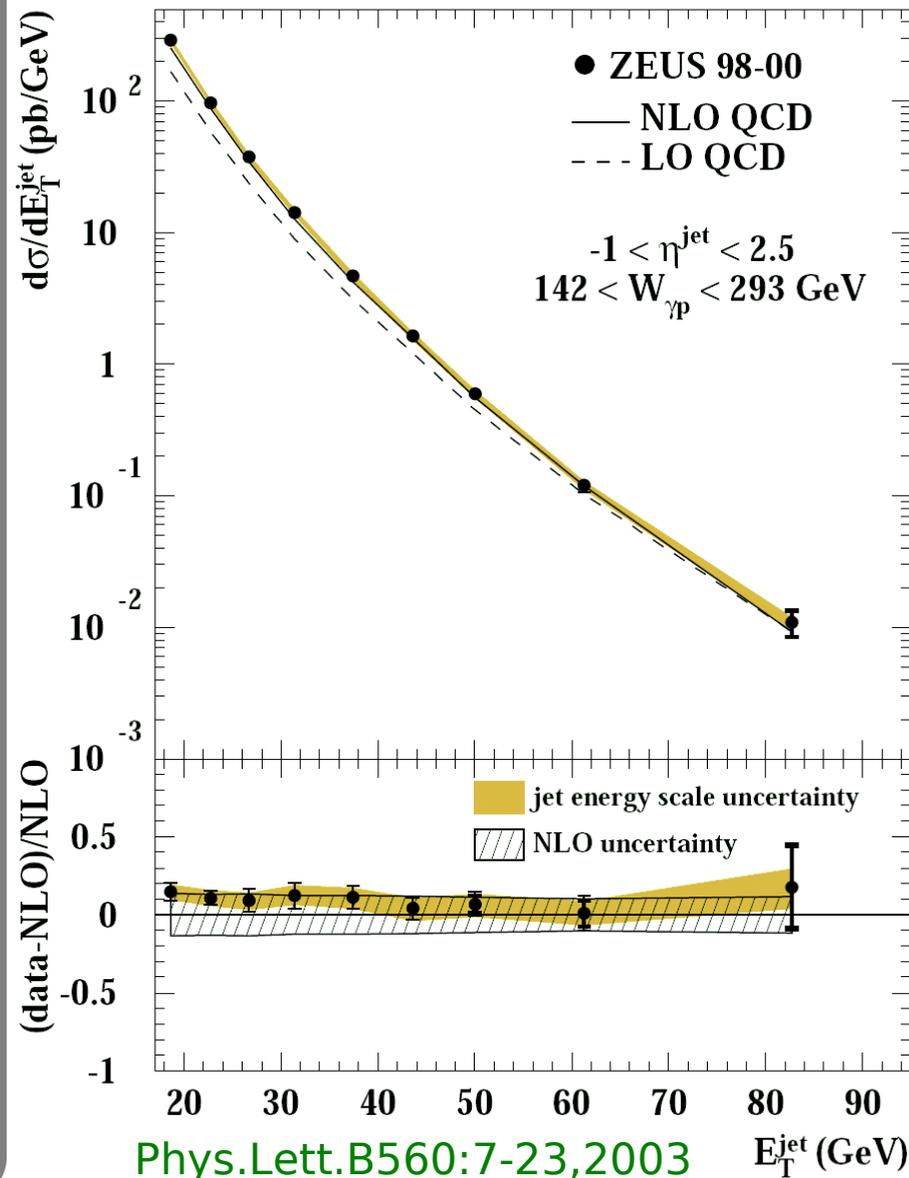
Inclusive Jets in γp

- ✗ Photoproduction: quasi real photons, scattered electron stays in beampipe
- ✗ Resolved photon process, similar to hadron-hadron (RHIC energies)



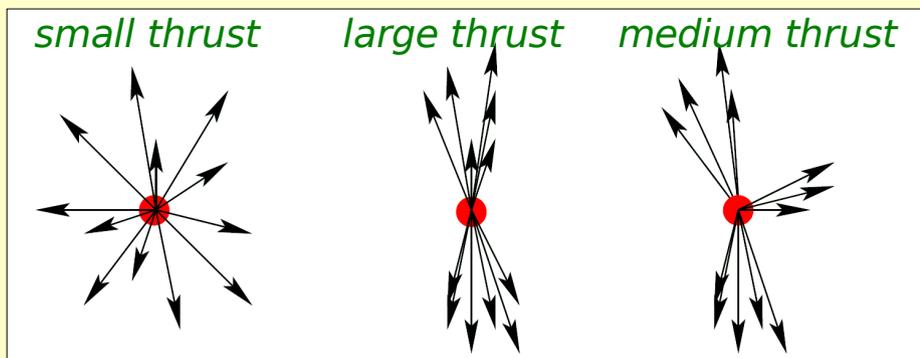
- ✗ Large cross section, can go to high jet E_t
- ✗ NLO (Klasen et al.), $\mu_R = \mu_F = E_t$, MRST99 (proton), GRV (photon)
- ✗ Fitted $\alpha_s(m_Z) = 0.1224 \pm 0.0001$ (stat.)
 $+0.0022$ (exp.) $+0.0054$ (th.)
 -0.0019 (exp.) -0.0042 (th.)
- ✗ Consistent value (different process!)

ZEUS



Event Shapes

- ✗ Introduced historically before jets: event shapes
- ✗ Calculate from 4-vectors of HFS a real number, topological feature



- ✗ QCD sensitive, more inclusive than jets: no E_t cut \Rightarrow large statistics
- ✗ Ratio of momenta \Rightarrow had. energy scale cancels (largest exp. uncert. for jets!)
- ✗ But: hadronisation effects very large (upto 100%)

\Rightarrow application for ansatz beyond models:
Power Corrections

Thrust

$$T_C = \max_{\vec{n}_T} \frac{\sum |\vec{p}_h \cdot \vec{n}_T|}{\sum |\vec{p}_h|}$$

Jet Mass

$$\rho = \frac{(\sum E_h)^2 - (\sum \vec{p}_h)^2}{(2 \sum |\vec{p}_h|)^2}$$

C-Parameter

$$C = \frac{3}{2} \frac{\sum_{h,i} |\vec{p}_h| |\vec{p}_i| \sin^2 \theta_{hi}}{(\sum |\vec{p}_h|)^2}$$

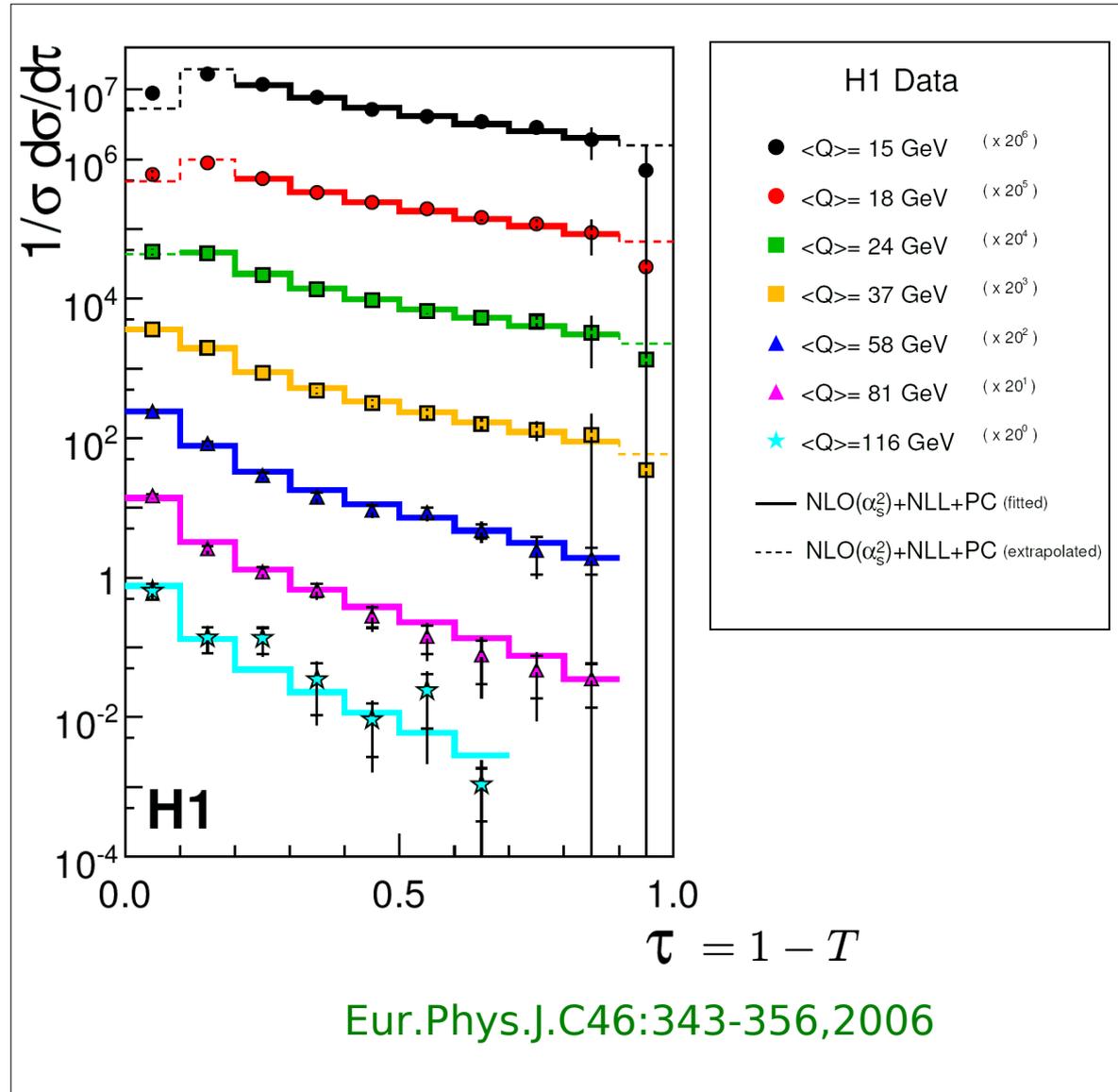
Thrust , Broadening (boson axis)

$$T = \frac{\sum |\vec{p}_{z,h}|}{\sum |\vec{p}_h|} \quad B = \frac{\sum |\vec{p}_{\perp h}|}{2 \sum |\vec{p}_h|}$$

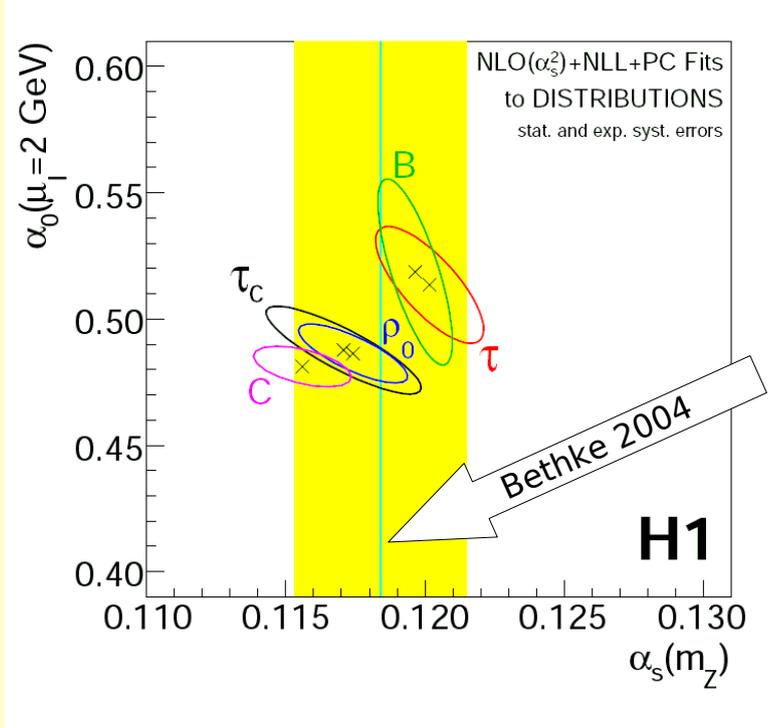
- ✗ Sum over particles in current hemisphere (reject remnant)

Event Shapes

- ✗ Differential distributions as function of scale Q
- ✗ Not statistically limited (except highest Q)
- ✗ Asymptotic freedom: higher scales \Rightarrow smaller $\alpha_s \Rightarrow$ collimated HFS $\Rightarrow \tau$ peaks at 0
- ✗ Theory:
 - ✗ DISASTER++ (Graudenz)
 - ✗ Soft gluon resummation at NLL (Dasgupta, Salam)
 - ✗ Power corrections (Dokshitzer, Webber)
- ✗ Good description over full Q range, but not valid everywhere
- ✗ Also available: τ_c, B, ρ, C



Event Shapes

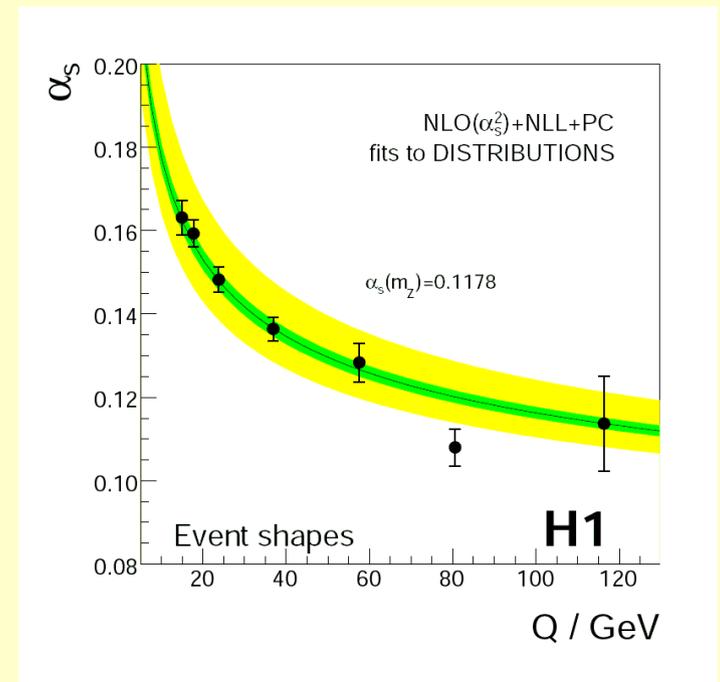


✘ Simultaneous fit of $\alpha_s(m_Z)$ and power correction parameter $\alpha_0(2\text{GeV})$

✘ Universal $\alpha_0 = \mu_I^{-1} \int_0^{\mu_I} \alpha_{\text{eff}}(k) dk$ required for power corrections, similar value in e^+e^-

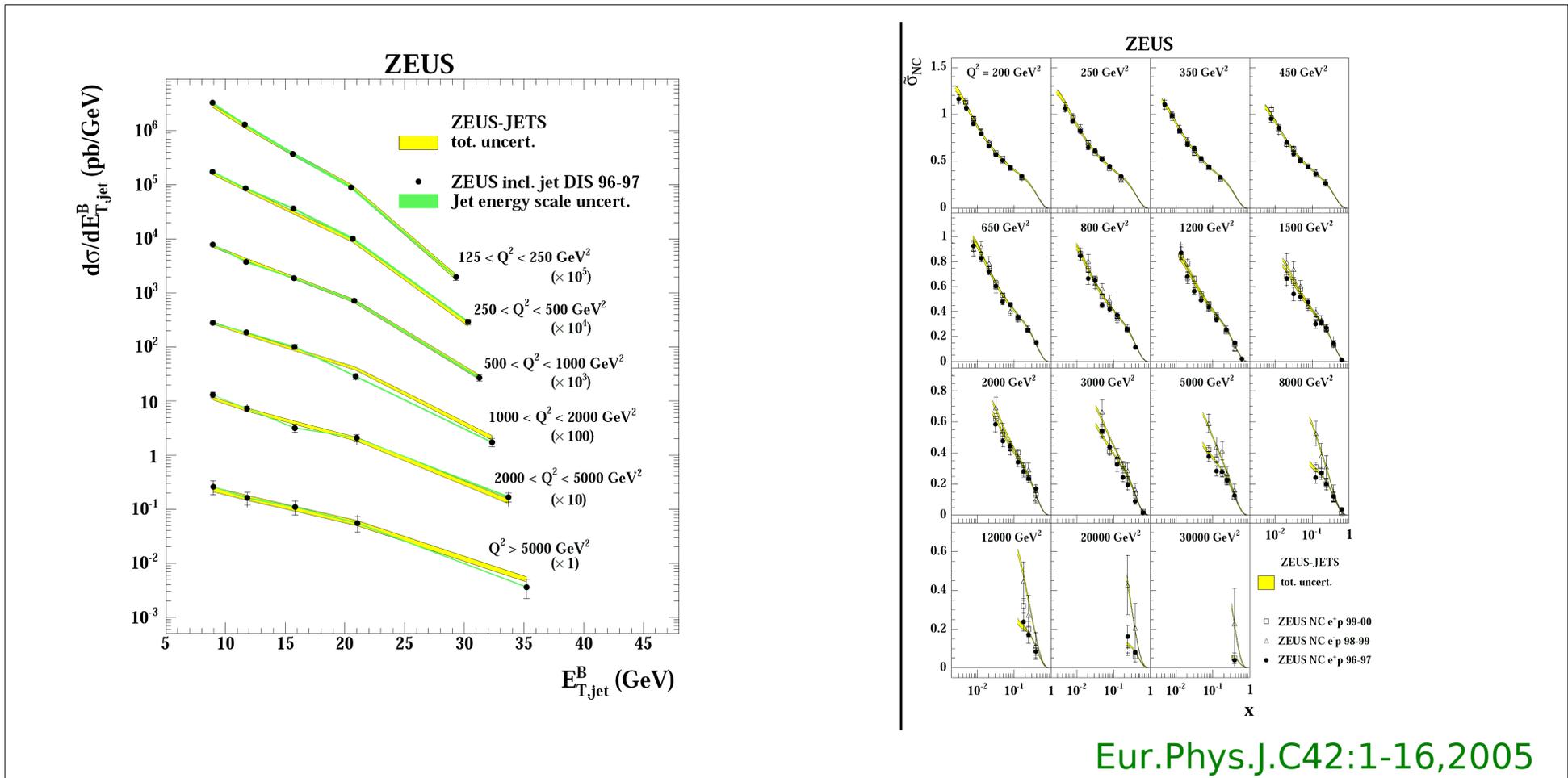
✘ Combine 5 event shapes into average:

$$\alpha_s(m_Z) = 0.1198 \pm 0.0013(\text{exp.})_{-0.0043}^{+0.0056}(\text{th.})$$



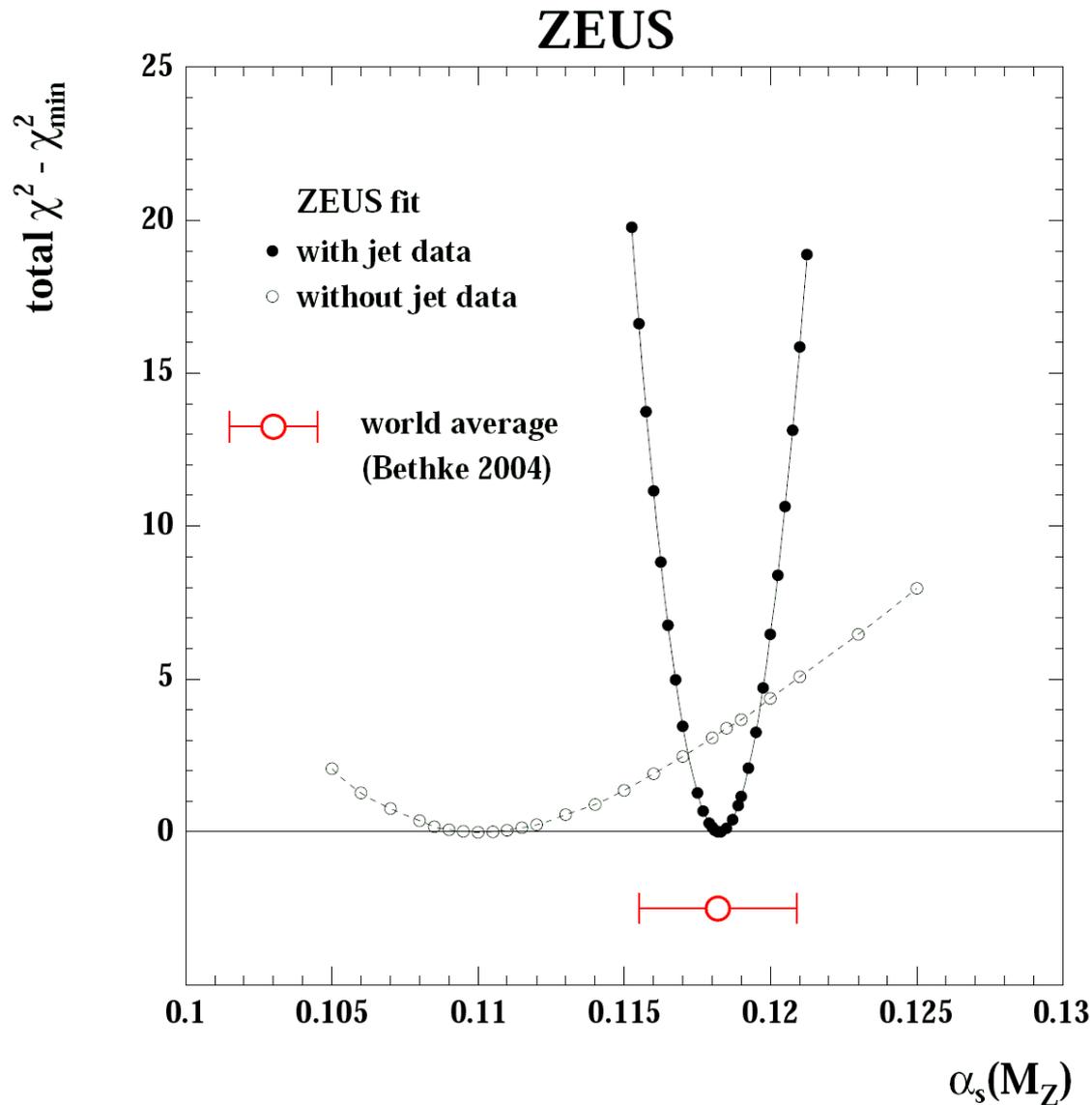
✘ Asymptotic freedom clearly demonstrated, huge range in Q

Merging F_2 and Jets in a Fit



- ✗ ZEUS-JETS QCD fit: inclusive cross sections + incl. jets in DIS + dijets in γp
- ✗ Take care of correlated experimental uncertainties
- ✗ Jets improve gluon at higher x

Combining F_2 and Jets in a Fit



- ✗ Jets constrain $\alpha_s(m_Z)$
- ✗ Inclusive data alone prefer low value of strong coupling
- ✗ Compare to other incl. fits:
H1: $\alpha_s(m_Z) = 0.1151$
BCDMS: $\alpha_s(m_Z) = 0.1107$
- ✗ General issue? More data and improved theory will tell....

HERA Average

✘ Great diversity in determinations of $\alpha_s(m_Z)$ at HERA

✘ Consistent with each other

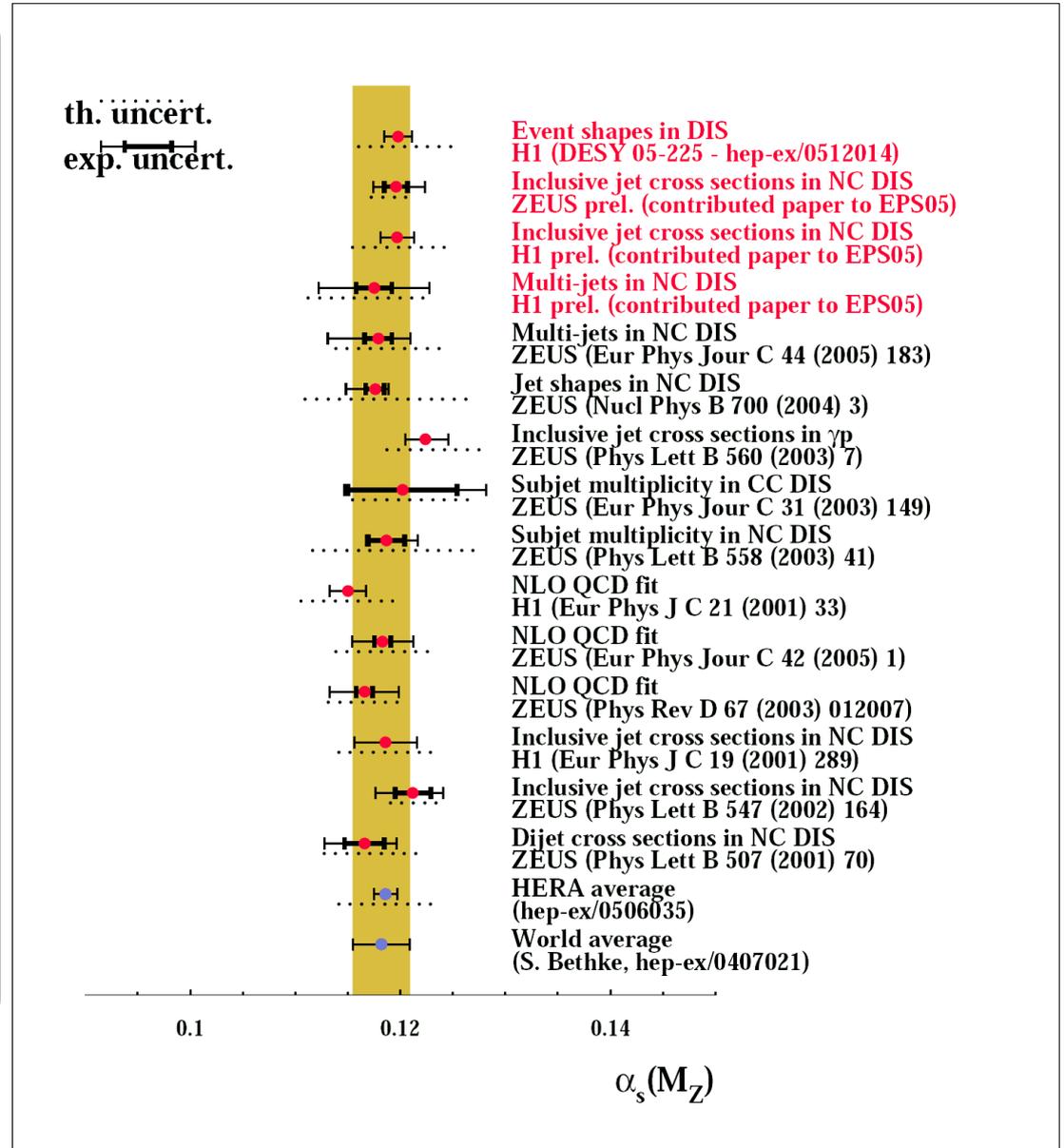
✘ Theoretical uncertainties dominant

✘ Build HERA average (without red ones)

$$\alpha_s(m_Z) = 0.1186 \pm 0.0011 \text{ (exp.)} \pm 0.0050 \text{ (th.)}$$

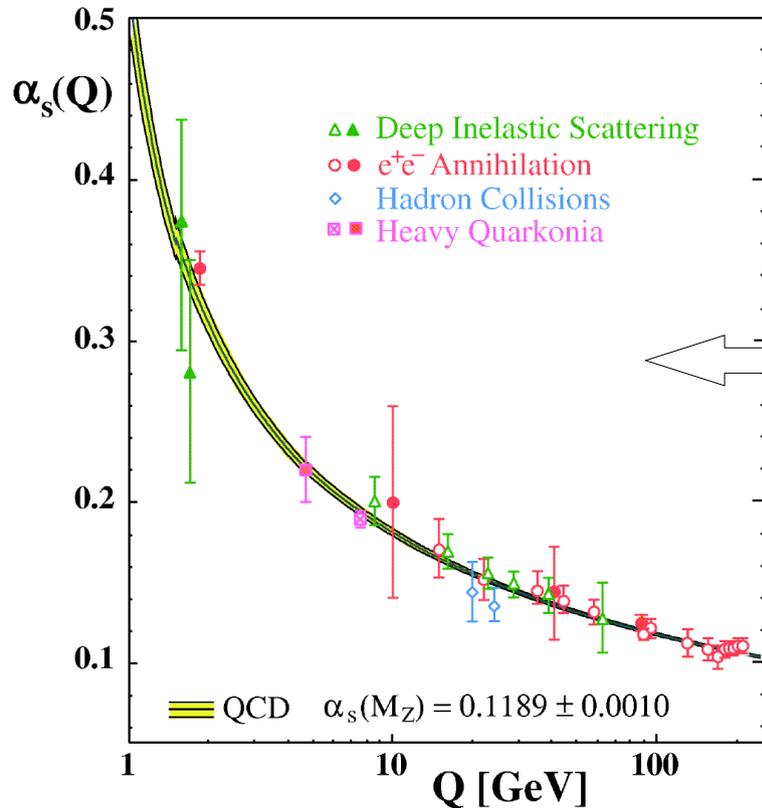
✘ Compatible with Bethke2004

✘ With competitive precision



sent to DIS05

World average



hep-ex/0606035

- ✗ The world averages used to include only incl. DIS data
- ✗ Brand new determination from Bethke incorporates the HERA average (with jets)

$$\alpha_s(m_Z) = 0.1189 \pm 0.0010$$

- ✗ Compare to 2004:

Bethke $\alpha_s(m_Z) = 0.1183 \pm 0.0027$

PDG $\alpha_s(m_Z) = 0.1187 \pm 0.002$

- ✗ Big improvement in uncertainty mainly due to new data: τ decays and lattice theory of heavy hadron masses
- ✗ After 30 years of QCD: better than 1%!

Summary

- ✗ Plenty of α_s determinations from **HERA** available
- ✗ The **precision** is competitive to e^+e^- annihilation analyses
- ✗ **Diversity** important to test universality of QCD
- ✗ Precision needed for QCD itself and for background predictions e.g. at **LHC**
- ✗ Still: theory at NLO induces large **theory errors**
- ✗ Looking forward to **NNLO** calculations on the way...
- ✗ ... and to fits to the wealth of **HERA II** data still to come!

 Nobelprize.org



The Nobel Prize in Physics 2004

“the discovery of asymptotic freedom
in the theory of the strong interaction”



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