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Jet cross sections in NC DIS
and measurement of α_s at HERA

Introduction
NC DIS Jet production
NLO pQCD vs. measurements
 α_s & its scale dependence
Summary & Outlook

The strong coupling constant: α_s

α_s is fundamental parameter of QCD

--> must be determined from experiment!

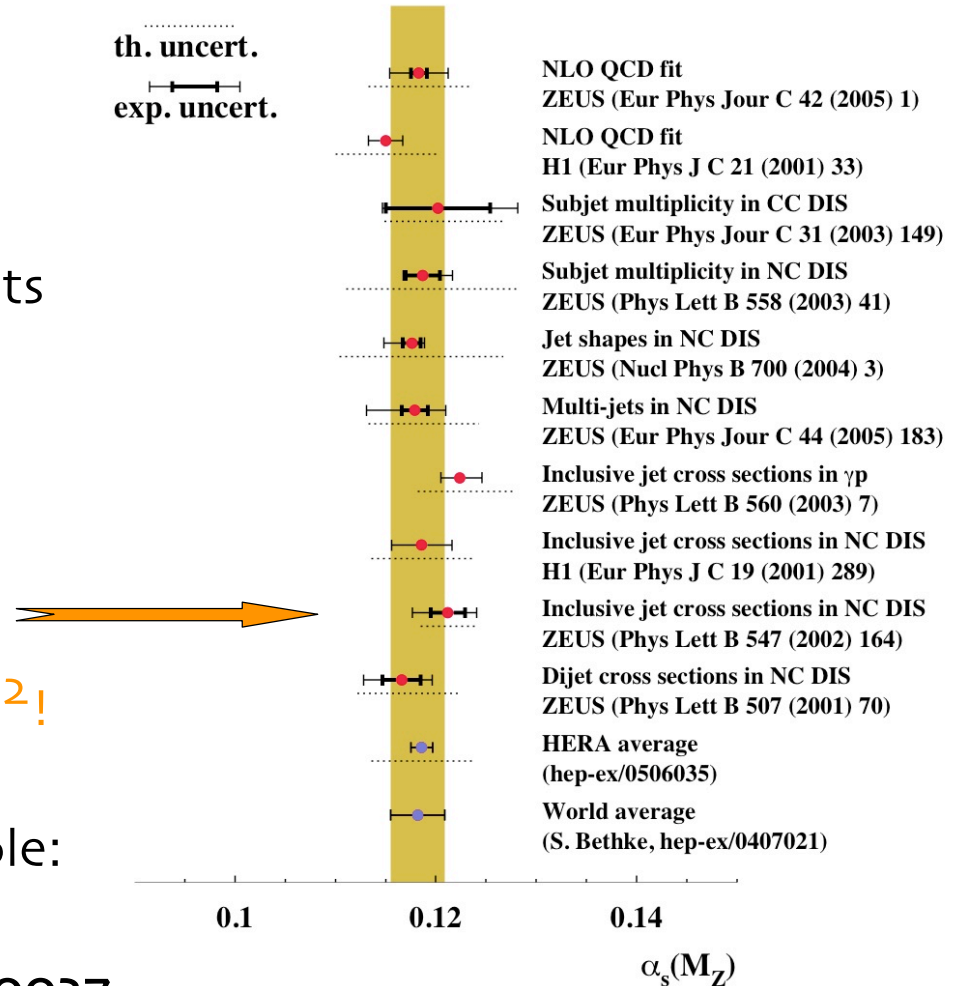
For precise determination:

- many measurements
- diverse phenomena
- HERA:** - internal structure of jets
 - structure functions
 - event shapes
 - jet cross sections

Inclusive jets yield smallest theoretical uncertainty at high Q^2 !

$\alpha_s(M_Z)$ measurements compatible:

- amongst themselves
- with world average: 0.1182 ± 0.0027



HERA: H1 and ZEUS experiments

HERA: $e^\pm p \rightarrow e'X$

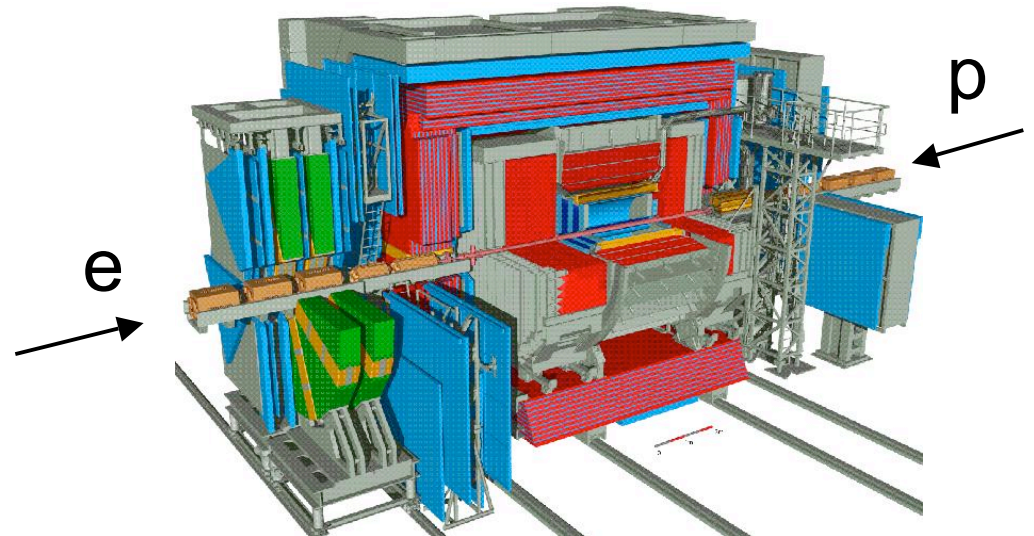
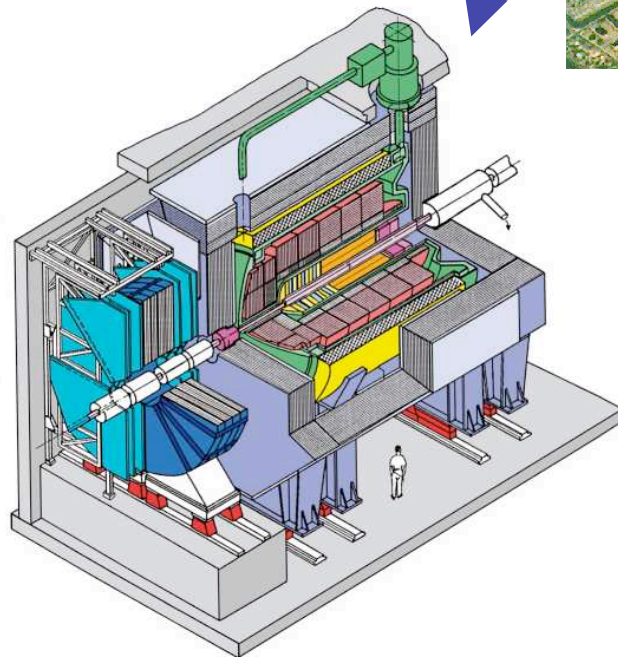
$e^\pm p$ cm energy

after(before) 1998:

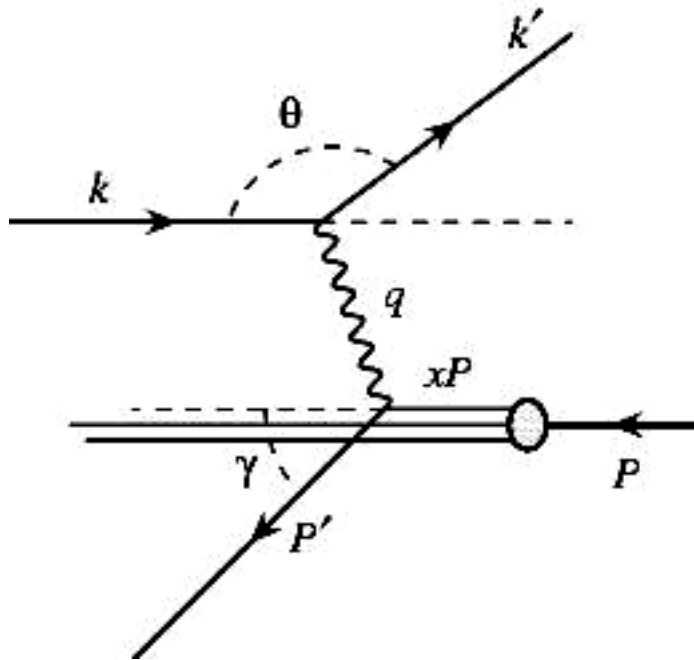
$\sqrt{S} = 318(300) \text{ GeV}$



DESY (Hamburg, Germany)



Deep Inelastic Scattering at HERA



Charged current: exchange of W^\pm

Neutral current: exchange of γ or Z^0

- Q^2 is the probing power
- x is the Bjorken scaling variable
- y is the inelasticity

$$Q^2 = -q^2 = -(k - k')^2$$

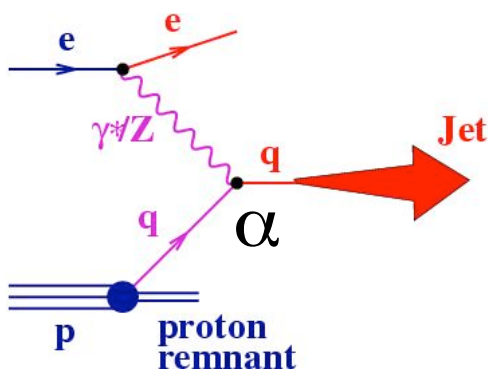
$$x = \frac{Q^2}{2p \cdot q} \quad y = \frac{p \cdot q}{p \cdot k}$$

$$s = (p + k)^2 \quad Q^2 = x \cdot y \cdot s$$

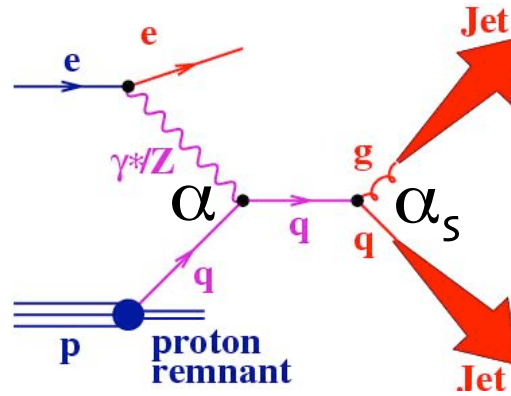
Jets in NC DIS at HERA

Jet production in NC DIS ($Q^2 \gg \Lambda_{\text{QCD}}^2$)

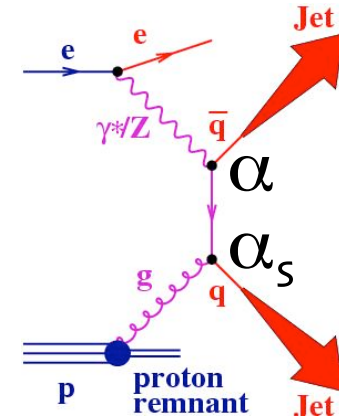
- at $O(\alpha_s)$, three diagrams contribute to jet production cross section



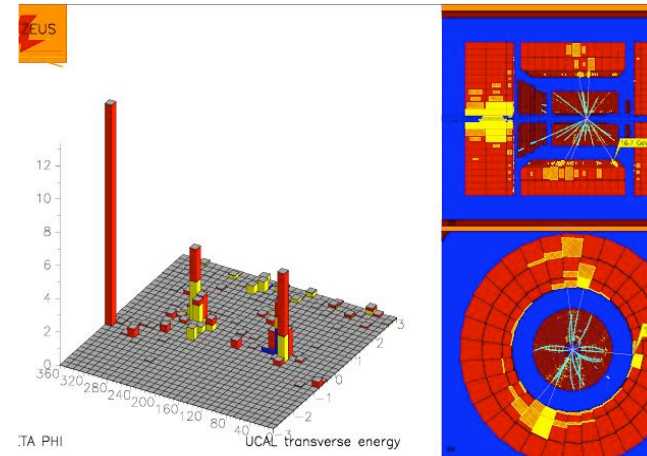
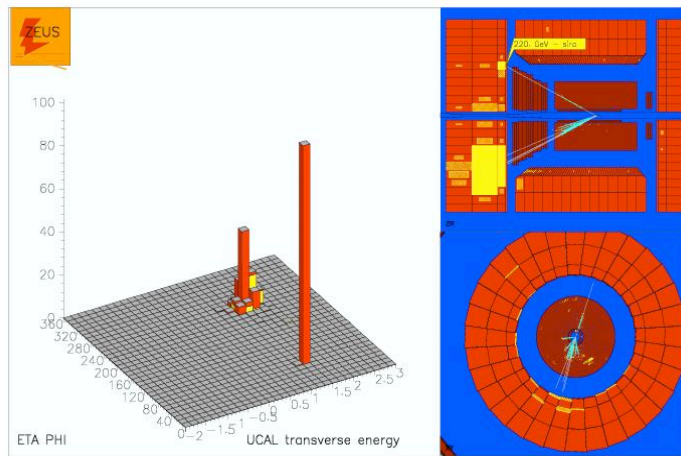
QPM $O(\alpha)$



QCD Compton $O(\alpha_s)$

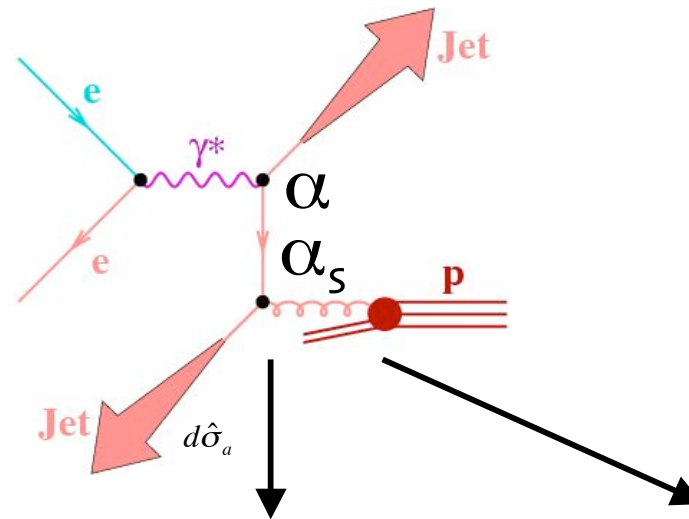


BGF $O(\alpha_s)$



Jets cross sections in NC DIS

Cross section for $ep \rightarrow e + \text{jet} + \text{jet} + X$ at high Q^2 :



$$d\sigma_{jet} = \sum_{a=q,\bar{q},g} \int dx d\hat{\sigma}_a(x, \alpha_s(\mu_R), \mu_R, \mu_F) f_a(x, \mu_F)$$

$d\hat{\sigma}_a$ is the subprocess cross section, calculable in pQCD

-> hard process (short-distance structure of interaction)

f_a are the experimentally determined Parton Distributions Functions

-> proton structure (long-distance structure of interaction)

Allows test of color dynamics, determination of α_s , test of proton PDFs

NLO Calculations of jet cross sections

Differential cross sections were calculated at $O(\alpha_s^2)$ by ZEUS (H1) with DISENT (NLOJET++). Ingredients needed for pQCD calculation:

- assume value of $\alpha_s(M_Z)$: 0.1175 (0.118) (α_s is calculated at 2 loops)
- assume parametrizations for proton PDFs:
 - MRST99 set (CTEQ5M1)
- choose hard scale:
 - Renormalization scale $\mu_R = E_{T,B}$ of jet
 - Factorization scale $\mu_F = Q$
- correct calculations for hadronization effects (calculations are for jets of partons and measurements are done at hadron level)

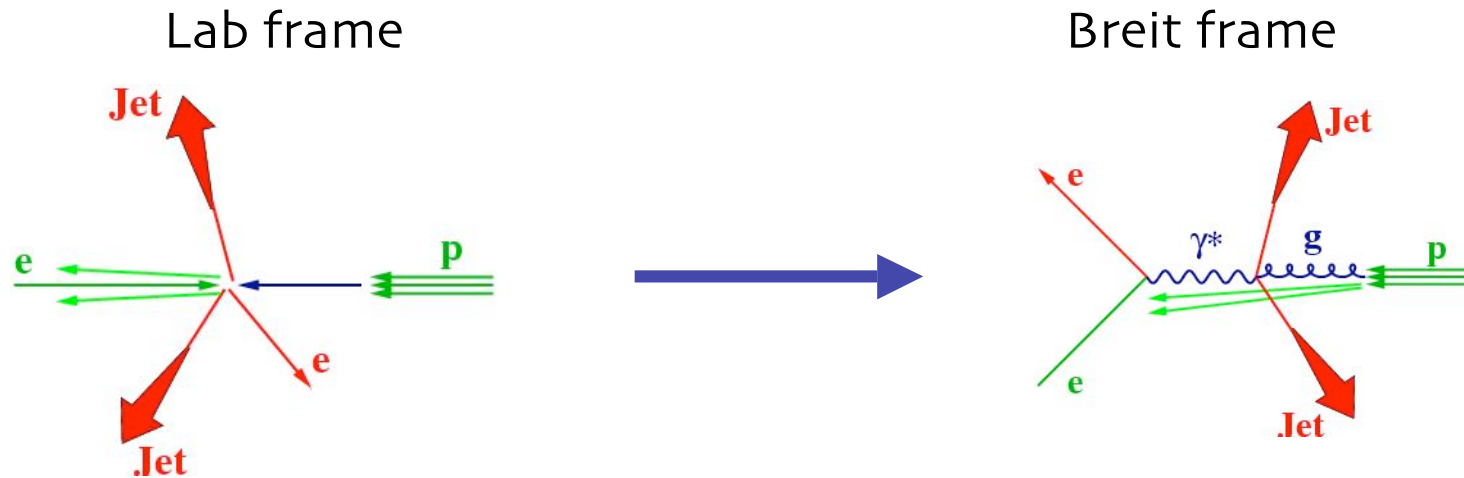
Contributions to the theoretical uncertainty:

- on value of $\alpha_s(M_Z)$: 0.1182 ± 0.0027
- on parametrizations of proton PDFs: w/40 sets of CTEQ6
- terms beyond NLO: variation of μ_R by factors of 2 & 1/2 (μ_F by 4 & 1/4)
- from hadronization corrections: use different LO QCD MCs

Jet search: The Breit Frame

Breit frame -> natural frame to measure NC DIS jet xs:

- suppression of QPM contribution (final state quark: negligible E_T)
- suppression of beam remnant jet (negligible E_T)
- lowest order non-trivial contributions: $\gamma^*g \rightarrow q\bar{q}$ and $\gamma^*g \rightarrow qg$



Jets are reconstructed in Breit frame using a K_T -cluster algorithm:

- invariant under longitudinal boosts
- xs predicted are infrared and collinear safe

$$d_{ij} = \min(E_T^i, E_T^j)^2 \times (d\eta_{ij}^2 + d\phi_{ij}^2)$$

Measurements of $d\sigma/dE_{T,B}(\text{jet})$: ZEUS

$d\sigma/dE_{T,B}(\text{jet})$ measurement vs. NLO prediction

Data:

98-00 $\rightarrow \mathcal{L} = 81.7 \text{ pb}^{-1}$

$Q^2 > 125 \text{ GeV}^2$

$E_{T,B}^{\text{jet}} > 8 \text{ GeV}$

$-2 < \eta_B^{\text{jet}} < 1.5$

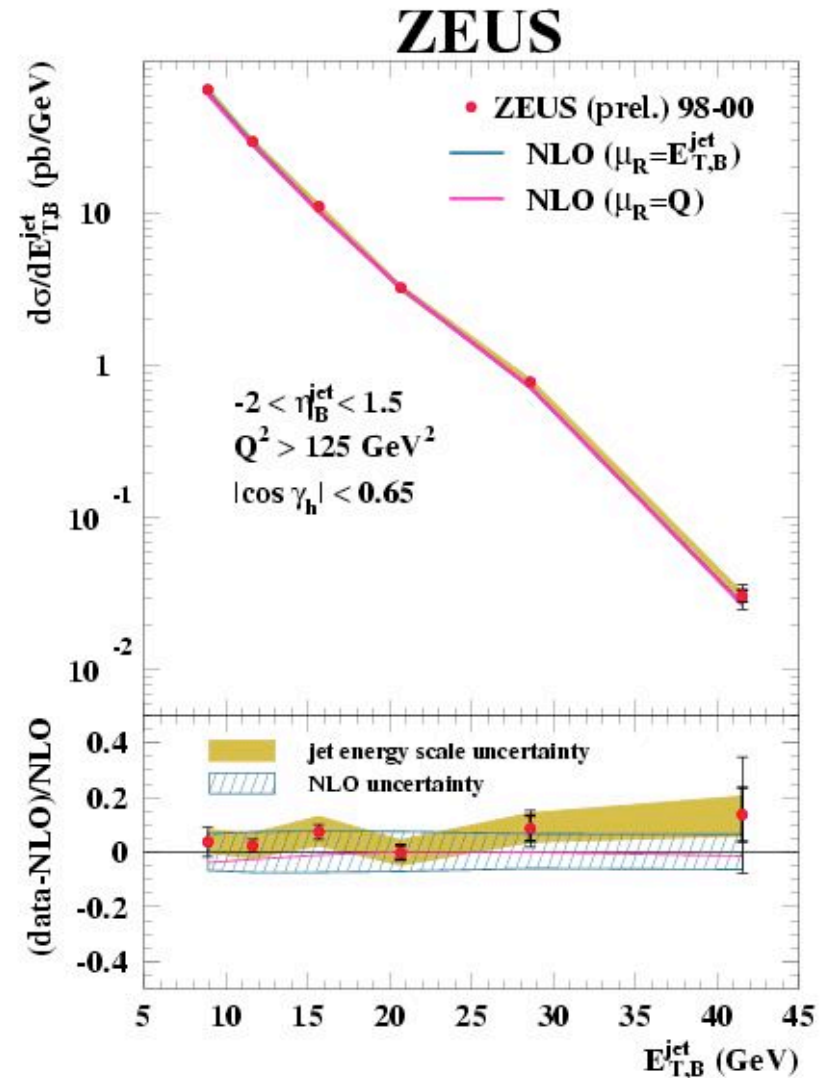
Measured inclusive jet cross sections are well described by predictions.

Experimental uncertainties on xs:

- jet energy scale ($\sim 5\%$)

Theoretical uncertainties on xs:

- terms beyond NLO ($\sim 5\%$)
- assumed value of α_s (4%)
- uncertainties on PDFs (3%)



Measurements of $d^2\sigma/dE_T dQ^2$: H1

$d^2\sigma/dE_T dQ^2$ measurement vs. NLO prediction

Data:

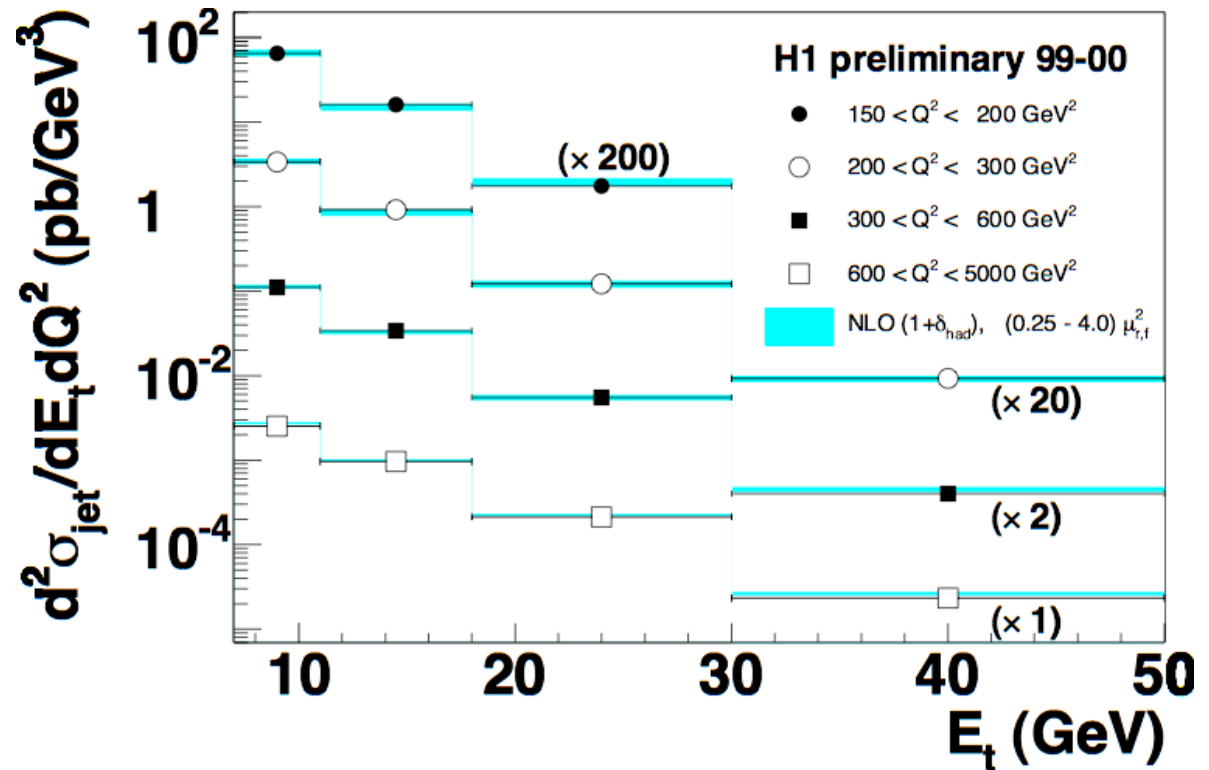
99-00 $\rightarrow \mathcal{L} = 61.25 \text{ pb}^{-1}$

Kinematic region:

$150 < Q^2 < 5000 \text{ GeV}^2$

$E_T^{\text{jet}} > 7 \text{ GeV}$

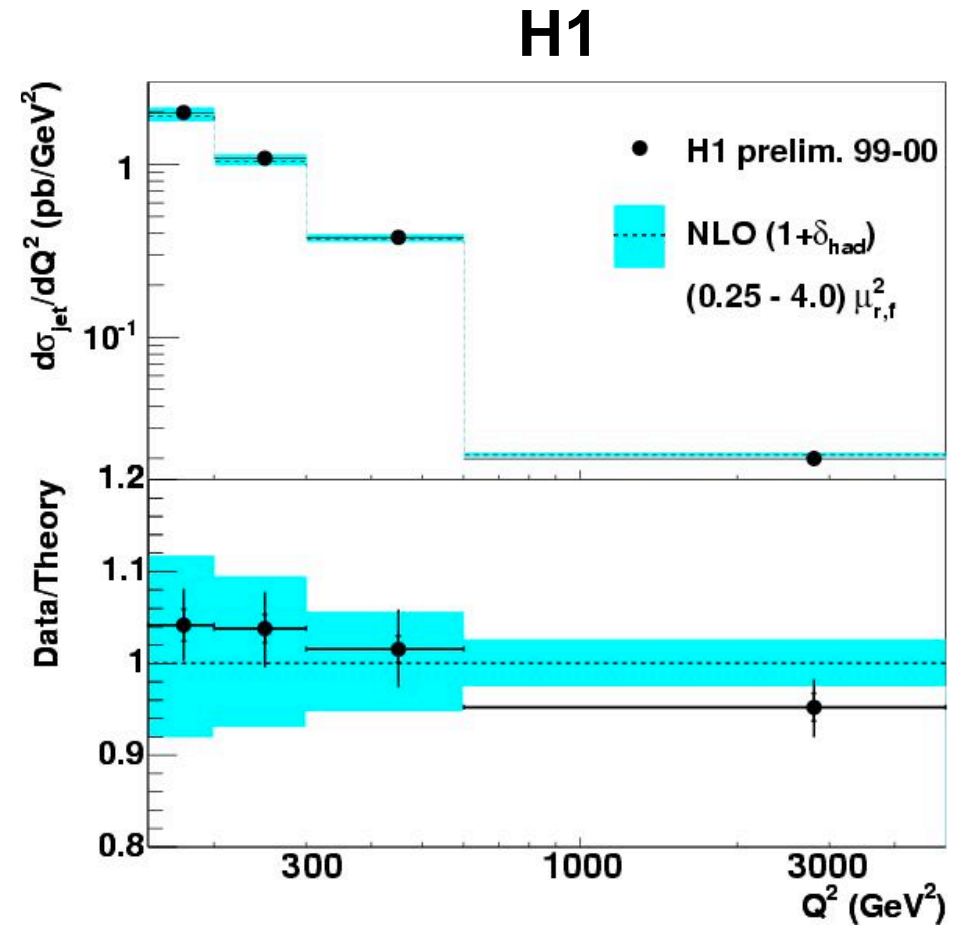
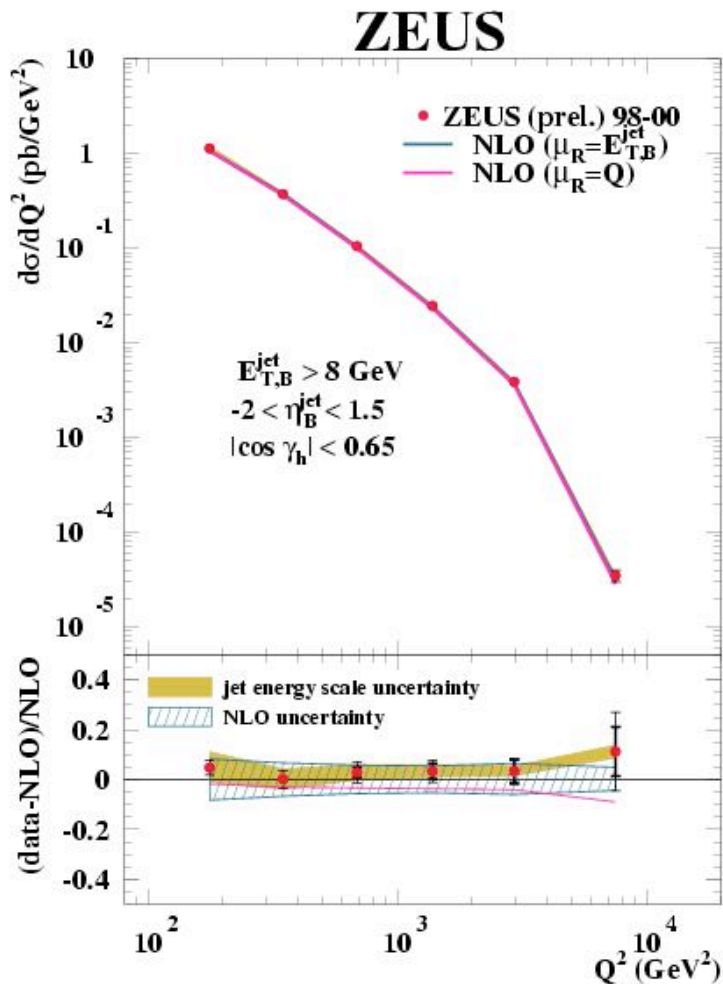
$-1 < \eta^{\text{lab}} < 2.5$



Measured inclusive jet cross sections are well described by predictions.

Measurements of $d\sigma/dQ^2$

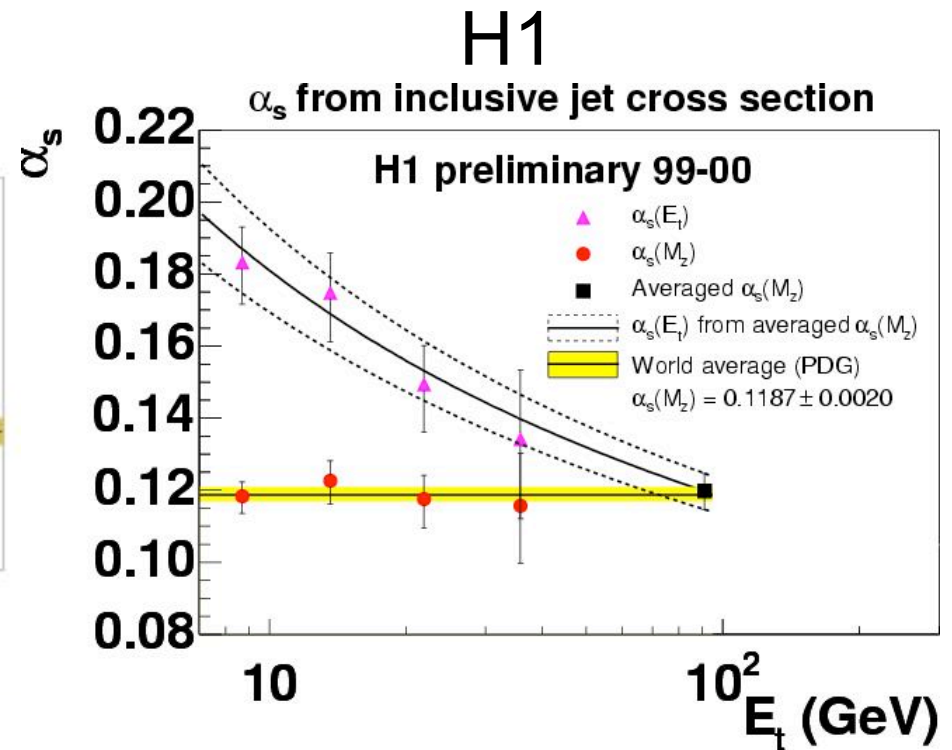
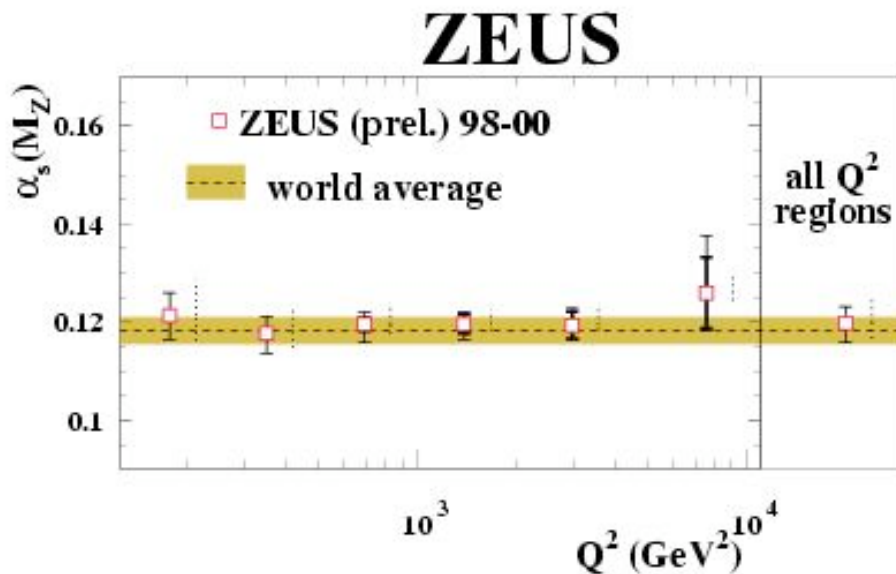
$d\sigma/dQ^2$ measurement vs. NLO prediction



Data are well described by NLO predictions.
 The theoretical uncertainties are higher at low Q^2 .

Measurement of $\alpha_s(M_Z)$

Values of α_s have been determined from the measured $d\sigma/dE_{T,B}(\text{jet})$ and $d\sigma/dQ^2$ cross sections:

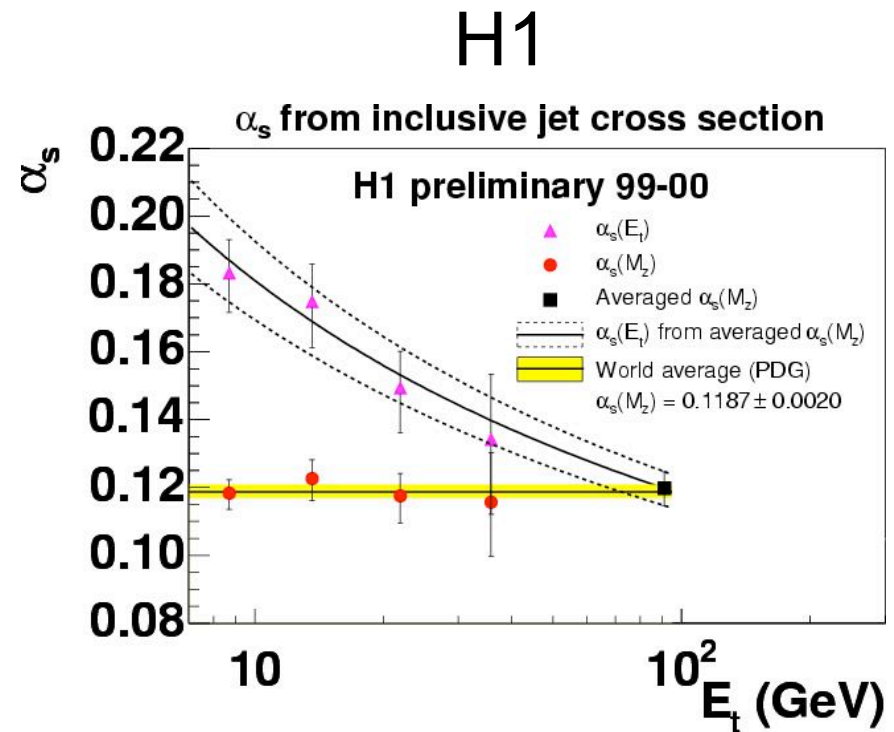
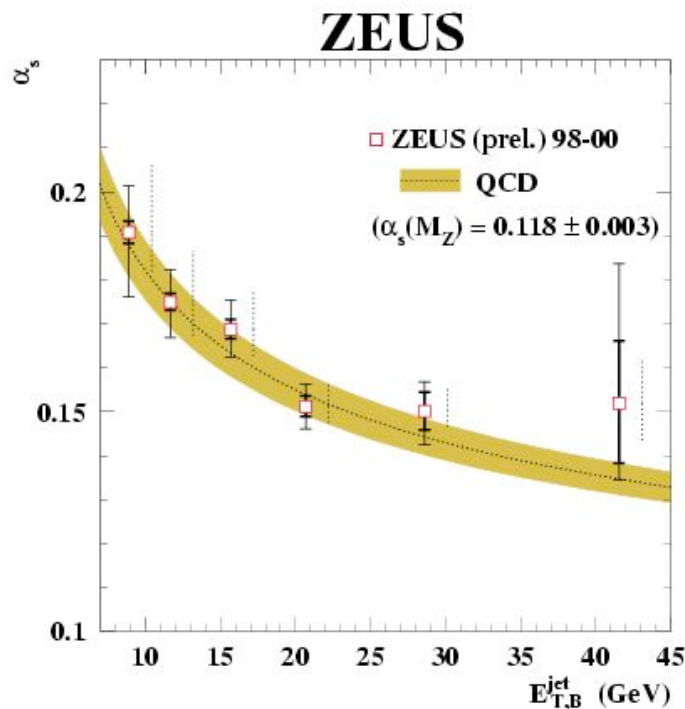


ZEUS: $Q^2 > 500 \text{ GeV}^2$: $\alpha_s(M_Z) = 0.1196 \pm 0.0006(\text{stat.})^{+0.0019}_{-0.0025}(\text{exp.})^{+0.0029}_{-0.0017}(\text{th.})$

H1: All E_T regions: $\alpha_s(M_Z) = 0.1197 \pm 0.0016(\text{exp.})^{+0.0046}_{-0.0048}(\text{th.})$

$\alpha_s(M_Z)$ and energy scale dependence

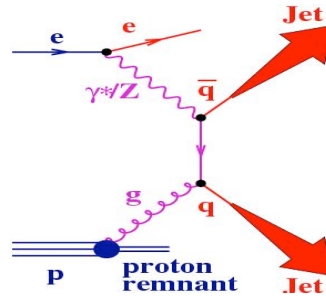
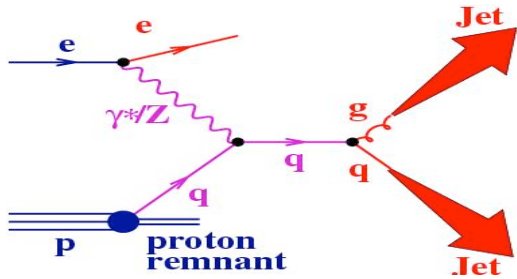
The measured $d\sigma/dE_{T,B}(\text{jet})$ and $d\sigma/dQ^2$ have been used to test the energy-scale dependence of α_s :



Measurement is in good agreement with the QCD predictions over a large range in Q and E_T .

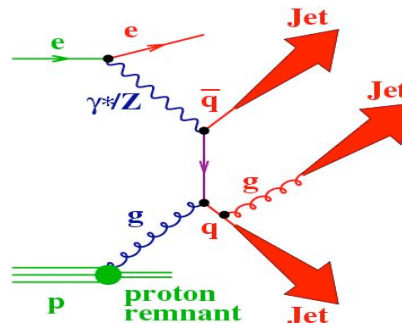
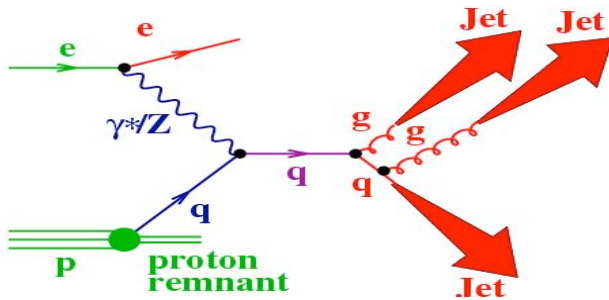
Multijet production in NC DIS at HERA

one- and two-jet events



$$O(\alpha_s)$$

three-jet events



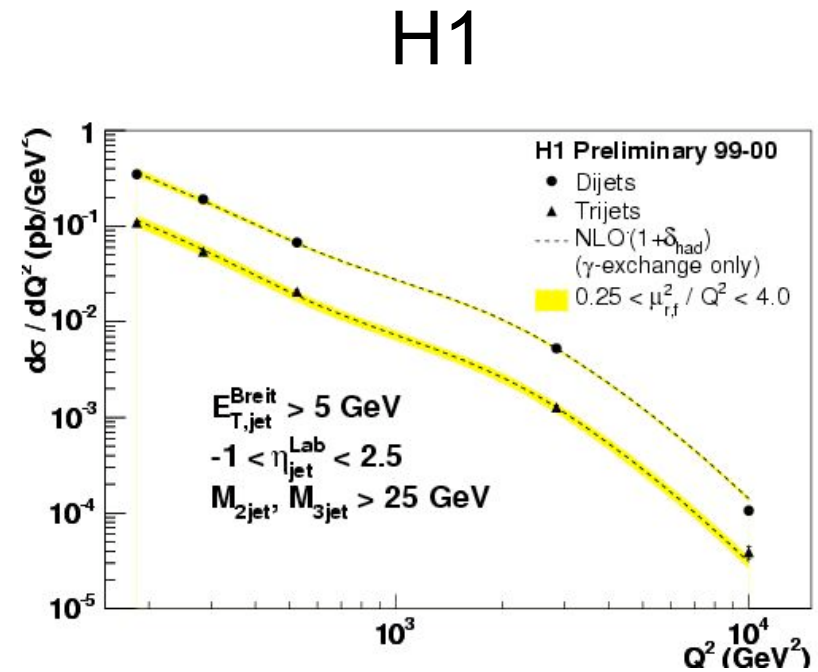
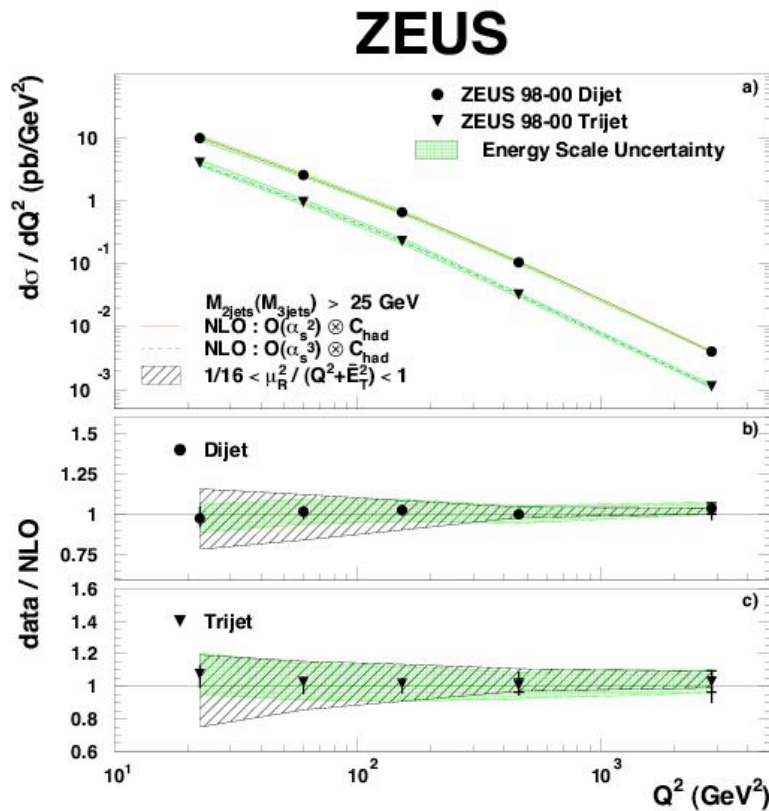
$$O(\alpha_s^2)$$

Three jet events are processes in which:

- gluon is radiated in final state
- splitting of a gluon into a $q\bar{q}$ pair

These events provide direct tests of pQCD beyond LO: $\sigma_{3\text{jets}} \propto O(\alpha_s^2)$

Dijet and trijet cross sections in NC DIS



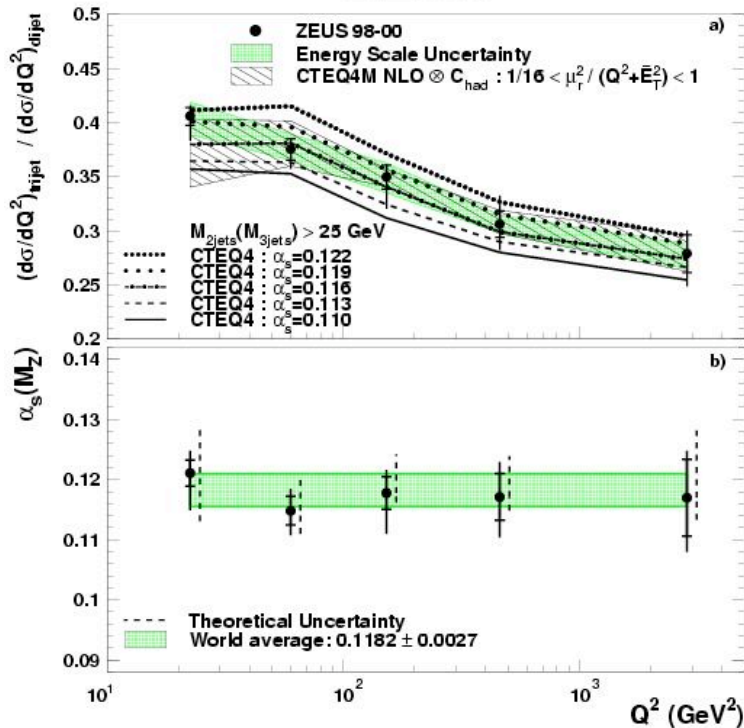
$M_{2jet}, M_{3jet} > 25$ GeV
 $10 < Q^2 < 5000$ GeV² $150 < Q^2 < 15000$ GeV²

Measured dijet and trijet cross sections
are well described by NLO predictions.

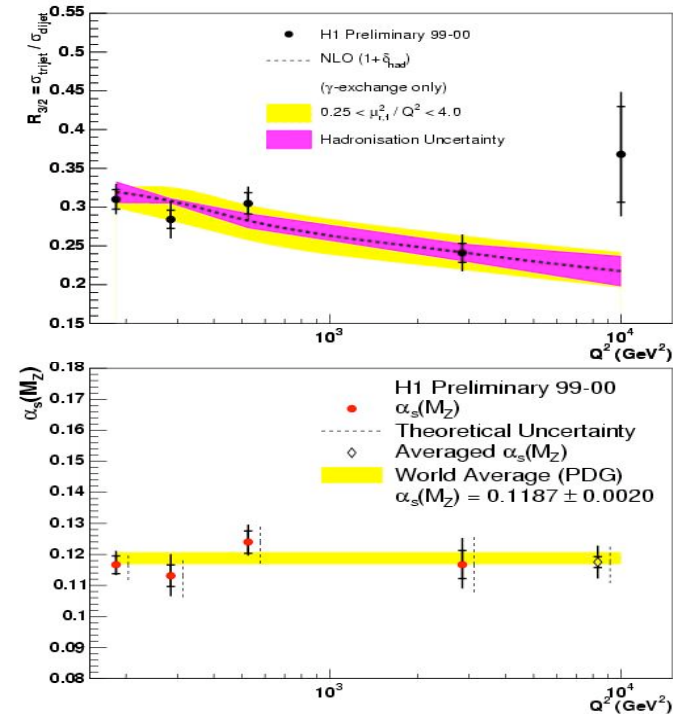
$\alpha_s(M_Z)$ from multijet cross sections

Ratio: experimental and theoretical uncertainties cancel out in the ratio
 ---> more accurate test of color dynamics

ZEUS



H1



$$\alpha_s(M_Z) = 0.1179 \pm 0.0013(\text{stat.})^{+0.0028}_{-0.0046}(\text{exp.})^{+0.0064}_{-0.0046}(\text{th.}) \quad \alpha_s(M_Z) = 0.1175 \pm 0.0017(\text{stat.}) \pm 0.0050(\text{exp.})^{+0.0054}_{-0.0068}(\text{th.})$$

Ratio yields precise measurements at LOW Q^2 .

Summary

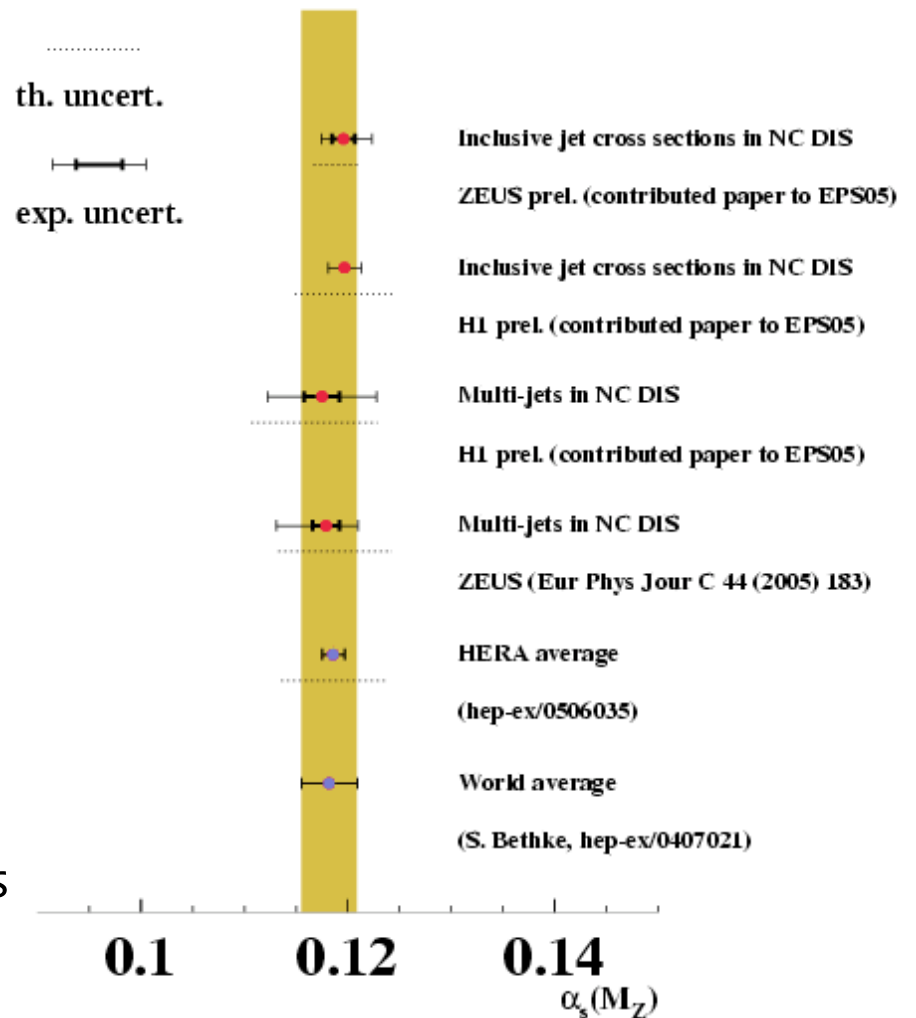
HERA is a unique machine for testing QCD:

Precise measurements of α_s have been made. The measurements agree:

- with one another
- with the world average:
 0.1182 ± 0.0027
- with the HERA average:
 $0.1186 \pm 0.0011(\text{exp}) \pm 0.0050(\text{th})$

However, limited by theoretical uncertainties at lower Q^2

The energy-scale dependence of α_s has been tested -> in agreement with the running of α_s as predicted by QCD

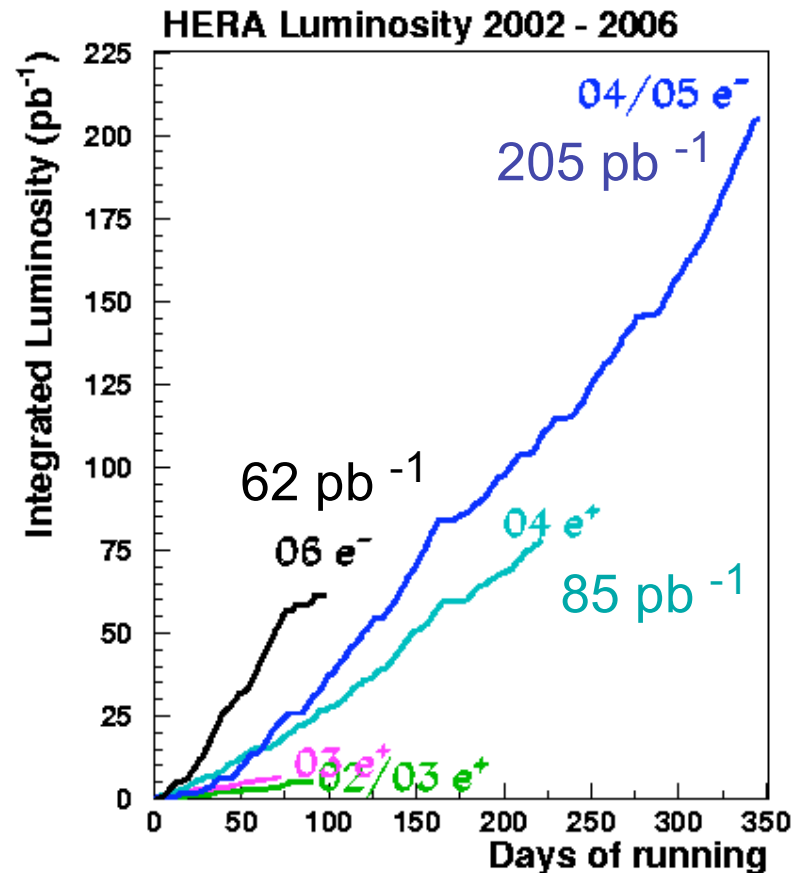


Outlook

Analyses presented here
use HERA I luminosity

HERA II phase:

- Luminosity delivered $> 350 \text{ pb}^{-1}$
- higher statistics allow (even) more precise measurements
---> especially at higher Q^2/E_T where the theoretical uncertainties are smaller.



Bkp: Measurements of $\alpha_s(M_Z)$

$\alpha_s(M_Z)$ values:

- determined from $d\sigma/dE_{T,B}(\text{jet})$ and $d\sigma/dQ^2$ cross sections
- combined fits to single $\alpha_s(M_Z)$ value

ZEUS

- for all $E_{T,B}$ (jet) regions:

$$\alpha_s(M_Z) = 0.1201 \pm 0.0006(\text{stat.})_{-0.0038}^{+0.0033} (\text{exp.})_{-0.0032}^{+0.0049} (\text{th.})$$

- for all Q^2 regions:

$$\alpha_s(M_Z) = 0.1198 \pm 0.0006(\text{stat.})_{-0.0039}^{+0.0034} (\text{exp.})_{-0.0033}^{+0.0049} (\text{th.})$$

- for $Q^2 > 500 \text{ GeV}^2$ (smallest uncertainties):

$$\alpha_s(M_Z) = 0.1196 \pm 0.0006(\text{stat.})_{-0.0025}^{+0.0019} (\text{exp.})_{-0.0017}^{+0.0029} (\text{th.})$$

H1

- for all E_T regions:

$$\alpha_s(M_Z) = 0.1197 \pm 0.0016(\text{exp.})_{-0.0048}^{+0.0046} (\text{th.})$$