

# Measurement of forward jet production at low $x$ in DIS

on behalf of the

H1 collaboration

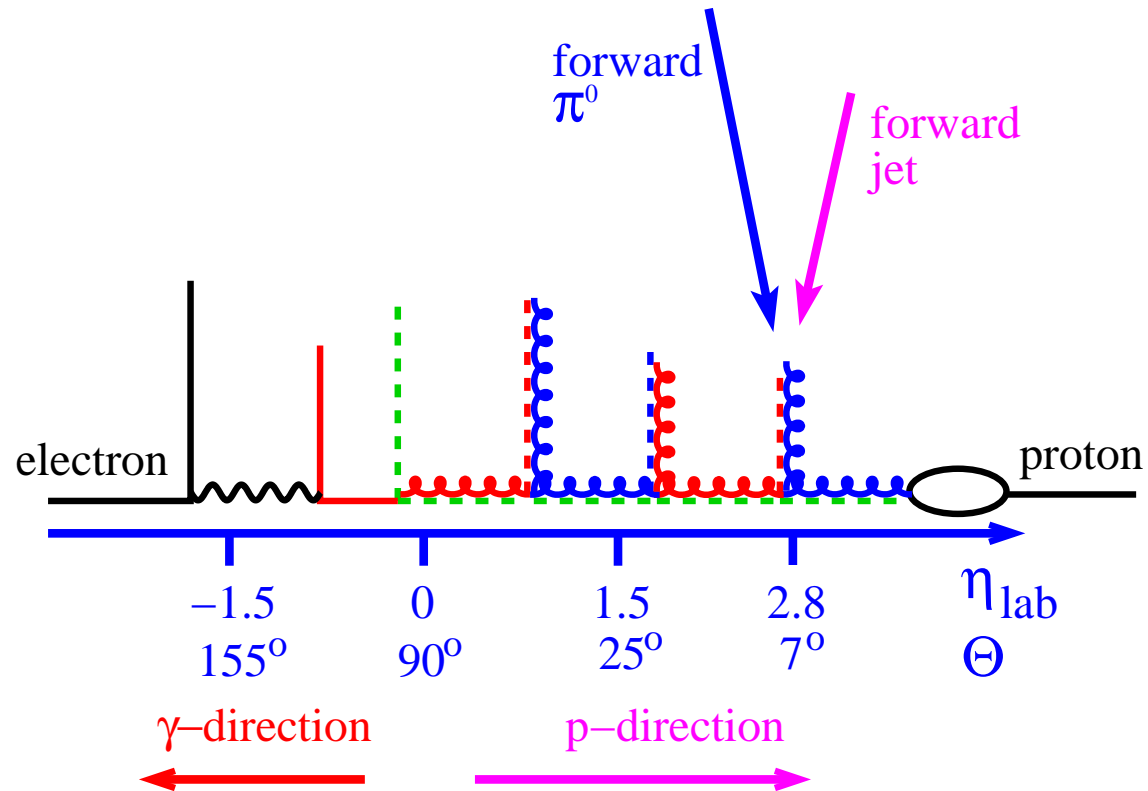
DIS 2005, Madison USA

Albert Knutsson, University of Lund

## Outline

- Why is the forward region important?
- Forward jet selection
- Theoretical Calculations / MC Models
- Results
- Conclusions

# Why Forward?



$F_2$  - very **inclusive** - very well described by DGLAP.

Dijet cross-section, Jet Rates - measure **hard** subsystem.

Energetic jet/particle in forward region - information on **full evolution ladder**.

# Physics motivation, continued...

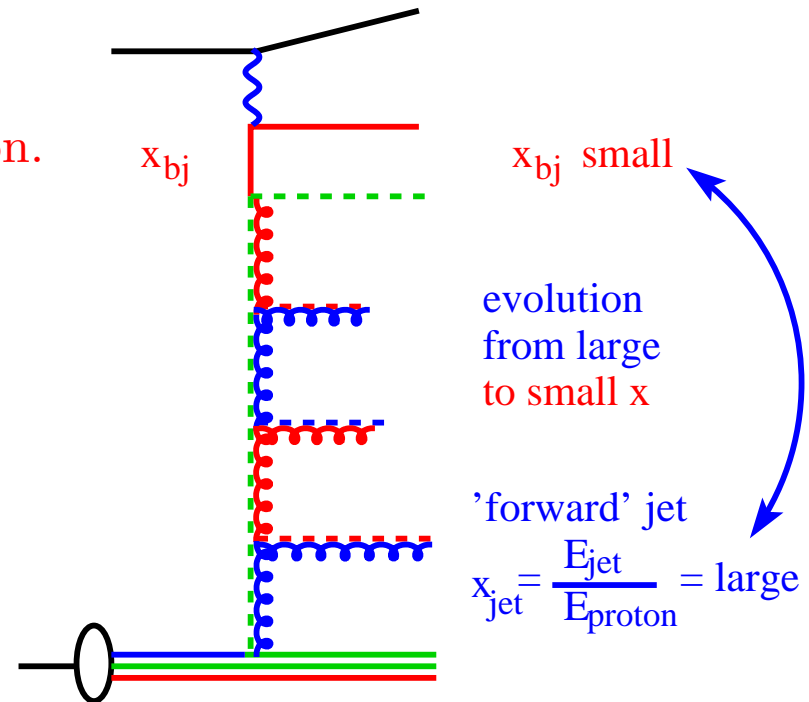
Test QCD at small  $x$ .

Signals of parton dynamics beyond DGLAP?

Events with energetic jet in the forward region.

Target phase space for evolution in  $x$   
(BFKL)  
 $x_{jet} \gg x_{Bj}$ .

Suppress phase space for evolution in  $Q^2$ .  
(Suppress DGLAP)  
 $p_{t, forward\ jet}^2 \sim Q^2$ .



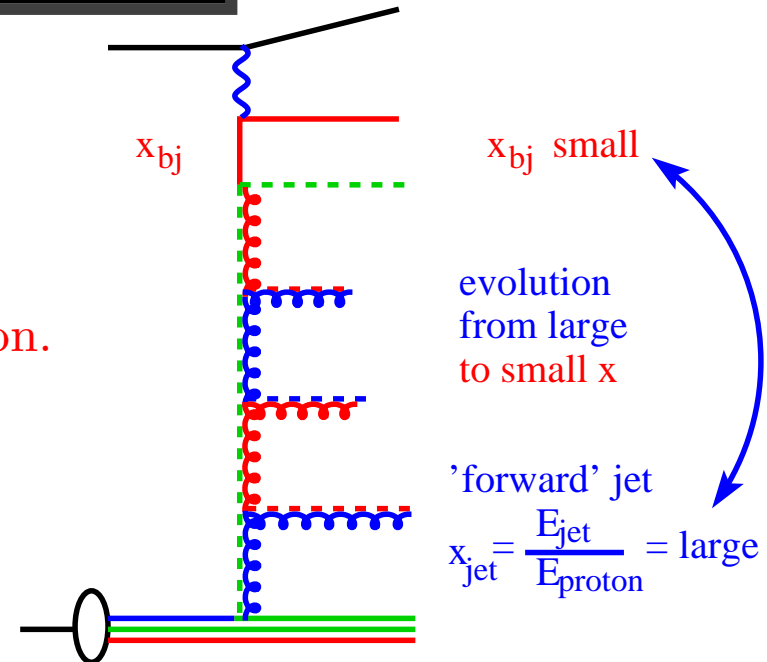
# Forward Jets

Jet algorithm: Inclusive  $k_t$ -algorithm

Events with energetic jet in the forward region.

Target phase space for evolution in  $x$ .

Suppress phase space for evolution in  $Q^2$ .



Forward jet

$$1.74 < \eta_{jet} < 2.79$$

$$p_t > 3.5 \text{ GeV}$$

Suppress QPM

$$x_{JET} = \frac{E_{JET}}{E_p} > 0.035$$

Suppress DGLAP

$$0.5 < \frac{p_t^2}{Q^2} < 5$$

If  $N_{\text{forward jet}} > 1 \rightarrow$  Most forward jet is selected

# Kinematic range and Measurements

## Kinematic range

$$5 < Q^2 < 85 \text{ GeV}^2$$

$$0.1 < y < 0.7$$

$$0.0001 < x_{Bj} < 0.004$$

$$10 \text{ GeV} < E'_e$$

## Measurements

Forward jet cross-sections

$$\frac{\frac{d\sigma}{dx_{Bj}}}{d^3\sigma} \\ \frac{d^3\sigma}{dx_{Bj} dp_t^2 dQ^2}$$

2+Forward jet cross-sections,  $\frac{d\sigma}{d\Delta\eta_2}$

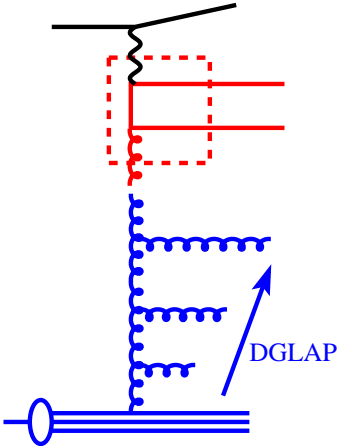
As a function of the **rapidity**

between the **forward jet** and

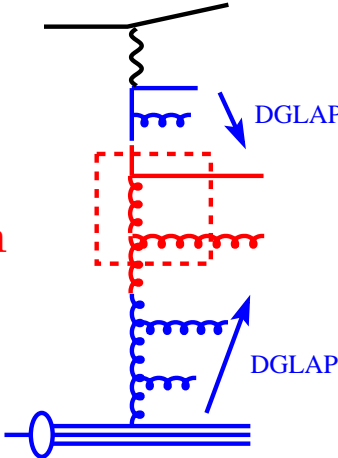
the **most forward di-jet**.

# QCD Models

RAPGAP: LO ME+PS: **DGLAP** evolution  
 where the parton ladder is strongly **ordered**  
 in  $Q^2$  and  $k_t^2$ .



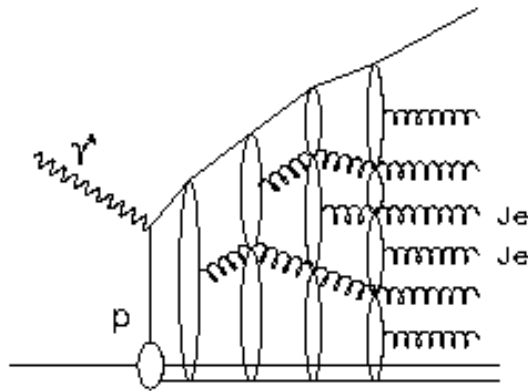
RAPGAP RES  $\gamma$ : RAPGAP with an **additional DGLAP** evolution  
 parton ladder from the **hard subsystem** to the photon.



PDF: CTEQ6L ,  $\gamma$ PDF: SaS1D Scales:  $\mu_r^2 = \mu_f^2 = Q^2 + p_t^2$

## QCD Models continue...

CDM (ARIADNE): LO ME (QPM, BGF). Color Dipole Model (QCDC and higher orders). Random walk in  $k_t$ .

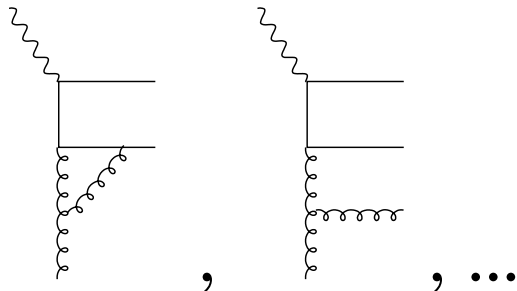


PDF: CTEQ6L

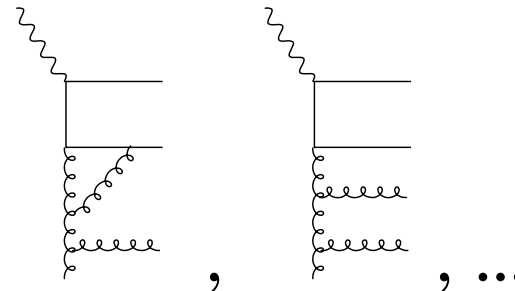
CASCADE: LO ME. Initial state CCFM partons showers with emissions ordered in angle.

# Fixed Order Calculations

DISENT: NLO di-jet ( $\alpha_s^2$ ).  
(Forward jet cross-sections.)



NLOJET++: NLO 3-jet ( $\alpha_s^2$ ).  
(2+forward jet cross-sections.)

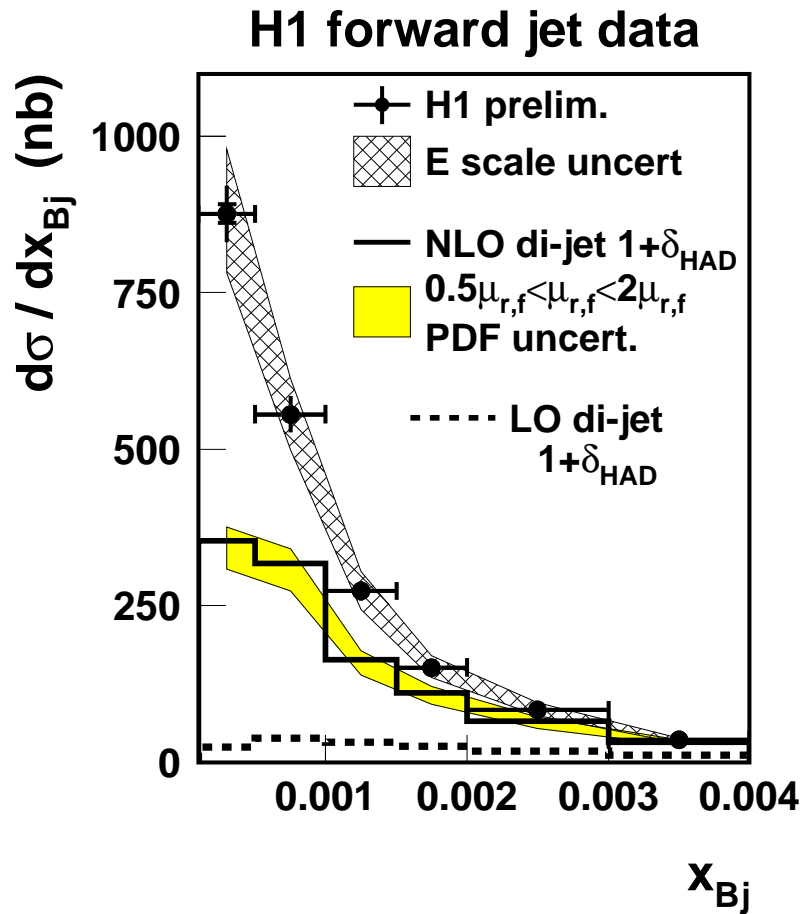


(Need to correct for hadronization effects.)



$$\frac{d\sigma}{dx_{Bj}}$$

## Comparison to Exact Calculations (DISENT)



$$\mu_r^2 = p_t^2$$

$$\mu_f^2 = \langle p_{t, fwdjet}^2 \rangle = 45 \text{ GeV}^2$$

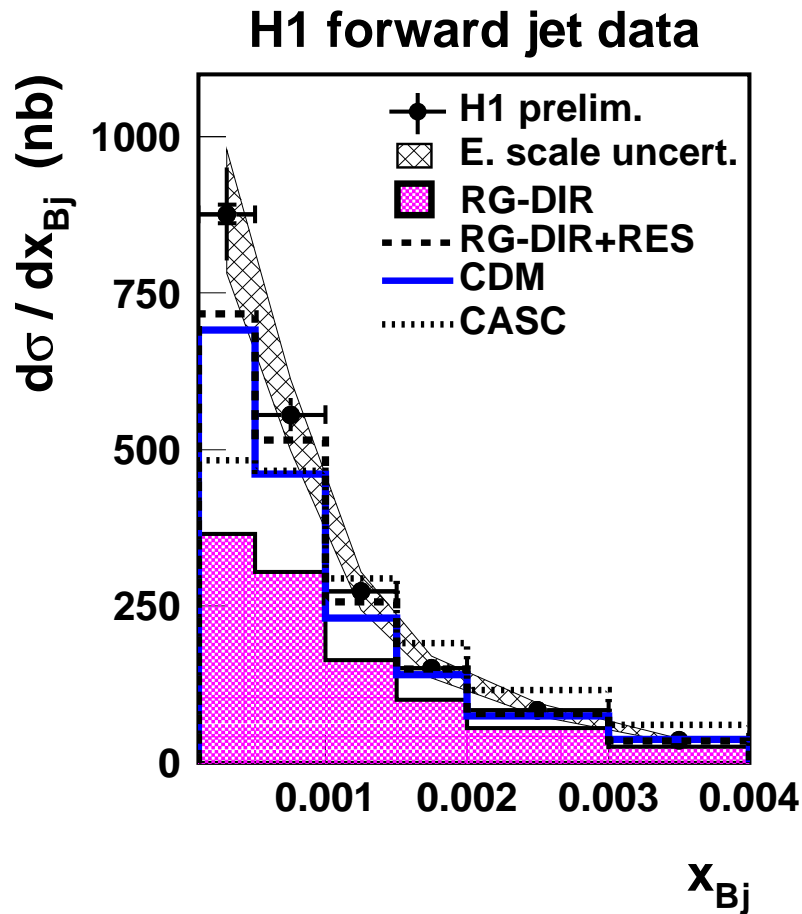
$$0.25\mu_{r,f}^2 < \mu_{r,f}^2 < 4\mu_{r,f}^2$$

PDF: CTEQ6M

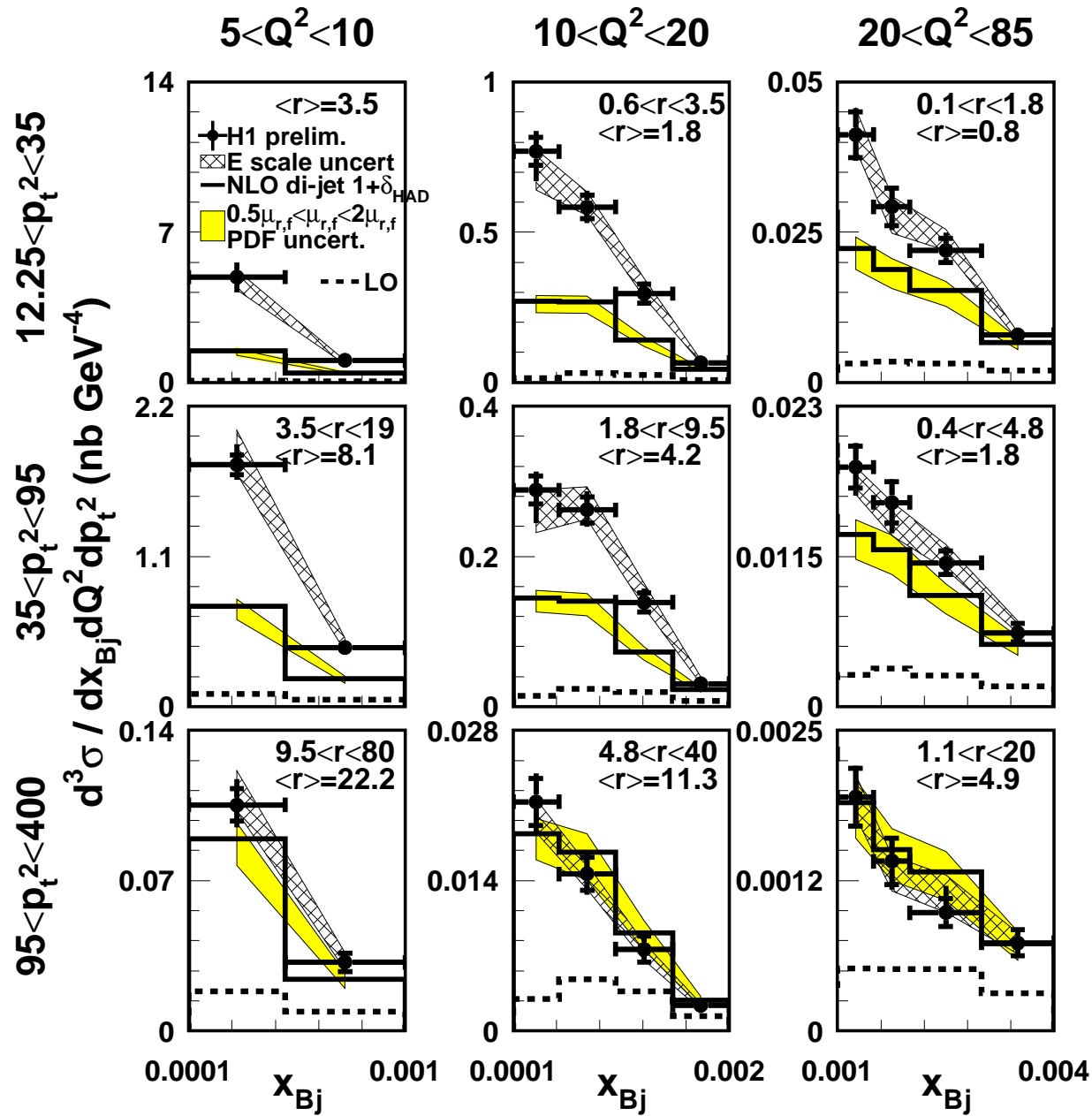
- NLO di-jet ok for larger  $x_{Bj}$ .
- LO contribution ( $\alpha_s$ )  $\ll$  NLO contribution ( $\alpha_s^2$ )

$$\frac{d\sigma}{dx_{Bj}}$$

## Comparison to QCD Models



- PS with DGLAP evolution similar to NLO.
- RG DIR+RES best.
- CDM and RG DIR+RES too low for lower  $x_{Bj}$ .
- CASCADE too low at lower  $x_{Bj}$ , too high at higher  $x_{Bj}$ .
- All models too low in lowest  $x_{Bj}$ -bin.



$$\frac{d^3 \sigma}{dx_{Bj} dp_t^2 dQ^2}$$

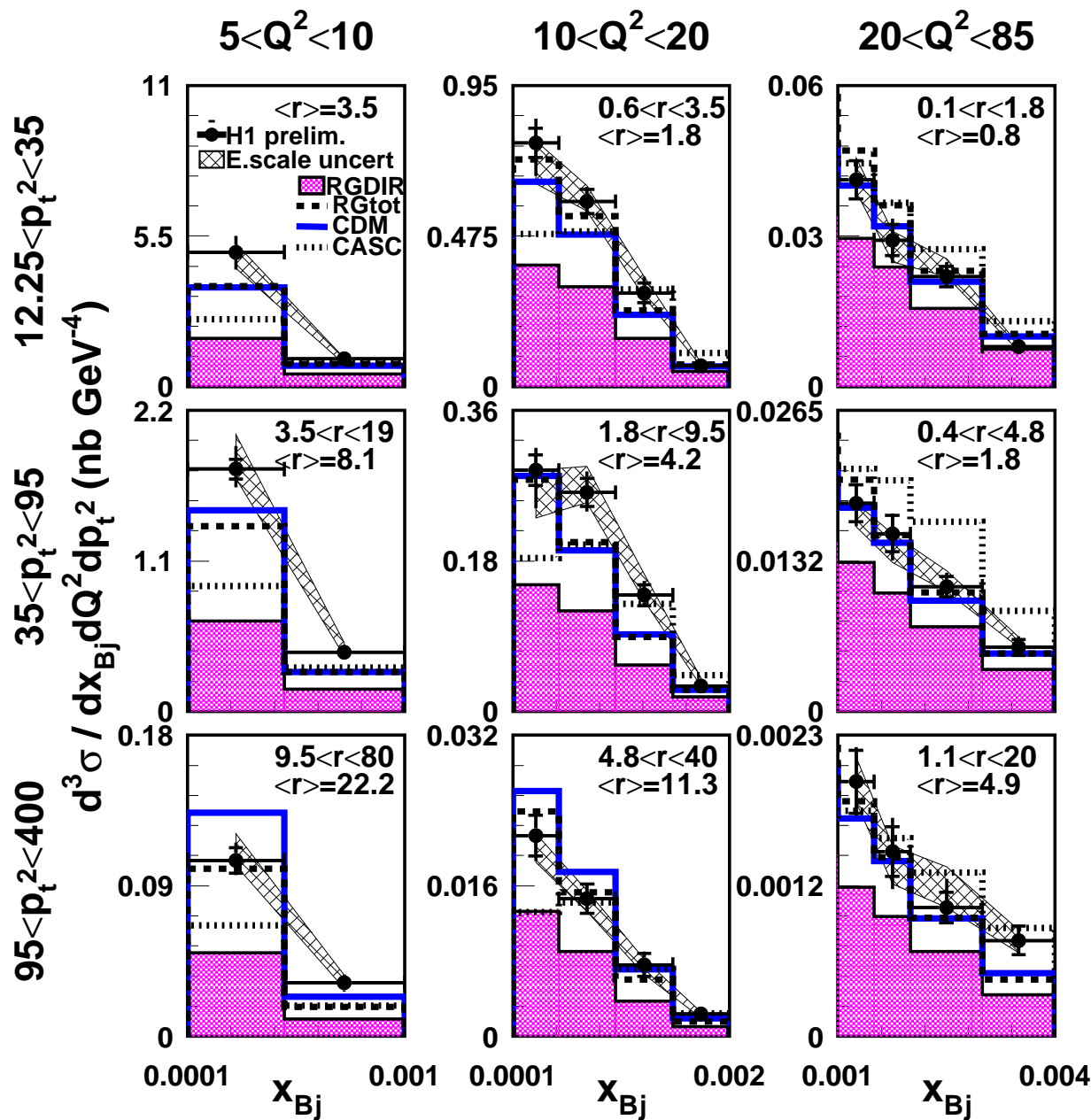
Cross-section as a function of  $x_{Bj}$  in  $3 \times 3$   $p_t^2$ - $Q^2$  bins. No  $\frac{p_t^2}{Q^2}$ -cut.  
 (Different regions in  $\frac{p_t^2}{Q^2} = r$ .)

Large  $x_{Bj}$ ,  $Q^2$  and  $p_t^2 \Rightarrow$   
 NLO describes data

Smaller  $x_{Bj}$ ,  $Q^2$  and  $p_t^2 \Rightarrow$   
 NLO insufficient

Note different ranges in  $x_{Bj}$ !

$$\mu_r^2 = p_t^2, \quad \mu_f^2 = \langle p_{t, \text{fwdjet}}^2 \rangle = 24, 55 \text{ resp. } 183 \text{ GeV}^2$$



$$\frac{d^3 \sigma}{dx_{Bj} dp_T^2 dQ^2}$$

Comparison to QCD models.

$p_T^2 < Q^2$  ( $r < 1$ )-

DGLAP-like dynamics

$p_T^2 \sim Q^2$  ( $r \sim 1$ )-

BFKL-like dynamics

$p_T^2 > Q^2$  ( $r > 1$ )-

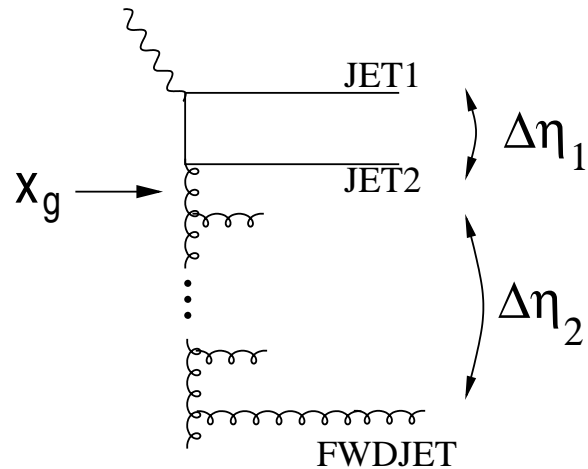
resolved  $\gamma$ -like dynamics

- RAPGAP DIR - fails, but is closest to the data in the most DGLAP like region
- RAPGAP DIR+ RES  $\gamma$  - Good
- CDM - Alright, but problems in res.  $\gamma$  region.
- CASCADE - Goes in the right direction.

## 2+forward jet cross-section, $\frac{d\sigma}{d\Delta\eta_2}$

Select **two hardest jets** ( $p_t > 6$  GeV) JET1 and JET2 -  
in addition to the forward jet ( $p_t > 6$  GeV) - **2+Forward  
Jet Event**. (No  $\frac{p_t^2}{Q^2}$ -cut.)

$$\eta_e < \eta_{JET1} < \eta_{JET2} < \eta_{FWDJET}$$

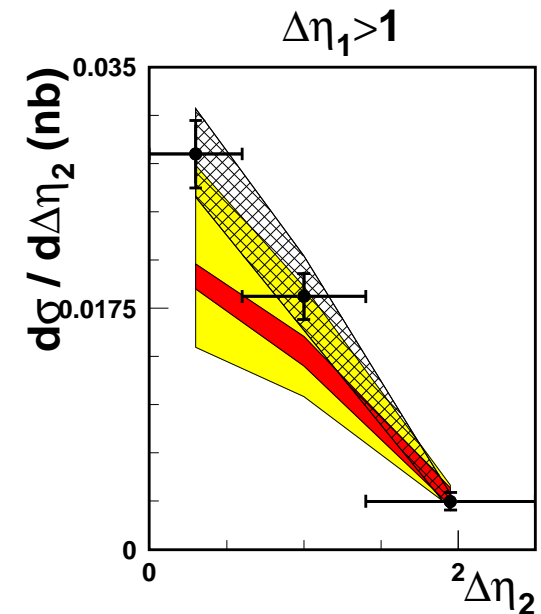
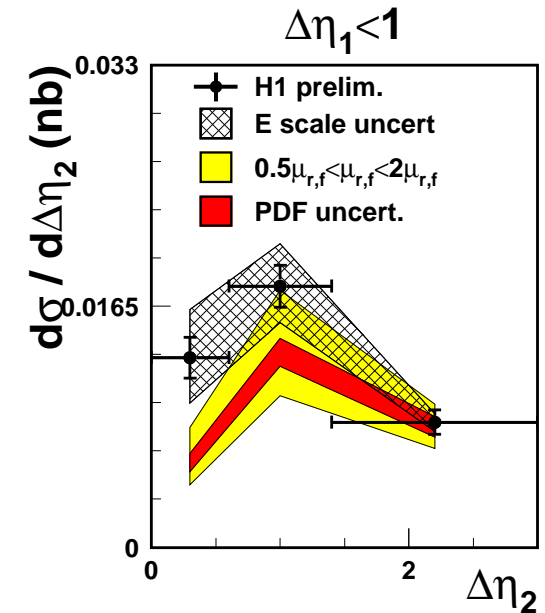


$$\Delta\eta_1 = \eta_{JET2} - \eta_{JET1}$$

$$\Delta\eta_2 = \eta_{FWDJET} - \eta_{JET2}$$

$\Delta\eta_1 < 1$ : small  $\eta$  separation between the two hard jets - small  $x_g$  - room for many emissions - long ladder favoured

$\Delta\eta_1 > 1$ : large  $\eta$  separation between the two hard jets - Shorter parton ladder

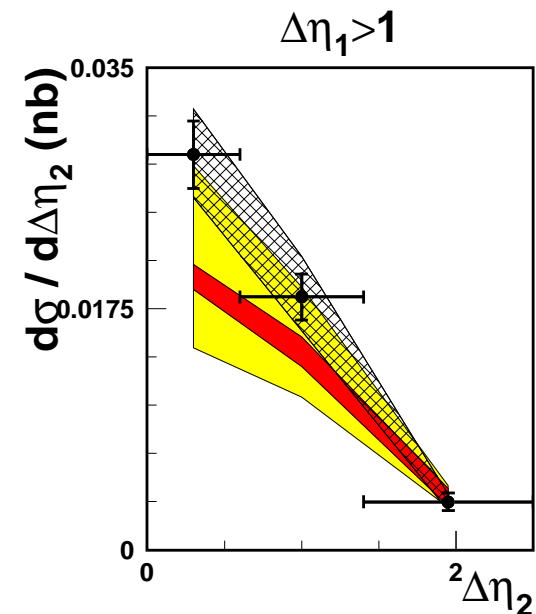
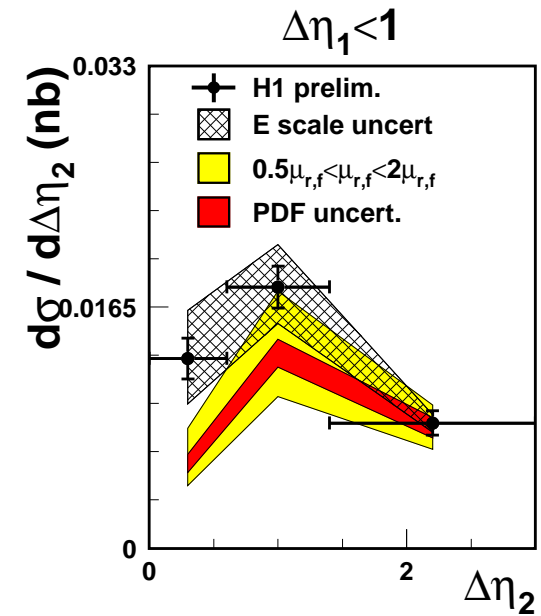


2+forward jet cross-section  
 NLO 3-jet  $1 + \delta_{had}$  calculations  
 (NLOJET++)

$$\mu_r^2 = \mu_f^2 = \frac{p_{t,JET1}^2 + p_{t,JET2}^2 + p_{t,FWDJET}^2}{3}$$

$$0.25\mu_{r,f}^2 < \mu_{r,f}^2 < 4\mu_{r,f}^2$$

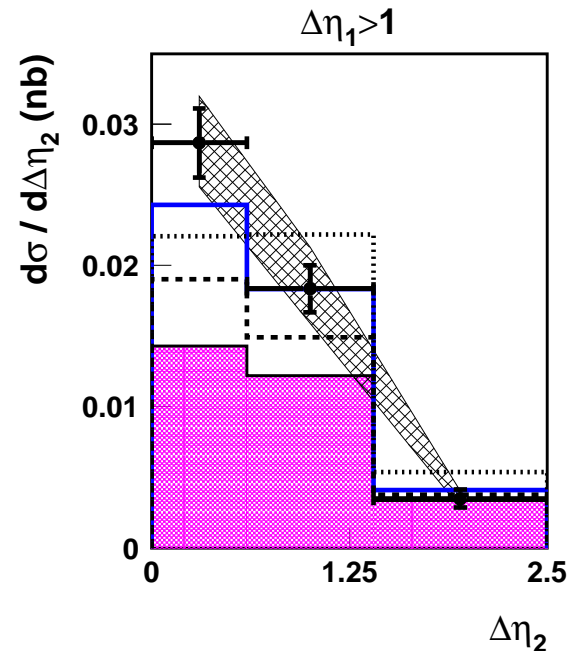
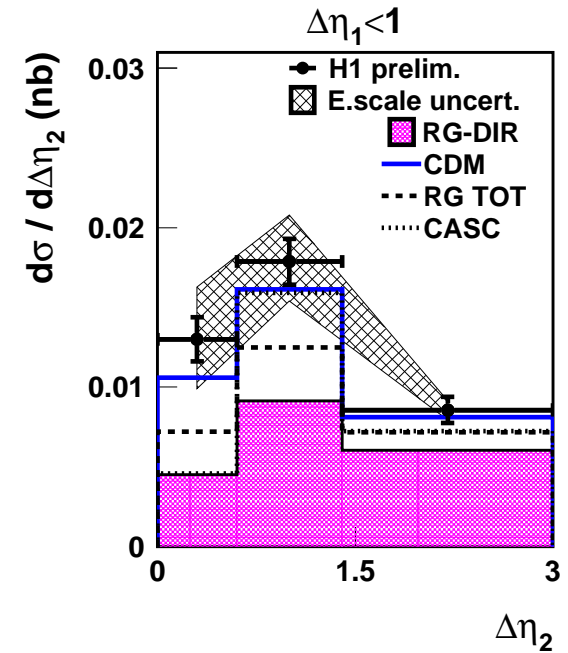
Data within scale uncertainty  
 for  $\Delta\eta_1 > 1$  ("short ladder"-region)



## 2+forward jet cross-section, $\frac{d\sigma}{d\Delta\eta_2}$

### QCD Generators

- CDM close to describe the data.
- CASCADE closer to data than RG-DIR
- ME+PS fails, except for at high  $\Delta\eta_2$  where  $\Delta\eta_1 > 1$  (the "non-BFKLish"-region), as is the case for the resolved photon model.



## Conclusions - Forward Jet Measurement

- Large  $x_{Bj}$ ,  $Q^2$  and  $p_t^2$  → NLO dijet describes forward jet cross section.  
Small  $x_{Bj}$ ,  $Q^2$  and  $p_t^2$  → NLO dijet fails.
- - DGLAP LO ME+PS (RAPGAP) and NLO di-jet fail for fwd jet cross-sections
  - CDM and LO ME+PS DIR+RESolved  $\gamma$  OK (except 2+fwdjet)
  - CASCADE is in improvement compared to simple DGLAP evolution.
- 2+fwd cross-section -  
Models not ordering the transverse momenta still predict a higher cross-section.  
CDM good.
- Data suggests that more hard radiation (CDM, RES- $\gamma$ , CASCADE) is needed compared to NLO and simple DGLAP evolution.
- Models that break the ordering of transverse momenta give better agreement with data (CDM, RES- $\gamma$ , CASCADE), while simple DGLAP evolution restricts the phase space too much.