



Les Rencontres de Physique  
de la Vallée d'Aoste

# QCD Studies at HERA

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representing the ZEUS and H1  
Collaborations

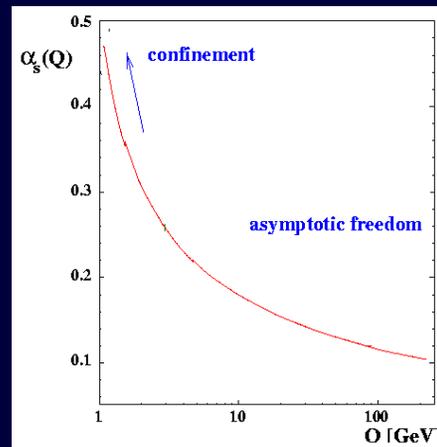


# HERA and QCD

- Talk could/should cover >50% of HERA I physics!
- Have to be selective

## QCD Prejudices

- Nice theory
- Hard to be precise!
- Quarks produced, but hadrons seen



- Experiments
  - Data has few % accuracy for a number of measurements
- NLO QCD
  - Theory getting to same level in some regions
  - Boldly going to places where no theory has gone before!
  - Factorisation and renormalisation scale uncertainties?
- NNLO QCD
  - First calculations coming
  - We want more!

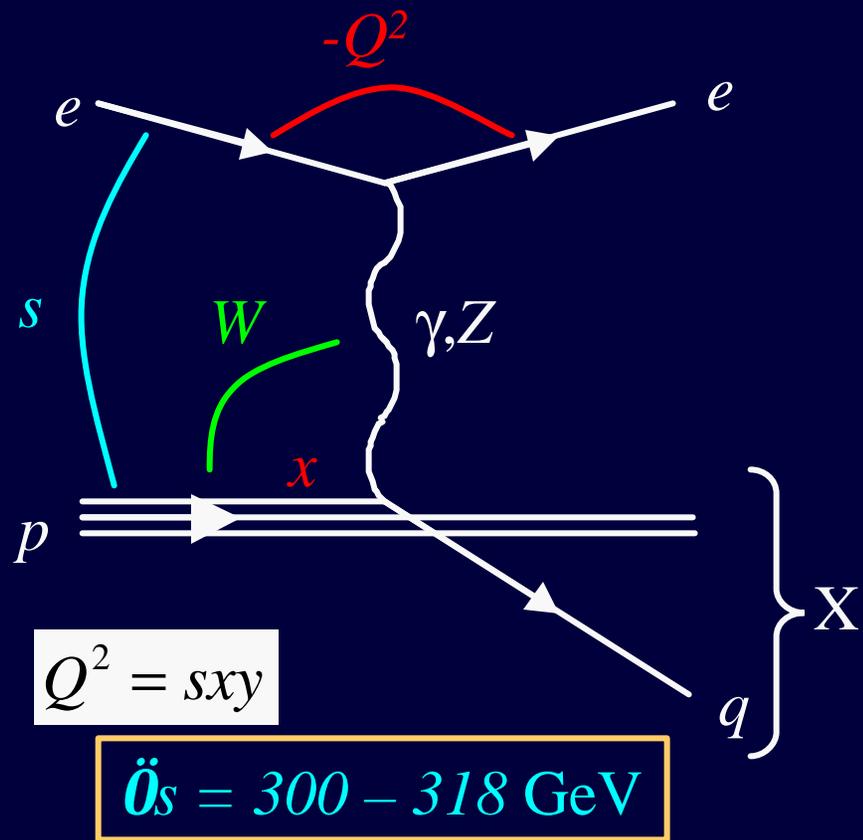
# Topics

- Parton Density Functions
  - $F_2$ ,  $F_L$  and  $xg(x)$
- Determination of  $\alpha_s$ 
  - From PDFs
  - High  $E_T$  inclusive jets and dijets
  - Jet substructure
- 3 jet production
- Dijets in photoproduction
  - Direct vs. resolved photons
  - Comparison with NLO QCD predictions
- Data vs. theory at highest  $Q^2$
- Heavy flavour production

# HERA Kinematics

- Lots of interdependent variables used!
- $s$ :  $e$ - $p$  c.m. energy
- $Q^2 = -q^2$ : 4-momentum transfer squared
- $x$ : fraction of proton momentum carried by quark
- $y$ : inelasticity parameter
- $W$ :  $\gamma$ - $p$  c.m. energy

Lowest order diagram

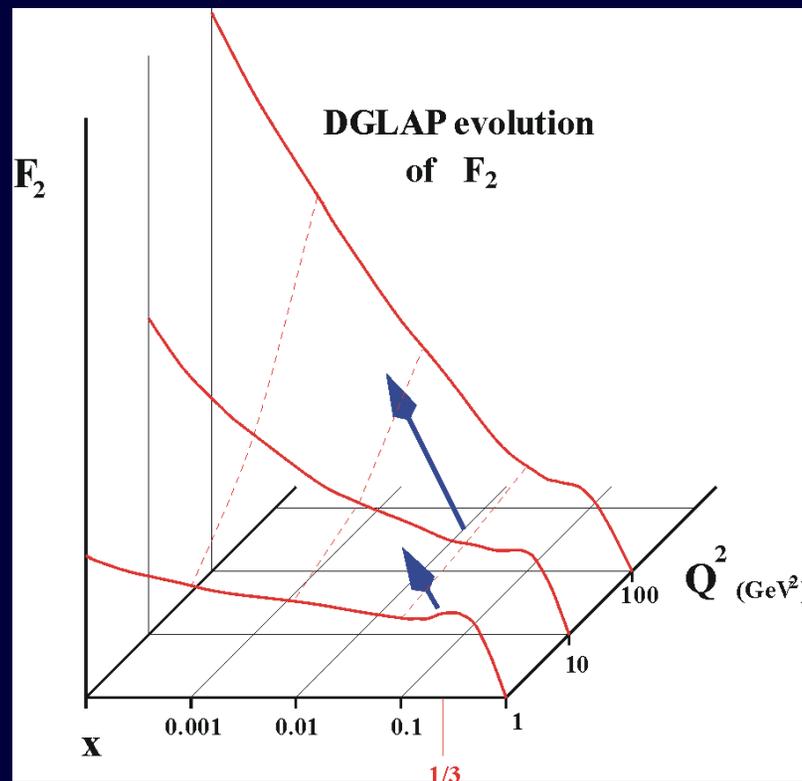
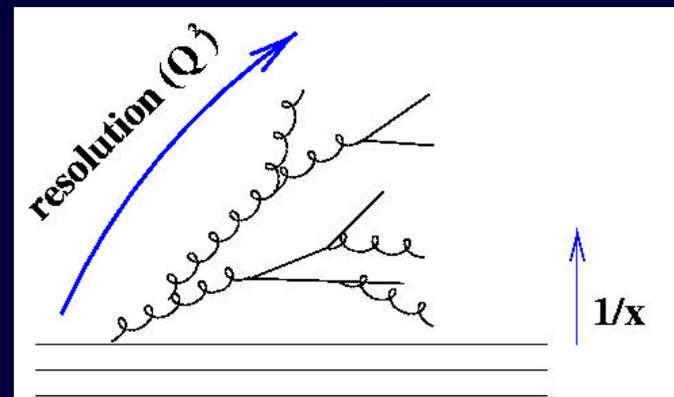


# QCD and PDFs

- Factorise cross section into short range  $\otimes$  PDFs

$$\mathcal{S}_{DIS} \square f_p(x) \otimes \hat{\mathcal{S}}$$

- Use DGLAP to evolve parton density functions
- Experimental data has to constrain input at  $Q_0^2$

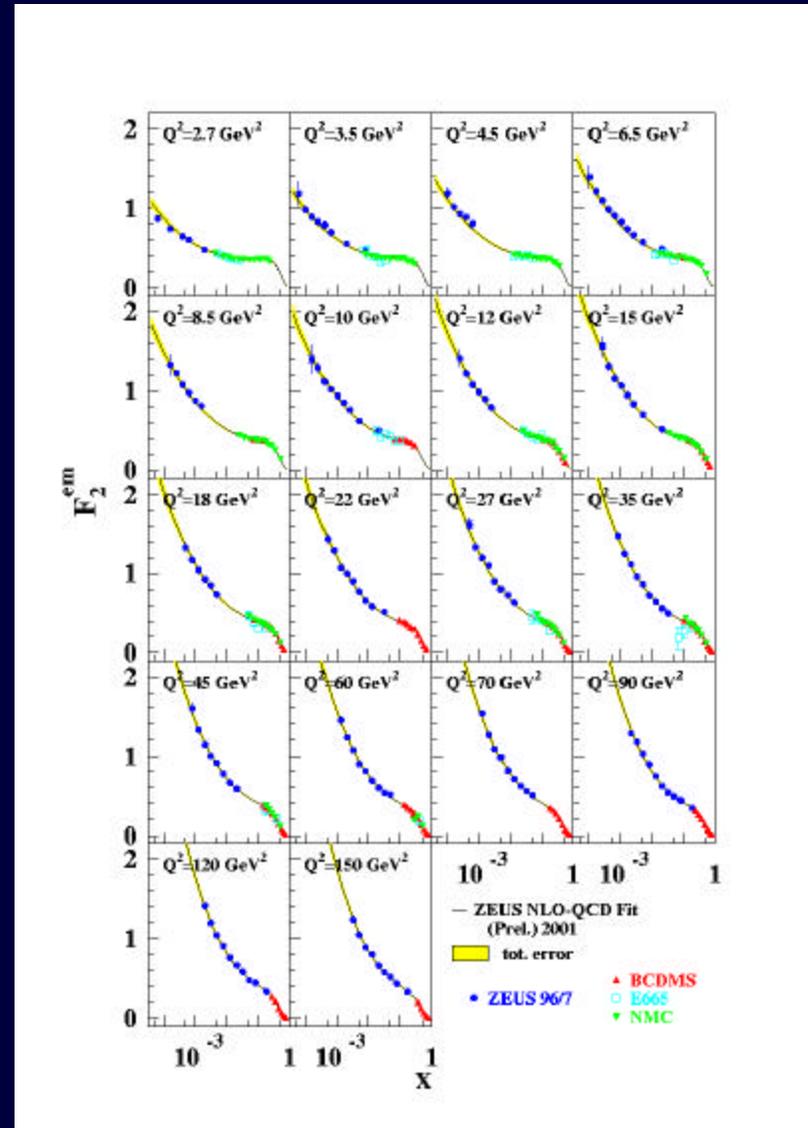


# $F_2$ Results

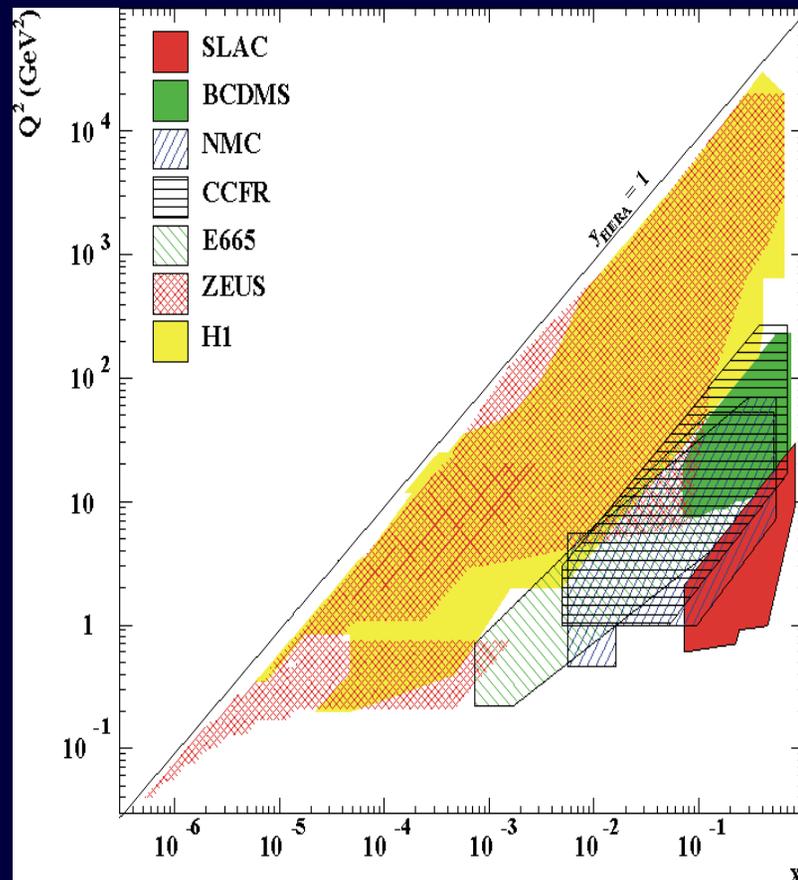
$$\frac{d^2s}{dx dQ^2} = \frac{2pa^2}{xQ^4} (Y_+ F_2 - y^2 F_L \pm Y_- xF_3)$$

$$y = Q^2/xs \quad Y_{\pm} = (1 \pm (1-y)^2)$$

- Structure functions:
  - $F_2$
  - $F_L$ : longitudinal component
  - $xF_3$ : small for  $Q^2 \ll M_Z^2$



# Fit of PDFs



- Fit HERA data on  $F_2$
  - Include best fixed target data
  - Have to parametrise PDFs
- $$f = p_1 x^{p_2} (1-x)^{p_3} (1 + p_4 \sqrt{x} + p_5 x)$$
- Do fits with fixed and free  $\alpha_s$

# ZEUS and H1 Fits

- ZEUS

- ZEUS + BCDMS, E665, NMC
- Start at  $Q_0^2 = 7 \text{ GeV}^2$
- $p_4 = 0$  plus additional constraints
- Heavy quarks: RT variable flavour number scheme

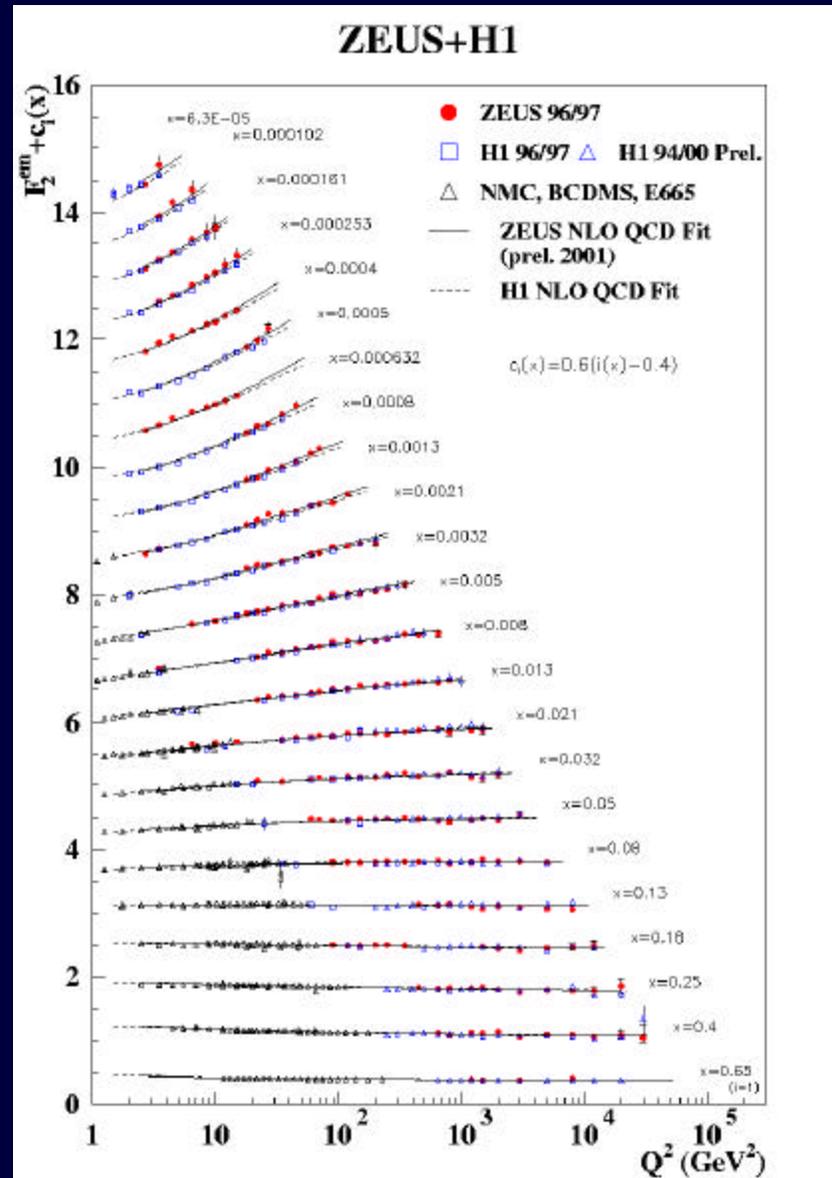
- H1

- H1 + BCDMS
- Start at  $Q_0^2 = 4 \text{ GeV}^2$
- $p_4 = 0$  for the gluon
- Heavy quarks: Fixed flavour number scheme

NLO DGLAP equations used

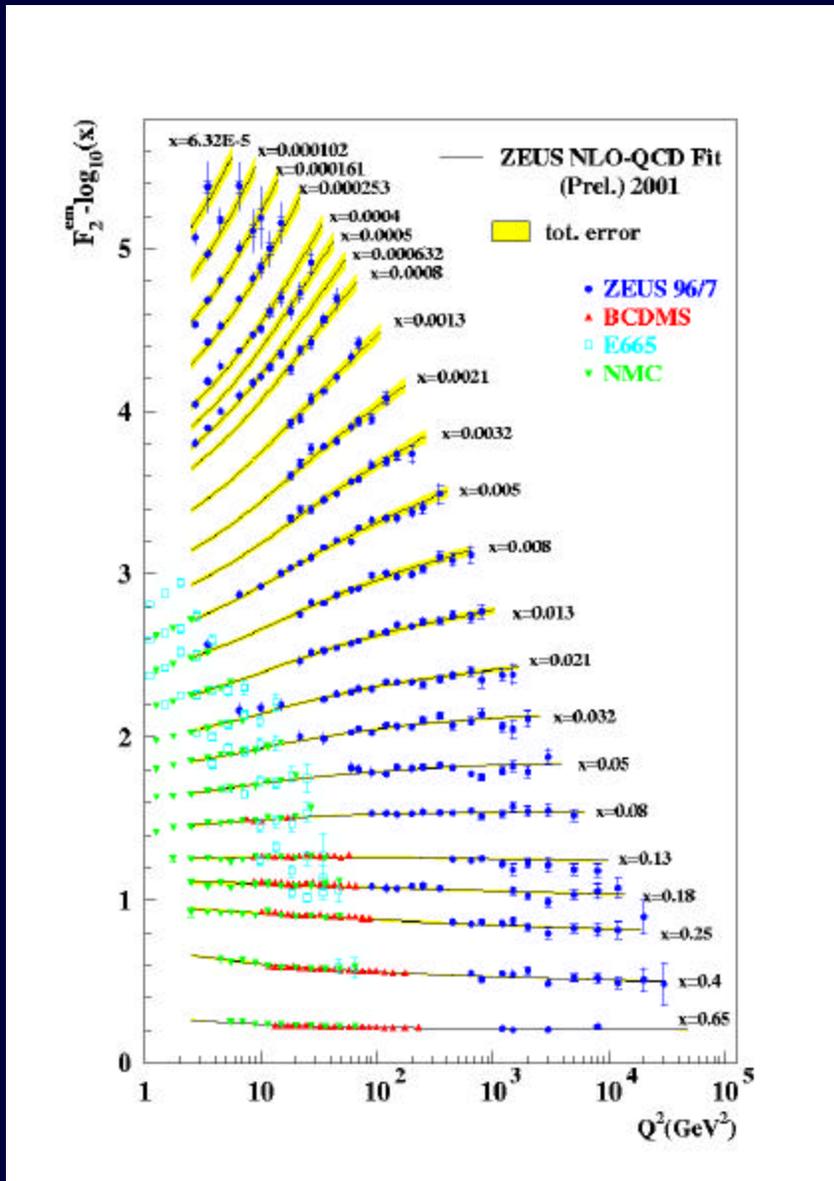
# HERA Fits

- Over very large range ZEUS and H1 data and fits agree very well
- Some differences at small  $x$
- Limited statistics at large  $Q^2$



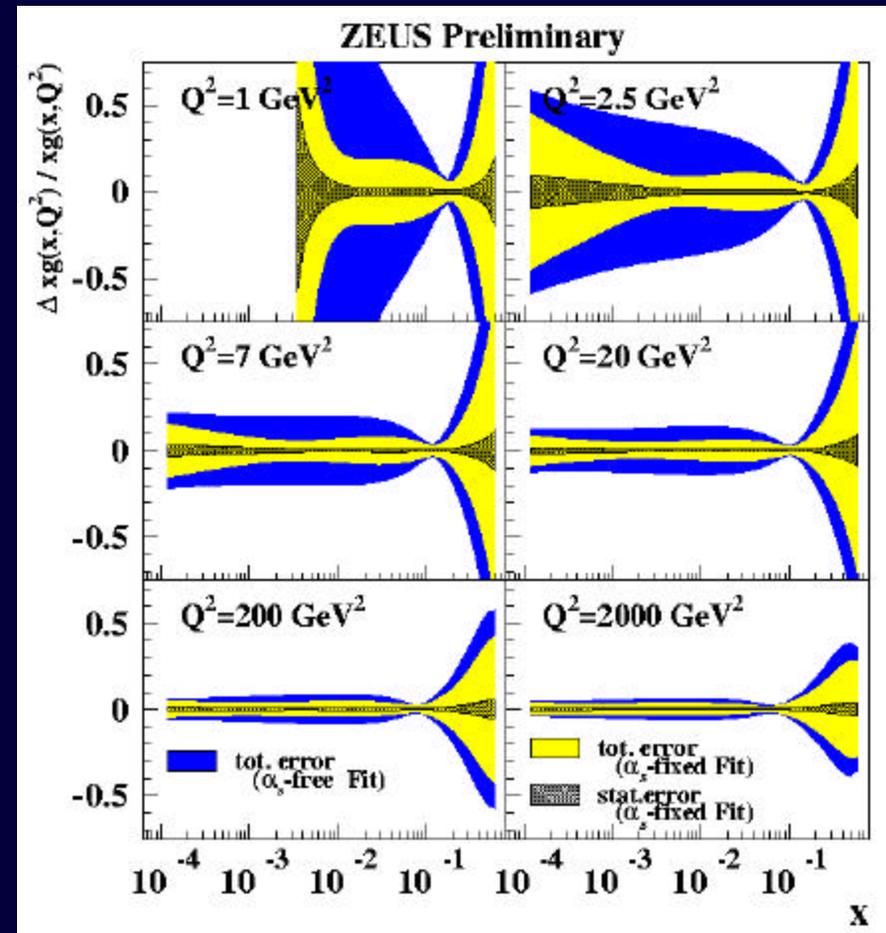
# Errors on PDFs

- Fits now calculate errors on PDFs
- Correlations between experimental errors taken into account
- Low  $x$  and high  $Q^2$  regions have largest errors



# H1 and ZEUS Gluon Density

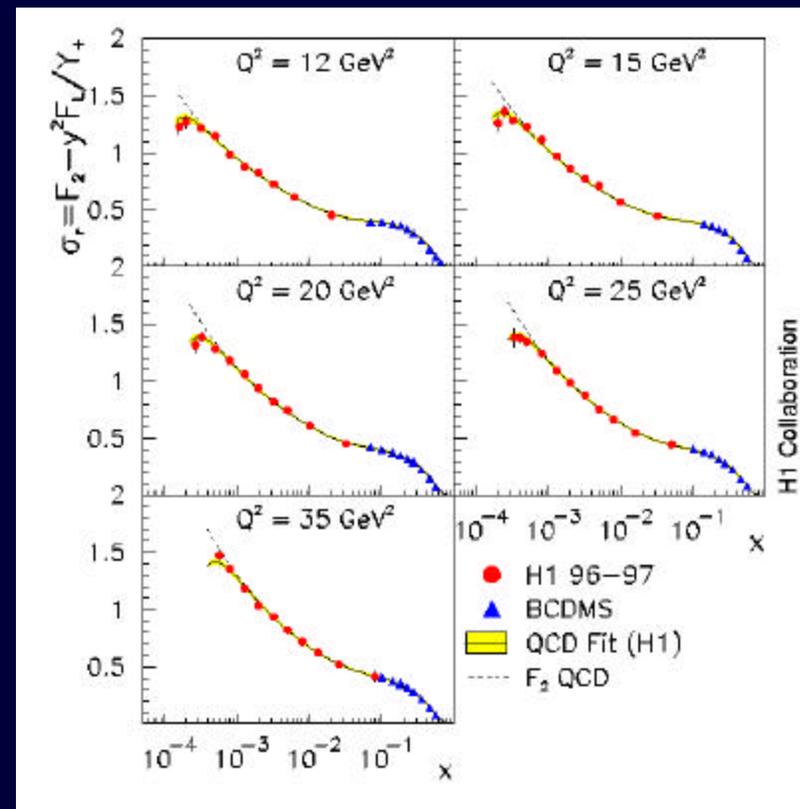
- Fit of gluon distribution
- See evolution of gluon density as a function of  $Q^2$
- Can overlay H1 and ZEUS distributions
- General agreement – differences probably due to:
  - heavy flavour scheme
  - $xg(x)$  parameterisation
- $\alpha_s$  correlation clearly visible in error on  $xg(x)$



# $F_L$ Results

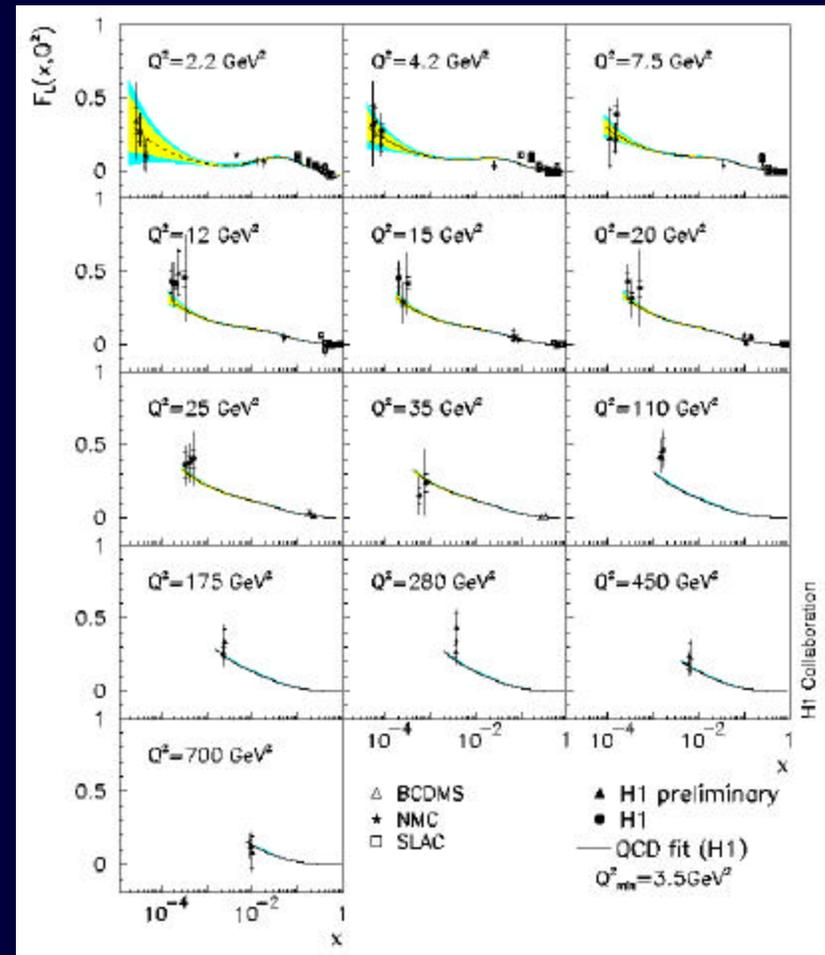
- Really need different  $s$   
 $Q^2 = sxy$
- ZEUS used ISR events
- H1 measure  $\sigma_r$ ; use  $F_2$  from lower  $y$  to predict value at high  $y$  (low  $x$ )
  - DGLAP gives very consistent picture
  - Works best at higher  $Q^2$

$$\frac{Q^4 x}{2pa^2 Y_+} \square \frac{d^2 s}{dx dQ^2} = \sigma_r = F_2 - \frac{y^2}{Y_+} F_L$$



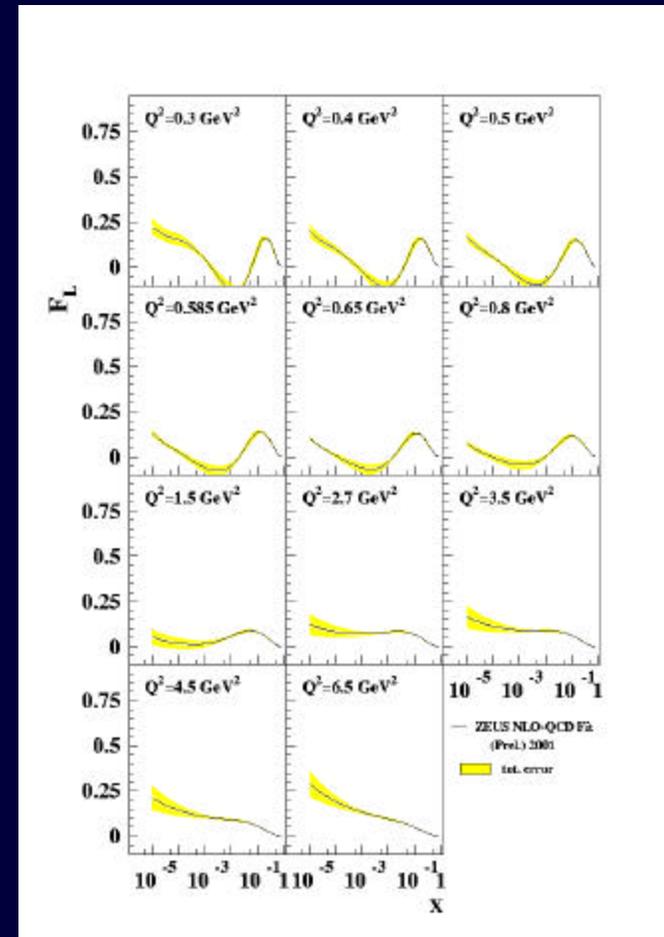
# $F_L$ using derivative

- Can also use  $\partial s / \partial \ln y$ 
  - Works best at low  $Q^2$
  - $F_2$  and  $F_L$  contributions similar
- Plot  $\partial s / \partial \ln y$  as a function of  $y$  for different  $Q^2$  ranges



# Lower Limit of pQCD

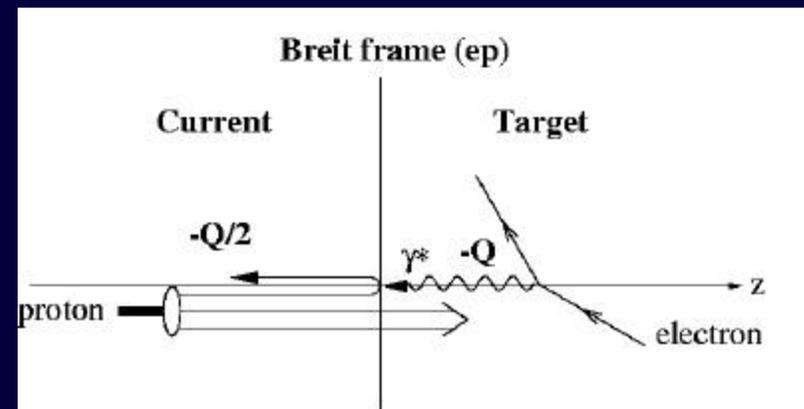
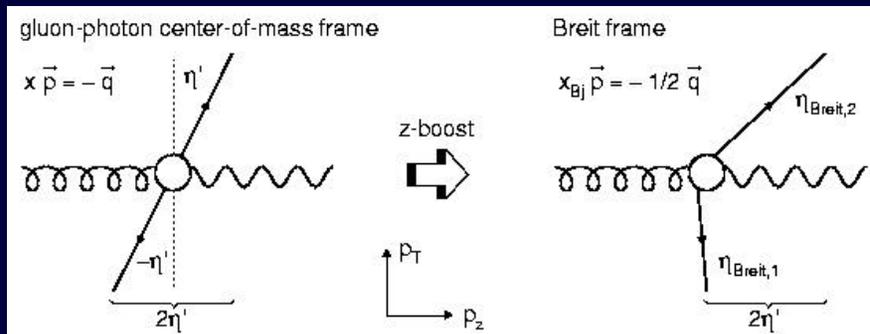
- Use PDF fits and DGLAP evolution
- See that QCD description only fails below about  $0.8 \text{ GeV}^2$
- Same effect seen in  $F_L$  determination - value physical for  $Q^2 > 0.8 \text{ GeV}^2$



# Measurements with Jets

- Often made in Breit frame
- Breit frame defined as  $2x\vec{p} + \vec{q} = 0$
- Related to  $\gamma$ - $p$  c.m. by a longitudinal boost

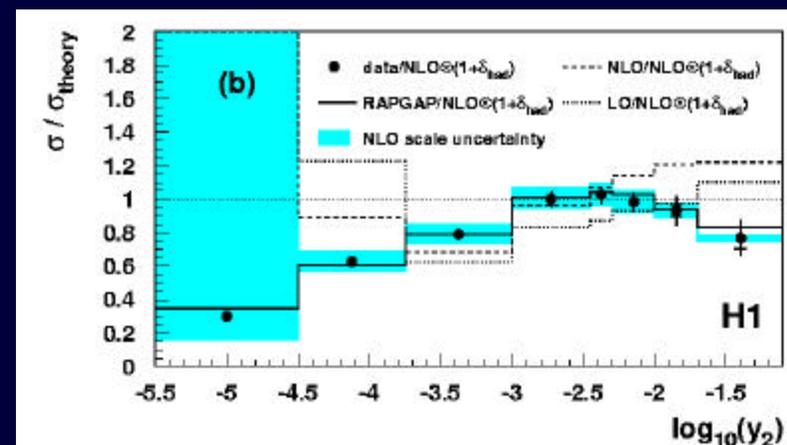
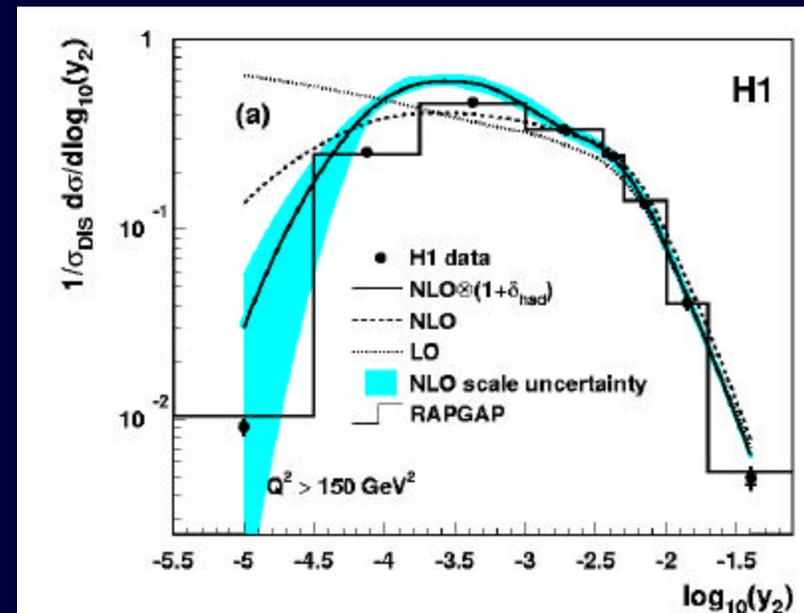
Single jets have no transverse energy



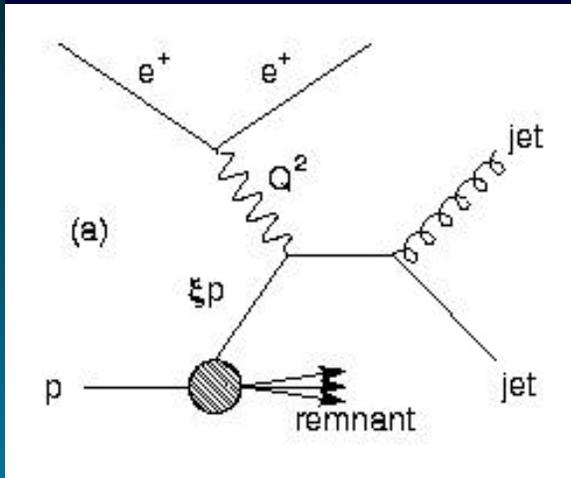
Current jet can be compared with  $e^+e^-$  jets

# Jets in PQCD

- Use typical clustering algorithms to define jets
- How far can one lower  $y_{\text{cut}}$  and still describe jets with pQCD?
- Surprisingly far – 30% of events in DIS can be classified as having 2 or more jets with  $y_{\text{cut}} \sim 0.001$

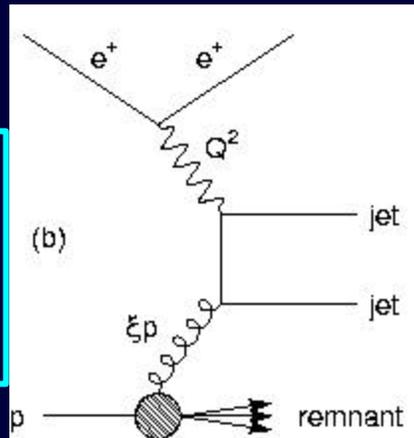


# Jets in Breit frame – H1 and ZEUS



QCDC:  
Dominates  
at high  $Q^2$

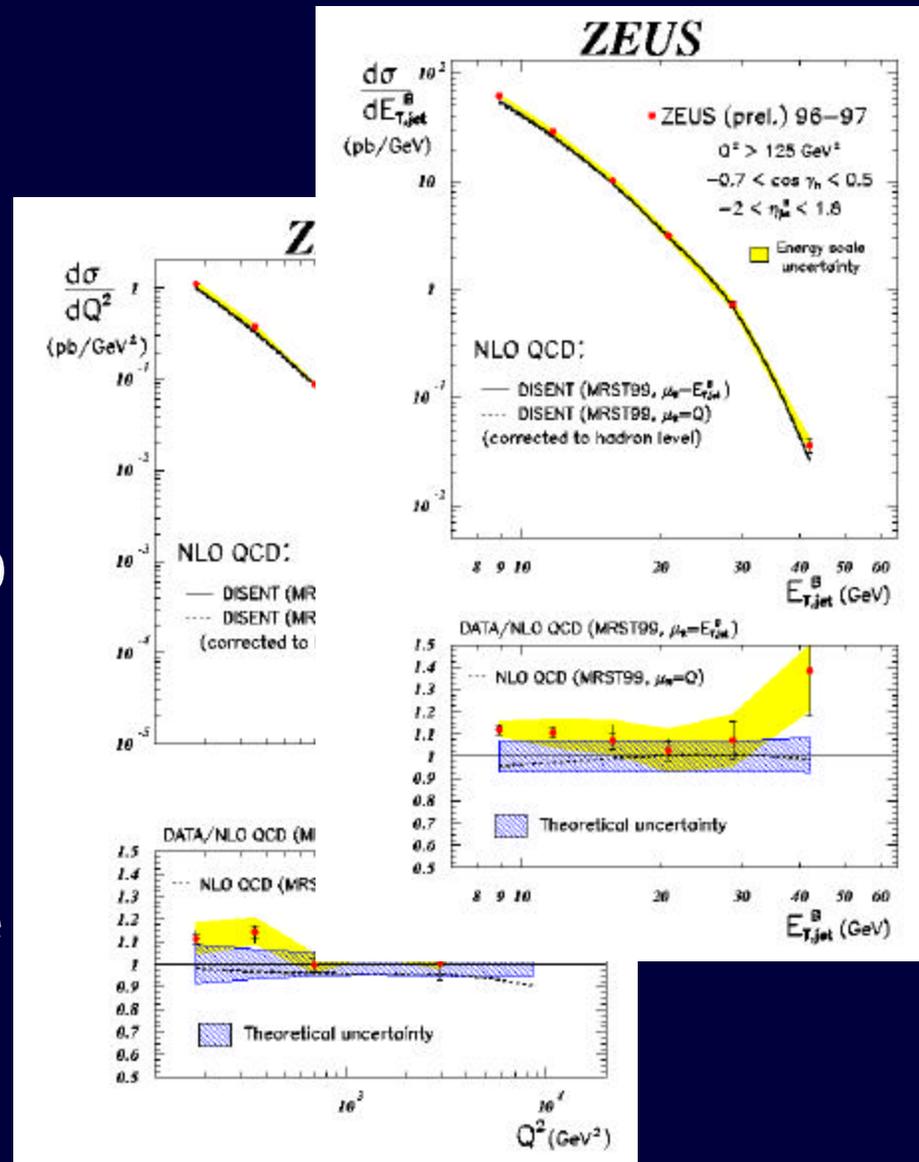
BGF:  
Dominates  
at low  $Q^2$



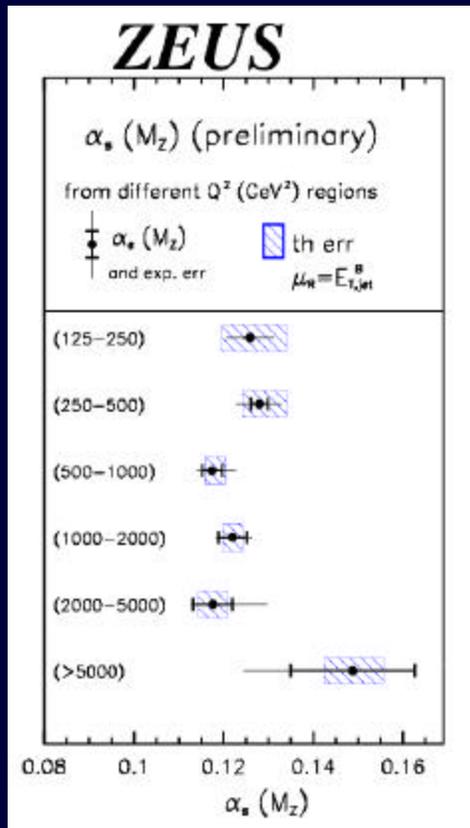
- Jets with significant  $E_T$  usually produced via QCD Compton or boson-gluon fusion process.
- Production rate clearly depends on  $\alpha_s$ , but data mostly sensitive to  $\mathbf{a_s \cdot xg(x)}$
- Breit frame provides good separation from proton remnant

# Jet Cross Section

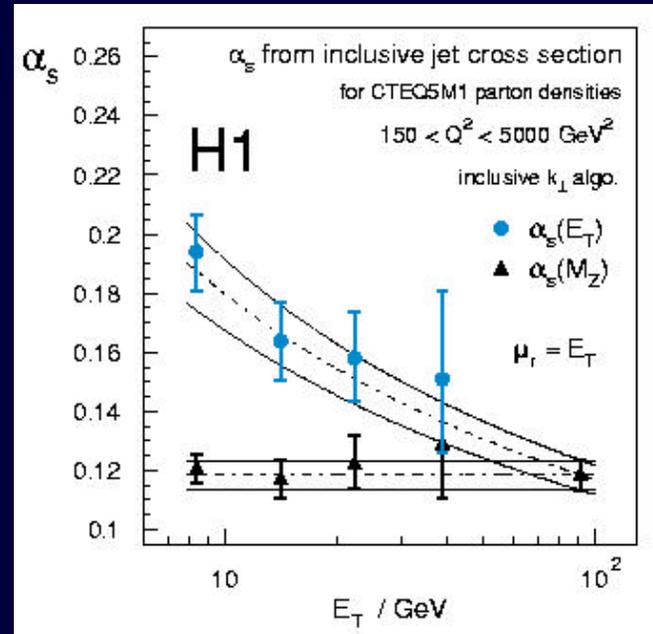
- Select DIS events with high  $E_T$  jets
- Compare inclusive jet cross sections with NLO QCD prediction
- 2 scales:  $Q^2$  &  $E_T$
- **Good agreement seen**
- How much should scale be varied?  
A factor of 2?



# Inclusive Jet Cross Sections



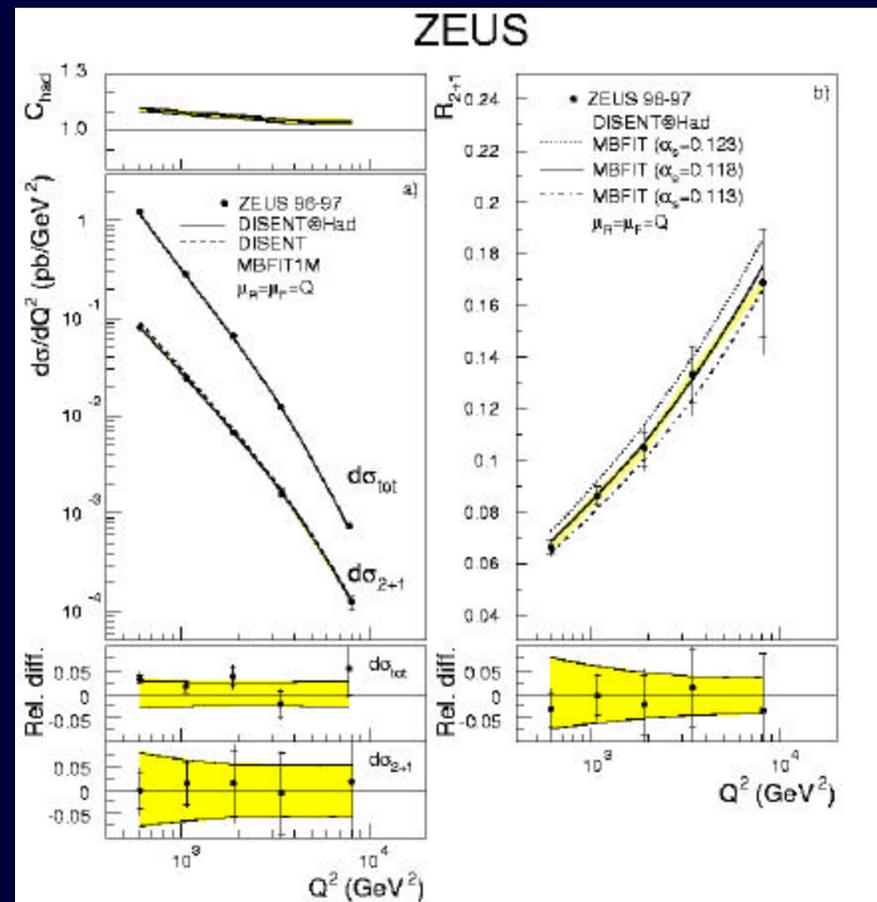
- Can determine  $\alpha_s$  in different  $E_{T,jet}$  regions or as a function of  $E_T$
- Extraction reliable for  $Q^2 > 500 \text{ GeV}^2$  or  $E_T > 15 \text{ GeV}$
- Running seen in a single experiment



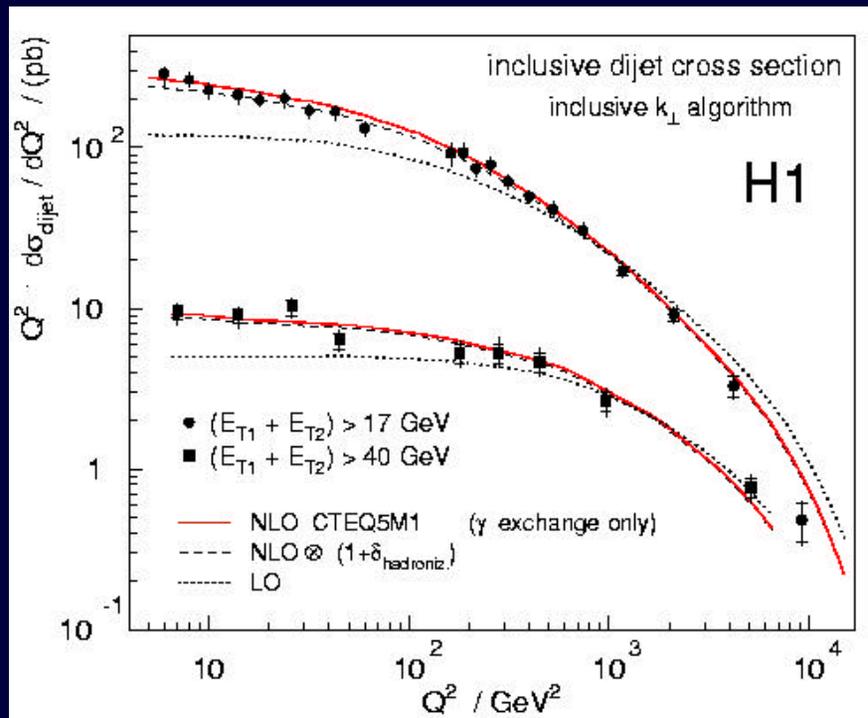
Theory error ~5% due to renormalisation and factorisation scale uncertainty

# ZEUS Dijet Cross Sections

- Cross section for single and dijet production
- Ratio of dijet to single jet cross section proportional to  $\alpha_s$



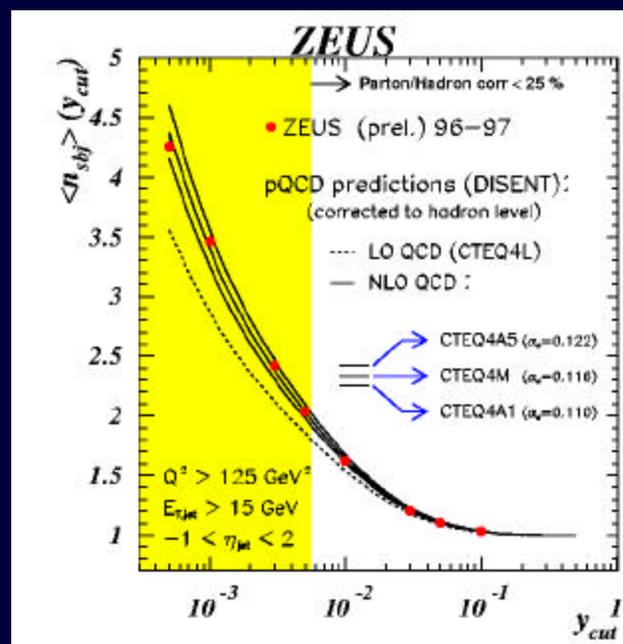
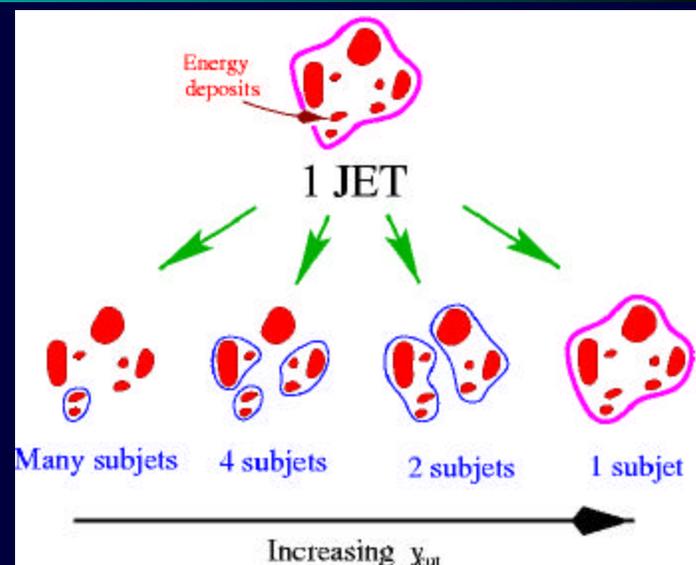
# H1 Dijet Cross Sections



- Dijet cross section with different  $E_T$  cuts
- Different jet algorithms compared at high  $Q^2$
- **NLO is clearly needed**
- $a_s$  extraction uses  $150 \leq Q^2 \leq 5000 \text{ GeV}^2$

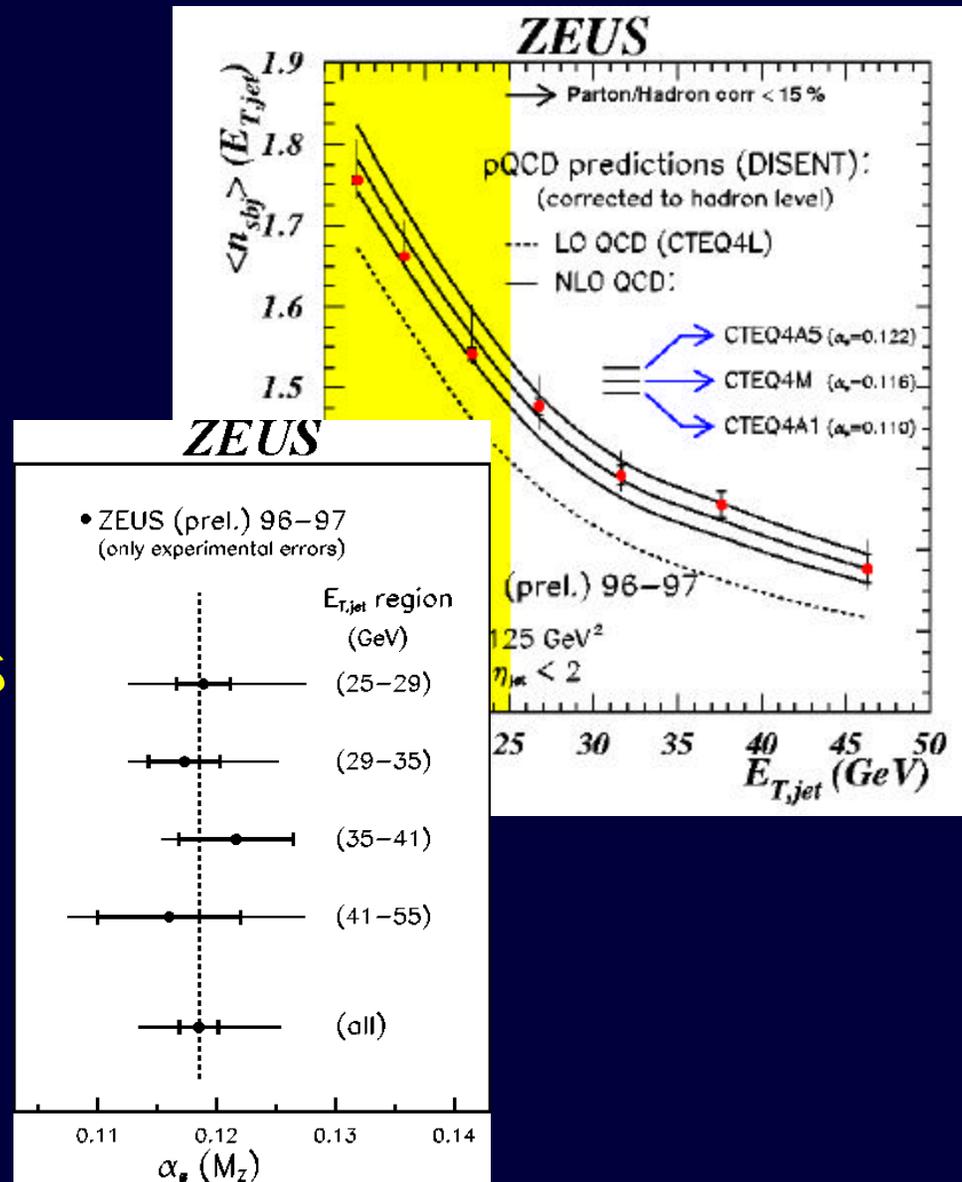
# Jet Substructure - ZEUS

- Look for jet-like components inside a jet
- Find jets in lab system to keep large single jet sample
- Subjets calculated in NLO
- Pick a region where parton/hadron corrections are  $< 15\%$



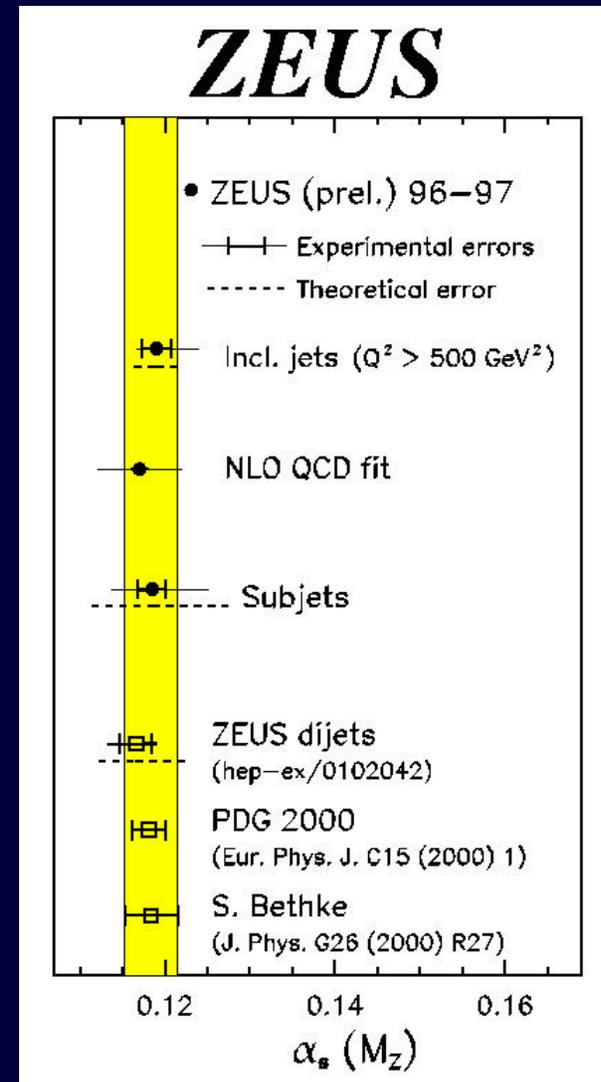
# Jet Substructure

- Measurements are sensitive to  $\alpha_s$
- $\alpha_s$  values are consistent in different  $E_T$  regions
- Systematic errors mainly from factorisation and renormalisation scale uncertainty



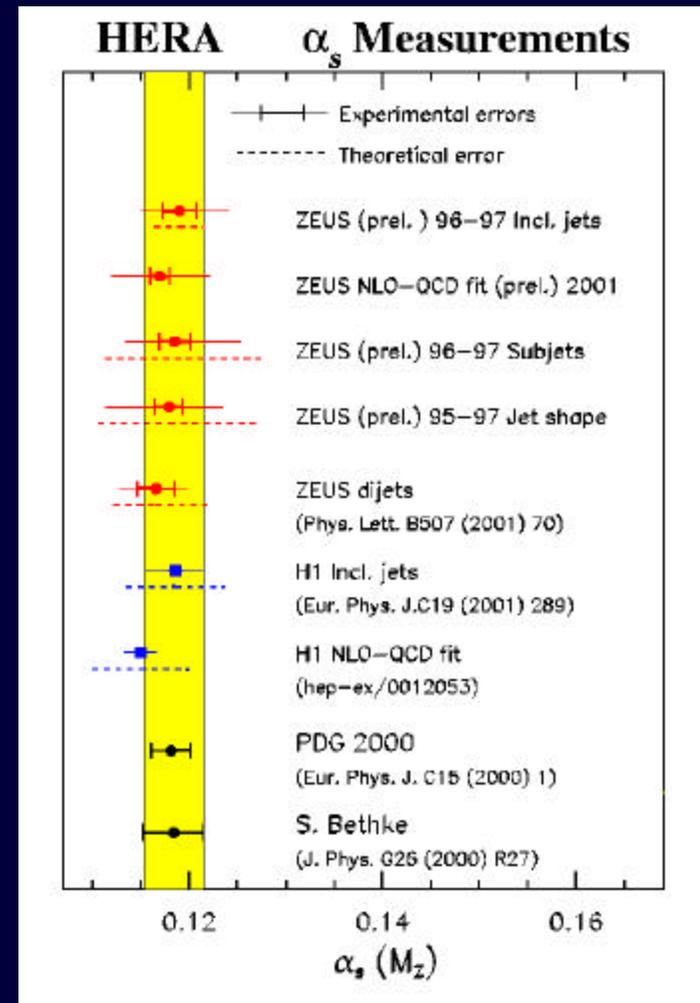
# ZEUS $\alpha_s$ Summary

- Comparison of different ZEUS measurements shows good agreement between them all
- In jet measurements theory error dominates
- Needs theoretical input on scale uncertainty (NNLO calculations)



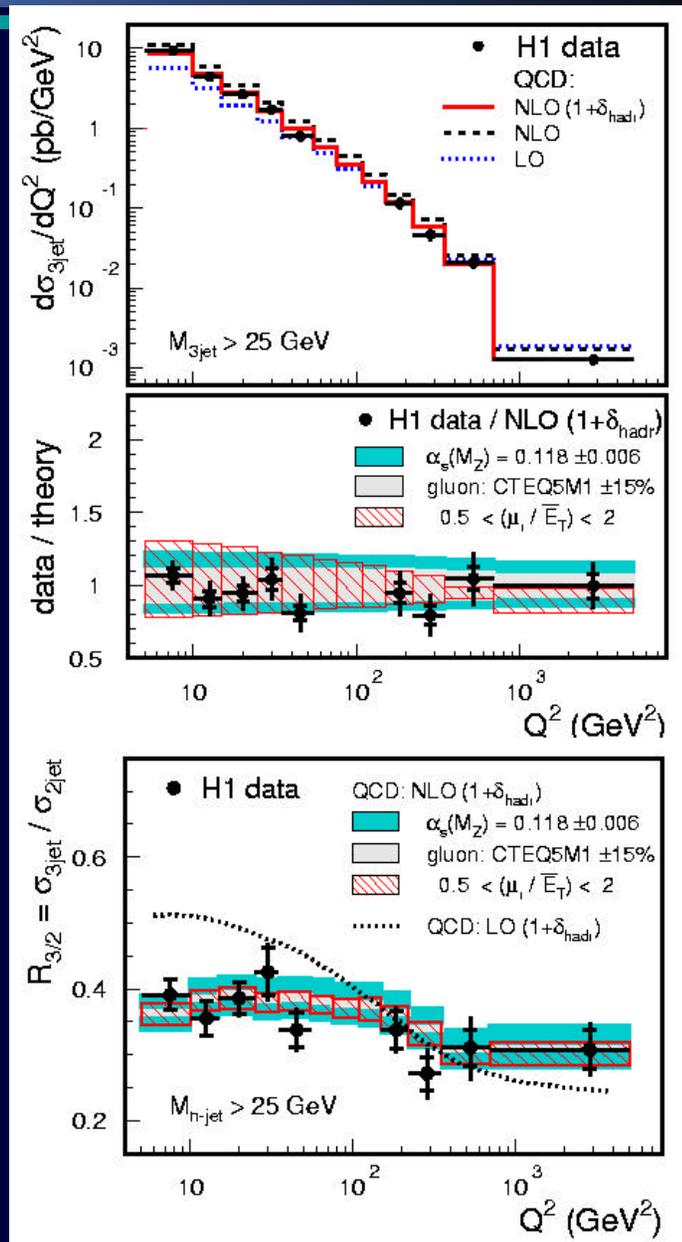
# Compare with PDG and Bethke world average

- Good agreement
- HERA results are competitive
- Running of  $\alpha_s$  seen in single experiment
- Influence on world average depends on reducing theoretical uncertainties



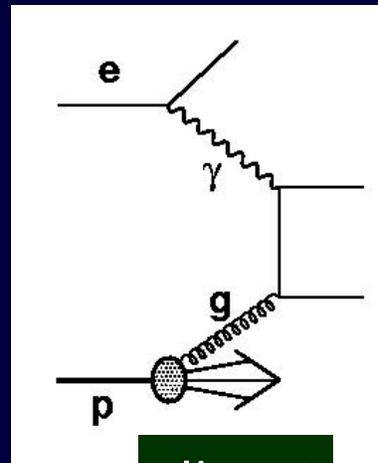
# Three Jets – H1

- Look at 3 jet cross section as a number of variables
- Cross section is proportional to  $a_s^2$  in lowest order
- Again well described by NLO calculations

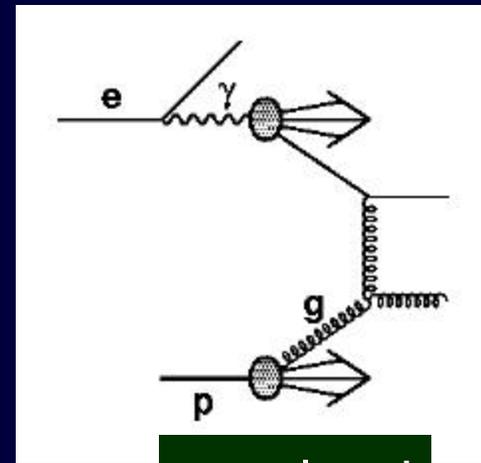


# Dijets in Photoproduction

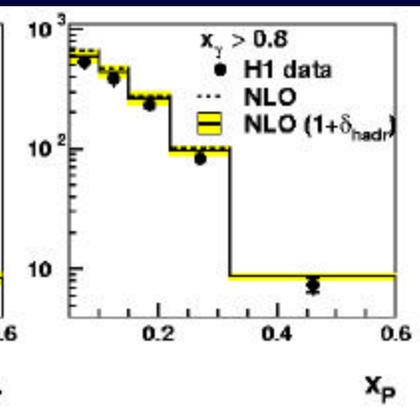
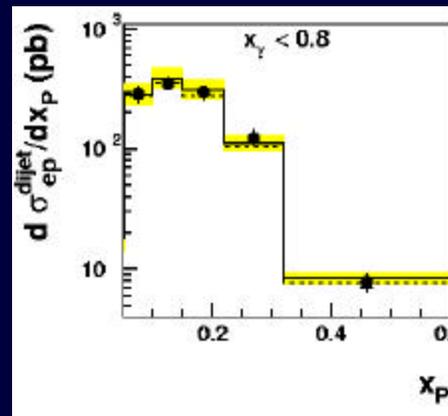
- Select events with 2 high  $E_T$  jets
- Measure cross section as a function of:
  - $E_T$
  - $x_g$
  - $x_p$
- NLO clearly needed especially at high  $x_g$



direct

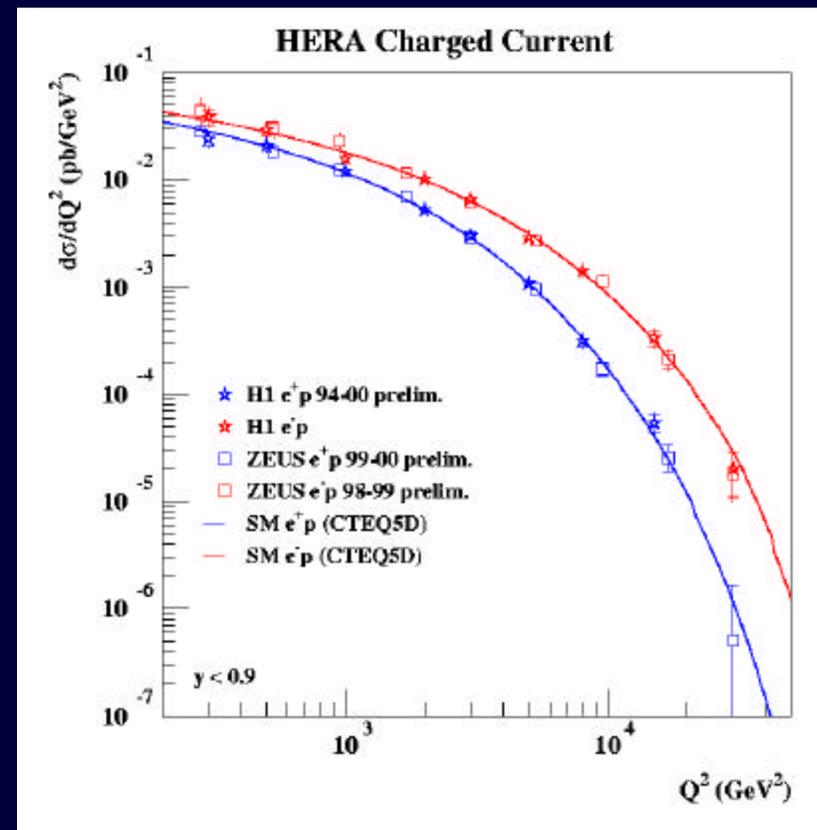


resolved



# High $Q^2$

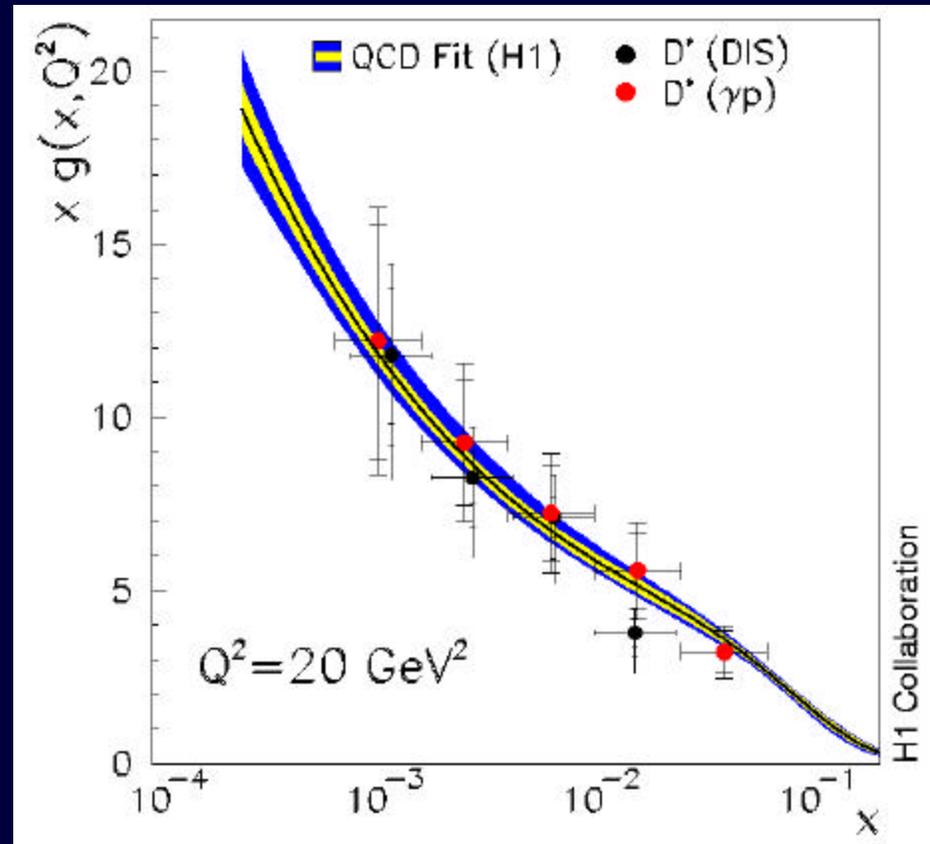
- Clearly see effect of W/Z exchange in cross section
- Newest HERA data extend kinematic range – good agreement with expectation seen
- **QCD + EW effects completely explain data**
- **More statistics + longitudinal lepton polarisation coming with HERA II**



## Quark mass provides hard scale

# Charm and Gluons

- Boson-gluon fusion is main production mechanism
- Charm production directly proportional to gluon content
- With current statistics PDF fits still do a better job

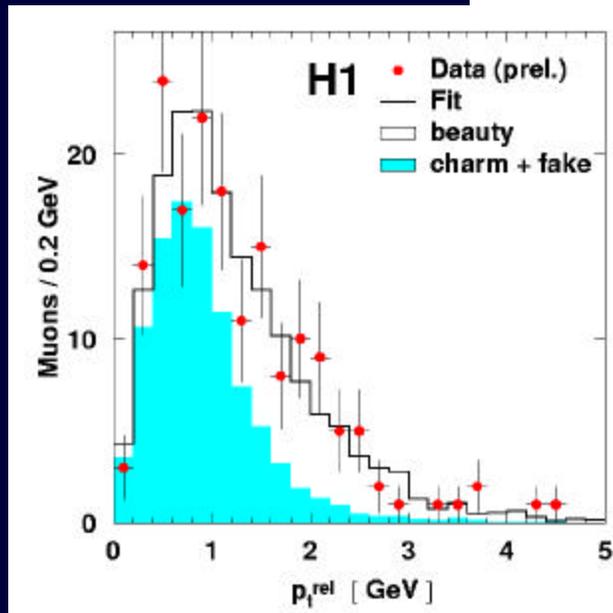
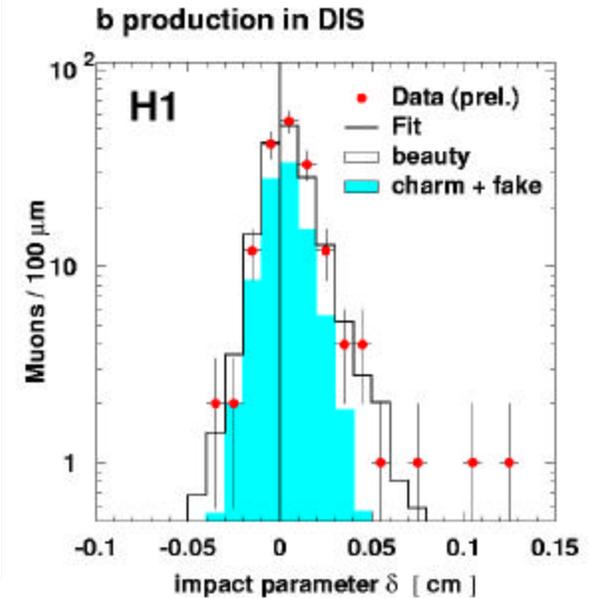


# $b$ Quarks at HERA

- $c$  quark production cross section in marginal agreement with expectations
- $b$  quark production 2 to 3 orders of magnitude smaller than  $c$  (c.f. LEP)
- Should be calculable in pQCD,  $b$  should be better than  $c$  as scale is harder
- Use semileptonic muon decay mode to identify  $b$ 's
  - ZEUS also uses electrons
- H1 can use silicon microvertex detector as well

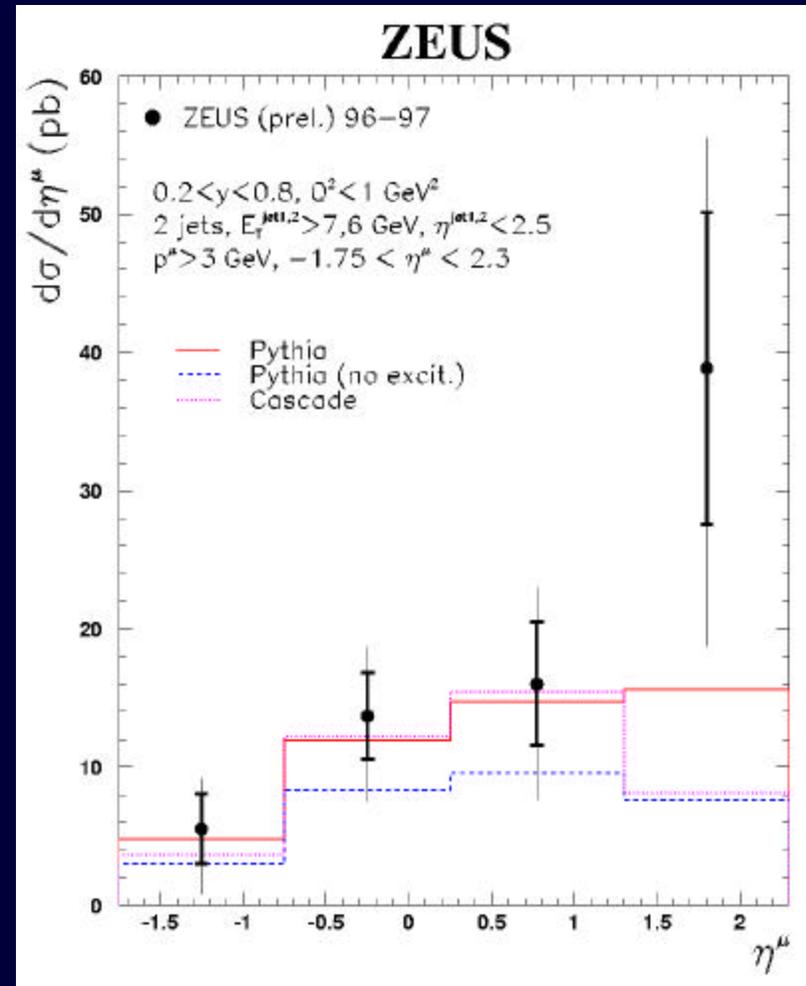
# H1 Results

- Combine muon tag with impact parameter
- S/B about 1:1
- Clear  $b$  signal



# HF in Photoproduction + DIS

- Signal seen in photoproduction and DIS
- Ratio of data to expectation about a factor of 2 too high!
- 2-3  $\sigma$  effect
- ZEUS result is consistent
- Smaller discrepancy if  $b$  excitation included
- Really need HERA II + microvertex detectors



# Conclusions

- HERA data provides many precise tests of pQCD
- NLO QCD reaches places that no other theory can reach!
- NLO predictions show remarkably good agreement with measurements over a huge kinematic range
- Errors due to scale uncertainties often dominate
- NNLO calculations needed
- Different  $\alpha_s$  results are precise and agree well with each other and world average
- $b$  quark production cross section is still a problem
- Heavy quark results will benefit from HERA II lumi and microvertex detectors
- HERA II programme with 5x lumi + polarised lepton beams getting underway
- 1 fb<sup>-1</sup> per experiment by 2006

# $\alpha_s$ – the numbers

ZEUS incl. jets	$0.1190 \pm 0.0017(\text{stat})^{+0.0049}_{-0.0023}(\text{exp})^{+0.0026}_{-0.0026}(\text{th})$
ZEUS NLO fit	$0.1172 \pm 0.0008(\text{stat}) \pm 0.0054(\text{syst})$
ZEUS Subjets	$0.1185 \pm 0.0016(\text{stat})^{+0.0067}_{-0.0048}(\text{exp})^{+0.0089}_{-0.0071}(\text{th})$
ZEUS Jet shape	$0.1179 \pm 0.0014(\text{stat})^{+0.0054}_{-0.0065}(\text{exp})^{+0.0094}_{-0.0073}(\text{th})$
ZEUS dijets	$0.1166 \pm 0.0019(\text{stat})^{+0.0024}_{-0.0033}(\text{exp})^{+0.0057}_{-0.0044}(\text{th})$
H1 incl. Jets	$0.1186 \pm 0.0030(\text{exp})^{+0.0039}_{-0.0045}(\text{th})$
H1 NLO-QCD fit	$0.1150 \pm 0.0017(\text{exp})^{+0.0009}_{-0.0005}(\text{model}) \pm 0.005(\text{scale})$
PDG 2000	$0.1181 \pm 0.002$
Bethke	$0.1184 \pm 0.0031$