



Low x workshop, Lisbon, Portugal, June 28 - July 1, 2006

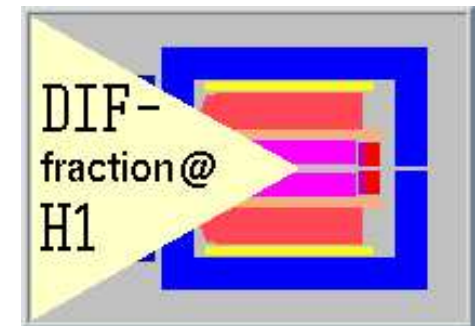
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# H1 measurements on $F_2^{D(3)}$ and $F_2^{D(4)}$ and diffractive PDF

S. Levonian, DESY

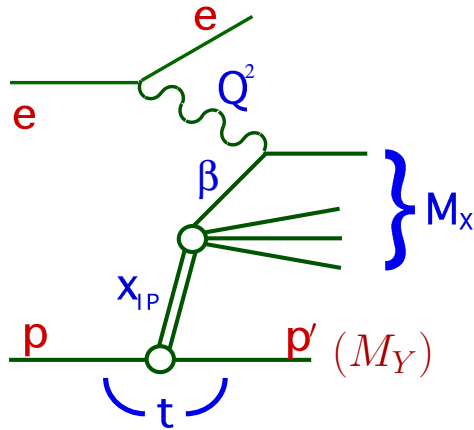
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- Data samples and Phenomenological framework
- $(x_{\mathbb{P}}, t)$  - dependencies and Pomeron trajectory
- $(Q^2, \beta)$  - dependencies and diffractive PDFs
- Summary and Outlook



# Diffraction at HERA

- Fundamental aim: understand high energy limit of QCD (gluodynamics; CGC ?)
- Novelty: for the first time probe partonic structure of diffractive exchange
- Practical motivations: study factorisation properties of diffraction; try to transport to  $hh$  scattering (e.g. predict diffractive Higgs production at LHC)



$$x_P (= \xi) = \frac{Q^2 + M_X^2}{Q^2 + W^2}$$

(momentum fraction of colour singlet exchange)

$$\beta = \frac{Q^2}{Q^2 + M_X^2} = x_q / P = \frac{x}{x_P}$$

(fraction of exchange momentum, coupling to  $\gamma^*$ )

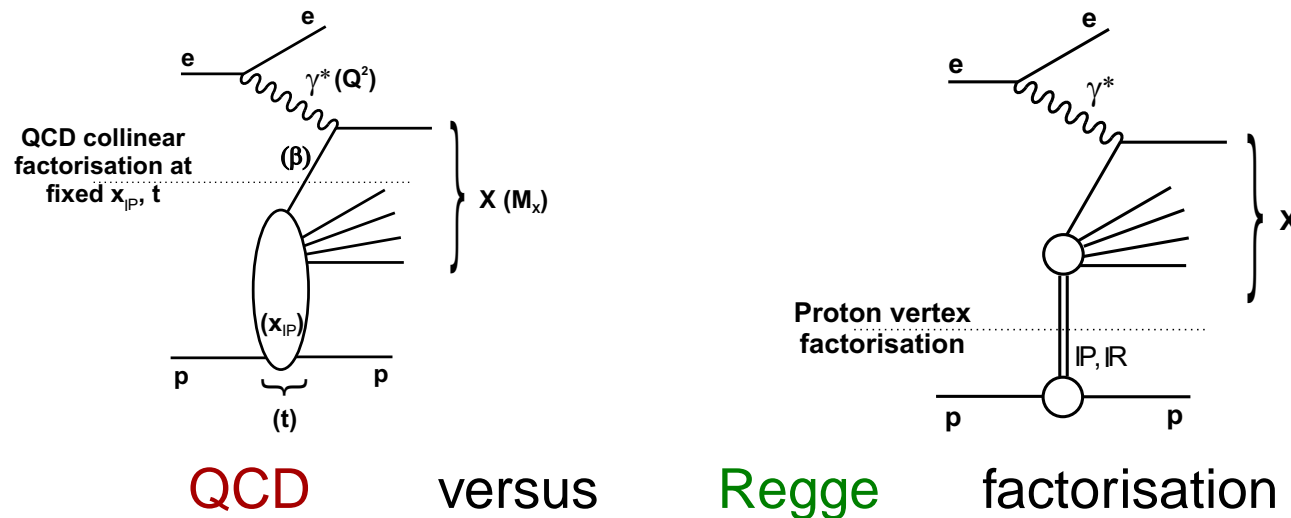
$$t = (p - p')^2$$

(4-momentum transfer squared)

$$\frac{d^4\sigma}{dx_P dt d\beta dQ^2} = \frac{4\pi\alpha^2}{\beta Q^4} \left(1 - y + \frac{y^2}{2}\right) \sigma_r^{D(4)}(x_P, t, \beta, Q^2)$$

$$\sigma_r^{D(4)} = F_2^{D(4)} - \frac{y^2}{2(1 - y + y^2/2)} F_L^{D(4)} \Rightarrow F_2^{D(3)} = \int dt F_2^{D(4)}$$

# Factorisation properties in diffractive DIS



## QCD factorisation

(leading twist, coll.approx.  
for DDIS: Collins et al.)

## Regge factorisation

(conjecture, e.g. RPM  
by Ingelman, Schlein)

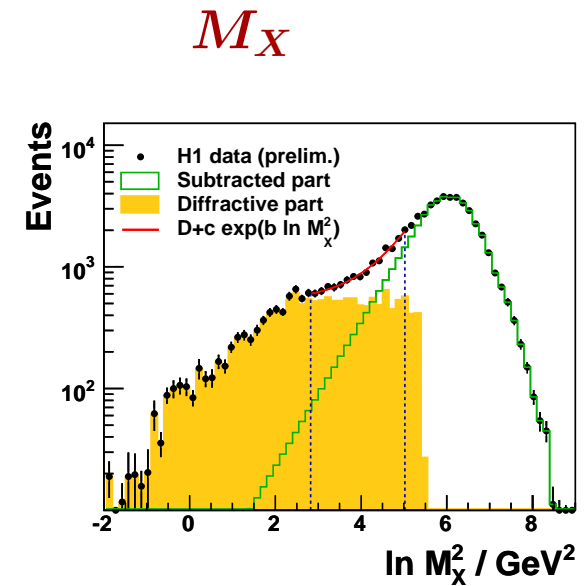
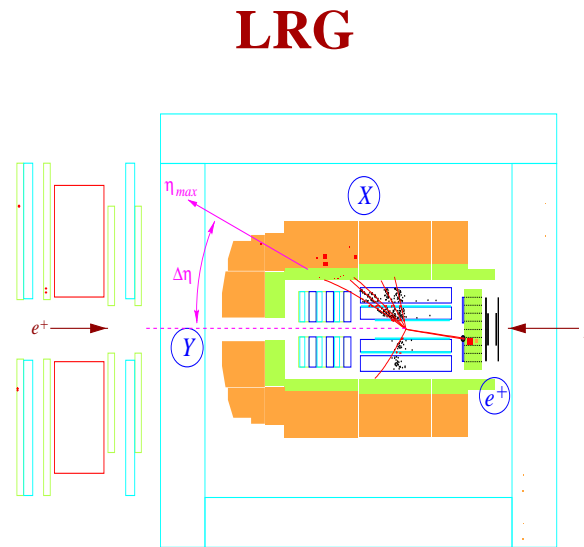
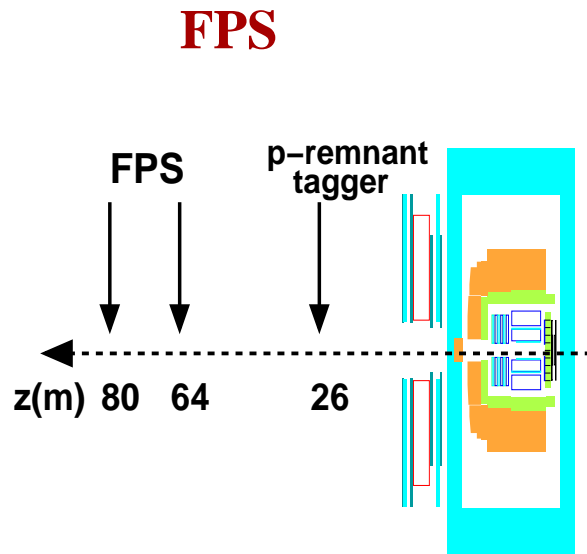
$$\sigma_r^{D(4)} \propto \sum_i \hat{\sigma}^{\gamma^* i}(x, Q^2) \otimes f_i^D(x, Q^2; x_P, t) + \mathcal{O}(1/Q)$$

- $\hat{\sigma}^{\gamma^* i}$  – hard scattering part, same as in inclusive DIS
  - $f_i^D$  – diffractive PDF's, valid at fixed  $x_P, t$  which obey (NLO) DGLAP
- ⇒ Inhomogeneous term ('direct Pomeron') not considered

$$F_2^{D(4)}(x_P, t, \beta, Q^2) = \Phi(x_P, t) \cdot F_2^{IP}(\beta, Q^2)$$

- In this case shape of diffractive PDF's is independent of  $x_P, t$   
while normalization is controlled by Regge flux  $\Phi(x_P, t) = A_P \frac{e^{\beta_P t}}{x_P^{2\alpha_P(t)-1}}$
- Sub-leading  $\mathbf{R}$  contributions are included in the same manner

# Selecting Diffractive Events at HERA



- clean sample, free of p-dissociative bgr
- provides  $t$  measurement
- access to high  $x_{\mathbb{P}} \Rightarrow$  better constrain sub-leading terms
- limited statistics (beam cond., geom. acceptance)

- large statistics, bigger phase space coverage:  
 $3.3 < \eta_{\text{gap}} < 7.5$  (tag)  $\eta_{\text{max}} < 3.3$  (meas)
- integrate over  $t > -1 \text{ GeV}^2$
- some dissociative admixture remains in the sample:  
 $M_Y < 1.6 \text{ GeV}$
- $M_X$  method is not well adapted to H1 detector and hence is used only to study systematics and in limited  $\eta$  range

# Data Samples

- FPS sample** (hep-ex/0606003)

1999-2000 data ( $28 \text{ pb}^{-1}$ ,  $2 < Q^2 < 50 \text{ GeV}^2$ )

$0.08 < |t| < 0.5 \text{ GeV}^2$ ,  $x_P < 0.10$

Precision =  $(8-30)\%_{\text{stat}} \oplus 12\%_{\text{syst}} \oplus 10\%_{\text{norm}}$

- LRG samples** (hep-ex/0606004)

1997 data ( $2 \text{ pb}^{-1}$ ,  $3 < Q^2 < 13.5 \text{ GeV}^2$ )

1997 data ( $11 \text{ pb}^{-1}$ ,  $13.5 < Q^2 < 105 \text{ GeV}^2$ )

1999-2000 data ( $62 \text{ pb}^{-1}$ ,  $Q^2 > 133 \text{ GeV}^2$ )

$M_Y < 1.6 \text{ GeV}$ ,  $|t| < 1 \text{ GeV}^2$ ,  $x_P < 0.05$

Precision =  $(5-20)\%_{\text{stat}} \oplus (5-15)\%_{\text{syst}} \oplus (6-8)\%_{\text{norm}}$

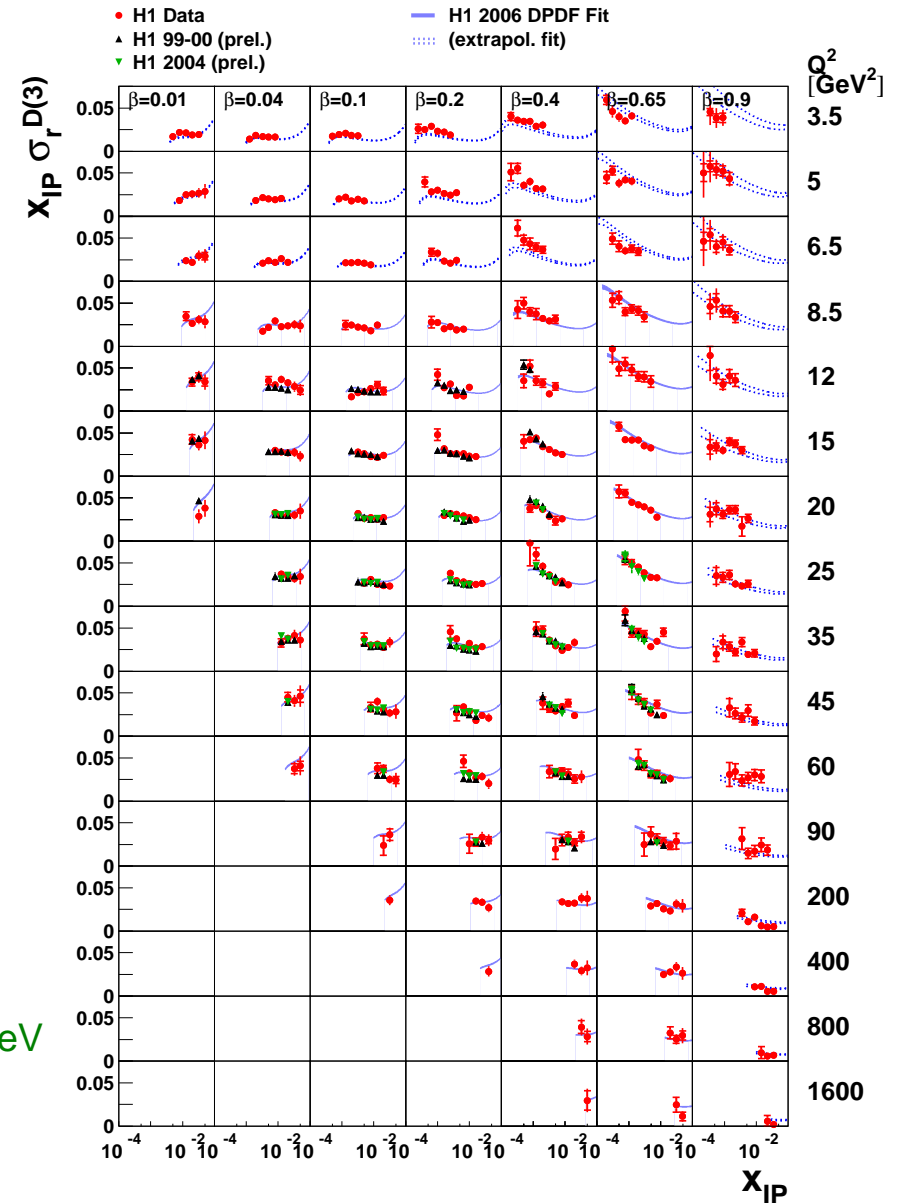
- LRG samples** (preliminary at DIS 2006)

1999-2000 data ( $34 \text{ pb}^{-1}$ ,  $10 < Q^2 < 105 \text{ GeV}^2$ )

2004 data ( $34 \text{ pb}^{-1}$ ,  $17.5 < Q^2 < 105 \text{ GeV}^2$ )

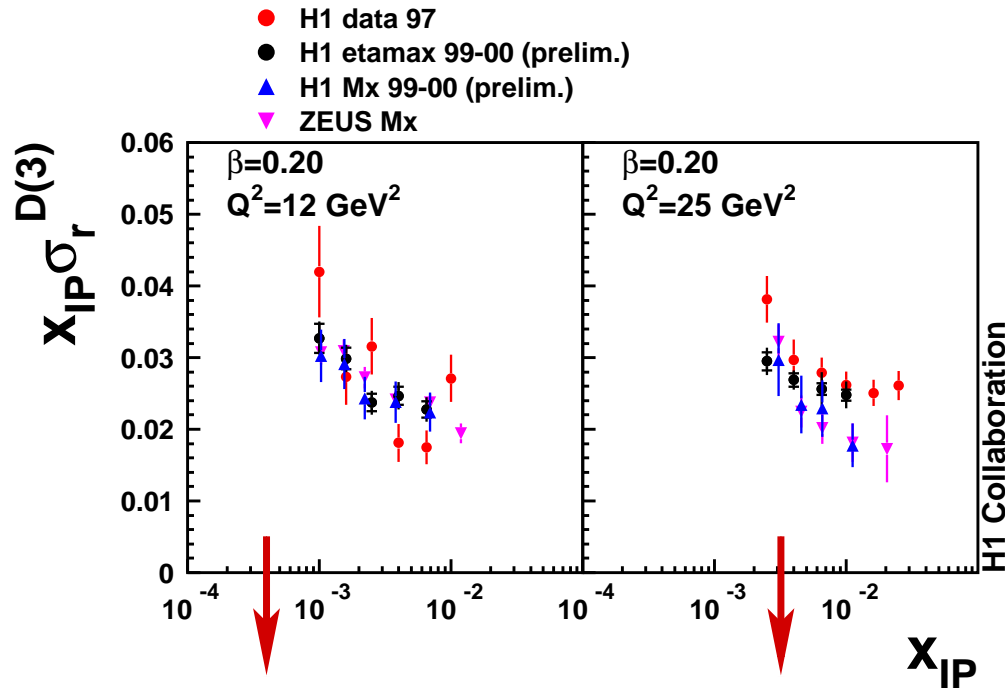
$M_Y < 1.6 \text{ GeV}$ ,  $|t| < 1 \text{ GeV}^2$ ,  $x_P < 0.1$ ,  $M_X > 4 \text{ GeV}$

Precision =  $(3-10)\%_{\text{stat}} \oplus (5-15)\%_{\text{syst}} \oplus (6-8)\%_{\text{norm}}$



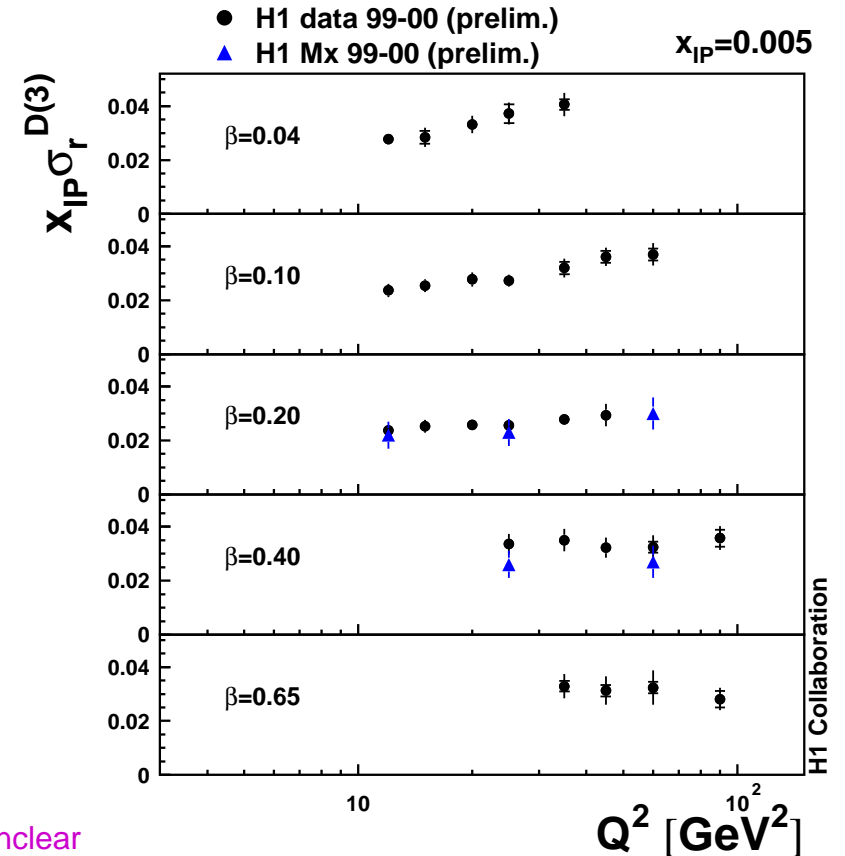
# LRG data: $\eta_{\max}$ vs $M_X$ results

- Compare all data sets in two specific bins



- Bin of typical agreement between data sets and methods

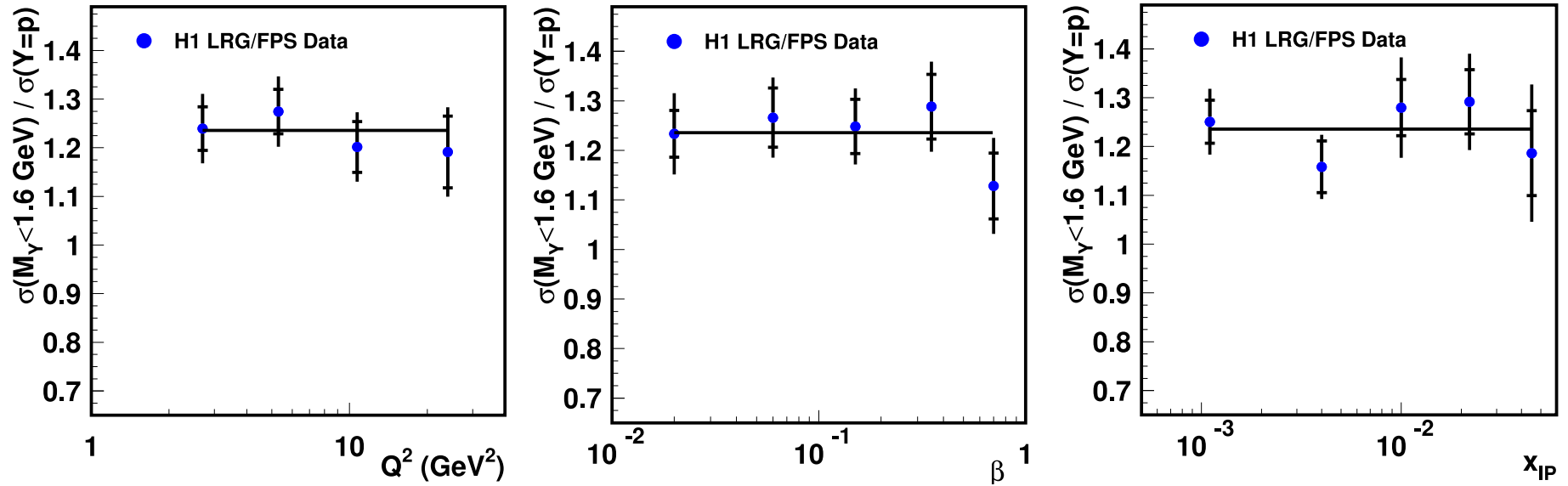
- Bin of worst agreement
  - $\Rightarrow$  large systematics for  $M_X$
  - $\Rightarrow$  syst. difference  $M_X/\eta_{\max}$  unclear



- Good overall agreement between all data samples with only few exceptions
- Too few  $M_X$  points  $\rightarrow$  method is not well adapted to H1 apparatus

## Comparison of LRG vs FPS results

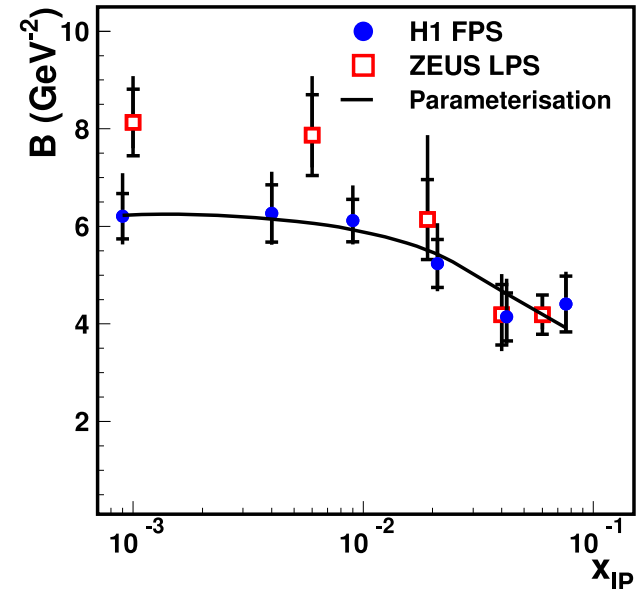
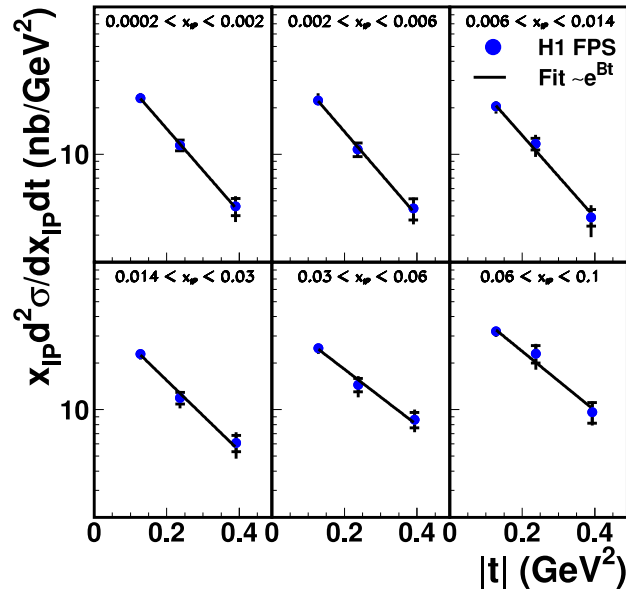
Plot LRG/FPS ratio as a function of  $Q^2$ ,  $\beta$  and  $x_{IP}$  after intergration over the other two:



$$\frac{\sigma(M_Y < 1.6 \text{ GeV})}{\sigma(Y = p)} = 1.23 \pm 0.03(\text{stat}) \pm 0.16(\text{syst})$$

- $M_Y$  dependence factorises within errors (consistent with DIFFVM prediction:  $1.15^{+0.15}_{-0.08}$ )
- Dominant uncertainty arises from the normalisation of FPS and LRG data

# $t$ Dependence and $\alpha'_{\mathcal{P}}$



$B = B_{\mathcal{P}} + 2\alpha'_{\mathcal{P}} \ln(1/x_{\mathcal{P}})$  at small  $x_{\mathcal{P}}$ :

$$\alpha'_{\mathcal{P}} = 0.06^{+0.19}_{-0.06} \text{ GeV}^{-2}$$

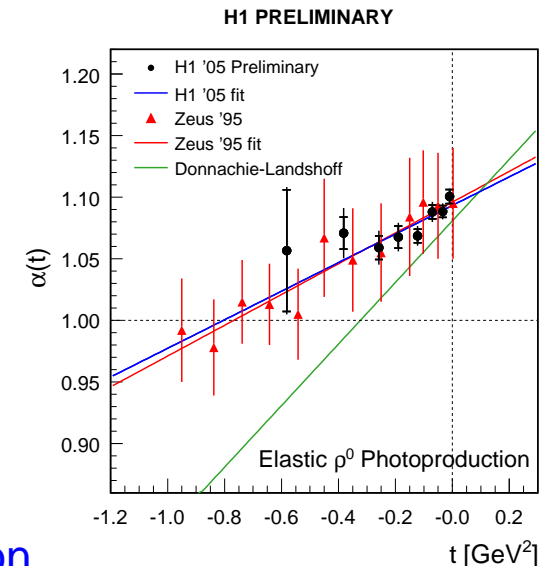
$$B_{\mathcal{P}} = 5.5^{+2.0}_{-0.7} \text{ GeV}^{-2}$$

from fit of  $F_2^{D(4)}$  at large  $x_{\mathcal{P}}$ :

$$\alpha'_{\mathcal{R}} = 0.3^{+0.6}_{-0.3} \text{ GeV}^{-2}$$

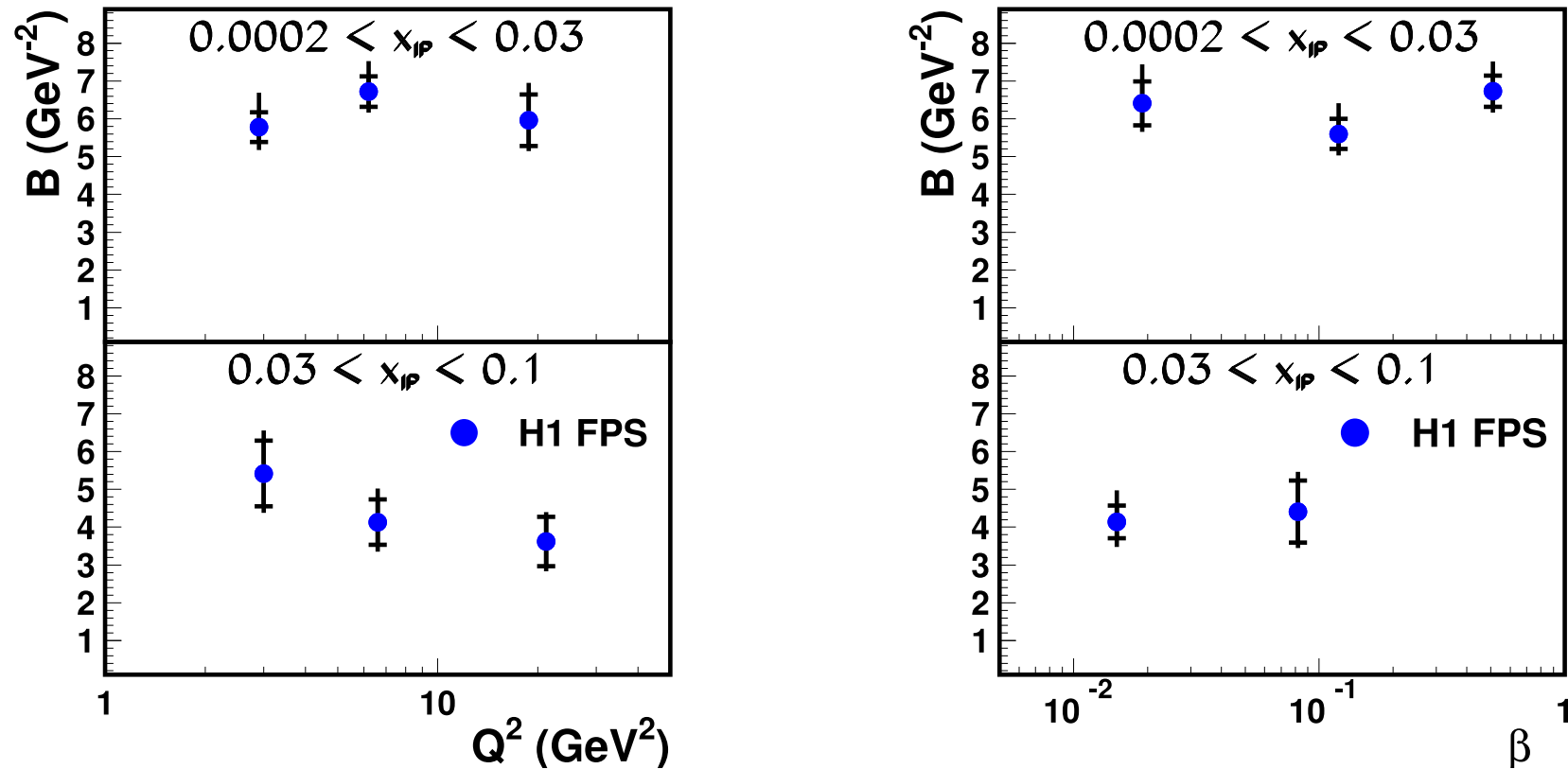
$$B_{\mathcal{R}} = 1.6^{+1.6}_{-0.4} \text{ GeV}^{-2}$$

★ Measured  $\alpha'_{\mathcal{P}}$  is smaller than that in  $hh$  reactions  
and consistent with  $\mathcal{P}$  trajectory measured in VM production





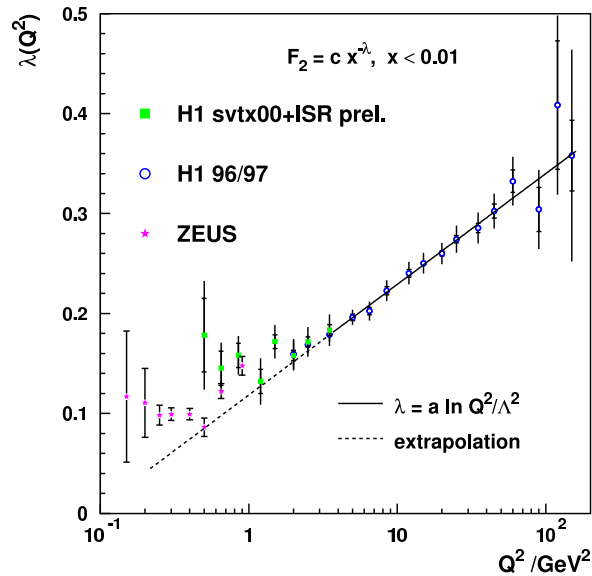
## $t$ slope dependence on $Q^2$ and $\beta$



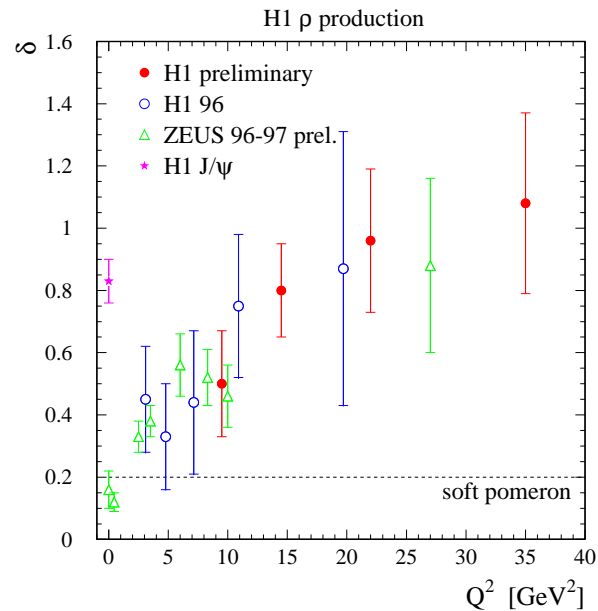
- $t$  dependence does not change with  $Q^2$  or  $\beta$  at fixed  $x_{IP}$
- Supports proton vertex factorisation for  $t$  dependence within errors

Question: what about  $x_{IP}$  dependence and  $\alpha_{IP}(0)$  ?

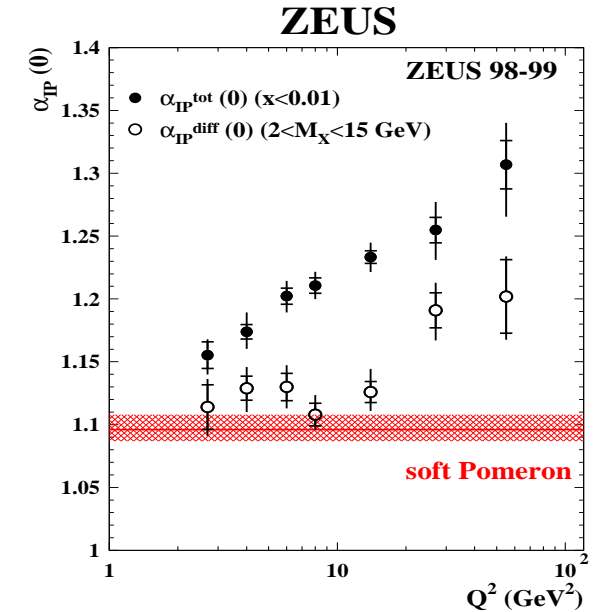
# Pomeron intercept in inclusive, elastic and diffractive DIS



$$\alpha_{\mathbb{P}}(0) = 1 + \lambda$$



$$\alpha_{\mathbb{P}}(0) \simeq 1 + \frac{\delta}{4}$$



- Similar behaviour of  $\alpha_{\mathbb{P}}(0)$  vs  $Q^2$  in inclusive DIS and elastic VM production (expected from Optical Theorem)
- In diffractive DIS more complicated behavior is observed, inconclusive so far (significant extra systematics from  $F_L^D$  and  $\alpha'_{\mathbb{P}}$  uncertainties)

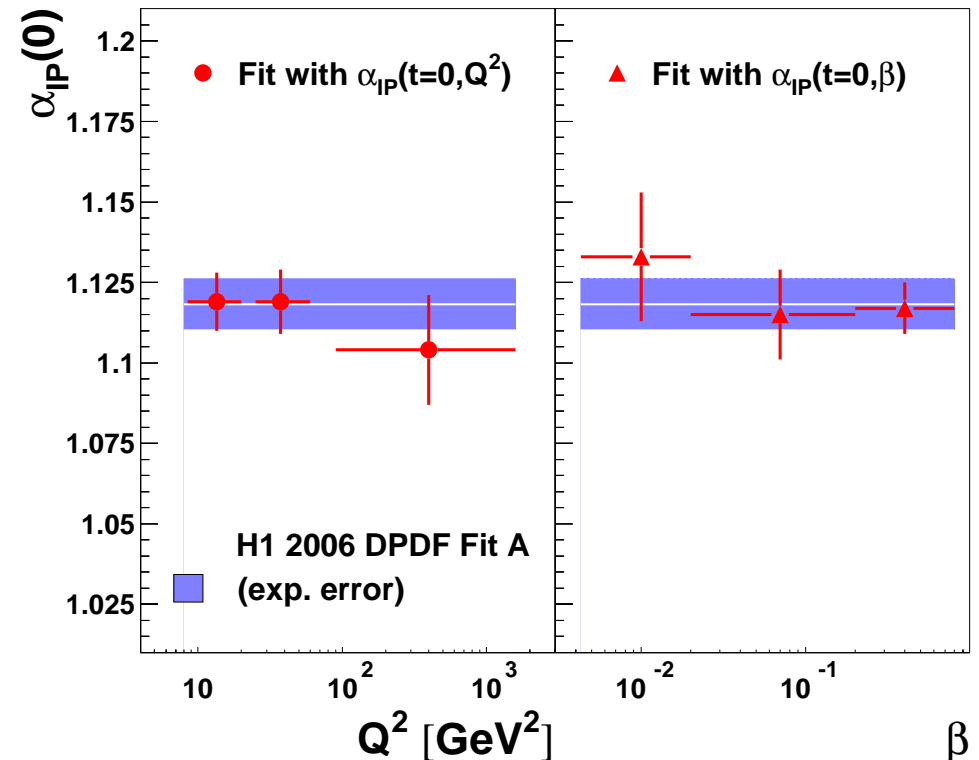
# $x_{\mathbb{P}}$ dependence and Effective Pomeron Intercept

- From FPS data:  $\alpha_{\mathbb{P}}(0) = 1.114 \pm 0.018(\text{stat}) \pm 0.012(\text{syst})_{-0.020}^{+0.040}(\text{model})$

- From QCD fit to LRG data:

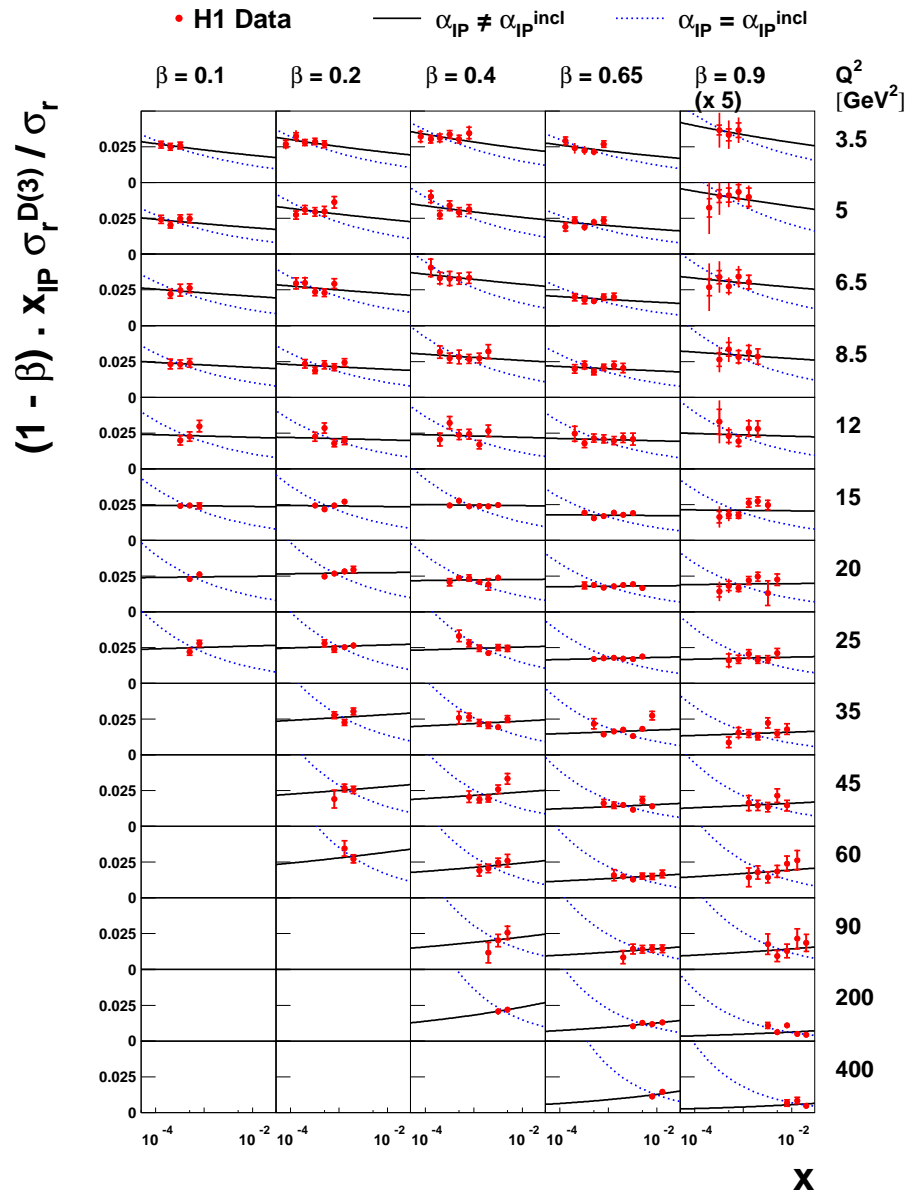
$$\alpha_{\mathbb{P}}(0) = 1.118 \pm 0.008(\text{exp})_{-0.010}^{+0.029}(\text{mod})$$

- Dominant uncertainty arises from strong correlation with  $\alpha'_{\mathbb{P}}$
- No significant variation with  $Q^2$  or  $\beta$  observed
- $\alpha_{\mathbb{P}}(0)$  is only slightly above 'soft Pomeron' value of 1.08

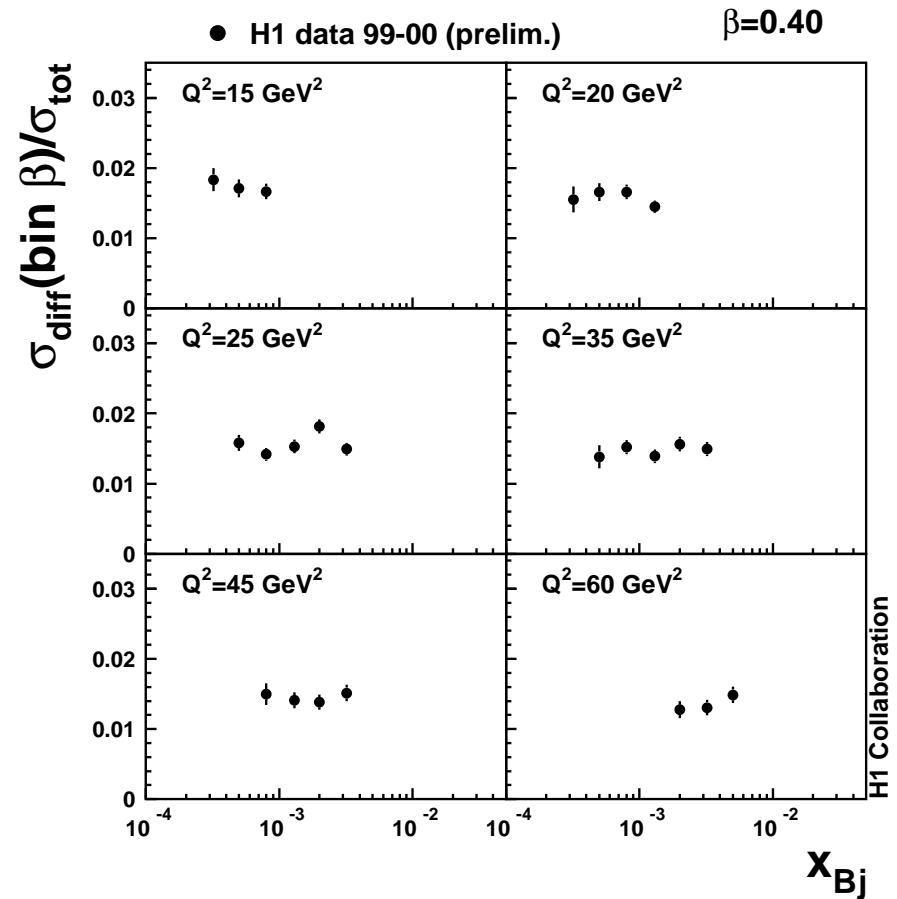


★ Consistent with Regge factorisation hypothesis in studied region

# Diffractive to inclusive ratio $\sigma_r^{D(3)} / \sigma_r$



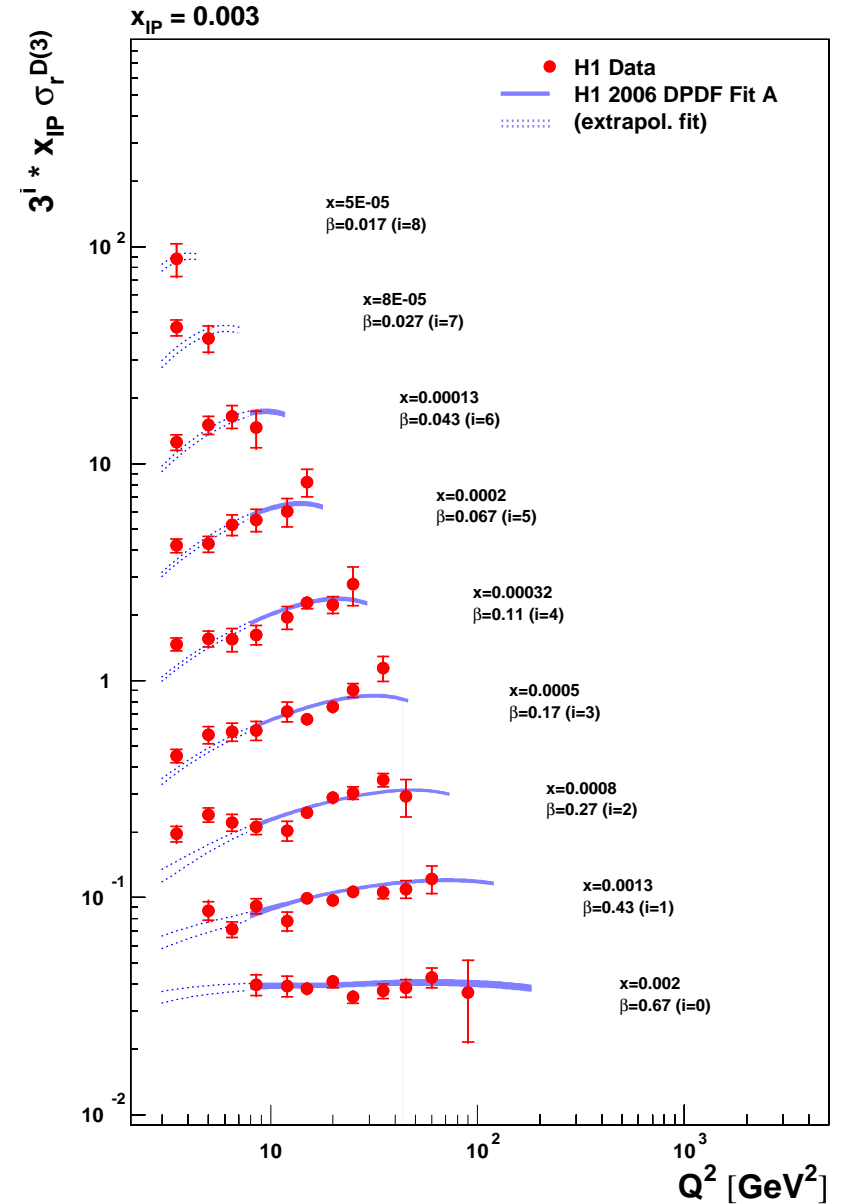
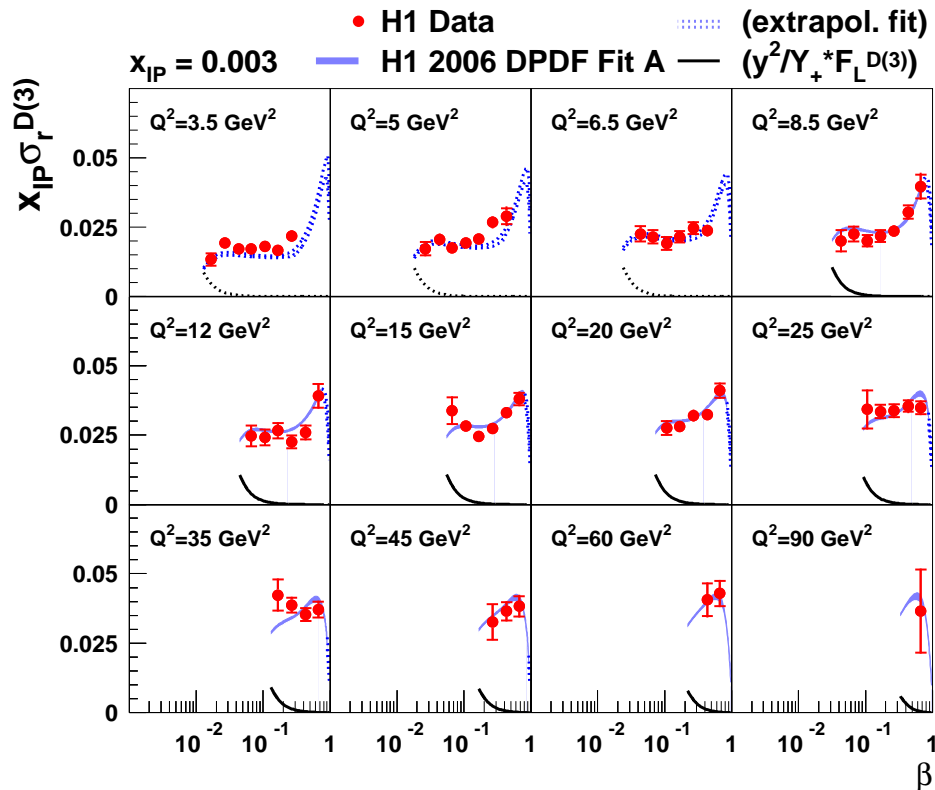
- Remarkably flat in contrast to Regge prediction
- Cannot be described with the same  $\alpha_P(0)$  even if it is  $Q^2$  dependent



# $\beta$ and $Q^2$ Dependence at fixed $x_{\mathbb{P}} = 0.003$

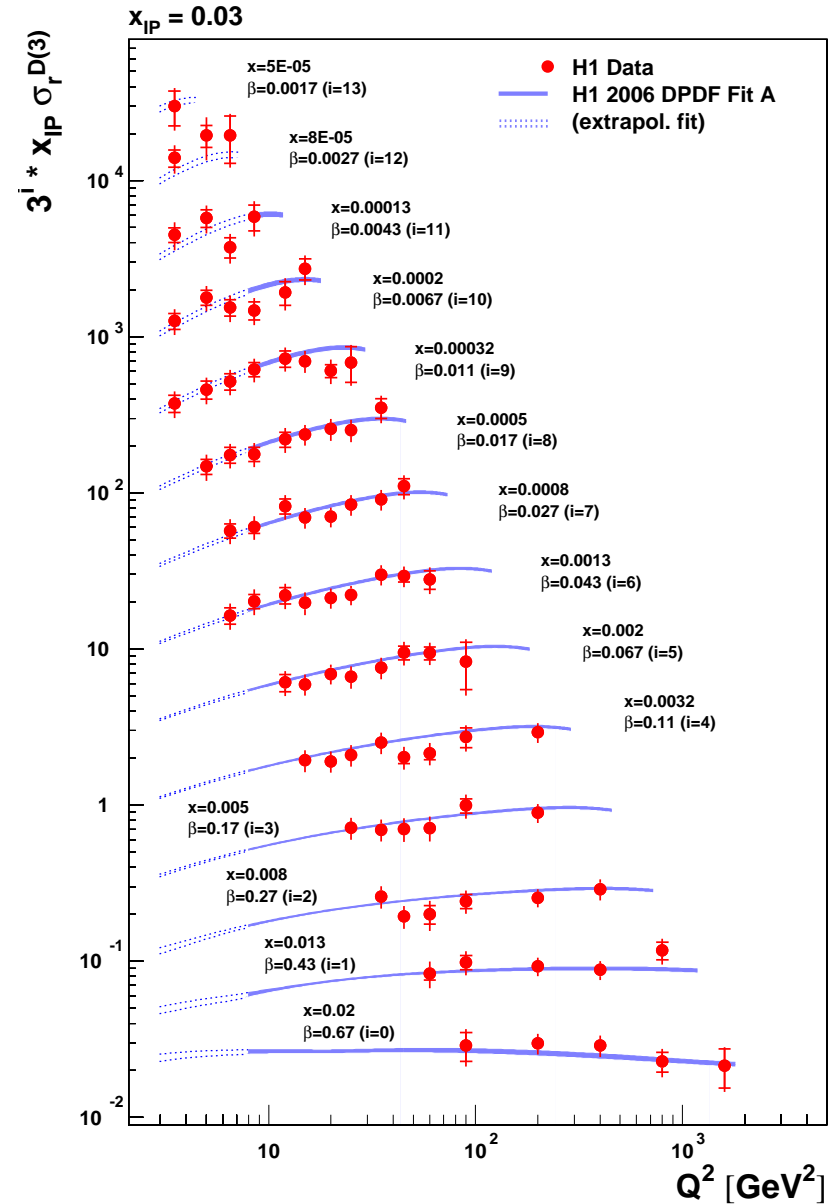
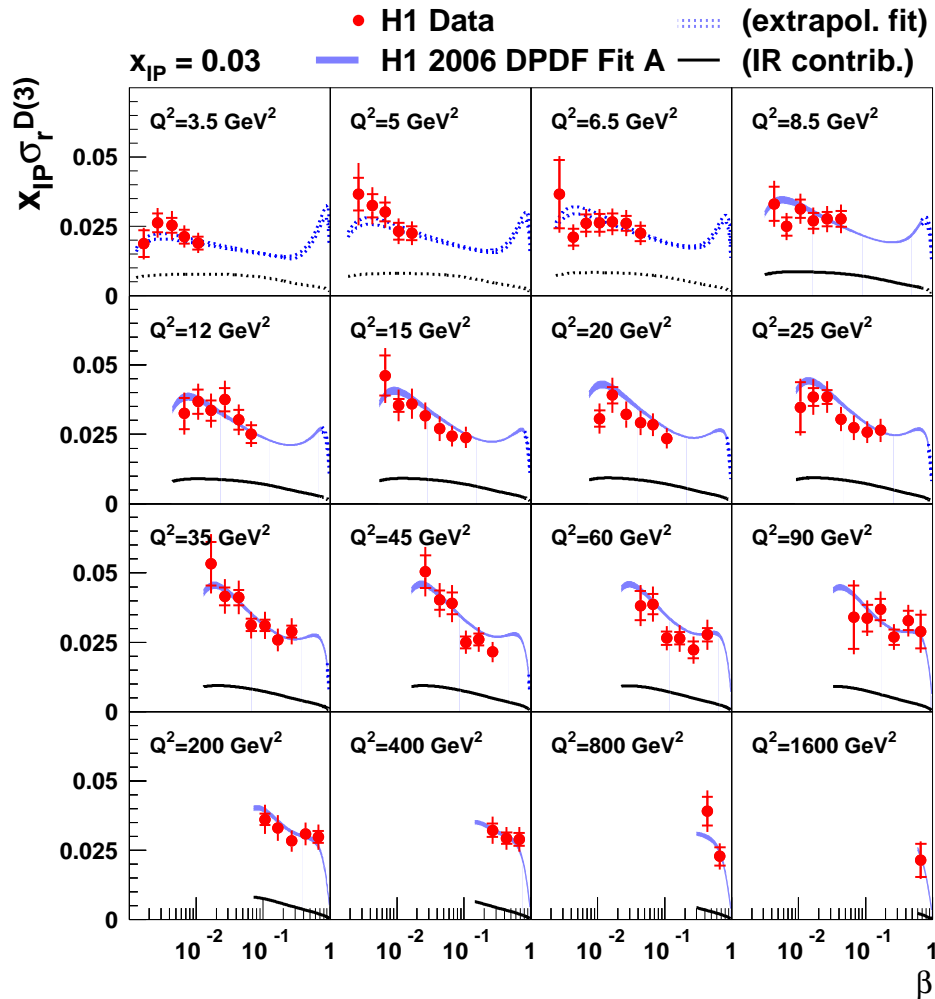
**LRG data:**  $Q^2, \beta$  dependencies at 5 fixed values of  $x_{\mathbb{P}}$  (0.0003, 0.001, 0.003, 0.01, 0.03)

- Data are compared to H1 2006 DPDF Fit and its error band (assuming  $p$ -vertex fact'n)



# $\beta$ and $Q^2$ Dependence at fixed $x_{IP} = 0.03$

Sub-leading ( $\mathcal{R}$ ) contribution becomes important in largest  $x_{IP}$  bin



# NLO QCD Fit

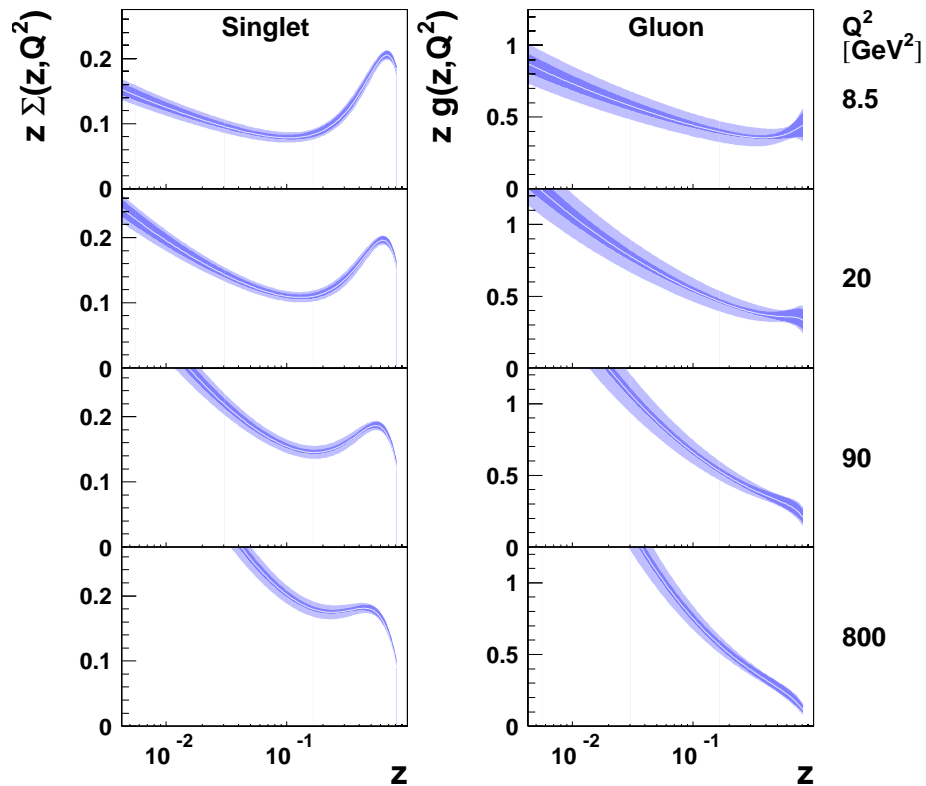
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- Use NLO DGLAP evolution of DPDFs (massive charm,  $\Lambda_{QCD}^{(n_f=3)} = 399 \text{ MeV}$ )
- Assume Regge factorisation for  $p$ -vertex with flux factors  $f_{\mathbb{P},\mathbb{R}} = A_{\mathbb{P},\mathbb{R}} \frac{e^{B_{\mathbb{P},\mathbb{R}}t}}{x_{\mathbb{P}}^{2\alpha_{\mathbb{P},\mathbb{R}}(t)-1}}$
- Parametrisation at starting scale:  $z f_i(z, Q_0^2) = A_i z^{B_i} (1-z)^{C_i}$  with  $Q_0^2$  optimized wrt  $\chi^2$  (Chebyshev polynomials are used as cross-check and provide similar results)
- $\mathbb{R}$  PDFs are taken from Owens- $\pi$  with normalisation as the only free parameter
- Fit 190 data points at 5 fixed  $x_{\mathbb{P}}$  values with  $Q^2 > Q_{\min}^2$  and  $M_X > 2 \text{ GeV}$ ,  $\beta \leq 0.8$   
 $Q_{\min}^2 = 8.5 \text{ GeV}^2$  is chosen from the fit stability requirement
- Free parameters: **Fit A** –  $\alpha_{\mathbb{P}}(0), n_{\mathbb{R}}, A_q, B_q, C_q, A_g, C_g$     **Fit B** –  $C_g = 0$   
 ( $B_g$  is dropped from both fits as the data was found to be insensitive to it)

# H1 2006 DPDF Fit Results

## Fit A (log $z$ scale)

$$Q_0^2 = 1.75 \text{ GeV}^2 \quad \chi^2 \simeq 158/183 \text{ d.o.f.}$$



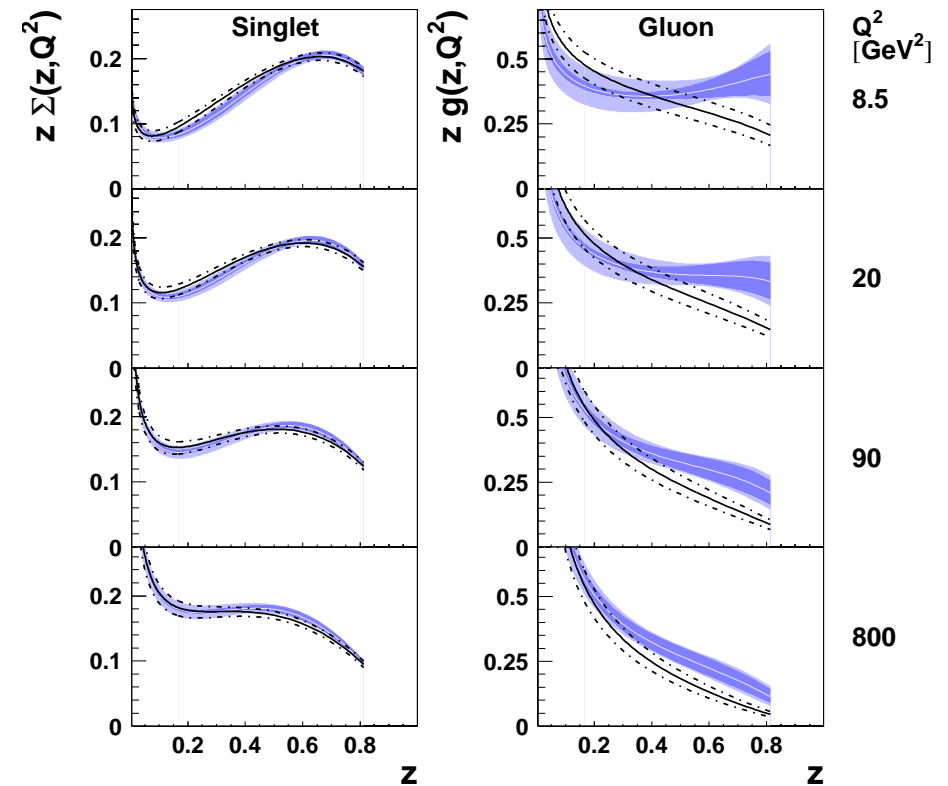
H1 2006 DPDF Fit A  
 (exp. error)  
 (exp.+theor. error)

$\sim 70\%$  gluons  
 integrated over  $z$

☹ Singlet constrained to  $\sim 5\%$

## Fit A vs Fit B (linear $z$ scale)

$$Q_0^2 = 2.5 \text{ GeV}^2 \quad \chi^2 \simeq 164/184 \text{ d.o.f.}$$



H1 2006 DPDF Fit A  
 (exp. error)  
 (exp.+theor. error)

— H1 2006 DPDF Fit B  
 ..... (exp.+theor. error)

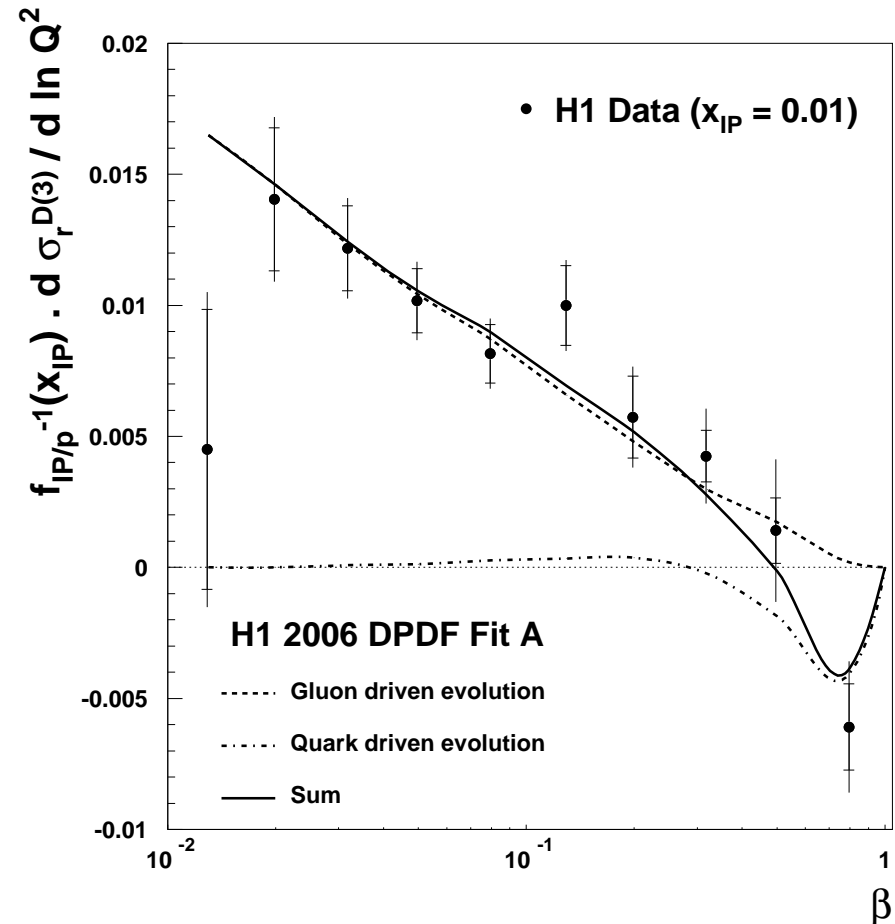
☹ Large gluon variations at high  $z$



## Sensitivity to Gluon at different $z$

$$\frac{dF_2^{D(3)}}{d \ln Q^2} \sim \frac{\alpha_s}{2\pi} [P_{qg} \otimes g + P_{qq} \otimes \Sigma]$$

- Measure normalised  $\ln Q^2$  derivative of  $\sigma_r^{D(3)}$  at fixed  $x_{\mathbb{P}}$  and  $\beta$
- Compare to NLO QCD Fit decomposed into different contributions
- At low  $\beta$ , evolution is driven by  $g \rightarrow qq$ , hence strong sensitivity to gluon
- At high  $\beta$ ,  $q \rightarrow qg$  contribution becomes important; additionally relative error on derivative grows – hence sensitivity to gluon is lost



★ Need other observables directly sensitive to gluon (jets, charm, ...)

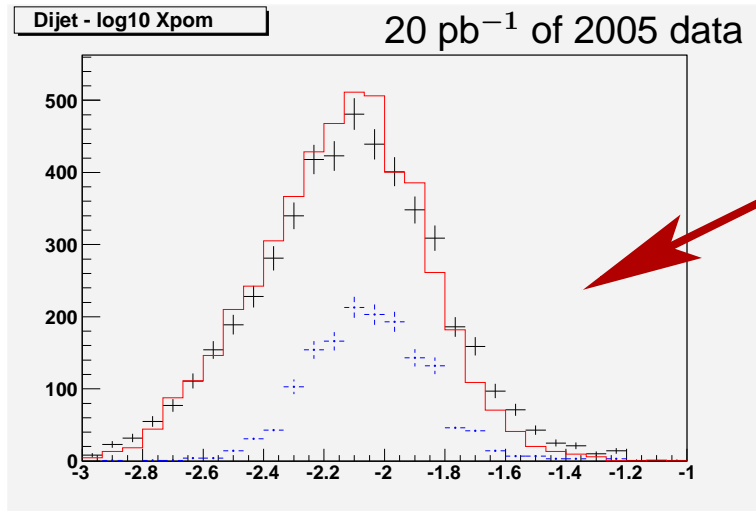
# Summary

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- FPS and LRG measurements based on HERA-1 data are published. New preliminary results are available also from first HERA-2 data. Large kinematic range is covered with good precision. Agreement between data samples and methods
- Within present uncertainties Regge factorisation is compatible with data.  
 $x_{\mathbb{P}}$  dependence is described by  $\alpha_{\mathbb{P}}(t) \simeq 1.118 + 0.06t$
- New set of DPDFs is obtained from NLO QCD fit of  $F_2^{D(3)}$  at  $Q^2 > 8.5 \text{ GeV}^2$ :
  - singlet quarks well constrained ( $\sim 5\%$ )
  - gluon is known to  $\sim 15\%$  in low  $z$  region and poorly constrained at high  $z$
- Over the bulk of the measured range the ratio of diffractive to inclusive cross sections is remarkably flat as a function of energy at fixed  $Q^2$  and  $M_X$ , in contrast to naïve Regge expectation
- In future need to improve experimental precision and consolidate theoretical framework (soft vs hard Pomeron, rôle of inhomogeneous term, evidence for 'direct  $\mathbb{P}$ ' in data?)

# Outlook

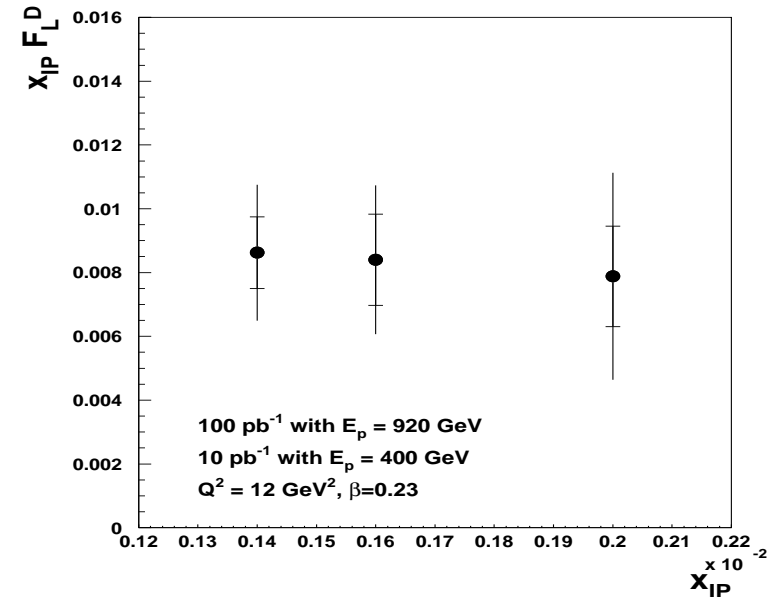
**Experimental part:** Full use of HERA-2 data (Q: nothing is forgotten? Only one year remains)



- 20 times more FPS data ( $\mathcal{L}$ , running eff., detector eff.)
- New VFPS pots with high acceptance (40% at  $x_P \sim 0.01$ )

⇒ test factorisation in more detail:  $\alpha_P(Q^2, \beta)$

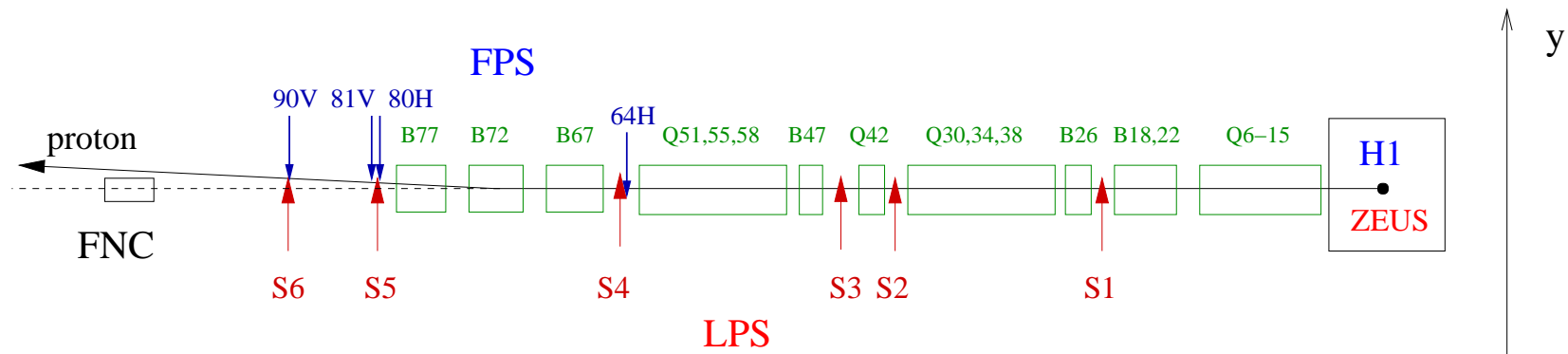
- 10-15 pb<sup>-1</sup> with reduced  $E_p$  running ⇒ Measure  $F_L^D$ 
  - reduce  $F_L^D$  uncertainty contribution to syst.errors
  - direct sensitivity to gluon, better constrain DPDFs



**Theory part:** Consolidate the framework (HERA-LHC Workshop)

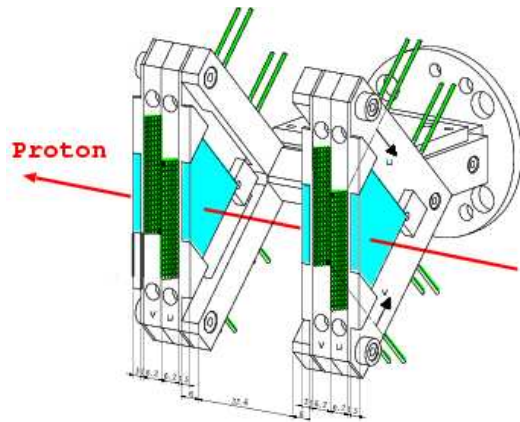
BACKUP SLIDES...

# HERA I Proton Spectrometer

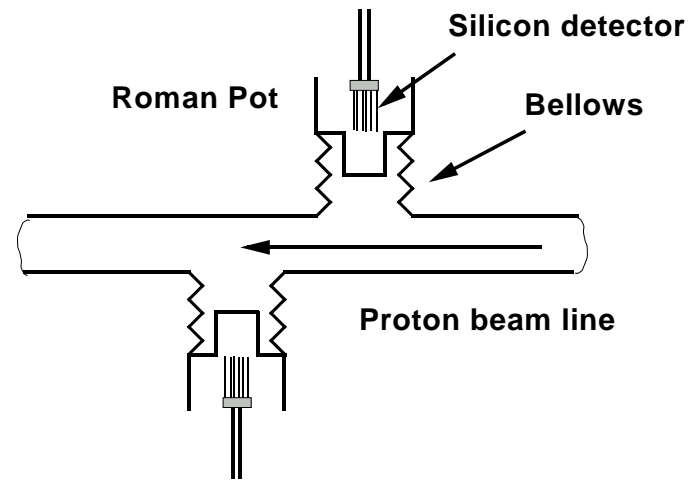


Forward Proton Spectrometer

Leading Proton Spectrometer



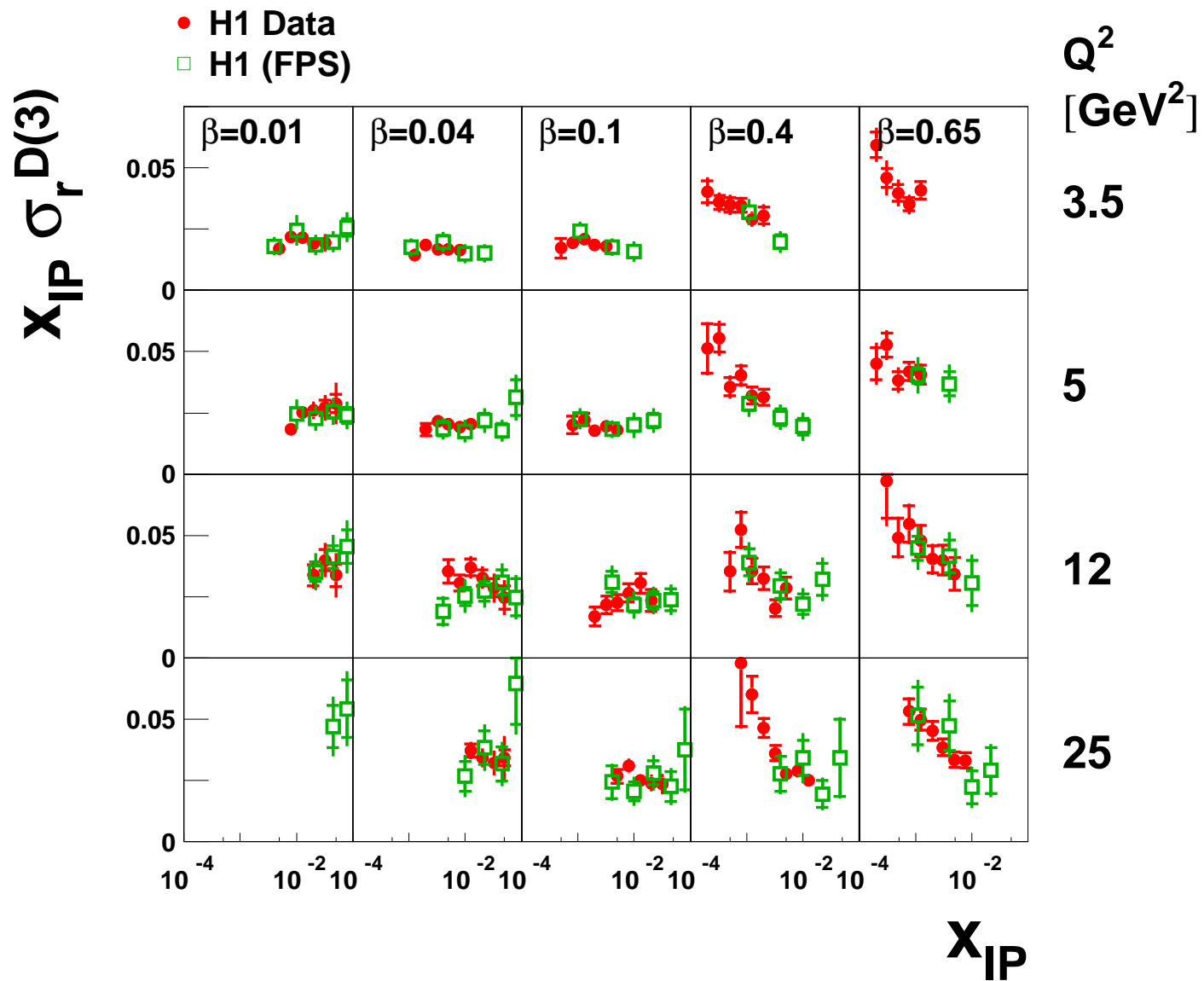
Scintillating fibre detector



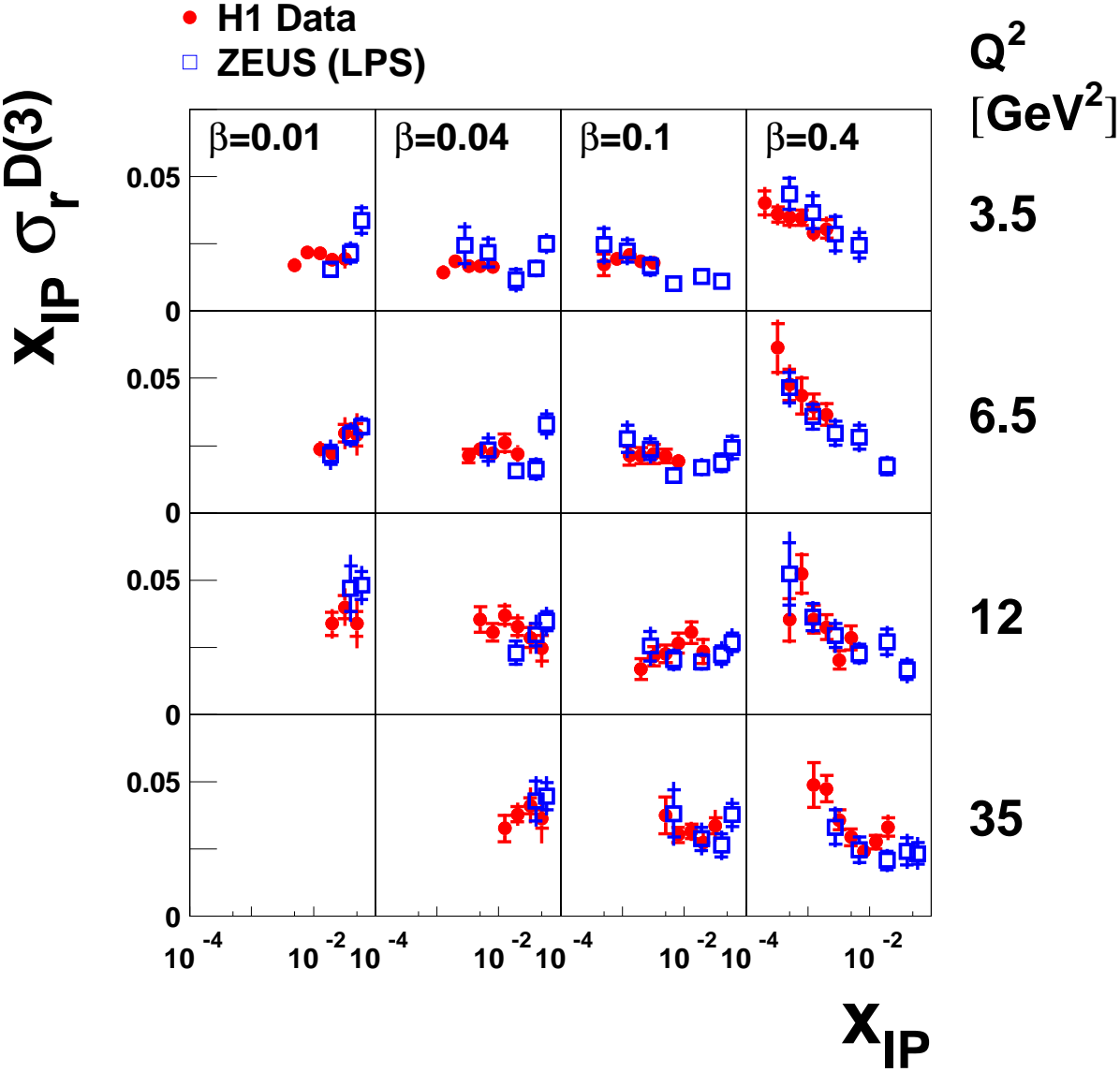
Silicon Micro-Strip Detector

- Free of dissociation bkgd
- p 4-momentum measurement  $\rightarrow t$
- Low statistic (acceptance)

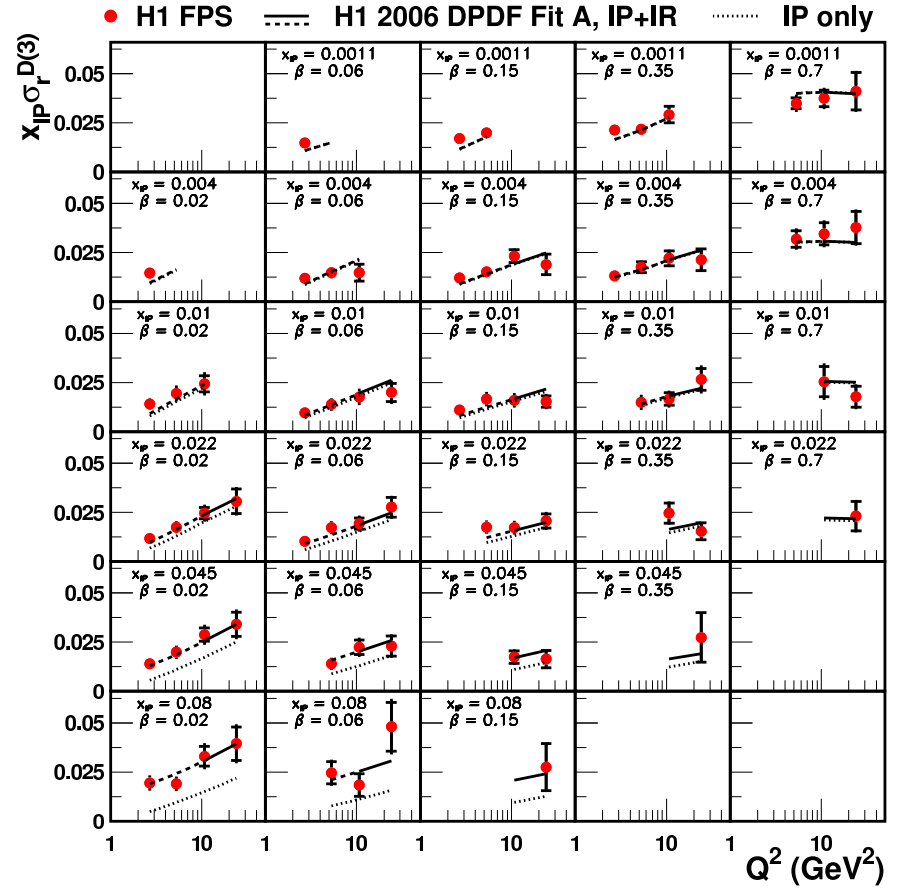
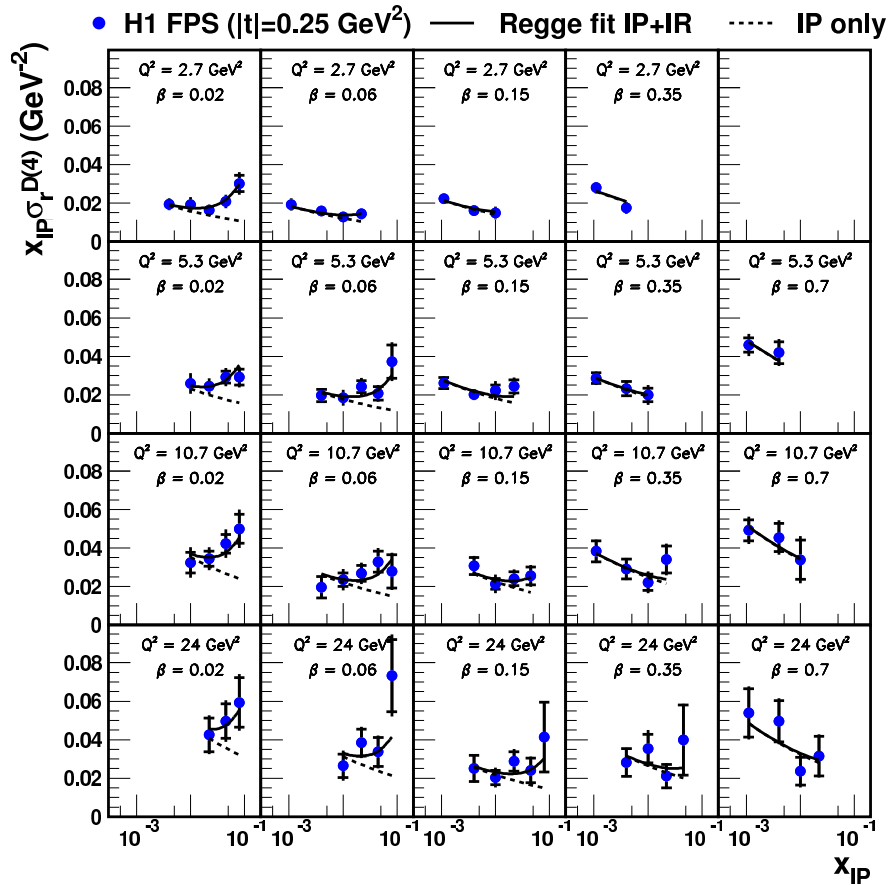
# LRG vs FPS data in fixed $Q^2$ , $\beta$ binning scheme



# LRG(H1) vs LPS(ZEUS) data

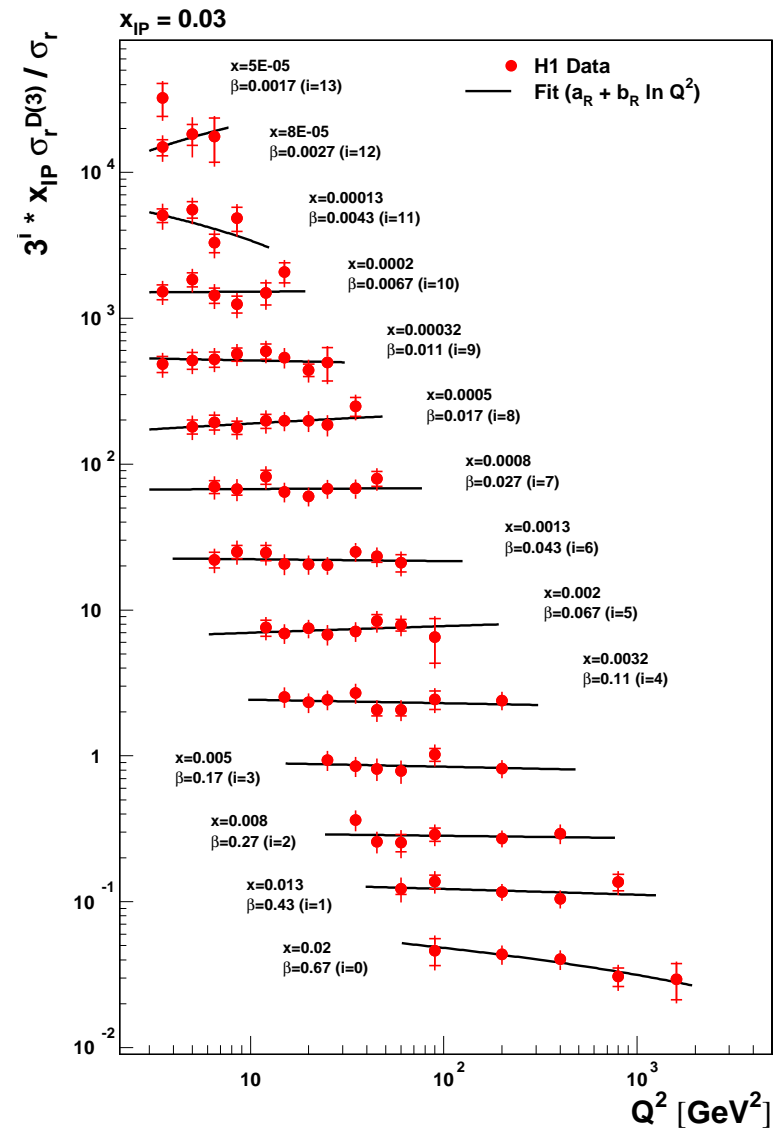
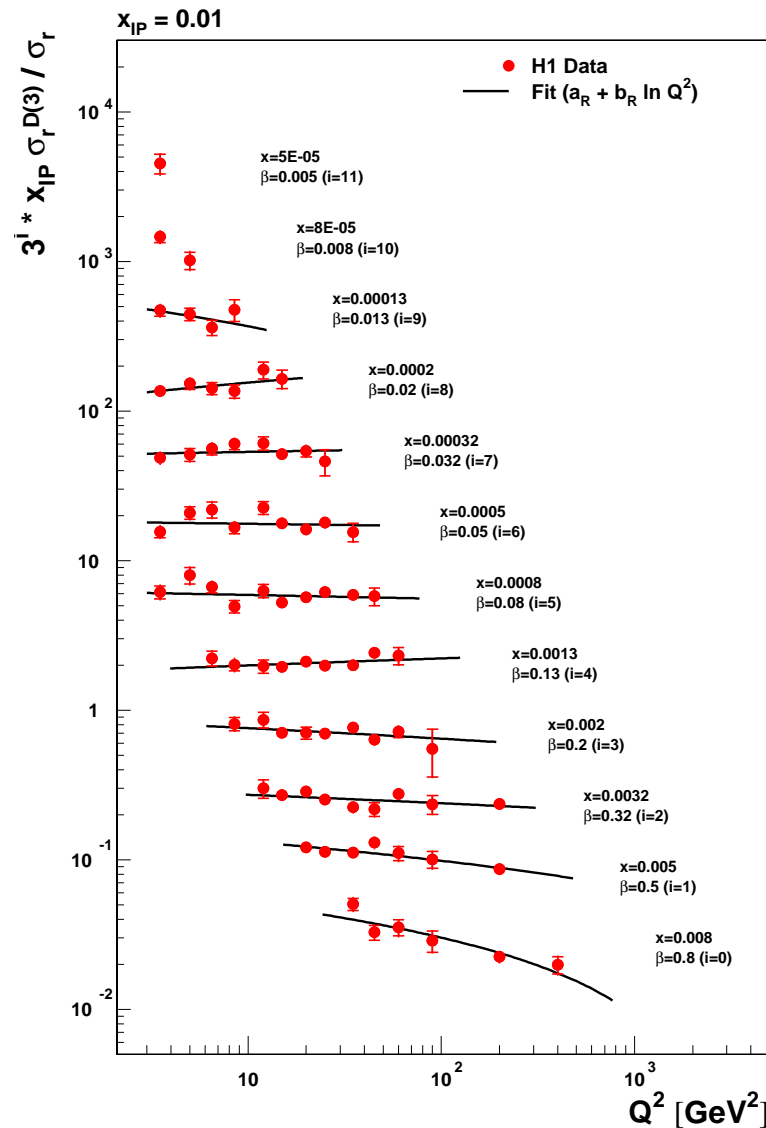


# FPS $F_2^{D(4)}$ and $F_2^{D(3)}$ compared to H1 2006 DPDF Fit results





# Diffractive to inclusive ratio $\sigma_r^{D(3)} / \sigma_r$ vs $Q^2$



# Diffractive CC cross sections

