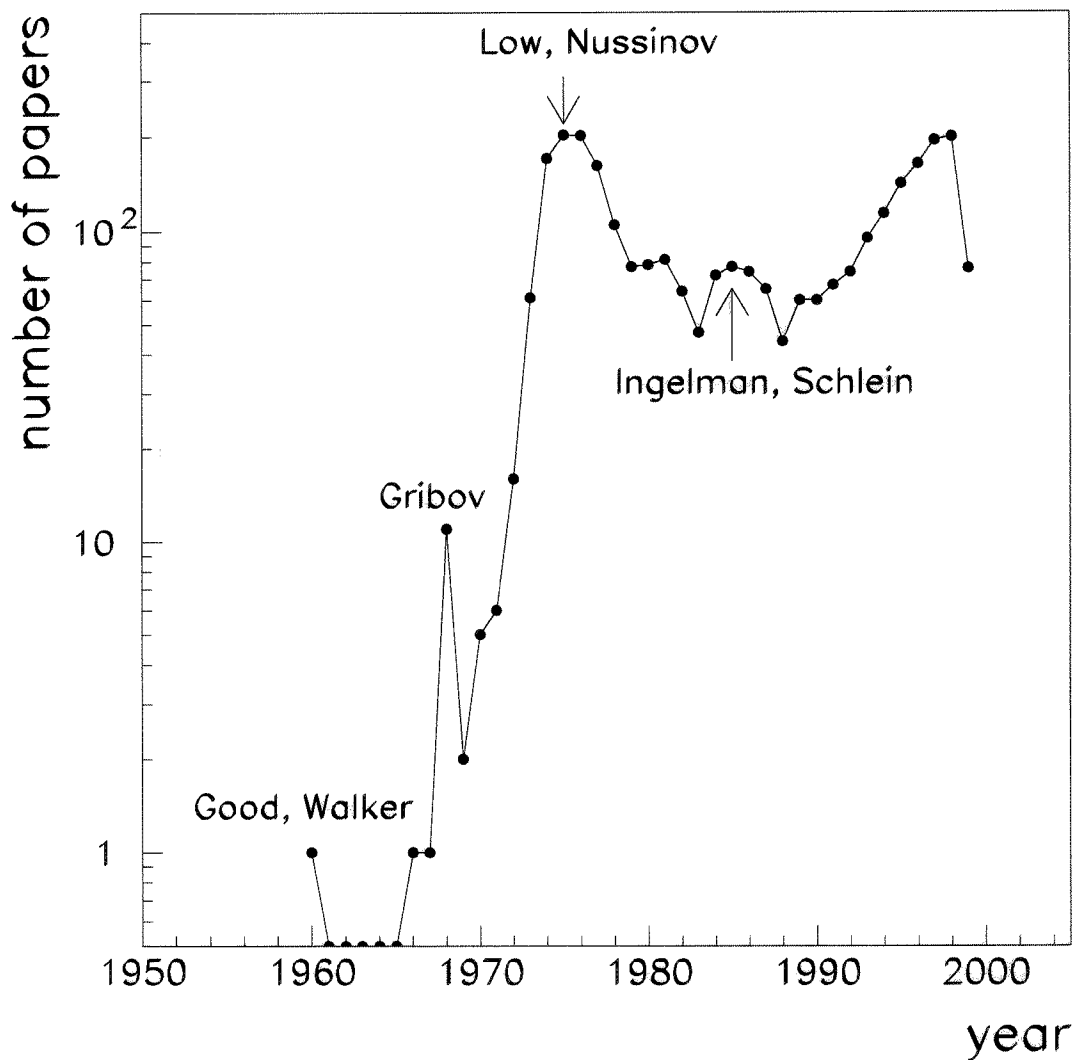


# Diffraction and the Pomeron

Halina Abramowicz (Tel Aviv University)  
Stanford, August 1999

- Introduction
- Inclusive processes - diffractive parton distributions
- Exclusive production of vector mesons - hard diffraction
- Hard color singlet exchange
- Double gaps
- Conclusions

## History of diffraction



Good and Walker : different components of the projectile absorbed differently by target  $\Rightarrow$  new physical states

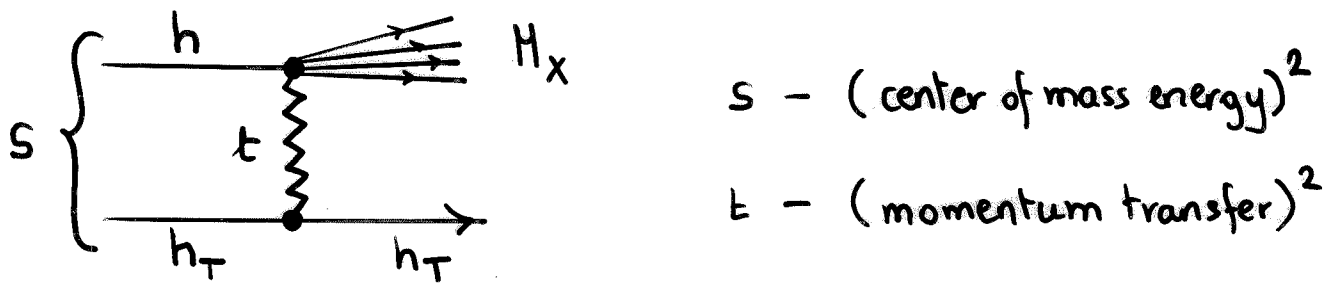
Gribov : Reggeon calculus and the  $\mathbb{P}$

Low, Nussinov :  $\mathbb{P}$  in QCD  $\approx$  2 gluon exchange

Ingelman, Schlein : perturbative QCD description of the  $\mathbb{P}$

# Diffractive Scattering

definition by description



quantum numbers of the target are preserved

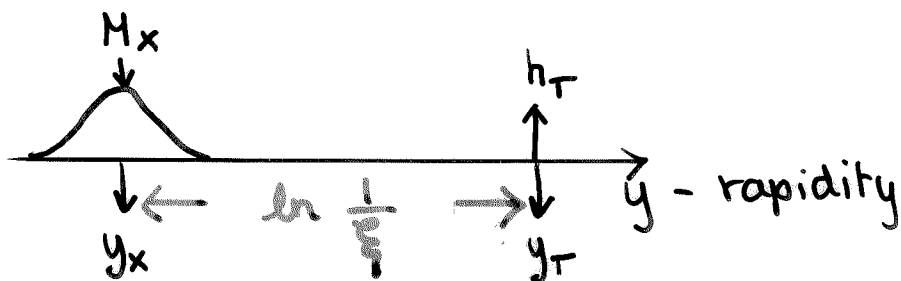
Coherence requires

- $\sqrt{|t|} < \frac{1}{R_T}$        $R_T - \text{radius of the target}$   
 $f(t) \sim e^{-b|t|}$        $b \approx \frac{R_T^2}{6}$

- $|t_{\text{min}}| = \left[ \frac{(M_x^2 - m_T^2) m_T}{s} \right]^2 \approx \left( \frac{M_x^2}{s} \right)^2$

$$x_P \equiv \frac{1}{\xi} = \frac{M_x^2}{s} < \frac{1}{R_T} \approx 0.15 \div 0.20$$

- presence of a large rapidity gap



$$\Delta y = y_T - y_x = \ln \frac{s}{m_T M_x} \approx \ln \frac{1}{\xi} > 2$$

- In the  $t$  channel exchange of quantum numbers of vacuum  $\Rightarrow$  Pomeron

# Pomeron $\mathbb{P}$

- derived by Gribov in Reggeon calculus  
right most singularity in the complex  
angular momentum plane - universal

- named Pomeron by Gell-Mann

Pomeranchuk theorem:

$$\text{for } s \rightarrow \infty \quad \sigma(hh) = \sigma(h\bar{h})$$

- parametrized by Donnachie and Landshoff

$$\alpha_{\mathbb{P}}(t) = 1 + \epsilon + \alpha' t$$

$$\epsilon = 0.08$$

(from  $\sigma_{\text{tot}}$   $\pi p, K p, p p, \bar{p} p$ )

$$\alpha' = 0.25 \text{ GeV}^{-2}$$

(from elastic  $pp$ )

$\mathbb{P}$ : universal Regge trajectory with quantum numbers of vacuum

Regge phenomenology: for  $s \gg m, t$

$$\sigma_{\text{tot}}(ab) \sim s^{\alpha_{\mathbb{P}}(0) - 1}$$

$$\frac{d\sigma_{\text{el}}}{dt}(ab \rightarrow ab) = \frac{\sigma_{\text{tot}}^2(ab)}{16\pi} e^{2(b_0^{\text{el}} + \alpha' \ln s)t}$$

$$\begin{aligned} \frac{d^2\sigma_{\text{D}}}{dt dM_X^2}(ab \rightarrow Xb) &\sim \frac{1}{M_X^2} \left(\frac{s}{M_X^2}\right)^{2(\alpha_{\mathbb{P}}(t) - 1)} \\ &\sim \frac{1}{M_X^2} \left(\frac{s}{M_X^2}\right)^{2(\alpha_{\mathbb{P}}(0) - 1)} e^{2(b_0^{\text{sd}} + \alpha' \ln \frac{s}{M_X^2})t} \end{aligned}$$

- $\sigma_{\text{el}}/\sigma_{\text{tot}}$  &  $\sigma_{\text{D}}/\sigma_{\text{tot}} \sim s^{\alpha_{\mathbb{P}}(0) - 1}$  (unitarity limit?)

- shrinkage of the  $t$  slope

- large enhancement of  $\frac{d\sigma_{\text{D}}}{dx_{\mathbb{P}}} \sim \left(\frac{1}{x_{\mathbb{P}}}\right)^{1+2\epsilon}$

# Diffraction and QCD

In QCD/PAM large rapidity gaps from ONE parton radiation are suppressed

$$P(\text{LRG} = \Delta y) \sim e^{-C_P(\alpha_s, \mu) \Delta y}$$

⇒ diffraction in QCD through interacting partons

Tests of our understanding of QCD dynamics

⇒  $\mathbb{P}$  in QCD  $\equiv$  search for dynamical origin of rapidity gaps  $\Rightarrow$  color singlet exchange

Simplest model of  $\mathbb{P}$  = 2 gluon exchange  
(Low, Nussinov)

Confusion: In QCD rapidity gaps are not universal

The  $\mathbb{P}$  trajectory is universal in soft interactions

In the unlucky case that we don't understand QCD dynamics the alternative is

$\mathbb{P}$  à la Ingelman and Schlein, universal with partonic structure to be probed as that of hadrons  $\leftarrow$  partonic content of strong interactions

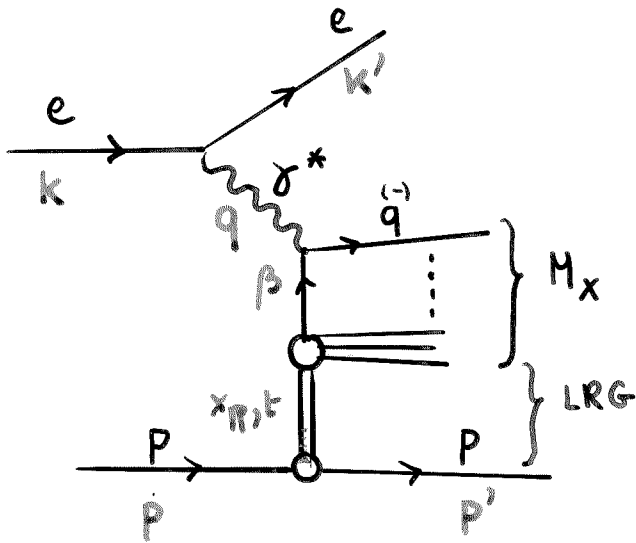
# Diffraction at HERA

$$ep \rightarrow epX$$

$$E_e = 27.5 \text{ GeV}$$

$$E_p = 820 \text{ GeV} \quad (\text{H1, ZEUS})$$

$$E_p = m_p \quad (\text{HERMES})$$



$$Q^2 = -q^2 = -(k-k')^2$$

$$W = (q+p)^2$$

$$t = (p-p')^2$$

$$x = \frac{Q^2}{2p \cdot q}$$

$$y = \frac{p \cdot q}{p \cdot k}$$

Additional variables:

$$\left(\frac{e}{p}\right) x_p = \frac{q \cdot (p-p')}{q \cdot p} = \frac{Q^2 + M_x^2 - t}{Q^2 + W^2 - m_p^2} \approx \frac{Q^2 + M_x^2}{Q^2 + W^2}$$

→ fraction of the proton momentum transferred to the "exchange"

$$\beta = \frac{Q^2}{2(p-p') \cdot q} = \frac{Q^2}{Q^2 + M_x^2 - t} \approx \frac{Q^2}{Q^2 + M_x^2}$$

→ fraction of the "exchange" momentum carried by the quark

$$\beta \cdot x_p = x$$

# Diffraction structure function $F_2^D$

$$\frac{d^4 \sigma(ep \rightarrow epX)}{dx_{\mathbb{P}} dt dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} (1+(1-y)^2) \frac{d^2 F_2^D(x_{\mathbb{P}}, t, x, Q^2)}{dx_{\mathbb{P}} dt}$$

( $\sigma_L/\sigma_T$  neglected)

- QCD factorization holds for diffractive DIS  
(Collins, Berger & Soper, Trentadue & Veneziano)

$$\frac{d^2 F_2^D(x_{\mathbb{P}}, t, x, Q^2)}{dx_{\mathbb{P}} dt} = \sum_i \int dz \frac{d^2 f_{i/p}^D(x_{\mathbb{P}}, t, z, \mu^2)}{dx_{\mathbb{P}} dt} \hat{F}_i\left(\frac{x}{z}, \frac{Q^2}{\mu^2}\right)$$

$\uparrow$  diffractive parton distribution functions (DPDF)       $\uparrow$  hard scatt. same as for inclusive DIS (pQCD)

DPDFs evolve in  $z$  and  $\mu^2$  following DGLAP equations as the proton PDFs

$$z = x_{\mathbb{P}} \cdot \beta \quad \Rightarrow \quad \text{for fixed } x_{\mathbb{P}} \text{ evolution in } \beta$$

- If postulate Regge factorization (Ingelman & Schlein)

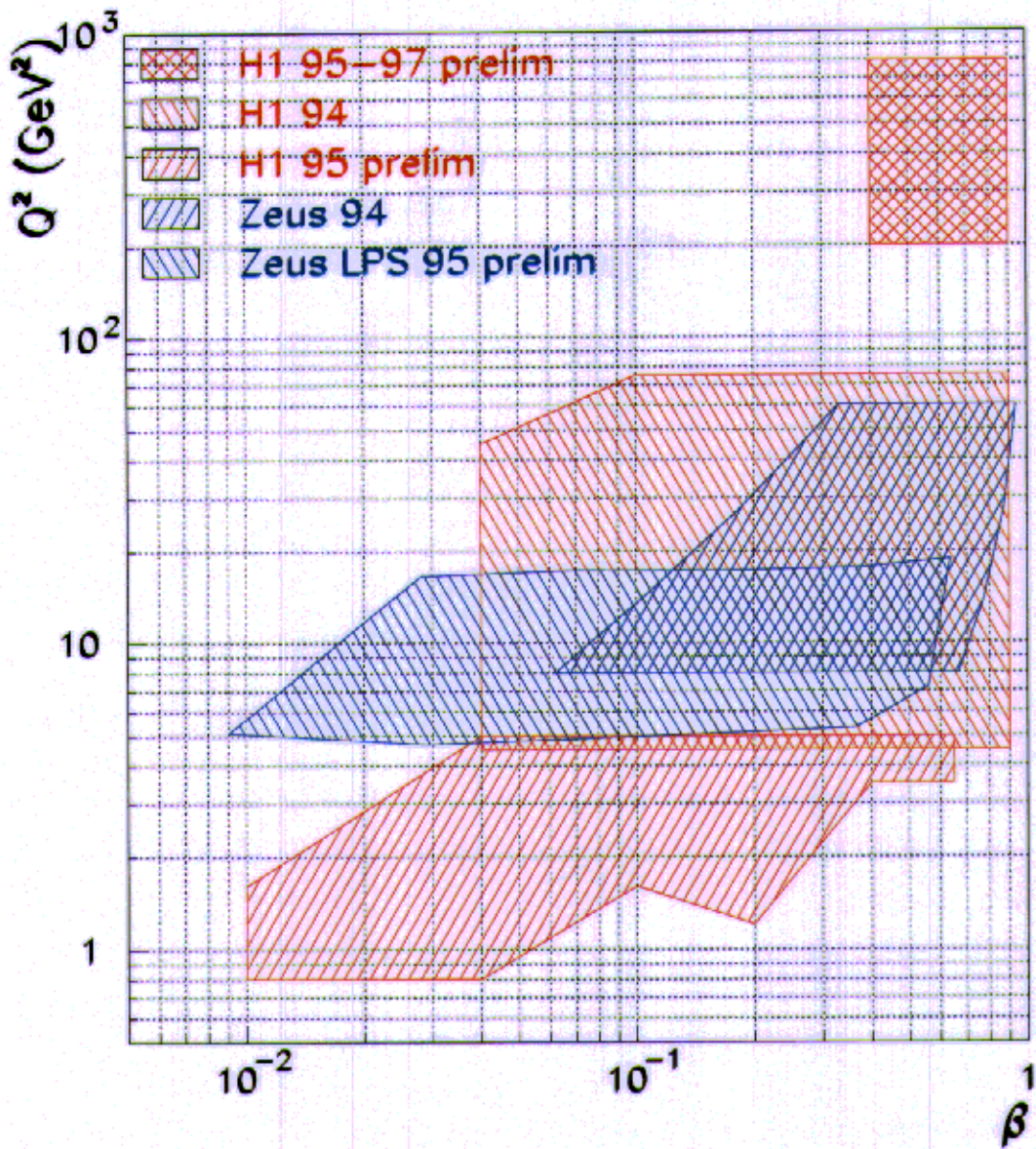
$$\frac{d^2 F_2^D(x_{\mathbb{P}}, t, x, Q^2)}{dx_{\mathbb{P}} dt} = f_{\mathbb{P}/p}(x_{\mathbb{P}}, t) F_2^{\mathbb{P}}(\beta, Q^2)$$

note:

$$F_2^{D(4)} \equiv \frac{d^2 F_2^D}{dx_{\mathbb{P}} dt}$$

$$F_2^{D(3)} \equiv \int dt \frac{d^2 F_2^D}{dx_{\mathbb{P}} dt}$$

# Diffractive Structure Function $F_2^{D(3)}$

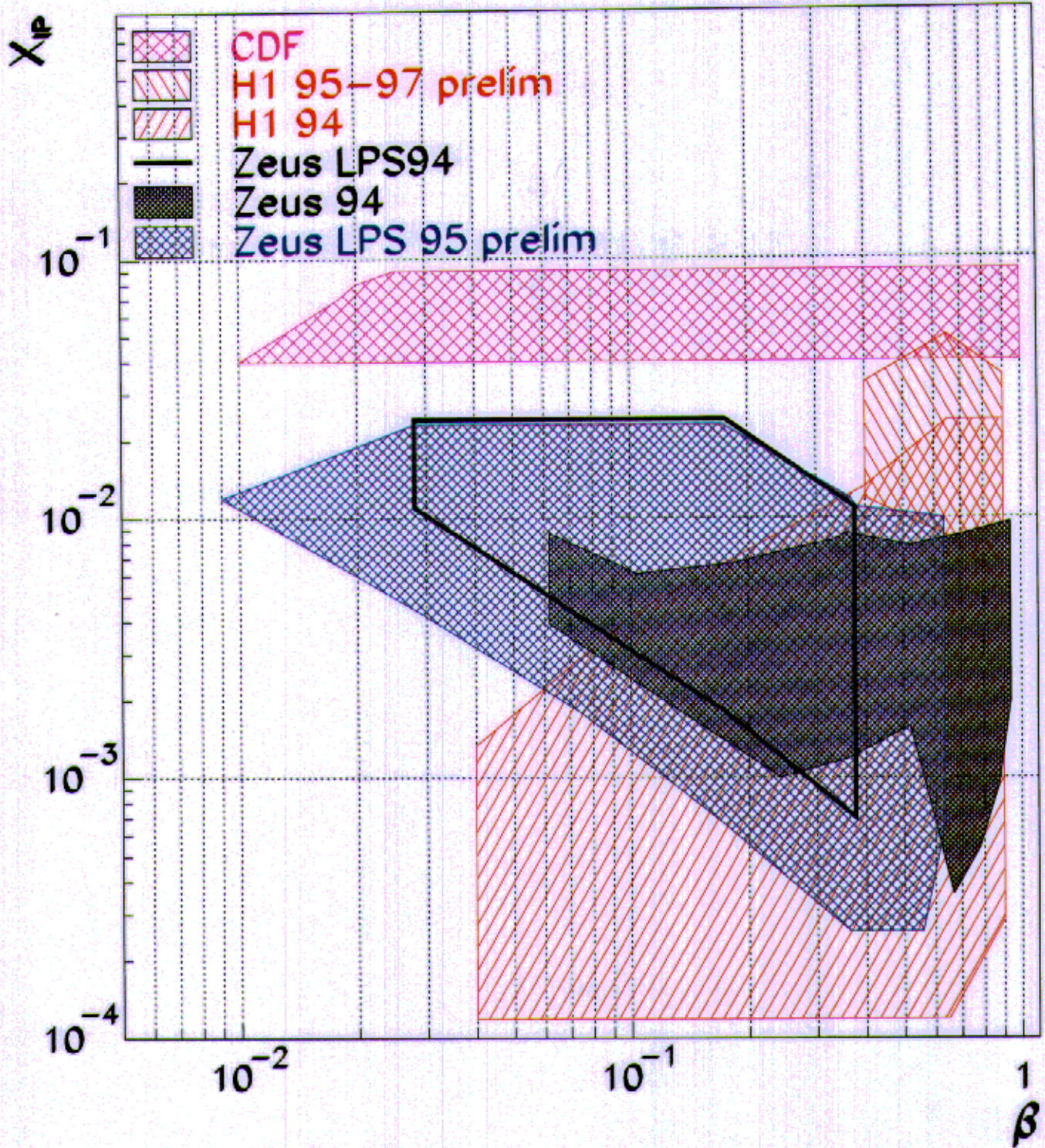


$$10^{-4} < x_{\text{pp}} \leq 0.05$$

Large fraction of events with LRG

10% ÷ 15%





# Energy dependence in $\gamma^*p$ - summary

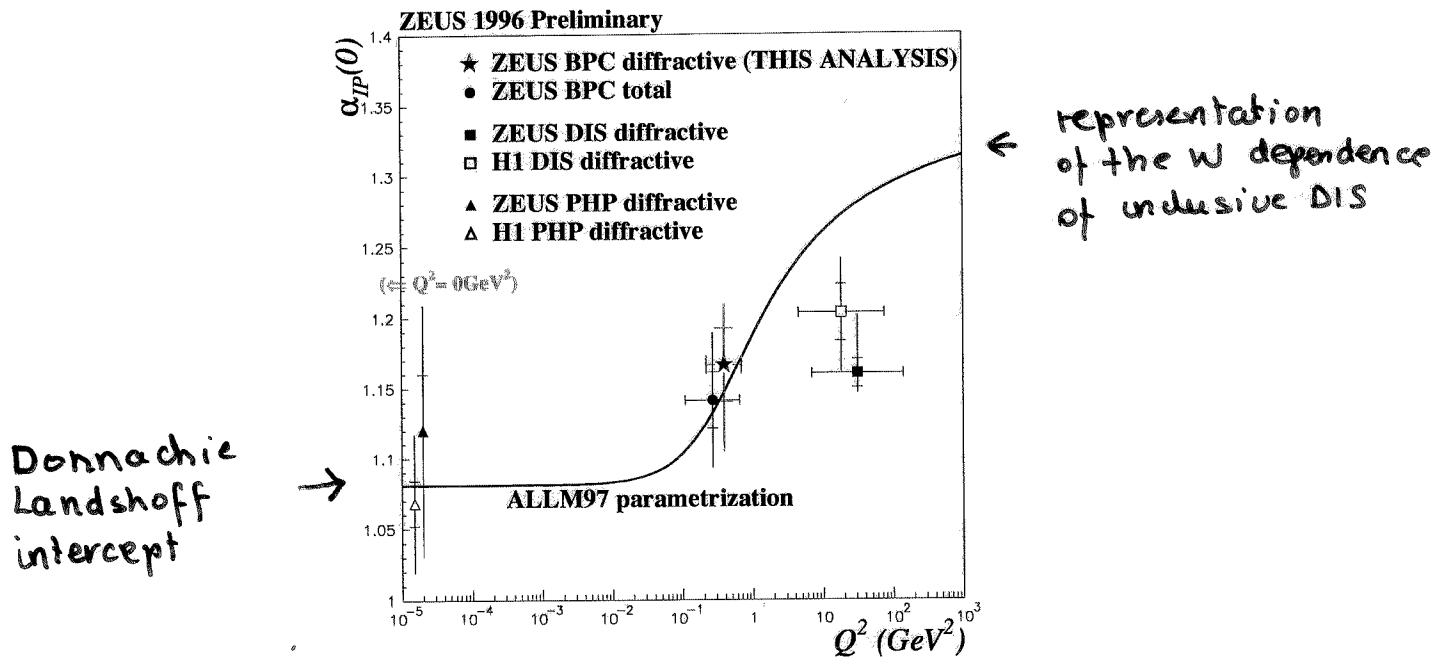
Check Regge factorization:  $x_P F_2^{D(3)}(x_P, \beta, Q^2) = \frac{C(\beta, Q^2)}{x_P^{2\bar{\alpha}_P - 2}}$

$$\alpha_P(0) = \bar{\alpha}_P + \frac{\alpha'_P}{b}$$

b slope measured with ZEUS LPS - no  $Q^2$  dependence found

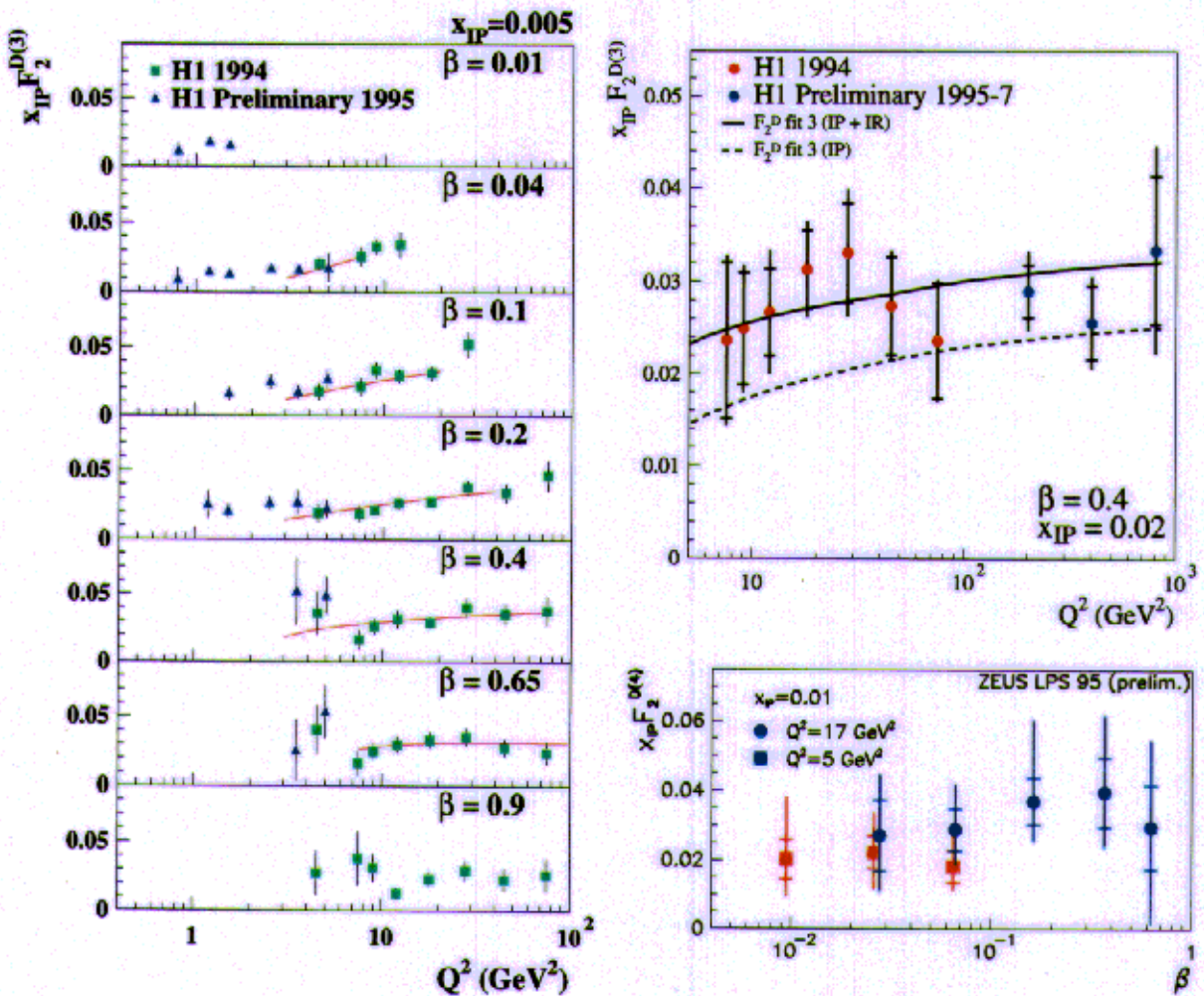
$$b \simeq 7 \pm 1(\text{stat}) \pm 1(\text{syst}) \text{ GeV}^{-2}$$

$$\text{assume } \alpha'_P = 0.25 \text{ GeV}^{-2}$$



- At low  $Q^2$  data compatible with Regge phenomenology
- At high  $Q^2$  diffractive cross section has the same  $W$  dependence as the inclusive cross section.
- $Q^2$  dependence of  $\alpha_P(0)$  requires more precise measurements

# Update on $F_2^{D(3)}$

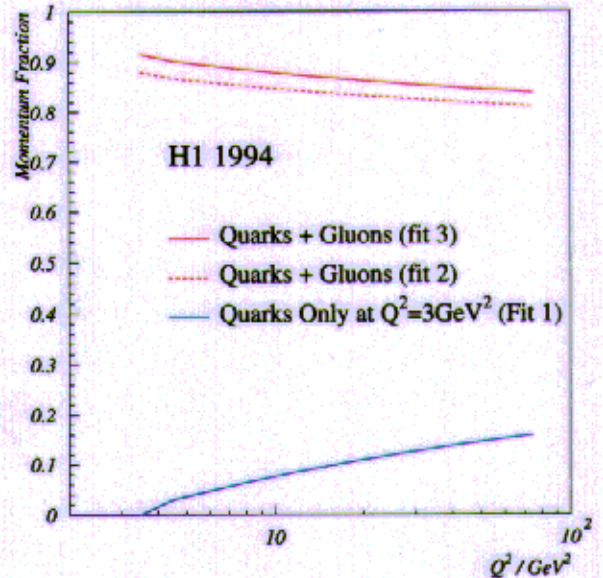
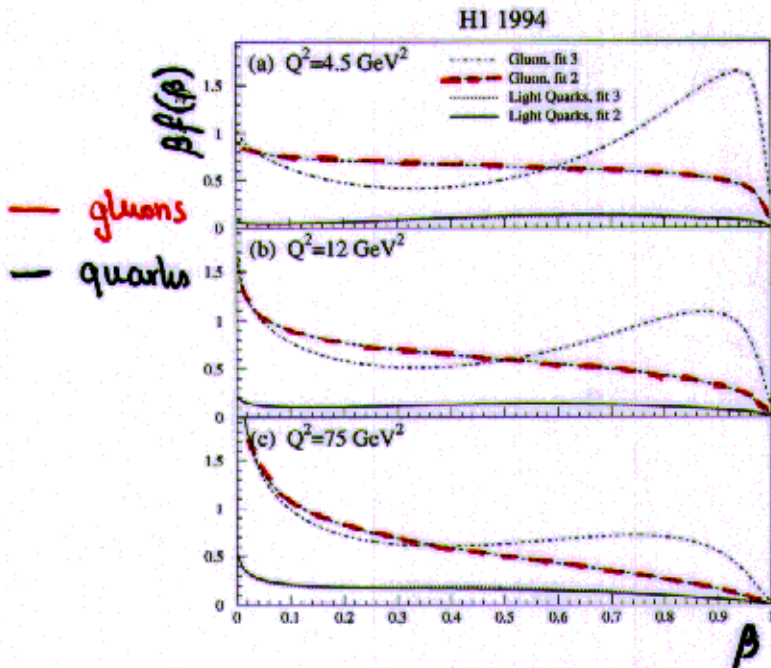


Very different from the proton case - for DGLAP evolution to hold **large** gluon content is required

# Diffractive parton distributions

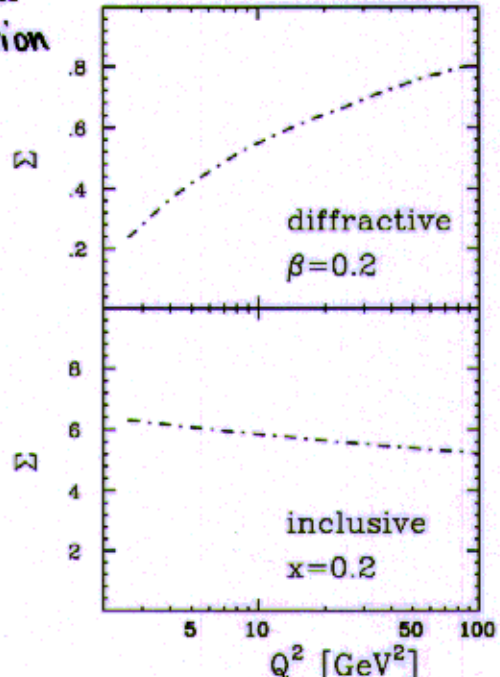
Input to DGLAP evolution from fit to data

Fraction of IP Momentum Carried by Gluons

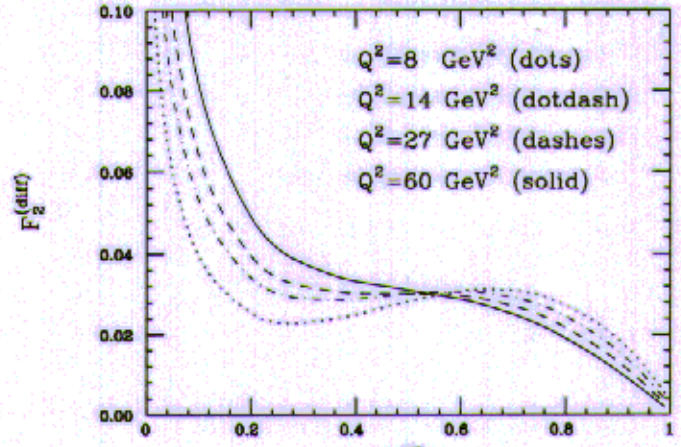


quark evolution  
 Difference in evolution

from Hautmann, Kunszt, Soper



Quark evolution



Diffractive scattering is driven by gluons

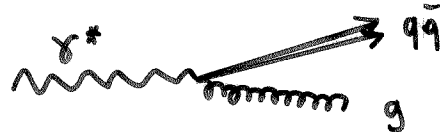
DPDF - convenient way to parametrize our lack of "knowledge"

# Models for diffractive DIS

In the target rest frame

(1)  $\gamma^* \rightarrow q\bar{q}$  or  $q\bar{q}g$  color dipoles

$$\tau_{\text{fluctuation}} \sim \frac{1}{2mX} \quad (\sim 10-100 \text{ fm at HERA})$$



(2) the dipoles interact with the target T

If small transverse size -  $r$  (large relative  $k_T$ )

pQCD:  $\sigma_{q\bar{q}T} = \frac{\pi^2}{3} r^2 \alpha_s(Q^2) \times G_T(x, Q^2 \approx \frac{\lambda}{r^2})$  } color transparency

$$\sigma_{q\bar{q}gT} \approx \sigma_{ggT} = \frac{9}{4} \sigma_{q\bar{q}T}$$

If large transverse size -  $r$  (small relative  $k_T$ )

non-perturbative effects dominate

(3) diffraction = quasielastic scattering of dipoles

$$\left. \frac{d\sigma_0}{dt} \right|_{t=0} = \frac{\sigma_{\text{dipole}T}^2}{16\sigma}$$

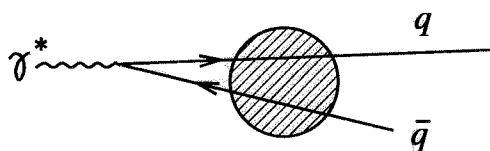
(4) fold in the wave function of  $\gamma_T^*$  and  $\gamma_L^*$  (pQCD)

# Essence of diffractive dynamics

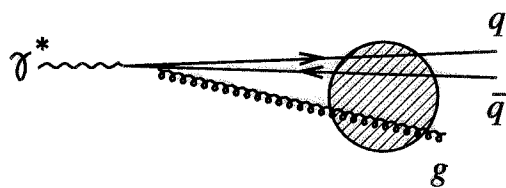
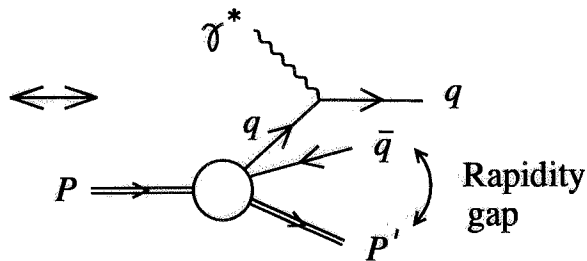
Equivalence between  $\gamma^*$  fluctuations  
and diffractive partons - (BHG)

Target rest frame

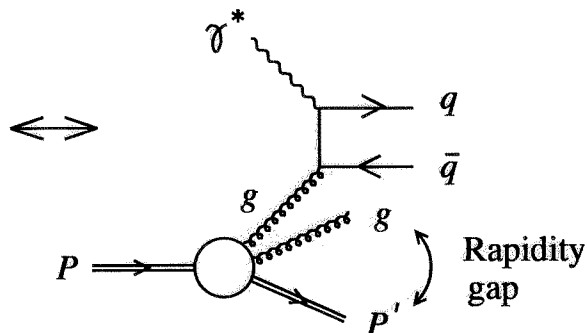
Breit frame



a) quark distribution



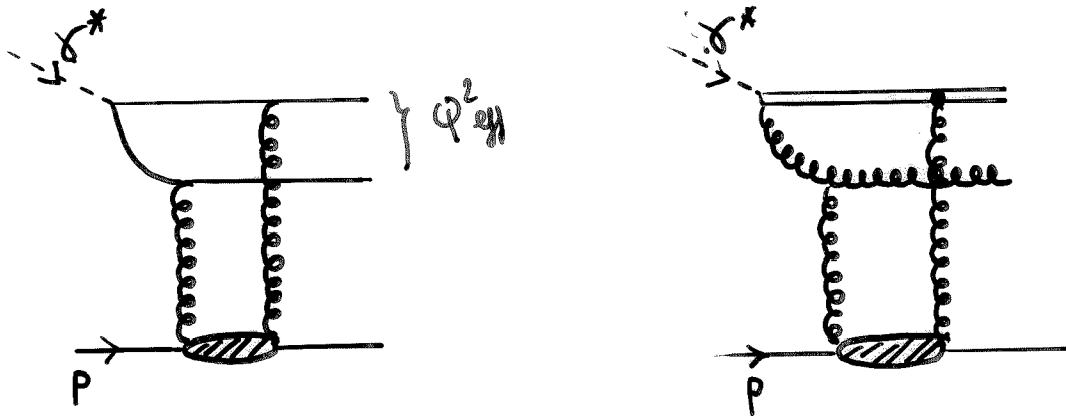
b) gluon distribution



Models differ in the treatment of the 'blobs'

- $\beta$  distribution  $\leftarrow$  photon partonic fluctuation
- $x_P$  dependence  $\leftarrow$  "blob"
- gluons dominate  $\leftarrow \sigma_{q\bar{q}g} > 2\sigma_{q\bar{q}}$

# Models for diffractive DIS



2-gluon exchange models:

- assume dominance of small dipoles
- $\times G(x, Q_{eff}^2)$  to describe inclusive DIS

⇒ Bartels, Ellis, Kowalski, Wüsthoff [BEKW]

Gotsman, Levin, Maor (gluon ladder with screening)

Biatas, Peschanski (BFKL ladder)

Ryskin

Nikolaev, Zakharov (parametrize dipole cross sections)

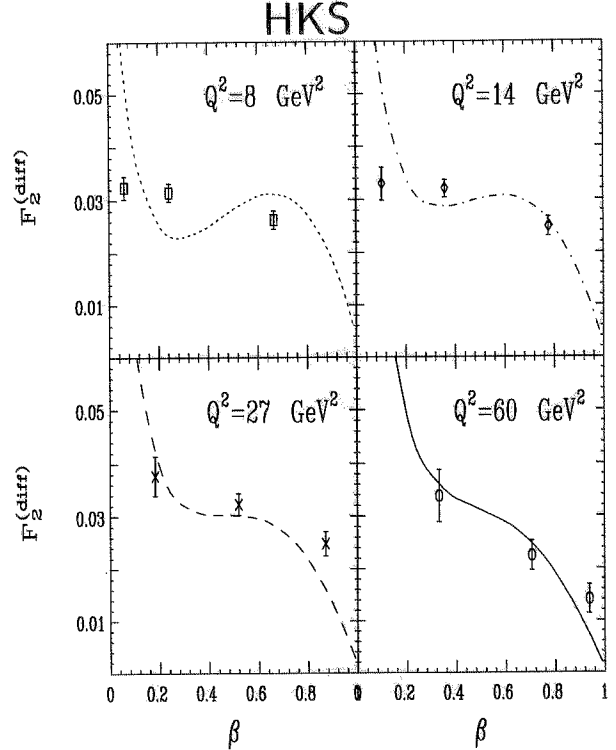
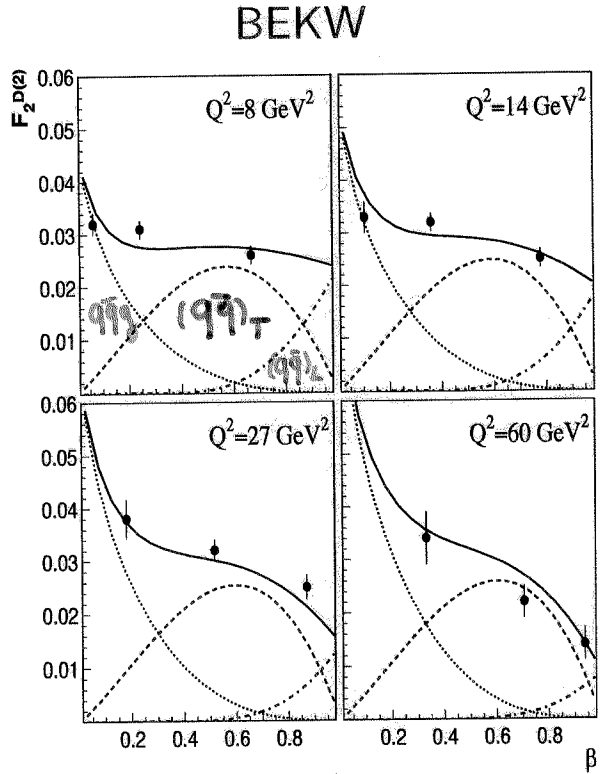
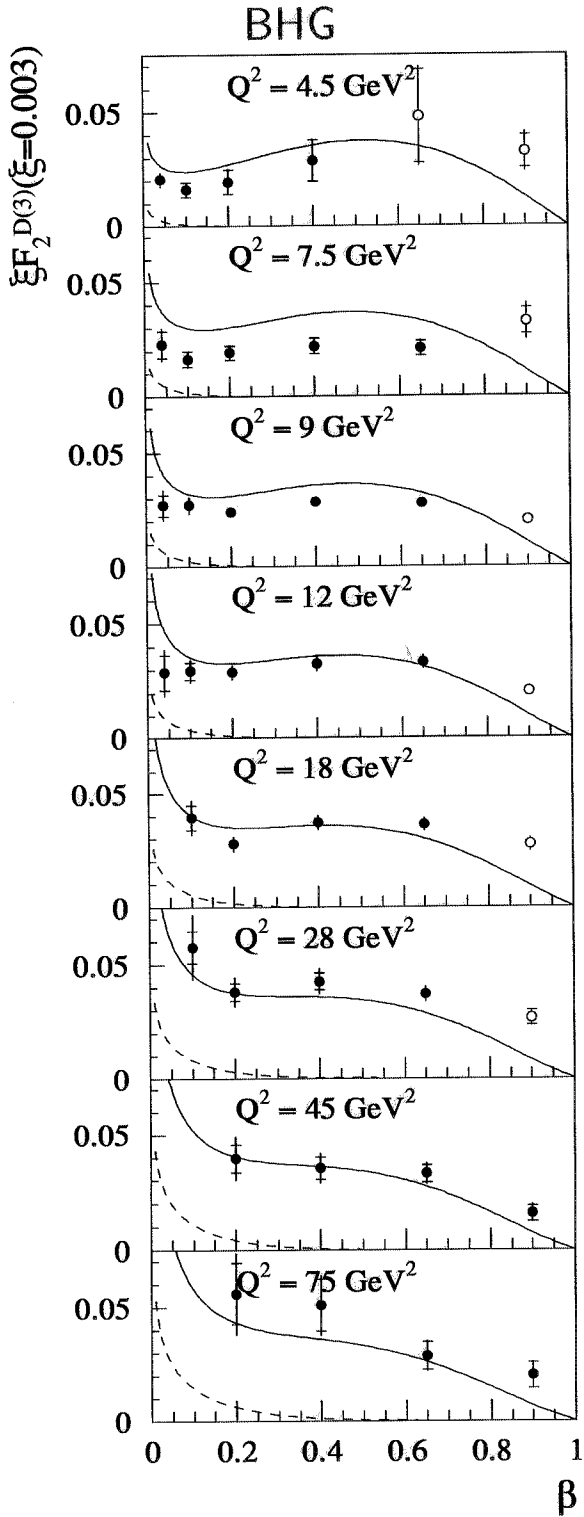
⇒ Hautmann, Kunszt, Soper (scattering of small target)

[HKS]

Semiclassical approximation:

- include both small and large configurations
- represent the color field of the proton
- generate rapidity gap as a result of soft color interactions

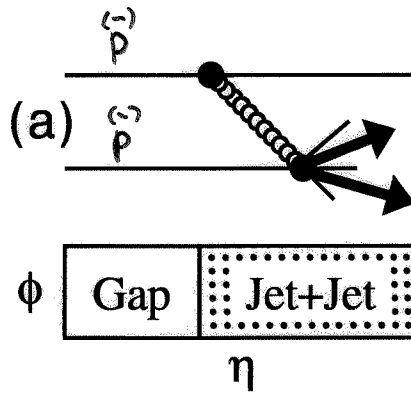
# β distribution and models





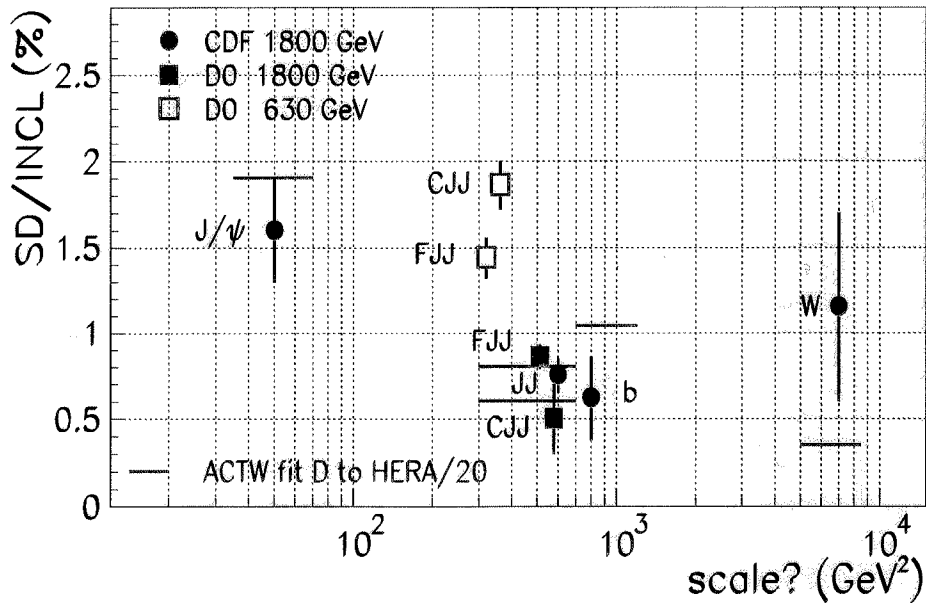
# Diffraction in $p\bar{p}$ (FNAL)

QCD factorization cannot be proven for hadron-hadron diffractive scattering - non factorizable contributions identified (Collins)



$$R_{\text{sample}} = \frac{\text{single diff}}{\text{inclusive}} = \frac{\text{sample with LRG}}{\text{sample}}$$

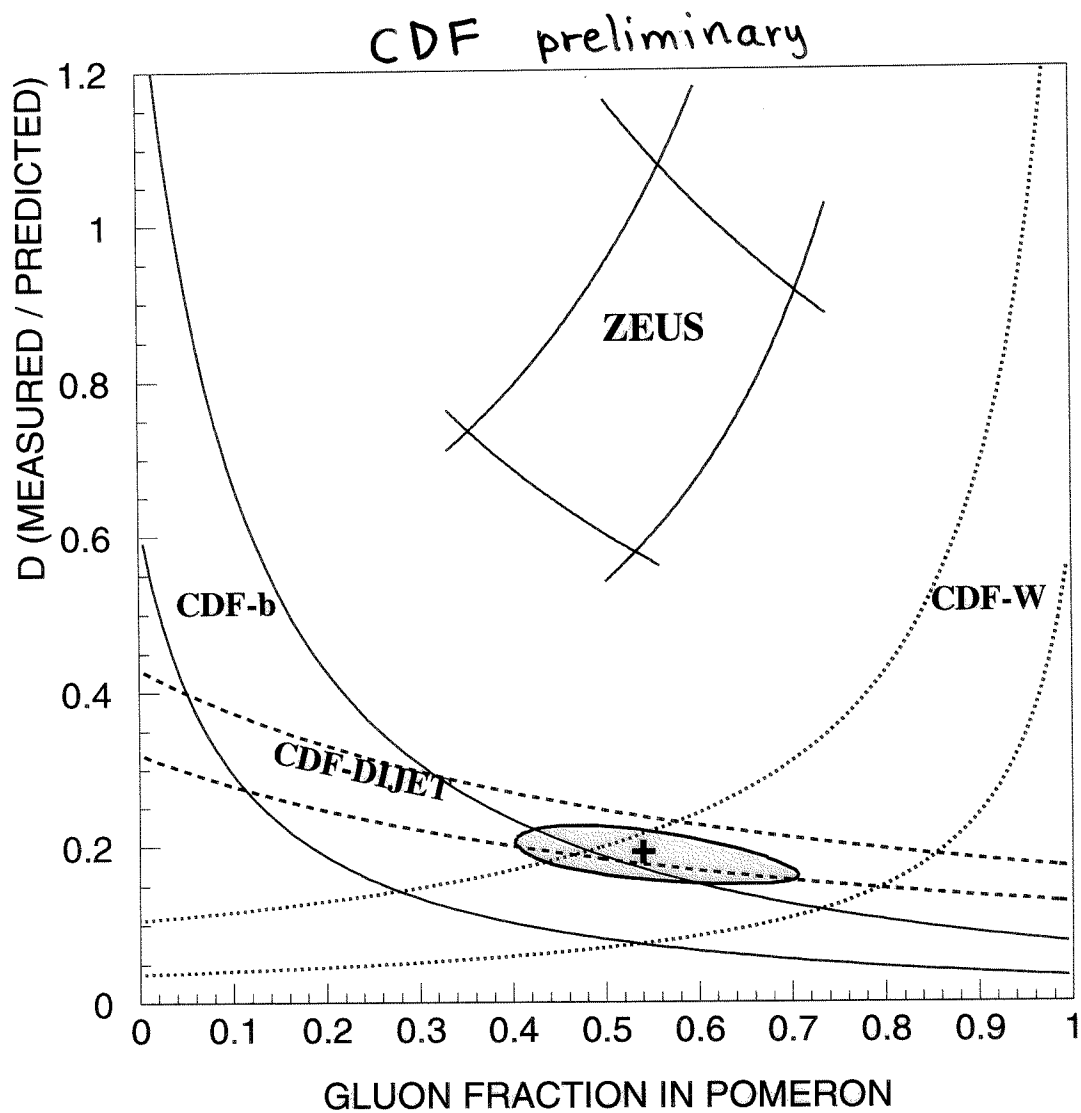
corrected with hard gluon MC



ACTW - Alvero, Collins, Terron, Whitmore

# QCD factorization breaking

Rates smaller than expected from diffractive parton distributions of HERA

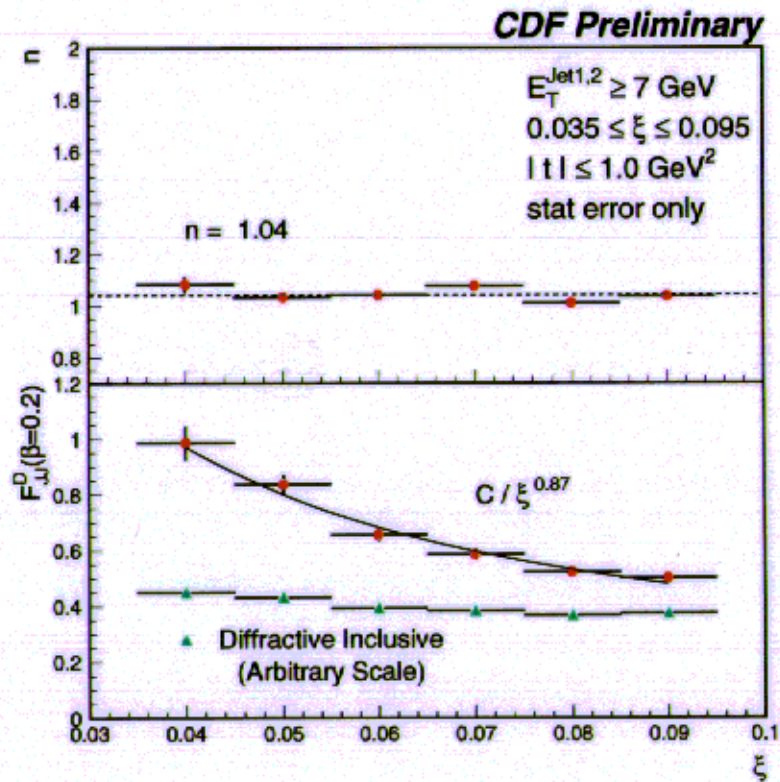
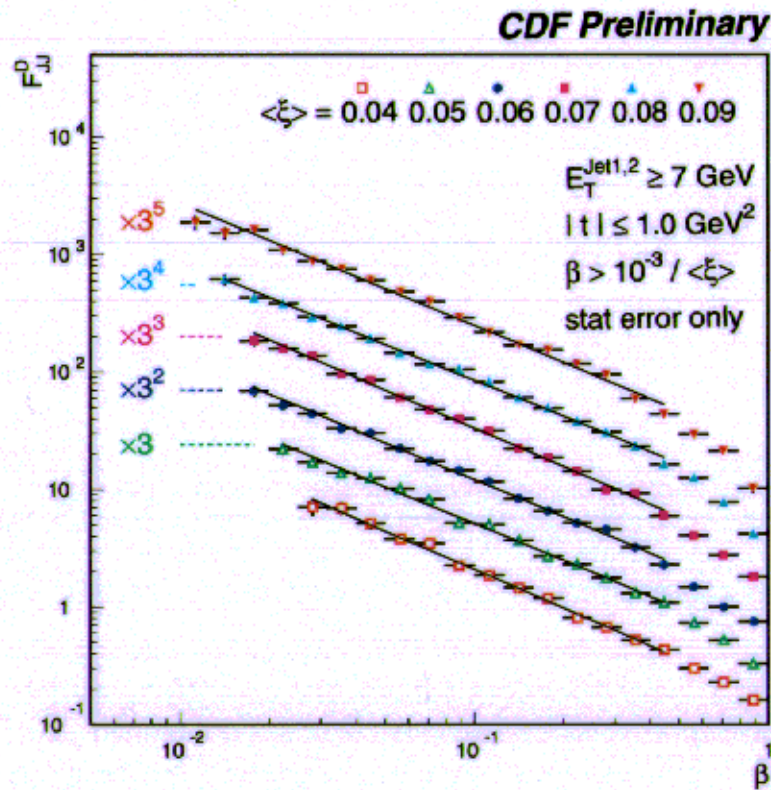


$$f_g = 0.54^{+0.16}_{-0.14}$$

$\bar{p}$  detected in Roman Pots + 2 jets

$$F_{JJ}^D(x_{\bar{p}}) = R_{SD/ND}(x_{\bar{p}}) \cdot F_{JJ}(x_{\bar{p}}) \quad F_{JJ}^{(0)}(x_{\bar{p}}) = x_{\bar{p}} \left[ g^{(0)}(x_{\bar{p}}) + \frac{4}{9} \sum [q_i^{(0)}(x_{\bar{p}}) + \bar{q}_i^{(0)}(x_{\bar{p}})] \right]$$

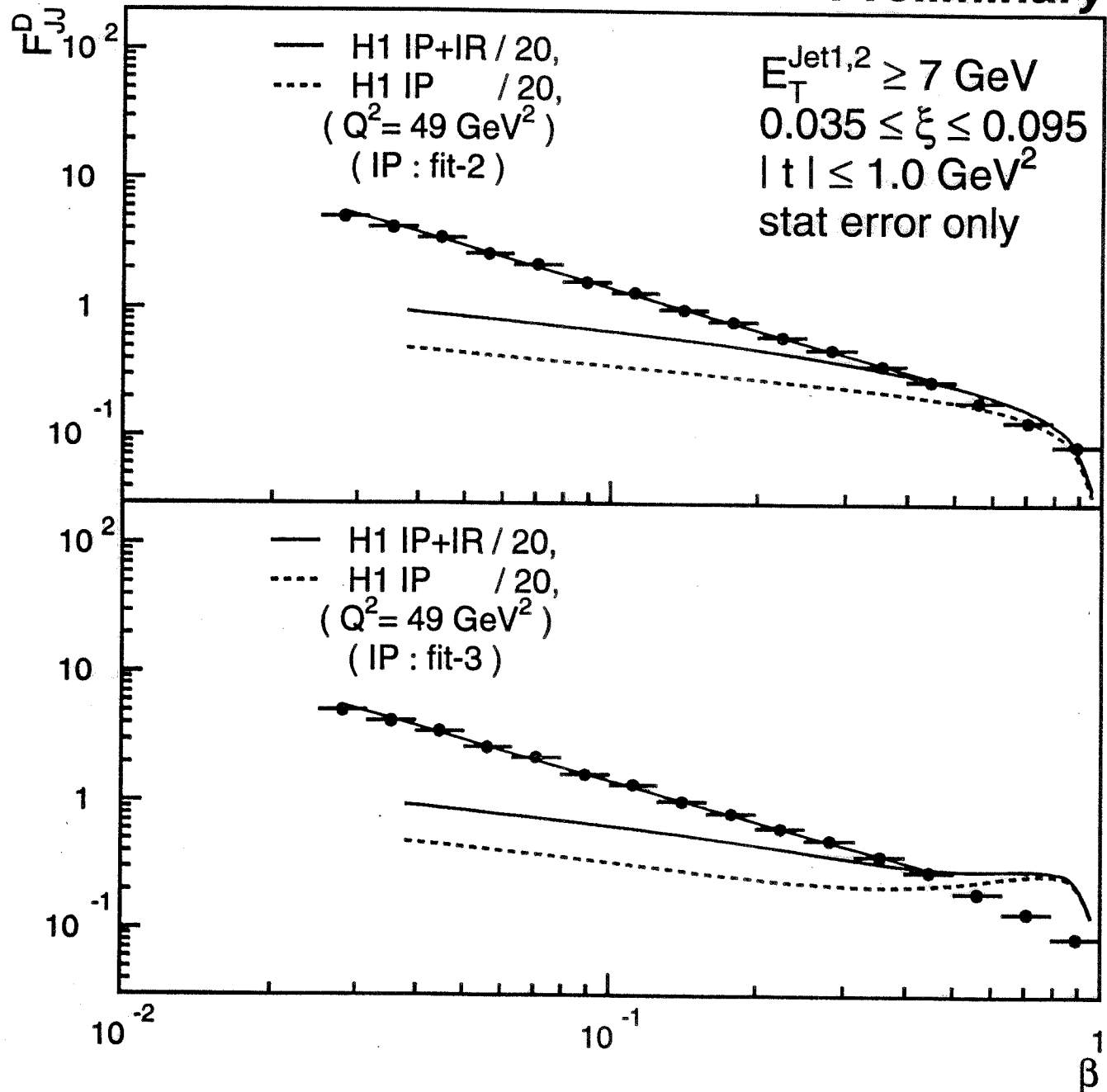
## Diffractive Structure as a function of $\xi$ & $\beta$



These distribution can be fitted to  $C/\beta^n$  in the region of  $10^{-3}/\langle \xi \rangle < \beta < 0.5$ .

- The slope is almost constant over the measured  $\xi$  range.
- $F_{JJ}^D$  is falling with  $\xi$ ,  $\propto 1/\xi^{0.87}$ .

# CDF Preliminary



Disagreement both in shape and normalization with DPDF from HERA

Conclusions from studying diffraction in the presence of a hard scale:

- LRG (diffraction in QCD) are correlated with the presence of a large gluon component in the hard interaction

$$P_{g,q}^D(x, Q^2) = \frac{\int f_{g,q}^D\left(\frac{x}{x_P}, Q^2, x_P, t\right) dt dx_P}{f_{g,q}(x, Q^2)}$$

- ⇒ (Frankfurt & Strikman) for  $x < 10^{-3}$   $Q^2 = 4 \text{ GeV}^2$   
 $P_g^D \approx 0.4$  (black body limit  $P_g^0 = 0.5!!!$ )  
 $P_q^D \approx 0.15$

- Unique situation – input distribution to DGLAP quasi-known:

⇒ points to semi-hard nature of diffractive scattering in DIS

(absorption of large size  $q\bar{q}$  configurations?)

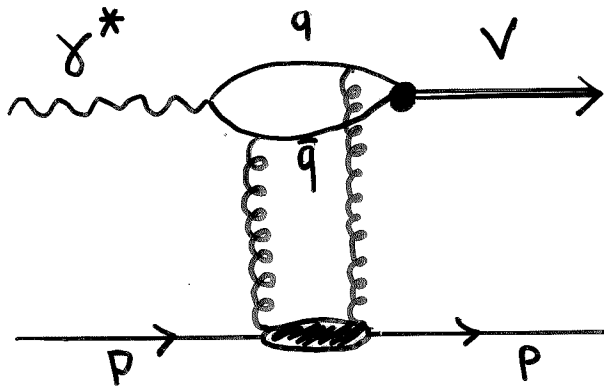
proposed by Mueller, modeled by Wuesthoff & Golec-Biernat)

- Direct relation between diffraction with a hard scale in DIS and  $p\bar{p}$  not expected in QCD

⇒ the factor 20 remains to be elucidated (survival probability for a LRG – proposed by Bjorken, calculated by Levin, Gotsman, Raor)

# Exclusive Vector Meson production in DIS

candidate for hard diffractive scattering  
 $\Rightarrow$  pQCD



Expectations:

- SU(4) restoration  $\xi:\omega:\phi:\mathbb{J}/\psi = 9:1:2:8$

If  $q\bar{q}$  small configuration  $\Rightarrow$  resolves gluons

$\uparrow$   
 either  $\gamma_L^*$   
 or  
 $V = c\bar{c}, b\bar{b}$

(factorization proven  
 by Collins, Frankfurt  
 Stiekman)

- $\sigma_L \propto \frac{\alpha_s^2(Q_{eff}^2)}{Q^6} |xG(x, Q_{eff}^2)|^2$

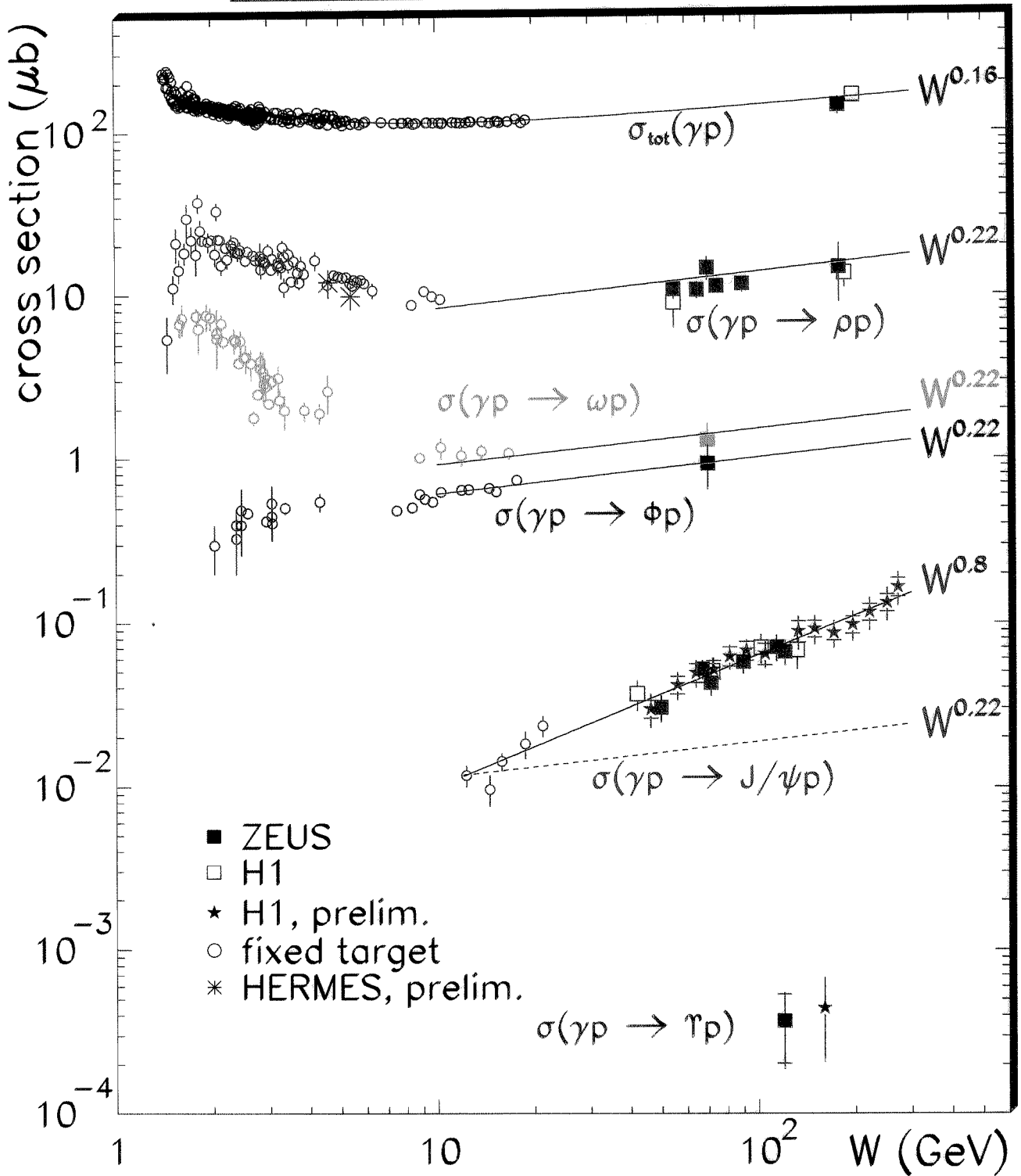
$\Rightarrow$  fast increase of  $\sigma(\gamma^*p \rightarrow Vp)$  with  $W^2 \sim \frac{1}{x}$

$\Rightarrow$  universality of  $t$  dependence  $\sim e^{b_{2g}t}$   
 $b_{2g} \sim 4 \text{ GeV}^{-2}$   $\alpha' \rightarrow 0$

$\Rightarrow$   $Q^2$  dependence slower than  $\frac{1}{Q^6}$

Exclusive vector meson in  $\gamma p$

$Q^2 \approx 0$



## $\alpha'$ in hard processes

reminder:

$$\frac{d\sigma}{dt} \sim e^{bt}$$

$$b = b(W_0) + 4\alpha' \ln\left(\frac{W}{W_0}\right)$$

Interpretation of  $\alpha'$  by Gribov:

diffusion of partons of the exchanged ladder in the impact parameter space ( $r$ )

Random walk

- number of steps  $\sim \Delta y$

- in each step  $\Delta r \sim \frac{1}{k_t}$

$\Rightarrow$  apparent increase of the radius of the projectile

$$\Delta R^2 \sim \frac{\Delta y}{k_t^2}$$

soft partons:  $k_t \sim k_{t0}$  small  $\rightarrow \alpha' \sim \frac{1}{k_{t0}^2}$

hard partons:  $k_t$  large  $\rightarrow \alpha' \rightarrow 0$

If pQCD occupies most of the phase space

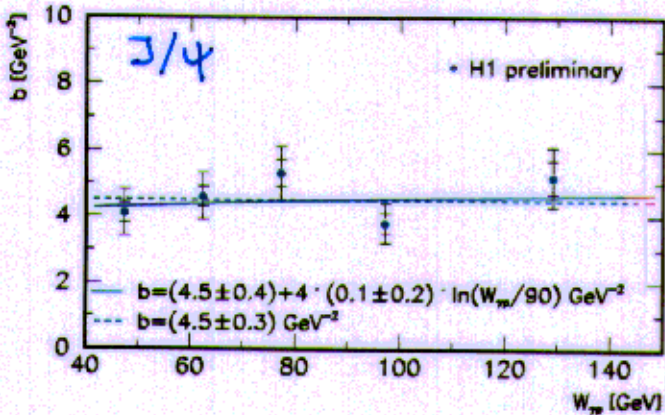
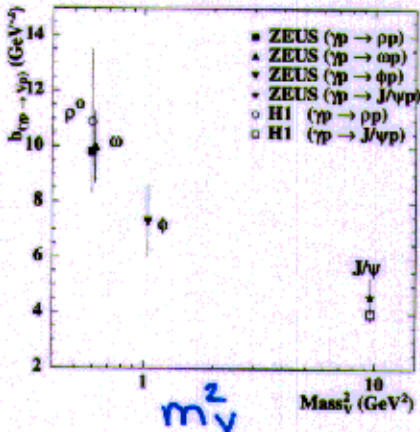
$\alpha'$  has to be small



# Shrinkage: $f(t)$ dependence on $W$

for fixed  $W$  assume  $f(t) \sim e^{bt}$

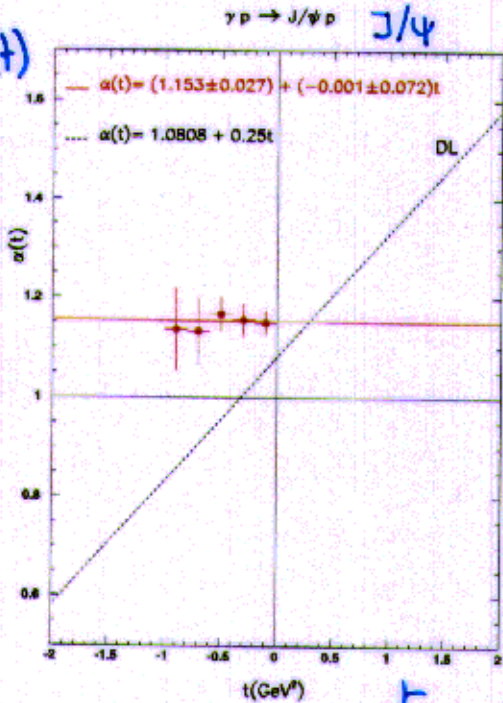
b



- The heavier the quark the smaller the hadron
- $b(W) \simeq \text{const}$  for  $J/\psi$

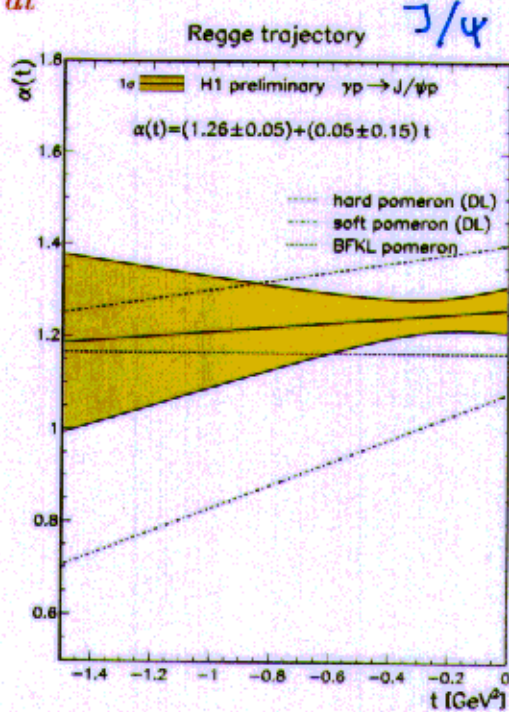
for fixed  $t$  fit  $\frac{d\sigma}{dt} \sim W^{4(\alpha(t)-1)}$

$\alpha(t)$



HERA + low energy PLB424(98)191

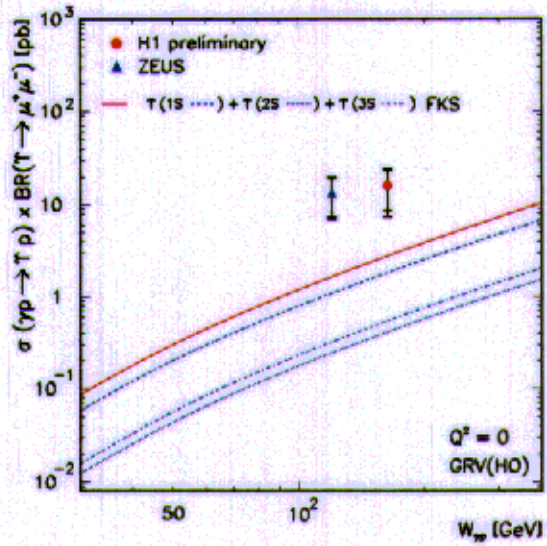
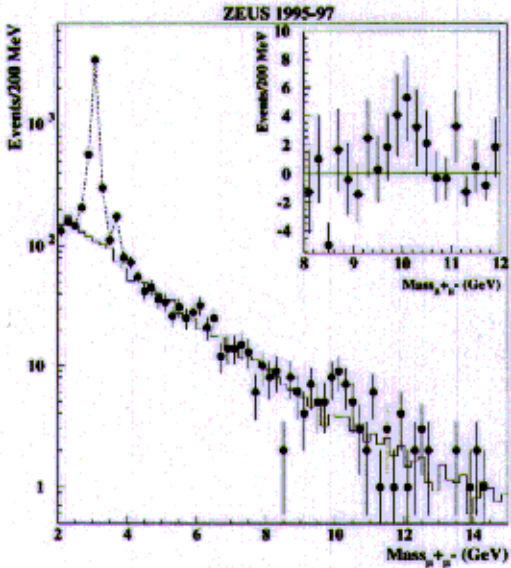
A. Levy



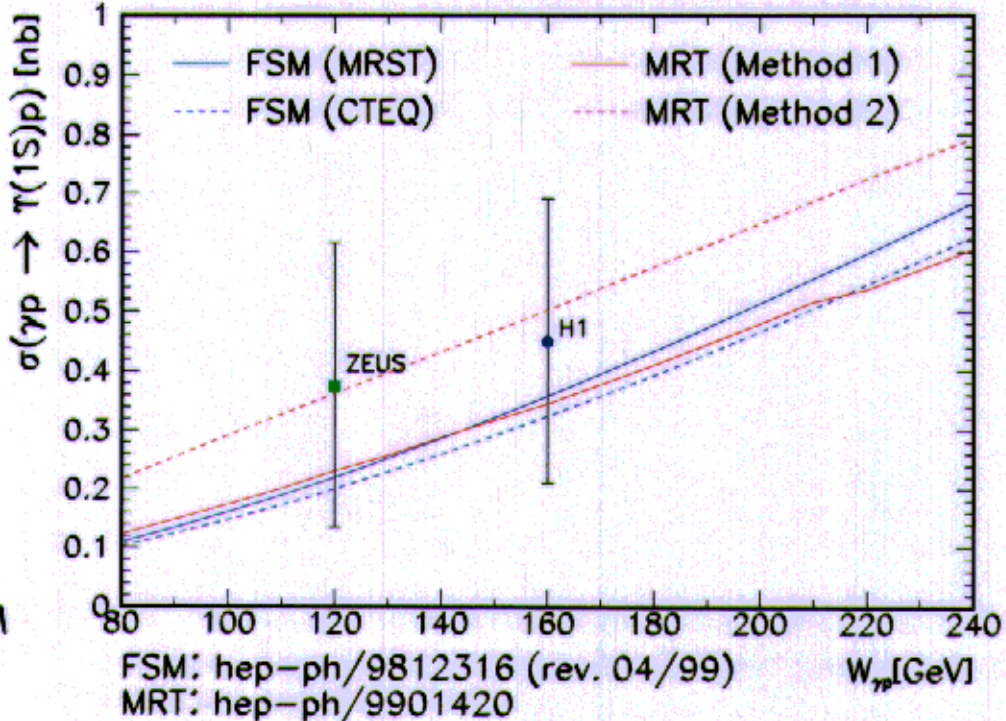
H1 data only

$\alpha'$  - small  $\Rightarrow J/\psi$  photoproduction ( $Q^2 \approx 0$ ) is a hard process

# Exclusive $\Upsilon$ in $\gamma p$



## After the measurements:

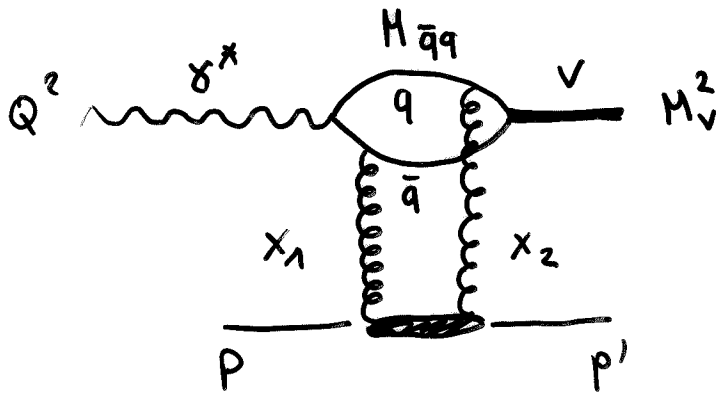


Frankfurt } FSM  
 Strikman }  
 McDermott }  
 Martin } MRT  
 Ryskin }  
 Teubner }

Important ingredients: skewed parton distributions

$\frac{\text{Re } A}{\text{Im } A} \neq 0, \text{ large}$

# Skewed parton distributions



for review see

X. Ji, J Phys G24(98)1181

A. Radyushkin, PLB449(99)81

$$x_1 = \frac{M_{q\bar{q}}^2 + Q^2}{W^2 + Q^2}$$

$$x_2 = \frac{M_{q\bar{q}}^2 - M_V^2}{W^2 + Q^2}$$

$$\delta = x_1 - x_2 = \frac{M_V^2 + Q^2}{W^2 + Q^2} \neq 0$$

$$x g(x, Q^2) \rightarrow x_2 g(x_1, x_2, Q^2)$$

enhancement factor

$$\left( \frac{x_2 g(x_1, x_2, Q^2)}{x g(x, Q^2)} \right)^2 \approx 2$$

Skewed parton distributions / off-diagonal / non-forward  
probe of non perturbative effects  
at the amplitude level

⇒ generalize other non-perturbative information

such as: parton densities

vector meson type distribution amplitudes

form factors

## Real part of the scattering amplitude

$$\left. \frac{d\sigma_{el}}{dt} \right|_{t=0} = (1 + \eta^2) \frac{\sigma_{tot}^2}{16\pi}$$

$$\eta = \frac{\text{Re } A}{\text{Im } A}$$

Gribov - Migdal relation

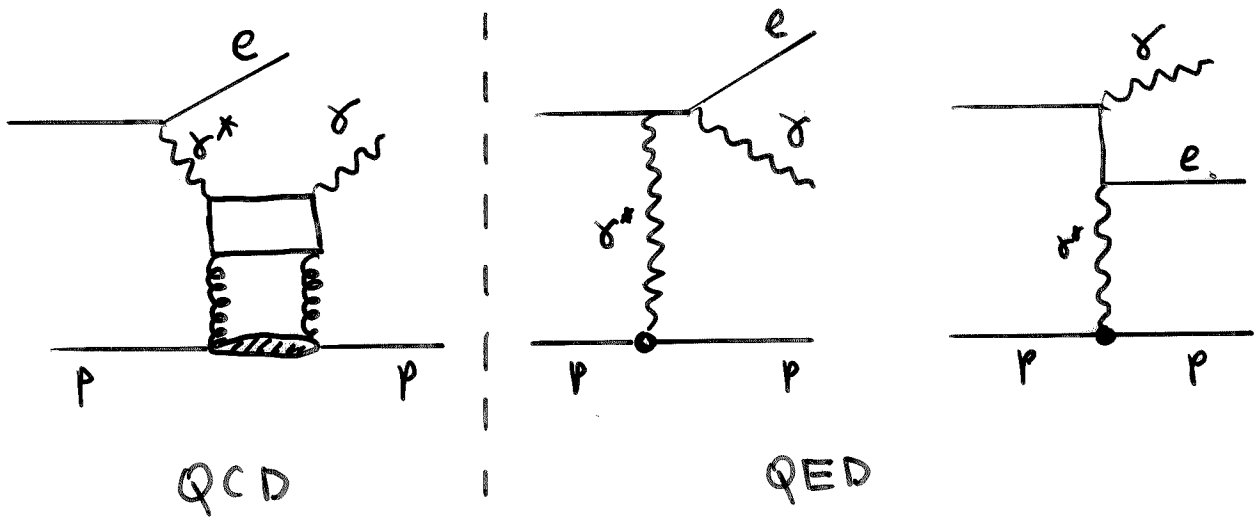
$$\eta \approx \frac{\sqrt{s}}{2} \frac{d \ln \sigma_{tot}}{d \ln W^2}$$

$$\text{If } \sigma_{tot} \sim (W^2)^\alpha \Rightarrow \eta = \frac{\sqrt{s}}{2} \alpha$$

since  $\alpha \neq 0$   $\eta$  large

$$(1 + \eta^2) \approx 1.5 \div 1.7$$

# Deeply Virtual Compton Scattering

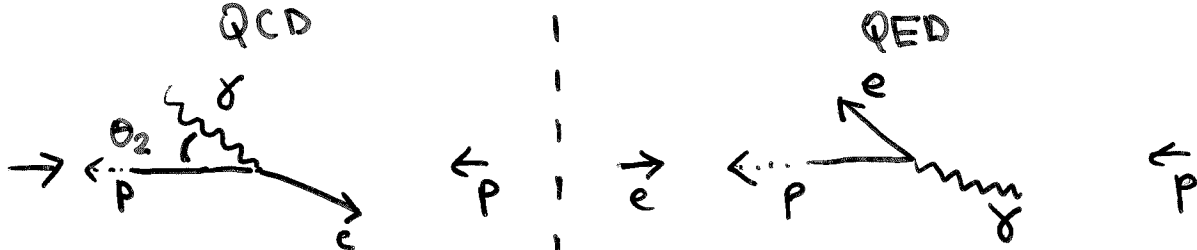


Interference

- measure skewed parton distributions without hadronic uncertainties
- measure  $\text{Re}(A_{\text{QCD}})$  via interference with QED

⇒ calculations by Frankfurt, Freund, Stalman  
MC by Pat Savall

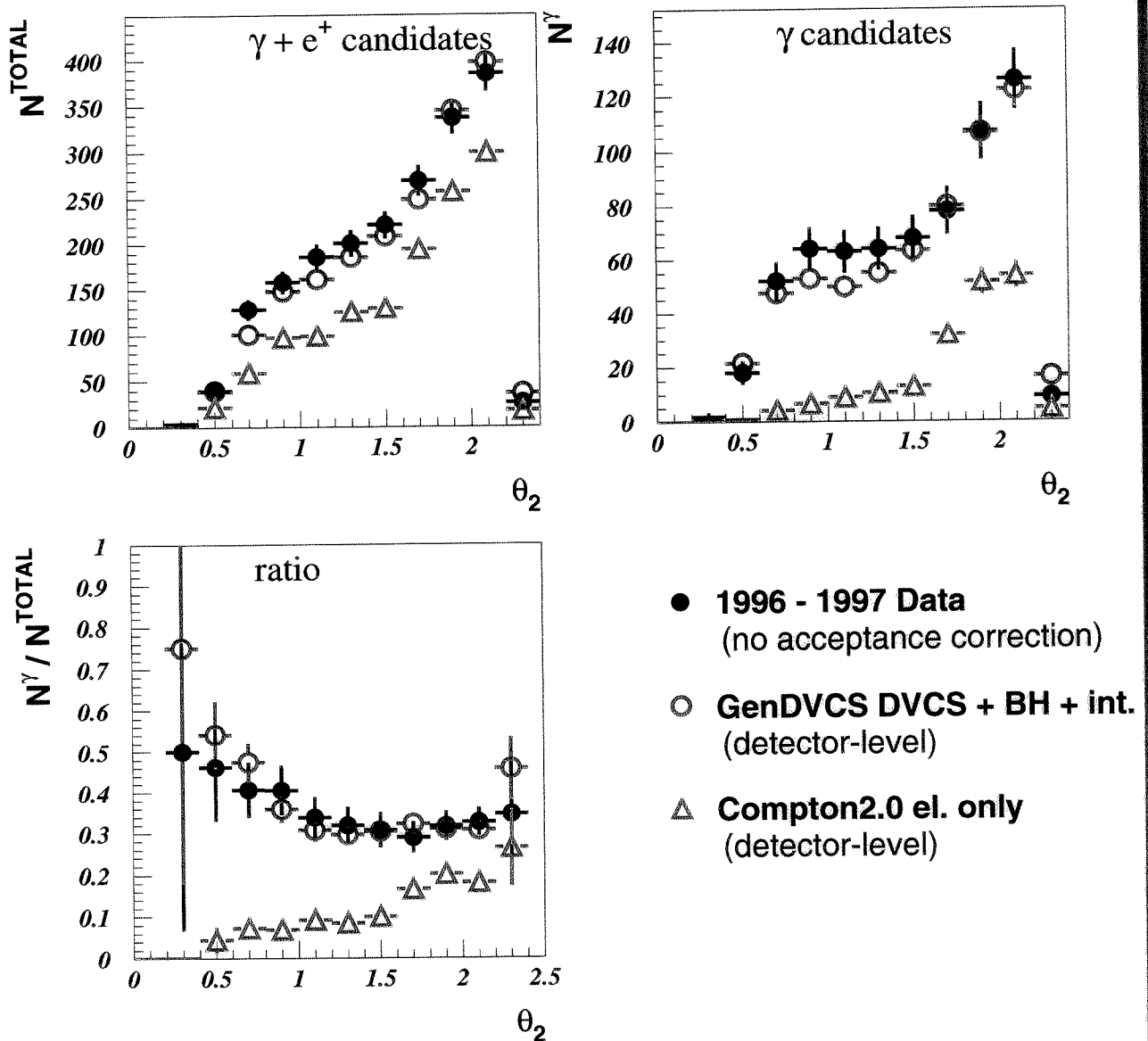
Experimental strategy:



Major difference when  $(e \text{ or } \gamma)$  in the proton direction

# DVCS - $\theta_2$ DISTRIBUTIONS

## ZEUS 1996/97 Preliminary

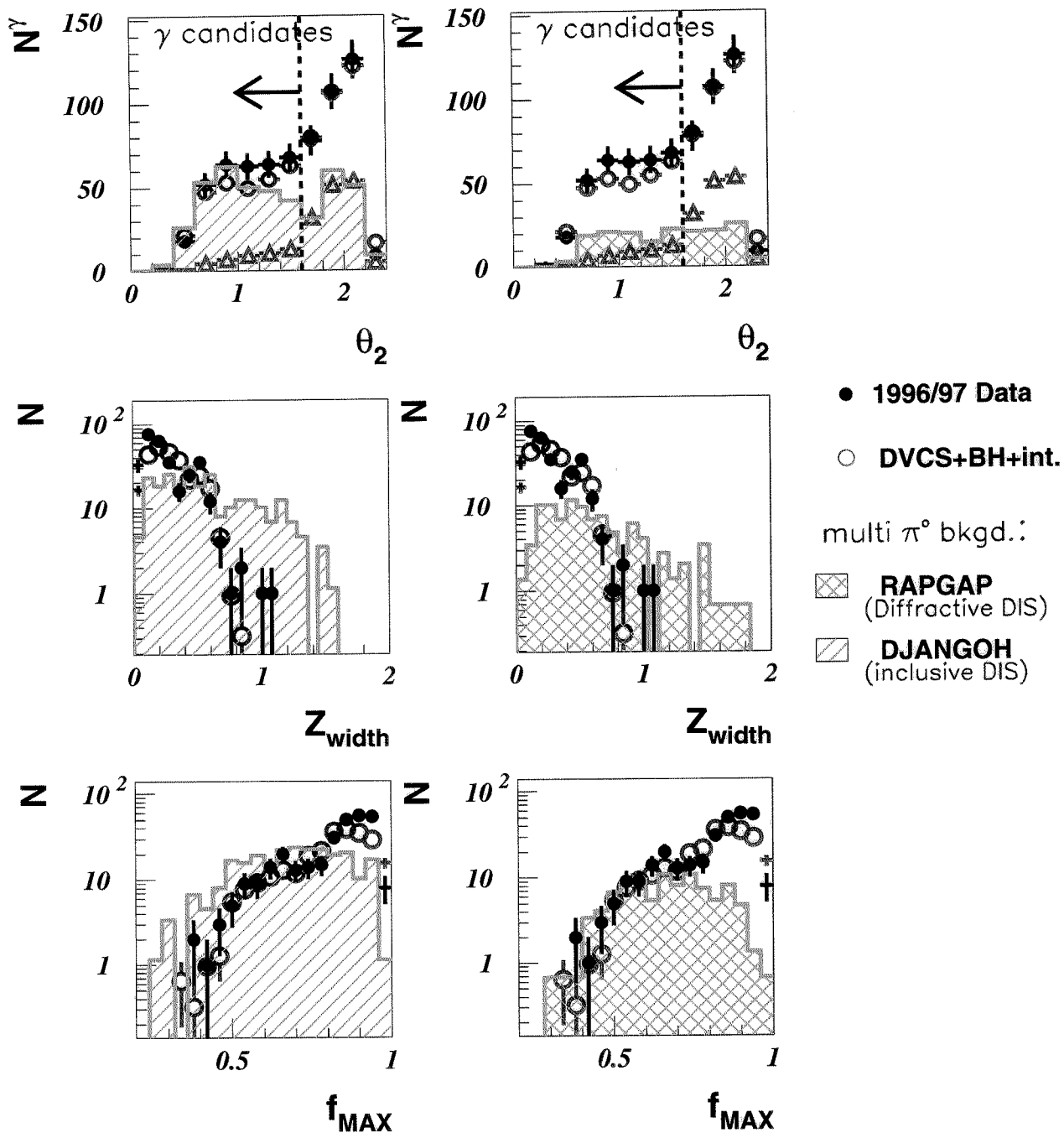


→ Appears to be clear signal for DVCS!

But, processes like  $ep \rightarrow ep\pi^0$ ,  $ep \rightarrow ep\pi^0\pi^0$ ,  $ep \rightarrow ep\pi^0\eta$ , ... potentially fake this signal.

# DVCS - $\gamma$ CAND. SHOWER SHAPES

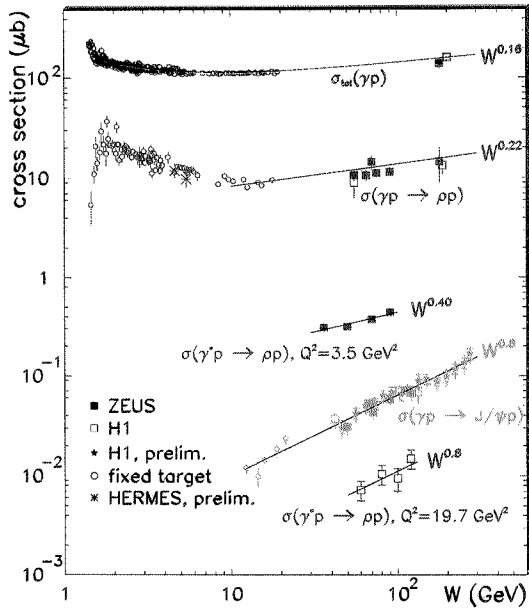
## ZEUS 1996/97 Preliminary



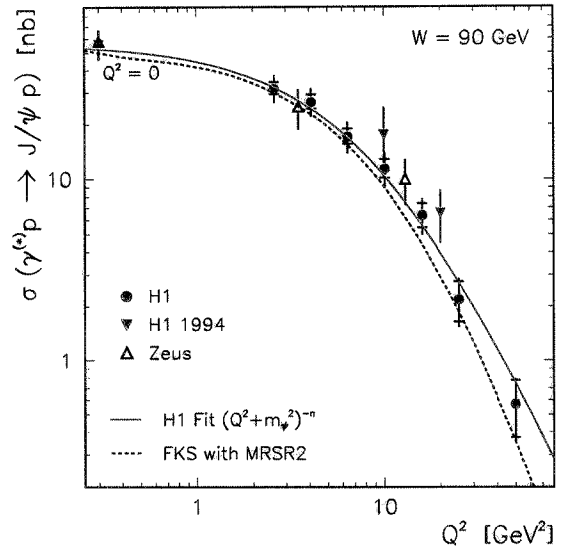
$\rightarrow \pi^0 / \eta$  hypothesis cannot account for shower shapes.

# Exclusive VM in $\gamma^*p$

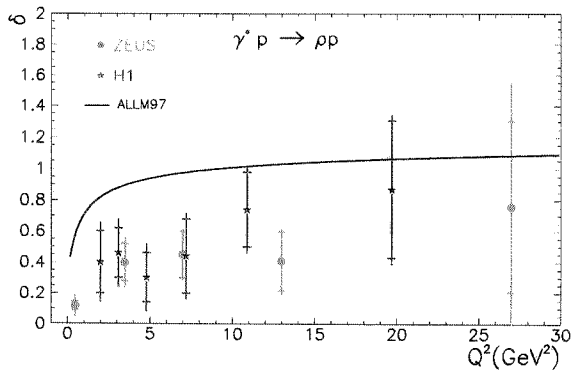
$W$  dependence



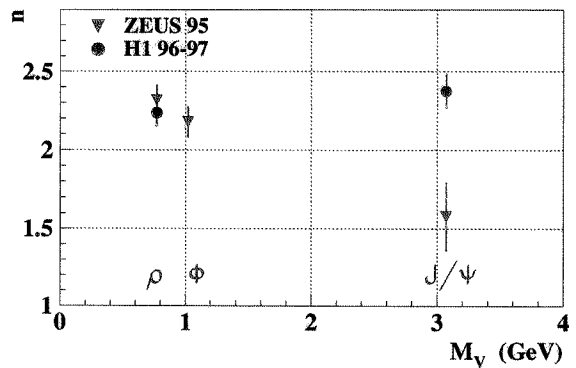
$Q^2$  dependence



for fixed  $Q^2$  fit  
 $\sigma_{\gamma^*p}(W) \sim W^{4\delta}$



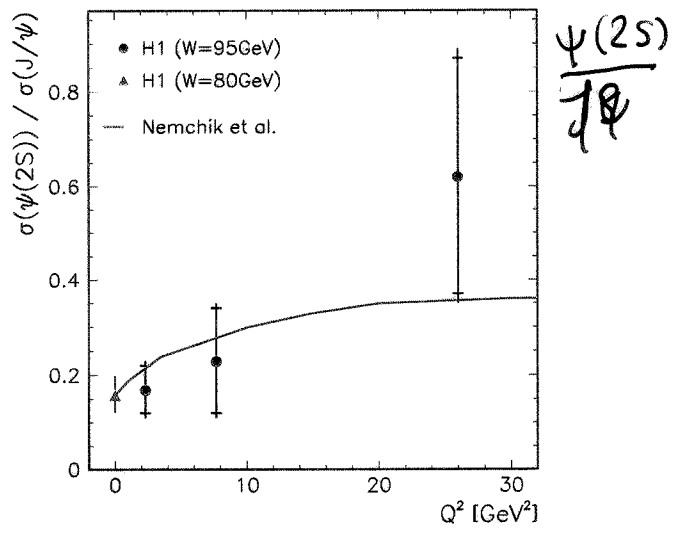
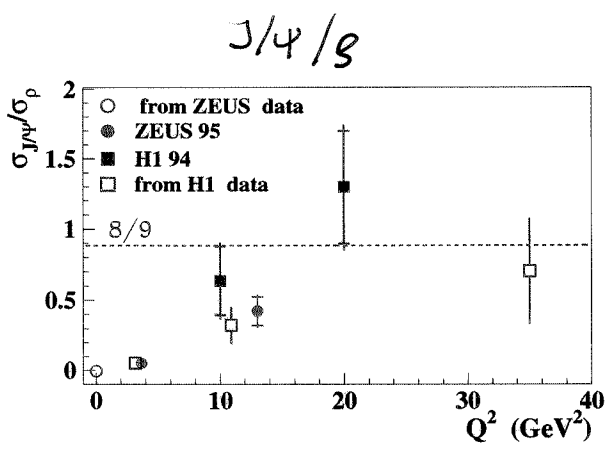
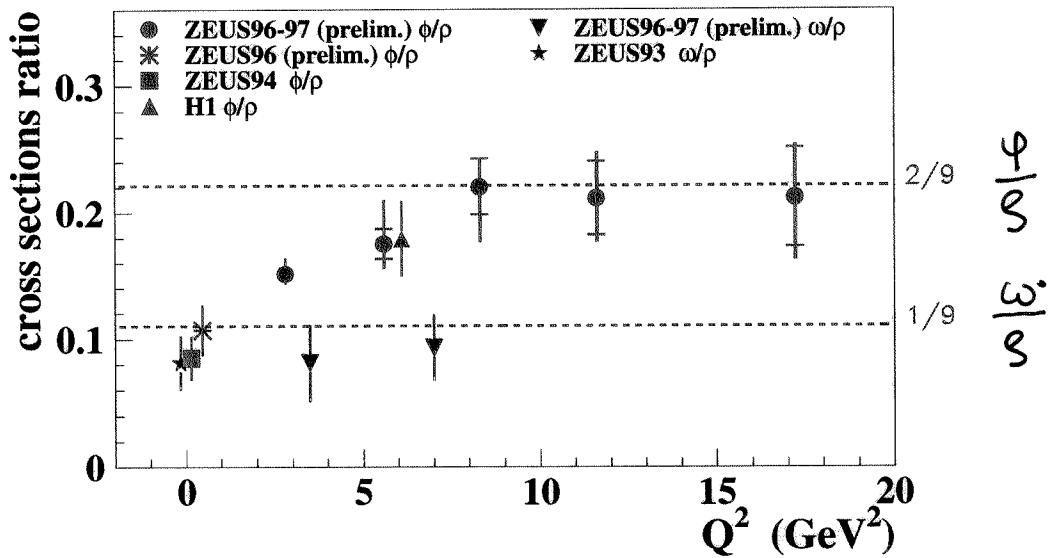
for fixed  $W$  fit  
 $\sigma_{\gamma^*p}(Q^2) \sim (Q^2 + M_{VM}^2)^{-n}$





$$\rho : \omega : \phi : J/\psi ?$$

From  $\gamma q$  coupling expect 9:1:2:8



- democratic gluons
- $\psi(2S)$  wave function scanning

# Conclusions from exclusive hard processes

Amazing success of perturbative QCD  
in terms of highly non-trivial

- $W$  and  $Q^2$  dependence
- universality of  $t$  distribution
- existence of DVCS
- cross section ratios for various VM states
- $S$ -channel helicity non-conservation (not discussed)

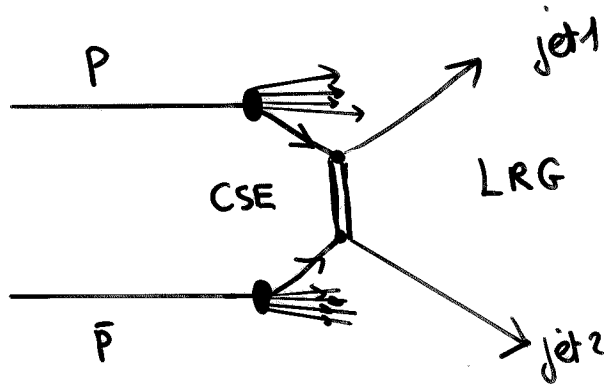
Immediate consequence of the role of the size  
of interacting "parton" states in determining the  
cross section = non-universality of LRG in QCD

Experimental dream - clean measurements

- Expect:
- better understanding of VM wave functions
  - low  $Q^2$  gluonometer
  - skewed parton distributions

# High $t$ Color Singlet Exchange

Proposed by Bjorken to study origin of LRG



Probe BFKL evolution?

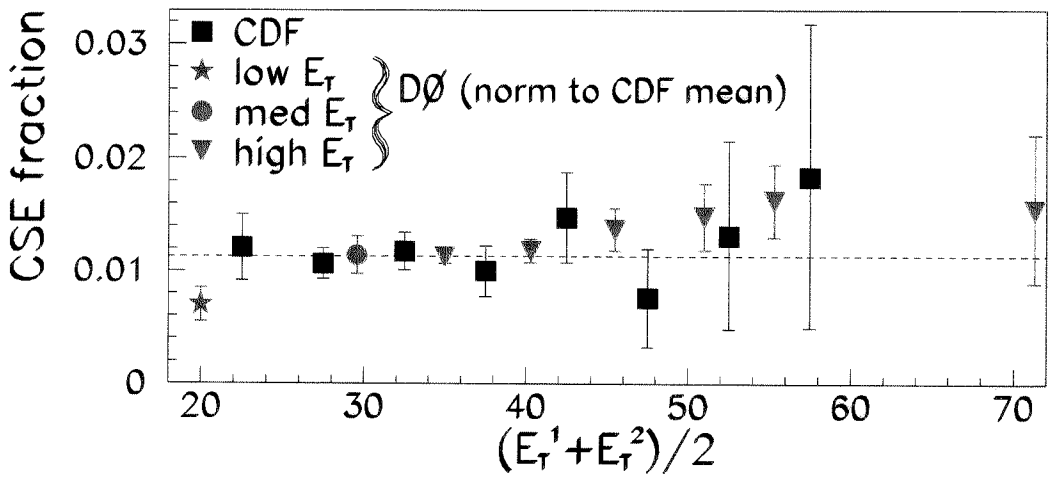
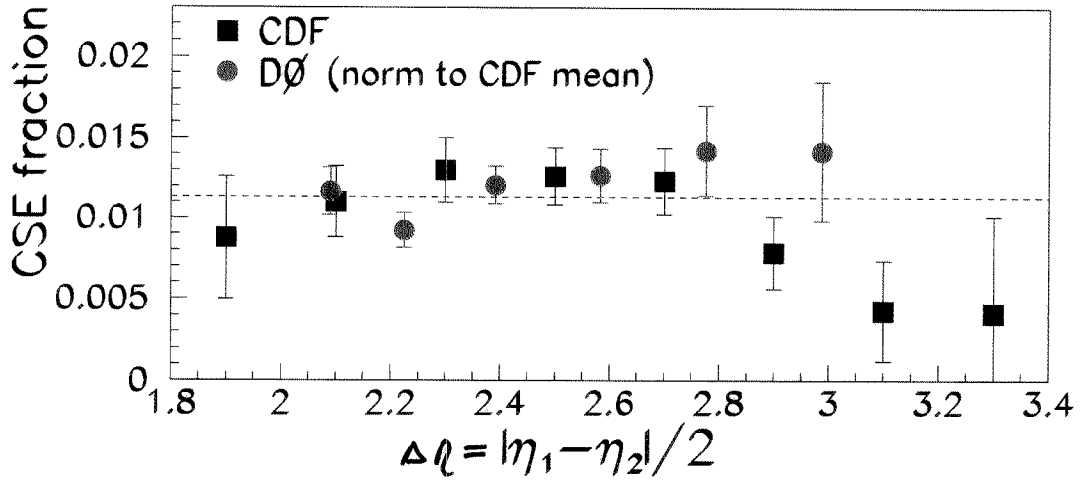
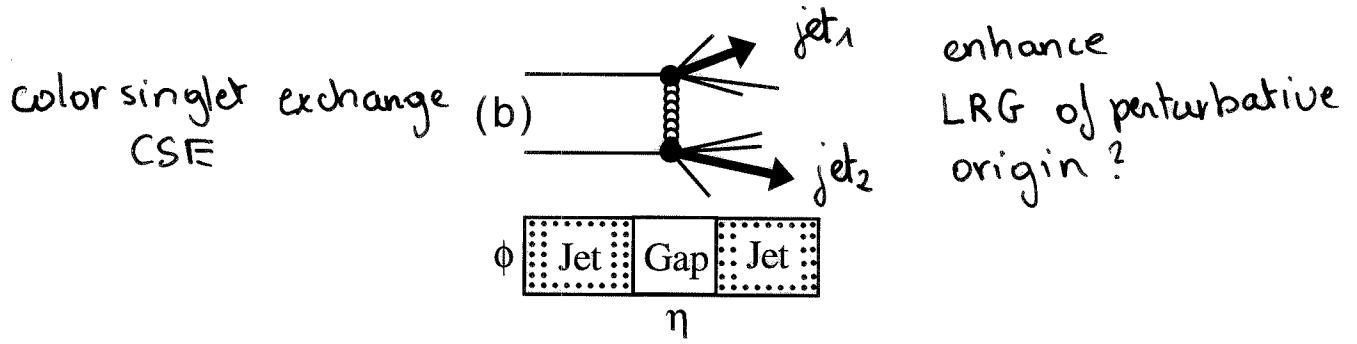
$\Rightarrow$  evolution only in  $x$ , no  $k_t$  ordering

- $E_{T1} \approx E_{T2}$   $\leftarrow$  no  $Q^2$  evolution
- $A\eta$  large  $\leftarrow$  space for  $x$  evolution
- LRG requirement  $\leftarrow$  BFKL gluon ladder  
hard QCD Pomeron?

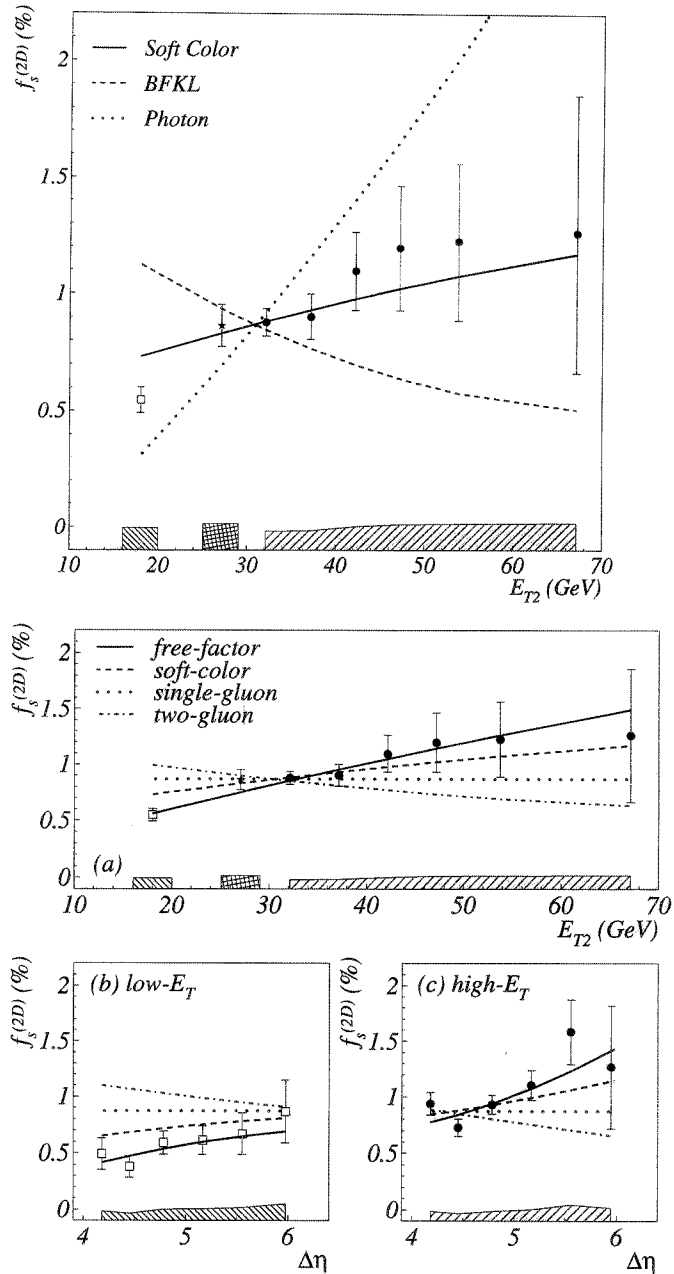
Experimentally: how to define LRG

Theoretically: LRG survival probability  
(multi parton interactions)

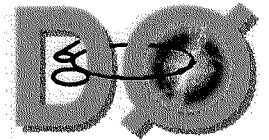
# High $t$ color singlet in $p\bar{p}$ (FNAL)



# Origin of large $t$ color singlet in $p\bar{p}$

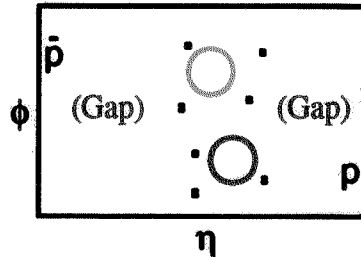
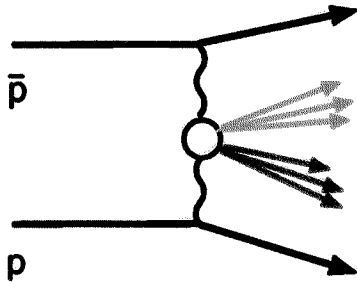


The color singlet exchange seems to couple predominantly to quarks



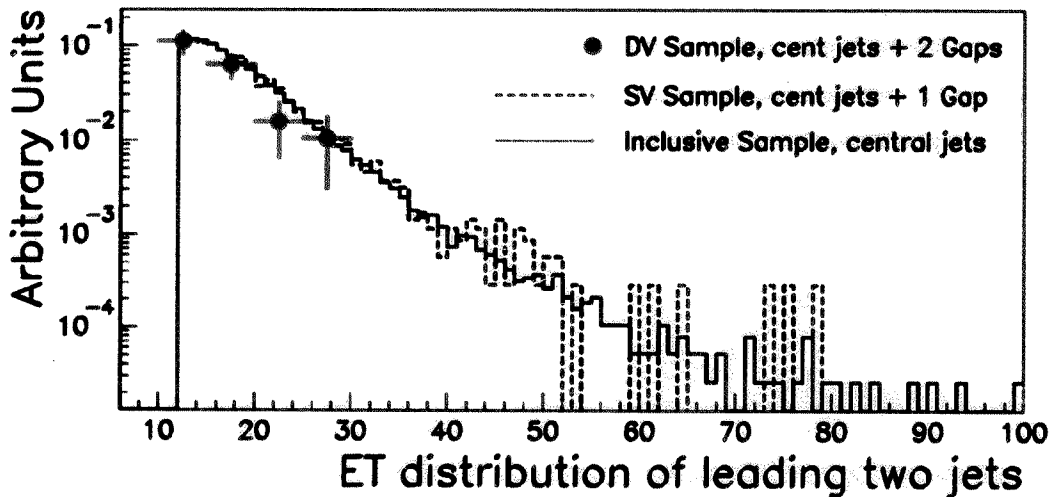
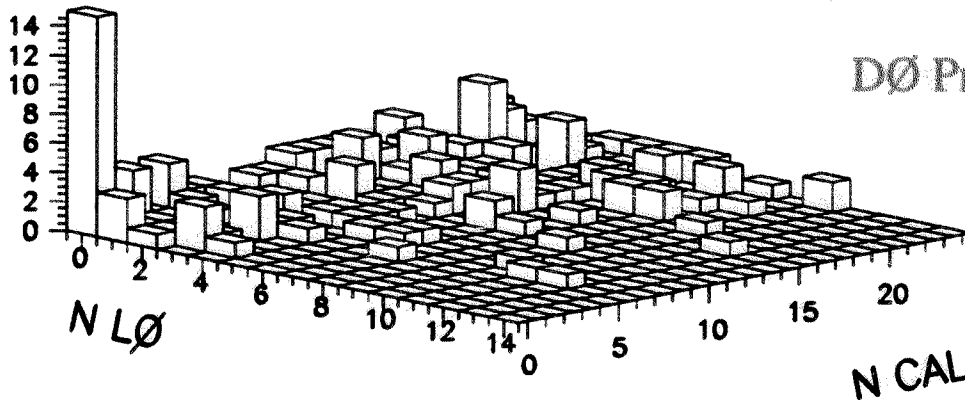
# Double Gaps at 630 GeV

$|\text{Jet } \eta| < 1.0, E_T > 12 \text{ GeV}$



**Gap Region**  
 $2.5 < |\eta| < 5.2$

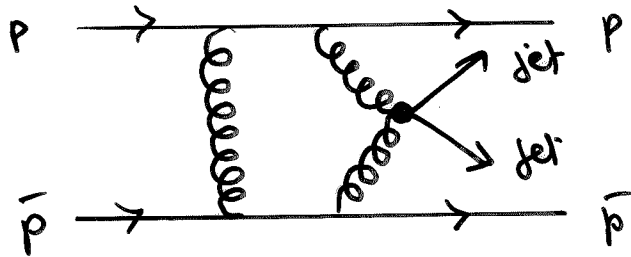
Demand gap on one side, measure multiplicity on opposite side



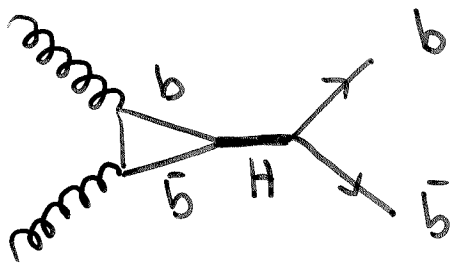
# Motivation for double gaps

(of M. Albrow)

Non factorizable double  $\mathbb{P}$  exchange

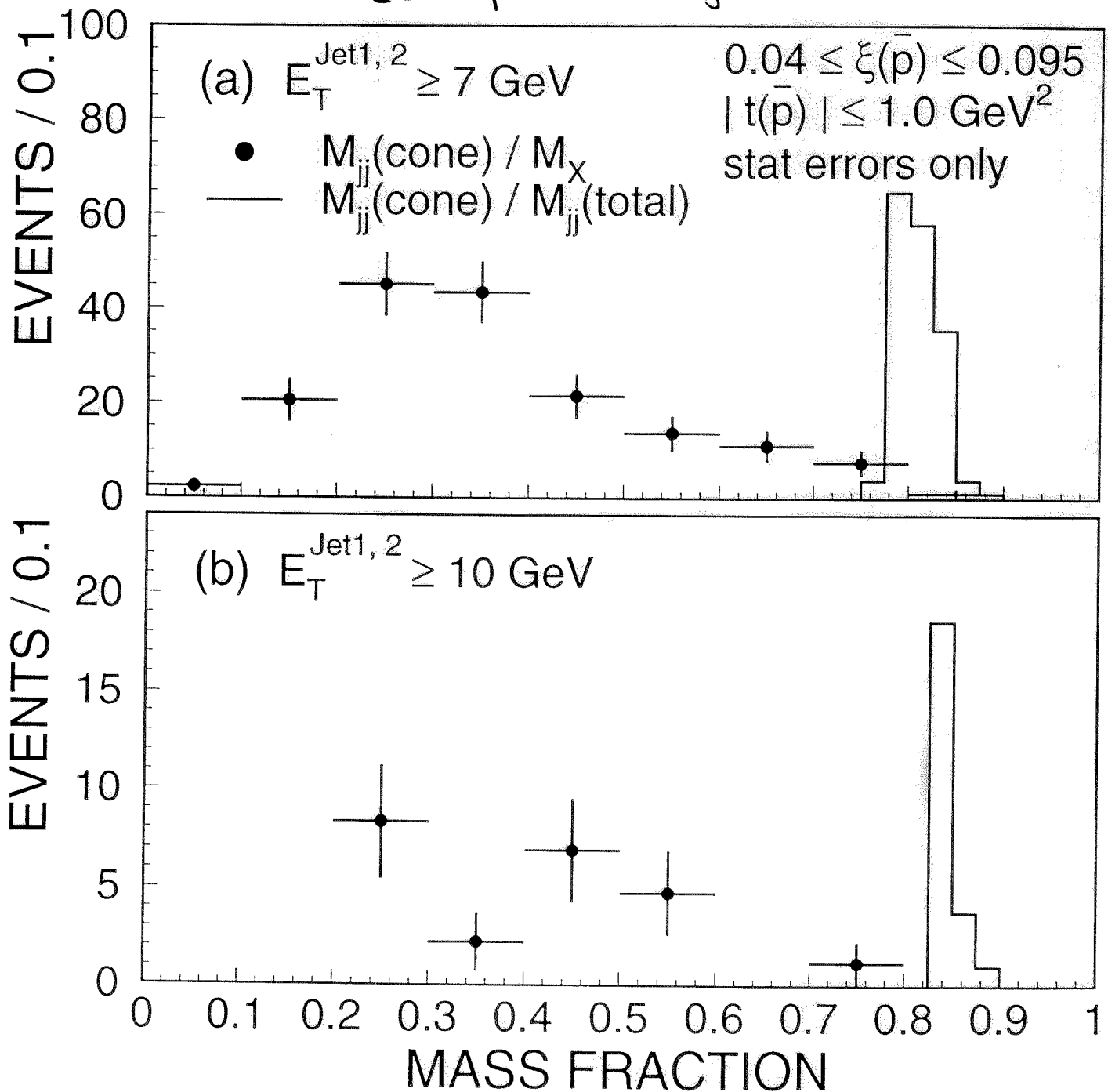


Search for Higgs in a missing mass experiment



$$P\bar{P} \rightarrow P\bar{P} \text{ \#\#}$$

CDF preliminary





## Summary

- Expanded understanding of QCD dynamics at high energy
- “New” language in terms of sizes of interacting states - interplay between hard and soft contributions
- Many features of the theoretical expectations and of the data to explore
- Important implications for scattering off nuclear target

WHY?

Citation from L. Frankfurt:

“It may allow us to produce in LAB new form of (partonic dense matter) in a controlled manner !!!”