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**Hadronic Final States in  
Diffractive Scattering at HERA**

**Armen Bunyatyan**

**Max-Planck-Institut für Kernphysik, Heidelberg  
and Yerevan Physics Institute**

**Representing the H1 and ZEUS Collaborations**

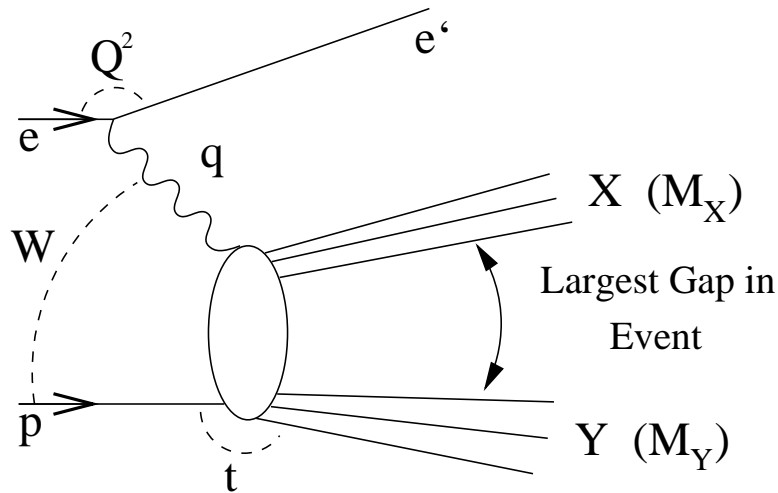
## Outline:

- Introduction
- Event Shapes
- Energy Flow
- Hadron Production
- Dijet Production
- Open Charm Production
- Rapidity Gap Between Jets
- Summary

## Introduction

- Hard scattering in diffractive processes have been observed in  $p\bar{p}$  (UA8, Tevatron) and  $ep$  (H1, ZEUS) collisions.
- The contribution of diffractive processes to the  $ep$  interaction cross-section has been measured in terms of a diffractive structure function  $F_2^{D(3)}(x_{\mathbb{P}}, \beta, Q^2)$ .
- These measurements were successfully interpreted in terms of resolved Pomeron ( $\mathbb{P}$ ) model with diffractive parton densities which are dominated by gluons at the starting scale and evolved with DGLAP.  
A Pomeron model with only quarks at starting scale is not able to describe the measurements.
- The many hadronic final state observables are sensitive to the QCD structure of diffraction and provide independent tests of the pomeron structure extracted from  $F_2^{D(3)}$ .

## Kinematics of Diffractive $ep$ scattering



$$Q^2 = -q^2$$

photon virtuality

$$x = \frac{Q^2}{2q \cdot p}$$

Bjorken scaling variable

$$W^2 = (p + q)^2$$

$\gamma^*p$  CM energy squared

$$t = (p - p_Y)^2$$

4-momentum transfer squared

$$M_X, (M_Y)$$

Inv. mass of system  $X$  ( $Y$ )

$$\beta = \frac{Q^2}{2q \cdot (p - Y)}$$

fraction of  $IP$  momentum  
carried by struck quark

$$x_{\mathcal{P}} = \frac{q \cdot (p - Y)}{q \cdot p}$$

fraction of  $p$  momentum  
transferred to  $IP$

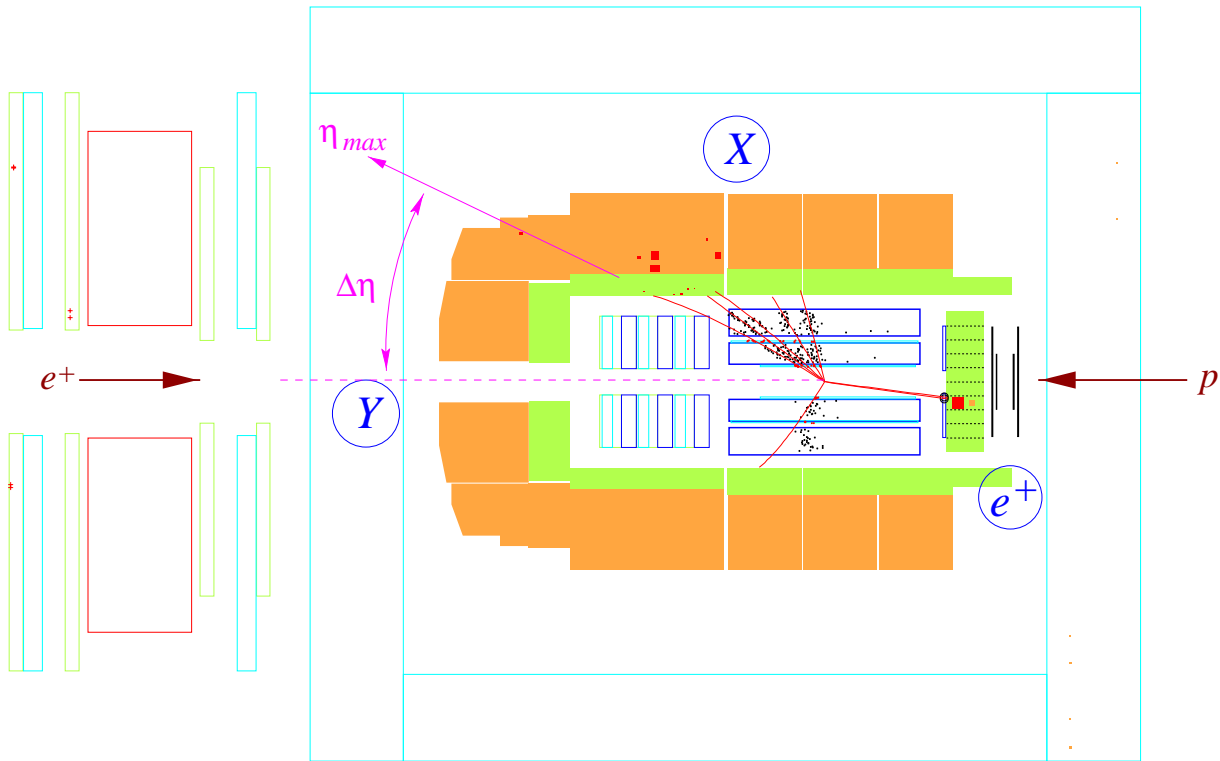
$$x_{\mathcal{P}} \simeq 1 - E_Y / E_p$$

$$x_{\mathcal{P}} \beta = x$$

$$M_X \ll W, \text{ small } M_Y (\simeq m_p), \text{ small } |t| (\lesssim 1 \text{ GeV}^2)$$

- $Q^2 \approx 0, |t| \approx 0$ : similar to soft hadron-hadron interactions
- $Q^2 \gg 0$ :  $\gamma^*$  probes  $IP$  structure
- large  $|t|$ : search for perturbative  $IP$

## Selection of diffractive events



## Selection: Leading Proton Tag

- Leading Proton is measured in very forward detectors
- Proton with  $z \simeq E'_p / E_p \gtrsim 0.97$  ( $x_P \lesssim 0.03$ )  
 $\implies M_Y = M_p$  (pure single diffraction)

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## Selection: Large Rapidity Gap Events

No colour field between hadronic subsystems  $X$  and  $Y$   
 $\implies$  no hadronic activity in the forward part of detector  
 $\implies$  **Large Rapidity Gap**  $\Delta\eta \simeq \ln(W^2 / M_X^2)$   
 (pseudorapidity  $\eta = -\ln \tan \theta / 2$ )

- Proton is not directly measured
- $x_P \lesssim 0.05$

# Models for diffractive hard scattering

- factorizable models:

- Monte-Carlo programs:

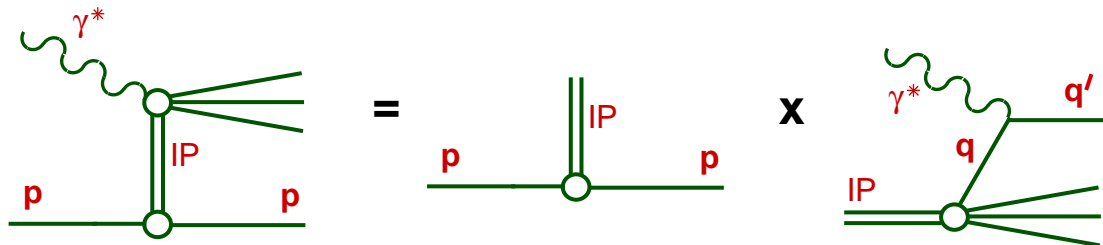
RAPGAP (Jung), POMPYT (Bruni, Ingelman)

- also Alvero, Collins, Terron, Whitmore;

Kunst, Stirling;...

- flux of spacelike  $\mathbb{P}$  from proton

- $\gamma^*$  couples to parton from  $\mathbb{P}$



$$F_2^{D(3)}(x_{\mathbb{P}}, \beta, Q^2) \propto f_{\mathbb{P}/p}(x_{\mathbb{P}}) \times F_2^{\mathbb{P}}(\beta, Q^2)$$

- parton densities in  $\mathbb{P}$  can be taken from the QCD fits to  $F_2^{D(3)}$  data:

- \* “leading gluon” distribution (fits 2 and 3)

- \* “quark-based” distribution (fit 1)

⇒ test universality of parton distributions

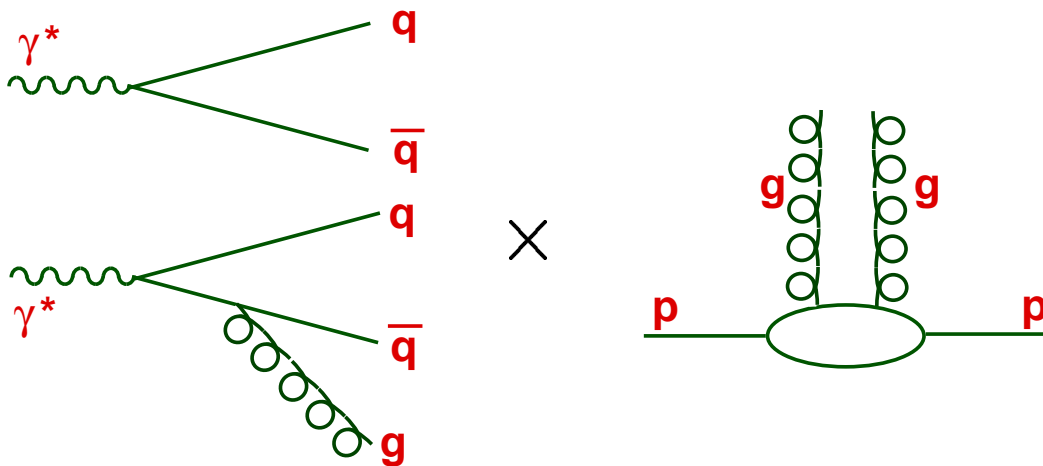
- **2-gluon exchange models:**

- Monte-Carlo programs:

RIDI (Ryskin, Solano), RAPGAP

- Nikolaev, Zakharov, Genovese, Ryskin, Diehl, Bartels, Ellis, Kowalski, Wüsthoff, Lotter, Bialas, Peschanski,...

- $q\bar{q}$ ,  $q\bar{q}g$  production via  $gg$ -exchange/BFKL ladder



- **Soft Colour Interactions:**

- Monte-Carlo programs:

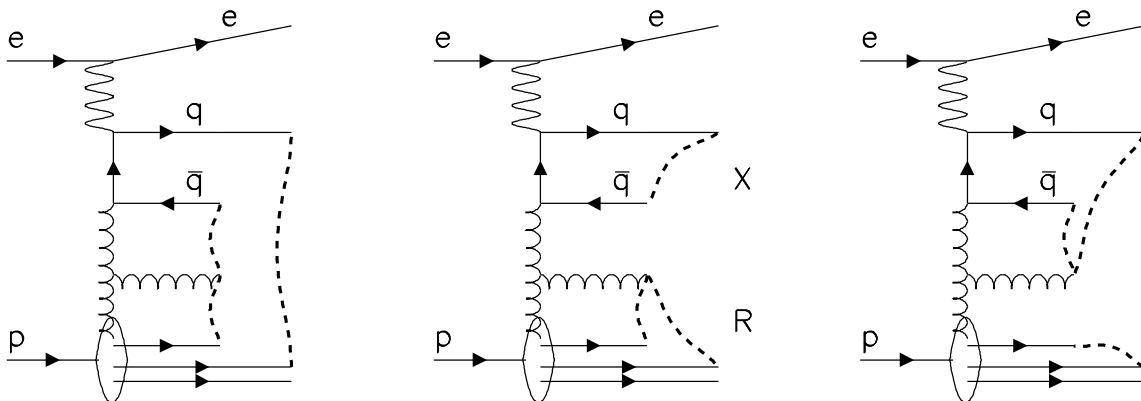
LEPTO (Edin, Ingelman, Rathsman)

- Alternative model without  $\mathbb{P}$  concept

- Start from standard DIS (dominantly BGF at low  $x$ )

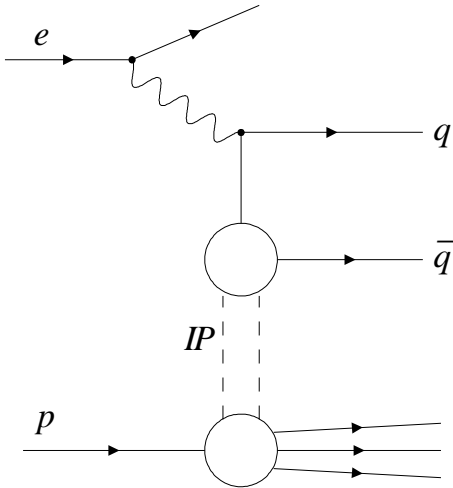
- Colour rearrangement on the hadronic final states

- Attempt of unifying standard DIS and diffraction



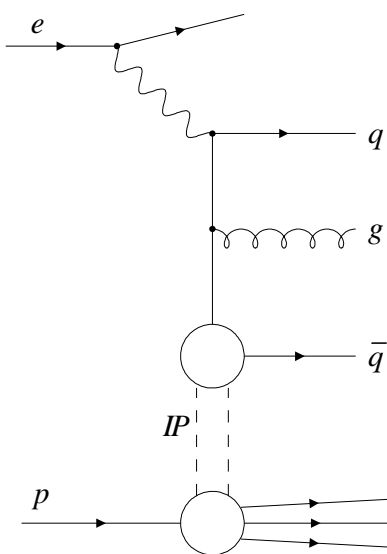
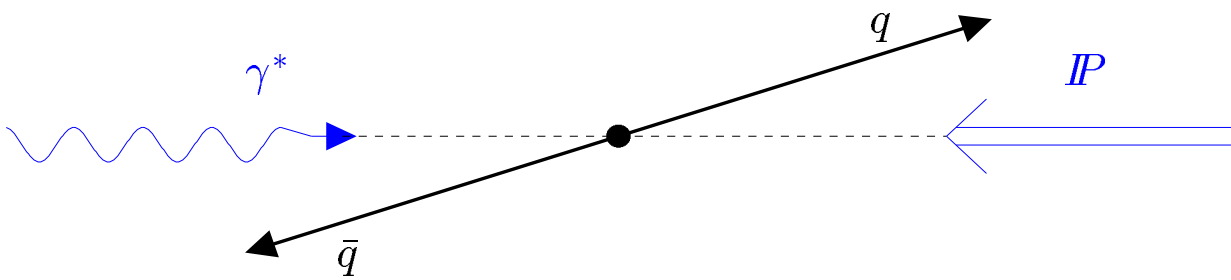
# Expectations for hadronic final states

## Quark-dominated $IP$



### Lowest order $\mathcal{O}(\alpha_{em})$

- Aligned-jet (AJM) configuration
- Triplet-antitriplet system with low  $p_T$
- Small  $p_T$  from intrinsic  $k_T$  of quarks
- Some  $p_T$  from hadronization and particle decays

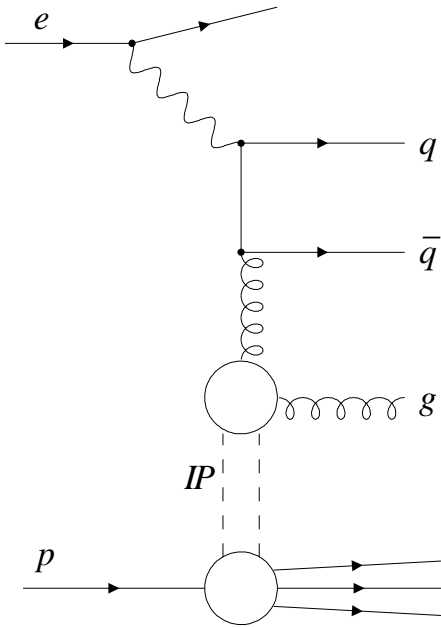


### Higher order $\mathcal{O}(\alpha_{em}\alpha_s)$ — QCD-C

- Three-parton topology
- Significant  $p_T$

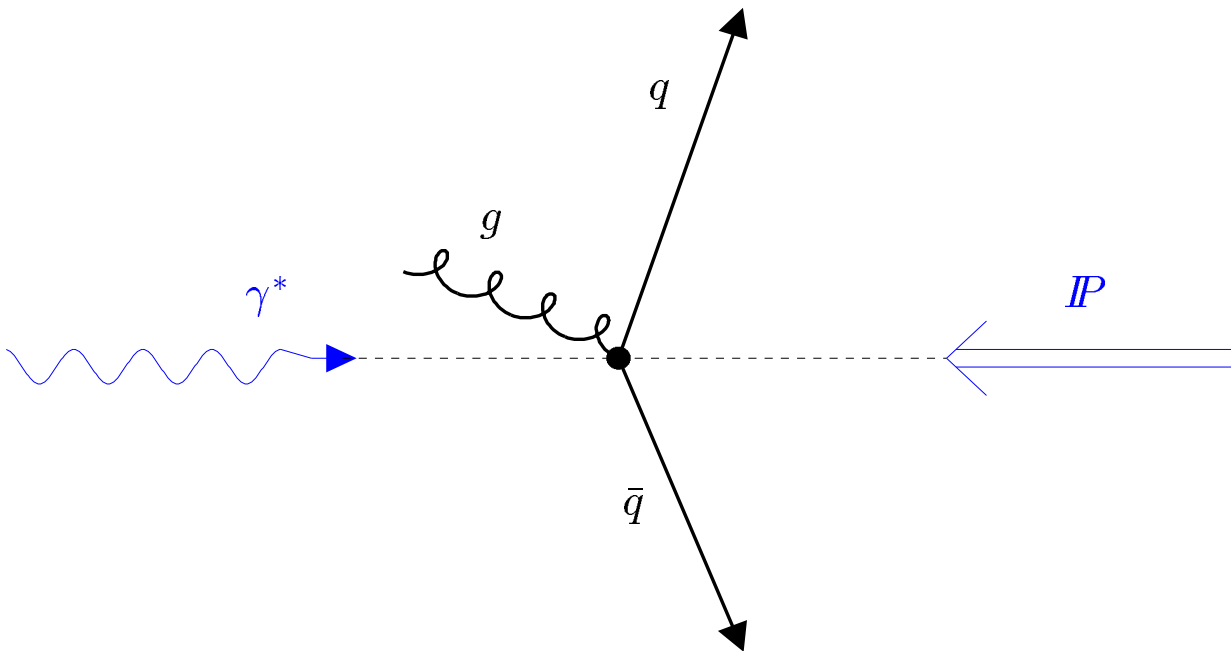


## Gluon-dominated $IP$



### Lowest order $\mathcal{O}(\alpha_{em}\alpha_s)$ — BGF

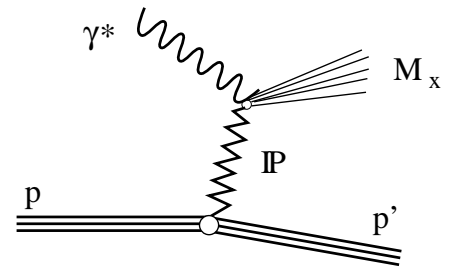
- BGF:  $q$  and  $\bar{q}$  not aligned along  $\gamma^*$  axis  $\rightarrow$  large  $p_T$
- Higher parton multiplicity in final state
- Additional octet-octet colour field



# Global Event Shapes: Definition of variables

- Thrust

$$T = \max \frac{\sum_i |\mathbf{n} \cdot \mathbf{p}_i|}{\sum_i |\mathbf{p}_i|}$$

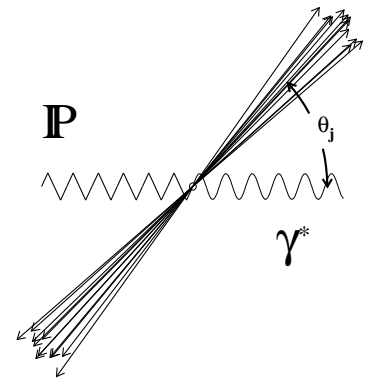


- Sphericity

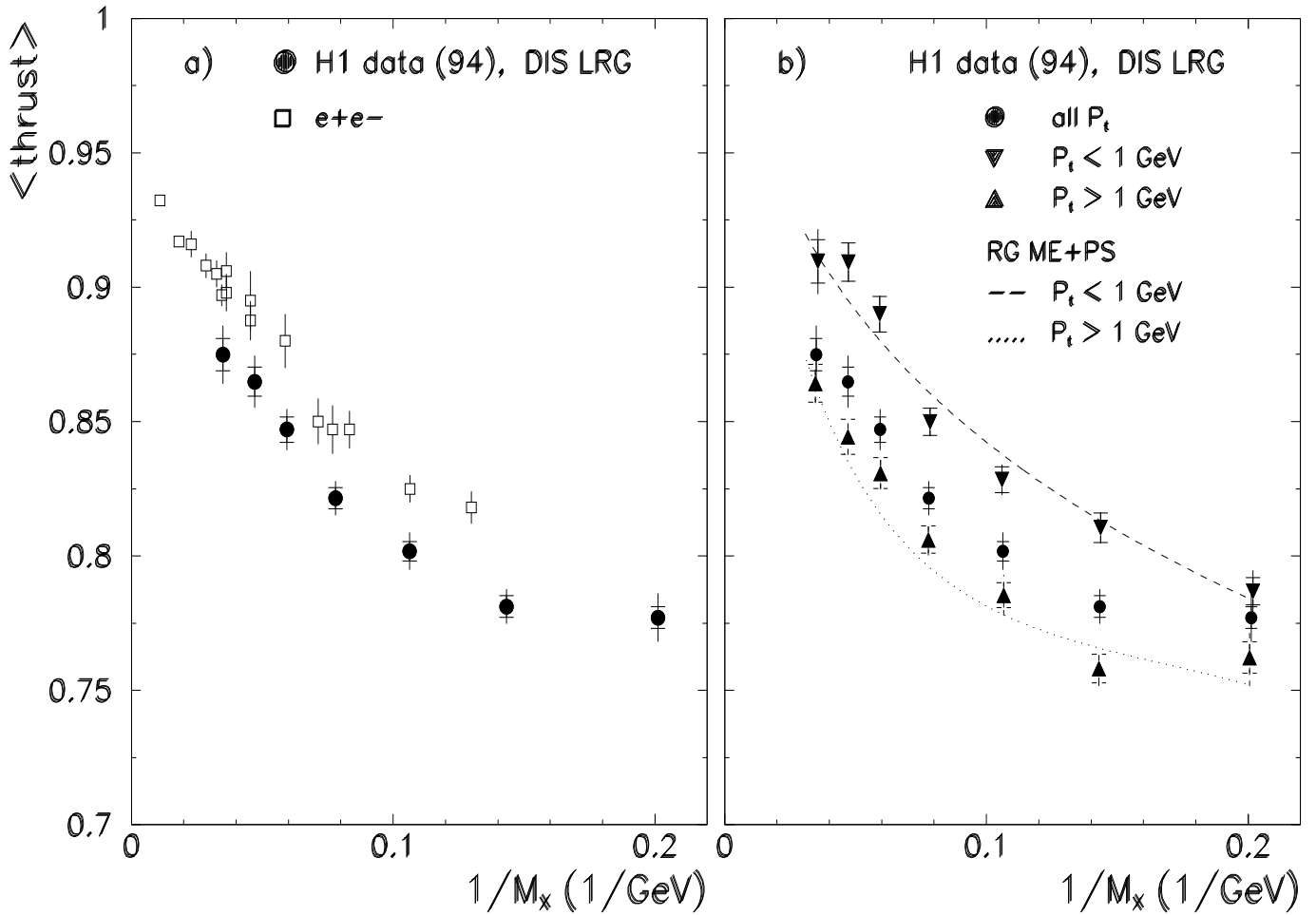
$$S^{\alpha\beta} = \frac{\sum_i p_i^\alpha p_i^\beta}{\sum_i |\mathbf{p}_i|^2} \quad \alpha, \beta \in x, y, z$$

eigenvalues of  $S^{\alpha\beta}$ :  $\lambda_1 \geq \lambda_2 \geq \lambda_3$

$$S = \frac{3}{2}(\lambda_2 + \lambda_3)$$



Particle Trajectories	Thrust	Sphericity
	$\rightarrow \frac{1}{2}$	$\rightarrow 1$
	$\rightarrow 1$	$\rightarrow 0$
	$\approx \frac{3}{4}$	$\approx \frac{1}{2}$



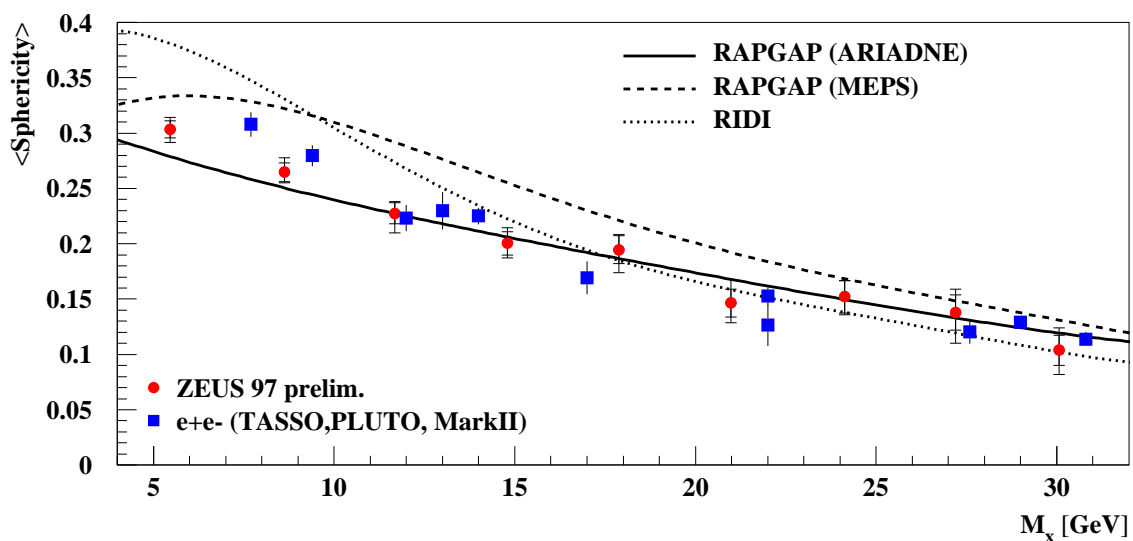
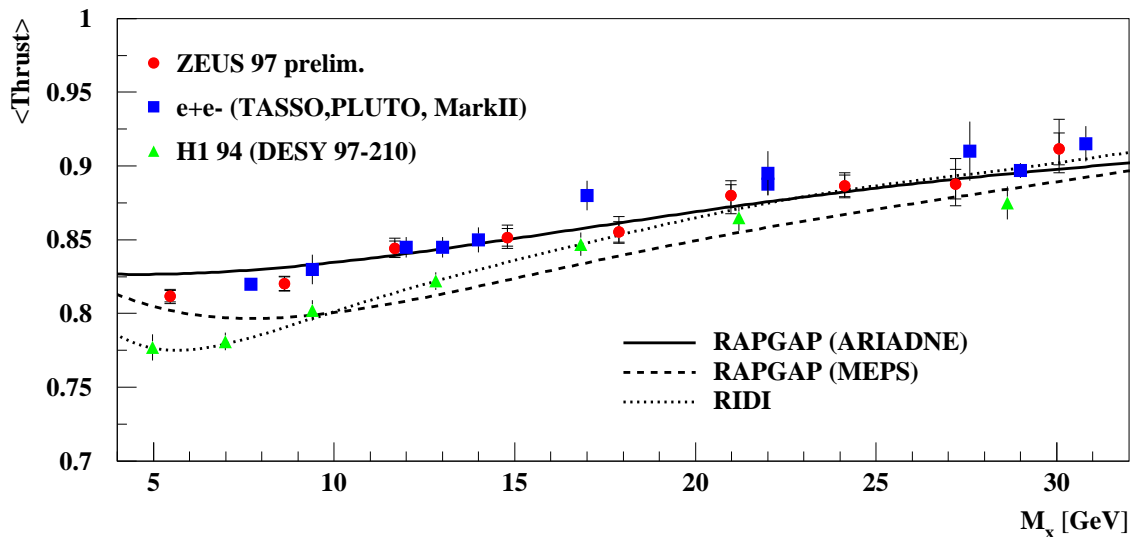
**H1: large rapidity gap**

$10 < Q^2 < 100 \text{ GeV}^2, y < 0.5$

$x_{\mathbb{P}} < 0.05, 4 < M_X < 36 \text{ GeV}$

$|t| < 1 \text{ GeV}^2, M_Y < 1.6 \text{ GeV}$

- $\langle T \rangle$  increases with  $M_X \implies$  increasing of back-to-back correlations, dominant two jet topology of the final state
- For fixed  $M_X$  average thrust is lower for larger  $P_t$  (w.r.t. incoming proton direction)  $\implies \geq 3$  parton configuration
- $\langle T \rangle_{LRG} < \langle T \rangle_{ee} \implies q\bar{q}$  states with limited  $p_T$  hadronization are not sufficient: higher parton multiplicities are more important in DIS LRG events than in  $e^+e^-$
- **RAPGAP**-factorizable Pomeron model, with gluon dominated  $\mathbb{P}$  parton densities from H1 fits to  $F_2^{D(3)}$  data, gives good description of  $\langle T \rangle$ .



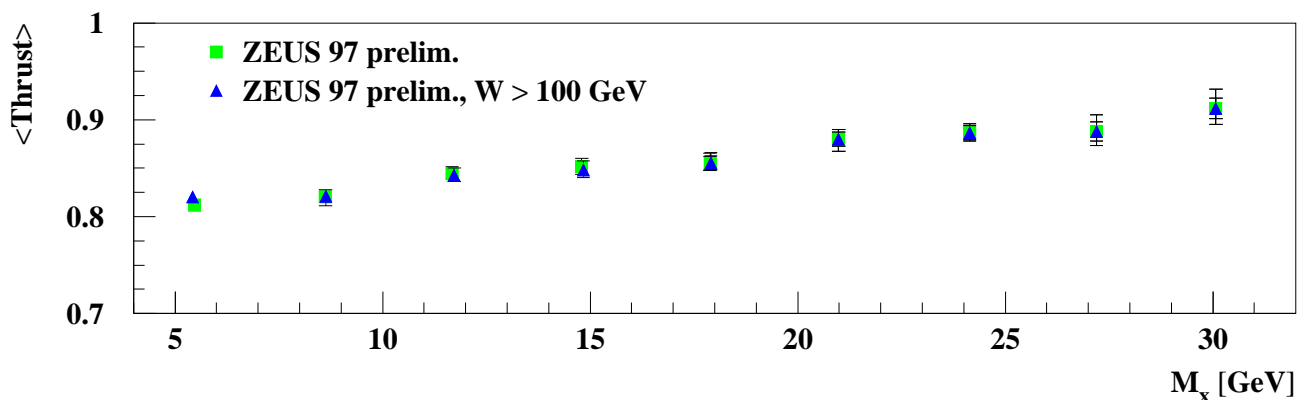
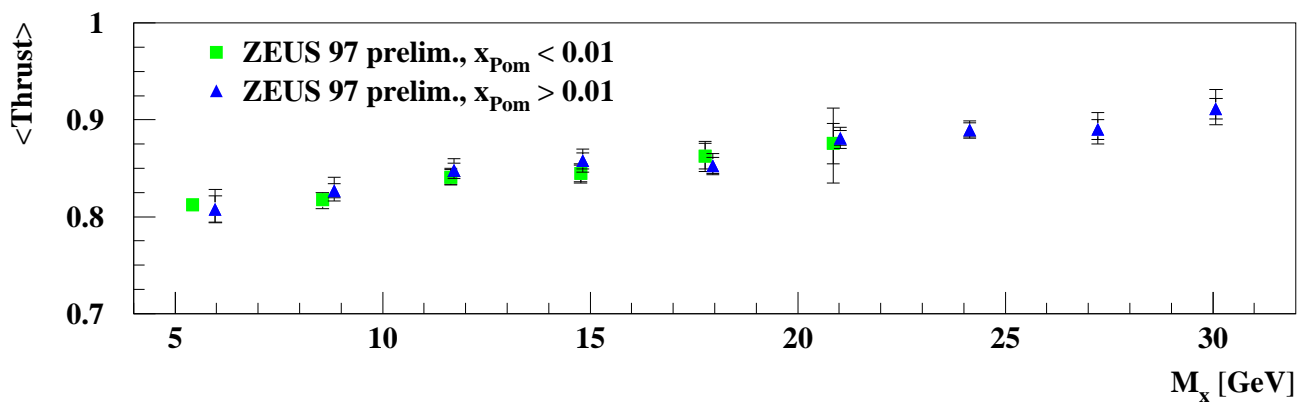
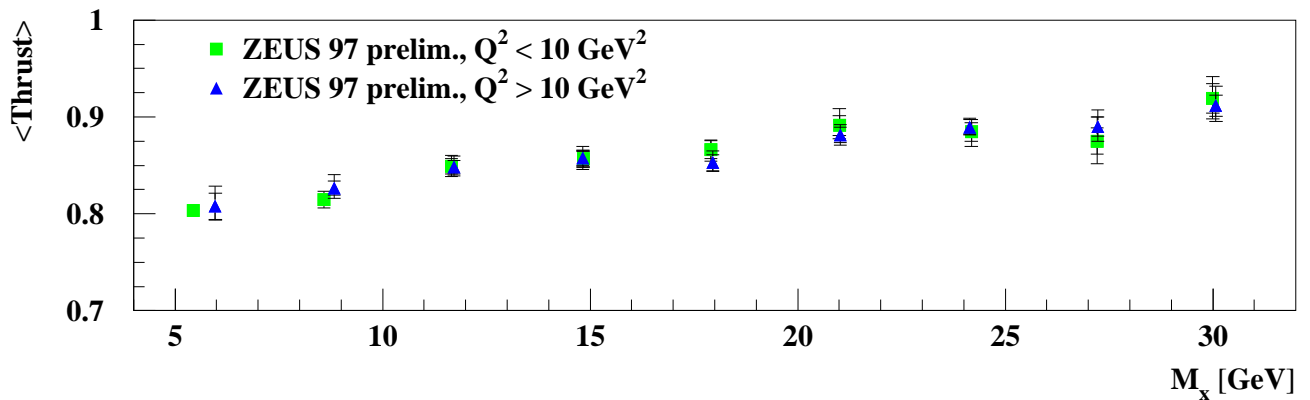
ZEUS: leading proton  
 $4 < Q^2 < 90 \text{ GeV}^2$ ,  $0.03 < y < 0.95$   
 $0.0003 < x_P < 0.03$ ,  $4 < M_X < 35 \text{ GeV}$

- ZEUS measurement consistent with  $e^+e^-$
- H1 sees less collimated events than ZEUS (need more gluons)  
 ⇒ discrepancy between experiments!  
 (might be due to different event selection/kinematics: H1-Large rapidity gap, ZEUS- leading proton )

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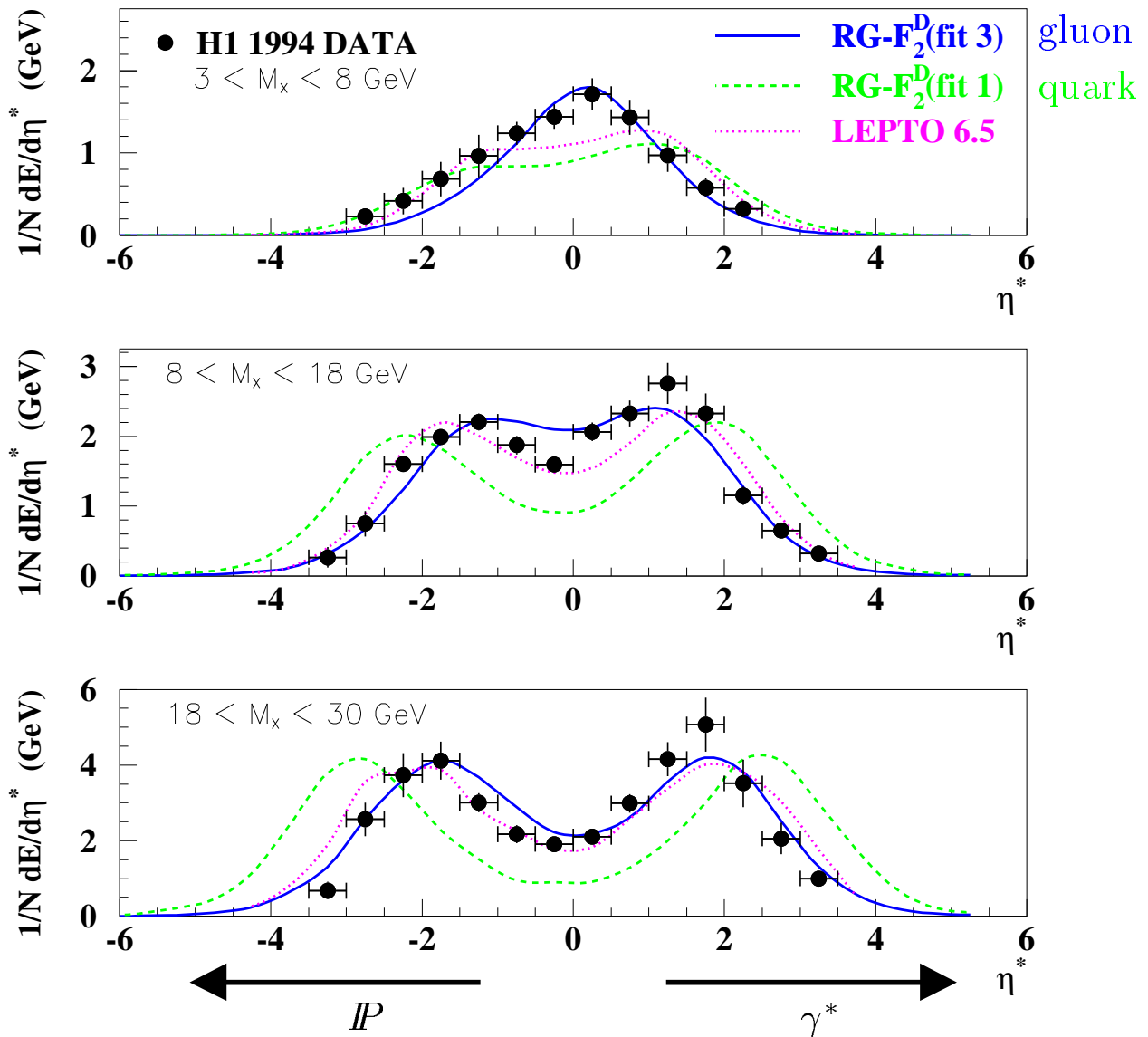
- RIDI fails at low  $M_X$ , but closer to H1
- RAPGAP (Ariadne) gives best description. Difference between ARIADNE and MEPS ⇒ Fragmentation mechanism is important

## Global Event Shape $Q^2$ , $x_{\mathcal{P}}$ and $W$ dependence



- no dependence on  $Q^2$
- no dependence on  $x_{\mathcal{P}}$
- no influence from low  $W$  contribution
- (same holds for Sphericity)

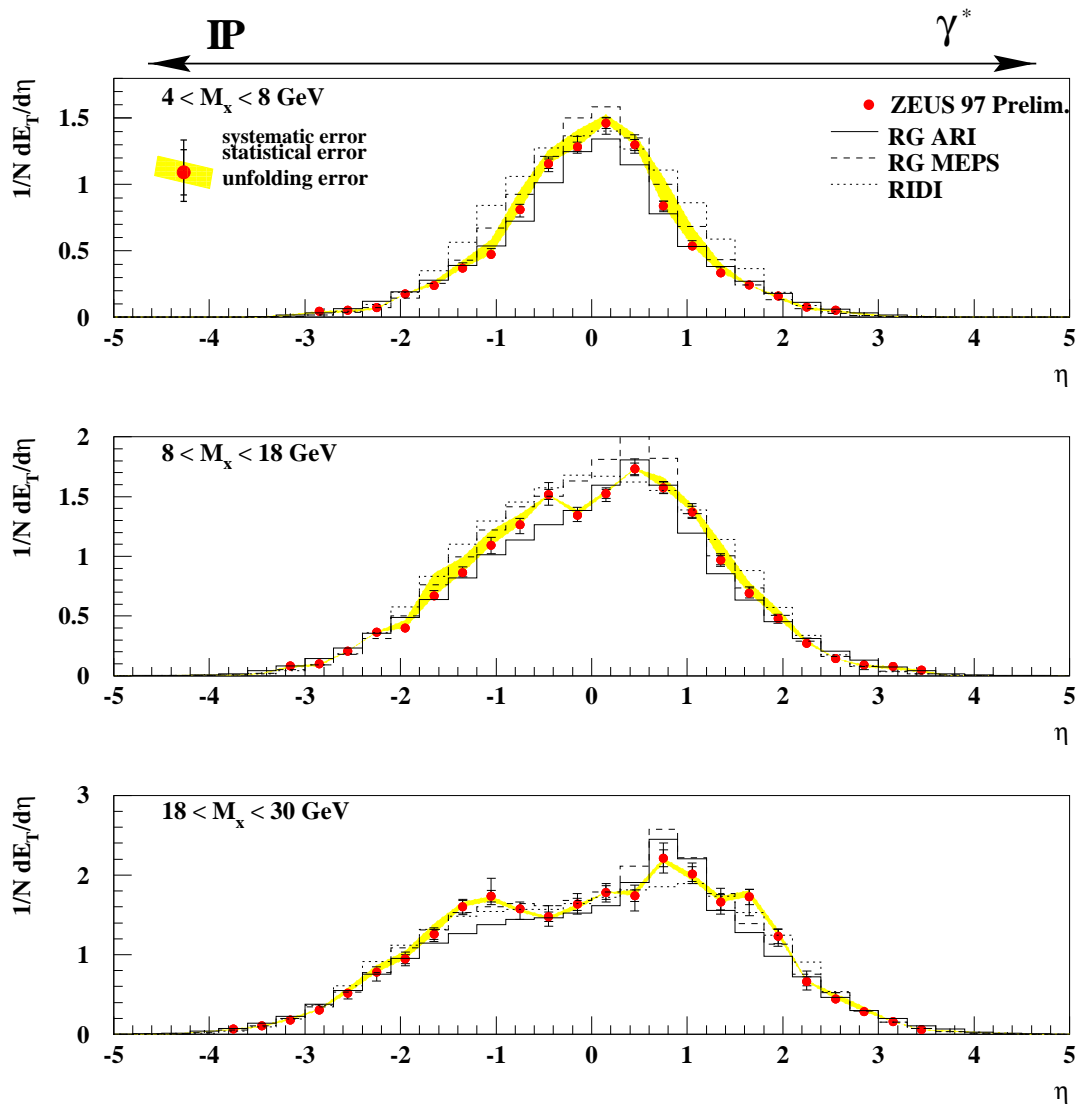
# Energy flow in $\gamma^* IP$ CMS- $1/N dE/d\eta^*$



**H1: large rapidity gap**  
 $7.5 < Q^2 < 100 \text{ GeV}^2, 0.05 < y < 0.6$   
 $x_{IP} < 0.025, 3 < M_X < 30 \text{ GeV}$   
 $|t| < 1 \text{ GeV}^2, M_Y < 1.6 \text{ GeV}$

- General agreement between H1 and ZEUS-leading proton data
  - “Two jet” structure develops at higher  $M_X$
  - Slight enhancement of energy in the current hemisphere
  - Well described by **RAPGAP (gluon)**, but not by **RAPGAP (quark)**
- $\Rightarrow$  large contribution from gluons !

# Transverse Energy Flow $1/N dE_T/d\eta^*$



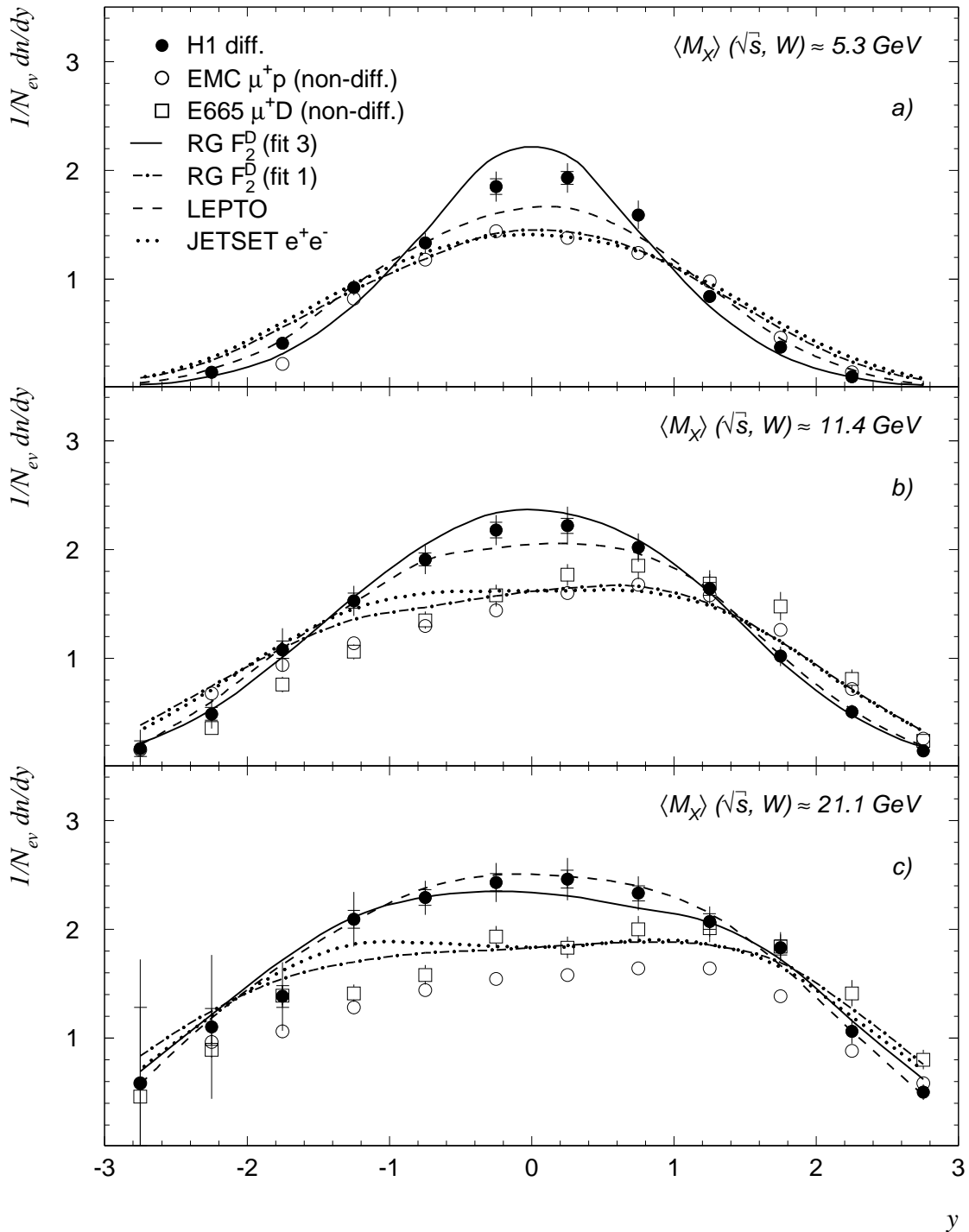
**ZEUS: leading proton**

$4 < Q^2 < 90 \text{ GeV}^2$ ,  $0.03 < y < 0.95$

$0.0003x_P < 0.03$ ,  $4 < M_X < 30 \text{ GeV}$

- “Two jet” structure is visible at higher  $M_X$
- Enhancement of transverse energy in the current hemisphere ( $\gamma^*$ -side)

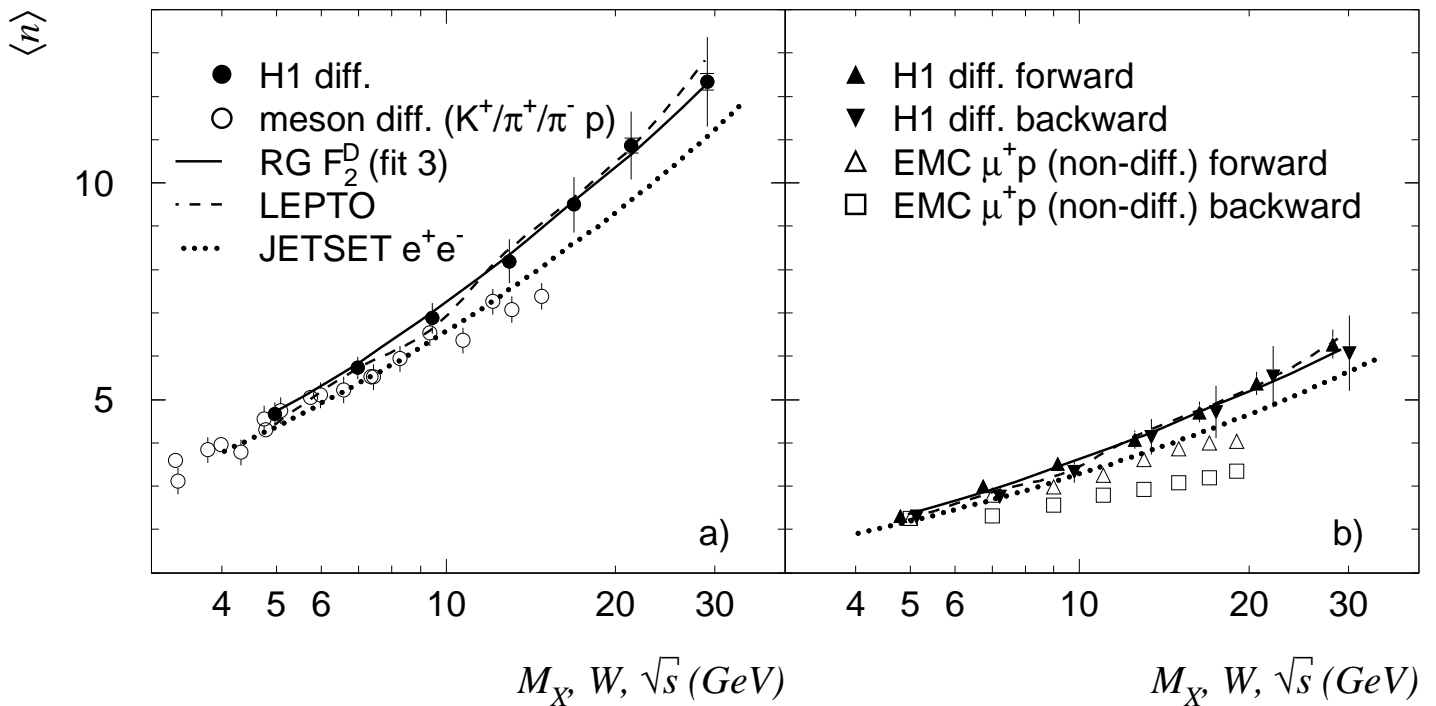
# Charged Particle Rapidity Distribution



- In central region particle density is larger than in  $\mu N$  interactions at  $W^2 \approx M_X^2$
- Symmetrical about  $y = 0$
- RAPGAP with a quark based  $\mathcal{IP}$  predicts the rapidity spectra close to  $e^+e^-$  and  $\mu N \implies q\bar{q} + \text{gluon radiation is not sufficient}$
- RAPGAP with hard gluon dominated  $\mathcal{IP}$  and LEPTO describe the rapidity spectra (but deviations in the lowest  $M_X$  bin).

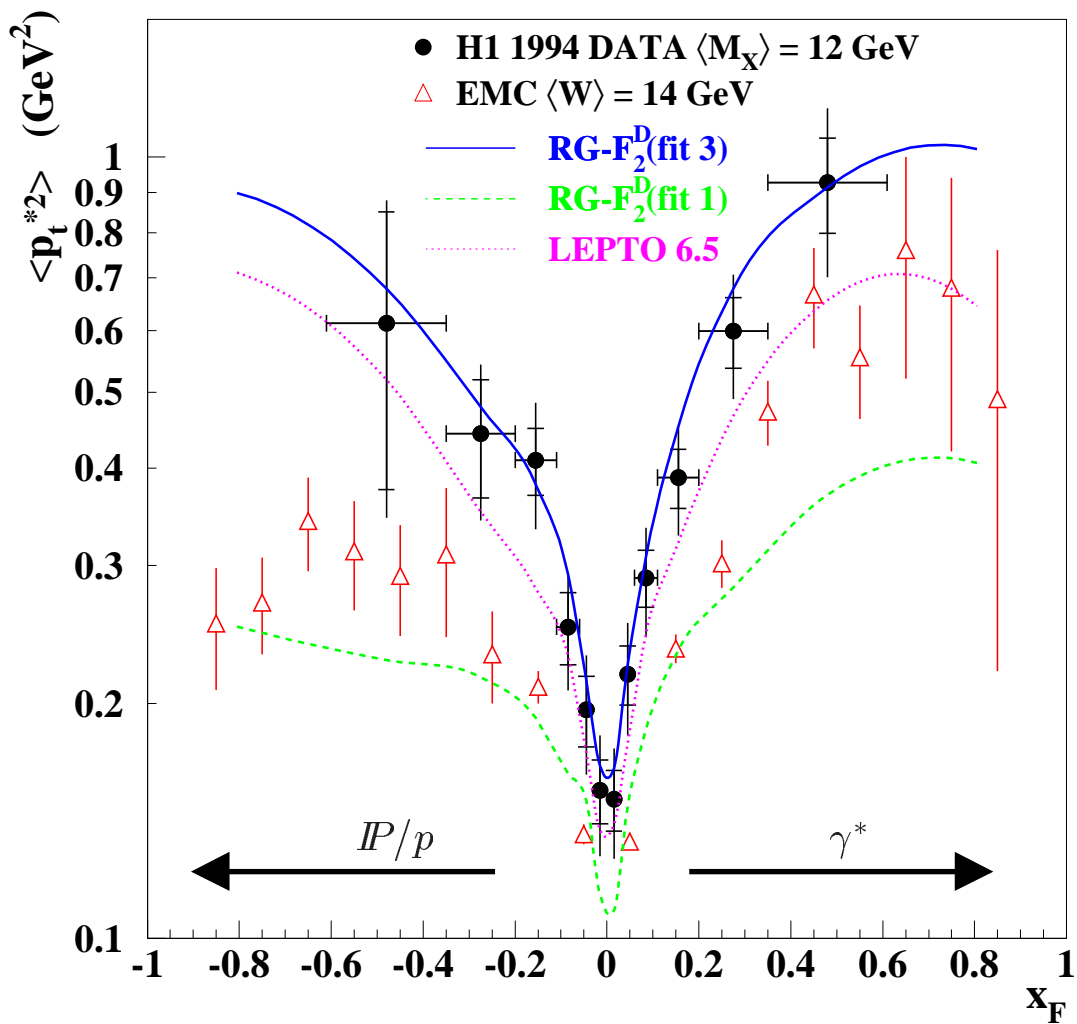


# Charged particle multiplicity



- Average multiplicity  $\langle n \rangle$  rises with  $M_X$  ( $W, \sqrt{s}$ )
- At low masses ( $M_X < 10 \text{ GeV}$ ) similar to  $e^+e^-$  and meson diffraction  $\implies$   
hadronisation of single string between the quark and antiquark
- At higher masses ( $M_X > 10 \text{ GeV}$ )  $\langle n \rangle$  rises faster than in  $e^+e^-$  and meson diffraction  $\implies$   
contribution from more complex ( $q\bar{q}g$ ) parton configuration
- Forward-backward symmetry (unlike the  $\mu p$  data)

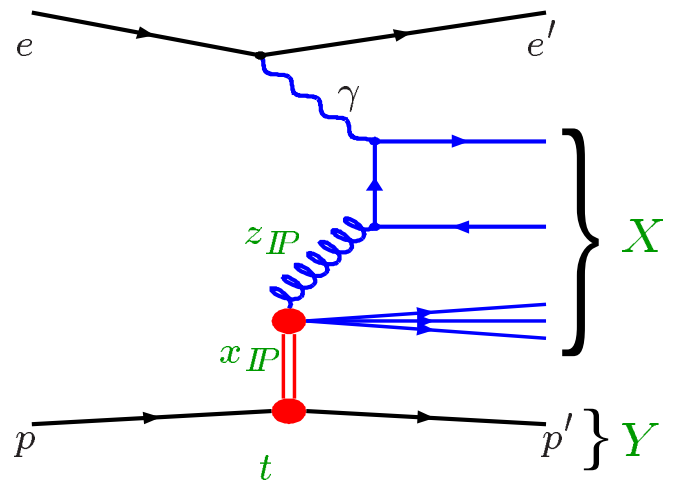
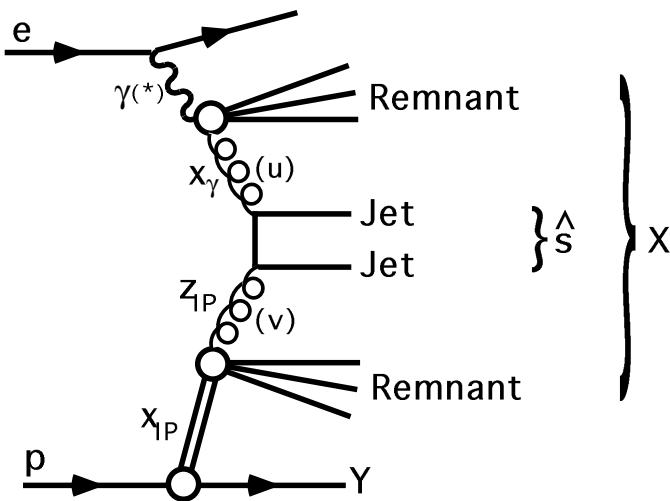
## “Seagull plot” ( $\langle p_T^{*2} \rangle$ vs $x_F$ )



- $\langle p_T^{*2} \rangle$  is higher in diffractive data than in  $\gamma^* p$ 
    - ⇒ Larger contribution from scattering from gluons, increasing role of BGF processes
  - Symmetry between target and current hemispheres ⇒
    - in non-diffractive  $\gamma^* p$  the high  $p_T$  radiation is suppressed from extended  $p$  remnant
    - in diffractive  $\gamma^* p$ — more point-like partonic system in the target fragmentation region
  - Good agreement between H1 and ZEUS
- 
- Well described by RAPGAP (gluonic  $IP$ ), LEPTO and RIDI
  - Predictions of RAPGAP (quark based  $IP$ ) are too low for all  $x_F$

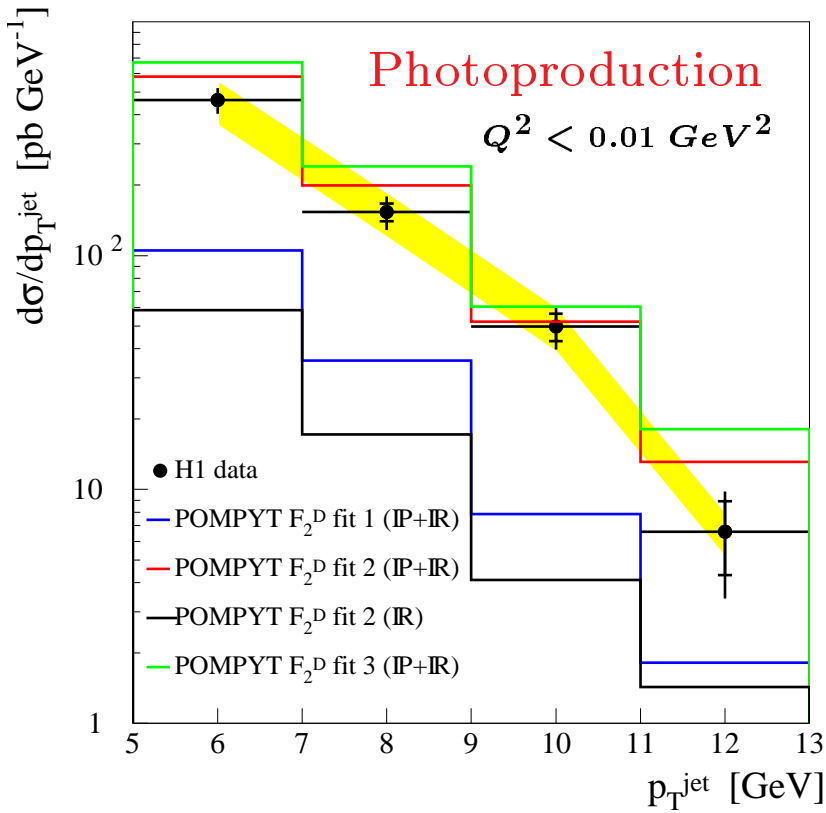
## Charm and high $p_T$ Jet production

- Ideal test of underlying dynamics of diffraction:
  - Cross-sections are calculable.
  - Production mechanism sensitive to the gluon content.



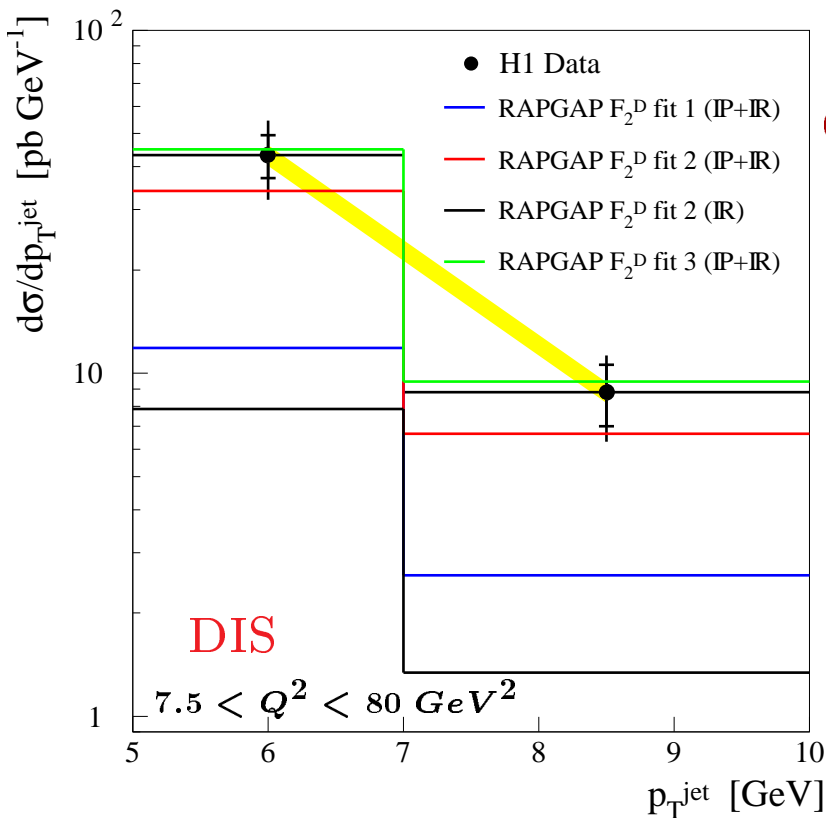
- **2-Jets are reconstructed in the central detectors.**
- Jets are identified as a collimated energy deposited in  $\eta - \phi$  space, within the cone of  $R = \sqrt{\Delta\eta^2 + \Delta\phi^2} = 1$ .
- $p_T^{jet}$  is defined relative to  $\gamma^*$  axis in the rest frame of  $X$ .
- Measurements are made both in photoproduction  $Q^2 \simeq 0$  and in DIS regimes
- In photoproduction regime distinguish between the 'direct' ( $x_\gamma = 1$ ) and 'resolved' ( $x_\gamma < 1$ ) processes: ( $x_\gamma$  – fraction of  $\gamma$  momenta involved in the hard interaction).

# $p_T^{jet}$ -spectra



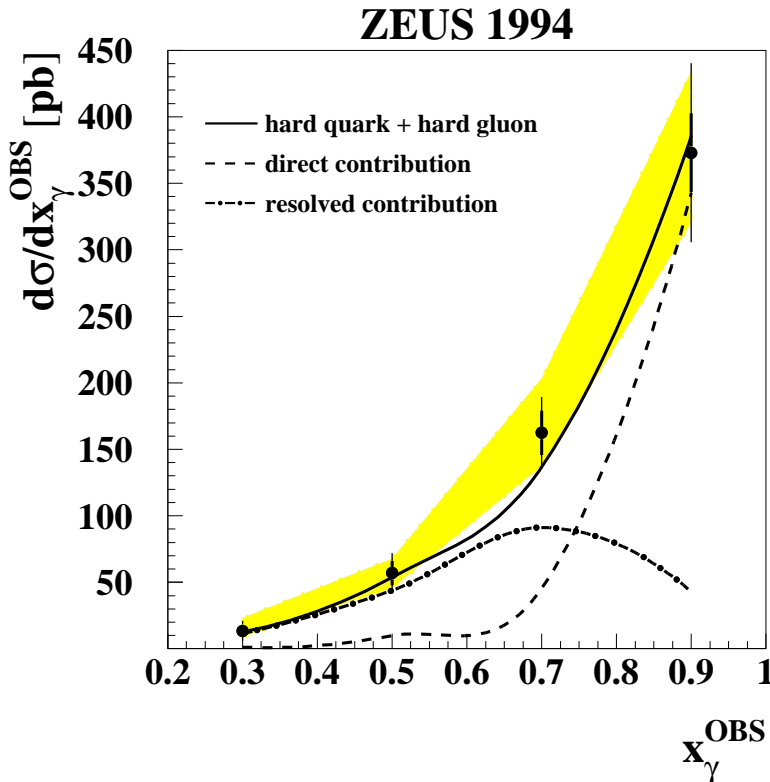
Data reasonably well described by gluon dominated  $IP$

Quark dominated  $IP$  is too low by a factor  $\sim 5$



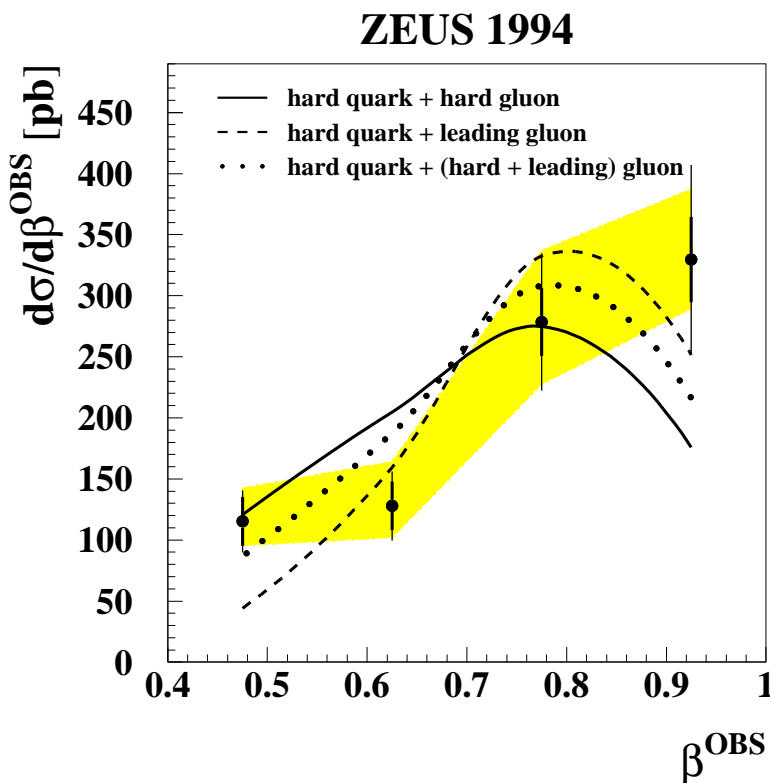
Contribution of sub-leading exchange  $\sim 15\%$

$x_{\gamma}^{jets}, z_{IP}^{jets}$  : fraction of  $\gamma, IP$  momentum transferred to the system  $X$  (i.e. entering the hard scattering)

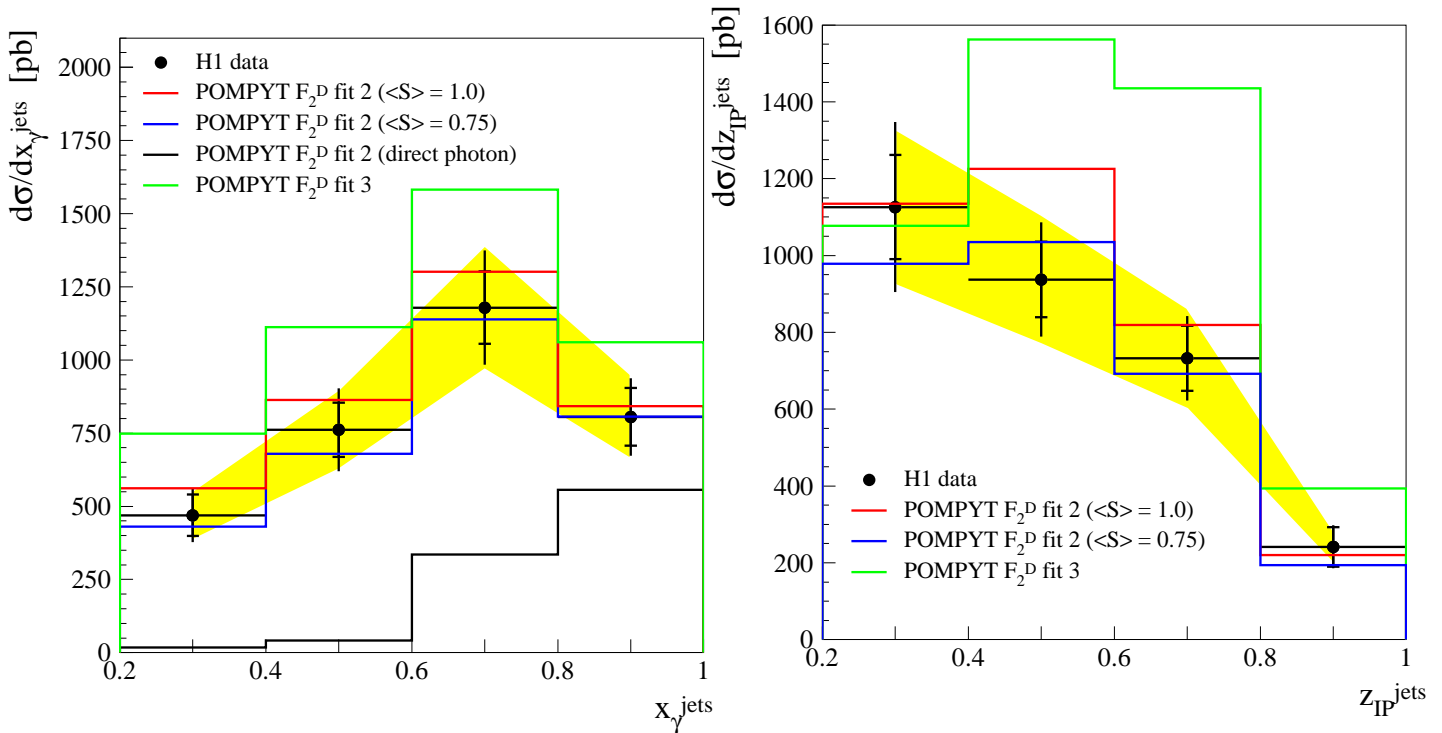


**ZEUS:** Large rapidity gap:

$$0.001 < x_{IP} < 0.03, \\ p_T^{jet} > 6 \text{ GeV}$$



- Both Direct ( $x_{\gamma} = 1$ ) and Resolved ( $x_{\gamma} < 1$ ) photon contributions observed
- Gluon dominated  $IP$  gives good description of ZEUS data



**H1: Large rapidity gap:  $x_P < 0.05$ ,  $p_T^{\text{jet}} > 5 \text{ GeV}$**

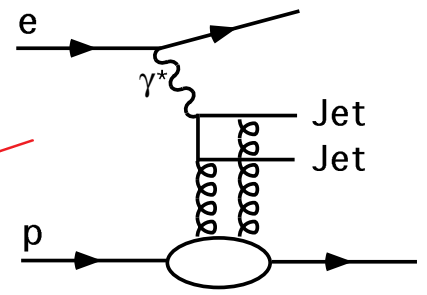
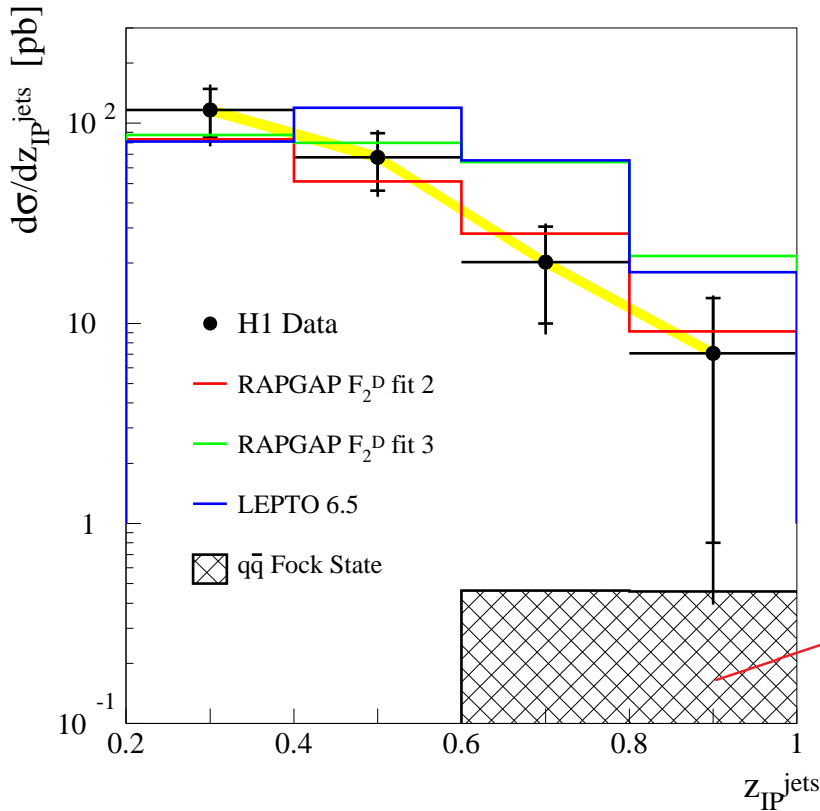
- MC predicts too high cross-section for H1
- H1 and ZEUS- different kinematic ranges (H1: lower  $p_T$ , higher  $x_P \implies$  lower  $x_{\gamma}$ , more resolved photon contribution)
- In diffractive resolved photoproduction additional interactions between the extended beam remnants would be expected to **destroy** rapidity gaps  $\implies$  **breaking** of diffractive factorization.

$$d\sigma_{\text{true}}^D(ep \rightarrow epX) < d\sigma^D(ep \rightarrow epX)$$

$$d\sigma_{\text{true}}^D = \langle S \rangle \cdot d\sigma^D, \text{ where } \langle S \rangle - \text{rapidity gap survival probability, } \langle S \rangle \leq 1$$

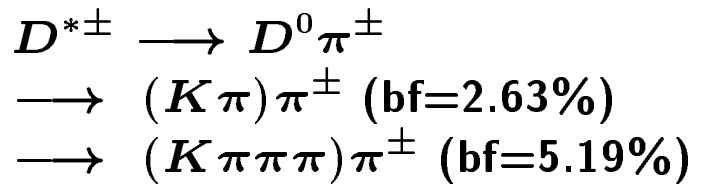
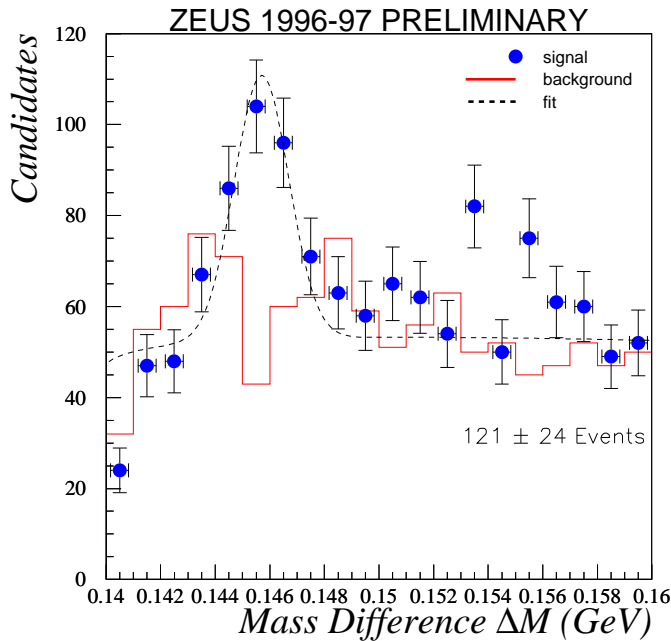
- To estimate: apply a constant weight  $\langle S \rangle$  to the MC events with  $x_{\gamma} < 0.8$ .
- $\langle S \rangle$  at the order of 0.4–0.8 gives reasonable description of data ( $\sim 0.1$  at Tevatron!).

# $z_{\mathcal{P}}^{jets}$ distribution in DIS



- Gluon dominated  $\mathcal{P}$  gives good description
- In 2 gluon exchange model the  $q\bar{q}$  state alone cannot describe data  $\implies q\bar{q}g$  states are required
- No evidence for a large 'super-hard  $\mathcal{P}$ ' contribution ( $z_{\mathcal{P}} = 1$ )

# Open Charm Production

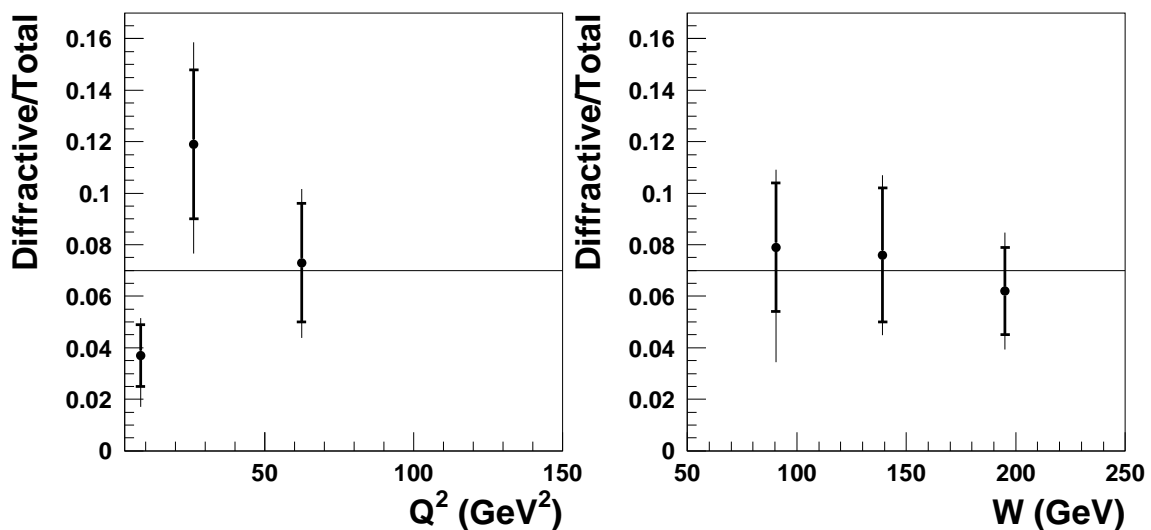


## Ratio of diffractive $D^{*\pm}$ to total $D^{*\pm}$ production

$$\text{Ratio } (D^* \rightarrow K \pi \pi) = 7.0 \pm 1.3^{+1.7}_{-1.8} \%$$

$$\text{Ratio } (D^* \rightarrow K 4\pi) = 8.9 \pm 2.4^{+1.7}_{-1.6} \%$$

## ZEUS 1995-97 PRELIMINARY



- Ratio of diffractive to total  $D^*$  production is consistent with ratio of diffractive to inclusive DIS ( $\sim 10\%$ )
- no significant  $Q^2$  or  $W$  dependence



$D^* \rightarrow K4\pi$

(ZEUS preliminary)

$$1 < Q^2 < 480 \text{ GeV}^2, 0.04 < y < 0.7$$
$$2 < p_T(D^{*\pm}) < 9 \text{ GeV}, |\eta(D^{*\pm})| < 1.5$$
$$x_P < 0.015, \beta < 0.8$$

$$N_{D^*} = 121 \pm 24$$

$$\sigma = 526 \pm 110^{+200}_{-240} \text{ pb}$$

$D^* \rightarrow K\pi\pi$

(ZEUS preliminary)

$$3 < Q^2 < 150 \text{ GeV}^2, 0.02 < y < 0.7$$
$$p_T(D^{*\pm}) > 1.5 \text{ GeV}, |\eta(D^{*\pm})| < 1.5$$
$$0.002 < x_P < 0.012, \beta < 0.8$$

$$N_{D^*} = 59 \pm 9$$

$$\sigma = 379 \pm 66^{+99}_{-140} \text{ pb}$$

interpolate  $D^* \rightarrow K4\pi$  to this kinematic region:

$$\sigma = 398 \pm 83^{+154}_{-180} \text{ pb}$$

**ZEUS: good agreement between different decay channels !**

$D^* \rightarrow K\pi\pi$

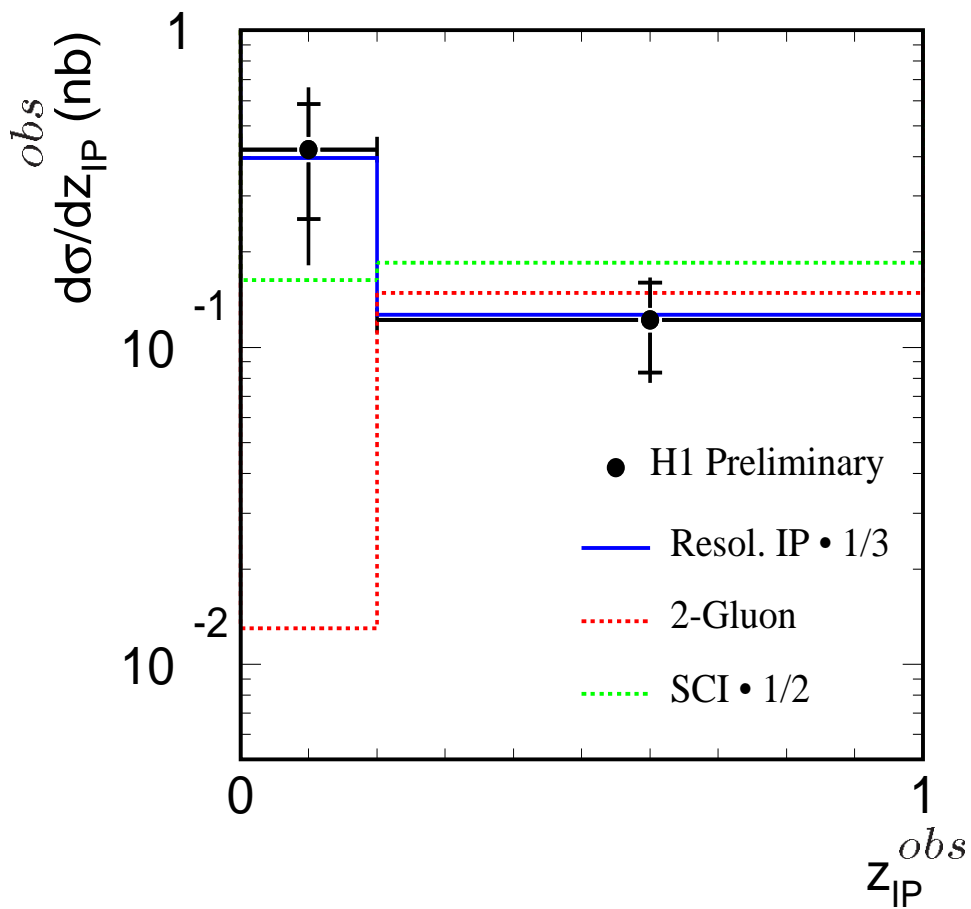
(H1 preliminary)

$$2 < Q^2 < 100 \text{ GeV}^2, 0.05 < y < 0.7$$
$$p_T(D^*) > 2. \text{ GeV}, |\eta(D^*)| < 1.5$$
$$x_P < 0.04, M_Y < 1.6 \text{ GeV}$$
$$|t| < 1 \text{ GeV}^2$$

$$N_{D^*} = 38 \pm 10$$

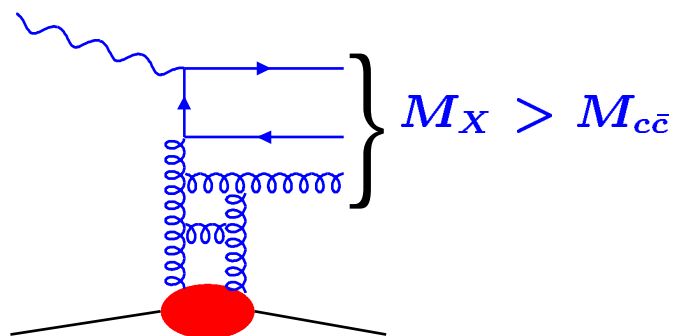
$$\sigma = 154 \pm 40 \pm 35 \text{ pb}$$

# Differential cross section $d\sigma/dz_{\mathcal{I}P}^{obs}$ (H1)



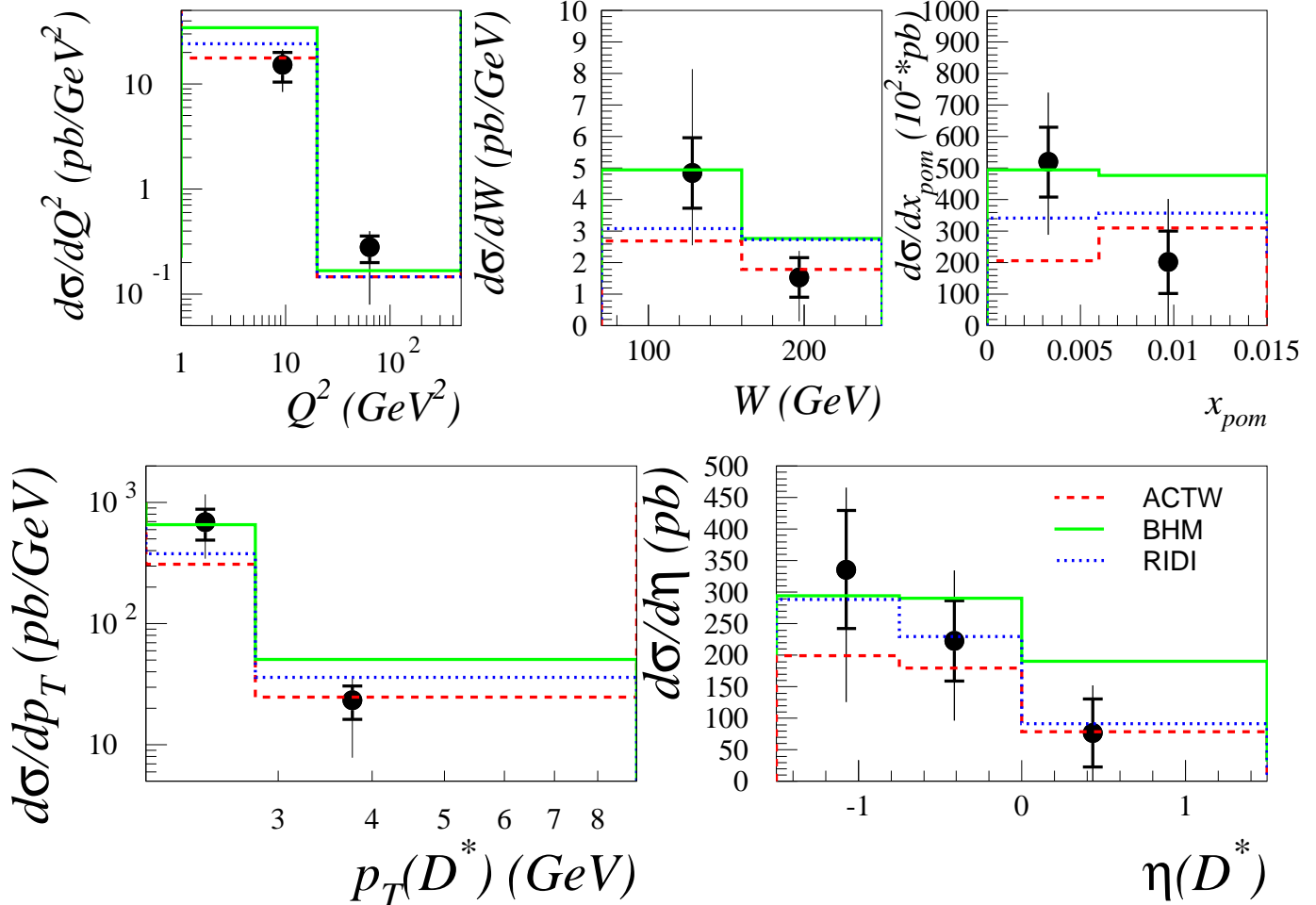
$$z_{\mathcal{I}P}^{obs} = \beta \cdot \left(1 + \frac{\hat{s}}{Q^2}\right) = \frac{(M_{c\bar{c}}^2 + Q^2)}{(M_X^2 + Q^2)}$$

- The large fraction of charm production at low  $z_{\mathcal{I}P}^{obs}$  (resolved  $\mathcal{I}P$ )
- The 2-gluons model with only  $c\bar{c}$  configuration is disfavoured  
 → higher order contributions (e.g. gluons) are required



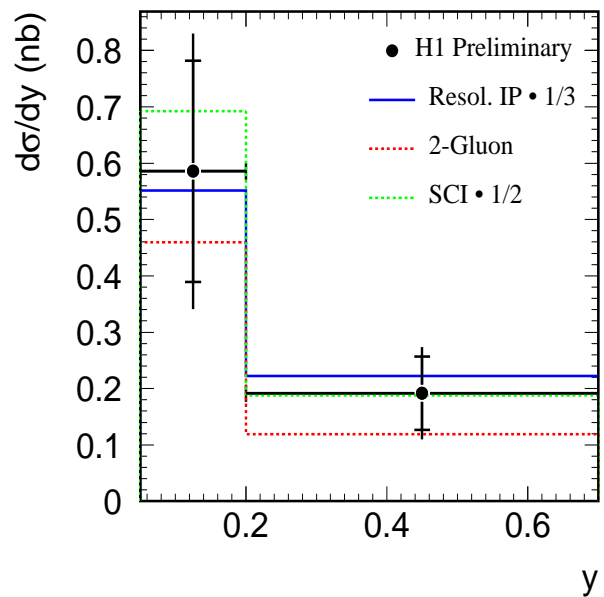
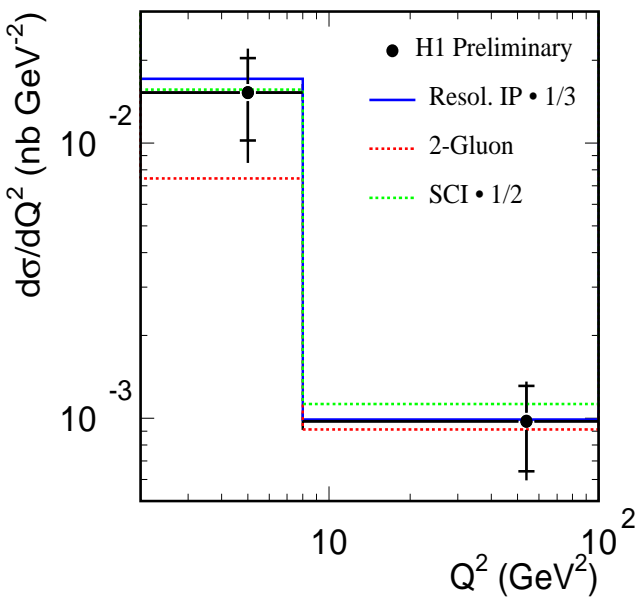
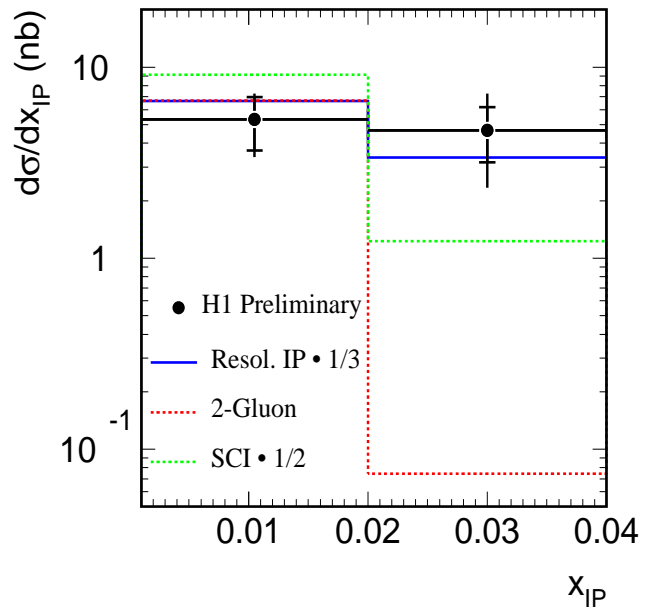
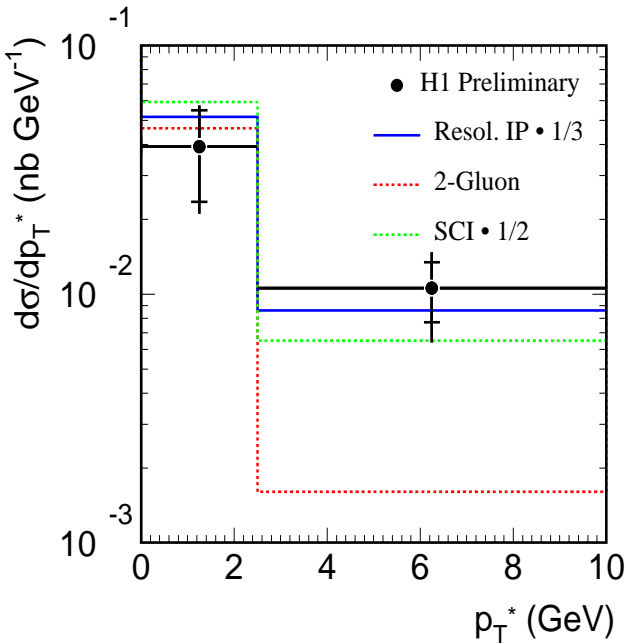
# Differential cross sections– $D^* \rightarrow K4\pi$ (ZEUS)

ZEUS 1996-97 PRELIMINARY



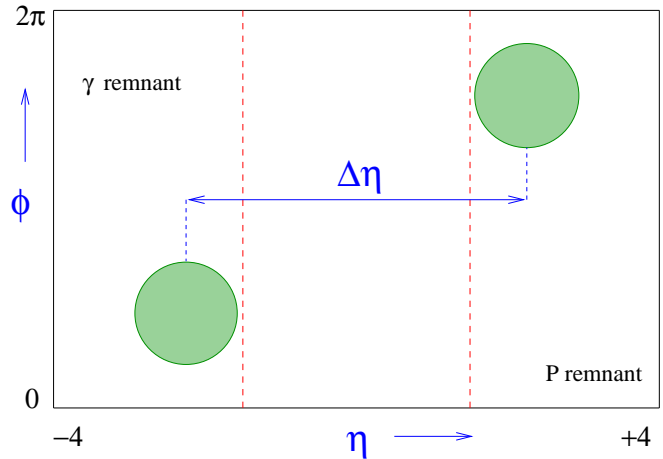
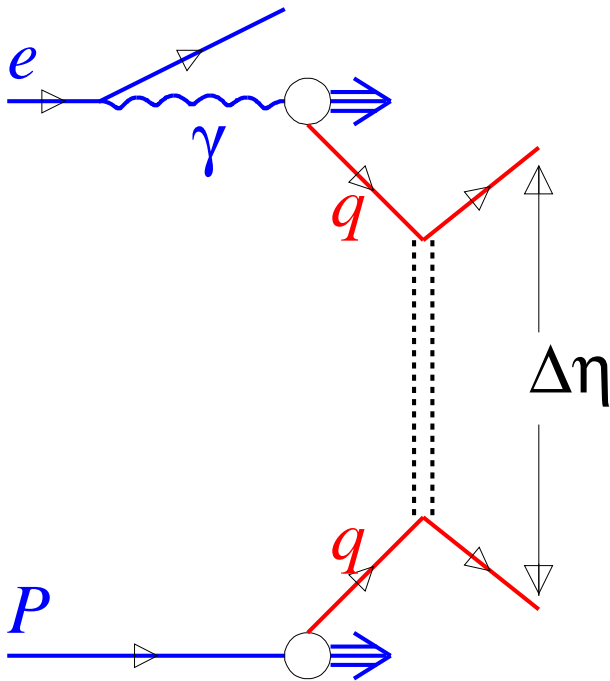
- **Models:**
  - **ACTW (Alvero, Collins, Terron, Whitmore)** – gluon dominated resolved  $\mathcal{IP}$  model
  - **BHM (Buchmüller, Hebecker, McDermott)** – Semi-classical model
  - **RIDI (Ryskin)** – pQCD model with higher order corrections
- **Agreement in normalization  $\implies \mathcal{IP}$  is gluon dominated object**
- **Similar conclusions are for differential cross-sections for  $D^* \rightarrow K\pi\pi$  ZEUS measurement**

# Differential cross sections: $D^* \rightarrow K\pi\pi$ (H1)



- Shape of distributions agree well with resolved  $IP$  model.
- 2-gluon model ( $q\bar{q}$ ) fails in high  $p_T$ , high  $x_{IP}$  ( $M_X$ ) range  
 → need  $q\bar{q}g$  states !
- Resolved  $IP$  and SCI models fail in normalization (factor 2-3 !)
- Parton densities from  $F_2^{D(3)}$  do not describe open charm  
 ⇒ in contrast to other H1 measurements !
- Disagreement between H1 and ZEUS results !
- large uncertainties of  $g$  densities in  $IP$  ?  
 breaking of factorization ?

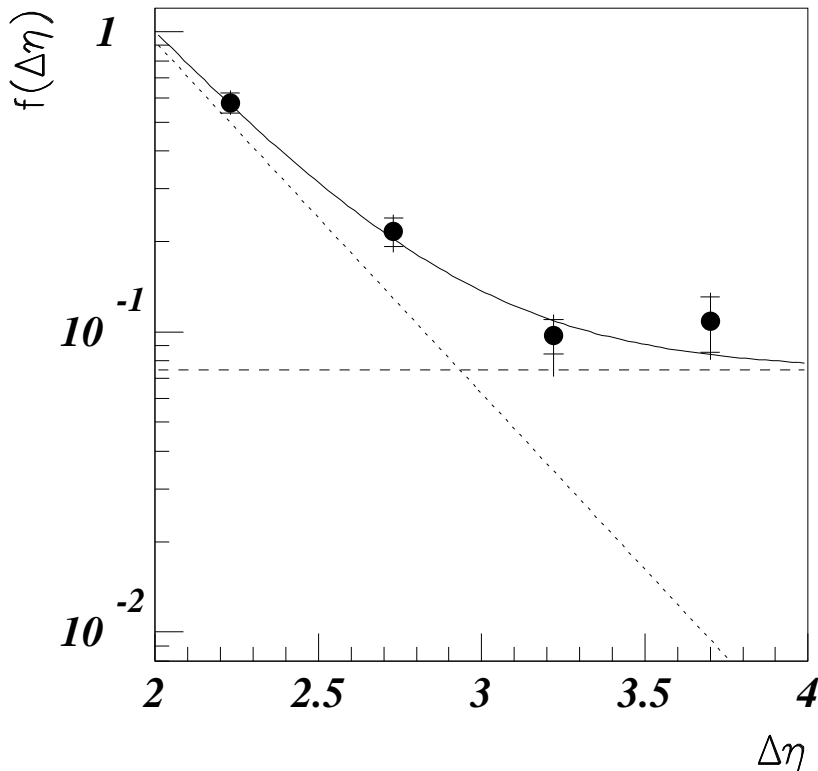
# Rapidity gap between jets in photoproduction



- Phase space is restricted to the region where QCD is applicable (square of the four momentum transfer  $|t|$  is large)
- Elastic parton-parton scattering is calculated with LLA of BFKL (Mueller & Tang)

$$\frac{d\hat{\sigma}}{dt} = (\alpha_s C_F)^4 \frac{2\pi^3}{t^2} \frac{e^{2w_0 Y}}{(7\alpha_s N_c \zeta(3) Y)^3}, \quad w_0 = N_c 4 \ln 2 \frac{\alpha_s}{\pi}$$

- ‘Gap fraction’ –  $f(\Delta\eta)$  – proportion of events containing high  $P_t$  jets for which there is a gap in rapidity between the jets as a function of the jet-jet separation  $\Delta\eta$ .
- For colour non-singlet exchange: exponential fall-off with increasing  $\Delta\eta$   
 $\Rightarrow$  At sufficiently large  $\Delta\eta$ , a colour singlet exchange will dominate.



(ZEUS, Phys.Lett. B369 (1996) 55)

$$Q^2 < 4 \text{ GeV}^2$$

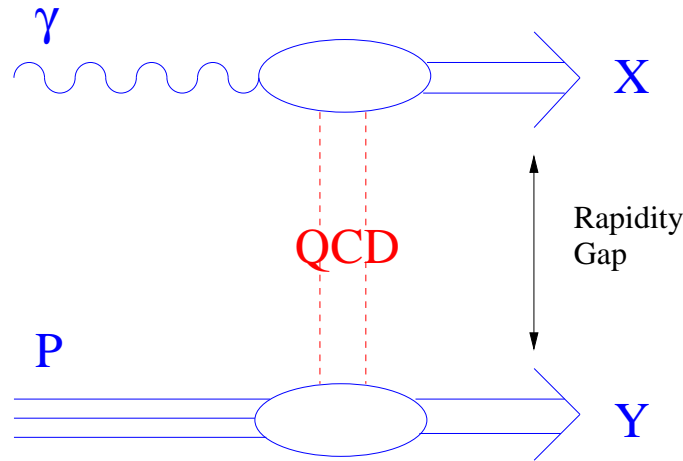
$$135 < W < 280 \text{ GeV}$$

$$E_T^{jet} > 5 \text{ GeV}$$

$$\eta^{jet} < 2.5$$

- Di-jet photoproduction events contain an excess of events with rapidity gap between two jets over the expectations of colour exchange processes at the level of  $f(\Delta\eta) = 0.11 \pm 0.02_{-0.02}^{+0.01}$ .
- In  $p\bar{p}$  collisions at Tevatron  $f(\Delta\eta) \simeq 0.01$   
 $\Rightarrow$  difference in rapidity gap survival probability at  $\gamma p$  and  $p\bar{p}$ .
- Disadvantage of the “rapidity gap between jet” method:  
the accessible gap size is limited by detector acceptance

**A new approach: study inclusive  $\gamma p \rightarrow XY$  double dissociative process at high  $|t|$ .**

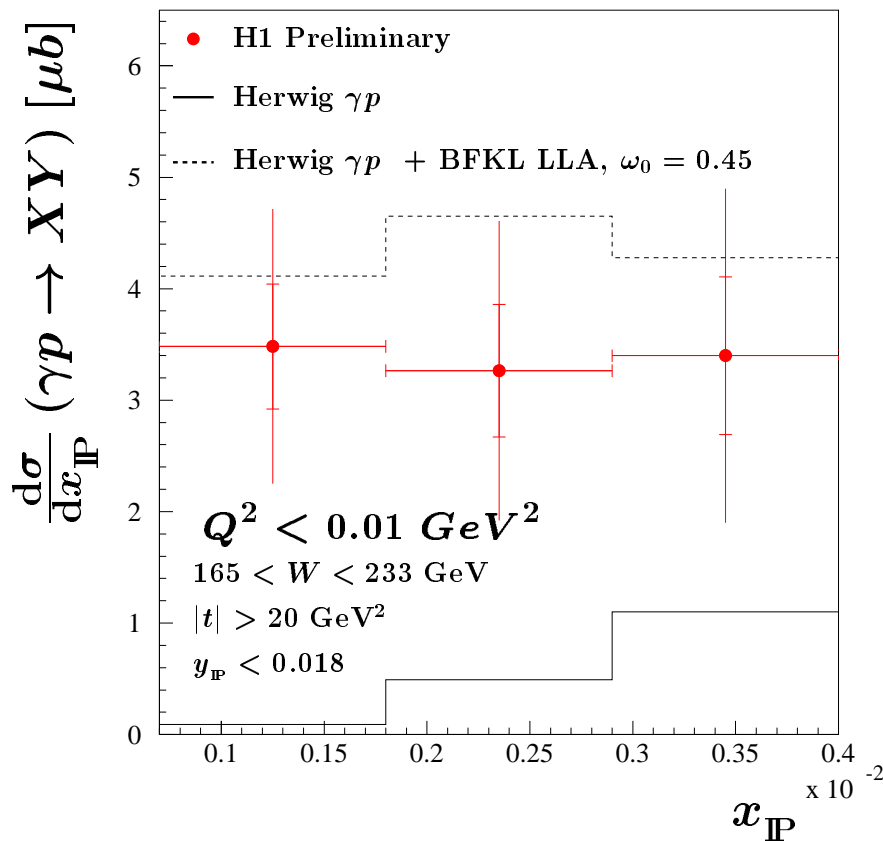


$$W^2 = (\gamma + P)^2$$

$$t = (P - Y)^2$$

$$x_{\mathbb{P}} = \frac{\gamma \cdot (P - Y)}{\gamma \cdot P} \simeq \frac{M_X^2 - t}{W^2}$$

$$y_{\mathbb{P}} = \frac{P \cdot (\gamma - X)}{\gamma \cdot P} \simeq \frac{M_Y^2 - t}{W^2}$$



- **Good agreement between data and Monte-Carlo ( $\gamma p$ + BFKL LLA) in shape and normalization for value of parameter  $\omega_0 = 0.45$ .**

# Summary

The different hadronic final state observables have been studied in diffractive  $ep$  interactions at HERA.

- Measurements of event shape evolution with  $M_X$ , the energy flow, charged particle multiplicities are in general consistently described by resolved  $\mathbb{P}$  model with gluon dominated parton densities evolving with DGLAP.  
→ Same model gives consistent description of hadronic final state and inclusive  $F_2^D(3)$  measurements.
- Several 2-gluon models exist, free parameters can be tuned to describe H1 and ZEUS data. → need  $q\bar{q} + q\bar{q}g$  states !
- The ‘rapidity gap survival probability’ for resolved  $\gamma p$  interactions at HERA is larger than for  $p\bar{p}$  interactions at Tevatron.
- For production of  $D^*$ , the shapes of distributions are well reproduced by models, but  
→ H1 sees discrepancy to results of other hadronic final states and to ZEUS results:  
breaking of factorization ? → need understanding.  
Luminosity upgrade at HERA will allow precise measurement of open charm in diffractive DIS.
- An excess of events with a large rapidity gap between jets is observed over the expectations of colour exchange processes.
- The double dissociation photoproduction cross-section is measured at large  $|t|$  and is in agreement with the model based on the exchange of a strongly interacting colour singlet object.