



# Search for collective effects in small system obtained in ep collisions at HERA

Chuan Sun (孙川) for H1 Collaboration  
Stony Brook University/Shandong University

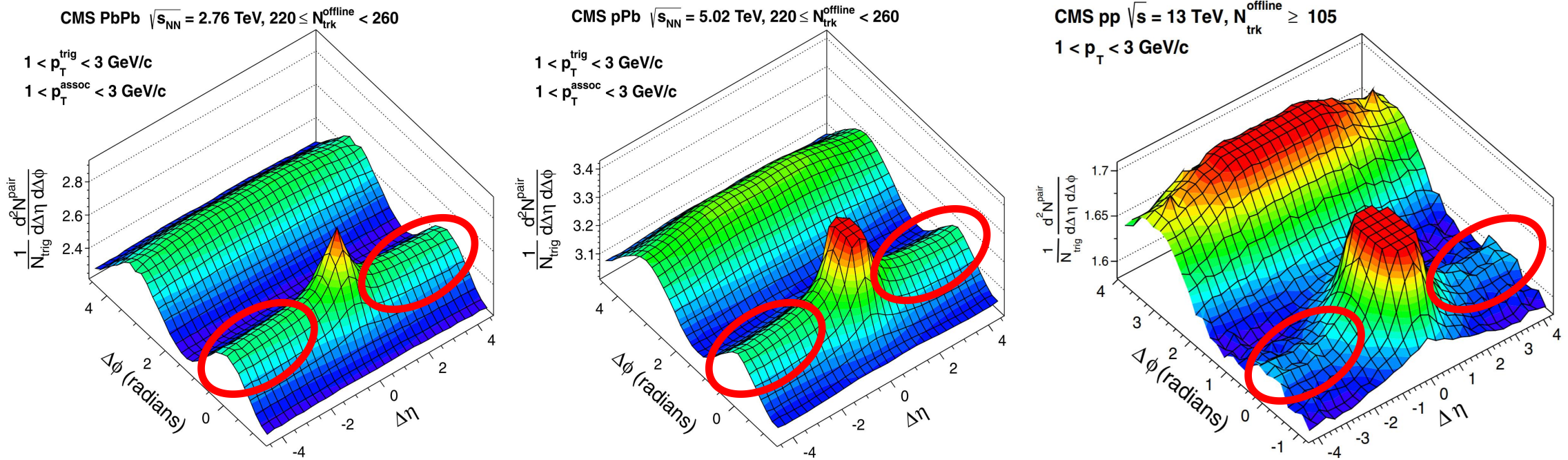


Stony Brook  
University



# Collectivity in small system

PLB 724 213–240 (2013) ; PRL 116, 172302 (2016)



Lots of evidence of collectivity in high multiplicity pp and pPb collisions, similar to heavy-ion collisions attributed to the perfect liquid nature of QGP

**What about even smaller system?**

# Collectivity in small system

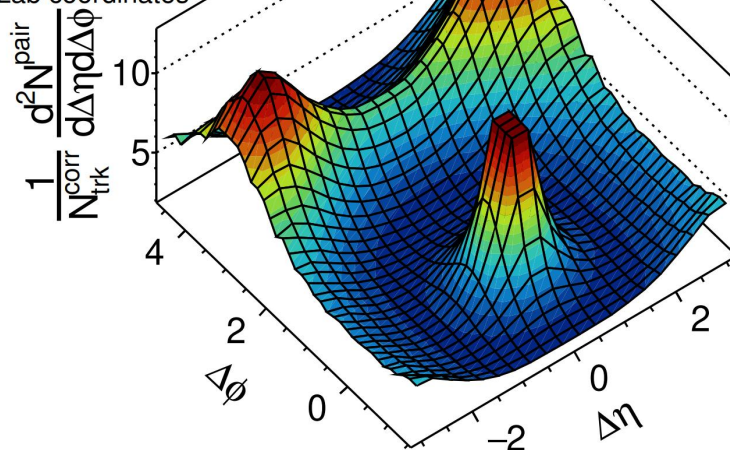
PRL 123, 212002 (2019)

ALEPH  $e^+e^- \rightarrow \text{hadrons}$ ,  $\sqrt{s} = 91\text{GeV}$

$N_{\text{trk}} \geq 30$ ,  $|\cos(\theta_{\text{lab}})| < 0.94$

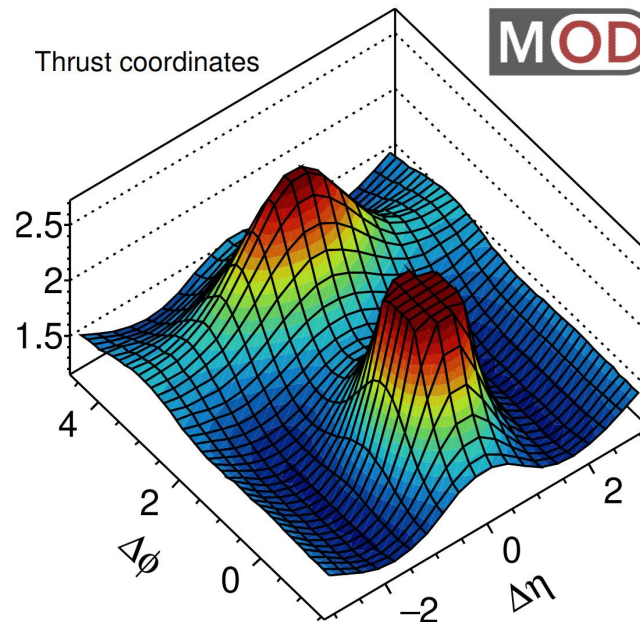
$p_{\text{T}}^{\text{lab}} > 0.2\text{ GeV}$

Lab coordinates



Thrust coordinates

MOD



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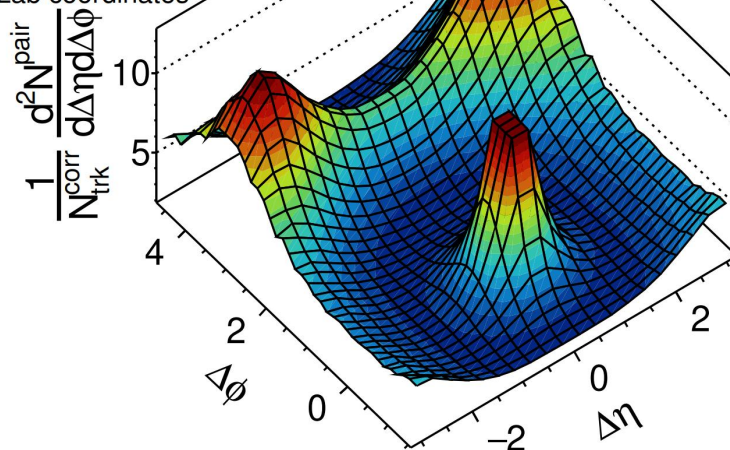
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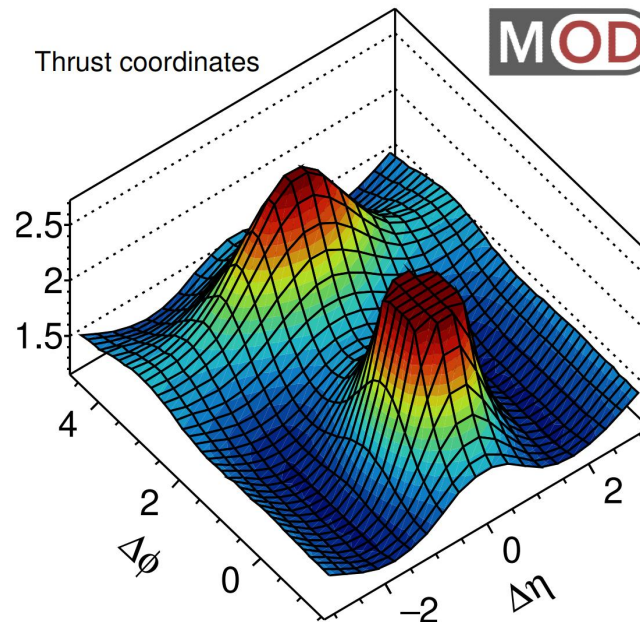
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Lab coordinates



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Lots of evidence of collectivity in high multiplicity pp and pPb collisions, similar to heavy-ion collisions attributed to the perfect liquid nature of QGP

**What about even smaller system? in  $e^+e^-$  or ep collisions**

In deep-inelastic scattering(DIS) and photoproduction events:

Two-particle correlation(Ridge,  $V_{n\Delta}$ ), Four-particle correlation( $C_2\{4\}$ )

# H1 at HERA

## HERA Collider

Operated from 1992 to 2007

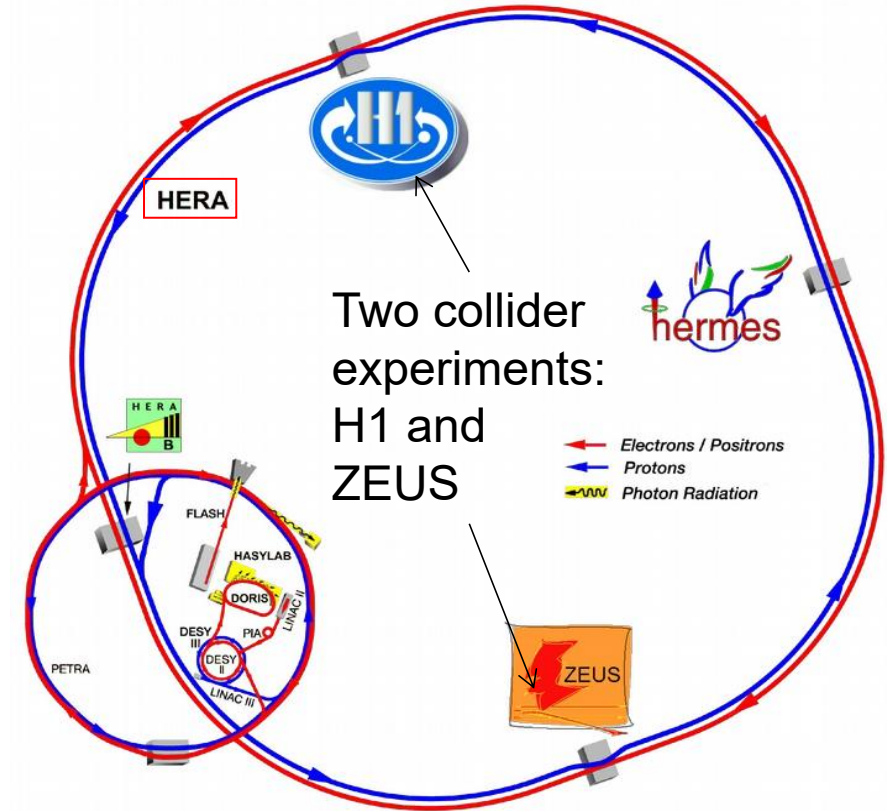
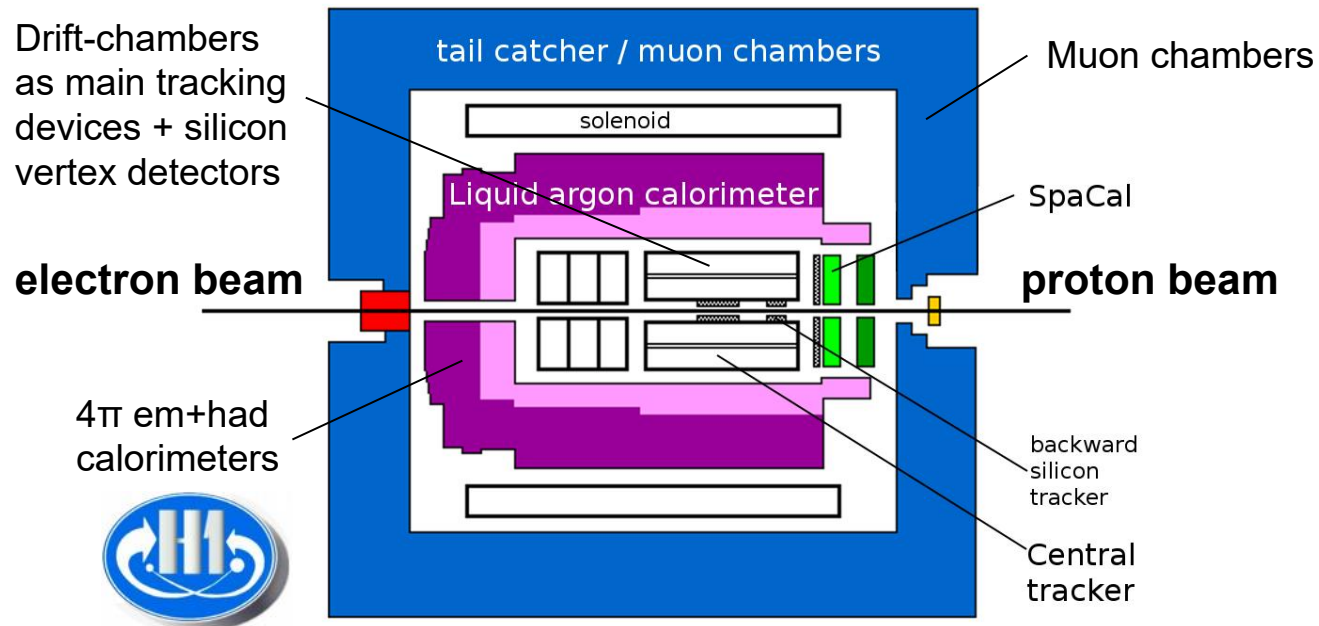
Circumference 6.3 km

Asymmetric detectors

Electrons or positrons colliding with protons

$E_e=27.6$  GeV,  $E_p=460 - 920$  GeV

Centre-of-mass system is boosted to proton-direction



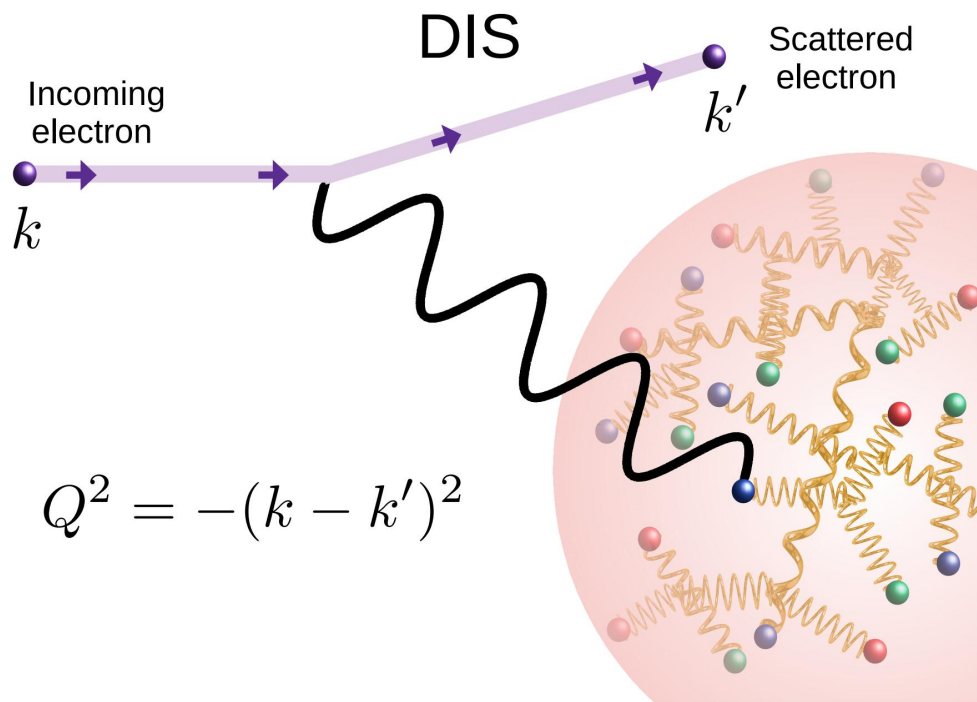
## H1 Detector

Central tracker acceptance  $|\eta| < 1.6$

LAr calorimeter for hadronic final state

SpaCal calorimeter for detecting electrons with  $5 < Q^2 < 100$  GeV<sup>2</sup>

# DIS and photoproduction



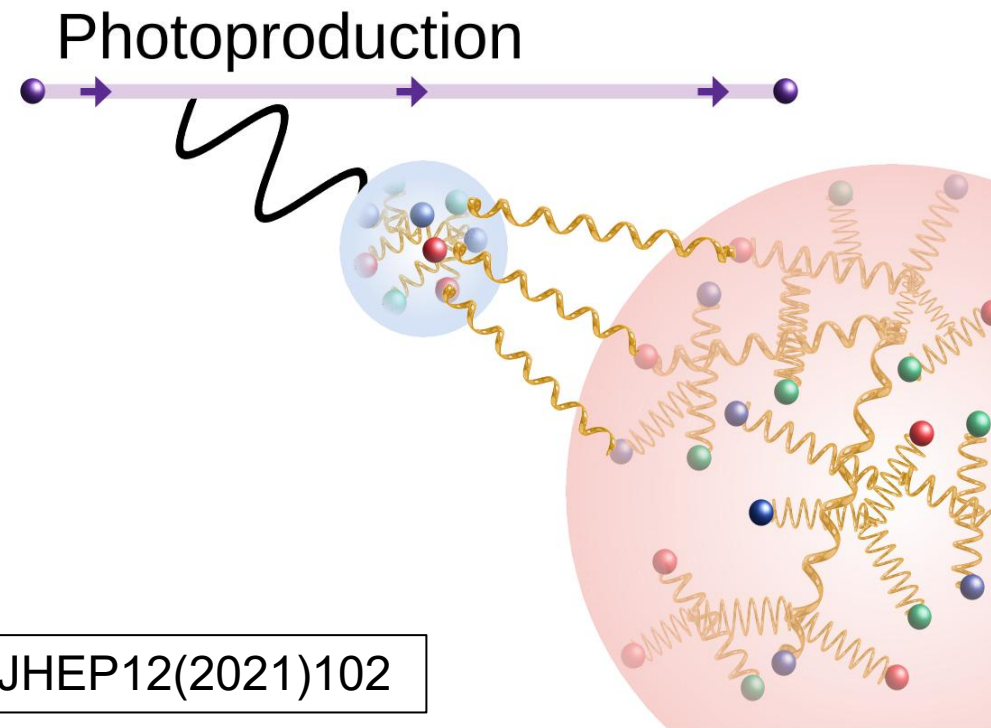
**DIS** defined by large virtualities:

$$Q^2 \gg \Lambda_{QCD}^2$$

Transverse radius ( $R_t$ ) of the probed region are given by:

$$R_t \sim \frac{1}{Q}$$

PRD 95, 114008 (2017)



JHEP12(2021)102

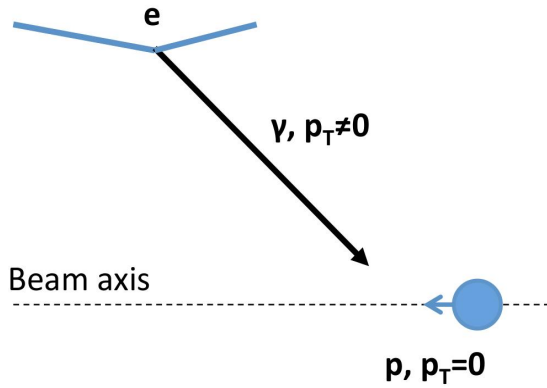
**Photoproduction** defined by small virtualities:

$$Q^2 \ll \Lambda_{QCD}^2$$

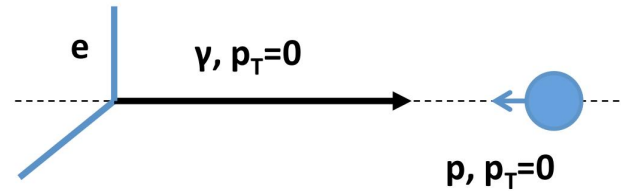
Exchange photon may fluctuate into partons  
Large interaction regions probed  
Scattering may be hadron-like

# Search for collectivity in ep DIS

Lab Frame

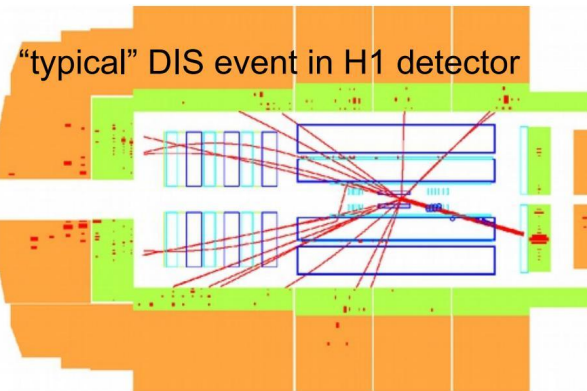


Hadronic CMS frame

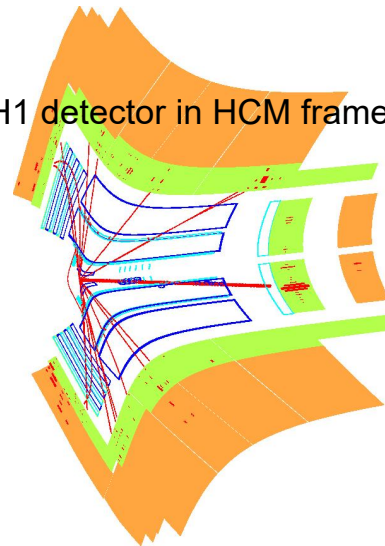


**lab frame:**  
inhomogeneous  $p_T$  space

**HCM frame:**  
homogeneous  $p_T$  space



H1 detector in HCM frame



**Search for collectivity with H1 data in HCM frame**

# Two-particle correlation functions in ep DIS

H1prelim-20-033: [https://www-h1.desy.de/publications/H1preliminary.short\\_list.html](https://www-h1.desy.de/publications/H1preliminary.short_list.html)

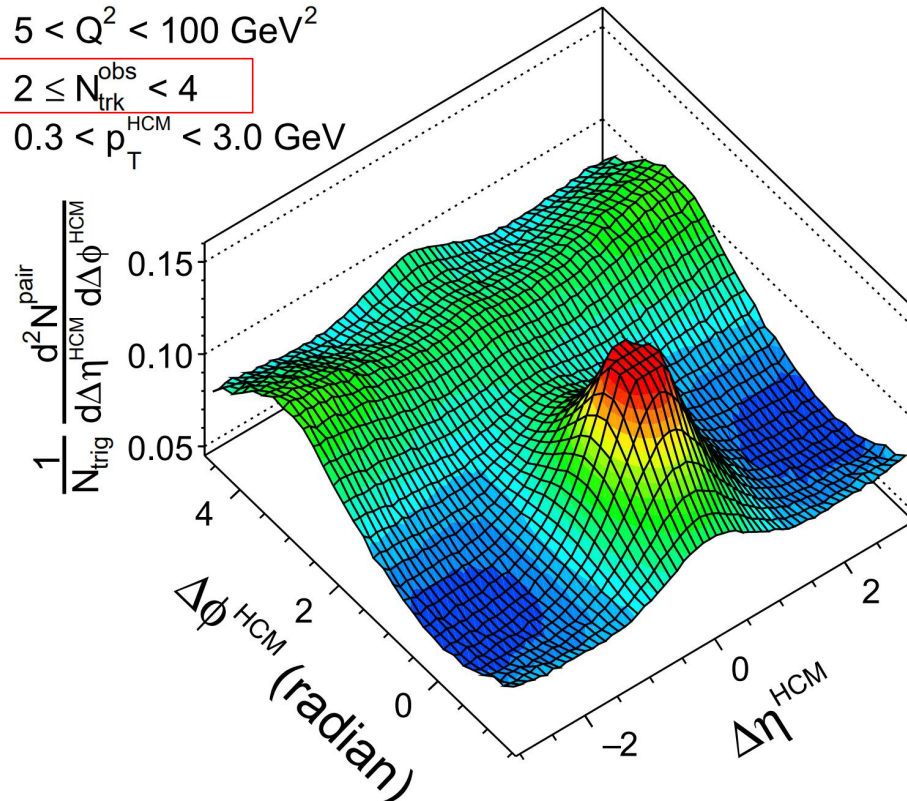
**H1 Preliminary**

ep  $\sqrt{s} = 319$  GeV

$5 < Q^2 < 100$  GeV<sup>2</sup>

$2 \leq N_{\text{trk}}^{\text{obs}} < 4$

$0.3 < p_{\text{T}}^{\text{HCM}} < 3.0$  GeV



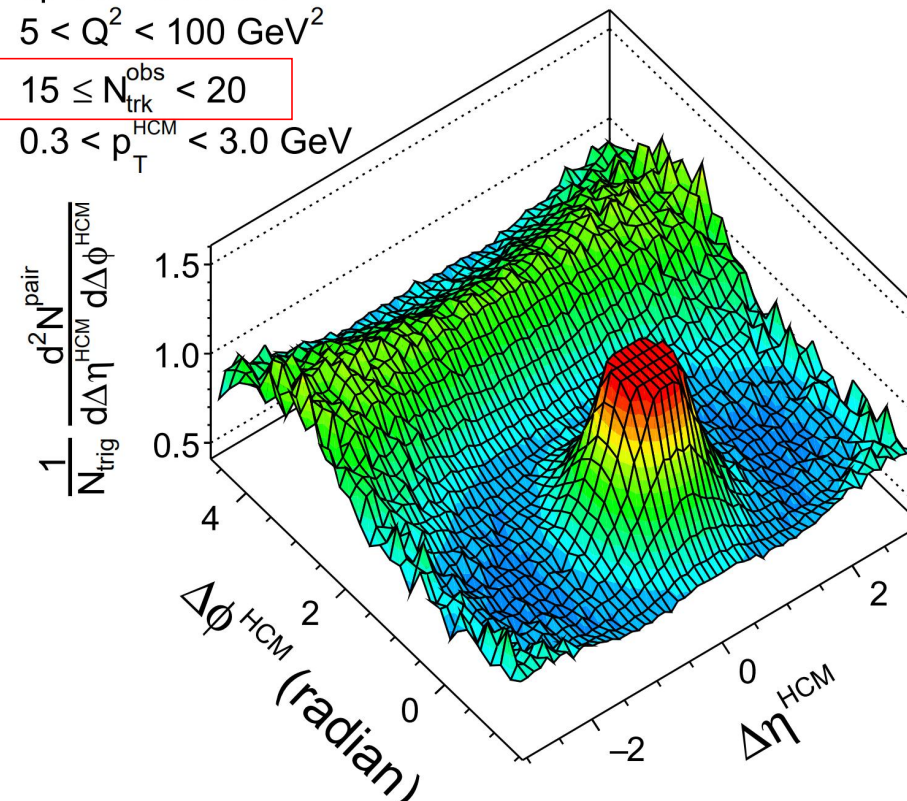
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ep  $\sqrt{s} = 319$  GeV

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$15 \leq N_{\text{trk}}^{\text{obs}} < 20$

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No near-side long-range ridge with H1 DIS data

Extract ridge yield limits through ZYAM and bootstrap procedure

**DIS HCM**



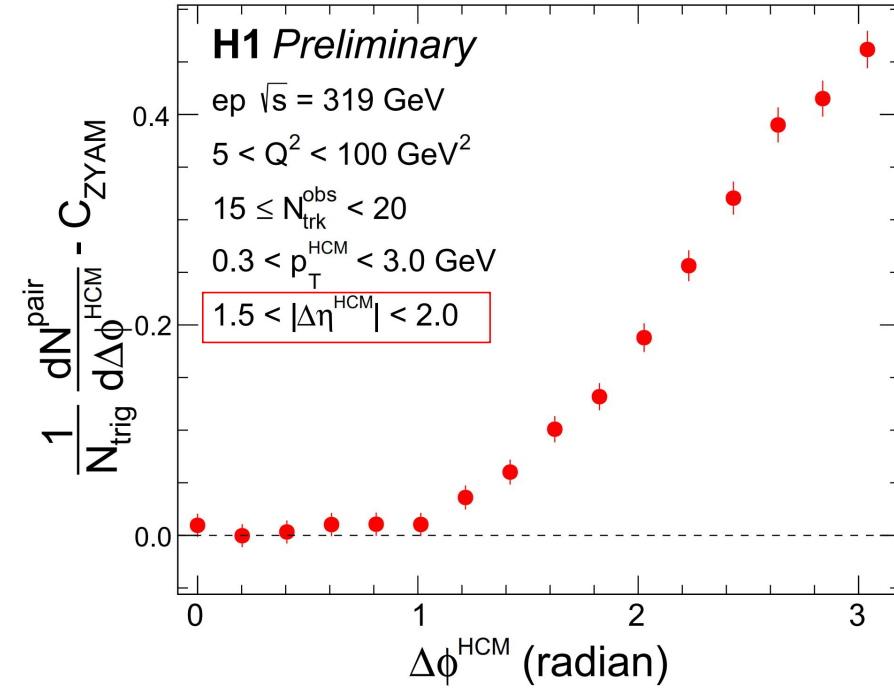
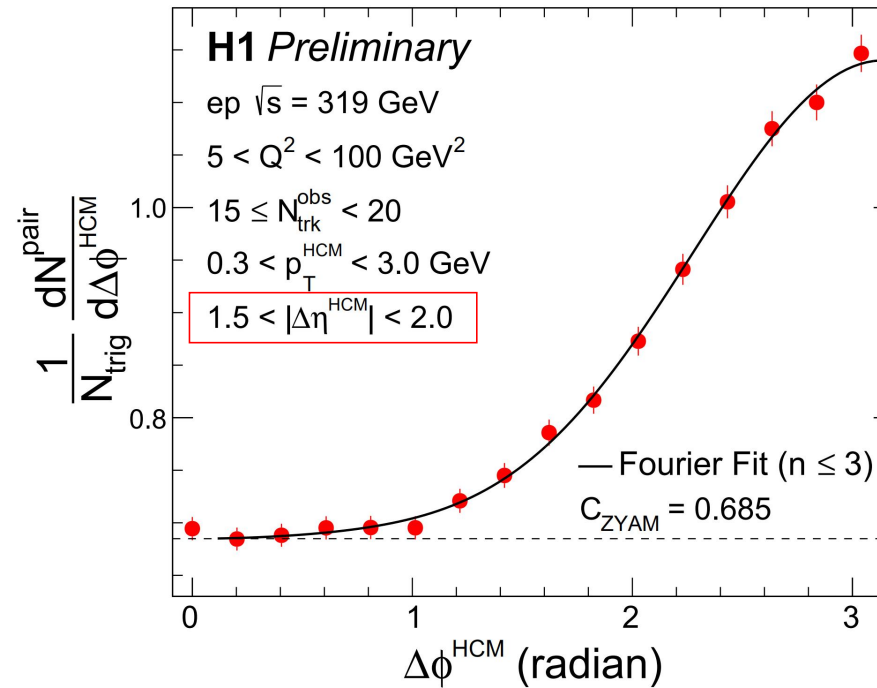
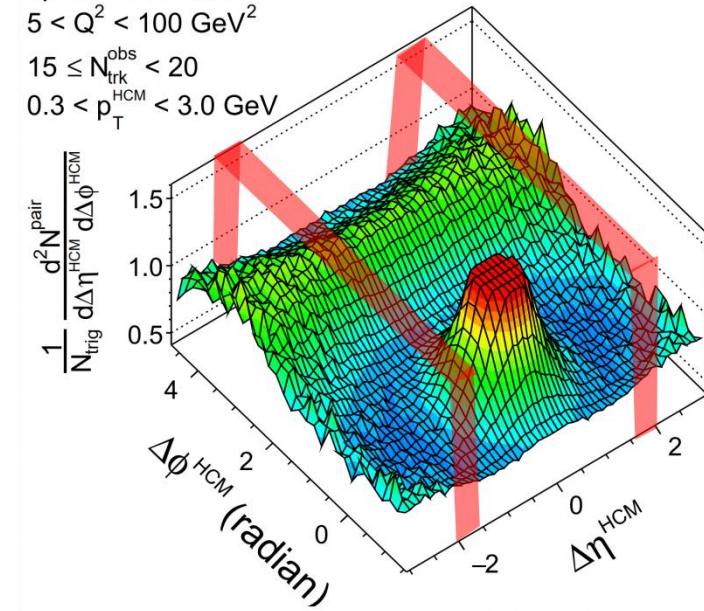
# Ridge yield extraction procedure

PRC 81 014905 (2010)

## Zero-yield-at-minimum(ZYAM)

**H1 Preliminary**

ep  $\sqrt{s} = 319$  GeV  
 $5 < Q^2 < 100$  GeV<sup>2</sup>  
 $15 \leq N_{\text{trk}}^{\text{obs}} < 20$   
 $0.3 < p_{\text{T}}^{\text{HCM}} < 3.0$  GeV



Step1: long-range 1D projection

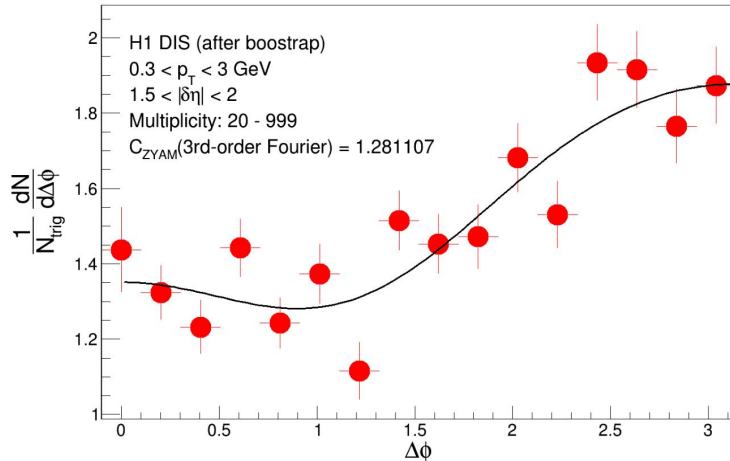
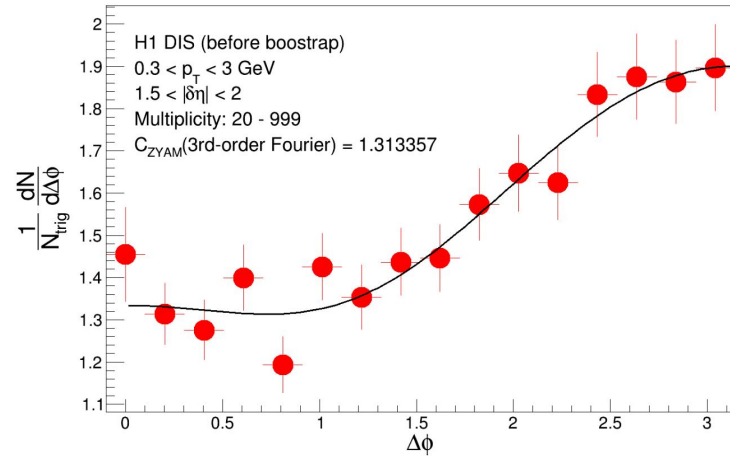
Step2: third-order Fourier fit

Step3: subtraction

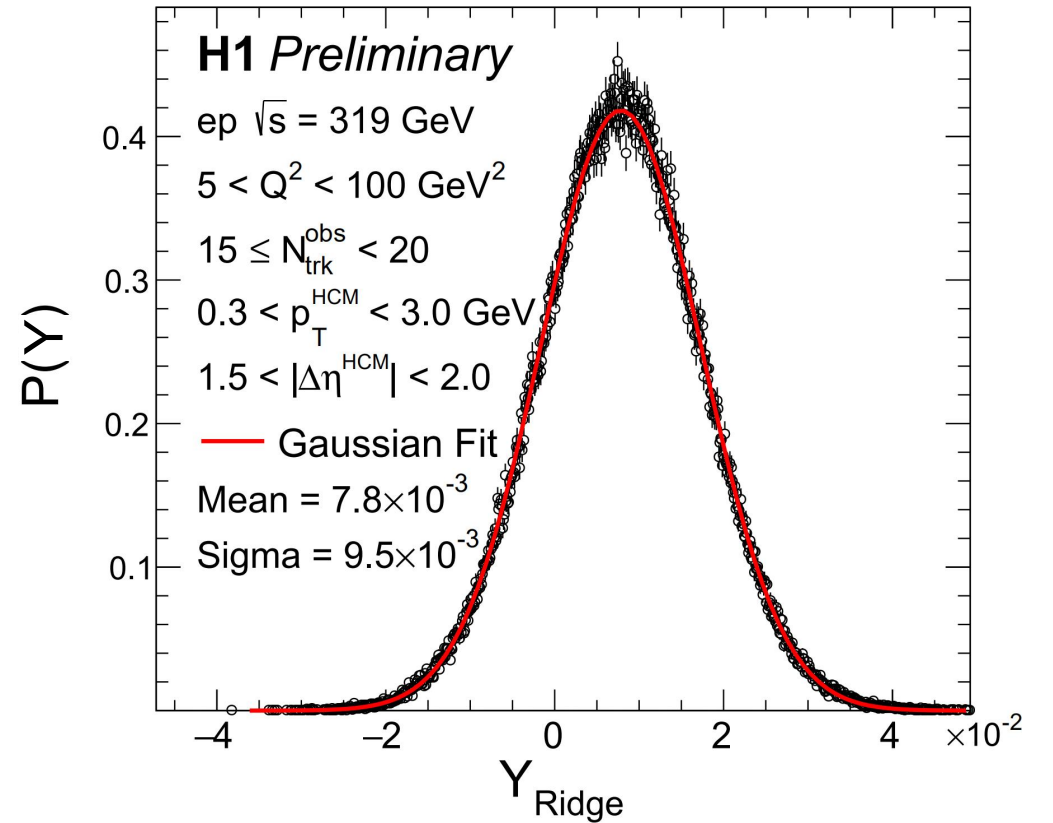
Then integrate from  $\Delta\phi=0$  to where the minimum value of ZYAM occurs as the ridge yield value

# Bootstrap procedure

Each azimuthal differential yield distribution is varied according to their statistical and systematic uncertainties  
One time bootstrap, one new ridge yield value

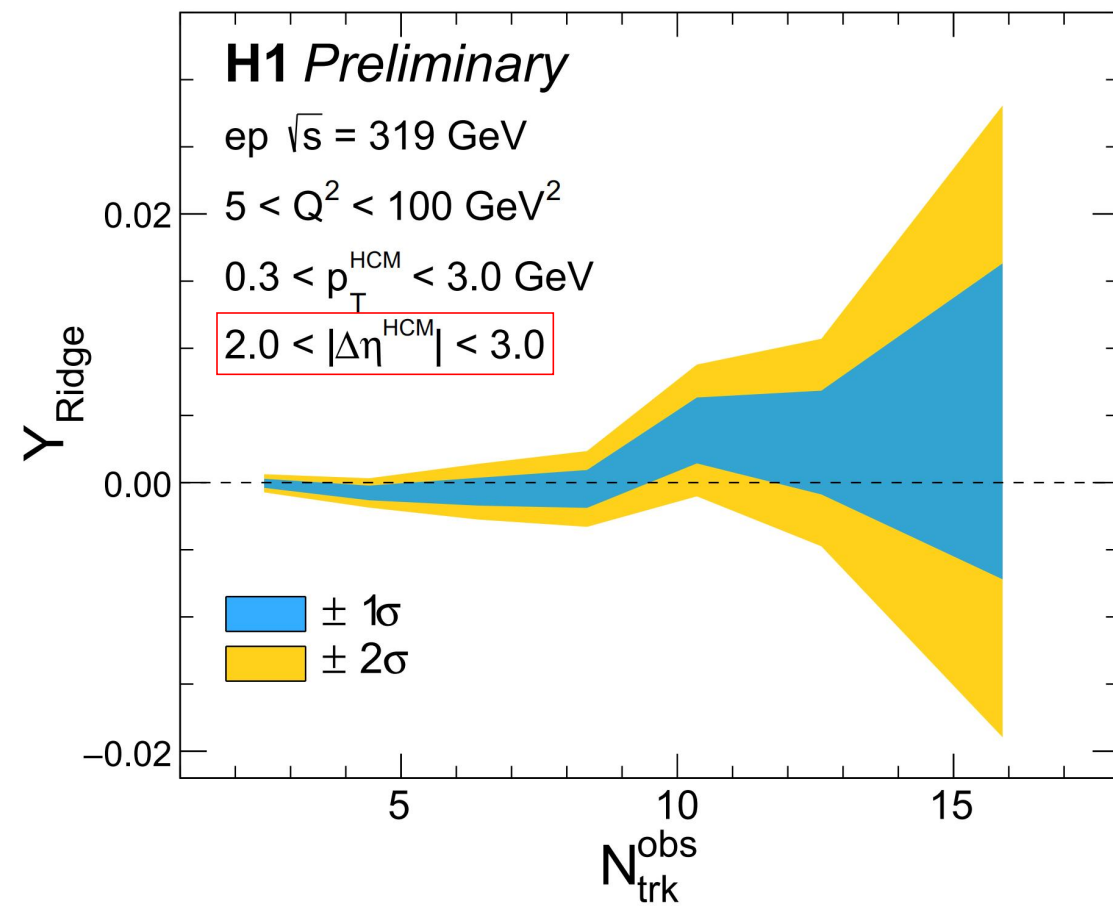
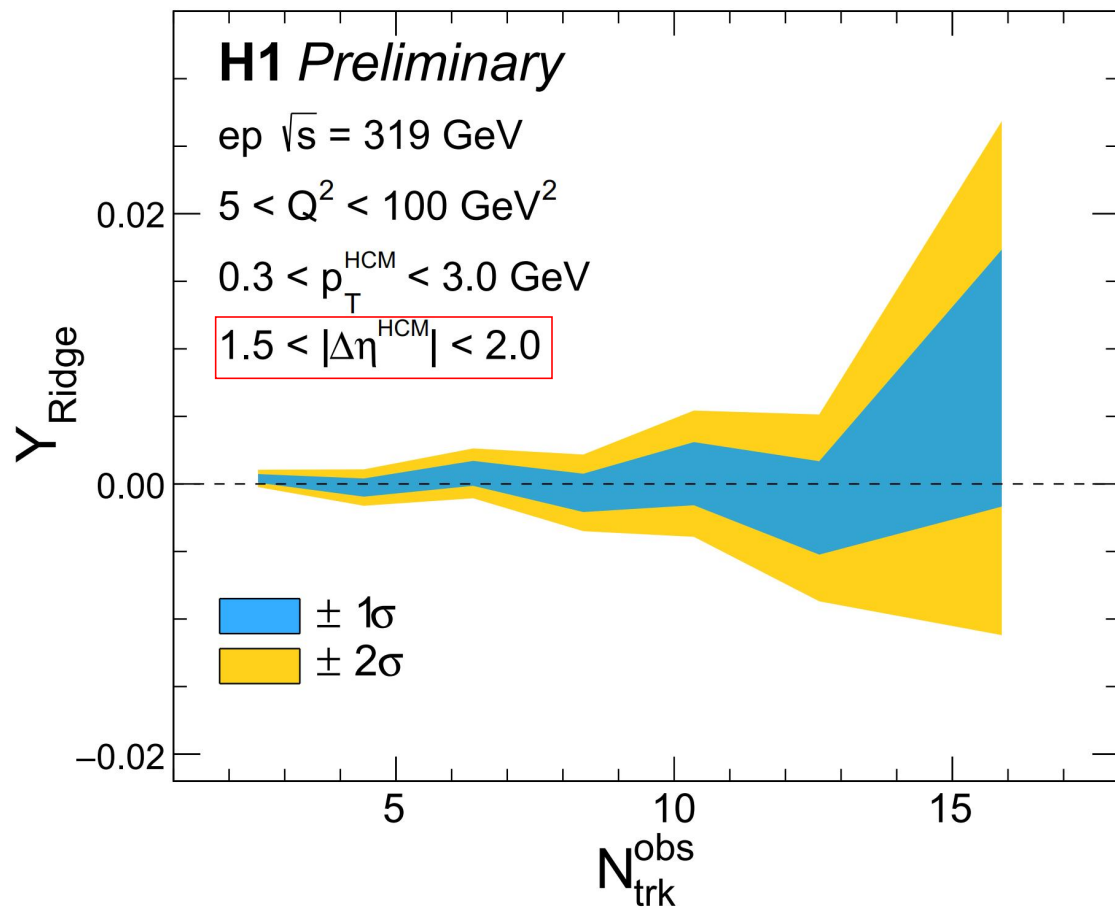


Each yield distribution is sampled  $2.5 \times 10^5$  times



Ridge yield limit extracted from the mean and sigma value of the Gaussian function

# Ridge yield limits in ep DIS



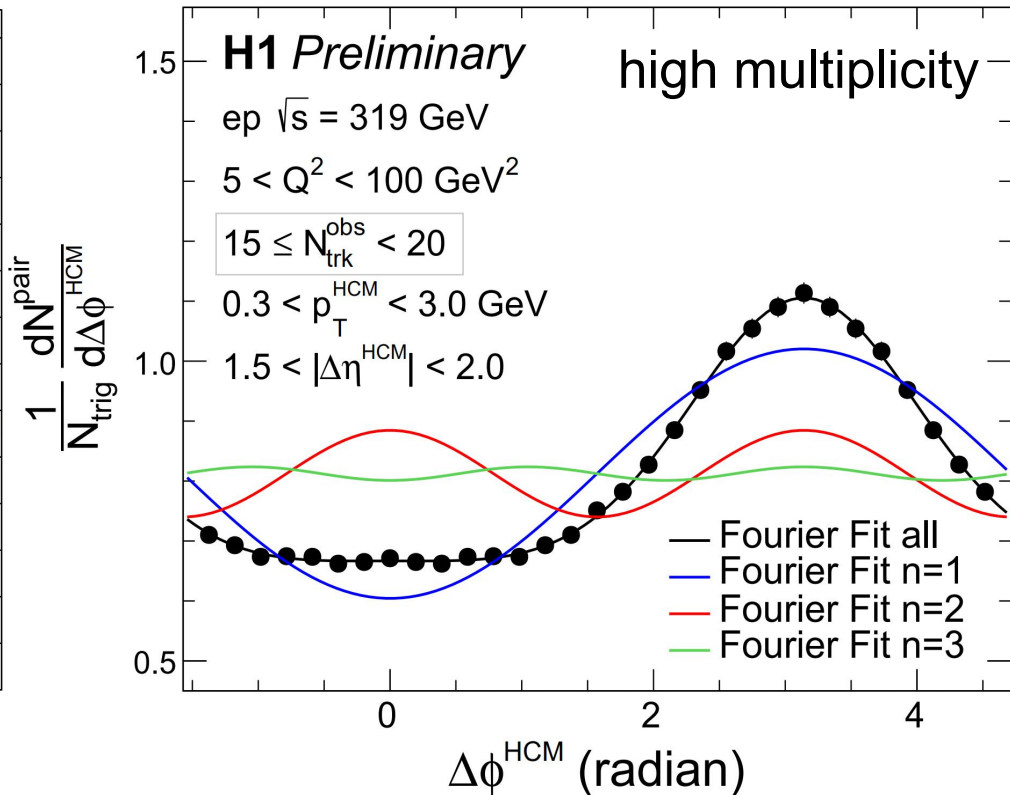
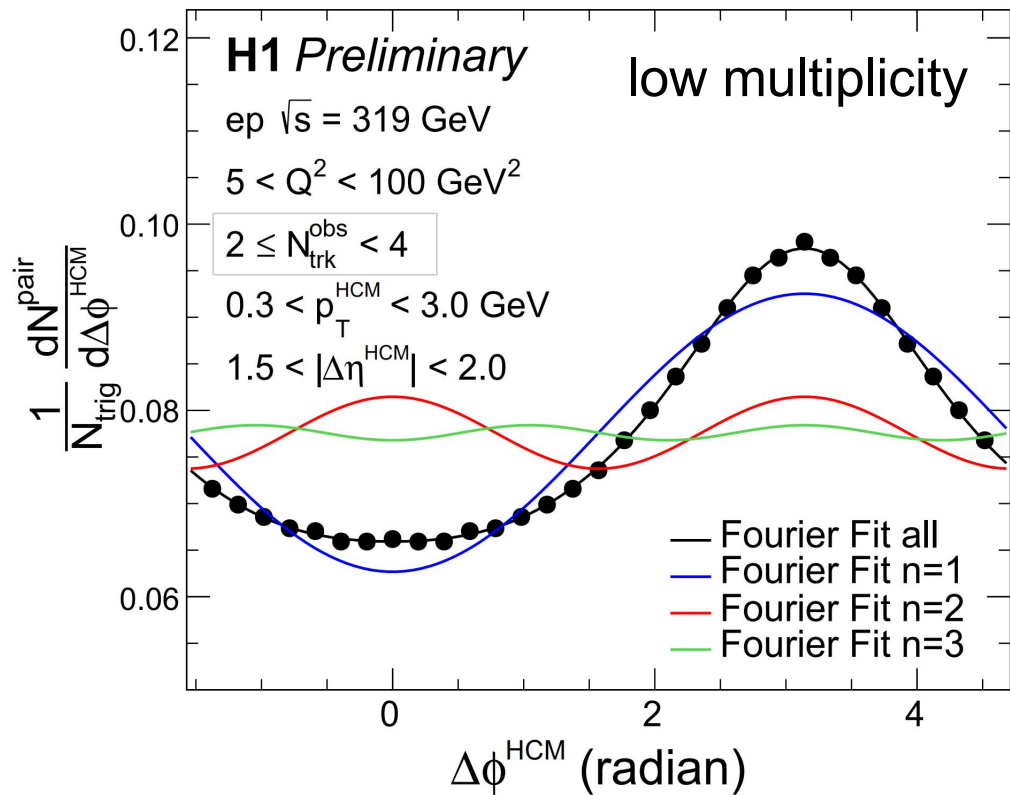
Limits set for ridge yield  
Small room for existence of ridge

**DIS HCM**

# Fourier coefficient $V_{n\Delta}$ extraction procedure

Long-range 1-D projections of 2PC functions onto  $\Delta\phi$  direction

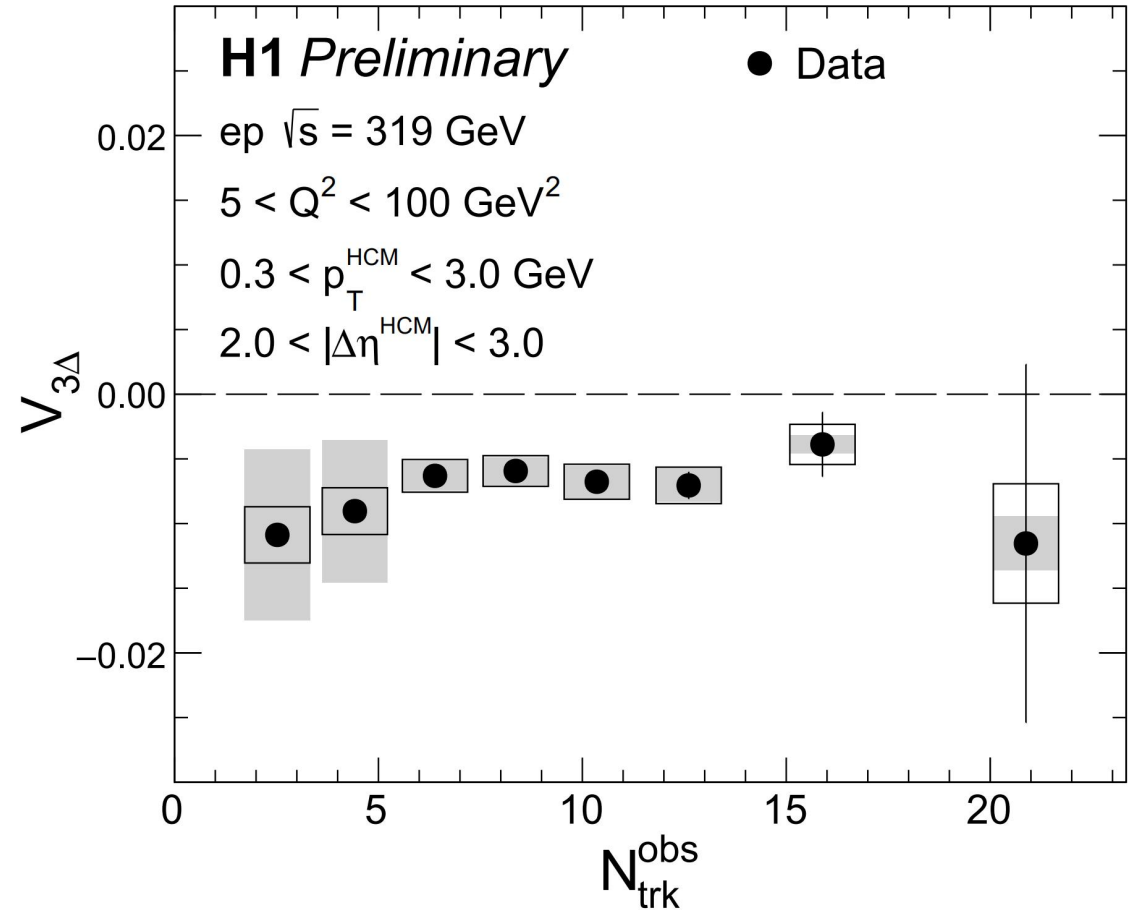
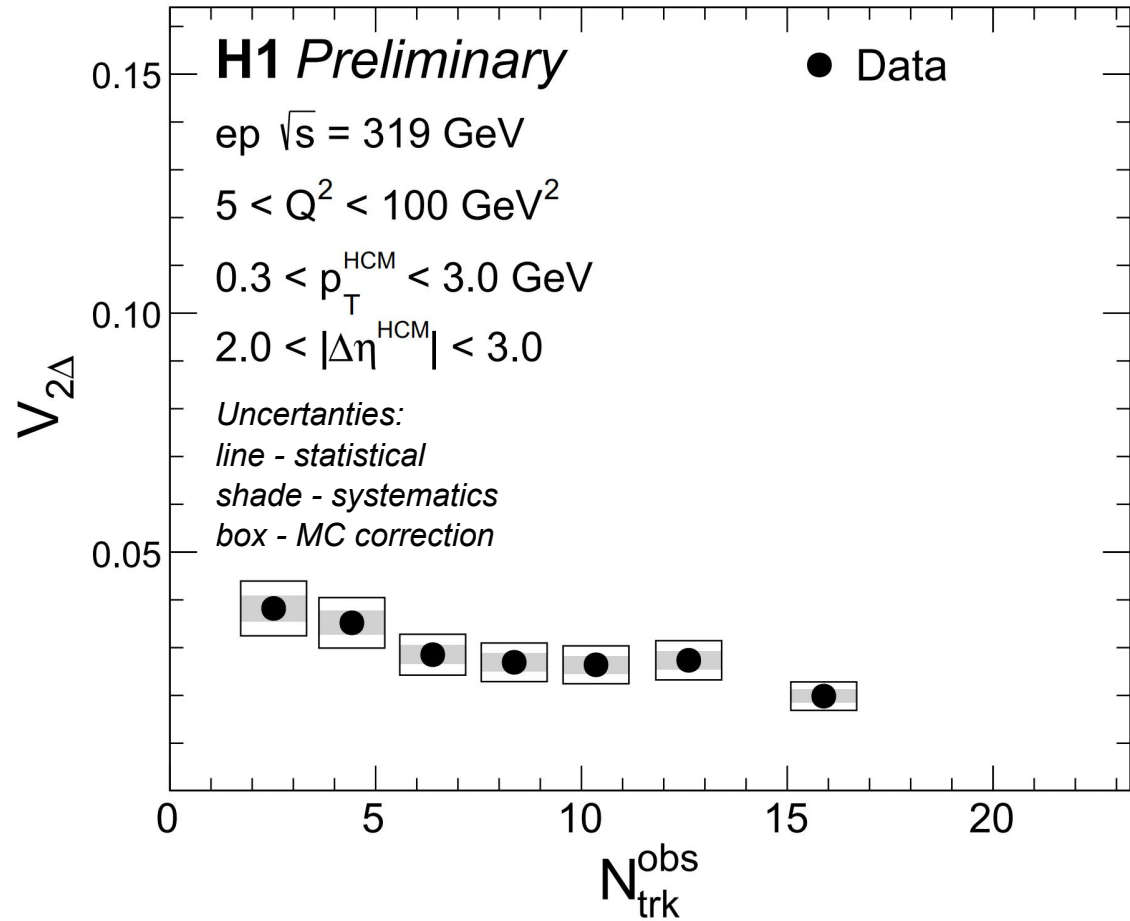
$$\frac{1}{N_{trig}} \frac{dN^{pair}}{d\Delta\phi} = \frac{N_{assoc}}{2\pi} \left( 1 + \sum_n 2V_{n\Delta} \cos(n\Delta\phi) \right)$$



Similar shapes in low and high multiplicity

**DIS HCM**

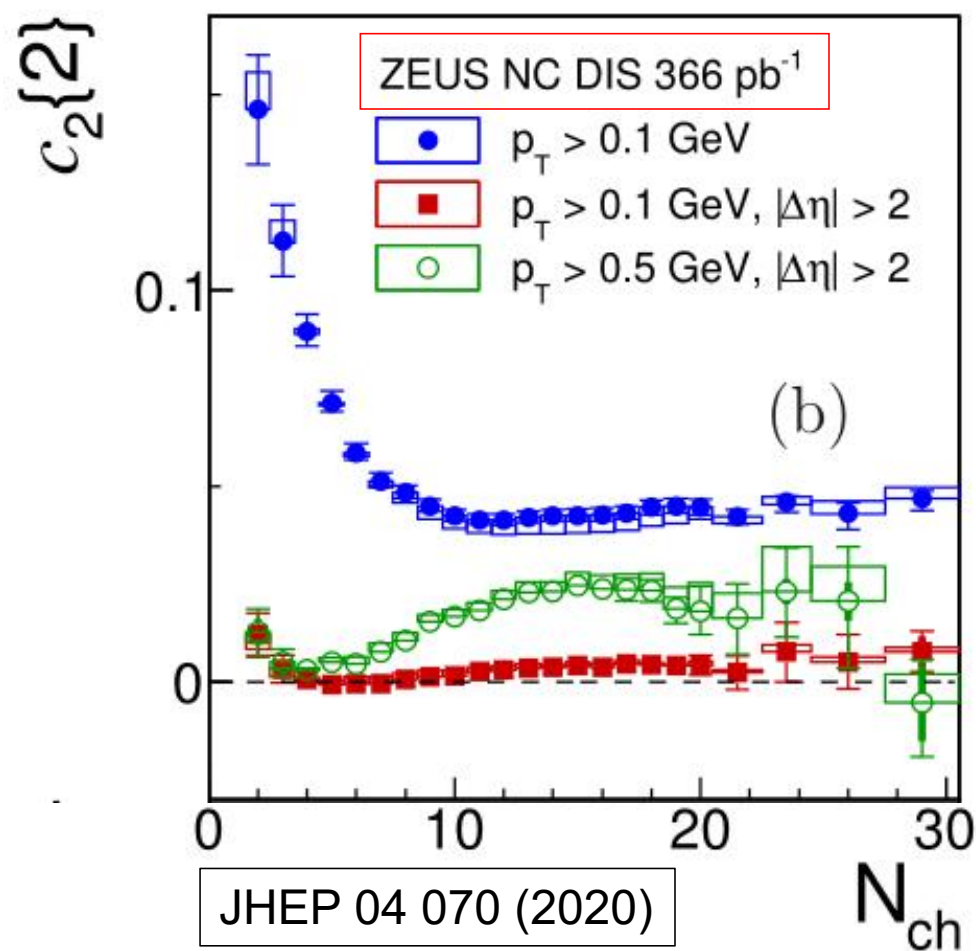
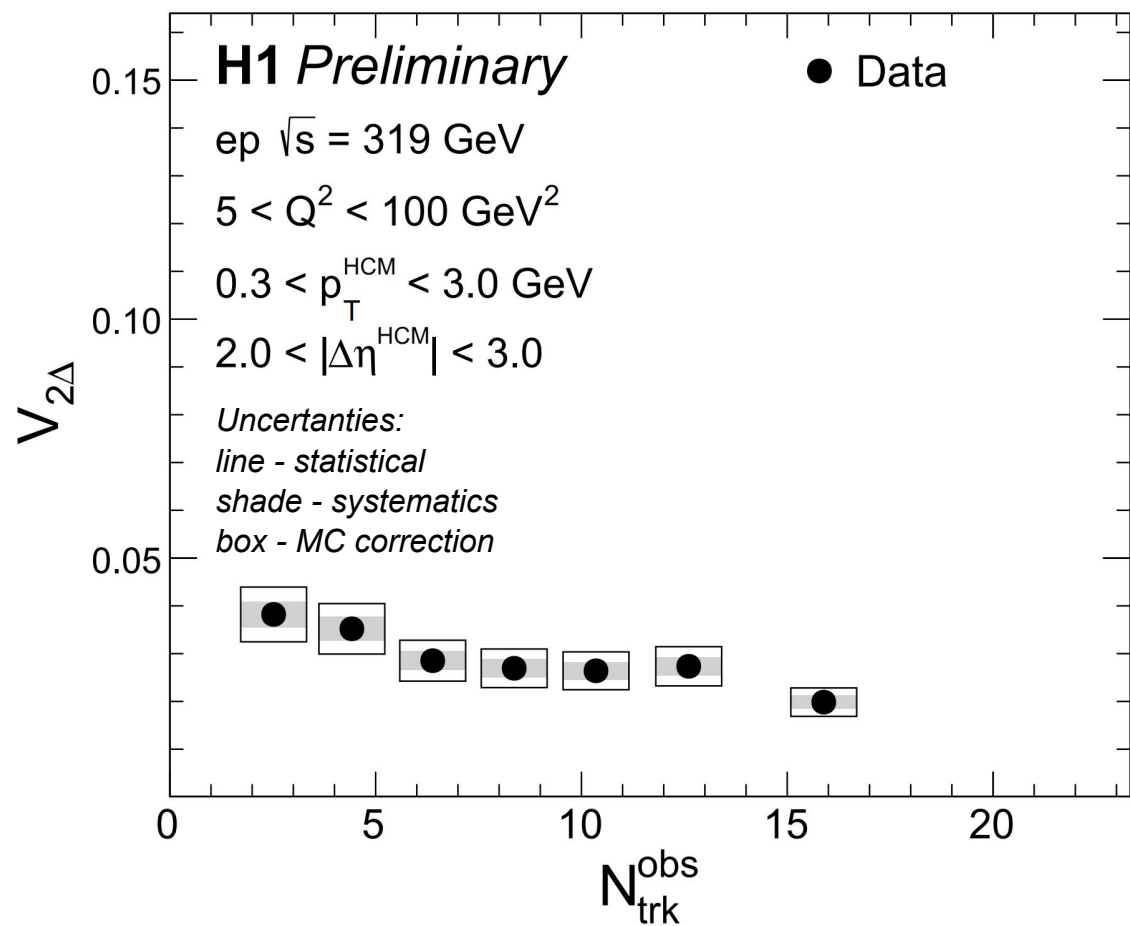
# Fourier coefficient $V_{n\Delta}$ in ep DIS



$V_{2\Delta}$  value drops in high multiplicity

Negative  $V_{3\Delta}$  means it dominated by non-flow correlation

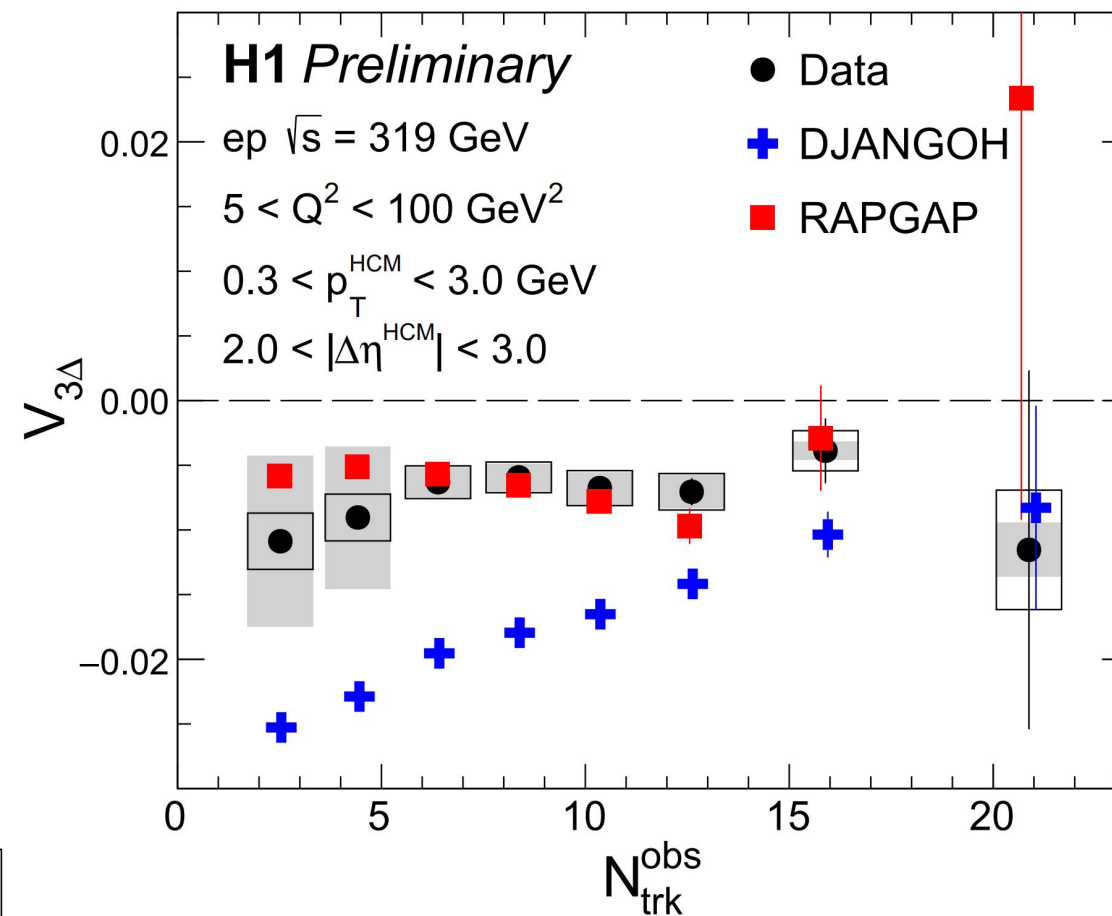
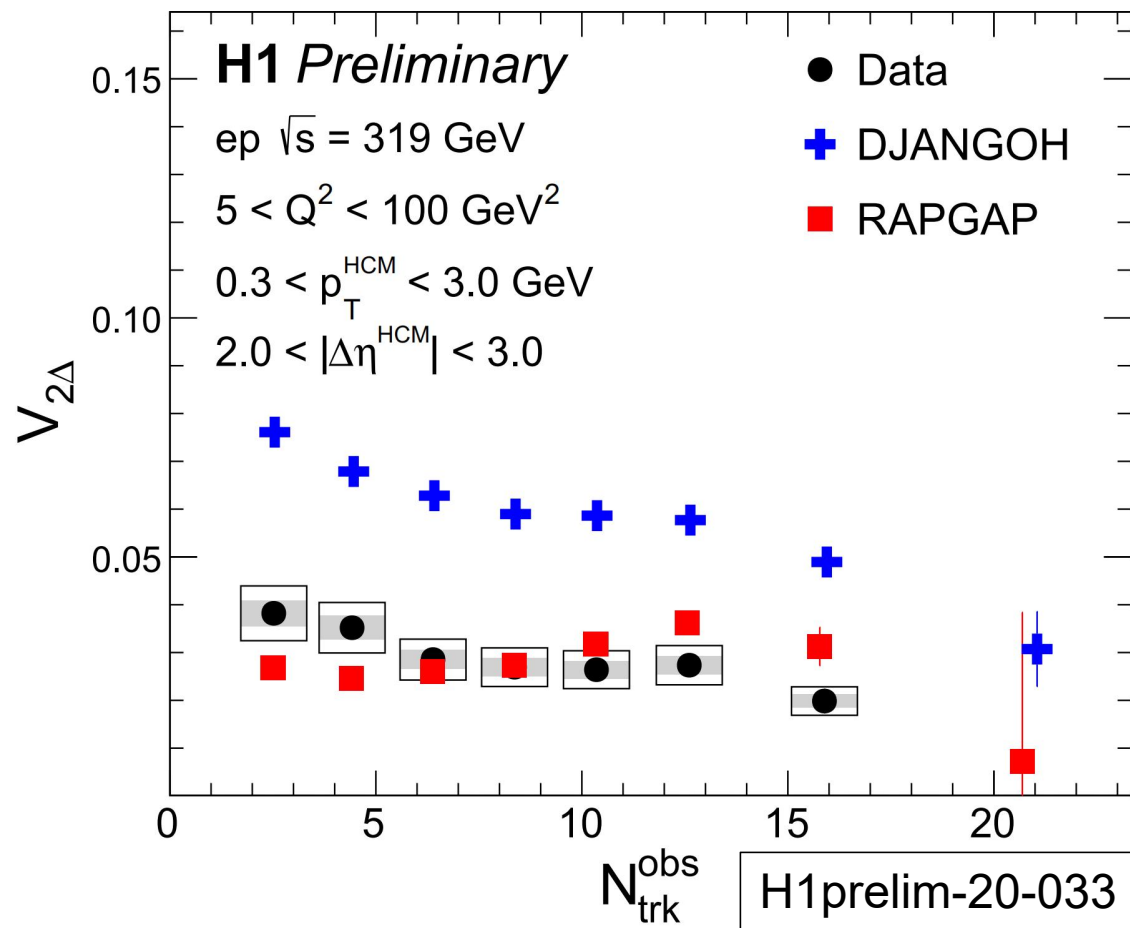
# Fourier coefficient $V_{n\Delta}$ in ep DIS (Compared with ZEUS)



$V_{2\Delta}$  has similar trend as ZEUS result

DIS HCM

# Fourier coefficient $V_{n\Delta}$ in ep DIS

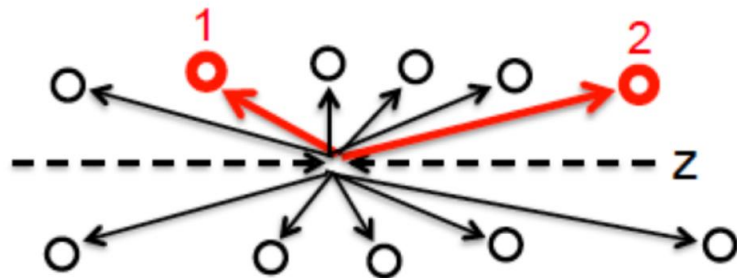


RAPGAP has better description on DIS data than DJANGO  
 Data can be described by MC(RAPGAP) w/o collectivity

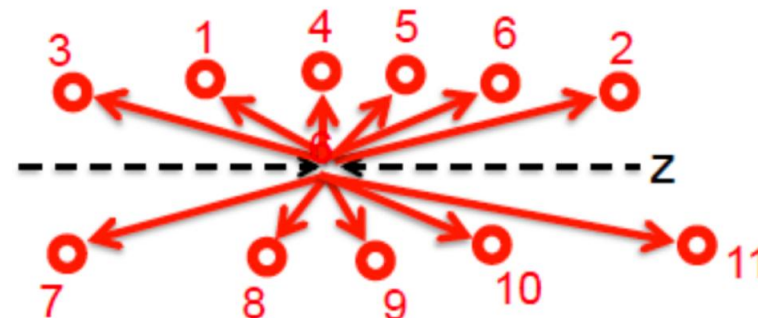
**DIS HCM**

# Multi-particle correlation

Two-particle correlation



Multi-particle correlation



$$\langle 2 \rangle = \langle e^{in(\phi_1 - \phi_2)} \rangle = \frac{Q_n^2 - M}{M(M-1)}$$

$$Q_n \equiv \sum_{i=1}^M e^{in\phi_i}$$

$$\langle 4 \rangle = \langle e^{in(\phi_1 + \phi_2 - \phi_3 - \phi_4)} \rangle = \frac{Q_n^4 - 2\text{Re}[Q_{2n} Q_n^{*2}] - 4(M-2)Q_n^2 + 2M(M-3) + Q_{2n}^2}{M(M-1)(M-2)(M-3)}$$

$$c_n\{4\} = \langle\langle 4 \rangle\rangle - 2\langle\langle 2 \rangle\rangle^2$$

$$v_n\{4\} = \sqrt[4]{-c_n\{4\}}$$

Few particle correlation is suppressed

Collective behavior leads to negative  $C_n\{4\}$

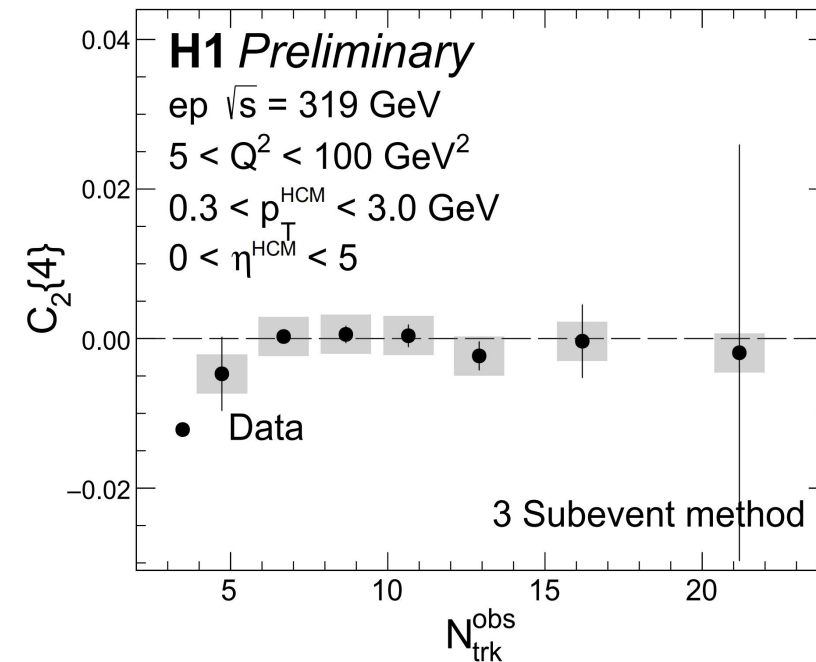
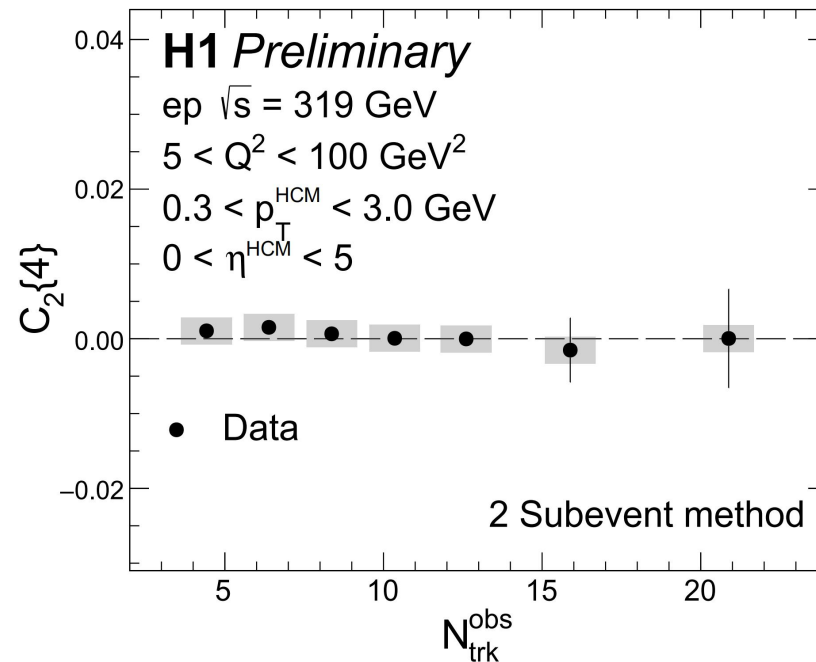
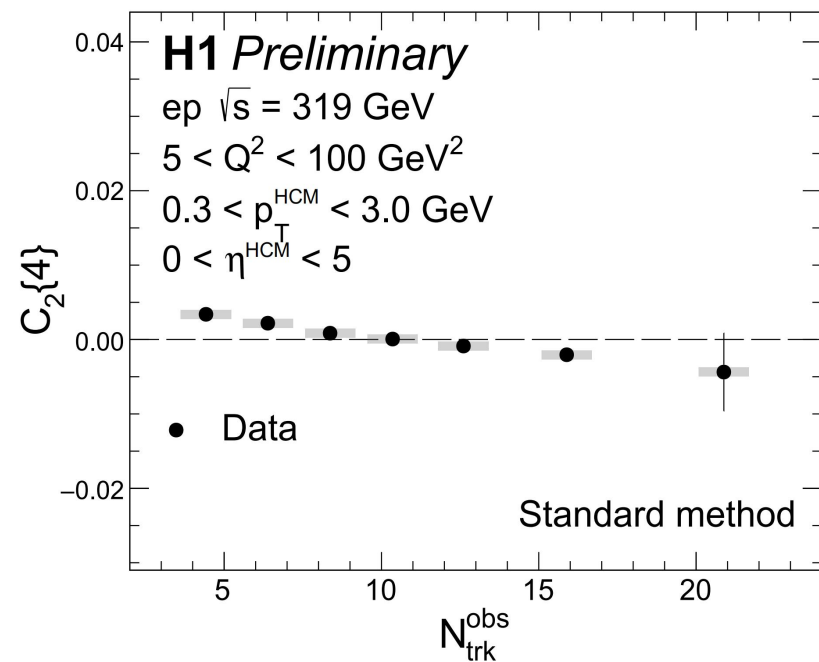
Subevent cumulants also investigated to further suppress non-flow

PRC 83, 044913 (2011)

PRC 96, 034906 (2017)



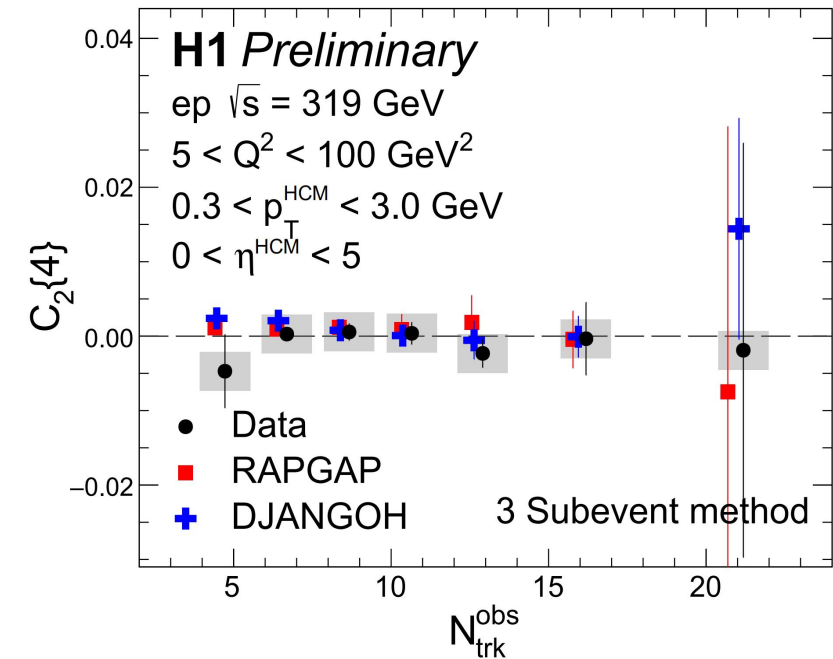
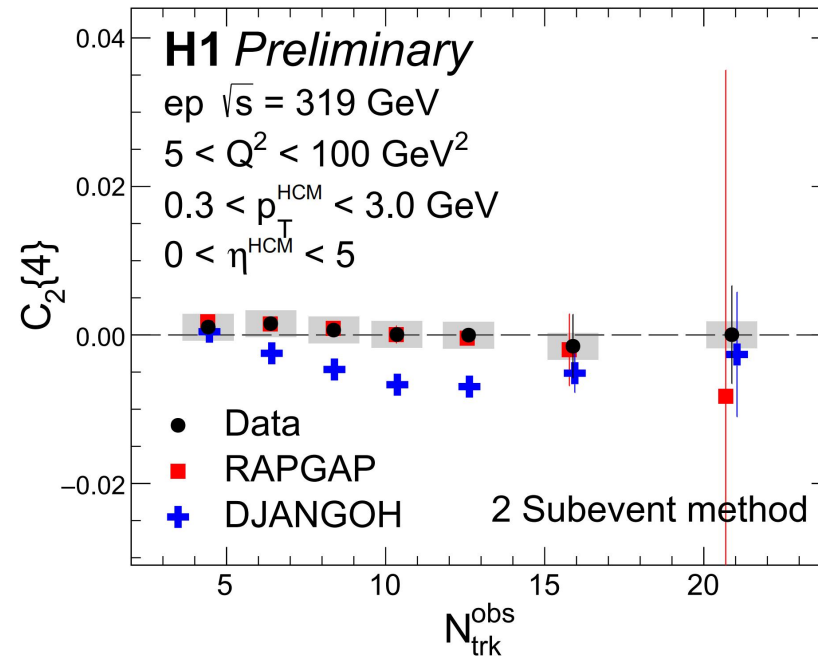
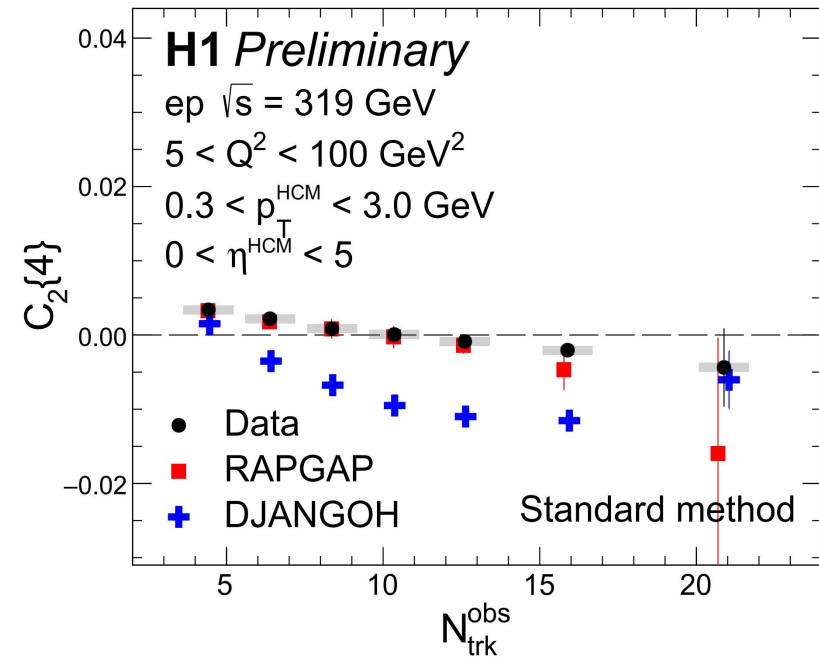
# Multi-particle correlation in ep DIS



No obvious negative  $C_2\{4\}$  in DIS

**DIS HCM**

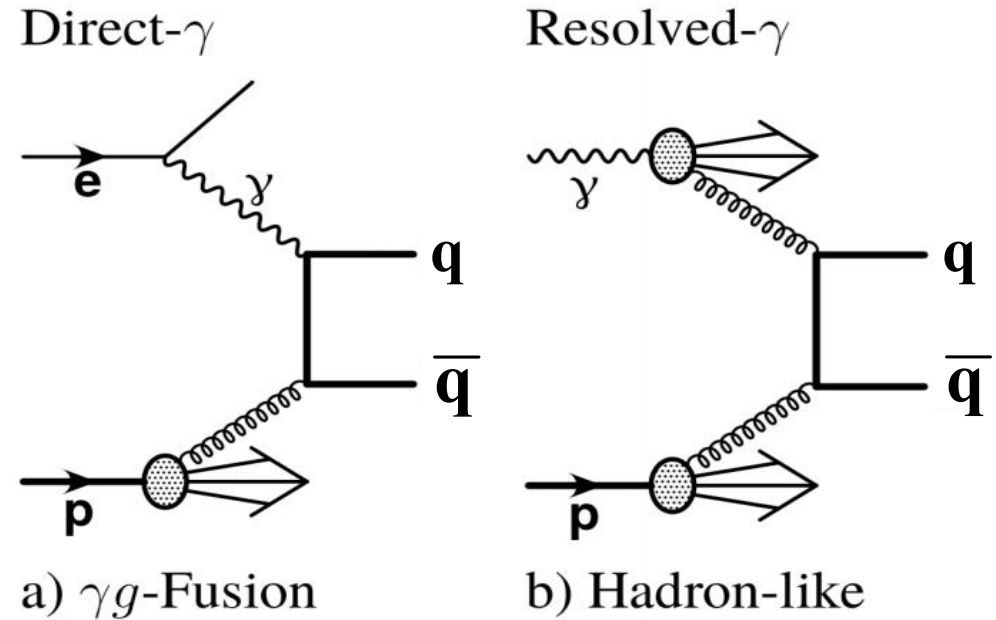
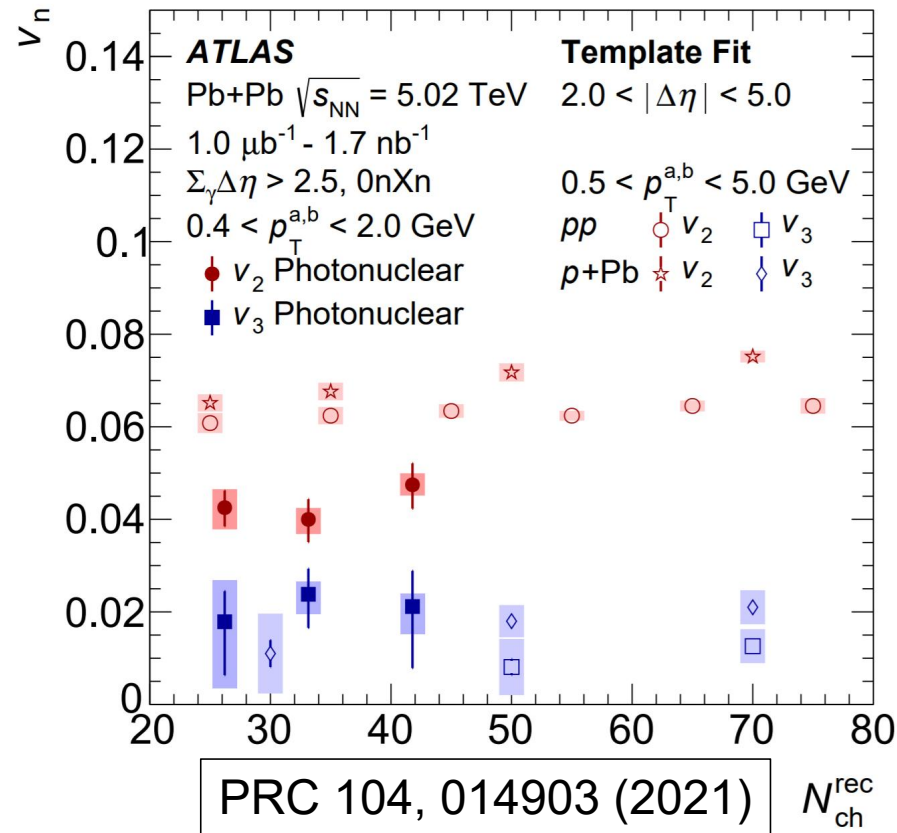
# Multi-particle correlation in ep DIS



No obvious negative  $C_2\{4\}$  in DIS  
RAPGAP can describe data

DIS HCM

# Search for collectivity in ep photoproduction



Non-zero  $v_2$  values observed in PbPb ultra-peripheral collisions  
**Evidence of collectivity in photo-nuclear collisions**

The resolved photoproduction process in ep collisions can be regarded as hadronic collisions  
**Collectivity in high multiplicity ep photoproduction?**

# Ridge yield limit in ep photoproduction

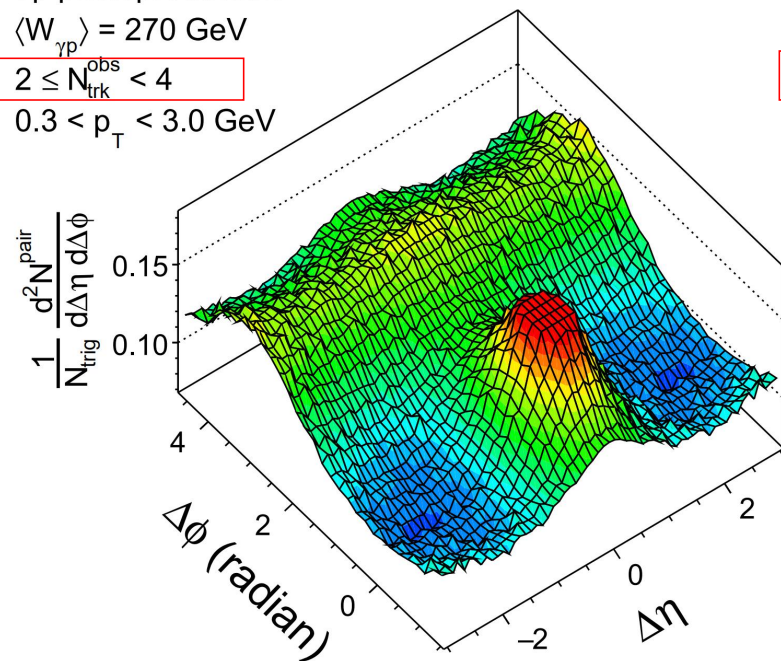
**H1 Preliminary**

ep photoproduction

$\langle W_{\gamma p} \rangle = 270$  GeV

$2 \leq N_{\text{trk}}^{\text{obs}} < 4$

$0.3 < p_{\text{T}} < 3.0$  GeV



low multiplicity

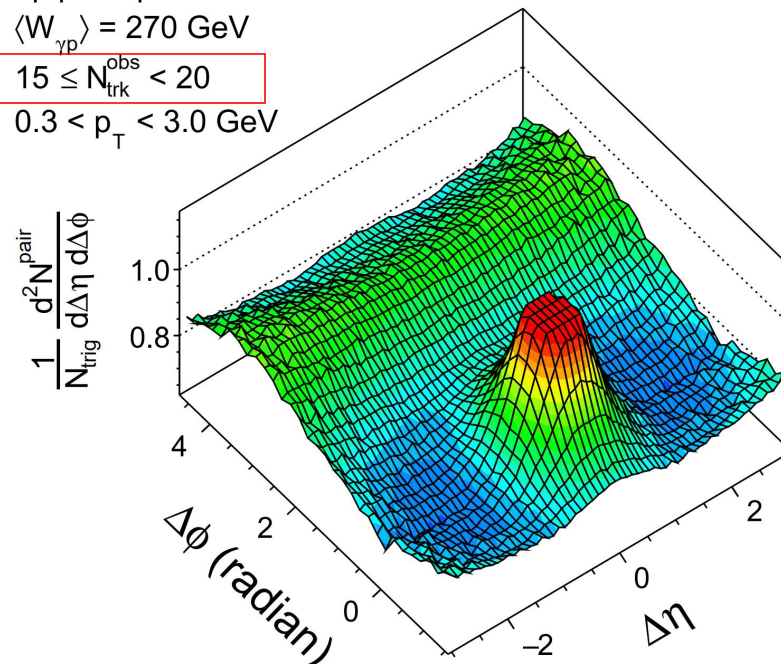
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high multiplicity

No near-side long-range ridge observed

**photoproduction**

# Ridge yield limit in ep photoproduction

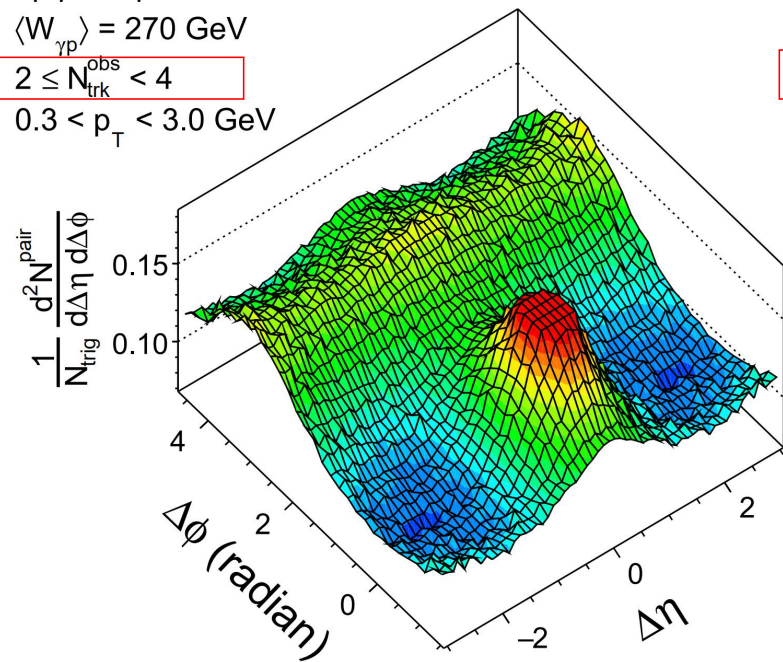
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ep photoproduction

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low multiplicity

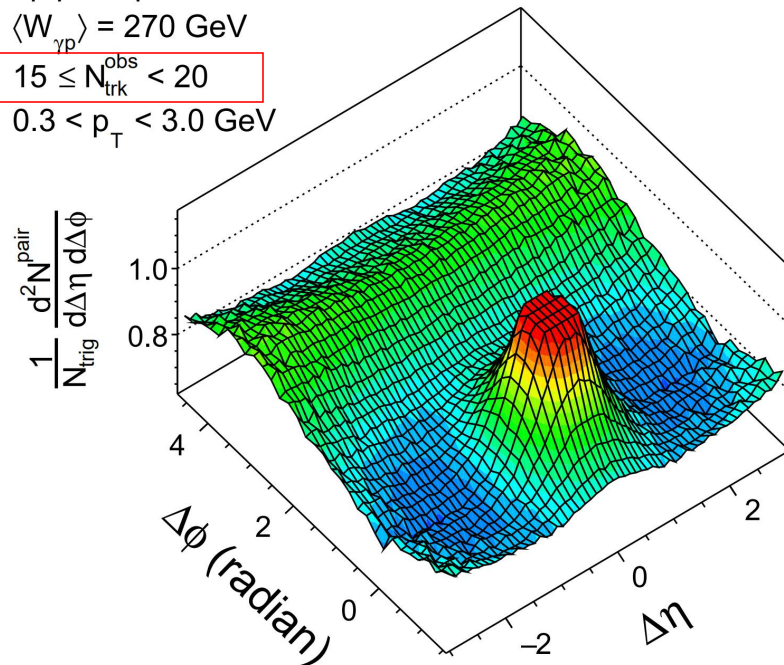
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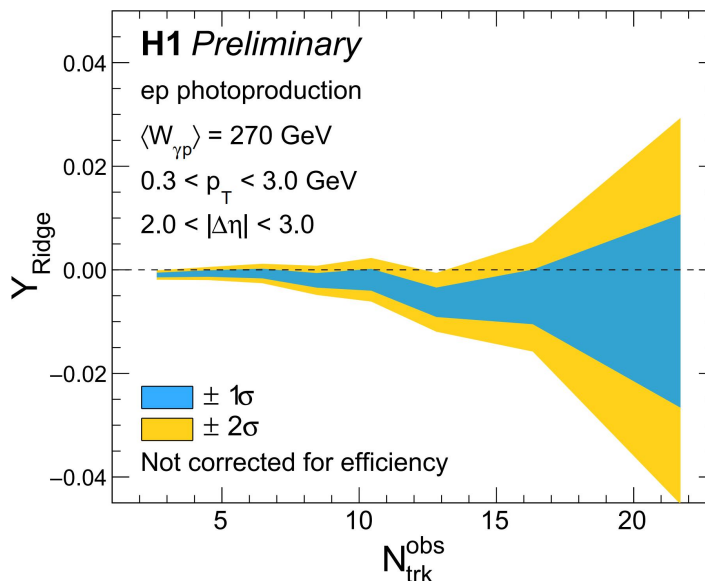
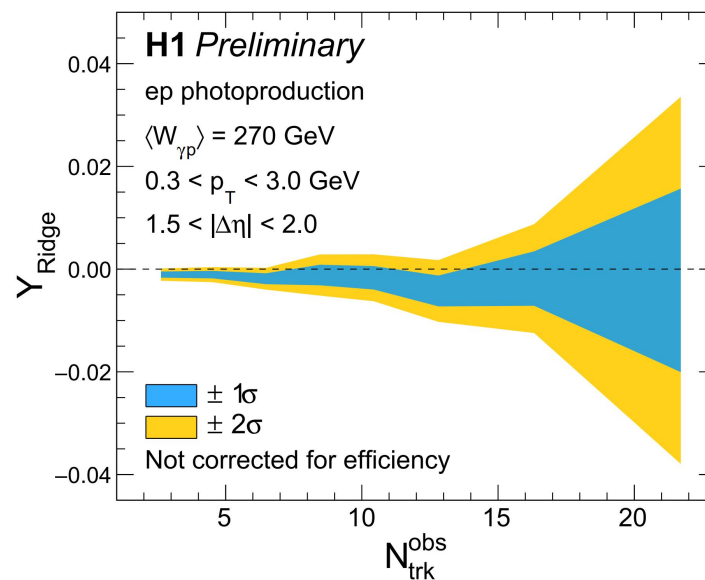
$0.3 < p_T < 3.0$  GeV



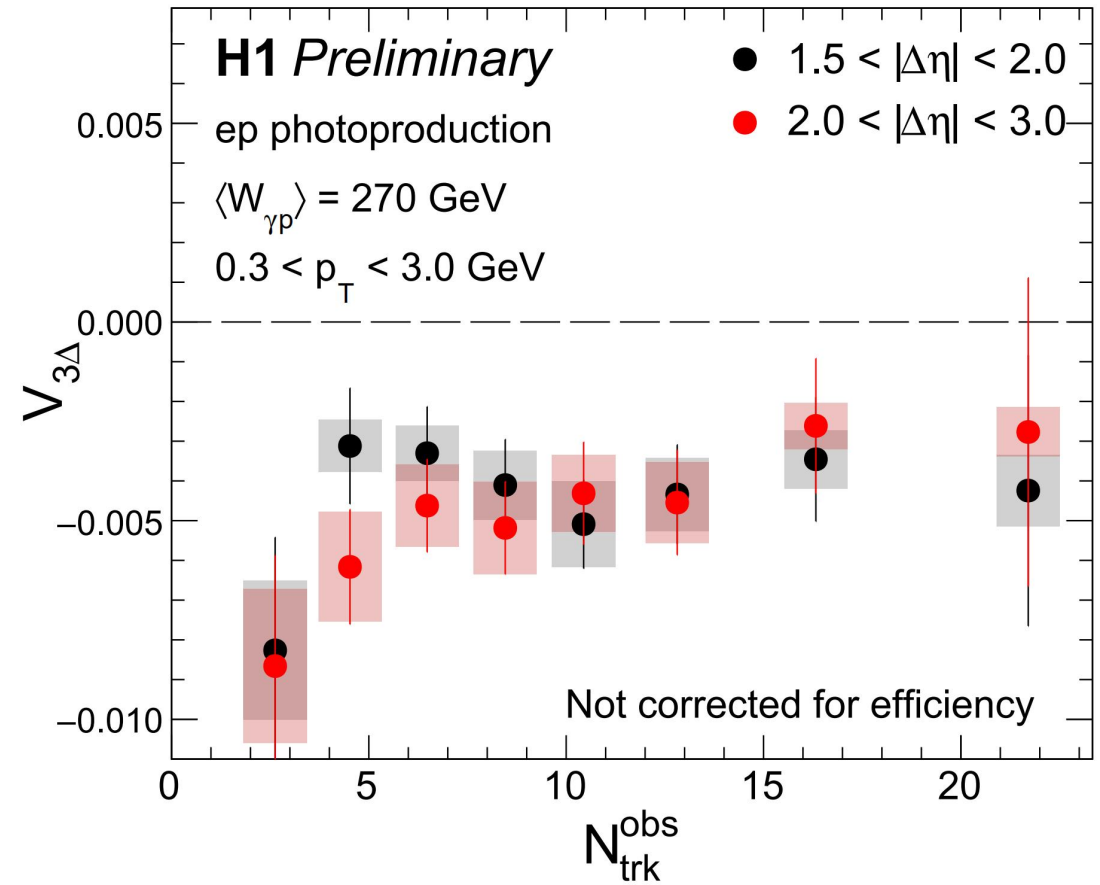
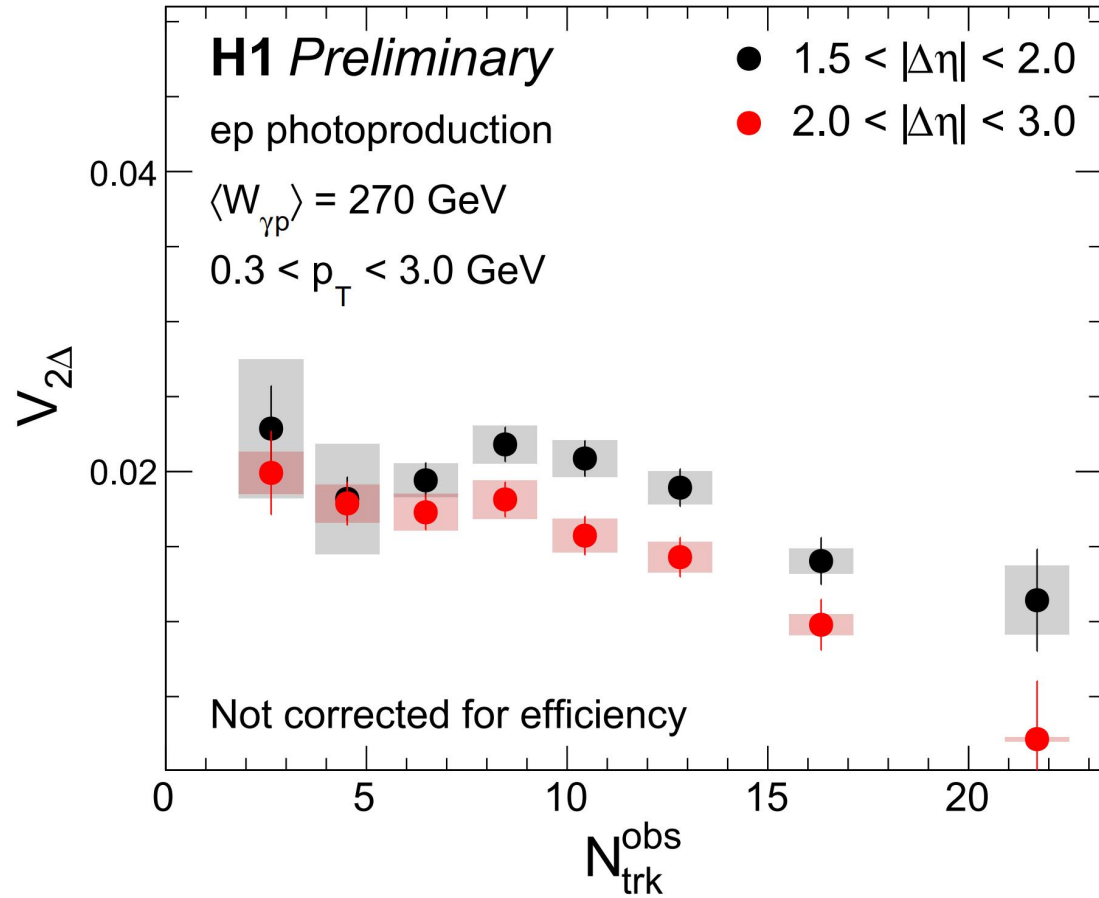
high multiplicity

No near-side long-range ridge observed  
Small room for existence of ridge

**photoproduction**

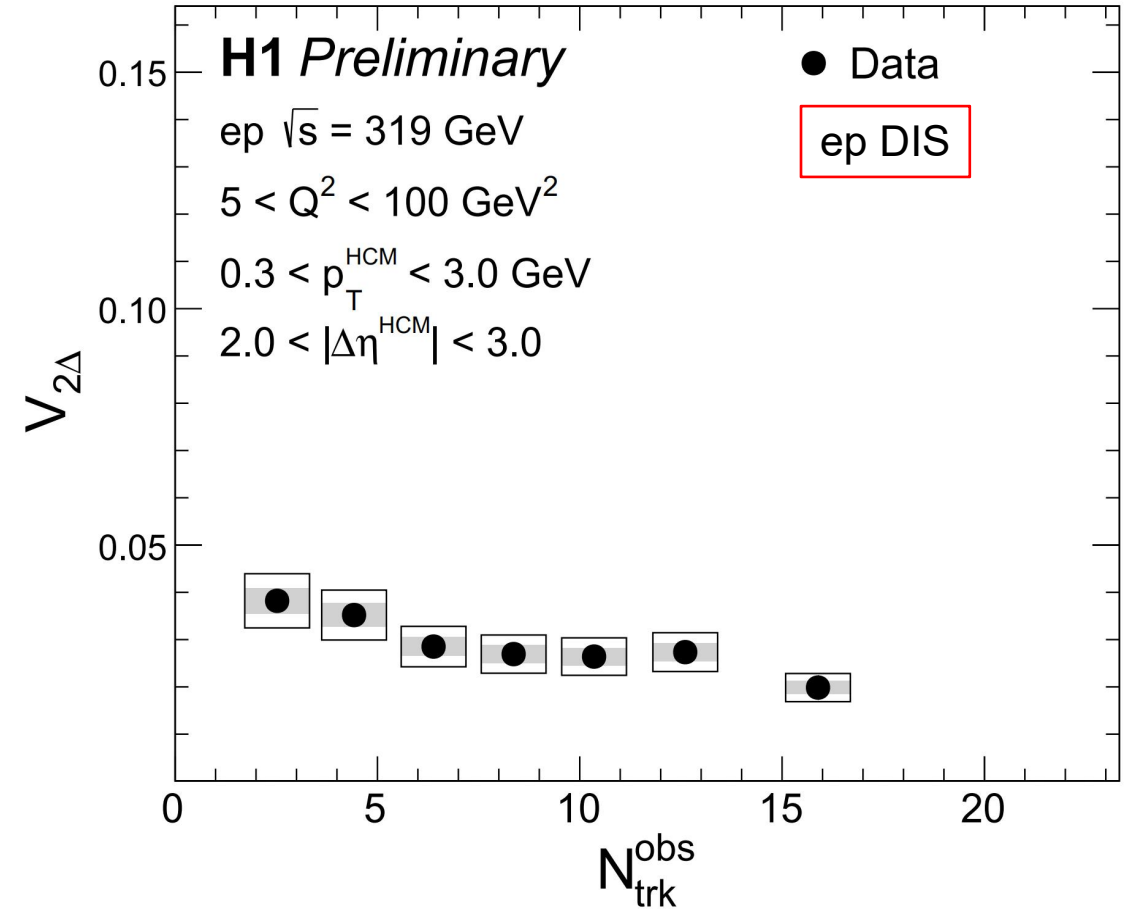
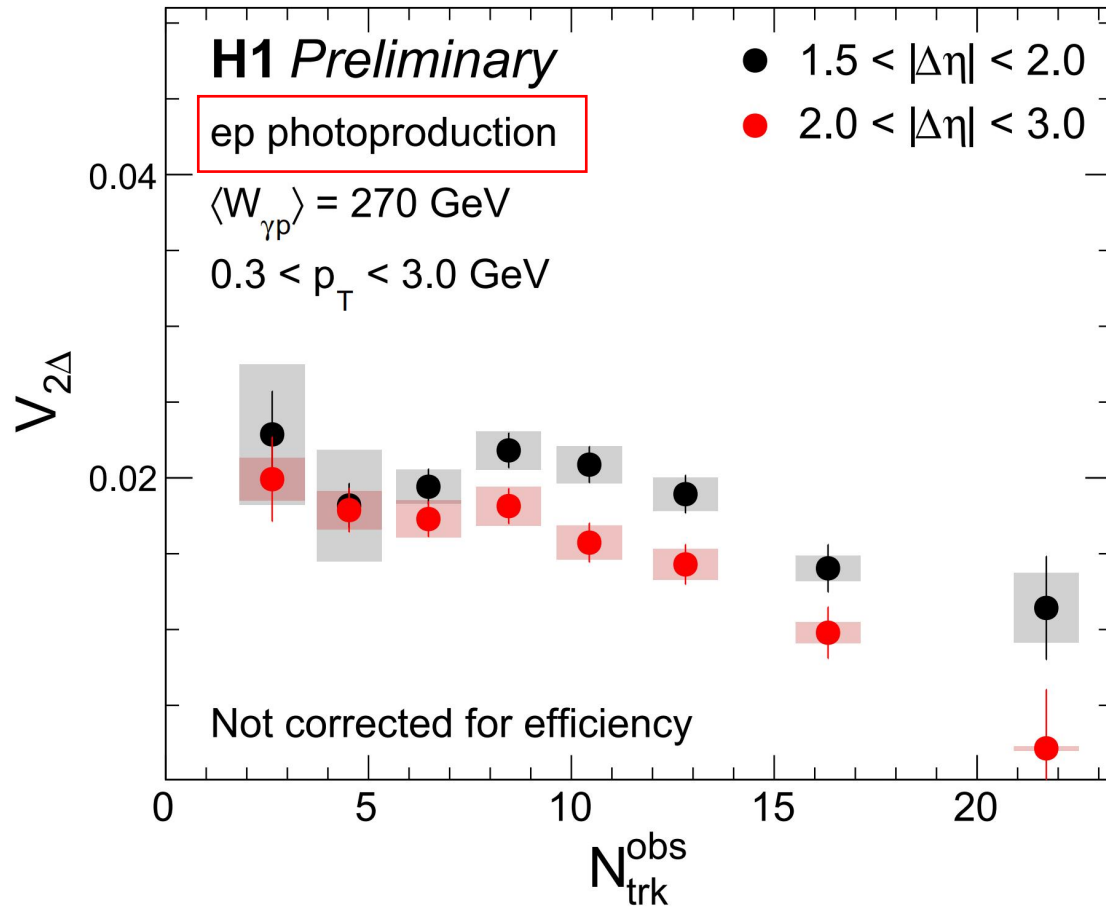


# Fourier coefficient $V_{n\Delta}$ in ep photoproduction



photoproduction

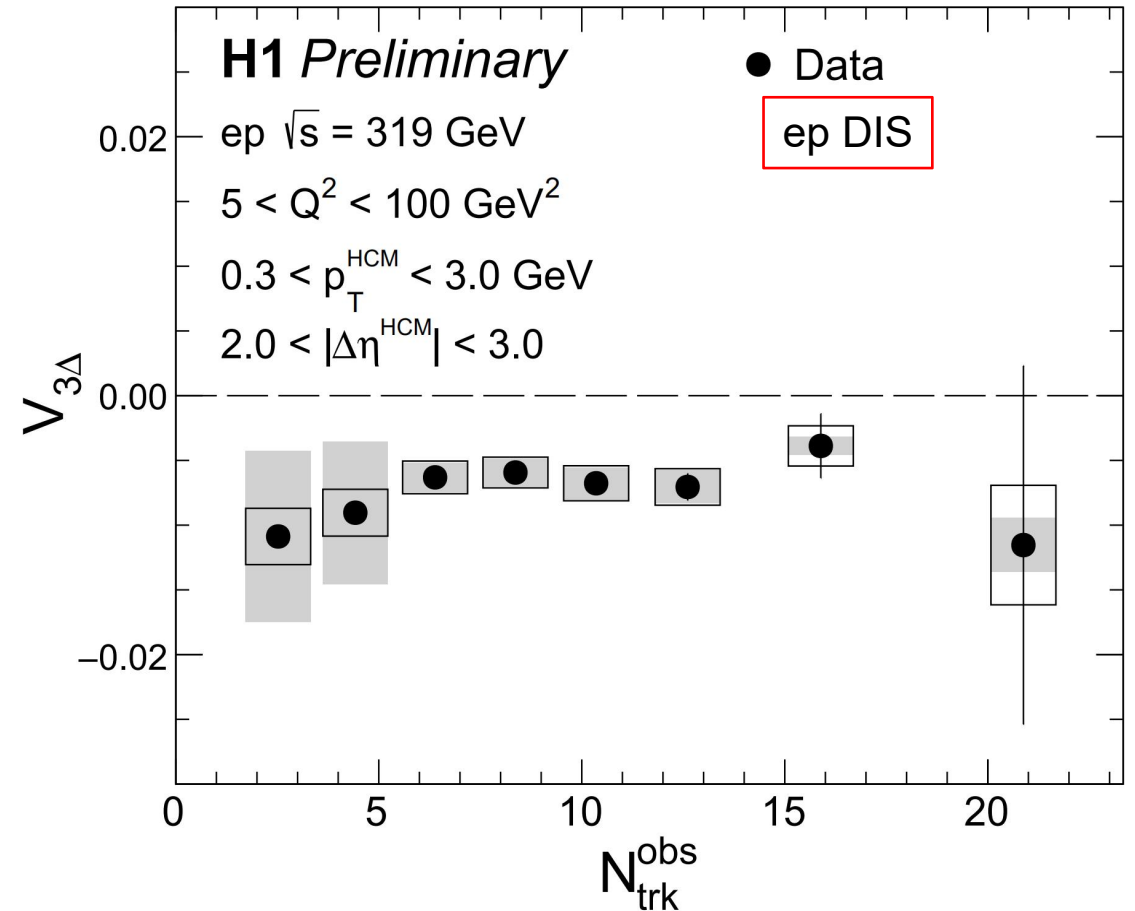
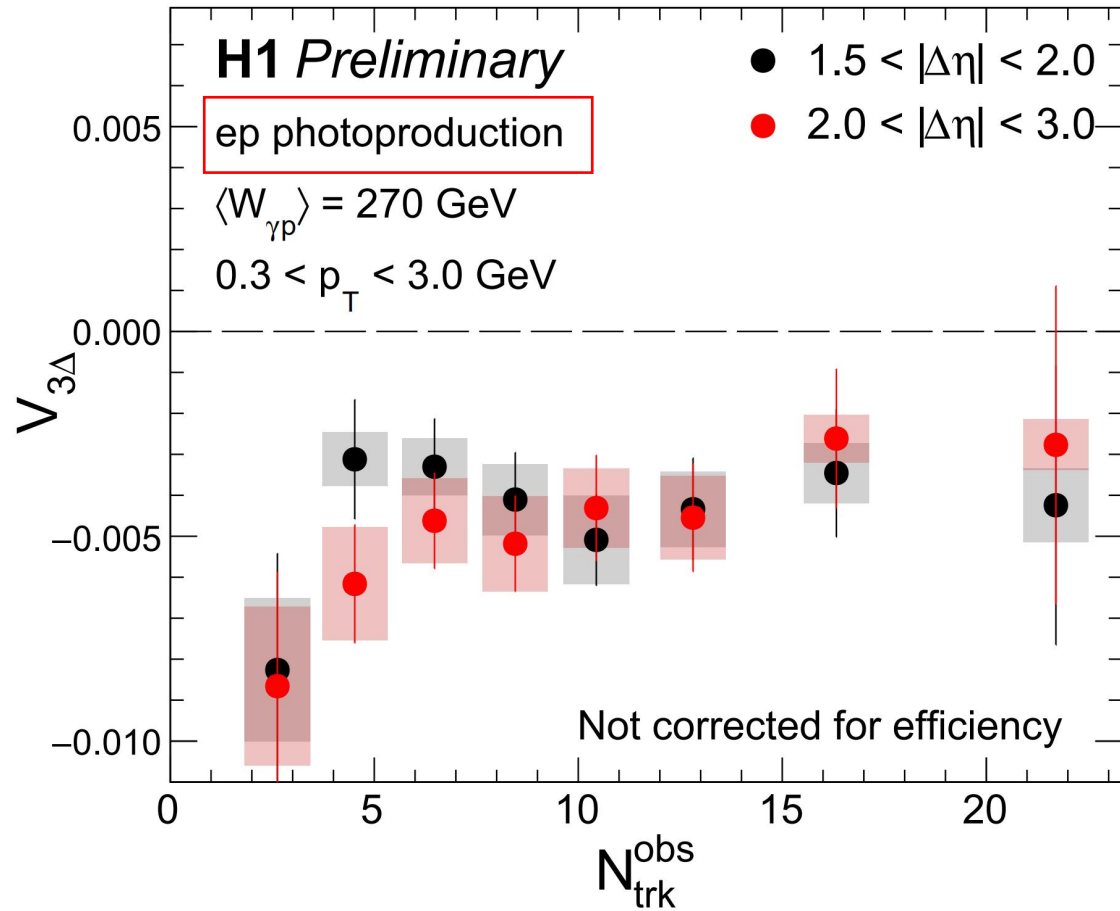
# Fourier coefficient $V_{n\Delta}$ in ep photoproduction



Similar  $V_{2\Delta}$  behavior in photoproduction data as in DIS

**photoproduction**

# Fourier coefficient $V_{n\Delta}$ in ep photoproduction

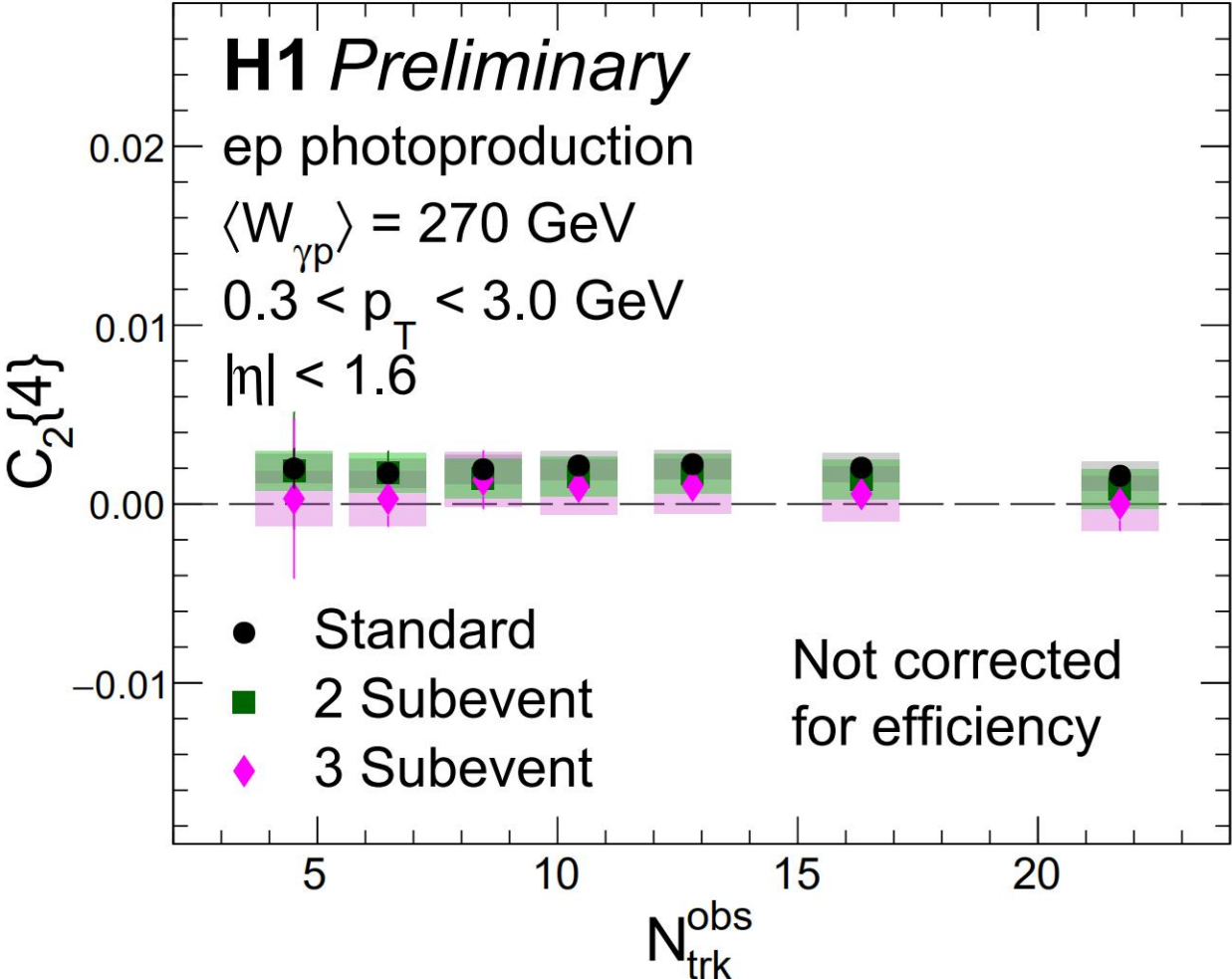


Similar  $V_{3\Delta}$  behavior in photoproduction data as in DIS

photoproduction



# Multi-particle correlation in ep photoproduction



No evidence of negative  $C_2\{4\}$ , no sign of collectivity

photoproduction

# Summary

## No collectivity observed in either DIS or photoproduction in H1 ep collisions

No long-range near-side ridge

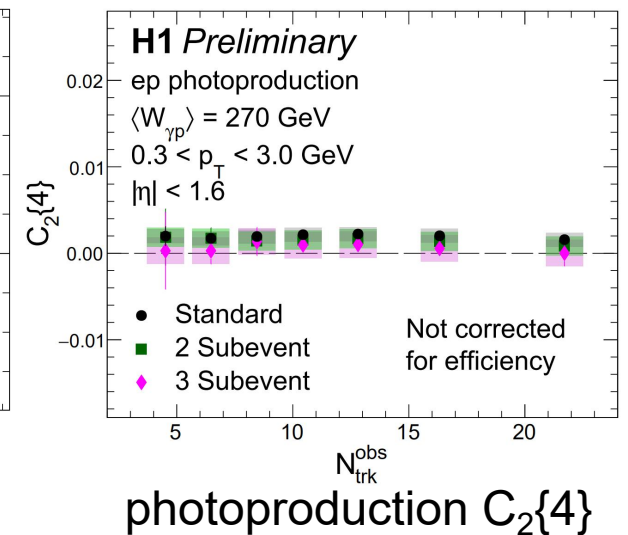
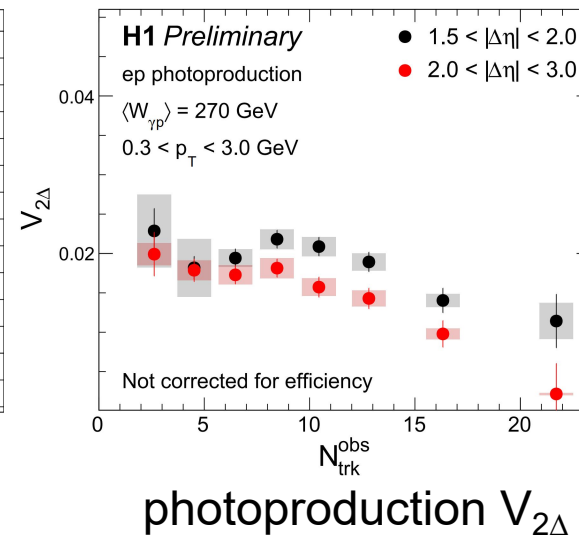
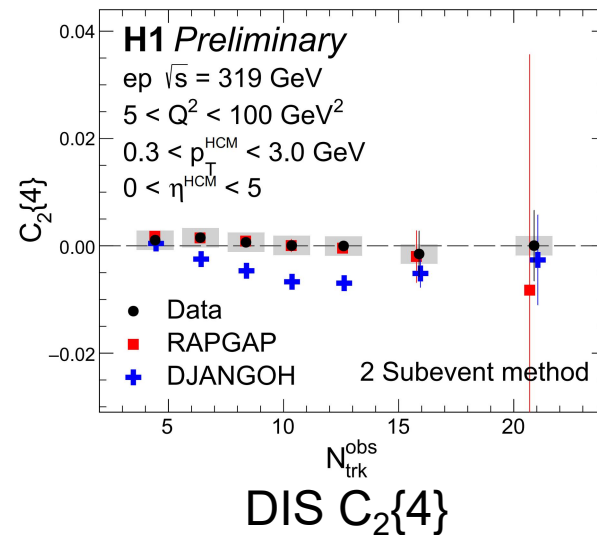
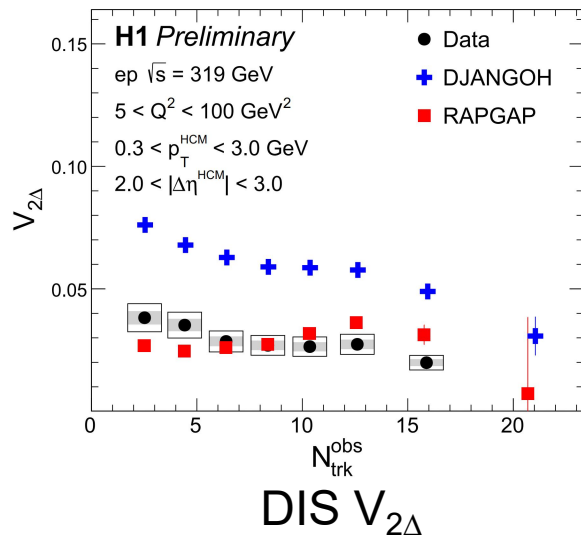
Decreasing  $V_{2\Delta}$  and negative  $V_{3\Delta}$

No negative  $C_2\{4\}$

Compared with MC simulation:

$V_{2\Delta}$  and  $V_{3\Delta}$  in DIS can be described by RAPGAP w/o collectivity

$C_2\{4\}$  can also be described by RAPGAP w/o collectivity



# Summary

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No long-range near-side ridge

Decreasing  $V_{2\Delta}$  and negative  $V_{3\Delta}$

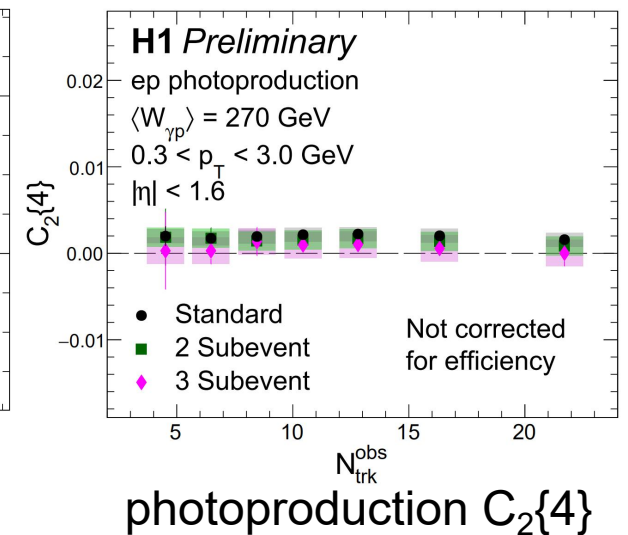
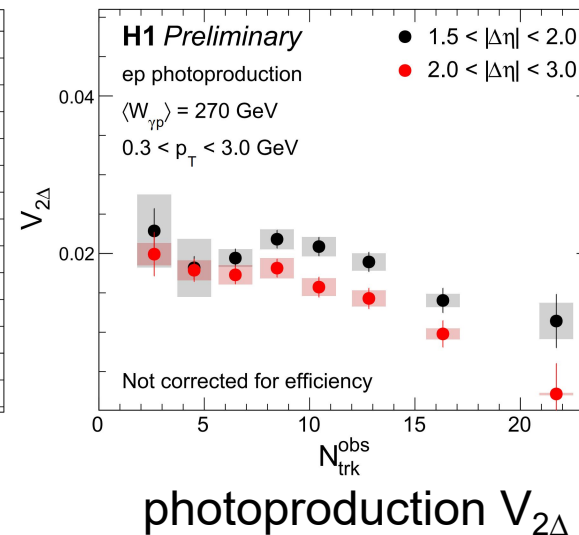
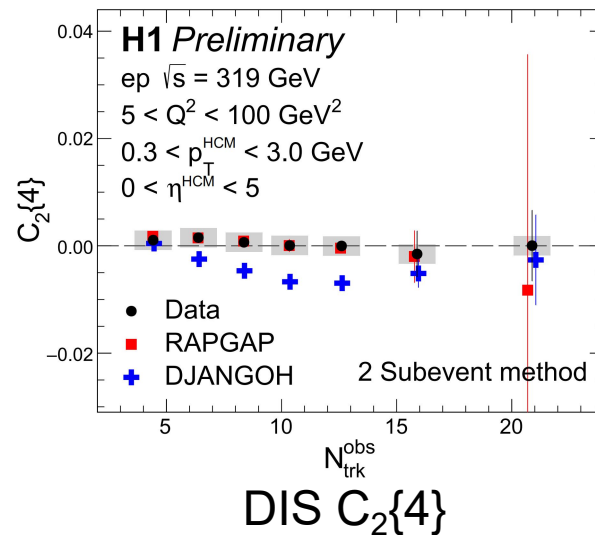
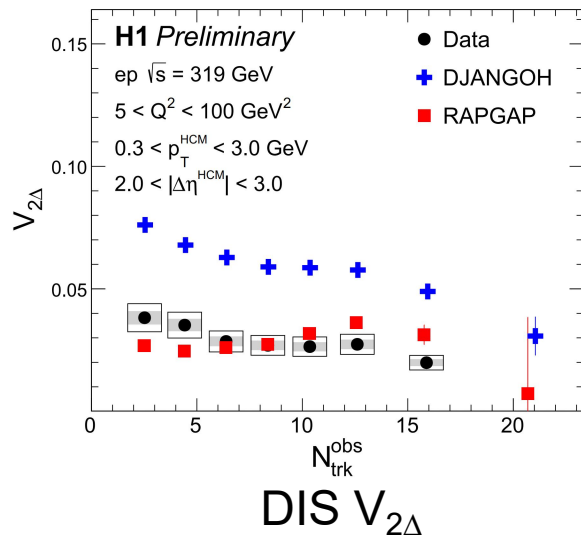
No negative  $C_2\{4\}$

Compared with MC simulation:

$V_{2\Delta}$  and  $V_{3\Delta}$  in DIS can be described by RAPGAP w/o collectivity

$C_2\{4\}$  can also be described by RAPGAP w/o collectivity

Is there any collectivity in high multiplicity eA collisions? Stay tuned for EIC



# Thanks for attention

## No collectivity observed in either DIS or photoproduction in H1 ep collisions

No long-range near-side ridge

Decreasing  $V_{2\Delta}$  and negative  $V_{3\Delta}$

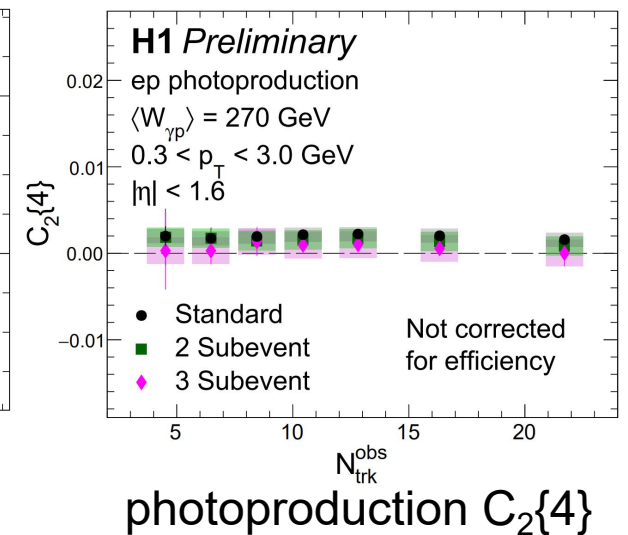
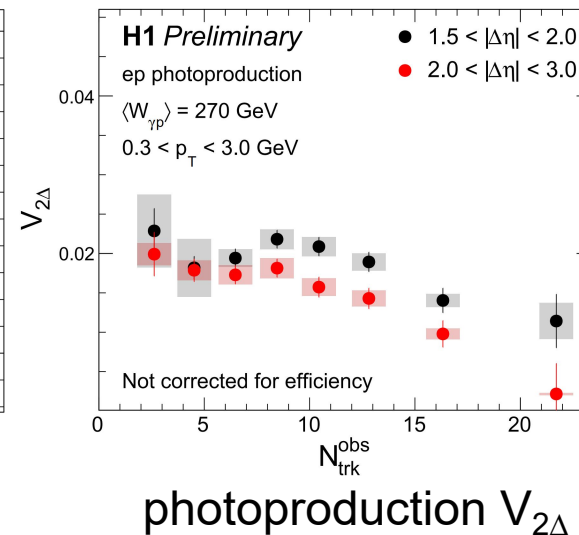
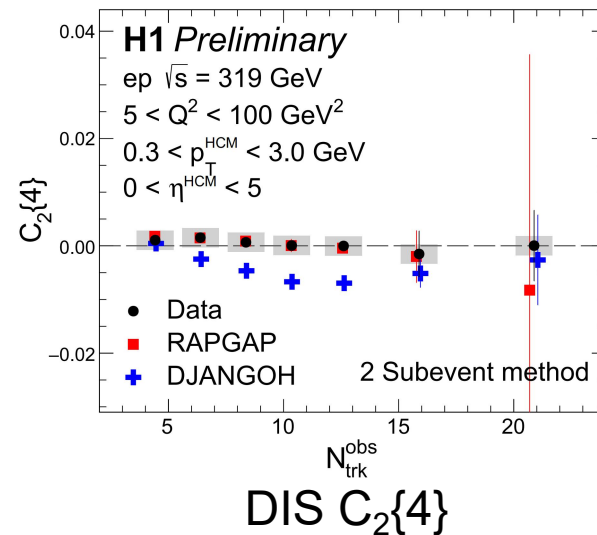
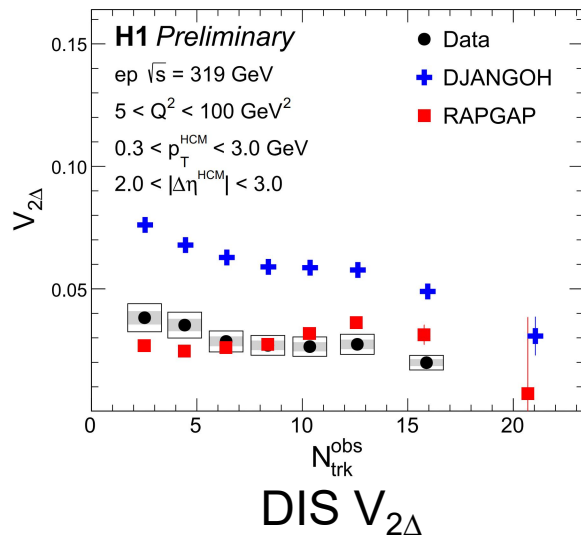
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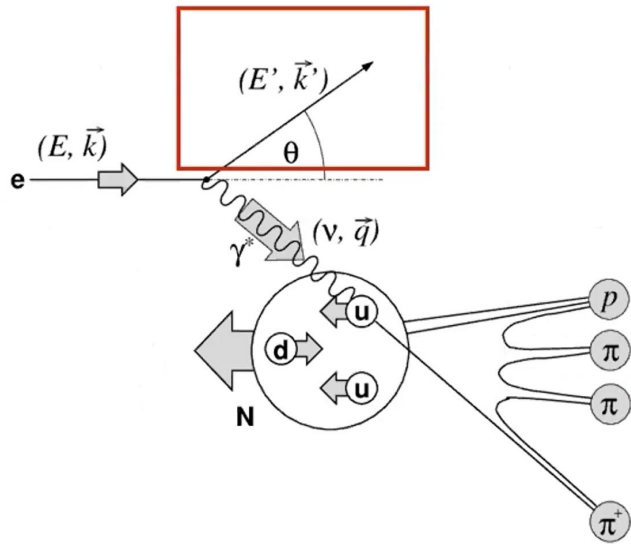
Is there any collectivity in high multiplicity eA collisions? Stay tuned for EIC



Thanks for your attention!

# Back up

# Kinematics in DIS

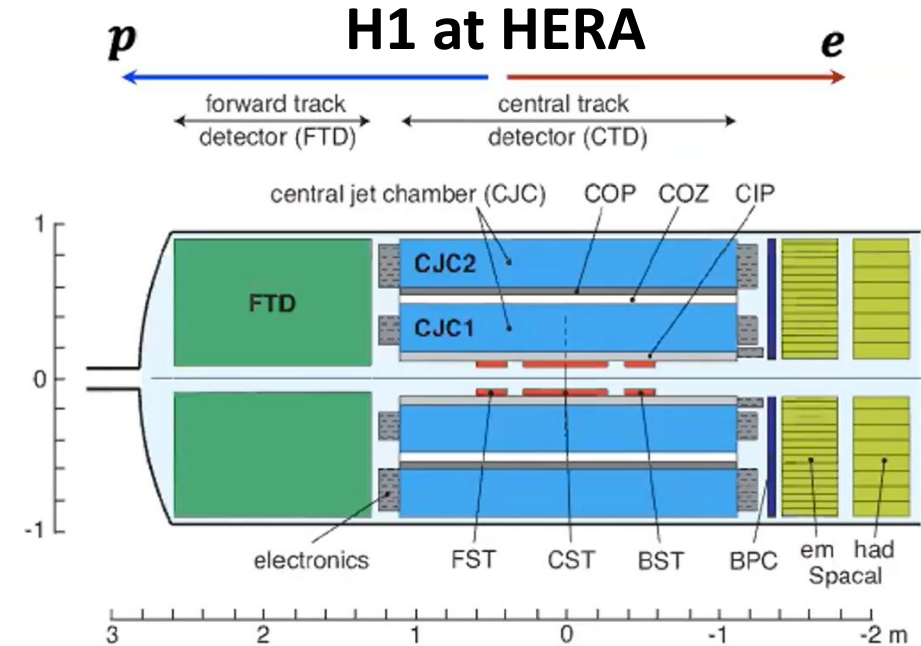


$$Q^2 = -q^2$$

$$y = \frac{\nu}{E_e} = \frac{E_e - E_{e'}}{E_e}$$

$$s = (k + P)^2$$

$$x = \frac{Q^2}{sy}$$



**Textbook:** we only need to measure scattered electron for kinematics. However, at HERA, there are as least 4-6 different methods to construct kinematics, and each method has its pros and cons. Not only electron is used.

**SpalCal, EM Calorimeter** to detect scattered electrons in degrees.  
 CTD covers from 25-155 degrees. (backward~-1.5unit)  
 FTD+FST covers 5-25 degrees.(forward~3unit)

# Two-particle correlation method

In our analysis, the 2PC functions are filled with the difference  $\Delta\eta$ ,  $\Delta\Phi$  of particle pairs. The trigger particle is the charged particles in an event passing track selections. So in the same event, the signal distribution is per-trigger-particle yield of correlated pairs, including detector acceptance effects:

$$S(\Delta\eta, \Delta\phi) = \frac{1}{N_{trig}} \frac{d^2 N^{same}}{d\Delta\eta d\Delta\phi}$$

The mix-event background distributions is constructed with trigger particles from one event are correlating with all of the associated particles from different events within  $|Z_{VTX}| < 2\text{cm}$ . In this analysis, each event is paired with 5 randomly chosen events. The result is given by

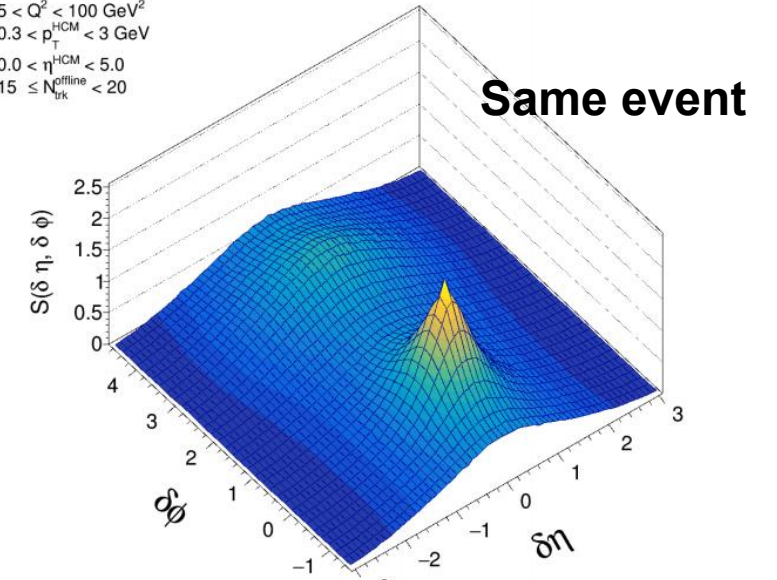
$$B(\Delta\eta, \Delta\phi) = \frac{1}{N_{trig}} \frac{d^2 N^{mix}}{d\Delta\eta d\Delta\phi}$$

The signal distribution, divided by the background distribution, is the final 2PC function. The pair acceptance of the detector can be corrected.

$$\frac{1}{N_{trig}} \frac{d^2 N^{pair}}{d\Delta\eta d\Delta\phi} = B(0, 0) \times \frac{S(\Delta\eta, \Delta\phi)}{B(\Delta\eta, \Delta\phi)}$$

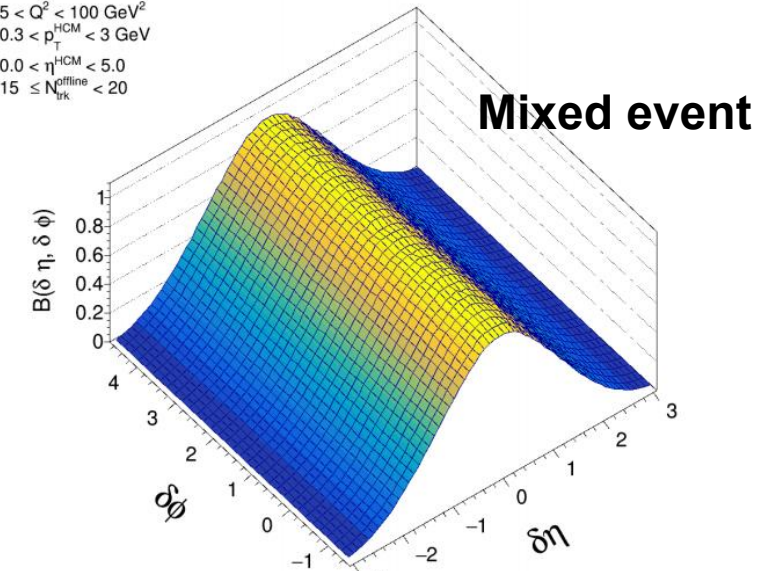
H1 DIS Data ( HCM frame )

$5 < Q^2 < 100 \text{ GeV}^2$   
 $0.3 < p_T^{HCM} < 3 \text{ GeV}$   
 $0.0 < \eta^{HCM} < 5.0$   
 $15 \leq N_{trk}^{offline} < 20$



H1 DIS Data ( HCM frame )

$5 < Q^2 < 100 \text{ GeV}^2$   
 $0.3 < p_T^{HCM} < 3 \text{ GeV}$   
 $0.0 < \eta^{HCM} < 5.0$   
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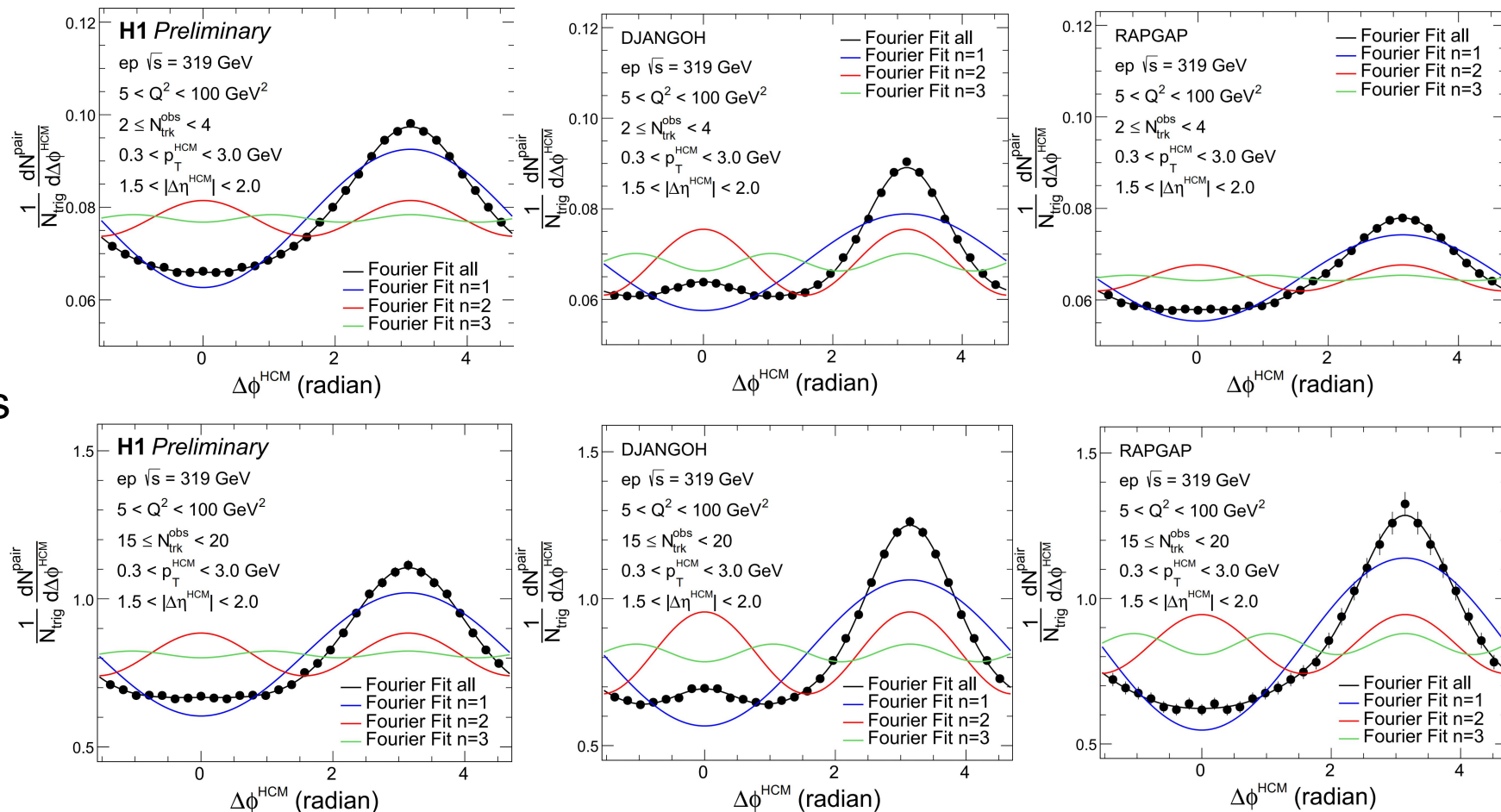




# Fourier coefficient $V_{n\Delta}$ extraction procedure

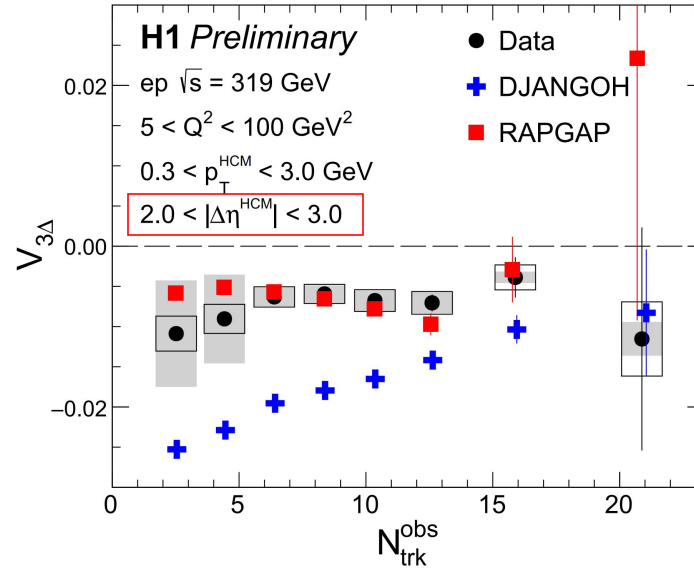
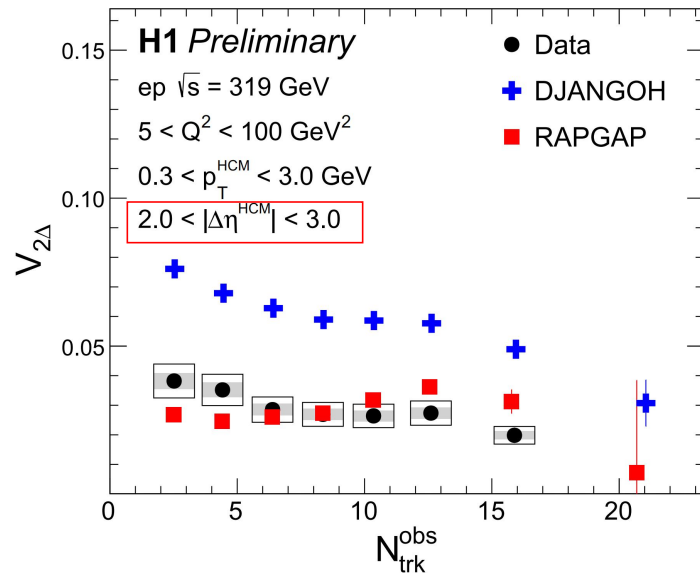
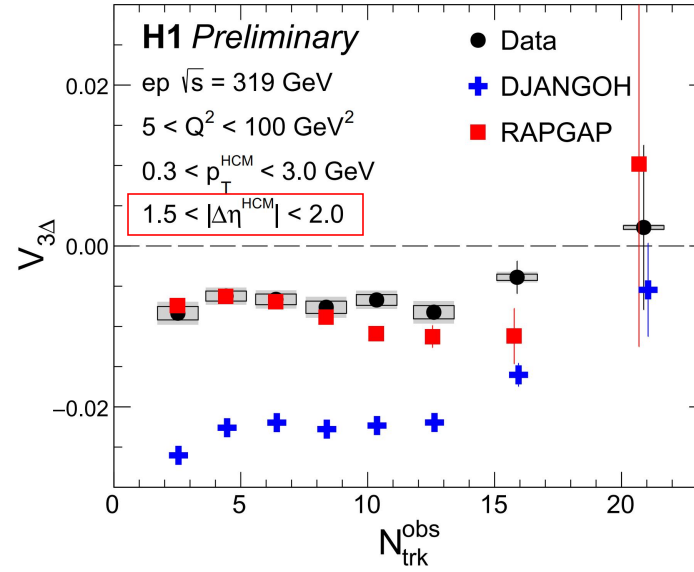
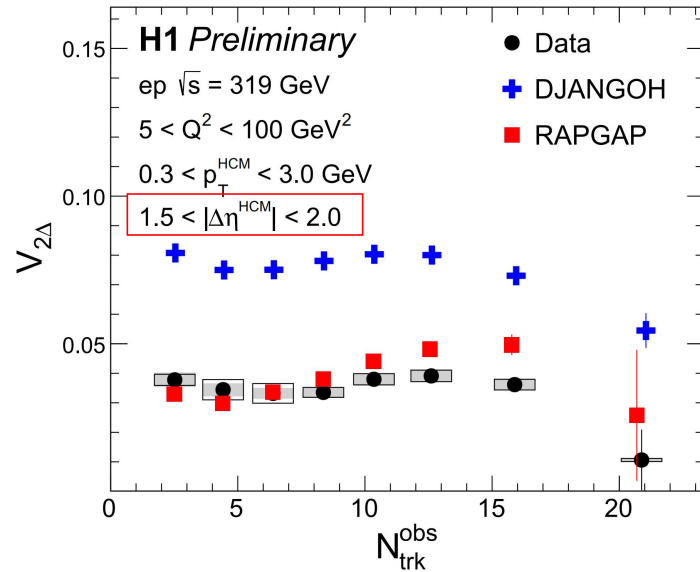
The azimuthal anisotropy harmonics are determined from a Fourier decomposition of long-range two-particle correlation functions on  $\Delta\phi$  direction.

## 1-D comparisons



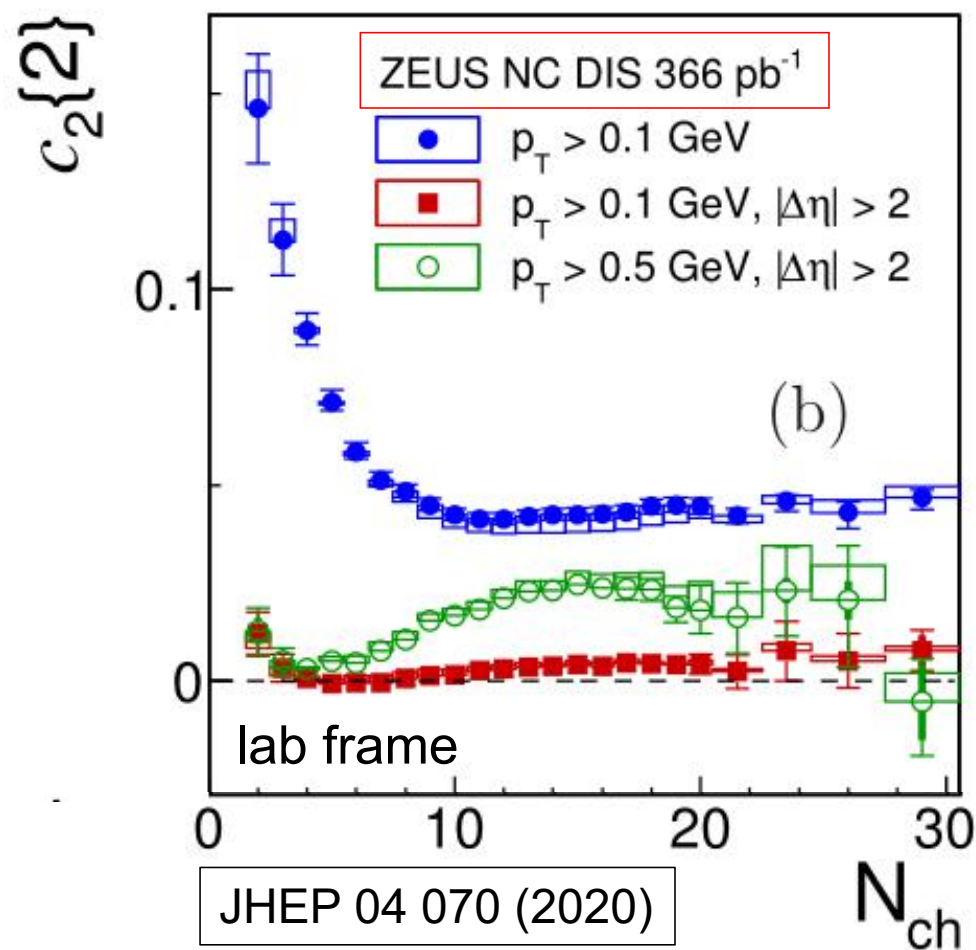
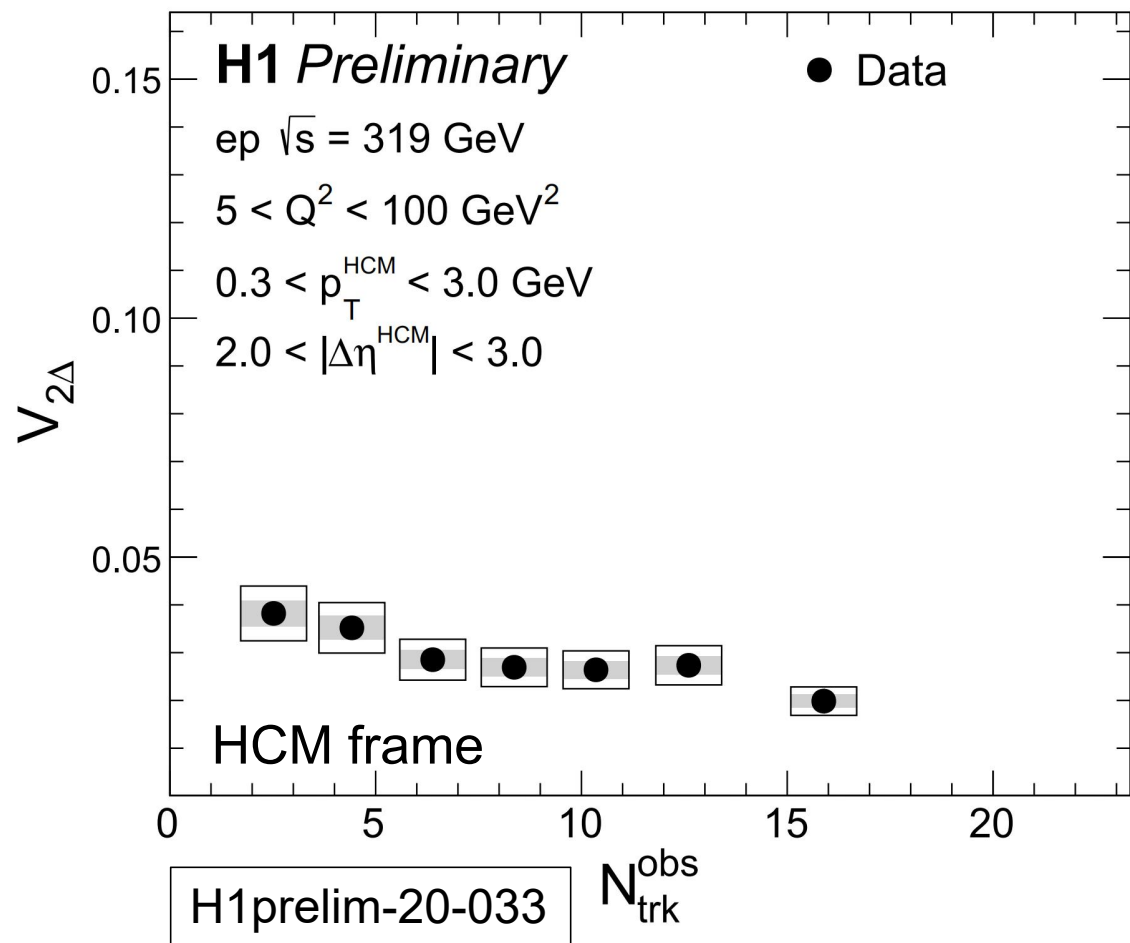
The comparison between data and MCs. Similar shapes in high and low multiplicity.

# Fourier coefficient $V_{n\Delta}$



MC RAPGAP has better description on DIS data than MC DJANGO  
 Data can be described by MC w/o collectivity

# Fourier coefficient $V_{n\Delta}$ in ep DIS



Similar trend as ZEUS result

**DIS HCM**

# Mechanism in RAPGAP and DJANGO

Comput.Phys.Commun. 86 (1995) 147-161

Sov.J.Nucl.Phys. 15 (1972) 438-450, Yad.Fiz. 15 (1972) 781-807

## The RAPGAP 3.1

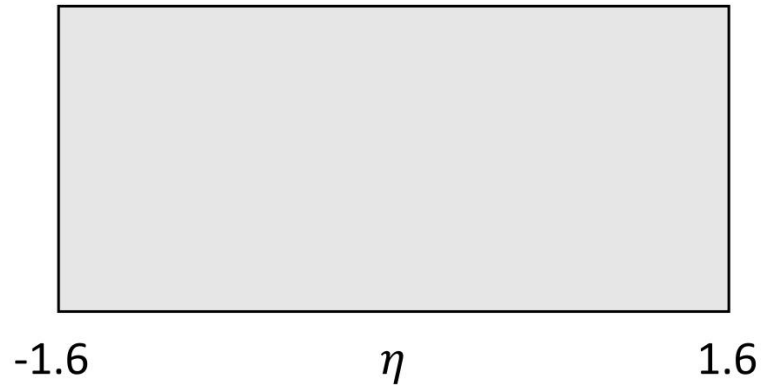
MC event generator matches **first order QCD matrix elements to the Dokshitzer-Gribov-Lipatov-Altarelli-Parisi (DGLAP) parton showers** with strongly ordered transverse momenta of subsequently emitted partons. The factorisation and renormalisation scales are set to  $u_f = u_r = \sqrt{Q^2 + \hat{p}_T^2}$ , where  $\hat{p}_T$  is the transverse momentum of the outgoing hard parton from the matrix element in the center-of-mass frame of the hard subsystem. The CTEQ 6L leading order parametrisation of the parton density function (PDF) is used.

## The DJANGO 1.4

MC event generator used the **Color Dipole Model (CDM) as implemented in ARIADNE, which models first order QCD processes and creates dipoles between colored partons**. Gluon emission is treated as radiation from these dipoles, and new dipoles are formed from the emitted gluons from which further radiation is possible. The radiation pattern of the dipoles includes interference effects, thus modelling gluon coherence. The transverse momenta of the emitted partons are not ordered in transverse momentum with respect to rapidity, producing a configuration **similar to the Balitsky-Fadin-Kuraev-Lipatov (BFKL) treatment of parton evolution**. The CTEQ 6L at leading order is used as the PDF.

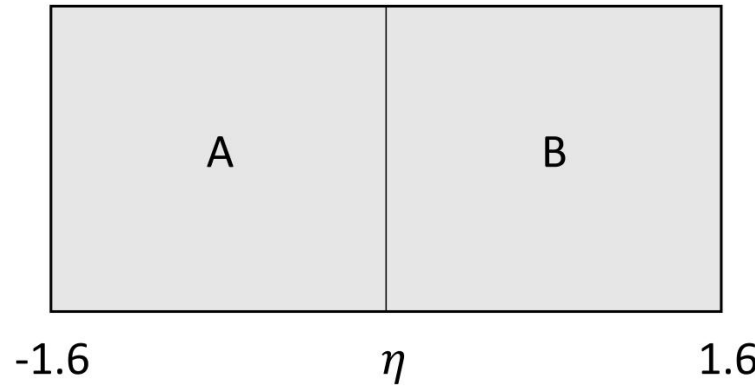
# Multi-particle correlation

Standard method



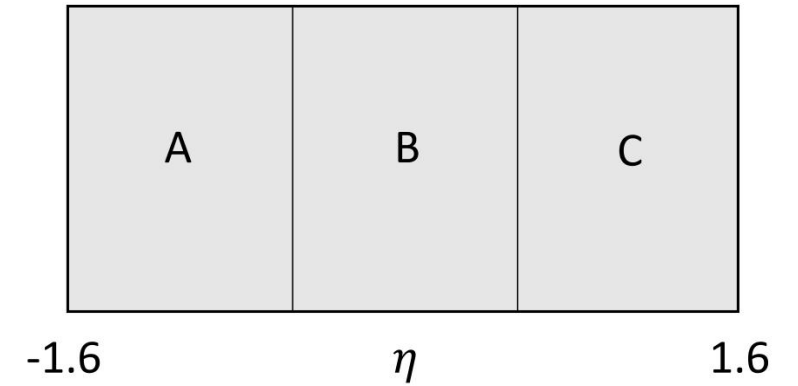
4 particles from the same range

2 sub-event method



2 particles from A  
2 particles from B

3 sub-event method



1 particle from A  
2 particles from B  
1 particle from C

More advanced sub-event methods can further suppress few particle correlation

Method paper: Phys. Rev. C **96**, 034906, arXiv.1701.03830

2 and 3-subevent methods provide more reliable results on collectivity