



Groomed Event Shapes in e+p DIS + Lessons for EIC*

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HERA4EIC Workshop, June 8

*EIC Lessons are my personal opinions as a newcomer, not representative of the H1 collaboration!



Event Shapes

- Inclusive observables where all particles contribute
 - E.g. Thrust measures degree of collimation along an axis
- Sensitive to QCD across scales
- Calculable to high precision in perturbation theory
 - Fixed-order QCD \rightarrow tail of thrust distribution
 - Soft-collinear effective theory (SCET) calculations → peak of thrust distribution
- Used extensively in e⁺e⁻ and Breit frame e+p collisions

$$au = 1 - T$$
 with T

$$\frac{\sum_{h} \left| \vec{p}_{z,h} \right|}{\sum_{h} \left| \vec{p}_{h} \right|}$$



Inclusive DIS & Breit Frame

- HERA-II data
 - $Q^2 > 150 \text{ GeV}^2$, 0.2 < y < 0.7
 - No direct $x_{Bj.}$ cut applied
 - 352 pb⁻¹ collected
- Breit Frame
 - Defined as the frame where $2x_{Bi}P + q = 0$
 - Exchanged boson reverses struck parton's momentum
 - Parton has \overrightarrow{xP} incoming, $-\overrightarrow{xP}$ outgoing



Inclusive DIS – Event Selection

- DIS kinematics reconstructed with IS method
 - Factors out QED ISR
 - Does **not** assume that incoming electron has 27.6 GeV of energy at the hard vertex
 - Infer electron energy from longitudinal momentum balance
- Require 50 GeV < $\Sigma(E-P_z)$ < 60 GeV
 - Ensures low amount of QED ISR and detector losses in current hemisphere
 - Effectively constrains an unmeasured ISR photon to have < 2.5 GeV of energy
 - Also removes all non-DIS background (photoproduction, beam-gas, etc.)
- Fiducial volume cut applied to ensure high electron purity



$$E_{I\Sigma}^{e'} = \frac{\Sigma_{HFS} + E_{e'}(1 - \cos \theta_{e'})}{2}$$
$$x_{I\Sigma} = \frac{E_{e'}}{E_p} \frac{\cos^2 \theta/2}{y_{\Sigma}}$$
$$y_{I\Sigma} = y_{\Sigma} = \frac{\Sigma}{\Sigma + E(1 - \cos \theta)}$$
$$Q_{I\Sigma}^2 = \frac{E^2 \sin^2 \theta}{1 - y_{\Sigma}}$$

Centauro

- Jet algorithm with asymmetric clustering distance measure
 - Suited for clustering Bornlevel DIS in the Breit frame
- Here Centauro is used to produce a clustering tree for the full event





Centauro jets will be an important EIC measurement!



Doesn't preferentially capture struck quark

. . . .

Not longitudinally invariant

Figure 2. Jet clustering in the Breit frame using the longitudinally-invariant anti- $k_T(LI)$, Centauro, and spherically-invariant anti- k_T (SI) algorithms in a DIS event simulated with PYTHIA 8. Each particle is illustrated as a disk with area proportional to its energy and the position corresponds to the direction of its momentum projected onto the unfolded sphere about the hard-scattering vertex. The vertical dashed lines correspond to constant θ and curved lines to constant ϕ . All the particles clustered into a given jet are colored the same.

Event Grooming in DIS

- Whole event is clustered into one "jet"
- Iteratively de-cluster until grooming condition is passed
 - Analogous to Soft Drop in p+p
- Groomed events are similar to groomed jets!



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Breit Frame Event Displays



Figure 2. Visualization of three PYTHIA 8 events at $\sqrt{s} = 63$ GeV and $Q \sim 10$ GeV before and after grooming. The particles in this events are represented by disks on the unfolded sphere. Green disks represent particles that pass grooming where grayed-out particles are removed from the event by the grooming procedure. For the grooming parameter we use here $z_{\rm cut} = 0.1$

Grooming Benefits

- No underlying event, why groom?
 - Less affected by lab-frame detector acceptance
 - Mitigate QCD remnant, ISR
 - No theoretically challenging non-global logarithms
- Ungroomed detector-level shows significant difference from particle-level
 - Detector acceptance, efficiencies
- Grooming events brings particle-level and detector-level distributions into much better agreement!



Observables

- After grooming procedure, a subset of particles survives
 - Event shape is calculated with these particles
 - Two event shapes studied here
- Groomed Invariant Mass (GIM) $M_{Gr.}^2 = (\sum p_i^{\mu})^2$

• Groomed 1-Jettiness τ_1^b (analogous to thrust)

$$\tau_{1} = \frac{2}{Q^{2}} \sum_{i \in \text{gr. ent.}} \min(q_{B} \cdot p_{i}, q_{J} \cdot p_{i})$$

$$\tau_{1}^{b} \rightarrow q_{J} = q + xP,$$

$$q_{B} = xP$$



 p_J

 $\mathcal{H}_B ackslash \mathcal{H}_J$

 $= -p_{B}^{\perp}$

Observables





Groomed vs. Ungroomed 1-jettiness



Grooming enables precision measurement!

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Groomed Invariant Mass - Factorization



 $p = (p^+, p^-, p^\perp)$ *n*-collinear: $p_n \sim Q(z_{\text{cut}}, 1, \sqrt{z_{\text{cut}}})$, soft: $p_s \sim Qz_{\text{cut}}(1, 1, 1)$,

region 1: $1 \gg z_{\rm cut} \gg m_{\rm gr.}^2/Q^2$

Jet Direction (Breit $\eta = -\infty$) = \overline{n} -collinear direction Beam Direction (Breit $\eta = -\infty$) = n-collinear direction Soft Radiation (Isotropic) Collinear-soft radiation, wide-angle soft radiation mostly along jet direction collinear-soft: $p_{cs} \sim Q(\lambda, z_{cut}, \sqrt{z_{cut}\lambda})$,

 $\times \left[1 + \mathcal{O}\left(z_{\text{cut}}, \frac{m_{\text{gr.}}}{z_{\text{out}}Q^2}\right) \right], \quad (15)$

 \bar{n} -collinear: $p_{\bar{n}} \sim Q(1, \lambda, \sqrt{\lambda})$,

$$\frac{d\sigma}{dxdQ^2dm_{\rm gr.}^2} = H(Q, y, \mu) S(Qz_{\rm cut}, \mu) \sum_f \mathcal{B}_{f/P}(x, Q^2 z_{\rm cut}, \mu) \int de_{\bar{n}} de_{cs} \, \delta(m_{\rm gr.}^2 - e_{\bar{n}} - e_{cs}) \left[J(e_{\bar{n}}, \mu^2) \right] \mathcal{C}(e_{cs} z_{\rm cut}, \mu^2)$$

In Region 1, shape of distribution should depend only on jet and collinear-soft functions, which are independent of Q

Groomed Invariant Mass - Factorization



 $p = (p^+, p^-, p^\perp)$ *n*-collinear: $p_n \sim Q(z_{\text{cut}}, 1, \sqrt{z_{\text{cut}}})$, soft: $p_s \sim Qz_{\text{cut}}(1, 1, 1)$,

region 1: $1 \gg z_{\rm cut} \gg m_{\rm gr.}^2/Q^2$

Grooming causes only Jet and Collinear-soft radiation to contribute to shape of distribution in the single-jet (low invariant mass) limit! $\begin{array}{ll} \text{collinear-soft:} & p_{cs} \sim Q(\lambda, z_{\text{cut}}, \sqrt{z_{\text{cut}}\lambda}) \ , \\ \\ & \bar{n}\text{-collinear:} & p_{\bar{n}} \sim Q(1, \lambda, \sqrt{\lambda}) \ , \end{array}$

 $\times \left[1 + \mathcal{O}\left(z_{\text{cut}}, \frac{m_{\text{gr.}}}{z_{\text{cut}}O^2}\right)\right], \quad (15)$

$$\frac{d\sigma}{dxdQ^2dm_{\rm gr.}^2} = H(Q, y, \mu) \underbrace{S(Qz_{\rm cut}, \mu)}_{f} \underbrace{\sum_{f} \mathcal{B}_{f/P}(x, Q^2 z_{\rm cut}, \mu)}_{f} \int de_{\bar{n}} de_{cs} \,\,\delta(m_{\rm gr.}^2 - e_{\bar{n}} - e_{cs})}_{Q(e_{\bar{n}}, \mu^2)} \underbrace{\mathcal{C}(e_{cs} z_{\rm cut}, \mu^2)}_{f} \int de_{\bar{n}} de_{cs} \,\,\delta(m_{\rm gr.}^2 - e_{\bar{n}} - e_{cs})}_{Q(e_{\bar{n}}, \mu^2)} \underbrace{\mathcal{C}(e_{cs} z_{\rm cut}, \mu^2)}_{Q(e_{\bar{n}}, \mu^2)} \int de_{\bar{n}} de_{cs} \,\,\delta(m_{\rm gr.}^2 - e_{\bar{n}} - e_{cs})}_{Q(e_{\bar{n}}, \mu^2)} \underbrace{\mathcal{C}(e_{cs} z_{\rm cut}, \mu^2)}_{Q(e_{\bar{n}}, \mu^2)} \int de_{\bar{n}} de_{cs} \,\,\delta(m_{\rm gr.}^2 - e_{\bar{n}} - e_{cs})}_{Q(e_{\bar{n}}, \mu^2)} \underbrace{\mathcal{C}(e_{cs} z_{\rm cut}, \mu^2)}_{Q(e_{\bar{n}}, \mu^2)} \underbrace{\mathcal{C}(e_{\bar{n}}, \mu^2)}_{Q(e_{\bar{n}}, \mu^2)} \underbrace$$

In Region 1, shape of distribution should depend only on jet and collinear-soft functions, which are independent of Q





- Data is corrected for real QED ISR and FSR
- Uncertainty on data is statistical ⊕ systematic
 - Dominated by model uncertainty from bin-by-bin correction
- RAPGAP and DJANGOH
 - Standard H1 MCs
 - Both use LEPTO for matrix elements $O(\alpha_s)$
- DJANGOH:
 - Color dipole model PS + string fragmentation
- RAPGAP:
 - DGLAP PS + string fragmentation

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Results – Groomed 1 Jettiness



- PYTHIA Version 8.3
 - VINCIA Antenna Shower
 - DIRE Dipole shower + multijet merging
- Herwig Version 7.2 (Angular-ordered)
 - NLO \bigoplus PS AO Shower, subtractive matching
 - Merging Dipole shower + multijet merging
- SHERPA Version 2.2.12 (MEPS@NLO)
 - AHADIC++ Cluster Fragmentation
 - Lund String Fragmentation

- Best tail region from SHERPA, RAPGAP
 - Fixed-order, multijets, hard splittings
- Best peak region from DIRE, Herwig Merging
 - Resummation, parton shower, hadronization

 $\min(q_B \cdot p_i, q_J \cdot p_i)$

 $i \in \text{gr. ent}$

Results – Groomed Invariant Mass $M_{Gr.}^2 = (\sum_i p_i^{\mu})^2$



- PYTHIA Version 8.3
 - VINCIA Antenna Shower
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 - AHADIC++ Cluster Fragmentation
 - Lund String Fragmentation

- $Q^{2}_{Min.} = 150 \text{ GeV}^{2}$
- Best high mass region from SHERPA
 - Fixed-order, multijets, hard splittings
- Best low mass region from Herwig, DIRE
 - Resummation, parton shower, hadronization

Results – Groomed Invariant Mass $M_{Gr.}^2 = (\sum_i p_i^{\mu})^2$



- PYTHIA Version 8.3
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- Generally, predictions become less accurate at lower \mathbf{z}_{cut}
 - Less grooming → Less removal of remnant hemisphere radiation
 - Remnant hemisphere is typically less well described by MC models

Comparison to Analytic Prediction

- Analytic SCET
 - From Y. Makris [1]
 - Evaluated at two values of $\Omega_{\rm NP}$
 - Shape function mean
 - No fixed-order calculation yet incorporated
- Agreement improves with increasing $z_{cut,} \Omega_{NP}$
 - Non-perturbative effects are significant!
 - Factorization validity improves to higher z_{cut}

$$rac{d\sigma_{ ext{had.}}}{dxdQ^2dm_{ ext{gr.}}^2} = \int d\epsilon rac{d\sigma}{dxdQ^2dm_{ ext{gr.}}^2} ig(m_{ ext{gr.}}^2 - rac{\epsilon^2}{z_{ ext{cut}}}ig) f_{ ext{mod.}}(\epsilon) \ ,
onumber \ f_{ ext{mod.}}(\epsilon) = N_{ ext{mod.}} rac{4\epsilon}{\Omega^2} \expig(rac{2\epsilon}{\Omega}ig)$$



Groomed Invariant Mass - EIC

- At small invariant masses, individual hadron masses play a large role
- Analytic prediction formulated at small masses, in the region defined by:

 $1 \gg z_{\rm cut} \gg m_{
m gr.}^2/Q^2$

- EIC will have advantages in this region
 - Hadron ID, high statistics
 - More differential measurement possible
 - New theory tools+data for high-precision studies of NP sector
- Small angles also important
 - Good angular resolution needed



Lessons for EIC – Breit Frame

- Good reconstruction of event kinematics is vital for performing measurements in the Breit frame
- Breit frame is a powerful tool for jet-related studies, but comes with additional uncertainty from boost reconstruction that needs to be under control
- QED ISR/FSR can have devastating effects on Breit frame measurements if not properly handled
 - These photons are typically quite energetic and at midrapidity in the Breit frame
 - Easy to confuse for interesting hadronic final state effects!



Lessons for EIC – E - P_z

- I Σ method first described by Bernardi & Bassler in 1994
 - hep-ex/9412004
- For this analysis, the I Σ method yielded the best boost reconstruction and thus the highest purity for the measurement
- This method clearly relies very heavily on the measurement of $\boldsymbol{\Sigma}$

$$\Sigma = \sum_{h} (E_h - p_{z,h})$$

- E-P_z maximized by particles in electron-going (-z) direction, large for barrel, small for forward-going
 - Important to reconstruct backward + barrel momenta well
 - At low-x, IS method is similar to electron method in resolution, hadrons go mostly backward

$$\Sigma = \sum_{h} (E_h - p_{z,h})$$

$$E_{I\Sigma}^{e'} = \frac{\Sigma_{HFS} + E_{e'}(1 - \cos \theta_{e'})}{2}$$

$$x_{I\Sigma} = \frac{E_{e'}}{E_p} \frac{\cos^2 \theta/2}{y_{\Sigma}}$$

$$y_{I\Sigma} = y_{\Sigma} = \frac{\Sigma}{\Sigma + E(1 - \cos \theta)}$$

$$Q_{I\Sigma}^2 = \frac{E^2 \sin^2 \theta}{1 - y_{\Sigma}}$$

Conclusion

- H1 has performed the first measurement of groomed event shapes in DIS
 - H1prelim-22-033
 - See also the ungroomed 1-jettiness preliminary: H1prelim-21-032
- Data has been compared to a variety of MC predictions from SHERPA*, PYTHIA, HERWIG, DJANGOH, RAPGAP, as well as analytic predictions from SCET
 - Signifies that DIS MC models could use improvement, especially with EIC fast approaching
 - HERA data will necessarily play an important role in this initiative!
- Good Breit frame reconstruction enables a wide range of QCD studies
 - Jets, TMDs, spin, hadronic physics, things yet unstudied → maximize capability for generic tools

*SHERPA authors already undertaking a DIS tuning campaign utilizing this data!

Bibliography

[1] - Revisiting the role of grooming in DIS, Y. Makris - arXiv:2101.02708

[2] – Groomed and energy-energy-correlation event shapes at EIC, Y. Makris - LBL Seminar: Oct. 2020

[3] – PYTHIA 8.3 Manual - arXiv:2203.11601

[4] – SHERPA 2.2.12 Manual - sherpa.hepforge.org/doc/SHERPA-MC-2.2.12.html

[5] – herwig.hepforge.org

Backup

H1 Detector

- HERA
 - World's only high energy electron-proton collider

 $E_e = 27.6 \, \, ext{GeV}, E_p = 920 \, \, ext{GeV} \
ightarrow \sqrt{s} = 319 \, \, ext{GeV}$

- 352 pb⁻¹ collected in HERA-II run period from 2003-2007
- H1 Experiment
 - Hermetic detector with asymmetric design
 - Drift chamber + silicon tracking
 - High-resolution LAr calorimeter
 - Trigger on high-energy hadronic or EM LAr cluster
 - > 99% efficient for y < 0.7



H1 LAr Calorimeter Specifications

Electromagnetic part	Hadronic part
$10 \text{ to } 100 \text{ cm}^2$	$50 \text{ to } 2000 \text{ cm}^2$
20 to 30 X_0 (30784)	4.7 to 7 λ_{abs} (13568)
$\approx 11\%/\sqrt{E_e} \oplus 1\%$	$\approx 50\%/\sqrt{E_h} \oplus 2\%$

Lessons for EIC - QED

- ISR typically unmeasured in detector
 - For observables where all final state particles contribute, radiative MC can give significantly different results if ISR photon is included in final state
 - E-P_z cut helps
 - Having radiative and non-radiative MC
- Typically want to compare data (radiative) to QCD theory (non-radiative)
 - If you don't measure the photon, only have to correct for lower e_{beam} energy at hard vertex



Lessons for EIC - QED

- FSR handled by recombining particles within a lab-frame cone of R = 0.2 of the scattered electron with the scattered election
 - FSR photon is very close to scattered election, typically within calorimeter position resolution
 - FSR photon conversions can fake as HFS tracks



- Cone cut removes genuine HFS particle only 0.75% of the time, typically low energy
 - Momentum balance disfavors HFS particles being near election

Lessons for EIC – Kine Reco

• At HERA, electron method was made difficult in kinematic regions where the electron was low energy (high y) and/or near to HFS particles (low x)

• These regions are vital to EIC physics

- At EIC, PID detectors should make purity of scattered electron a bit better
 - Low mass detectors will also improve the feasibility of the electron method
- However, electron method will always suffer from QED radiation





Figure 2: Comparison x_{method}/x at low Q^2 ($Q^2 > 7 \ GeV^2$) for the Σ , mixed, DA and e methods. From top to bottom, each row represent a bin in y: very high (0.5-0.8), high (0.2-0.5), medium (0.1-0.2), low (0.05-0.1), very low (0.01-0.05).

- Data is corrected for real QED ISR and FSR
- Uncertainty on data is statistical ⊕ systematic
- RAPGAP and DJANGOH
 - Standard H1 MCs
 - Both use LEPTO for matrix elements $O(\alpha_S)$
- DJANGOH:
 - Color dipole model for parton shower + string fragmentation
- RAPGAP:
 - DGLAP parton shower + string fragmentation



- SHERPA
 - Version 2.2.12
 - MEPS@NLO
- AHADIC++:
 - SHERPA native cluster hadronization model
- Lund:
 - Lund string model from PYTHIA
- Both models provide good description of fixed-order region



- Herwig
 - Version 7.2.2
- NLO \oplus PS:
 - Herwig internal implementation of MC@NLO via Matchbox
- Merging:
 - Dipole shower with multijet merging



- PYTHIA
 - Version 8.3
 - No external matrix elements
- DIRE:
 - Dipole resummation
 - Excellent description in resummation region
- VINCIA:
 - Antenna shower





Figure 4. Pseudorapidity (top panel) and momentum fraction z_{jet} (bottom panel) of jets clustered with anti- $k_T(LI)$, anti- $k_T(LI)$ and Centauro algorithms in the Breit frame. Here \mathcal{N} is an overall normalization constant chosen to improve readability and is the same for all curves in a graph.







Centauro

- Jet algorithm with asymmetric clustering measure
 - Treat current hemisphere and beam hemisphere differently
- Typical longitudinally-invariant jet algorithms cluster in (rapidity, azimuthal angle) space and fail to capture the born-level configuration in the Breit frame
 - Particles close to struck-parton direction have divergent rapidity, and therefore divergent distance between each other!
 - Makes study of single-jet Born level configuration impossible!
- Use spherically invariant clustering (polar angle, azimuthal angle) in the struck-parton direction and longitudinally invariant in beam direction
- Tends to create one hard jet in struck-parton direction and many weak single particle jets in beam direction, which can easily be filtered away









Figure 8.9: Pseudorapidity regions in the H1 detector.



z_{cut}	0.05	0.1	0.2
Pythia8.3	0.31%	1.3%	6.3%
Pythia+Vincia	0.52%	1.7%	6.9%
Pythia+DIRE	0.47%	1.2%	5.6%
SHERPA+AHADIC++	0.03%	0.31%	3.6%
SHERPA+LUND	0.09%	0.59%	4.9%
HERWIG	0.038%	0.36%	3.6%
HERWIG+Merging	0.04%	0.39%	3.6%
HERWIG+MC@NLO	0.04%	0.39%	3.8%
DJANGO (Gen.)	0.09%	0.5%	4.0%
RAPGAP (Gen.)	0.07%	0.4%	3.7%
DJANGO (Det.)	1.0%	2.3%	7.8%
RAPGAP (Det.)	0.9%	2.2%	7.6%

 Table 1: Percentage of events that fail grooming. Rapgap and Djangoh are listed for both detector and generator level.