

K. Wichmann @DIS22
on behalf of H1 and ZEUS Collaborations

HERAPDF2.0 Jets and estimation of $\alpha_s(M_Z)$ @ NNLO

EPJ C 82, 243 (2022) arXiv:2112.01120

Santiago de Compostela

467 hr
2.266 km

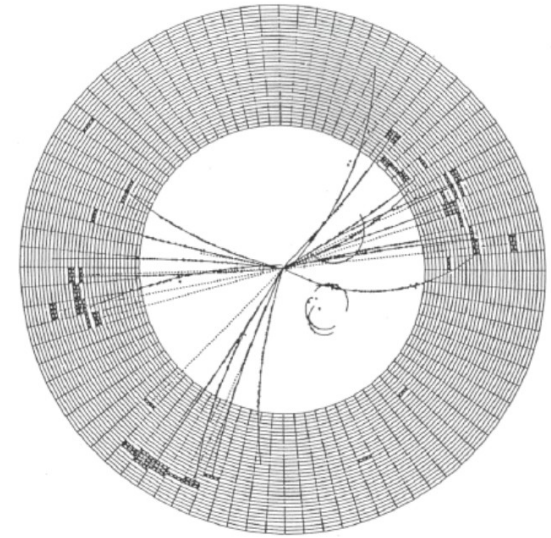


Jets produced @ DESY for over 40 years

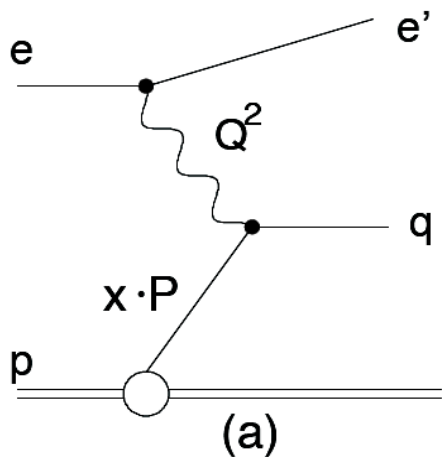
At HERA direct information on gluon and $\alpha_s(M_Z)$ comes from jet production

→ Possible simultaneous determination of parton densities and $\alpha_s(M_Z)$

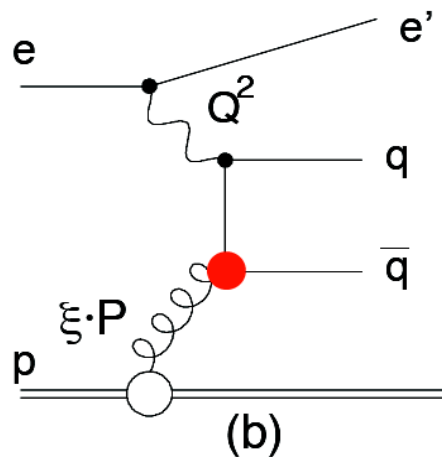
Jets at PETRA, 1979



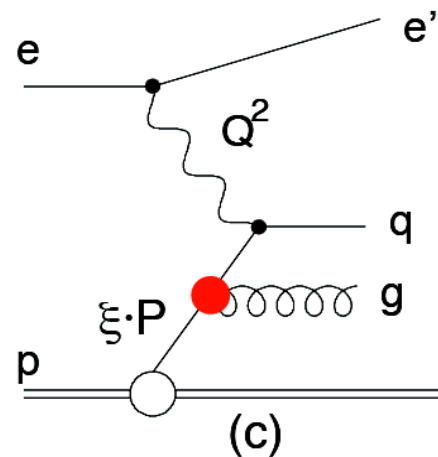
Jets at HERA



elweak coupling



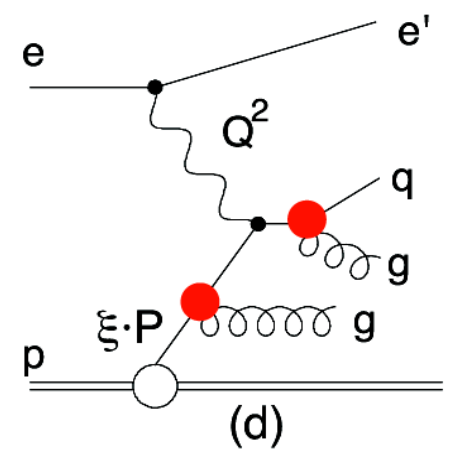
$\propto \alpha_s$



$\propto \alpha_s$

dijets

*** SUMS (GeV) *** PTOT 35.788 PTRANS 29.964 PLONG 15.788 CHARGE -2
TOTAL CLUSTER ENERGY 15.169 PHOTON ENERGY 4.693 NR OF PHOTONS 11

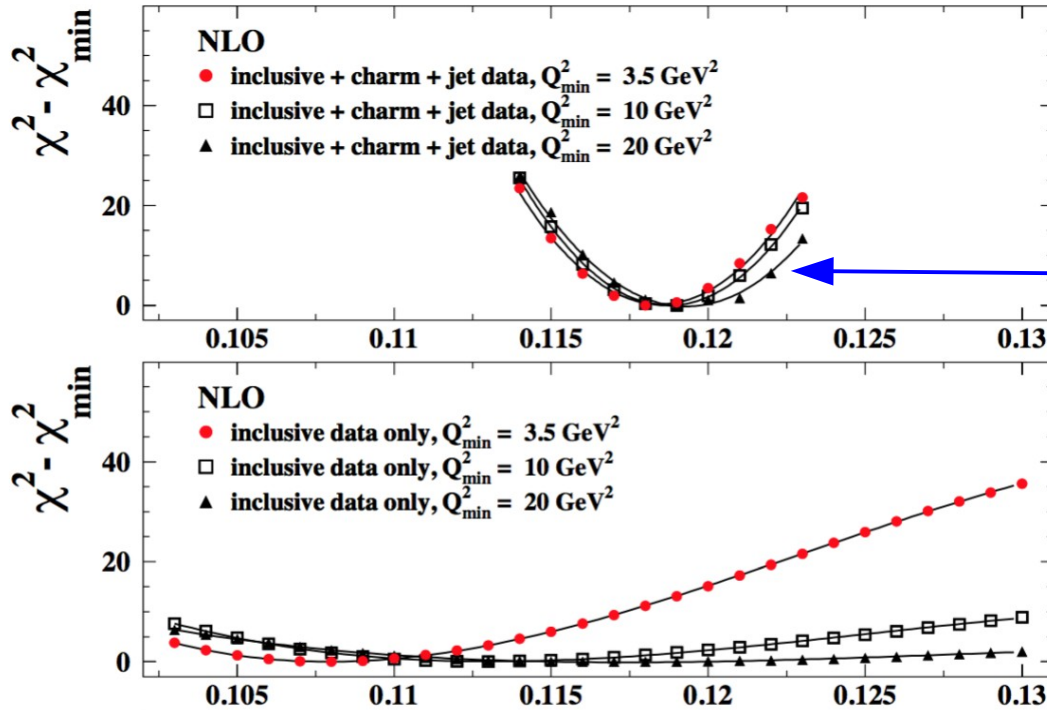


$\propto \alpha_s^2$

trijets

Why study jets @ HERA?

H1 and ZEUS



- HERA inclusive data carry little information on $\alpha_s(M_Z)$
- Jet data sensitive to $\alpha_s(M_Z)$



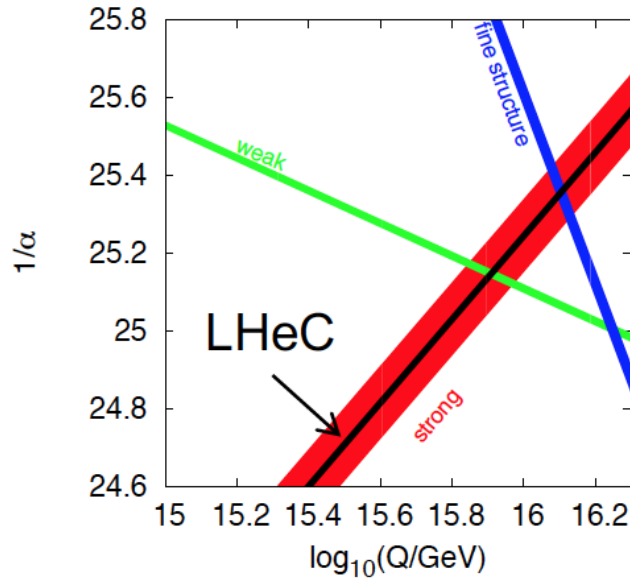
New NNLO calculations for HERA ep jet production available now

- Implemented in FastNLO and APPELGRID → fast cross section calculation possible

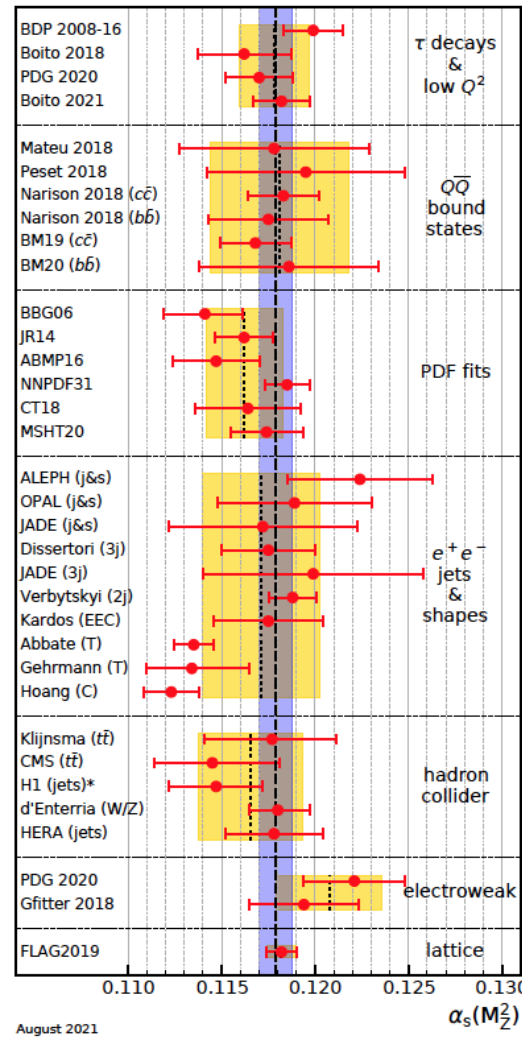
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→ Possible simultaneous determination of PDFs and $\alpha_s(M_Z)$ at NNLO

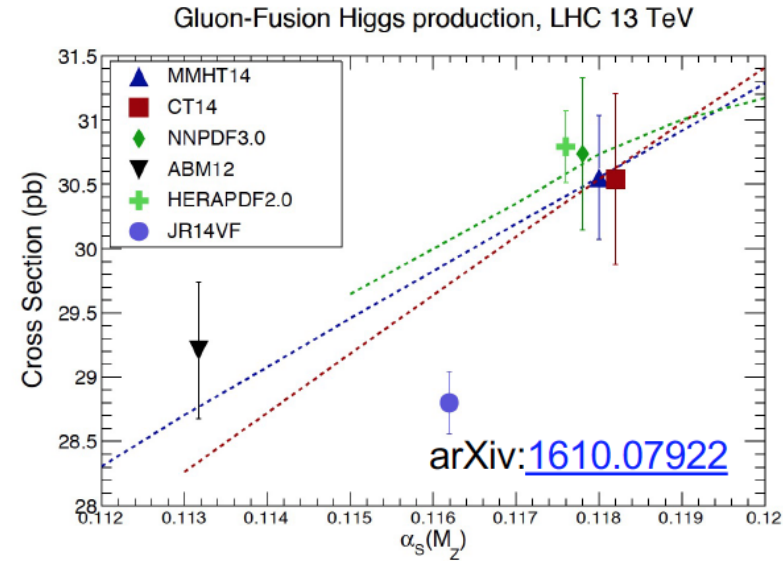
motivation and impact at LHC



- α_s is least known coupling constant; needed to constrain GUT scenarios; cross section predictions, including Higgs; ...



PDG21: $\alpha_s = 0.1175 \pm 0.0010$ (w/o lattice)



- PDFs and/or α_s limit: precision SM and Higgs measurements, BSM searches, ...

- what is true α_s central value and uncertainty? new precise determinations have important role to play

HERAPDF2.0 parameterisation

$$xf(x) = Ax^B(1-x)^C(1+Dx+Ex^2)$$

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g},$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2),$$

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x),$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$$

- Additional constrains

- A_{u_v}, A_{d_v}, A_g : constrained by the quark-number sum rules and momentum sum rule

- $B_{\bar{U}} = B_{\bar{D}}$:

- $x\bar{s} = f_s x\bar{D}$ at starting scale, $f_s = 0.4$

Updates in the procedure

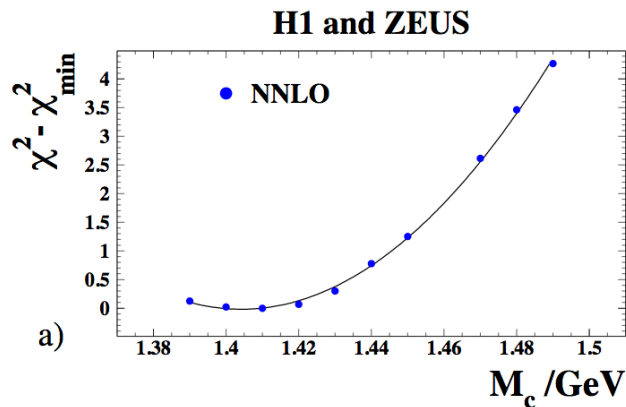
- scale choice changes:
- factorisation: $\mu_F^2 = (Q^2 + p_t^2)$
- cf. $\mu_F^2 = Q^2$ in previous NLO analysis; updated since not a good choice for low Q^2 jet data; change makes almost no difference for high Q^2 jets
- renormalisation: $\mu_R^2 = (Q^2 + p_t^2)$
- cf. $\mu_R^2 = (Q^2 + p_t^2)/2$ in previous NLO analysis
- NNLO fit with $\mu_R^2 = (Q^2 + p_t^2)$ gives $\Delta X^2 = -15$ cf. $\mu_R^2 = (Q^2 + p_t^2)/2$ and vice versa for NLO fit
- scale uncertainties treated as completely correlated between bins and datasets

† p_t denotes p_t^{jet} in the case of inclusive jet cross sections and $\langle p_t \rangle$ for dijets

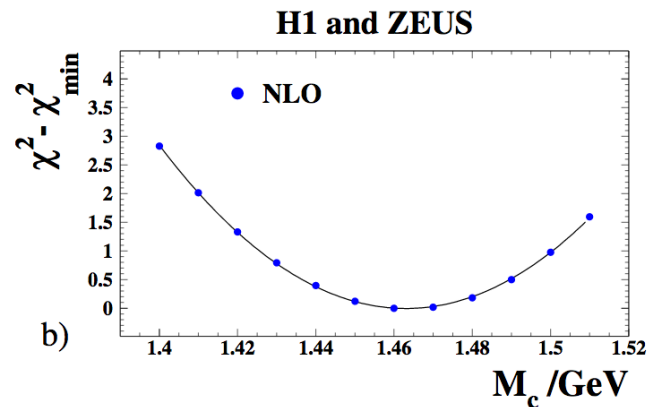
- improved treatment of hadronisation uncertainties; NOW included together with exp. systematics; treated as $1/2$ correlated, $1/2$ uncorrelated between bins and datasets
- (small) uncertainties on theory predictions included

Estimation of charm & beauty masses

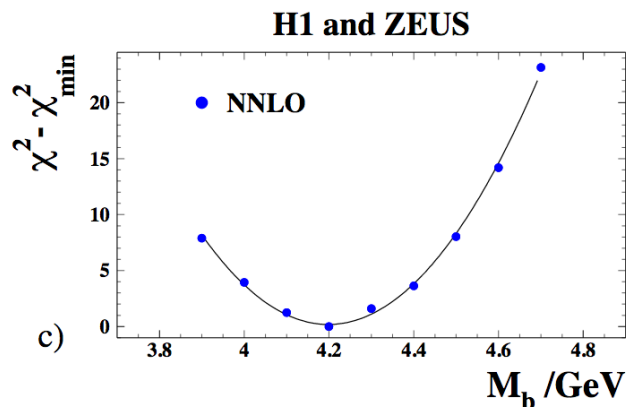
- new HERA combined charm and beauty data: EPJ C78 (2018), 473
 - updated estimation of M_c and M_b
 - Heavy Quark (HQ) coefficient functions evaluated using Thorne-Roberts Optimised Variable Flavour Number Scheme



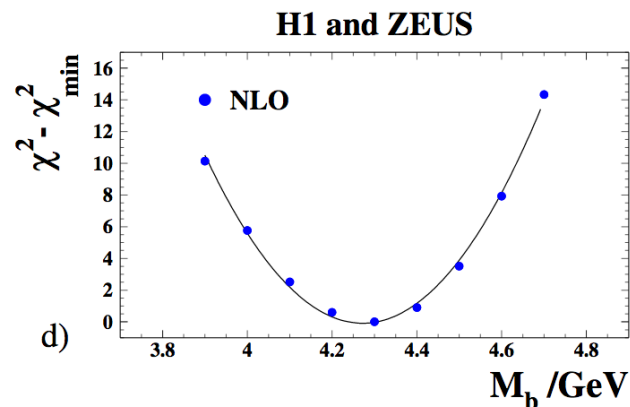
$$M_c = 1.41 \pm 0.04$$



$$M_c = 1.46 \pm 0.04$$



$$M_b = 4.2 \pm 0.1$$



$$M_b = 4.2 \pm 0.1$$

HERA jet data used in PDF fit

- Inclusive jets and dijets included
- Trijets from HERAPDF2Jets NLO excluded → no NNLO predictions
- **H1 low Q^2 data** added - particularly sensitive to $\alpha_s(M_Z)$
- Some data points excluded due theory limitations
 - Data at low scale $\mu = (p_{t2} + Q_2) < 10 \text{ GeV}$ → scale variations are large (~25% NLO and ~10% NNLO)
 - 6 ZEUS Dijet data points at low p_{t2} for which predictions are not truly NNLO

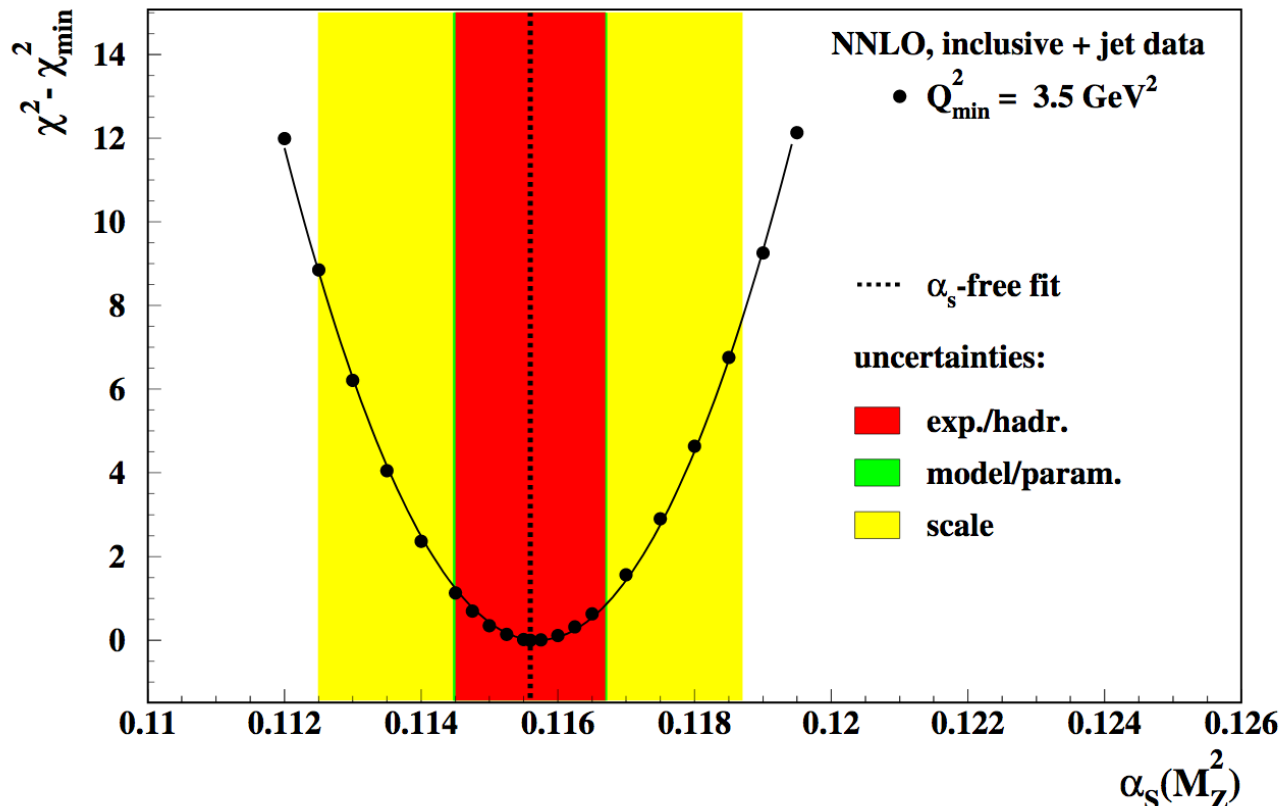
Data set	taken		$Q^2 [\text{GeV}^2]$ range		\mathcal{L} pb ⁻¹	e^+/e^-	\sqrt{s} GeV	Norma- lised	All points	Used points
	from	to	from	to						
H1 HERA I normalised jets	1999	2000	150	15000	65.4	e^+p	319	yes	24	24
H1 HERA I jets at low Q^2	1999	2000	5	100	43.5	e^+p	319	no	28	20
H1 normalised inclusive jets at high Q^2	2003	2007	150	15000	351	e^+p/e^-p	319	yes	30	30
H1 normalised dijets at high Q^2	2003	2007	150	15000	351	e^+p/e^-p	319	yes	24	24
H1 normalised inclusive jets at low Q^2	2005	2007	5.5	80	290	e^+p/e^-p	319	yes	48	37
H1 normalised dijets at low Q^2	2005	2007	5.5	80	290	e^+p/e^-p	319	yes	48	37
ZEUS inclusive jets	1996	1997	125	10000	38.6	e^+p	301	no	30	30
ZEUS dijets	1998-2000 &	2004-2007	125	20000	374	e^+p/e^-p	318	no	22	16

- Possibilities for PDF fit with jet data
 - With fixed $\alpha_s(M_Z)$
 - With free $\alpha_s(M_Z)$ or doing $\alpha_s(M_Z)$ scan → $\alpha_s(M_Z)$ value

α_s @ NNLO from HERA jets

- $\alpha_s(M_Z)$ determined with experimental, model, param. and hadr. uncertainties
- In fits with free $\alpha_s(M_Z)$ **scale uncertainty** important

H1 and ZEUS



$$\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 \text{ (exp)} \begin{matrix} +0.0001 \\ -0.0002 \end{matrix} \text{ (model + parameterisation)}$$

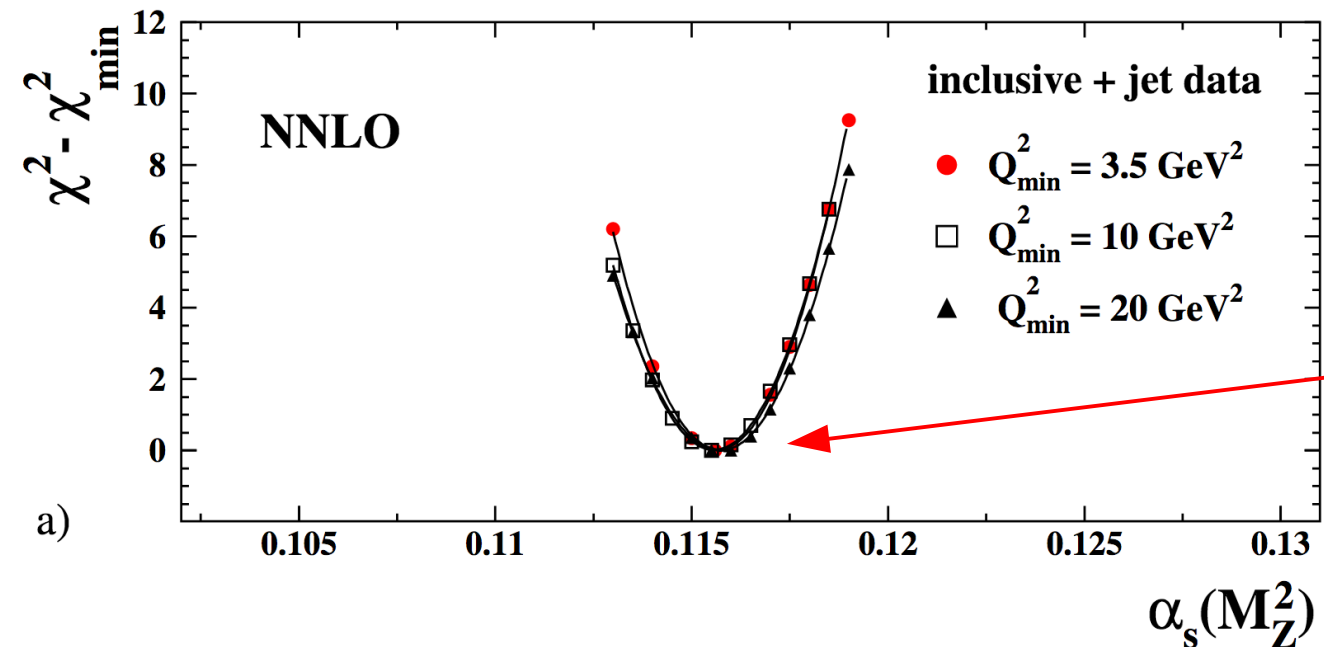
$$\pm 0.0029 \text{ (scale)}$$

Checking robustness of results

- HERA data at low x and Q^2 may be subject to need for $\ln(1/x)$ resummation or higher twist effects (eg arXiv:1506.06042, 1710.05935)

→ χ^2 scans performed with harder Q^2 cuts

H1 and ZEUS



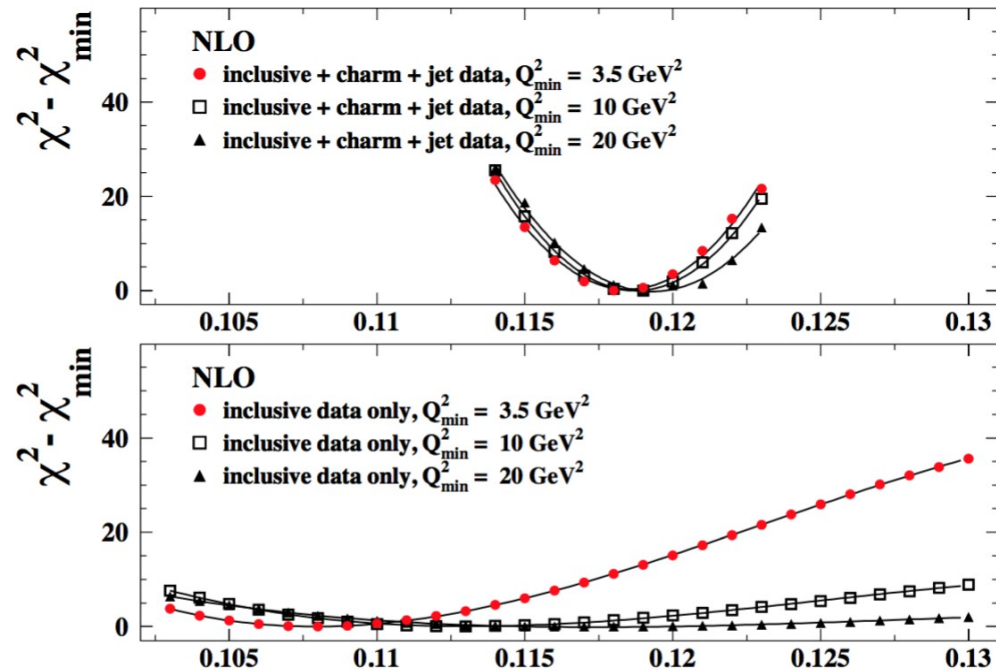
Q^2 cuts do not result in any significant change to the value of $\alpha_s(M_Z)$

- Alternative parameterisations checked
 - No negative gluon term and no NG but additional Dg parameter
 - both give the same result
 - consistent with nominal

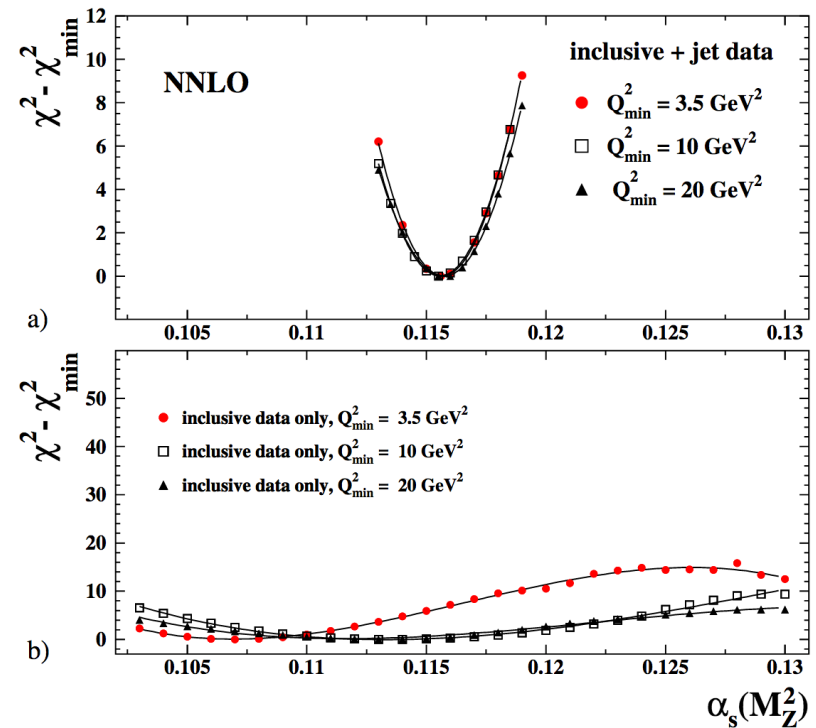
$$\alpha_s(M_Z^2) = 0.1151 \pm 0.0010 \text{ (exp)}$$

Completing NLO picture

H1 and ZEUS



H1 and ZEUS



- Similar behavior and level of precision at NLO and NNLO
- However direct comparison of 2015 and 2022 results not possible
→ different scale choice and slightly different jet data sets
- After unifying (details in backup)

$\alpha_s(M_Z) = 0.1186 \pm 0.0014 \text{ (exp) NLO}$

$\alpha_s(M_Z) = 0.1144 \pm 0.0013 \text{ (exp) NNLO}$

Comparison to other HERAPDF2.0 fits

- For previous NLO results scale uncertainty applied as 50% correlated and 50% uncorrelated between bins and data sets (due to inclusion of HQ and trijet data)
- Using the previous procedure at NNLO:

NNLO

$$\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 \text{ (exp)} \begin{matrix} +0.0001 \\ -0.0002 \end{matrix} \text{ (model + parameterisation)}$$

$$\pm 0.0022$$

HERAPDF2.0Jets NLO

$$\alpha_s(M_Z^2) = 0.1183 \pm 0.0009 \text{ (exp)} \pm 0.0005 \text{ (model/parameterisation)} \\ \pm 0.0012 \text{ (hadronisation)} \begin{matrix} +0.0037 \\ -0.0030 \end{matrix} \text{ (scale)} .$$

Scale uncertainties reduced

→ as expected for NNLO calculations

comparison to other HERA DIS results

1. **H1** NNLO jet study using fixed PDFs, includes H1 inclusive-jet and di-jet:

$$\text{H1 jets } \mu > 2m_b \quad 0.1170 \quad (9)_{\text{exp}} \quad (7)_{\text{had}} \quad (5)_{\text{PDF}} \quad (4)_{\text{PDF}\alpha_s} \quad (2)_{\text{PDFset}} \quad (38)_{\text{scale}}$$

with similar breakup of uncertainties and similar μ , new HERA result:

$$\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 (\text{exp+had+PDF}) \quad {}^{+0.0001}_{-0.0002} (\text{model + parameterisation}) \quad \pm 0.0029 (\text{scale})$$

H1 also provided a **PDF+ α_s** fit to H1 inclusive and jet data

$$0.1147 \quad (11)_{\text{exp,NP,PDF}} \quad (2)_{\text{mod}} \quad (3)_{\text{par}} \quad (23)_{\text{scale}}$$

analysis required $Q^2 > 10\text{GeV}^2$; NEW HERA result re-evaluated with this cut (rather than $>3.5\text{GeV}^2$), is:

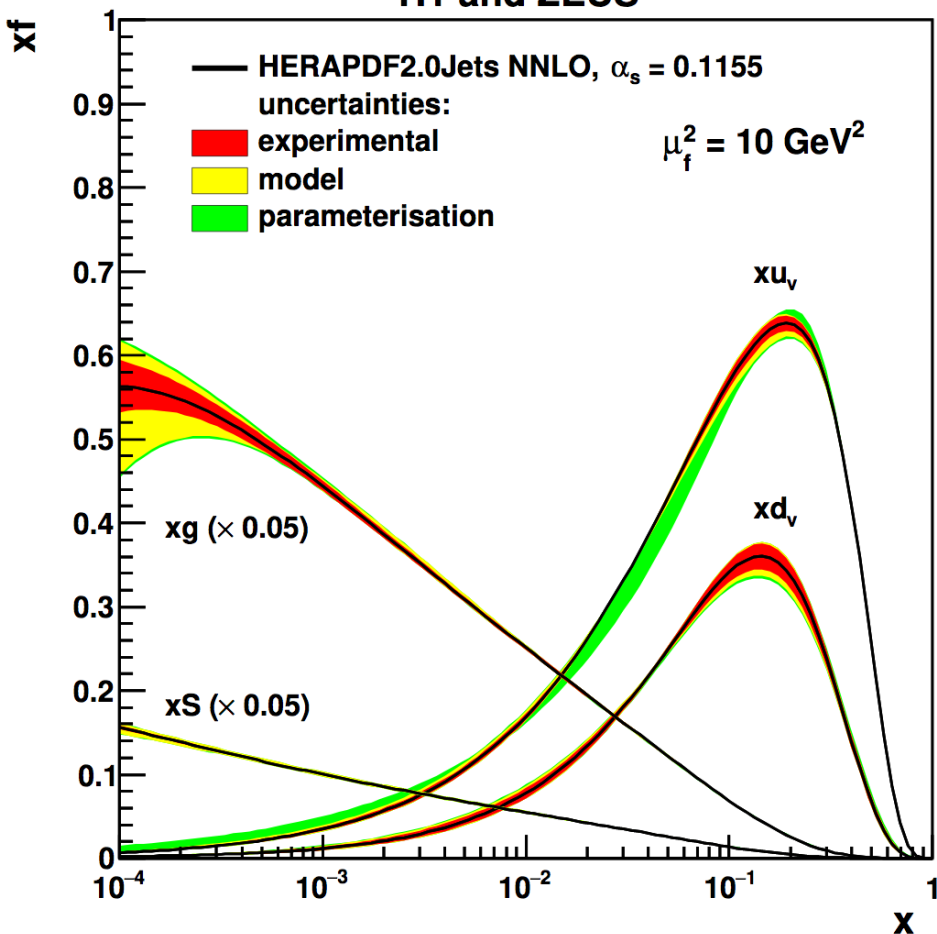
$$\alpha_s(M_Z^2) = \boxed{0.1156} \pm 0.0011 (\text{exp}) \pm 0.0002 (\text{model + parameterisation}) \pm \boxed{0.0021} (\text{scale})$$

2. **NNLOJet+APPLfast** using fixed PDFs, includes H1+ZEUS inclusive-jet:

$$\text{HERA inclusive jets } \mu > 2m_b \quad 0.1171 \quad (9)_{\text{exp}} \quad (5)_{\text{had}} \quad (4)_{\text{PDF}} \quad (3)_{\text{PDF}\alpha_s} \quad (2)_{\text{PDFset}} \quad (33)_{\text{scale}}$$

Fit with fixed $\alpha_s = 0.1155$

H1 and ZEUS



Experimental uncertainties:

- Hessian method
- Conventional $\Delta\chi^2 = 1 \rightarrow 68\% \text{ CL}$

Parameter	Central value	Downwards variation	Upwards variation
Q_{\min}^2 [GeV ²]	3.5	2.5	5.0
f_s	0.4	0.3	0.5
M_c [GeV]	1.41	1.37*	1.45
M_b [GeV]	4.20	4.10	4.30
μ_{f0}^2 [GeV ²]	1.9	1.6	2.2*

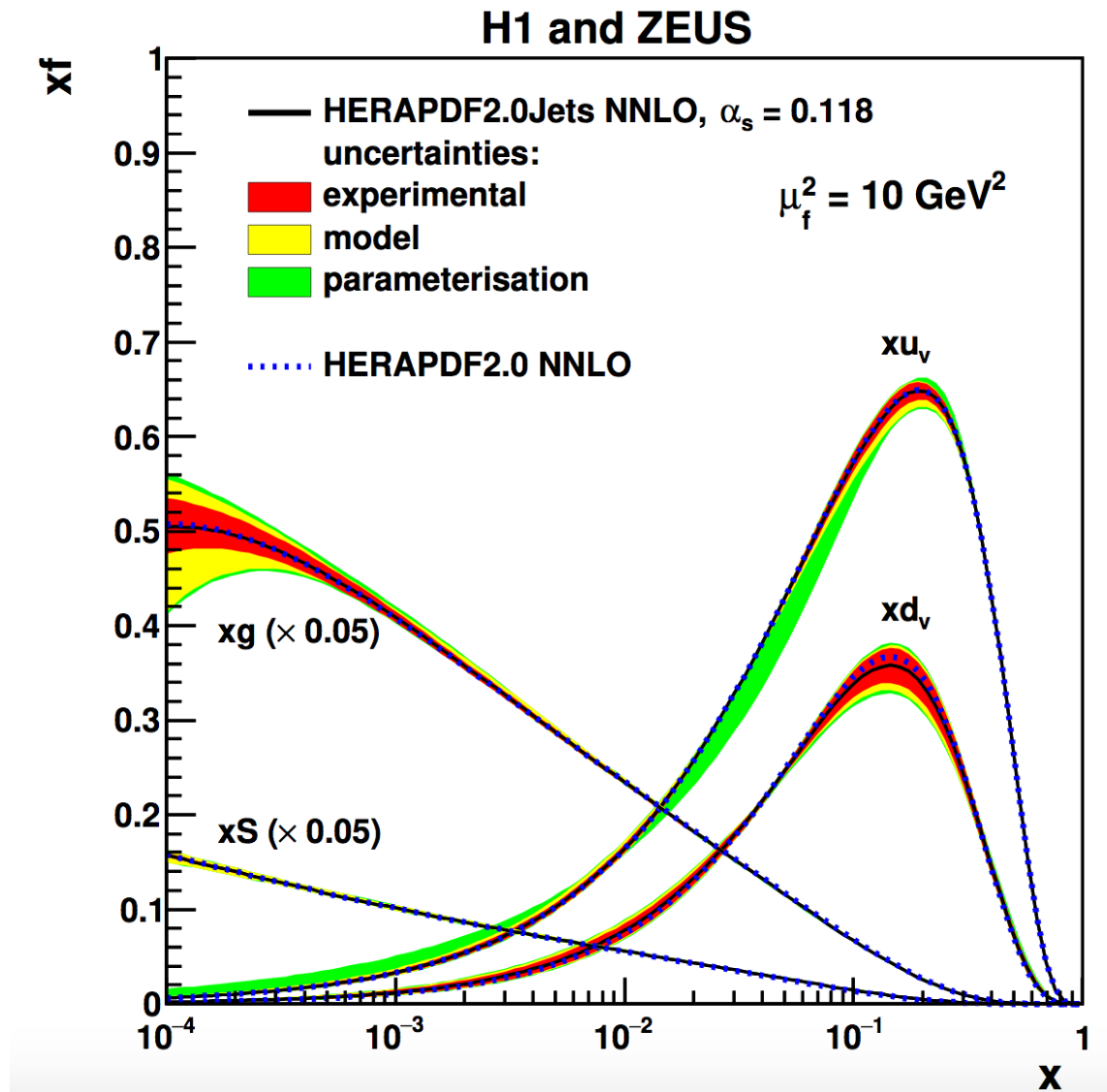
Parametrisation uncertainties
- largest deviation

Model uncertainties
- all variations added in quadrature

Adding D and E parameters to each PDF

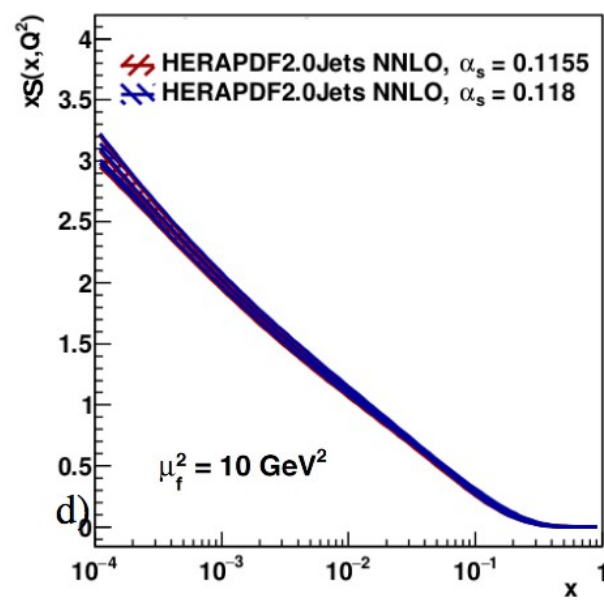
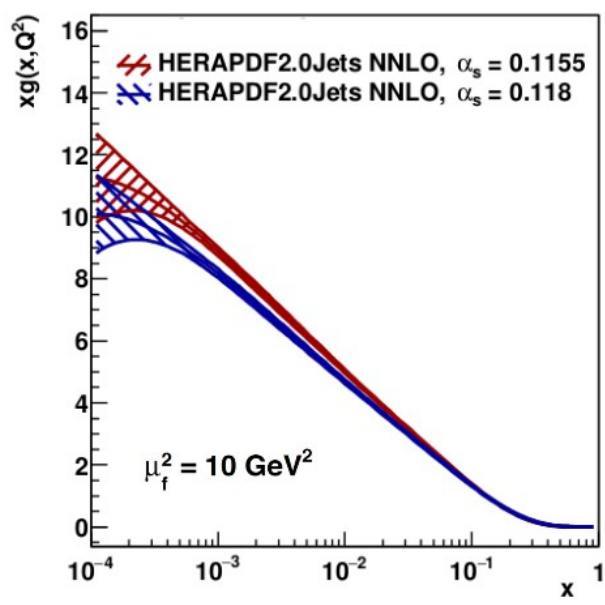
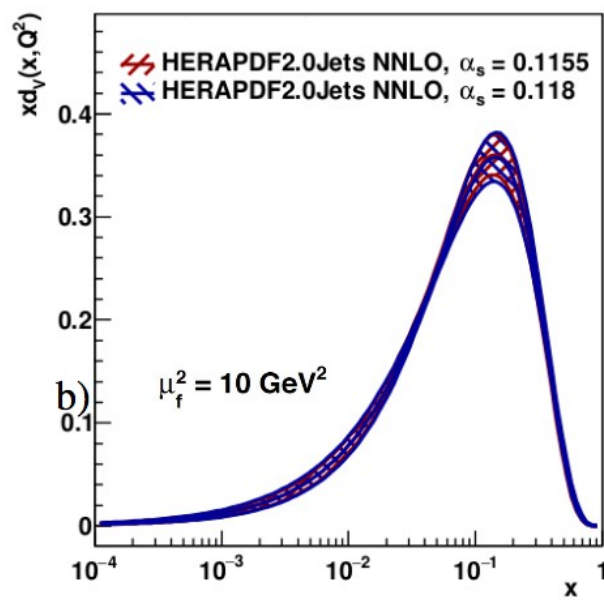
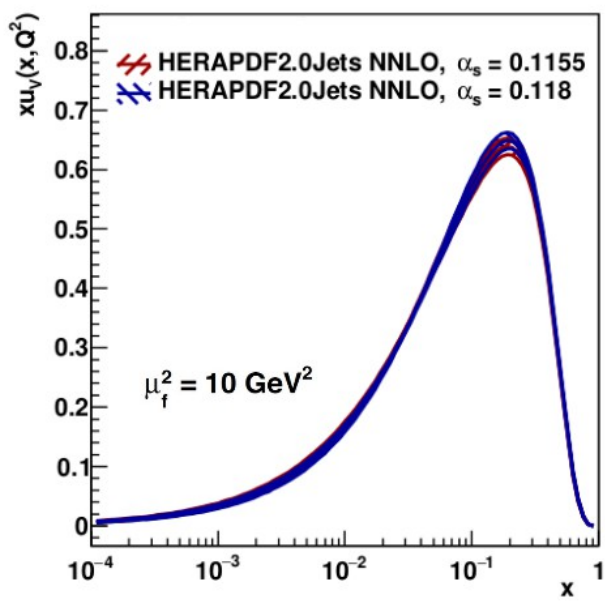
Fit with fixed $\alpha_s = 0.118$

How does it compare to HERAPDF2.0? **Well!**

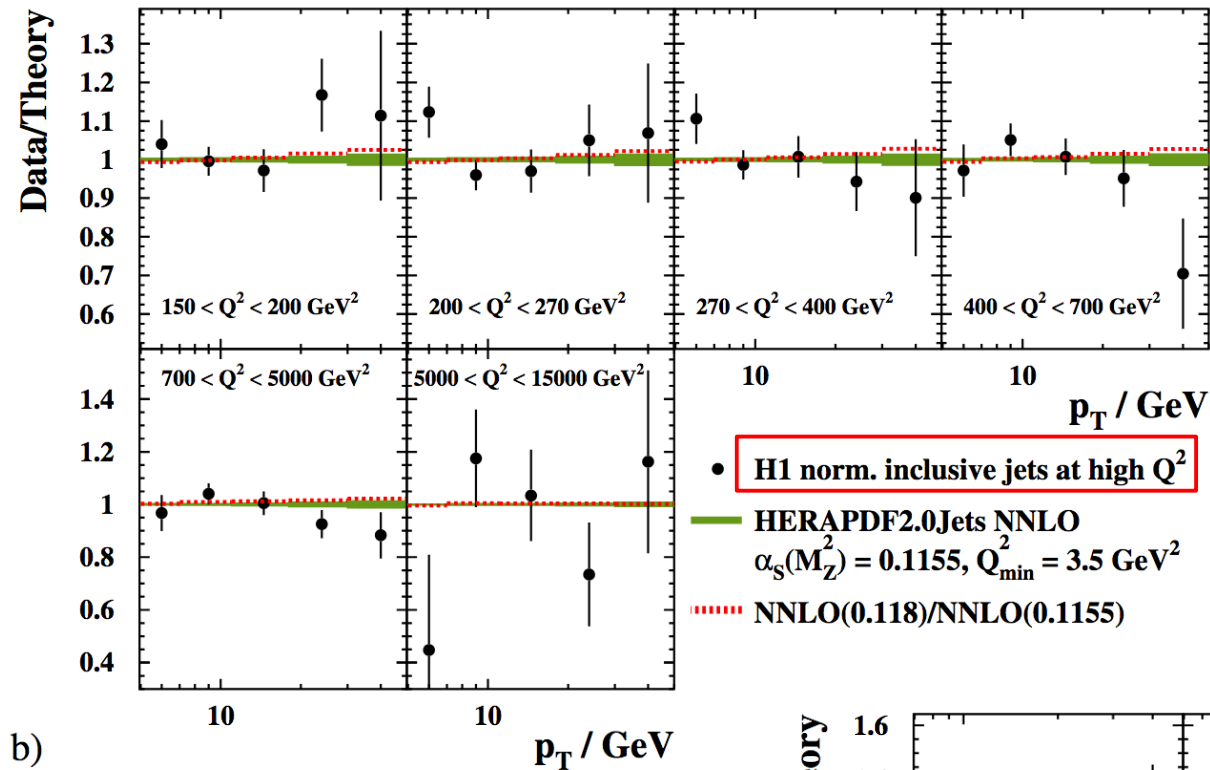


... and how it compares to $\alpha_s = 0.1155$

H1 and ZEUS



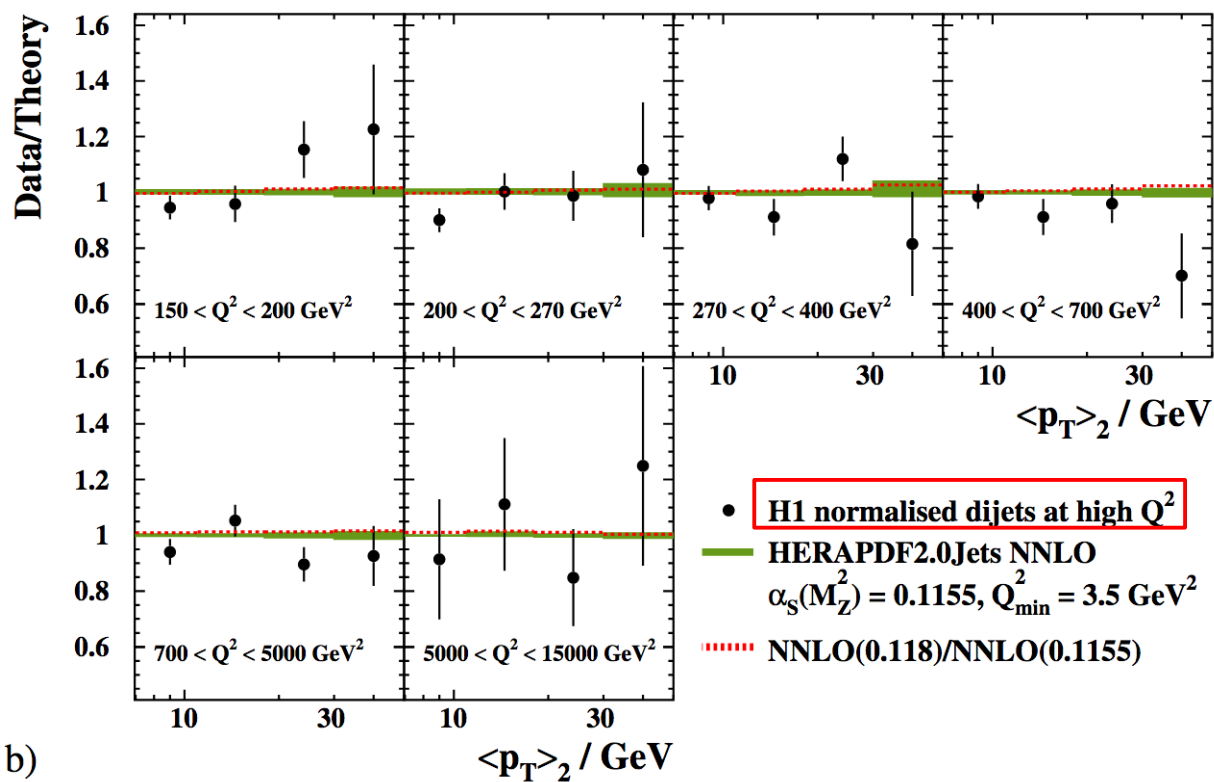
H1 and ZEUS



Comparison of theory predictions to H1 HERA II normalised jets @ high Q^2
 → good agreement for all data used in PDF fits

b)

H1 and ZEUS

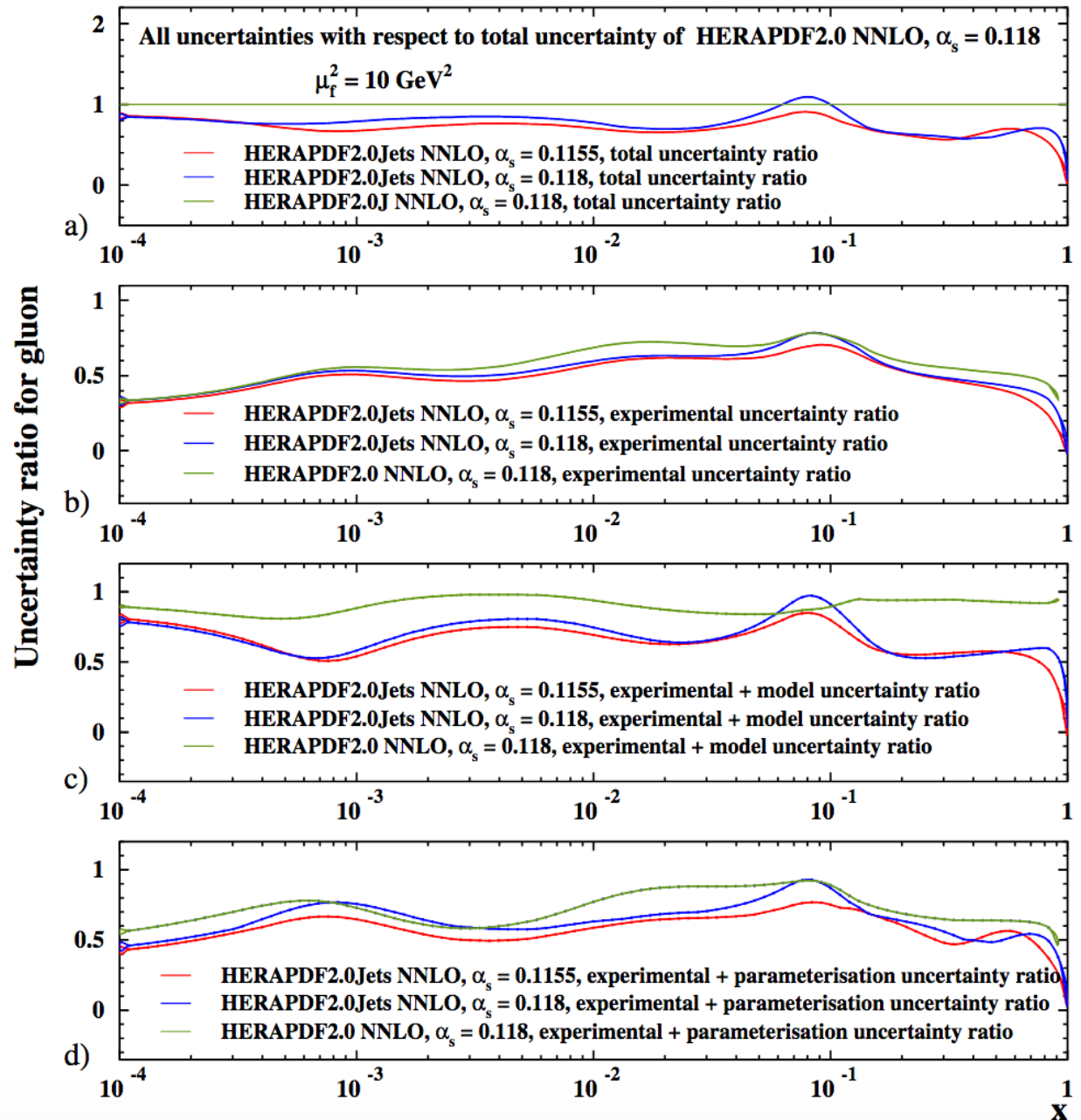


b)

Uncertainties

- Reduction of low- x gluon ($x < 10^{-3}$) uncertainties due to reduced model/param uncertainties in variations of M_c and μ_f^2
- Reduction of high- x gluon ($x > 10^{-3}$) uncertainties due to reduced model/param/exp uncertainties
- The same for other scales

H1 and ZEUS



HERAPDF2 el camino completed!



- HERAPDF2.0 family completed
→ NNLO fit including jet data performed
- Two new PDF sets
→ HERAPDF2.0Jets NNLO $\alpha_s(M_Z) = 0.118$ → PDG
→ HERAPDF2.0Jets NNLO $\alpha_s(M_Z) = 0.1155$ → value favoured by our fit
- Jet data allow us to constrain $\alpha_s(M_Z)$

$$\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 \text{ (exp)} \begin{matrix} +0.0001 \\ -0.0002 \end{matrix} \text{ (model + parameterisation)} \pm 0.0029 \text{ (scale)}$$

- Comparing to NLO at the same footing

NNLO $\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 \text{ (exp)} \begin{matrix} +0.0001 \\ -0.0002 \end{matrix} \text{ (model + parameterisation)} \pm 0.0022$

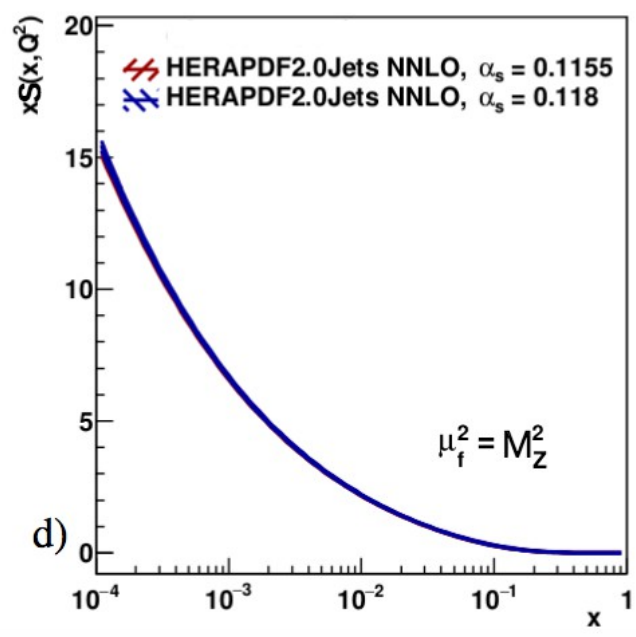
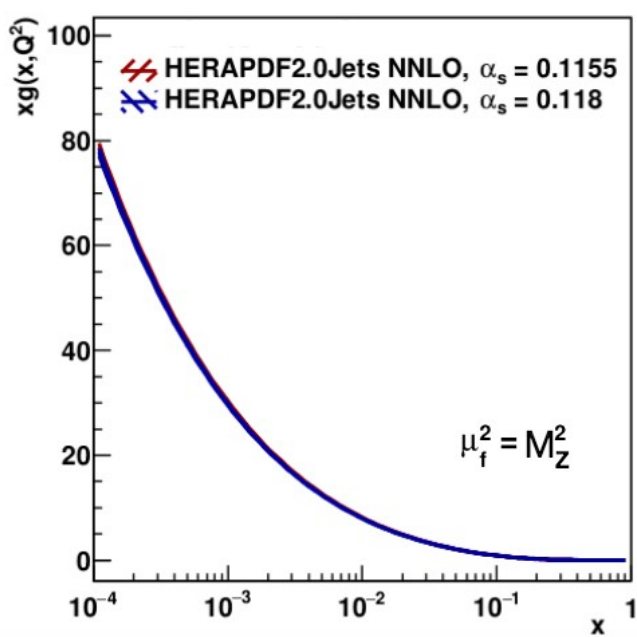
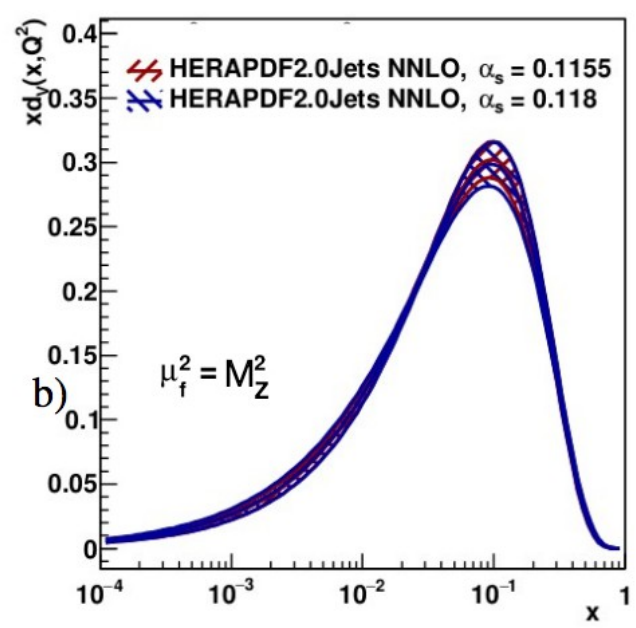
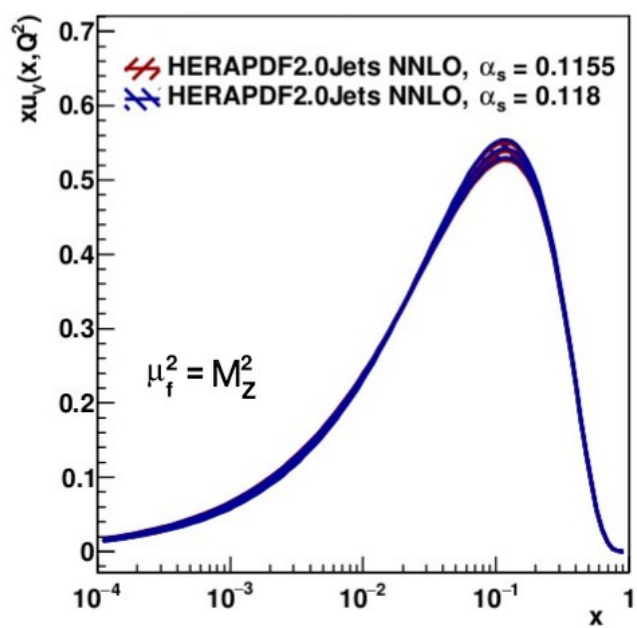
NLO $\alpha_s(M_Z^2) = 0.1183 \pm 0.0009 \text{ (exp)} \pm 0.0005 \text{ (model/parameterisation)} \pm 0.0012 \text{ (hadronisation)} \begin{matrix} +0.0037 \\ -0.0030 \end{matrix} \text{ (scale)}$

Systematic shift downwards at NNLO and reduction of scale uncertainty

Additional slides

... and how it compares to $\alpha_s = 0.1155$

H1 and ZEUS



Some remarks on NLO to NNLO comparison- (not in the paper)

Our present NNLO result using $\frac{1}{2}$ correlated and $\frac{1}{2}$ uncorrelated scale uncertainty

$$\alpha_s(M_Z) = 0.1156 \pm 0.0011(\text{exp})^{+0.0001}_{-0.0002}(\text{model+parametrisation}) \pm 0.0022(\text{scale})$$

where “exp” denotes the experimental uncertainty which is taken as the fit uncertainty, including the contribution from hadronisation uncertainties.

Maybe compared with the NLO result

$$\alpha_s(M_Z) = 0.1183 \pm 0.0008(\text{exp}) \pm 0.0012(\text{had})^{+0.0003}_{-0.0005}(\text{mod/param})^{+0.0037}_{-0.003}(\text{scale})$$

BUT

- the choice of scale was different;
- the NLO result did not include the recently published H1 low- Q^2 inclusive and dijet data [28];
- the NLO result did not include the newly published low p_T points from the H1 high- Q^2 inclusive data;
- the NNLO result does not include trijet data;
- the NNLO result does not include the low p_T points from the ZEUS dijet data;
- the NNLO analysis imposes a stronger kinematic cut $\mu > 10 \text{ GeV}$
- the treatment of hadronisation uncertainty differs.

All these changes with respect to the NLO analysis had to be made to create a consistent environment for a fit at NNLO. at the same time, an NLO fit cannot be done under exactly the same conditions as the NNLO fit since the H1 low Q^2 data cannot be well fitted at NLO. However, an NLO and an NNLO fit can be done under the common conditions:

(from A. Cooper-Sarkar, alpha-s 2022 workshop)

An NLO and an NNLO fit can be done under the common conditions:

- choice of scale, $\mu_f^2 = \mu_r^2 = Q^2 + p_T^2$;
- exclusion of the H1 low- Q^2 inclusive and dijet data;
- exclusion of the low- p_T points from the H1 high- Q^2 inclusive jet data;
- exclusion of trijet data;
- exclusion of low- p_T points from the ZEUS dijet data;
- exclusion of data with $\mu < 10$ GeV
- hadronisation uncertainties treated as correlated systematic uncertainties as done in the NNLO analysis.

The values of $\alpha_s(M_Z)$ obtained for these conditions are:

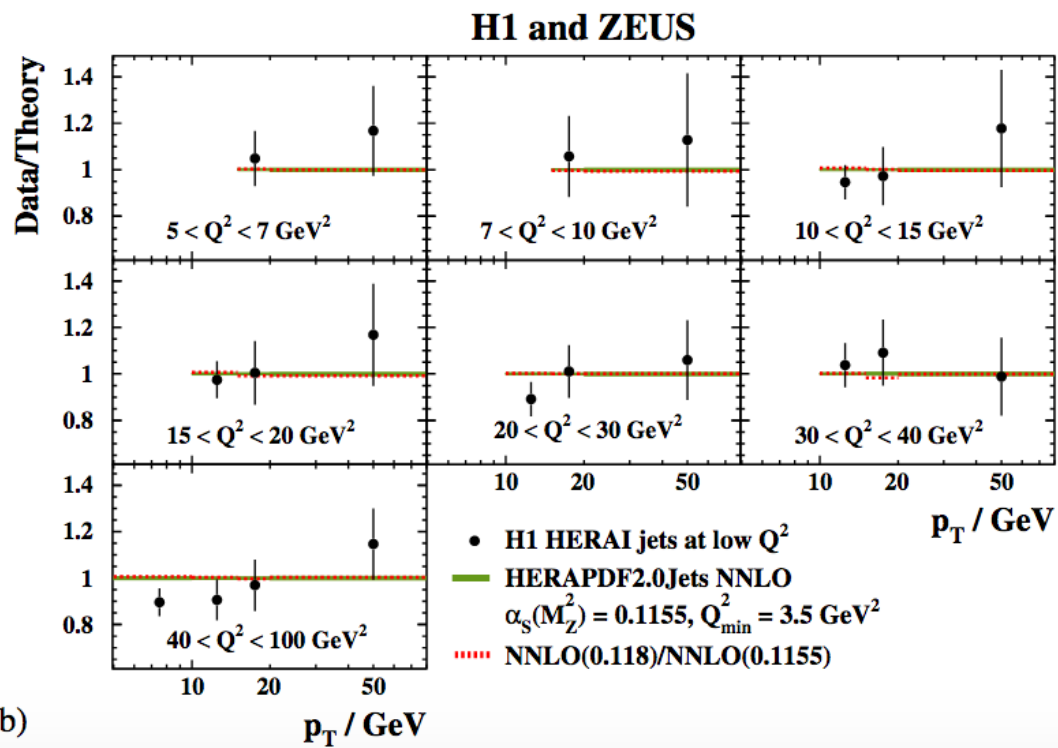
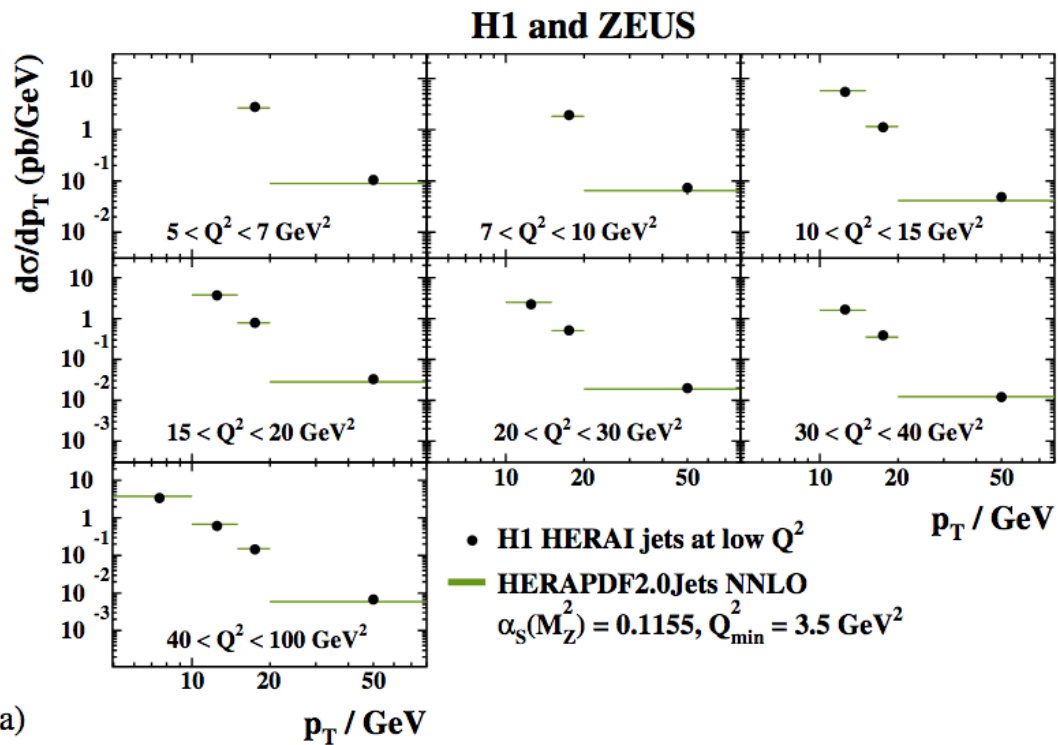
$0.1186 \pm 0.0014(\text{exp})$ NLO and $0.1144 \pm 0.0013(\text{exp})$ NNLO.

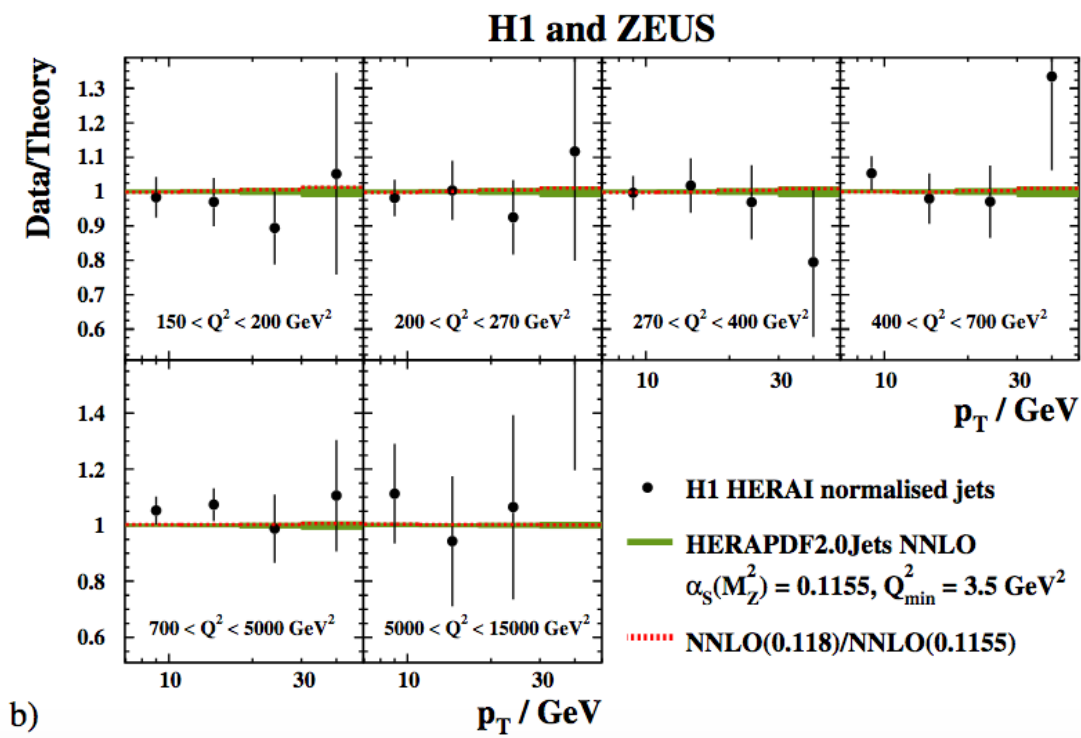
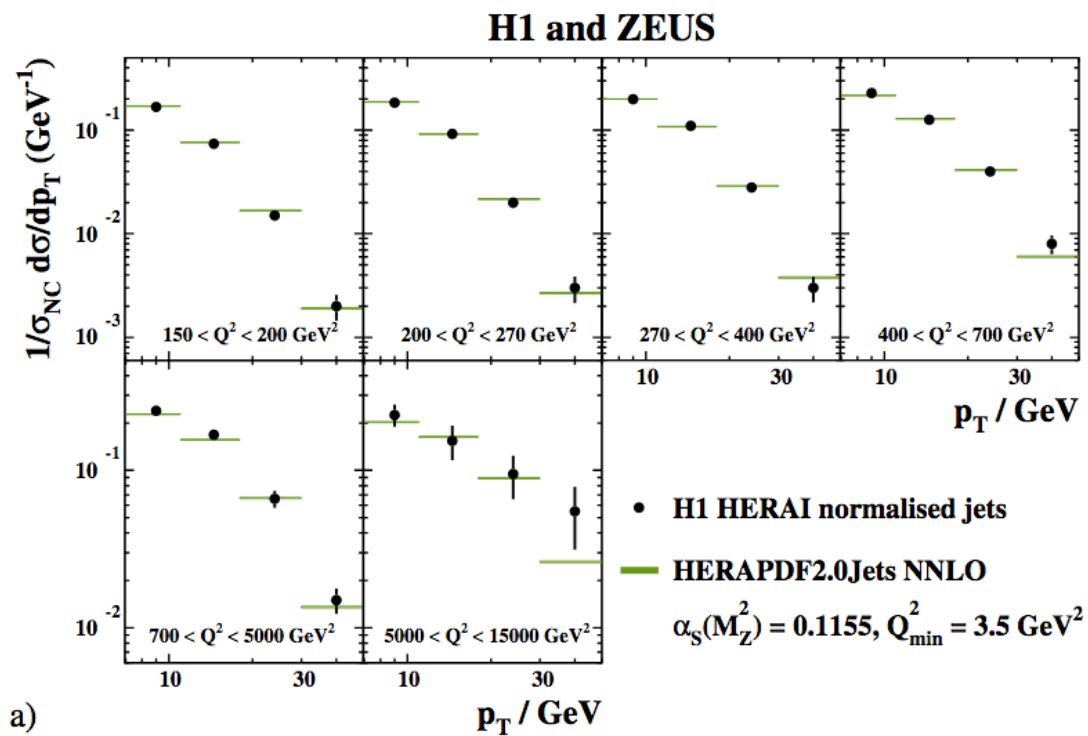
The change of the NNLO value from the preferred value of 0.1156 is mostly due to the exclusion of the H1 low Q^2 data and the low- p_T points at high Q^2

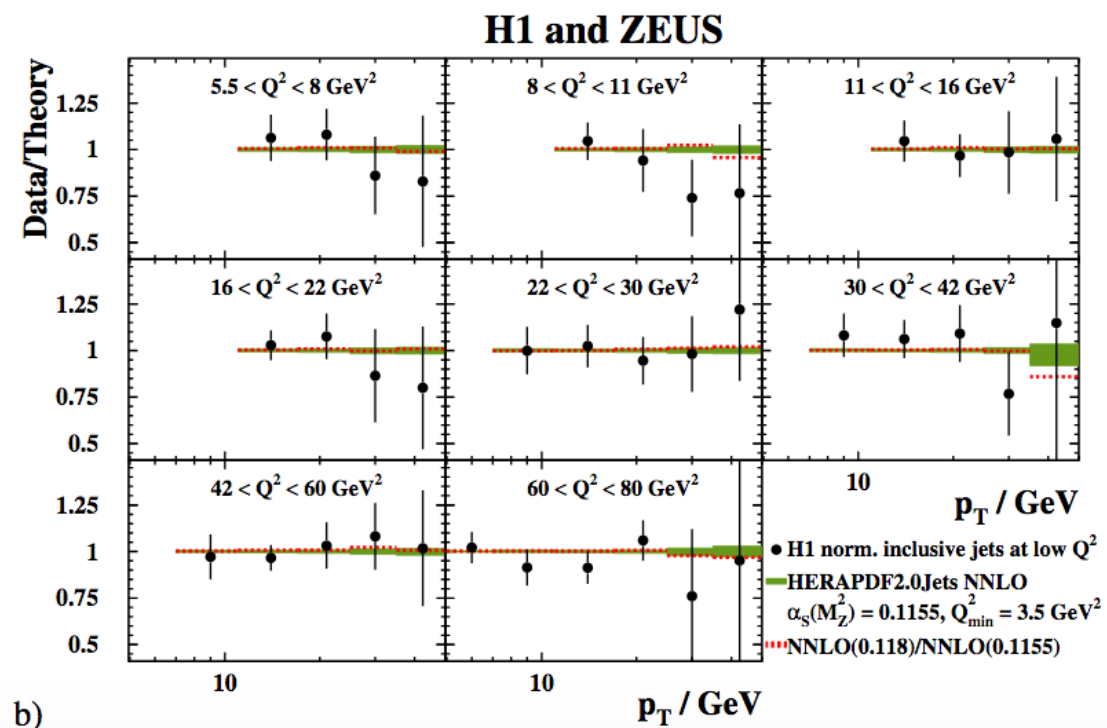
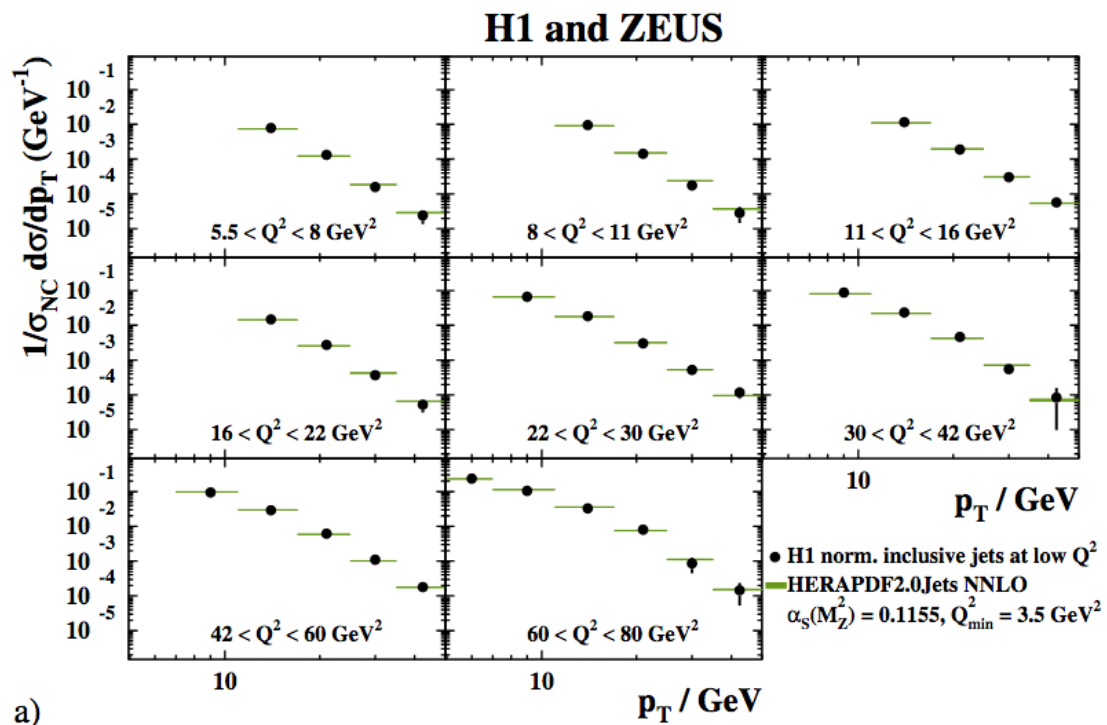
What do we mean when we say the H1 low Q^2 jets cannot be well fitted at NLO?

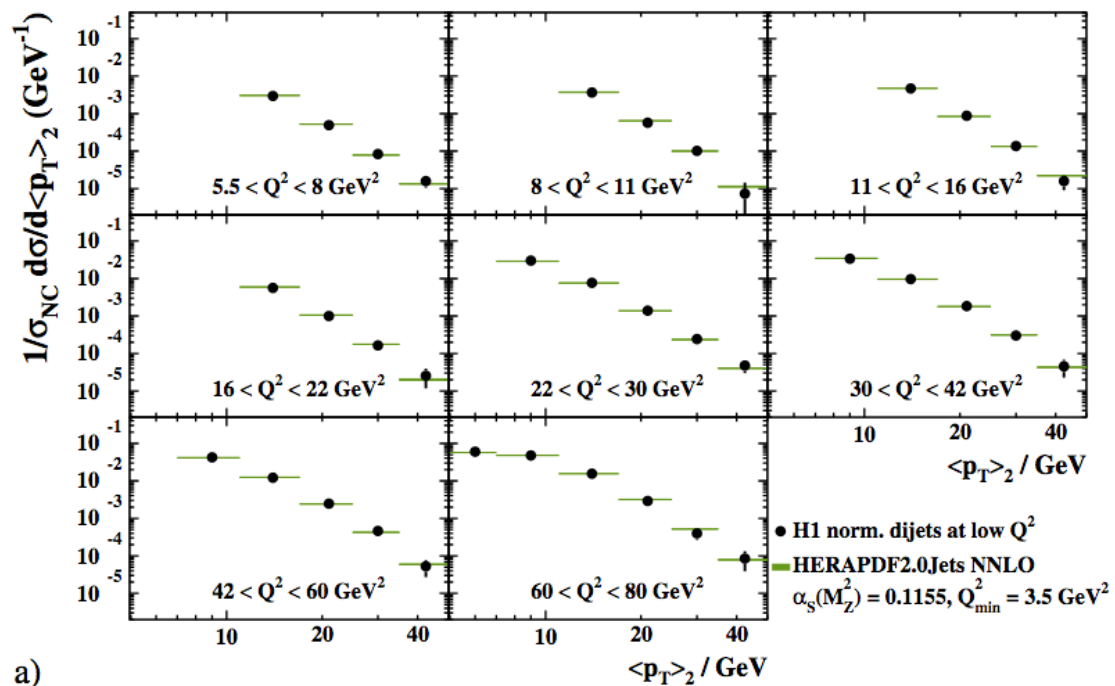
Simply this, that at NNLO the increase in overall χ^2 of the fit when the 74 data pts of these data are added is ~ 80 (exact value depends on $\alpha_s(M_Z)$ and on scale choice)

Whereas at NLO the increase in overall χ^2 of the fit when the 74 data pts of these data are added is ~ 180 .

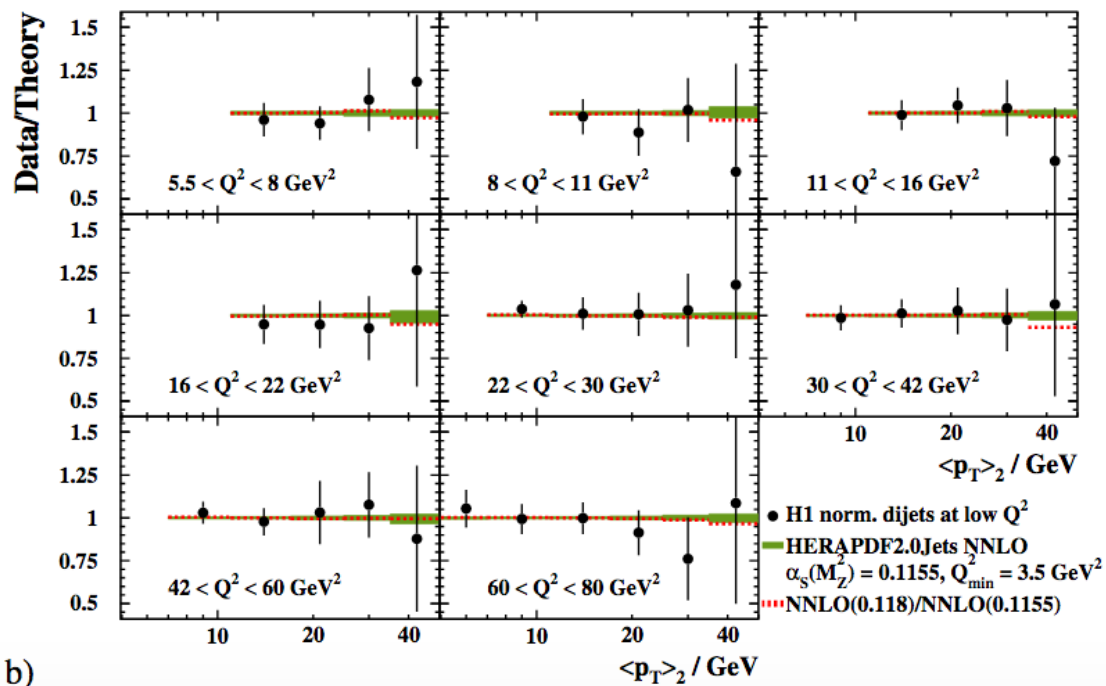




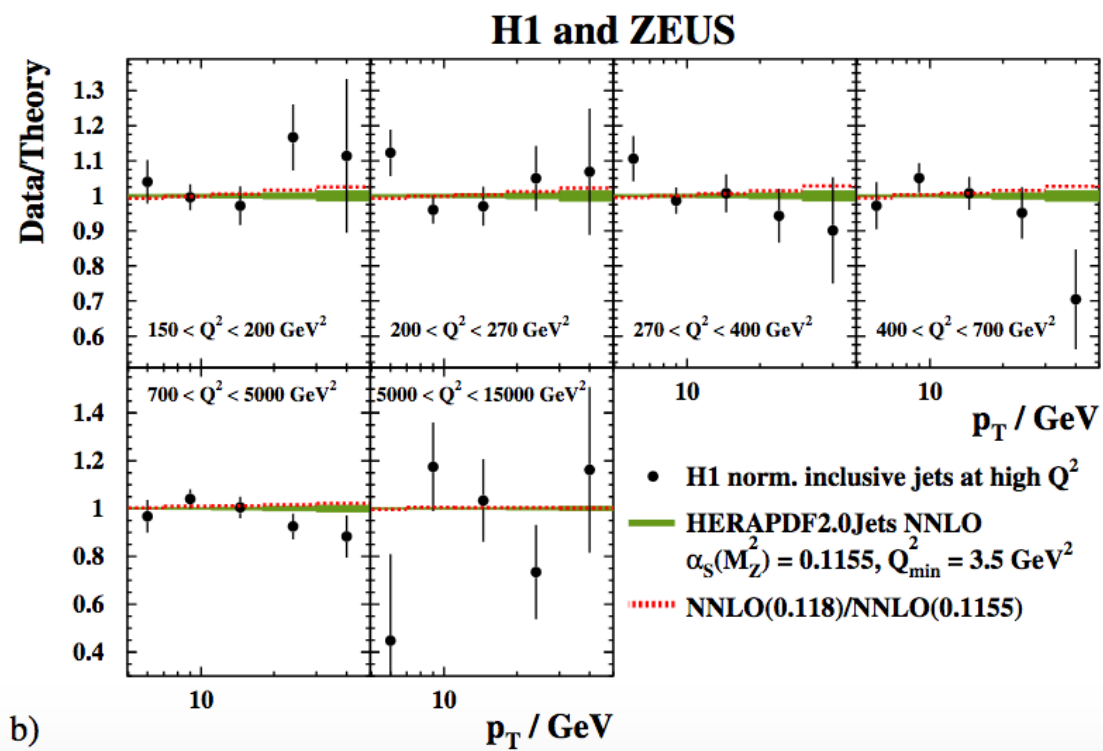
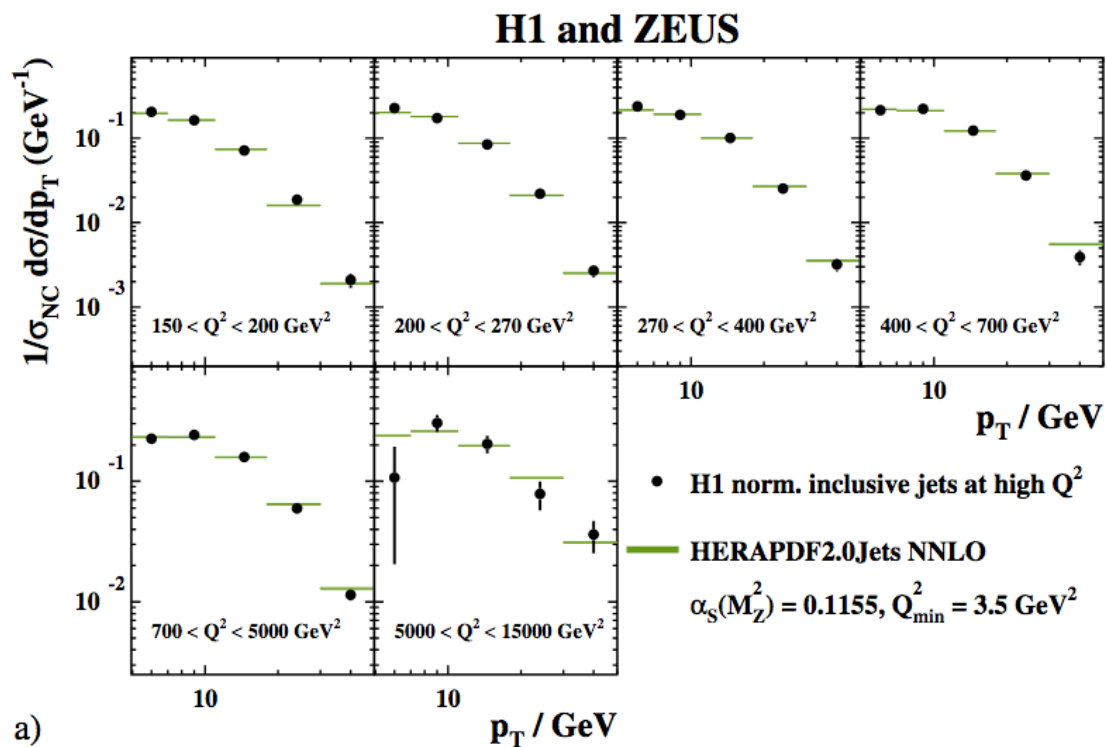


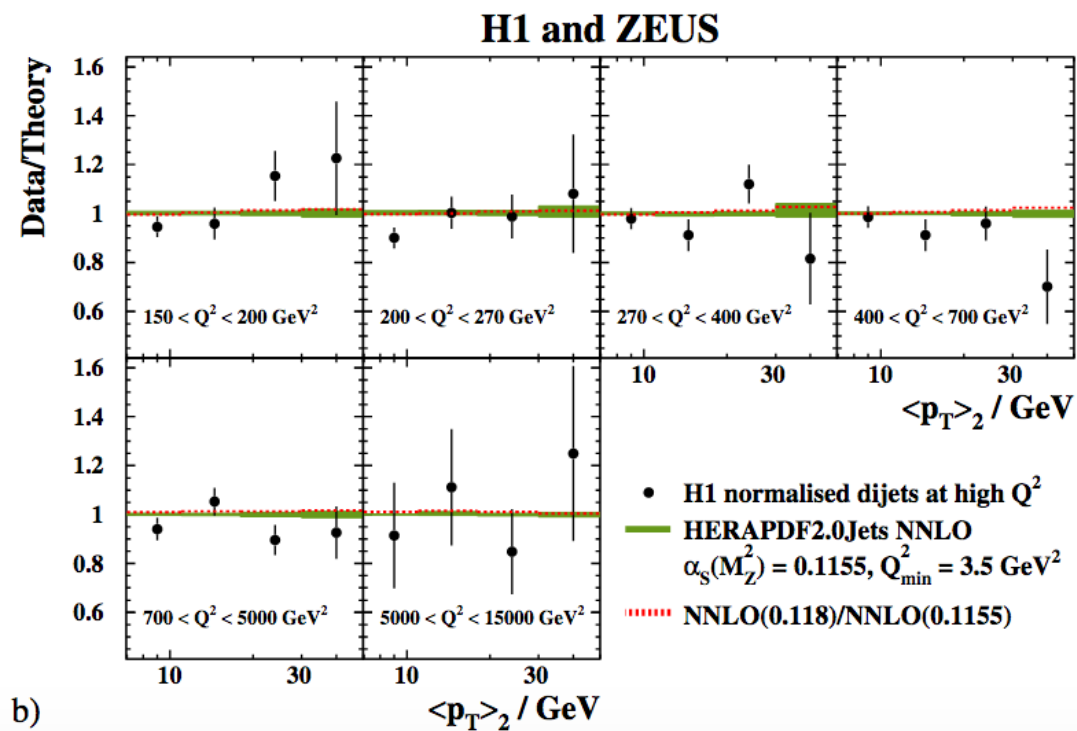
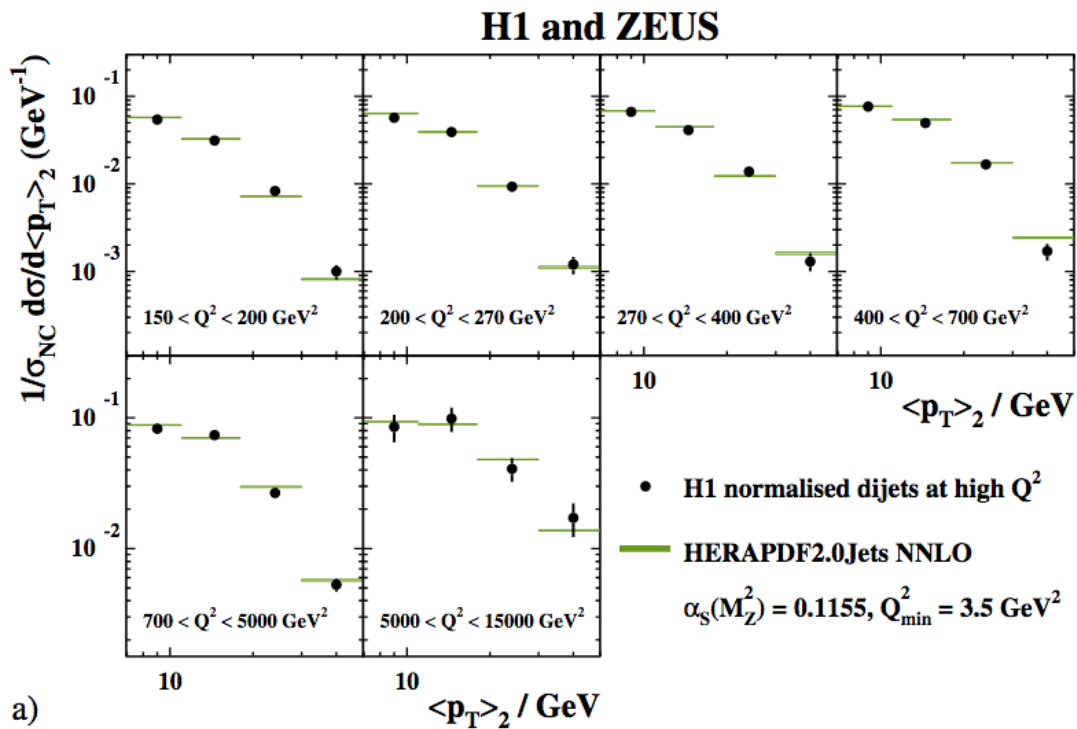
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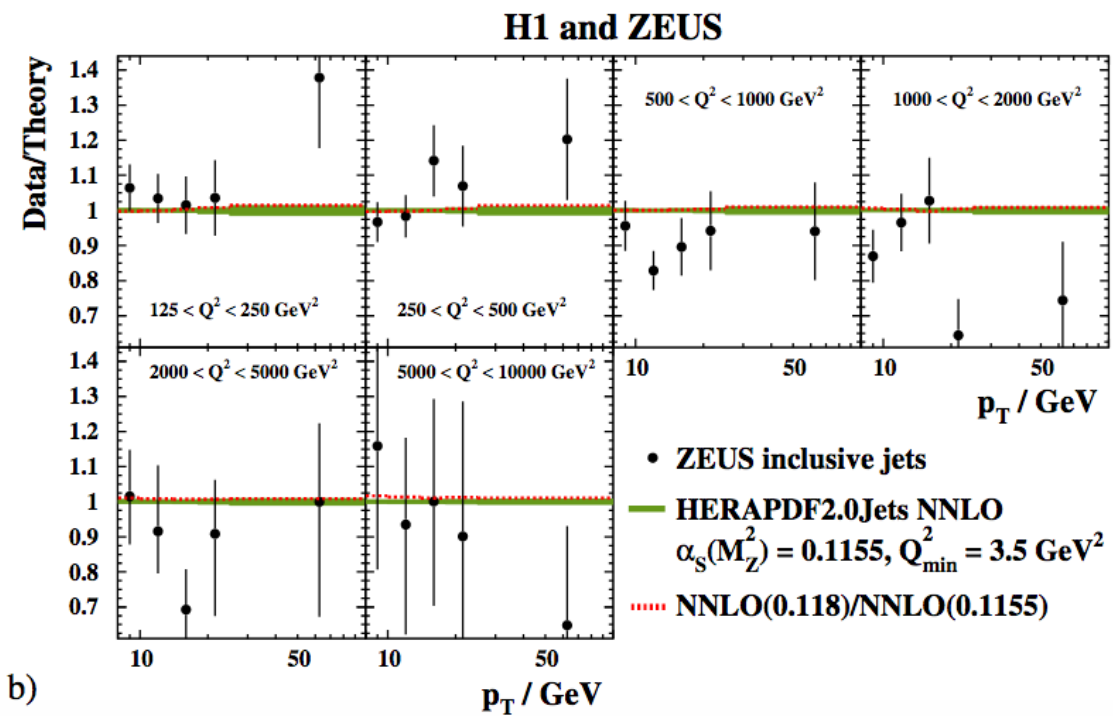
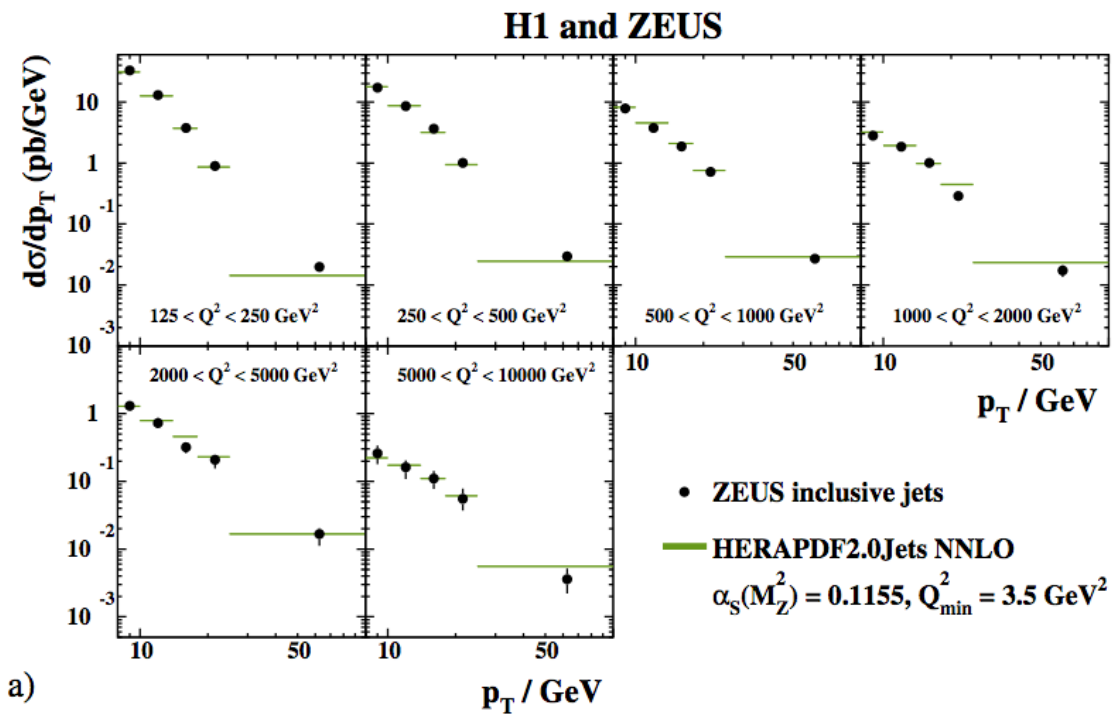
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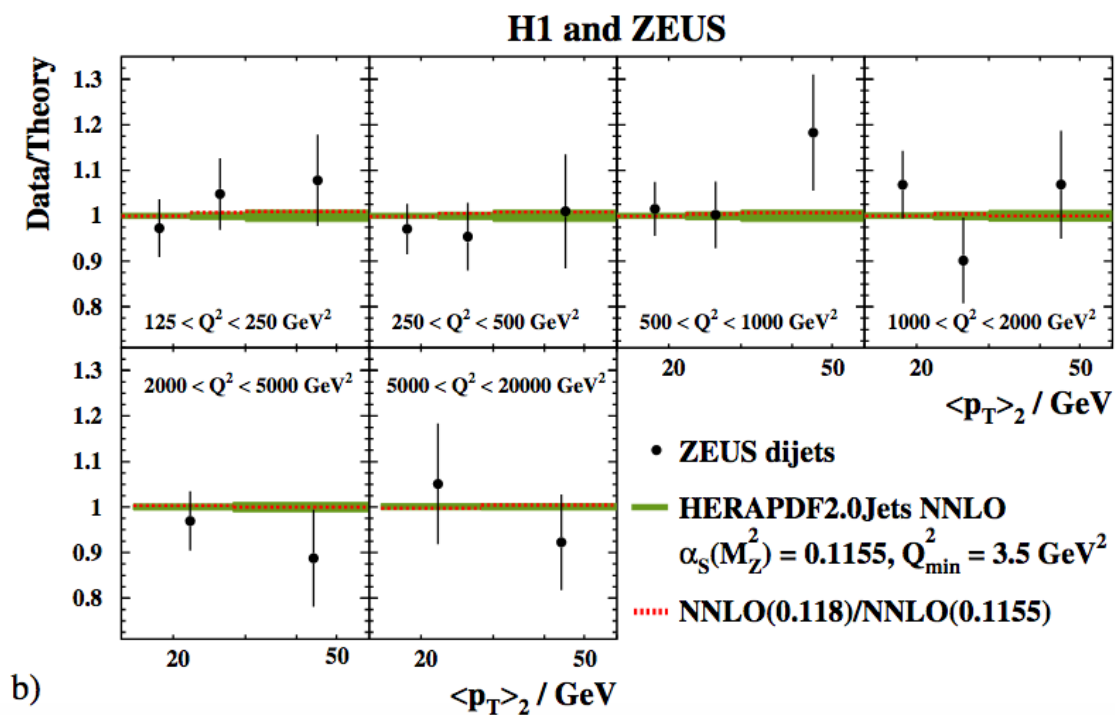
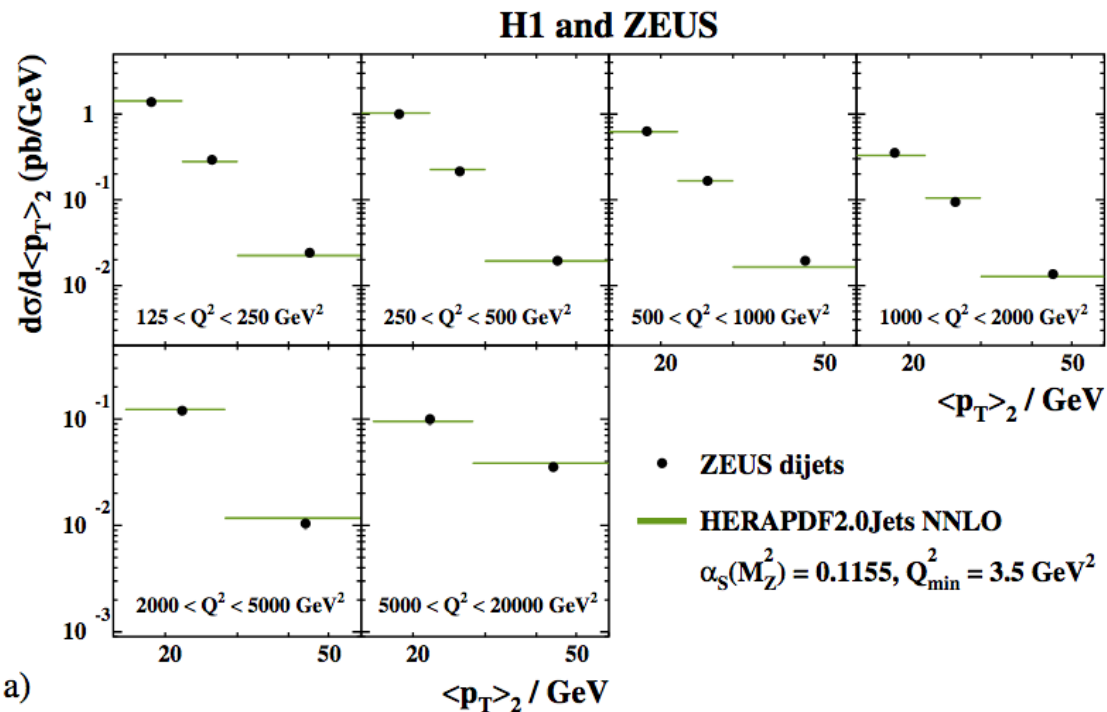
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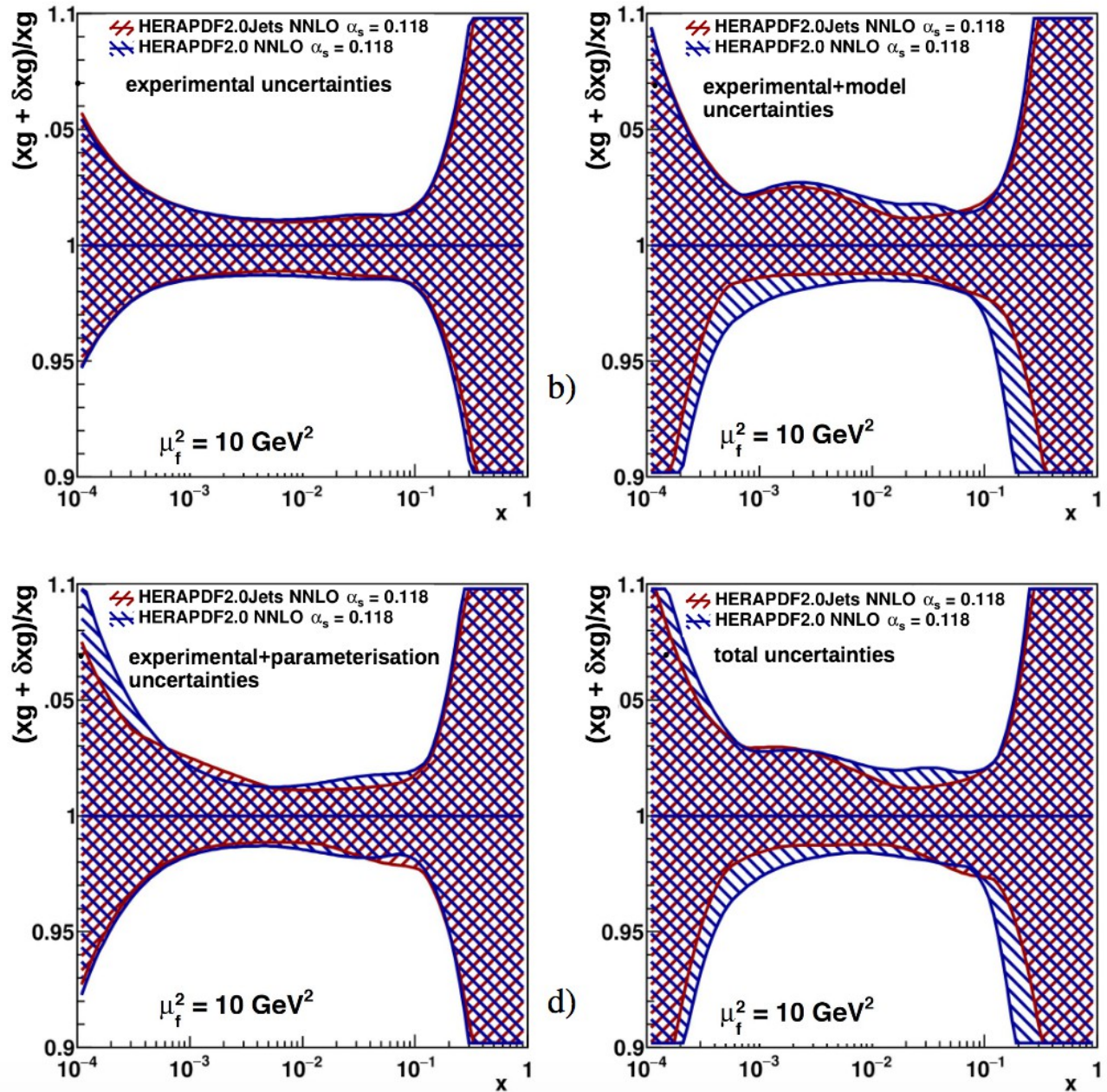






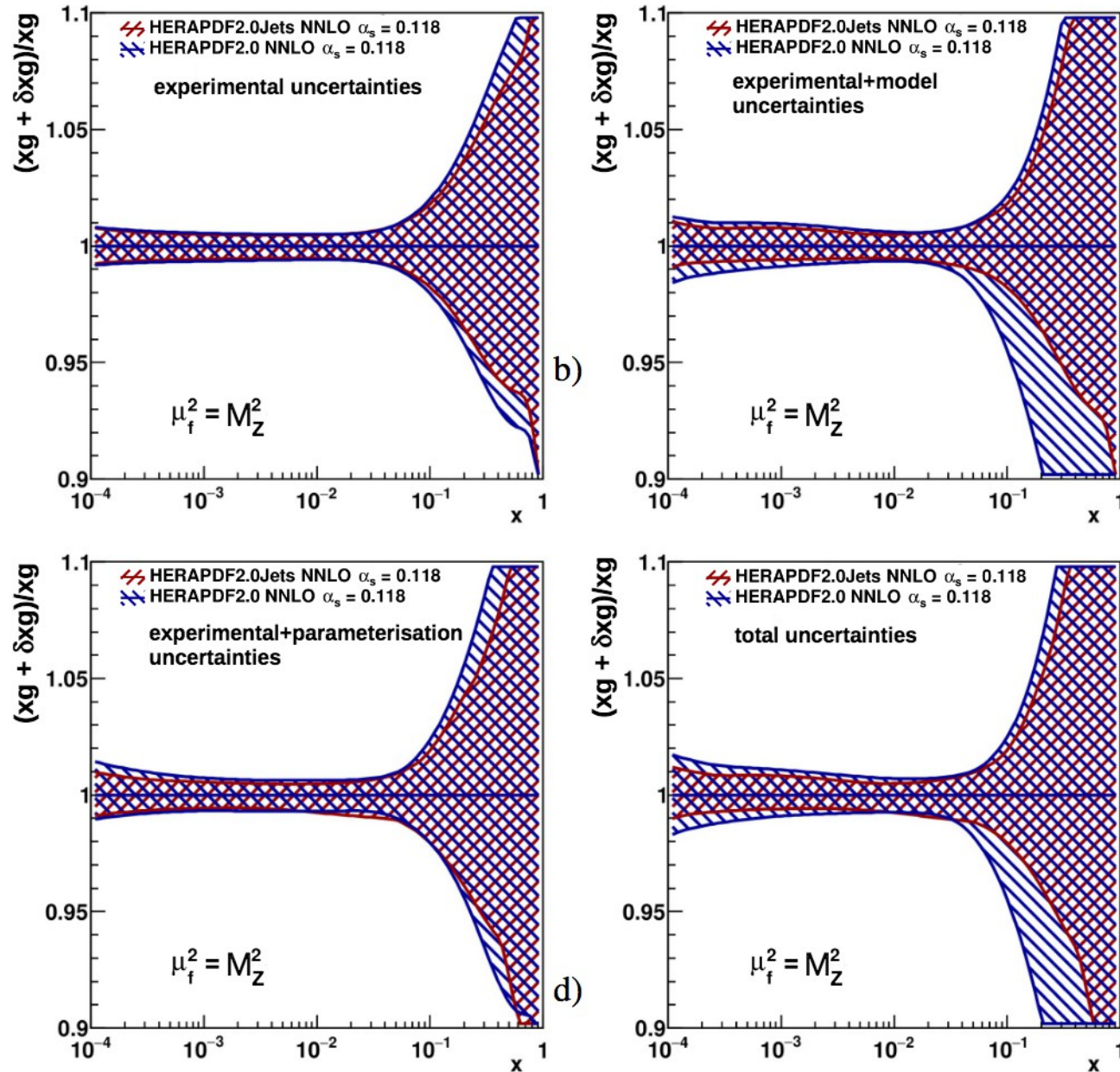
Uncertainties

H1 and ZEUS



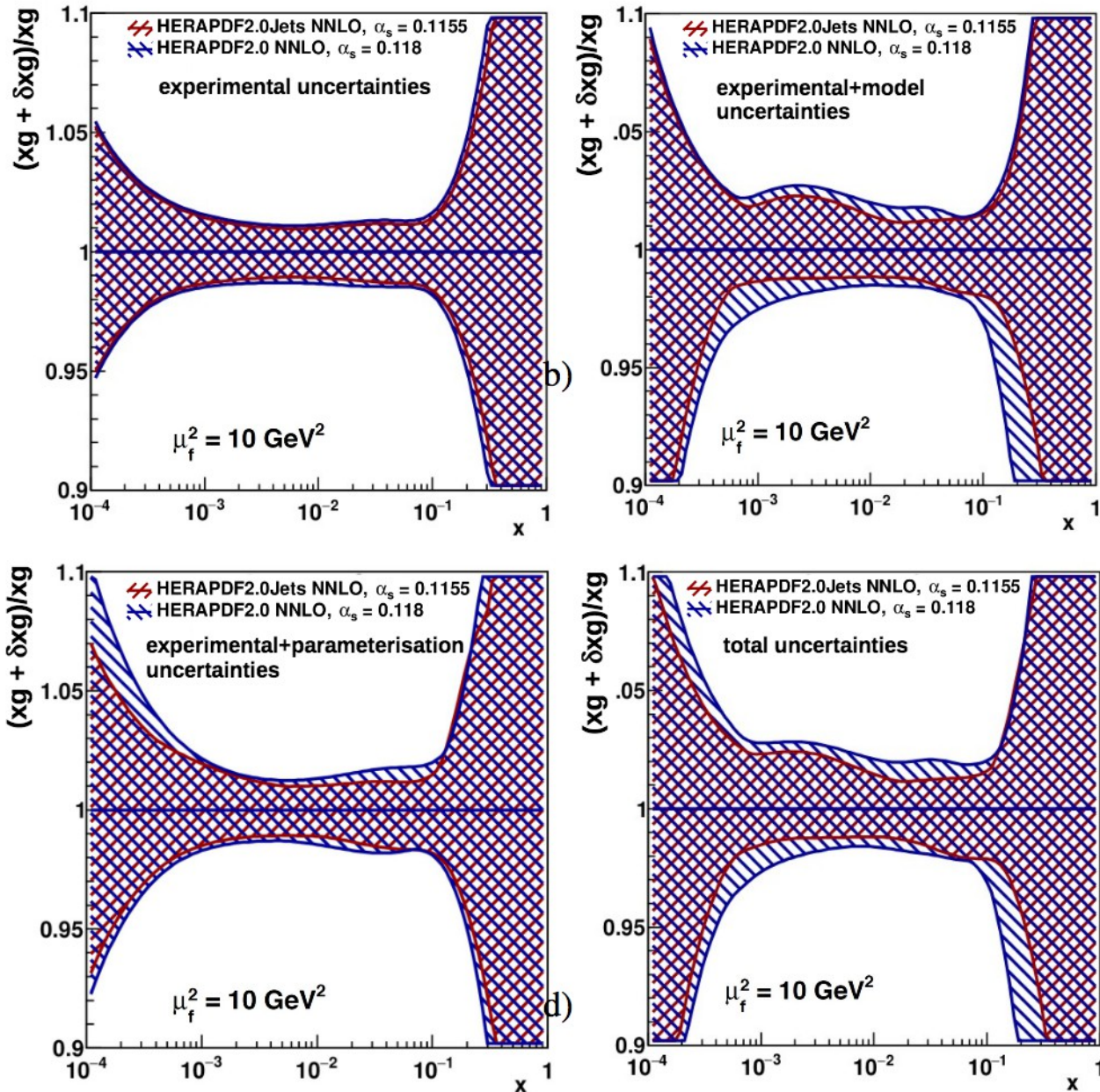
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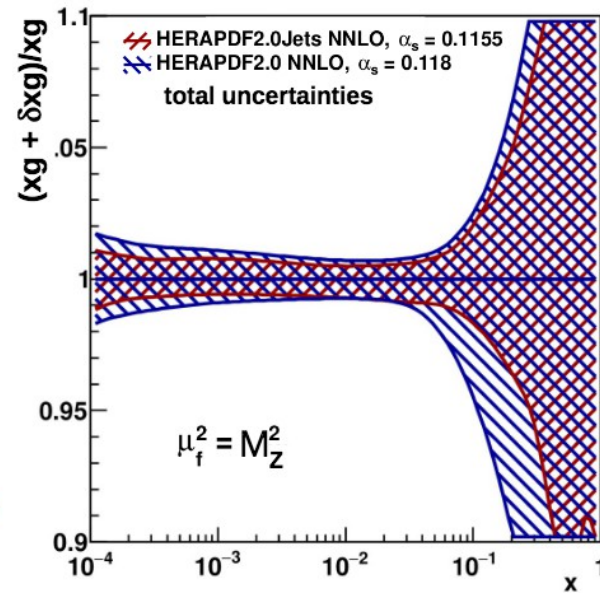
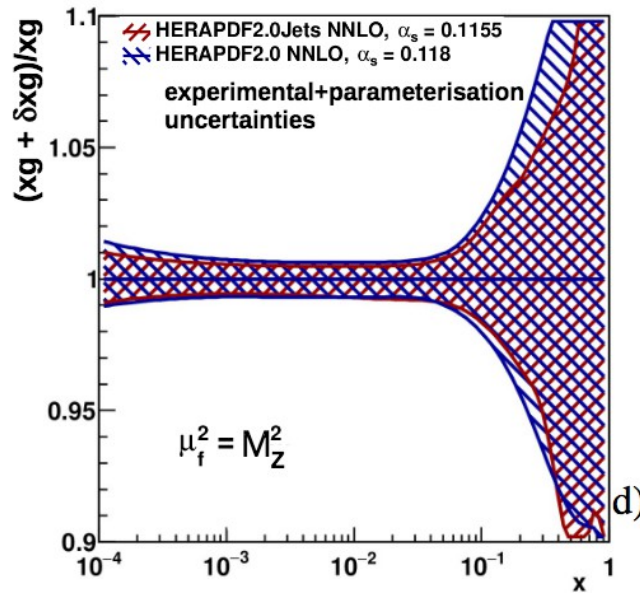
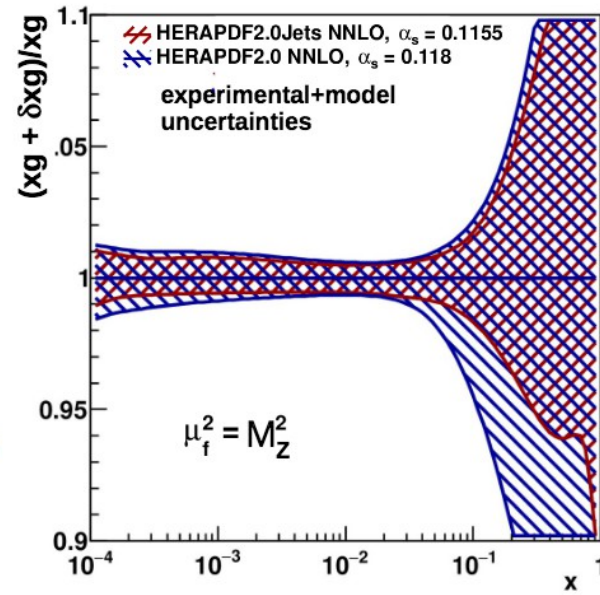
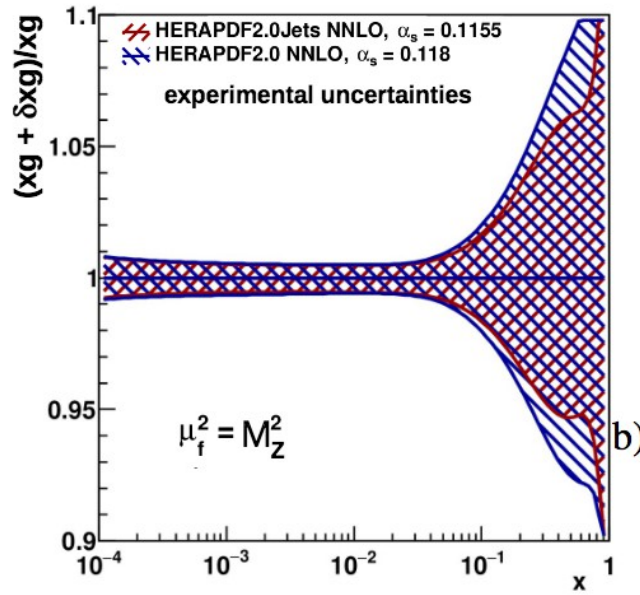
Uncertainties

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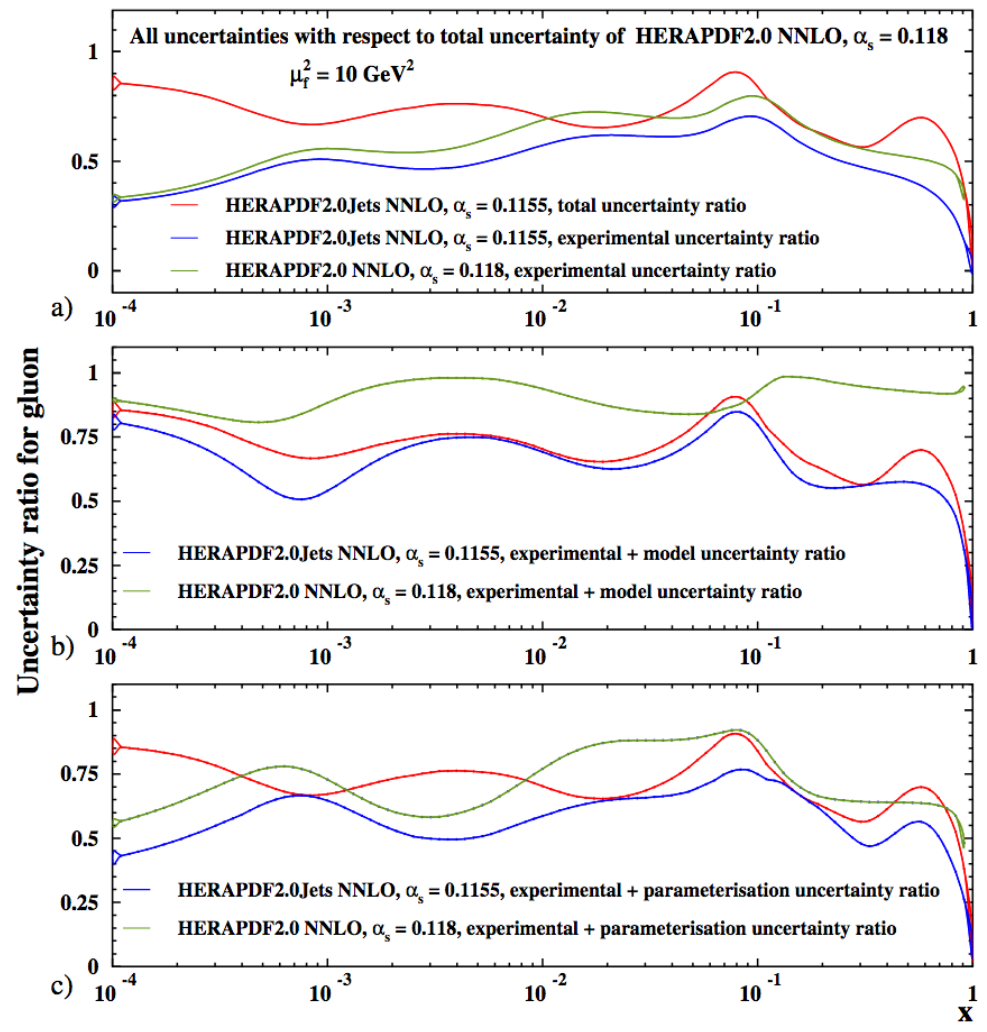


Uncertainties

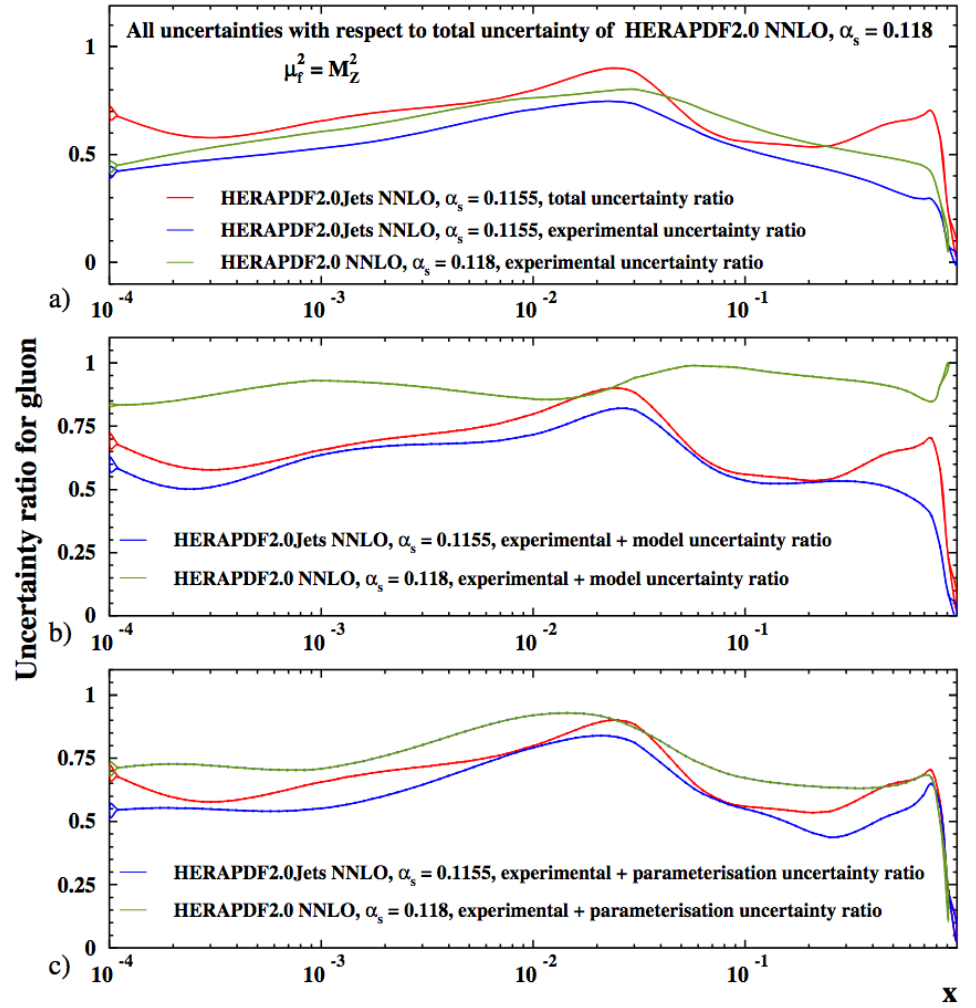
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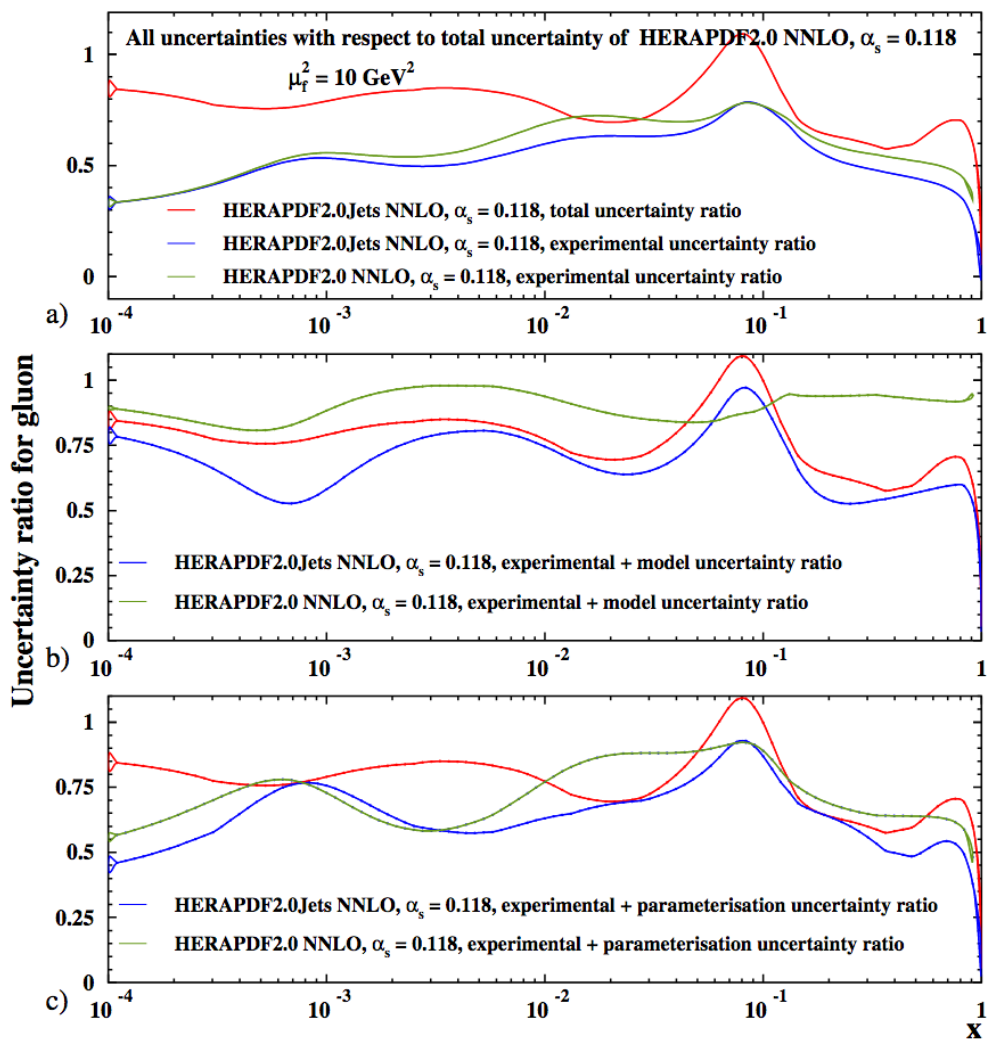
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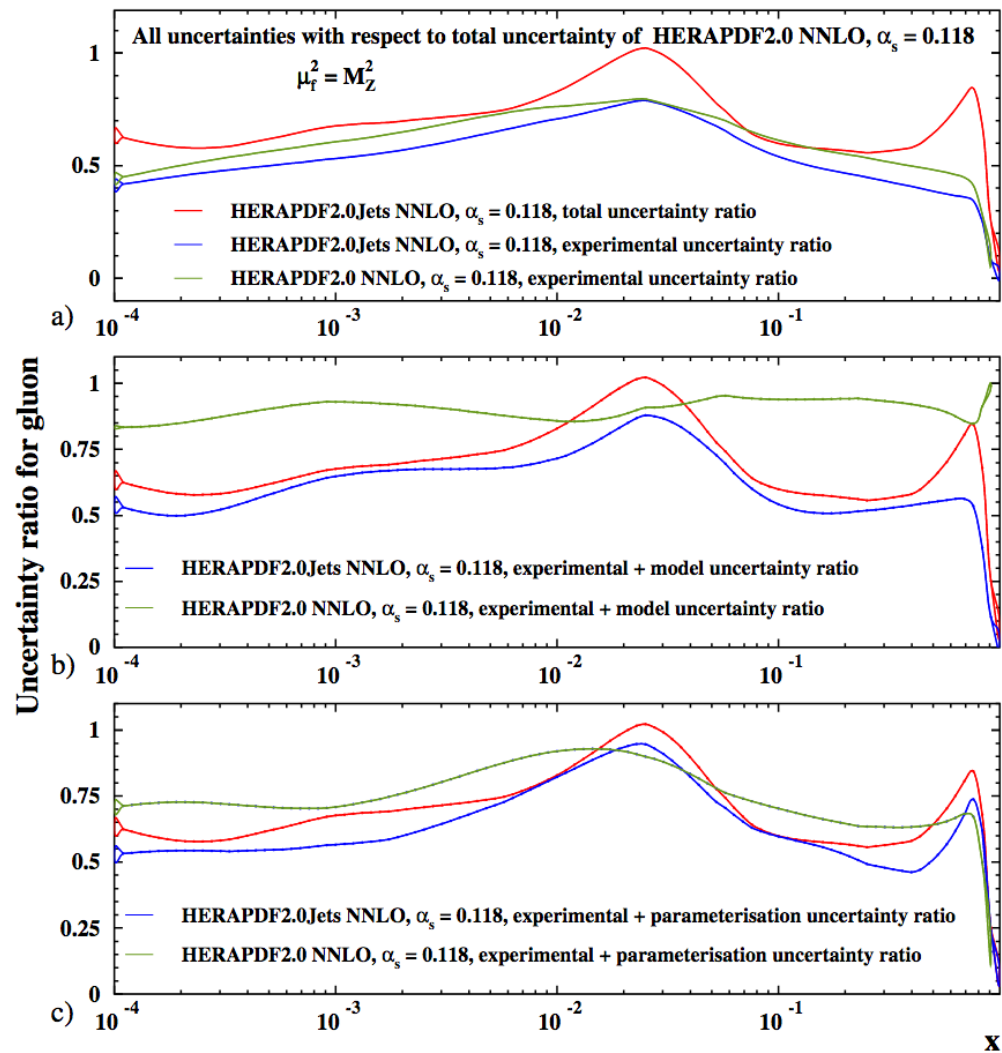
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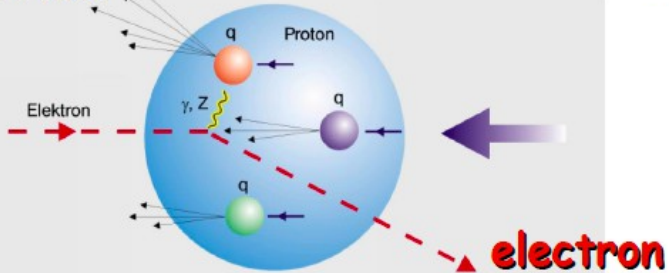
H1 and ZEUS



H1 and ZEUS



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