

Measurement of the cross-section ratio $\sigma_{\psi(2S)}/\sigma_{J/\psi(1S)}$ in exclusive photoproduction at HERA

Grzegorz Grzelak

(on behalf of the ZEUS collaboration)

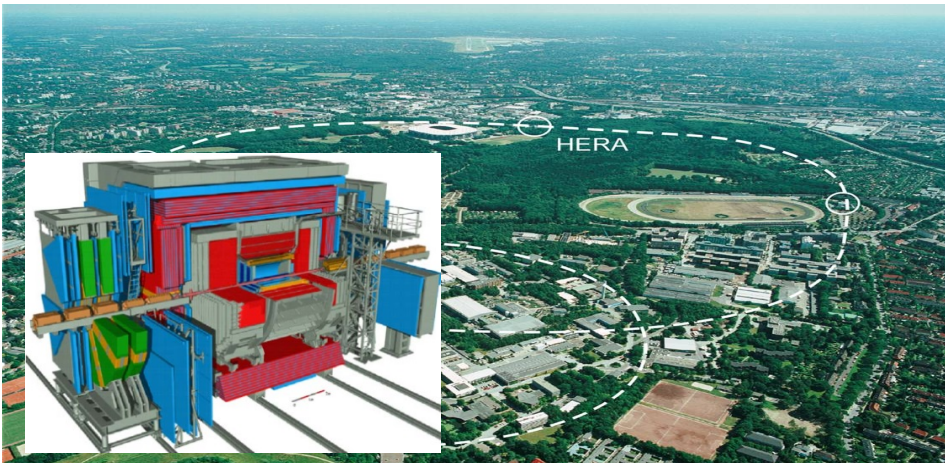
Faculty of Physics
University of Warsaw



XXIXth International Workshop on Deep-Inelastic Scattering and Related Subjects (DIS 2022)
Santiago de Compostela, Spain, May 2nd – 6th 2022

HERA and ZEUS: 1992 – 2007, DESY, Hamburg

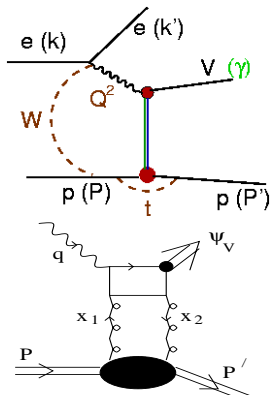
HERA: world's first and only $e^\pm p$ collider, $E_e = 27.5 \text{ GeV}$, $E_p = 920 \text{ GeV}$ ($\sqrt{s} = 318 \text{ GeV}$)



ZEUS: multipurpose, hermetic detector (MVD, CTD, CAL, F/B/RMUON, BAC, ...)

Total luminosity: $\int \mathcal{L} \sim 500 \text{ pb}^{-1}$ collected during HERA I + II running periods

Production of Vector Mesons in Exclusive Diffraction in ep Scattering



Exclusive process: proton stays intact
 Proton dissociation also possible \rightarrow
 background

pQCD: M_V^2 and Q^2 - set the scale at which the W and $|t|$ are probed
 Process sensitive to the **gluon density** in the proton

Kinematics: $M_V^2, Q^2, W, |t|$

M_V^2 - vector meson mass squared

$Q^2 (= -q^2 = -(k - k')^2)$ - the photon virtuality
 (emitted by the incoming electron):

- $Q^2 \approx 0$ GeV² PHP (*Photoproduction*)
- larger Q^2 for DIS (*Deep Inelastic Scattering*)

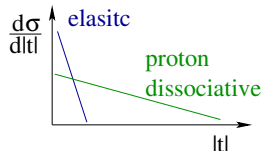
$W = (q + P)^2$ - invariant mass of the γp system

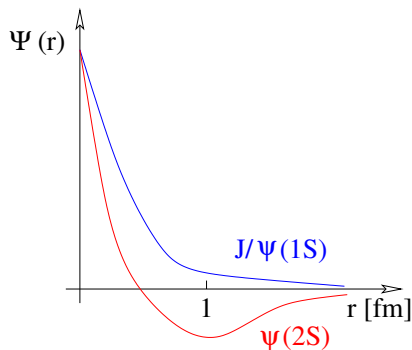
$$W \approx \sqrt{2E_P(E - p_Z)}_V$$

$|t|$ - 4-momentum transfer at the proton vertex

$$t = (P - P')^2$$

$$t \approx -p_{T,V}^2$$



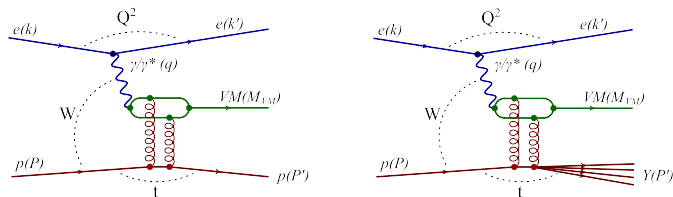


$$\text{Ratio } R = \frac{\sigma_{\gamma p \rightarrow \psi(2S)p}}{\sigma_{\gamma p \rightarrow J/\psi(1S)p}}$$

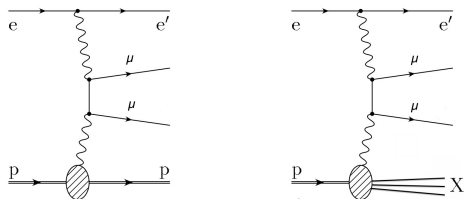
- sensitive to radial wave function of charmonium
- provides insight into the dynamics of the hard process

- $J/\psi(1S)$ and $\psi(2S)$ have the same quark composition but distinctive wave functions
- $\psi(2S)$ has a node at ≈ 0.4 fm
- $\langle r_{\psi(2S)}^2 \rangle \approx 2 \langle r_{J/\psi(1S)}^2 \rangle$
- pQCD models predict $R \sim 0.17$ in PHP and **rise of R with Q^2 in DIS**
- $\psi(2S)$ cross section is expected to be suppressed w.r.t. the J/ψ production
- (Both Vector Mesons masses are much smaller than the γp center-of-mass energy)

- **Signal MC:** DIFFVM (VM production in ep scattering)

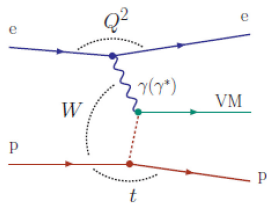
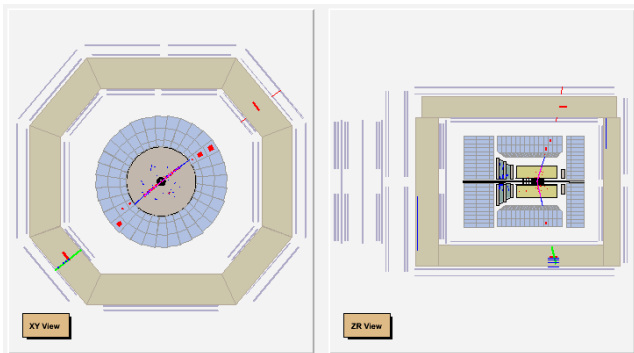


- **Background MC:** GRAPE (Bethe-Heitler continuum $\mu^+\mu^-$)



- **HERA II DATA:** $\mathcal{L} = 373 \text{ pb}^{-1}$ (2003 - 2007)
- **Investigated decay channels:**
 - $\psi(2S) \rightarrow J/\psi + \pi^+\pi^-$, $\psi(2S) \rightarrow \mu^+\mu^-$, $J/\psi(1S) \rightarrow \mu^+\mu^-$
- **exclusive (elastic) photoproduction sample**

Example of Final State Topology for $ep \rightarrow J/\psi p$, $J/\psi \rightarrow \mu^+ \mu^-$



Exclusive process, reaction mediated by exchange of **colorless** object; **proton stays intact.**

J/ψ and $\psi(2S)$ are detected in the 2- or 4-prong final states ($\mu^+ \mu^-$ or $\mu^+ \mu^- \pi^+ \pi^-$)
very clean final state topology:

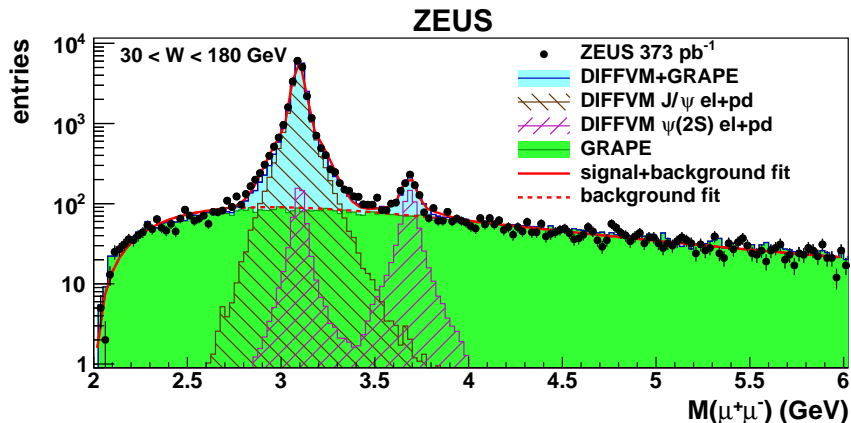
Photoproduction ($Q^2 < 1 \text{ GeV}^2$): two or four charged particles and nothing else
 \implies **experimental challenge: triggering on soft muons**

(Electroproduction ($Q^2 > 1 \text{ GeV}^2$): scattered electron also visible in the detector)

NOTE THE OPENING ANGLE OF THE DECAY PRODUCTS

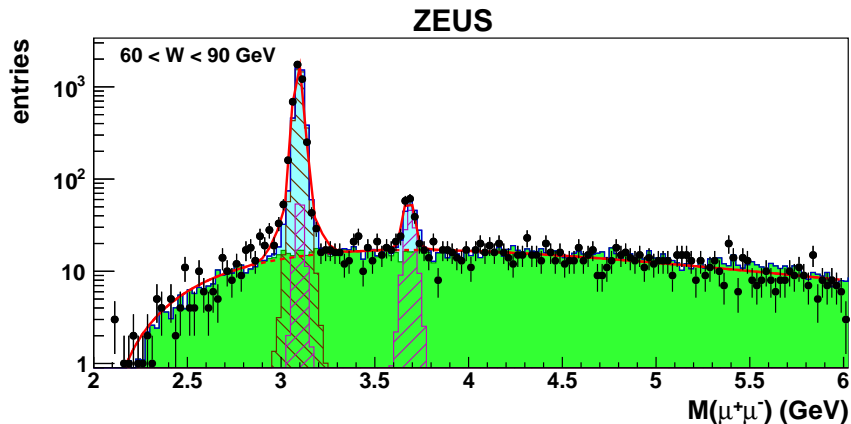
- **Exclusive Muon Triggers** (F/B/R/MUON or BAC)
- **Tracking and Vertex**
 - $N_{track} = 2$, oppositely charged tracks matched to the primary vertex ($\eta \in (-1.9, 1.9)$)
 - **both tracks identified as a muon in CAL, at least one in F/B/RMUON or BAC**
 - $p_T > 1.0$ GeV of each track
 - anti-COSMIC cuts (CAL timing, acolinearity: $\cos(\mu^+, \mu^-) < -0.985$)
- **Elasticity/Exclusivity and Photoproduction cuts** (on CAL Energy)
 - no scattered electron found in CAL
 - $E_{clu} < 0.5$ GeV for clusters not matched to muons (or pions)
(corresponds to an effective cut on $Q^2 < 1$ GeV²)
 - $E(\theta < 0.12rad) < 1$ GeV
the sum of the energy in the FCAL cone around the beam-pipe;
to suppress proton-dissociative events, $ep \rightarrow e + VM + Y$
(corresponds to a requirement for $M_Y \lesssim 5$ GeV)
- **Kinematic range (analysis phase space):**
 - $30 < W < 180$ GeV
 - $|t| < 1.0$ GeV²
 - $Q^2 < 1$ GeV² (median $Q^2 \approx 3 \times 10^{-5}$ GeV²)

- **Signal Extraction, Mass spectra**

$M(\mu^+\mu^-)$ 

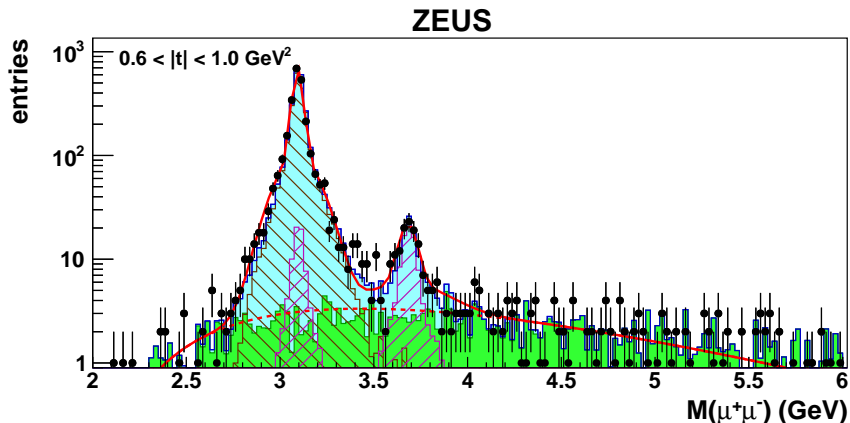
- full phase space: $30 < W < 180 \text{ GeV}$, $|t| < 1.0 \text{ GeV}^2$
- events yield: $\sim 23\,000$ J/ψ and ~ 700 $\psi(2S)$
- resonant background under J/ψ peak

$M(\mu^+\mu^-)$



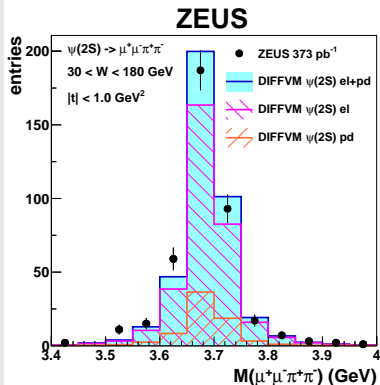
- **W2 bin:** $60 < W < 90$ GeV, $|t| < 1.0$ GeV²
- central rapidity region, long tracks, mass resolution: $\sigma_M(\mu\mu) \sim 22$ MeV

$M(\mu^+\mu^-)$

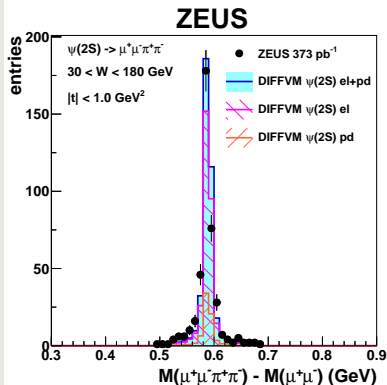


- **t5 bin:** $30 < W < 180$ GeV, $0.6 < |t| < 1.0$ GeV²
- higher $|t|$, small Bethe-Heitler continuum $\mu^+\mu^-$ contribution
- **BUT:** high contamination proton dissociative events → $\mu^+\mu^-$ spectra

$$M(\mu^+ \mu^- \pi^+ \pi^-)$$



$$M(\mu^+ \mu^- \pi^+ \pi^-) - M(\mu^+ \mu^-)$$



- events yield: $\sim 400 \psi(2S)$
- better resolution on mass difference \rightarrow cascade decay of $\psi(2S)$
- proton dissociative fraction: $f_{p,diss} = 0.16 \pm 0.01$ from t -spectra fit

- W and $|t|$ distributions: 2-prongs

- **Cross section ratio**

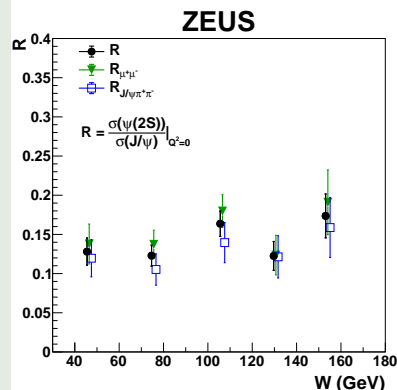
Cross section ratio $R = \frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$, full kinematic range

$30 < W < 180$ GeV, $|t| < 1.0$ GeV², $Q^2 < 1.0$ GeV²

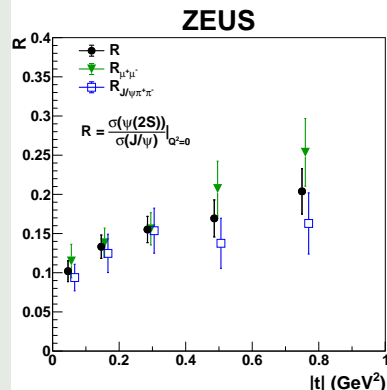
$\psi(2S)$ decay mode	$R = \frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$
$\mu^+ \mu^-$	0.154 ± 0.012
$J/\psi(\rightarrow \mu^+ \mu^-) \pi^+ \pi^-$	0.125 ± 0.019
combined	$0.146 \pm 0.010^{+0.016}_{-0.020}$

- $$R_{J/\psi\pi\pi} = \frac{N_{\psi(2S)}}{N_{J/\psi(1S)}} \cdot \frac{Acc_{J/\psi(1S) \rightarrow \mu^+ \mu^-}}{Acc_{\psi(2S) \rightarrow J/\psi\pi^+\pi^-}} \cdot \frac{1}{BR_{\psi(2S) \rightarrow J/\psi\pi^+\pi^-}} \cdot \frac{1 - f_{p.diss}^{\psi(2S)}}{1 - f_{p.diss}^{J/\psi(1S)}}$$
- $$R_{\mu\mu} = \frac{N_{\psi(2S)}}{N_{J/\psi(1S)}} \cdot \frac{Acc_{J/\psi(1S) \rightarrow \mu^+ \mu^-}}{Acc_{\psi(2S) \rightarrow \mu^+ \mu^-}} \cdot \frac{BR_{J/\psi(1S) \rightarrow \mu^+ \mu^-}}{BR_{\psi(2S) \rightarrow \mu^+ \mu^-}} \cdot \frac{1 - f_{p.diss}^{\psi(2S)}}{1 - f_{p.diss}^{J/\psi(1S)}}$$
- $Acc_i = \frac{N_i^{reco}}{N_i^{true}}, f_{p.diss}^i$ - fraction of proton dissociative events
- $BR(\psi(2S) \rightarrow J/\psi\pi^+\pi^-) = (34.68 \pm 0.3)\%$, $BR(\psi(2S) \rightarrow \mu^+\mu^-) = (0.80 \pm 0.06)\%$,
 $BR(J/\psi \rightarrow \mu^+\mu^-) = (5.961 \pm 0.033)\%$, $BR(\psi(2S) \rightarrow \mu^+\mu^-\pi^+\pi^-) = (2.07 \pm 0.02)\%$ (PDG 2020)
- both channels have similar precision and provide consistent results**

R vs. W



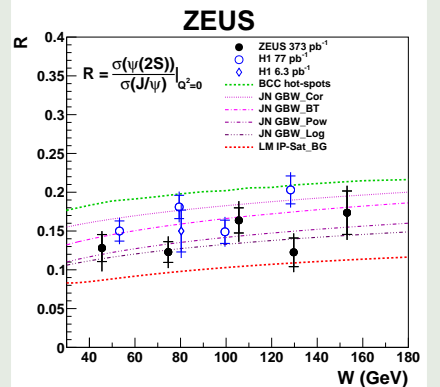
R vs. $|t|$



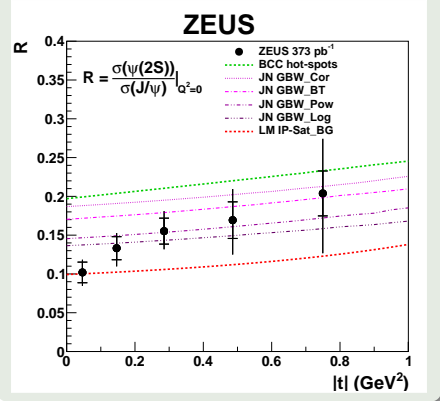
- $R_{\mu\mu}$ (2-prongs channel), $R_{J/\psi\pi\pi}$ (4-prongs channel) and combined R (full dots)
- statistical errors only
- **good agreement between two channels**

cross section ratio $R = \sigma_{\psi(2S)}/\sigma_{J/\psi(1S)}$: Final Results

R vs. W



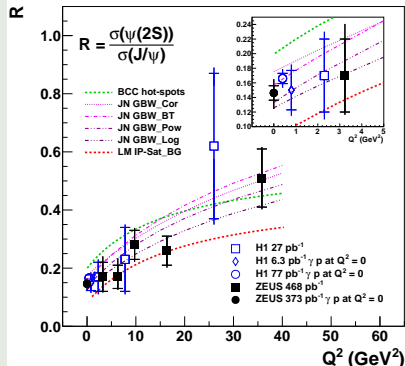
R vs. $|t|$



- for R vs. W ZEUS (full dots) and H1 (open markers) results are compared
- **no W dependence observed, moderate increase with $|t|$**
- good agreement between data and theoretical models (see next page)
- errors at high- $|t|$ points dominated by systematics (\rightarrow proton dissociative fraction)

R vs. Q^2

ZEUS



theoretical models:

- Bendova, Cepila and Contreras (BCC hot-spots):
 - Phys. Rev. D **99**, 034025 (2019).
- Jan Nemchik et al. (JN):
 - Eur. Phys. J. C **79**, 154 (2019).
 - Eur. Phys. J. C **79**, 495 (2019).
 - Phys. Rev. D **103**, 094027 (2021).
- Lappi and Mäntysaari (LM IP-Sat):
 - Phys. Rev. C **83**, 065202 (2011).
 - Phys. Rev. D **87**, 034002 (2013).
 - PoS (DIS2014), 069 (2014).

- ZEUS (full dot) and H1 (open markers) photoproduction results plotted at $Q^2 \sim 0$
- DIS results are also presented vs. Q^2 : ZEUS (full squares) and H1 (open squares)
- good agreement between data and theoretical models (\rightarrow backup plots, page 30)
- **better precision of photoproduction points**

- **Cross section ratio $R = \frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$** in photoproduction using HERA II data was measured by ZEUS in the kinematic range: $30 < W < 180$ GeV, $|t| < 1.0$ GeV²
- first ZEUS measurement of R in photoproduction (at $Q^2 = 0$):
 $R = 0.146 \pm 0.01(\text{stat.})_{-0.022}^{+0.016}(\text{syst.})$
- first HERA result for R vs. $|t|$ in photoproduction
- **moderate rise of cross section ratio as a function of $|t|$**
- **no W dependence observed within experimental errors**
- consistent results for 2- and 4-prongs decay channels
- comparable precision in both decay channels
- **theoretical calculations of the ratio $\frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$ for exclusive vector-meson production has been compared to the experimental data**
- **→ majority of the predictions are consistent with the data**
- **data start to exhibit constraining power**

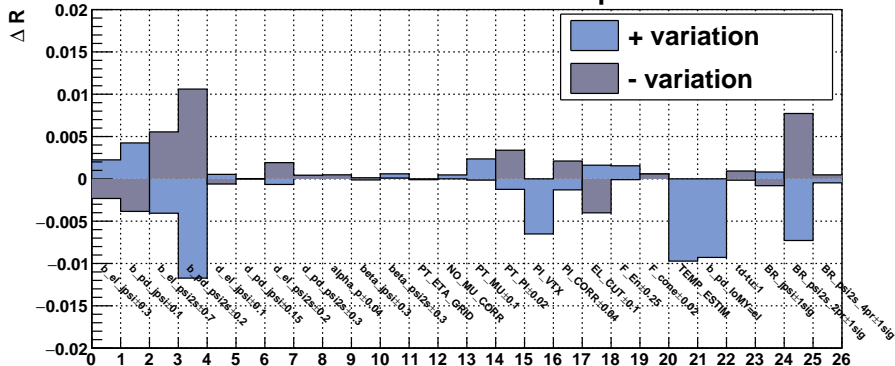
Thank You For Your Attention

BACKUP PLOTS FOLLOWS...

- **Systematics**

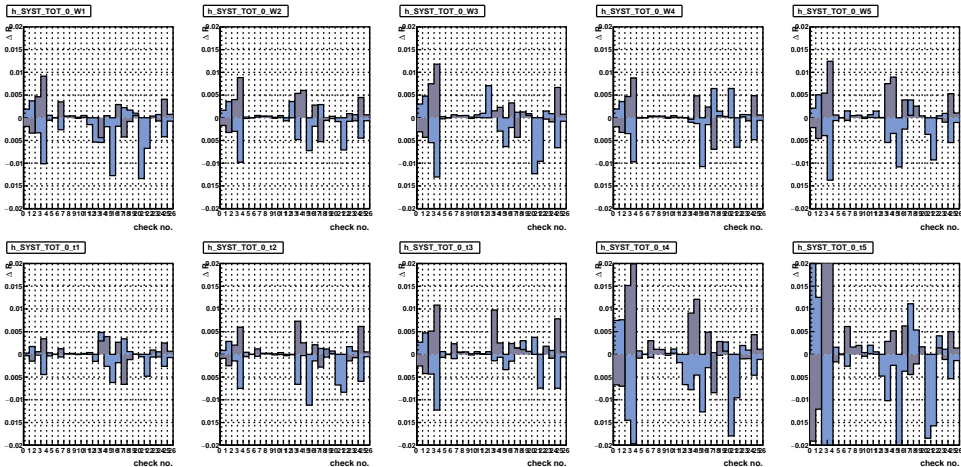
h_SYST_TOT_0

R GLOBAL: SYST error components



- biggest contributions from:
- b -slope variation of t -dependence (esp. for b_{pd} of $\psi(2S)$)
- event number estimator (MC templates fit instead of Gaussian fit)
- slow pions vertexing
- $BR(\psi(2S) \rightarrow \mu^+ \mu^-)$

R: components of SYST. error in W and $|t|$ bins



- upper row: contributions in 5 W bins
- bottom row: contributions in 5 $|t|$ bins
- bin order as on previous page

- **Theoretical Models**

- **Bendova, Cepila and Contreras (BCC hot-spots) :**
- Phys. Rev. D **99**, 034025 (2019).
- model with hot spots randomly sampled in the transverse plane bound by the size of the proton
- The slope parameter b is 4.72 GeV^{-2} and it is fixed by the combined H1 and ZEUS data from 2013 for JPsi photoproduction t -distribution.
- the same b -slope for both JPsi and Psi2s

- **Jan Nemchik (JN) et al. :**
- Eur. Phys. J. C **79**, no.6, 495 (2019).
- Eur. Phys. J. C **79**, no.2, 154 (2019).
- calculations have been performed for various combinations of quarkonium wave functions:
 - **Cor** (Cornell potential)
 - **BT** (Buchmüller-Tye)
 - **Pow** (Power-law potential)
 - **Log** (Logarithmic potential)
- and models for the dipole cross sections:
 - BGBK, **GBW** ← **used on the plots**
 - for each combinations calculations are performed with and w/o skewness in the gluon density
- the same b -slope parameters for both quarkonium states

- **Lappi and Mntysaari (LM IP-Sat) :**
 - the BFKL evolution plus the IP-Sat model to predict vector-meson production in ep and electronion collisions in the dipole picture
 - 2S parameters from arXiv:1406.2877 (PoS DIS2014 (2014) 069)
 - 1S parameters from hep-ph/0606272 (Phys.Rev. **D74** (2006) 074016)
 - Calculation described in (Phys.Rev. **C83** (2011) 065202)
 - **IP-Sat** dipole from fit (Phys.Rev. **D87** (2013) no.3, 034002)
 - Wave function: Boosted Gaussian (**BG**), $Q^2 = 0 \text{ GeV}^2$
 - Skewedness and real part corrections included
-
- predictions of all models were calculated within the phase space of this analysis:
 - $30 < W < 180 \text{ GeV}$
 - $|t| < 1.0 \text{ GeV}^2$
 - $Q^2 \sim 0$ (photoproduction points)

- **Signal extraction, cuts, control plots, ...**

2-prongs: Signal extraction: fit parameterization

- **Double Gaussian** shape: $G(x)$ or $g(x) = N \cdot \Delta \cdot \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{(x-m)^2}{2\sigma^2}\right)$
where: N – number of events, Δ – mass bin width,
 m – mean value, σ – RMS

- for J/ψ : $N_1 \cdot G_1(x) + N_2 \cdot G_2(x)$

- for ψ' : $N'_1 \cdot g_1(x) + N'_2 \cdot g_2(x)$

- introducing: $N = N_1 + N_2$, $N' = N'_1 + N'_2$, $R = \frac{N'}{N}$

- **with additional constraints**: $m_1 = m_2$, $m'_1 = m'_2$,
 $\frac{\sigma'_1}{\sigma_1} = \frac{\sigma'_2}{\sigma_2} = \alpha$, $\xi = \frac{N_1}{N} = \frac{N'_1}{N'}$ (**scaling of the mass resolution**)

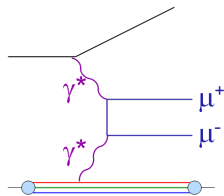
- final formulae:

$$F(x) = N \cdot ((\xi \cdot G_1(x) + (1 - \xi) \cdot G_2(x)) + R \cdot (\xi \cdot g_1(x) + (1 - \xi) \cdot g_2(x))) + BG(x)$$

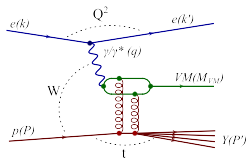
- **background function**: $BG(x) = A \cdot (x - B)^C \cdot \exp(-D(x - B) - E(x - B)^2)$
where A, B, C, D, E are fit parameters, B fixed ($= 2p_{t,min}^\mu$)

- (only differences w.r.t. the 2-prong channel)
- $N_{track} = 4$, (two oppositely charged pairs, sorted by p_T)
- **highest momentum pair: muon candidates**
lowest momentum pair: pion candidates
- no anti-COSMIC cuts
- transverse momentum of pion candidates: $p_T^\pi > 0.12$ GeV;
- $2.8 < M(\mu^+ \mu^-) < 3.4$ GeV (J/ψ window)
- $M(\mu^+ \mu^- \pi^+ \pi^-) - M(\mu^+ \mu^-)$ in (0.5 – 0.7) GeV window (cascade decay of $\psi(2S)$)

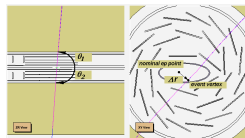
- QED di-muons (like $\gamma^* \gamma^* \rightarrow \mu^+ \mu^-$) from the Bethe-Heitler process



- J/ψ and $\psi(2S)$ mesons production with the dissociation of the proton

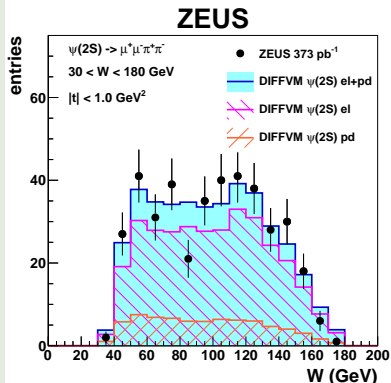


- Cosmic muons can mimic $\mu^+ \mu^-$ pairs when passing close to the interaction point

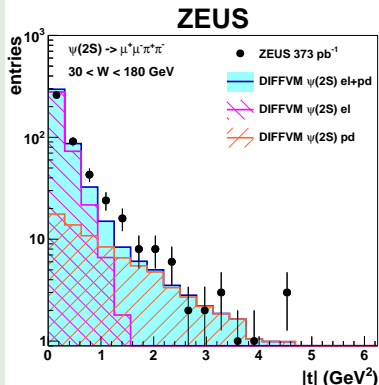


4-prongs: W and $|t|$ distributions: $\psi(2S)$ mass window

W : $3.4 < M(\mu^+\mu^-\pi^+\pi^-) < 4.0$ GeV



$|t|$: $3.4 < M(\mu^+\mu^-\pi^+\pi^-) < 4.0$ GeV



- proton dissociation dominates for $|t| > 1.0$ GeV²
- proton dissociative fraction: $f_{p,diss} = 0.16 \pm 0.01$ ($|t| < 1.0$ GeV²) from t -spectra fit

- **Monte Carlo**

DIFFVM – A Monte Carlo Generator for Diffractive Processes in ep Scattering.

B. List

CERN –EP/OPAL–,
CH–1211 Genève 23, Switzerland
Benno.List@cern.ch

A. Mastroberardino

Calabria University, Physics Dept.,
Cosenza, Italy
mastrobe@vxdesy.desy.de

- soft diffractive processes in the Regge framework and Vector Dominance Model

- $\frac{d\sigma}{dQ^2} \propto \frac{1}{(1+Q^2/M_Y^2)^{1.5}}$

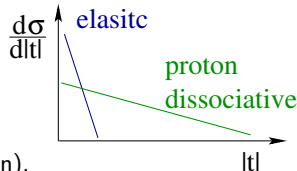
- $\frac{d\sigma}{d|t|} \propto W_{\gamma p}^{4\epsilon} e^{-b|t|} \quad (4\epsilon = \delta) \text{ (elastic)}$

- $\frac{d^2\sigma}{d|t|dM_Y^2} \propto W_{\gamma p}^{4\epsilon} e^{-b'|t|} M_Y^{-\beta} \text{ (p.diss)}$

- $\frac{d\sigma}{dM_Y^2} \sim \frac{f(M_Y^2)}{M_Y^{2(1+\epsilon)}}$ for $M_Y^2 < 3.6 \text{ GeV}^2$ (p resonance region),

- $\frac{d\sigma}{dM_Y^2} \sim \frac{1}{M_Y^{2(1+\epsilon)}}$ for $M_Y^2 \geq 3.6 \text{ GeV}^2$ (continuum region)

- assuming SCHC: s-channel helicity conservation



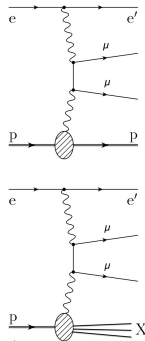
GRAPE-Dilepton (Version 1.1)

A generator for dilepton production in ep collisions

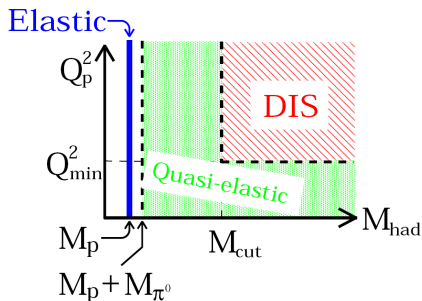
Tetsuo Abe

Department of Physics, University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113-8654, Japan

- based on the **exact matrix elements** in the electroweak theory at tree level via $\gamma\gamma$, γZ^0 , $Z^0 Z^0$ and via photon internal conversion (QED Compton)
- **Feynman amplitudes** are generated by the automatic calculation system **GRACE**
- **proton vertex** covers the whole kinematical region
- interface to PYTHIA and SOPHIA
→ complete hadronic final state
- covers **elastic, quasi-elastic and DIS processes**



GRAPE generator - simulate QED lepton pair (Bethe-Heitler)



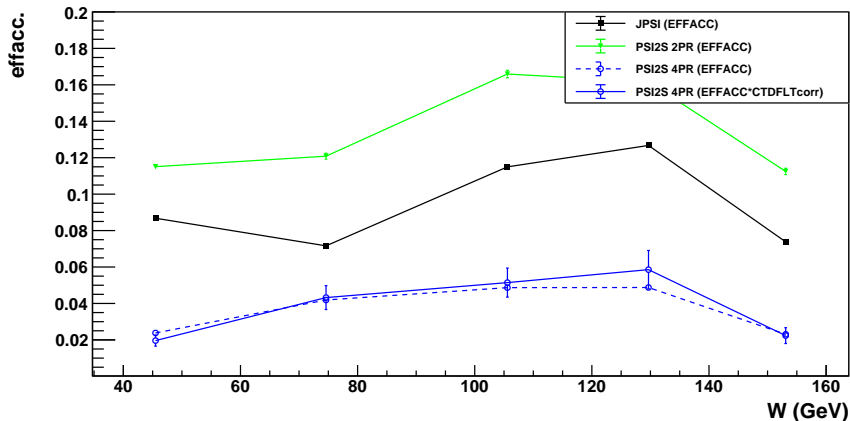
Important for the **shape of the BH $M_{\mu^+\mu^-}$ spectrum** (sidebands)
 and for the **BH t -dependence**: low t - elastic BH, higher t - QEL BH

- **Tuning of DIFFVM Monte Carlo**

- Reweighting of MC sample at generator level
- **|t| dependence**: $\sim \exp(-b|t|)$, generated with $b_{el} = 4.0$, $b_{pd} = 1.0$
reweighted to:
 $b_{el} = 4.6 \pm 0.3$, $b_{pd} = 1.0 \pm 0.1$ (JPSI)
 $b_{el} = 4.3 \pm 0.7$, $b_{pd} = 0.7 \pm 0.2$ (PSI2S)
- shrinkage added by reweighting: $b = b_0 + 4.0\alpha' \log(W/W_0)$;
 $\alpha' = 0.12 \pm 0.04 \text{ GeV}^{-2}$, $W_0 = 90 \text{ GeV}$ (elastic only)
- **W dependence**: $\sigma \sim W^\delta$,
generated with $\delta = 0.88$ for both elastic and p.diss
reweighted to:
 $\delta_{el} = 0.67 \pm 0.10$, $\delta_{pd} = 0.42 \pm 0.15$ (JPSI)
 $\delta_{el} = 1.10 \pm 0.20$, $\delta_{pd} = 0.70 \pm 0.30$ (PSI2S)
- **M_Y dependence**: $\sim \frac{1}{M_Y^\beta}$, generated with $\beta = 2.5$
reweighted to $\beta = 2.4 \pm 0.3$ (both JPSI and PSI2S, p.diss only)
- **all parameters are subject to systematics checks**

- **selection efficiency**

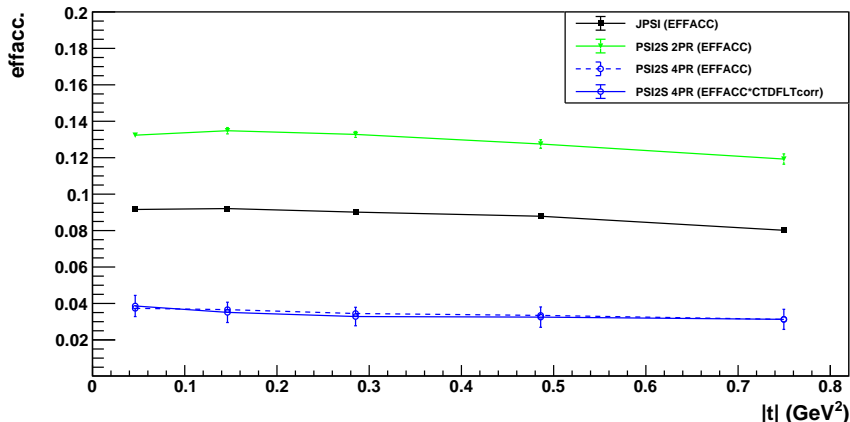
EFFACC (el) of JPSI, PSI2S-2PR, PSI2S-4PR vs. W



- JPSI, PSI2S 2- and 4-prong ($2 \div 16\%$)
- Higher di-muon acceptance for higher mass state (PSI2S)
- different angular coverage for final state muons
- second W bin ($W2$) is the “dip” for di-muon acceptance

Acceptance*efficiency in $|t|$ bins: elastic

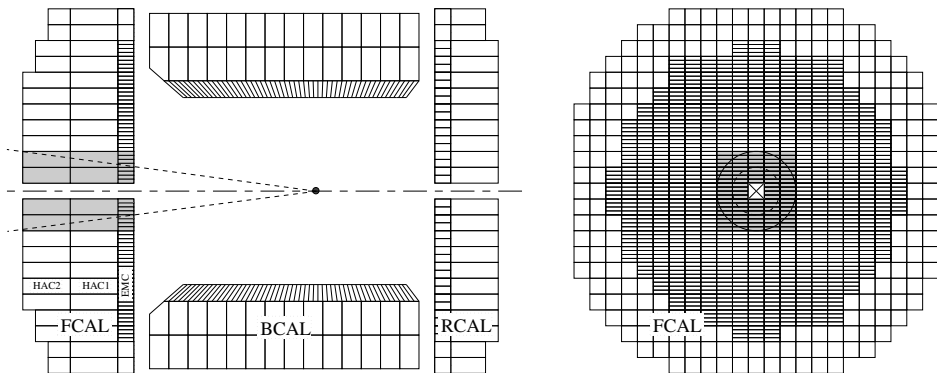
EFFACC (el) of JPSI, PSI2S-2PR, PSI2S-4PR vs. $|t|$



- JPSI, PSI2S 2- and 4-prong (**4 ÷ 12%**)
- Higher di-muon acceptance for higher mass state (**PSI2S**)
- flat in $|t|$ (no angular correlations to $|t|$)
- dashed line after CTD FLT corrections

- **extracting fractions of proton dissociation**

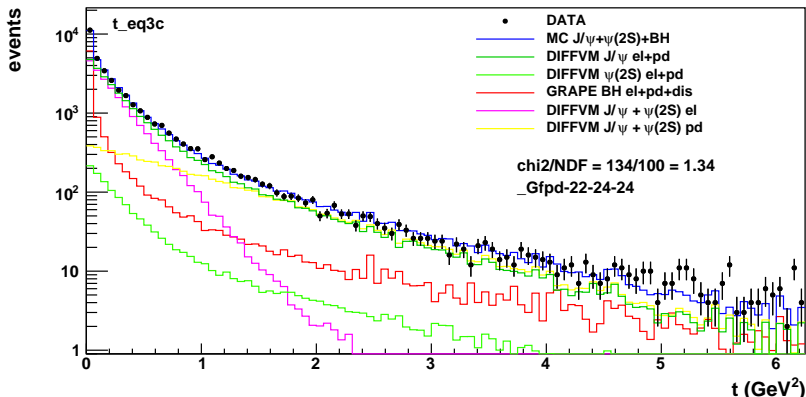
Proton dissociation taggers



- Energy in forward cone to **suppress p.diss events**: $\theta_{max} = 0.12 \text{ rad}$
- using EFO : “Energy Flow Objects” (trackers + CAL info):

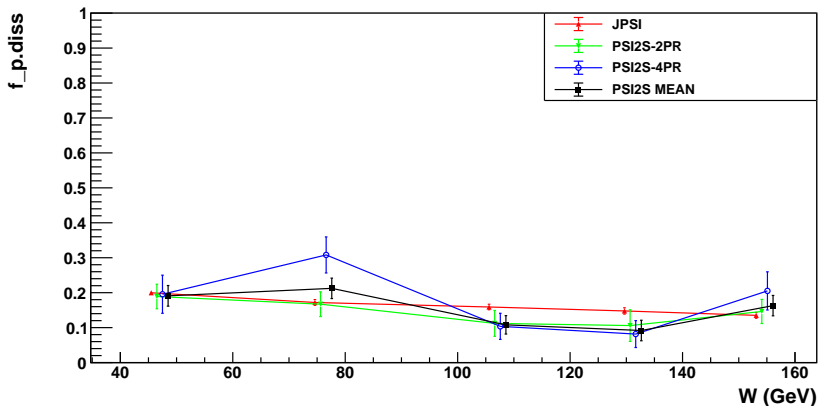
$$\left(\sum_{EFOs} E(\theta_{EFO} < \theta_{max}) \right) < 1 \text{ GeV}$$

2-prongs: $|t|$ distribution: all 2-prong events



- spectra like this are used to evaluate the p.diss fractions (use longer “lever arm” then integrate it up to $|t| = 1.0$ GeV²)
- using root package TFractionalFitter (TFF)
- fitted $f_{p.diss} = 0.17$ and $= 0.16$ (JPSI and PSI2S, BH subtracted)
- p.diss take over elastic around ~ 1 GeV² (yellow and magenta histos)

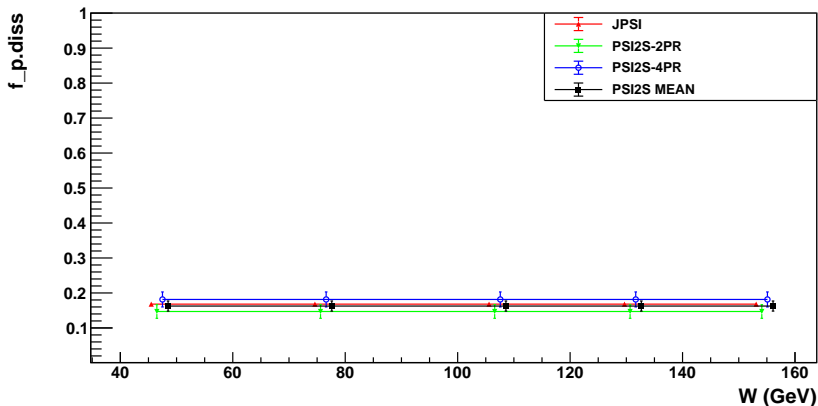
fraction $f_{p,diss}$: JPSI and PSI2S 2PR, 4PR vs. W



- average value $\sim 17\%$ JPSI and $\sim 16\%$ PSI2S (mean)
- compatible results for 2- and 4-prong channels, no W dependence
- **black**: weighted mean for PSI2S 2- and 4-prong
- bigger fluctuations for PSI2S 2- and 4-prongs

$f_{p,diss}$ fractions in W bins (TFF estimator)

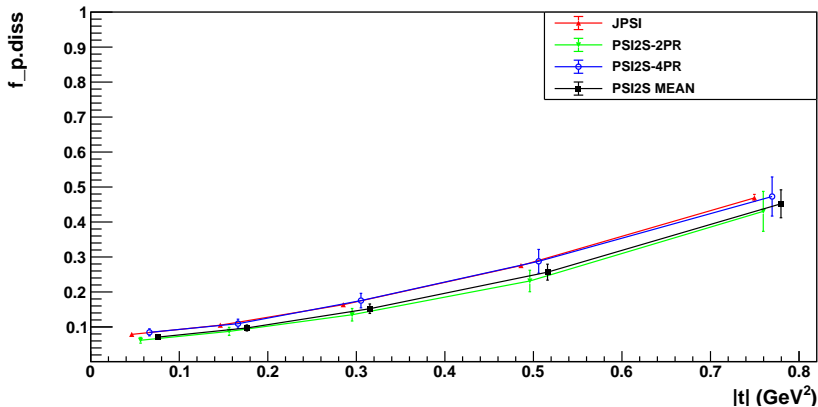
fraction $f_{p,diss}$: JPSI and PSI2S 2PR, 4PR vs. W



- average value $\sim 17\%$ JPSI and $\sim 16\%$ PSI2S (mean)
- **black**: weighted mean for PSI2S 2- and 4-prong (used in analysis)
- **for R analysis: the same mean value is used for all W bins**
- no significant impact on final ratio R ($f_{p,diss}$ fractions cancels out)

$f_{p,diss}$ fractions in $|t|$ bins (TFF estimator)

fraction $f_{p,diss}$: JPSI and PSI2S 2PR, 4PR vs. $|t|$



- compatible results for 2- and 4-prong channels
- **black**: weighted mean for PSI2S 2- and 4-prong (used in analysis)
- negligible effect on final R analysis ($f_{p,diss}$ fractions cancels out)
- bigger impact on systematics for large $|t|$ due to the b -slope variation !

- **Modeling of nucleon resonance states**
- (low M_Y proton dissociation)

- $\frac{d\sigma}{dM_Y^2} \sim \frac{1}{M_Y^{2(1+\epsilon)}}$ for $M_Y^2 \geq 3.6 \text{ GeV}^2$ (continuum region)
- $\frac{d\sigma}{dM_Y^2} \sim \frac{f(M_Y^2)}{M_Y^{2(1+\epsilon)}}$ for $M_Y^2 < 3.6 \text{ GeV}^2$ (p resonance region)
- $f(M_Y^2)$ from the **fit the the p.diss cross section on deuterium**:
 $pD \rightarrow YD$ (Phys. Rep. **101** (3) (1983), 169)
- for $M_Y < 1.9 \text{ GeV}$ several resonances are included
(Pomeron carries quantum numbers of the vacuum ($l=0, G = P = C = +$)
only N^{*+} states with $J^P = \frac{1}{2}^+, \frac{3}{2}^-, \frac{5}{2}^-, \dots$)
- $N^{*+} = N(1440), N(1520), N(1680), N(1700)$
- N^{*+} decays into: $N\pi, \Delta\pi, N\rho, N\pi\pi$ included (BR from PGD 1992)
- N^{*+} decays isotropically in their rest frame
- dissociation in the continuum state carried by JETSET
(splitting proton into $q - qq$ system, q couples to \mathbb{P} , leaving qq spectator)

- $d\sigma \sim L_{\mu\nu} W^{\mu\nu}$

- hadron tensor:

$$W^{\mu\nu} = W_1 \left(-g^{\mu\nu} + \frac{q^\mu q^\nu}{q^2} \right) + W_2 \frac{1}{M_p^2} \left(p_P^\mu - \frac{p_P \cdot q}{q^2} q^\mu \right) \left(p_P^\nu - \frac{p_P \cdot q}{q^2} q^\nu \right)$$

- $W_{1,2}(Q_P^2, M_{had})$ are proton electromagnetic structure functions

- for $M_{had} < 2$ GeV $W_{1,2}$ parameterized by Brasse at al. (Nucl. Phys. **B 110** (1976) 413.) (resonance region)

- for $M_{had} > 2$ GeV $W_{1,2}$ parameterized by ALLM97 (hep-ph/9712415) (continuum)

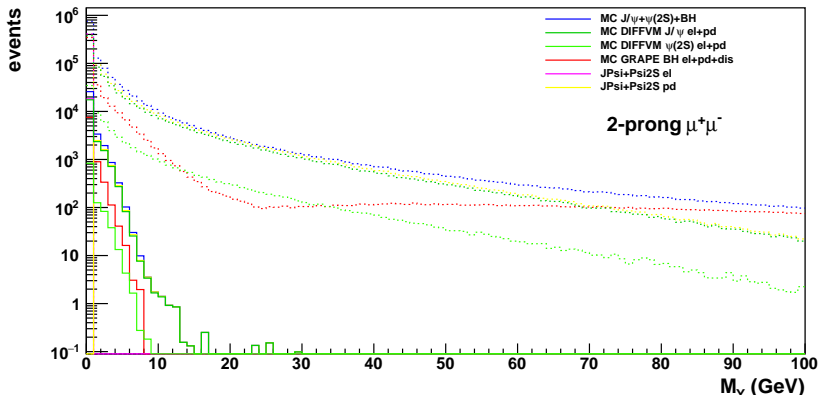
- both parameterizations from **fits to experimental total $\gamma^* p$ cross sections**

- exclusive hadronic final state generated by SOPHIA

- (plus DIS di-leptons diagrams, in the framework of QPM, using PDF's)

MC generator level: M_Y before and after selection cuts

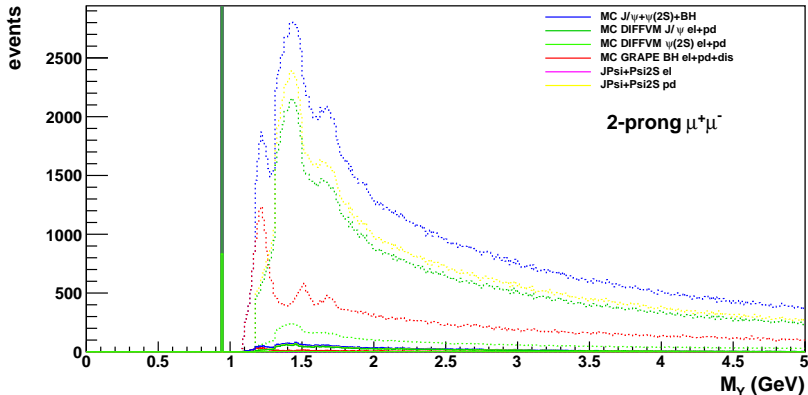
M_Y gener before and after cuts



- M_Y at generator level (not measured quantity ! \rightarrow lost in beam-pipe)
- before and after selection cuts
- **GRAPE (BH) does include DIS scattering \rightarrow rise of xsec. for large M_Y**
- DIFFVM in DIS mode generates only **electroproduction** (with proton dissociation, “rapidity gap events”) \rightarrow this is OK

MC generator level: zoom at low $M_Y < 5$ GeV (lin scale)

M_Y gener before and after cuts

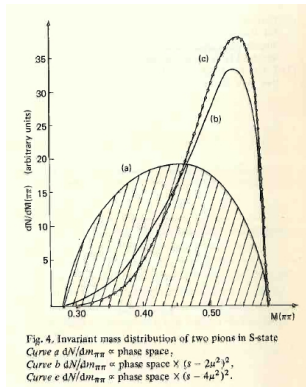


- different structure of nucleon resonances between GRAPE and DIFFVM (!?)
- which is right ?
- how much it is important for p.diss BG subtraction ?

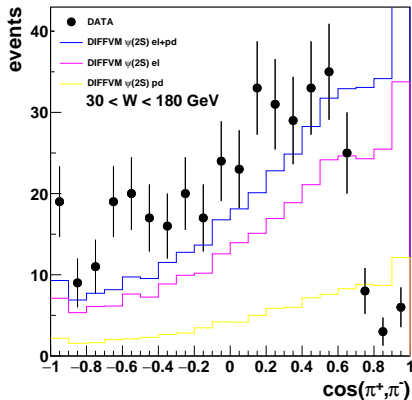
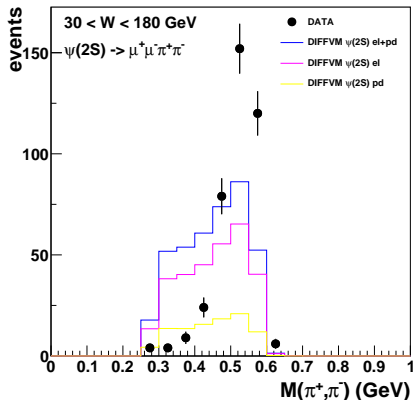
- **Pions phase space reweighting**

Pions phase space reweighting (DIFFVM 4-prongs)

- $weight = (M(\pi^-, \pi^+)^2 - 4.0 * M_\pi^2)^2$
- ref: Phys_Lett_B61_1976_183.pdf
- final $\pi^+\pi^-$ interaction is not in pure S-state
- → for the impact of this correction see next 2 pages

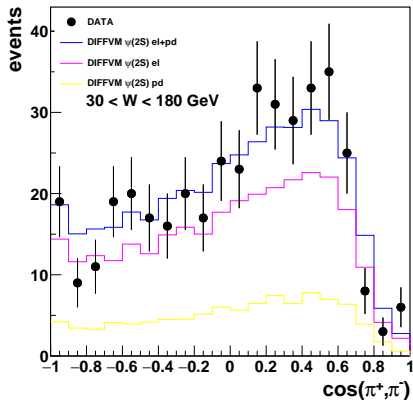
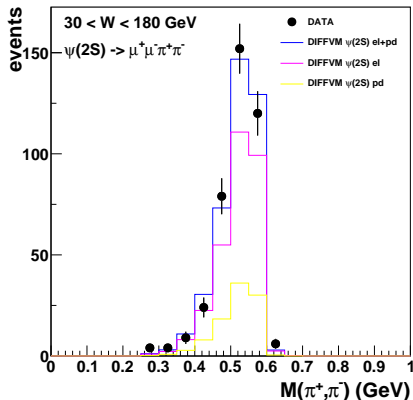


4-PRONGS: $M(\pi^-, \pi^+)$, $\cos(\pi^-, \pi^+)$



- $\psi' \rightarrow J/\psi + \pi^+ \pi^-$
- $M(\pi^-, \pi^+)$, $\cos(\pi^-, \pi^+)$
- DIFFVM MC **before** pions phase space reweighting

4-PRONGS: $M(\pi^-, \pi^+)$, $\cos(\pi^-, \pi^+)$



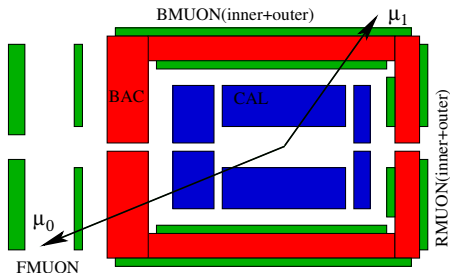
- $\psi' \rightarrow J/\psi + \pi^+ \pi^-$
- $M(\pi^-, \pi^+)$, $\cos(\pi^-, \pi^+)$
- DIFFVM MC **after** pions phase space reweighting

- **Muon effic. corrections**

Muon effic. corrections: TAG and PROBE

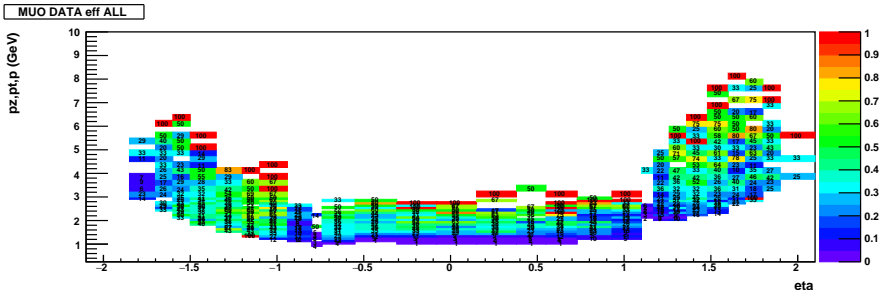
- TAG: “the triggering” muon
- PROBE: “the tested” muon
- effic in given $(p_{t_{eff}}^j, \eta^j)$ bin:

$$\epsilon = N_{PROBE}^j / N_{TAG}^i$$



- **one step correction** for (FLT and SLT and TLT and off-line REC)
- separate maps for F/B/R/MUO, BAC and CAL (off-line only)
- evaluated for single muon **in $(p_{t_{eff}}, \eta)$ bins**, where as $p_{t_{eff}}$ is used:
(motivated by the CAL/BAC geometry and scaling of the muon path length)
 - p in Forecap
 - p_t in Barrel
 - p_z in Rearcap
- proper identification of **the triggering muon** is crucial
- → the DATA/MC ratio delivers the correction weight: $\epsilon_x = \frac{\epsilon_{DATA}}{\epsilon_{MC}}$

Muon correction maps: (p_z, p_t, p vs. η) - DATA



- muon tomography
- probability (%) to fire FLT-SLT-TLT-REC chain by single muon on ($p_z, p_t, p; \eta$) grid
- X-axis (along eta): Rear-MUO, Barrel-MUO, Forward-MUO detectors
- only events with $M(\mu^+, \mu^-) < 6$ GeV
(ie. in the phase space range of di-muon mass fits)
- current choice for p_z, p_t, p grid: 100 MeV per bin ($p_{eff} < 3$ GeV), 250 MeV per bin ($p_{eff} > 3$ GeV)
- size of the grid is subject to systematics