

ZEUS measurement of the cross-section ratio $\sigma(\Psi(2S))/\sigma(J/\Psi)$ in exclusive ep scattering at HERA

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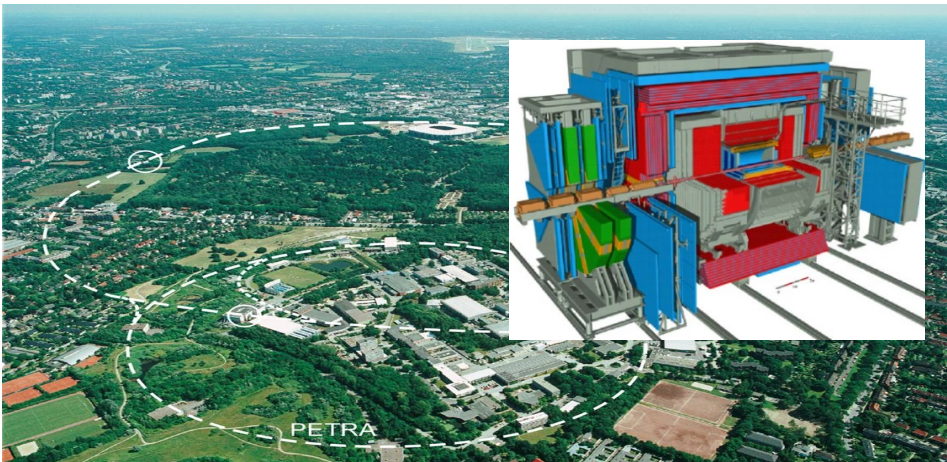


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Cavallerizza Reale, Torino, Italy, May 13-17, 2019.*

- 1 Experimental apparatus: the HERA accelerator and the ZEUS detector
- 2 Introduction: Vector Meson Production in Exclusive Diffraction in ep Scattering
- 3 Analysis: Events selection and extraction of the signal
- 4 Results: Cross section ratio $\psi(2S)/J/\psi(1S)$ in DIS (electroproduction)
- 5 Results: Cross section ratio $\psi(2S)/J/\psi(1S)$ in photoproduction
- 6 Summary

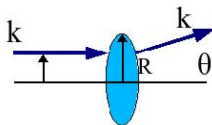
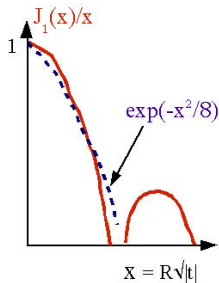
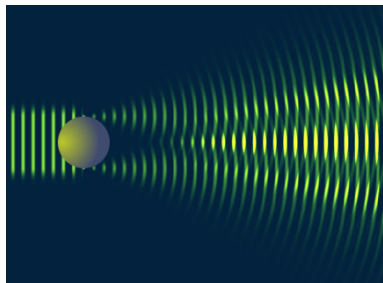
HERA and ZEUS: 1992 – 2007, DESY, Hamburg

HERA: world's first and only $e^\pm p$ collider, $E_e = 27.5 \text{ GeV}$, $E_p = 920 \text{ GeV}$ ($\sqrt{s} = 318 \text{ GeV}$)



ZEUS: multipurpose, hermetic detector (MVD, CTD, CAL, F/B/RMUON, BAC, ...)

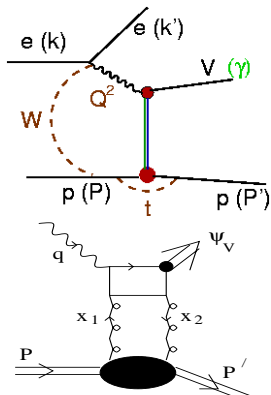
Total luminosity: $\int \mathcal{L} \sim 500 \text{ pb}^{-1}$ collected during HERA I + II running periods



Light Scattering in Fraunhofer approximation (wavelength $\lambda \sim 1/k \ll R$)

- $|t| = 4k^2 \sin^2(\theta/2)$
- $d\sigma/dt \sim e^{-b|t|}$ (first diffractive peak approximated from Bessel function)
- $b = (R/2)^2 \rightarrow$ transverse size of the target
- in the presented studies: **target \equiv proton** and **photon energy $\gg 1$ GeV**

Production of Vector Mesons in Exclusive Diffraction in ep Scattering



Exclusive process: proton stays intact
 Proton dissociation also possible \rightarrow
 background

pQCD: M_V^2 and Q^2 - set the scale at which the W and $|t|$ are probed

Kinematics: $M_V^2, Q^2, W, |t|$

M_V^2 - vector meson mass squared

$Q^2 (= -q^2 = -(k - k')^2)$ - the photon virtuality
 (emitted by the incoming electron):

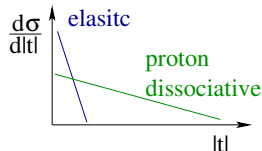
- $Q^2 \approx 0$ GeV² PHP (*Photoproduction*)
- larger Q^2 for DIS (*Deep Inelastic Scattering*)

$W = (q + P)^2$ - invariant mass of the γp system

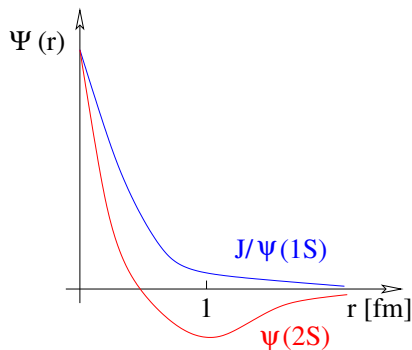
Process sensitive to the
gluon density in the proton

$|t|$ - 4-momentum transfer at the proton vertex

$t = (P - P')^2$



Cross section ratio $\psi(2S)/J/\psi(1S)$: physics motivation



$$\text{Ratio } R = \frac{\sigma_{\gamma p \rightarrow \psi(2S)p}}{\sigma_{\gamma p \rightarrow J/\psi(1S)p}}$$

- sensitive to radial wave function of charmonium
- provides insight into the dynamics of the hard process

- $J/\psi(1S)$ and $\psi(2S)$ have distinctive wave functions
- $\psi(2S)$ has a node at ≈ 0.4 fm
- $\langle r_{\psi(2S)}^2 \rangle \approx 2 \langle r_{J/\psi(1S)}^2 \rangle$
- pQCD models predict $R \sim 0.17$ in PHP and moderate rise of R with Q^2 in DIS
- ψ' cross section is expected to be suppressed w.r.t. the J/ψ production

- Investigated decay channels:

- $\psi(2S) \rightarrow J/\psi + \pi^+\pi^-$, $\psi(2S) \rightarrow \mu^+\mu^-$, $J/\psi(1S) \rightarrow \mu^+\mu^-$

- HERA I+II: $\mathcal{L} = 468 \text{ pb}^{-1}$ (1996 - 2007) with $5 < Q^2 < 80 \text{ GeV}$ (DIS)

- subsample of 114 pb^{-1} (HERA I) with $2 < Q^2 < 5 \text{ GeV}$ (DIS)

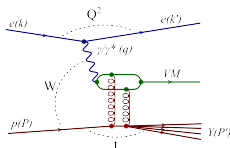
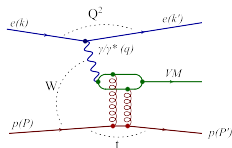
- HERA II: $\mathcal{L} = 333 \text{ pb}^{-1}$ (2003 - 2007) $Q^2 < 1 \text{ GeV}$ (PHP)

- MC Samples: Signal: **DIFFVM** for exclusive VM production (J/ψ and ψ')

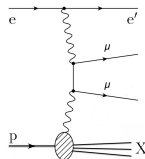
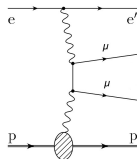
- $\frac{d\sigma}{dQ^2} \sim \frac{1}{(1+Q^2/M_V^2)^{1.5}}$

- $\frac{d\sigma}{d|t|} \sim \exp(-b|t|)$,

$b = 4.0 \text{ GeV}^{-2}$



- Background: **GRAPE** for non resonant muon pair production (Bethe-Heitler process)



Events selection (DIS channel)

$$\psi(2S) \rightarrow \mu^+ \mu^- \pi^+ \pi^- \Rightarrow$$

Event selection:

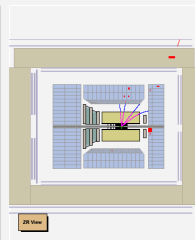
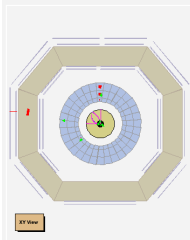
- scattered electron $E_{e'}$ > 10 GeV in CAL
- 2 (4 for $\psi(2S)$ 4-prongs decay) non-electron tracks from primary vertex, net charge = 0
- two tracks identified as muons (CAL, F/B/R/MUO, BAC)
- no other deposits not matched to tracks (above CAL noise)
 - proton remains undetected

Kinematic range:

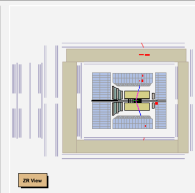
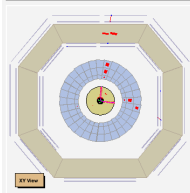
- (2) $5 \leq Q^2 \leq 80 \text{ GeV}^2$
- $30 \leq W \leq 210 \text{ GeV}$
- $|t| \leq 1 \text{ GeV}^2$

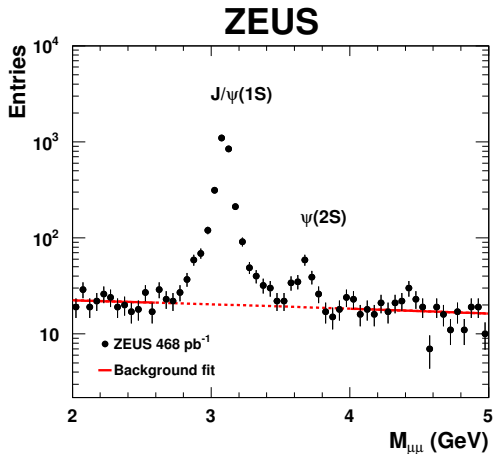
$$J/\psi(1S) \rightarrow \mu^+ \mu^- \Rightarrow$$

iZeus Run 52671 Event 17004 date: 9-01-2005 time: 23:59:12				
E=19.2 GeV	E _e =4.62 GeV	E-p _e =36.5 GeV	E _e =0 GeV	E _e =1.55 GeV
E _e =17.6 GeV	p _e =1.13 GeV	p _e =1.12 GeV	p _e =-0.144 GeV	p _e =-17.4 GeV
phi=-0.13	t _e =100 ns	t _e =-0.0658 ns	t _e =-1.41 ns	t _e =-1.33 ns
E _{SRA} =16.8 GeV	Q _{SRA} =3.01	Q _{SRA} =-0.65	Prob _{SRA} =0.999	x _{SRA} =0.00
y _{SRA} =0.15	Q _{SRA} ² =11.86 GeV ²			



iZeus Run 61827 Event 72057 date: 8-01-2007 time: 22:39:07				
E=21 GeV	E _e =5.15 GeV	E-p _e =39.4 GeV	E _e =0.087 GeV	E _e =3.5 GeV
E _e =17.5 GeV	p _e =1.38 GeV	p _e =1.38 GeV	p _e =-0.0155 GeV	p _e =-18.3 GeV
phi=0.01	t _e =100 ns	t _e =1.13 ns	t _e =1.86 ns	t _e =1.74 ns
E _{SRA} =17.4 GeV	Q _{SRA} =3.02	Q _{SRA} =-2.05	Prob _{SRA} =0.999	x _{SRA} =0.00
y _{SRA} =0.12	Q _{SRA} ² =10.25 GeV ²			

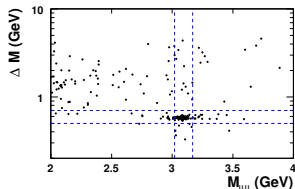




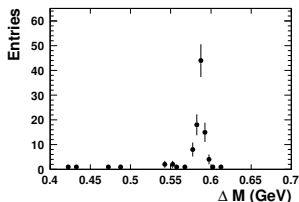
- $J/\psi(1S) \rightarrow \mu^+\mu^-$
- $\psi(2S) \rightarrow \mu^+\mu^-$
- BG (BH): $\gamma\gamma \rightarrow \mu^+\mu^-$

- mass intervals for side-band straight-line background fit and signal extraction:
 BG: 2.00 – 2.62 GeV and 4.05 – 5.00 GeV
 Signal $J/\psi(1S)$: 3.02 – 3.17 GeV , Signal $\psi(2S)$: 3.59 – 3.79 GeV

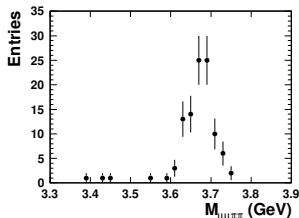
Selection specific for $\psi(2S) \rightarrow \mu^+ \mu^- \pi^+ \pi^-$ channel



- ΔM vs. $M_{\mu^+\mu^-}$
 $\Delta M = M(\mu^+ \mu^- \pi^+ \pi^-) - M(\mu^+ \mu^-)$
cascade decay of $\psi(2S)$



- $0.5 < \Delta M < 0.7$ GeV
 $3.02 < M_{\mu^+\mu^-} < 3.17$ GeV



- $M(\mu^+ \mu^- \pi^+ \pi^-)$ after cleanup
very clean signature
(≤ 3 background events at 90% CL)

Cross section ratio $R = \frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$ (DIS) for full kinematic range

For $30 \leq W \leq 210$ GeV, $5 \leq Q^2 \leq 80$ GeV², $|t| \leq 1$ GeV²

$\psi(2S)$ decay mode	$R = \frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$
$\rightarrow J/\psi(\rightarrow \mu^+\mu^-)\pi^+\pi^-$	$0.26 \pm 0.03^{+0.01}_{-0.01}$
$\rightarrow \mu^+\mu^-$	$0.24 \pm 0.05^{+0.02}_{-0.03}$
combined	$0.26 \pm 0.02^{+0.01}_{-0.01}$

Nucl. Phys. **B 909** (2016) 934.

- both channels provide consistent results

- $$R_{\psi(2S) \rightarrow J/\psi \pi^+ \pi^-} = \frac{\sigma_{\psi(2S)}}{\sigma_{J/\psi(1S)}} = \frac{N_{\psi(2S)}}{N_{J/\psi(1S)}} \cdot \frac{Acc_{J/\psi(1S) \rightarrow \mu^+ \mu^-}}{Acc_{\psi(2S) \rightarrow J/\psi \pi^+ \pi^-}} \cdot \frac{1}{BR_{\psi(2S) \rightarrow J/\psi \pi^+ \pi^-}}$$

- $$R_{\psi(2S) \rightarrow \mu^+ \mu^-} = \frac{\sigma_{\psi(2S)}}{\sigma_{J/\psi(1S)}} = \frac{N_{\psi(2S)}}{N_{J/\psi(1S)}} \cdot \frac{Acc_{J/\psi(1S) \rightarrow \mu^+ \mu^-}}{Acc_{\psi(2S) \rightarrow \mu^+ \mu^-}} \cdot \frac{BR_{J/\psi(1S) \rightarrow \mu^+ \mu^-}}{BR_{\psi(2S) \rightarrow \mu^+ \mu^-}}$$

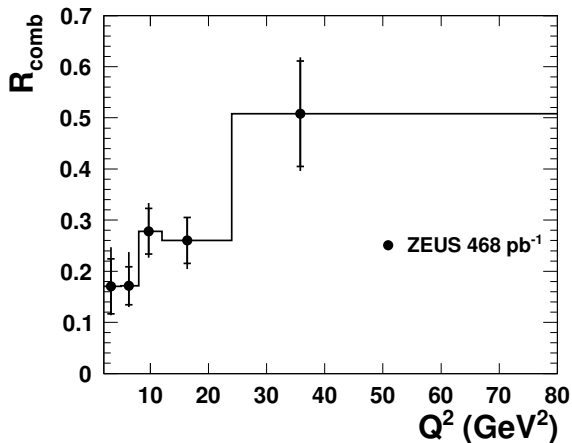
- $$Acc_i = \frac{N_i^{reco}}{N_i^{true}}$$

- $$BR(\psi(2S) \rightarrow J/\psi \pi^+ \pi^-) = (33.6 \pm 0.4)\%, BR(\psi(2S) \rightarrow \mu^+ \mu^-) = (7.7 \pm 0.8) \times 10^{-3},$$

- $$BR(J/\psi \rightarrow \mu^+ \mu^-) = (5.93 \pm 0.06)\%$$

Ratio $R = \frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$ vs. Q^2 (DIS: combined 2- and 4-prong channels)

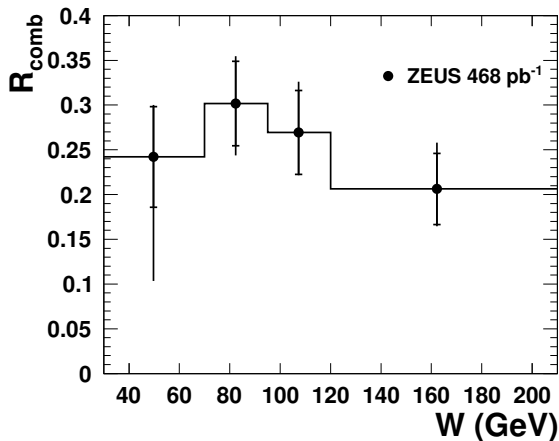
ZEUS



● R rises with Q^2

Ratio $R = \frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$ vs. W (DIS: combined 2- and 4-prong channels)

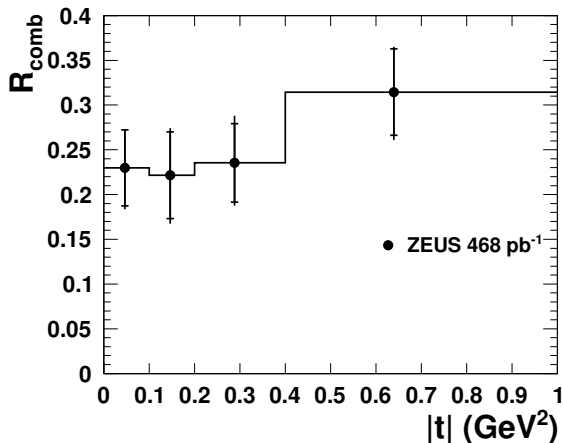
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- R independent of W

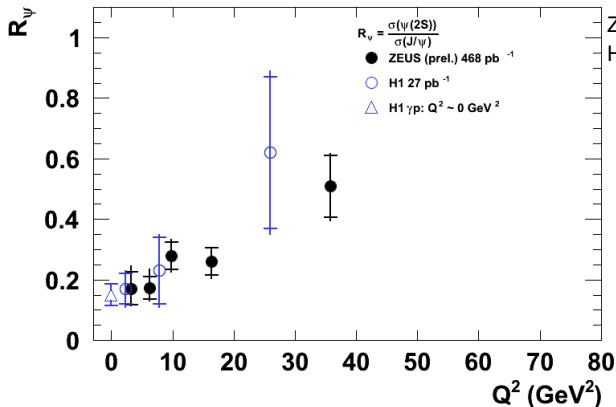
Ratio $R = \frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$ vs. $|t|$ (DIS: combined 2- and 4-prong channels)

ZEUS

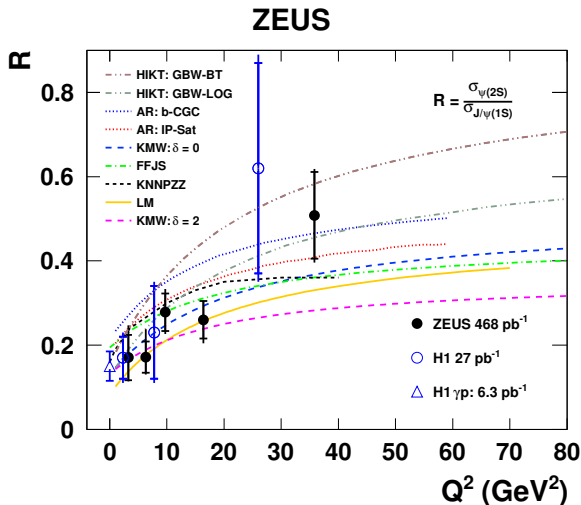


- R independent of $|t|$

ZEUS

ZEUS: Nucl. Phys. **B 909** 934 (2016)H1: EPJ **C10** 373 (1999)

- ZEUS: full HERA I + HERA II data sample (468 pb^{-1}) (incl. low- Q^2 point)
- both ZEUS and H1 measurements are in agreement: R increases with Q^2
- ZEUS improved accuracy due to the increased statistic of HERA I+II data



theoretical models:

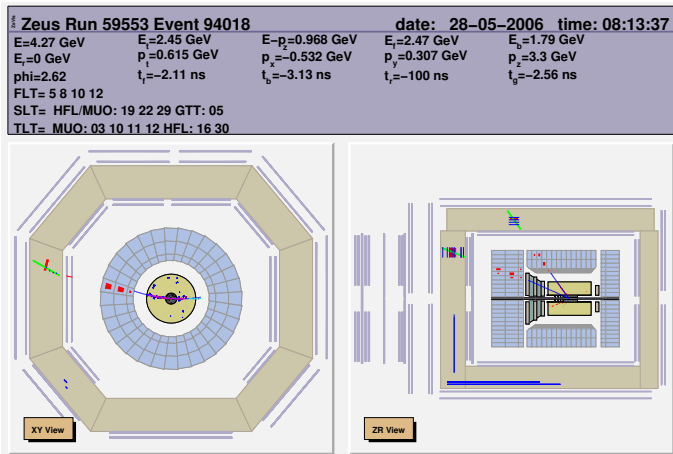
- HIKT: J. Hüfner et al., Phys. Rev. **D 62**, 094022 (2000).
- KNNPZZ: B.Z. Kopeliovich, et al., Phys. Rev. **D 44**, 3466 (1991), Phys. Lett. **B 324**, 469 (1994), Phys. Lett. **B 341**, 228 (1994), J. Exp. Theor. Phys. **86**, 1054 (1998).
- AR: N. Armesto and A.H. Reazeian, Phys. Rev. **D 90**, 054003 (2014).
- LM: T. Lappi and H. Mäntysaari, Phys. Rev. **C 83**, 065202 (2011).
- FFJS: S. Fazio et al., Phys. Rev. **D 90**, 016007 (2014).
- KMW: H. Kowalski, L. Motyka and G. Watt, Phys. Rev. **D 74**, 074016 (2006).

- All models predict the rise of $\sigma(\psi(2S))/\sigma(J/\psi)$ with Q^2
- ...data begin to discriminate some models (see also backup plots for more details)

Cross section ratio $R = \frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$ in photoproduction

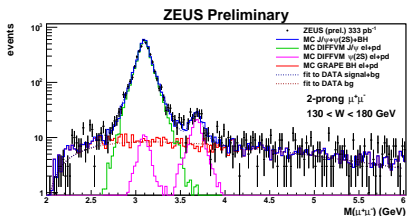
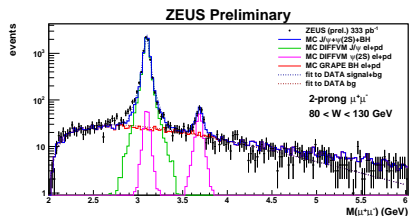
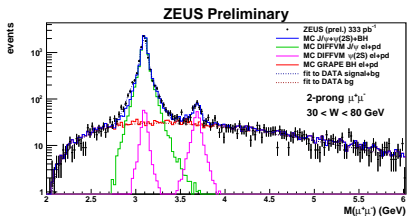
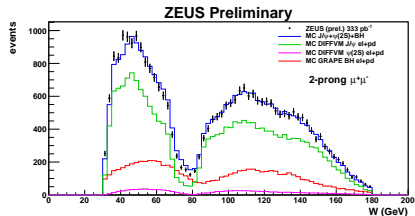
- Cross section ratio $R = \frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$ in photoproduction

Event selection (photoproduction channel)



- no scattered electron observed in the calorimeter, otherwise selection very similar to DIS channel
- very clean signature, **selection** entirely **driven by muons** starting from trigger
- $30 < W < 180$ GeV (limited by muon chambers)
- experimental challenge: very good understanding of muon efficiency for all components

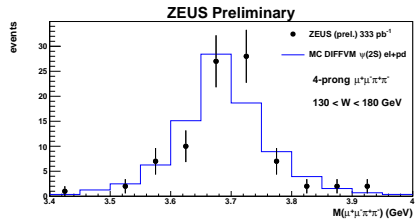
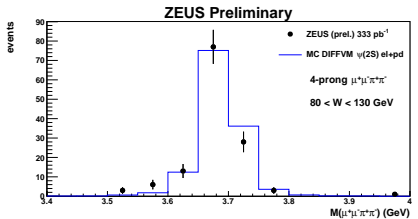
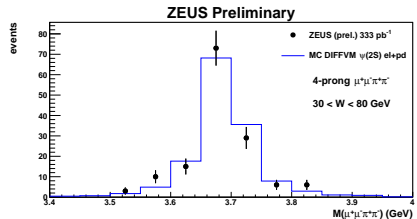
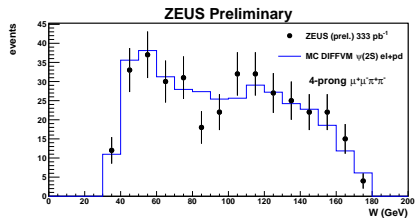
2-prong sample: $\psi(2S) \rightarrow \mu^+ \mu^-$ (photoproduction)



- W and $M(\mu^+\mu^-)$ distributions for 3 W intervals (30-80), (80-130), (130-180) GeV
- DIFFVM J/ψ , $\psi(2S)$ and GRAPE BH MC normalized to data (fractional fit)
- double Gaussian fit to data for signal extraction

- $W = \sqrt{2E_P(E_{TOT} - P_Z)}$, $P_Z = p^{\mu^+} \cos(\theta^{\mu^+}) + p^{\mu^-} \cos(\theta^{\mu^-})$

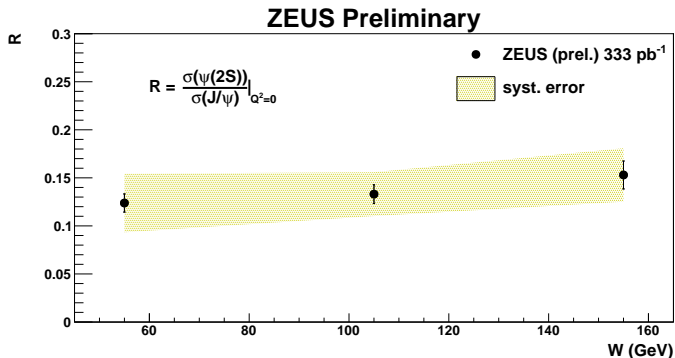
4-prong sample: $\psi(2S) \rightarrow \mu^+ \mu^- \pi^+ \pi^-$ (photoproduction)



- $W, M(\mu^+ \mu^- \pi^+ \pi^-)$ distributions for 3 W intervals (30-80), (80-130), (130-180) GeV
- very clean (almost) background free channel
- DIFFVM $\psi(2S)$ MC normalized to data

- $W = \sqrt{2E_P(E_{TOT} - P_Z)}$,
 $P_Z = p^{\mu^+} \cos(\theta^{\mu^+}) + p^{\mu^-} \cos(\theta^{\mu^-}) + p^{\pi^+} \cos(\theta^{\pi^+}) + p^{\pi^-} \cos(\theta^{\pi^-})$

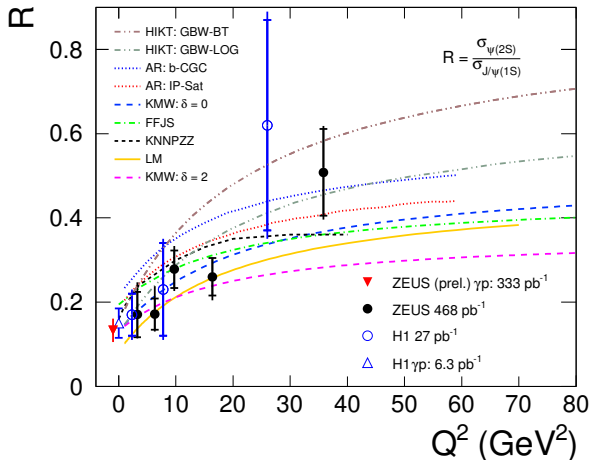
$$R = \frac{\sigma_{\gamma p \rightarrow \psi(2S)p}}{\sigma_{\gamma p \rightarrow J/\psi(1S)p}} \text{ vs. } W \text{ at } Q^2 = 0 \text{ GeV}^2 \text{ (photoproduction)}$$



- **average R values** over 2- and 4-prong channels
- moderate rise of R with photon-proton centre-of-mass W
- systematics dominated by 2- and 4-prong channel difference

$$R = \frac{\sigma_{\gamma p \rightarrow \psi(2S)p}}{\sigma_{\gamma p \rightarrow J/\psi(1S)p}} \text{ vs. } Q^2 \text{ including new } Q^2 = 0 \text{ measurement}$$

ZEUS preliminary



theoretical models:

- HIKT: J. Hüfner et al., Phys. Rev. **D 62**, 094022 (2000).
- KNNPZZ: B.Z. Kopeliovich, et al., Phys. Rev. **D 44**, 3466 (1991), Phys. Lett. **B 324**, 469 (1994), Phys. Lett. **B 341**, 228 (1994), J. Exp. Theor. Phys. **86**, 1054 (1998).
- AR: N. Armesto and A.H. Reazeian, Phys. Rev. **D 90**, 054003 (2014).
- LM: T. Lappi and H. Mäntysaari, Phys. Rev. **C 83**, 065202 (2011).
- FFJS: S. Fazio et al., Phys. Rev. **D 90**, 016007 (2014).
- KMW: H. Kowalski, L. Motyka and G. Watt, Phys. Rev. **D 74**, 074016 (2006).

● highest precision $Q^2 = 0 \text{ GeV}^2$ measurement

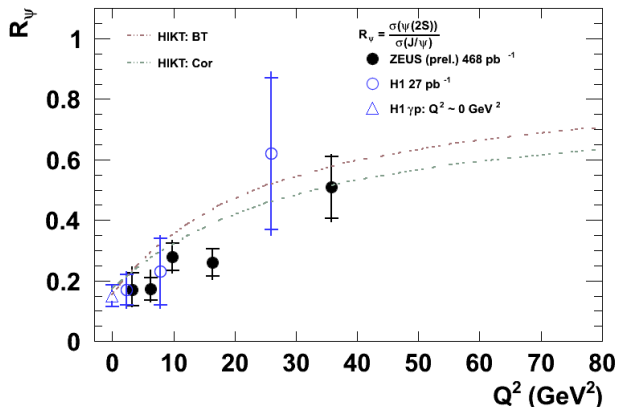
● $R = 0.1332 \pm 0.0065(\text{stat.}) \pm 0.0270(\text{syst.})$ (average over full phase space)

- **Ratio of $\frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$** using HERA I+II data was measured for the first time by ZEUS in the kinematic range: $30 \leq W \leq 210$ GeV, $2 \leq Q^2 \leq 80$ GeV², $|t| \leq 1$ GeV² for exclusive DIS and in $30 \leq W \leq 180$ GeV for photoproduction ($Q^2 \approx 0$)
- The accuracy has been improved compared to the H1 HERA I results
- The ratio increases with Q^2 and is constant as a function of W and $|t|$
- Theoretical calculations of the ratio $\frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$ for exclusive vector-meson production has been compared to the experimental data
→ majority of the predictions are consistent with the data
- **data start to exhibit constraining power**

Thank You For Your Attention

BACKUP PLOTS FOLLOW...

ZEUS



Phys. Rev. **D 62** 094022 (2000)

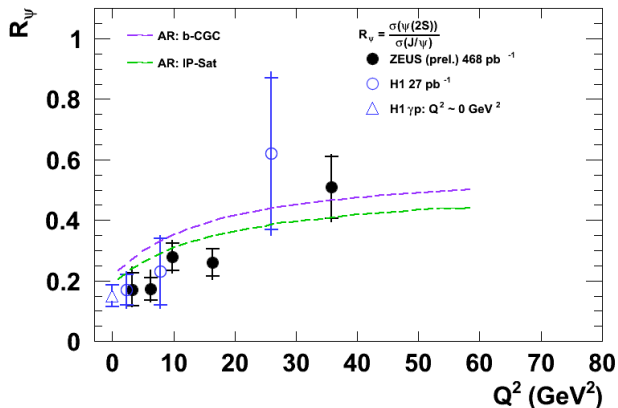
Phys. Rev. **D 59** 14017 (1999)

Phys. Rev. **D 62** 054022 (2000)

$$V(r) \sim -\frac{k}{r} + \frac{r}{a^2}$$

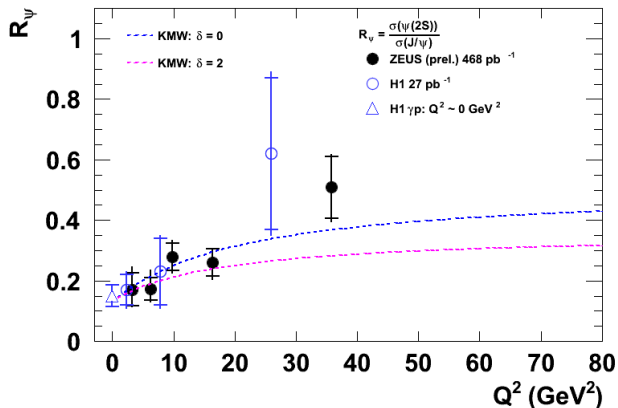
- HIKT: Hüfner et al. → adopt the light-cone dipole formalism to describe VM production, the dipole - proton interaction cross section is constrained by inclusive low-x DIS data from HERA (BT and Cor: different charmonium potentials with $m_c \approx 1.5$ GeV)
- HIKT - BT: overestimates lower Q^2 points

ZEUS

Phys. Rev. D **90** 054003 (2014)

- AR: Armesto and Rezaeian → two predictions are presented: results from the Impact-Parameter dependent Color Glass Condensate (b-CGC) and the gluon Saturation (IP-Sat) dipole models
- b-CGC overestimates lower Q^2 points

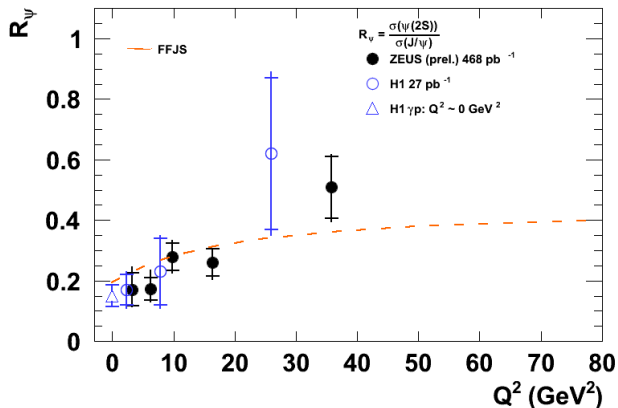
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Phys. Rev. D **74** 074016 (2006)

- KMW: Kowalski, Motyka, Watt → impact parameter dependent saturated dipole model, based on the QCD description and an assumption of universality of the gluon distribution and proton shape: $\delta = 0$ non-relativistic wave functions, $\delta = 2$ relativistic boosted Gaussian model

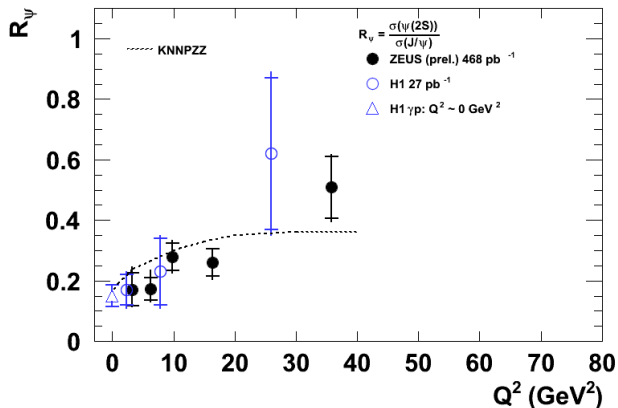
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Phys. Rev. D **90** 016007 (2014)

- FFJS: Fazio et al. → two component Pomeron model to predict the cross sections for Vector Meson production. The Pomeron is universal, containing two terms, a “soft” and a “hard” one: relative weights: $\sim \tilde{Q}^2 = Q^2 + M_V^2$.

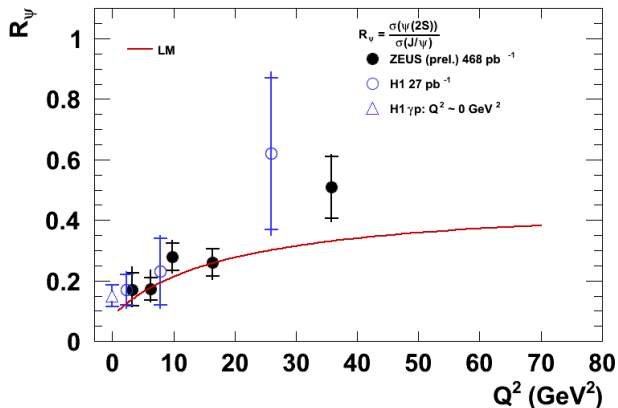
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Phys. Lett. B 342 228 (1994)

- KNNPZZ: Kopeliovich et al. \rightarrow describe the BFKL Pomeron in terms of the colour-dipole cross section which is a solution of the generalized BFKL equations

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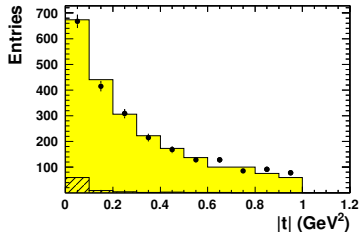
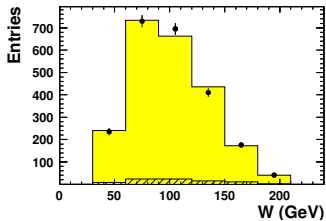
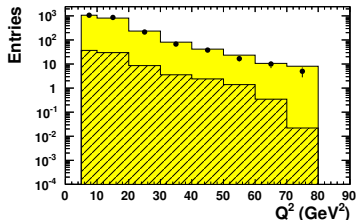


Phys. Rev. C **83** 065202 (2011)

- LM: Lappi and Mäntysaari → use the BFKL evolution as well as the dipole picture in the IP-Sat model to predict VM production

Control plots for $J/\psi \rightarrow \mu^+ \mu^-$ channel

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$J/\psi(1S) \rightarrow \mu^+ \mu^-$

• ZEUS 468 pb⁻¹

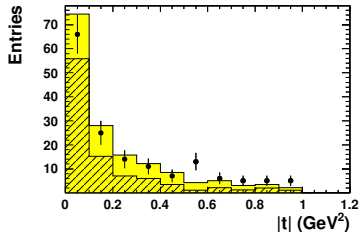
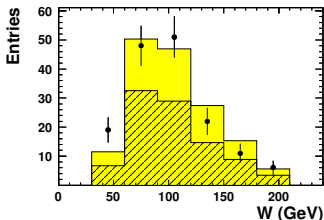
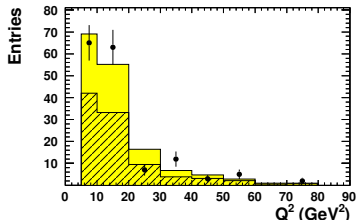
■ DIFFVM + BH

▨ BH

- MC reweighted in Q^2 , $|t|$ and J/ψ decay angles to match the data
- good description \rightarrow detector efficiency calculation

Control plots for $\psi(2S) \rightarrow \mu^+ \mu^-$ channel

ZEUS



$\psi(2S) \rightarrow \mu^+ \mu^-$

• ZEUS 468 pb⁻¹

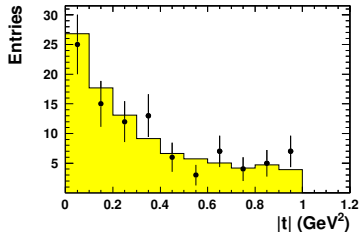
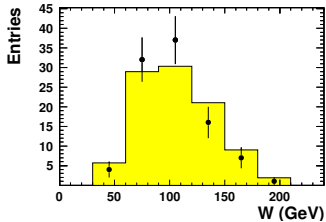
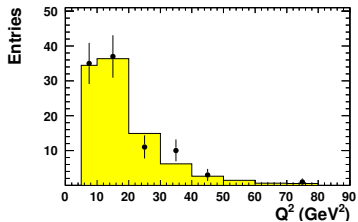
■ DIFFVM + BH

▨ BH

- MC reweighted in Q^2 , $|t|$ and $\psi(2S)$ decay angles using $J/\psi \rightarrow \mu^+ \mu^-$ weights
- good description \rightarrow detector efficiency calculation

Control plots for $\psi(2S) \rightarrow \mu^+ \mu^- \pi^+ \pi^-$ channel

ZEUS



$\psi(2S) \rightarrow J/\psi(1S) \pi^+ \pi^-$

• ZEUS 468 pb⁻¹

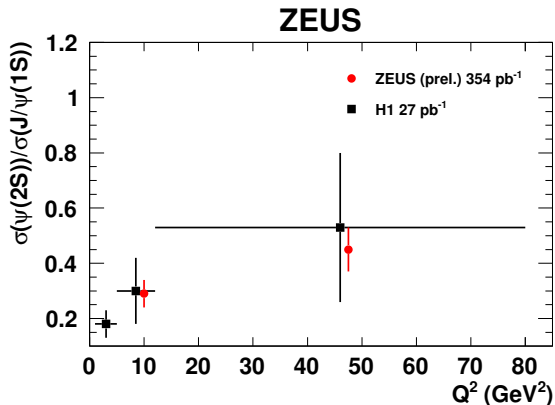
■ DIFFVM

● MC reweighted in Q^2 and $|t|$
using $J/\psi \rightarrow \mu^+ \mu^-$ weights

● good description \rightarrow detector efficiency calculation

ZEUS to H1 comparison (in H1 phase space and H1 bins)

- cross check: ZEUS data analyzed in Q^2 bins used by H1: [EPJ **C10** (1999) 373.]
(5 – 12) GeV^2 and (12 – 80) GeV^2
- $40 < W < 180$ GeV and $1 < Q^2 < 80$ GeV^2



- both measurements are in agreement
- improved accuracy due to the increased statistic of HERA II data

Systematics checks (2-prongs and 4-prongs channels)

- varying the $M_{\mu\mu}$ window for signal event counting:
 - for $J/\psi(1S)$: from 3.02 – 3.17 GeV to 3.05 – 3.15 GeV and 2.97 – 3.19 GeV
 - for $\psi(2S)$: from 3.59 – 3.79 GeV to 3.62 – 3.75 GeV and 3.55 – 3.80 GeVchanges the values of $R_{\mu\mu}$ by 6% and $R_{J/\psi\pi\pi}$ by 2%
- varying the cut on pions transverse momenta p_T from 0.12 GeV to 0.15 GeV changes the $R_{J/\psi\pi\pi}$ by 4.5%
- changing the background fit function from linear to quadratic changes the values of $R_{\mu\mu}$ by 11% and $R_{J/\psi\pi\pi}$ by 0.5%
- changing the reconstruction of kinematic variables from “constrained” to “electron” method changes the values of $R_{\mu\mu}$ and $R_{J/\psi\pi\pi}$ by 1.5%
- not reweighting the MC samples changes the values of $R_{\mu\mu}$ by 3% and $R_{J/\psi\pi\pi}$ by 1%
- applying more restrictive cuts on the number of (soft/noisy) tracks not associated with the event vertex changes the values of $R_{\mu\mu}$ by 5% and $R_{J/\psi\pi\pi}$ by 3%

Total systematic uncertainties are: $\delta R_{\mu\mu} = {}^{+7}_{-14}\%$, $\delta R_{J/\psi\pi\pi} = {}^{+4}_{-5}\%$ and $\delta R = {}^{+3}_{-5}\%$

$\psi(2S) \rightarrow \mu^+ \mu^-$ channel:

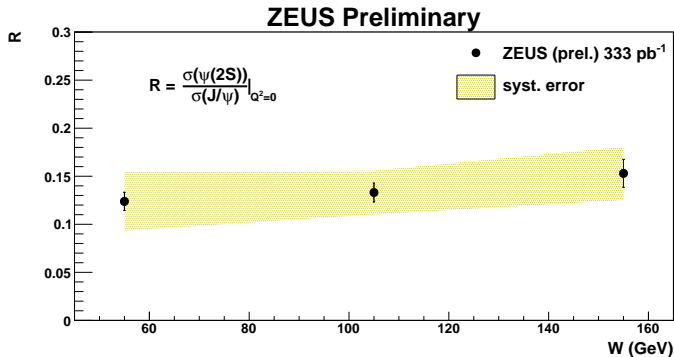
- **exclusive muon triggers**
- vertex consistent with ep interaction
- $N_{track} = 2$ (oppositely charged)
- $p_T > 1$ GeV (of each track)
- **muon identification:**
 - at least one track identified by muon detectors or BAC
 - both tracks matched to MIP clusters in CAL
- no scattered beam-electron in the CAL
- $\cos(\mu^+, \mu^-) > -0.9$ (cosmic rejection)
- elasticity cut (no CAL clusters other than 2 MIPs)
- $30 < W < 180$ GeV, $|t| < 5$ GeV², $2 < M(\mu^+, \mu^-) < 6$ GeV.

$\psi(2S) \rightarrow \mu^+ \mu^- \pi^+ \pi^-$ channel:

(differences w.r.t. the 2-prong channel)

- $N_{track} = 4$ (two oppositely charged pairs, sorted by p_T)
- highest momentum pair: muon candidates
lowest momentum pair: pion candidates
- transverse momentum of pion candidates: $p_T^\pi > 0.12$ GeV;
- $2.8 < M(\mu^+ \mu^-) < 3.4$ GeV (J/ψ window)
- $M(\mu^+ \mu^- \pi^+ \pi^-) - M(\mu^+ \mu^-)$ in (0.5 – 0.7) GeV window
(cascade decay of $\psi(2S)$)

$$R = \frac{\sigma_{\gamma p \rightarrow \psi(2S)p}}{\sigma_{\gamma p \rightarrow J/\psi(1S)p}} \text{ vs. } W \text{ at } Q^2 = 0 \text{ GeV}^2$$



- $R_{\psi(2S) \rightarrow J/\psi \pi^+ \pi^-} = \frac{\sigma_{\psi(2S)}}{\sigma_{J/\psi(1S)}} = \frac{N_{\psi(2S)}}{N_{J/\psi(1S)}} \cdot \frac{Acc_{J/\psi(1S) \rightarrow \mu^+ \mu^-}}{Acc_{\psi(2S) \rightarrow J/\psi \pi^+ \pi^-}} \cdot \frac{1}{BR_{\psi(2S) \rightarrow J/\psi \pi^+ \pi^-}}$
- $R_{\psi(2S) \rightarrow \mu^+ \mu^-} = \frac{\sigma_{\psi(2S)}}{\sigma_{J/\psi(1S)}} = \frac{N_{\psi(2S)}}{N_{J/\psi(1S)}} \cdot \frac{Acc_{J/\psi(1S) \rightarrow \mu^+ \mu^-}}{Acc_{\psi(2S) \rightarrow \mu^+ \mu^-}} \cdot \frac{BR_{J/\psi(1S) \rightarrow \mu^+ \mu^-}}{BR_{\psi(2S) \rightarrow \mu^+ \mu^-}}$
- $BR(\psi(2S) \rightarrow J/\psi \pi^+ \pi^-) = (34.49 \pm 0.3)\%$, $BR(\psi(2S) \rightarrow \mu^+ \mu^-) = (7.9 \pm 0.9) \times 10^{-3}$,
 $BR(J/\psi \rightarrow \mu^+ \mu^-) = (5.961 \pm 0.033)\%$