

Hard and Precision QCD @ HERA

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on behalf of the H1 and ZEUS collaborations



Munich

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Combination of
open c & b
prod. data in
DIS

Comparison to
NLO & α NNLO

Extraction of
 m_c & m_b in NLO



New multijet
cross sections in
DIS

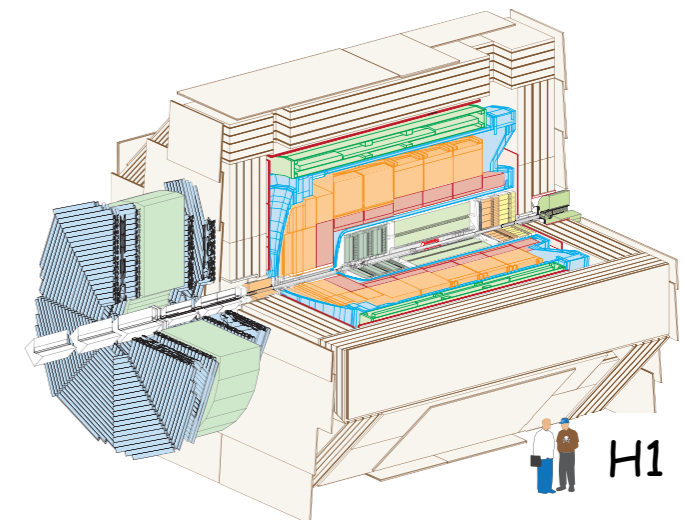
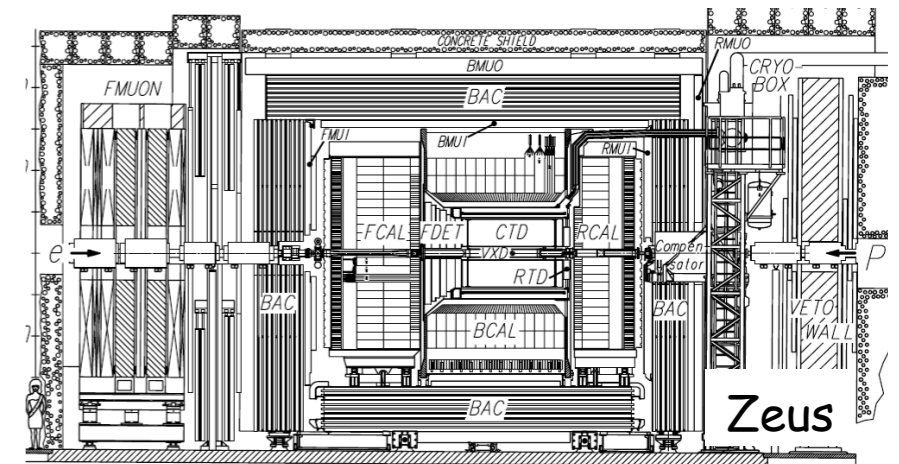
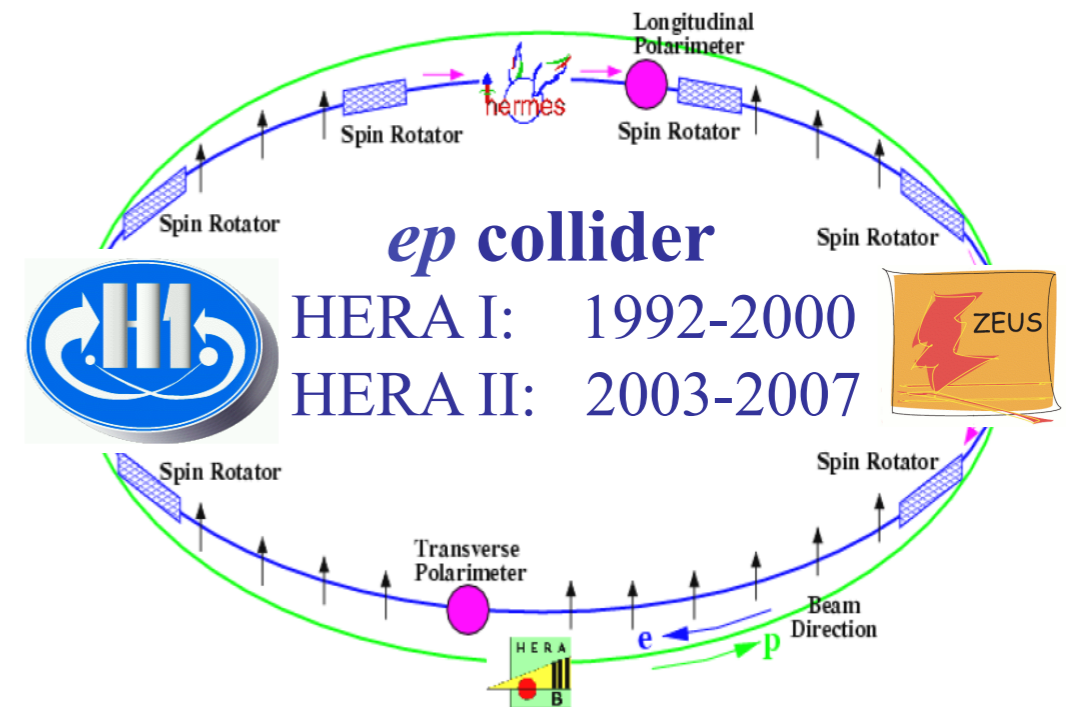
Extraction of
 $\alpha_s(M_Z)$ in NNLO

Prompt photons
plus jets in DIS



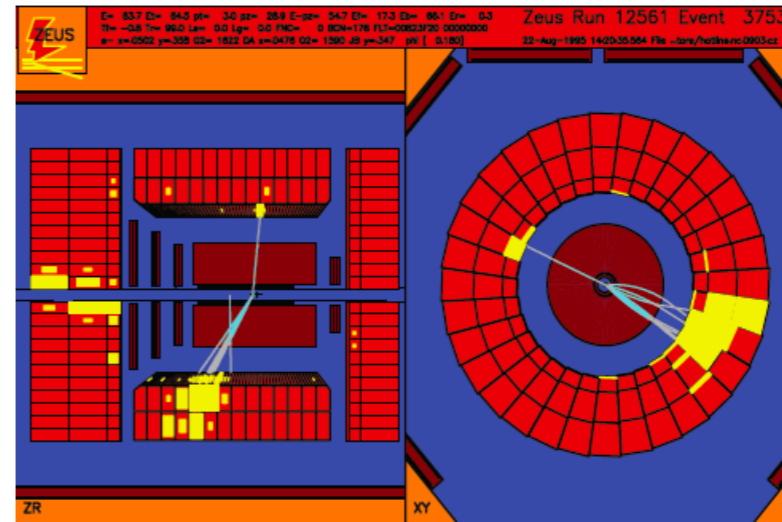
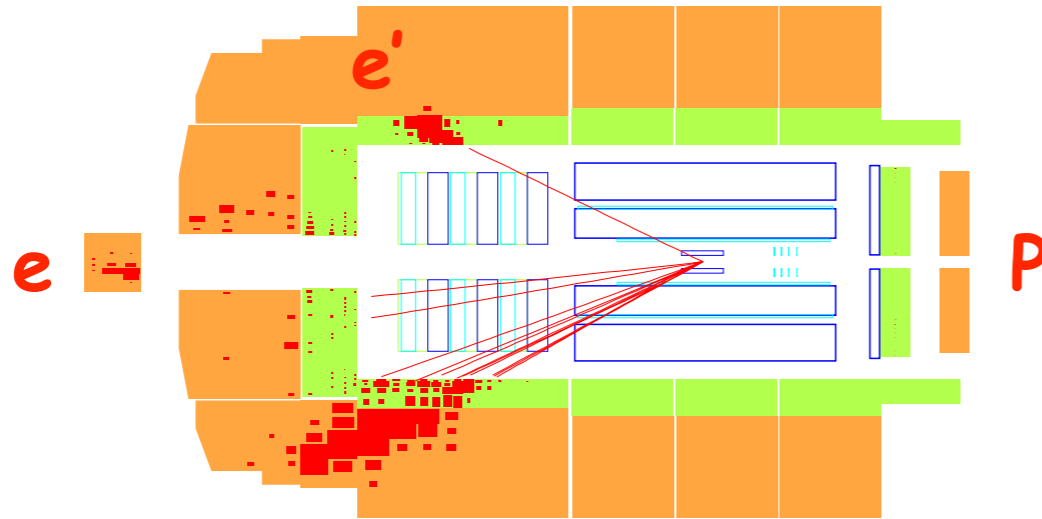
HERA ep Collider, H1 & ZEUS

- H1 & ZEUS experiments collected a combined data sample of $\sim 1\text{fb}^{-1}$
- $\sim 75\%$ of data taken with polarized ($\sim 30\%$) lepton beams, with about equal numbers of e^- and e^+ and positive and negative polarization.
- HERA was the only ep-collider and allowed to investigate a wide range of physics (DIS, DIFF, PHP) and processes.
- Measurement of the proton structure has been a central part of the program.
- H1 & ZEUS provide well calibrated datasets, e.g. hadronic energy scale uncertainty $\sim 1\%$.
- H1 & ZEUS have published > 130 papers since the end of data taking in 2007.



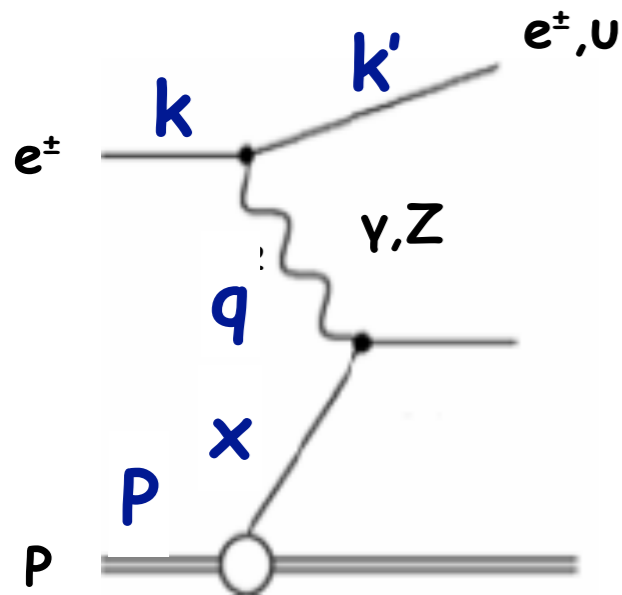
Inclusive DIS kinematics

$$e p \rightarrow e (\nu) X$$



X

Measurement



virtuality

$$Q^2 = -(k - k')^2$$

$$Q_e^2 = \frac{E_e'^2 \sin^2 \theta_e}{1 - y_e}$$

inelasticity

$$y = (\mathbf{P} \cdot \mathbf{q}) / (\mathbf{P} \cdot \mathbf{k})$$

$$y_e = 1 - (E_e' / 2E_e)(1 - \cos \theta_e')$$

Bjorken x

$$x_{Bj} = Q^2 / (2\mathbf{P} \cdot \mathbf{q})$$

$$x_e = \frac{Q_e^2}{4E_p E_e y_e}$$

$$Q^2 = xys \quad s = (\mathbf{k} + \mathbf{P})^2$$

Heavy quark production in DIS

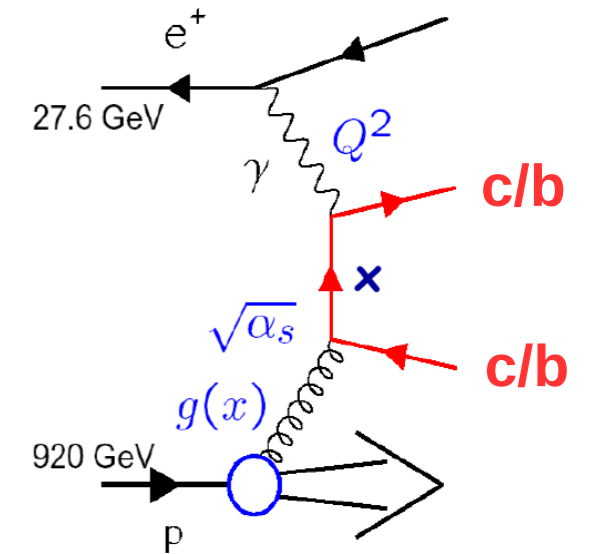
- Main prod. process is photon-gluon fusion
- Combine H1 & ZEUS measurements based on different tagging techniques
 - reconstructed D^{*+} , D^+ and D^0 meson decays
 - μ and e from semi-leptonic decays
 - analysis of tracks (VTX) exploiting lifetime info
- Extension of previous combination for charm [EPJ C 73 (2013) 2311]

- 3 new charm data sets
- 5 beauty data sets
- 13 analyses in total
- Reduced cross sections

$$\sigma_{\text{red}}^{Q\bar{Q}} = \frac{d^2\sigma^{Q\bar{Q}}}{dx_Bj dQ^2} \cdot \frac{xQ^4}{2\pi\alpha^2(1+(1-y)^2)}$$

- H1prelim-17-071, ZEUS-prel-17-01]

Data set	Tagging	Q^2 range [GeV ²]	N_c	\mathcal{L} [pb ⁻¹]	\sqrt{s} [GeV]	N_b
1 H1 VTX [8]	VTX	5 - 2000	29	245	318	12
2 H1 D^{*+} HERA-I [9]	D^{*+}	2 - 100	17	47	318	
3 H1 D^{*+} HERA-II (medium Q^2) [10]	D^{*+}	5 - 100	25	348	318	
4 H1 D^{*+} HERA-II (high Q^2) [11]	D^{*+}	100 - 1000	6	351	318	
5 ZEUS D^{*+} 96-97 [12]	D^{*+}	1 - 200	21	37	300	
6 ZEUS D^{*+} 98-00 [13]	D^{*+}	1.5 - 1000	31	82	318	
7 ZEUS D^0 2005 [14]	D^0	5 - 1000	9	134	318	
8 ZEUS μ 2005 [7]	μ	20 - 10000	8	126	318	8
9 ZEUS D^+ HERA-II [2]	D^+	5 - 1000	14	354	318	
10 ZEUS D^{*+} HERA-II [3]	D^{*+}	5 - 1000	31	363	318	
11 ZEUS VTX HERA-II [4]	VTX	5 - 1000	18	354	318	17
12 ZEUS e HERA-II [5]	e	10 - 1000		363	318	9
13 ZEUS μ + jet HERA-I [6]	μ	2 - 3000		114	318	11



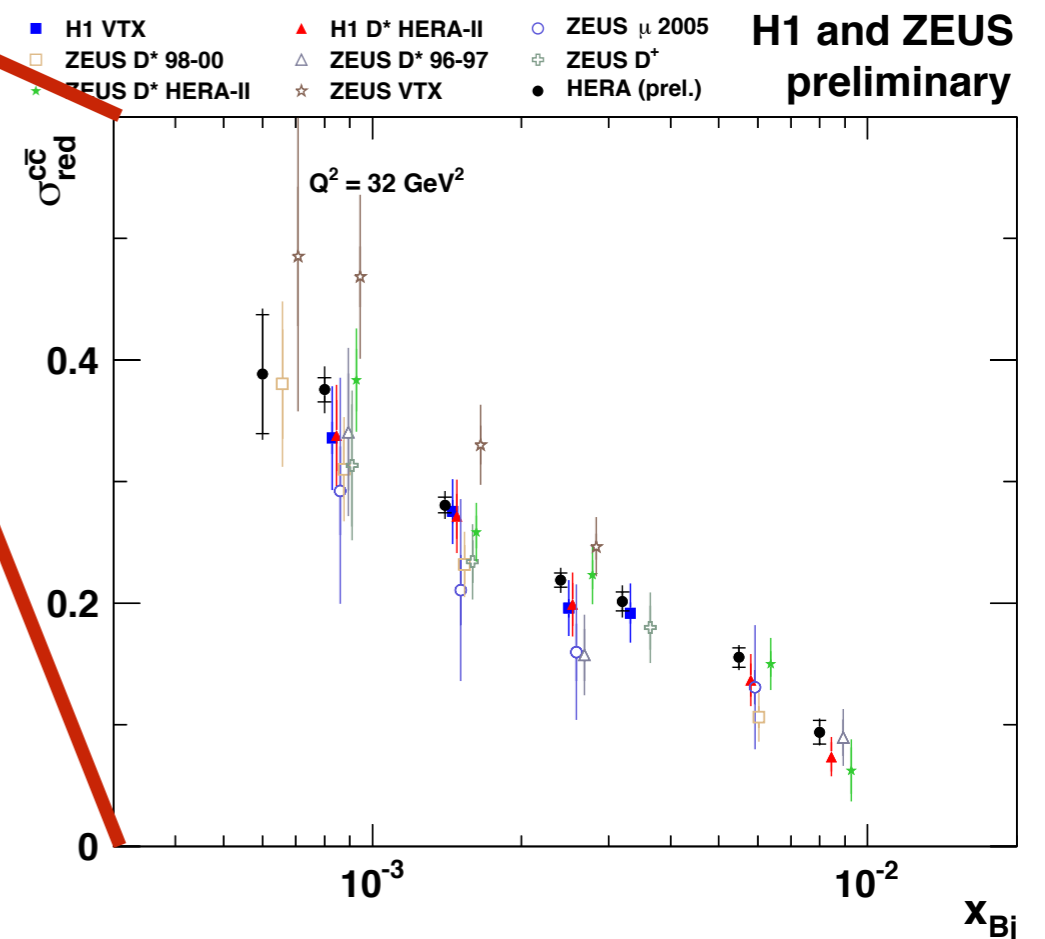
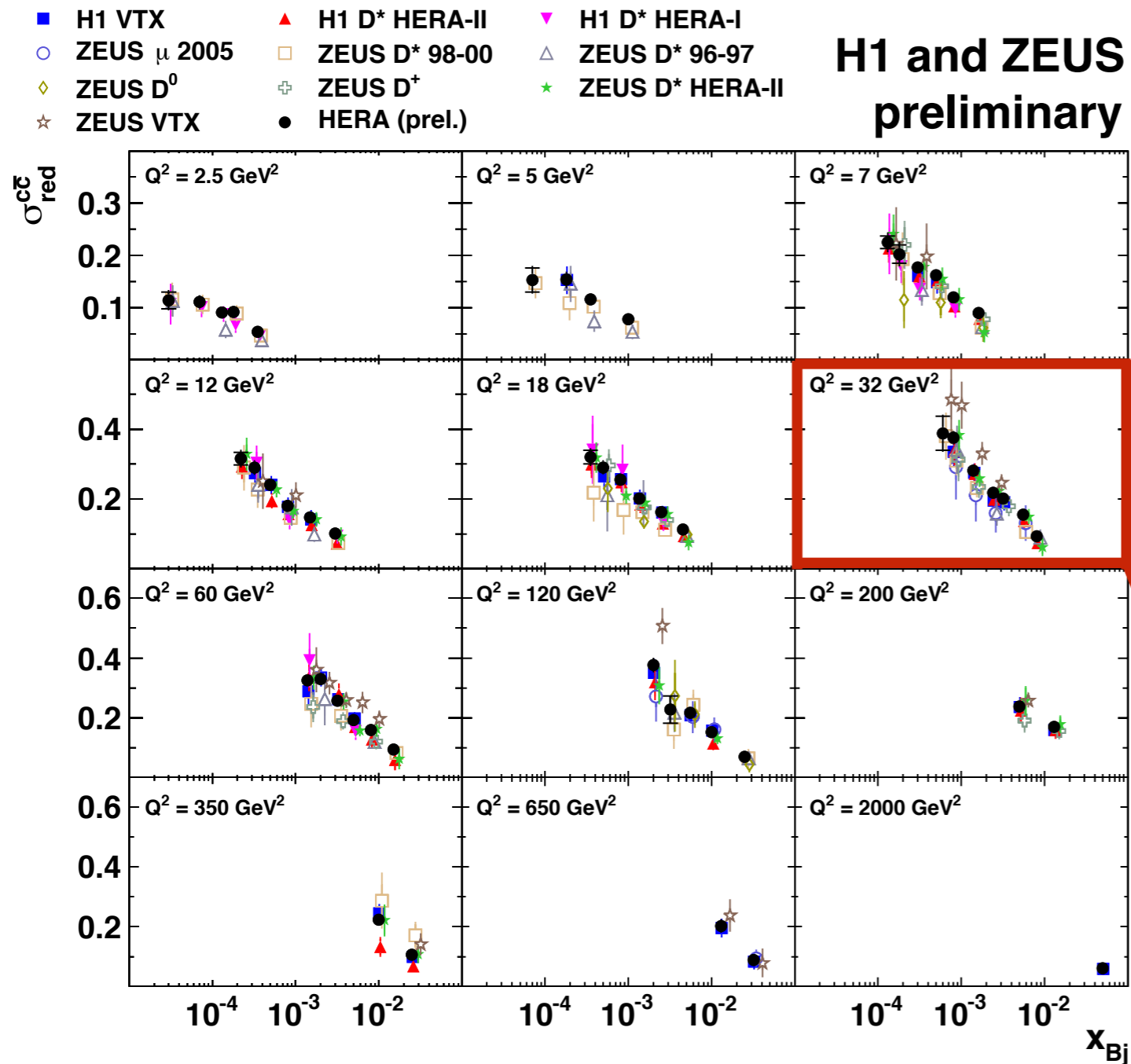
up to 30% of the inclusive prod. is due to charm, up to 1% due to beauty

NLO calculations:

- FFNS: PDFs contain only u, d, s, g . Heavy quarks are generated in ME (multiple scales)
- VFNS: massless quarks in ME.

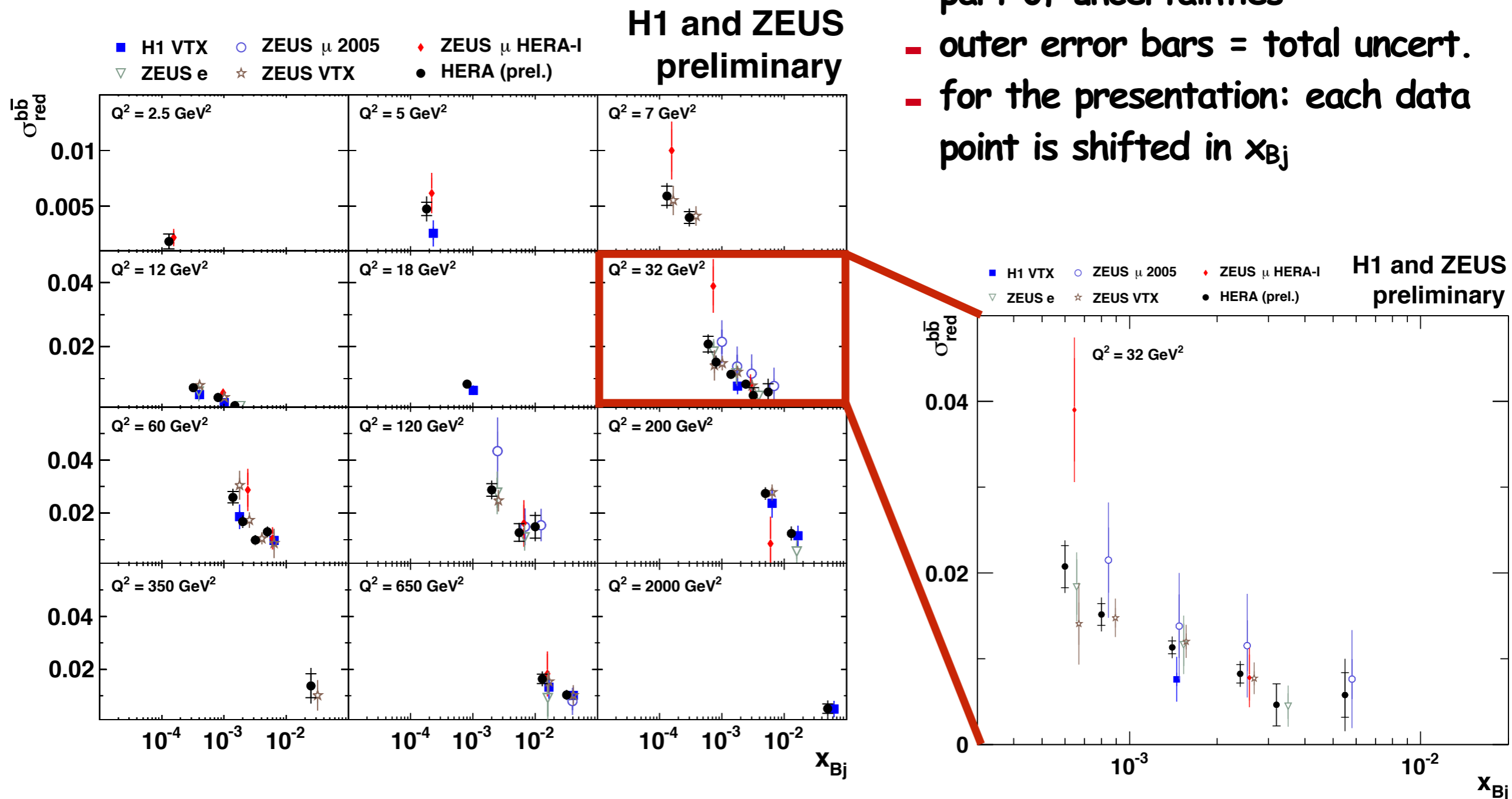
Combination of c cross sections in DIS

- 209 c + 52 b data points combined simultaneously \rightarrow 52 c + 27 b data points
- accounting for correlations in c & b data sets as well as between them
- good consistency: $\chi^2/\text{ndf} = 149/187$



➤ Significant improvement in precision compared to input data

Combination of b cross sections in DIS



➤ 1st combination of b cross sections

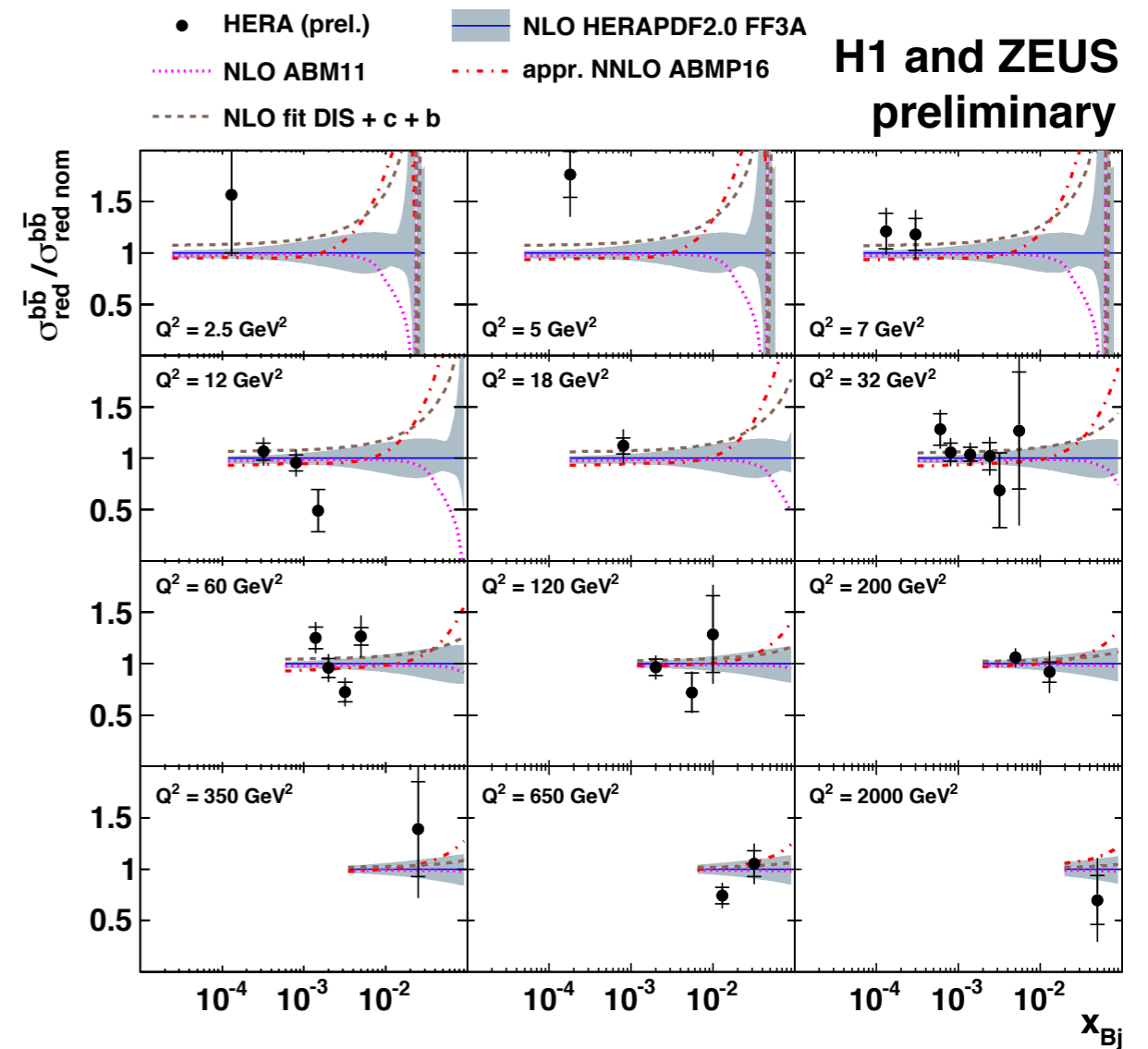
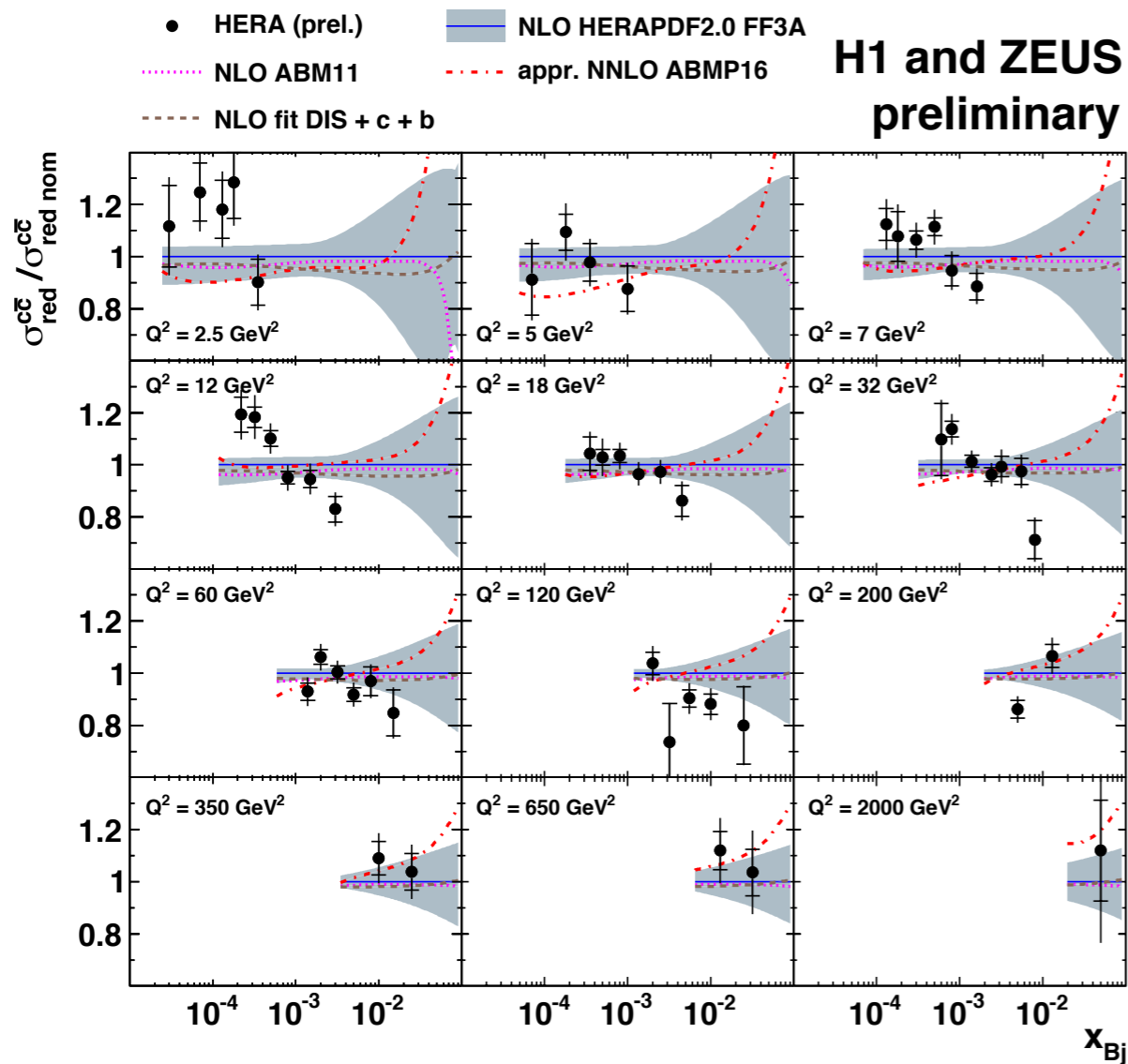
Ratios to NLO QCD

Predictions from OPENQCDRAD

- HERAPDF2.0 FF3A
- ABM11
- ABMP16 + approx. NNLO
- PDF-fit

$$\mu_R = \mu_F = (Q^2 + 4m_{c,b}^2)^{1/2}$$

cross sections are normalized to NLO predictions using HERAPDF2.0 FF3A



QCD provides reasonable overall description of the data; no improvement by approx. NNLO; slope diff. at $Q^2 \approx 12 \text{ GeV}^2$
 dominant theory uncertainty from variation of scale (factor of 0.5 to 2)

Extraction of c & b masses

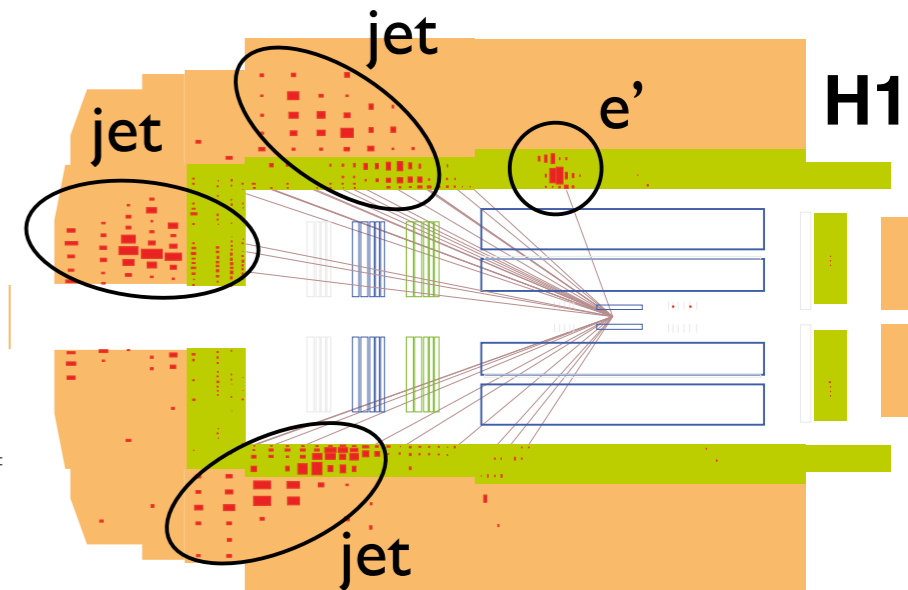
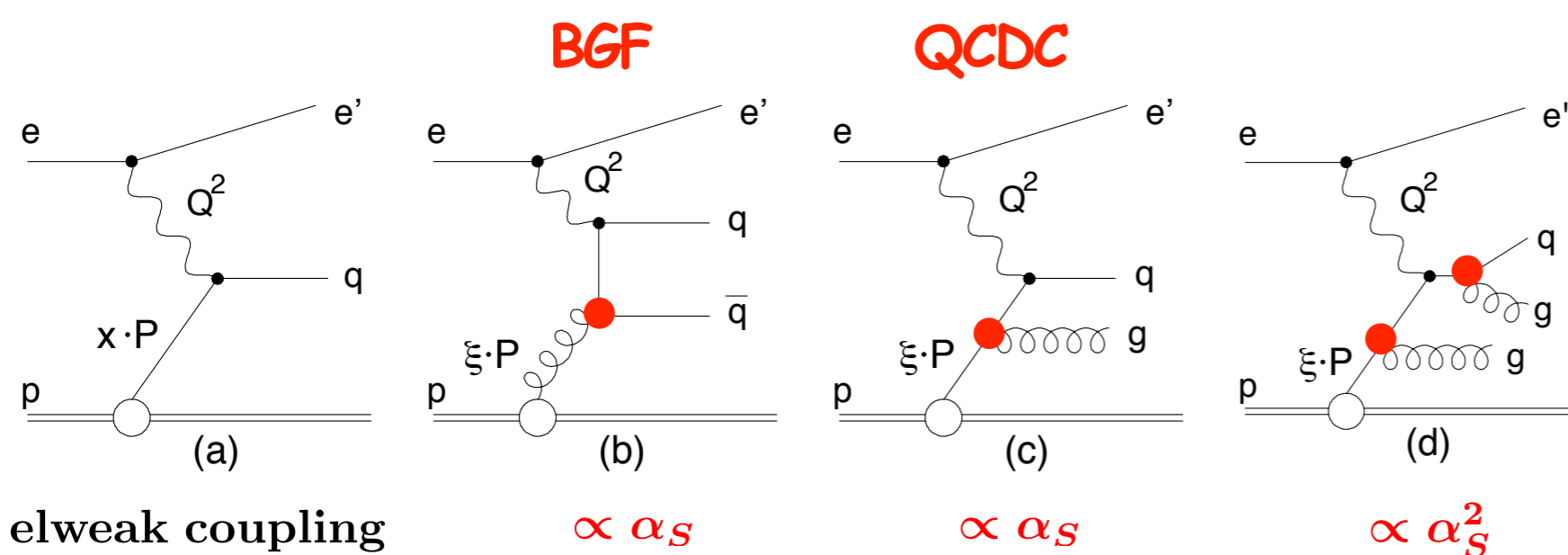
- Perform QCD fit in NLO in FFNS ($n_f = 3$):
 - besides c & b data, inclusive HERA NC & CC data are used
 - m_c & m_b are free parameters in the fit
 - the light flavor PDFs are parameterized as in the HERAPDF2.0 fit

$$m_c(m_c) = 1290_{-41}^{+46}(\text{fit}) \quad +_{-14}^{+62}(\text{mod}) \quad +_{-31}^{+7}(\text{par}) \text{ MeV}$$

$$m_b(m_b) = 4049_{-109}^{+104}(\text{fit}) \quad +_{-32}^{+90}(\text{mod}) \quad +_{-31}^{+1}(\text{par}) \text{ MeV}$$

- the QCD fit gives $\chi^2/\text{ndf} = 1435/1208$
- the **model** uncertainties are significant and are dominated by the variation of the scale (factor 0.5 to 2)
- the c & b masses given are the running masses in the $\overline{\text{MS}}$ scheme; consistent with the PDG values: $m_c(m_c) = 1270 \pm 30 \text{ MeV}$ and $m_b(m_b) = 4180 \pm 30 \text{ MeV}$

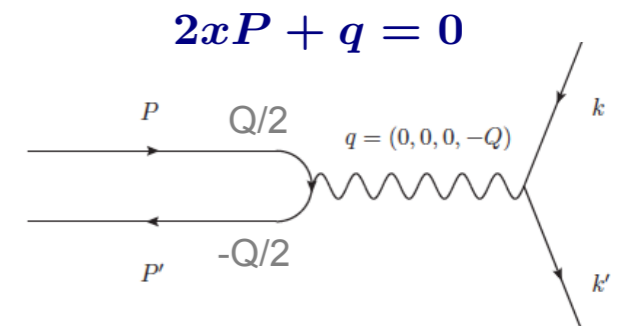
Multijetproduction in NC DIS



Jets in DIS are measured in the Breit frame:

- virtual boson collides head-on with parton from proton
- jets reconstructed using the k_T algorithm
- each jet must have a minimum P_T in the Breit frame
 - jets depend already in LO on $\alpha_S \otimes g$ (or q or $qbar$) in IS and on α_S in FS, allowing for a determination of α_S
 - **BGF** dominant in largest phase space region (lower Q^2 , lower x)
 - **QCDC** important for high- p_T jets (high x)

boost events into Breit frame:



Jets in DIS at low Q^2

- Simultaneous measurement and unfolding of
 - inclusive jets, dijet and trijet as well as incl. NC DIS cross sections
 - accounting for correlations & detector effects

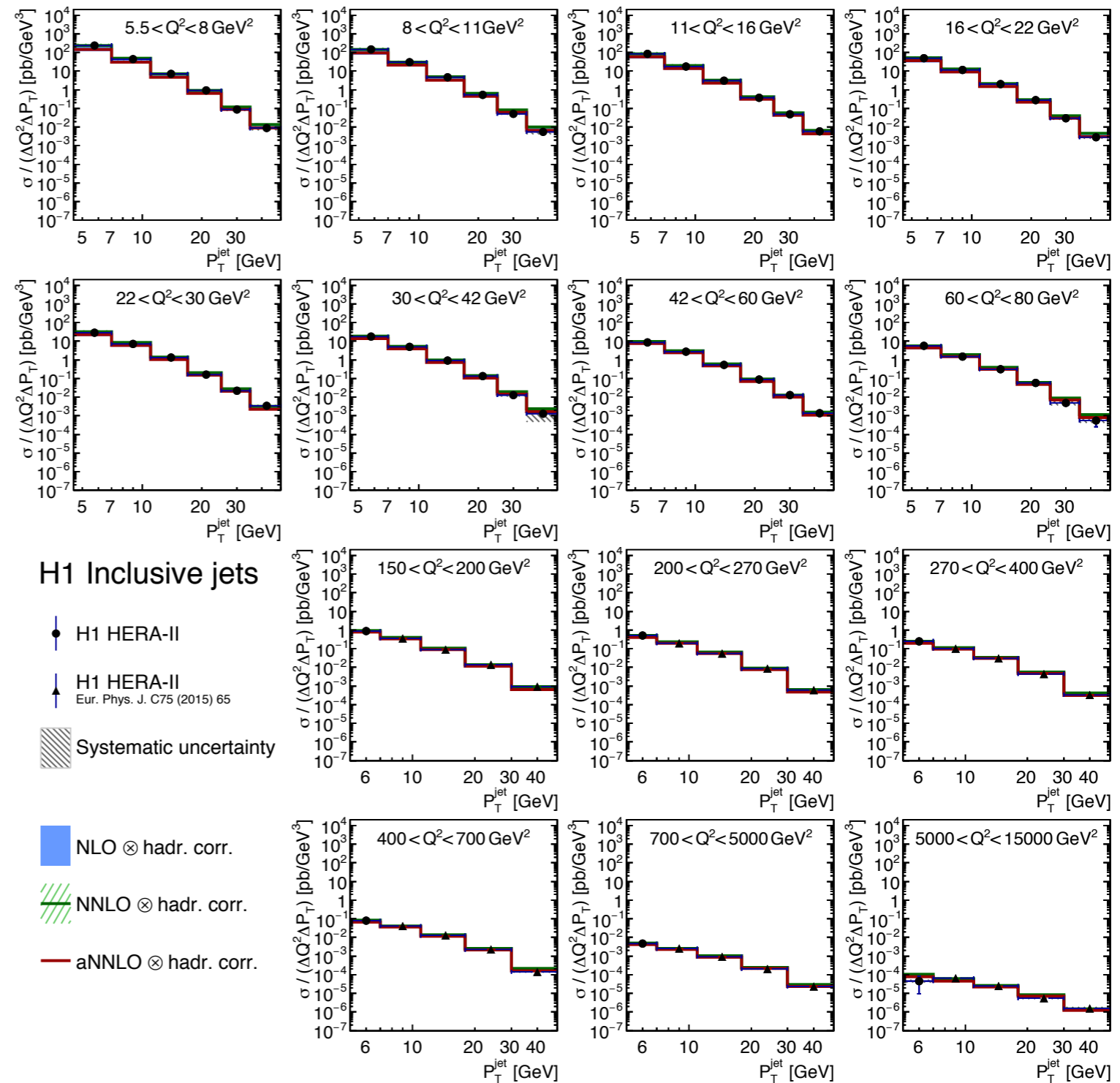
Phase space of cross sections:

NC DIS	$5.5 < Q^2 < 80 \text{ GeV}^2$
	$0.2 < y < 0.6$
(inclusive) Jets	$P_T^{\text{jet}} > 4.5 \text{ GeV}$
	$-1.0 < \eta^{\text{lab}} < 2.5$
Dijet and Trijet	$\langle P_T^{\text{jet}} \rangle_2 > 5.0 \text{ GeV}$
Measure average p_T	$\langle P_T^{\text{jet}} \rangle_3 > 5.5 \text{ GeV}$

EPJ C 77 (2017) 4, 215

- Include extension of previous high- Q^2 result

EPJ C 75 (2015) 2, 65



High precision data over wide kinematic range

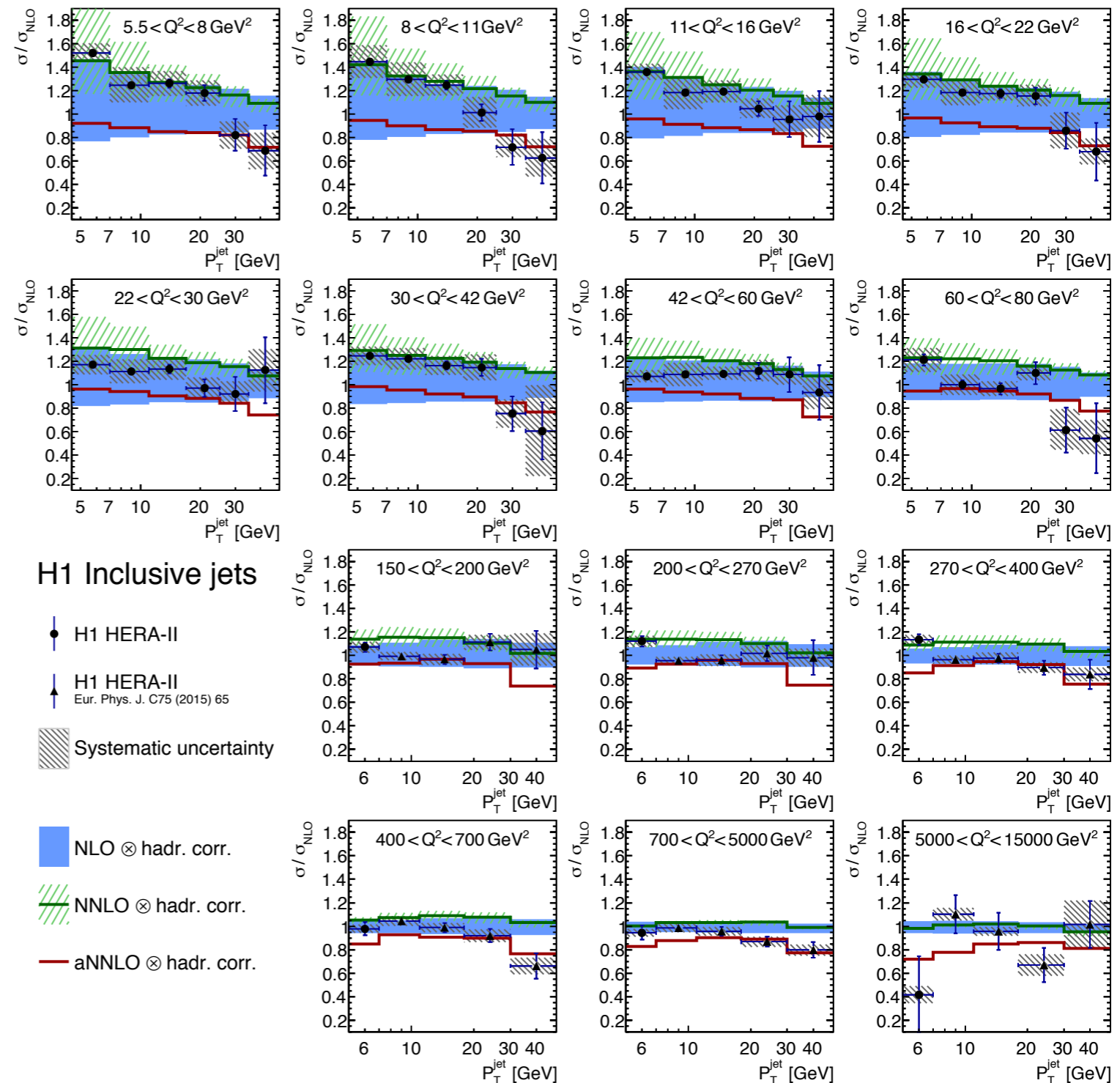
Comparison to NLO & aNNLO & NNLO

$$\frac{\sigma_{\text{jet}}}{\sigma_{\text{NLO}}} \quad \& \quad \frac{\sigma_{\text{aNNLO}}}{\sigma_{\text{NLO}}} \quad \& \quad \frac{\sigma_{\text{NNLO}}}{\sigma_{\text{NLO}}}$$

- **NLO QCD (NLOjet++)**
 - [PRL 87 \(2001\) 082001](#)
 - reasonable description of data
 - large scale uncertainty

- **Approximate NNLO (JETVIP)**
 - threshold resummation
 - [PR D 92 \(2015\) 074037](#)
 - somewhat improved shape

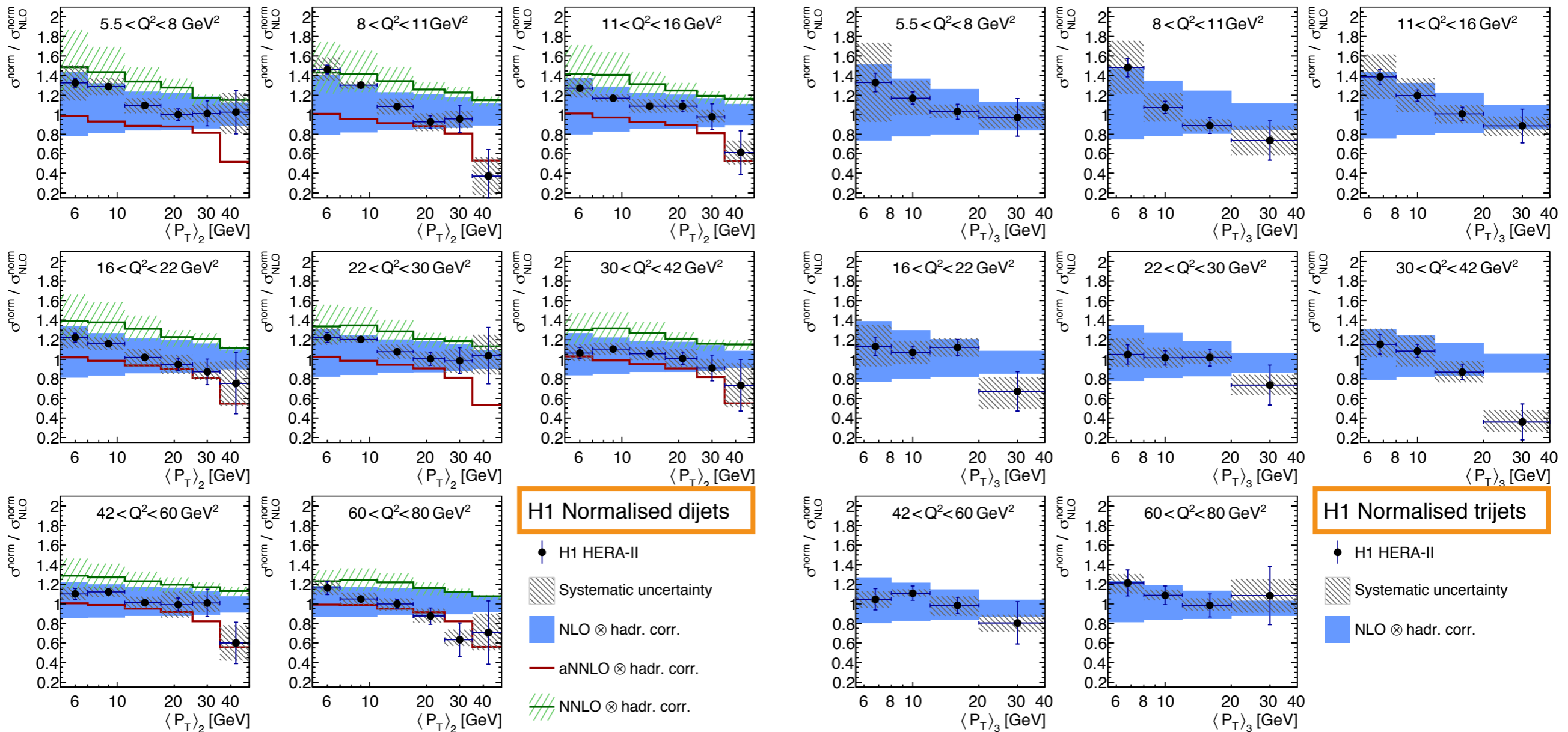
- **NNLO QCD (NNLOJET)**
 - [PRL 117 \(2016\) 042001](#)
 - improved description
 - significantly reduced scale uncertainty, particularly for higher scales



Dijet & Trijet production in DIS

$$\frac{\sigma_{\text{jet}}}{\sigma_{\text{NLO}}} \quad \& \quad \frac{\sigma_{\text{aNNLO}}}{\sigma_{\text{NLO}}} \quad \& \quad \frac{\sigma_{\text{NNLO}}}{\sigma_{\text{NLO}}}$$

but for jet cross sections normalized to $\sigma(\text{NC DIS})$ in the respective Q^2 and P_T bin



- Dijet: in NNLO improved description of shape
- Trijet: in NLO good description at moderate precision

Extraction and running of α_s at NLO

From comb. fit to normalized incl. jet, dijet and trijet cross sections at low and high Q^2 :

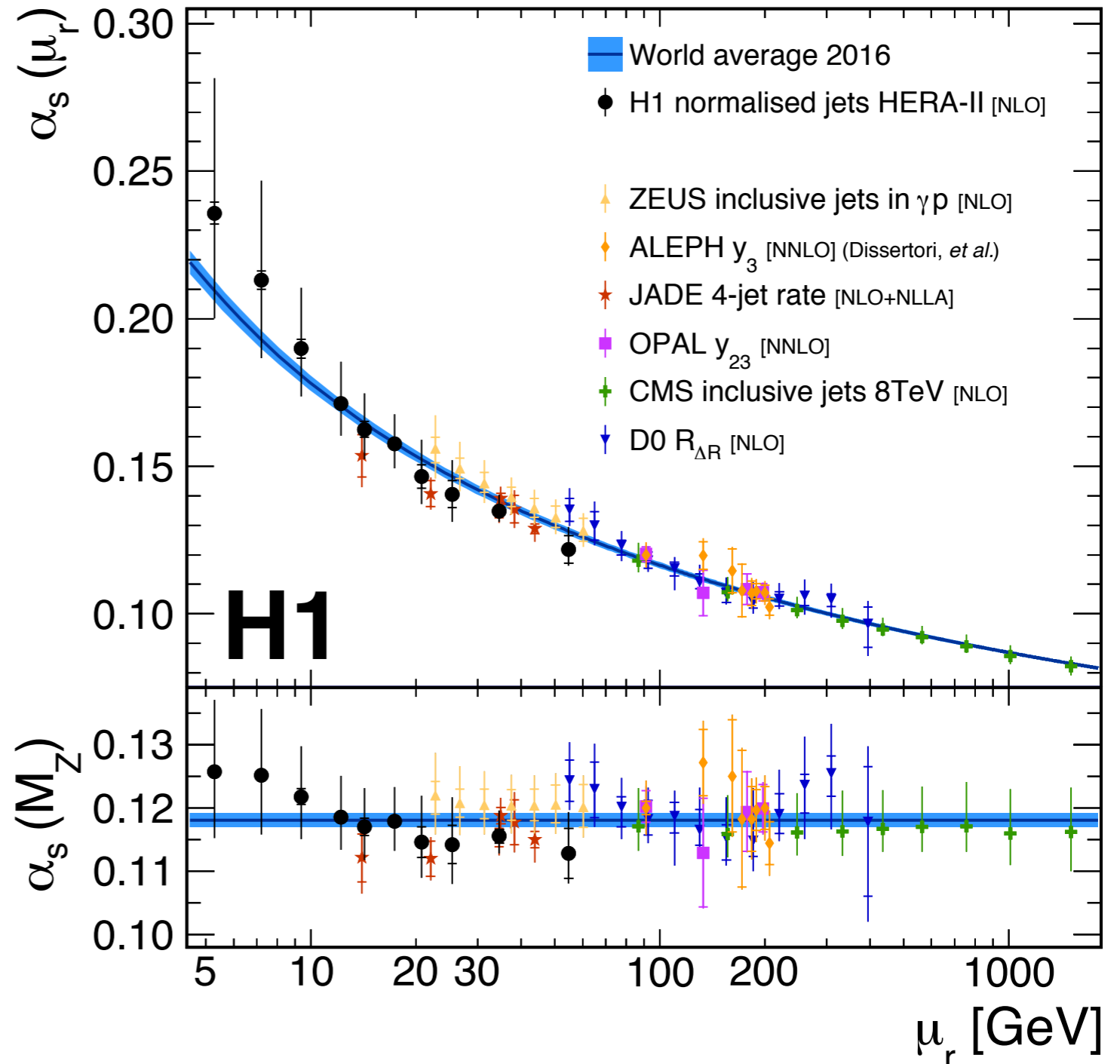
$$\alpha_s(M_Z) = 0.1172 \text{ (4)}_{\text{exp}} \text{ (3)}_{\text{PDF}} \text{ (7)}_{\text{PDF}(\alpha_s)} \text{ (11)}_{\text{PDF}_{\text{set}}} \text{ (6)}_{\text{had}} \text{ } \left(\begin{smallmatrix} +51 \\ -43 \end{smallmatrix} \right)_{\text{scale}}$$

▪ [EPJ C 77 \(2017\) 4, 215](#)

- high exp. precision
- large scale uncertainty

Running of $\alpha_s(\mu_R)$:

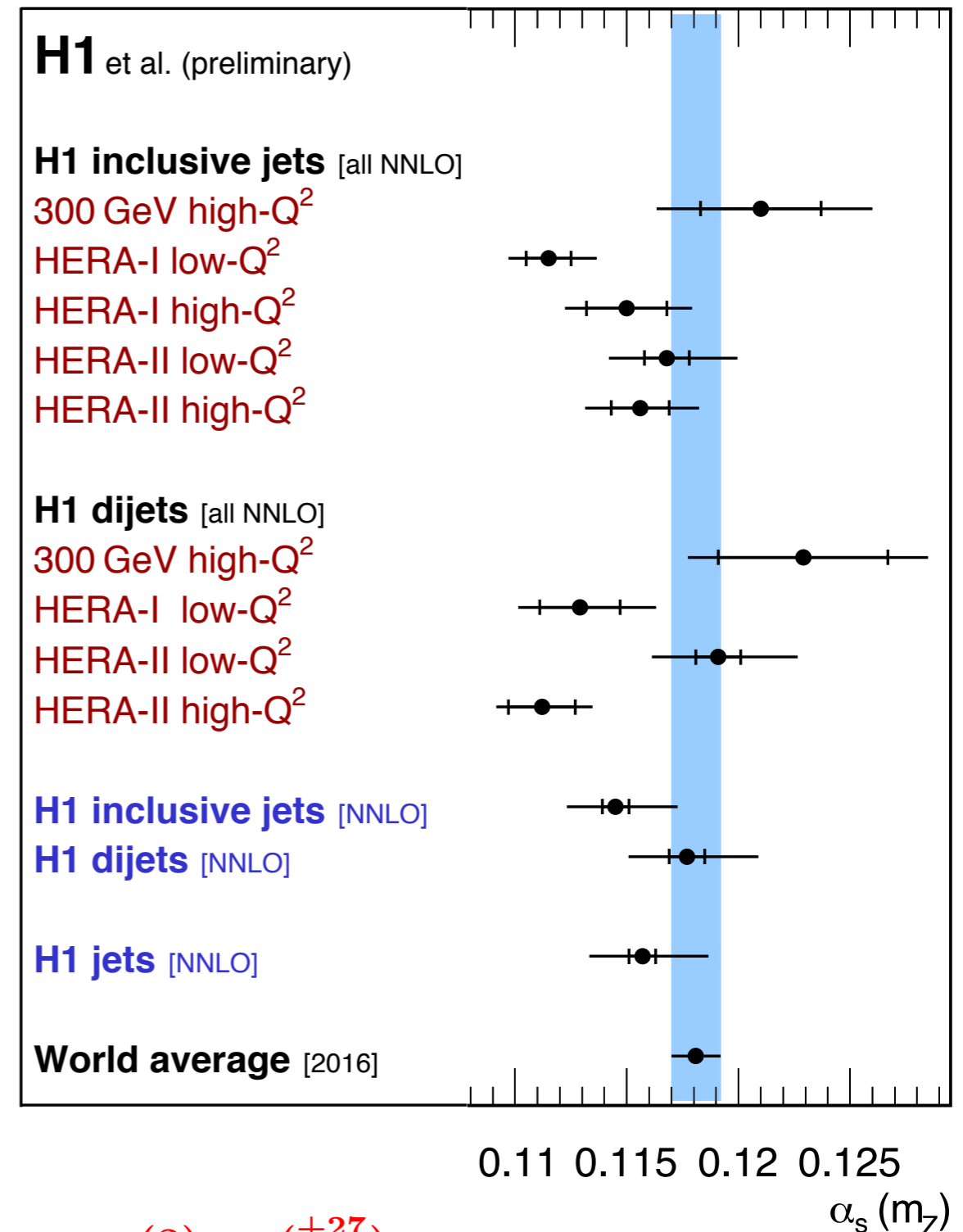
- data points are grouped into 10 groups with comparable values of μ_R
- $\alpha_s(M_Z)$ is fitted for each group
- $\alpha_s(\mu_R)$ is obtained from $\alpha_s(M_Z)$ using RGE
- consistent with other results from HERA, PETRA, LEP, Tevatron and LHC & QCD



Extraction of α_s at NNLO

H1-prelim-17-031: H1 in collaboration with V.Bertone, T.Gehrmann, C.Gwenlan, A.Huss, J.Niehues and M.Sutton

- New NNLO fits to all suitable H1 inclusive jet and dijet measurements (203 data points)
- Full error breakdown
 - corr. & uncorr. exp. uncertainties
 - theory uncertainty: scale variation (factors 0.5 and 2)
 - various PDF uncertainties
 - hadronisation uncertainties
- $\alpha_s(M_Z)$ results from distinct data sets and from all of them ('H1 jets')
 - all fits yield good χ^2 , indicating consistency of data
 - high exp. precision
 - uncertainties due to PDFs are sizeable
 - scale uncertainty is dominant, but considerably reduced w.r.t. NLO

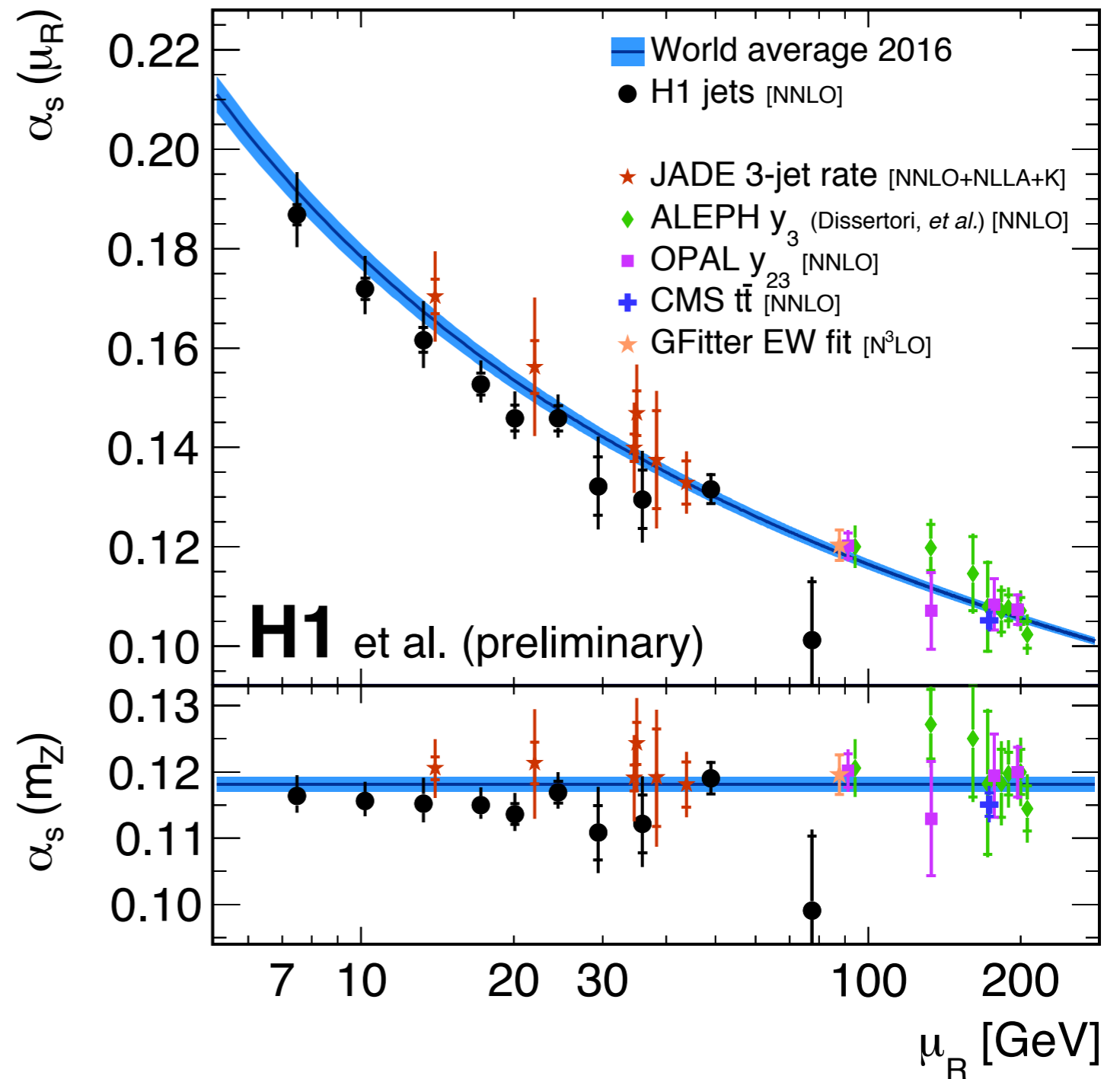


$$\alpha_s(M_Z) = 0.1157 \text{ (6)}_{\text{exp}} \text{ (6)}_{\text{PDF}} \text{ (12)}_{\text{PDF}(\alpha_s)} \text{ (2)}_{\text{PDFset}} \text{ (3)}_{\text{had}} \text{ (+27)}_{\text{scale}} \text{ (-21)}$$

Running of α_s at NNLO

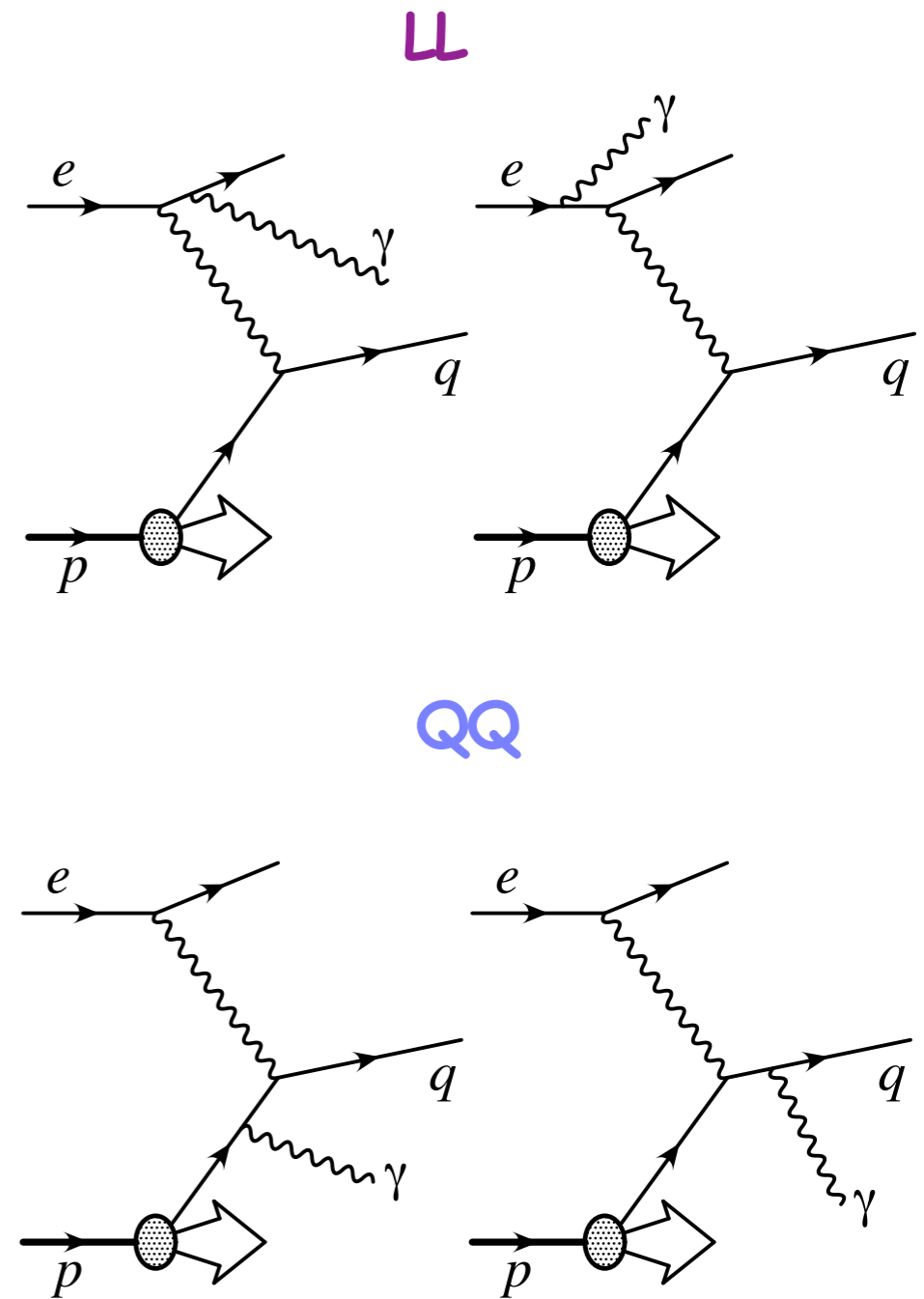
- Repeat fits to 10 groups of data points at similar scales
- Values of α_s are consistent with other extractions at NNLO
- Running is consistent with other experiments and with QCD
- Value of α_s consistent with the world average, however a bit lower

$$\alpha_s(M_Z) = 0.1157 (6)_{\text{exp}} \left(\begin{smallmatrix} +38 \\ -25 \end{smallmatrix} \right)_{\text{pdf,theo}}$$



Prompt photons + jets in DIS

- Photons with high P_T may be:
 - radiated from the incoming or outgoing lepton (LL)
 - produced in a hard QCD interaction (QQ)
 - radiated from a quark within a jet ($f_{q \rightarrow \gamma}(z)$)
 - a decay product of π^0 or η mesons within a jet
- LL and QQ photons are relatively isolated from other particles (use isolation criteria).
- Prompt QQ photons emerge directly from the hard interaction and (with jets) allow a more direct test of the ME.
- New preliminary results, using combined photon-jet-electron variables, allow more detailed ways to test theory. ZEUS-prel-16-001, previous ZEUS results in PL B 715 (2012) 88



Prompt photons + jets in DIS

- Use segmentation of the barrel calorimeter in Z-direction to suppress photons from meson decays
- Main requirements:
 - $4 < E_T^\gamma < 15 \text{ GeV}$
 - $E_T^{\text{jet}} > 2.5 \text{ GeV}$
 - $10 < Q^2 < 350 \text{ GeV}^2$
- Measure diff. cross sections as a function of:

$$x_\gamma = \sum_{\gamma, \text{jet}} (E^i - p_Z^i) / (2E_e y_{\text{JB}})$$

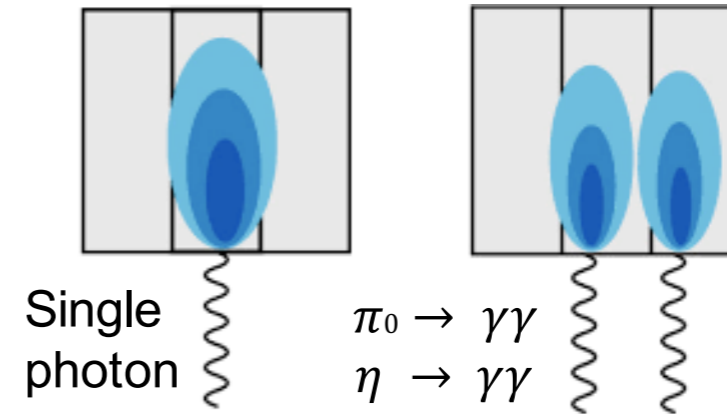
$$x_p = \sum_{\gamma, \text{jet}} (E^i + p_Z^i) / 2E_p$$

$$\Delta\eta = \eta_{\text{jet}} - \eta_\gamma$$

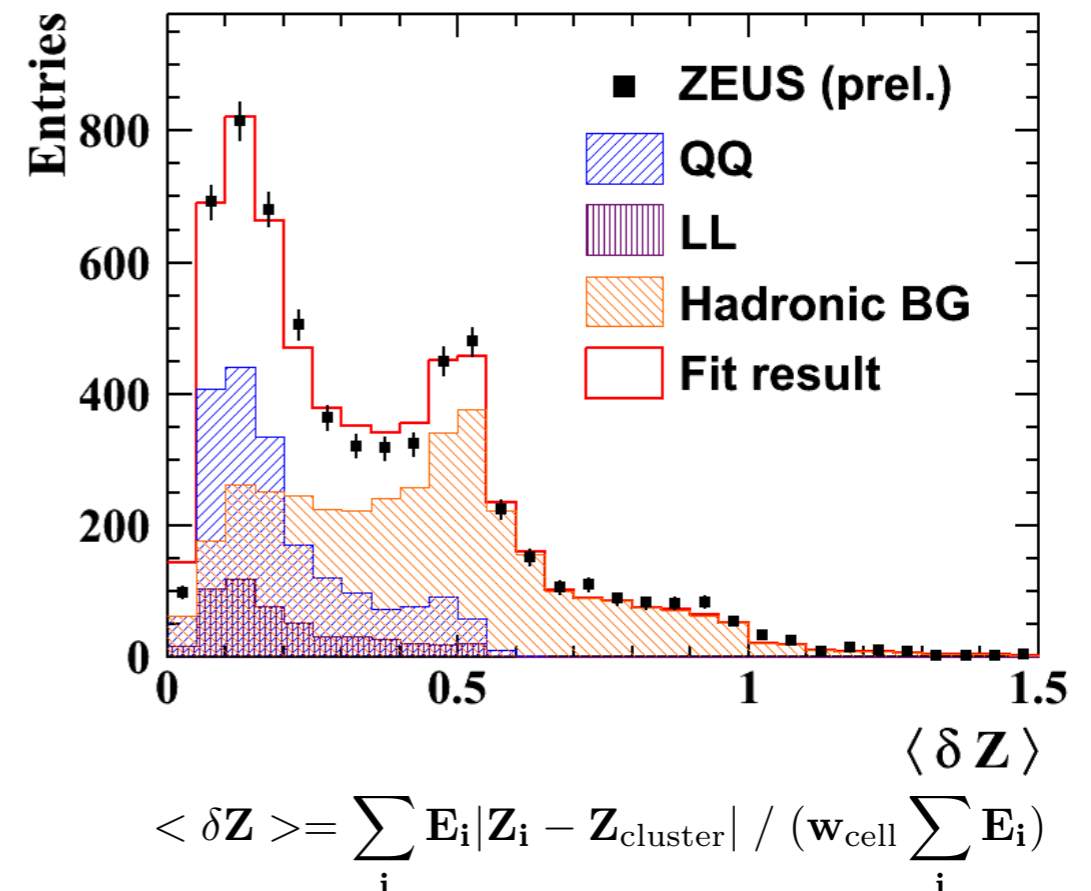
$$\Delta\phi = \phi_{\text{jet}} - \phi_\gamma$$

$$\Delta\phi_{e,\gamma} = \phi_e - \phi_\gamma$$

$$\Delta\eta_{e,\gamma} = \eta_e - \eta_\gamma$$



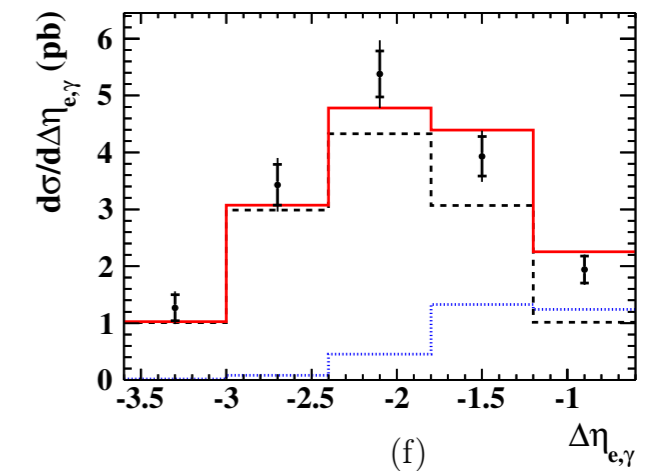
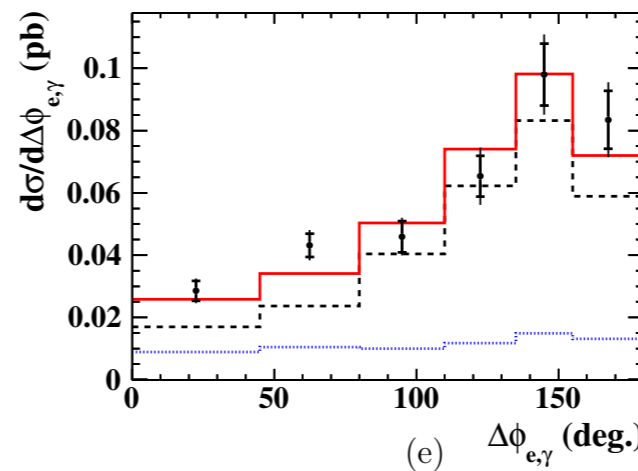
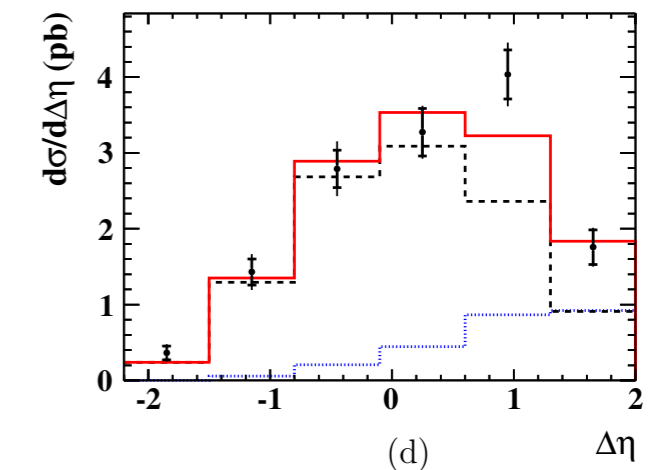
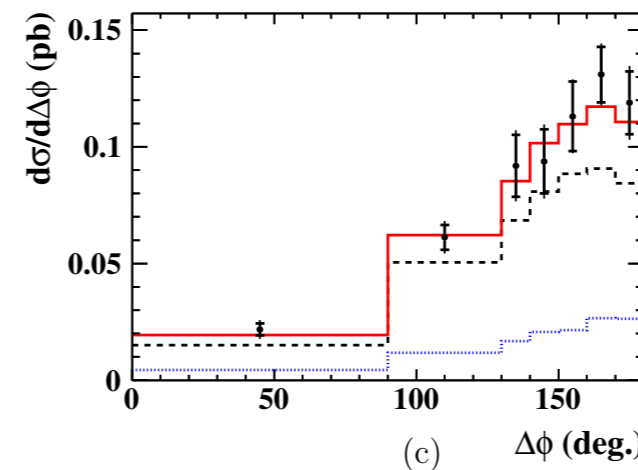
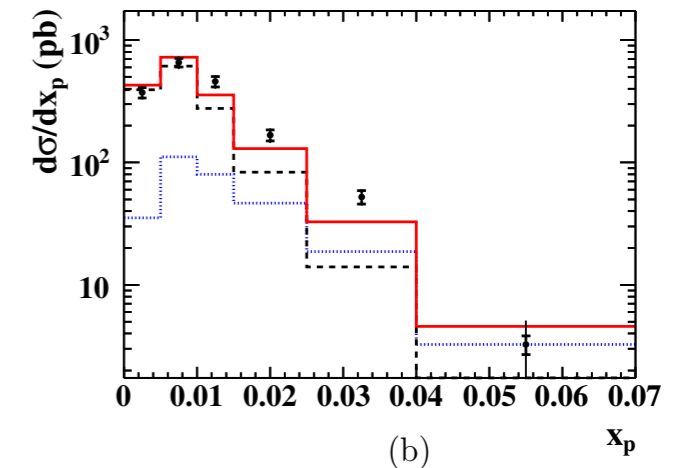
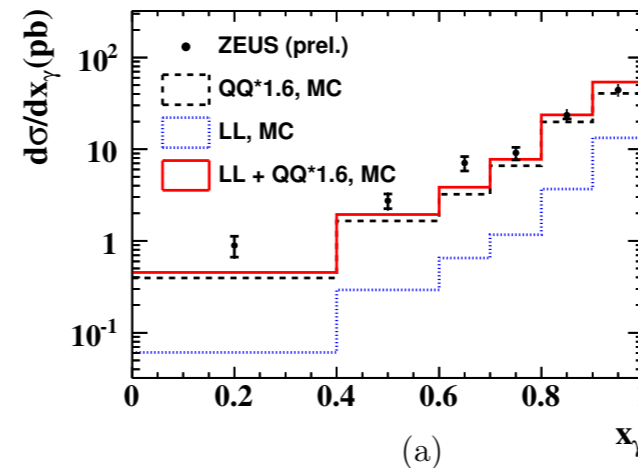
ZEUS preliminary



Prompt photons + jets in DIS

ZEUS preliminary

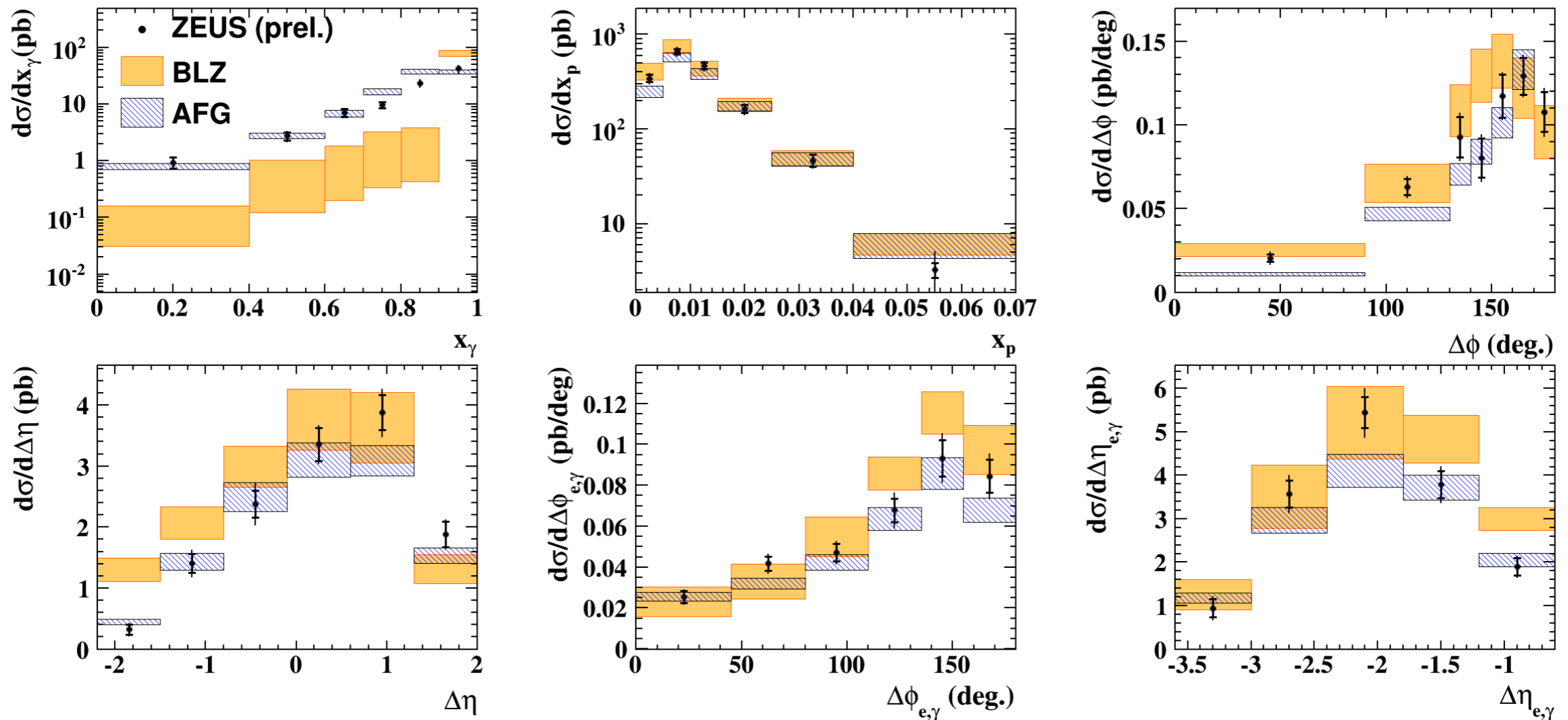
- LO + LLog MC (Djangoh for LL + Pythia for QQ) provides a good description of the data
 - if the LO QQ contribution is weighted by a factor of 1.6
 - and the LL contribution is taken as is in the MC



Prompt photons + jets in DIS

Collinear factorisation in NLO (AFG), Aurenche, Fontannaz and Guillet : *EPJ C 75 (2015) 64*,
arXiv:1704.08074v1

k_T -factorisation (BLZ), Baranov, Lipatov and Zotov: *PR D 81 (2010) 094034*



- AFG provides a reasonably good description of data
- BLZ fails to describe data particularly for x_γ and $\Delta\eta$

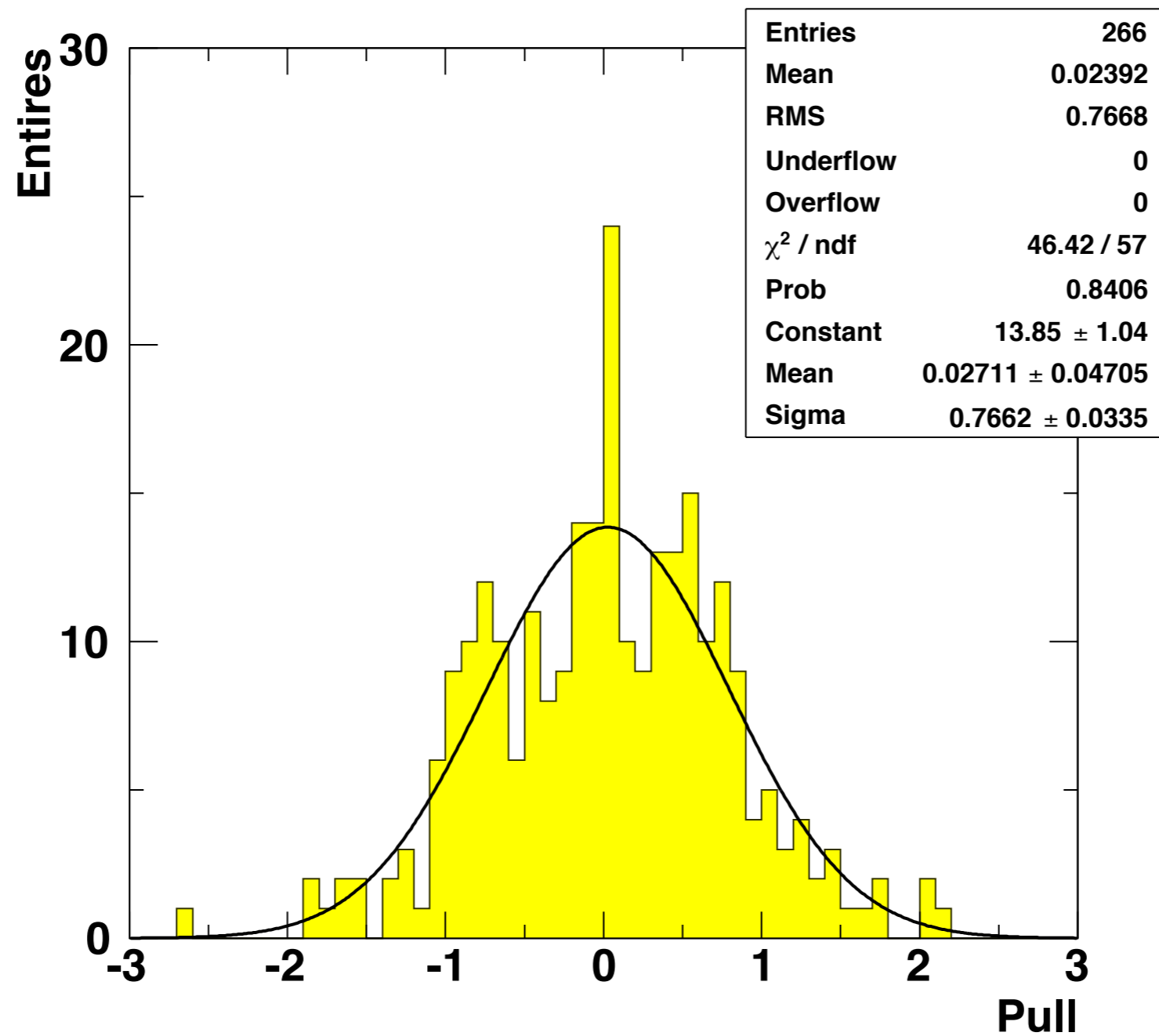
Summary

- New combination of charm & beauty cross sections in DIS by H1 & ZEUS
 - improved precision
 - FFNS in NLO & aNNLO provide overall satisfactory description of data
 - PDF fit to inclusive & c & b data in DIS at HERA alone yields values for running quark masses consistent with PDG
- New results on multijet prod. at low Q^2 & previous results at high Q^2 by H1
 - satisfactory description by NLO, improved shape in P_T by NNLO with significantly reduced scale uncertainty compared to NLO, particularly at higher scales
 - extraction of α_s and running of α_s in NNLO using all suitable H1 HERA inclusive jet and dijet data: $\alpha_s(M_Z) = 0.1157 (6)_{\text{exp}} (+^{38}_{-25})_{\text{pdf,theo}}$
- New results on prompt photons & jets in DIS by ZEUS
 - agree better with AFG (coll. fact. NLO) than with BLZ (k_T fact.)
 - agree also, after QQ rescaling, with Djangoh & Pythia

back-up slides



Pull dist. for the c & b combination



Jet cross sections

$$\sigma_i = \sum_{k=g,q,\bar{q}} \int dx f_k(x, \mu_F) \hat{\sigma}_{i,k}(x, \mu_R, \mu_F) \cdot C_{\text{had},i}$$

- α_s dependence calculated in orders of α_s :
 - in hard coefficients

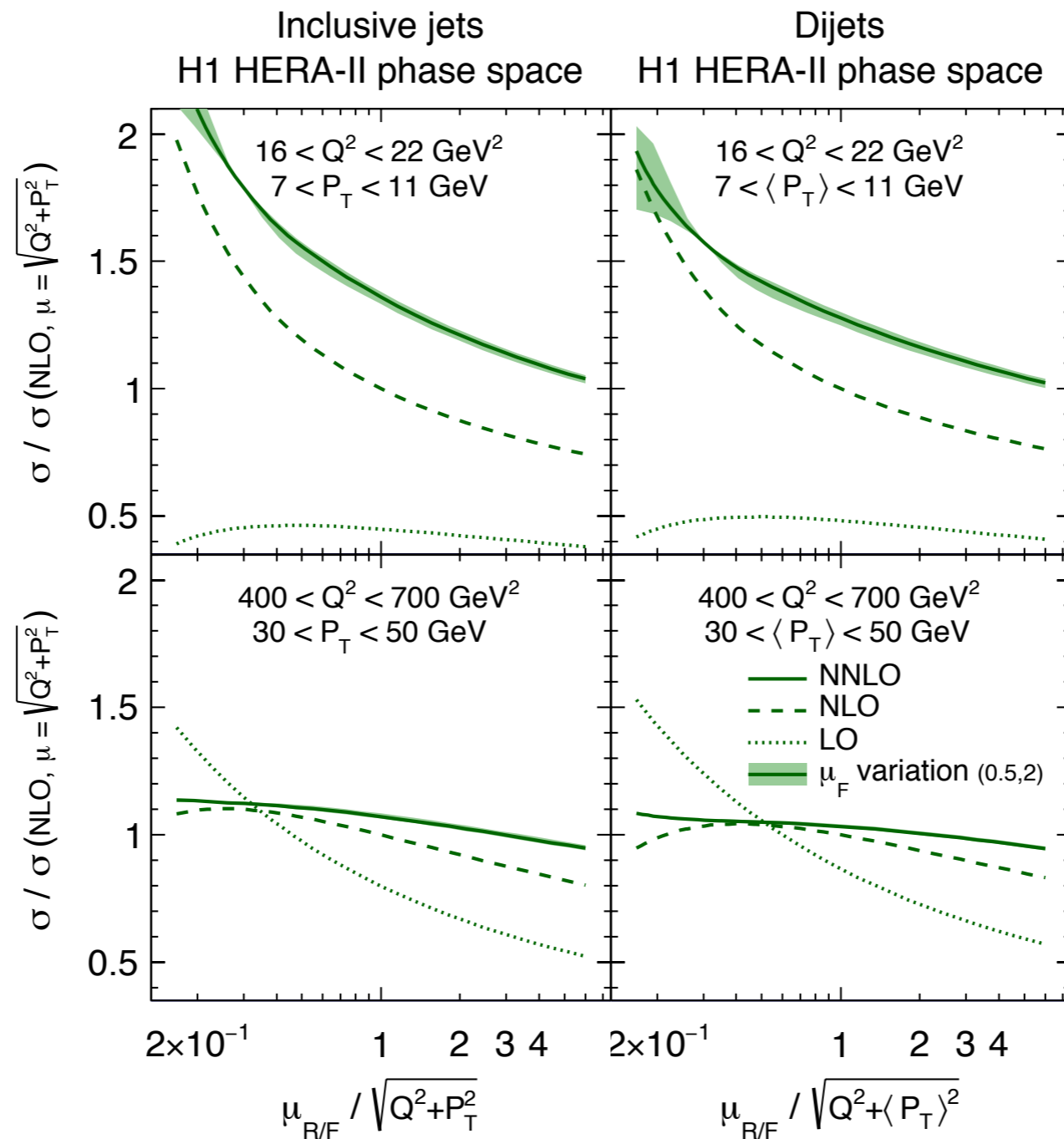
$$\hat{\sigma}_{i,k} = \sum_{n=1} \alpha_s^n(\mu_R) \hat{\sigma}_{i,k}^{(n)}(x, \mu_R, \mu_F)$$

$$\mu_R^2 \frac{d\alpha_s}{d\mu_R^2} = \beta(\alpha_s)$$

- in PDF (splitting functions)

$$\mu_F^2 \frac{df}{d\mu_F^2} = \mathcal{P}(\alpha_s) \otimes f$$

Scale dependence

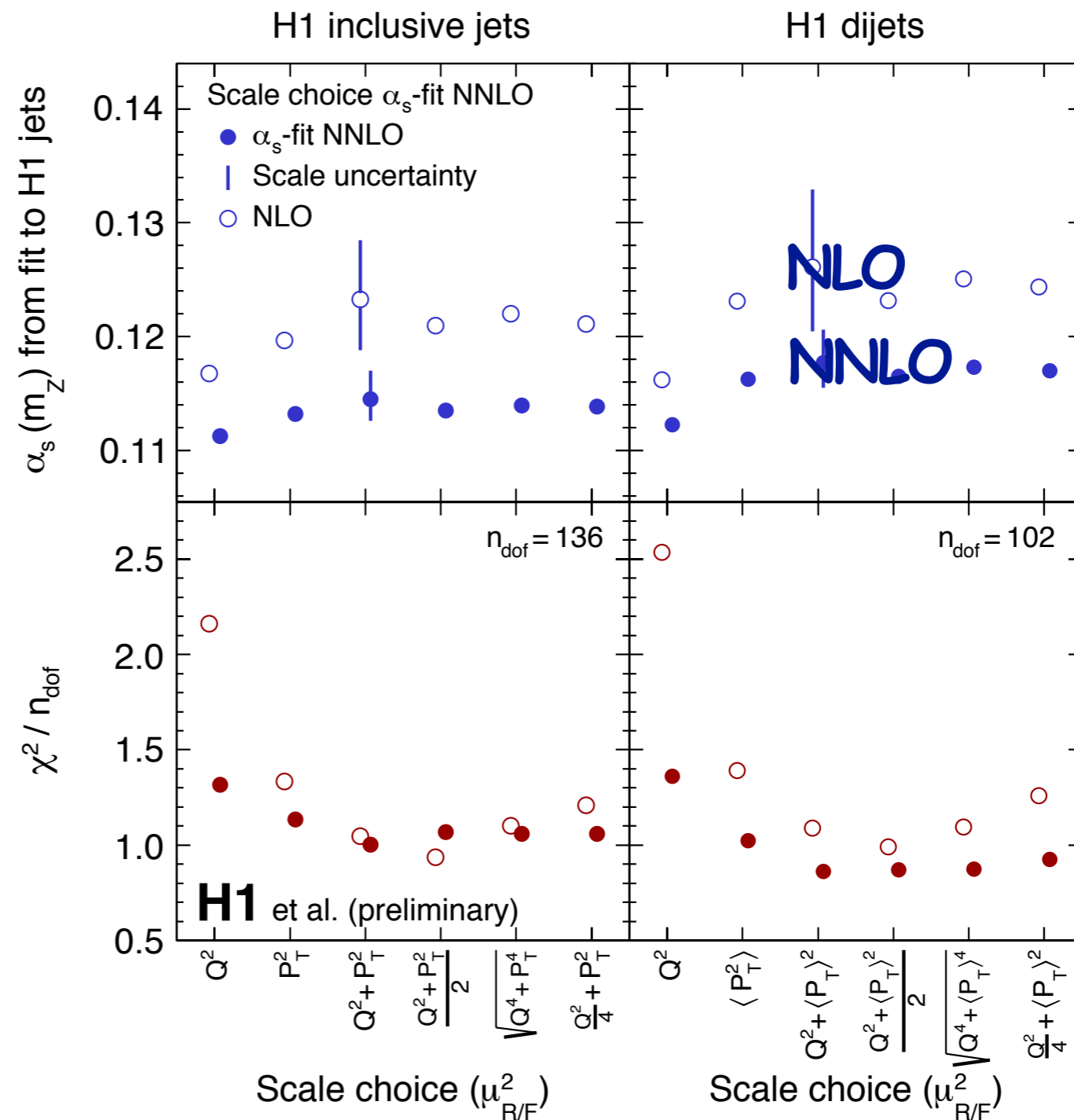


all calculations are done using
NNPDF3.0 NNLO

Dependence of α_s on scale choice

Study various scales consisting of Q^2 and P_T or $\langle P_T \rangle$

Reduced scale dependence in NNLO



Extraction of α_s

Fit theory to jet data, using:

$$\chi^2 = \sum_{i,j} \log \frac{S_i}{\sigma_i} (V_{\text{exp}} + V_{\text{had}} + V_{\text{PDF}})_{ij}^{-1} \log \frac{S_j}{\sigma_j}$$

taking experimental, PDF and hadronization uncertainties into account

- define theory inputs (order in α_s , PDFs, scales, ...)
- minimise χ^2 using Minuit and obtain α_s
- propagate exp., PDF, had. uncertainties