

# Measurement of Jet Cross Sections in Deep-inelastic Scattering at HERA and Extraction of $\alpha_s$ at NNLO

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for the H1 Collaboration together with  
V. Bertone, J. Currie, C. Gwenlan, T. Gehrmann, A. Huss, J. Niehues, M. Sutton

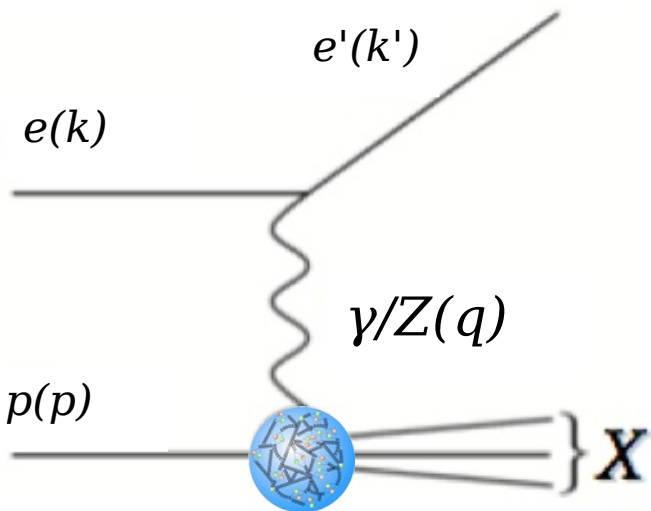
EPS Conference on High Energy Physics 2017  
Venice, Italy  
07.07.2017



# Deep-inelastic ep scattering

**Neutral current scattering (NC)**

$$ep \rightarrow e'X$$



**Kinematic variables**

Photon virtuality

$$Q^2 = -q^2 = -(k - k')^2$$

Inelasticity

$$y = \frac{p \cdot q}{p \cdot k}$$

**HERA ep collider in Hamburg**



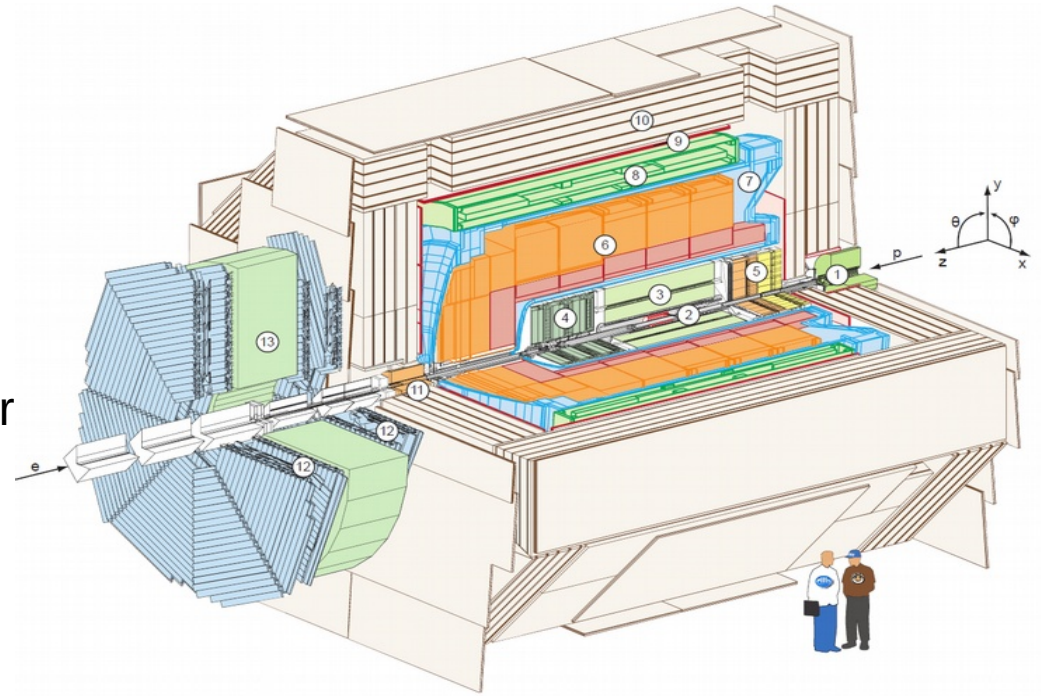
**Data taking periods**

- HERA I: 1994 – 2000
- HERA II: 2003 – 2007
- $\sqrt{s} = 300$  or  $319$  GeV

# H1 Experiment at HERA

## ***H1 multi-purpose detector***

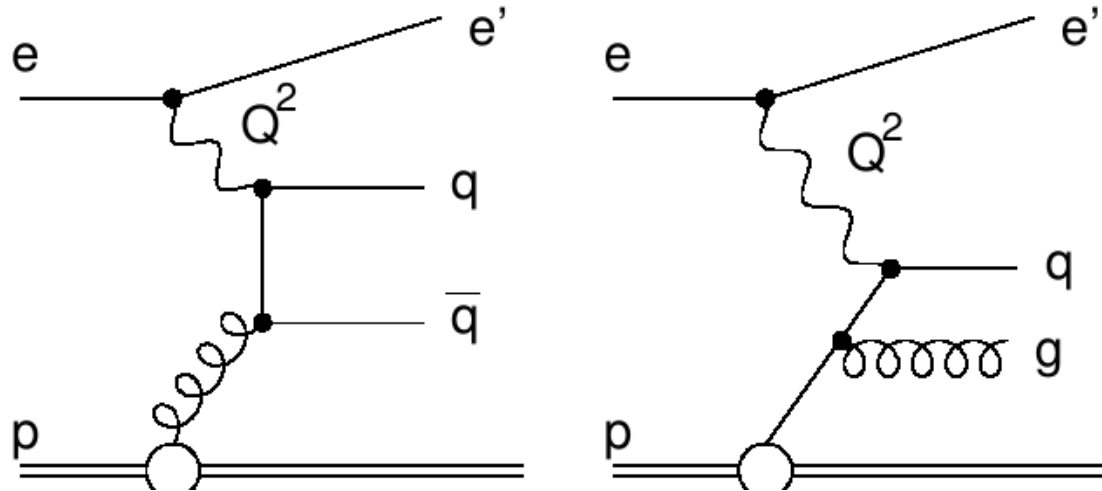
- Asymmetric design
- Trackers:
  - silicon tracker, jet chambers, proportional chambers, ...
- Calorimeters
  - Liquid Argon sampling calorimeter
  - SpaCal: scintillating fiber calorimeter
- Superconducting magnet: 1.15T
- Muon detectors



## ***Excellent experimental precision***

- Overconstrained system in NC DIS
- Electron measurement: 0.5 – 1% scale uncertainty
- Jet energy scale: 1%
- Luminosity: 2.5%

# Jet production in $ep$ scattering

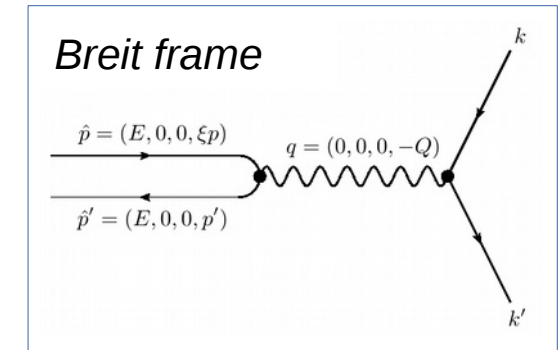


## **Jet measurements are performed in Breit reference frame**

- Virtual boson collides 'head-on' with parton from proton

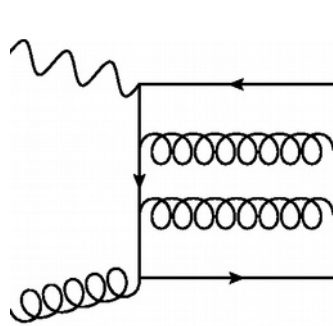
## **Jet measurements directly sensitive**

- to  $\alpha_s$  already at leading-order
- to gluon content of proton
- Trijet measurement at  $O(\alpha_s^2)$  in leading-order

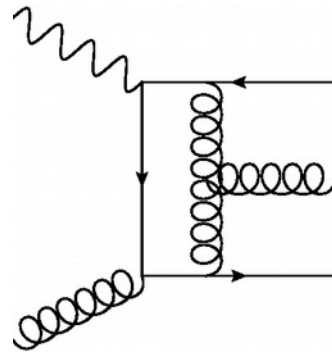


# DIS jet production in NNLO

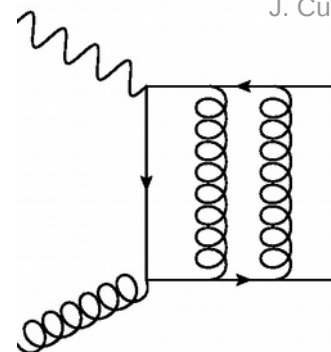
J. Currie, et al. [RPL 117 (2016) 042001]  
 J. Currie, et al. [arXiv:1703.05977]



Double-real



Real-virtual



Double-virtual

$$d\sigma_{NNLO}^{RR,S} \approx \underbrace{X(\{p_X\})}_{\text{antenna}} \overbrace{d\Phi_3(\{p_X\})}^{\text{Antenna PS}} \times \underbrace{|\mathcal{M}(\{\widetilde{p}_m\})|^2}_{\text{reduced ME}} \overbrace{d\Phi_m(\{\widetilde{p}_m\})}^{\text{reduced PS}} \times \underbrace{\mathcal{J}(\{\widetilde{p}_m\})}_{\text{jet function}}$$

## A bit of history

- 1973 asymptotic freedom of QCD  
 [PRL 30(1973) 1343 & 1346]
- 1993 NLO studies of DIS jet cross sections  
 [Phys. Rev. D49 (1994) 3291]
- 2016 NNLO corrections for DIS jets  
 [Phys. Rev. Lett. 117 (2016) 042001], [arXiv:1703.05977]

## Antenna subtraction

- Cancellation of IR divergences with local subtraction terms
- Construction of (local) counter terms
- Move IR divergences across different phase space multiplicities

# Measurement of Jet Production Cross Sections in Deep-inelastic $ep$ Scattering at HERA

H1 Collaboration  
Eur.Phys.J. C77 (2017) 4, 215  
[arxiv:1611.03421]

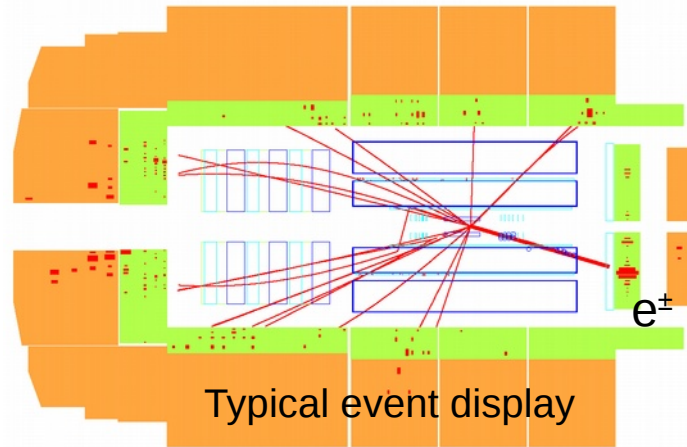
# Analysis strategy and kinematic range

## Simultaneous measurement

- Inclusive jet, dijet trijet and NC DIS cross sections
- $k_T$  jets with  $R=1$ ,  $-1 < \eta^{\text{lab}} < 2.5$

$$5.5 < Q^2 < 80 \text{ GeV}^2$$

$$4.5 < P_T^{\text{jet}} < 50 \text{ GeV}$$



## Regularised unfolding optimised for accurate description of relevant 'migrations'

- 'extended phase space'
- Account for statistical correlations
- Matrix: 3381 x 12800 elements

## Migration Matrix

	$\epsilon_1$	$\epsilon_2$	$\epsilon_3$
Detector level	Reconstructed Trijet events which are not generated as Trijet event $\epsilon_3$		Trijet $Q^2, <p_T>_3, y,$ Trijet-cuts $\epsilon_3$
		Dijet $Q^2, <p_T>_2, y,$ Dijet-cuts $\epsilon_2$	
	Reconstructed jets without match to generator level $\epsilon_1$	Incl. Jet $p_T^{\text{jet}}, Q^2, y, \eta$ $\epsilon_1$	
	NC DIS $Q^2, y$ $\epsilon_1$		
	Hadron level		

H1, EPJ C75 (2015) 2

# Dijet cross sections

## Dijet cross sections

- as a function of  $Q^2$  and  $\langle p_T \rangle_2$
- $\langle P_T \rangle_2 = (P_{T^{\text{jet}1}} + P_{T^{\text{jet}2}})/2$   
with:  $P_{T^{\text{jet}}} > 4 \text{ GeV}$
- Ratio to NLO predictions shown

## NLO (*nlojet++*, *NNPDF30\_nlo*)

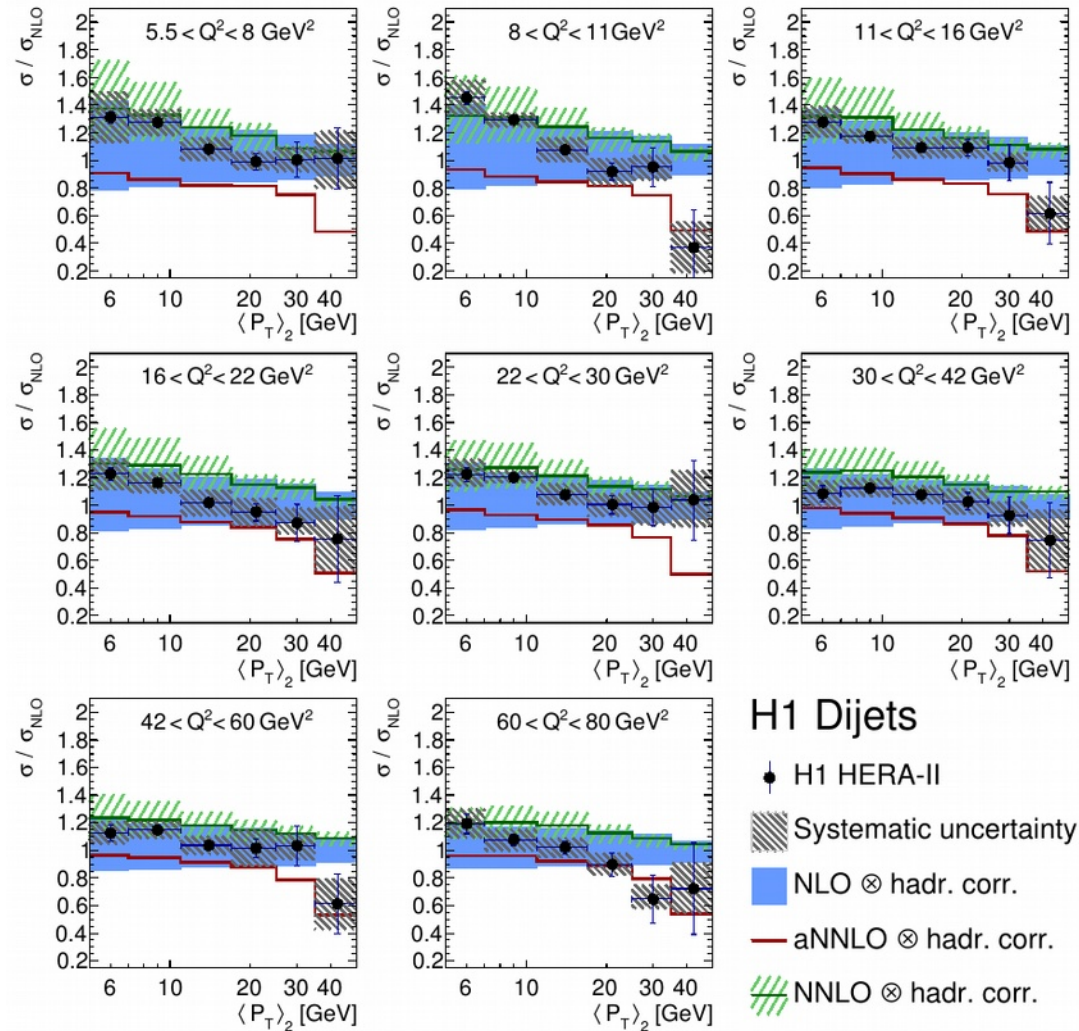
- reasonable description
- large scale uncertainties

## approximate NNLO (*JetVip*, *NNPDF30\_nnlo*)

- improved shape description

## NNLO (*NNLOJET*, *NNPDF30\_nnlo*)

- good description data
- NNLO predictions with reduced scale uncertainties than NLO



## H1 Dijets

- H1 HERA-II
- Systematic uncertainty
- NLO  $\otimes$  hadr. corr.
- aNNLO  $\otimes$  hadr. corr.
- NNLO  $\otimes$  hadr. corr.



# Inclusive jet cross sections

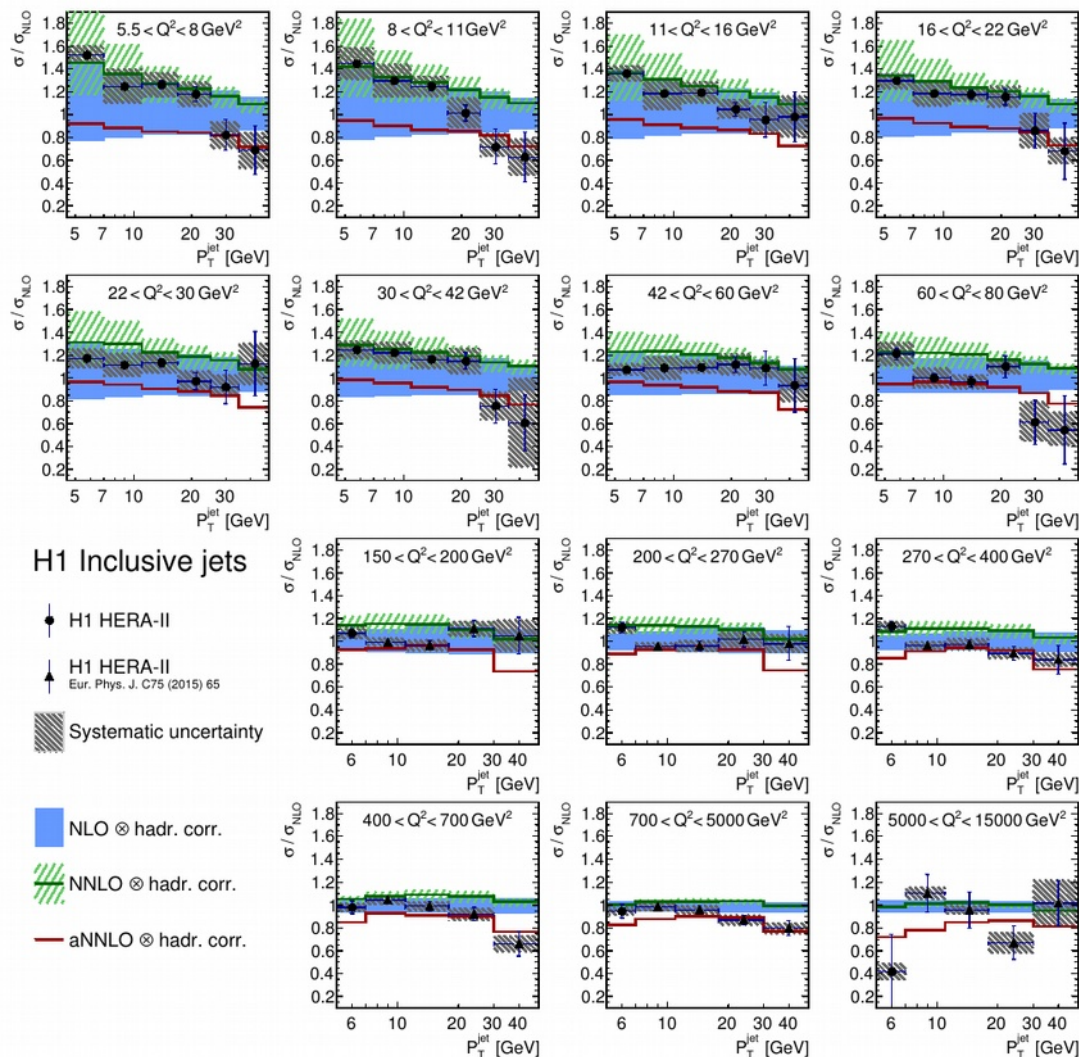
## Inclusive jet cross sections

- low  $Q^2$ :  $4.5 < P_T < 50$  GeV (new!)
- high  $Q^2$ :  $5 < P_T < 7$  GeV (new!)
- high  $Q^2$ :  $7 < P_T < 50$  GeV (EPJ C75 (2015) 2, 65)
- NNLO with reasonable description within (scale) uncertainties
- aNNLO with somewhat improved shape

## NNLO predictions

- NNLO provides improved shape and normalisation description
- NNLO with reduced scale uncertainties

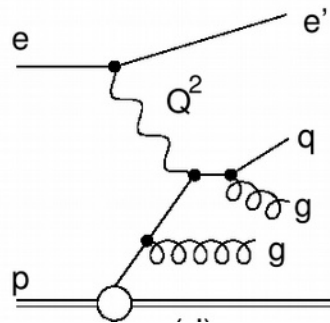
Also normalised (inclusive) jet cross sections measured -> see backup



# Trijet cross sections

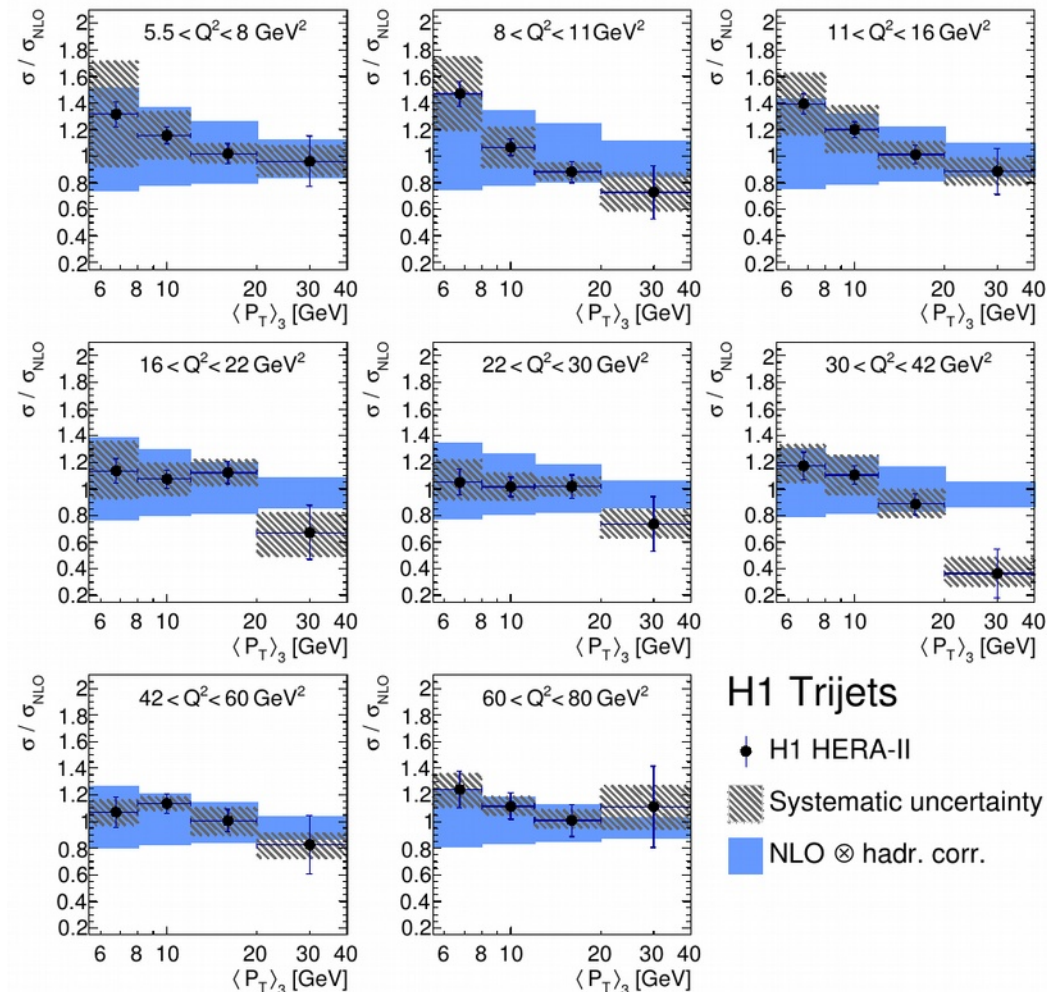
## Trijet cross sections

- Leading order  $O(\alpha_s^2)$
- No NNLO predictions available yet



Example for LO matrix element

- Data well described by NLO (nlojet++)
- Data typically with smaller uncertainties than NLO theory
- Similar trend as dijets
  - low scales: NLO undershoots data
  - high  $\langle P_T \rangle$ : NLO overshoots data
- Normalised trijets also measured



## H1 Trijets

- H1 HERA-II
- Systematic uncertainty
- NLO  $\otimes$  hadr. corr.

# Determination of $\alpha_s(m_Z)$ in next-to-next-to-leading order QCD using H1 jet cross section measurements

H1prelim-17-031

H1 Collaboration together with

V. Bertone, J. Currie, C. Gwenlan, T. Gehrmann, A. Huss, J. Niehues, M. Sutton  
[available at [https://www-h1.desy.de/publications/H1preliminary.short\\_list.html](https://www-h1.desy.de/publications/H1preliminary.short_list.html)]

# Why $\alpha_s$ ?

*Strong coupling  $\alpha_s$  enters in the calculation of every process that involves the strong interaction*

## PDG world average (2016)

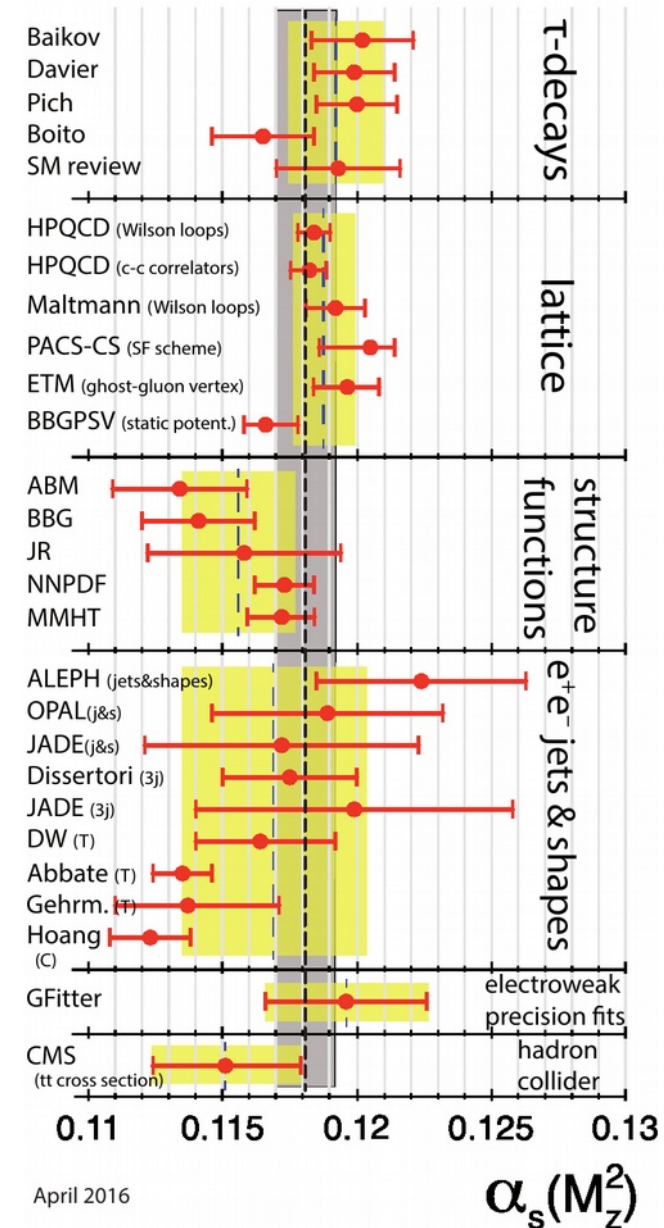
- $\alpha_s(m_Z) = 0.1181 \pm 0.0011$  [PDG2016]
- $\sim 0.9\%$  relative uncertainty

## Uncertainty on $\alpha_s$

- Important for precision phenomenology
- Notable examples: Higgs production cross sections, branching ratios

## Jet measurements

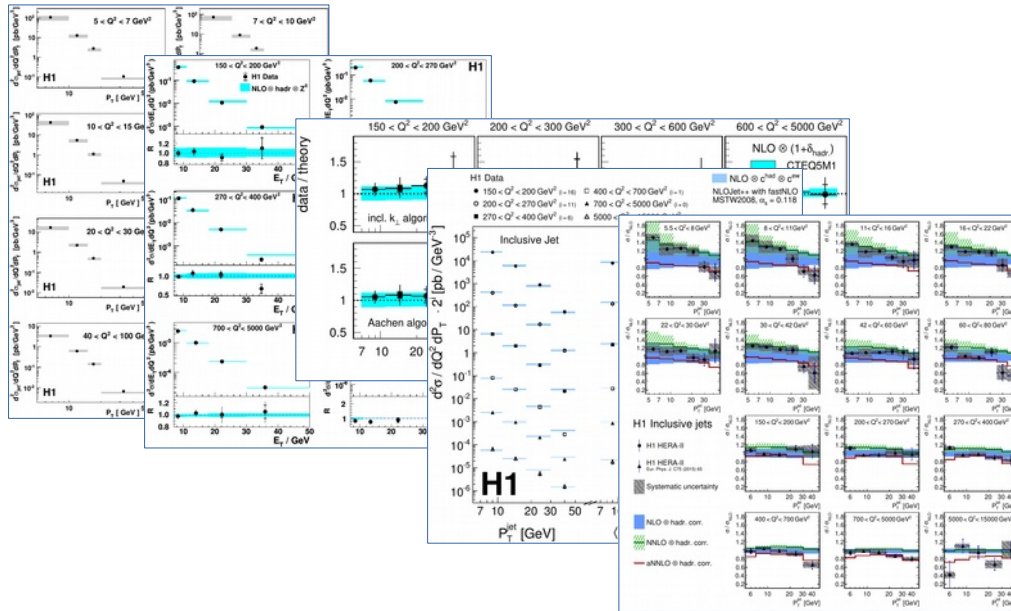
- Direct constraint on  $\alpha_s$
- So far no NNLO results available



# Inclusive jet and dijet cross sections at H1

## Inclusive jet cross sections

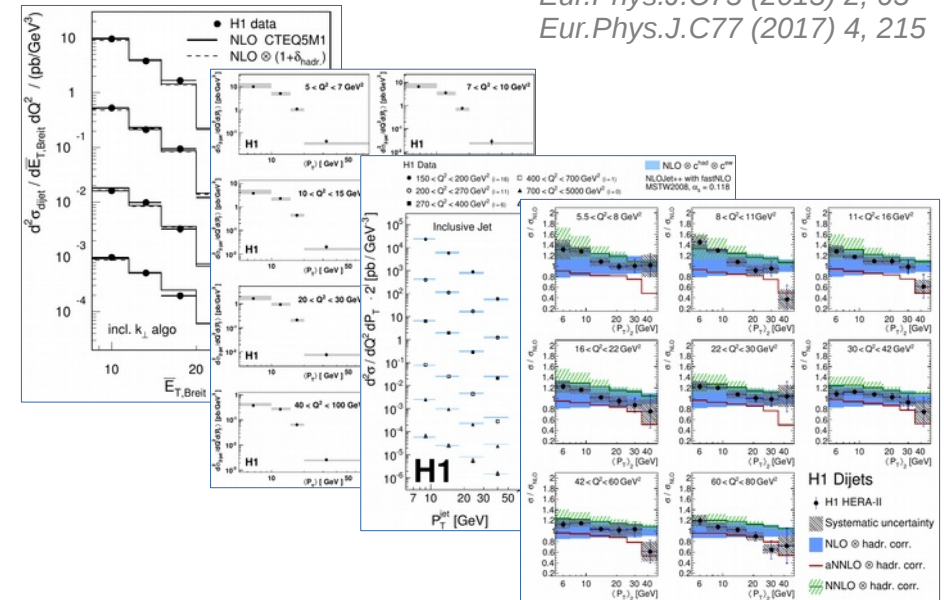
- Measurements at HERA-I & HERA-II
- low- $Q^2$  and high- $Q^2$
- Different  $\sqrt{s}$



## Dijet cross sections

- as a function of  $Q^2$  and  $\langle p_T \rangle_2$
- HERA-I & HERA-II
- low- $Q^2$  and high- $Q^2$
- Different  $\sqrt{s}$

*Eur.Phys.J.C65 (2010) 363*  
*Eur.Phys.J.C67 (2010) 1*  
*Eur.Phys.J.C19 (2001) 289*  
*Eur.Phys.J.C75 (2015) 2, 65*  
*Eur.Phys.J.C77 (2017) 4, 215*



All H1 inclusive jet and dijet data is employed for  $\alpha_s$  determination in NNLO

# $\alpha_s(m_Z)$ dependence of cross sections

**Jet cross sections directly sensitive to  $\alpha_s$**

$$\sigma_i = \sum_{n=1}^{\infty} \sum_{k=g,q,\bar{q}} \int dx f_k(x, \mu_F) \hat{\sigma}_{i,k}^{(n)}(x, \mu_R, \mu_F) \cdot C_{\text{had}}$$

- Two  $\alpha_s$ -dependencies

PDFs  $\frac{\partial f}{\partial \alpha_s} = \frac{\mathcal{P} \otimes f}{\beta}$

Hard ME's

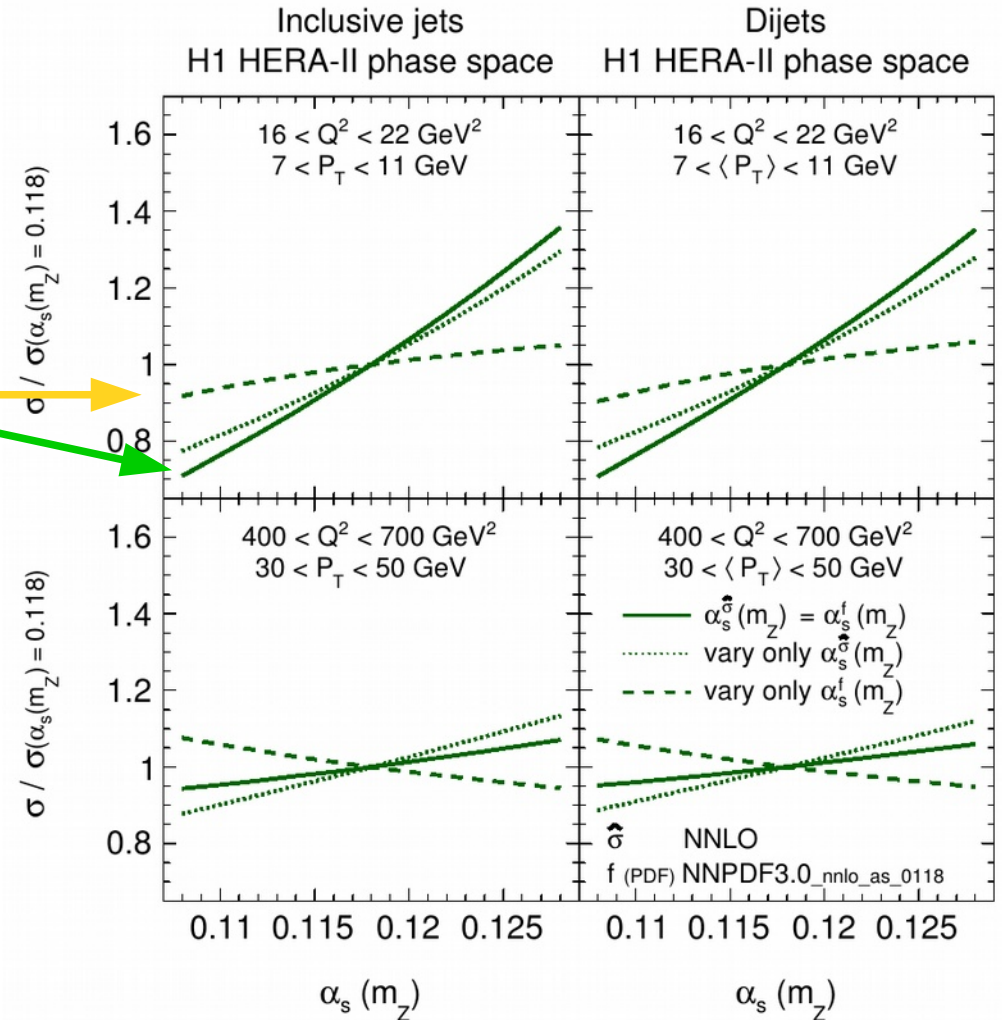
$$\hat{\sigma}_{i,k}^{(n)} = \alpha_s^n(\mu_R) \tilde{\sigma}_{i,k}^{(n)}(x, \mu_R, \mu_F)$$

**At lower scales**

- Predominant  $\alpha_s$ -sensitivity from hard coefficients
- PDF's provide increased sensitivity

**At higher scales**

- opposite dependence for hard coefficients and PDFs

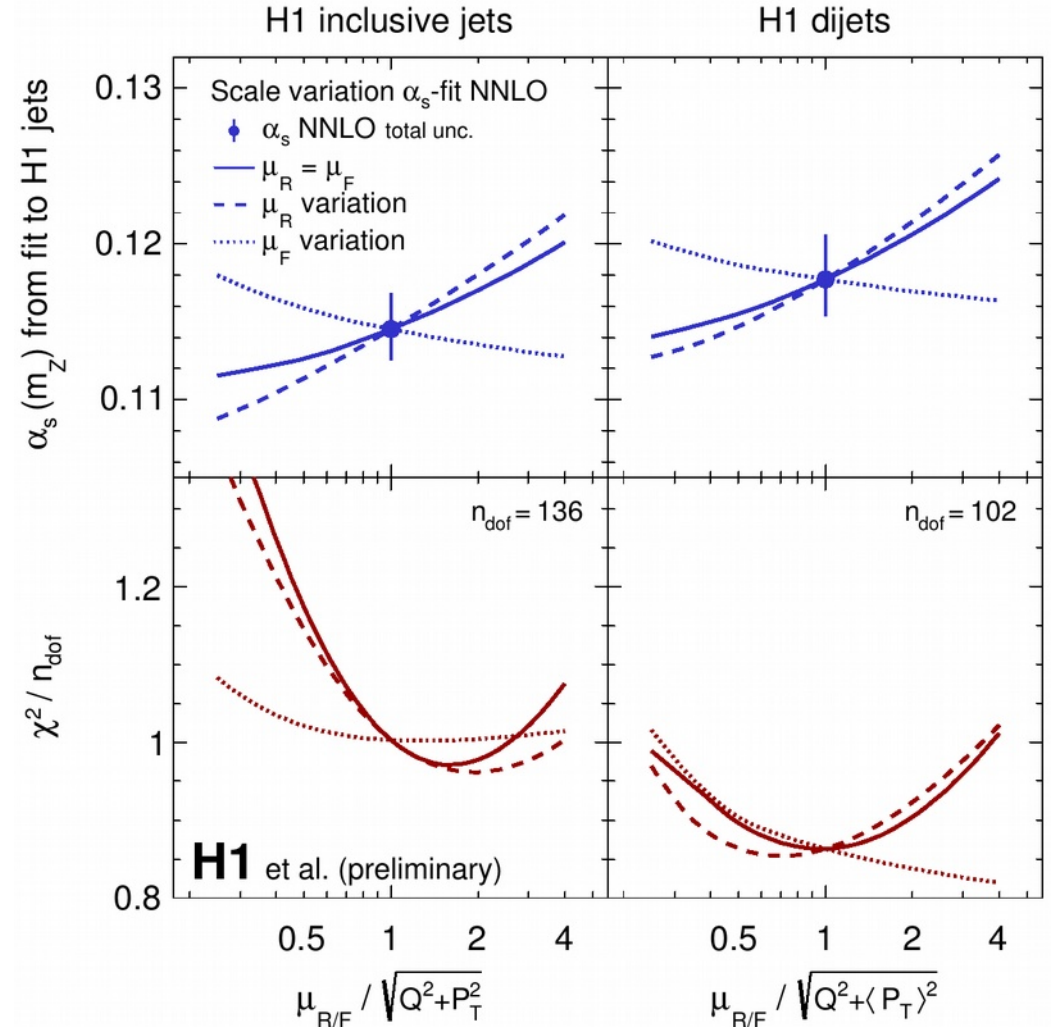


# Scale dependence of $\alpha_s$ fit

- $\alpha_s$  results as a function of scale factors to nominal scale

$$\mu_R^2 = \mu_F^2 = Q^2 + P_T^2$$

- $\mu_r$  variation with more impact than  $\mu_f$
- $\chi^2$  values as a technical parameter  
-> not intended to be a parabolas
- $\chi^2$  values increase for large scale factors  
-> large scale factors disfavored  
-> A-priori chosen scale appears to be reasonable



# Scale choice for $\alpha_s$ fit

- Study various definition for scales ( $\mu_r, \mu_f$ ) built from  $Q^2$  and  $p_T$   
 $p_T$  denotes:  $p_T^{\text{jet}}$  or  $\langle p_T \rangle$

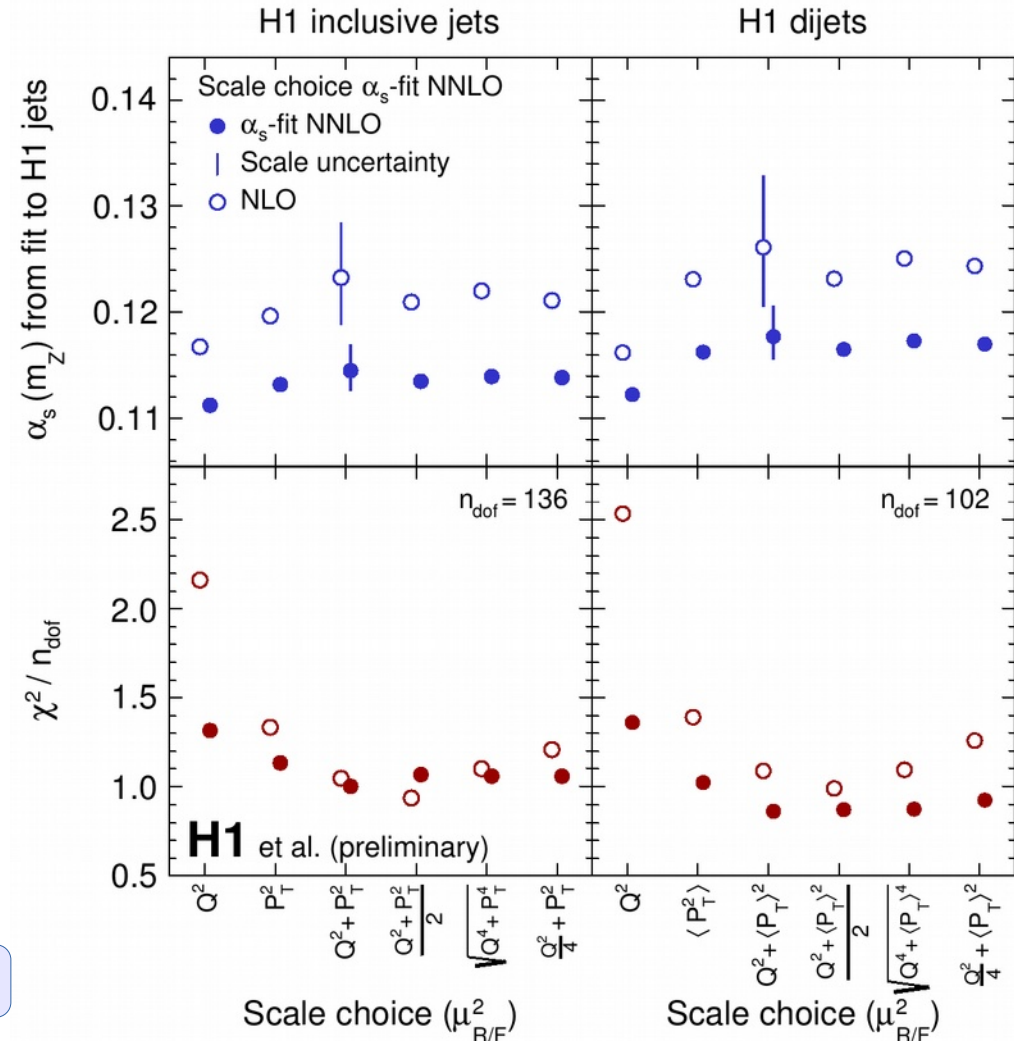
## $\alpha_s$ results and $\chi^2$ values

- Spread of results covered by scale uncertainty (variation by 0.5 & 2)
- $\chi^2$  values are all reasonable for different choices

## NLO vs. NNLO

- Reduced scale uncertainty in NNLO
- NNLO with reduced scale-dependence of  $\alpha_s$  and  $\chi^2$  values
- NLO with larger  $\chi^2$  values

NNLO with reduced scale dependence





# Strong coupling in NNLO from H1 jets

## Uncertainty breakdown includes

- Experimental and hadronisation uncertainty
- Scale uncertainties (factors: 0.5, 2)
- (various) PDF uncertainties

## $\alpha_s$ results from individual data sets

- High experimental precision
- All fits with good  $\chi^2$   
-> consistency of data

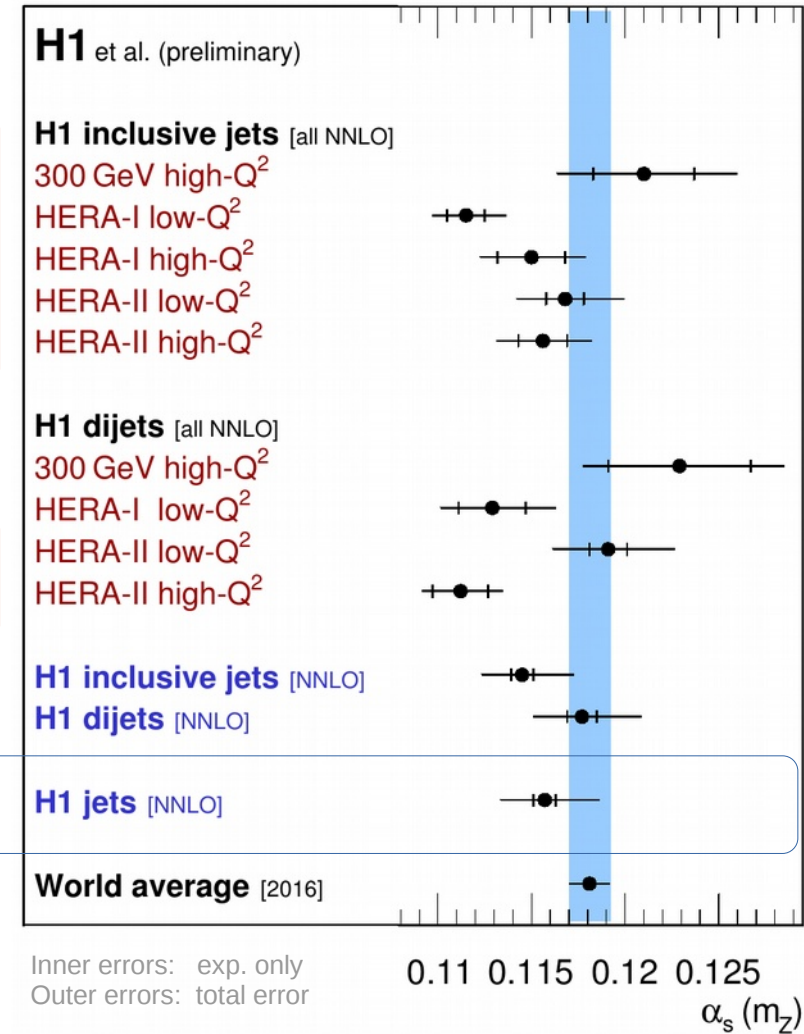
## 'H1 jets'

- Inclusive jet and dijet data taken together
- 203 data points

$$\alpha_s(M_Z) = 0.1157 (6)_{\text{exp}} (3)_{\text{had}} (6)_{\text{PDF}} (12)_{\text{PDF}\alpha_s} (2)_{\text{PDFset}} \left( \begin{smallmatrix} +27 \\ -21 \end{smallmatrix} \right)_{\text{scale}}$$

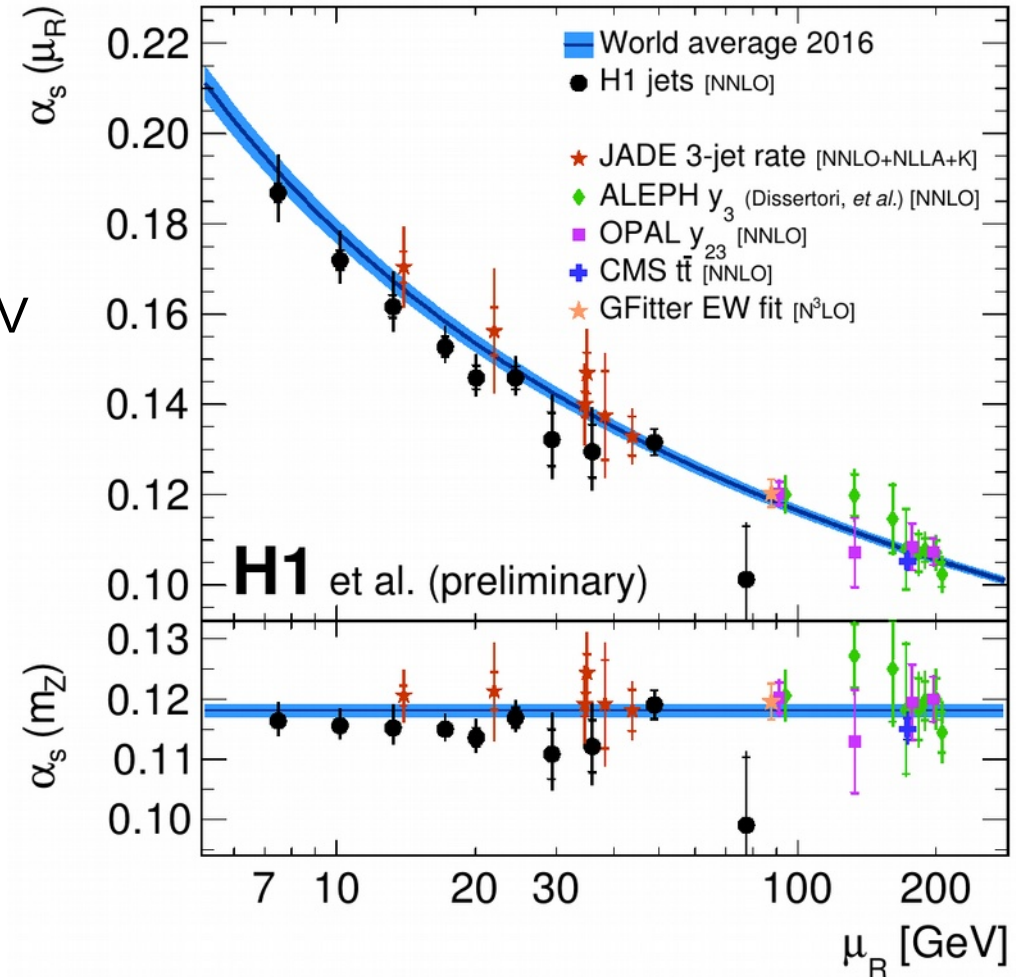
- High exp. precision
- Scale uncertainty dominates
- PDF uncertainties sizeable

$$\chi^2/n_{\text{dof}} = 1.03$$



# Test running of strong coupling in NNLO

- Repeat fits to groups of data points
- Theory uncertainty often larger than experimental uncertainty
- Confirmation of 'running' between 7–90 GeV
- Consistency with other extractions and with other processes
- Scale uncertainty is largest uncertainty for most intervals
- NNLO with small scale uncertainty (also) at lower scales



# Summary

## **New measurement of jet cross sections in NC DIS** [EPJ C77 (2017) 4, 215]

- Inclusive jet, dijet and trijet cross sections
- Normalised jet cross sections with reduced experimental uncertainty
- Data well described by (new) NNLO predictions
- NNLO corrections are important at lower scales



## **Strong coupling constant determined in NNLO** [H1prelim-17-031]

- Explore all H1 inclusive jet and dijet cross section measurements (1995 – 2007)

$$\alpha_s(m_Z) = 0.1157(6)_{\text{exp}} \left( \begin{matrix} +31 \\ -26 \end{matrix} \right)_{\text{theo}}$$

- High experimental precision & competitive theoretical precision
- Probe running of  $\alpha_s$  over one order of magnitude with H1 jet data
- [https://www-h1.desy.de/publications/H1preliminary.short\\_list.html](https://www-h1.desy.de/publications/H1preliminary.short_list.html)  
Preprint ready in 5-7 weeks



H1 in collaboration with  
V. Bertone, J. Currie, T. Gehrmann,  
C. Gwenlan, A. Huss, J. Niehues, M. Sutton

## **Precision QCD phenomenology with jets in NNLO accuracy**

- Fruitful collaboration of theoreticians and experimentalists



# Fit methodology

## $\alpha_s$ from $\chi^2$ -minimisation

- $\alpha_s(m_Z)$  is a free parameter to NNLO theory prediction  $\sigma_i$
- $\chi^2$  calculated as: ( $\zeta$ =Data,  $\sigma_i$ =NNLO,  $V$ =covariance matrices)

$$\chi^2 = \sum_{i,j} \log \frac{S_i}{\sigma_i} (V_{\text{exp}} + V_{\text{had}} + V_{\text{PDF}})^{-1}_{ij} \log \frac{S_j}{\sigma_j}$$

## Perform fits to

- All 9 individual data sets
- All 5 inclusive jet data sets (137 data points)
- All 4 dijet data sets (103 data points)
- All H1 jet data taken together (denoted as 'H1 jets')  
(exclude HERA-I dijet data as correlations to inclusive jets are not known)
- Data points at a similar scale  $\mu$
- Data points above a certain scale value  $\mu_{\text{min}}$

## Additional cuts

- remove data below  $\mu < 2m_b$ , to avoid effects from heavy quark masses
- drop HERA-I, low- $Q^2$  dijets with  $\langle p_T \rangle < 7$  GeV, because of IR issue

# Selection of data sets

Kinematic range of H1 jet data

Data set [Ref.]	$\sqrt{s}$ [GeV]	int. $\mathcal{L}$ [pb <sup>-1</sup> ]	DIS kinematic range	Inclusive jets	Dijets $n_{\text{jets}} \geq 2$
300 GeV [1]	300	33	$150 < Q^2 < 5000 \text{ GeV}^2$ $0.2 < y < 0.6$	$7 < P_{\text{T}}^{\text{jet}} < 50 \text{ GeV}$	$P_{\text{T}}^{\text{jet}} > 7 \text{ GeV}$ $8.5 < \langle P_{\text{T}} \rangle < 35 \text{ GeV}$
HERA-I [2]	319	43.5	$5 < Q^2 < 100 \text{ GeV}^2$ $0.2 < y < 0.7$	$5 < P_{\text{T}}^{\text{jet}} < 80 \text{ GeV}$	$5 < P_{\text{T}}^{\text{jet}} < 50 \text{ GeV}$ $5 < \langle P_{\text{T}} \rangle < 80 \text{ GeV}$ $(\langle P_{\text{T}} \rangle > 7 \text{ GeV})^*$ $m_{12} > 18 \text{ GeV}$
HERA-I [3]	319	65.4	$150 < Q^2 < 15000 \text{ GeV}^2$ $0.2 < y < 0.7$	$5 < P_{\text{T}}^{\text{jet}} < 50 \text{ GeV}$	–
HERA-II [4]	319	290	$5.5 < Q^2 < 80 \text{ GeV}^2$ $0.2 < y < 0.6$	$4.5 < P_{\text{T}}^{\text{jet}} < 50 \text{ GeV}$	$P_{\text{T}}^{\text{jet}} > 4 \text{ GeV}$ $5 < \langle P_{\text{T}} \rangle < 50 \text{ GeV}$
HERA-II [5, 4]	319	351	$150 < Q^2 < 15000 \text{ GeV}^2$ $0.2 < y < 0.7$	$5 < P_{\text{T}}^{\text{jet}} < 50 \text{ GeV}$	$5 < P_{\text{T}}^{\text{jet}} < 50 \text{ GeV}$ $7 < \langle P_{\text{T}} \rangle < 50 \text{ GeV}$ $m_{12} > 16 \text{ GeV}$

# Inclusive jet cross sections by H1

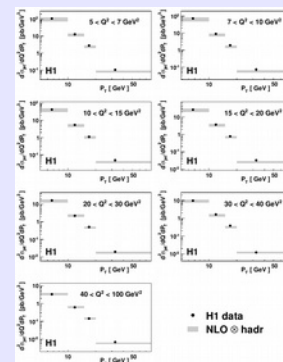
## Inclusive jet cross sections

- $d\sigma/dQ^2 dP_{T,jet}$
- 300 GeV, HERA-I & HERA-II
- low- $Q^2$  ( $<100 \text{ GeV}^2$ ) and high- $Q^2$  ( $>150 \text{ GeV}^2$ ) regions

## Consistency

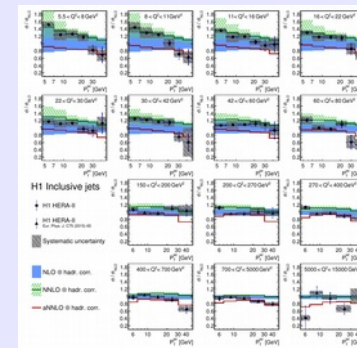
- kt-algorithm,  $R=1$
- $-1.0 < \eta < 2.5$
- $P_T$  ranges from 4.5 to 50 GeV

## HERA-I low- $Q^2$



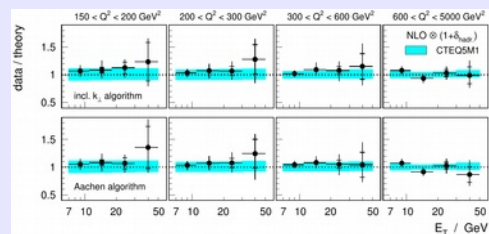
*Eur.Phys.J.C67 (2010) 1*

## HERA-II low- $Q^2$



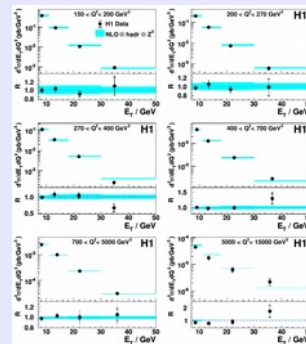
*Eur.Phys.J.C75 (2015) 2, 65*

## 300 GeV high- $Q^2$



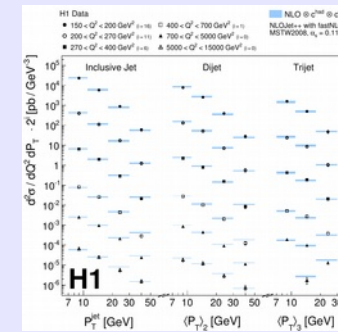
*Eur.Phys.J.C19 (2001) 289*

## HERA-I high- $Q^2$



*Phys.Lett.B653 (2007) 134*

## HERA-II high- $Q^2$



*Eur.Phys.J.C75 (2015) 2 arXiv:1611.03421*

# Dijet cross section by H1

## Dijet cross sections

- $d\sigma/dQ^2 d\langle p_T \rangle$
- 300 GeV, HERA-I & HERA-II
- low- $Q^2$  and high- $Q^2$

## Dijet definitions

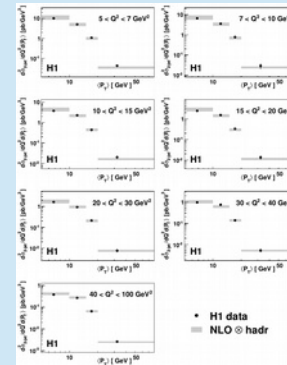
- $\langle p_T \rangle$  greater than 5, 7 or 8.5 GeV
- $P_T$  jet greater 4, 5 or 7 GeV
- Asymmetric cuts on  $p_{T,jet1}$  and  $p_{T,jet2}$
- $M_{12}$  cut for two data sets

## Earlier studies

- All inclusive jet and dijet data have been employed for  $\alpha_s$  extractions in NLO previously

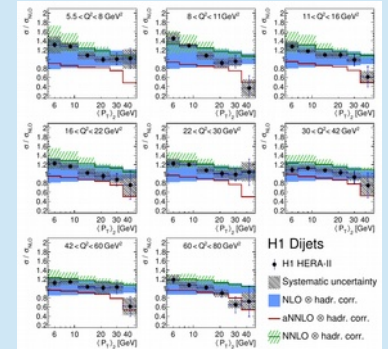
-> Data and uncertainties well-understood  
 -> NNLO theory is new

## HERA-I low- $Q^2$



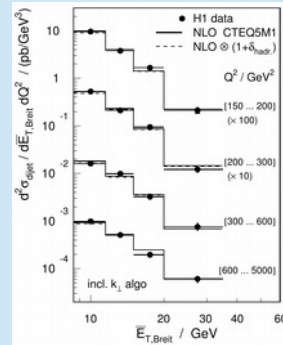
*Eur.Phys.J.C67 (2010) 1*

## HERA-II low- $Q^2$



*arXiv:1611.03421*

## 300 GeV high- $Q^2$

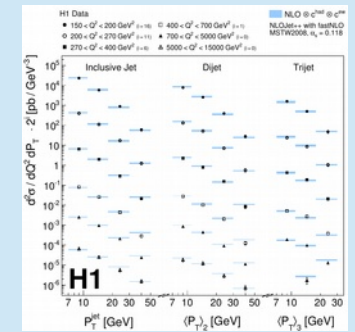


*Eur.Phys.J.C19 (2001) 289*

## HERA-I high- $Q^2$

Dijet cross sections not statistically independent from HERA-II analysis  
*Eur.Phys.J.C65 (2010) 363*

## HERA-II high- $Q^2$



*Eur.Phys.J.C75 (2015) 2*



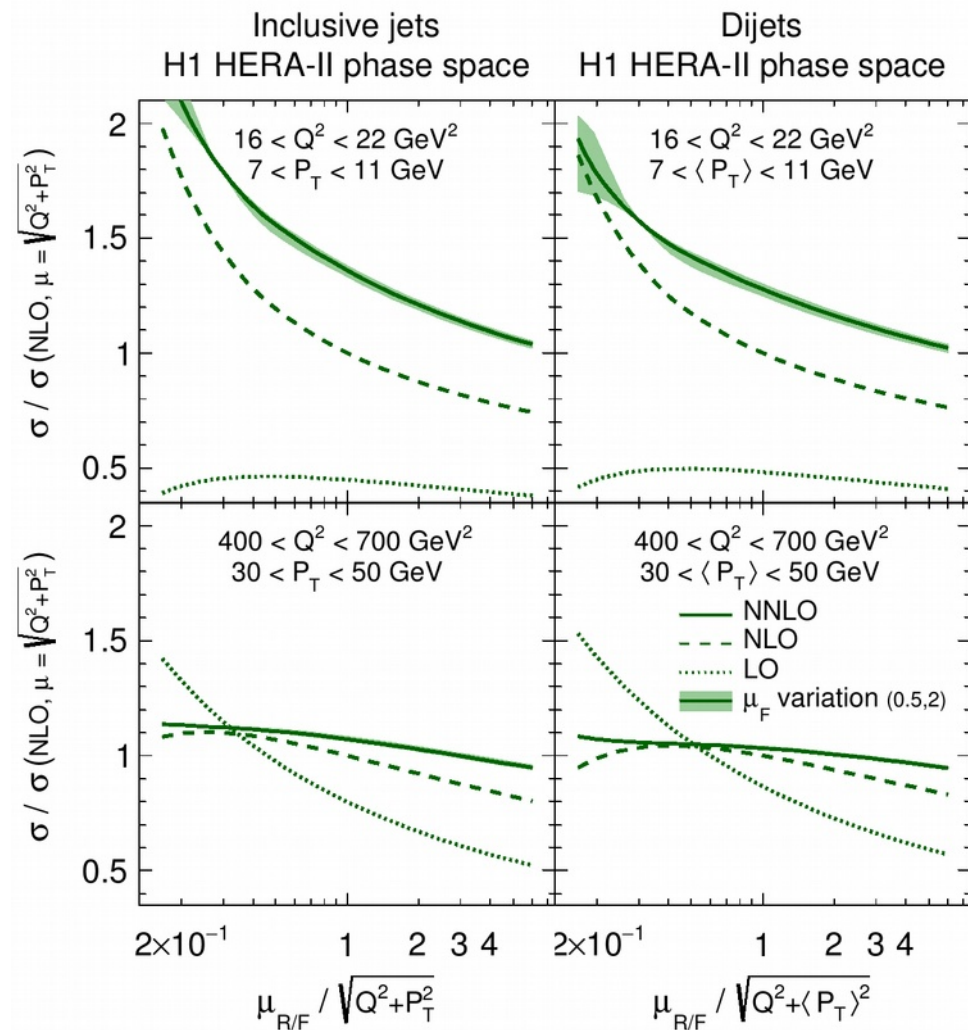
# Scale dependence of NNLO cross sections

## Scale dependence of NNLO cross sections

- Study simultaneous multiplicative variation of renormalisation and factorisation scale

## Scale dependence

- At lower scales
  - NNLO reduced scale dependence w.r.t. NLO
  - Still relevant scale dependence in NNLO
- At higher scales
  - Scale dependence reduced w.r.t. NLO
- $\mu_f$  dependence small
- Inclusive jets with higher scale dependence than dijets at lower scales



# $\alpha_s$ dependencies separately fitted

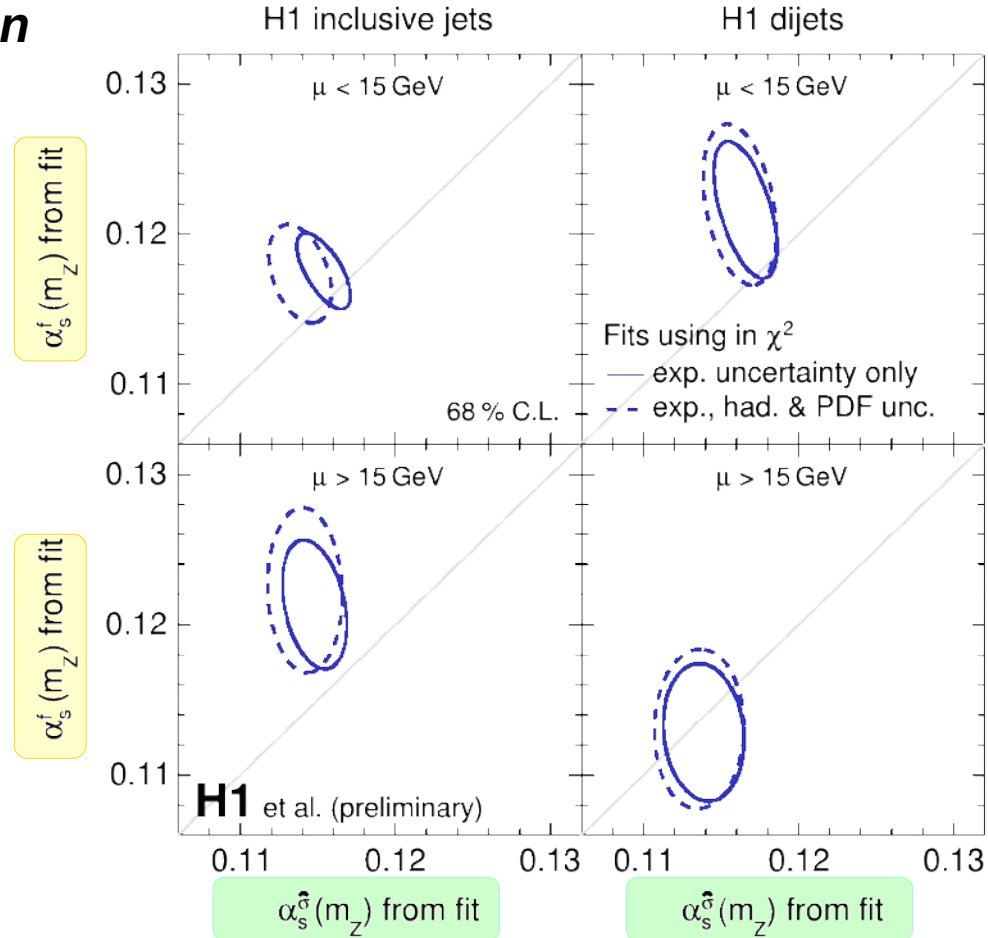
## Fits with two free $\alpha_s$ parameters in calculation

$$\sigma_i = f(\alpha_s^f(m_Z)) \otimes \hat{\sigma}_k(\alpha_s^{\hat{\sigma}}(m_Z)) \cdot c_{\text{had}}$$

- Separate fits for low- and high- $\mu$  data points
- Fits to Inclusive jet or dijet data

## Results

- Most sensitivity arises from **matrix elements**
- Best-fit  $\alpha_s$ -values in **PDF's** and **ME's** are consistent
- Significant anti-correlation at lower scales  
-> Increased sensitivity if both  $\alpha_s$ -values identified to be identical



# Dependence on the PDF

## PDF is external input NNLO calculation

### Choice of PDF set

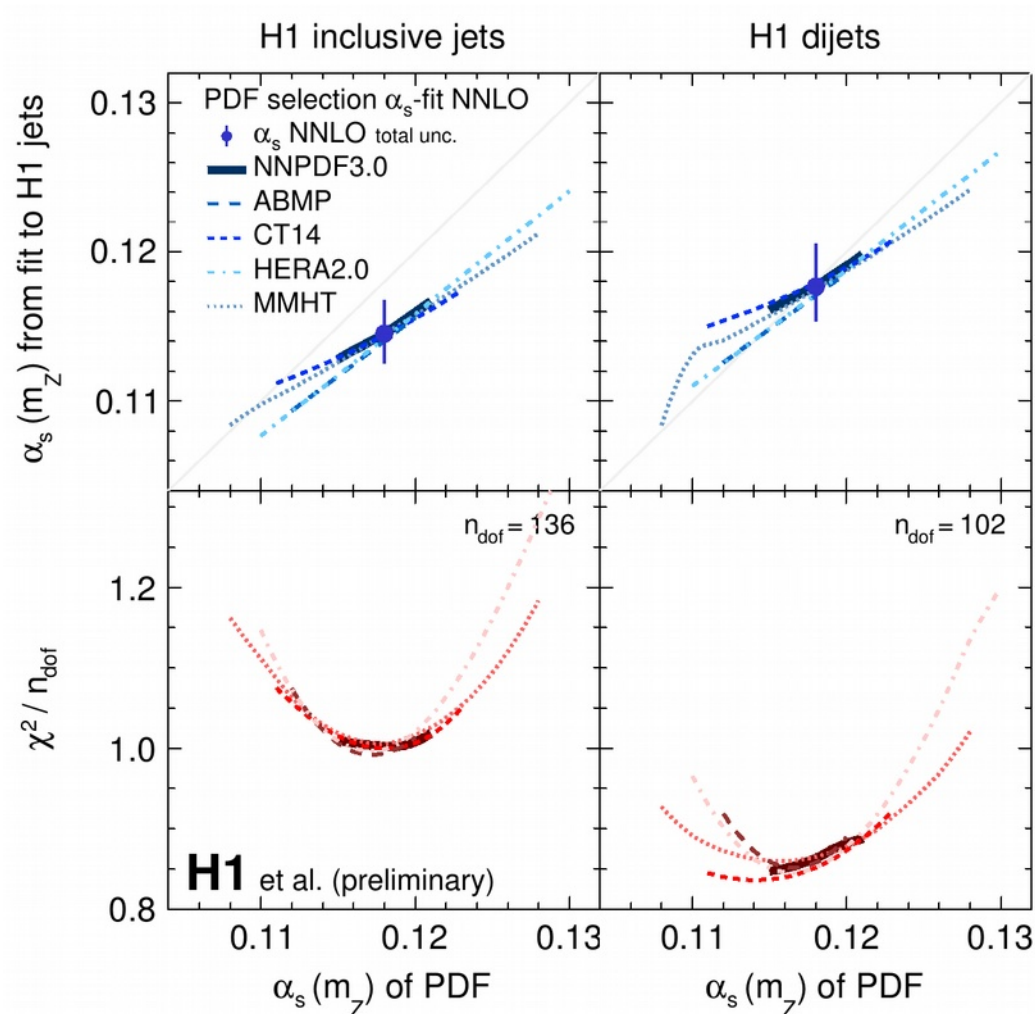
- Different PDF groups: different input data sets, PDF parameterisations, model parameters, fit methodology, etc...
- Different PDFs are consistent

### Choice of $\alpha_s$ as input to PDF

- $\alpha_s(m_Z)$  important input parameter to PDF fit
- Relevant correlation with fitted results
- Differences among different PDF sets

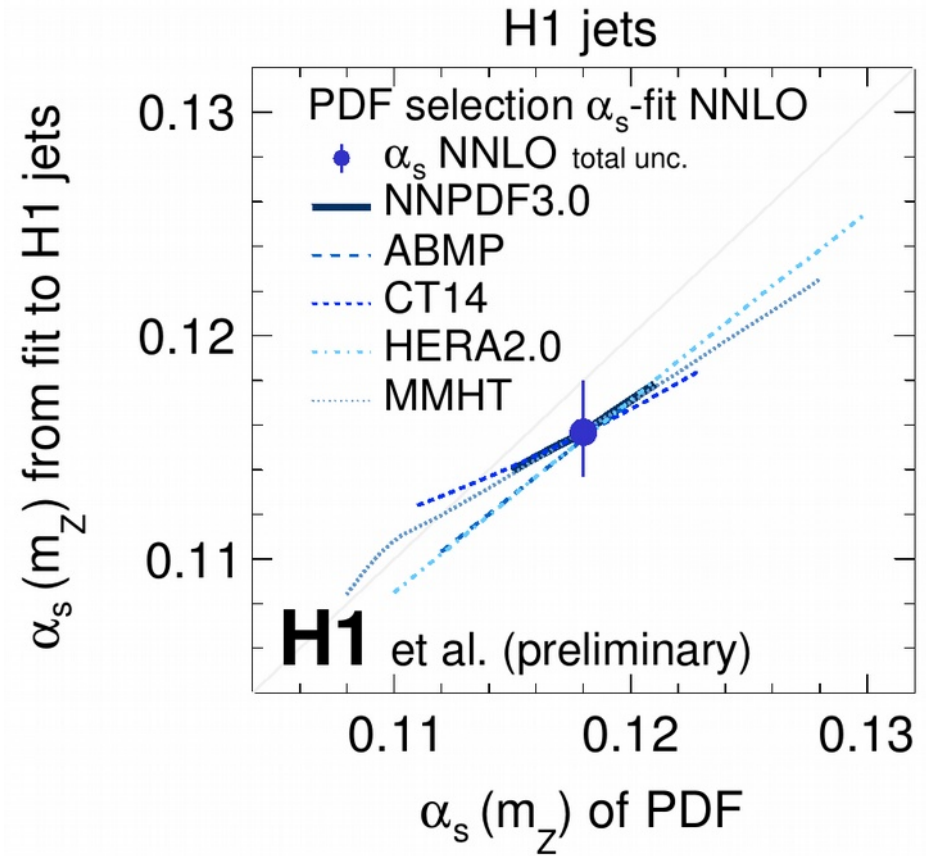
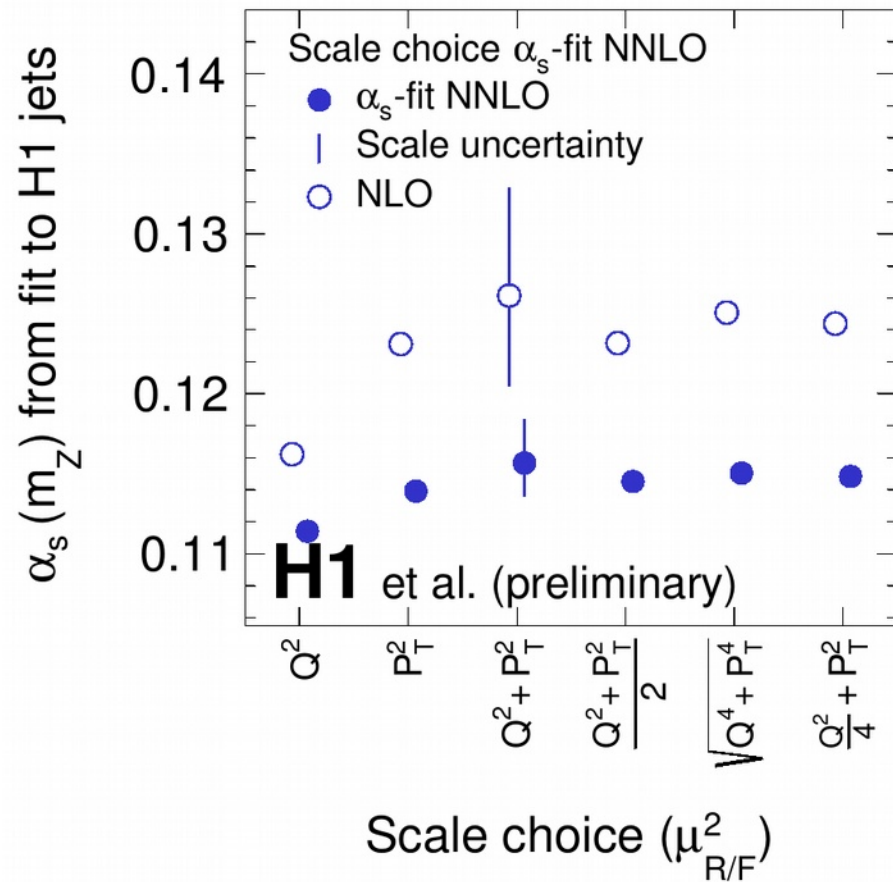
### Additional PDF uncertainties on result

- 'PDFset':  $1/2 \cdot \max(\Delta(\text{all PDFs}))$
- 'PDF $\alpha_s$ ':  $1/2 (\Delta\alpha_s = 0.004)$



# PDF dependence and scale choice

- Fits to 'H1 jets' (inclusive jets & dijet data taken together)



# Running from inclusive jets and dijets

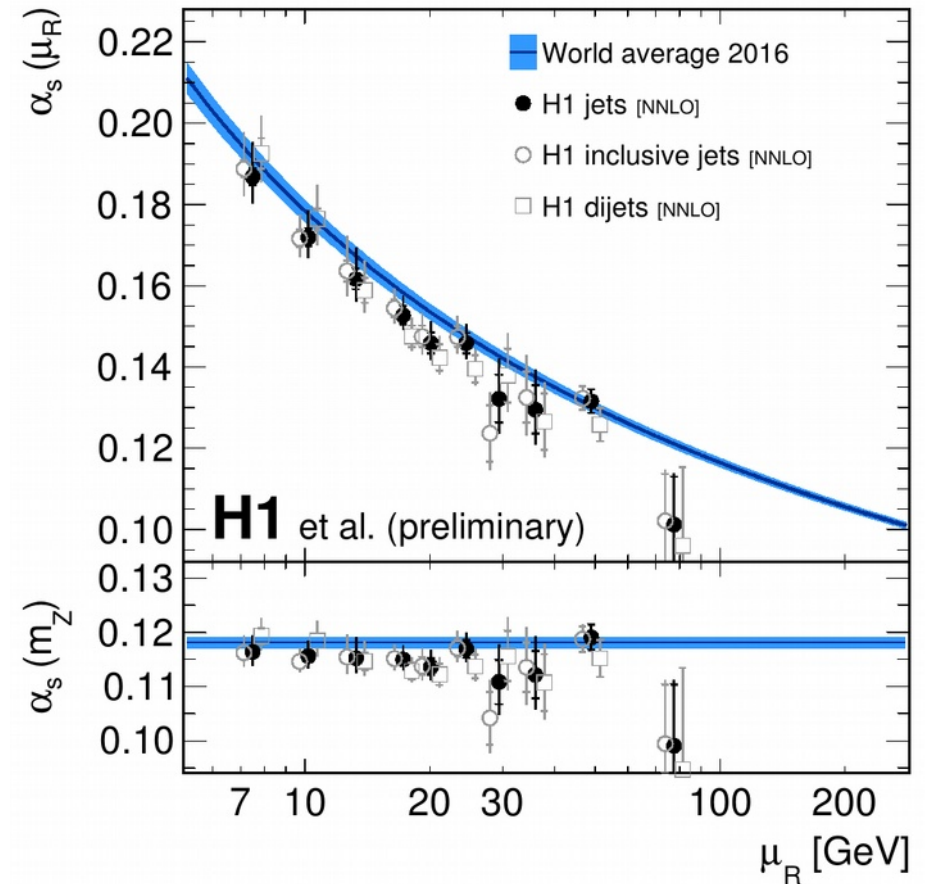
## Test running of strong coupling

- Repeat fits to groups of data points at similar scales
- All fits with good  $\chi^2$
- Study assumes running to be valid only within limited range covered by an interval

## Results

- Theory uncertainty often larger than experimental uncertainty
  - Consistency of inclusive jets and dijets
  - Consistency also down to lower scales (while otherwise data with  $\mu < 2m_B$  is excluded)
  - Scale uncertainty almost 'constant' at all scales
- > NNLO with small scale uncertainty (also) at lower scales

Confirmation of 'running' between 7-90 GeV



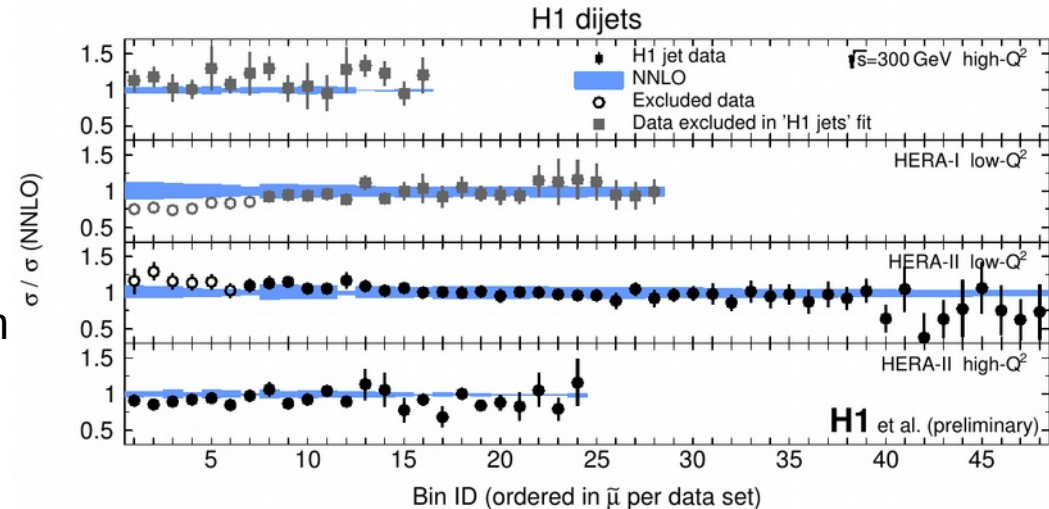
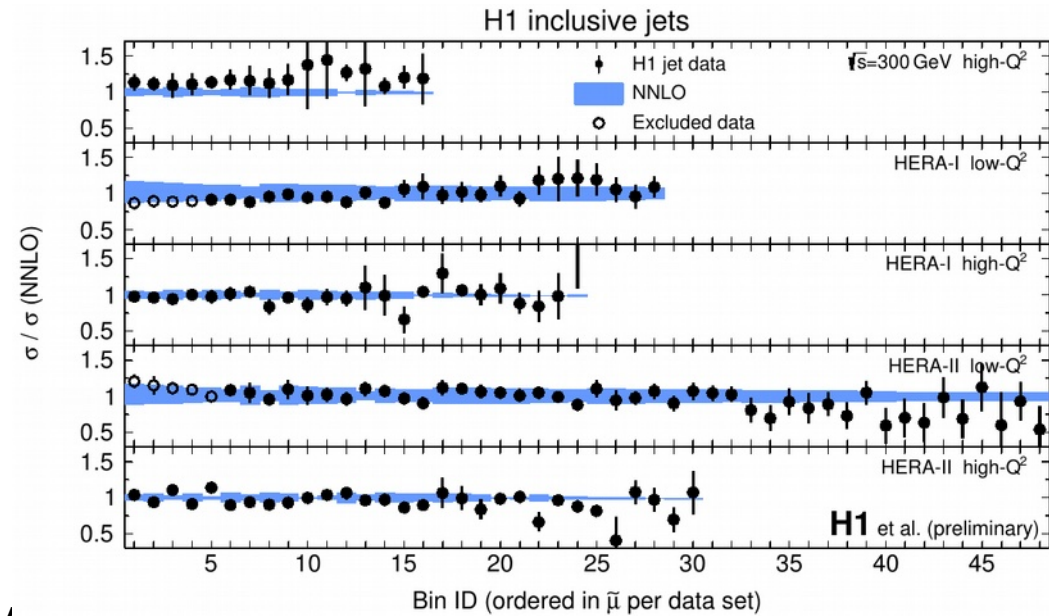
# NNLO cross sections

## Ratio of data to NNLO predictions

- Using:  $\alpha_s(m_Z) = 0.1157$
- Blue band: NNLO scale uncertainties
- Excluded data points (open symbols)
  - $\mu < 2m_b$
  - HERA-I low- $Q^2$  dijets:  $5 < \langle p_T \rangle < 7$  GeV
    - > because of symmetric cuts
    - > Issues with NNLO

## Conclusions

- Overall good agreement of NNLO predictions to H1 data
- Consistency of data
- All phase space regions in agreement with NNLO
  - > also confirmed by dedicated  $\chi^2$  studies





	Extended phase space for unfolding	Cross section phase space
NC DIS	$Q^2 > 3 \text{ GeV}^2$	$5.5 < Q^2 < 80 \text{ GeV}^2$
	$y > 0.08$	$0.2 < y < 0.6$
(inclusive) jets	$P_{\text{T}}^{\text{jet}} > 3 \text{ GeV}$	$P_{\text{T}}^{\text{jet}} > 4.5 \text{ GeV}$
	$-1.5 < \eta^{\text{lab}} < 2.75$	$-1.0 < \eta^{\text{lab}} < 2.5$
Dijet and trijet		$P_{\text{T}}^{\text{jet}} > 4 \text{ GeV}$
	$\langle P_{\text{T}}^{\text{jet}} \rangle > 3 \text{ GeV}$	$\langle P_{\text{T}}^{\text{jet}} \rangle > 5 [5.5] \text{ GeV}$

Phase space of measurement and phase space of unfolding

Predictions	NLO	aNNLO	NNLO
Program for jet cross sections	nlojet++	JetViP	NNLOJET
pQCD order	NLO	approximate NNLO	NNLO
Calculation detail	Dipole subtraction	Phase space slicing NNLO contributions from unified threshold resummation formalism	Antenna subtraction
Program for NC DIS	QCDNUM	APFEL	APFEL
Heavy quark scheme	ZM-VFNS	FONLL-C	FONLL-C
Order	NLO	NNLO	NNLO
PDF set	NNPDF3.0_NLO	NNPDF3.0_NNLO	NNPDF3.0_NNLO
$\alpha_s(M_Z)$	0.118	0.118	0.118
Hadronisation corrections	Djangoh and Rapgap		
Available for			
(Normalised) Inclusive jet	✓	✓	✓
(Normalised) Dijet	✓	✓	✓
(Normalised) Trijet	✓		

Summary of predictions



# Regularised unfolding

## Regularised unfolding using TUnfold

- Calculate unfolded distribution  $x$  by minimising

$$\chi^2(x, \tau) = (y - Ax)^T V_y^{-1} (y - Ax) + \tau L^T L$$

- Linear analytic solution
- Linear error propagation
- Statistical correlations are considered in  $V_y$

## Simultaneous unfolding of Inclusive jet, Dijet, Trijet, NC DIS

- Statistical correlations are considered
- Matrix constituted from  $O(10^6)$  entries
  - Two generators used
  - Difference between the two -> model uncertainty
- Up to 6 variables considered for migrations
- 'detector-level fake jets' (or events) are constrained with NC DIS data

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$x$  Hadron level  
 $y$  Detector level  
 $V_y$  Covariance matrix  
 $A$  Migration matrix  
 $\tau L^2$  Regularisation term

## Migration Matrix

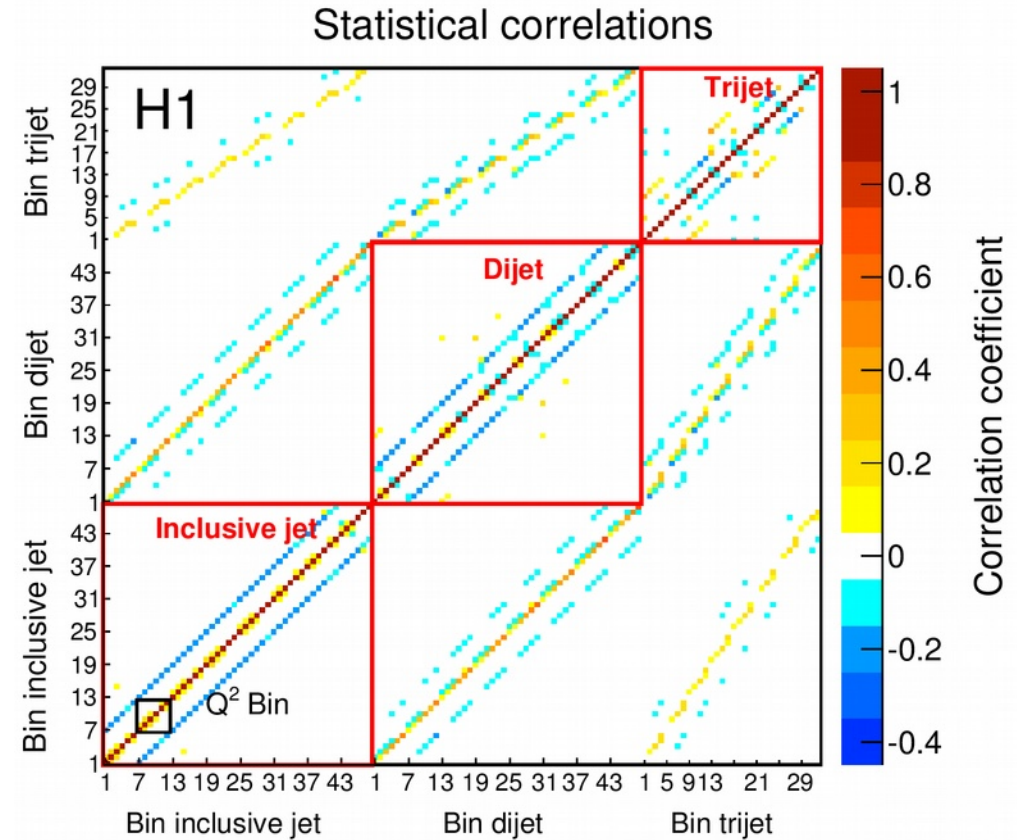
	$\varepsilon_1$	$\varepsilon_2$	$\varepsilon_3$
Detector level	Reconstructed Trijet events which are not generated as Trijet event		Trijet $Q^2, \langle p_T \rangle_3, y,$ Trijet-cuts
	Reconstructed Dijet events which are not generated as Dijet event	Dijet $Q^2, \langle p_T \rangle_2, y,$ Dijet-cuts	
	Reconstructed jets without match to generator level	Incl. Jet $p_T^{\text{jet}}, Q^2, y, \eta$	
	NC DIS $Q^2, y$		
	Hadron level		

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# Unfolding matrix and resulting correlations

**Migration Matrix**

		$\epsilon_j$			
		$\epsilon_{\beta_1-\beta_2-\beta_3}$	$\epsilon_1$	$\epsilon_2$	$\epsilon_3$
Detector level	Reconstructed Trijet events which are not generated as Trijet event				<b>Trijet</b> $Q^2, \langle p_T \rangle_3, y, \text{Trijet-cuts}$
	Reconstructed Dijet events which are not generated as Dijet event			<b>Dijet</b> $Q^2, \langle p_T \rangle_2, y, \text{Dijet-cuts}$	
	Reconstructed jets without match to generator level	<b>Incl. Jet</b> $p_T^{\text{jet}}, Q^2, y, \eta$			
	NC DIS $Q^2, y$				
		Hadron level			



# Dijet cross sections

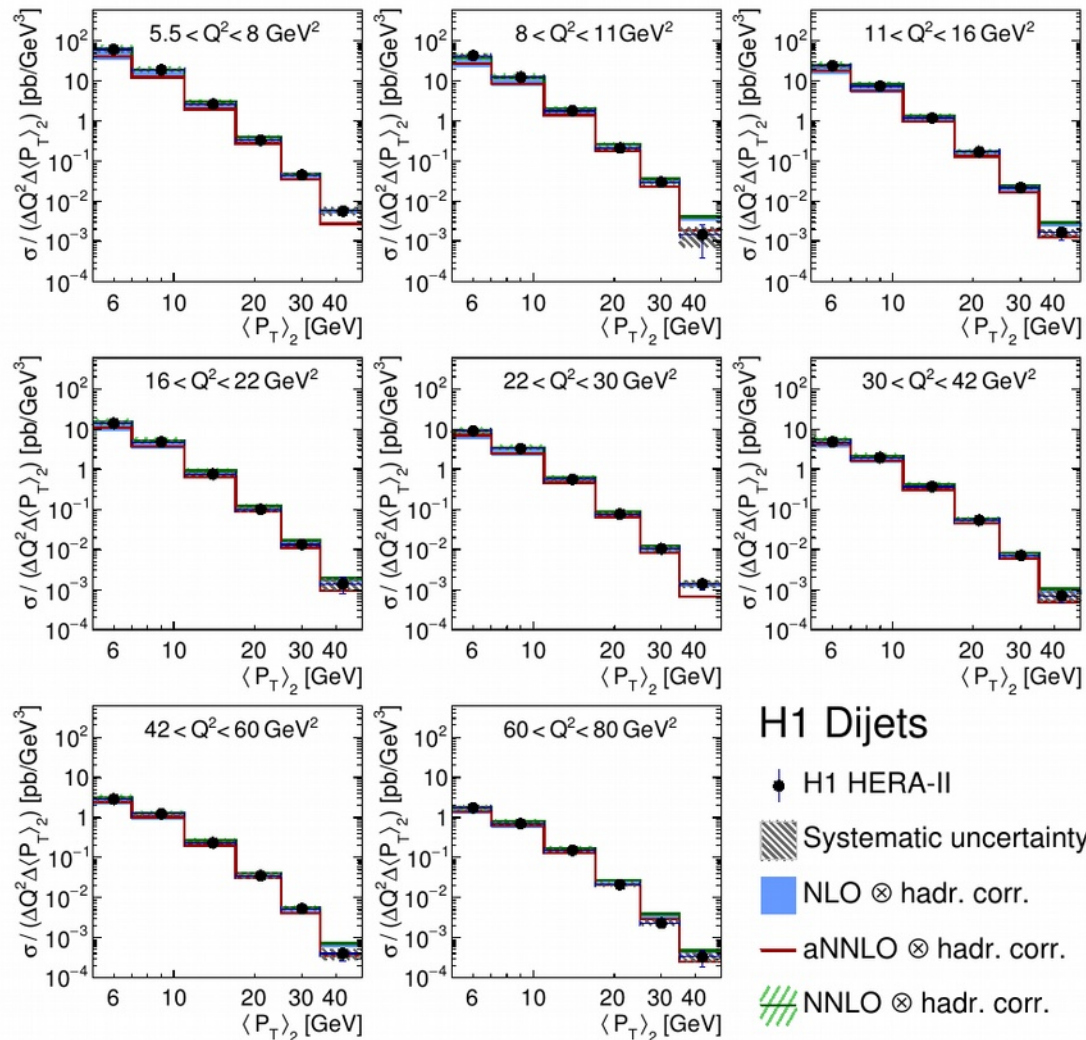
## Dijet cross sections

- as a function of  $Q^2$  and  $\langle p_T \rangle_2$
- $\langle P_T \rangle_2 = (P_{T\text{jet}1} + P_{T\text{jet}2})/2$   
with:  $P_{T\text{jet}} > 4$  GeV

## Comparison to Predictions

- NLO (nlojet++, NNPDF30\_nlo)
- approximate NNLO (JetVip, NNPDF30\_nnlo)
- NNLO (NNLOJET, NNPDF30\_nnlo)

**Predictions provide overall good description of data**

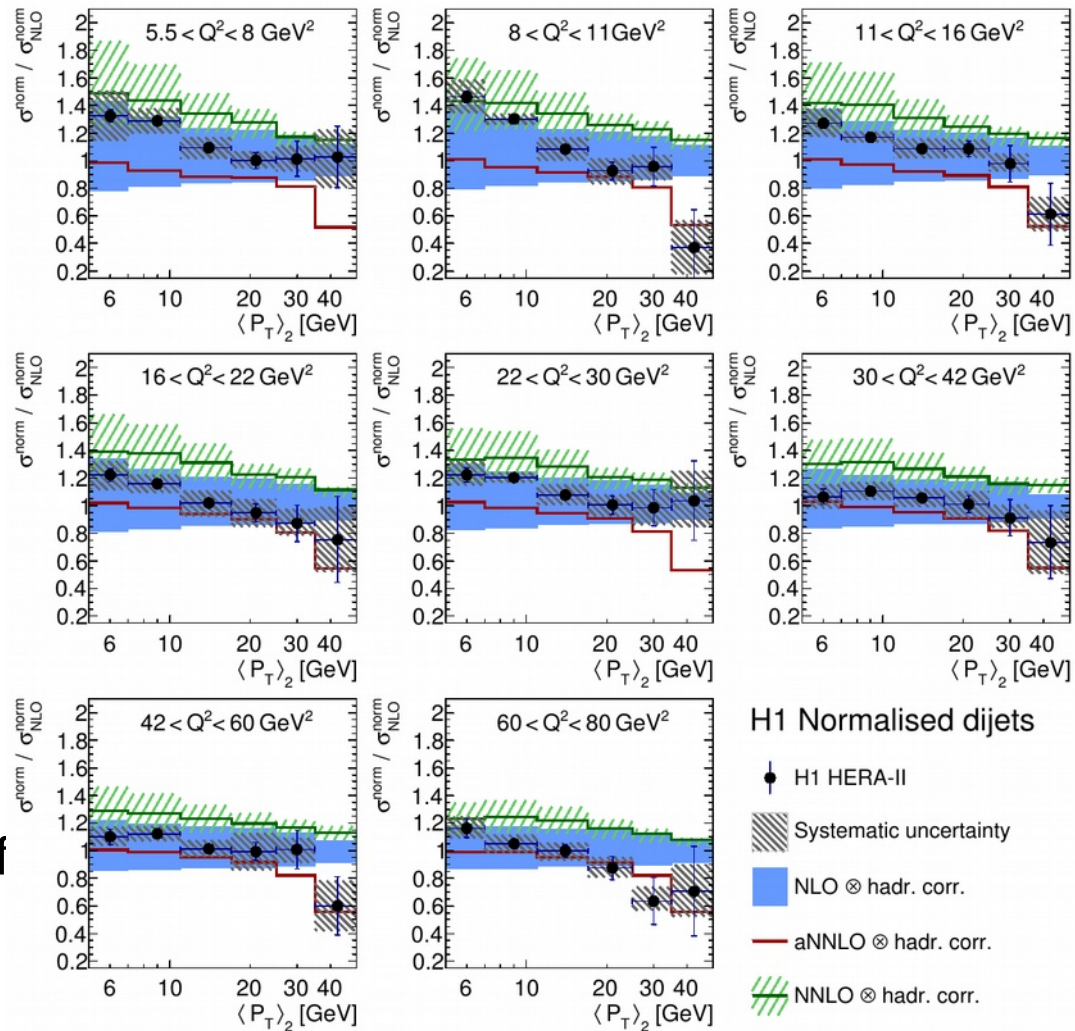


# Normalised dijet cross sections

- Normalisation w.r.t. NC DIS cross section in given  $Q^2$  range

$$\sigma_i^{\text{norm}} = \frac{\sigma_i}{\sigma_{i_q}^{\text{NC}}}$$

- (partial) cancellation of exp. uncertainties  
smaller benefit at lower  $Q^2$
- Overall good description by NLO, aNNLO and NNLO predictions
- NNLO slightly overshoots data  
-> Probably caused by normalisation of NC DIS predictions in NNLO



H1 Normalised dijets

- H1 HERA-II
- ▨ Systematic uncertainty
- NLO  $\otimes$  hadr. corr.
- aNNLO  $\otimes$  hadr. corr.
- ▨ NNLO  $\otimes$  hadr. corr.

# Normalised jet cross sections

## Normalised jet cross sections

- Normalised to:  
'inclusive neutral-current DIS cross section' in respective  $Q^2$  bin

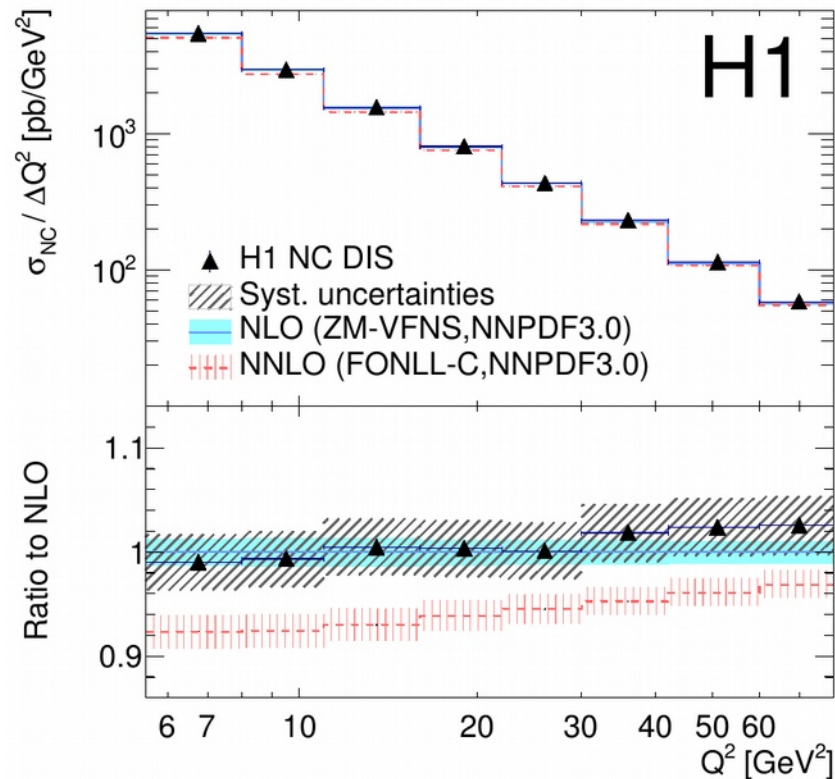
## Advantages

- Reduced experimental uncertainties
- Cancellation of normalisation uncertainty

## NC DIS predictions

- NLO (ZM-VFNS) and NNLO (FONLL-C) predictions provide a good description of the data
- PDFs are fitted to NC DIS cross sections

## Inclusive neutral-current DIS cross sections



# Reminder: inclusive jets @ high- $Q^2$

## *Eur. Phys. J. C75 (2015) 2*

- H1 HERA-II jet cross sections at high- $Q^2$
- Inclusive jet, dijet and trijet cross sections
- $150 < Q^2 < 15\,000 \text{ GeV}^2$

## *Inclusive jets in range*

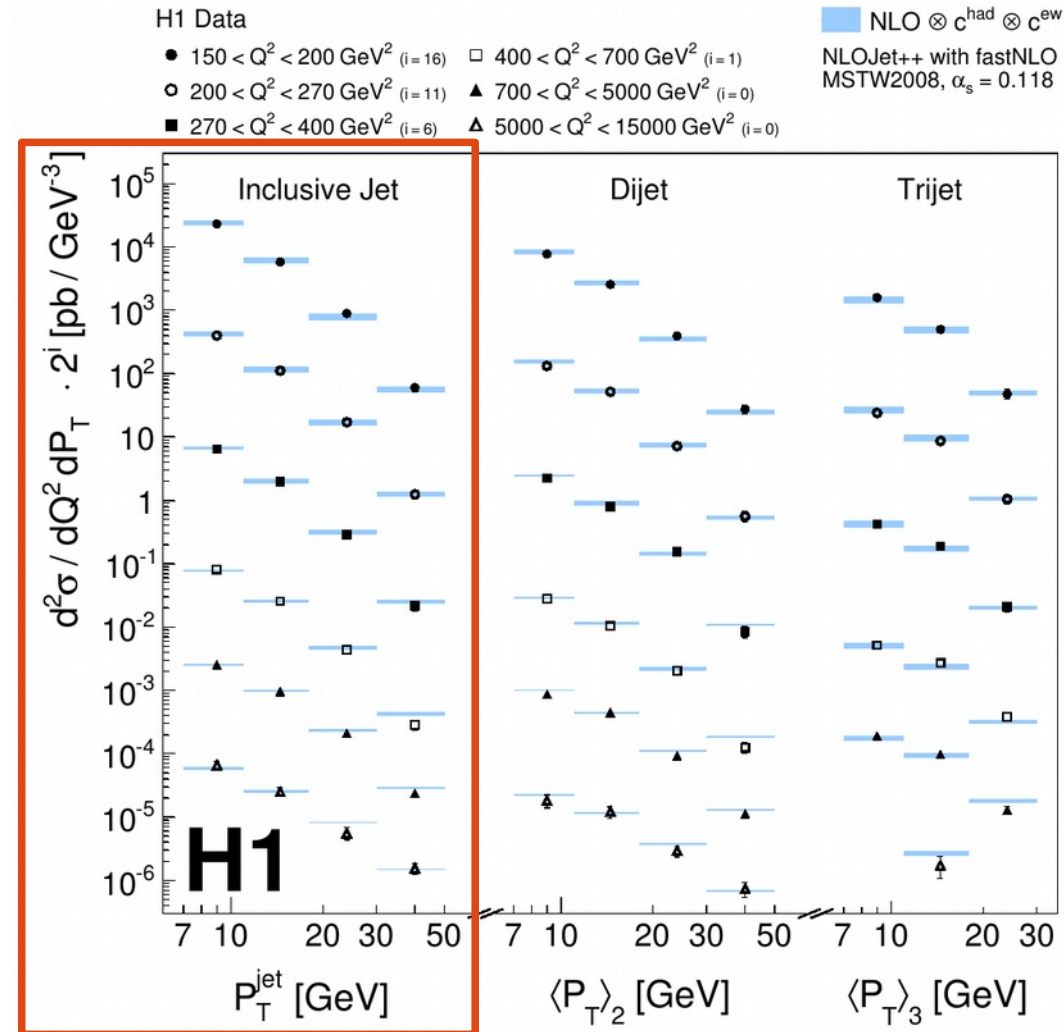
- $7 < p_T < 50 \text{ GeV}$

## *Recent studies showed*

- Inclusive jets are well measurable down to  $p_T \sim 4 \text{ GeV}$
- The original 'high- $Q^2$ '-analysis contained a cross section bin for inclusive jets for  $5 < p_T < 7 \text{ GeV}$

## *Extension to low- $p_T$ : $5 < p_T < 7 \text{ GeV}$*

- for each  $Q^2$  range
- Absolute and normalised cross sections



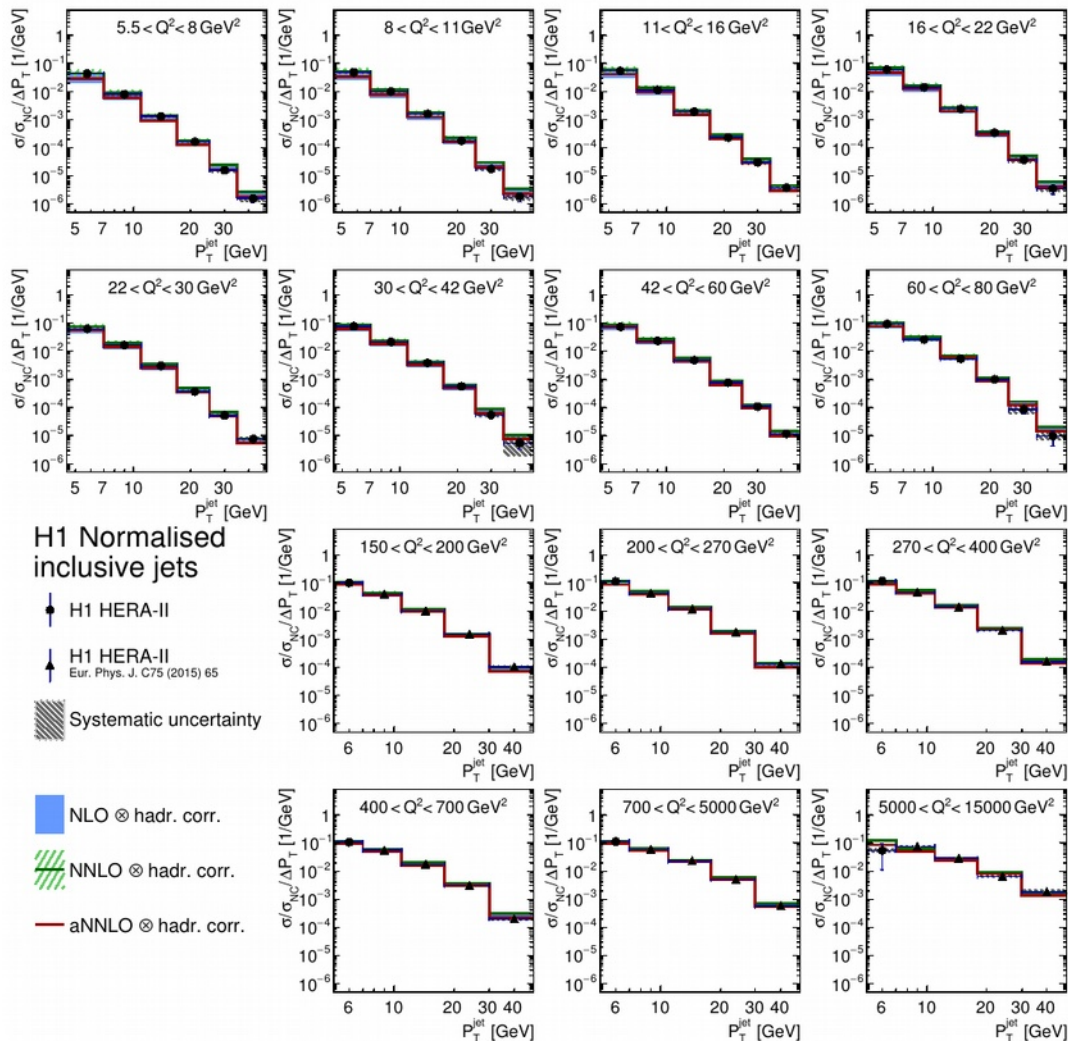
# Normalised inclusive jet cross sections

## Normalised inclusive jets

- Normalisation w.r.t. inclusive NC DIS cross section in respective  $Q^2$  bin
- Significant reduction of uncertainties at higher values of  $Q^2$

## Normalised jet cross sections

- Increase as a function of  $Q^2$  for a given  $P_T$  interval
- $Q^2$  and  $p_T$  are both important scales for inclusive jet production



# Determination of the strong coupling $\alpha_s(M_Z)$

## $\alpha_s(M_Z)$ from H1 HERA-II jets

- Normalised jet cross sections  
correlations of uncertainties considered

## Low- and high- $Q^2$ data

- Low- $Q^2$  jets [arxiv:1611.03421]
- high- $Q^2$  jets (Eur.Phys.J.C75 (2015) 2)

## $\alpha_s(M_Z)$ in NLO

- $\chi^2$  fit to all data points together:  $\alpha_s(M_Z)$

$$\alpha_s(M_Z) = 0.1173 (4)_{\text{exp}} (3)_{\text{PDF}} (7)_{\text{PDF}(\alpha_s)} (11)_{\text{PDFset}} (6)_{\text{had}} (+51)_{\text{scale}} (-43)$$

- Very high experimental precision
- Future improvements on dominating theory uncertainties in NNLO

World average (PDG2016)

$$\alpha_s(M_Z) = 0.1181 \pm 0.0011$$

