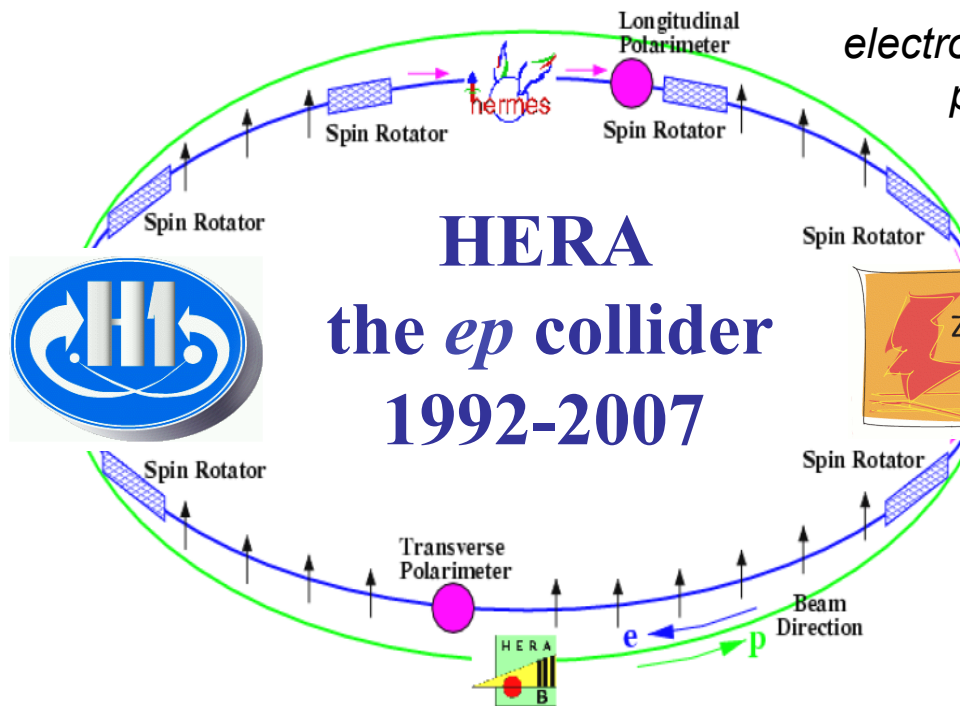


PDFs and hard QCD at HERA

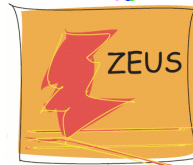
Vladimir Chekelian (MPI for Physics, Munich)

on behalf of the H1 and ZEUS Collaborations



HERA
the *ep* collider
1992-2007

electrons & positrons of $E_e=27.5$ GeV collided with protons of $E_p = 920, 820, 575$ and 460 GeV. Two multi-purpose collider experiments H1 & ZEUS collected in total 1 fb^{-1} .



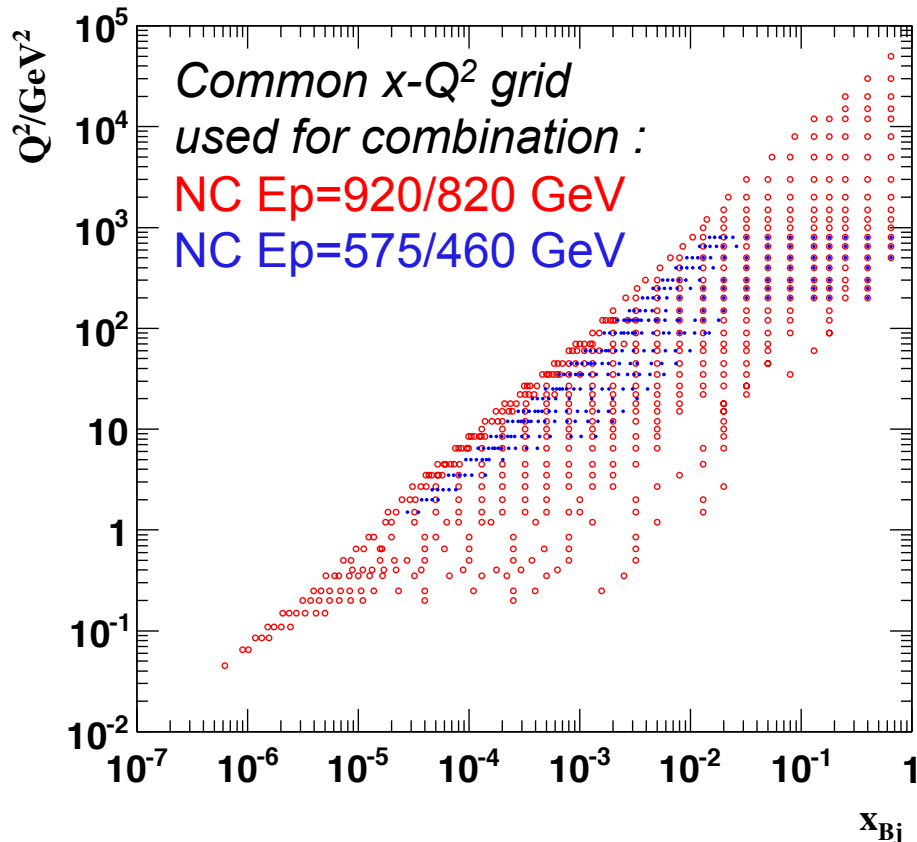
- **Combination of all inclusive NC&CC data from H1&ZEUS at HERA**

- $F_2, xF_3^{\gamma Z}, (F_2^{\gamma Z}, F_L, \sigma_{CC}^{tot}, \dots)$
- **HERAPDF 2.0 PDF set and its variants**
- **charm production and combination of D^***
- **jet production and α_s ; multi-jets at low Q^2**
- **prompt photon & jet production in DIS**

NC and CC inclusive data sets at HERA

41 NC and CC data sets from H1 and ZEUS corresponding to 1 fb^{-1}
 $0.045 \leq Q^2 \leq 50000 \text{ GeV}^2$, $6 \cdot 10^{-7} \leq x \leq 0.65$

H1 and ZEUS



21 data sets from HERA I

NC & CC at $E_p=920$ and 820 GeV

and 20 data sets from HERA II (2003-2007)

12 NC & CC sets at $E_p=920 \text{ GeV}$

4 NC sets at $E_p=575 \text{ GeV}$

4 NC sets at $E_p=460 \text{ GeV}$

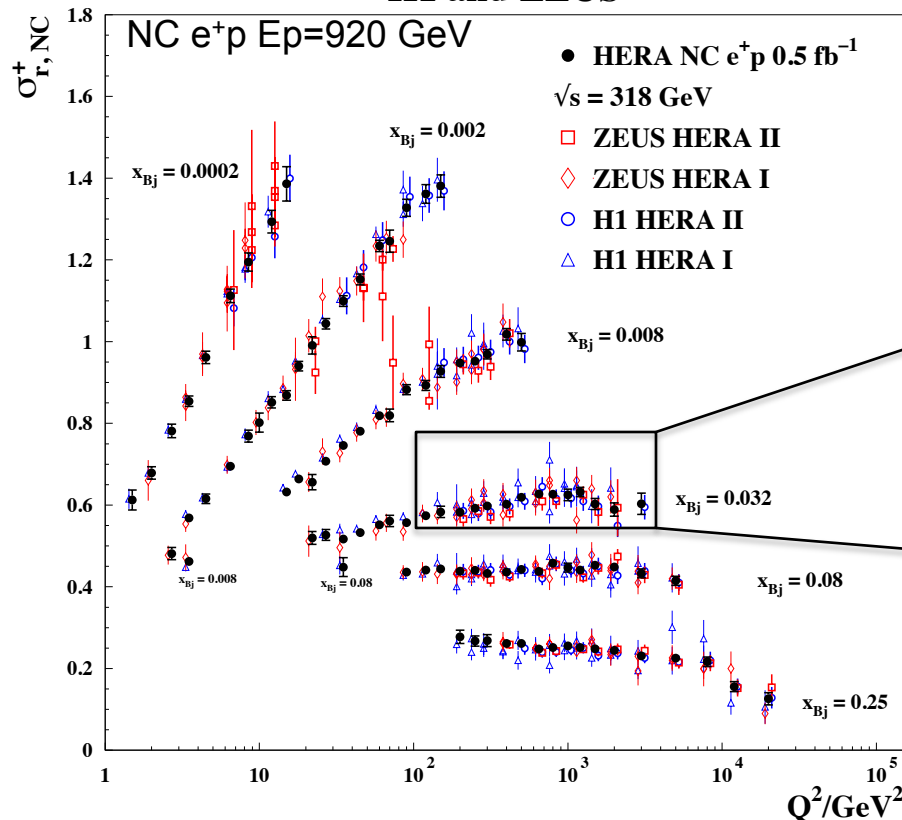
These data are collected over 15 years with changing beams and detectors conditions and different focus. It is important to handle them properly, e.g. in view of possible correlations

→ combine them into one coherent data set as it was done for HERA I before (JHEP 1001:109, 2010 and HERAPDF 1.0)

Averaging of all NC and CC data at HERA

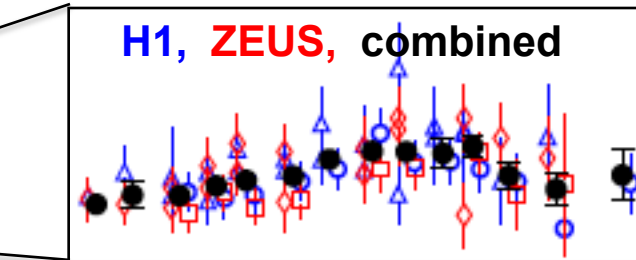
2927 cross sections are combined to 1307 points with 169 correlated systematic errors
and $\chi^2/d.o.f. = 1685/1620$

H1 and ZEUS



Coherent set of unpolarised $e^\pm p$ NC&CC
at four $\sqrt{s} = 318, 300, 251, 225$ GeV:
→ www.desy.de/h1zeus/herapdf20/
→ precise, complete and easy in use
→ with reduced stat. and syst. errors

H1, ZEUS, combined

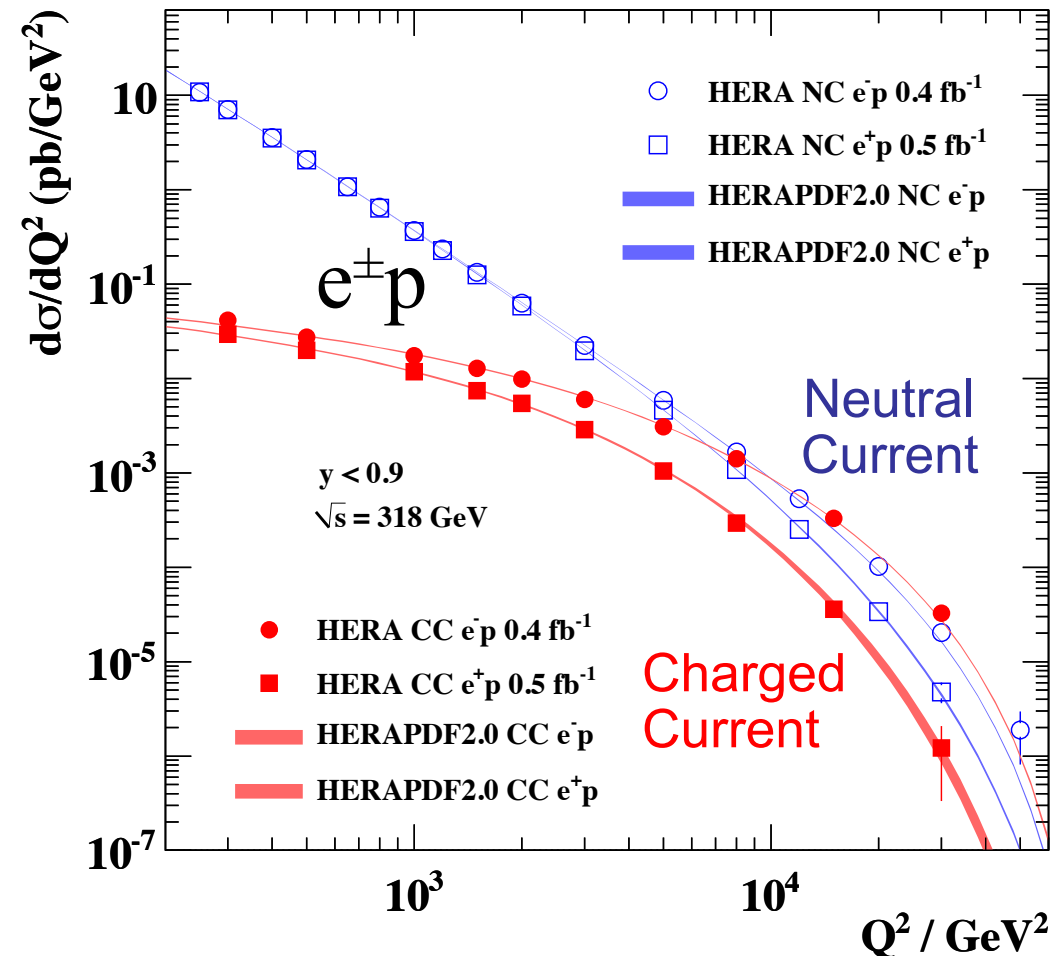


$e^\pm p$ NC&CC ($E_p=920$ GeV)
 $e^+ p$ NC ($E_p = 820, 575, 460$ GeV)
 $0.045 \leq Q^2 \leq 50000$ GeV², $6 \cdot 10^{-7} \leq x_{Bj} \leq 0.65$
total unc. < 1.5% for Q^2 up to 500 GeV²

→ up to 6 measurements are combined into one averaged point
→ correlated shifts are propagated to all points (even measured by single experim.)

Combined NC and CC $e^\pm p$ data

H1 and ZEUS



- single differential cross sections are obtained by integration over x of the combined NC and CC $e^\pm p$ data at $\sqrt{s}=318 \text{ GeV}$ and $y < 0.9$

- e^+p NC and e^-p NC are the same in the γ -exchange domain at low Q^2 and start to differ at high Q^2 due to γZ interference.

- CC is two orders of magnitude smaller than NC at $Q^2=200 \text{ GeV}^2$ and about the same at Q^2 around M_Z^2, M_W^2 , demonstrating **electroweak unification**.

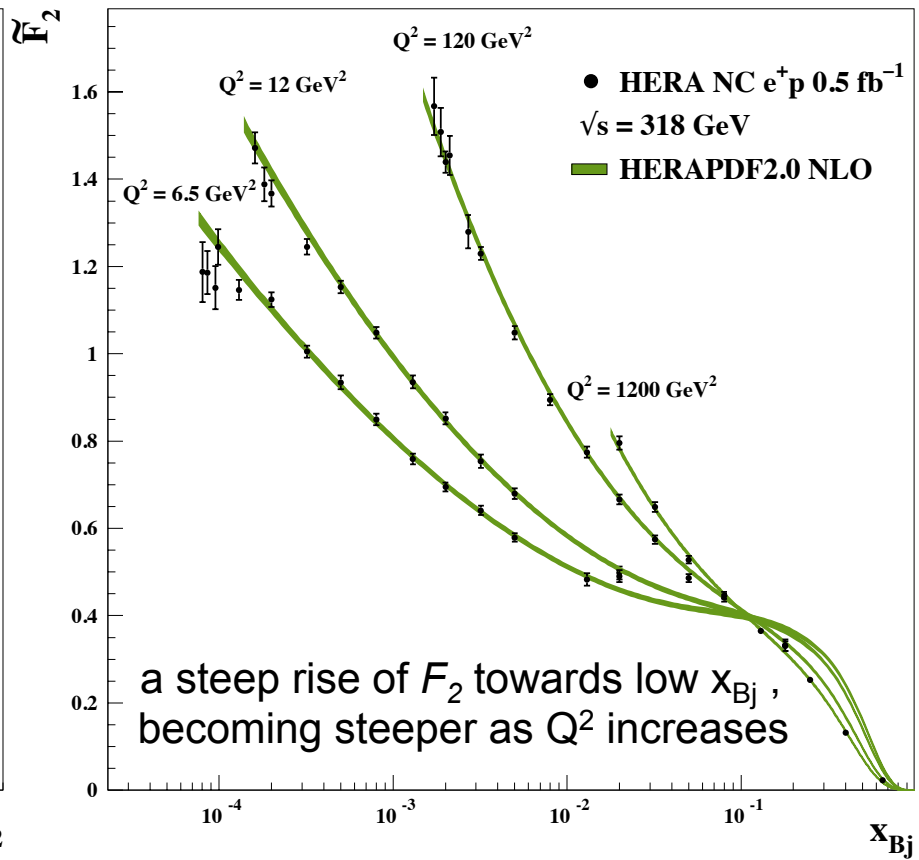
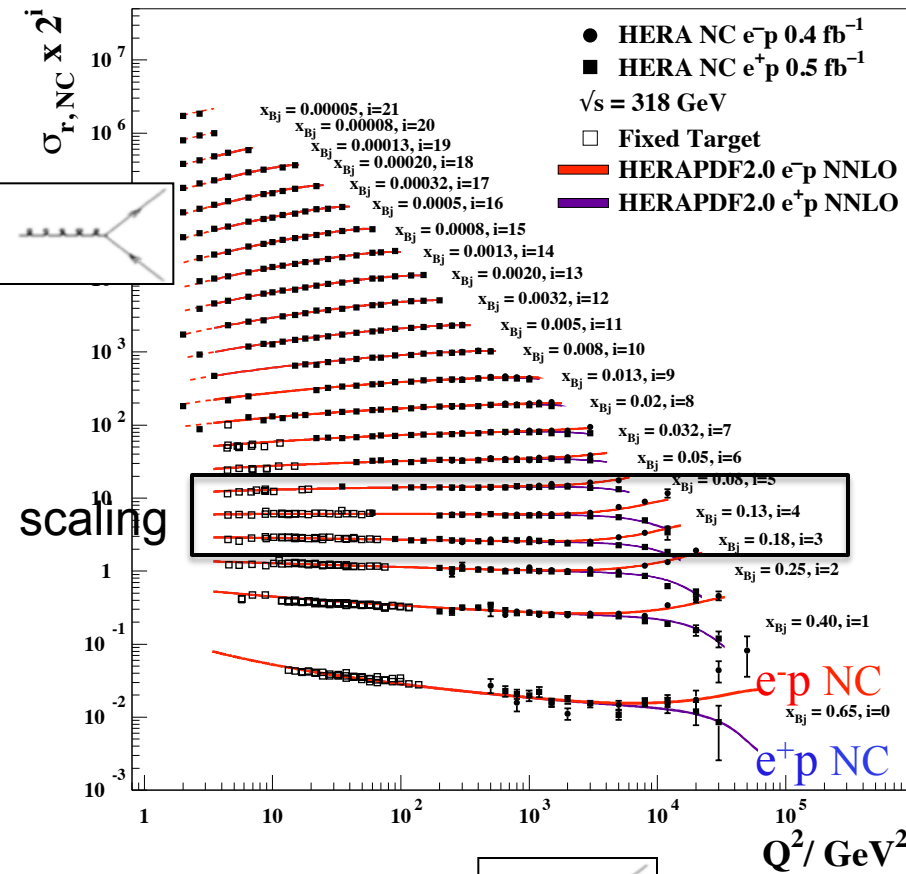
- remaining differences in CC are related to u, d content of the proton and to helicity factors.

Proton structure function F_2

$$\sigma_{r,NC}^{\pm} \equiv \frac{d^2\sigma_{NC}^{e^{\pm}p}}{dx dQ^2} \frac{xQ^4}{2\pi\alpha^2} \frac{1}{Y_{\pm}} \equiv \tilde{F}_2 - \frac{y^2}{Y_{+}} \tilde{F}_L \mp \frac{Y_{-}}{Y_{+}} x \tilde{F}_3 \quad Y_{\pm} = 1 \pm (1-y)^2$$

H1 and ZEUS

H1 and ZEUS

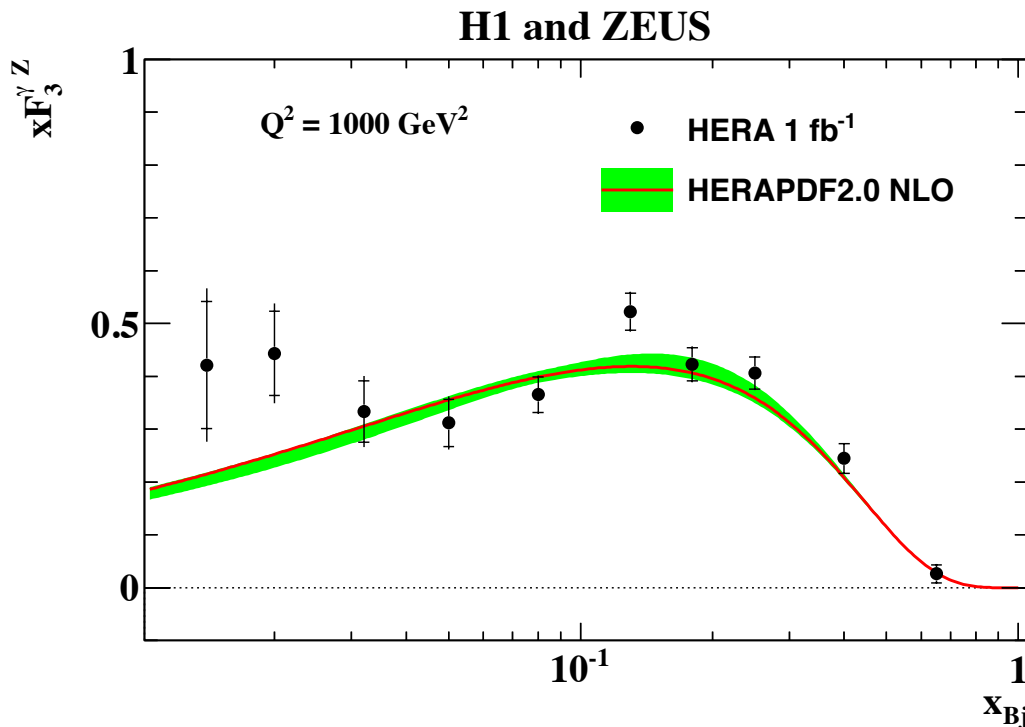


$e^\pm p$ NC: lepton charge dependence and xF_3

$$xF_3^{\tilde{}} = \frac{Y_+}{2Y_-} (\sigma_{r,\text{NC}}^- - \sigma_{r,\text{NC}}^+) \quad \text{charge asymmetry of } e^\pm p \text{ NC cross sections is mostly due to } \gamma Z \text{ interference}$$

$$xF_3^{\gamma Z} = -xF_3^{\tilde{}} (Q^2 + M_Z^2)/(a_e k Q^2)$$

$$\kappa^{-1} = 4 \frac{M_W^2}{M_Z^2} \left(1 - \frac{M_W^2}{M_Z^2} \right)$$



transform the $xF_3^{\gamma Z}(x, Q^2)$ measurements to $Q^2 = 1000 \text{ GeV}^2$ and average them to get $xF_3^{\gamma Z}(x)$ at $Q^2 = 1000 \text{ GeV}^2$

→ related to valence quark:
 $F_3^{\gamma Z} \approx (2u_v + d_v)/3$

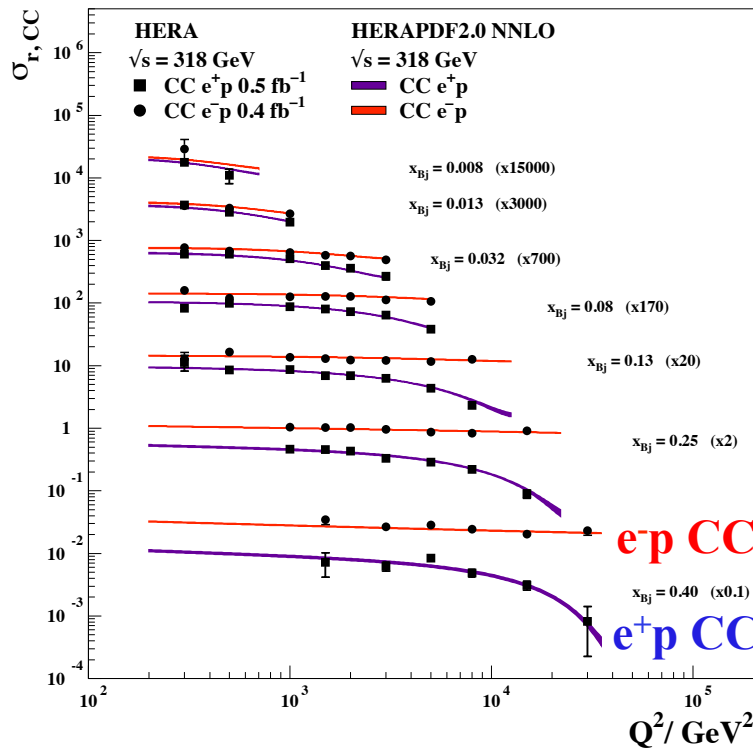
→ integration over the measured range $0.016 < x_{Bj} < 0.725$ gives
 $1.165 + 0.042 - 0.053$ for data and
 $1.314 \pm 0.057(\text{stat}) \pm 0.057(\text{syst})$ using
 HERAPDF2.0

$e^\pm p$ CC probe u/d composition of proton

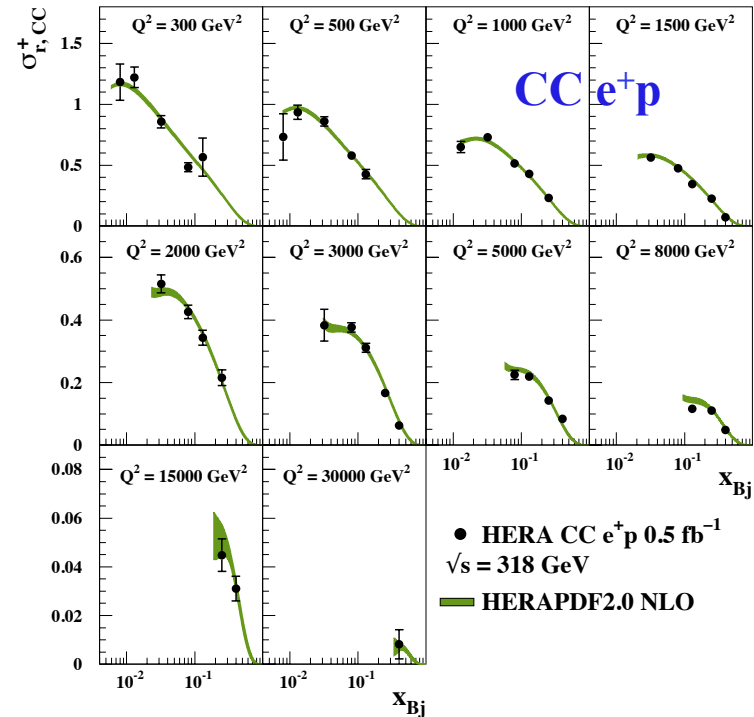
$$\sigma_{r,CC}^\pm \equiv \frac{2\pi x}{G_F^2} \left[\frac{M_W^2 + Q^2}{M_W^2} \right]^2 \frac{d^2 \sigma_{CC}^{e^\pm p}}{dx dQ^2}$$

$$\begin{aligned} \sigma_{r,CC}^+ &\sim (x\bar{u} + x\bar{c}) + (1-y)^2(xd + xs) \\ \sigma_{r,CC}^- &\sim (xu + xc) + (1-y)^2(x\bar{d} + x\bar{s}) \end{aligned}$$

H1 and ZEUS



H1 and ZEUS



e^+p CC at high x is related to d -quark (Q^2 dependence is due to helicity factor $(1-y)^2$)
 e^-p CC is dominated by u -quark and depends weakly on Q^2 at given x

HERAPDF2.0 QCD Fit

The combined $e^\pm p$ NC/CC HERA data set is the only input

- no nuclear, heavy target or HT corrections; consistency of data, $\Delta\chi^2 = 1$ criterion
- parametrisation of PDFs at starting scale $Q_0^2=1.9 \text{ GeV}^2$ with 14 free parameters

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g},$$

$$xu_v(x) = A_{uv} x^{B_{uv}} (1-x)^{C_{uv}} (1 + E_{uv} x^2), \quad x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x),$$

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}}, \quad x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$$

- QCD evolution of PDFs using DGLAP equations at NLO and NNLO
- Thorne-Roberts general mass variable-flavor-number scheme RTOPT (as used in MMHT)
- default $Q_{\min}^2=3.5 \text{ GeV}^2$, $f_s=0.40$ ($x\bar{s} = f_s x\bar{D}$ at Q_0^2)
- M_c and M_b values are optimized using HERA charm and beauty production data
- $\alpha_s(M_Z^2)=0.118$ is consistent with HERA jet data

→ available at www.desy.de/h1zeus/herapdf20/ and on LHAPDF:

HERAPDF2.0 at NLO and NNLO

also with a scan of $\alpha_s(M_Z^2)$ from 0.110 to 0.130 in steps of 0.001

additional PDF sets :

HERAPDF2.0HiQ2 at NLO and NNLO - $Q_{\min}^2=10 \text{ GeV}^2$

HERAPDF2.0AG at LO, NLO and NNLO - alternative gluon parameterisation (strictly positive)

HERAPDF2.0FF3A and FF3B - fixed flavor number schemes at NLO

Uncertainties of HERAPDF2.0

Three types of PDF uncertainties are considered:

Experimental uncertainty band

- Hessian method with $\Delta\chi^2 = 1$ verified by MC method - replicas of data

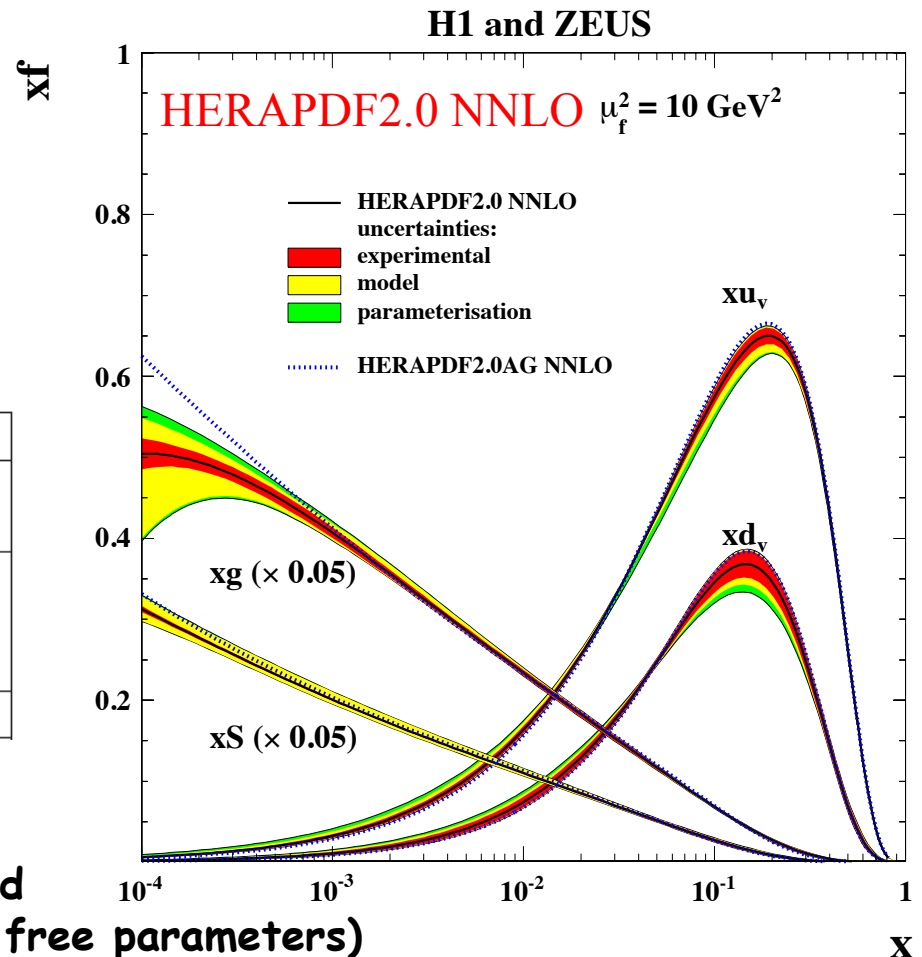
Model uncertainty band

- variation of model assumptions

Variation	Standard Value	Lower Limit	Upper Limit
Q_{\min}^2 [GeV ²]	3.5	2.5	5.0
Q_{\min}^2 [GeV ²] HiQ2	10.0	7.5	12.5
M_c (NLO) [GeV]	1.47	1.41	1.53
M_c (NNLO) [GeV]	1.43	1.37	1.49
M_b [GeV]	4.5	4.25	4.75
f_s	0.4	0.3	0.5

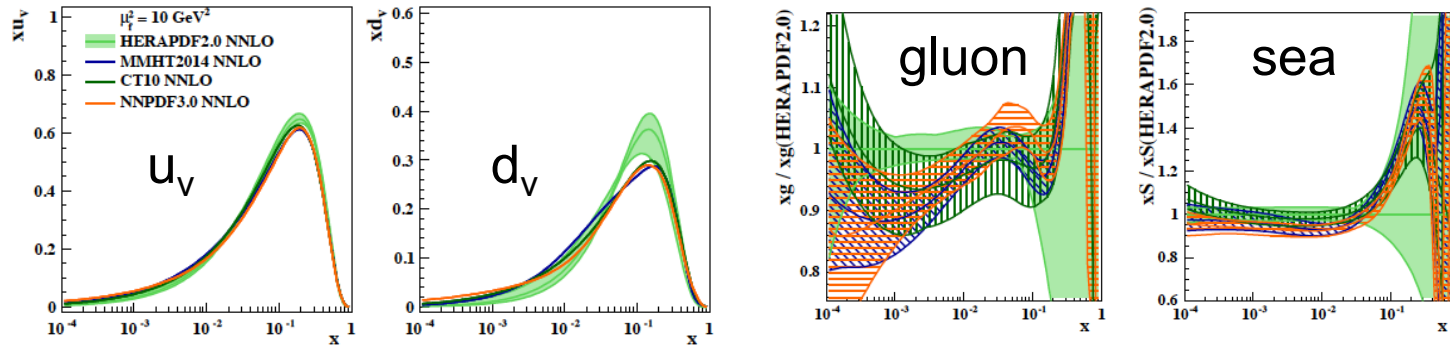
Parameterisation uncertainty band

- variation of the starting scale Q_0^2 and
 - form of parameterisation (number of free parameters)
- valid in the x -range covered by the QCD fit to HERA data

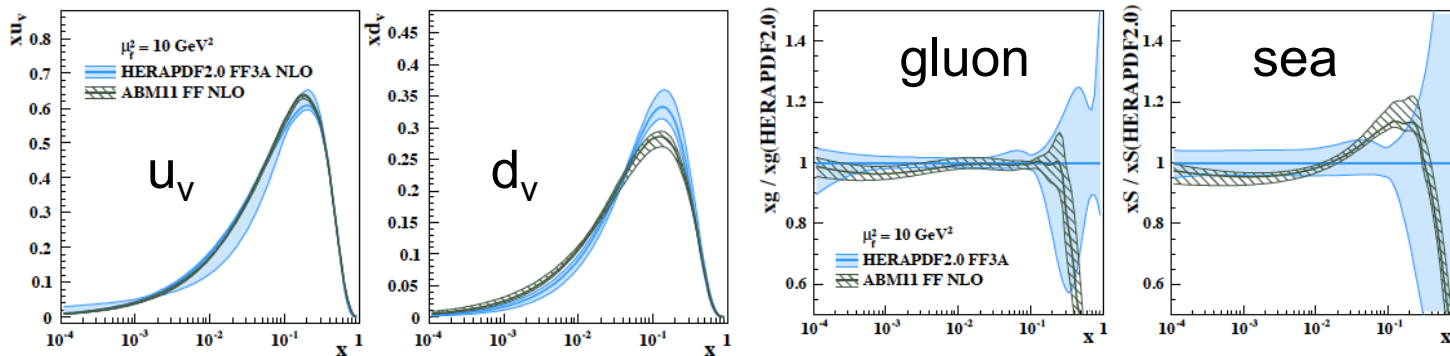


Comparison with modern PDFs from global fits

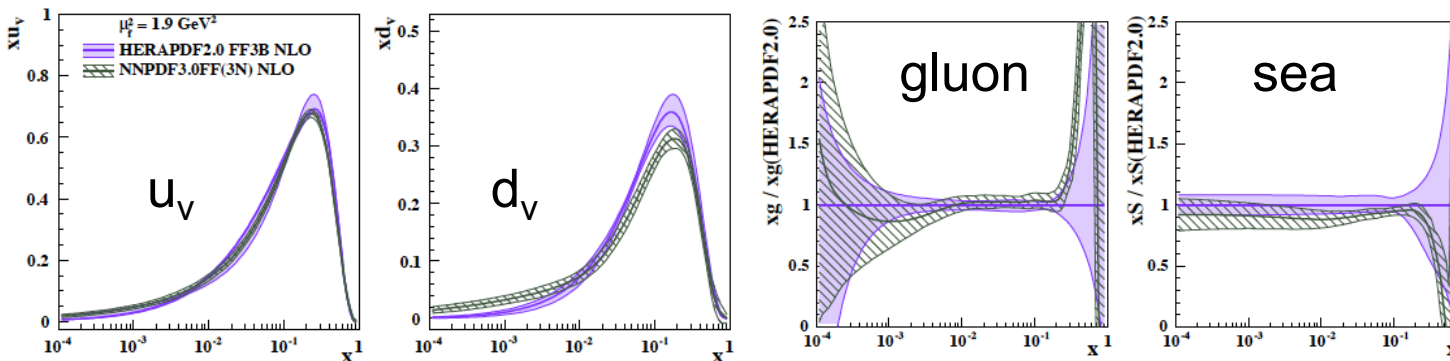
vs. PDFs using variable-flavor-number scheme: MMHT2014, CT10, NNPDF3.0



vs. PDFs using fixed-flavor-number scheme: ABM11 FF, NNPDF3.0FF(3N)



→ differences in valence quarks at high x: new HERA data



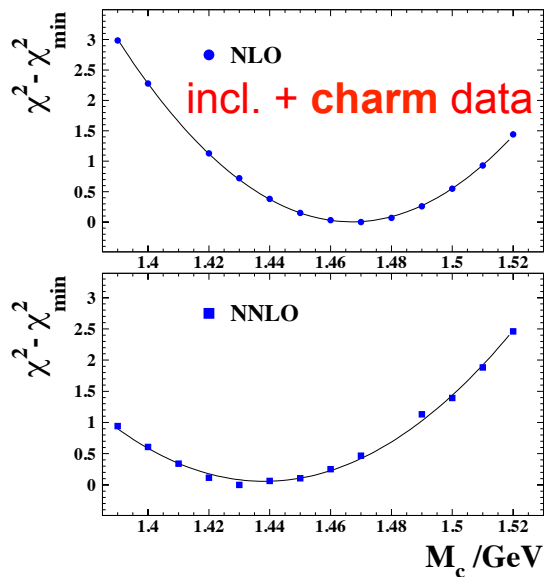
→ sea and gluon are consistent

Charm production in DIS

Charm mass parameter in HERAPDF2.0

M_c and M_b , charm and bottom mass parameters, are determined in χ^2 scans of the HERA charm and bottom data together with combined inclusive data

H1 and ZEUS



→ reduction of the M_c and M_b uncertainties in HERAPDF fits

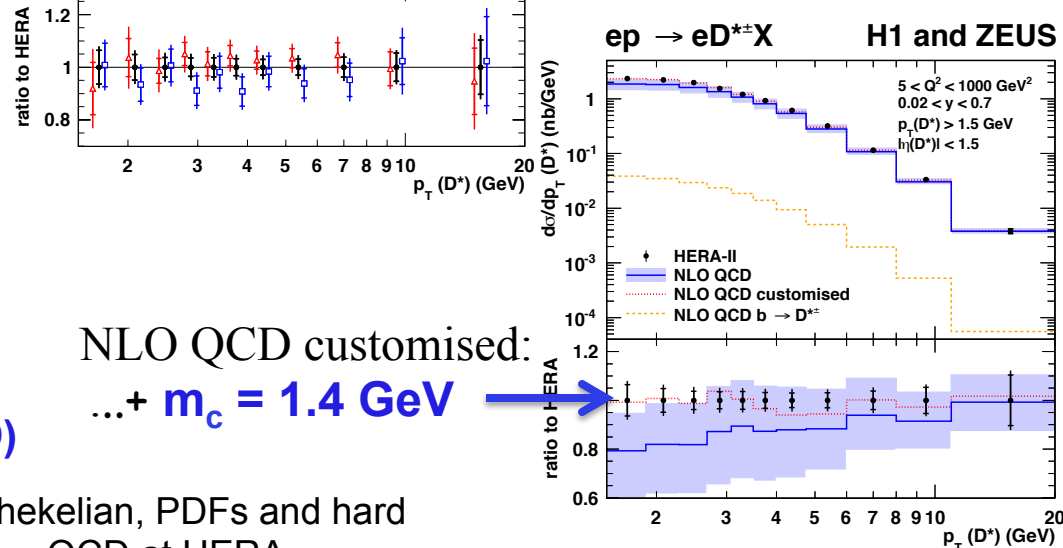
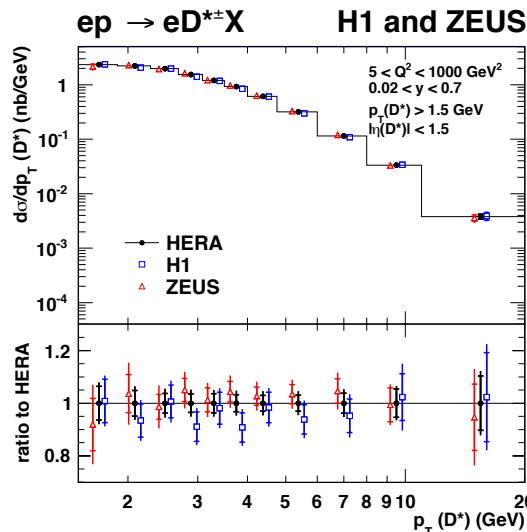
$M_c = 1.47$ (1.43) GeV at NLO (NNLO)

Combination of all D^* at HERA

in the visible phase space, including latest D^* cross section measurements by ZEUS. No need for extrapolation to the full phase space as in the former combination of available

charm data obtained using different techniques: D^* and D^\pm reconstruction, vertex fitting, leptons in the final state.

→ single diff.: P_T, η, z, Q^2, y and double diff. Q^2-y

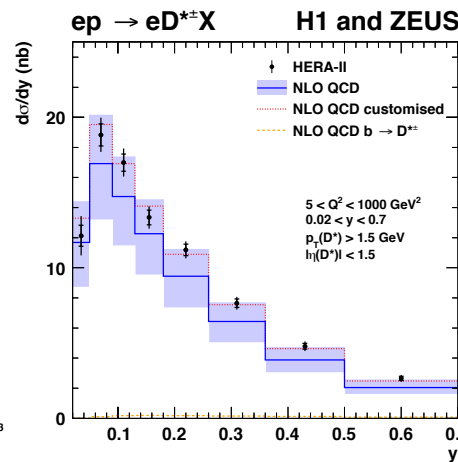
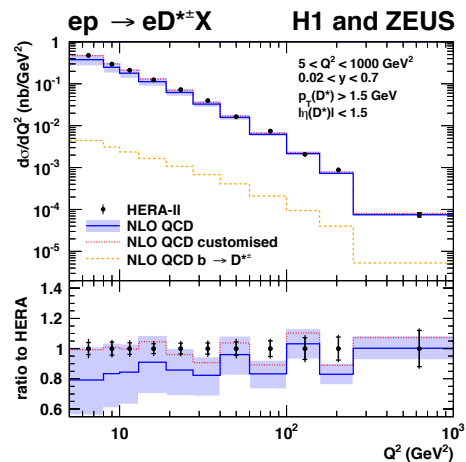
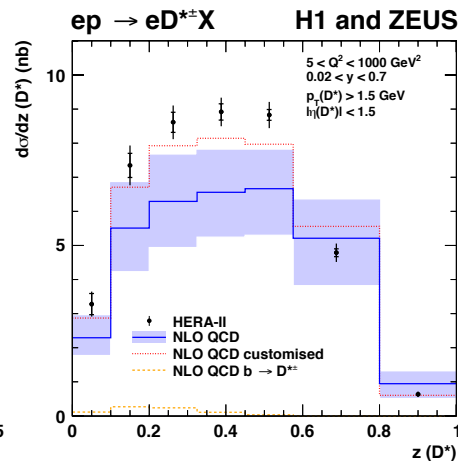
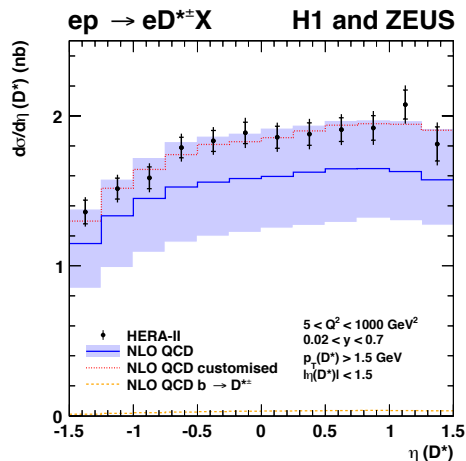


NLO QCD customised:
 ...+ $m_c = 1.4 \text{ GeV}$ →

Combined H1 & ZEUS visible D^* cross sections

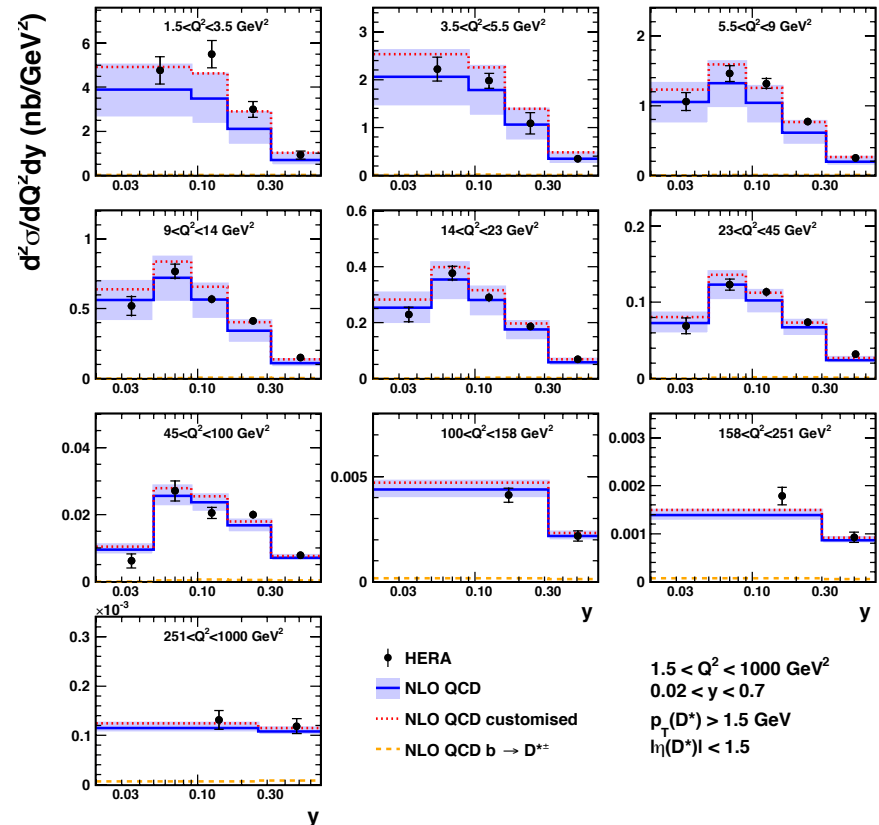
single differential: $d\sigma(D^*)/dP_T$,
 $d\sigma/d\eta$, $d\sigma/dz$, $d\sigma/dQ^2$, $d\sigma/dy$

double differential: $d^2\sigma/dQ^2dy$



ep → eD*[±]X

H1 and ZEUS



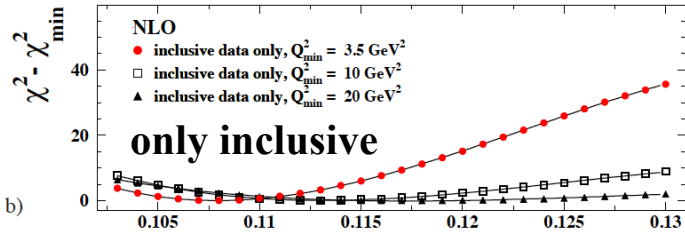
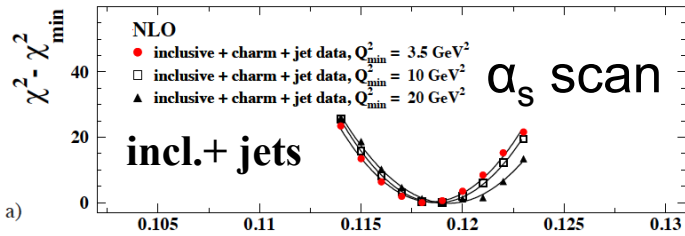
Jet production and the strong coupling constant

HERAPDF2.0 Jets NLO

include also HERA combined charm and selected jet production data :

→ α_s from a simultaneous fit with PDFs:

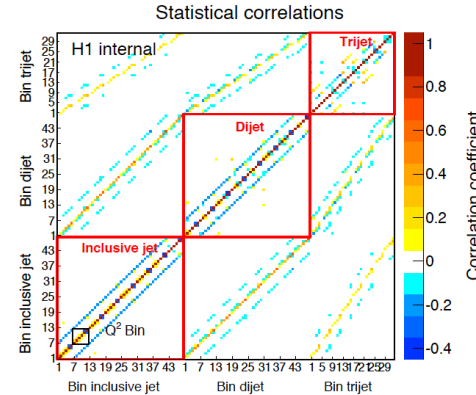
$$\alpha_s(M_Z^2) = 0.1183 \pm 0.0009(\text{exp}) \pm 0.0005(\text{model}) \pm 0.0012(\text{hadronisation})^{+37}_{-30}(\text{scale})$$



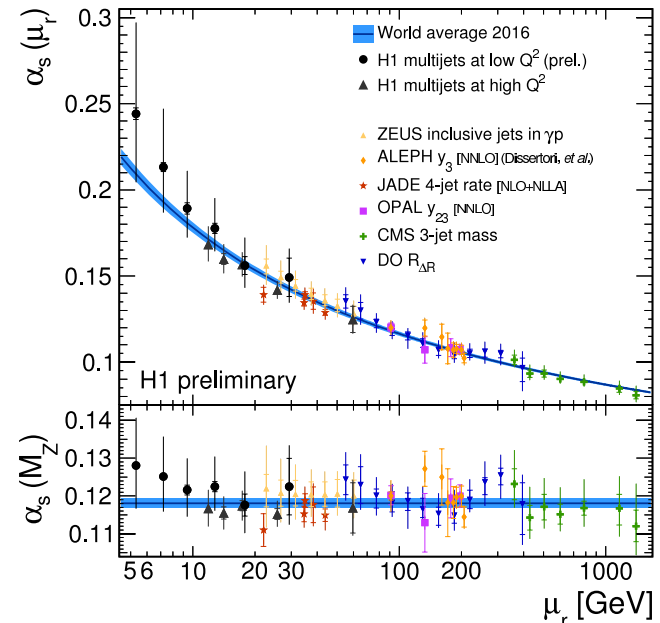
PDFs and the error bands are very close to HERAPDF2.0 obtained using inclusive data and M_c and M_b already optimized using charm and bottom HERA data and $\alpha_s=0.118$, consistent with the HERA multi-jet data. (slight increase of err. band is due to hadronisation).



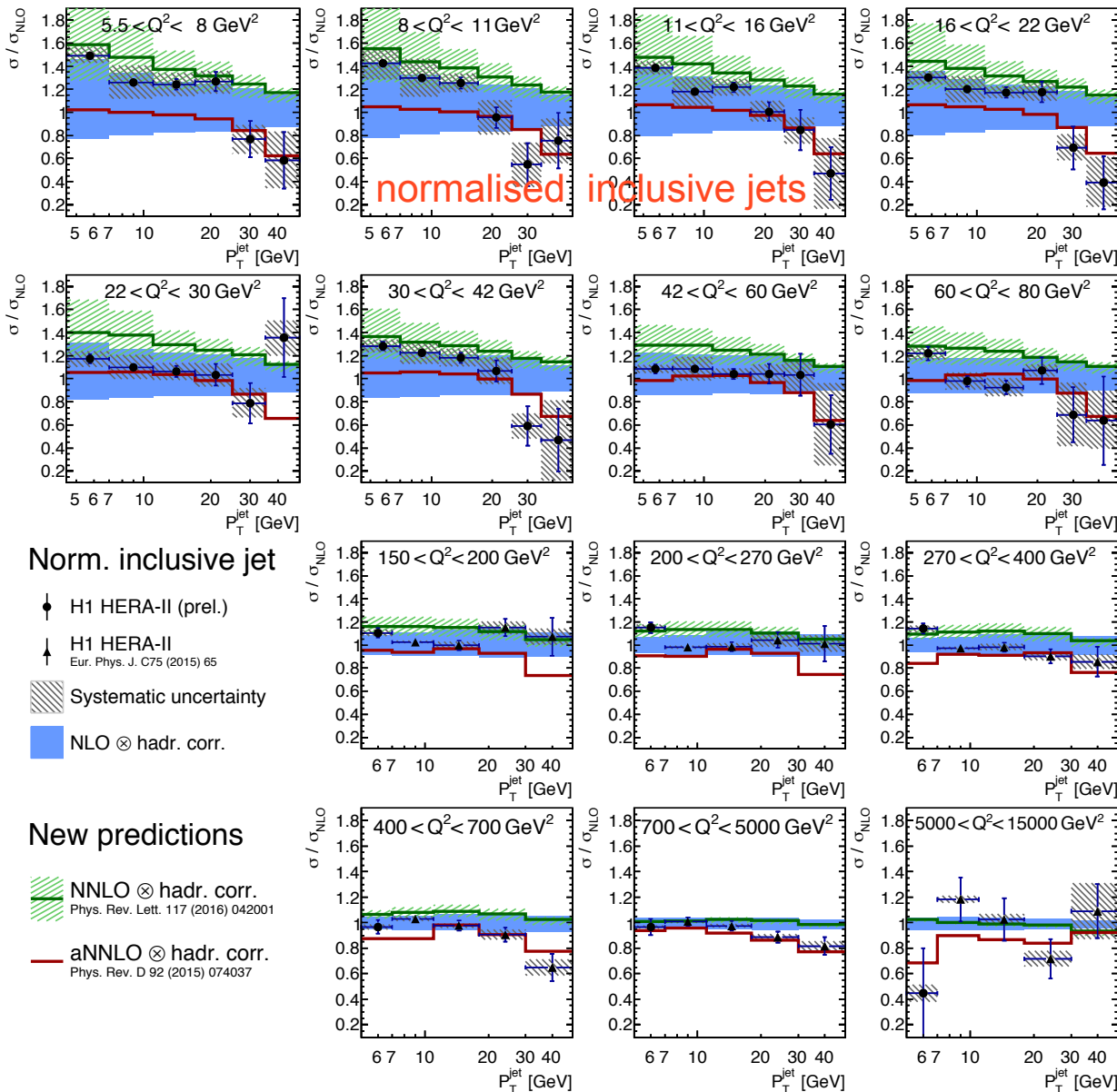
Multijet Production in ep DIS at low Q^2 by H1



Regularised unfolding of inclusive jets, dijets and trijets is used by H1 to obtain low Q^2 cross sections as it was done at high Q^2 in Eur.Phys.J.C75(2015)65



Multijet cross sections in DIS compared to NNLO



Inclusive jet, dijet and trijet cross sections, absolute and normalised to NC (with partial cancellation of systematics) are measured in Q^2 and P_T^{jet} bins
 $5.5 < Q^2 < 80 \text{ GeV}^2$ and
 $4.5 < P_T^{\text{jet}} < 50 \text{ GeV}$

For the first time normalised jet cross sections are compared to predictions at NNLO :

- full NNLO

Phys.Rev.Lett.117(2016)042001

- approximate NNLO

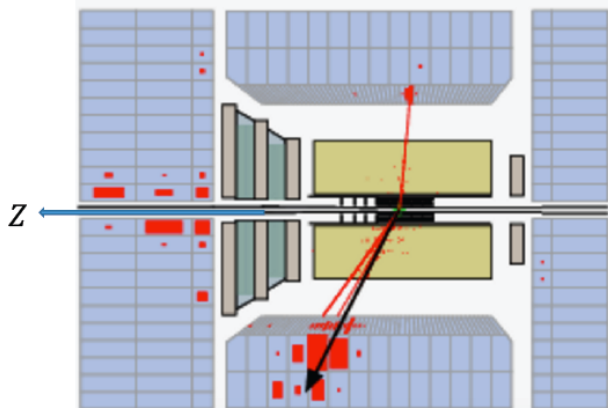
Phys.Rev. **D92** (2015) 074037

→ estimated experimental precision of $\alpha_s(M_Z)$ in fit to the H1 normalised jet cross sections at low and high Q^2 is 0.4%

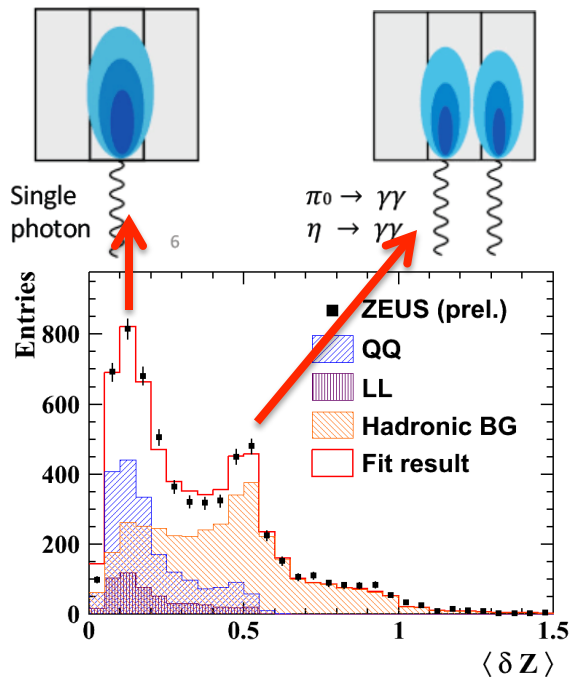
Prompt photon accompanied by jets in ep DIS

ZEUS-prel-16-001

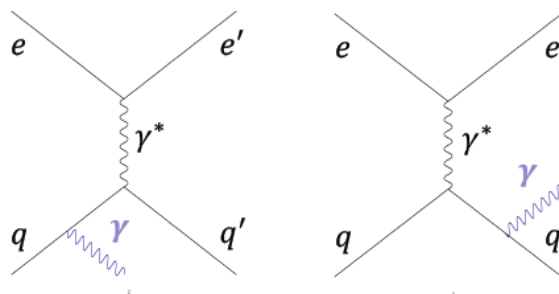
Prompt photons are produced
before quarks and gluons form hadrons



→ fine segmentation of BCAL in Z direction



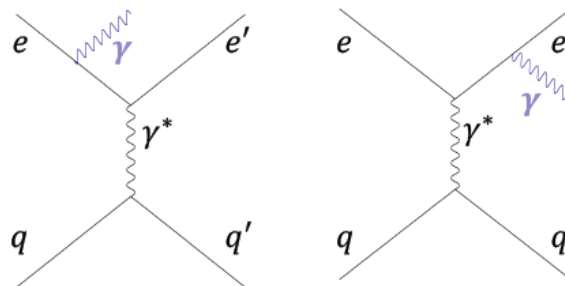
QQ - photons



γ is emitted from quark as part of hard process

→ hard process, similar to multi-jets

LL - photons



γ is radiated from incoming or outgoing lepton

→ theoretically well determined

Prompt photon cross section is measured as function of

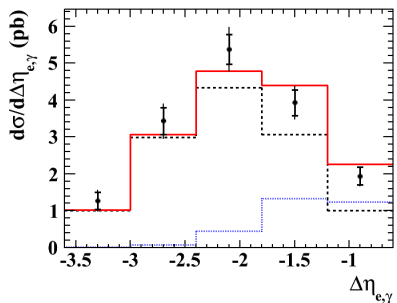
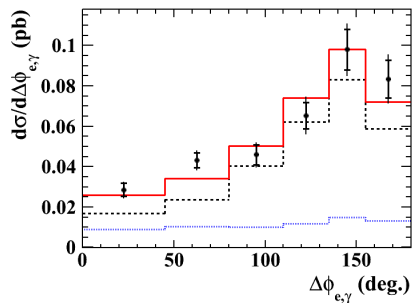
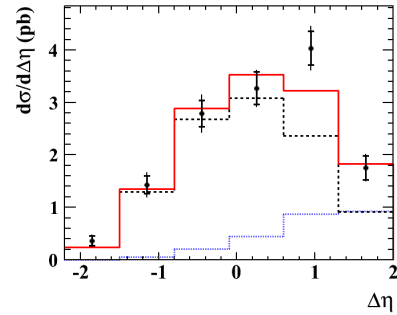
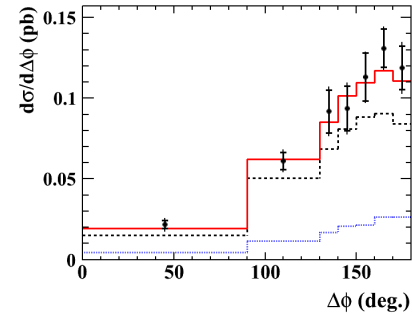
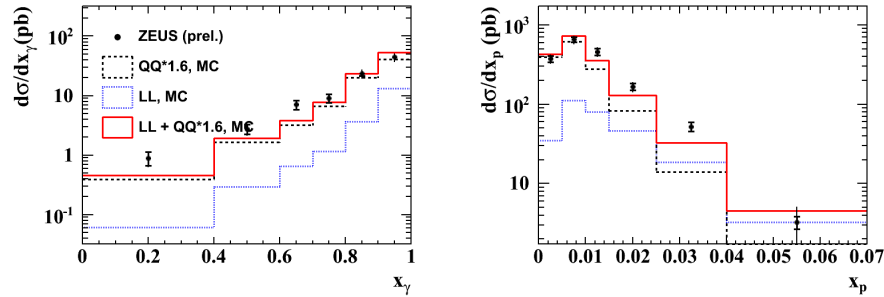
x_γ (x_p) - fractions of incoming photon (proton) energy taken by γ +jet (parton)

$\Delta\phi_{e,\gamma}$, $\Delta\eta_{e,\gamma}$ - between γ and scattered electron

$\Delta\phi$, $\Delta\eta$ - between γ and jet

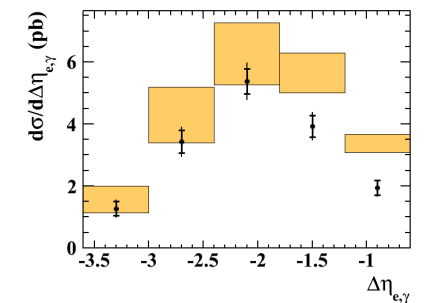
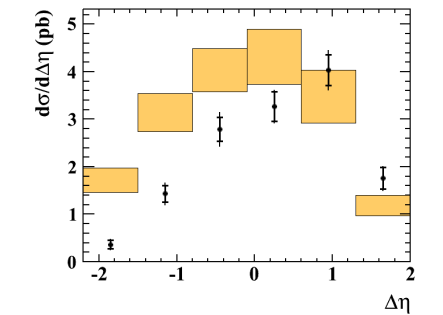
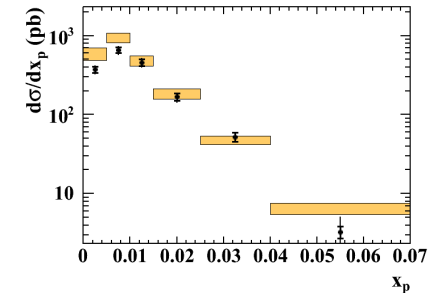
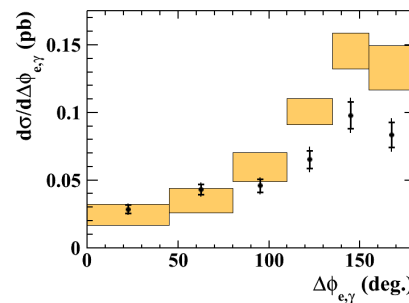
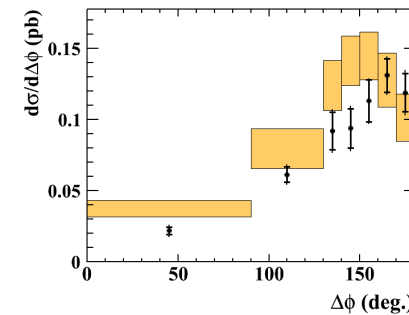
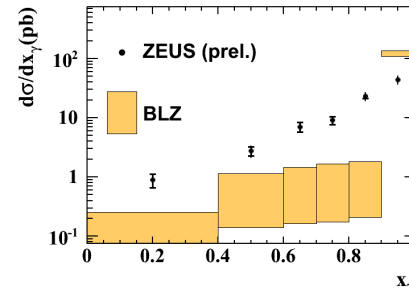
$$\begin{aligned} 10 < Q^2 < 350 \text{ GeV}^2 \\ 4 < E_T^\gamma < 15 \text{ GeV} \\ -0.7 < \eta^\gamma < 0.9 \\ 2.5 < E_T^{\text{jet}} < 35 \text{ GeV} \\ -1.5 < \eta^{\text{jet}} < 1.8 \end{aligned}$$

LL (Djangoh) + QQ (Pythia) scaled by 1.6



Comparison with BLZ model

Baranov-Lipatov-Zotov, Phys.Rev. D81, 094034 (2010)



Conclusions

H1 and ZEUS continue to deliver the HERA legacy results:

H1 and ZEUS completed the inclusive DIS program at HERA by combining all inclusive unpolarised measurements into one coherent data set of NC & CC e^+p & ep at $\sqrt{s} = 318, 300, 251$ and 225 GeV.

The combined inclusive HERA data on NC and CC are used as a sole input to the QCD analysis resulting in the set of parton distribution functions HERAPDF2.0 (together with its variants).

All H1 and ZEUS D^ production cross section measurements in DIS are combined in the visible phase space in P_T, η, z, Q^2 and y .*

*Inclusive jets, dijets, trijets cross sections (absolute and normalised to NC) are measured by H1 at low Q^2 and compared to predictions at NLO and NNLO
→ precise experimental input to α_s determinations*

Prompt photons accompanied by jets are measured in DIS by ZEUS

Dijets and Trijets in DIS compared to NLO, NNLO

normalised dijets

normalised trijets

