

# HERAFitter

## Open Source QCD Fit Platform to determine PDFs

Voica Radescu (DESY)  
for  
the HERAFitter Team

### Outline:

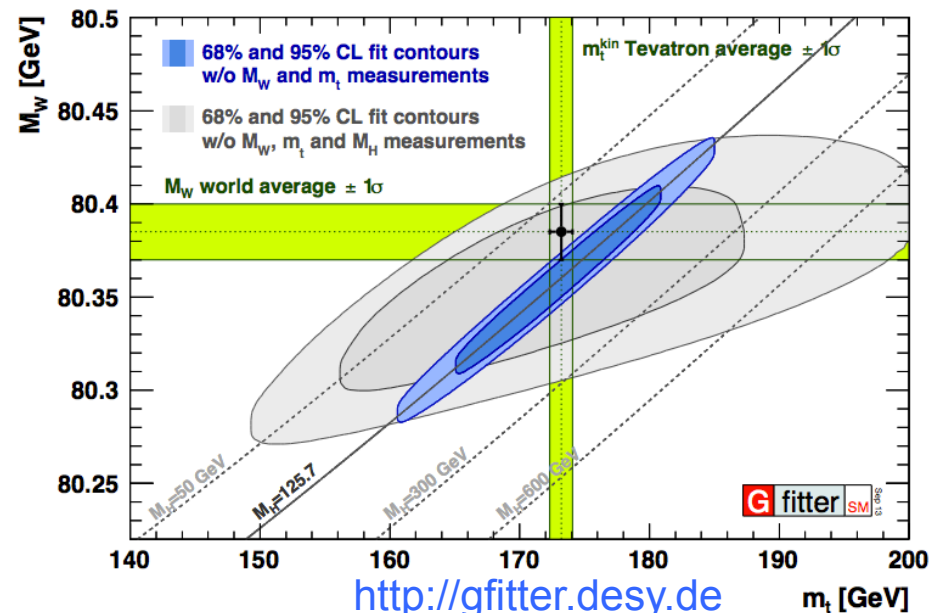
- Motivation
- Project Overview
- Application and Results



# Motivation

- Parton Distribution Functions are essential for precision physics at the LHC:
  - PDF uncertainties affect substantially theory predictions for BSM high mass production
  - PDFs are one of the main theory uncertainties in Higgs production
  - PDFs are one of the main theory uncertainties in  $M_W$  measurement

Uncertainty due to PDFs:  
 ~10 MeV for Tevatron  
[\[arxiv:1307.7627v2\]](https://arxiv.org/abs/1307.7627v2)  
 >10 MeV for LHC



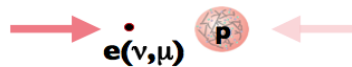
- PDF uncertainties arise from:
  - Uncertainties of experimental data
  - Differences among several groups: MSTW, CT, NNPDF, HERAPDF, ABM, JR
- **it is crucial to understand the theoretical differences**
- **it is important to provide accurate data (with correlation information) for better PDF discrimination**

# Proton Structure

**PDF extraction relies on the factorisation theorem:**

- cross sections: PDFs  $\otimes$  hard scattering coeff.

Main information on PDFs comes from DIS data at HERA which probes linear combination of quarks:

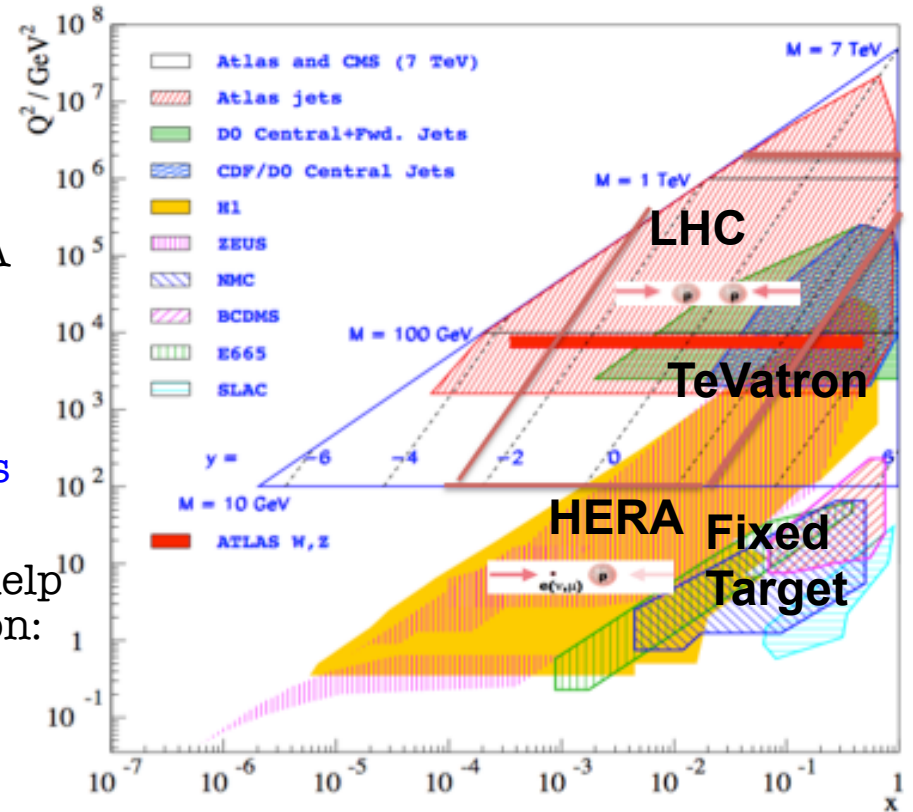


However, no flavour decomposition of the sea quarks

LHC introduces new observables and abundant data to help provide flavour separation and a better understood gluon:



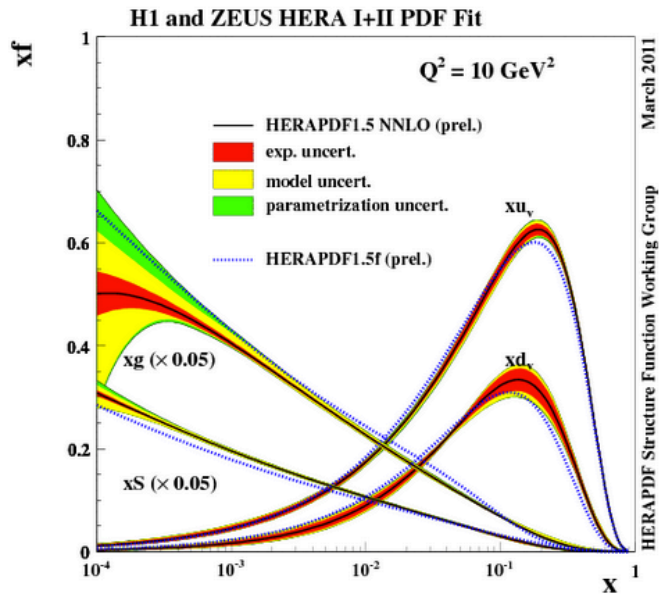
- Inclusive jets and dijets  $\rightarrow$  gluon and alphas
- W, Z production, asymmetries  $\rightarrow$  quark flavour separation
- W+charm  $\rightarrow$  direct sensitivity to s-quark
- Isolated photons  $\rightarrow$  gluon at medium and high x
- W,Z production with jets  $\rightarrow$  gluon at medium x
- ttbar, single top  $\rightarrow$  gluon and u, d



Coverage in x is essential  
QCD evolution is in  $Q^2$

# HERAFitter Project

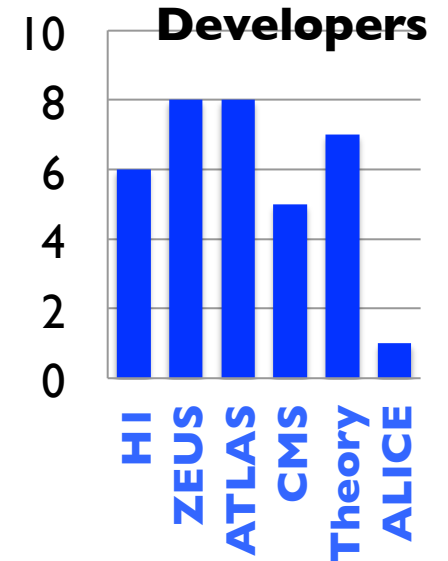
**HERAFitter is an open source QCD fit platform with a continuing rapid development**



H1prelim-11-042  
ZEUSprelim-11-002



- Apr 2014 — HERAFitter @ QCD Moriond
- Mar 2014 — **First HERAFitter Stable Release**
- Dec 2013 — Award winning poster at the conferences
- Sep 2013 — Third HERAFitter Beta Release
- Mar 2013 — **First PDF School based on HERAFitter**
- Oct 2012 — Second HERAFitter Beta Release
- May 2012 — **First LHC paper using HERAFitter**
- Mar 2012 — First HERAFitter Workshop
- Nov 2011 — First HERAFitter Invited presentation
- Oct 2011 — Presented to the LHC Community
- Sep 2011 — **First HERAFitter Beta Release**

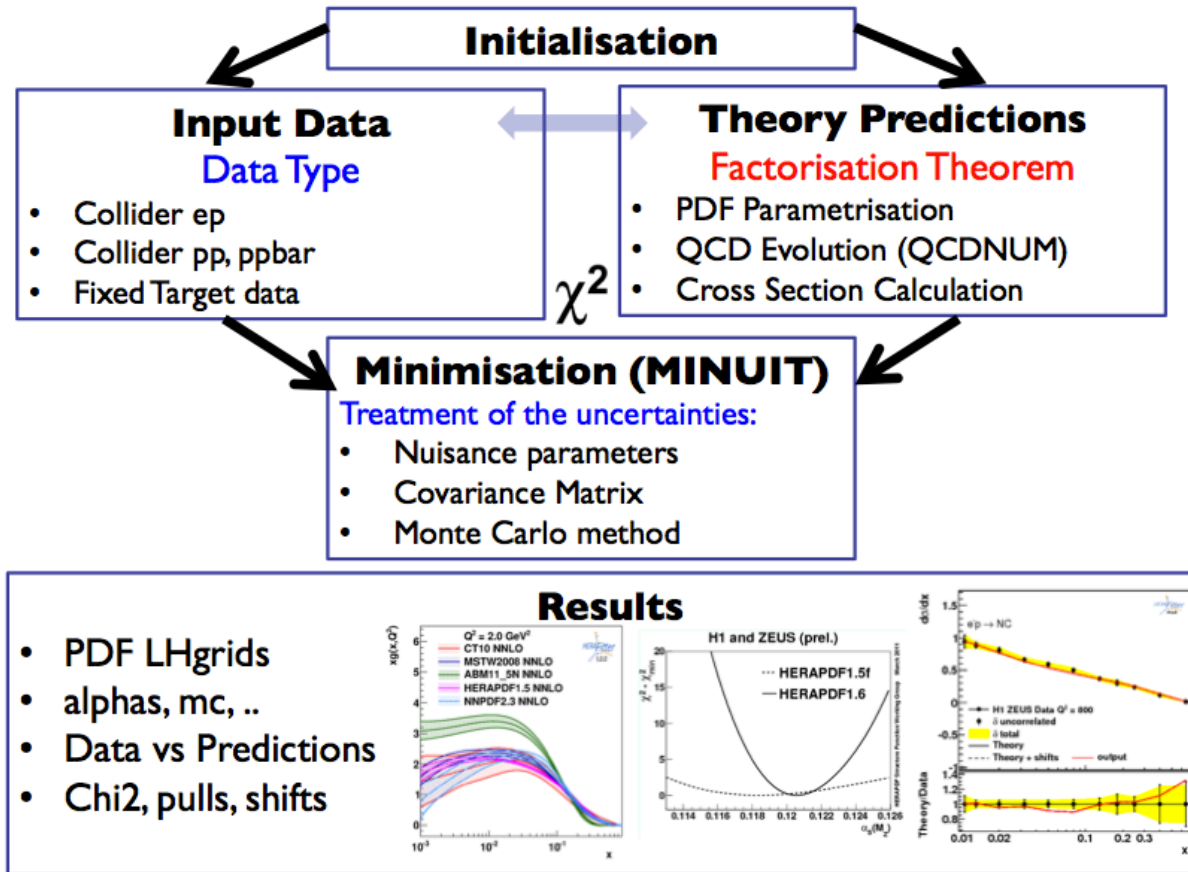


## HERAFitter:

- is a unique framework to address the theoretical differences
- provides means to the experimentalists to assess impact of new data

# Schematics of PDF extraction in HERAFitter

A flow diagram of a PDF extraction in a QCD fit machinery:



~2000 iterations

Performance: 15min – 2h

## On data side:

- Important to provide correlation information

## On theory side:

- Important to have fast tools to perform PDF fits i.e. APPLGRID, FASTNLO
  - grid techniques rely on factorisation theorem

# Heavy Flavour Schemes in DIS

Heavy quarks introduce additional scales which complicates the calculations:

- **VFNS (Variable Flavour Number Schemes):**

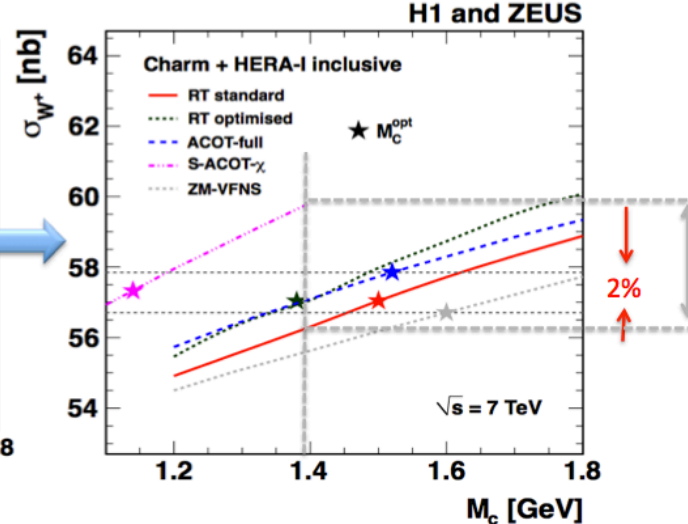
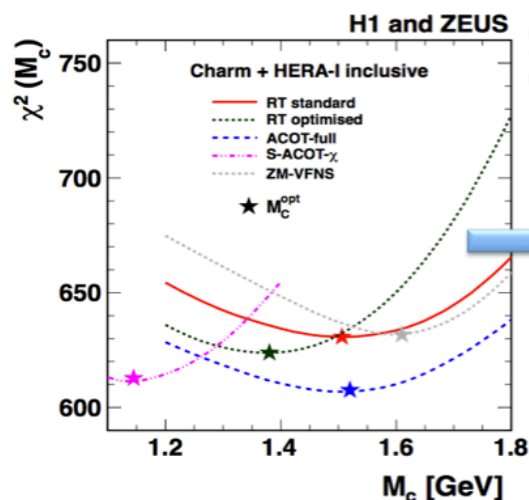
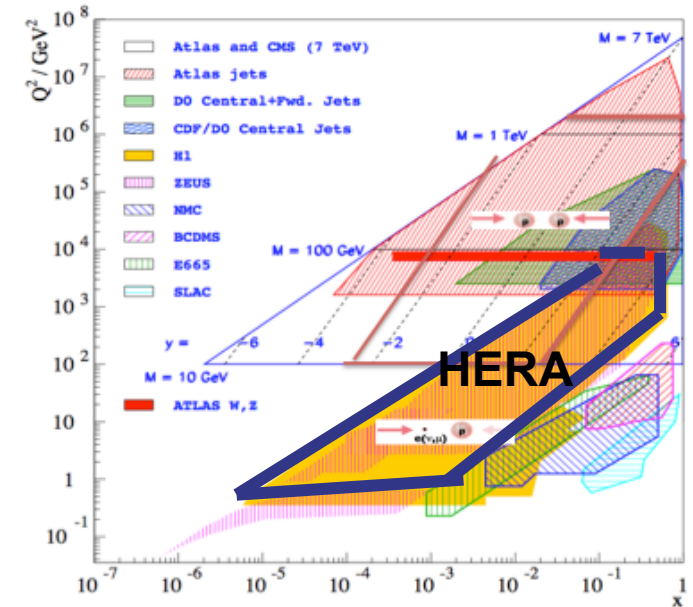
- ▾ RT-VFNS schemes → as used by MSTW group
- ▾ Zero Mass VFNS
- ▾ ACOT schemes → as used by CT(CTEQ) group

- **FFNS (Fixed Flavour Number Scheme)**

- ▾ via QCDNUM
- ▾ Via Openqcdrad-1.6 → as used by ABM

→ Variety of scheme options was studied by HERA in F2 charm HERA combined paper

[Eur. Phys. J. C73 (2013) 2311]



Spread in predictions for W and Z is reduced significantly when predictions are evaluated at the optimal  $M_c$  determined from F2 charm

# Quantitative Comparison between data and theory

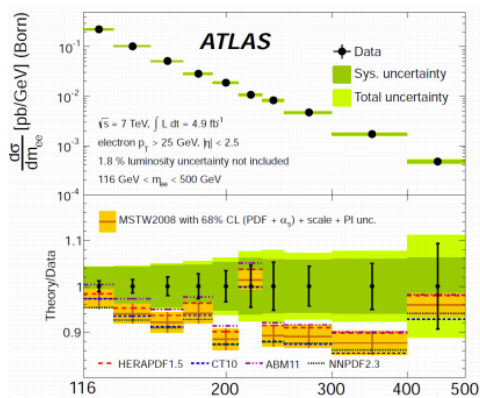
HERAFitter provides a quantitative assessment of level of agreement between data and theory by taking into account theoretical and experimental uncertainties

$$\chi^2 = \sum_i \left( \frac{\mu_i - m_i \left[ 1 + \sum_j b_j^{\text{exp}} \gamma_{ji}^{\text{exp}} + \sum_j b_j^{\text{theo}} \gamma_{ji}^{\text{theo}} \right]}{\Delta_i} \right)^2 + \sum_j (b_j^{\text{exp}})^2 + \sum_j (b_j^{\text{theo}})^2$$

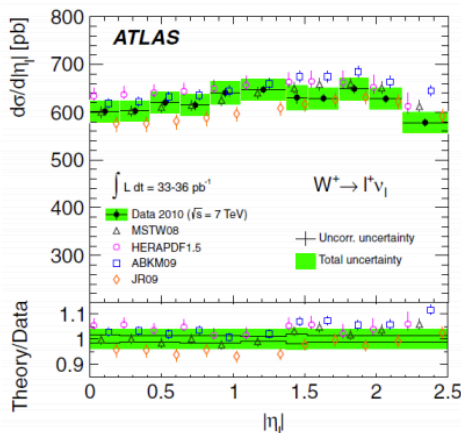
ATL-PHYS-PUB-2013-018

Used in ATLAS publications:

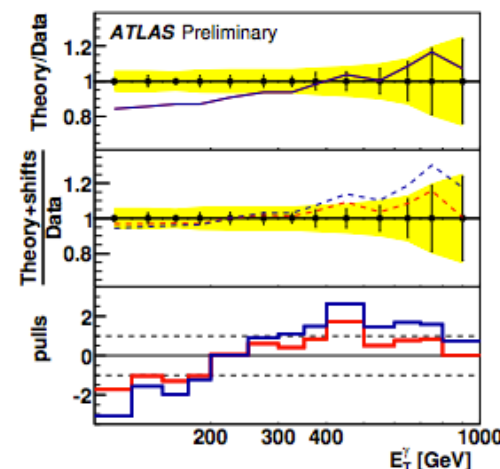
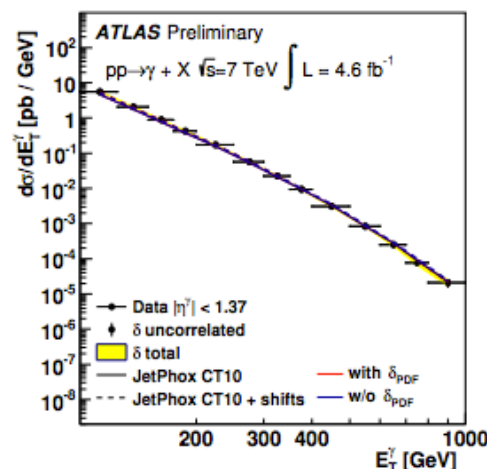
	Excluding PDF uncertainties		Including PDF uncertainties	
	$\mu_r = \mu_f = E_T^\gamma$	Envelope	$\mu_r = \mu_f = E_T^\gamma$	Envelope
CT10	49.1	34.7 - 63.1	29.8	20.0 - 38.4
MSTW2008	39.9	27.2 - 52.7	32.0	21.3 - 42.3
ABM11_5N	16.2	9.2 - 25.5	15.7	8.9 - 24.9
HERAPDF1.5	28.7	19.0 - 38.9	23.6	15.7 - 32.0
NNPDF2.3	33.5	22.6 - 44.7	27.6	18.7 - 36.9



Phys. Lett. B 725 (2013) 223

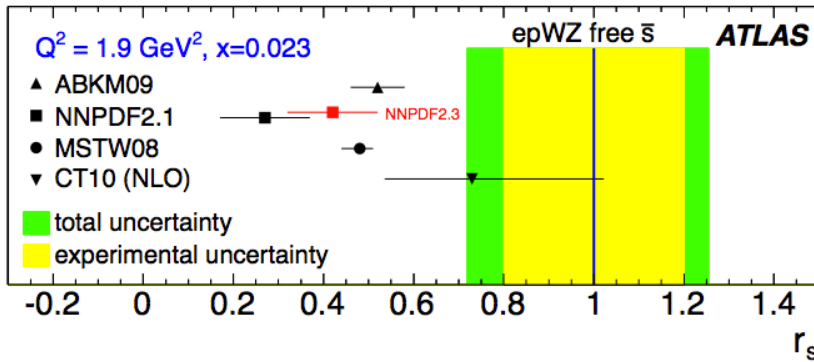


Phys. Rev. D 85 (2012) 072004

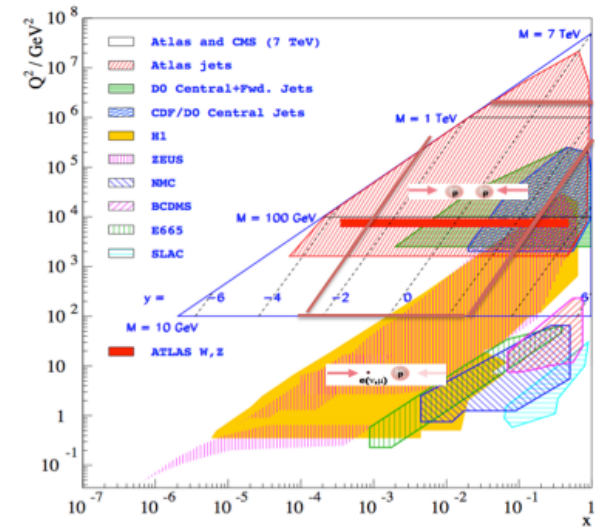


# Determination of the strange quark at the LHC

- **Using  $W^+$ ,  $W^-$ ,  $Z$  (35/pb) inclusive cross sections** – ATLAS [PRL 109 (2012) 012001] → kinematic region probed is at  $x \sim 0.01$ 
  - NNLO QCD Analysis (NLO is in agreement):



→ Result supports an SU(3) symmetric light sea

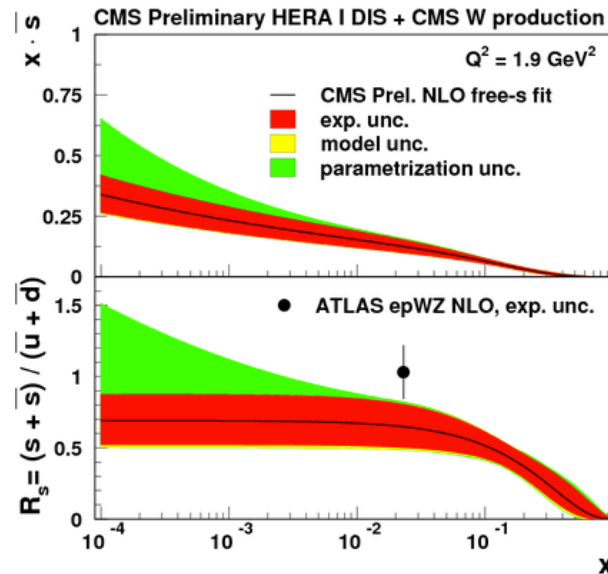
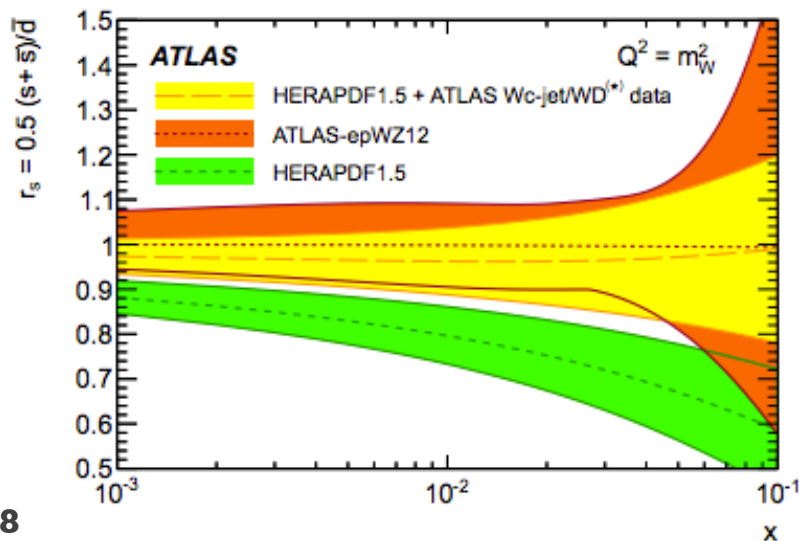


- **Using  $W^+$ charm production at 7 TeV (4.6/fb):**

ATLAS [arxiv:1402.6263]:

CMS (includes W asymmetry) [SMP-12-021]

- In good agreement with above:



NLO analyses

ATLAS:  $R_s = (s + \bar{s}) / 2\bar{d}$

CMS:  $R_s = (s + \bar{s}) / \bar{u} + \bar{d}$



# Sensitivity to gluon and strong coupling:

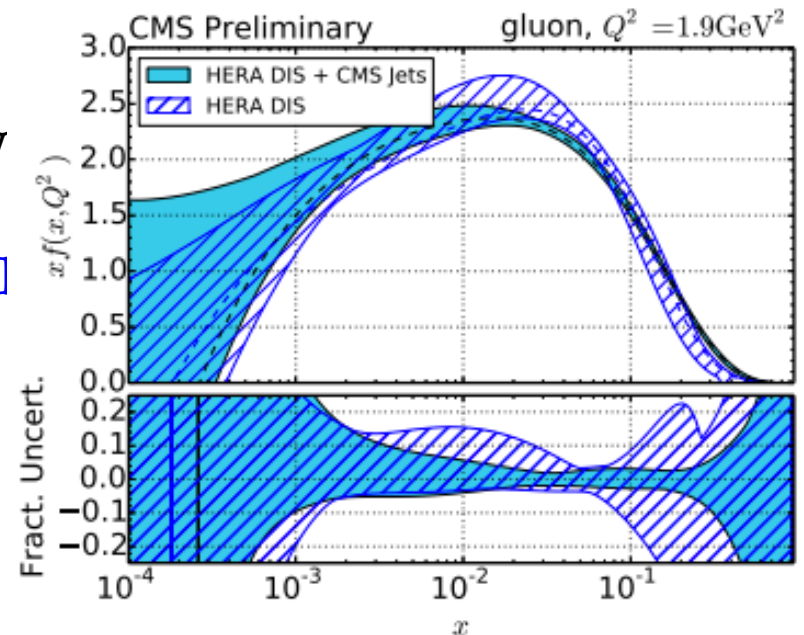
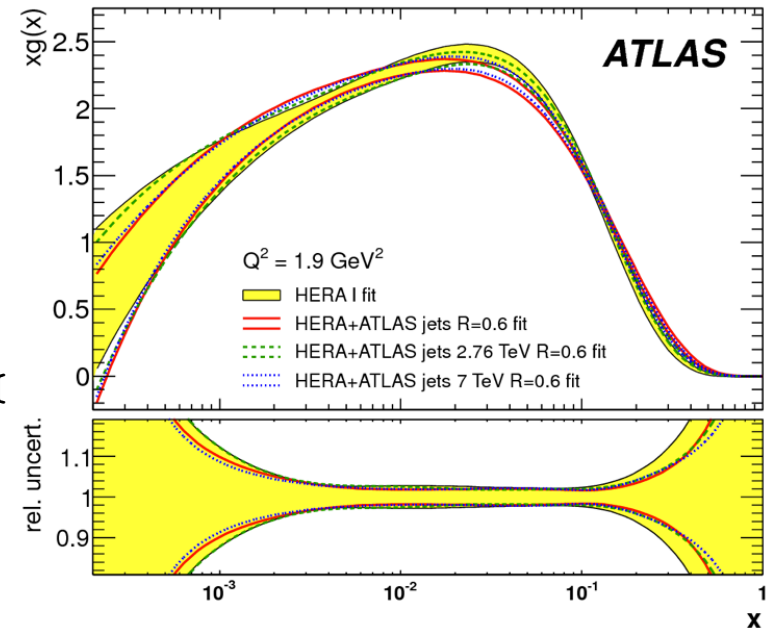
## Study sensitivity to the gluon PDF:

- Using ratio of jets at different beam energies – ATLAS [EPJC (2013) 73 2509]
  - ▽ Benefits from cancellation of common sys. unc.
  - ▽ Compare the gluon for PDF fit using just HERA I and a fit using HERA I + ATLAS 2.76, 7 TeV jet data (2010)
  
- Using inclusive jet cross section at 7 TeV CMS data from 2011 (5/fb) [SMP-12-028]:
  - ▽ PDFs are extracted and compared to fits using just HERA I and fits using HERA I + CMS 7 TeV jet data

## Extraction of the strong coupling [SMP-12-028]

- From PDF and alphas simultaneous fit:

$$\alpha_s(M_Z) = 0.1192^{+0.0017}_{-0.0015}$$



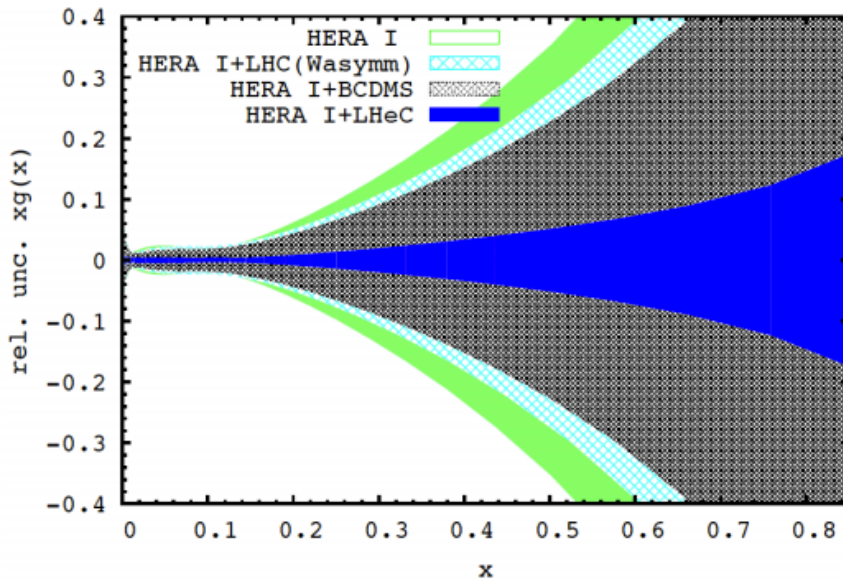
# Impact studies of LHeC on PDFs

[Journal of Phys. G 39 (2012)]

HERAFitter provides the possibility to perform impact studies using simulated data:

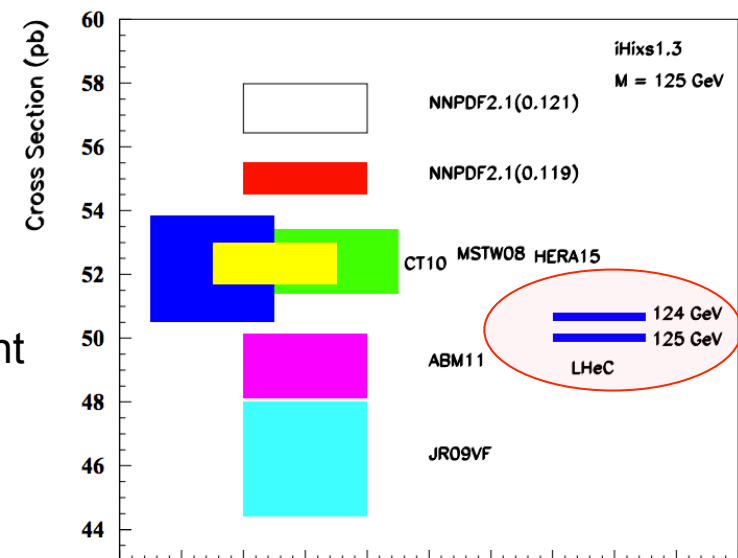
- LHeC can provide a complete PDF set with precise gluon, valence, and strong coupling:

LHeC promises per mille accuracy on alphas – using HERAFitter



case	cut [ $Q^2$ in GeV]	relative precision in %
HERA only (14p)	$Q^2 > 3.5$	1.94
HERA+jets (14p)	$Q^2 > 3.5$	0.82
LHeC only (14p)	$Q^2 > 3.5$	0.15
LHeC only (10p)	$Q^2 > 3.5$	0.17
LHeC only (14p)	$Q^2 > 20.$	0.25
LHeC+HERA (10p)	$Q^2 > 3.5$	0.11
LHeC+HERA (10p)	$Q^2 > 7.0$	0.20
LHeC+HERA (10p)	$Q^2 > 10.$	0.26

NNLO pp-Higgs Cross Sections at 14 TeV



HERAFitter provides LHAPDF grids:

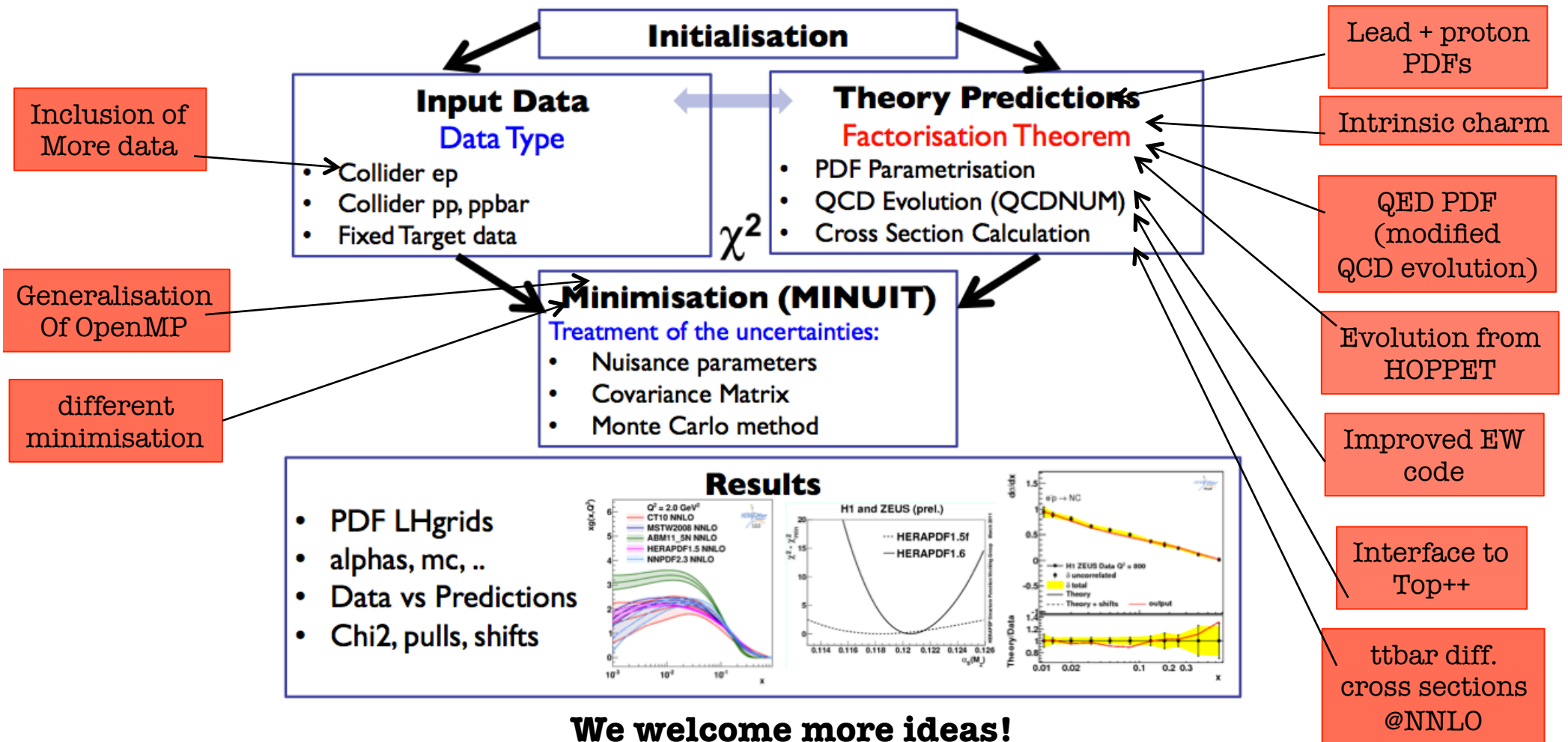
14 TeV  $gg \rightarrow H$  total cross section at the LHC calculated for a variety of PDFs at 68% CL

- precision from LHeC can add a very significant constraint on the mass of the Higgs
- **LHeC-NLO. LHgrid available in lhapdf v5.9.1**

# HERAFitter Prospects

HERAFitter has a modular structure facilitating fast developments

- Many new developments are planned to be implemented in future releases:



**We welcome more ideas!**

# HERAFitter Summary and Prospects

- HERAFitter is an open source QCD Framework and it has proved to be a successful platform that is well integrated in the high energy physics community:
  - driven by the abundant data in need for a careful QCD investigation
- HERAFitter infrastructure has increased the scientific output of the HERA and LHC data, provides a flexible environment for theory benchmarking.
  - ▽ Various treatments for heavy flavours;
  - ▽ Various options for data uncertainties treatment;
  - ▽ Various parametrisation techniques;
  - ▽ Various physics cases.
- **theory:** include new state of the art developments (i.e. ttbar differential cross-section)
- **experiment:** include new observables/measurements to improve PDFs

Stable release: [herafitter-1.0.0](https://github.com/HERAFitter/HERAFitter/releases/tag/1.0.0)

- [www.herafitter.org](http://www.herafitter.org)

**We welcome new developments!**

# Results using HERAFitter

- Following PDF grids have been generated since the start of the project:
  - **HERAPDF1.0, HERAPDF1.5, ATLAS-epWZ12, LHeC-NLO**
- HERAFitter has been used in the following publications:



“Determination of the strange quark density of the proton from ATLAS measurements of the W and Z cross sections” [[PRL 109 \(2012\) 012001](#)]

“Measurements of the inclusive jet cross section in pp collisions at 2.76 TeV and comparison to the inclusive jet cross section at 7 TeV using the ATLAS detector” [[EPJC \(2013\) 73 2509](#)]

“Measurement of the high-mass Drell-Yan differential cross-section in pp collisions at 7 TeV with the ATLAS detector” [[PLB 725 \(2013\) 223](#)]

“Measurement of the production of a W boson in association with a charm quark in pp collisions at  $\sqrt{s}=7$  TeV with the ATLAS detector”[]

“A study of the sensitivity to the proton parton distributions of the inclusive photon production cross section in  $pp$  collisions at 7 TeV measured by the ATLAS experiment at the LHC”



“Measurement of the muon charge asymmetry in pp W production at 7 TeV” [[SMP-12-021](#)]

“PDF constraints and extraction of the strong coupling constant from the inclusive jet cross section at 7 TeV” [[SMP-12-08](#)]



“Combination and QCD Analysis of Charm Production Cross Section Measurements in Deep Inelastic ep Scattering at HERA” [[EPJC \(2013\) 73 2311](#)]

“Inclusive Deep Inelastic Scattering at High  $Q^2$  with Longitudinally Polarised” [[JHEP 1209 \(2012\) 061](#)]



LHeC impact studies [[Journal of Phys. G 39 \(2012\)](#)]



“Parton Distribution Uncertainties using Smoothness Prior” [[PLB 695 \(2011\) 238](#)]



# Extra Slides

# Functional Forms for PDF parametrisation

- PDFs are parametrised at a starting scale as function of  $x$ , QCD evolves them in  $Q^2$
- Various functional forms can be tested within HERAFitter platform:
  - Standard Polynomials:

$$xf(x) = Ax^B(1-x)^C P_i(x),$$

- Log-Normal Distributions:

$$xf(x) = x^{p-b\log(x)}(1-x)^{q-\log(1-x)}$$

- Chebyshev Polynomials:

$$xg(x) = A_g(1-x) \sum_{i=0}^{N_g-1} A_{g_i} T_i \left( -\frac{2\log x - \log x_{min}}{\log x_{min}} \right),$$

$$xS(x) = (1-x) \sum_{i=0}^{N_S-1} A_{S_i} T_i \left( -\frac{2\log x - \log x_{min}}{\log x_{min}} \right).$$

- Use of External PDFs via LHAPDF interface to construct theoretical predictions.

# Chi square definitions

- Typical measurements sensitive to PDFs are precise, with statistical uncertainties below 10%, so they follow normal distribution which allows use of chi square minimization for determining optimal PDF parameters.
- The HERAFitter package allows for various types of data uncertainty treatment:
  - ▽ Various chi square representations:

- **Covariance Matrix Representation:**

$$\chi^2(m) = \sum_{i,j} (m_i - \mu_i) C_{ij}^{-1} (m_j - \mu_j) \quad C_{ij} = C_{ij}^{stat} + C_{ij}^{uncor} + C_{ij}^{sys}$$

- **Nuisance Parameters Representation:**

$$\chi^2(m, b) = \sum_i \frac{\left[ m^i - \sum_j \gamma_j^i m^i b_j - \mu^i \right]^2}{\delta_{i,stat}^2 \mu^i \left( m^i - \sum_j \gamma_j^i m^i b_j \right) + \left( \delta_{i,uncor} m^i \right)^2} + \sum_j b_j^2. \quad \mu^i \text{ is the measured central value}$$

- **Mixed form (covariance and nuisance parameter):**

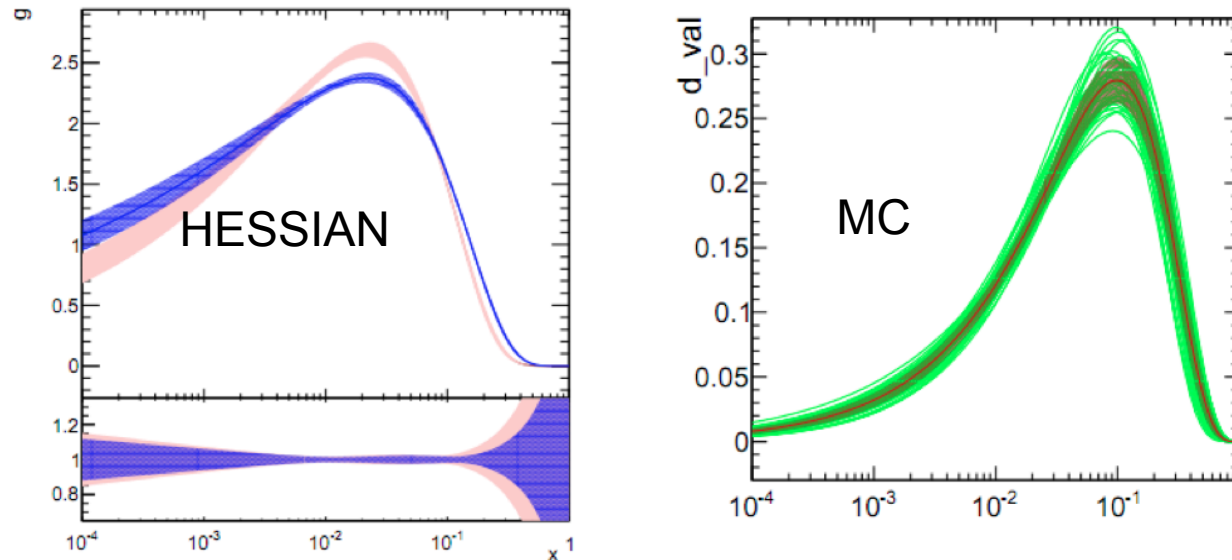
HERAFitter offers the possibility to include form of treating statistical, uncorrelated and correlated systematic uncertainties given in different forms.



# Experimental Uncertainties

HERAFitter allows for various types of data uncertainty treatment:

- Hessian and toy Monte Carlo error propagation



→ Monte Carlo Method for error estimation compared to Hessian error propagation:

- Benchmarking exercise with NNPDF group [arXiv:0901.2504]
- Regularisation methods: to constrain PDF's in a flexible parametrisation style:
  - Data Driven Regularisation (as used by NNPDF): fit and control samples
  - External Regularisation based on a penalty term in chisquare
- Possibility to include asymmetric uncertainties.

# Low x Physics

As an alternative to DGLAP, HERAFitter includes also Dipole models:

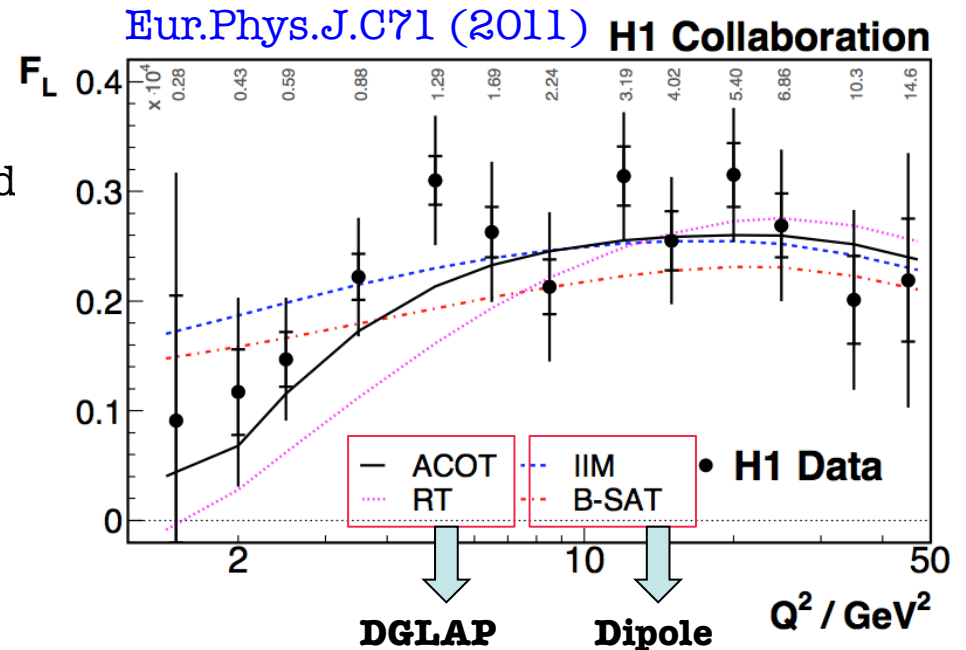
- Studied by the H1 collaboration in comparing different models on FL:

- **Dipole Models implemented in HERAFitter:**

- ▽ GBW model: first model
    - ▽ IIM (based on BK-equation)
    - ▽ BGK (based on GBW, but gluon evolved using DLGAP)

- **DGLAP Models:**

- ▽ RT as used by MSTW group
    - ▽ ACOT as used by CTEQ group



Unintegrated PDFs based on the kT-factorisation (CCFM) evolution.

- applicable only to NC ep scattering:

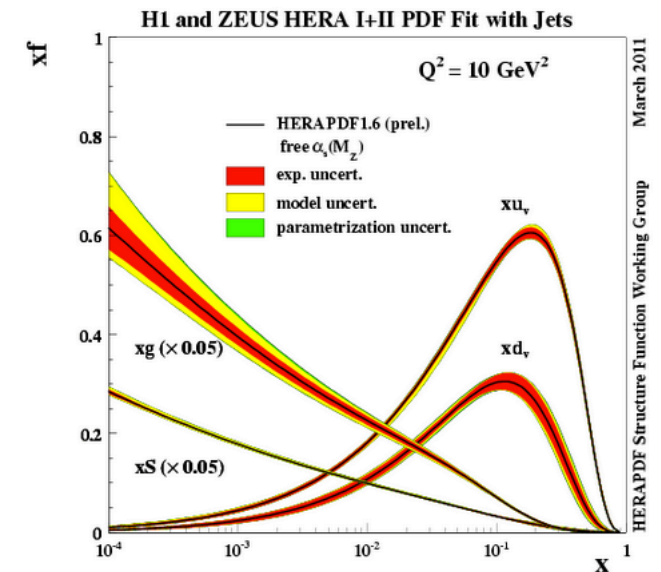
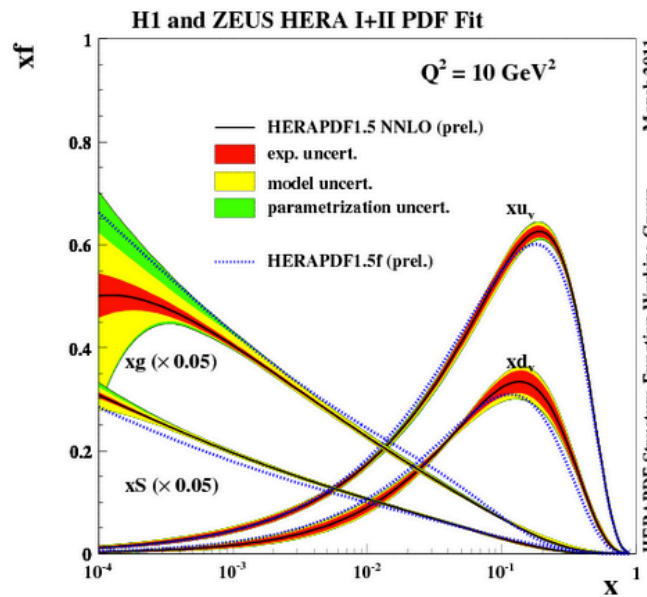
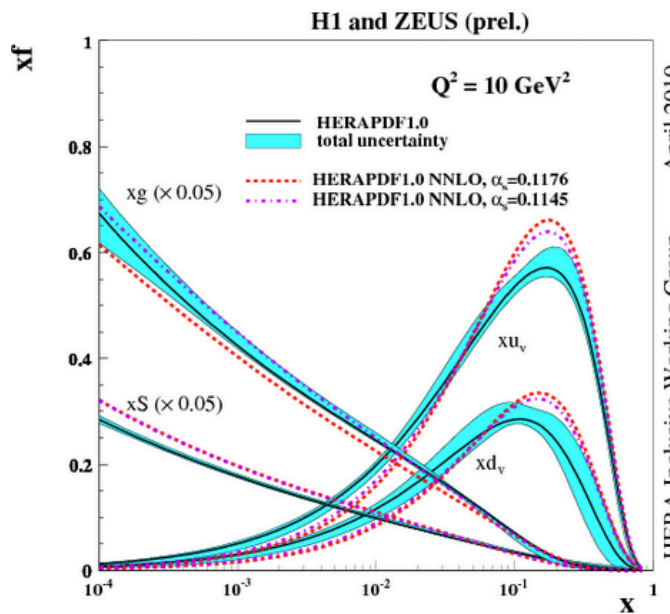
<https://www.herafitter.org/HERAFitter/HERAFitter/HERAFitterMeetings/Meeting2012-Oct-29?action=AttachFile&do=get&target=updf.pdf>

Diffractive DIS PDF fits.

## List of analyses using HERAFitter

Date	Group	Reference	Title
<b>NEW</b> 02.2014	LHC/ATLAS	arXiv:1402.6263	• Measurement of the production of a W boson in association with a charm quark in pp collisions at $\sqrt{s}=7$ TeV with the ATLAS detector
<b>NEW</b> 01.2014	R. Sadykov	arXiv:1401.1133	• Impact of QED radiative corrections on Parton Distribution Functions
<b>NEW</b> 01.2014	F. Hautmann and H. Jung	arXiv:1312.7875	• Transverse momentum dependent gluon density from DIS precision data
<b>NEW</b> 12.2013	A. Luszczak and H. Kowalski	arXiv:1312.4060	• Dipole model analysis of high precision HERA data
12.2013	LHC/ATLAS	ATL-PHYS-PUB-2013-018	• A study of the sensitivity to the proton parton distributions of the inclusive photon production cross section in $pp$ collisions at 7 TeV measured by the ATLAS experiment at the LHC
12.2013	LHC/CMS	CMS-SMP-12-021 / arXiv:1312.6283	• Measurement of the muon charge asymmetry in pp W production at 7 TeV
12.2013	LHC/CMS	CMS-SMP-12-028	PDF constraints and extraction of the strong coupling constant from the inclusive jet cross section at 7 TeV
2013	LHC/ATLAS	Phys. Lett. B 725 (2013) pp. 223	• Measurement of the high-mass Drell-Yan differential cross-section in pp collisions at $\sqrt{s}=7$ TeV
2013	LHC/ATLAS	EPJC (2013) 73 2509	• Measurement of the inclusive jet cross section in pp collisions at $\sqrt{s} = 2.76$ TeV and comparison to the inclusive jet cross section at $\sqrt{s} = 7$ TeV using the ATLAS detector
2013	LHC/ATLAS	Phys.Rev.Lett. 109 (2012) 012001	• Determination of the strange quark density of the proton from ATLAS measurements of the $W \rightarrow l \nu$ and $Z \rightarrow ll$ cross sections
2013	HERA/H1 and ZEUS	Eur. Phys. J. C73 (2013) 2311	• Combination and QCD Analysis of Charm Production Cross Section Measurements in Deep-Inelastic ep Scattering at HERA
2012	HERA/H1	JHEP 09 (2012) 061	• Inclusive Deep Inelastic Scattering at High $Q^2$ with Longitudinally Polarised Lepton Beams at HERA
2012	LHeC	J.Phys. G39 (2012) 075001	• A Large Hadron Electron Collider at CERN: Report on the Physics and Design Concepts for Machine and Detector

- HERAFitter roots to the PDF analyses performed by H1 and ZEUS:
  - HERAPDF1.0
  - HERAPDF1.5 (LO/NLO/NNLO)
  - HERAPDF1.6

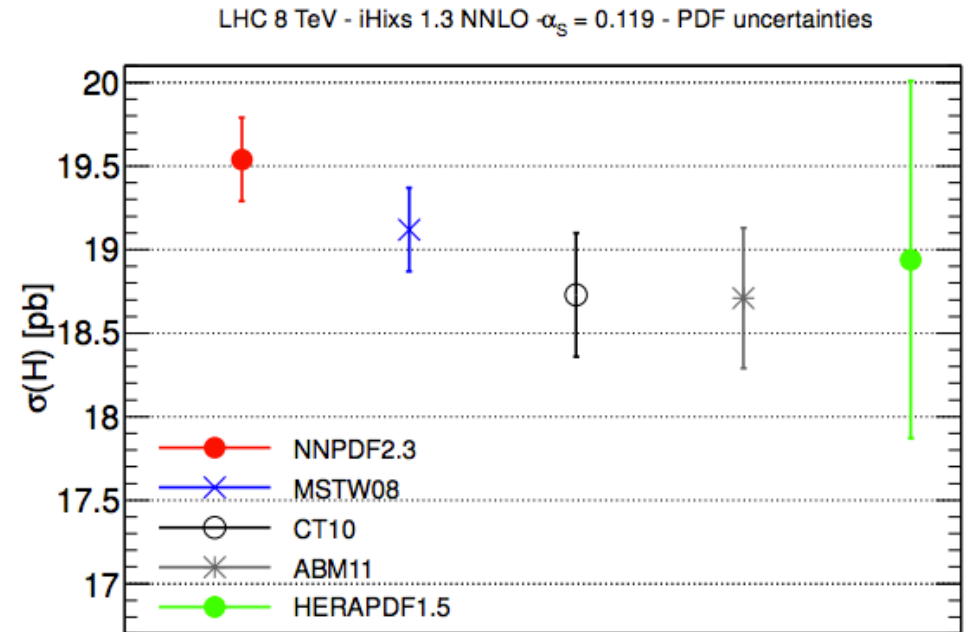


- To come soon: HERAPDF2.0

# Motivation

- Parton Distribution Functions are essential for precision physics at the LHC:
  - PDFs are one of the main theory uncertainties in  $M_W$  measurement
  - PDF uncertainties also affect substantially theory predictions for BSM high mass production

- PDF uncertainties arise from:
  - Precision of experimental data
  - Differences among several groups:
    - ▽ MSTW, CT, NNPDF, HERAPDF, ABM, JR
    - ▽ Current benchmarking of PDFs → 10% differences among PDF groups for predictions for the Higgs cross section



<http://nnpdf.hepforge.org/html/pdfbench/catalog/pdfbenchcatalog.pdf>

- **it is crucial to understand the theoretical differences**
- **it is important to provide accurate data for better PDF discrimination**