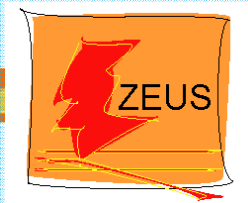


# The Charm and Beauty quark masses



## and their running at HERA



Achim Geiser  
DESY Hamburg

for the

**H1 and ZEUS**

collaborations + S. Moch



Low x workshop, Kyoto, Japan, 21. 6. 2014

DESY-12-172, EPJ C73 (2013) 2311

DESY-14-083, arXiv:1405.6915

H1-prelim-14-071, ZEUS-prel-14-006, +S. Moch

for more details on  
data analysis see  
talk O. Zenaiev

# running of $\alpha_s$ and quark masses

- $\alpha_s$  running depends on number of colours  $N_C$  and number of quark flavours  $N_F$

$$\alpha_s(Q^2) = \frac{\alpha_s(Q_0^2)}{1 + \alpha_s \times (11N_C - 2N_F)/12\pi \ln(Q^2/Q_0^2)}$$

- quark mass running depends on  $\alpha_s$ , e.g.

$$\begin{aligned} m_c(\text{pole}) &= m_c(m_c) (1 + 4/3 \alpha_s/\pi) \\ &= m_c(Q) (1 + \alpha_s/\pi (4/3 + \ln(Q^2/m_c^2))) \end{aligned}$$

leading  
order  
QCD  
formulae

- part of gluon field around quark not 'visible' any more when 'looking' at smaller distances/larger energy scales -> **effective mass decreases**

# the running b quark mass at LEP

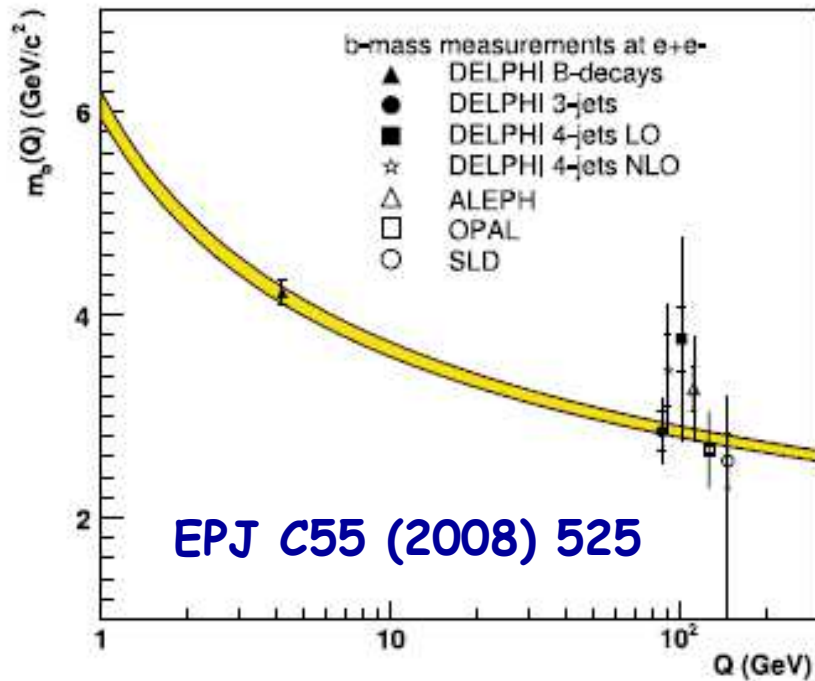


Fig. 6. The energy evolution of the  $\overline{MS}$ -running  $b$ -quark mass  $m_b(Q)$  as measured at LEP. DELPHI results from  $R_3^{b\ell}$  [7] at the  $M_Z$  scale and from semileptonic  $B$ -decays [31] at low energy are shown together with results from other experiments (ALEPH [4], OPAL [5] and SLD [6]). The masses extracted from LO and approximate NLO calculations of  $R_4^{b\ell}$  are found to be consistent with previous experimental results and with the reference value  $m_b(Q)$  (grey band) obtained from evolving the average  $m_b(m_b) = 4.20 \pm 0.07 \text{ GeV}/c^2$  from [17] using QCD RGE (with a strong coupling constant value  $\alpha_s(M_Z) = 0.1202 \pm 0.0050$  [30])

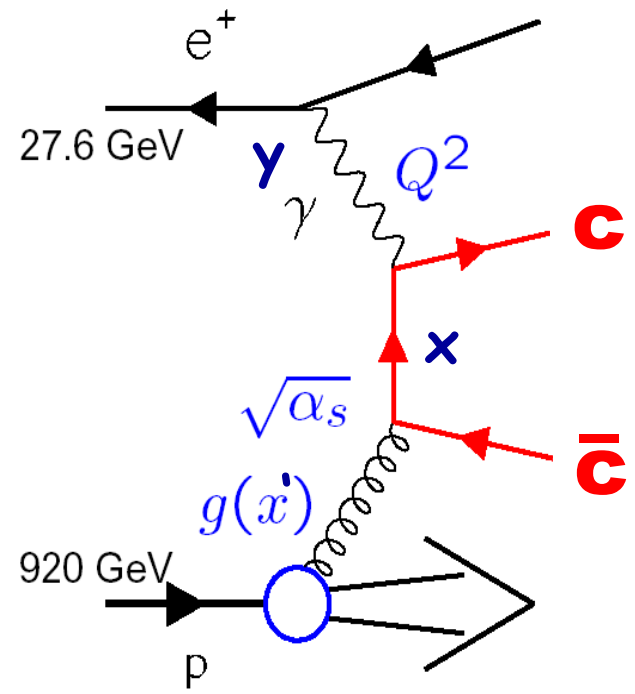
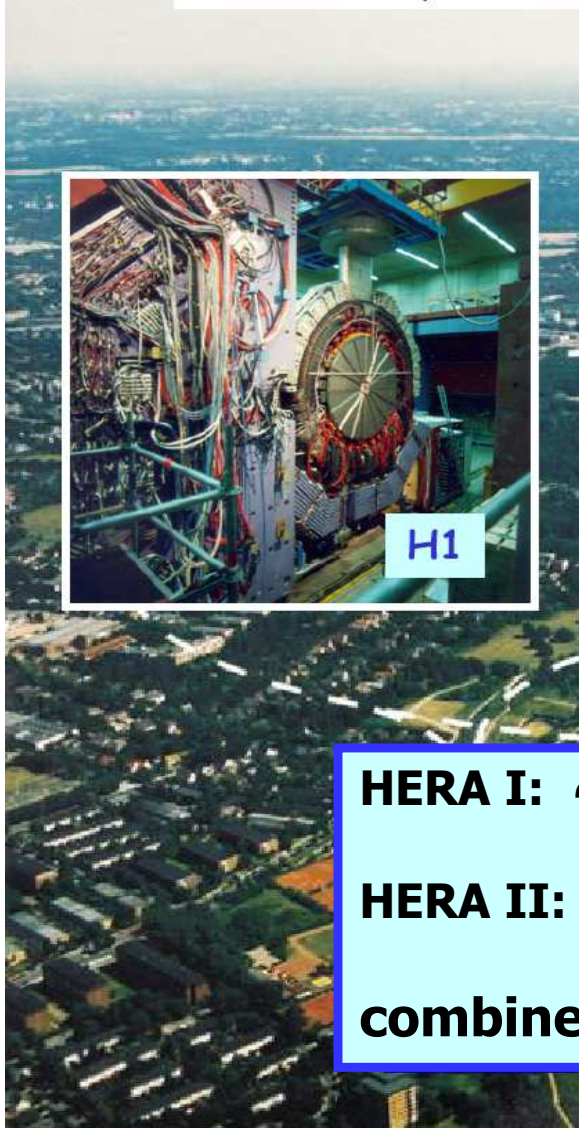
LEP:  $Z \rightarrow bb + \text{gluons}$ ,  
measurement of phase space/  
angular distributions

$$m(Q) = m(Q_0) \left(1 - \frac{\alpha_s}{\pi} \ln(Q^2/Q_0^2)\right)$$

charm mass running  
not explicitly measured  
(so far)



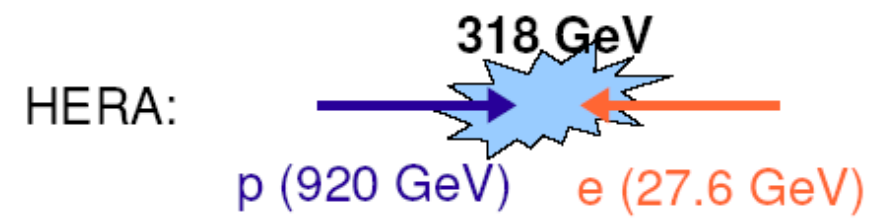
# The HERA ep collider and experiments



up to 30%  
of cross section



**HERA I:  $\sim 130 \text{ pb}^{-1}$  (physics)**  
**HERA II:  $\sim 380 \text{ pb}^{-1}$  (physics)**  
**combined:  $\sim 2 \times 0.5 \text{ fb}^{-1}$**



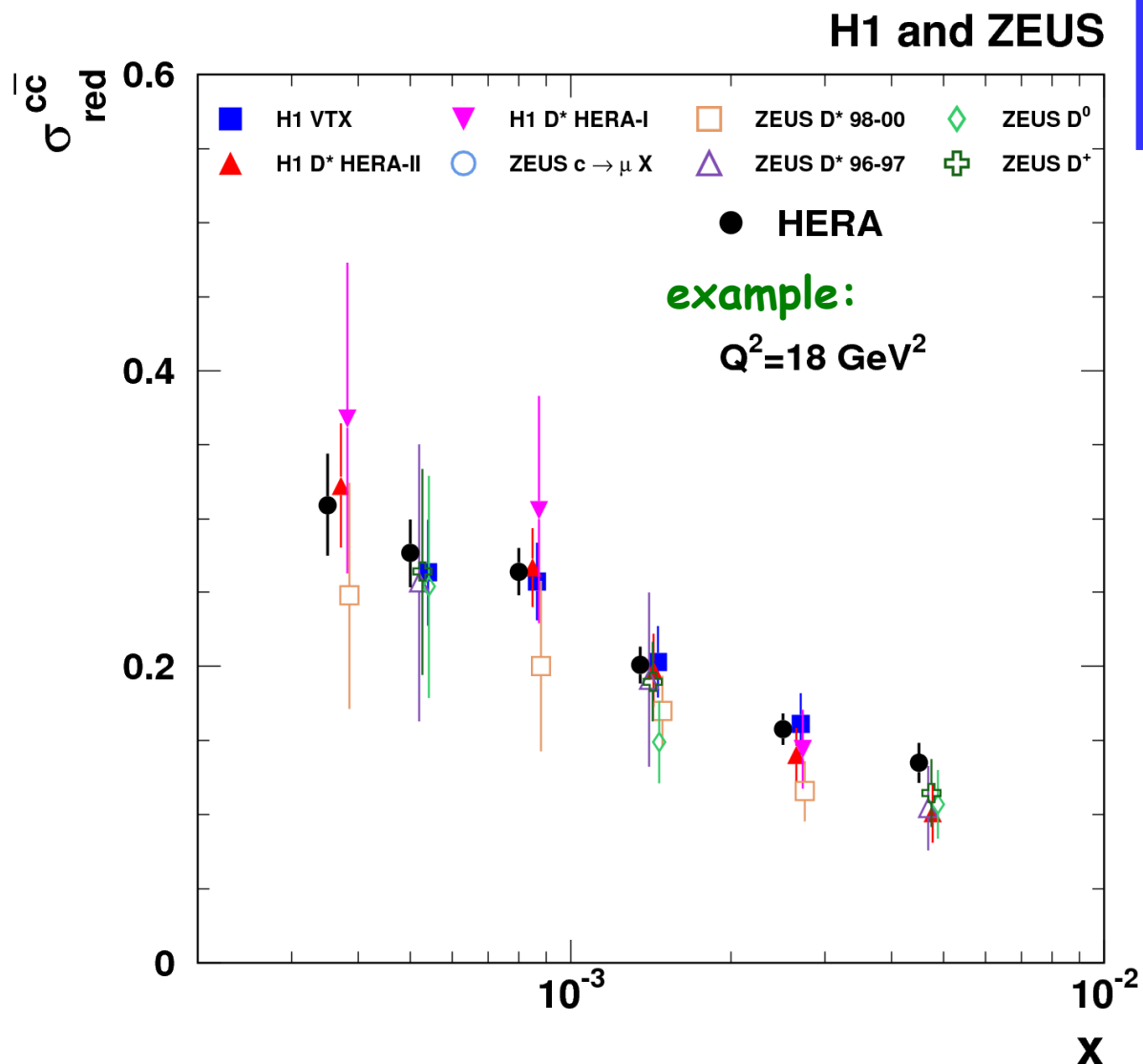


# HERA charm data combination



Measure cross section

$$\frac{d^2\sigma}{dx dQ^2} = \frac{2\pi\alpha^2}{Q^4x} \left\{ \left[ 1 + (1-y)^2 \right] \sigma_{red}^{cc} \right.$$

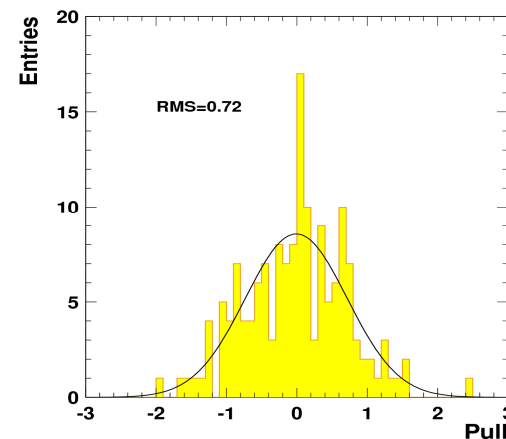


9 data sets  
(HERA I, HERA II)

5 charm tagging methods

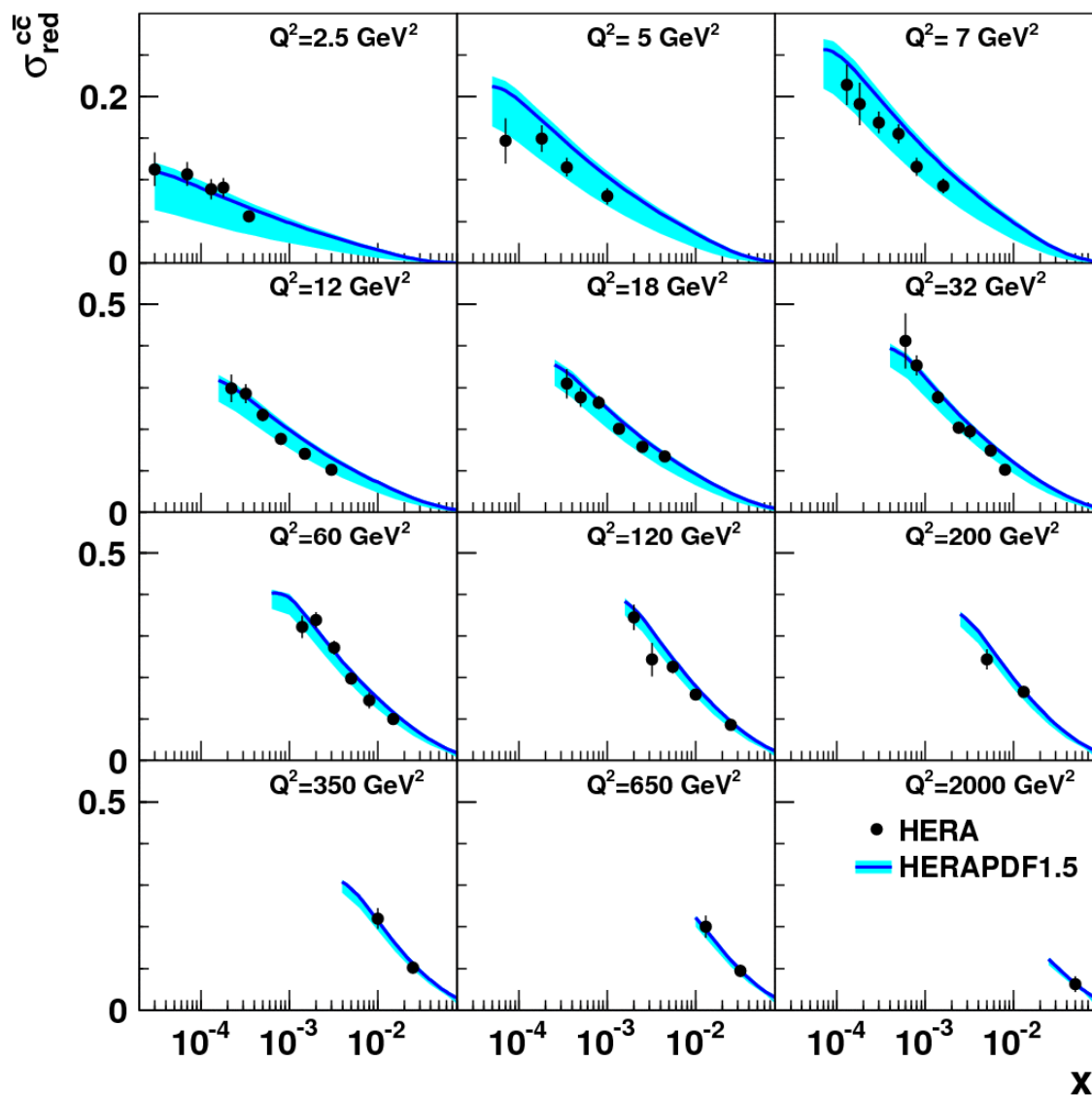
155 -> 52 data points

48 correlated systematic uncertainties



very good consistency of data:

## H1 and ZEUS

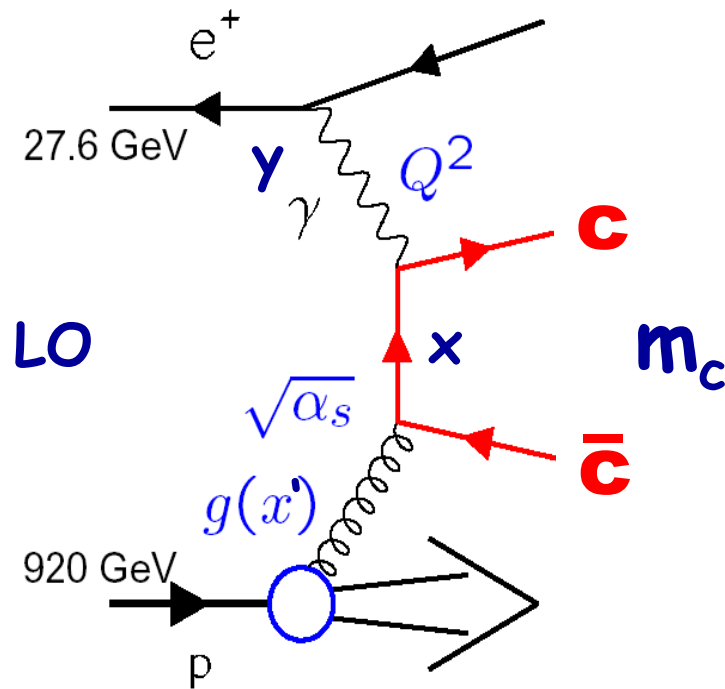


well described using  
HERAPDF1.5  
(fitted from inclusive  
DIS only)

strong charm mass  
dependence  
(blue band: 1.35  $\rightarrow$  1.6 GeV)

constrains PDFs,  
 $\rightarrow$  talk O. Zenaiev

# fixed flavour number scheme (FFNS)



+ NLO (+partial NNLO) corrections,

“natural” scale:  
 $Q^2 + 4m_c^2$

- no charm in proton
- full kinematical treatment of charm mass (multi-scale problem:  $Q^2, p_T, m_c \rightarrow$  logs of ratios)
- no resummation of logs



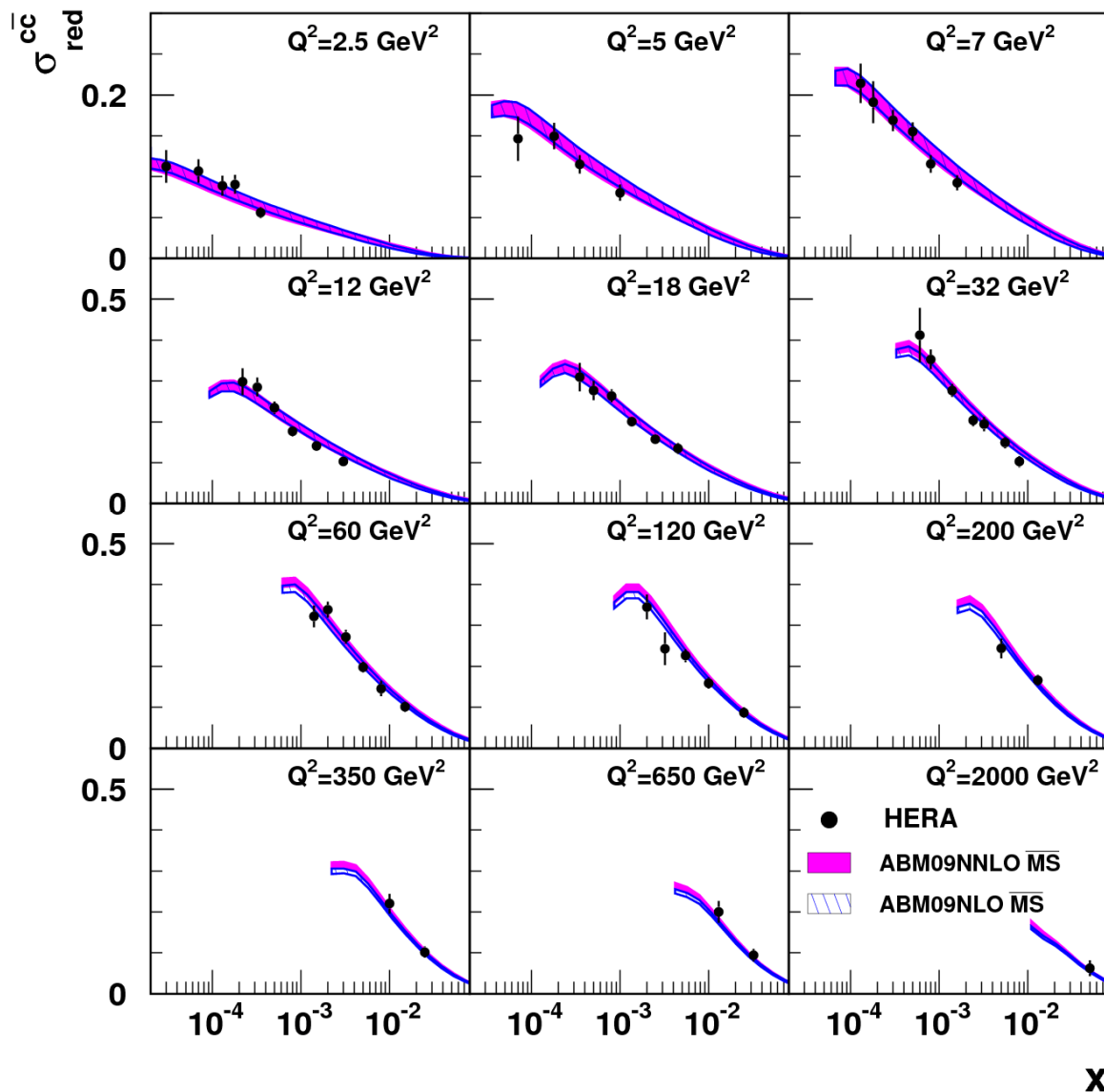


# comparison to ABM FFNS



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## H1 and ZEUS



very good description  
of data  
in full kinematic range

unambiguous treatment  
of  $m_c$  in all terms of  
calculation

here:  $\overline{\text{MS}}$  running mass

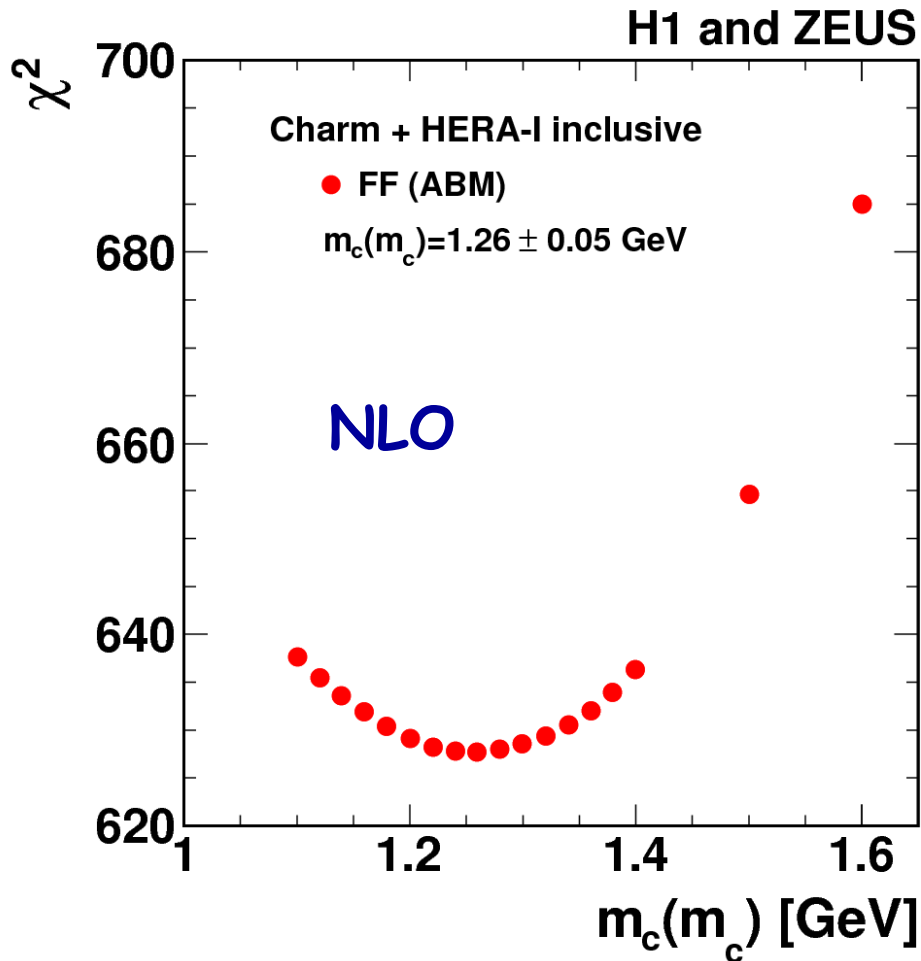
(similar predictions for  
pole mass)





# measurement of $\overline{MS}$ charm mass

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simultaneous fit of combined charm data and inclusive HERA I DIS data



$$m_c(m_c) = 1.26 \pm 0.05_{\text{exp}} \pm 0.03_{\text{mod}} \pm 0.02_{\alpha_s} \text{ GeV}$$

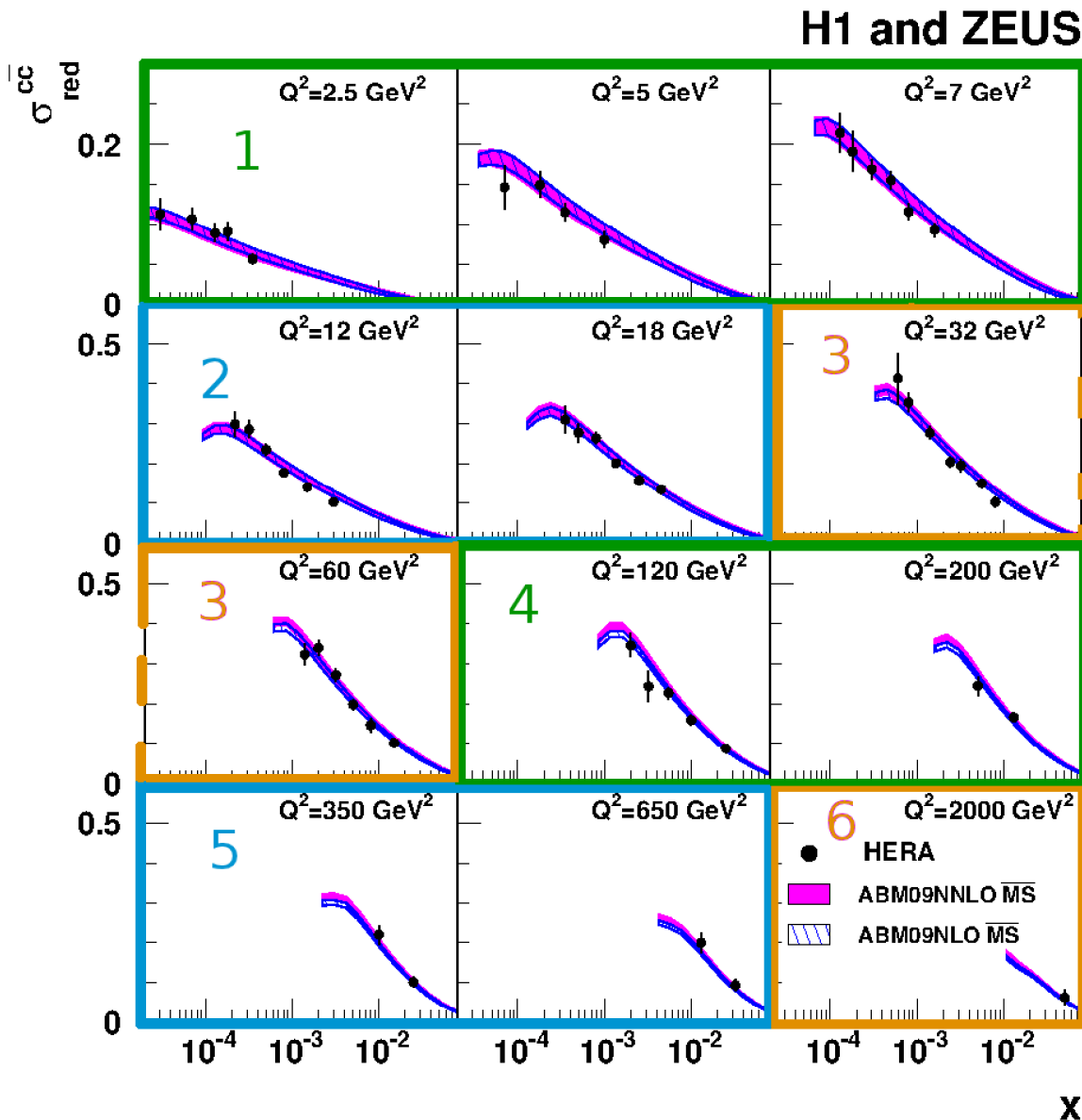
PDG:  $1.275 \pm 0.025 \text{ GeV}$  (lattice QCD + time-like processes)



# measurement of $m_c$ running



H1-prelim-14-071, ZEUS-prel-14-006, + S. Moch



**Step 1:**  
 extract  $m_c(m_c)$  separately  
 for 6 different kinematic  
 ranges in  $\mu^2 = Q^2 + 4m_c^2$

(take log average for central scale)



# $m_c$ fit and uncertainties



H1-prelim-14-071, ZEUS-prel-14-006, + S. Moch

use appropriate PDF set for each mass  
(from inclusive DIS data only),  
fit charm data

## Fit uncertainty

- Was estimated by taking  $\Delta\chi^2 = 1$  (dominant uncertainty)

## Parametrisation

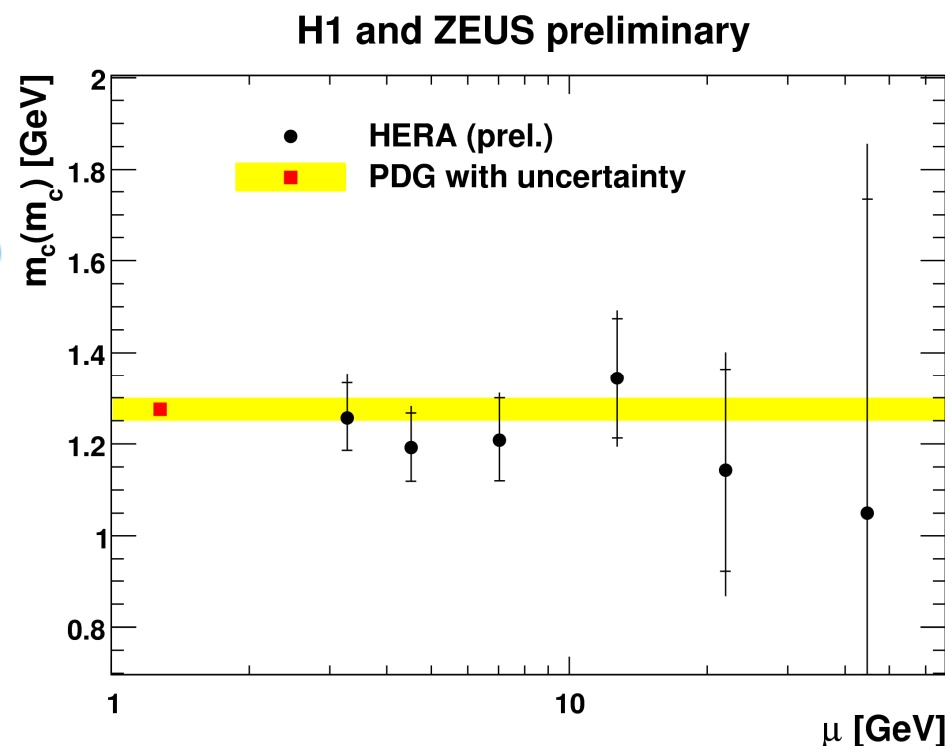
- Adding extra parameter in the PDF parametrisation

## Model uncertainty

- Variation of the strangeness suppression factor
- Lower cut on  $Q^2$  for inclusive data
- The evolution starting scale
- The b-quark mass

## Theory

- Variation of  $\alpha_s$
- Variation of the factorisation and renormalization scales of heavy quarks by factor 2 → outer error bar



sensitivity to  $m_c(m_c)$  decreases with increasing scale  $\mu^2 = Q^2 + 4m_c^2$

'in reality', have measured  $m_c(\mu)$  at each scale



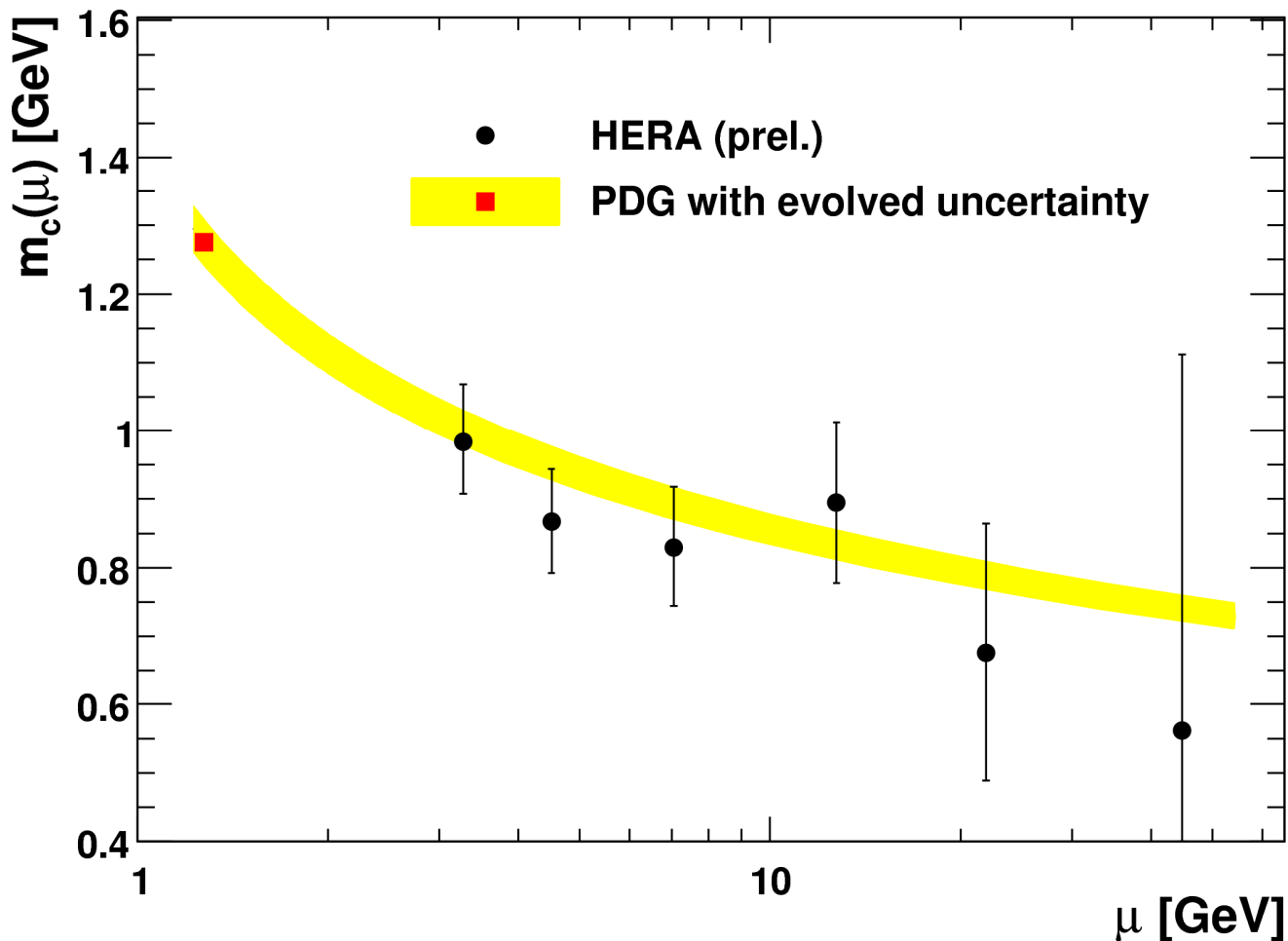
# the running charm quark mass



H1-prelim-14-071, ZEUS-prel-14-006, + S. Moch

translate back to  $m_c(\mu)$  using LO formula consistent with NLO  $\overline{MS}$  QCD fit (OpenQCDrad, Alekhin et al.)

## H1 and ZEUS preliminary



running mass  
concept in QCD  
is self-consistent !



# beauty in DIS at HERA



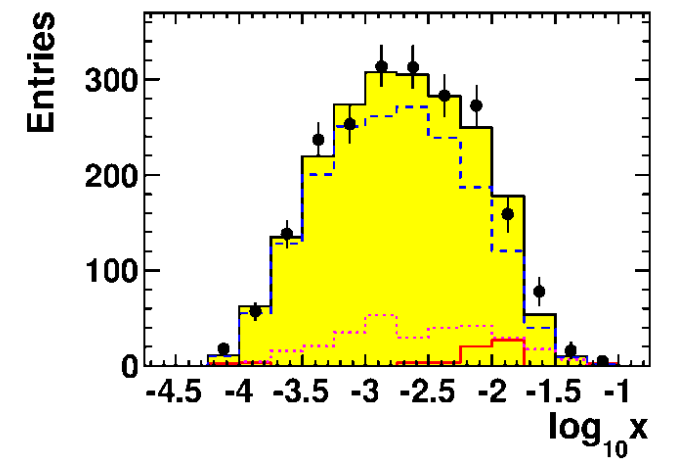
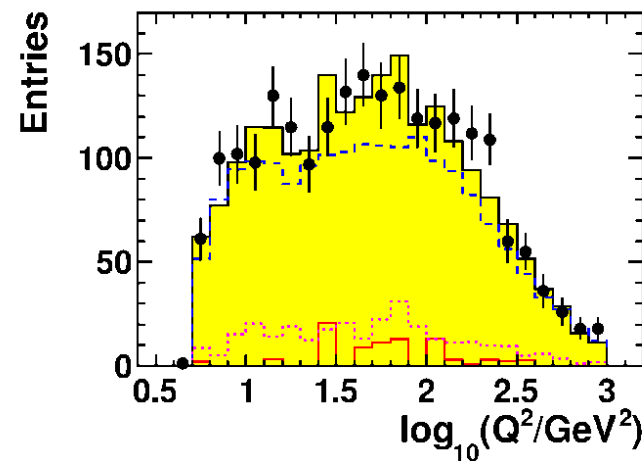
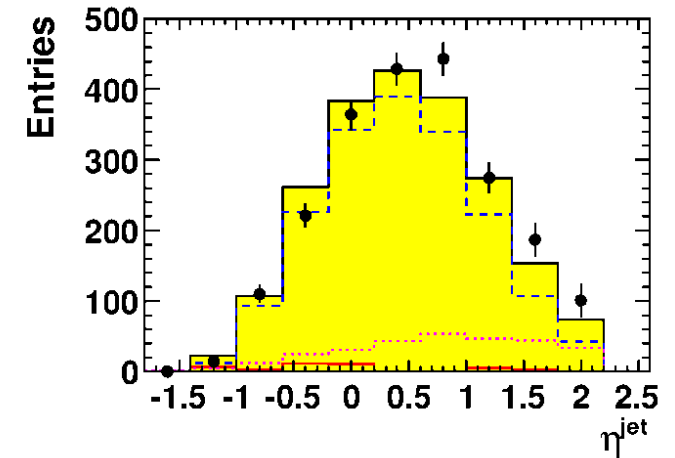
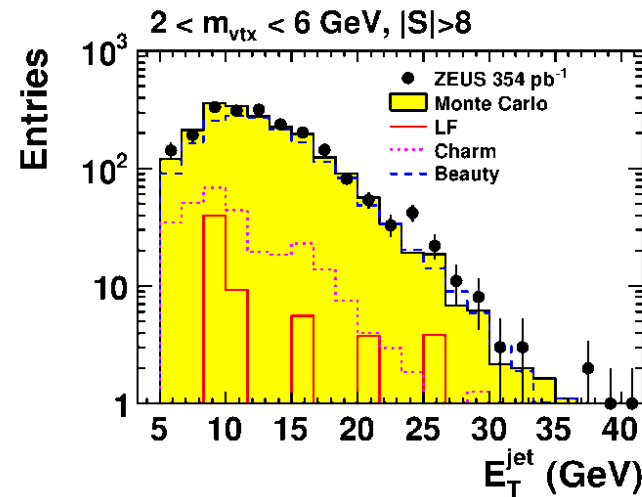
DESY-14-083

beauty cross section at HERA much smaller than charm,  
can use lifetime information (micro-vertex detector)

->  
beauty-enriched  
sample

(more in talk  
O. Zenaiev)

## ZEUS

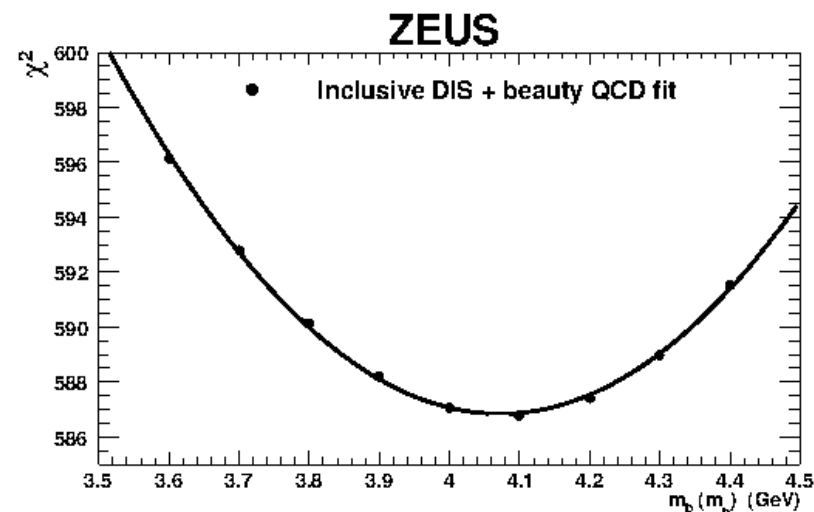
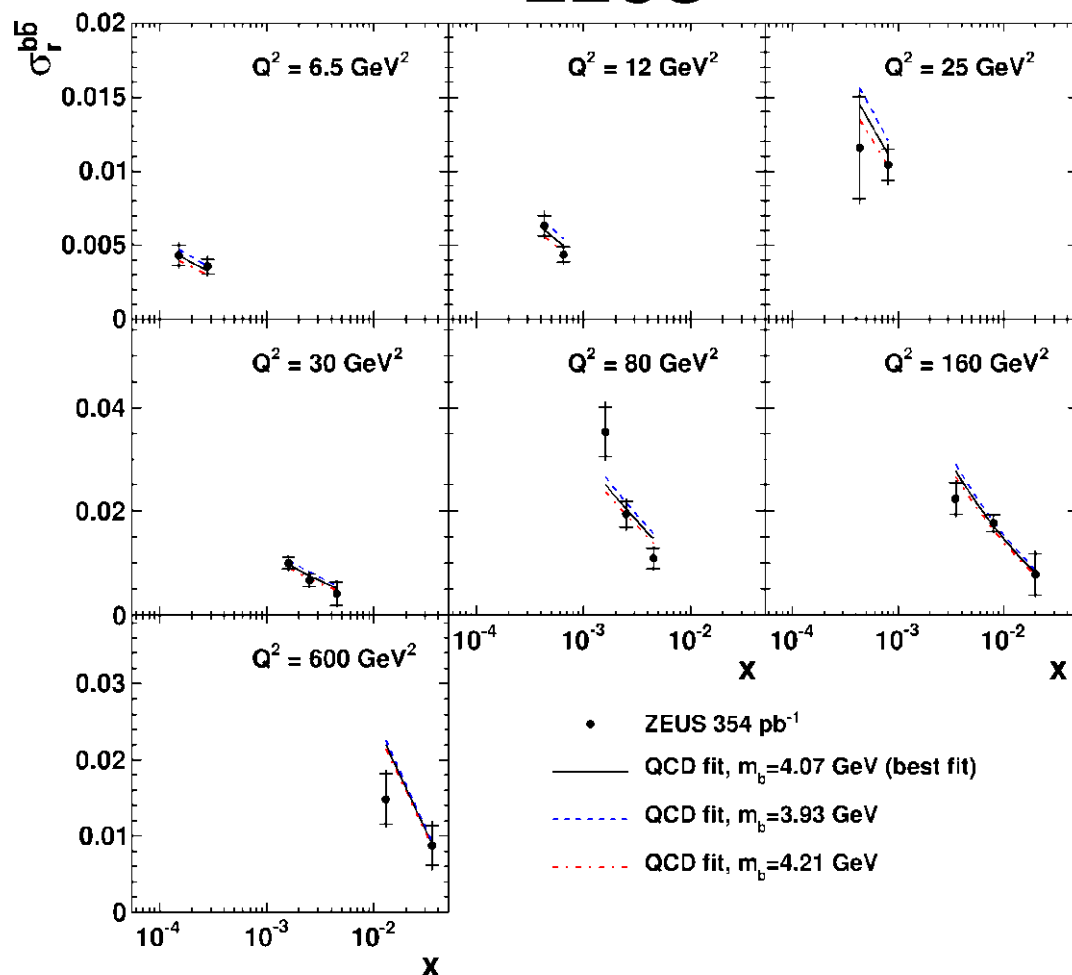




# $m_b$ from reduced beauty cross section

DESY-14-083

## ZEUS



ndf = 596

uncertainty evaluation  
similar to charm running case

$$m_b(m_b) = 4.07 \pm 0.14_{\text{fit}} \begin{matrix} +0.01 \\ -0.07 \end{matrix}_{\text{mod}} \begin{matrix} +0.05 \\ -0.00 \end{matrix}_{\text{par}} \begin{matrix} +0.08 \\ -0.05 \end{matrix}_{\text{th}} \text{ GeV}$$

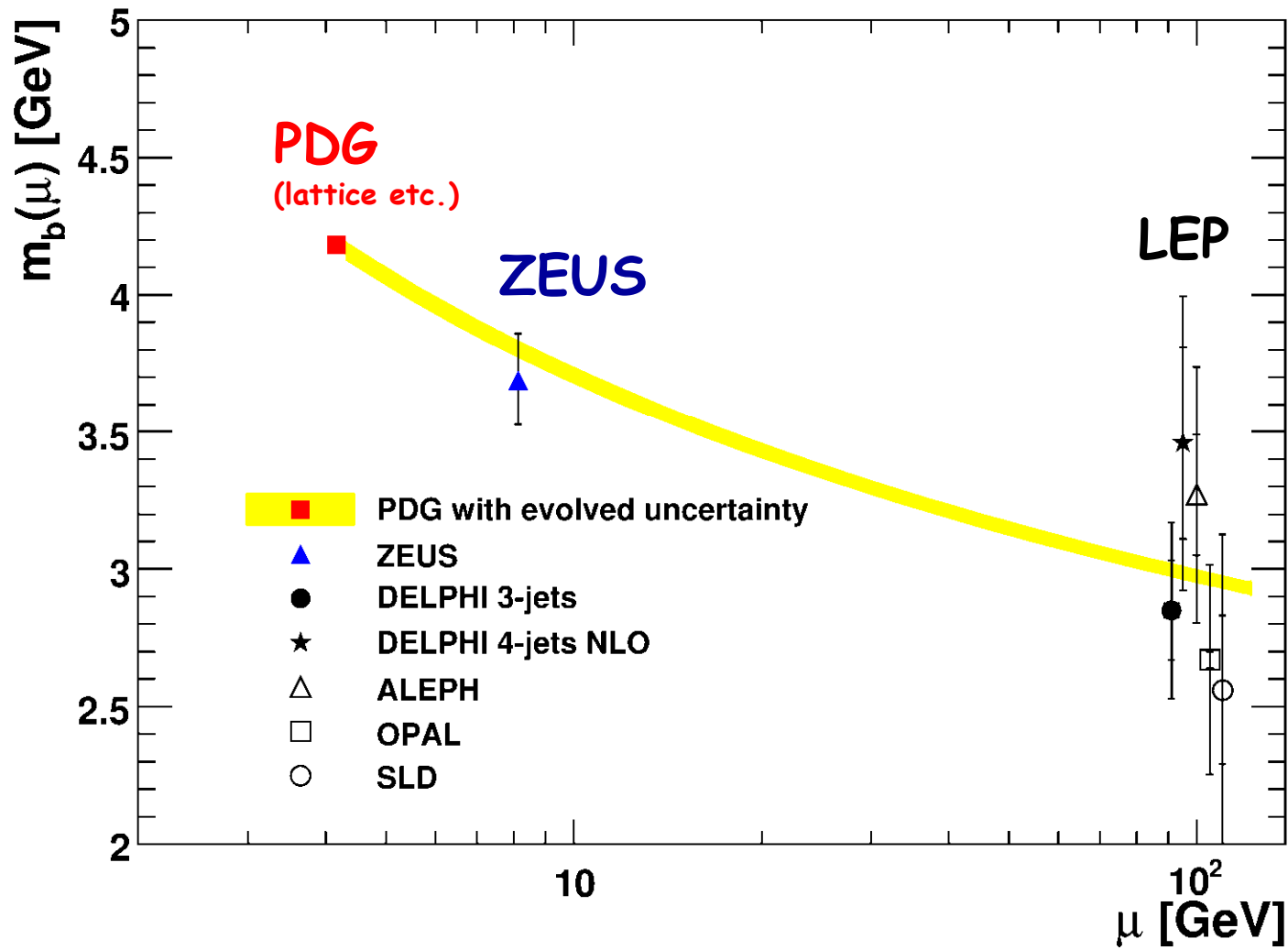
PDG:  $4.18 \pm 0.03$  GeV (lattice QCD + time-like processes)

# the running beauty quark mass



translate back to  $2m_b$

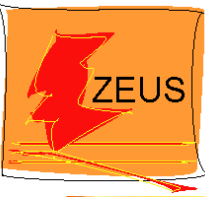
ZEUS



# Outlook

- so far, only HERA charm data have been combined; combination of beauty data could further improve b mass result, and constrain b mass running from HERA data
- $m_b/\sqrt{s}_{\text{HERA}} \sim m_t/\sqrt{s}_{\text{LHC}}$   
 $m_t$  has sizeable QCD+electroweak corrections  
 $m_c, m_b$  have QCD corrections only  
-> learn how to deal with QCD part of t quark mass running at LHC, and how to disentangle it from electroweak part ?
- reinterpret running of quark masses as running of corresponding Higgs Yukawa couplings !?





# Summary and conclusions



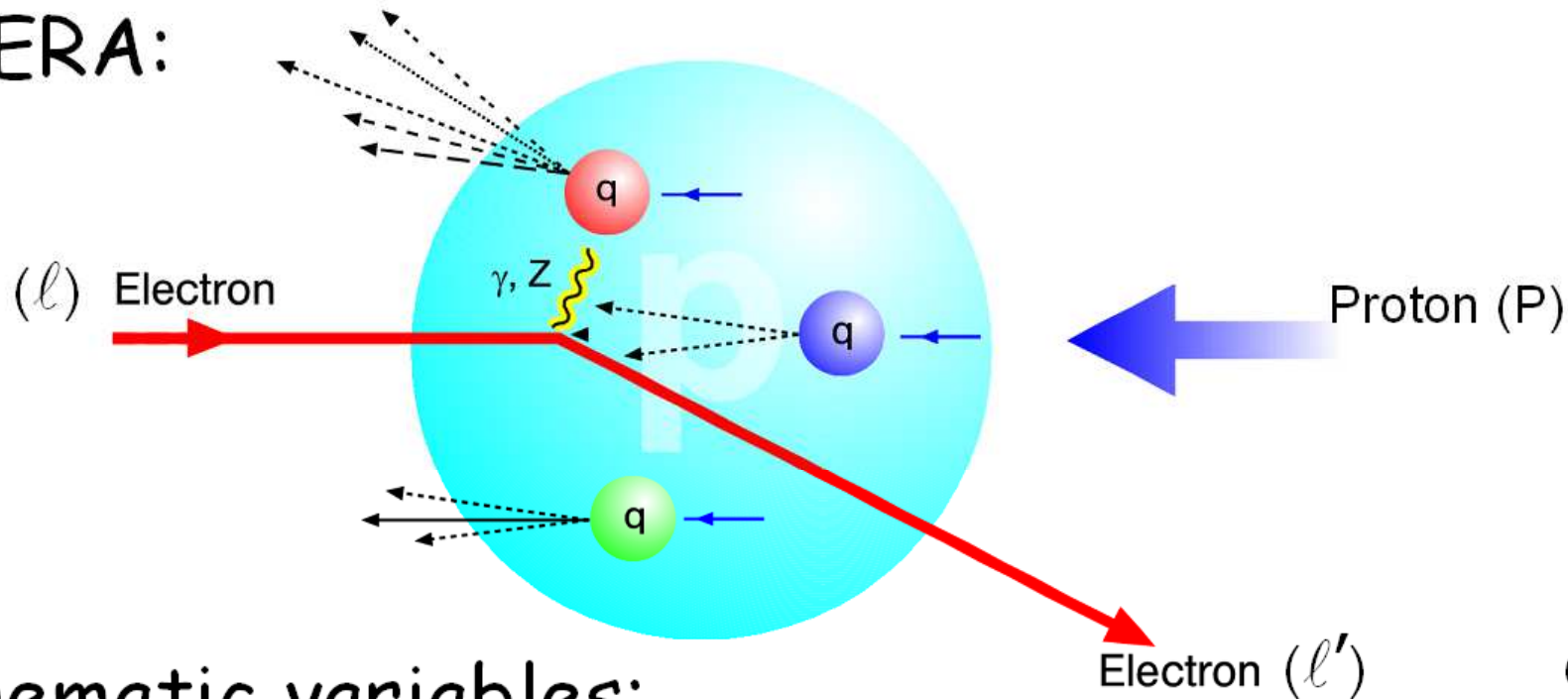
- HERA DIS charm data have been combined (except most recent, see talk O. Zenaiev)  
very good consistency, reduced uncertainties
- well-described by NLO QCD in FFNS  
-> **measure charm mass**  
$$m_c(m_c) = 1.26 \pm 0.05_{\text{exp}} \pm 0.03_{\text{mod}} \pm 0.02_{\alpha_s} \text{ GeV}$$
- split data into subsets spanning different scales  
-> **first measurement of charm mass running** (QCD consistency check)
- ZEUS DIS beauty data well described by NLO QCD  
-> **measure beauty mass**  
$$m_b(m_b) = 4.07 \pm 0.14_{\text{fit}} \begin{matrix} +0.01 \\ -0.07 \end{matrix}_{\text{mod}} \begin{matrix} +0.05 \\ -0.00 \end{matrix}_{\text{par}} \begin{matrix} +0.08 \\ -0.05 \end{matrix}_{\text{th}} \text{ GeV}$$
- compare to PDG and LEP  
-> **beauty mass running consistent with QCD**



# Backup

# Deep Inelastic ep Scattering at HERA

HERA:



kinematic variables:

$Q^2 = -q^2$	photon (or $Z$ ) virtuality, squared momentum transfer
$x = \frac{Q^2}{2Pq}$	Bjorken scaling variable, for $Q^2 \gg (2m_q)^2$ : momentum fraction of $p$ constituent
$y = \frac{qP}{lP}$	inelasticity, $\gamma$ momentum fraction (of $e$ )

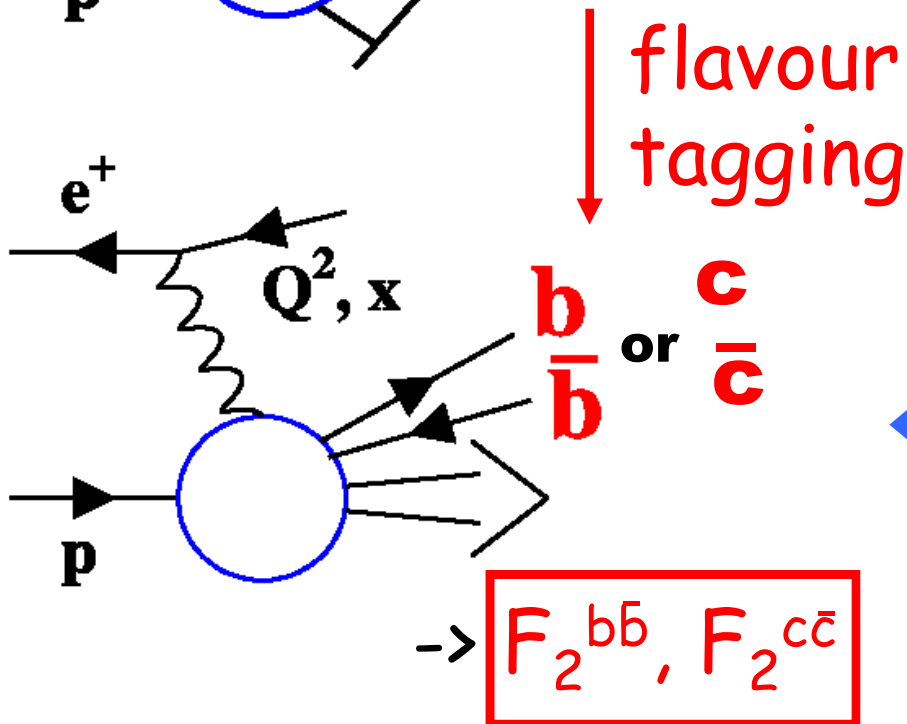
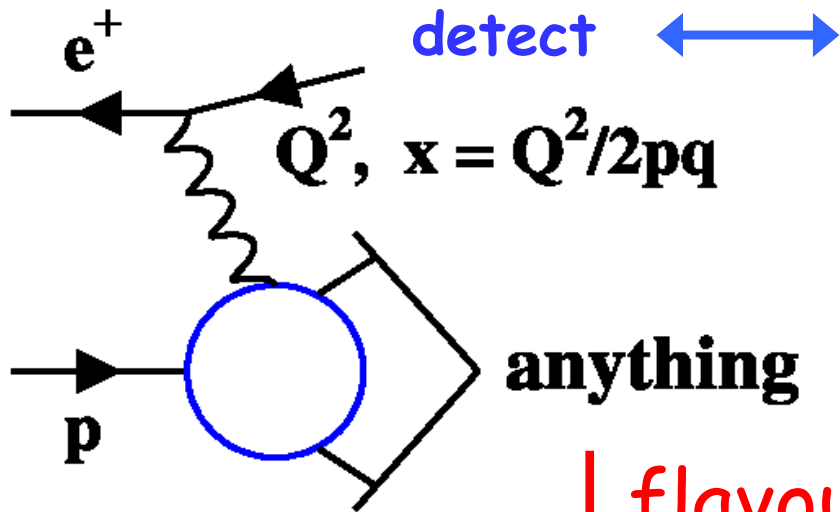
$Q^2 \lesssim 1 \text{ GeV}^2$ :  
photoproduction

$Q^2 \gtrsim 1 \text{ GeV}^2$ :  
DIS

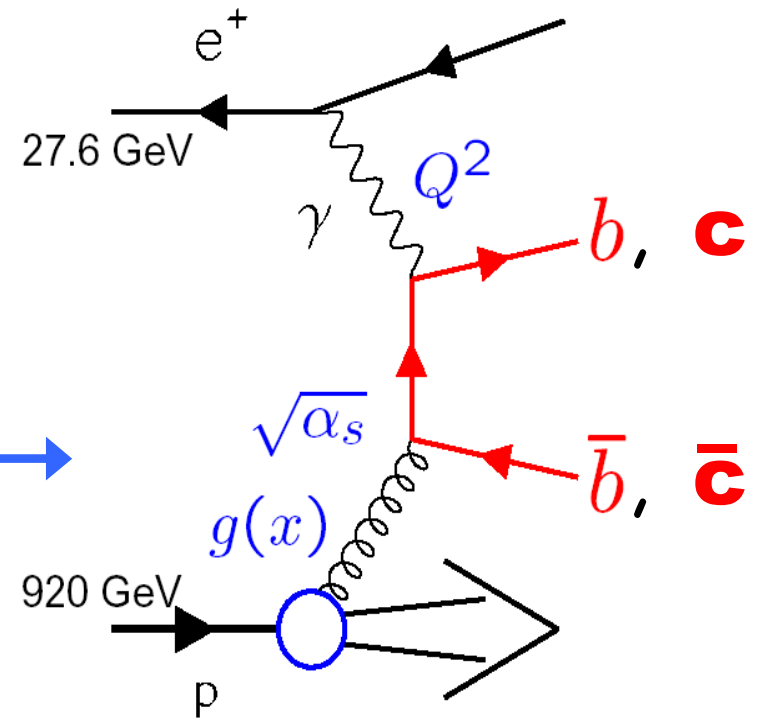
# Heavy flavour contributions to $F_2$

Measure cross section

$$\frac{d^2\sigma}{dx dQ^2} \approx \frac{2\pi\alpha^2}{Q^4 x} \left\{ \left[ 1 + (1-y)^2 \right] F_2(x, Q^2) \right\}$$



QCD





# Quark mass definitions

## Pole quark mass

- Based on (unphysical) concept of quark being a free parton
- Pole mass is ambiguous up to corrections of  $O(\Lambda_{QCD})$

## Running quark mass ( $\overline{MS}$ )

- $\overline{MS}$  (minimal subtraction scheme) mass definition  $m(\mu_R)$  realizes running mass (scale dependence)
- renormalization group equation (mass anomalous dimension  $\gamma$ )

$$\left( \mu_R^2 \frac{\delta}{\delta \mu_R^2} + \beta(\alpha_s) \frac{\delta}{\delta \alpha_s} \right) m(\mu_R) = \gamma(\alpha_s) m(\mu_R)$$

# Measurement of the charm quark mass running

From  $m_c(m_c)$  it was translated back to  $m_c(\mu)$  by 1-loop formula :

$$m_c(\mu) = m_c(m_c) \frac{\left(\frac{\alpha_s(\mu)}{\pi}\right)^{\frac{1}{\beta_0}}}{\left(\frac{\alpha_s(m_c)}{\pi}\right)^{\frac{1}{\beta_0}}}$$

Where  $\beta_0$  for  $N_f=3$  is  $\frac{9}{4}$

$$\mu = \sqrt{Q^2 + 4m_c^2},$$

This formula is the same that is used in the QCD fit (OpenQCDRad).

[arXiv:hep-ph/0004189]

$Q^2$  was chosen to be log average between  $Q^2$  of used bins

# Charm mass measurement

- $\chi^2$  mass scan had been performed by fitting charm data in FFNS ABM( $\overline{MS}$ ) scheme (OPENQCDRAD program) using HeraFitter package with following setup:
  - FFNS ABM (running mass)
  - Evolution starting scale set to  $Q_0=1.4 \text{ GeV}^2$
  - PDF parametrisation with 13 parameters
  - H12011  $\chi^2$  function definition
  - $\alpha_s(M_Z)=0.105$
  - Data below  $Q^2 = 3.5 \text{ GeV}^2$  removed
  - $m_b(m_b)$  was set to 4.75
  - Renormalization and factorization scale was set to  $\sqrt{Q^2 + 4m_q^2}$