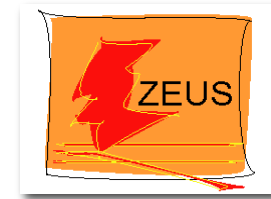




HERAPDF2.0 (prel.)

V. Radescu (DESY)

On behalf of H1 and ZEUS

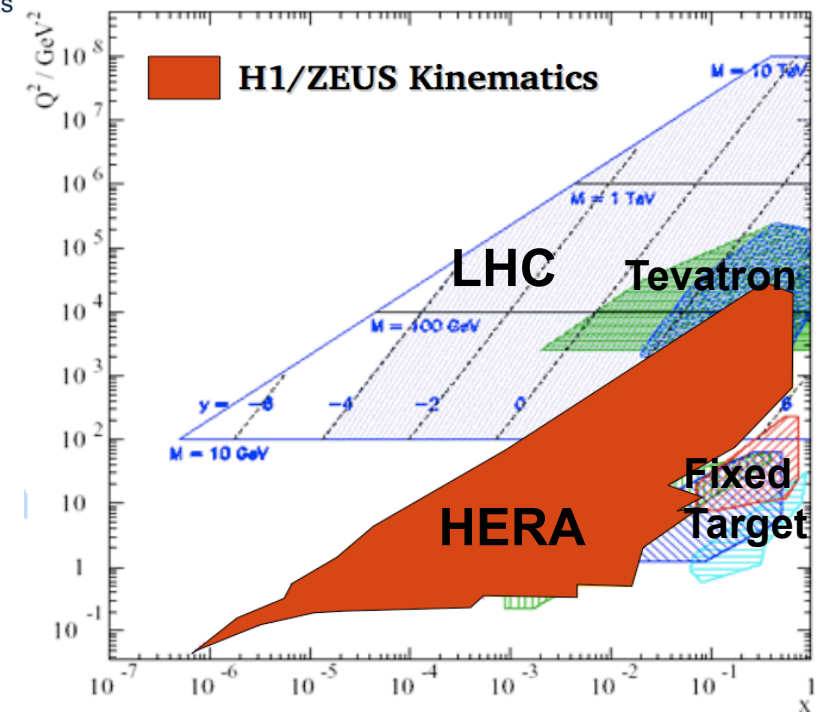


Warsaw, 28 April - 2 May 2014

XXII. International Workshop on Deep-Inelastic Scattering and
Related Subjects

Outline:

- HERAPDF analysis framework
 - QCD settings
 - PDF uncertainties
- Results and Comparison
- Summary

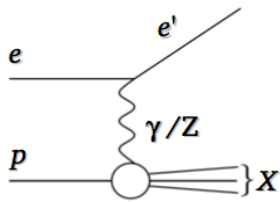


HERA at DESY

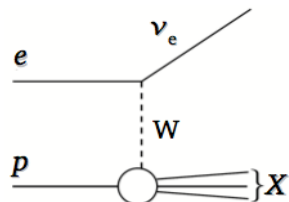
- ◆ HERA was world's only e^+p collider
 - ▶ located at DESY, Hamburg - Germany
 - ✧ In operation for 15 years (1992-2007)
 - ▶ H1 and ZEUS collider experiments
 - ✧ $\sim 1\text{fb}^{-1}$ of integrated luminosity of physics data.
- ◆ HERA provides unique opportunity to study the structure of the proton via DIS processes:



NC: $ep \rightarrow e'X$



CC: $ep \rightarrow \nu_e X$



o Kinematic variables:

o Virtuality of exchanged boson: $Q^2 = -q^2 = -(k - k')^2$

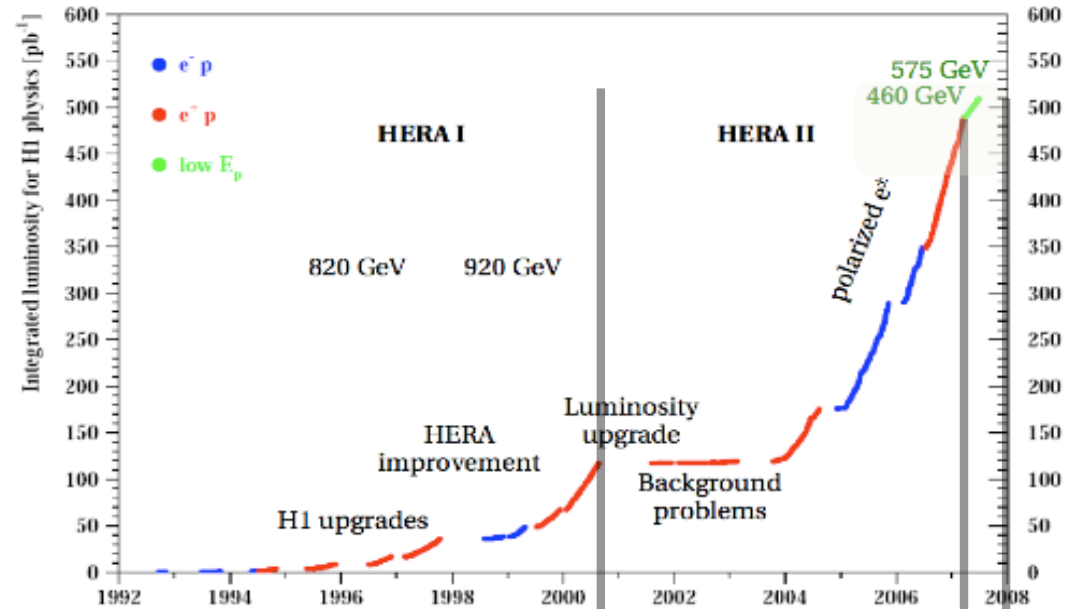
o Bjorken scaling variable:

$$x = \frac{Q^2}{2p \cdot q}$$

o Inelasticity:

$$y = \frac{p \cdot q}{p \cdot k}$$

o Invariant centre of mass: $s = (k + p)^2 = \frac{Q^2}{xy}$



HERAPDF1.0 ←

HERAPDF1.5prel [see Mandy's talk]

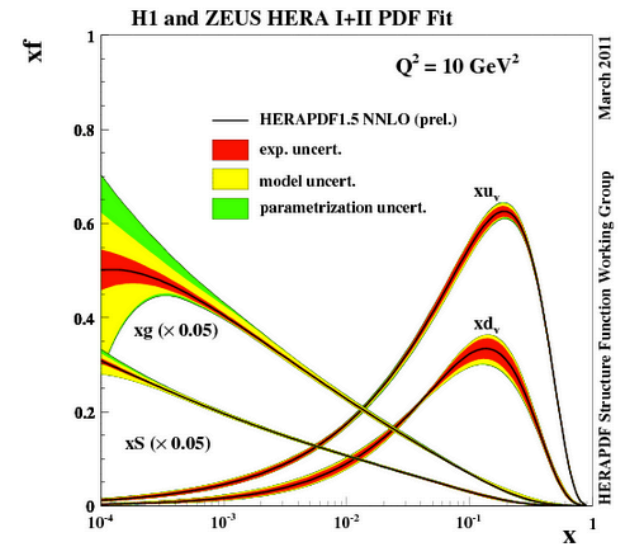
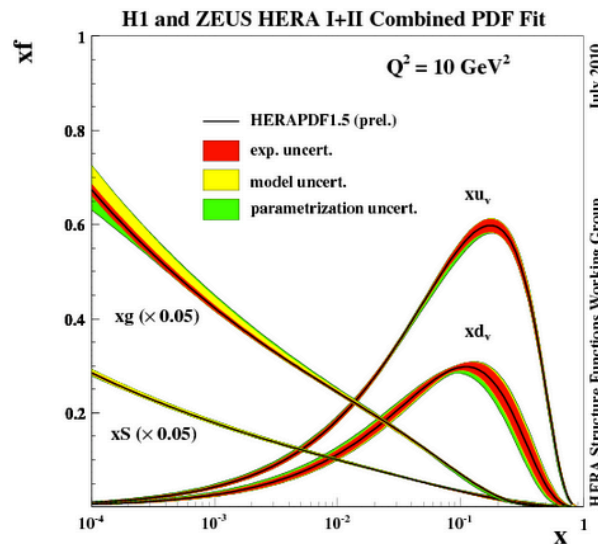
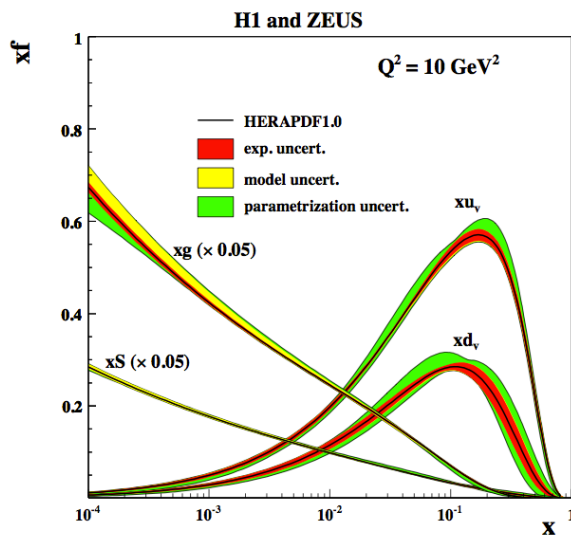
HERAPDF2.0prel → THIS TALK

HERA-I	1992-2000	$E_p=820,920$ GeV	$L \sim 0.1/\text{fb}$ per exp.
HERA-II	2003-2007	$E_p=920, 460, 575$ GeV	$L \sim 0.4/\text{fb}$ per exp.

Reminder of PDF sets from HERA

◆ Released to LHAPDF:

- ▶ HERAPDF1.0 NLO: based on published HERA I data (with All Uncertainties) [\[JHEP01 \(2010\) 109\]](#)
- ▶ HERAPDF1.5 NLO: based on preliminary HERA I+II data (with All Uncertainties) **RECOMMENDED**
- ▶ HERAPDF1.5 NNLO: based on preliminary HERA I+II data (with All Uncertainties) **RECOMMENDED**
- ▶ HERAPDF1.5 LO → see Mandy's talk



◆ Not released to LHAPDF:

- ▶ HERAPDF1.0 NNLO: based on published HERA I data (2 central lines with different alphas)
- ▶ HERAPDF1.6 NLO: based on preliminary HERA I+II and inclusive jets
- ▶ HERAPDF1.7 NLO: based on preliminary HERA I+II, inclusive jets, charm, low energy runs

New Data Combination from HERA

- ◆ New combination of HERA data using full set of inclusive measurements

[see O. Turkot's talk]

H1-prelim-14-042
ZEUS-prel-14-007

7 data sets with 165 sources of uncertainties

41 input files

```
HERA CC e+p 101 (920)
HERA CC e-p 102 (920)
HERA NC e-p 103 (920)
HERA NC e+p 104 (820)
HERA NC e+p 105 (920)
HERA NC e+p 106 (460)
HERA NC e+p 107 (575)
```

The preliminary HERA I+II combination is used as sole input in QCD fit platform to determine HERAPDF2.0

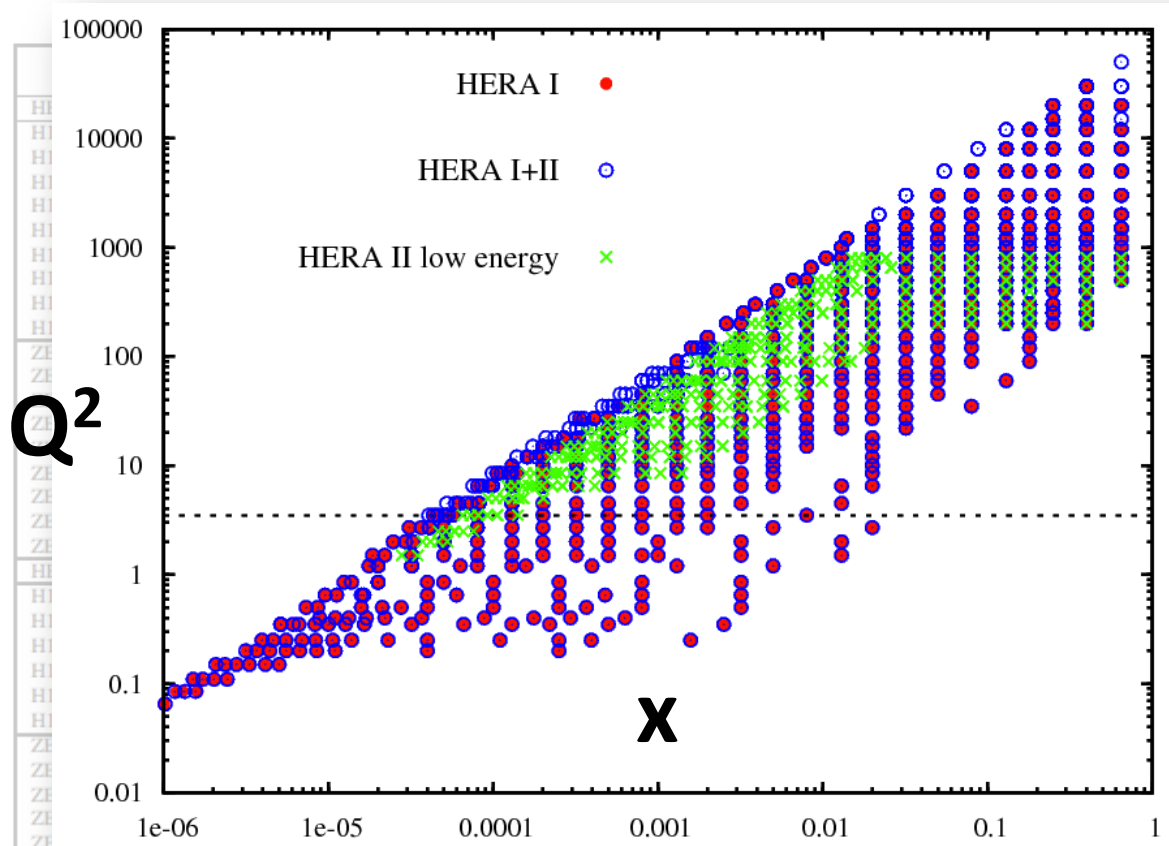
Data Set		x Grid		Q^2/GeV^2 Grid		\mathcal{L} pb ⁻¹	e^+/e^-	\sqrt{s} GeV
		from	to	from	to			
HERA I $E_p = 820$ GeV and $E_p = 920$ GeV data sets								
H1 svx-mb	95-00	0.000005	0.02	0.2	12	2.1	e^+p	301, 319
H1 low Q^2	96-00	0.0002	0.1	12	150	22	e^+p	301, 319
H1 NC	94-97	0.0032	0.65	150	30000	35.6	e^+p	301
H1 CC	94-97	0.013	0.40	300	15000	35.6	e^+p	301
H1 NC	98-99	0.0032	0.65	150	30000	16.4	e^-p	319
H1 CC	98-99	0.013	0.40	300	15000	16.4	e^-p	319
H1 NC HY	98-99	0.0013	0.01	100	800	16.4	e^-p	319
H1 NC	99-00	0.0013	0.65	100	30000	65.2	e^+p	319
H1 CC	99-00	0.013	0.40	300	15000	65.2	e^+p	319
ZEUS BPC	95	0.000002	0.00006	0.11	0.65	1.65	e^+p	300
ZEUS BPT	97	0.0000006	0.001	0.045	0.65	3.9	e^+p	300
ZEUS SVX	95	0.000012	0.0019	0.6	17	0.2	e^+p	300
ZEUS NC	96-97	0.00006	0.65	2.7	30000	30.0	e^+p	300
ZEUS CC	94-97	0.015	0.42	280	17000	47.7	e^+p	300
ZEUS NC	98-99	0.005	0.65	200	30000	15.9	e^-p	318
ZEUS CC	98-99	0.015	0.42	280	30000	16.4	e^-p	318
ZEUS NC	99-00	0.005	0.65	200	30000	63.2	e^+p	318
ZEUS CC	99-00	0.008	0.42	280	17000	60.9	e^+p	318
HERA II $E_p = 920$ GeV data sets								
H1 NC	03-07	0.0008	0.65	60	30000	182	e^+p	319
H1 CC	03-07	0.008	0.40	300	15000	182	e^+p	319
H1 NC	03-07	0.0008	0.65	60	50000	151.7	e^-p	319
H1 CC	03-07	0.008	0.40	300	30000	151.7	e^-p	319
H1 NC med Q^2 ^{*y.5}	03-07	0.0000986	0.005	8.5	90	182	e^+p	319
H1 NC low Q^2 ^{*y.5}	03-07	0.000029	0.00032	2.5	12	182	e^+p	319
ZEUS NC	06-07	0.005	0.65	200	30000	135.5	e^+p	318
ZEUS CC	06-07	0.0078	0.42	280	30000	132	e^+p	318
ZEUS NC	05-06	0.005	0.65	200	30000	169.9	e^-p	318
ZEUS CC	04-06	0.015	0.65	280	30000	175	e^-p	318
ZEUS NC nominal ^{*y}	06-07	0.000092	0.008343	7	110	44.5	e^+p	318
ZEUS NC satellite ^{*y}	06-07	0.000071	0.008343	5	110	44.5	e^+p	318
HERA II $E_p = 575$ GeV data sets								
H1 NC high Q^2	07	0.00065	0.65	35	800	17.2	e^+p	252
H1 NC low Q^2	07	0.0000279	0.0148	1.5	90	5.9	e^+p	252
ZEUS NC nominal	07	0.000147	0.013349	7	110	7.1	e^+p	251
ZEUS NC satellite	07	0.000125	0.013349	5	110	7.1	e^+p	251
HERA II $E_p = 460$ GeV data sets								
H1 NC high Q^2	07	0.00081	0.65	35	800	17.2	e^+p	225
H1 NC low Q^2	07	0.0000348	0.0148	1.5	90	12.2	e^+p	225
ZEUS NC nominal	07	0.000184	0.016686	7	110	13.9	e^+p	225
ZEUS NC satellite	07	0.000143	0.016686	5	110	13.9	e^+p	225

HERAPDF1.0

HERAPDF1.5

New Data Combination from HERA

- ◆ New combination of HERA data using the full set of inclusive measurements



sets with 165 sources of uncertainties

HERA	CC	e+p	101	(920)
HERA	CC	e-p	102	(920)
HERA	NC	e-p	103	(920)
HERA	NC	e+p	104	(820)
HERA	NC	e+p	105	(920)
HERA	NC	e+p	106	(460)
HERA	NC	e+p	107	(575)

ZEUS NC satellite	06-07	0.000071	0.008343	5	110	44.5	e^+p	318
HERA II $E_p = 575$ GeV data sets								
H1 NC high Q^2	07	0.00065	0.65	35	800	17.2	e^+p	252
H1 NC low Q^2	07	0.0000279	0.0148	1.5	90	5.9	e^+p	252
ZEUS NC nominal	07	0.000147	0.013349	7	110	7.1	e^+p	251
ZEUS NC satellite	07	0.000125	0.013349	5	110	7.1	e^+p	251
HERA II $E_p = 460$ GeV data sets								
H1 NC high Q^2	07	0.00081	0.65	35	800	17.2	e^+p	225
H1 NC low Q^2	07	0.0000348	0.0148	1.5	90	12.2	e^+p	225
ZEUS NC nominal	07	0.000184	0.016686	7	110	13.9	e^+p	225
ZEUS NC satellite	07	0.000143	0.016686	5	110	13.9	e^+p	225

The preliminary HERA I+II combination is used as a sole input in QCD fit platform to determine HERAPDF2.0 (prel)

High Q^2 NC Cross Sections

Neutral Current:

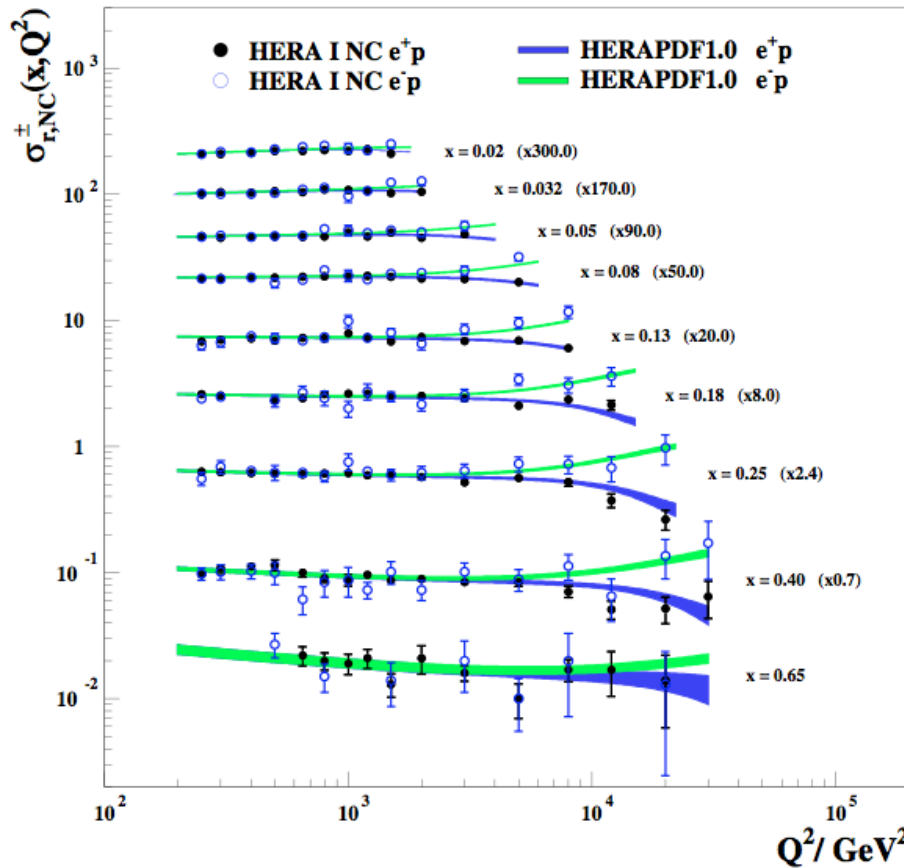
$$\sigma_r(x, Q^2) = \frac{d^2\sigma(e^\pm p)}{dx dQ^2} \frac{Q^4 x}{2\pi\alpha^2 Y_\pm} = F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2) \mp \frac{Y_-}{Y_+} xF_3(x, Q^2)$$

At High $Q^2 \Rightarrow$ interference term $Z\gamma \rightarrow xF_3$

$$Y_\pm = 1 \pm (1 - y^2)$$

HERAI only

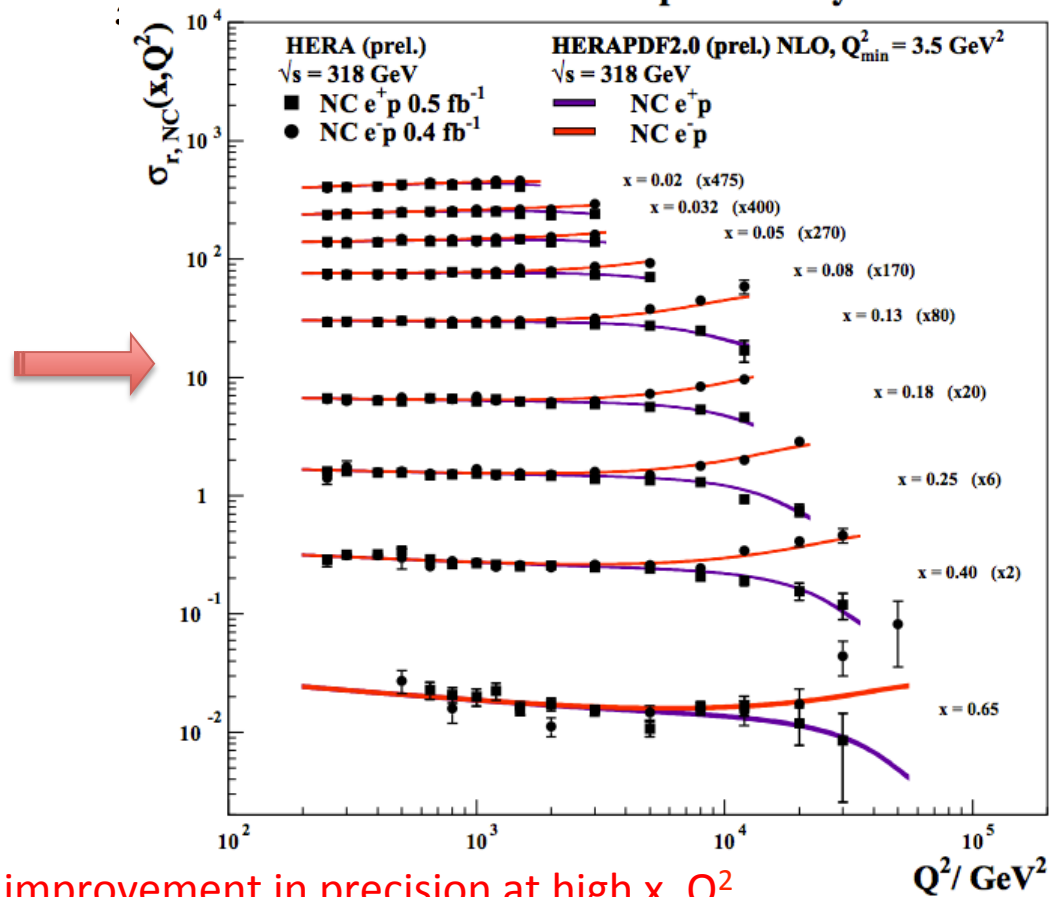
H1 and ZEUS



New HERAI+II

NC: $e p \rightarrow e' X$

H1 and ZEUS preliminary



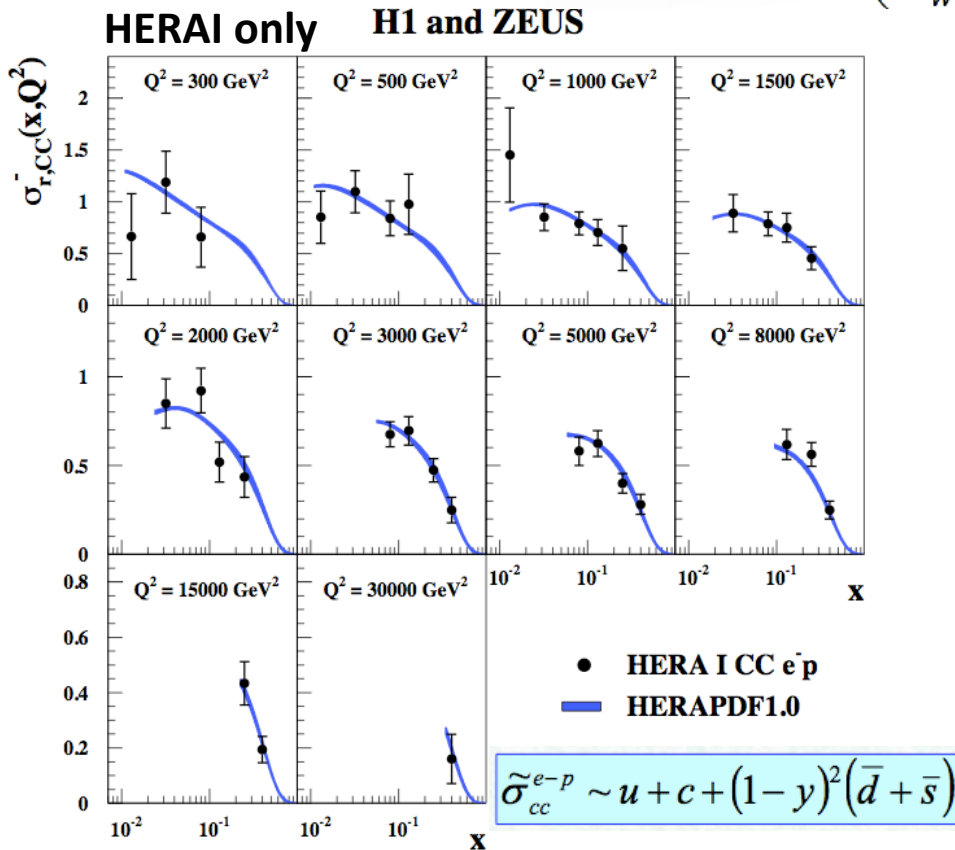
Larger HERA II luminosity yields in significant improvement in precision at high x, Q^2

High Q² CC cross sections

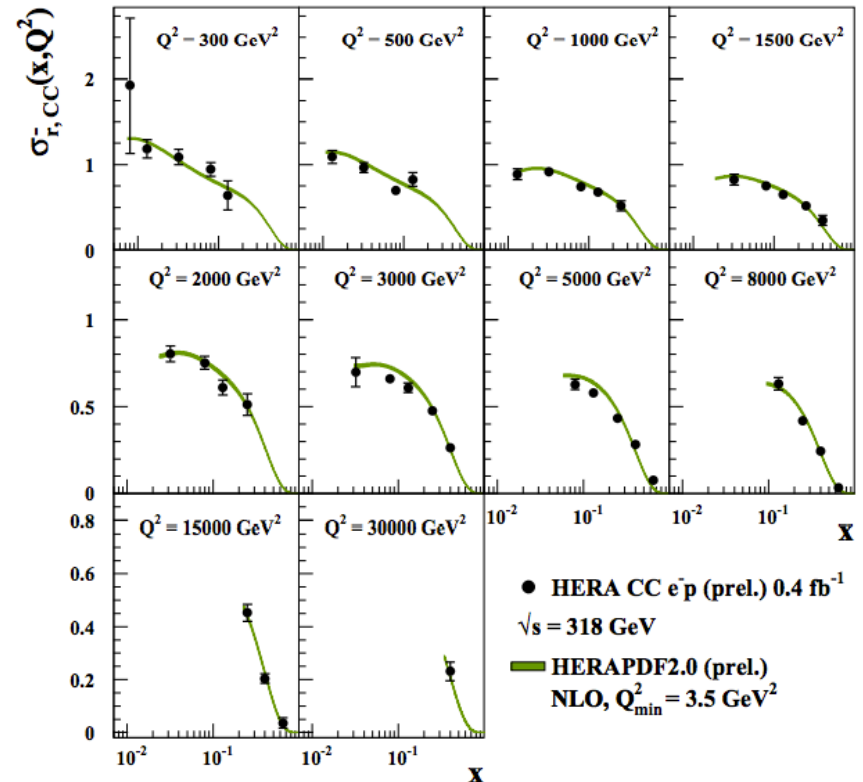
Charged Current: provides important flavour decomposition

$$e-p: \frac{d^2\sigma_{CC}^-}{dx dQ^2} = \frac{G_F^2}{2\pi} \left(\frac{M_W^2}{M_W^2 + Q^2} \right) [u + c + (1-y)^2(\bar{d} + \bar{s})]$$

$$e+p: \frac{d^2\sigma_{CC}^+}{dx dQ^2} = \frac{G_F^2}{2\pi} \left(\frac{M_W^2}{M_W^2 + Q^2} \right) [\bar{u} + \bar{c} + (1-y)^2(d + s)]$$



New HERAI+II H1 and ZEUS preliminary



Much more precise CC measurements after including new high Q² HERA II set!

QCD Settings for HERAPDF2.0

- ◆ The QCD settings are optimised for HERA measurements of proton structure functions

$$F_2(x, Q^2) = \frac{4}{9}(xU + x\bar{U}) + \frac{1}{9}(xD + x\bar{D}) \quad (\text{dominated by gamma exchange})$$

- ◆ PDFs are parametrised at the starting scale $Q_0^2=1.9 \text{ GeV}^2$ as follows:

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g},$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + D_{u_v} x + E_{u_v} x^2),$$

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x),$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$$

QCD Sum rules constrain
Normalisation parameters: A_g, A_{u_v}, A_{d_v}
And the condition that:

$$x\bar{u} \rightarrow x\bar{d} \text{ as } x \rightarrow 0.$$

relate $A_{\bar{U}}$ to $A_{\bar{D}}$, and with $x\bar{s} = f_s x\bar{D}$

- ▶ **Due to increased precision of data, more flexibility in functional form is allowed → 15 free parameters**

- ◆ PDFs are evolved via evolution equations (DGLAP) to NLO and NNLO ($\alpha_s(M_Z)=0.118$)[[QCDNUM](#)]
- ◆ Thorne-Roberts GM-VFNS for heavy quark coefficient functions – as used in MSTW
- ◆ Chi2 definition used in the minimisation [[MINUIT](#)] accounts for correlated uncertainties:

$$\chi^2 = \sum_i \frac{[\mu_i - m_i (1 - \sum_j \gamma_j^i b_j)]^2}{\delta_{i,\text{unc}}^2 m_i^2 + \delta_{i,\text{stat}}^2 \mu_i m_i (1 - \sum_j \gamma_j^i b_j)} + \sum_j b_j^2 + \sum_i \ln \frac{\delta_{i,\text{unc}}^2 m_i^2 + \delta_{i,\text{stat}}^2 \mu_i m_i}{\delta_{i,\text{unc}}^2 \mu_i^2 + \delta_{i,\text{stat}}^2 \mu_i^2}$$

m_i is the theoretical prediction

μ_i is the measured cross section

$\delta_{i,\text{stat}}, \delta_{i,\text{unc}}$ statistical and uncorrelated systematic uncertainty

γ_j^i correlated systematic uncertainties

b_j shifts

Sources of HERAPDF uncertainties

Experimental:

- ▶ Hessian method is used to evaluate experimental uncertainties
- ▶ Consistent data sets → use $\Delta\chi^2=1$

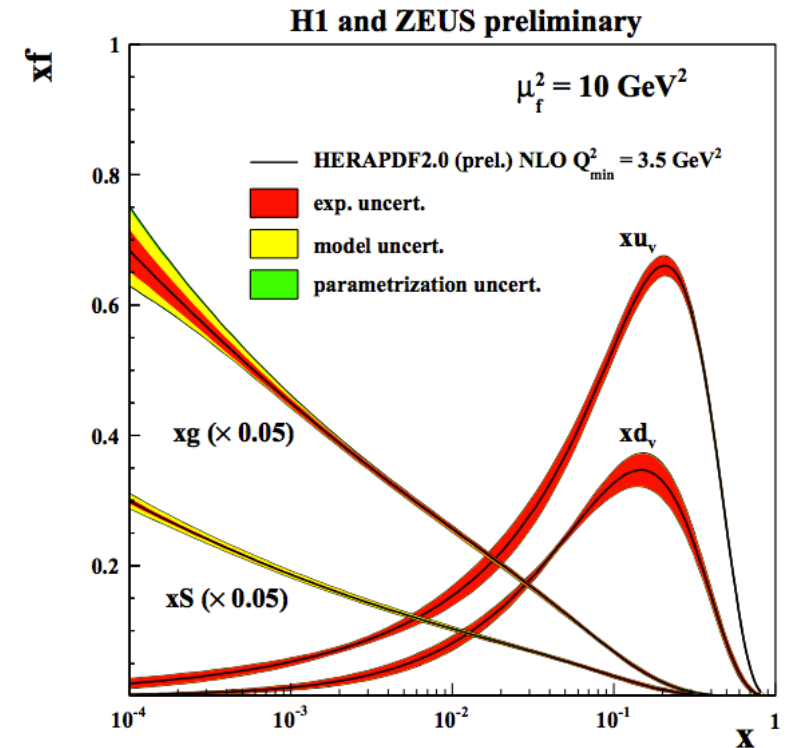
Model:

- ▶ Following variations have been considered

Variation	Standard Value	Lower Limit	Upper Limit
f_s	<u>0.4</u>	0.3	0.5
M_c^{opt} (NLO) [GeV]	1.47	1.41	1.53
M_c^{opt} (NNLO) [GeV]	1.44	1.38	1.50
M_b [GeV]	4.75	4.5	5.0
Q_{min}^2 [GeV ²]	10.0	7.5	12.5
Q_{min}^2 [GeV ²]	3.5	2.5	5.0
Q_0^2 [GeV ²]	1.9	1.6	2.2

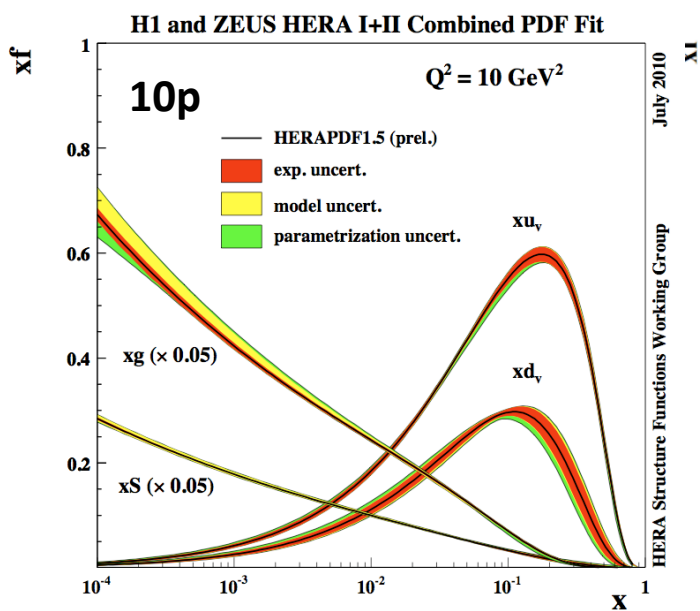
Parametrisation:

- ▶ An envelope is formed from PDF fits using variants of parametrisation form
 - ✦ Scanning of 16 parameter space with D or E as extra parameters of $(1 + Dx + Ex^2)$
 - ✦ Q_0^2 variation → dominant parametrisation uncertainty

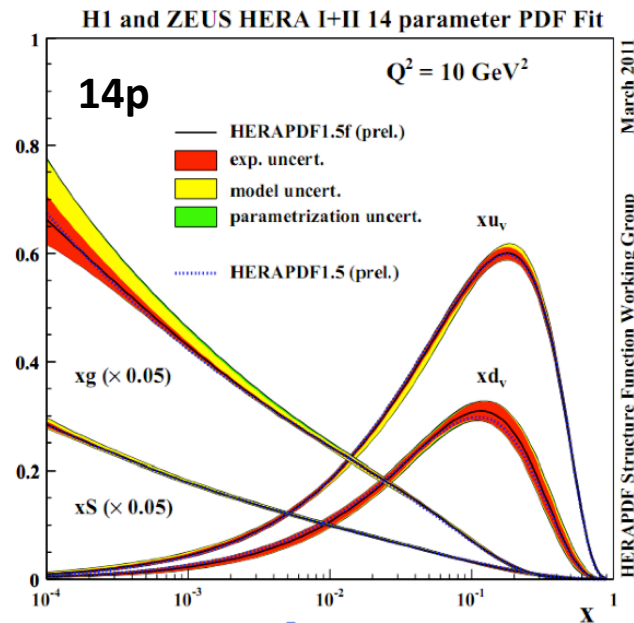


HERAPDF1.5 vs HERAPDF2.0 with $Q_{\min}^2 = 3.5 \text{ GeV}^2$

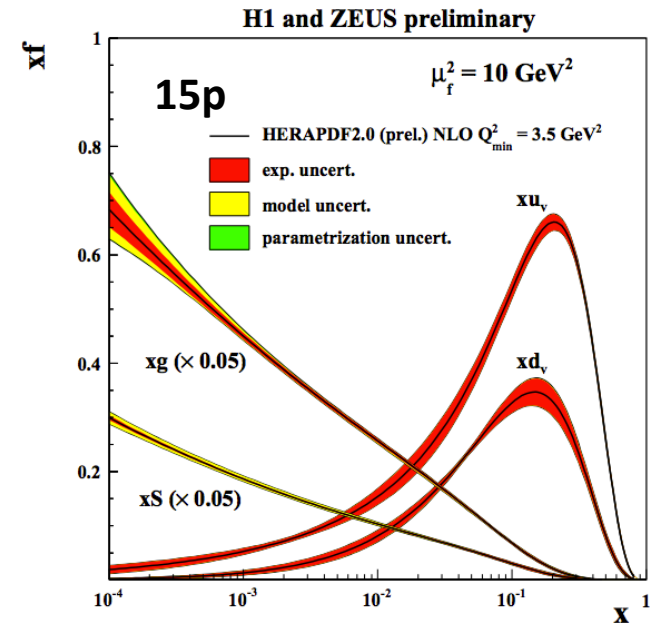
HERAPDF1.5-NLO(10p) \longrightarrow HERAPDF1.5-NLOf(14p) \longrightarrow HERAPDF2.0-NLO (15p)



We started with similar settings as used for HERAPDF1.0 (10 free parameters)



preliminary HERA II data
 Required additional flexibility (14 free parameters)

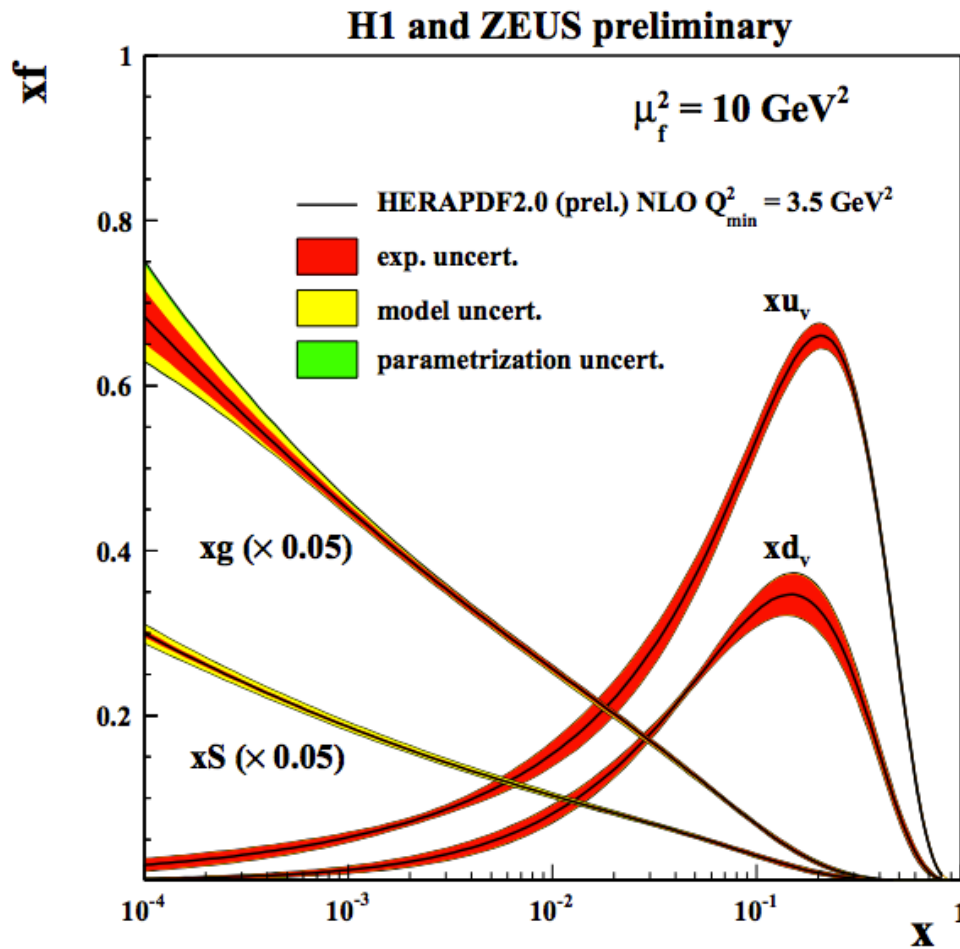


New HERA I+II combination (15 free parameters)

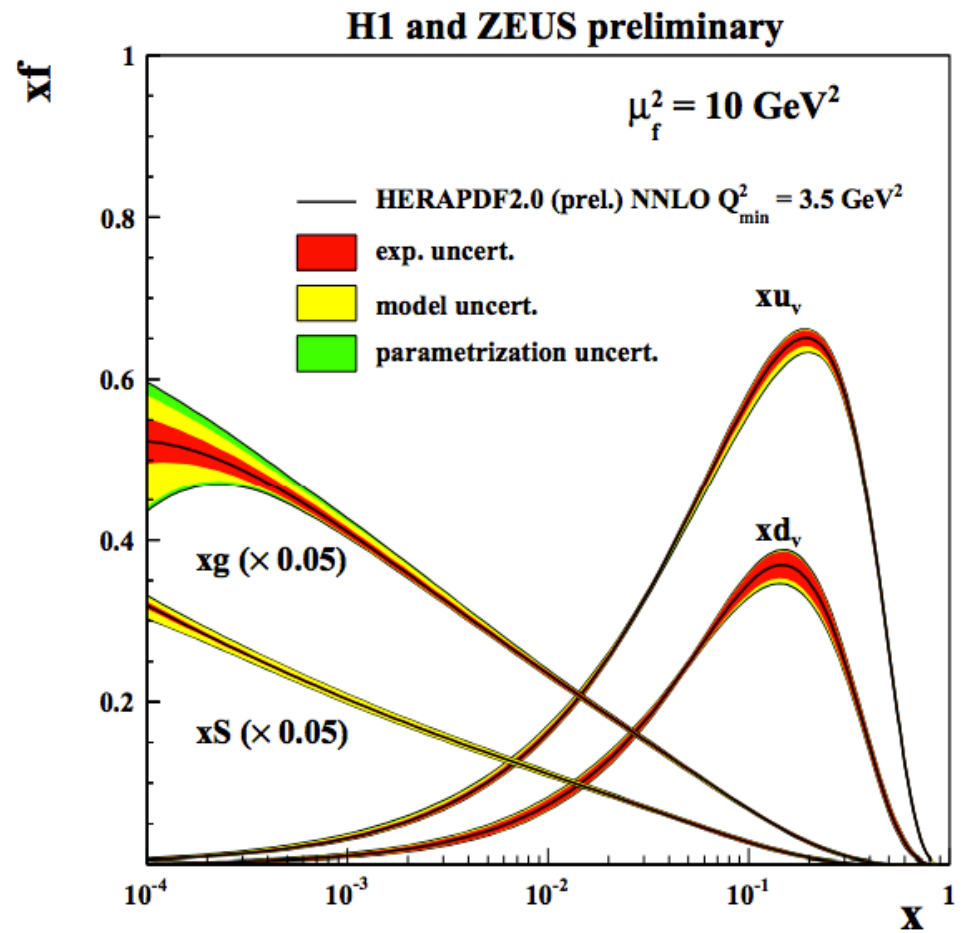
HERAPDF2.0 with $Q_{\min}^2 = 3.5 \text{ GeV}^2$ NLO vs NNLO

At NLO

At NNLO



Chi2/dof = 1386/1130

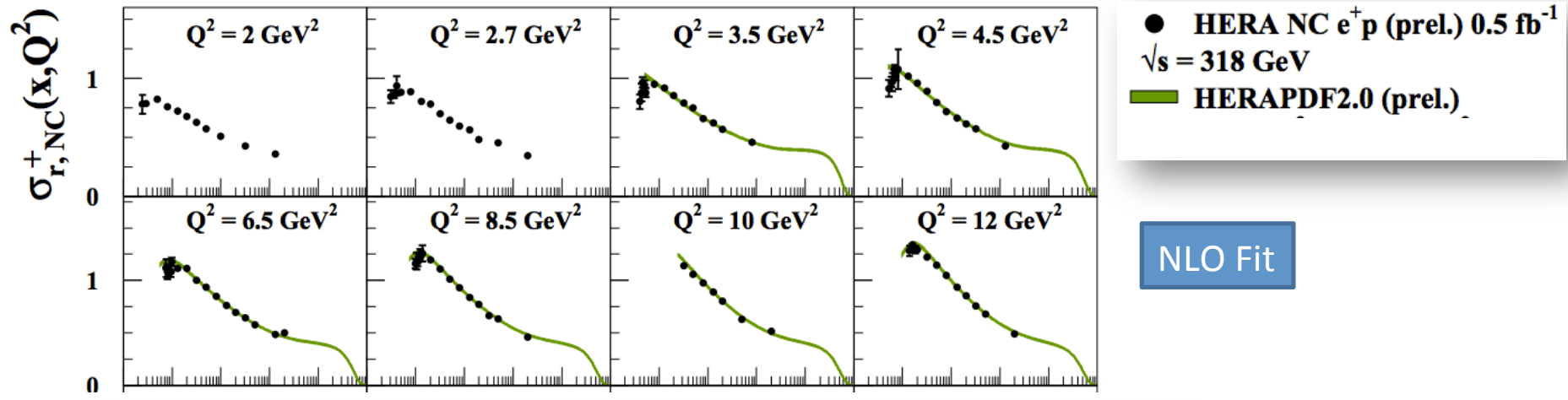


Chi2/dof = 1414/1130

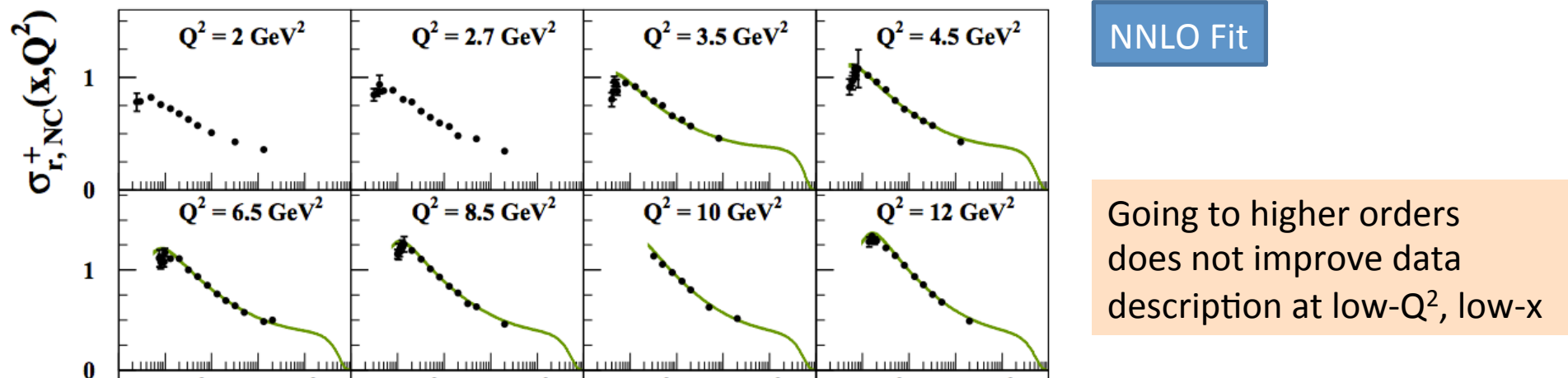
Low Q^2 Data vs HERAPDF2.0 ($Q^2_{\min}=3.5 \text{ GeV}^2$)

- ◆ How does fit at NLO and NNLO describe the low Q^2 data?

H1 and ZEUS preliminary



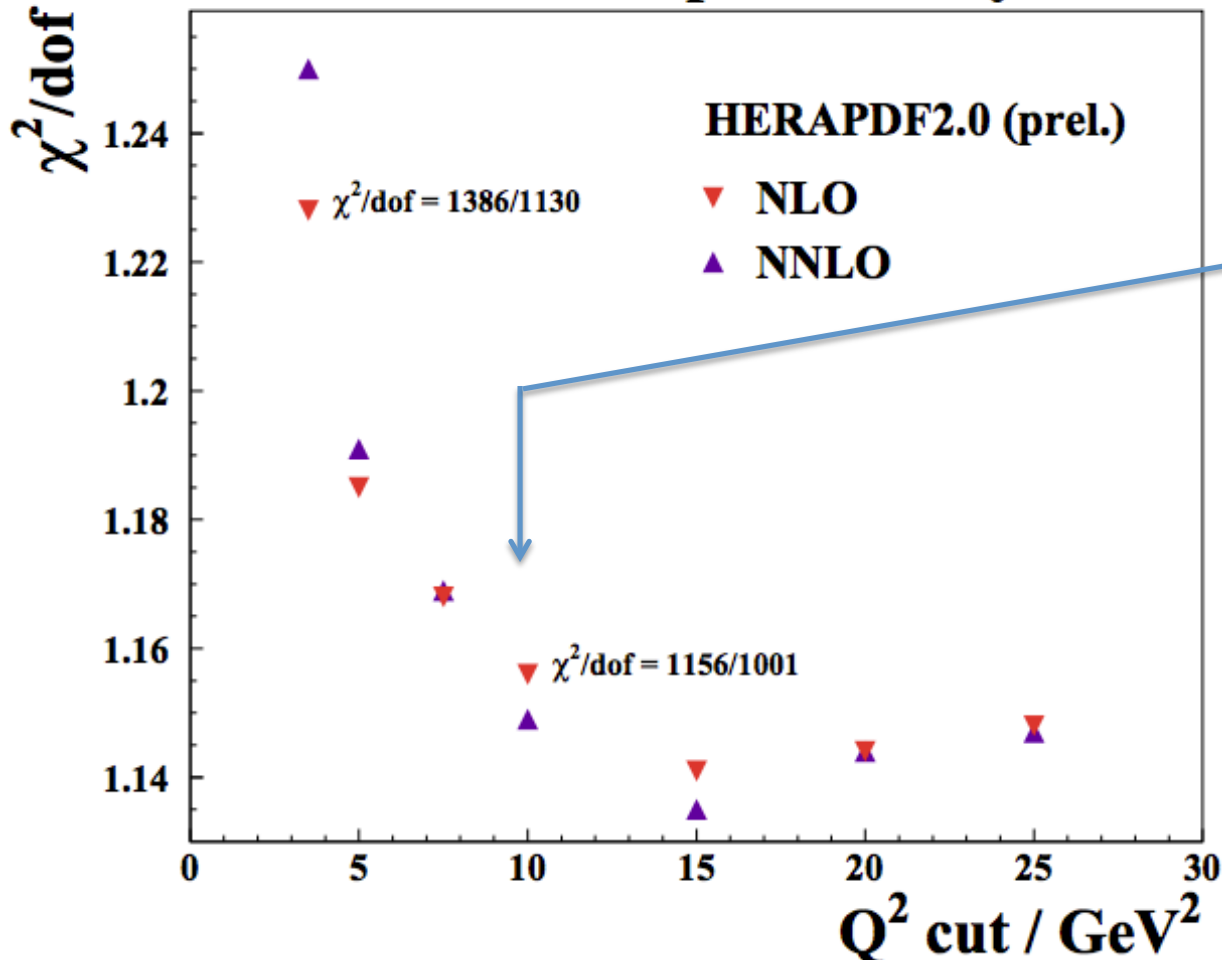
H1 and ZEUS preliminary



Q² cut dependence on fit results

- ◆ The Q² cut dependence on the fit is already included in the model variation for the HERAPDF sets, however usually we look at small range in cuts when assessing an uncertainty to Q²_{min} choice.

H1 and ZEUS preliminary



At Q²_{min} = 10 is when the fit stabilises with respect of chi2/dof vs Q²cut

For Q²_{min} = 3.5 GeV²

Chi2/dof (NLO) = 1386/1130

Chi2/dof(NNLO)= 1414/1130

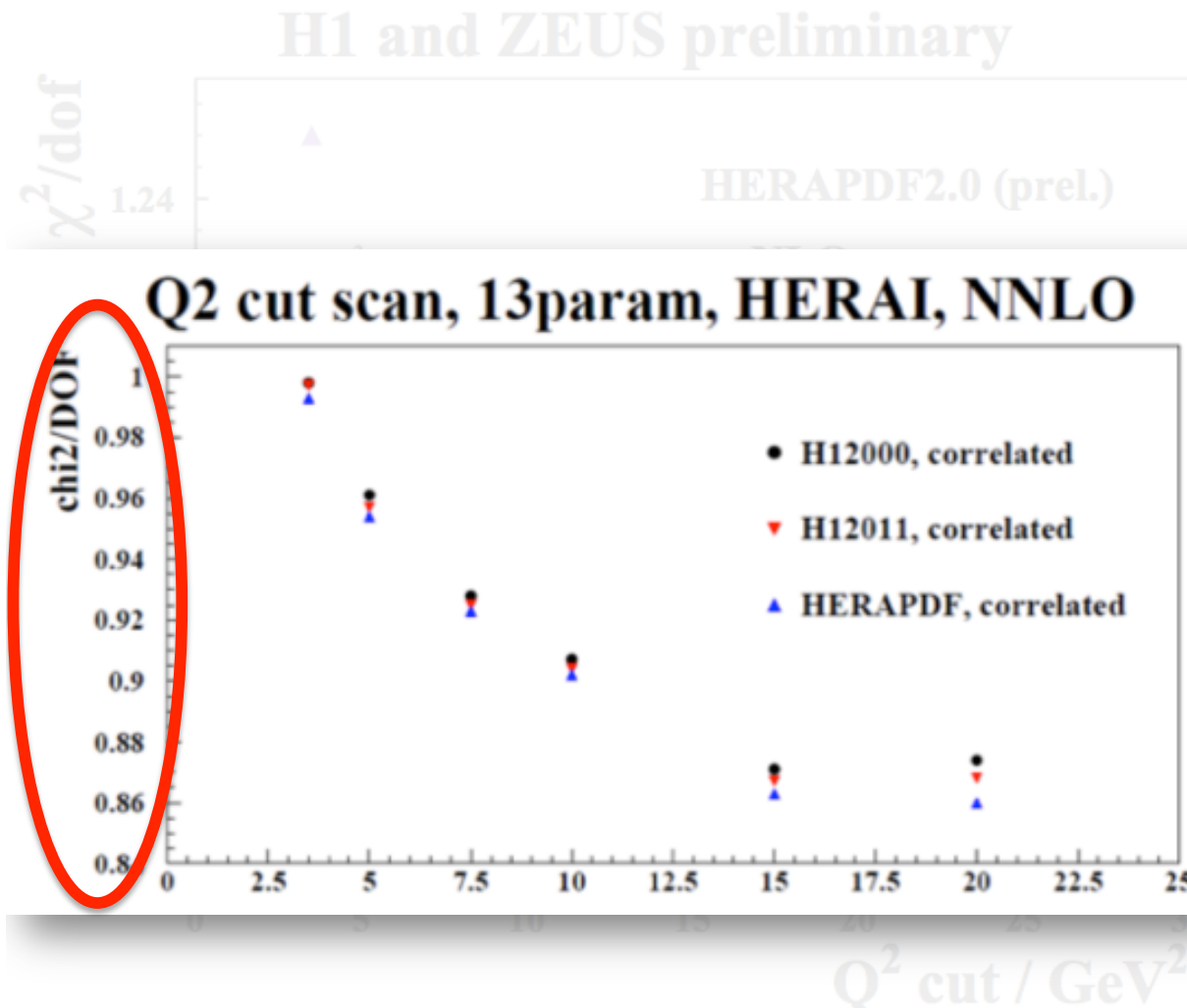
For Q²_{min} = 10 GeV²

Chi2/dof (NLO) = 1156/1001

Chi2/dof(NNLO)= 1150/1001

Q^2 cut dependence on fit results

- ◆ The Q^2 cut dependence on the fit is already included in the model variation for the HERAPDF sets, however usually we look at small range in cuts.



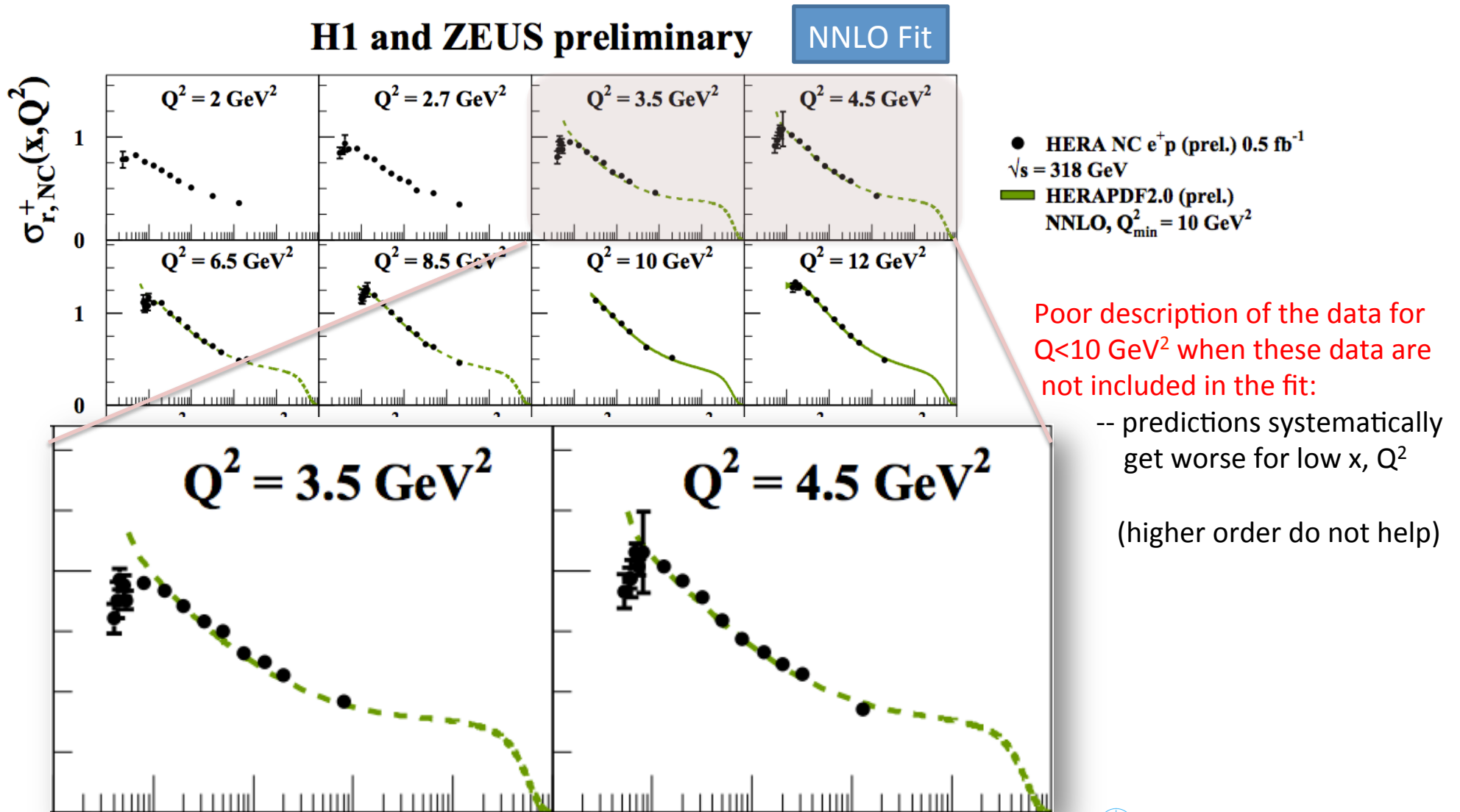
At $Q^2_{\text{min}} = 10 \text{ GeV}^2$ is when the fit stabilises with respect of χ^2/dof vs Q^2 cut

This was the case also for HERA I, but due to less precise high Q^2 data, was hidden in terms on χ^2/dof

(different symbols represent different forms for χ^2 definitions)

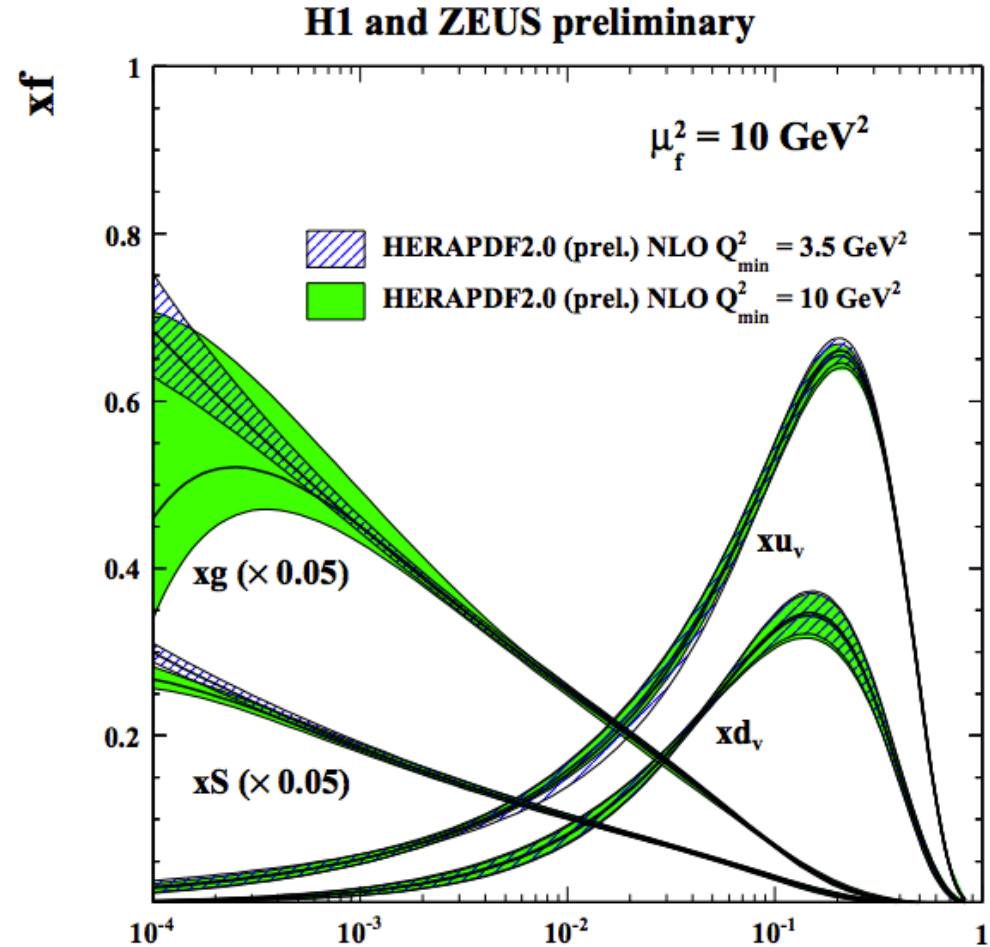
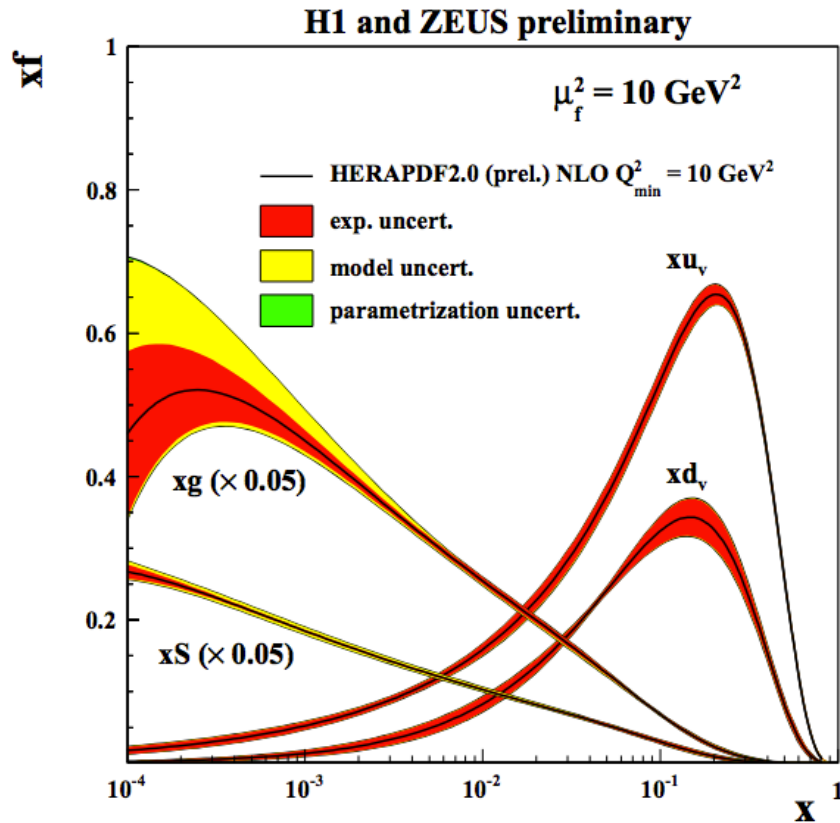
Low Q^2 Data vs HERAPDF2.0 ($Q^2_{\min}=10 \text{ GeV}^2$)

- ◆ How does fit performed with $Q^2_{\min}=10 \text{ GeV}^2$ describe the low Q^2 data?



HERAPDF2.0 with $Q_{\min}^2 = 3.5 \text{ GeV}^2$ vs $Q_{\min}^2 = 10 \text{ GeV}^2$ @ NLO

- ◆ How do PDFs compare between these 2 scenarios of Q_{\min}^2 choices?

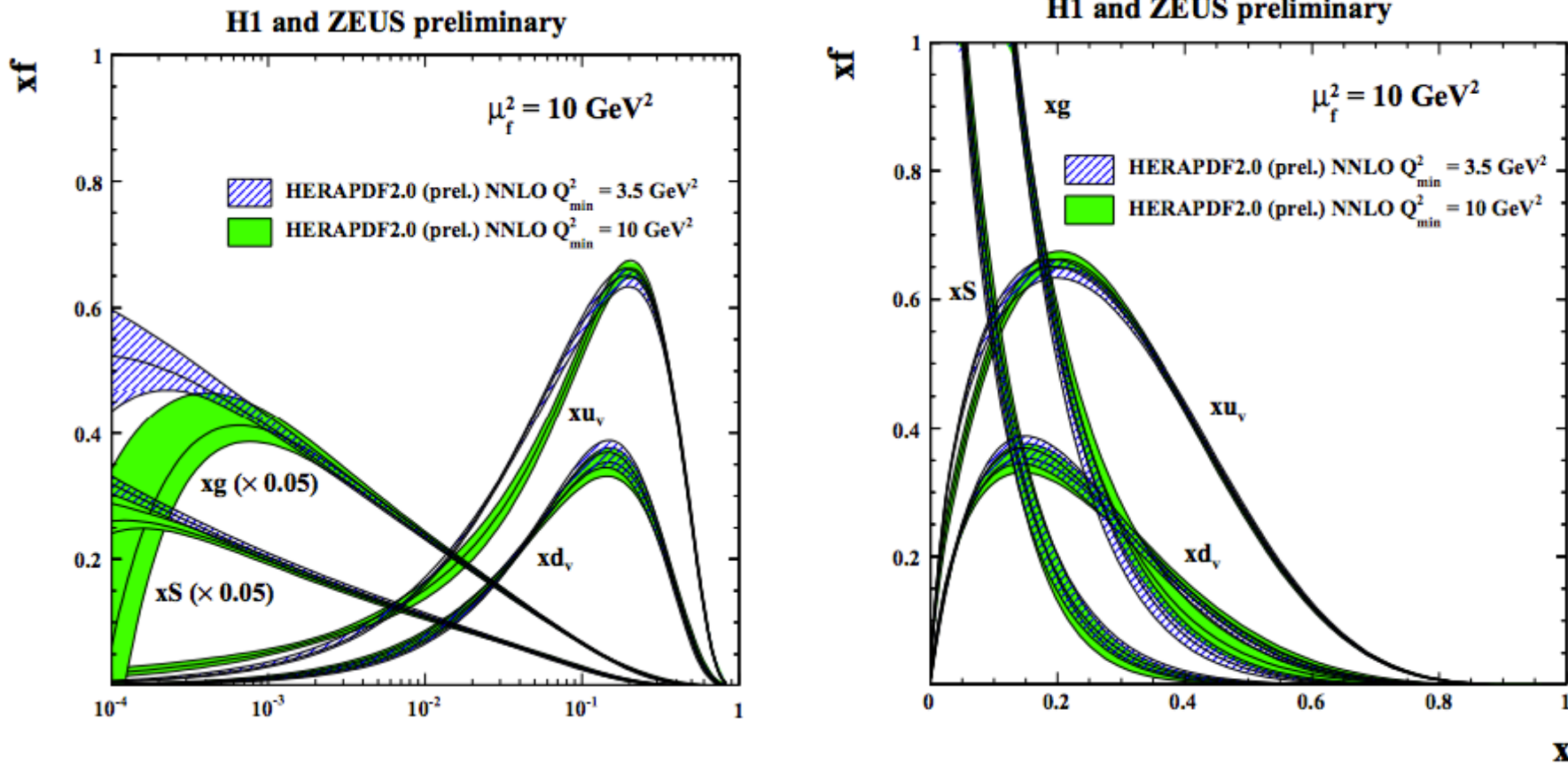


Q^2 cut variation is dominant model uncertainty and it gets enhanced for the fit with $Q_{\min}^2 = 10 \text{ GeV}^2$:

→ there is an interplay of the data cut at low Q^2 and impact on gluon at low x .

HERAPDF2.0 with $Q_{\min}^2 = 3.5 \text{ GeV}^2$ vs $Q_{\min}^2 = 10 \text{ GeV}^2$ @ NNLO

- ◆ How do PDFs compare between these 2 scenarios for Q_{\min}^2 choices?

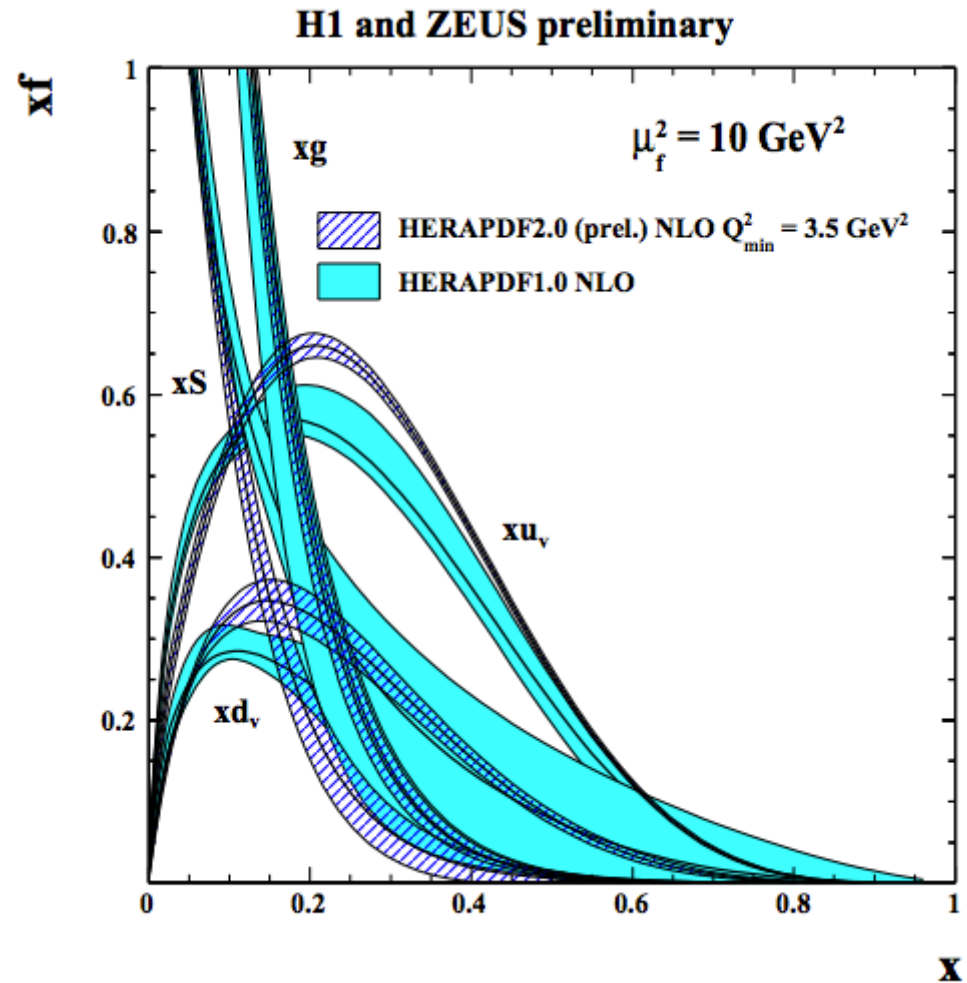


HERAPDF2.0 sets are compatible at high x , but at low x the Q^2 cut on data affects the shape of the gluon (more pronounced at NNLO)

- low $q^2 \leftrightarrow$ low x

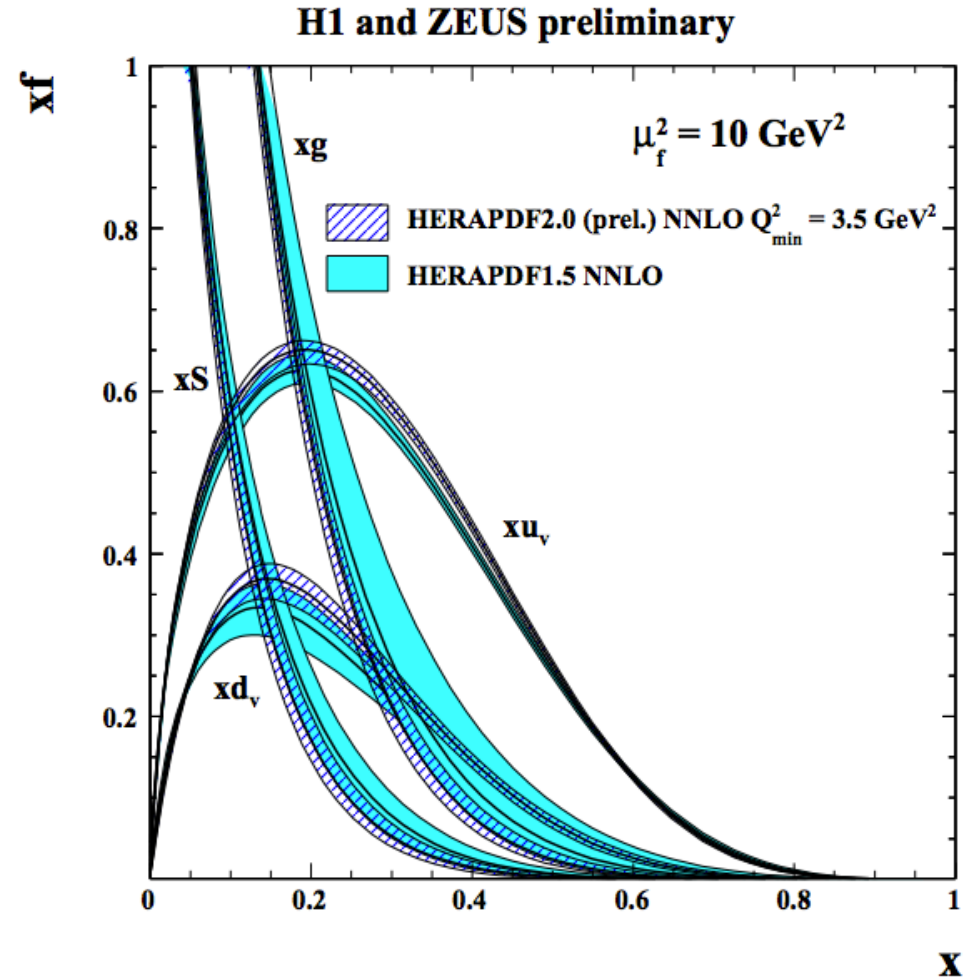
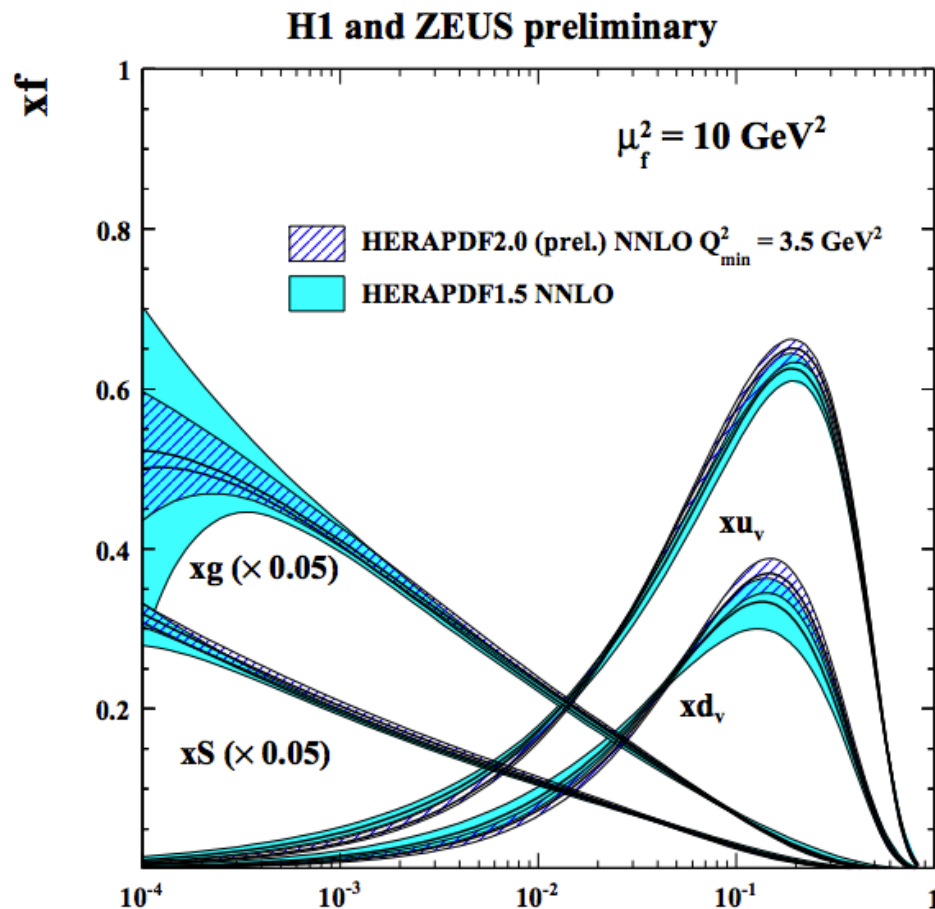
Comparison with HERAPDF1.0 @ NLO

- ◆ HERAPDF1.0 is based on HERA I only data
[JHEP01 (2010) 109]
 - ▶ It used a rigid parametrisation form (10p)
- ◆ Comparison with HERAPDF2.0:
 - ▶ Improved distributions at high x
 - ▶ Sea is softer at high x
 - ▶ Gluon is harder at high x



Comparison with HERAPDF1.5 @ NNLO

- ◆ Most used HERAPDF set is HERAPDF1.5NNLO, how does it compare to it?



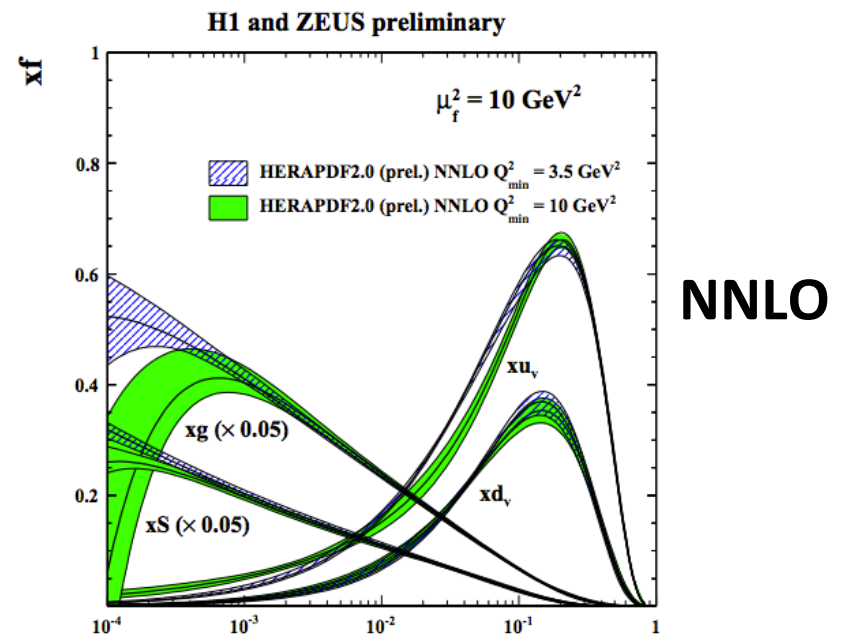
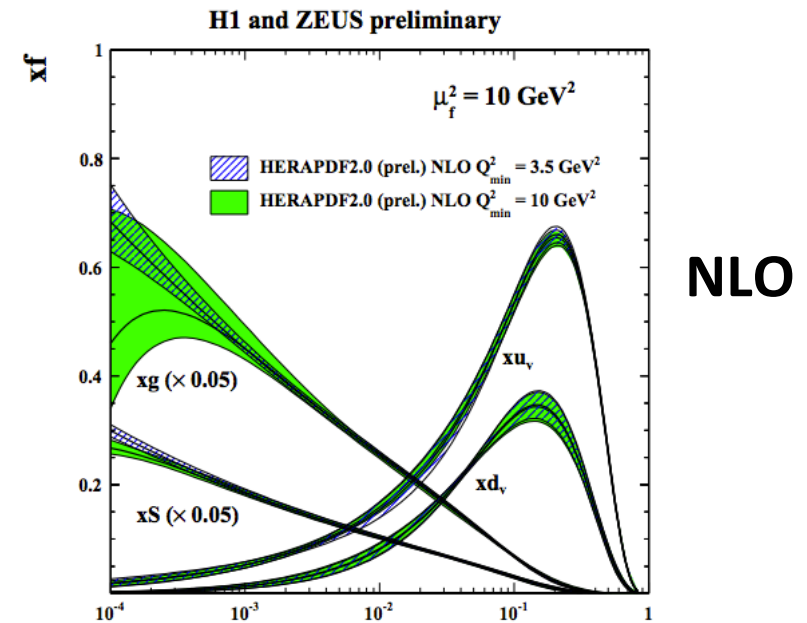
Shapes are similar:

- Gluon and sea at low and high x has improved and they become slightly softer
- Valence at high x has also improved

Summary

- ◆ HERA provides a clean determination of the proton's PDFs based solely on ep collider data
- ◆ New preliminary combined HERA I+II+low energy measurements improves precision of PDFs
- ◆ Q^2 dependence of fit observed and two sets, $Q^2 > 3.5 \text{ GeV}^2$ and $Q^2 > 10 \text{ GeV}^2$, provided

HERAPDF2.0(prel) at NLO and NNLO with full uncertainties

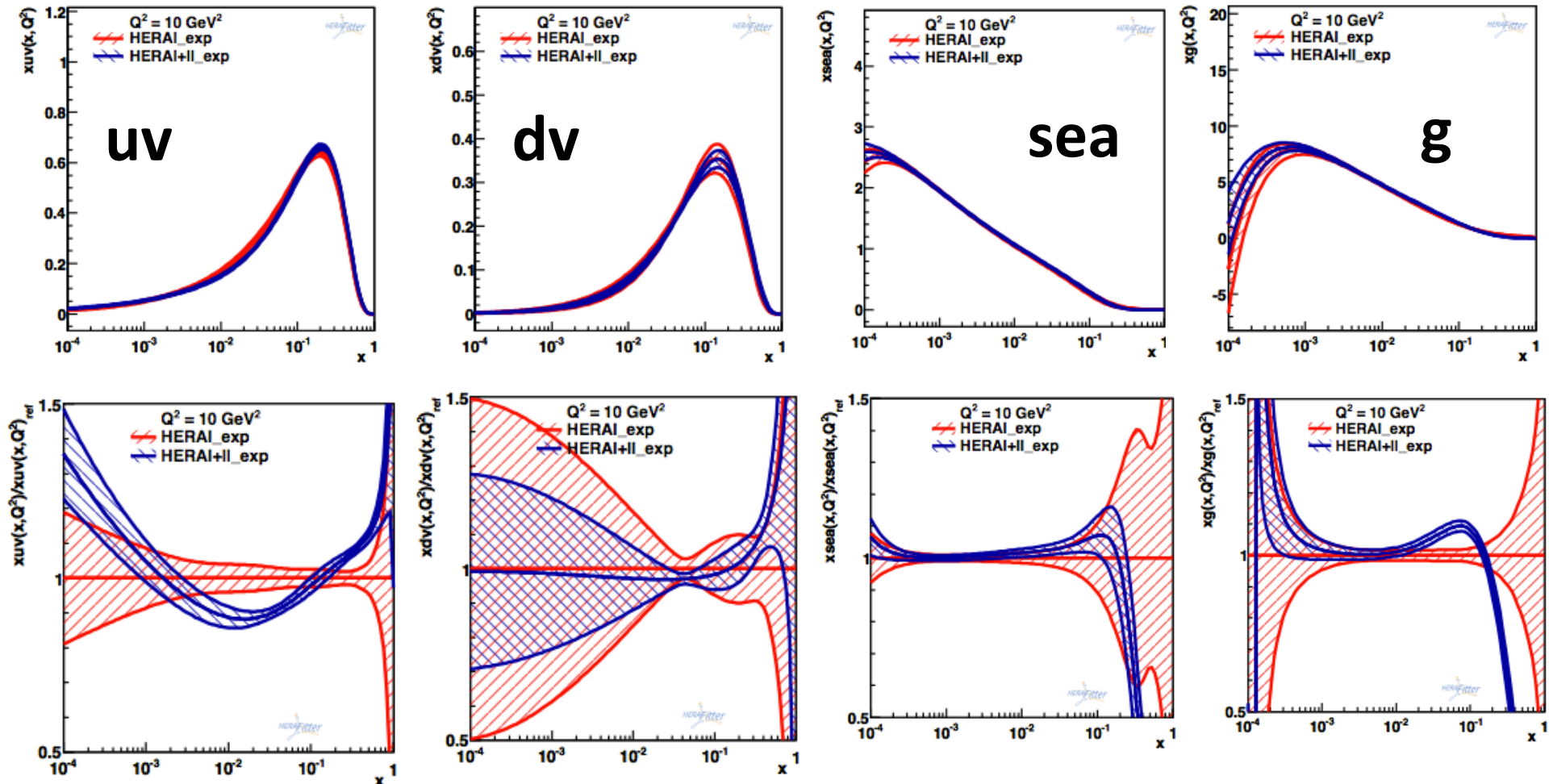


EXTRA

Impact of the experimental precision on PDFs

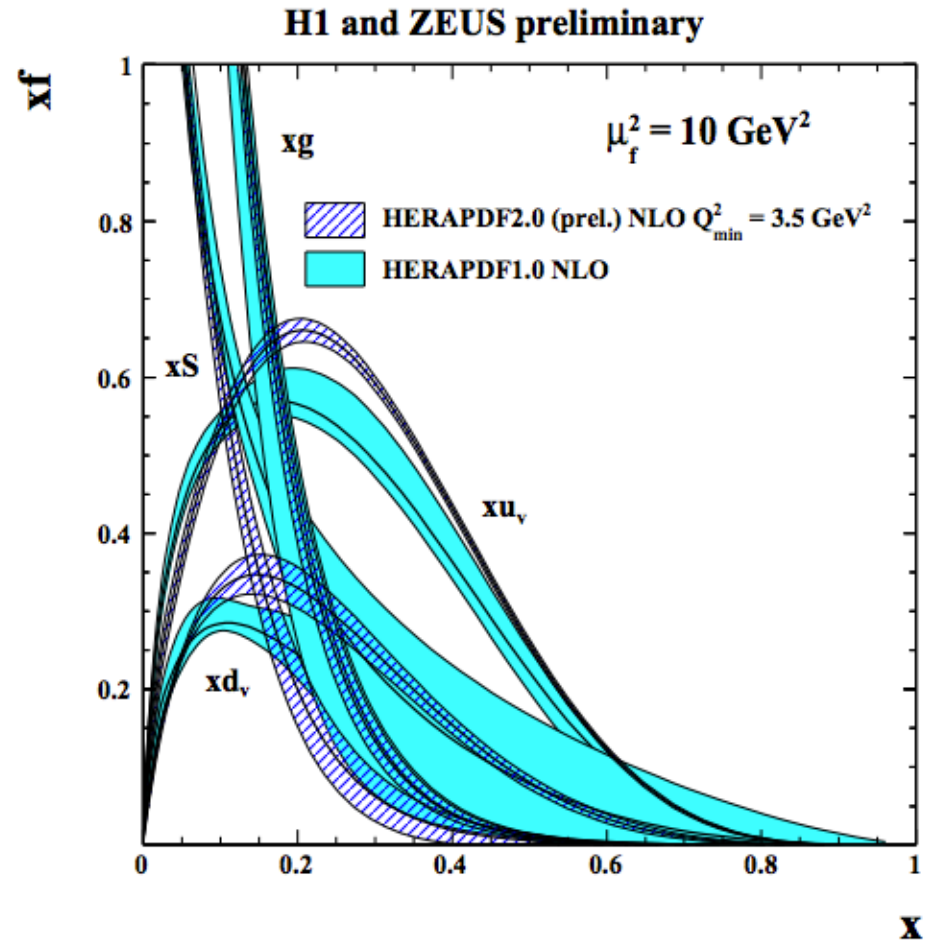
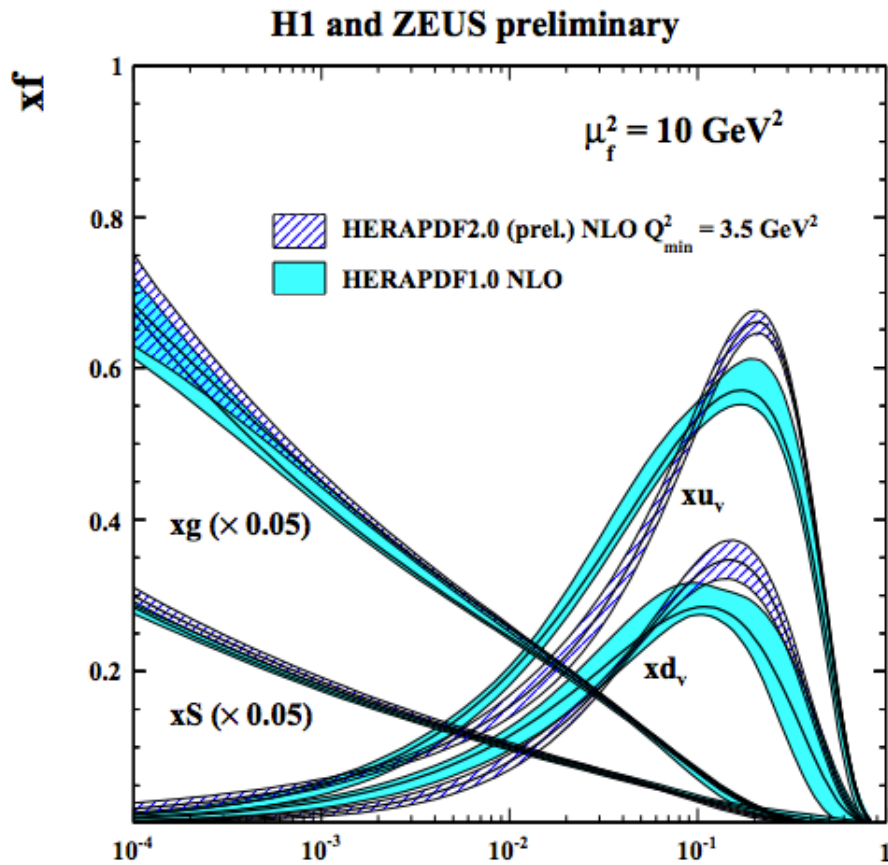
- ◆ HERA I+II preliminary data has an increased experimental precision with respect to HERA I which will also reflect on PDFs:

✧ refitting HERA I data under same conditions as new HERA I+II data and using only exp uncertainties:



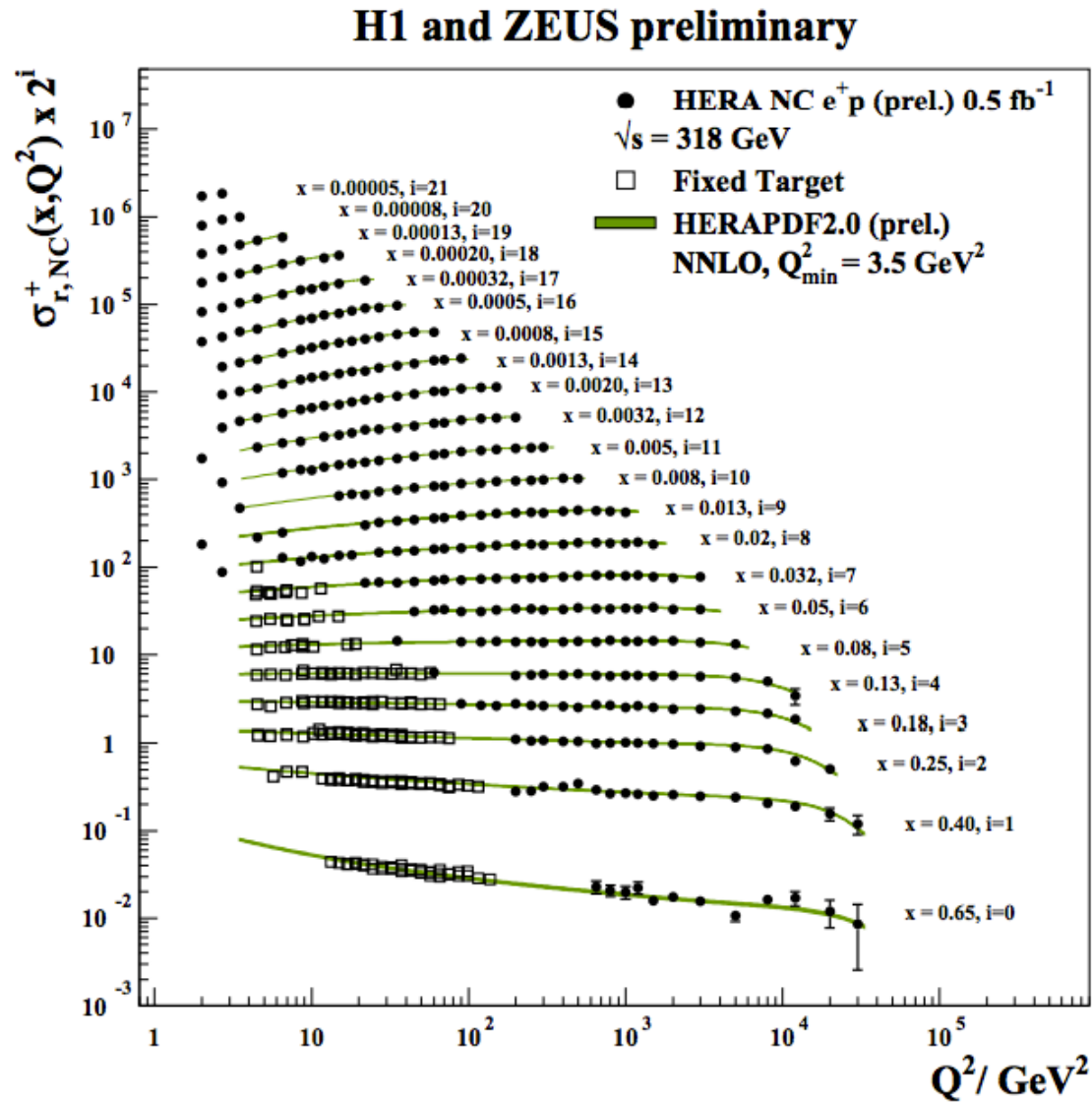
HERAPDF1.0 vs HERAPDF2.0

- ◆ HERAPDF1.0 used a rigid parametrisation form (10p)



Data vs Predictions

- ◆ Text book plot:



Low Energy data vs Fits

◆ 460 GeV p

575 GeV p

H1 and ZEUS preliminary

H1 and ZEUS preliminary

