

# HERAPDF



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on High Energy Physics

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Melbourne Convention and Exhibition Centre

Ringailė Plačakytė  
DESY

on behalf of:

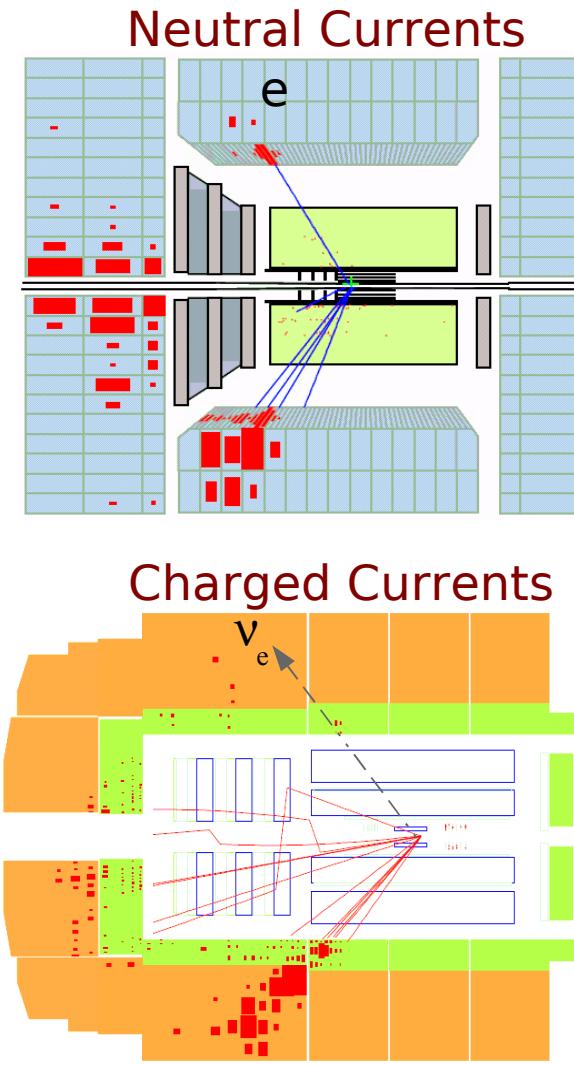


and



# $e p$ Scattering at HERA

DIS cross sections provide an access to parton distribution functions in proton:



$$\frac{d^2\sigma_{NC}^{e^\pm p}}{dxdQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[ Y_+ \tilde{F}_2^\pm \mp Y_- x \tilde{F}_3^\pm - y^2 \tilde{F}_L^\pm \right]$$

dominant contribution  
 important at high  $Q^2$   
 $Y_\pm = 1 \pm (1 - y)^2$   
 sizable at high  $y$

PDFs

LO:  $F_2 \approx x \sum_q e_q^2 (q + \bar{q})$  (in NLO  $(\alpha_s g)$  appears)  
 $x F_3 \approx x \sum_q 2e_q a_q (q - \bar{q})$

In LO  $e^+/e^-$  charged current cross sections are sensitive to different quark densities:

$$e^+ : \quad \tilde{\sigma}_{CC}^{e^+ p} = x[\bar{u} + \bar{c}] + (1 - y)^2 x[\bar{d} + s]$$

$$e^- : \quad \tilde{\sigma}_{CC}^{e^- p} = x[\bar{u} + c] + (1 - y)^2 x[\bar{d} + \bar{s}]$$

# HERAPDFs: Overview

## HERAPDF: only HERA $ep$ data

- uses consistent data with well understood correlations
- no need for nuclear corrections

provide compatible NLO and NNLO predictions with other PDF groups

*Overview of HERAPDFs (this talk):*

DATA	PDF set
H1-ZEUS CC,NC HERAI	HERAPDF1.0 (NLO,NNLO)
H1-ZEUS CC,NC HERAI+(prel.)II	<b>HERAPDF1.5 (NLO,NNLO)</b>
CC,NC HERAI+(prel.)II +jets	HERAPDF1.6
CC,NC HERAI +charm	HERAPDF1.0+charm
All data above	HERAPDF1.7
Planned: H1-ZEUS HERAI+II	HERAPDF2.0 (NLO,NNLO)

*recommended*

Part of HERAPDF project: **HERAFitter**

- open source QCD fitting tool to determine parton distribution functions

# HERAPDF strategy and settings

NLO,NNLO DGLAP evolution (QCDNUM, arXiv:1005.1481)

PDFs parametrised (at starting scale  $Q_0^2$ ) by:

$$xf(x, Q_0^2) = Ax^B(1-x)^C(1+Dx+Ex^2)$$

*A: overall normalisation  
B: small x behavior  
C:  $x \rightarrow 1$  shape*

- apply quark number and momentum sum rules

Fitted PDFs:  $xg, xu_v, xd_v, x\bar{U}=x\bar{u}(+x\bar{c}), x\bar{D}=x\bar{d}+x\bar{s}(+x\bar{b})$

The optimal number of parameters chosen when no further improvements in the  $\chi^2$  are observed

- more flexible parametrisation than in HERAPDF1.0 used in fits with HERA II data

$Q_0^2 = 1.9 \text{ GeV}^2$ ,  $\alpha_s = 0.1176$ ,  $Q_{\min}^2 = 3.5 \text{ GeV}^2$ , different HF schemes (RT in HERAPDF1.0)

Uncertainties separated into:

experimental

small uncertainties ( $\Delta\chi^2=1$ )

model

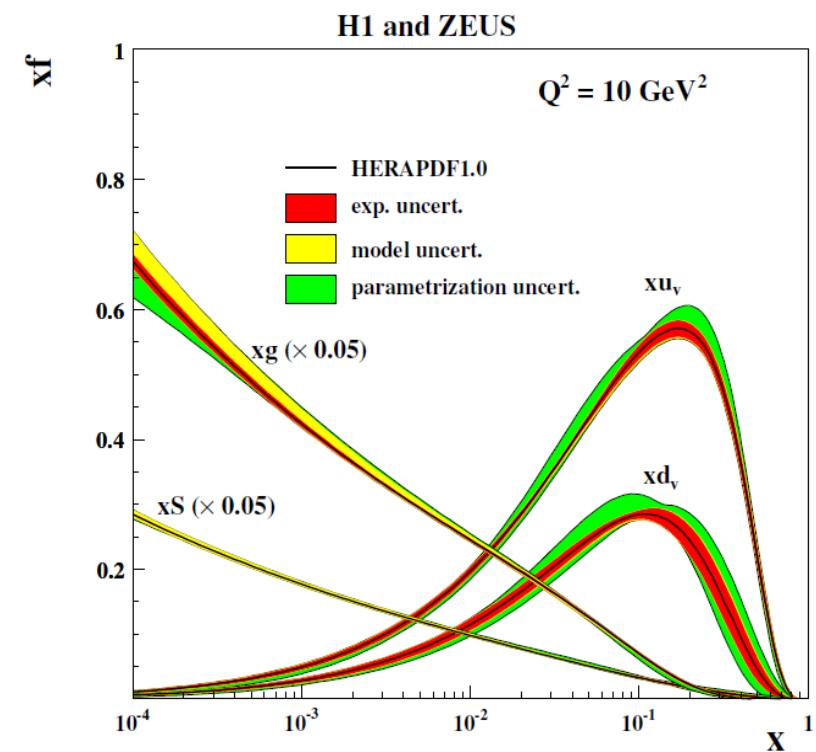
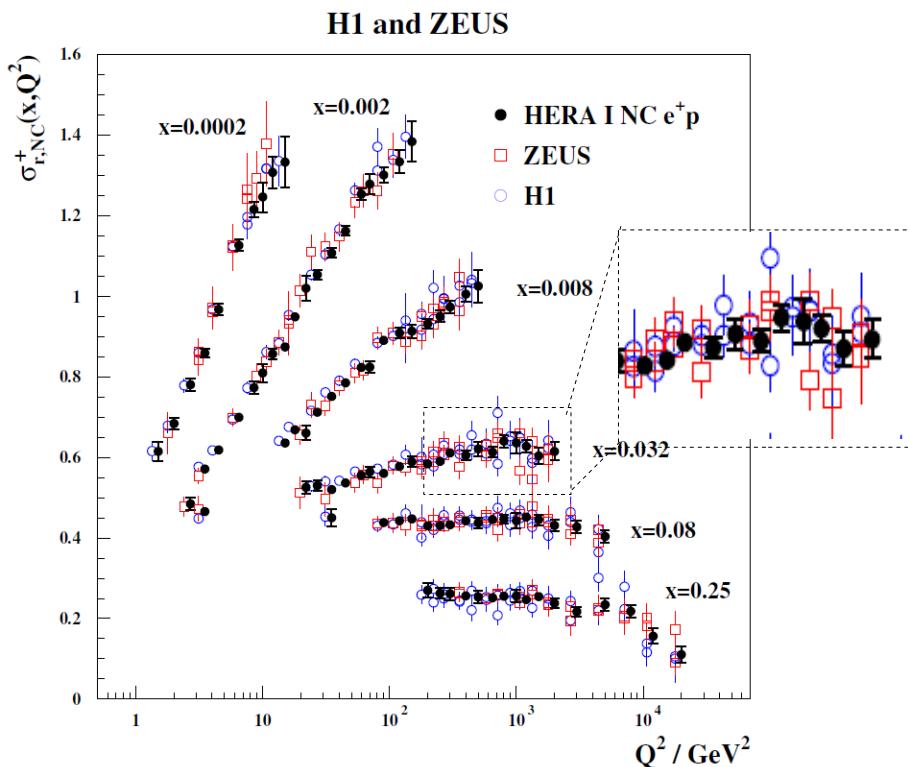
evaluated from variation of model parameters:  $Q_{\min}^2, f_s, m_c, m_b$

parametrisation

results from different parametrisation assumptions

# HERAPDF1.0

HERAPDF1.0: QCD fit to combined H1 and ZEUS HERA I CC,NC data  
- ultimate precision (experiments cross calibrate each other)



arXiv:0911.0884[hep-ex]

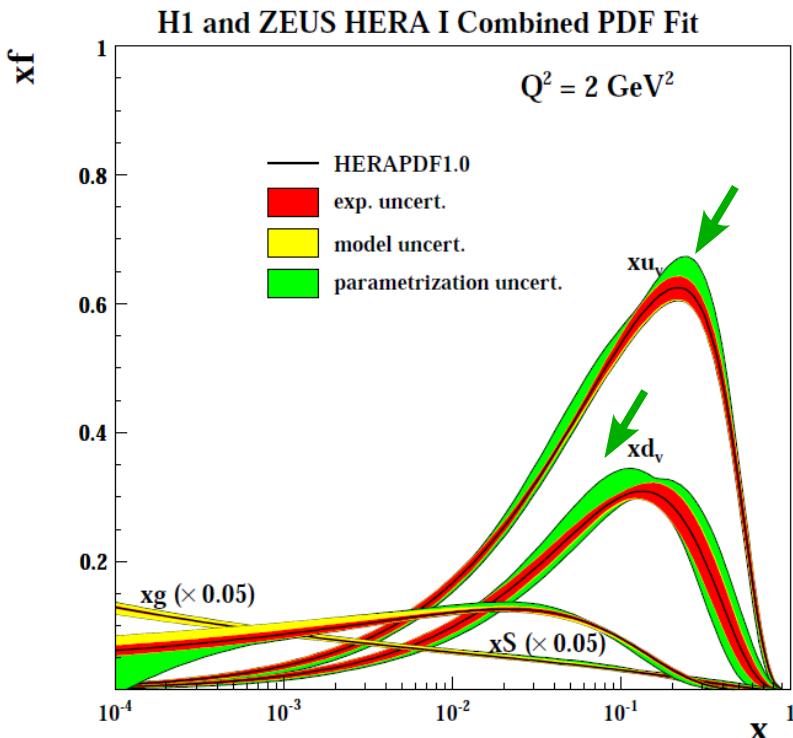
[https://www.desy.de/h1zeus/combined\\_results/index.php](https://www.desy.de/h1zeus/combined_results/index.php)

gluon - from  $F_2$  scaling violation,  $F_L$ , quarks - from CC (flavour separation), NC

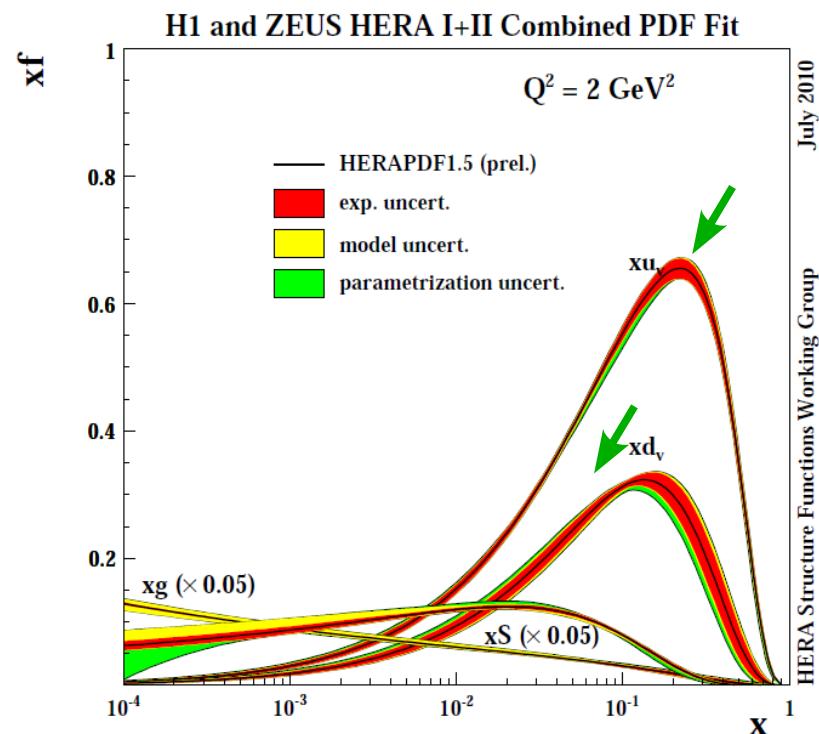
# HERAPDF1.5

High precision HERA II high  $Q^2$  data  
(now in process of publishing!)

HERA I



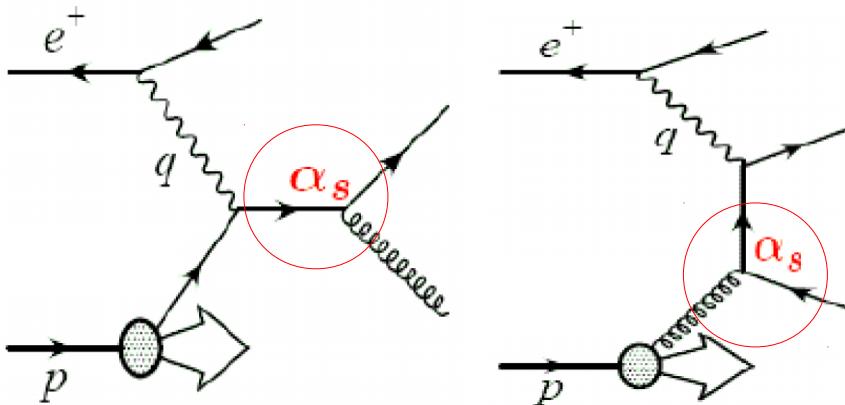
HERA I + II



Reduced uncertainties (mainly valence quarks)

# Inclusion of Jet Data: HERAPDF1.6

LO jet production in DIS:



Direct sensitivity to gluon and strong coupling constant

Reduce correlation of gluon and  $\alpha_s$  in PDF fit

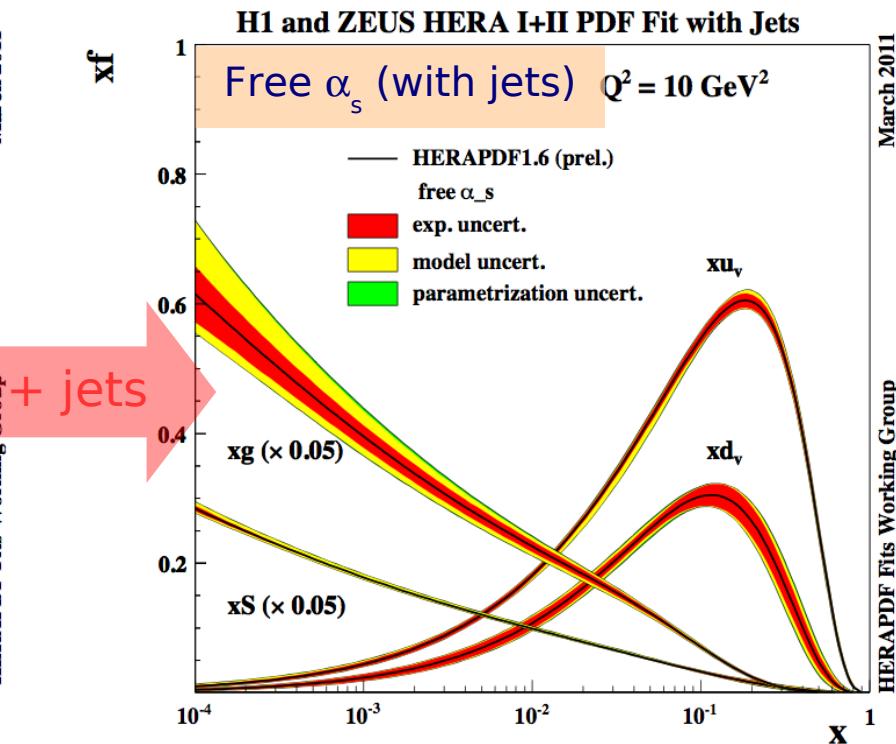
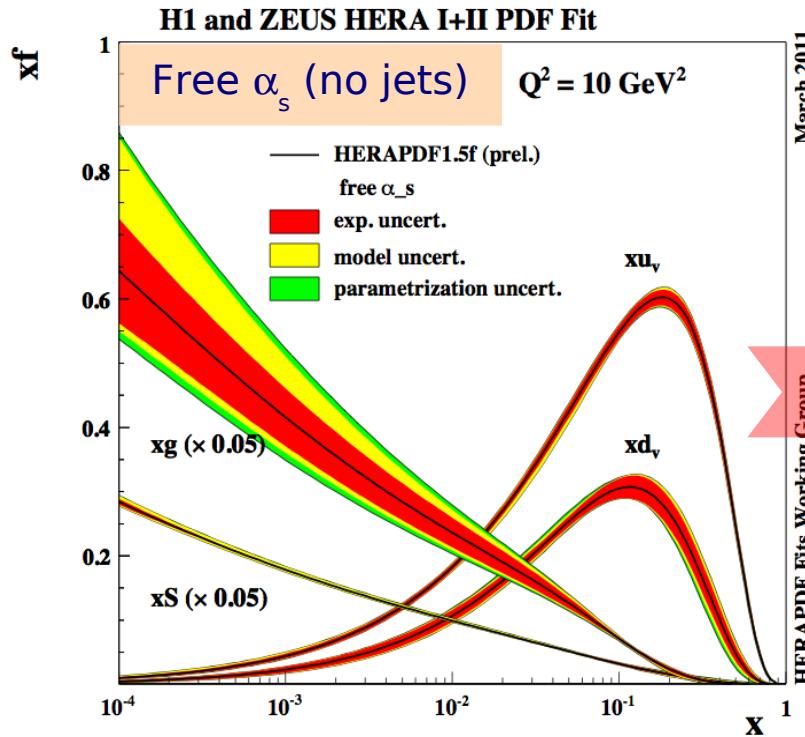
QCD fits with jet data

- allow to constrain simultaneously  $\alpha_s$  and gluon

**HERAPDF1.6:**

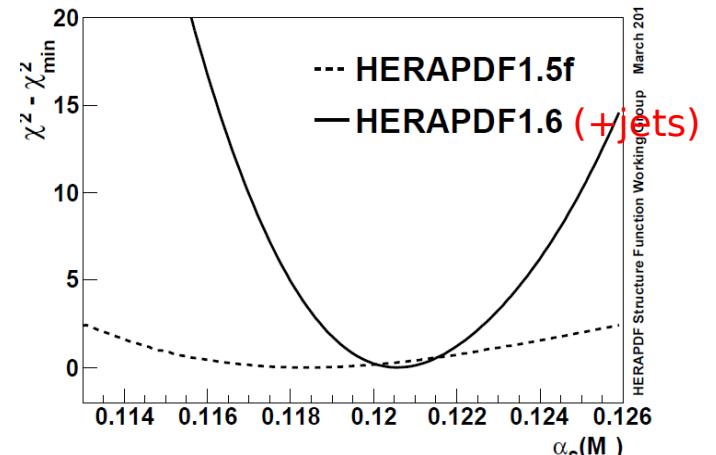
CC, NC HERA I+(prel.)II + 4 inclusive jet measurements from H1 and ZEUS

# Inclusion of Jet Data: HERAPDF1.6

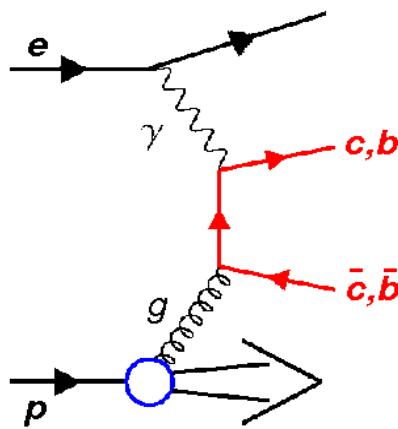


HERA jet data allow to constrain simultaneously  $\alpha_s$  and gluon

$$\rightarrow \alpha_s(M_Z) = 0.1202 \pm 0.0013(\text{exp}) \\ \pm 0.0007(\text{mod}) \pm 0.0012(\text{had}) {}^{+0.0045}_{-0.0036}(\text{th})$$



# Inclusion of Charm Data

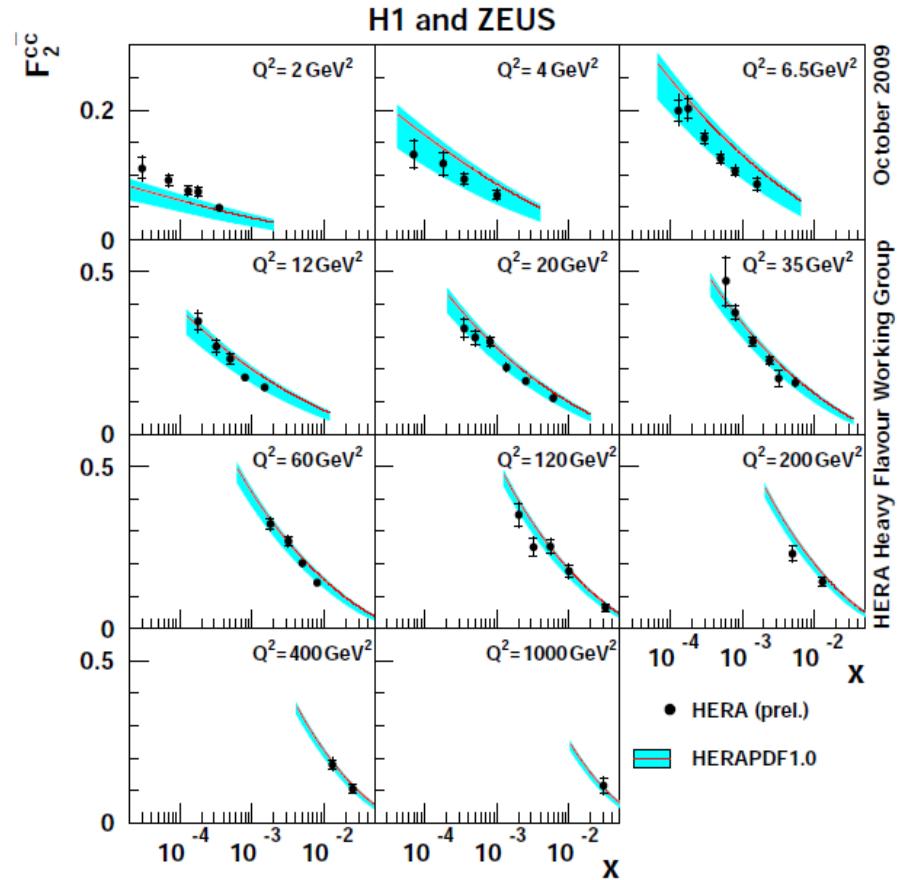


Direct access to the gluon

Heavy quark (HQ) treatment in PDFs  
is important

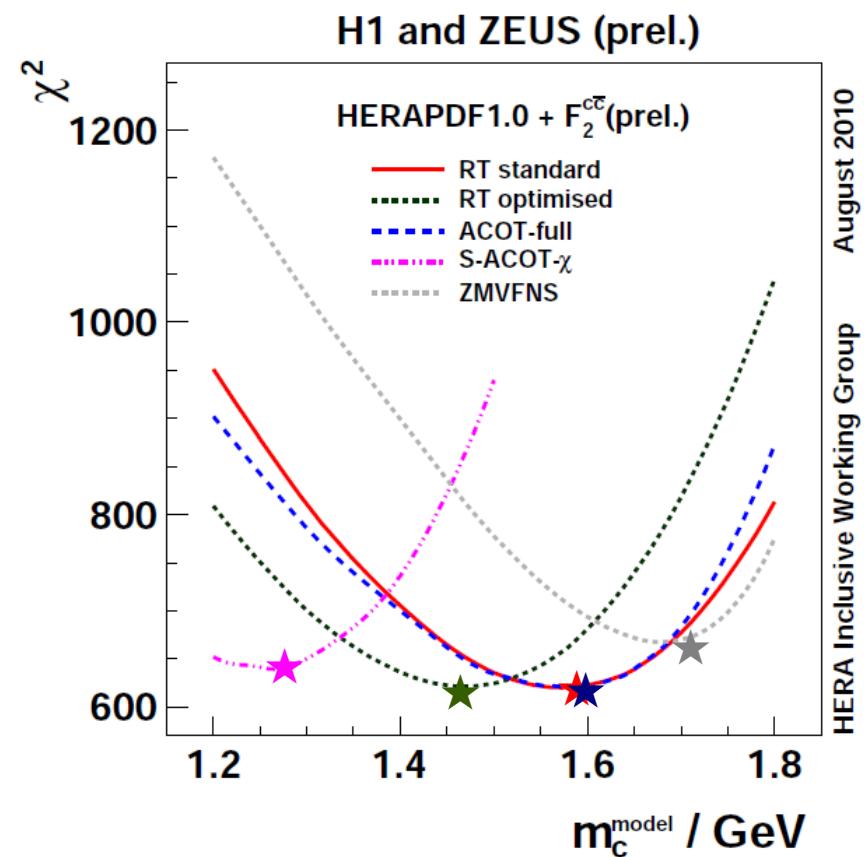
Different HQ schemes exist  
(different treatment of mass terms  
in perturbative calculation)

Combined HERA  $F_2^{cc}$  measurement

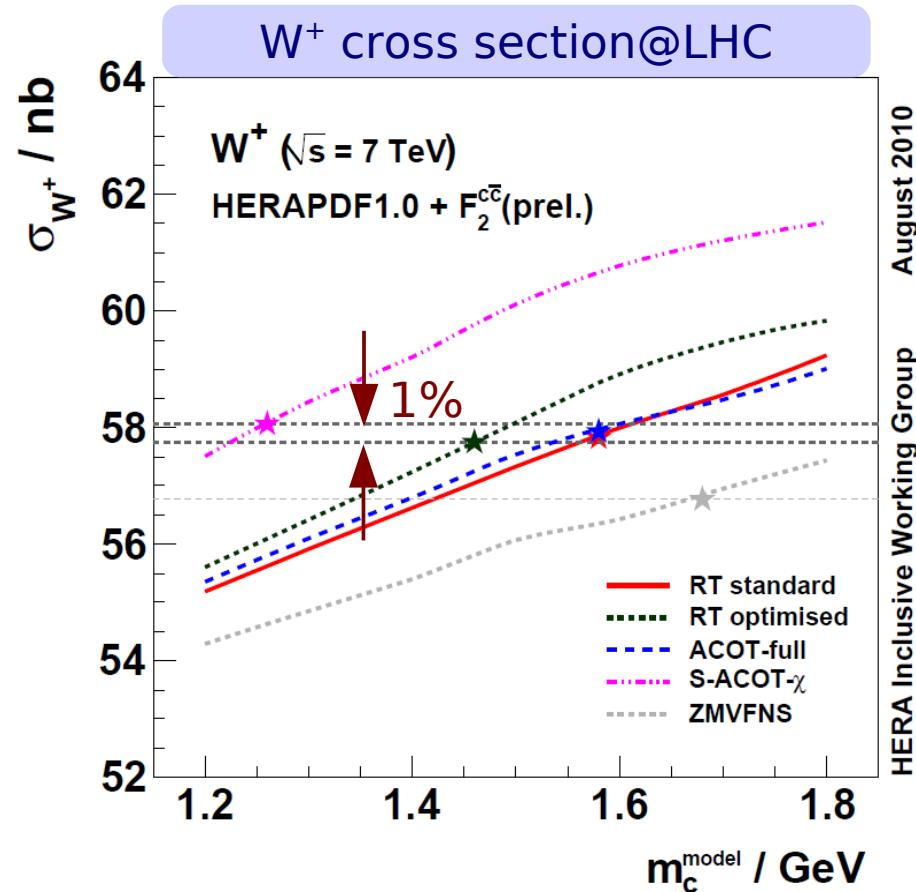


Data well described by HERAPDF prediction

# Inclusion of Charm Data



Different schemes prefer different  $m_c^{\text{model}}$



Variation between schemes  $\sim 7\%$   
Significantly reduced at  $m_c^{\text{model}}$  (opt) ( $\star$ )

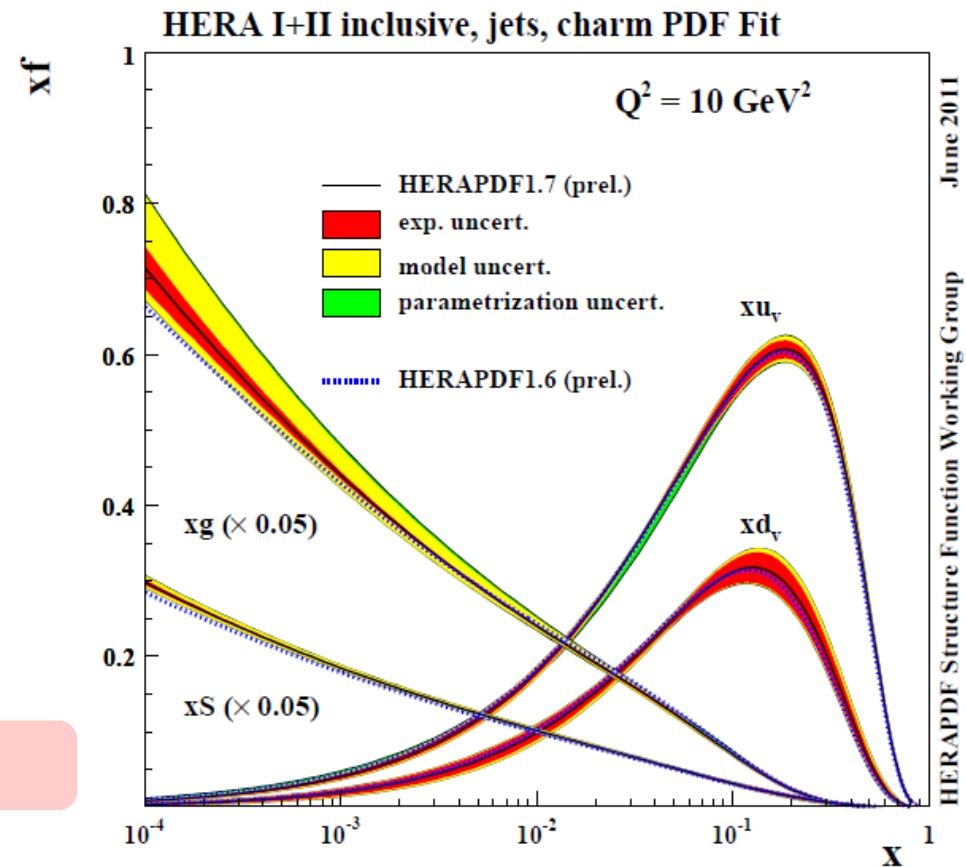
HERA charm measurements help to reduce uncertainties of predictions for the LHC

# Inclusion of All Data: HERAPDF1.7

What if fit all HERA data?

- inclusive + jets + charm + low energy data → **HERAPDF1.7**
- important consistency check

- flexible parametrisation  
(as in HERAPDF1.5f)
- heavy flavour treatment as in  
HERAPDF1.0  
→ motivates for RT optimised at  
 $m_c^{\text{model}}(\text{opt})$
- strong coupling constant = 0.119  
(as supported by the jet data)



# HERAFitter Project

**HERAFitter:** a set of PDF fitting tools for determination of the parton distribution functions

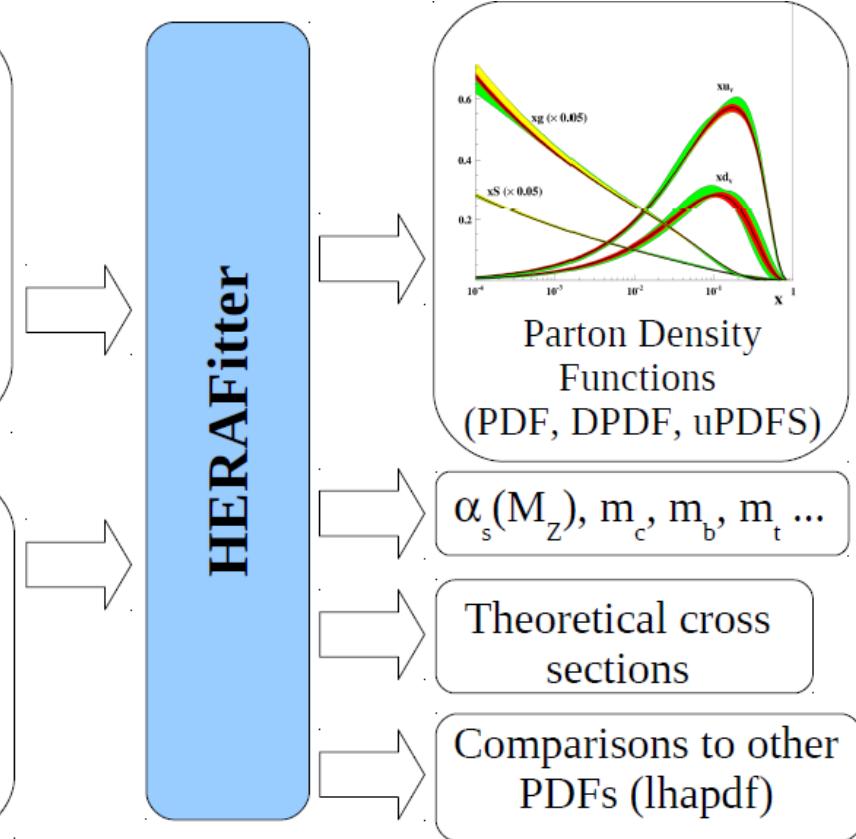
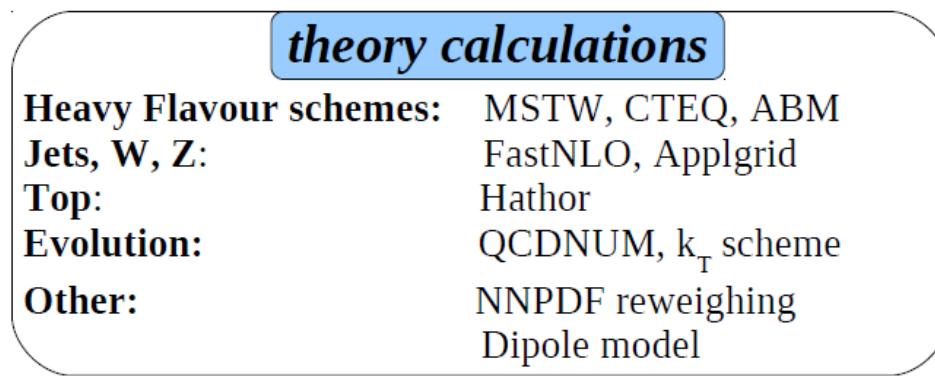
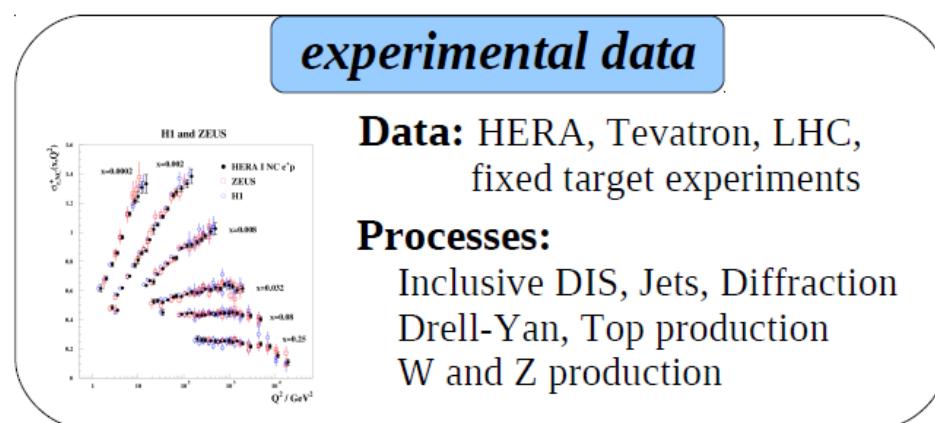
- developers: H1 and ZEUS, ATLAS, CMS
- the first beta version released in September 2011
- May 2012: **beta2 release**

The screenshot shows a web interface for the HERAFitter project. At the top, there's a header with the DESY logo, a search bar, and links for 'RingailePlacakyte', 'Settings', and 'Logout'. Below the header, the main title 'HERAFitter' is displayed. On the left, there's a sidebar with a 'Wiki' section containing links to 'WikiPolicy', 'RecentChanges', 'FindPage', 'HelpContents', and 'HERAFitter' (which is highlighted). Another sidebar on the far left lists 'Page' options like 'Edit (Text)', 'Edit (GUI)', 'Info', 'Subscribe', 'Add Link', 'Attachments', and 'More Actions'. The main content area has a heading 'Welcome to HERAFitter Project'. It describes HERAFitter as a QCD Fit Package used to determine HERAPDFs and part of the HERAPDF project. It includes a link to <https://www.desy.de/h1zeus>. There are sections for 'Downloads of HERAFitter software package', 'Registration' (with instructions to log in and send an email to [herafitter-help@desy.de](mailto:herafitter-help@desy.de)), 'HERAFitter Meetings' (listing 'User's Meetings' and 'Developer's Meeting'), 'Developers Info (restricted to developers)' (linking to 'Internal Developments'), and 'Getting help' (with an email link to [herafitter-help@desy.de](mailto:herafitter-help@desy.de)). The entire page has a light blue background with white text and some orange highlights.

HERAFitter package available online at <http://projects.hepforge.org/herafitter/>

# HERAfitter: Structure

Modular structure of HERAfitter:



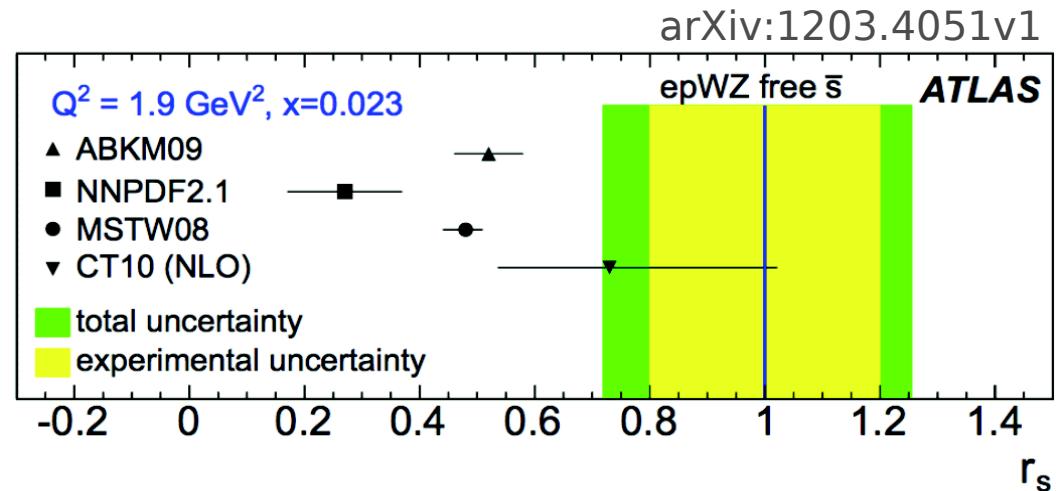
- active participation and support of many theory groups
- global benchmarking platform for PDFs and QCD

# HERAFitter: Usage

## New ATLAS result:

The differential  $W^\pm$ ,  $Z$  cross section data of ATLAS (2010, 35/pb) were jointly analysed with  $e^\pm p$  cross sections from HERA

→ ratio of  $W/Z$  cross sections together with  $y_Z$  shape provide a constraint on s-quark density



First LHC publication using HERAFitter

HERAFitter mail-support:

[herafitter-help@desy.de](mailto:herafitter-help@desy.de)

Monthly users' meetings:

<https://znwiki3.ifh.de/HERAFitter/HERAFitterMeetings>

# Summary

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**HERA** provides unique determinations of the proton structure and compatible NLO and NNLO predictions with other PDF groups

- published final HERA II CC,NC data will follow by H1-ZEUS combination and HERAPDF2.0 set
- HERA jet and charm data provide additional constraints on gluon density and  $\alpha_s$ , charm data help to reduce uncertainties of W,Z predictions at LHC

**HERAFitter** is open source QCD fit framework supported by many theory and experimental (H1, ZEUS, ATLAS and CMS) groups

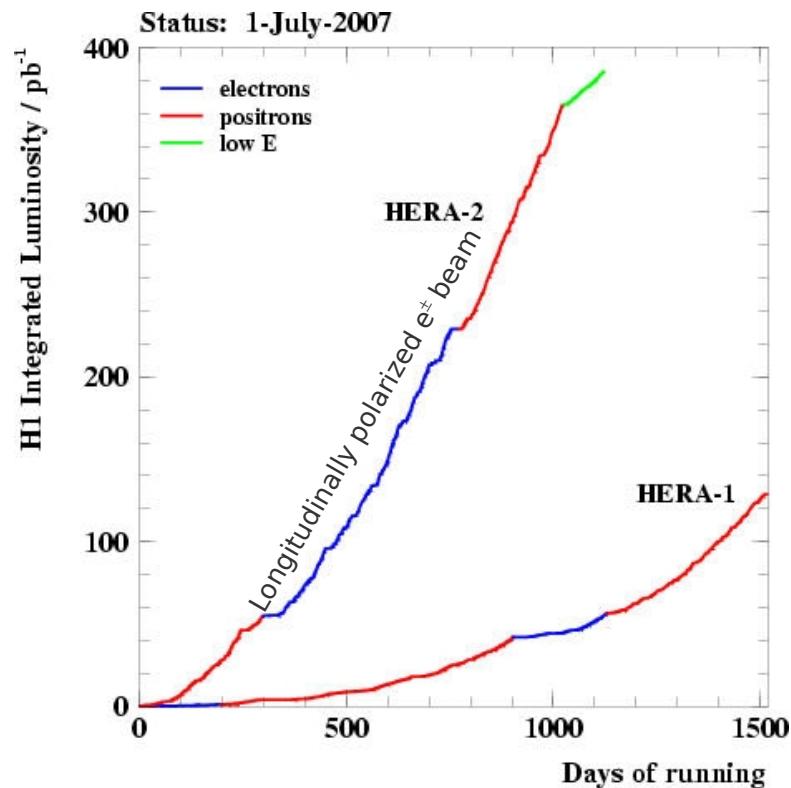
- has the potential to increase the scientific output of the LHC data and to provide a flexible environment for theory benchmarking

## **Back-up slides**

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# HERA Collider

World's only ep collider



- $e^\pm(27.5 \text{ GeV})$ ,  $p(460-920 \text{ GeV})$ ,  
 $\sqrt{s} = 225-318 \text{ GeV}$
- Two collider experiments:  
**H1** and **ZEUS**
- 1994-2000: HERA I data  
2003-2007 HERA II data  
(end of running 30.06.2007)
- $\sim 0.5 \text{ fb}^{-1}$  of luminosity recorded  
by each experiment

# Deep Inelastic Scattering (DIS)

Structure function factorisation:

each **structure function** can be written as a convolution of a hard-scattering coefficient **C** and non-perturbative parton distributions:

$$F_2^V(x, Q^2) = \sum_{i=q, \bar{q}, g} \int_x^1 dz \times C_2^{V,i}\left(\frac{x}{z}, Q^2, \mu_F, \mu_R, \alpha_S\right) \times f_i(z, \mu_F, \mu_R)$$

determined using  
measured cross  
section

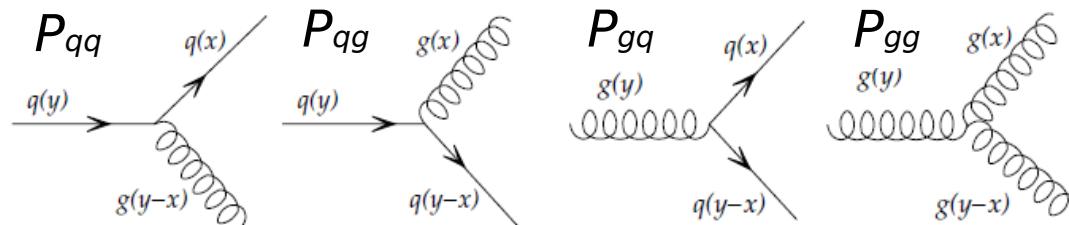
calculable in  
perturbative QCD

PDFs

PDF scale dependence is calculable in perturbative QCD  
(**DGLAP evolution**):

$$\begin{aligned} \frac{\partial q(x, Q^2)}{\partial \ln Q^2} &\propto \int_x^1 \frac{dz}{z} \left[ q(z, Q^2) P_{qq}\left(\frac{x}{z}\right) + g(z, Q^2) P_{qg}\left(\frac{x}{z}\right) \right] \\ \frac{\partial g(x, Q^2)}{\partial \ln Q^2} &\propto \int_x^1 \frac{dz}{z} \left[ q(z, Q^2) P_{gq}\left(\frac{x}{z}\right) + g(z, Q^2) P_{gg}\left(\frac{x}{z}\right) \right] \end{aligned}$$

Probability via splitting functions:



# PDF Determination

Experimentally measured  $\sigma(x, Q^2) \rightarrow F_2(x, Q^2)$

$Q^2$  dependence of  $F_2$  is given in pQCD (**DGLAP** evolution equations)

x-dependence of PDFs is not calculable in pQCD

- parametrise PDFs at the starting scale  $Q^2_0$
- evolve PDFs using **DGLAP** equations to  $Q^2 > Q^2_0$
- construct structure functions from PDFs and coefficient functions:  
predictions for every data point in  $(x, Q^2)$  - plane
- $\chi^2$ -fit to the experimental data

# HERAPDF strategy and settings

## DGLAP at NLO → QCD predictions

PDFs parametrised (at starting scale  $Q^2_0$ ) using standard parametrisation form:

$$\begin{aligned}xg(x) &= A_g x^{B_g} (1-x)^{C_g}, \\ xu_v(x) &= A_{uv} x^{B_{uv}} (1-x)^{C_{uv}} \left(1 + E_{uv} x^2\right), \\ xd_v(x) &= A_{dv} x^{B_{dv}} (1-x)^{C_{dv}}, \\ x\bar{U}(x) &= A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}}, \\ x\bar{D}(x) &= A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.\end{aligned}$$

*A*: overall normalisation

*B*: small  $x$  behavior

*C*:  $x \rightarrow 1$  shape

The optimal number of parameters chosen by saturation of the  $\chi^2$

- central fit with:

10 free parameters for HERA I data

13 for HERA I+II data

$xg, xu_v, xd_v, x\bar{U}, x\bar{D}$

where  $x\bar{U}=x\bar{u}$  and  $x\bar{D}=x\bar{d}+x\bar{s}$  at the starting scale ( $x\bar{s}=f_s x\bar{D}$  with  $f_s=0.31$ )

$A_g, A_{uv}, A_{dv}$  are fixed by sum rules

extra constrains for small  $x$  behavior of d- and u-type quarks:

$B_{uv}=B_{dv}, B_{\bar{U}}=B_{\bar{D}}, A_{\bar{U}}=A_{\bar{D}}(1-f_s)$  for  $\bar{u}=\bar{d}$  as  $x \rightarrow 0$

# Data in PDF fits

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## DIS:

ep (HERA) data: quarks and gluon at small  $x$  ( $F_L$ ), jets (moderate  $x$ ),  
CC - flavour separation, heavy quark structure functions

fixed target data: higher  $x$

neutrino DIS: flavour decomposition,  $x > 0.01$

## Drell-Yan:

quark-antiquark annihilation - high  $x$  sea quarks, deuterium target -  
 $\bar{u}/\bar{d}$  asymmetry

## High Pt jets at colliders:

high  $x$  gluon

## W/Z production:

different quark contributions

# PDF Fit Groups

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## MSTW

- includes all type of data (not yet most recent HERA data). LO, NLO and NNLO

## CTEQ

- includes all type of data (CT10 includes recent combined HERA data and more Tevatron data). NLO

## NNPDFs

- includes all type of data (except HERA jets). NLO, recently also LO and NNLO

## HERAPDF

- HERA (combined) data. NLO and NNLO

## AB(K)M

- DIS and fixed target DY data. NLO and NNLO

## GJR

- DIS, fixed target DY data and Tevatron jet data. NLO and NNLO (no jets)

# PDF Fit Groups

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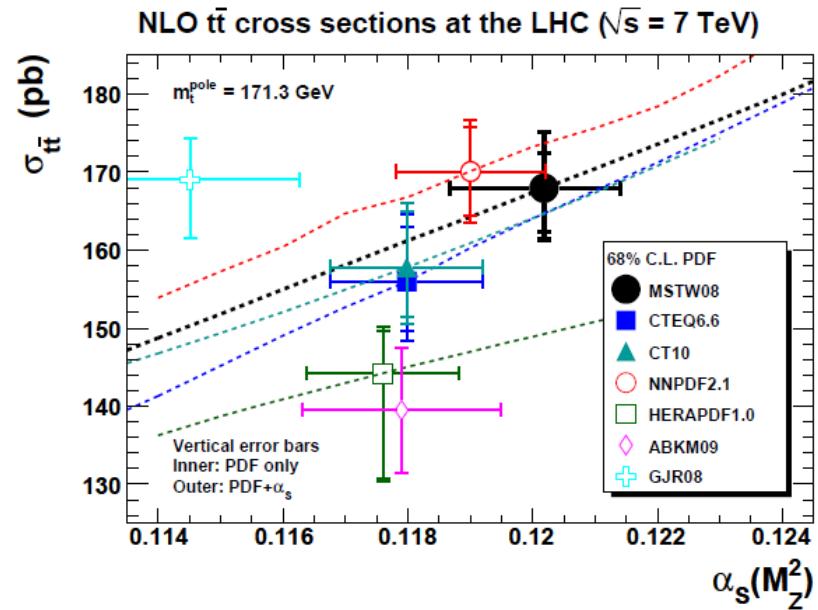
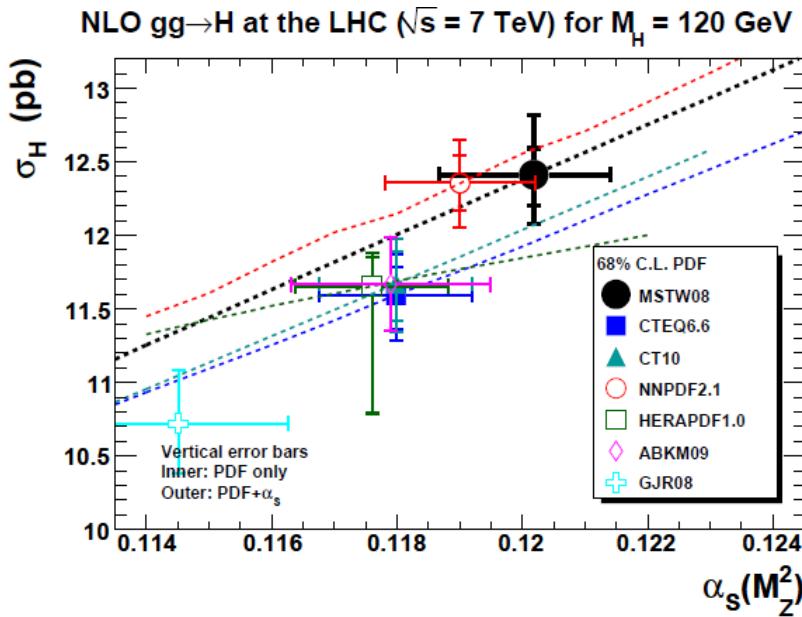
Main sources of difference between different PDFs:

- inclusion of different data
- methods of determining 'best fit'
- uncertainty treatment/sources
- assumptions in procedure (parametrisation)
- heavy flavour treatment
- PDF and  $\alpha_s$  correlation

... lead to differences in the cross section predictions

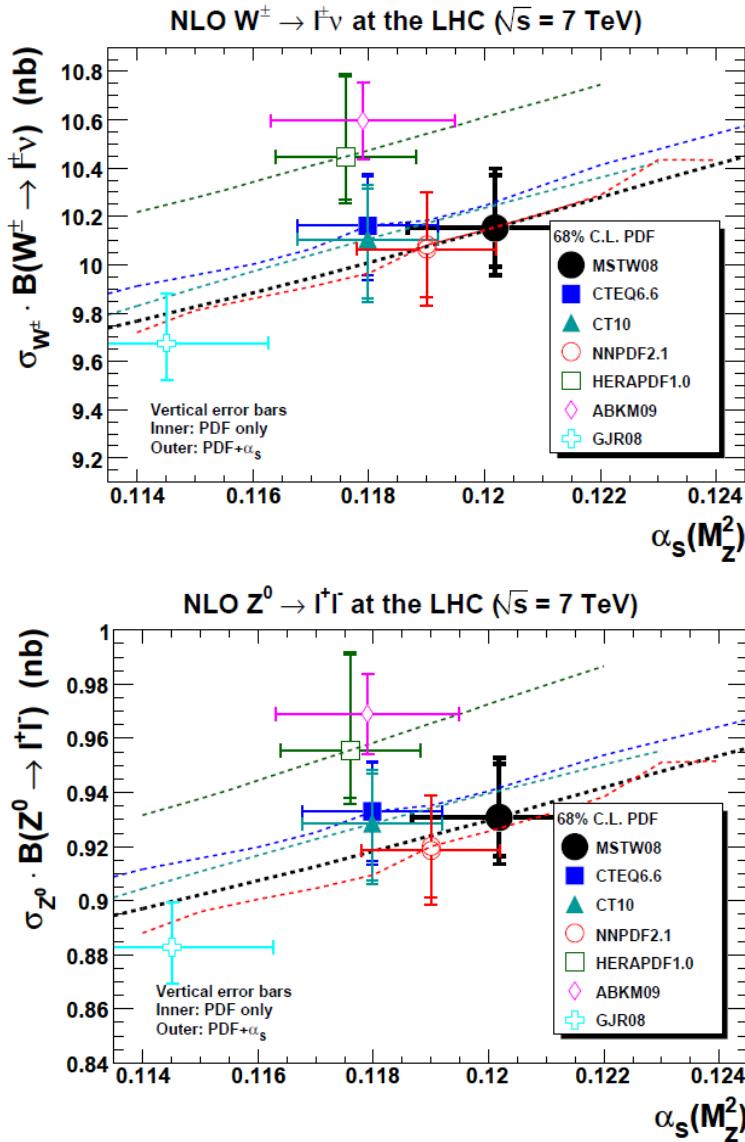
# PDF Fit Groups: Benchmarking (PDF4LHC)

Different PDF lead to differences in cross section predictions

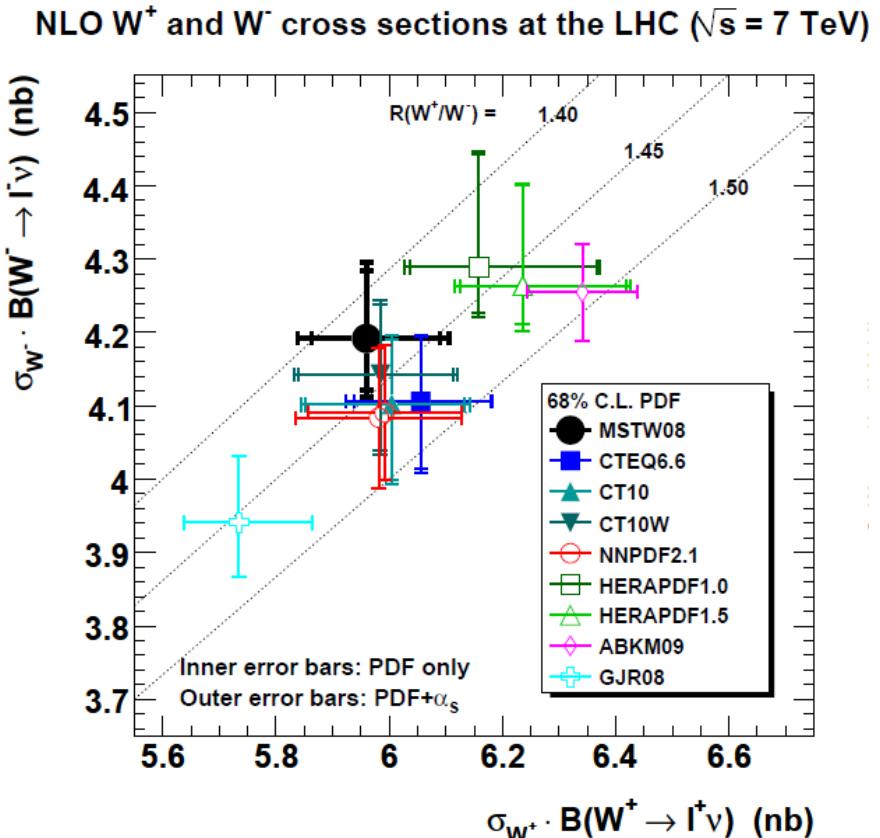


G.Watt  
arXiv:1106.5788v1

# PDF Fit Groups: Benchmarking

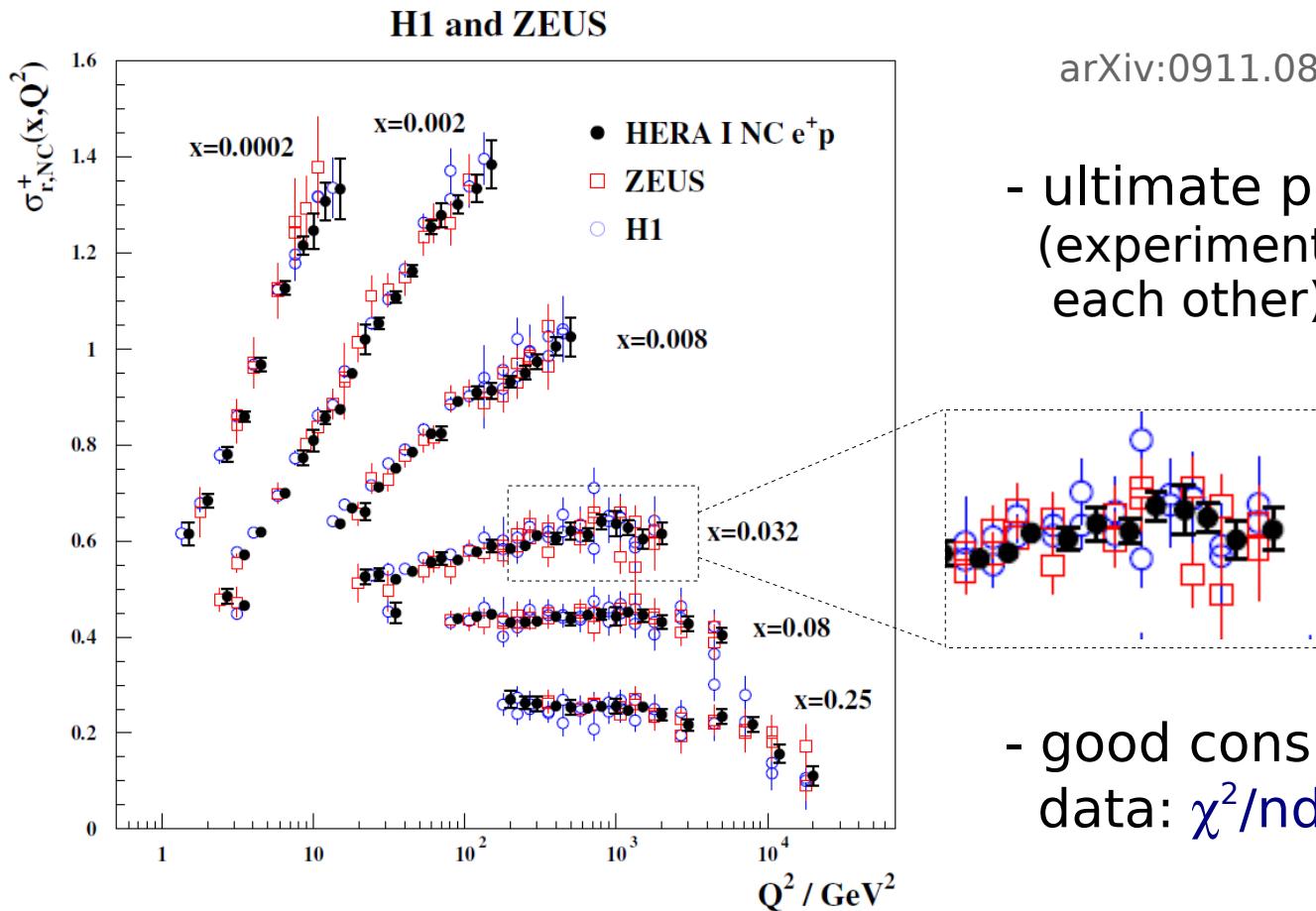


G.Watt



# Combination of HERA data

H1 and ZEUS neutral and charged current data from HERA I period were combined



arXiv:0911.0884[hep-ex]

- ultimate precision  
(experiments cross calibrate each other)

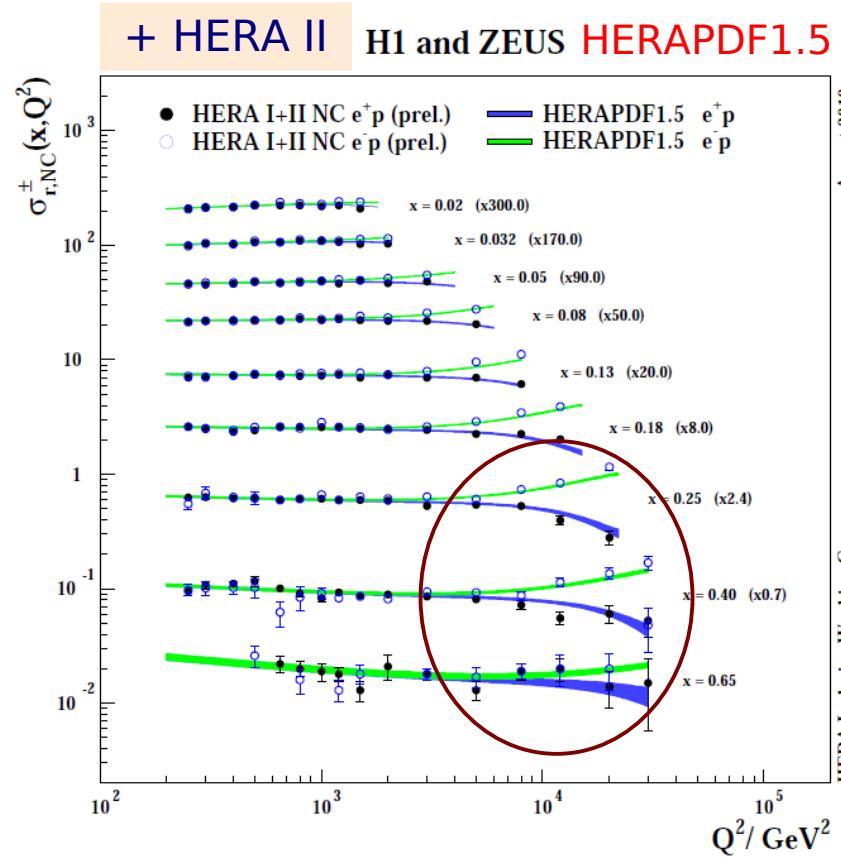
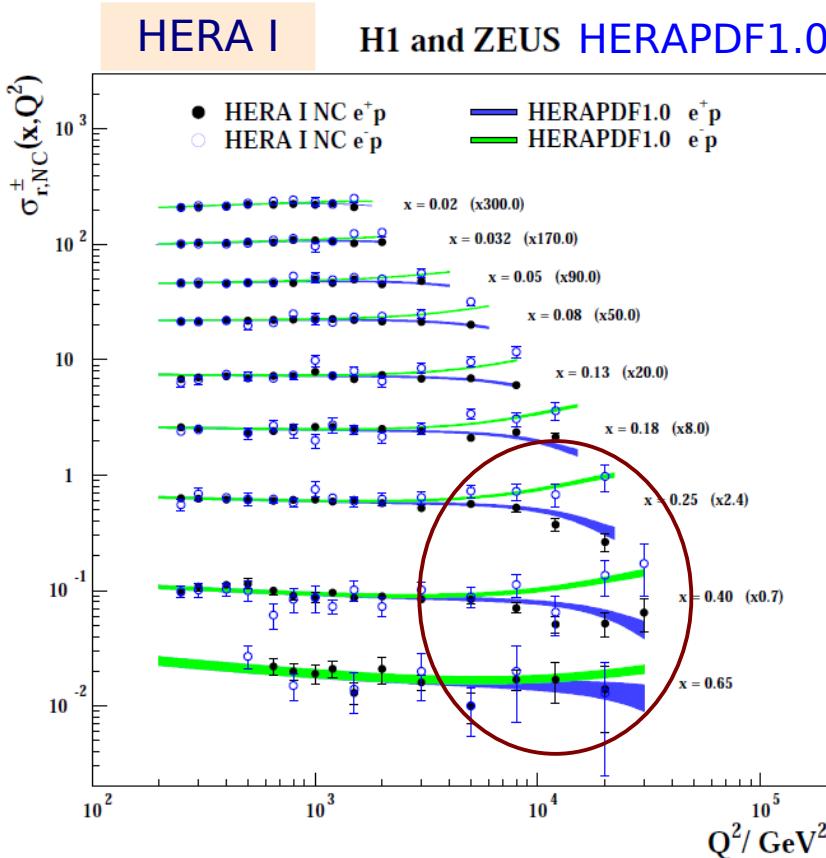
- good consistency of the data:  $\chi^2/\text{ndf} = 637/656$

QCD analysis of combined data → HERAPDF 1.0

# HERAPDF 1.5

HERAPDF1.0: combined inclusive HERA I arXiv:0911.0884[hep-ex]

HERAPDF1.5: combined inclusive HERA I and HERA II data



August 2010

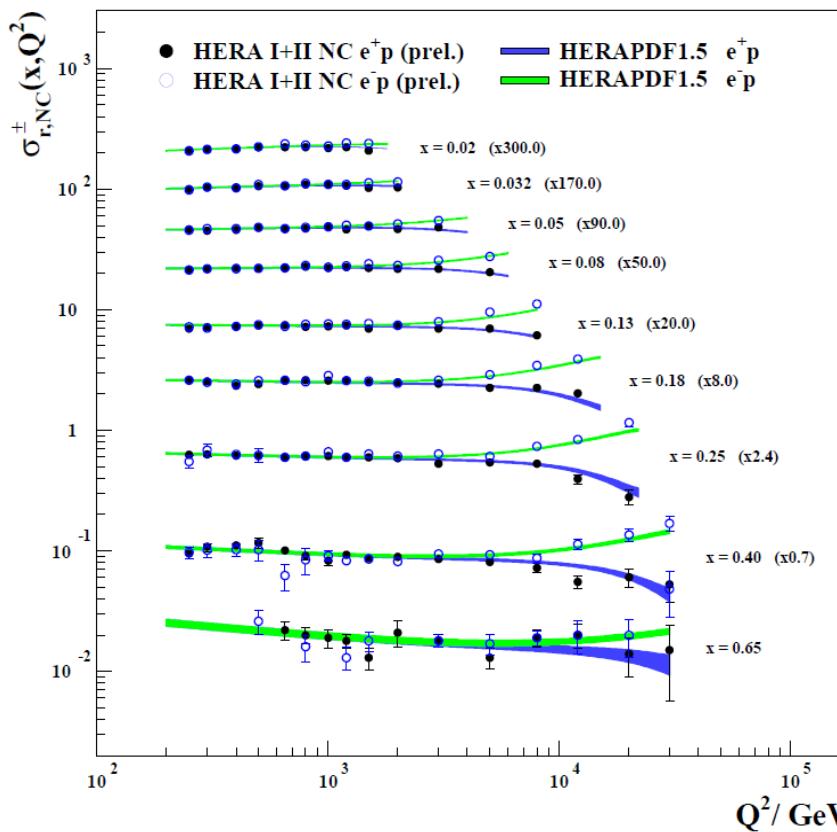
HERA Inclusive Working Group

Improved data precision → Improved PDFs

# HERA DIS Cross Sections vs HERA PDFs

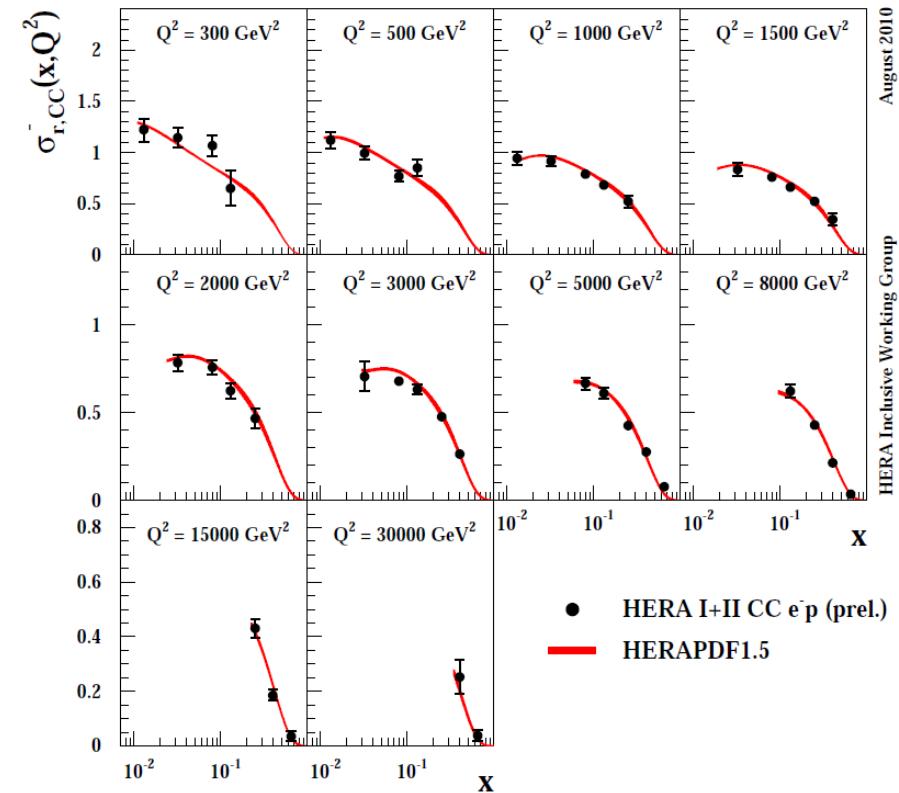
## Neutral Currents

H1 and ZEUS



## Charged Currents

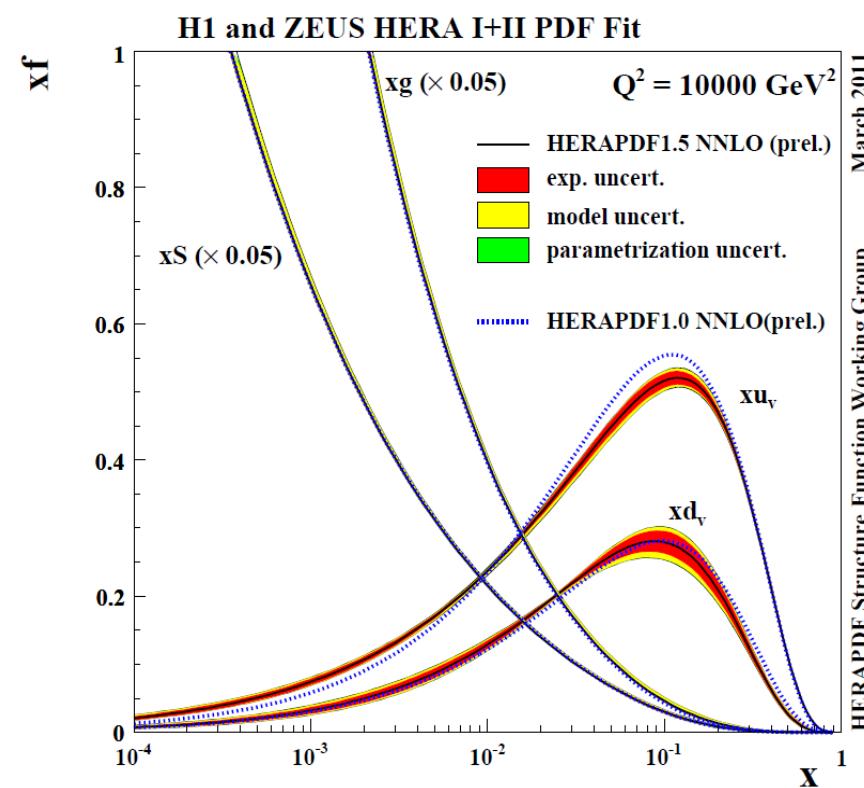
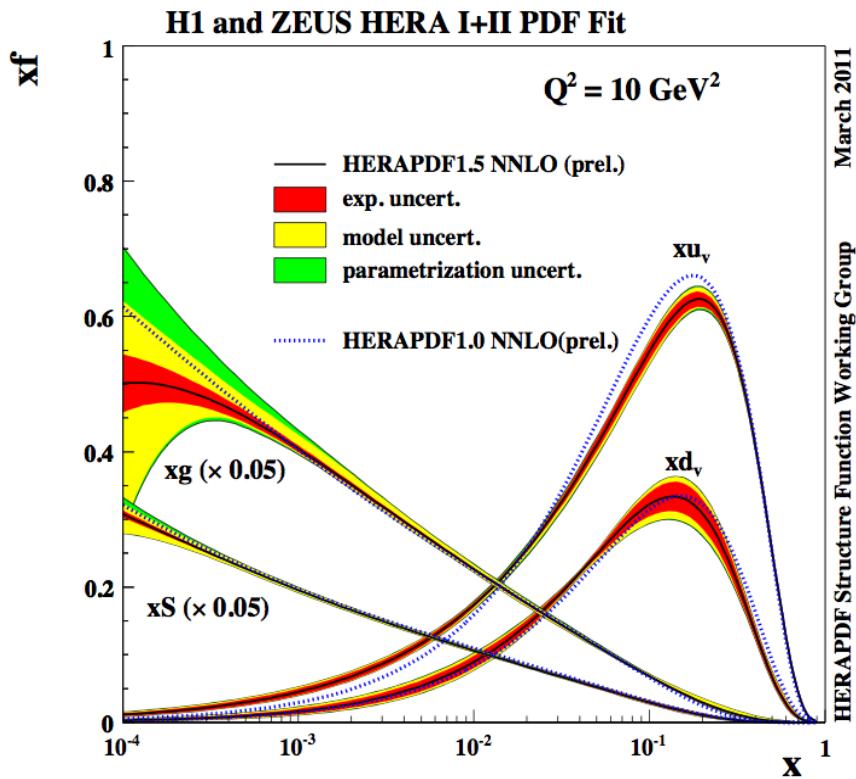
H1 and ZEUS



HERA PDF fit describes NC and CC data very well

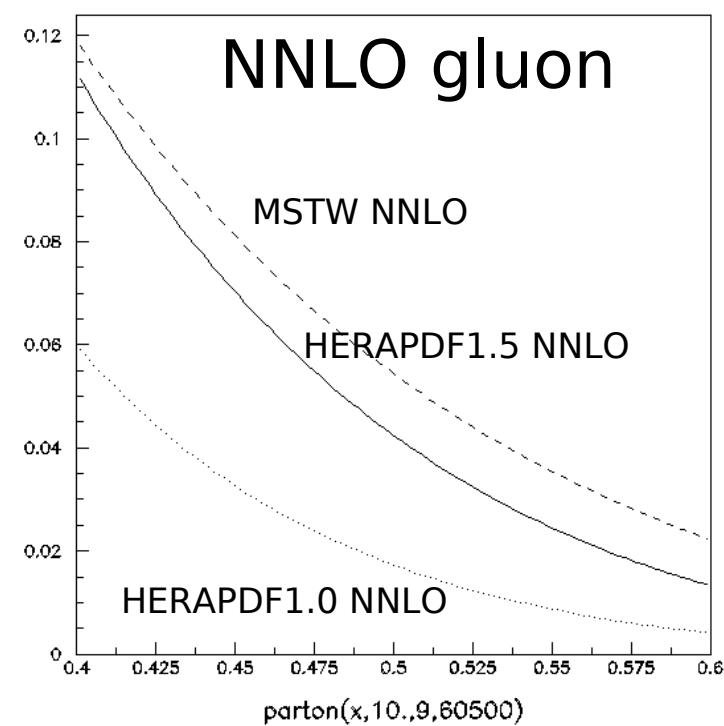
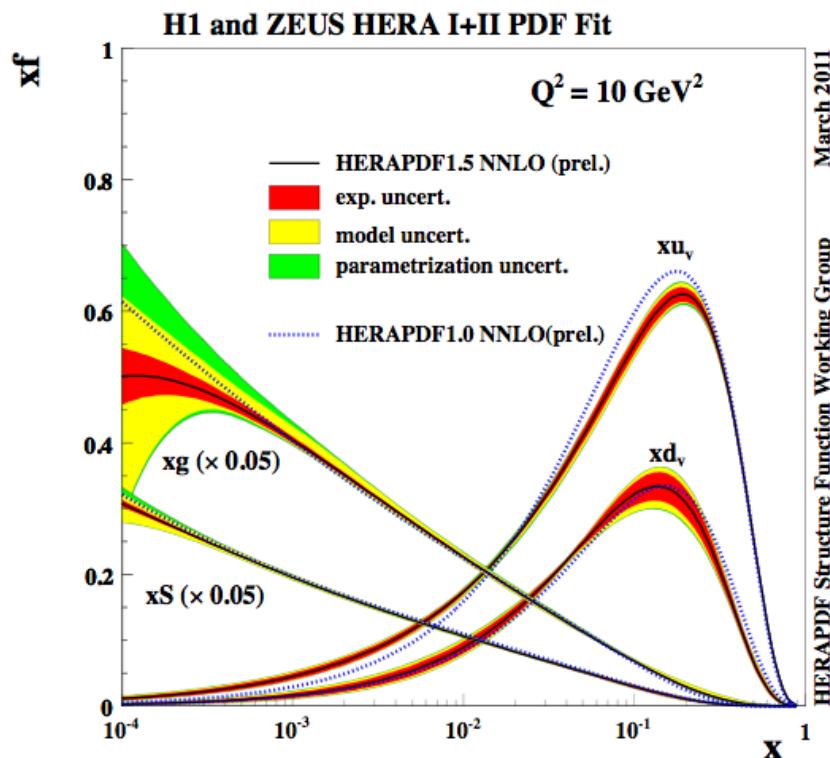
# HERAPDF at NNLO

**NNLO HERAPDF1.5 fit** is based on **HERA I + II inclusive ep data**  
→ uses more flexible parametrisation form



HERA PDFs can be used for NNLO predictions at LHC

# HERAPDF1.0 NNLO vs HERAPDF1.5 NNLO



HERAPDF1.5NNLO has a harder high- $x$  gluon than HERAPDF1.0  
- hence, would give a better agreement with Tevatron data

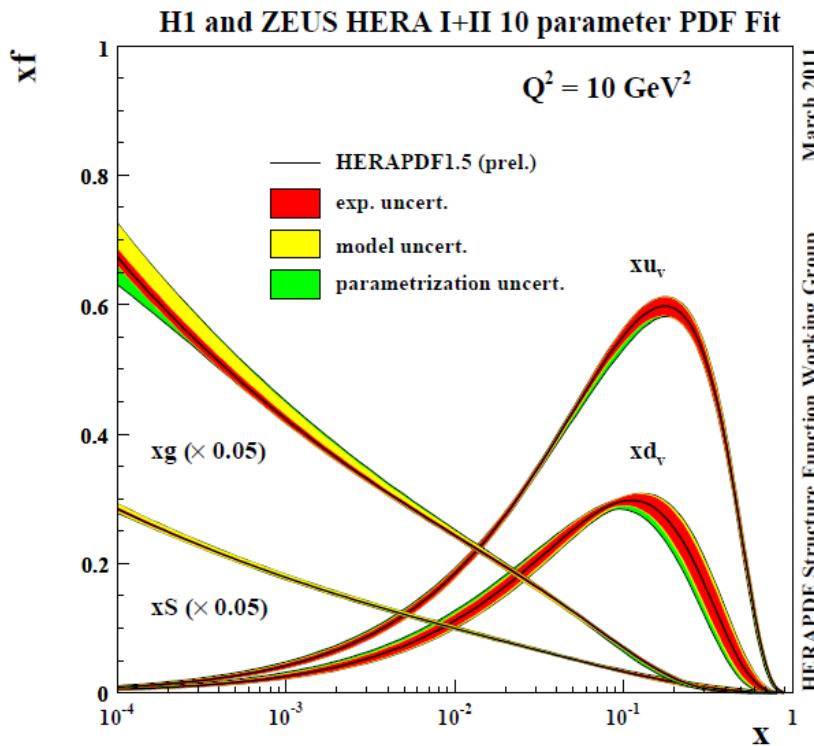
HERAPDF1.5 NNLO uncertainties  
are comparable to NNPDFs

# HERAPDF1.5f

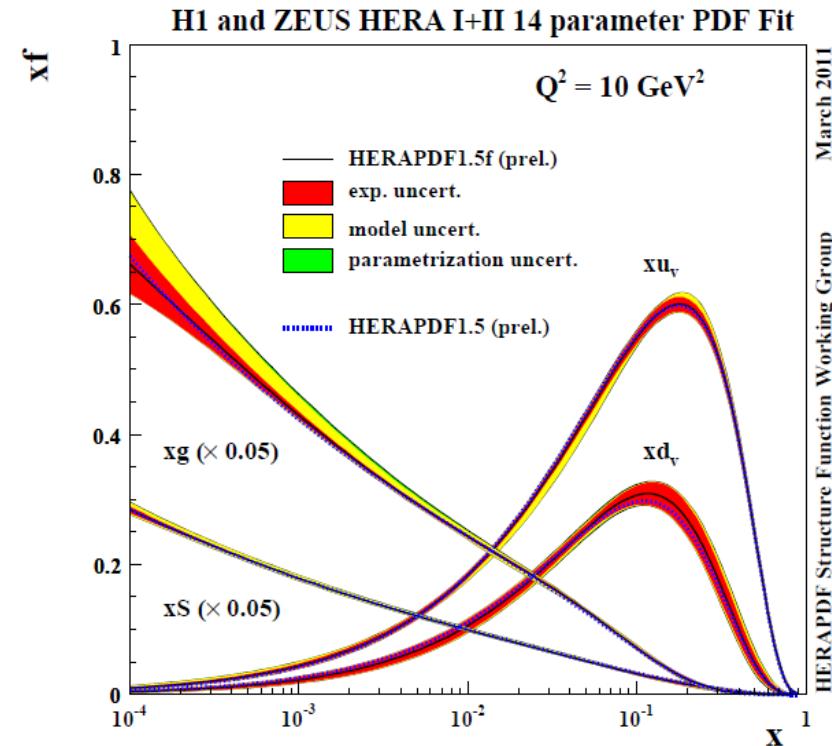
HERAPDF1.5f - more flexible parametrisation

→ gluon more flexible and low- $x$   $d$ -valence is freed from  $u$ -valence

HERAPDF1.5



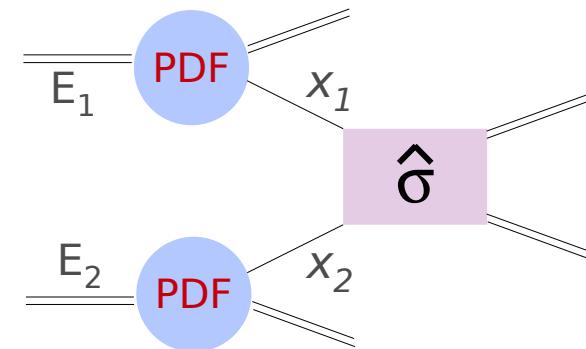
HERAPDF1.5f



Small difference in total uncertainty  
→ swap between **parametrisation** and **experimental** uncertainties

# Proton-Proton Collisions

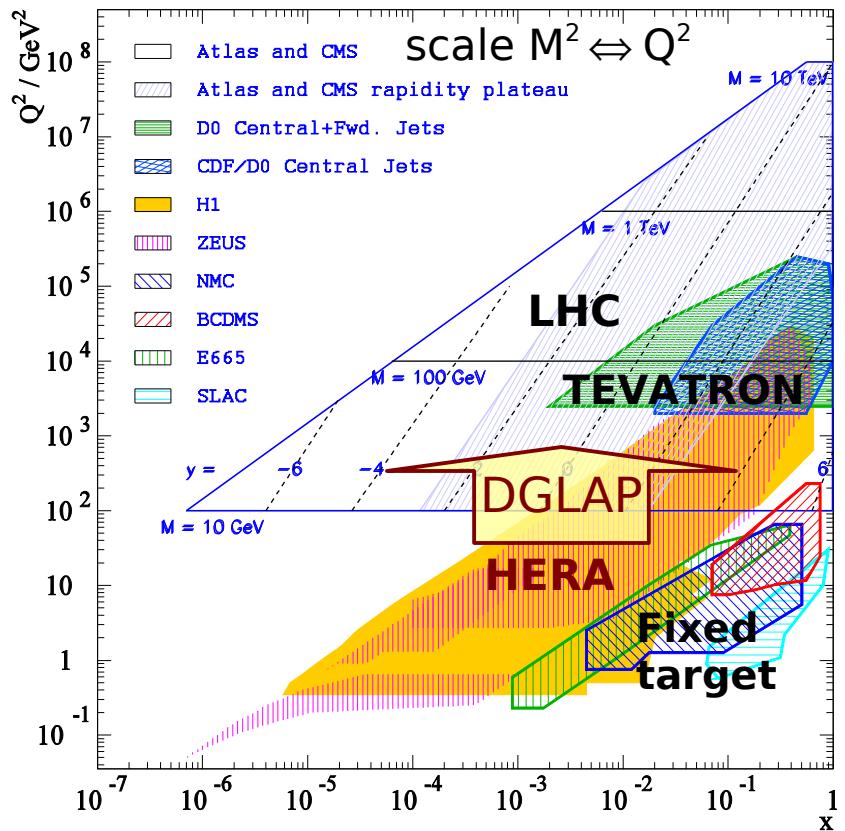
Same PDFs can be used to predict  $pp$  collisions



$\hat{\sigma}$  - perturbative QCD cross section

Factorisation:

$$\sigma \approx \hat{\sigma} \otimes \text{PDF}$$

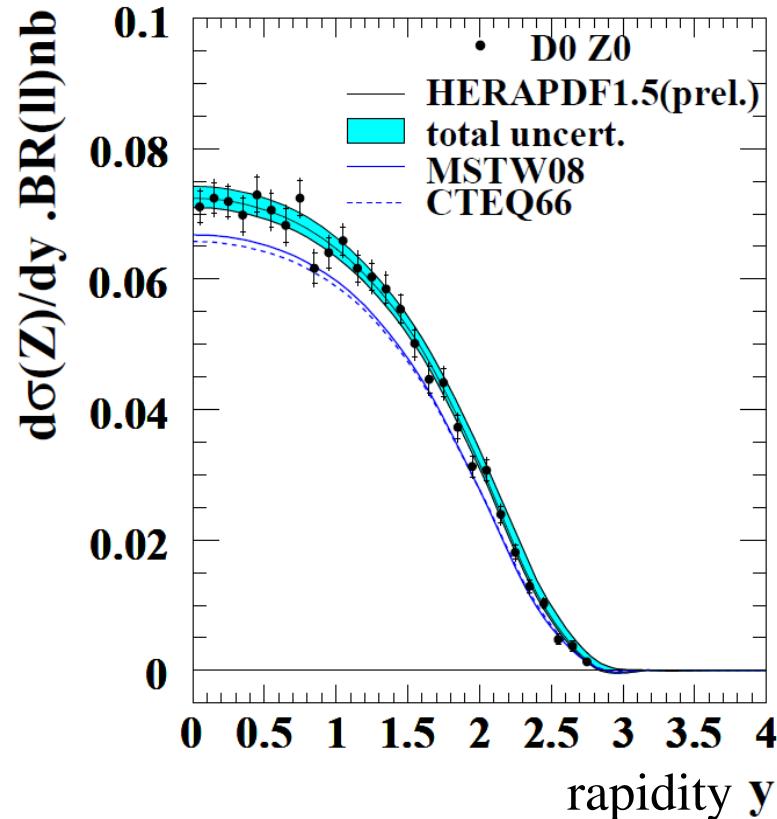
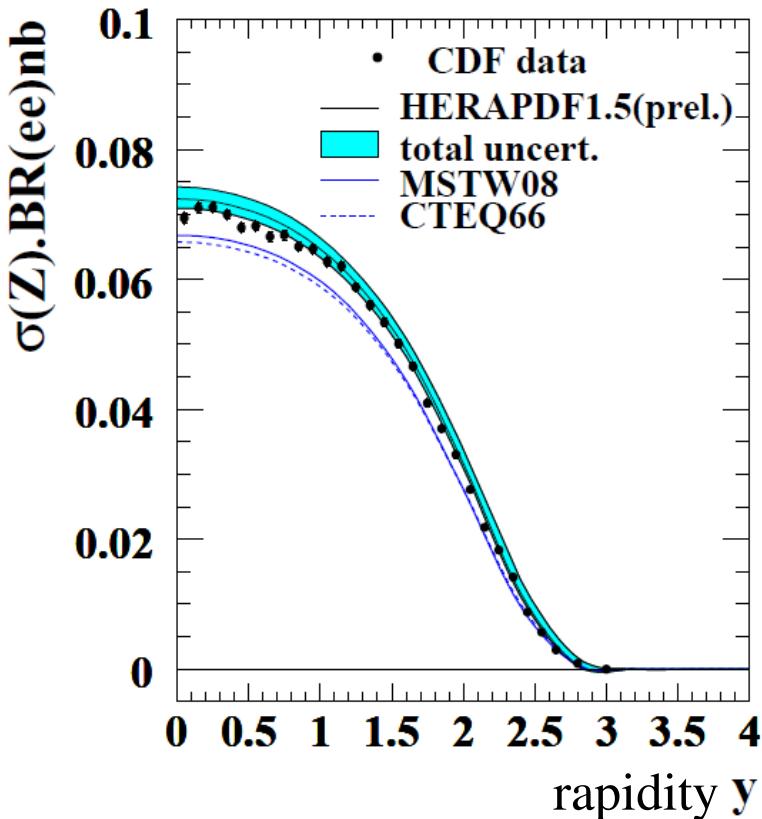


HERA covers  $x$  range of the LHC evolution in  $Q^2$  via DGLAP

# HERAPDF Predictions for Tevatron

$\sqrt{s} = 1.96 \text{ TeV}$

Z rapidity

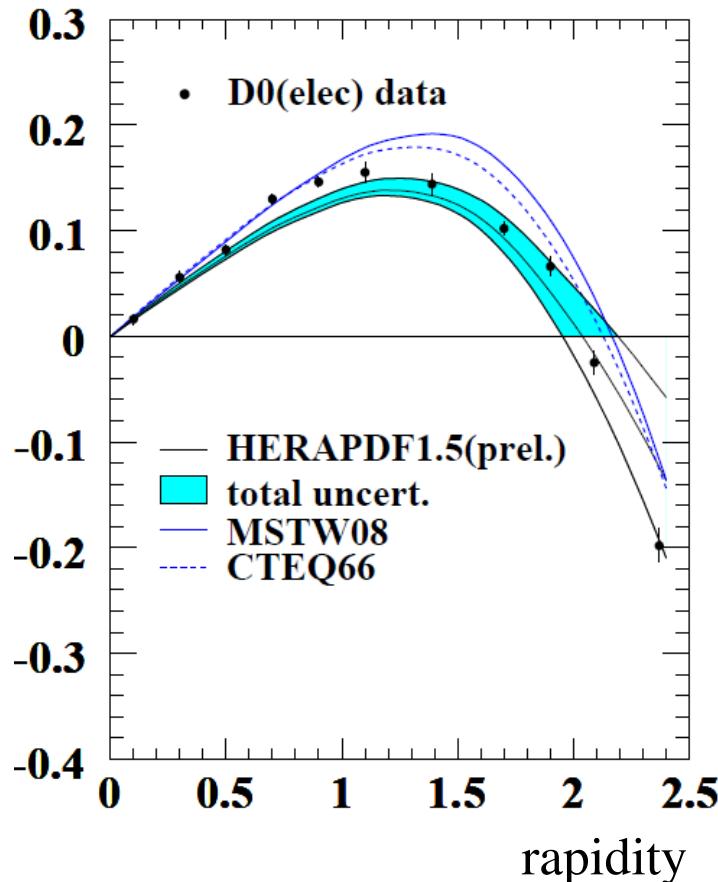
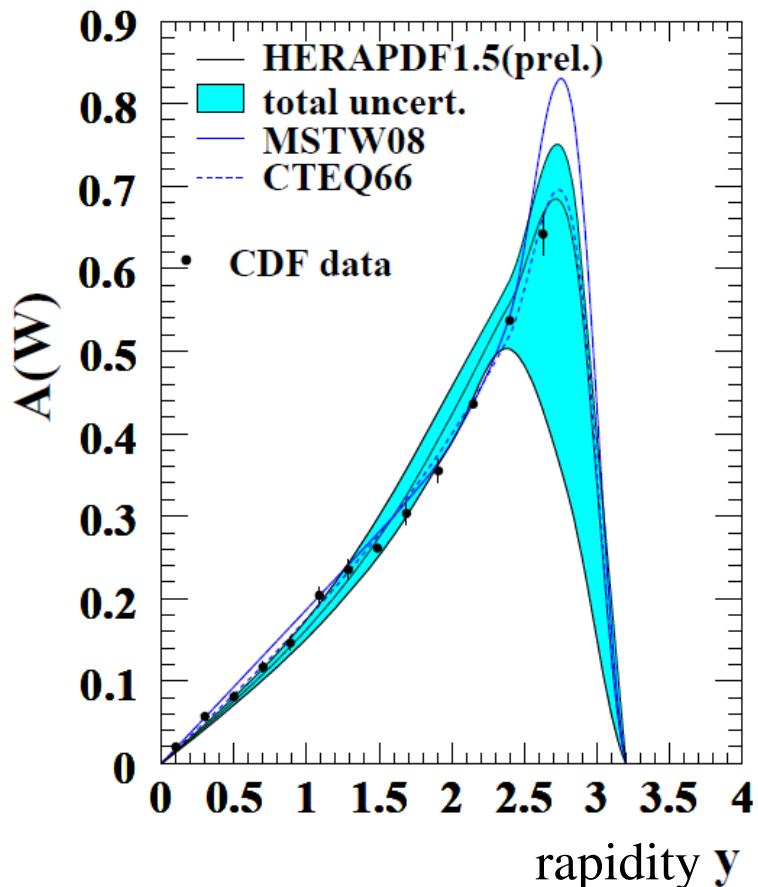


Predictions based on HERA PDFs describe Tevatron data well

# HERAPDF Predictions for Tevatron

$\sqrt{s} = 1.96 \text{ TeV}$

## W and W(lepton) asymmetry



Predictions based on HERA PDFs describe Tevatron data well

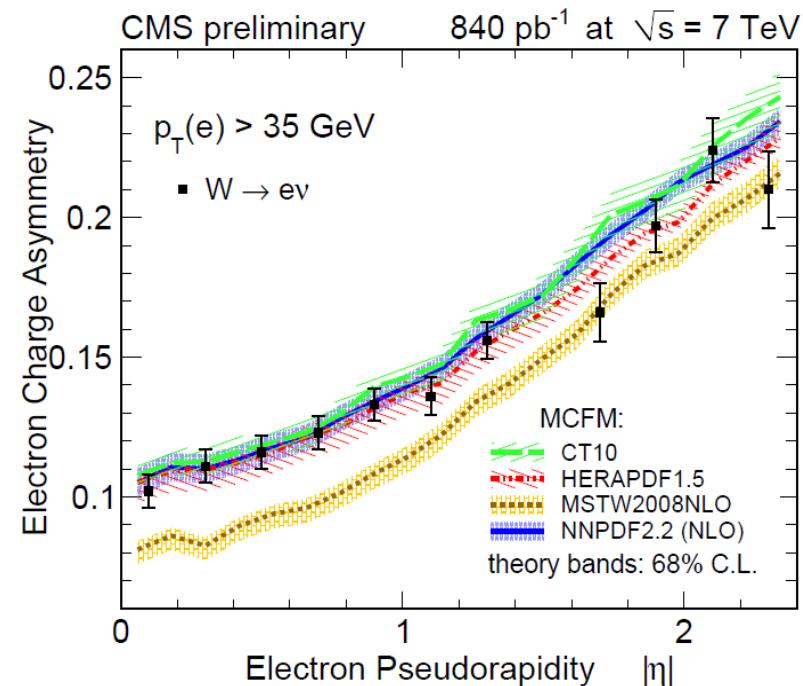
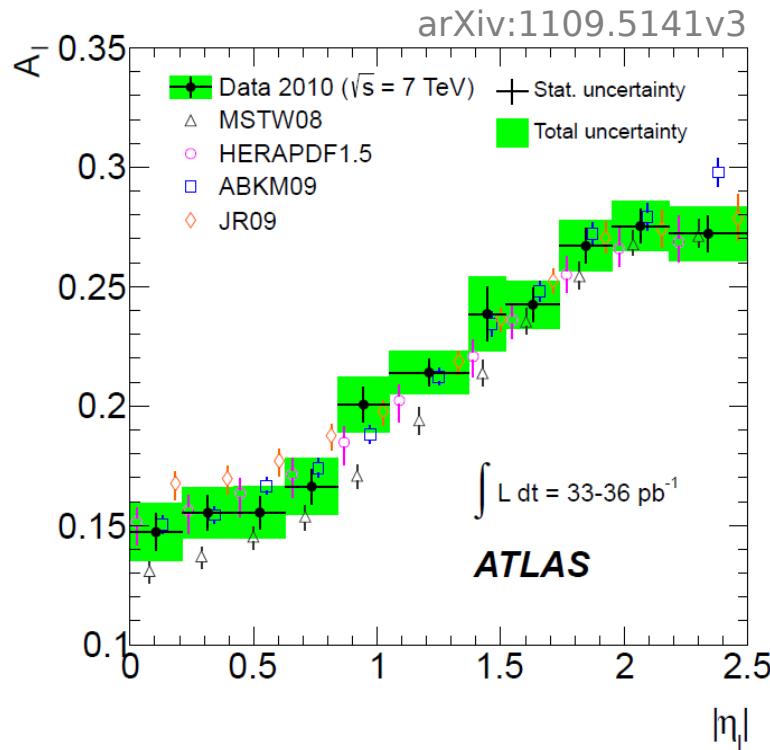
# HERAPDF Predictions for Asymmetries at LHC

W lepton asymmetry is sensitive to differences between u and d:

$$A_W = \frac{W^+ - W^-}{W^+ + W^-}$$

in terms of  
valence quarks:

$$A_W \approx \frac{u_v - d_v}{u_v + d_v + 2u_{sea}}$$



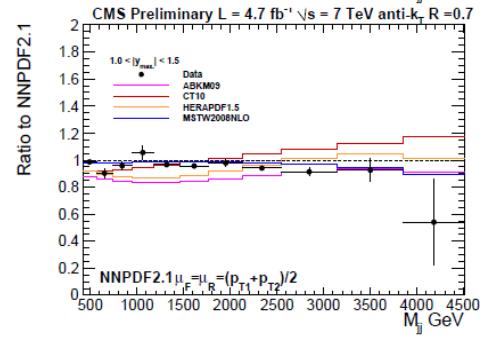
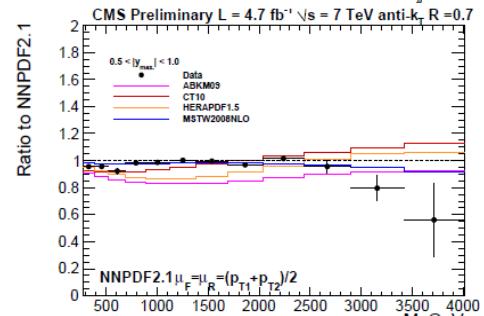
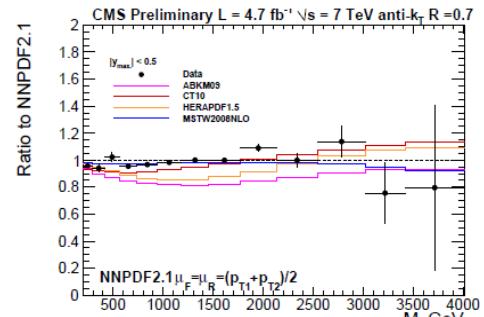
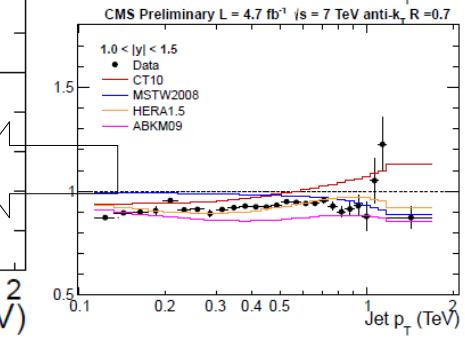
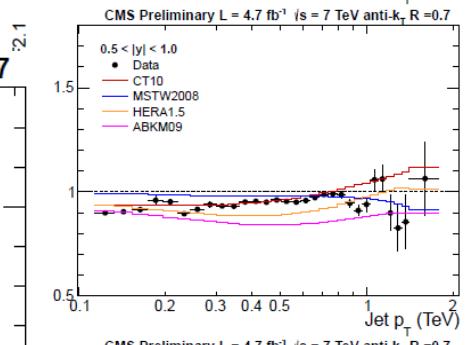
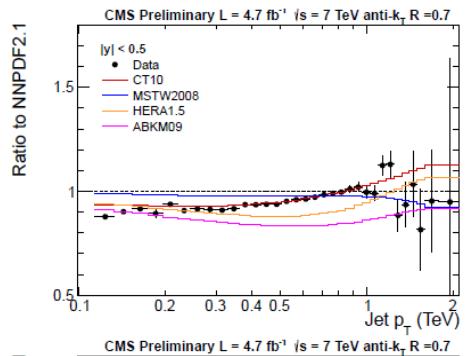
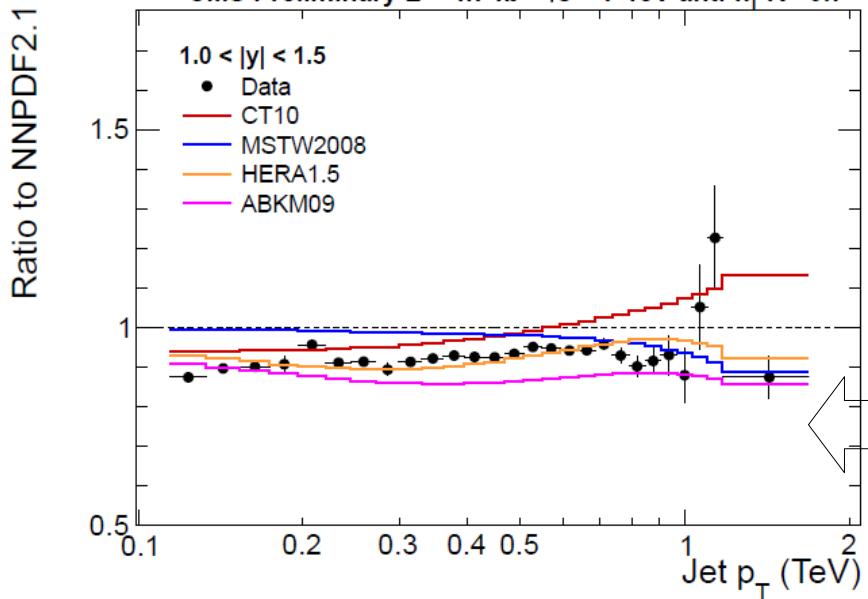
Latest results from ATLAS and CMS

# Example: Predictions for Jets at LHC

CMS-PAS-QCD-11-004

Jets have sensitivity to gluon and strong coupling constant

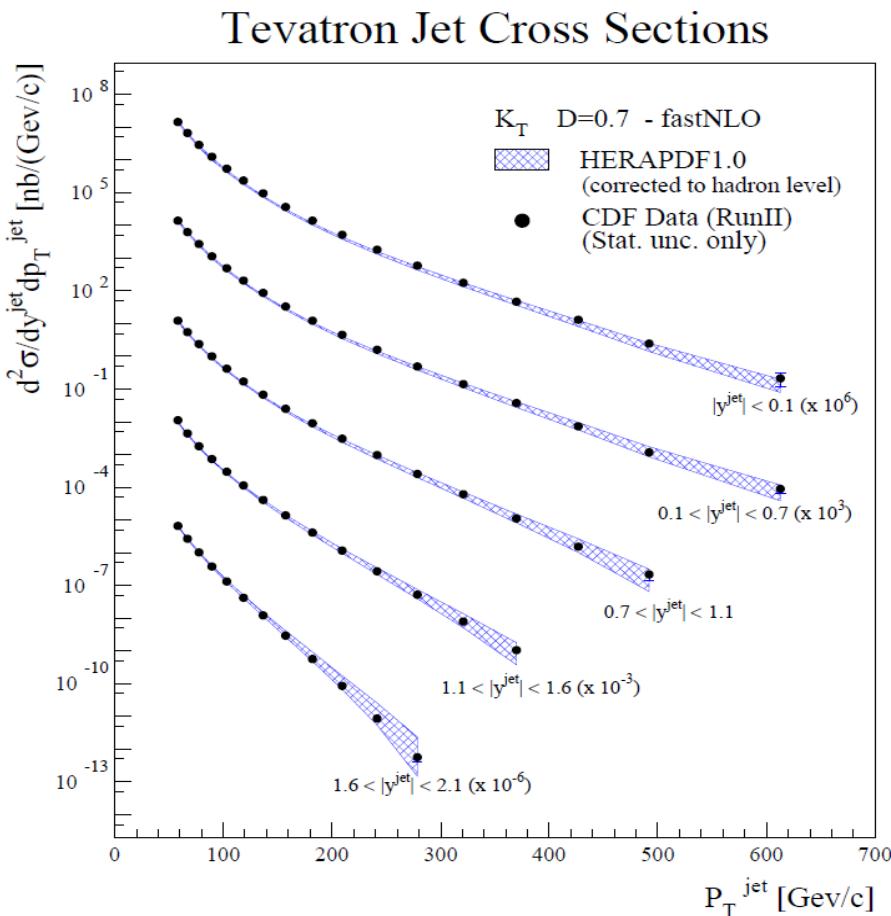
→ can help to understand and constrain gluon PDF at high- $x$   
(important for new physics)



Experimental uncertainties are comparable to theoretical ones  
→ using data in QCD fits can improve PDF uncertainties (correlations needed!)

# HERAPDF Predictions for Tevatron

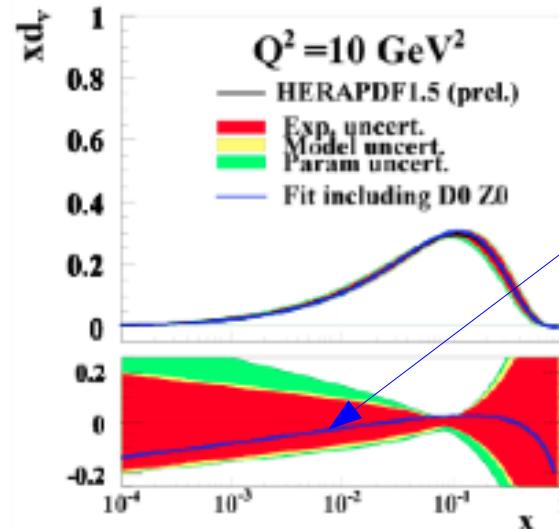
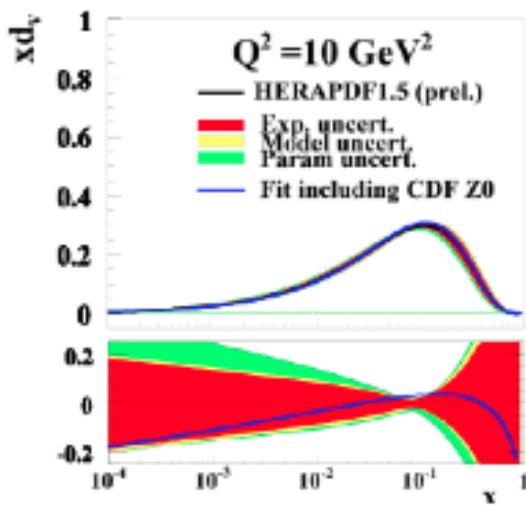
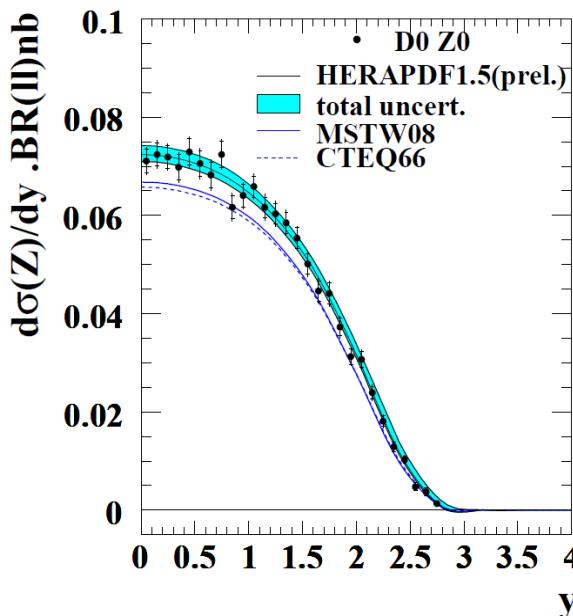
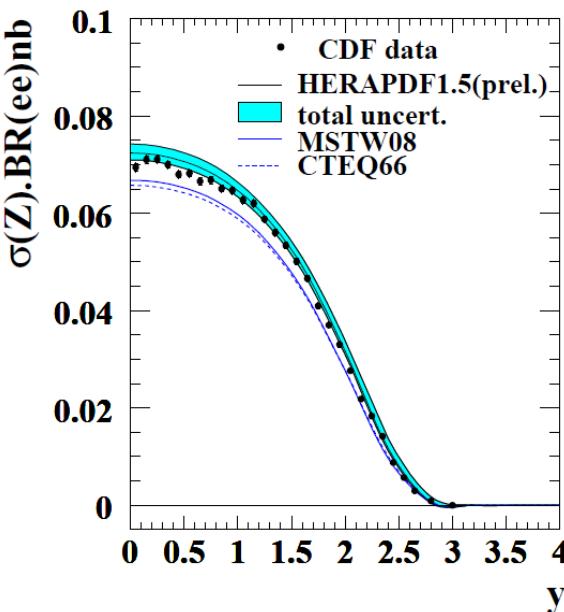
$\sqrt{s} = 1.96 \text{ TeV}$



→ if these data are fitted the resulting PDFs are within the HERAPDF1.5 errors bands

Predictions based on HERA PDFs describe Tevatron data well

# HERAPDF Predictions for Tevatron: Z rapidity



The description of CDF and D0 Z rapidity by HERAPDF1.5:

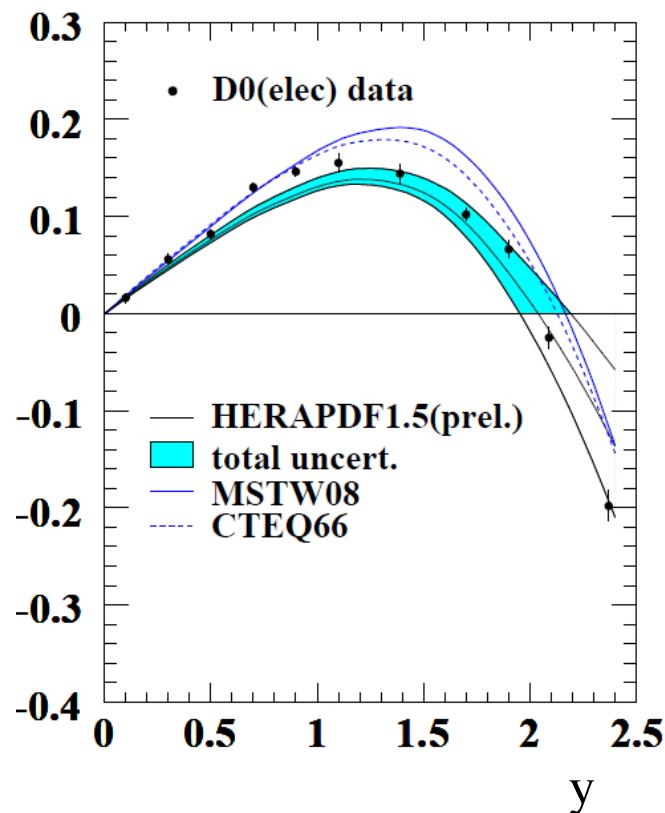
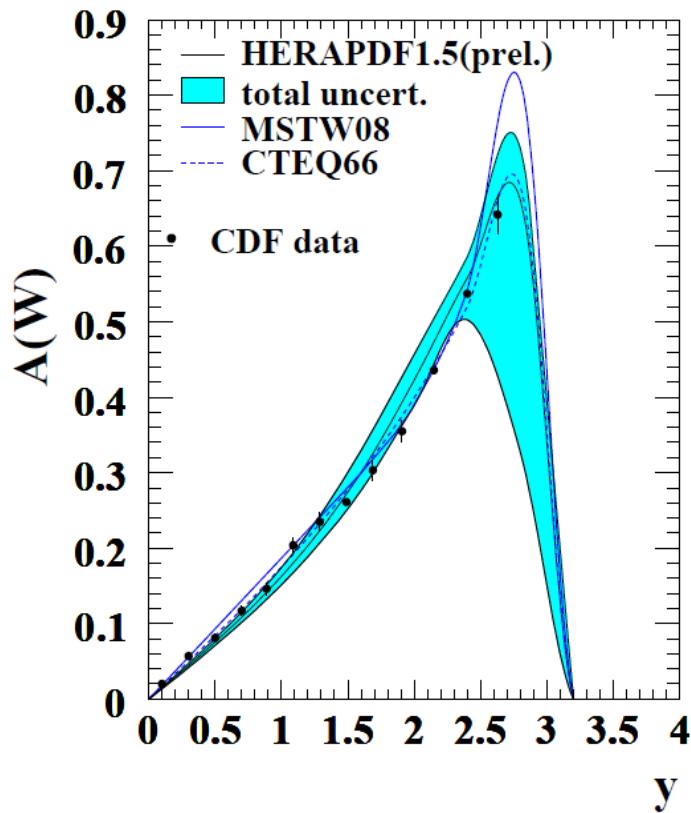
without fitting these data (not taking into account PDF uncert):  
 $\chi^2/\text{dof}=36/28$  CDF  
 $\chi^2/\text{dof}=23/28$  D0

**After fitting these data:**  
 $\chi^2/\text{dof}=27/28$  CDF  
 $\chi^2/\text{dof}=16/28$  D0

fit including TEVATRON data

Impact of Tevatron Z rapidity data on PDF shape is within uncertainties of HERAPDF

# HERAPDF Predictions for Tevatron: W asymmetry



Even without fitting the asymmetry data the agreement is quite good

After fit:

- $\chi^2/\text{dof} = 19/13$  CDF
- $\chi^2/\text{dof} = 25/11$  D0
  - the resulting PDFs lie within the HERAPDF1.5 error band

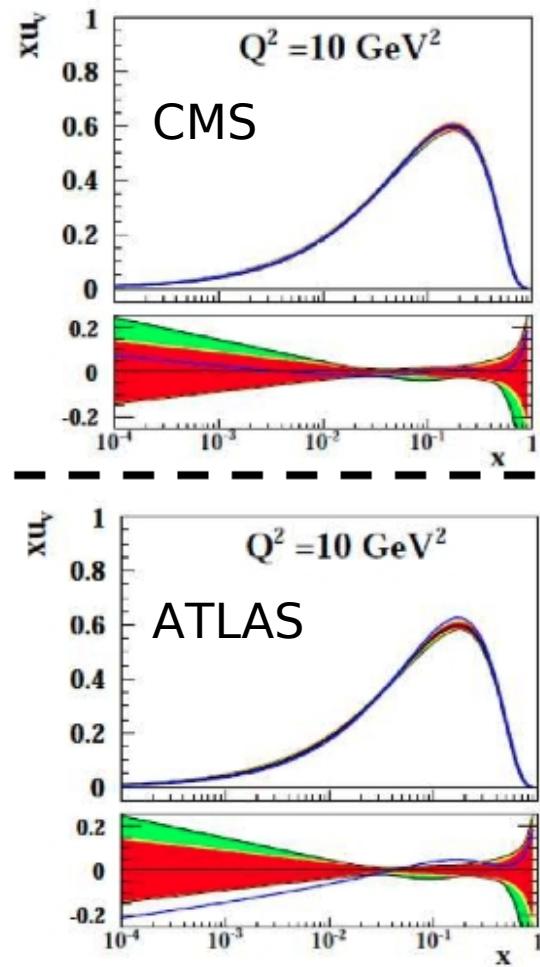
# HERADF Predictions for Asymmetries at LHC

Early LHC data are described fairly well

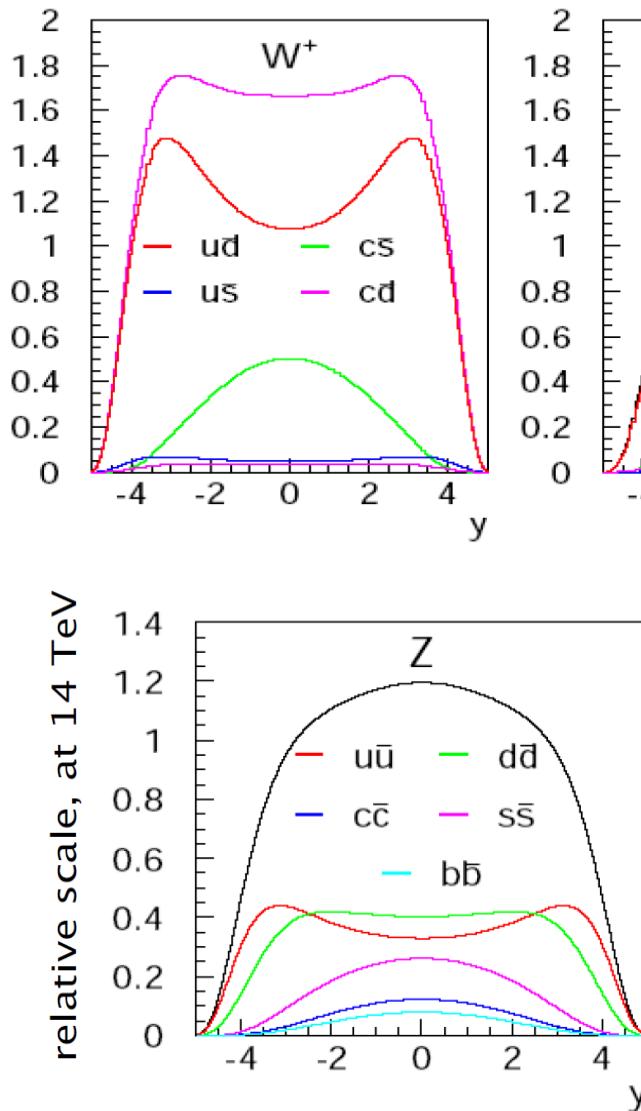
→ if these data are fit, the PDFs lie within the HERAPDF1.5 error band

	Before fit	After fit
- W asymmetry CMS:	$\chi^2/\text{dof} = 6.5/12$	3.7/12
- W asymmetry ATLAS:	$\chi^2/\text{dof} = 30/11$	16/11

ATLAS and CMS pull u valence quark in opposite directions



# Proton-Proton Collisions: W/Z production

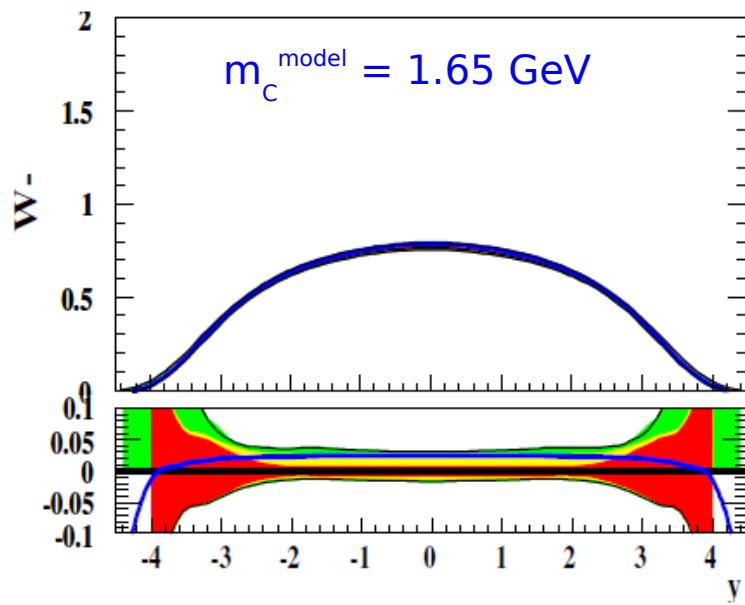


- for  $W$  **u** and **d** quarks dominate

- all flavours contribute to  $Z$

Precise parton distributions  
are needed for LHC analyses

# Impact on the LHC predictions



- variation of  $m_c^{\text{model}}$  changes predictions of Z/W cross sections at LHC by  $\sim 3\%$

A.M.Cooper-Sarkar,  
PDF4LHC, March 2010

- sensitivity to charm of the LHC cross section predictions comes from flavour sensitivity of the inclusive DIS data

$$xU = xu + xc \quad x\bar{U} = x\bar{u} + x\bar{c} \quad xD = xd + xs \quad x\bar{D} = x\bar{d} + x\bar{s}$$

- where  $U$  is fixed by  $F_2$  data

larger  $m_c^{\text{model}} \rightarrow$  less  $c$  in sea  $\rightarrow$  more  $u (= d)$

- important at low  $Q^2$  and low  $x$

# Heavy Quark treatment in QCD analysis

Factorisation:

$$F_2^{V,h}(x, Q^2) = \sum_{i=f, \bar{f}, g} \int_x^1 dz \cdot C_2^{V,i} \left( \frac{x}{z}, \frac{Q^2}{\mu^2}, \frac{\mu_F^2}{\mu^2} \alpha_s(\mu^2) \right) f_{i/h}(z, \mu_F, \mu^2)$$

i - number of active flavours in the proton       $m_c=1.5, m_b=4.7$  GeV

QCD analysis of the proton structure: treatment of HQ essential

Different prescriptions how to treat heavy quarks in PDF fits (HQ schemes):

Fixed Flavour Number Scheme (FFNS) *i-fixed*

c(b) quarks massive, only light flavours in the proton  $i=3(4)$

General-Mass Variable Flavour Number Scheme (GM-VFNS) *i-variable*

matched scheme, different implementation used by fit groups  $\rightarrow m_c^{\text{model}}$

Zero-Mass Variable Flavour Number Scheme (ZMVFNS)

all flavours massless (breaks at  $Q^2 \sim m_{HQ}^2$ )

# **QCD analysis of $F_2^{cc}$ data**

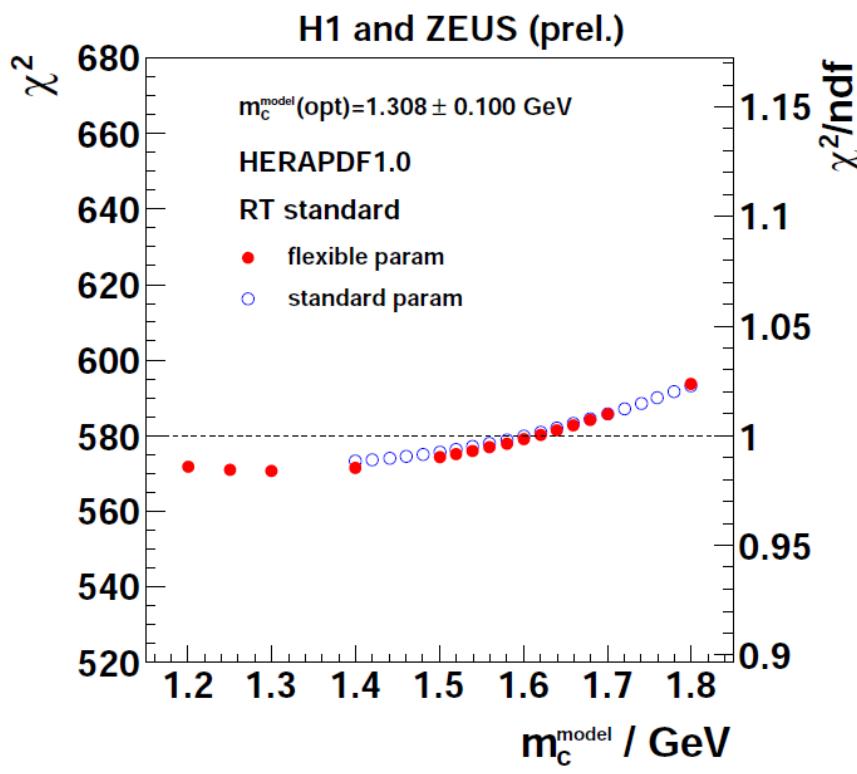
- different implementations of general mass variable flavour number scheme for heavy flavour treatment used in this study:

RT standard	used by MSTW08
RT optimised [arXiv:1006.5925]	
ACOT-full	used by CTEQ4,5,6HQ
S-ACOT- $\chi$	used by CTEQ6.5,6.6,CT10
ZMVFNS	used by NNPDF2.0

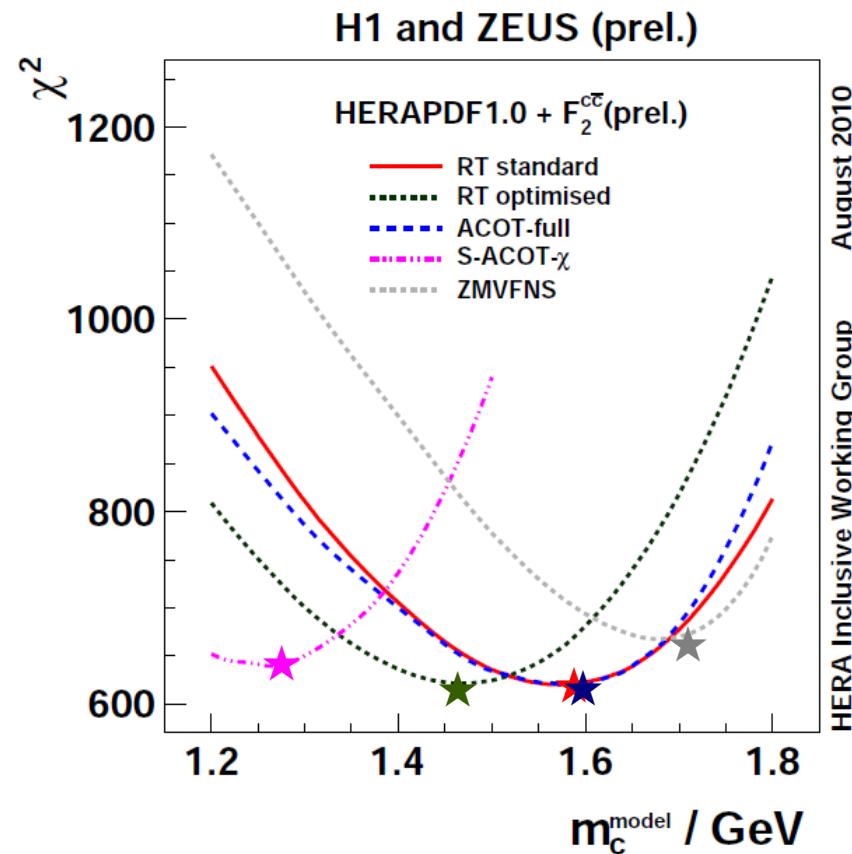
- the optimal value of parameter  $m_c^{\text{model}}$  is determined for each of these schemes ( $m_c^{\text{model}}(\text{opt})$ ), which gives the best description of the HERA data
  - PDFs are used in MCFM to calculate  $Z/W^\pm$  cross-section predictions

# Constraints on PDFs from HERA Charm Data

Inclusive ep data

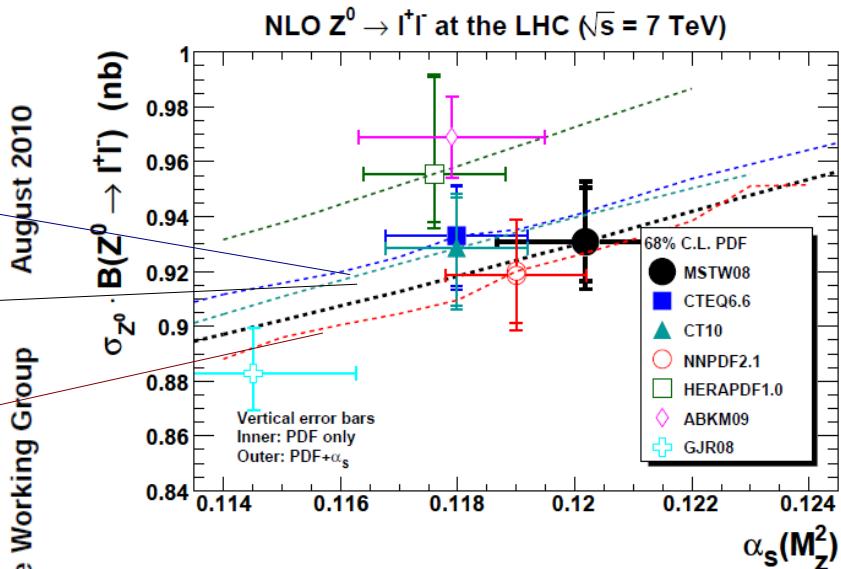
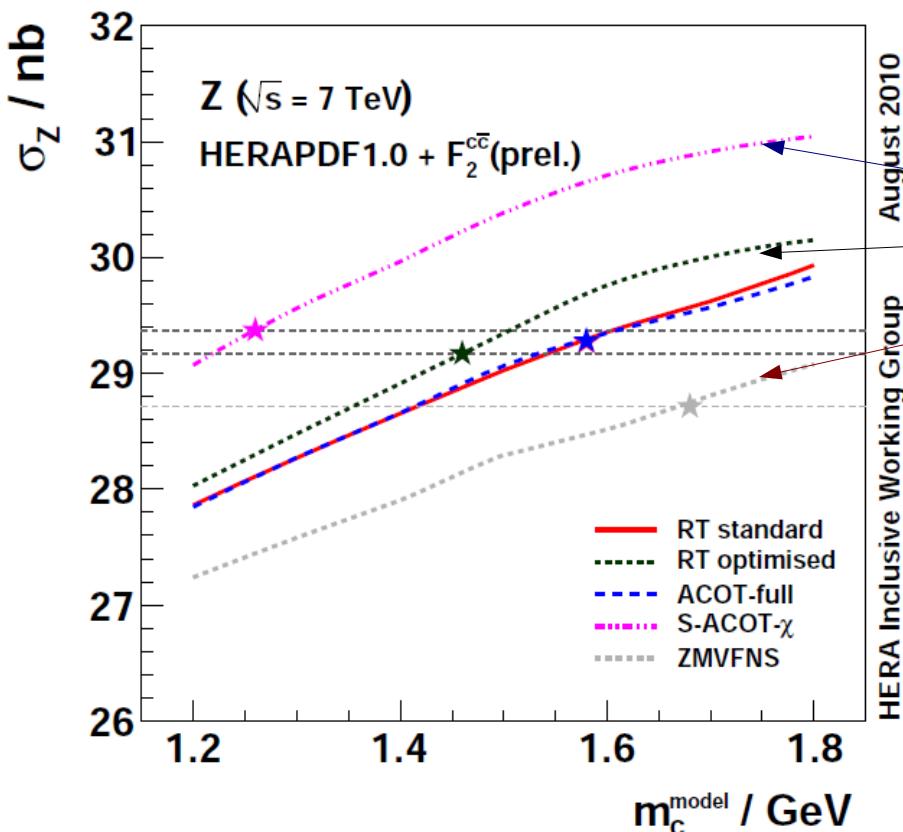


Different HQ schemes are tested



Different HQ schemes have different optimal  $m_c^{\text{model}}$

# Z/W cross sections at LHC

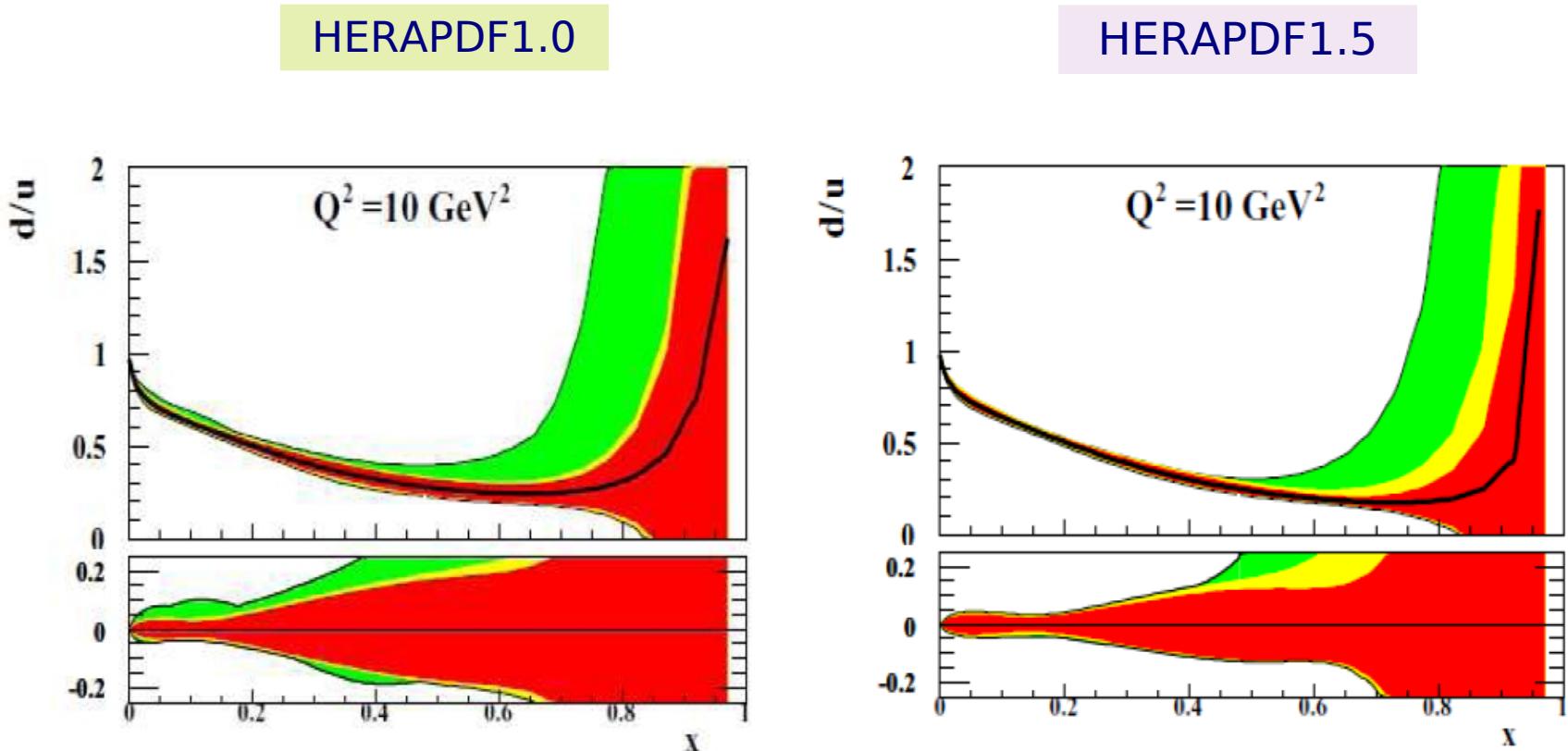


- comparison of Z cross sections  
 as a function of  $\alpha_s(M_Z^2)$

G.Watt, PDF4LHC 07.03.2011

(symbols indicate value of  $m_c^{\text{model}}(\text{opt})$ )

# HERAPDF 1.0 vs 1.5



Prediction based on HERAPDF1.5 have smaller experimental uncertainty in the u/d ratio