



# Combination of the Inclusive Diffractive Cross Sections at HERA

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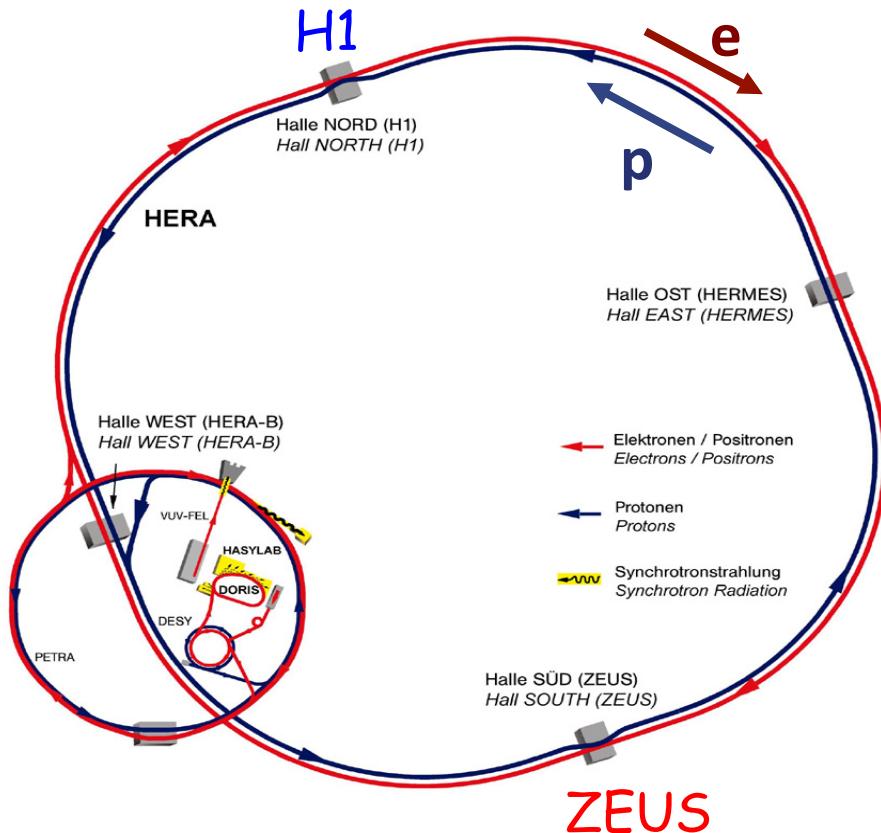
*on behalf of the H1 and ZEUS Collaborations*

- ❖ Diffraction in  $ep$  scattering
- ❖ Latest inclusive diffractive  $ep$  results
- ❖ Combination of diffractive cross sections

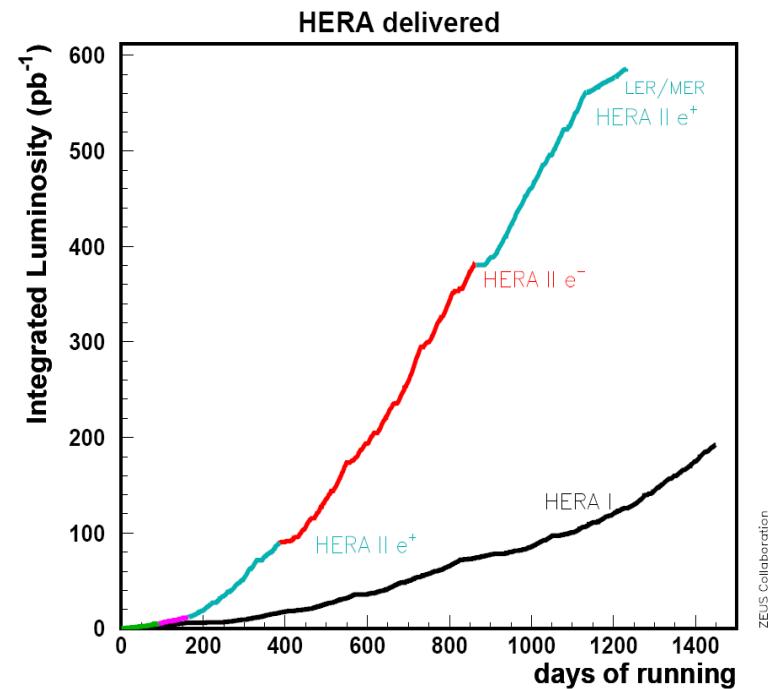


Universität Hamburg

# HERA Experiments



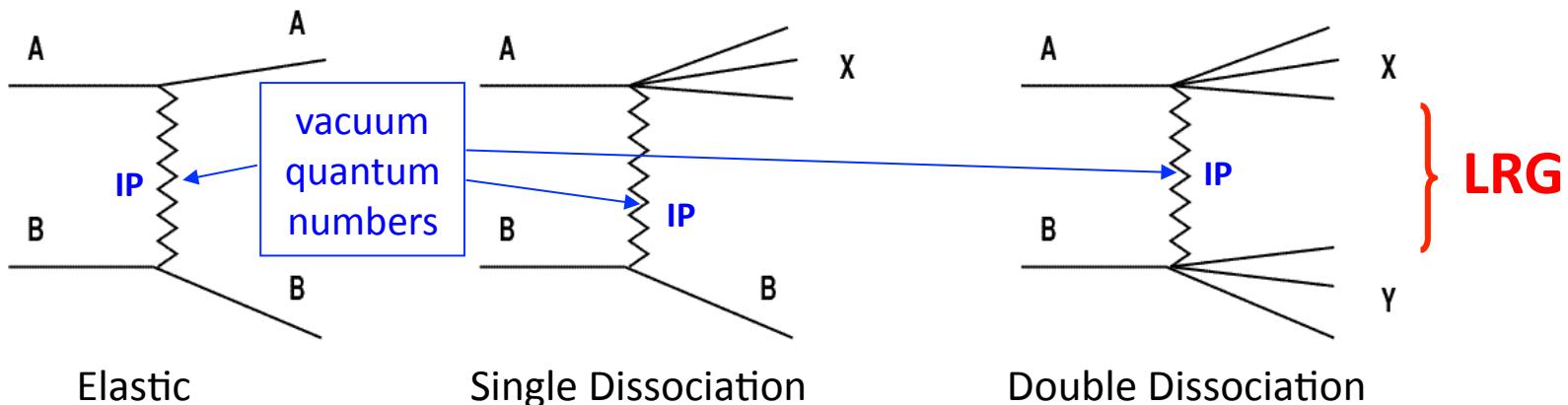
HERA I	1993-2000	$E_p = 820\text{-}920 \text{ GeV}$
HERA II	2003-2007	$E_p = 920\text{-}460\text{-}575 \text{ GeV}$
HERA I - II		$E_e = 27.5 \text{ GeV}$



0.5 fb $^{-1}$  collected by H1  
and ZEUS experiments

# Diffraction in Hadron Scattering

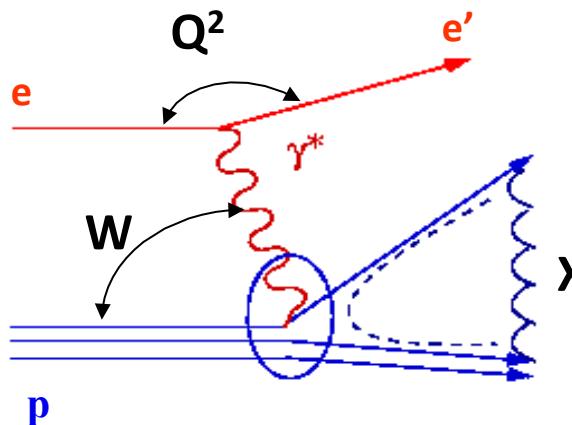
Diffraction is a feature of hadron-hadron interactions



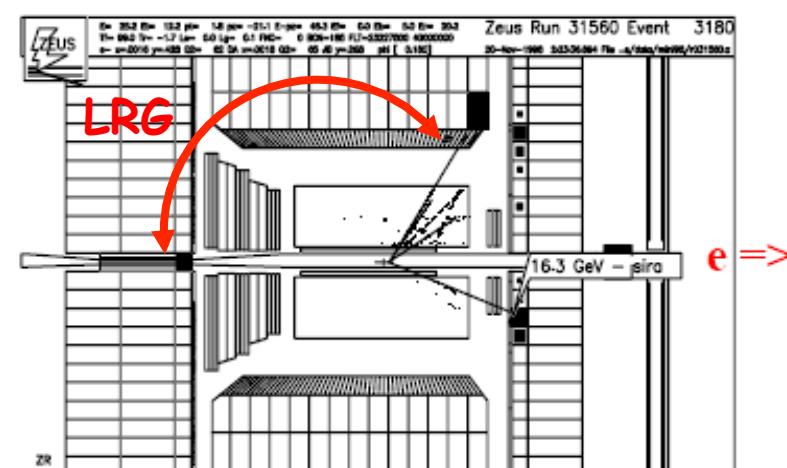
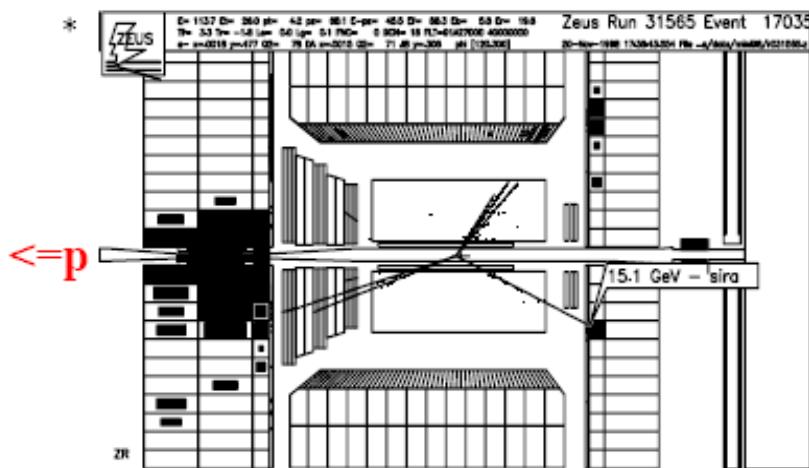
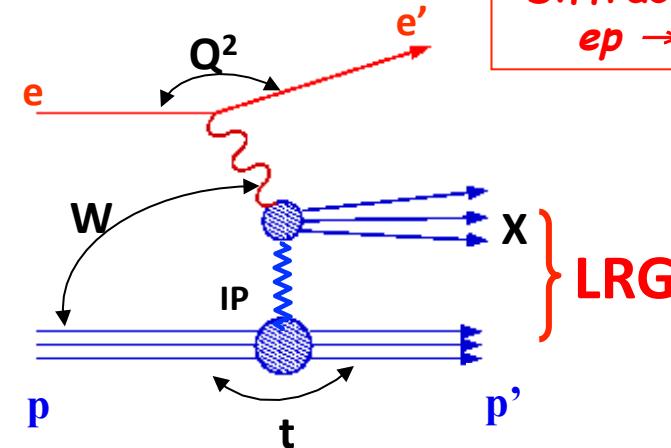
- ⇒ Beam particles emerge intact or dissociated into low-mass states  
→ Very small fractional momentum losses (within a few %)
- ⇒ Final-state systems separated by large polar angle  
(or pseudorapidity  $\eta = -\ln[\tan(\theta/2)]$ )  
→ **Large Rapidity Gap (LRG)**
- ⇒ Interaction mediated by t-channel exchange of an object with no quantum numbers (no colour)  
→ **Pomeron (IP)**

# Diffraction at HERA

**Standard DIS**  
 $ep \rightarrow e'X$



**Diffractive DIS**  
 $ep \rightarrow e'Xp'$



Diffractive events contribute up to 15% of the inclusive DIS cross section

# Kinematics and Cross Sections

$Q^2$  = virtuality of exchanged photon

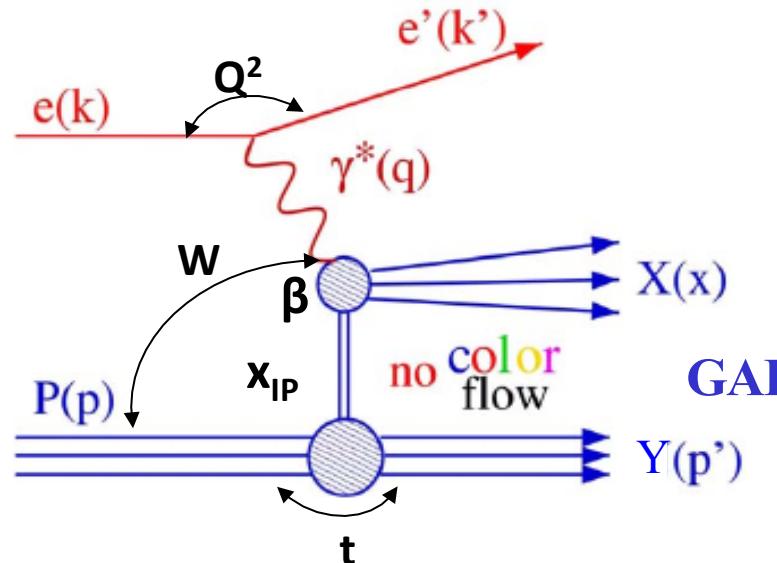
$x$  = Bjorken scaling variable

$y$  = inelasticity of virtual photon

$x_{IP}$  = fraction of proton momentum carried by IP

$\beta$  =  $x/x_{IP}$  = fraction of IP momentum carried by struck parton

$t$  = (4-momentum exchanged at p vertex) $^2$   
typically:  $|t| < 1 \text{ GeV}^2$



When Y is a resonance or a low mass state

↳ proton dissociation (p-diss)

$$\frac{d^4\sigma^{ep \rightarrow e'Xp}}{d\beta dQ^2 dx_{IP} dt} = \frac{2\pi\alpha^2}{\beta Q^4} Y_+ [F_2^{D(4)}(\beta, Q^2, x_{IP}, t) - \frac{y^2}{Y_+} F_L^{D(4)}(\beta, Q^2, x_{IP}, t)]$$

where  $Y_+ = 1 + (1-y)^2$

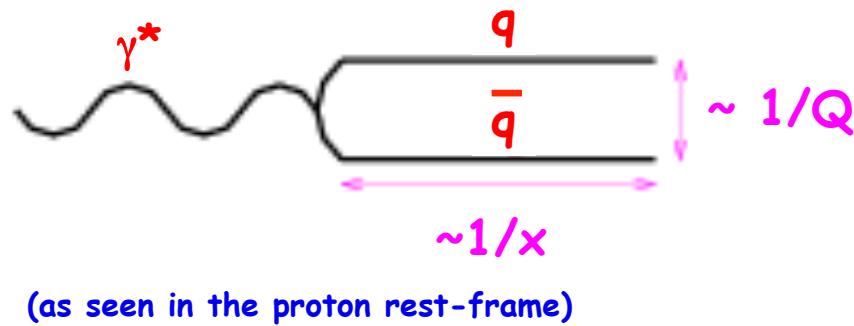
$$= \sigma_r^{D(4)}(\beta, Q^2, x_{IP}, t)$$

$$\sigma_r^{D(3)}(\beta, Q^2, x_{IP}) = \int \sigma_r^{D(4)}(\beta, Q^2, x_{IP}, t) dt$$

# Why Diffraction at HERA?

Real and virtual photons can fluctuate in hadronic states

$$\gamma^* \rightarrow \text{vector meson, } q\bar{q}, q\bar{q}g \dots$$



$Q$  = 'virtual mass' of the photon  
 $x$  = Bjorken scaling variable

At HERA very small  $x$  are reached:

- long hadronic lifetime of the photon
- diffractive photon-proton scattering in perfect analogy with diffractive hadron-hadron scattering

At HERA high  $Q^2$  are reached:

- short distances
- perturbative QCD

# Signatures and Selection Methods

## Proton Spectrometer (PS) method



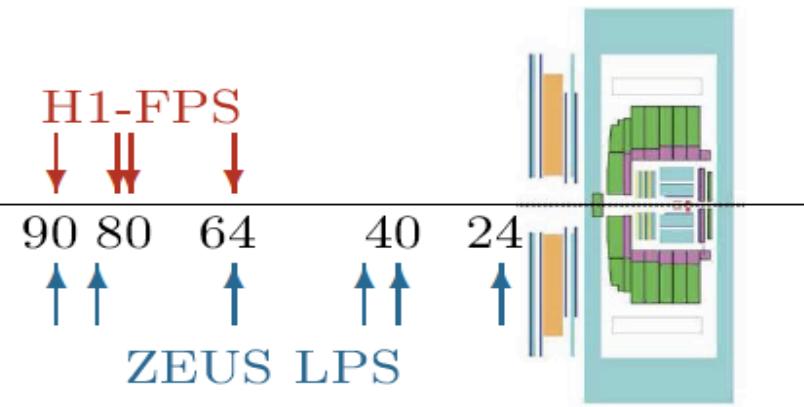
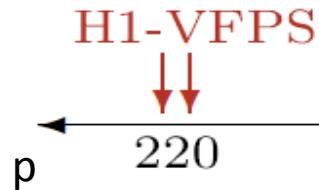
direct measurement of  $t, x_{IP}$   
high  $x_{IP}$  accessible  
no  $p$ -diss contribution



low statistics

# Signatures and Selection Methods

## Proton Spectrometer (PS) method



direct measurement of  $t$ ,  $x_{IP}$   
high  $x_{IP}$  accessible  
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low statistics

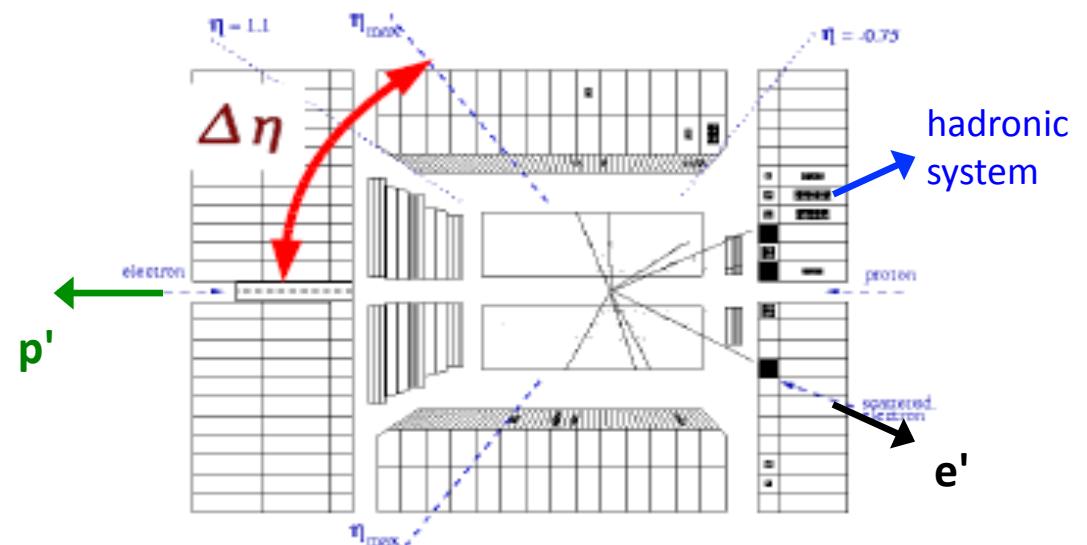


near perfect acceptance  
at low  $x_{IP}$



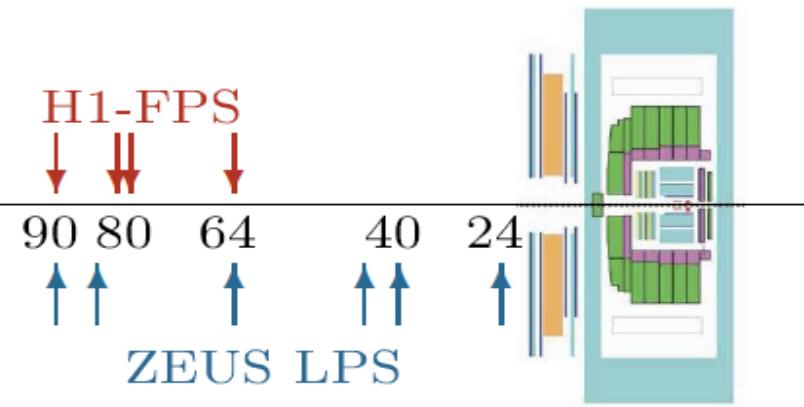
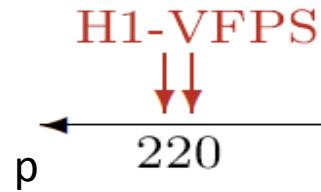
$p$ -diss contribution  
no  $t$  measurement

## Large Rapidity Gap (LRG) method



# Signatures and Selection Methods

## Proton Spectrometer (PS) method



direct measurement of  $t$ ,  $x_{IP}$   
high  $x_{IP}$  accessible  
no p-diss contribution



low statistics

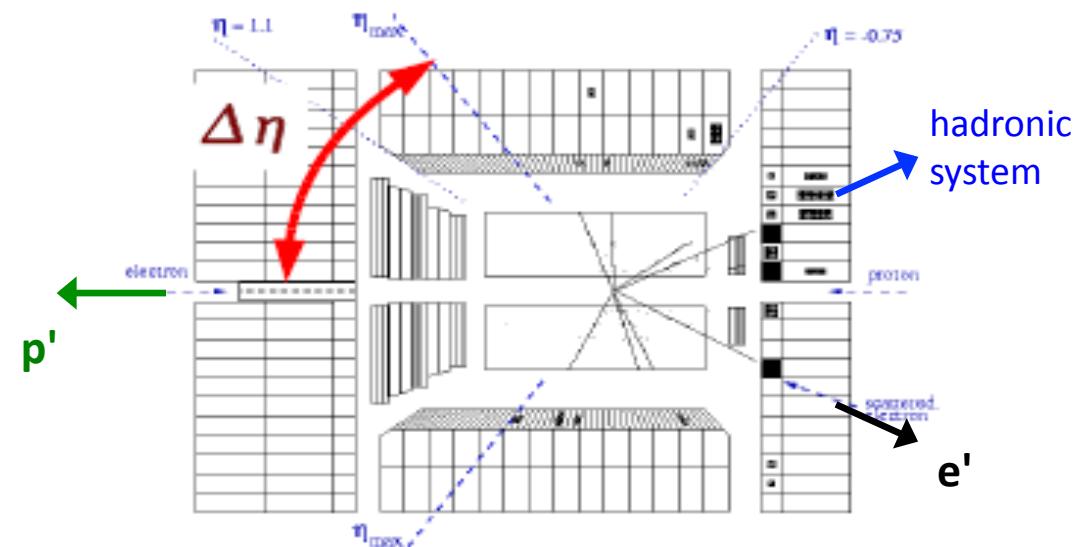


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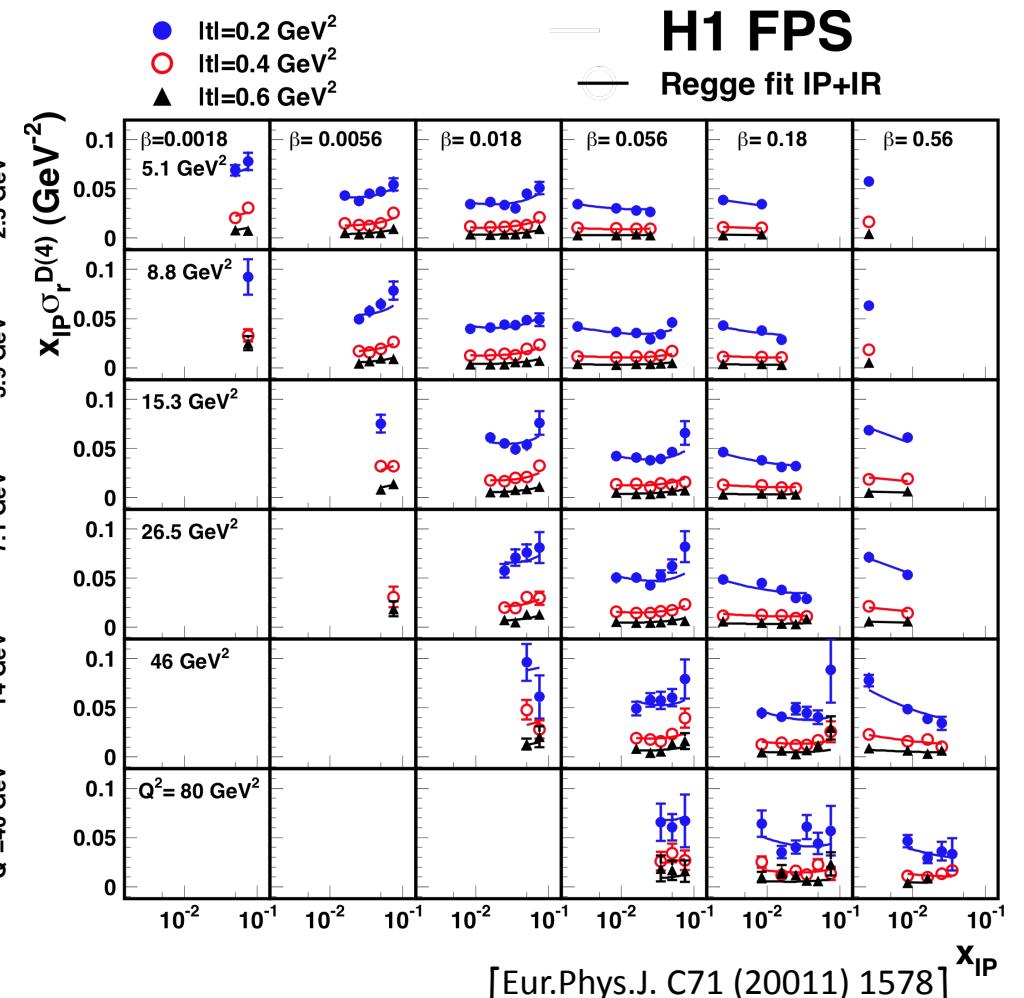
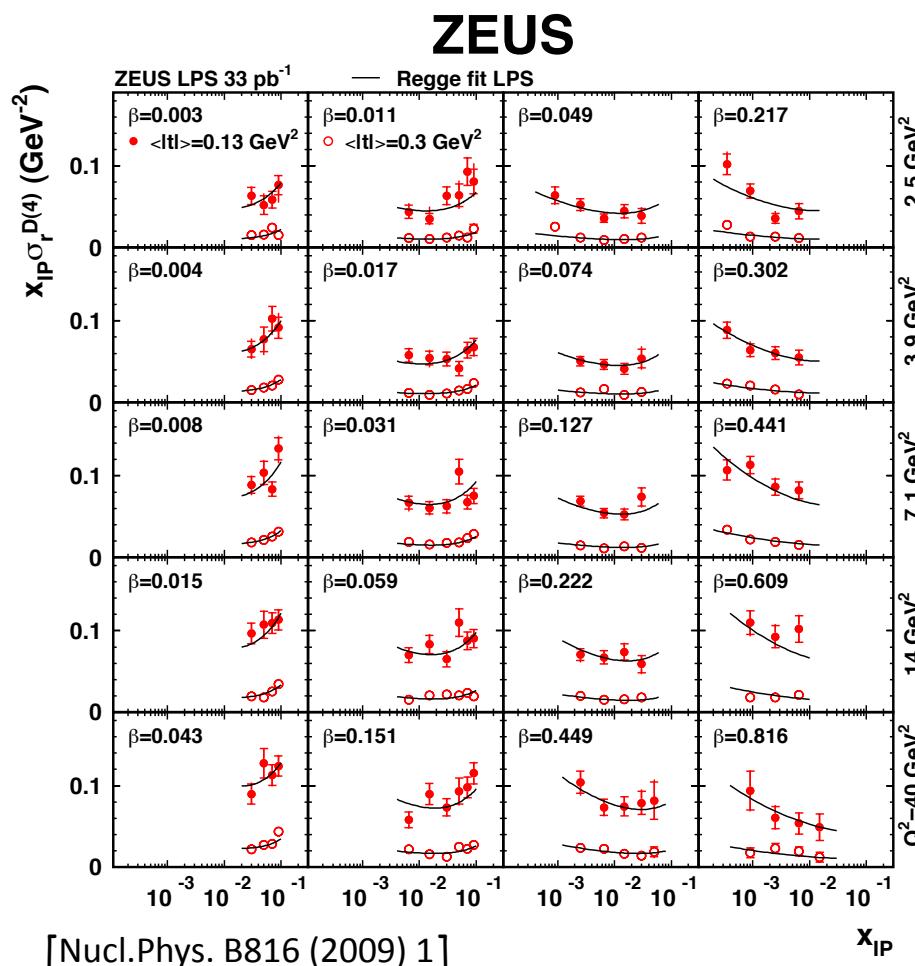


p-diss contribution  
no  $t$  measurement

## Large Rapidity Gap (LRG) method



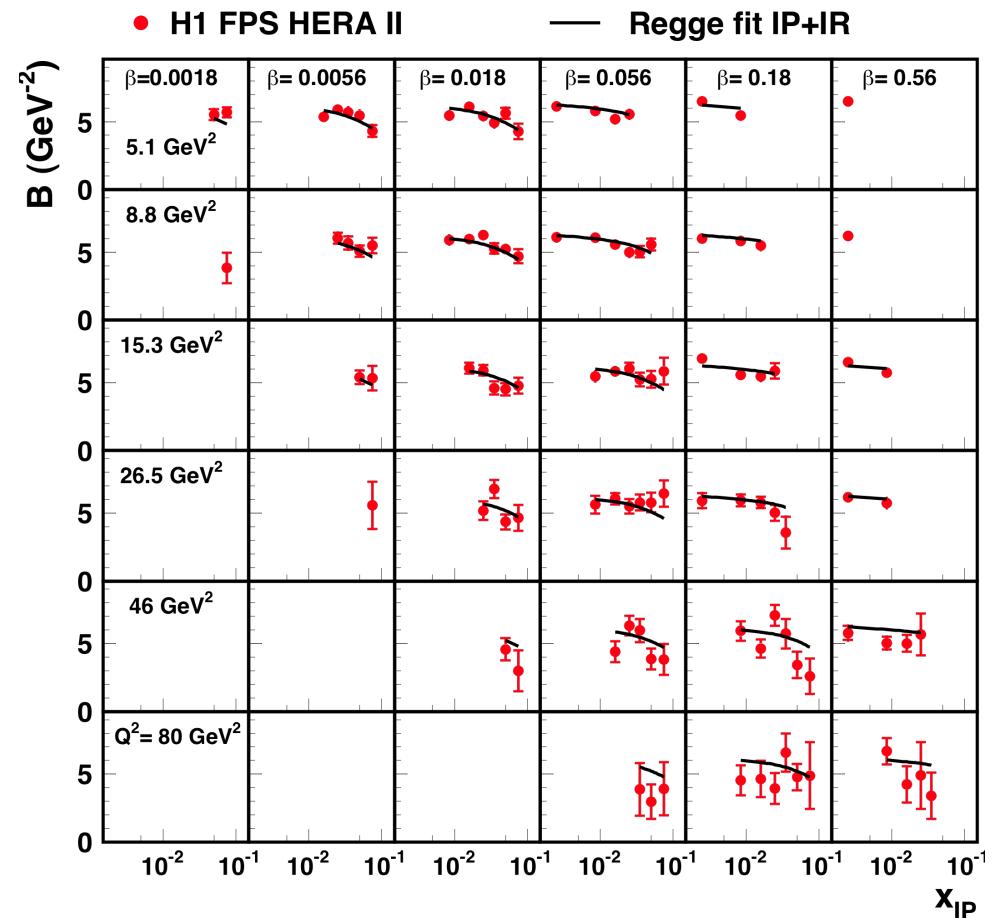
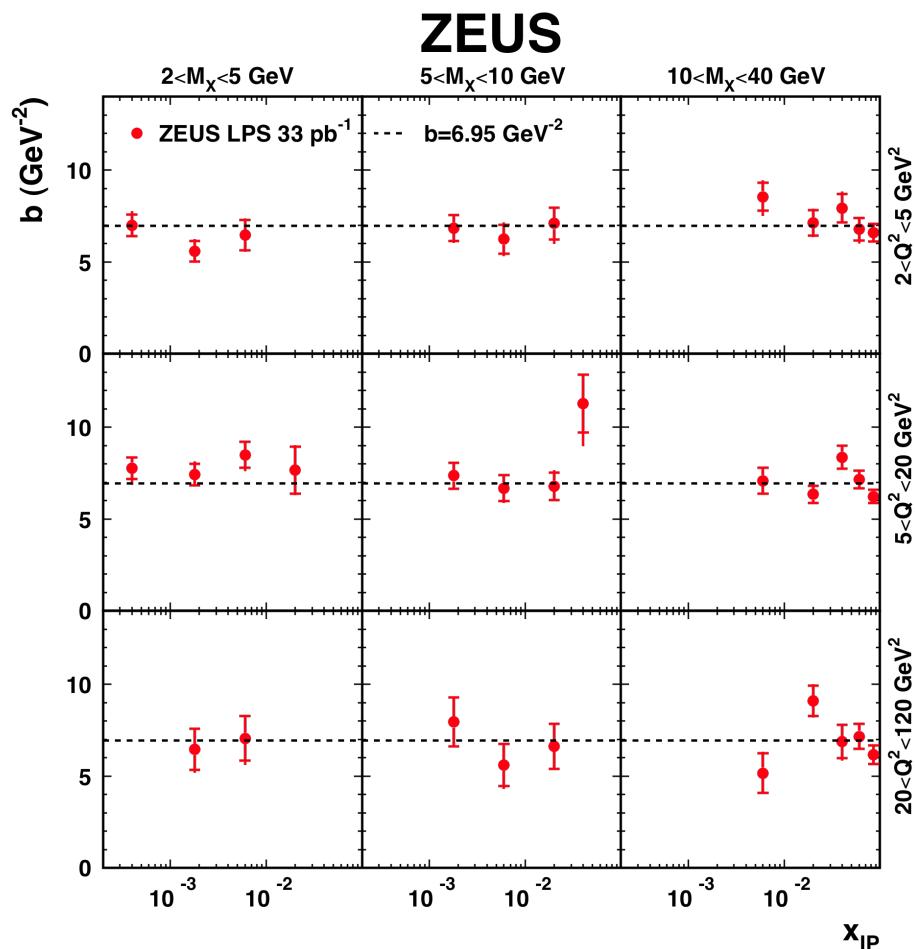
# $\sigma_r^{D(4)}$ from Proton Spectrometers



Precise measurement of  $\sigma_r^{D(4)}$  in bins of  $|t|$

$$d\sigma/dt \sim e^{bt}$$

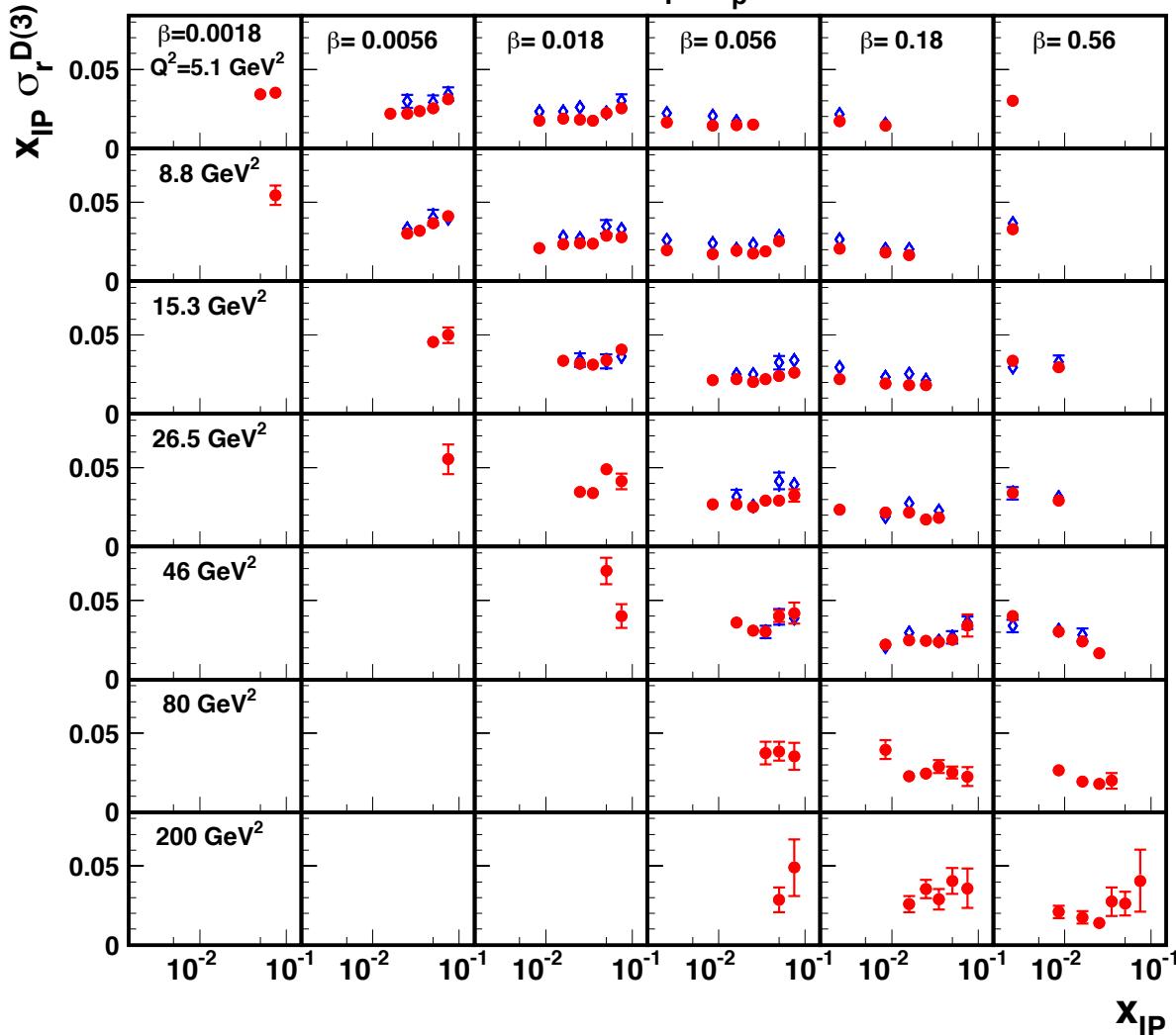
# t-slope



- ◆ ZEUS t-slope equal to  $7 \text{ GeV}^{-2}$  (constant through the kinematics)
- ◆ H1 t-slope between  $5$  and  $6 \text{ GeV}^{-2}$  (depending on  $x_{IP}$ )

# $\sigma_r^{D(3)}$ from Proton Spectrometers

- H1 FPS HERA II,  $M_Y = m_p$
- ◆ ZEUS LPS (interpol.),  $M_Y = m_p$



$$\sigma_r^{D(3)} = \int_{-1}^{t_{\min}} \sigma_r^{D(4)} dt$$

The measured  $b$  parameters are used to perform the integration to the range  $|t| < 1 \text{ GeV}^2$

Good agreement in shape between H1 and ZEUS

Fair agreement in normalization between H1 and ZEUS

H1 FPS HERA II norm unc  $\sim \pm 6\%$   
ZEUS LPS norm unc  $\sim + 11\% - 7\%$

H1 FPS HERA II / ZEUS LPS =  
 $0.85 \pm 0.01 (\text{stat}) \pm 0.03 (\text{syst})$   
 $+ 0.09 - 0.12 (\text{norm})$

# Data Sets for Combination

Data sets used for the first diffractive H1 & ZEUS combination

➤ H1 FPS HERA II

[Eur.Phys.J. C71 (2011) 1578]

Luminosity =  $156.6 \text{ pb}^{-1}$

Visible range  $|t| = 0.1 - 0.7 \text{ GeV}^2$

Norm unc  $\sim \pm 4.8\%$

➤ ZEUS LPS

[Nucl.Phys. B816 (2009) 1]

Luminosity =  $32.6 \text{ pb}^{-1}$

Visible range  $|t| = 0.09 - 0.55 \text{ GeV}^2$

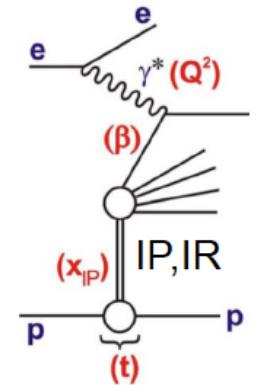
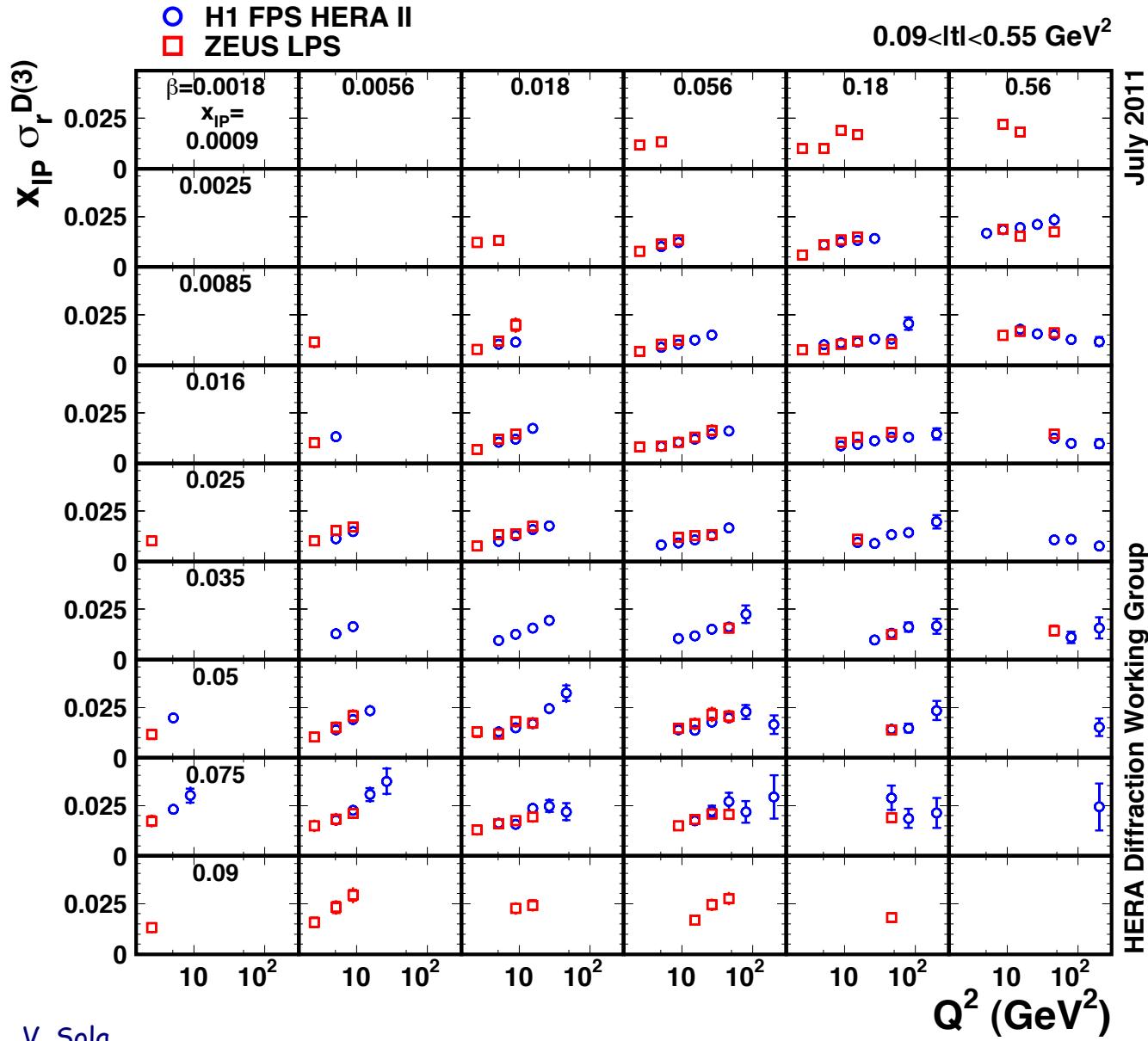
Norm unc  $\sim \pm 7\%$

Combination performed in the ZEUS visible  $t$  range  $|t| = 0.09 - 0.55 \text{ GeV}^2$

→ H1 FPS HERA II / ZEUS LPS =  $0.91 \pm 0.01 \text{ (stat)} \pm 0.03 \text{ (syst)} \pm 0.08 \text{ (norm)}$

Prior to combining ZEUS cross section points swam to H1 ( $Q^2, \beta, x_{IP}$ ) grid  
using ZEUS DPDF SJ [Nucl.Phys. B831 (2010) 1]

# $\sigma_r D(3)$ for Combination



Kinematic region covered by H1 and ZEUS data

$Q^2 = 2.5 - 200 \text{ GeV}^2$

$\beta = 0.0018 - 0.816$

$x_{IP} = 0.00035 - 0.09$

$|t| = 0.09 - 0.55$

# Combination Method

- ◊ The key assumption is that H1 and ZEUS experiments are measuring the same cross sections at the same kinematical points
- ◊ Averaging H1 and ZEUS diffractive data provides a model independent tool to study consistency of the data and to reduce systematic uncertainties
  - Experiments cross calibrate each other
- ◊ The combination method uses an iterative  $\chi^2$  minimization which includes full error correlations [A. Glazov, AIP Conf. Proc. 792 (2005) 237]

$$\chi_{exp}^2(M^{i,true}, \Delta\alpha_j) = \sum_i \frac{[M^{i,true} - (M^i + \sum_j \frac{\partial M^i}{\partial \alpha_j} \frac{M^{i,true}}{M^i} \Delta\alpha_j)]^2}{(\sigma_i \frac{M^{i,true}}{M^i})^2} + \sum_j \frac{(\Delta\alpha_j)^2}{\sigma_{\alpha_j}^2}$$

for a single data set

*i* = measured data point  
*j* = correlated systematic error source

$M^i$  measured central values

$\sigma_i$  statistical and uncorrelated systematic uncertainties

$M^{i,true}$  fitted combined H1 - ZEUS values

$\sigma_{\alpha_j}$  correlated systematic uncertainties

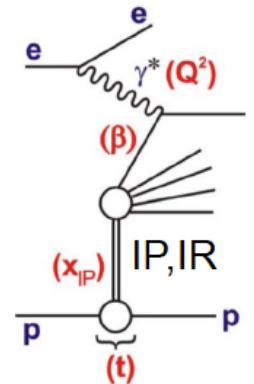
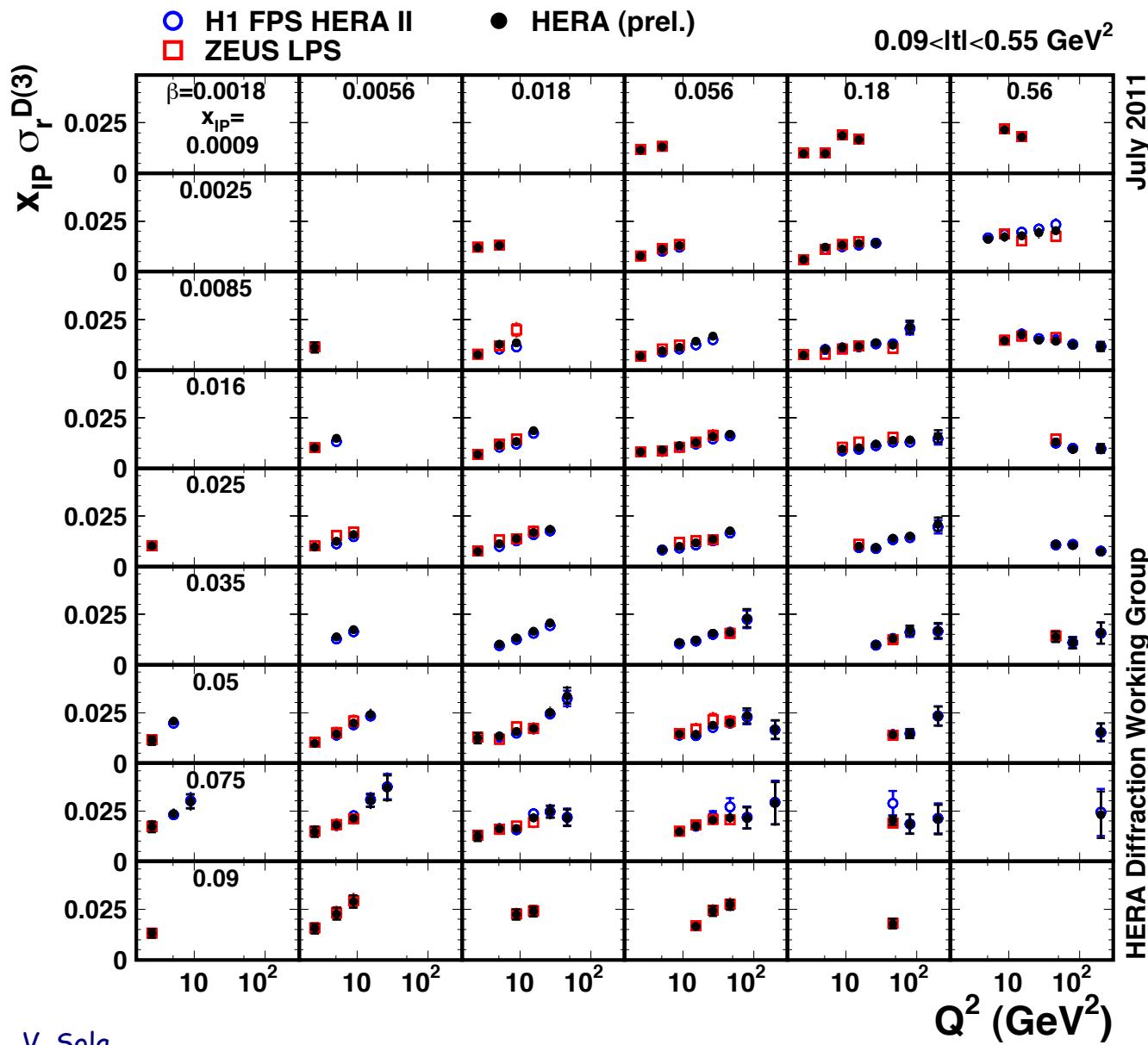
⇒ Full  $\chi^2$  is the sum over all  $\chi_{exp}^2$

# Procedural Uncertainties

Four procedural uncertainties are introduced

1. ZEUS swimming factors from H1 DPDF Fit B [Eur. Phys. J. C48 (2006) 715]  
→ Average effect ~ 1%
2. Additive vs multiplicative nature of the error sources  
→ Average effect ~ 4%
3. Correlated systematic error sources between H1 and ZEUS  
Identified 4 uncertainties of possible common origin
  - ♦ electromagnetic energy scale
  - ♦ background subtraction
  - ♦  $x_{IP}$  reweighting
  - ♦  $t$  reweightingCompare  $2^4$  averages taking all pairs as corr/uncorr in turn  
→ Average effect ~ 1%
4. Point-to-point correlated vs uncorrelated systematic error sources  
→ Average effect < 1%, up to 10% at lowest  $x_{IP}$

# Combined $\sigma_r D(3)$

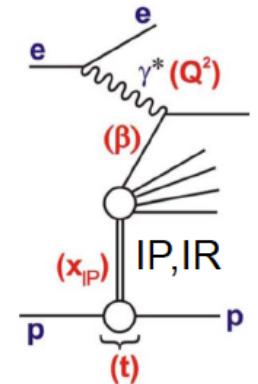
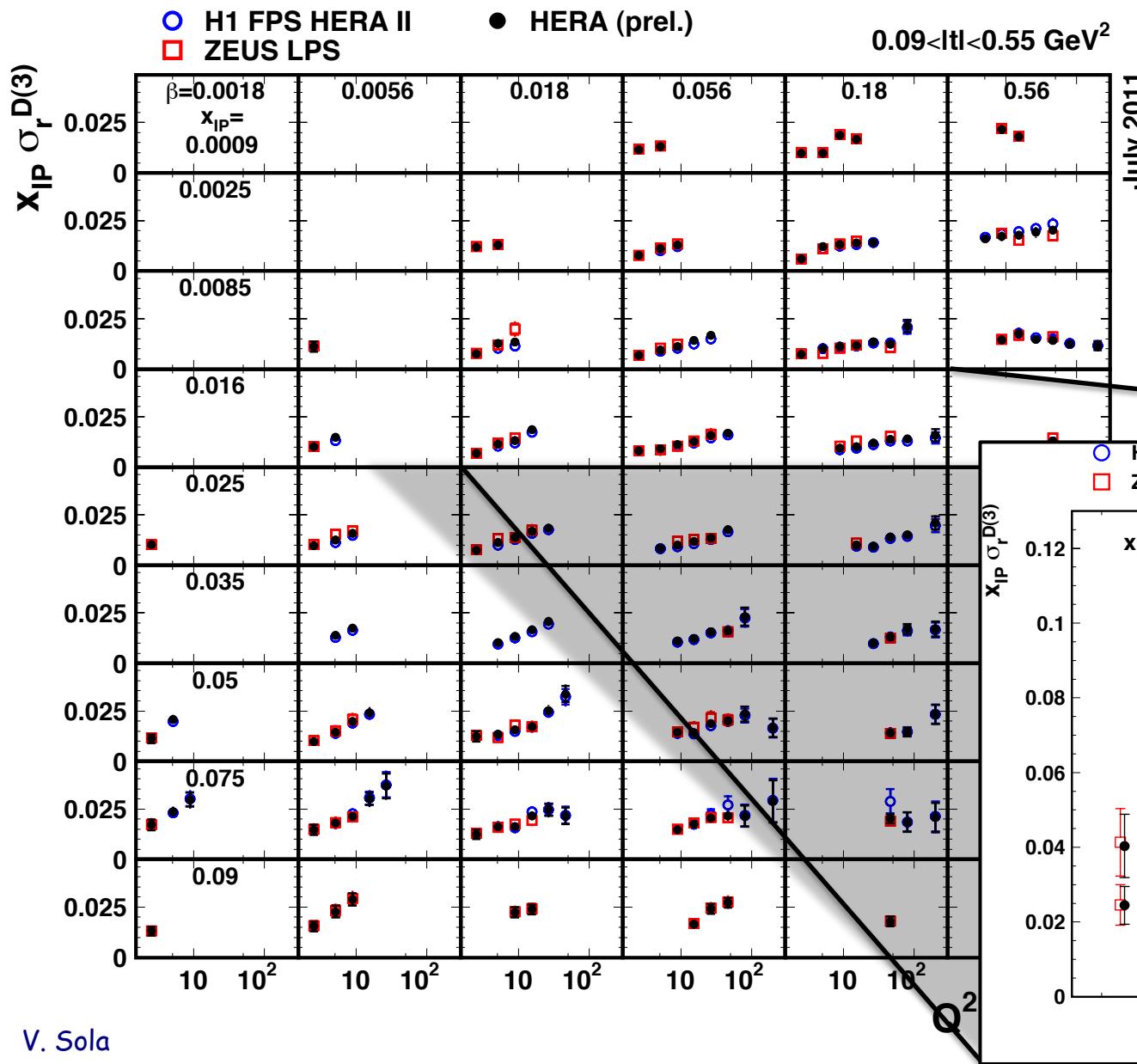


$$\chi^2/\text{ndf} = 52/58$$

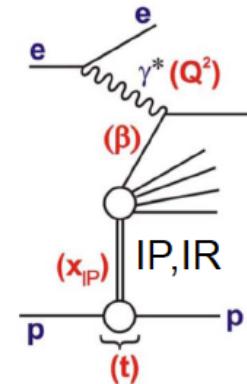
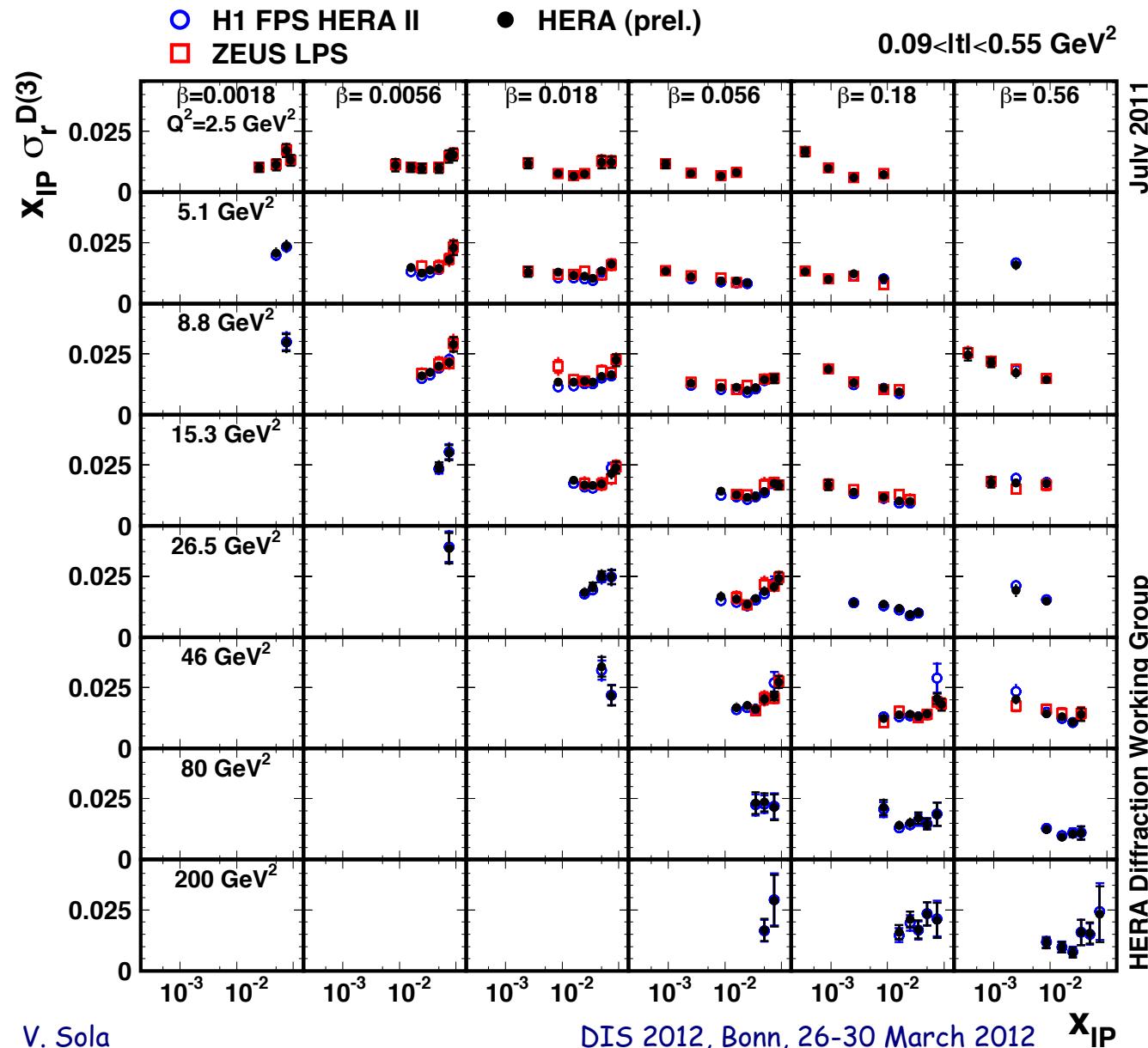
Nice and precise measurement of the scaling violation in diffraction

Improvement in precision with respect to the H1 FPS HERA II data by  $\sim 20\%$

# Combined $\sigma_r D(3)$



# Combined $\sigma_r^{D(3)}$



$$\chi^2/\text{ndf} = 52/58$$

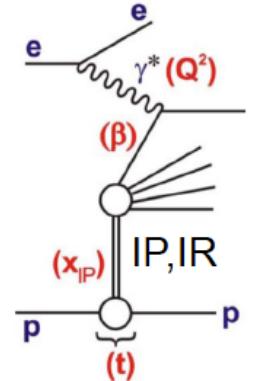
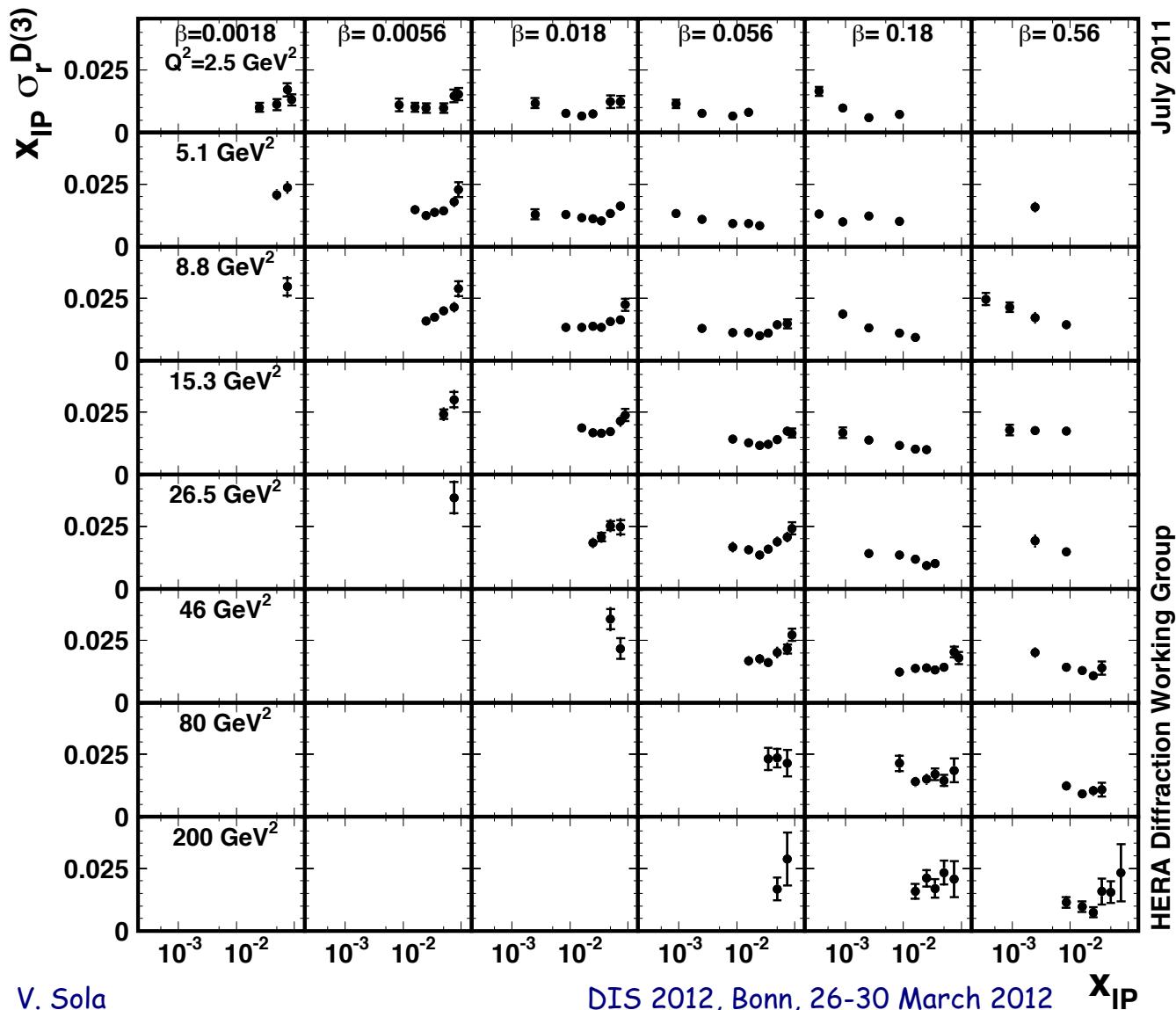
Nice and precise measurement of the  $X_{IP}$  dependence of  $\sigma_r^{D(3)}$

Improvement in precision with respect to the H1 FPS HERA II data by  $\sim 20\%$

# Combined $\sigma_r^{D(3)}$

● HERA (prel.)

$0.09 < |t| < 0.55 \text{ GeV}^2$



$$\chi^2/\text{ndf} = 52/58$$

Nice and precise measurement of the  $X_{IP}$  dependence of  $\sigma_r^{D(3)}$

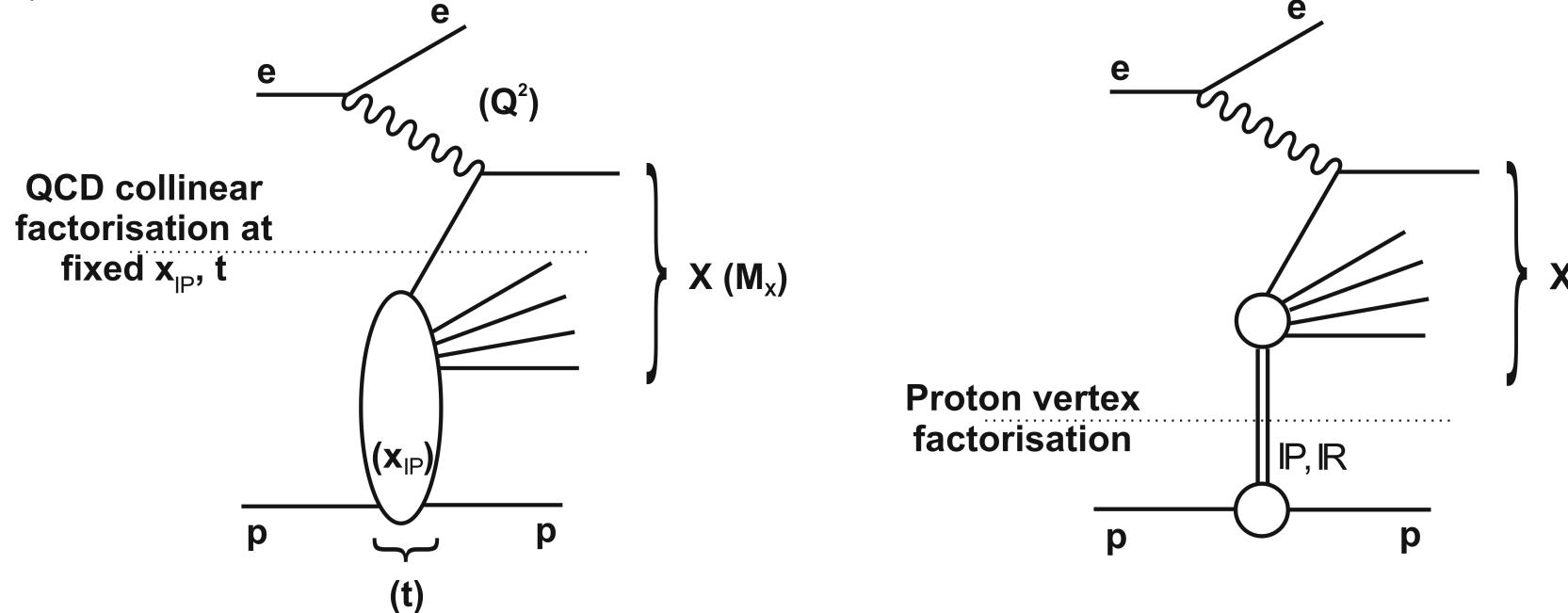
Improvement in precision with respect to the H1 FPS HERA II data by  $\sim 20\%$

# Summary

- ✓ 15 years of running HERA provided unique diffractive data
- ✓ First combination of the H1 and ZEUS diffractive data
  - ⇒ combined proton-tag results
  - ⇒ consistency between datasets
  - ⇒ the two experiments calibrate each other resulting in a reduction of systematic uncertainties
  - ⇒ results are about to be published
- ✓ Looking forward to combining all LRG, FPS and VFPS data

Thank You

# QCD Factorization in Hard Diffraction



The QCD factorization theorem in diffractive DIS allows to write the diffractive cross section as a convolution of universal diffractive parton densities  $f_i^D(x, Q^2, x_{IP}, t)$  and partonic cross sections

$$\sigma^D(\gamma^* p \rightarrow X p) \sim f_i^D(x, Q^2, x_{IP}, t) \otimes \sigma_{\gamma^* i}(x, Q^2)$$

Additionally, assuming Regge factorization, the diffractive parton densities are written as a term depending on  $x_{IP}$  (Pomeron flux) times the Pomeron parton densities

$$f_i^D(x, Q^2, x_{IP}, t) \sim f_{IP/p}(x_{IP}, t) \otimes f_{i/IP}^D(x/x_{IP}, Q^2)$$

⇒ Universal DPDFs apply in DIS when vacuum quantum numbers are exchanged

# Diffractive PDFs from NLO Fits

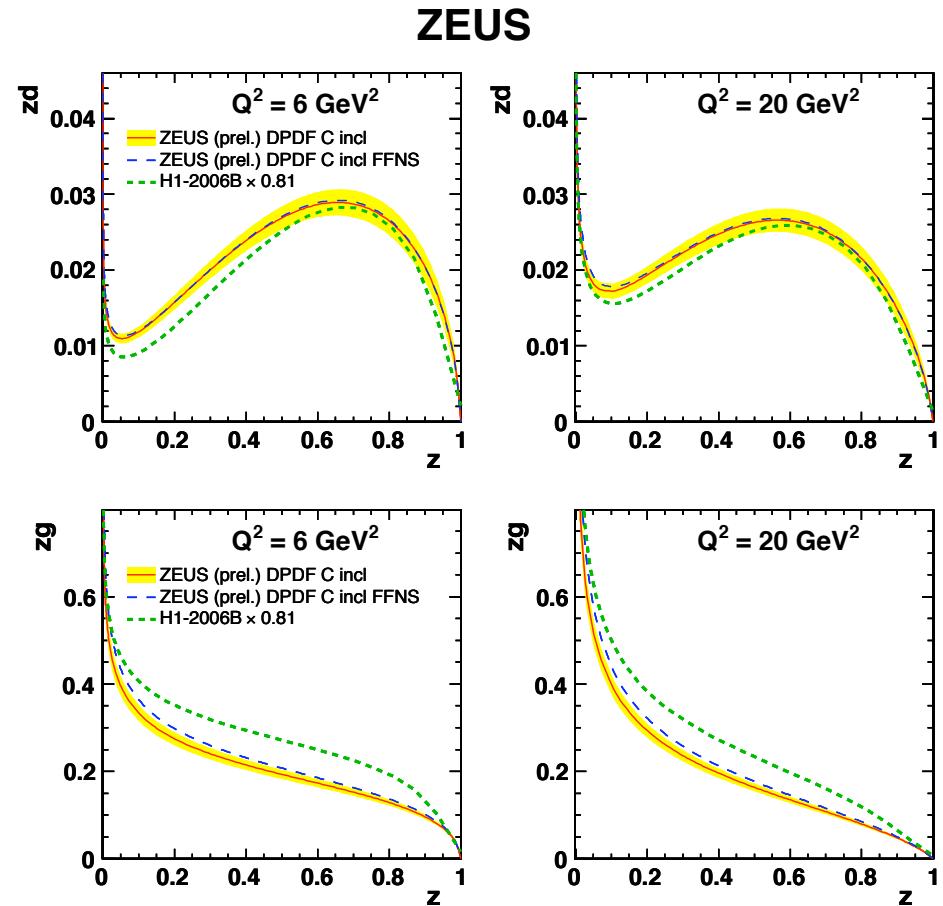
NLO QCD Fits:

- parametrize quark singlet and gluon at fixed  $Q^2$
- evolve with NLO DGLAP and fit

( $z$  = momentum fraction of the diffractive exchange entering the hard scattering)

Diffractive Parton Density Functions are obtained fitting the H1 and ZEUS diffractive reduced cross sections (published data sets only)

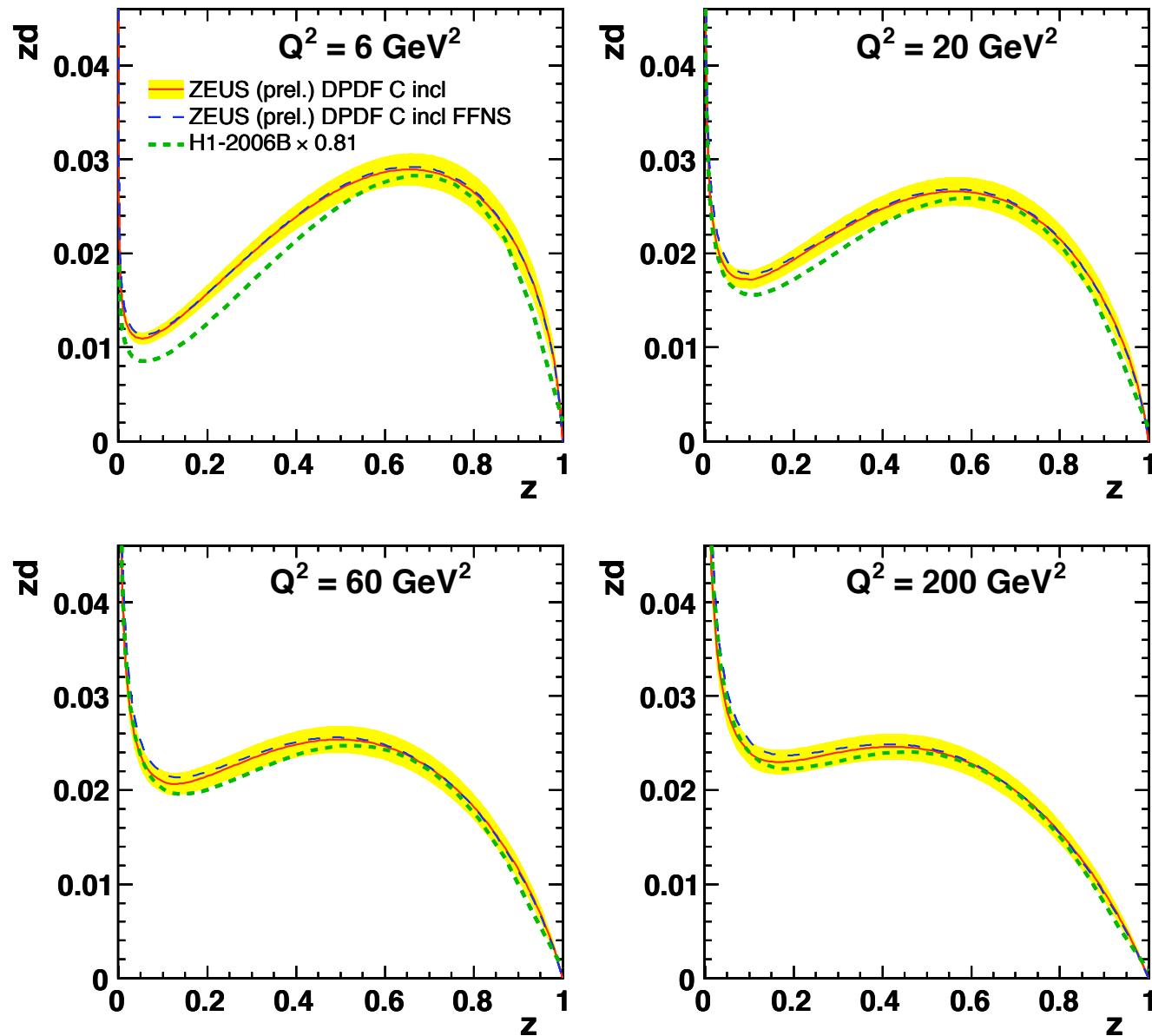
Differences in the reduced cross sections are reflected in different parton distribution extraction



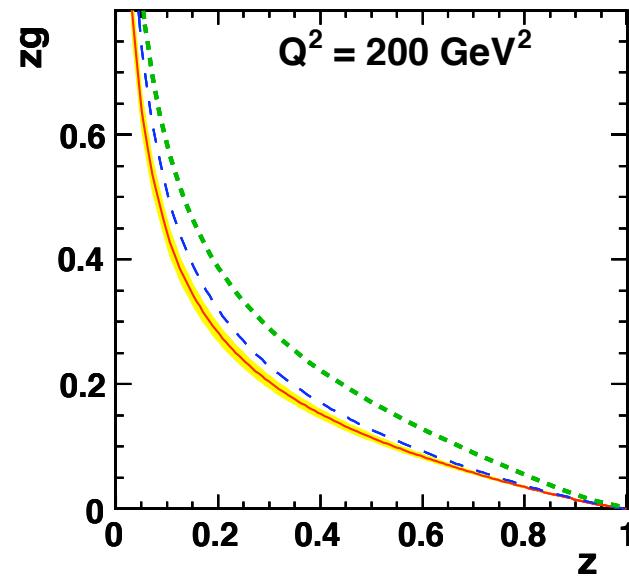
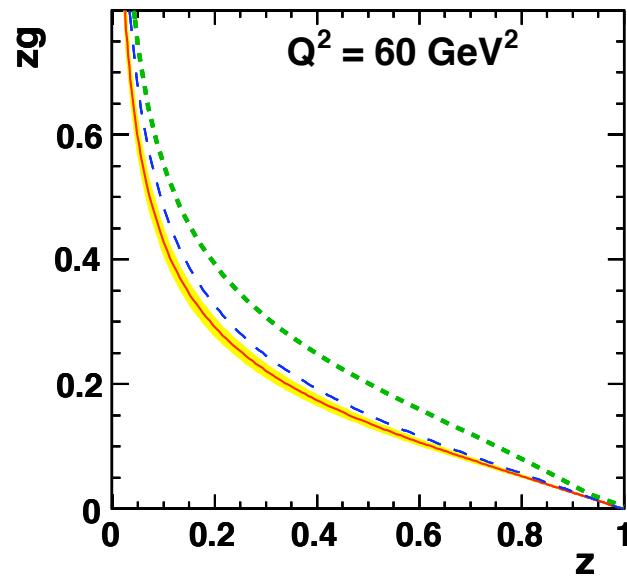
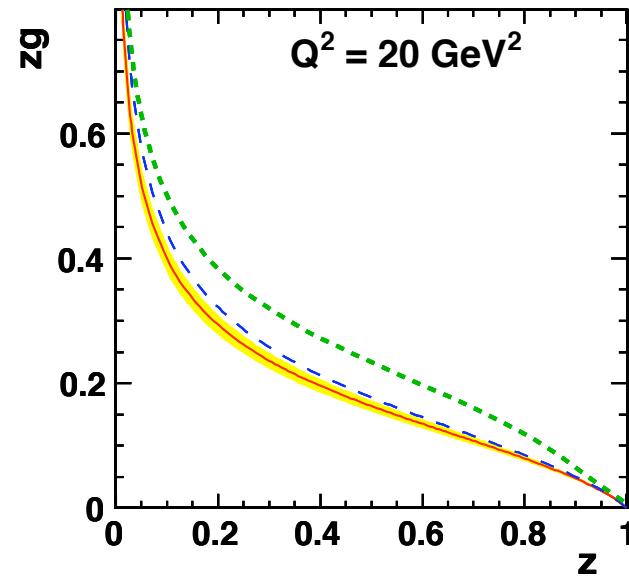
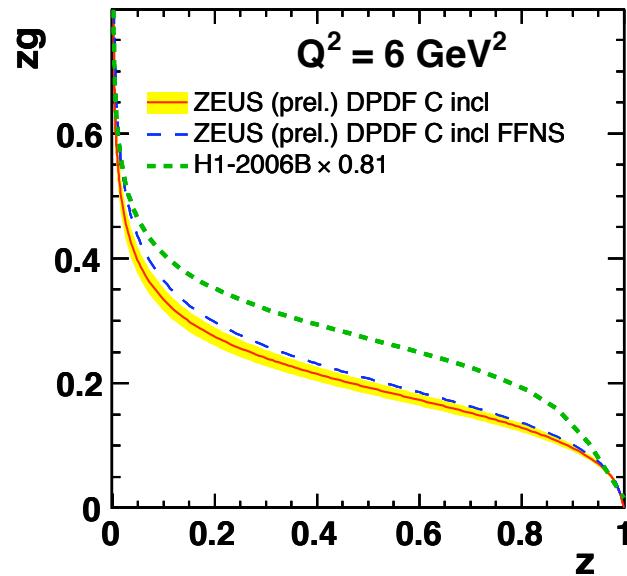
In order to obtain a precise and unique set of diffractive PDFs from HERA a deep and careful understanding of the H1 vs ZEUS results is needed

⇒ First attempt to combine H1 and ZEUS diffractive cross sections

# ZEUS

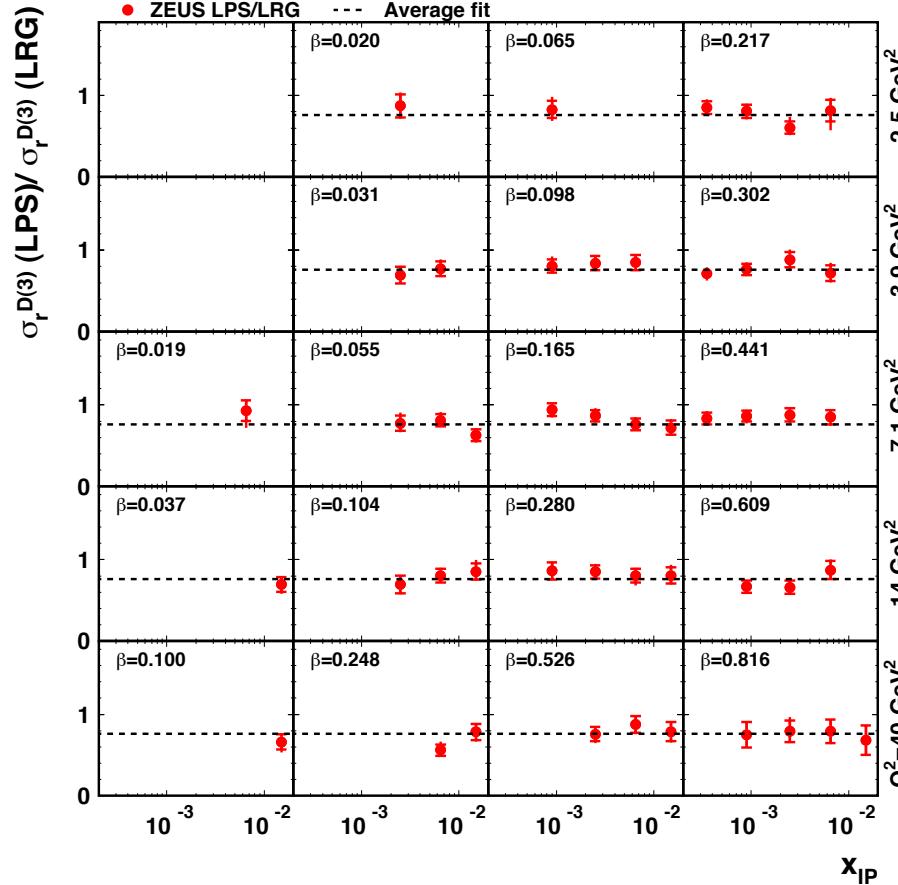
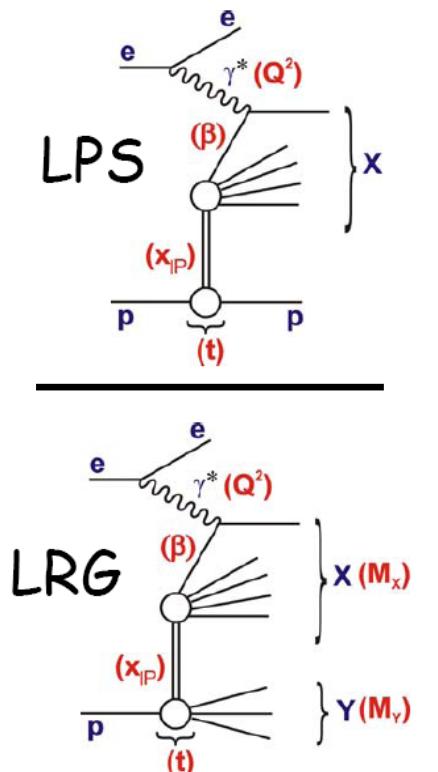


# ZEUS



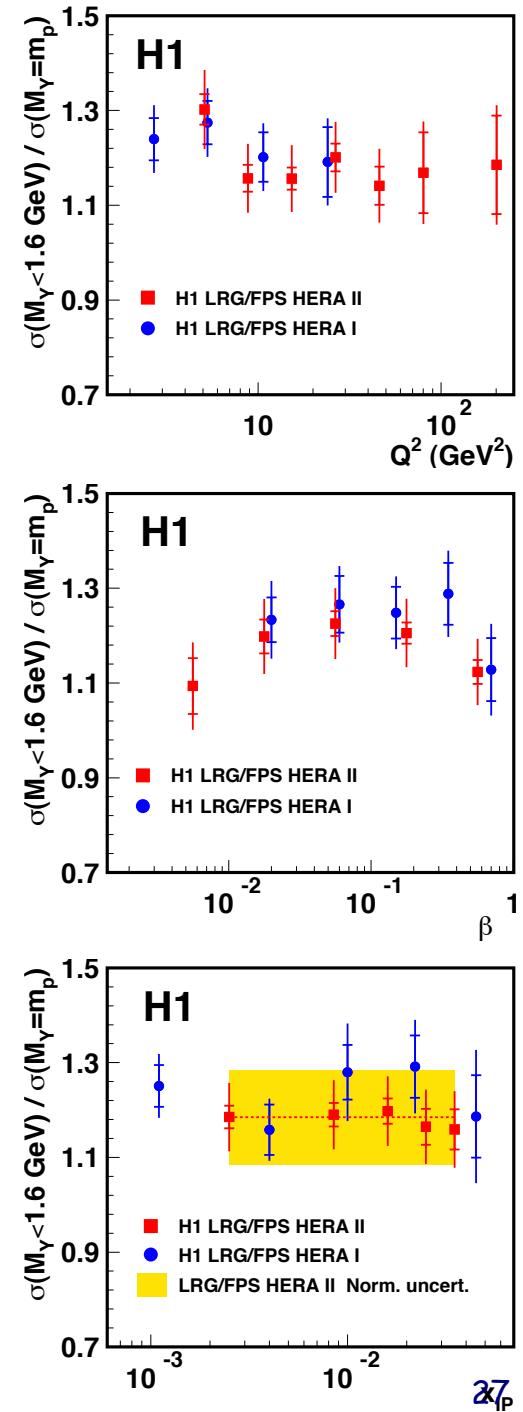
# LRG vs PS

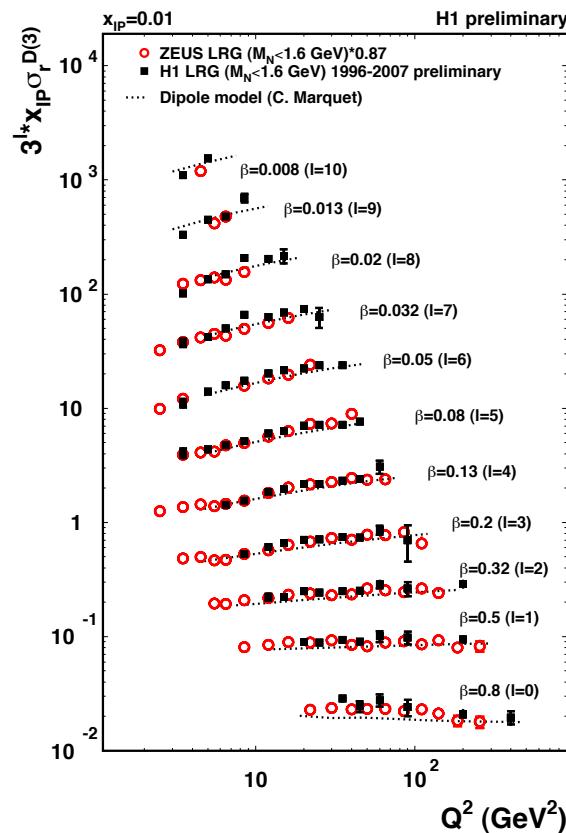
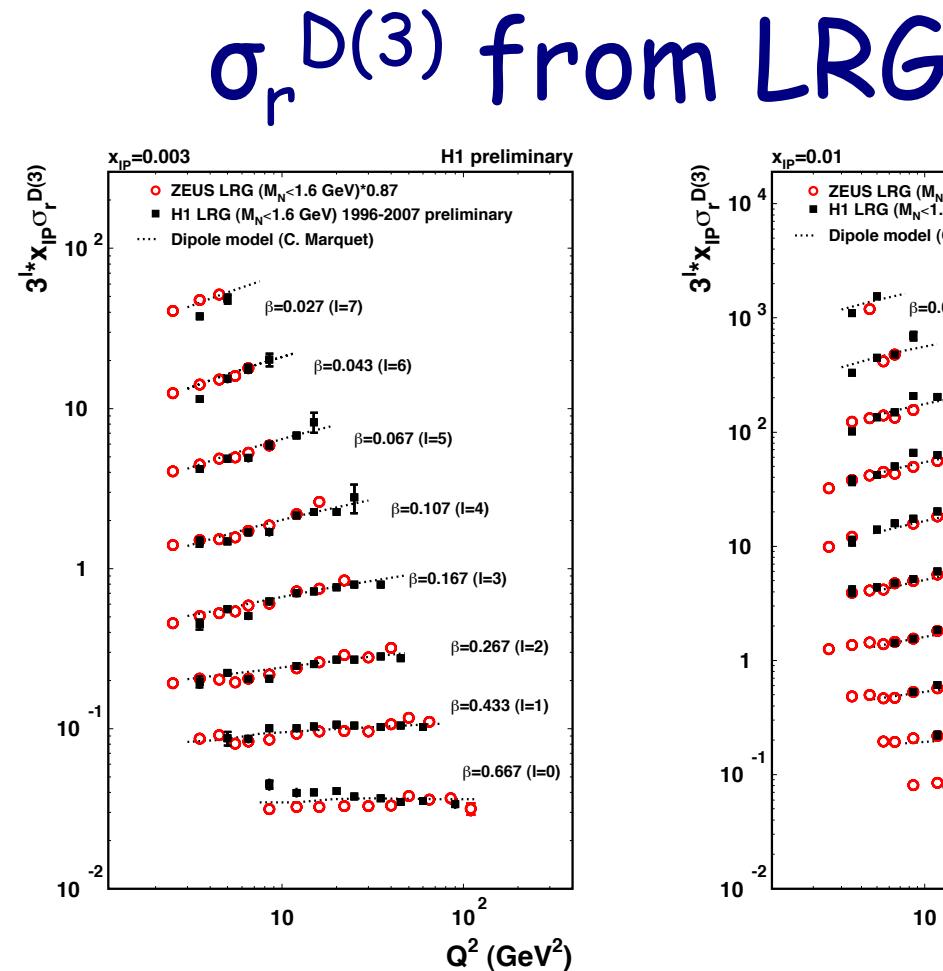
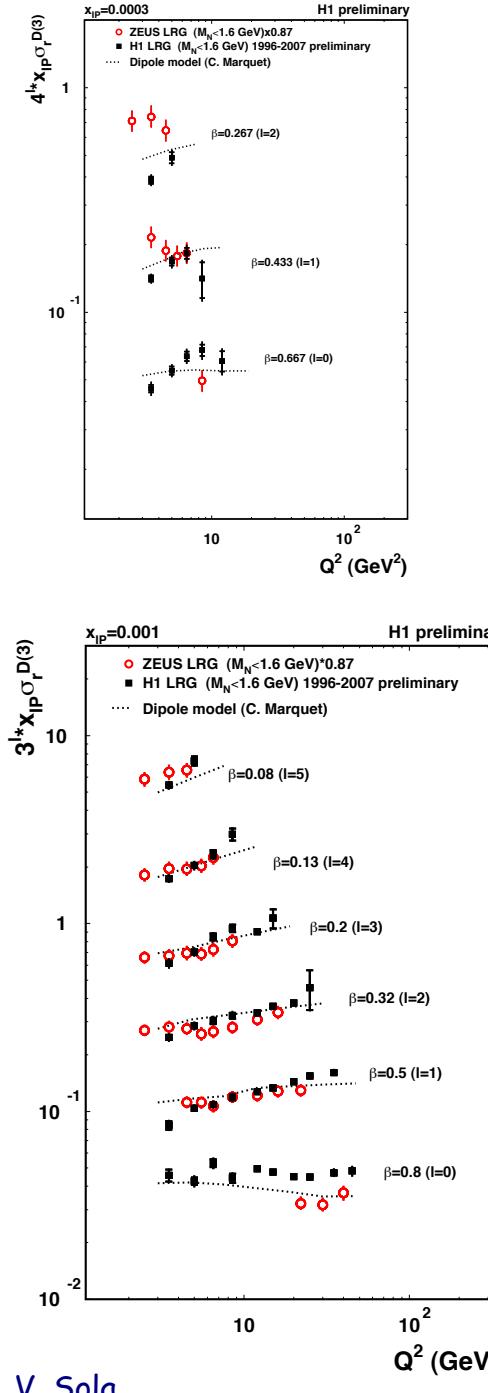
ZEUS



Estimation of p-diss contribution in LRG method  
→ ratio flat both in ZEUS and H1

⇒ PS data give the absolute normalization of  $\sigma_r^{D(3)}$





Inclusive diffractive measurements from HERA (LRG method)

- H1 '97 [Eur. Phys. J. C48 (2006) 715]
  - **ZEUS '99/2000** [Nucl.Phys. B816 (2009) 1]
  - H1 '99/2000
  - H1 '99 minimum bias
  - H1 HERA II
- } [H1prelim-10-013]  
DIS 2012, Bonn, 26-30 March 2012

# $t$ -slope vs $x_{IP}$

