



## Precision Tests of QCD Using Final State Jets and Particles

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*on behalf of the H1 and ZEUS Collaborations*

- Inclusive Jets in DIS at Low and High  $Q^2$ .
- Extraction of  $\alpha_s$ .
- Hadronic Final State Charge Asymmetry.



Lake Louise Winter Institute

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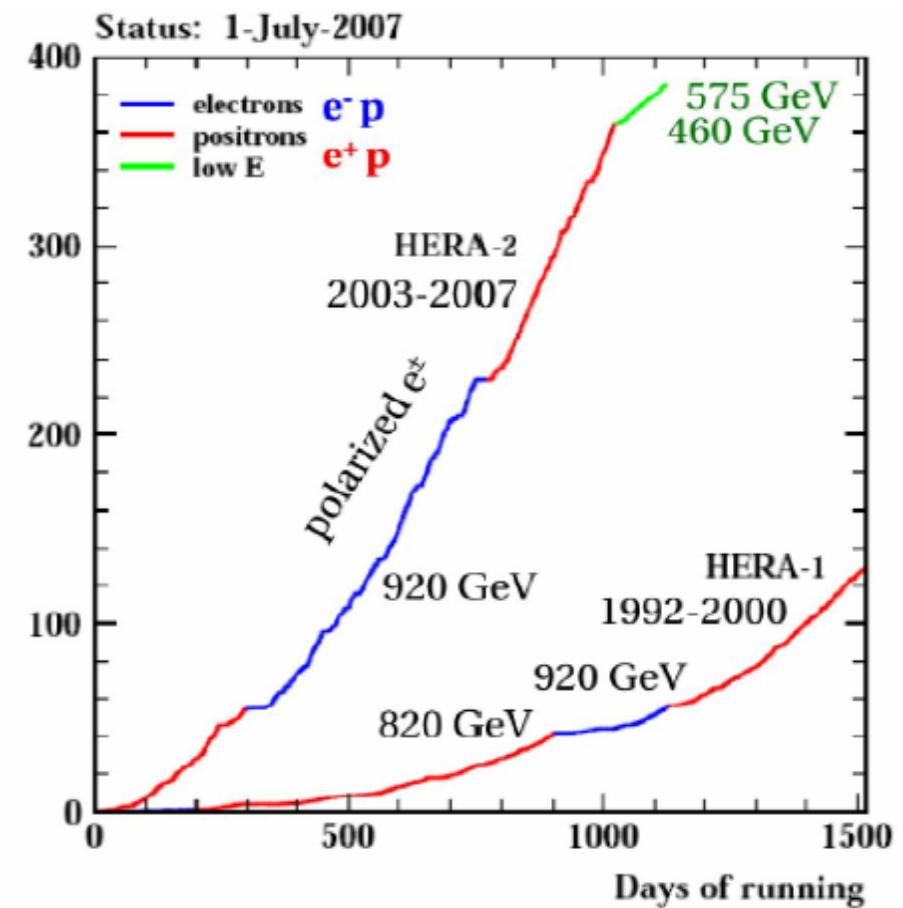
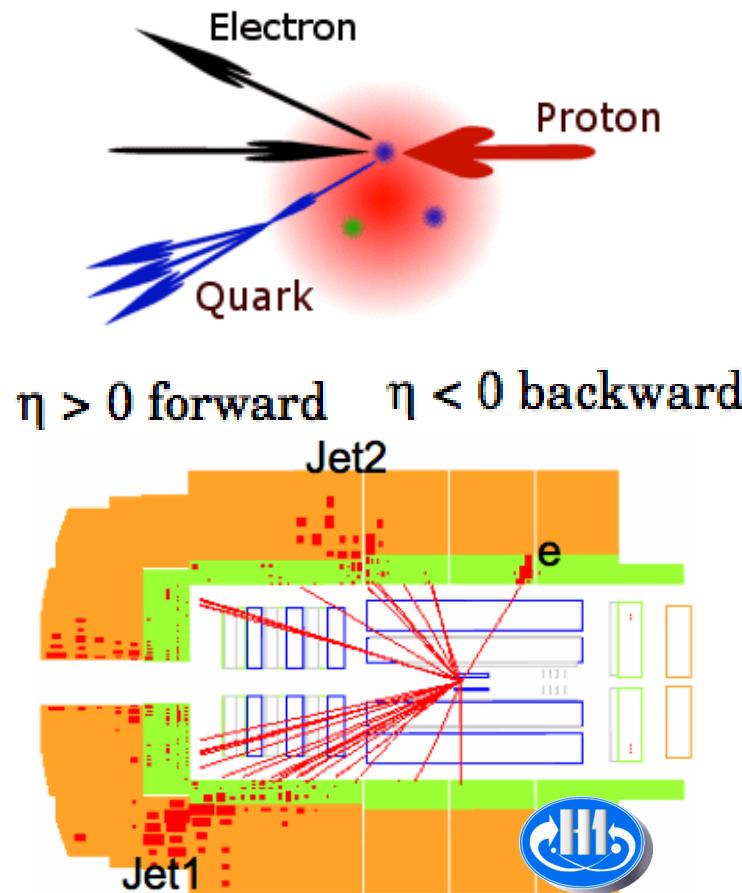


## Hadron-Elektron-Ring-Anlage (HERA) at DESY

$e^\pm p$  collider, HERA at DESY, Hamburg, Germany.

Luminosity collected:  $0.5\text{fb}^{-1}$  per experiment

$E_e = 27.6 \text{ GeV}$   $E_p = 920 \text{ GeV}$  ( $\sqrt{s} \approx 320 \text{ GeV}$ )

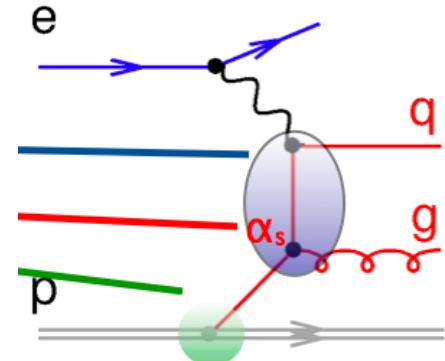




## Jet Production in DIS at HERA

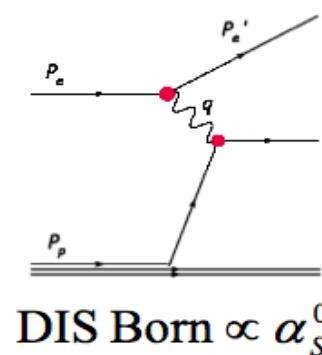
Jet X-section depends on:

- QCD matrix elements.
- Strong coupling  $\alpha_s$ .
- Parton density functions of the proton.

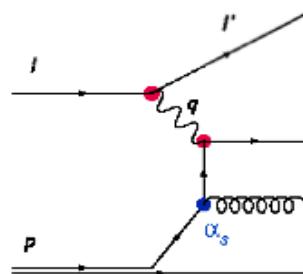


Experimental study and comparison with pQCD predictions give us access to:

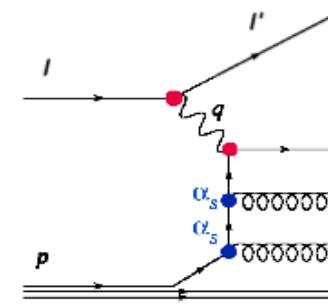
- Precision measurement of strong coupling constant  $\alpha_s$ .
- Stringent test of pQCD.



$$\text{DIS Born} \propto \alpha_s^0$$



$$\begin{aligned} 2\text{-jets} &\propto \alpha_s^1 \\ \text{Inclusive jets} &\propto \alpha_s^1 \end{aligned}$$



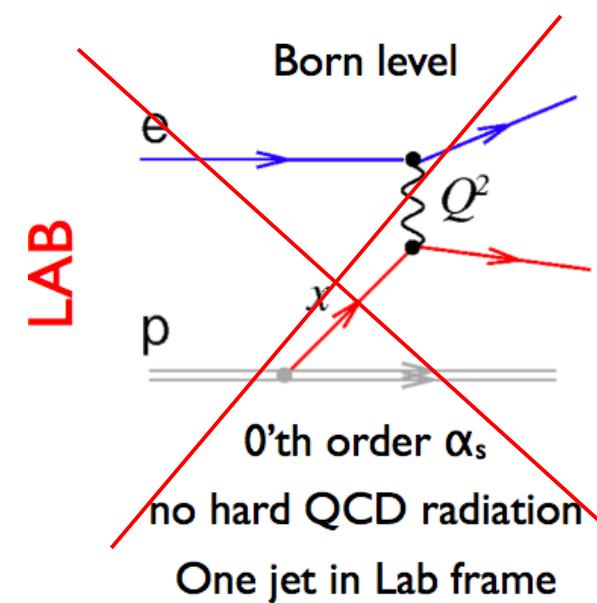
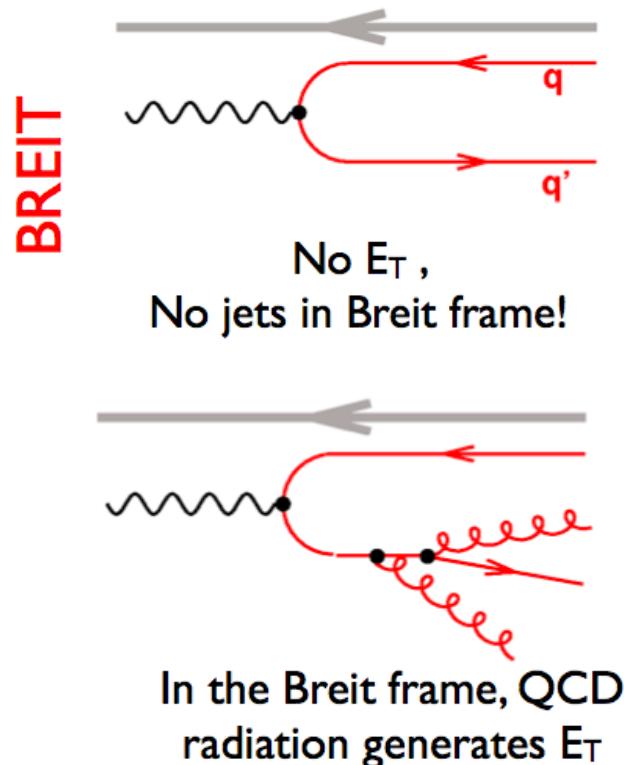
$$3\text{-jets} \propto \alpha_s^2$$

2-jet and inclusive jets cross sections sensitive to the proton gluon PDF



## Jet Finding: inclusive $k_T$ algorithm in the Breit frame.

- Suppression of the Born contribution (struck quark has zero  $E_T$ ).
- Suppression of the beam remnant jet (zero  $E_T$ ).
- Lowest order contribution from  $g^*q \rightarrow qq$  and  $g^*q \rightarrow qg$ .
- Direct sensitivity to hard QCD process ( $\alpha_s$ )  $\rightarrow$  gluon density.





## Jet Production at Low $Q^2$

**DATA H1 : From 1999-2000, luminosity of  $43.5 \text{ pb}^{-1}$  ;  $5 < Q^2 < 100 \text{ GeV}^2$  and  $0.2 < y < 0.77$**

### Measurement:

X-section, double X-section in fun. of  $Q^2$ ,  $P_T$ .

### Events selection:

Singe jet  $P_T > 5 \text{ GeV}$

### Experimental uncertainties:

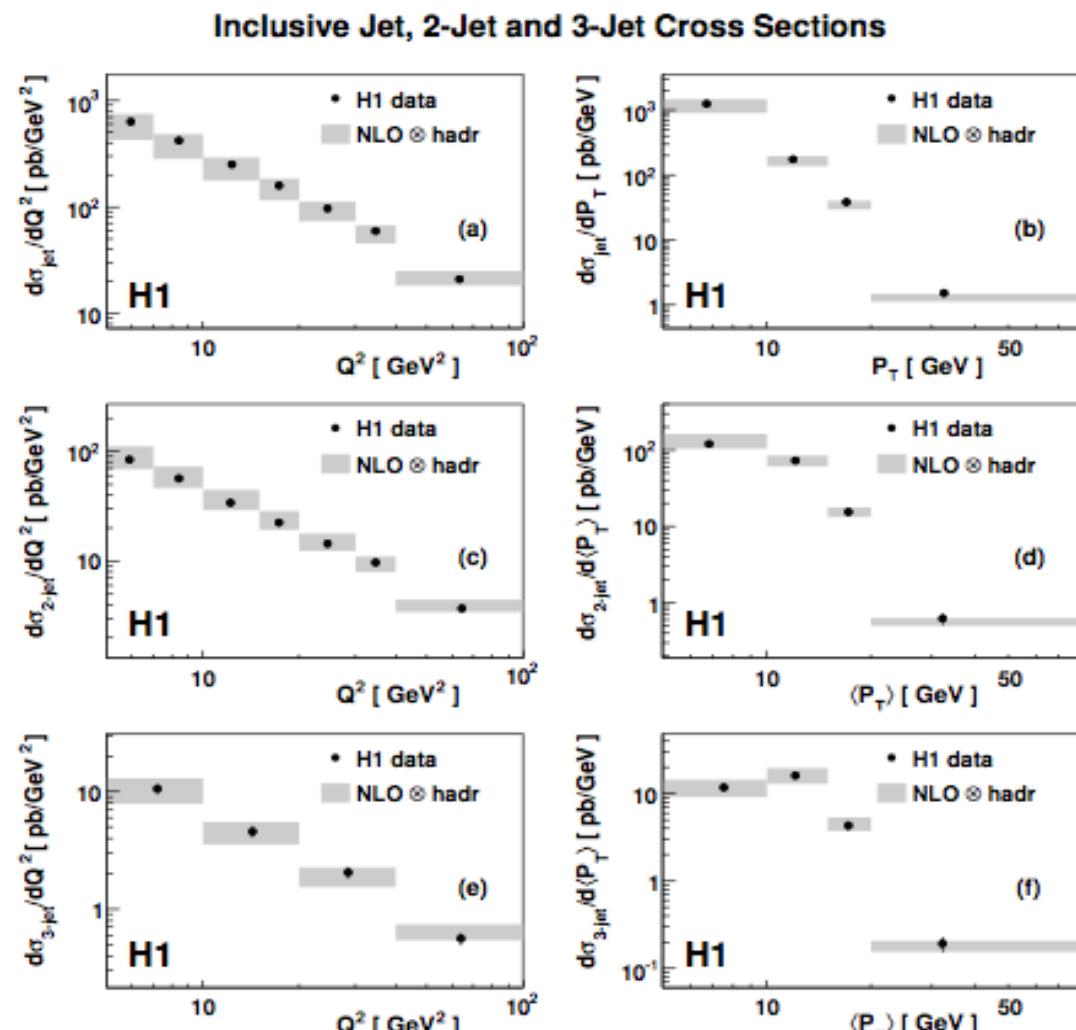
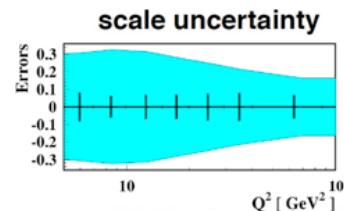
2% on energy and reconstructed HFS  $\Delta\sigma/\sigma = 4\text{-}10\%$

7% on scattered positron energy scale  $\Delta\sigma/\sigma = 1\%$

acceptance and QED radiation  $\Delta\sigma/\sigma = 2\text{-}10\%$

### Theoretical uncertainties.

- 15-30% renormalization scale dominates and increases with decrease of  $Q^2$ .





## Jet Production at High $Q^2$

**DATA ZEUS :** From 2005-2006, luminosity of  $188 \text{ pb}^{-1}$ ;  $Q^2 > 125 \text{ GeV}^2$

### Measurement:

- Single diff. inclusive NC jet X-section in function of  $Q^2$  or  $E_T$  or  $\eta_B^{\text{jet}}$ .
- Double diff. X-section in function of  $Q^2$  and  $E_T$

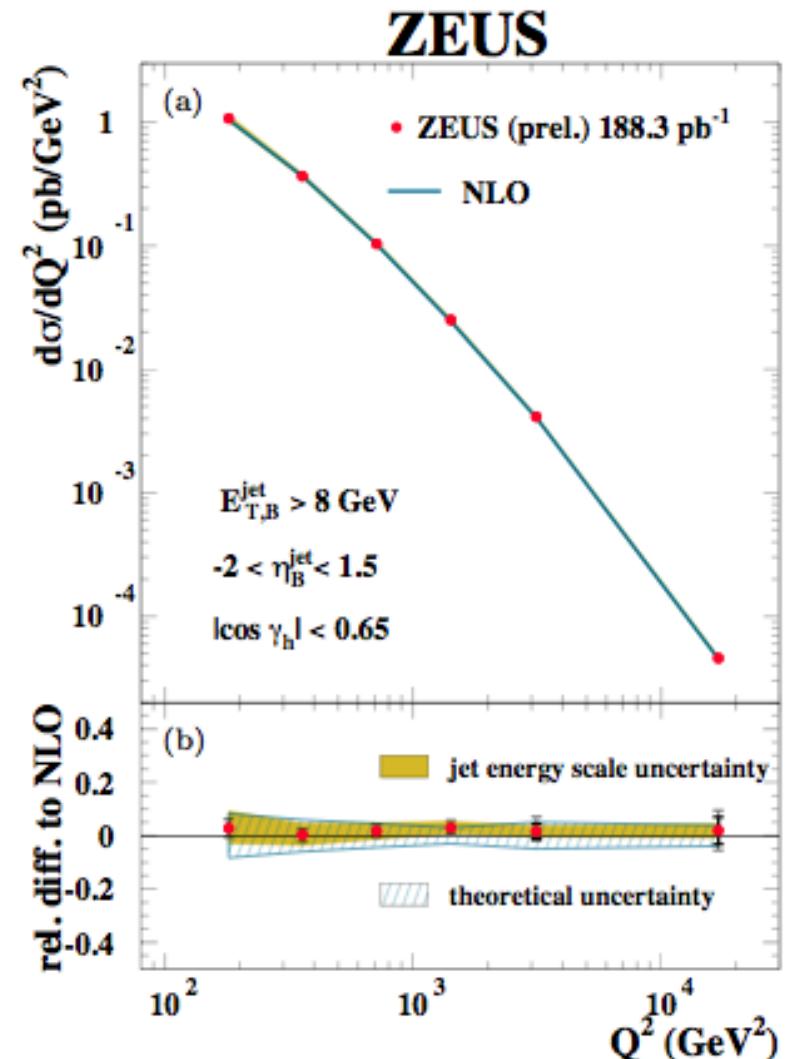
### Experimental uncertainties:

hadronic energy scale  $\Delta\sigma/\sigma = 5\%$

Model dependence of acceptance correction  $\Delta\sigma/\sigma = 3\%$

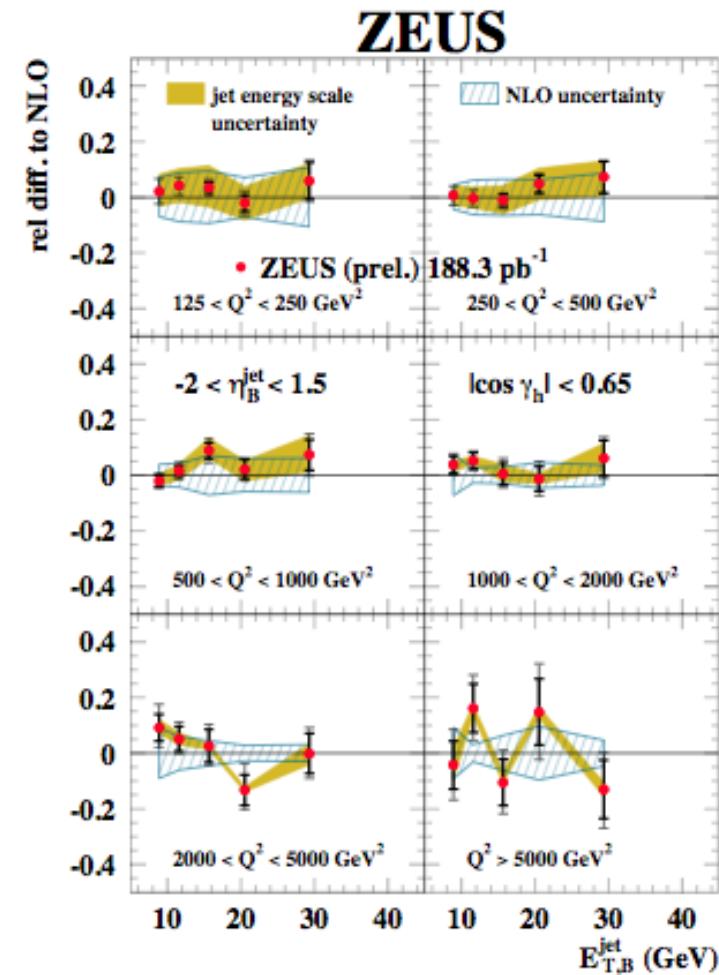
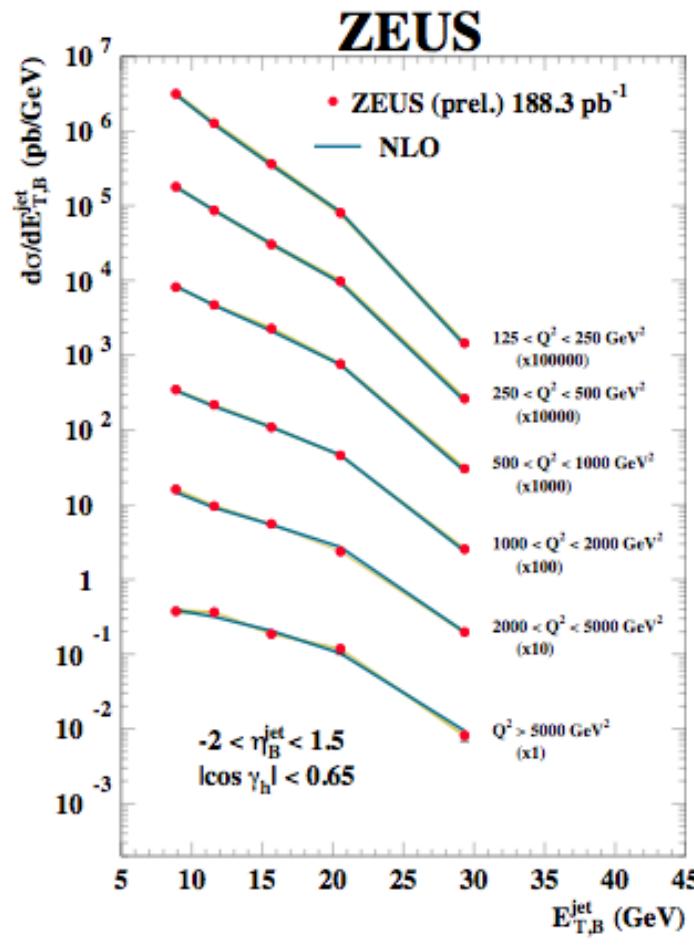
### Theoretical uncertainties.

- Still dominates over experimental, except at high  $Q^2$
- Very good description of data by NLO QCD (DISENT)
- ZEUS\_S PDF and  $\mu r = \mu f = E_T^{\text{jet}}$





## Jet Production at High $Q^2$



• Double differential inclusive jet X-section as a function of  $E_T$  and  $Q^2$  shows good description of all data by NLO QCD  
•  $\mu_R$  uncertainty dominates except at high  $E_{T,B}$  where the PDF uncertainty is dominant  $\Rightarrow$  potential to further constrain the gluon density in the proton.





## Jet Rates Measurement at High $Q^2$

**DATA H1 : From 1999-2007, luminosity of  $395 \text{ pb}^{-1}$ ;  $150 < Q^2 < 15000 \text{ GeV}^2$  and  $0.2 < y < 0.7$**

### Measurement:

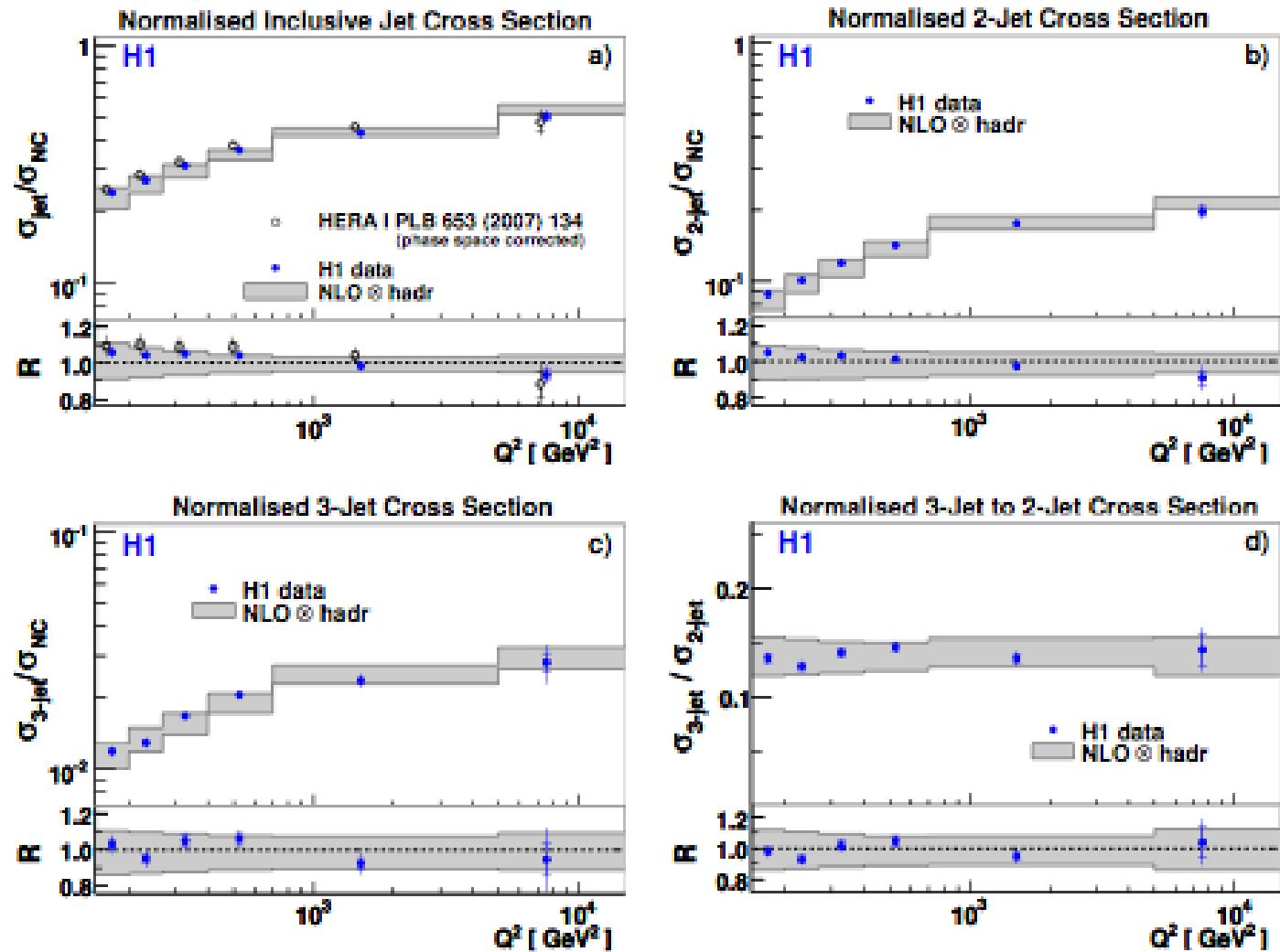
Normalised X-section reduce experimental uncertainty and influence of PDF's

### Events selection:

Singe jet s  $7 < P_T < 50 \text{ GeV}$   
2(3) jets,  $7 < P_T < 50 \text{ GeV}$   
and  $M_{12} > 16 \text{ GeV}$

### Experimental uncertainties

Hadronic energy scale dominates and shows 1-5% effect on X-section:  
Overall experimental uncertainty 3-6% up to 15% for highest  $P_T$

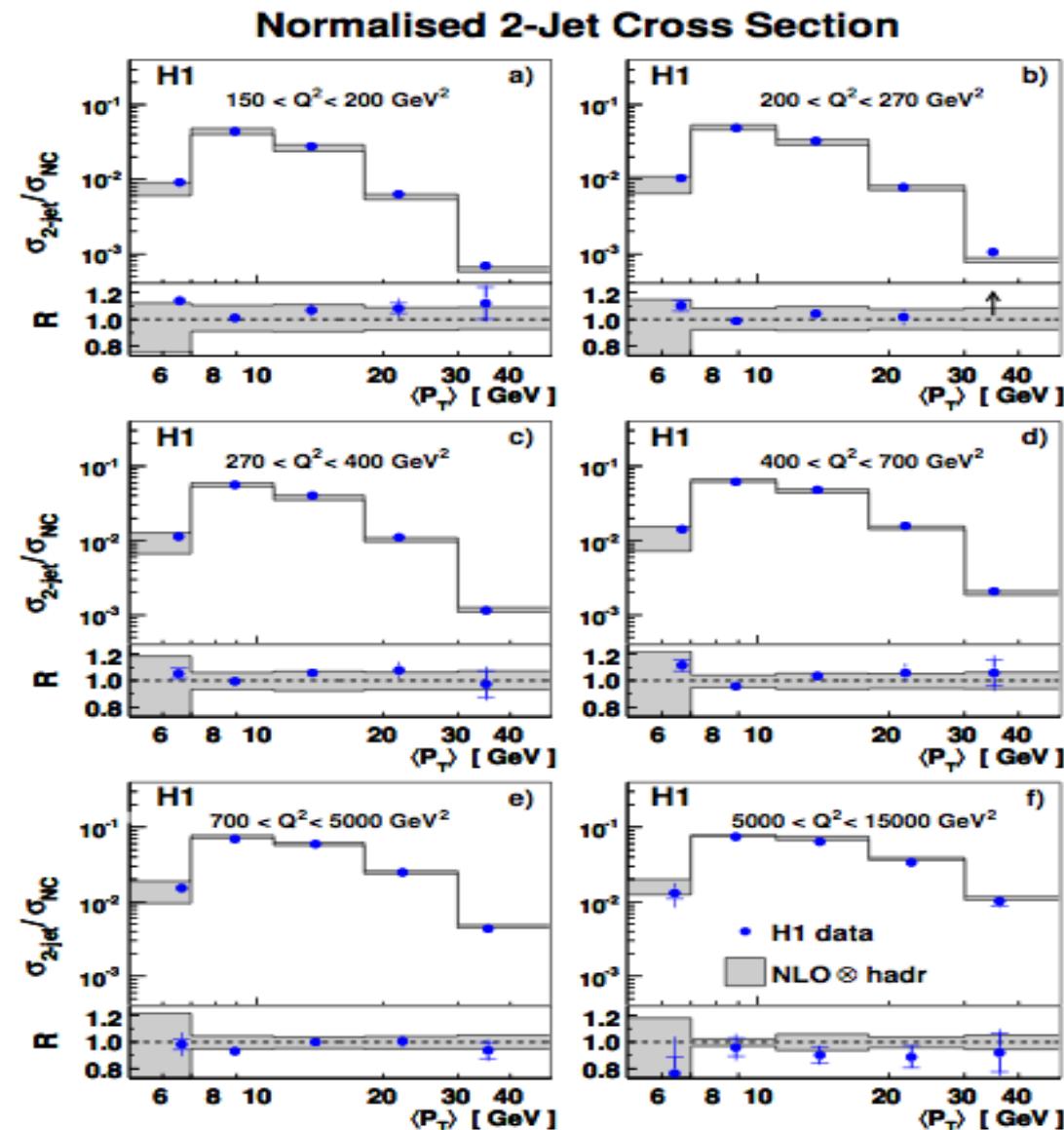




## Jet Rates Measurement at High $Q^2$

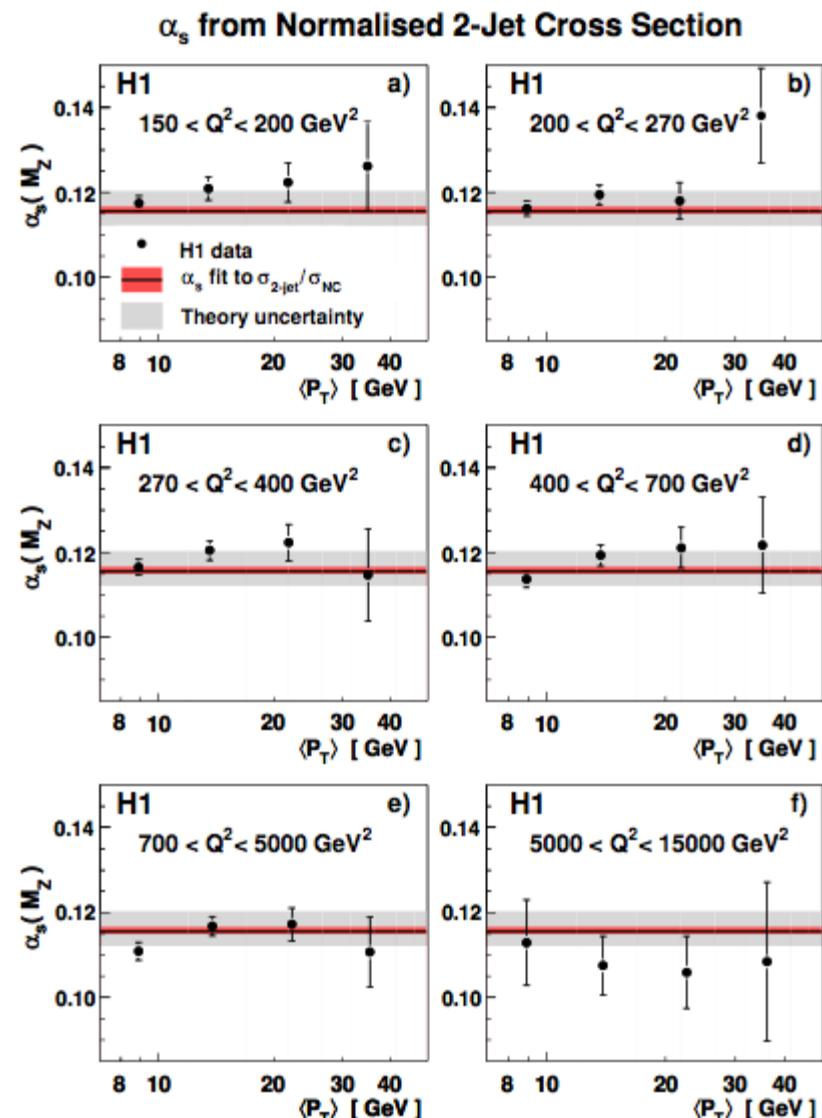
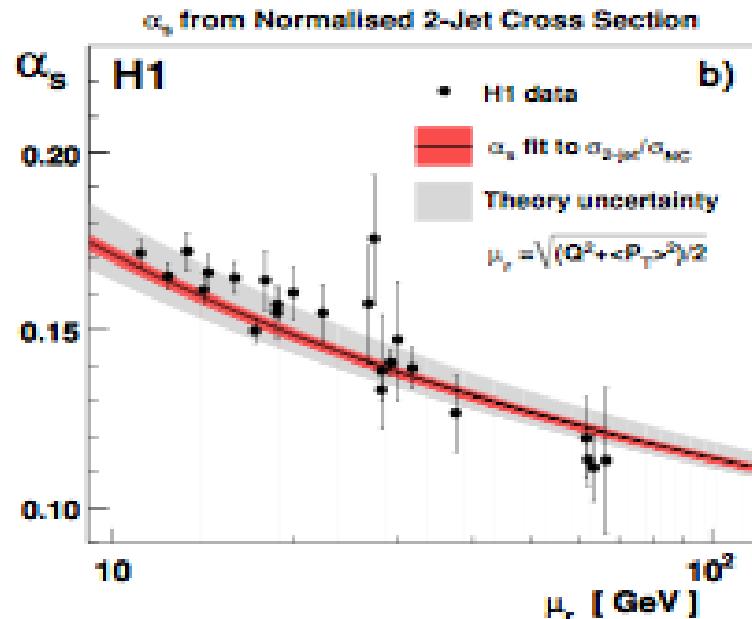
$$\frac{\sigma_{2\text{jet}}(Q^2, \langle p_T \rangle)}{\sigma_{NC}}$$

- Data are well described by NLO pQCD,
- Experimental uncertainties (2-6%)
- Theory error (5-10%), missing higher order  $\rightarrow \mu_R$  dependence



## Individual fits:

- o adjust  $\alpha_s$  in NLO QCD prediction to match each data point
- o evolve  $\alpha_s(M_Z)$  to relevant  $\mu_R$ .



## Combined fits:

- $\chi^2$  fit of NLO QCD predictions to data with  $\alpha_s(M_Z)$  as free parameter.
- Include correlated systematical errors (jet energy scale) by “Hessian procedure”.
- Statistical correlations are taken in account.



## Determination of $\alpha_s$ from jet rates at High $Q^2$

**Extraction of strong coupling constant:**

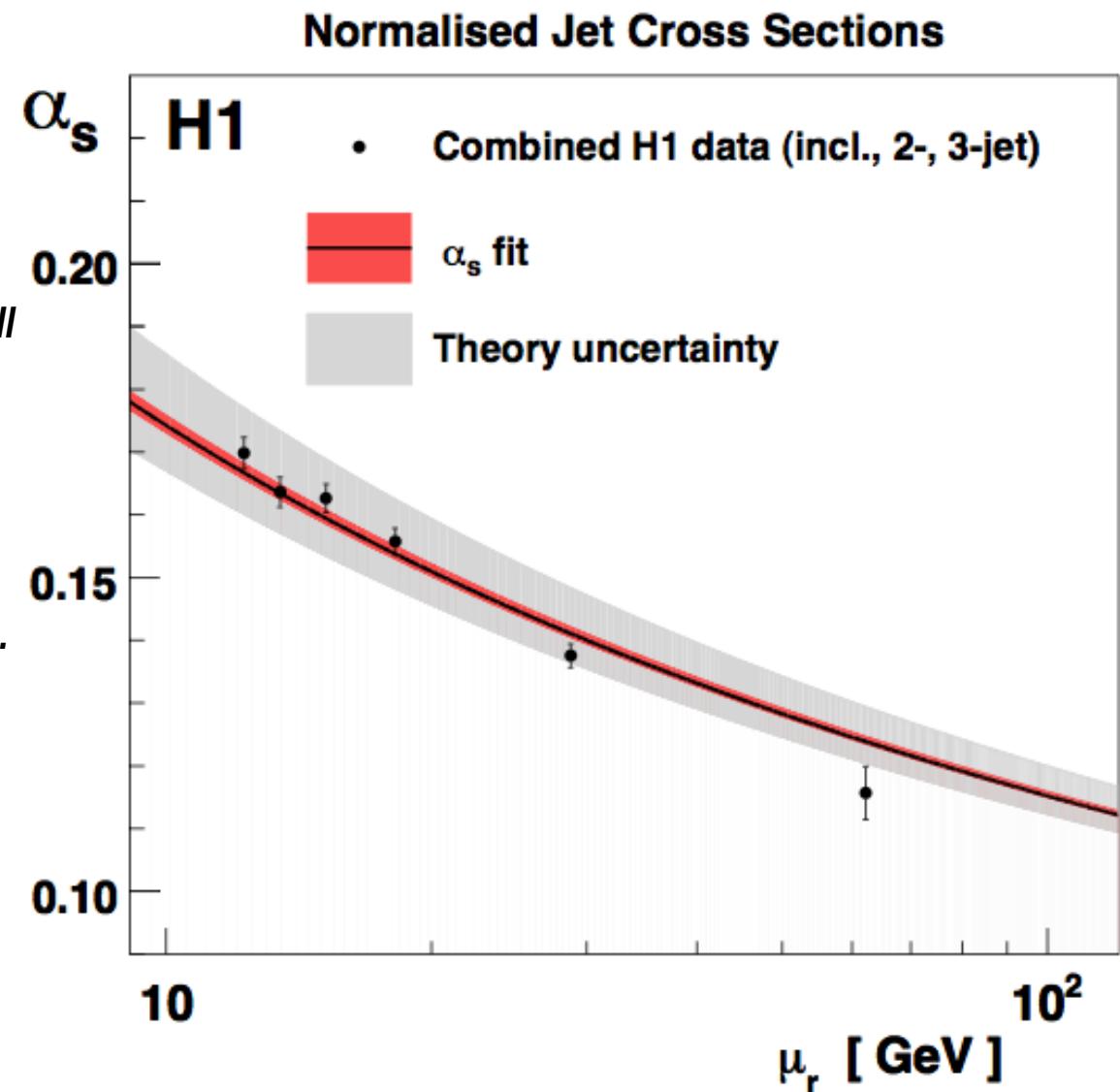
- $\alpha_s$  from multi-jet rates : Combined fit to all observables.

**Experimental uncertainty 0.6%.**

- result with best experimental precision.

**Total uncertainty 3.6%.**

**Running of  $\alpha_s$  agrees with QCD expectations.**





## Running of $\alpha_s$ from low and high $Q^2$

- $\alpha_s$  from low  $Q^2$  added to high  $Q^2$  curve, low  $Q^2$  data lie within the theory uncertainty of the high  $Q^2$  fit.

low  $Q^2$

H1 Experiment

$$\alpha_s(M_Z) = 0.1186 \pm 0.0014(\text{exp})^{+0.0132}_{-0.0101}(\text{theory}) \pm 0.0021(\text{pdf})$$

high  $Q^2$

H1 Experiment

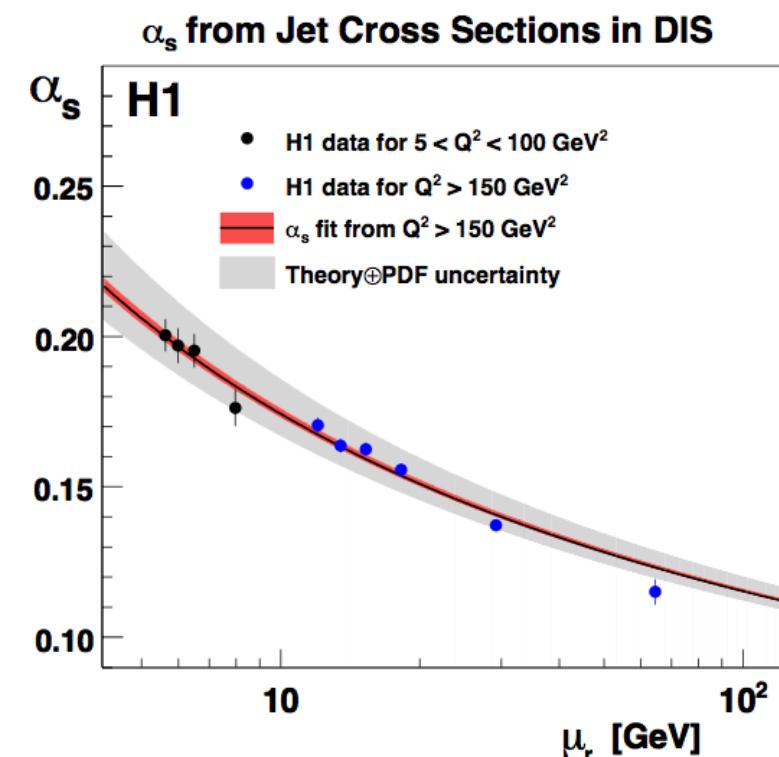
$$\alpha_s(M_Z) = 0.1168 \pm 0.0007 \text{ (exp.)}^{+0.0046}_{-0.0030} \text{ (th.)} \pm 0.0016 \text{ (PDF)}$$

ZEUS Experiment

- to minimize total uncertainty,  $\alpha_s$  extracted for  $Q^2 > 500 \text{ GeV}^2$

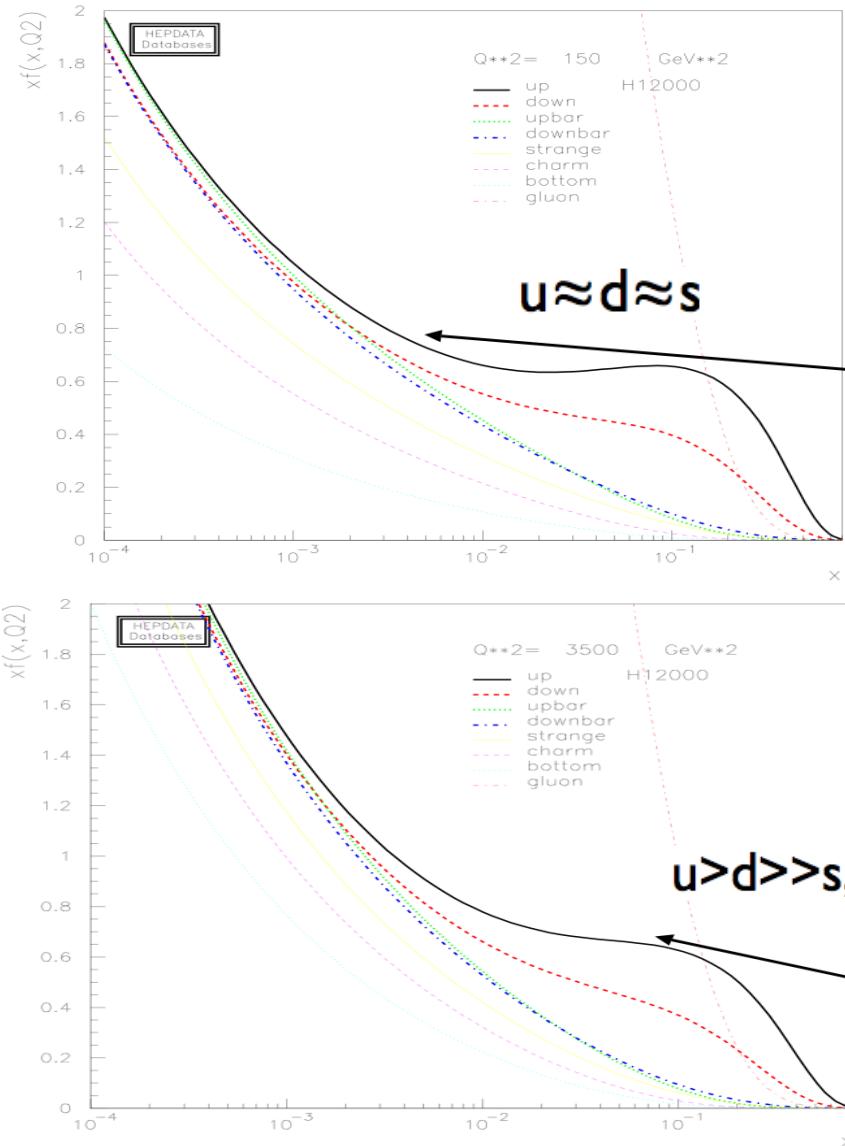
$$\alpha_s(M_Z) = 0.1192 \pm 0.0009 \text{ (stat.)}^{+0.0035}_{-0.0032} \text{ (exp.)}^{+0.0020}_{-0.0021} \text{ (th.)}$$

- 2.9% experimental uncertainty
- 3.5% total uncertainty.





# HFS Charge Asymmetry at High $Q^2$ (DIS) at HERA



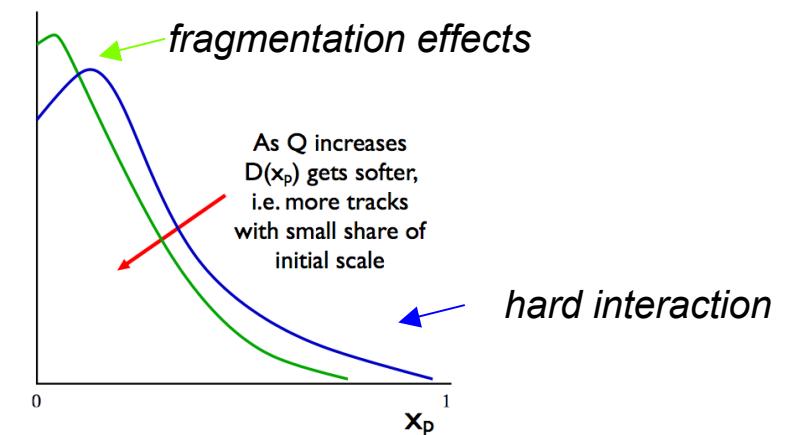
## Motivation:

- At low  $Q^2$  and low  $x_{bj}$  proton PDF dominated by sea quarks and gluons.
- At higher  $Q^2$  and large  $x_{bj}$  valence quark dominates.
- Contribution of  $u$  valence quarks from the proton to the hard interaction dominates at high  $Q^2$  over that from  $d$  valence quarks!

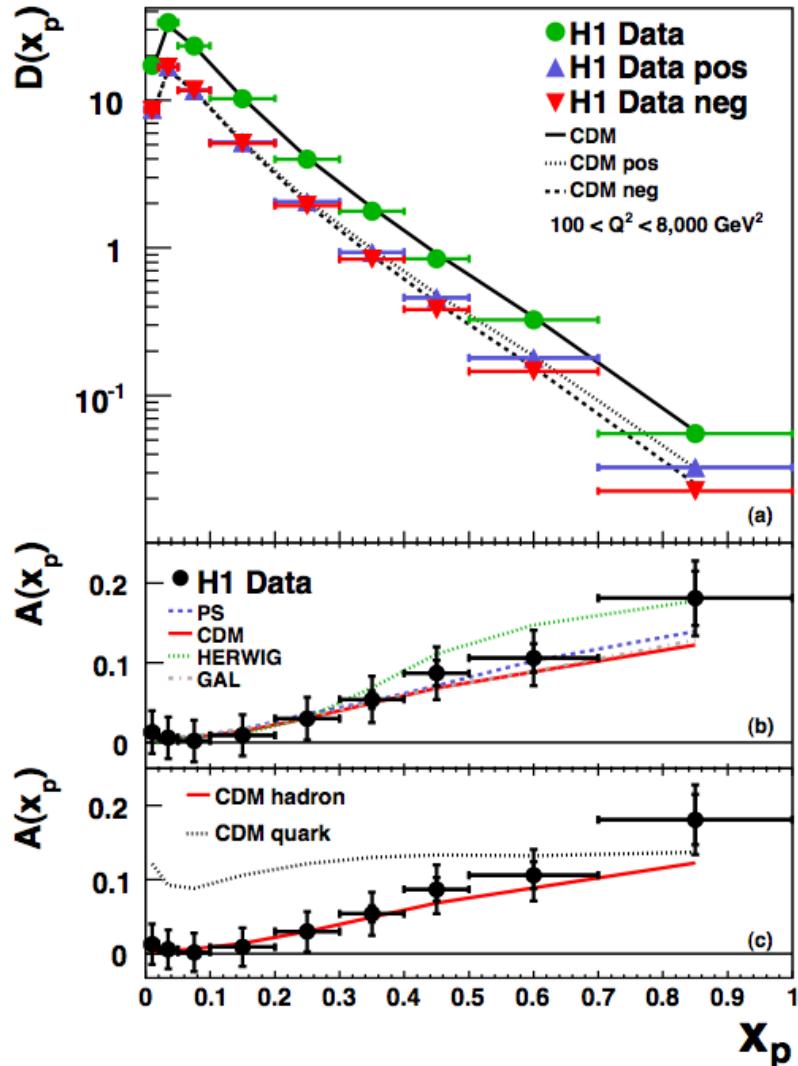
$$A(x_p, Q) = (D^+(x_p, Q) - D^-(x_p, Q)) / (D^+(x_p, Q) + D^-(x_p, Q))$$

$$D(x_p) = (1/N_{\text{event}})^* (dn/dx_p); \quad x_p = 2p_h/Q$$

- $A(x_p, Q)$  is charge asymmetry
- $P_h$  is momentum of charged particle in the current region of the Breit frame.
- $D(x_p)$  is event normalized, charged particle, scaled momentum distribution.



- DATA with integrated luminosity of  $44 \text{ pb}^{-1}$  and kinematic range  $100 < Q^2 < 8000 \text{ GeV}^2$  and  $0.05 < y < 0.6$



*Insight into non-perturbative regime of QCD.*

- **The Parton Shower model (PS)** **RAPGAP**
  - Evolution of the parton shower DGLAP
- **Coulor Dipole Model (CDM)** **DJANGO**
  - Parton evolution similar to BFKL
- **Soft Colour Interaction model (SCI) and generalised area law (GAL)** **LEPTO**
- The **RAPGAP, DJANGO and LEPTO** use Lund string model of hadronisation.

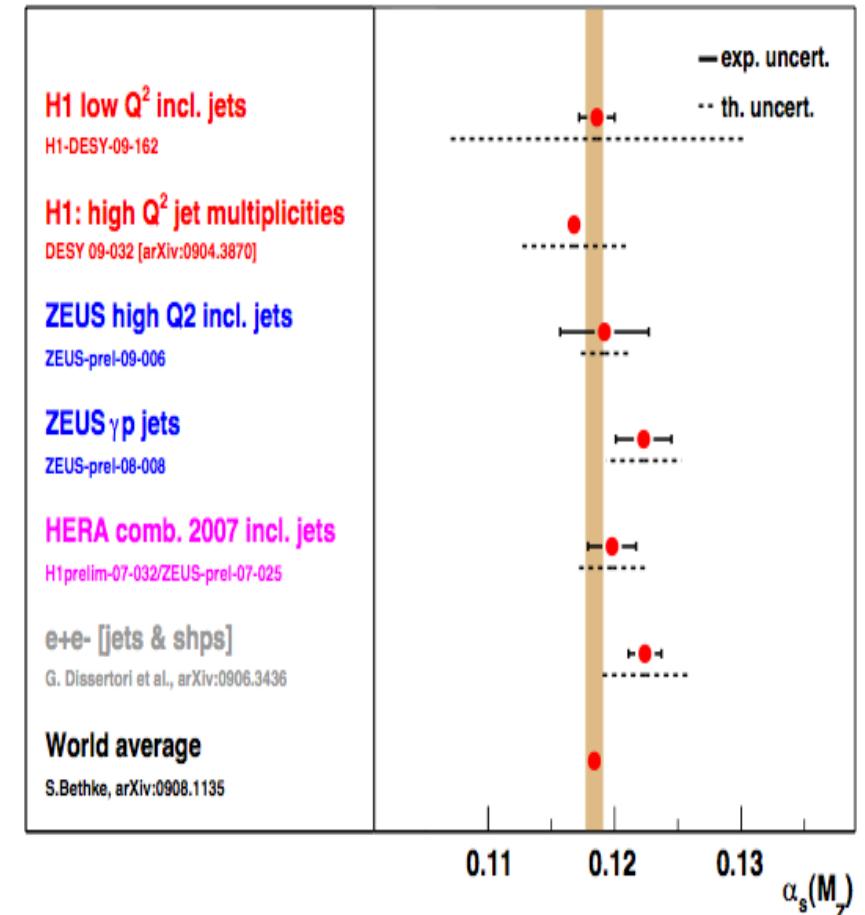
## Measurement

- At low  $x_p$ , similar distributions.
- At large  $x_p$ , clear difference in distributions.
- Difference described by MC.
- Asymmetry magnitude and evolution described by various MC models.
- Quark level prediction from CDM MC with hadronisation turned off.
- Similar asymmetry between data and CDM at large  $x_p$ .
- Consistent with expectation that fragmentation dominates at low  $x_p$  and hard interaction at large  $x_p$ .



## Summary

- **Precise  $\alpha_s$  extraction.**
  - ✓ very high experimental precision.
  - ✓ running  $\alpha_s$  verified over  $5 < Q^2 < 10\,000 \text{ GeV}^2$ .
- **Data are well described by NLO QCD.**
- **Theory scale uncertainties dominate over the experimental uncertainties.**
- **Higher order calculations necessary to take full advantage of the data.**
- **Measurement of charge asymmetry.**
  - ✓ At high  $x_p$  the asymmetry is directly related to valence quark content.



- H1: [http://www-h1.desy.de/general/home/intra\\_home.html](http://www-h1.desy.de/general/home/intra_home.html)
- ZEUS: <http://www-zeus.desy.de/>

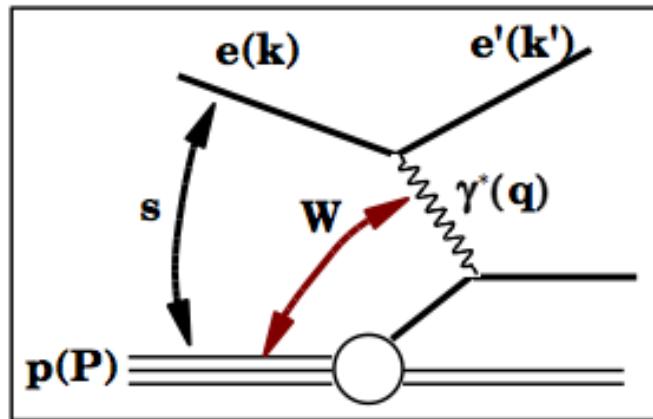


# *Backup !!*



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**Lake Louise Winter Institute**  
15<sup>th</sup>-20<sup>th</sup> February 2010, Alberta, Canada


**DIS**
**NC**

$$ep \rightarrow eX$$

 $\gamma^*, Z \text{ exchange}$ 
**CC**

$$ep \rightarrow \nu X$$

 $W \text{ exchange}$ 

$$e(\mathbf{k}) + p (\mathbf{P}) \rightarrow e'(\mathbf{k}') + X$$

- Centre of mass energy  $s = (P + k)^2$
- Energy of hadronic system  $W^2 = (P + q)^2$
- Photon virtuality  $Q^2 = -q^2 = -(k + k')^2$
- Inelasticity  $y = qP/kP \approx (W^2 + Q^2)/s$
- Bjorken-x  $x_{Bj} = Q^2/2qP \approx Q^2/sy$



Backup !!

# NLO pQCD Theory

