

Probing QCD at the Highest Q^2 Deep-Inelastic Scattering

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Physics In Collision

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Kobe, Japan

On behalf of the ZEUS and H1 Collaborations



1 Introduction

2 Structure Functions and Parton Distribution Functions

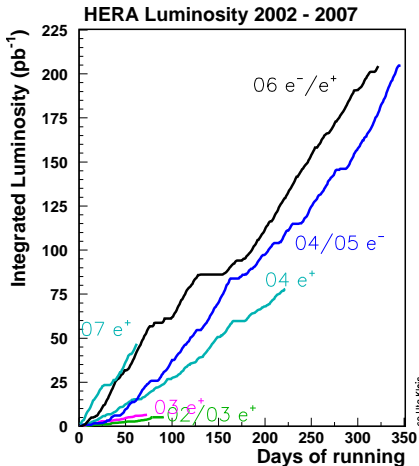
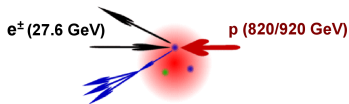
3 Jets

4 Summary





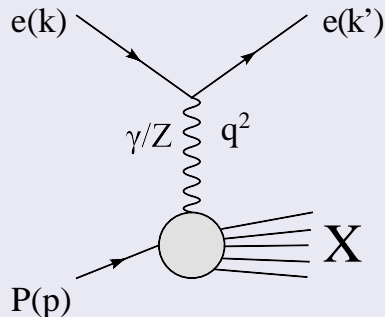
At HERA e^\pm were collided with protons at the interaction points of H1 and ZEUS with $\sqrt{s} \approx 320$ GeV



HERA I: ZEUS $\mathcal{L} \sim 130 \text{ pb}^{-1}$
HERA II: ZEUS $\mathcal{L} \sim 360 \text{ pb}^{-1}$



Neutral Current (NC)



Similar diagrams involving W exchange for Charged Current scattering (CC)

Kinematics

4-momentum transfer:

$$q = k - k'$$

Virtuality (resolving power):

$$Q^2 = -q^2$$

Parton momentum fraction:

$$x = \frac{Q^2}{2p \cdot q}$$

e Inelasticity:

$$y = \frac{q \cdot p}{k \cdot p}$$

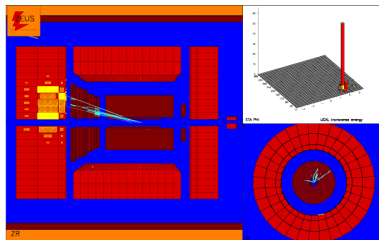
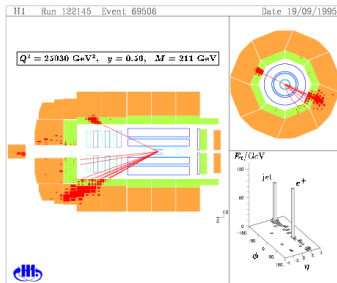
(CM energy)²:

$$s = (k + p)^2 \approx 4E_e E_p$$

γP CM energy/ M_X :

$$W = (p + q)^2$$





H1

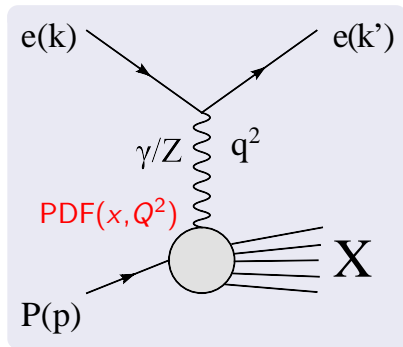
- Liquid Argon Calorimeter
- Optimised for precision measurement of the scattered lepton

ZEUS

- Depleted Uranium Calorimeter
- Optimised for precision measurement of the hadronic final state



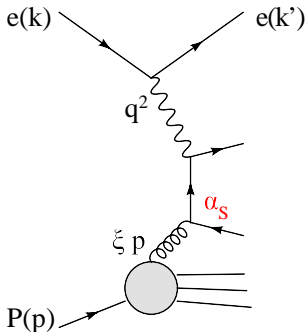
HERA was the premier machine for measuring structure functions and hence the parton distribution functions (PDFs) of the proton:



Scaling violations of structure functions give sensitivity to α_s

- Proton beam \rightarrow no need for nuclear corrections
- Different E_P data sets allow F_L measurement
- Electron beam \rightarrow cleaner than PP or $P\bar{P}$
- e^+/e^- data taking can exploit EW effects
- Several orders of magnitude reach in Q^2, x





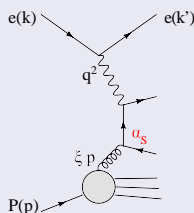
In DIS charm and beauty production comes mainly from BGF (Analogous with flavour creation processes in hadron-hadron collisions). One can measure the structure functions $F_2^{c\bar{c}}$ and $F_2^{b\bar{b}}$ by tagging events via:

- Impact Parameter
- D meson production
- semileptonic heavy quark decays

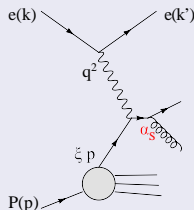
This gives sensitivity to the gluon PDF



Boson-Gluon Fusion



QCD Compton



The eP environment is excellent for jet physics.

- Jets are copiously produced at HERA.
- Minimal contribution from underlying event (at High Q^2)

k_T algorithm is the algorithm of choice at HERA

- Sensitivity to α_S in jet production cross sections
- Sensitivity to $g(x, Q^2)$ in cross sections
- Possibility of studying jet substructure



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NC Double Differential Cross-Section

$$\frac{d^2\sigma_{NC}^{e^\pm p}}{dx dQ^2} = \frac{2\pi\alpha^2 Y_\pm}{xQ^4} [F_2^{NC}(x, Q^2) - \frac{y^2}{Y_+} F_L^{NC}(x, Q^2) \mp \frac{Y_-}{Y_+} x F_3^{NC}(x, Q^2)] (1 + \delta_r)$$

$$\frac{d^2\sigma_{NC}^{e^\pm p}}{dx dQ^2} = \frac{d^2\sigma_{NC,Born}^{e^\pm p}}{dx dQ^2} (1 + \delta_r)$$

$$Y_\pm = 1 \pm (1 - y)^2$$

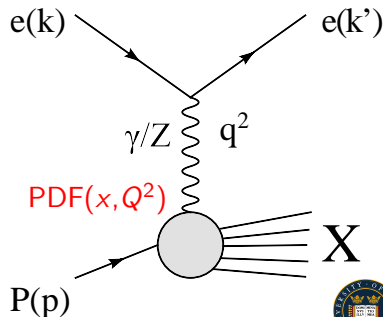
δ_r Electroweak radiative correction

Structure Functions

		LO QCD
F_2	Dominates most phase space	$\sum x(q_i + \bar{q}_i)$
$x F_3$	Parity violating (high Q^2)	$\sum x(q_i - \bar{q}_i)$
F_L	Longitudinal SF (high y)	0

From scaling violations:

$$F_L \approx \alpha_s x g(x, Q^2)$$



CC Double Differential Cross-Section

$$\frac{d^2\sigma_{CC}^{e^\pm p}}{dx dQ^2} = \frac{G_F^2 M_W^2}{4\pi x(Q^2 + M_W^2)^2} [Y_+ F_2^{CC}(x, Q^2) - y^2 F_L^{CC}(x, Q^2) \mp Y_- x F_3^{CC}(x, Q^2)] (1 + \delta_r)$$

Structure Functions

$$F_{2,e^+}^{CC} = x(\textcolor{red}{d} + s + \bar{u} + \bar{c})$$

$$xF_{3,e^+}^{CC} = x(\textcolor{red}{d} + s - \bar{u} - \bar{c})$$

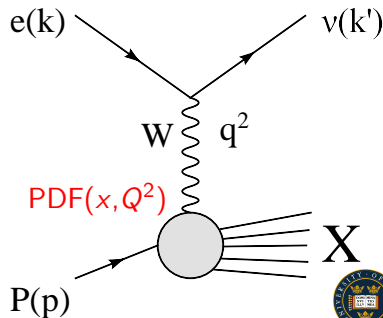
$$F_{2,e^-}^{CC} = x(\textcolor{red}{u} + c + \bar{d} + \bar{s})$$

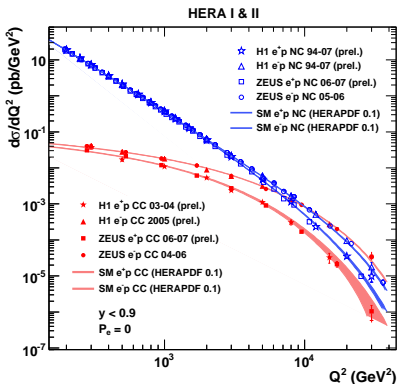
$$xF_{3,e^-}^{CC} = x(\textcolor{red}{u} + c - \bar{d} - \bar{s})$$

Reduced Cross Sections

$$\tilde{\sigma}_{e^+}^{CC} = x[(1-y)^2(\textcolor{red}{d} + s) + \bar{u} + \bar{c}]$$

$$\tilde{\sigma}_{e^-}^{CC} = x[(1-y)^2(\bar{d} + \bar{s}) + \textcolor{red}{u} + c]$$





ZEUS-prel-09-001

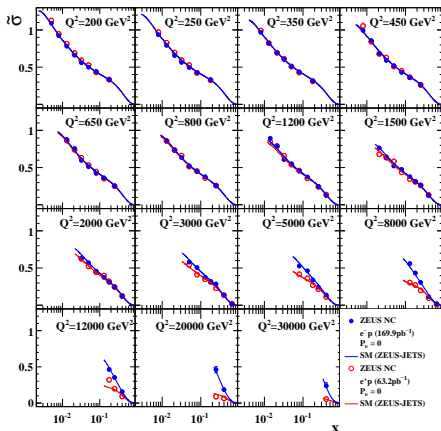
Differential cross section well described by SM

- NC cross section much larger at lower Q^2
- CC and NC similar for $Q^2 \approx M_V^2$
- Differences in e^+p and e^-p CC from PDFs
- Differences in e^+p and e^-p NC from EW effects

There are also also data subsets with longitudinally polarised e^\pm beams



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More important for PDF fitting are the reduced cross sections.

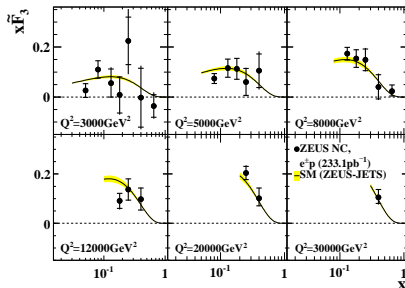
- Well described by SM prediction
- HERA II e^-p sample $10\times$ HERA I lumi
- Can now obtain much more precise $x F_3$ from $e^\pm p$ difference

Eur. Phys. J. C62 (2009) 625

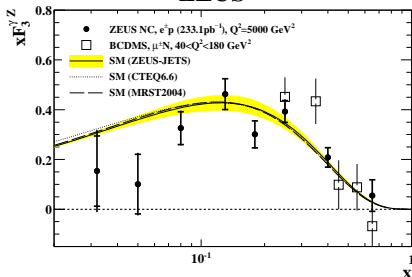


$$xF_3 \propto \sum x(q_i - \bar{q}_i)$$

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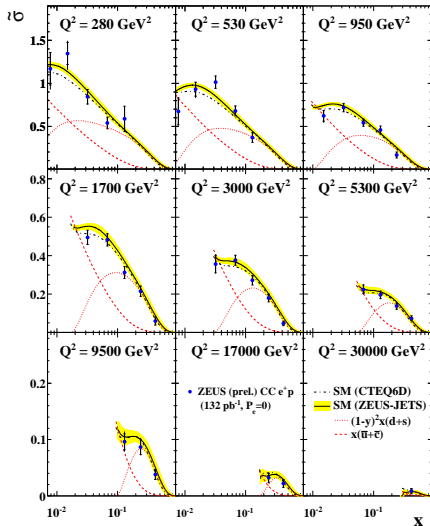
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Eur. Phys. J. C62 (2009) 625



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New measurements of CC DIS cross sections have been performed:

- Large e^-p sample (Eur. Phys. J. C61 (2009) 223)
- Large new e^+p sample (ZEUS-prel-09-002)

The flavour selecting properties of the charged exchange mean that e^+p data is particularly useful for constraining the d PDF.



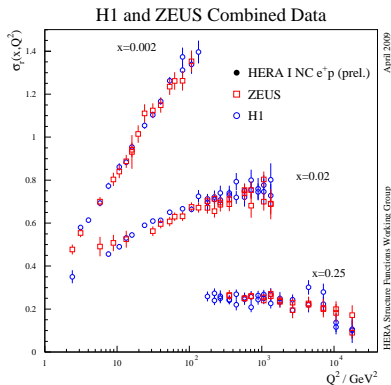
H1+ZEUS Combined Data

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Measuring F_i and PDFs at HERA
 F_2 and xF_3
Measurements of F_L
PDF Fits
Heavy Flavour Production
Isolated γ Production

In addition to new data, considerable progress has been made in combining results made using the data collected from 1994-2000.
Strategy:

- Swim measurements to common x , Q^2 grid
- Correct data to same E_p (920 GeV)
- Calculate average values and uncertainties^a using a global combination
- Evaluate procedural uncertainties



^a arXiv:0904.0929



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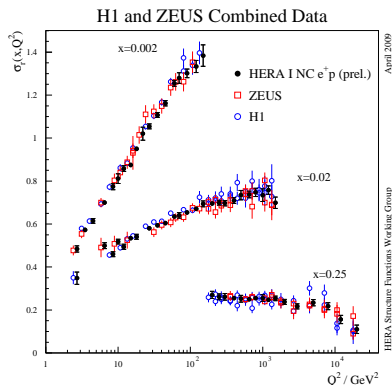
1402 points combined to 741 unique measurements

- $\chi^2/\text{ndf} = 637/656$
- 110 systematic uncertainties from experiments
- 3 systematic uncertainties from combination

Overall precision is improved:

- $3 < Q^2 < 500 \text{ GeV}$ 2% precision
- $20 < Q^2 < 100 \text{ GeV}$ 1% precision

H1prelim-09-045,ZEUS-prel- 09-011



Recall that for unpolarised $e^\pm p$ scattering:

$$\frac{d^2\sigma^{e^\pm p}}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} [Y_+ F_2(x, Q^2) - y^2 F_L(x, Q^2) \mp Y_\mp x F_3(x, Q^2)]$$

For now we can neglect $x F_3$ and write an expression of the reduced cross section (σ_r)

$$\sigma_r = \left(\frac{xQ^4}{2\pi\alpha^2 Y_+} \right) \frac{d^2\sigma^{e^\pm p}}{dx dQ^2} = \left[F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2) \right]$$

for F_L Measurements at different y for the same x, Q^2 required.
Solution? **Use different beam energies**

Choice of energies is made to maximise difference in $\frac{y^2}{Y_+}$



Measuring F_L at HERA

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E_p (GeV)	460	575	920
H1 \mathcal{L} (pb $^{-1}$)	12	6	22
ZEUS \mathcal{L} (pb $^{-1}$)	14	7	44

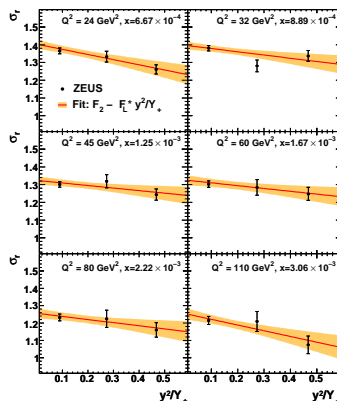
- The first direct measurements of F_L have now been published^a.
- In addition H1 have produced a new measurement^b in an extended Q^2 range:
 $2.5 < Q^2 < 800 \text{ GeV}$
- For $Q^2 > 10 \text{ GeV}$ measurement in good agreement with pQCD

^aPhys. Lett. B665 (2008) 139,

DESY-09-046

^bH1prelim-09-044

ZEUS



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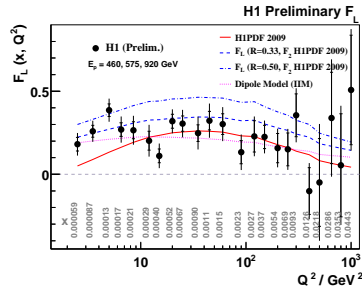
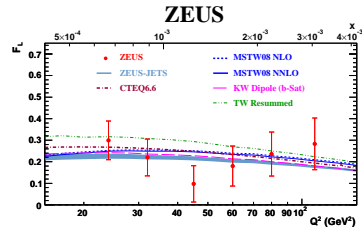
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^aPhys. Lett. B665 (2008) 139,

DESY-09-046

^bH1prelim-09-044



Both H1 and ZEUS have performed their own PDF fits.
Analysis is made using the DGLAP equations:

DGLAP Equations

$$\frac{\partial q_i(x, \mu^2)}{\partial \ln \mu^2} = \frac{\alpha_s(\mu^2)}{2\pi} \int_x^1 \frac{dz}{z} \left(\sum_j P_{q_i q_j} \cdot q_j\left(\frac{x}{z}, \mu^2\right) + P_{q_i g} \cdot g\left(\frac{x}{z}, \mu^2\right) \right)$$

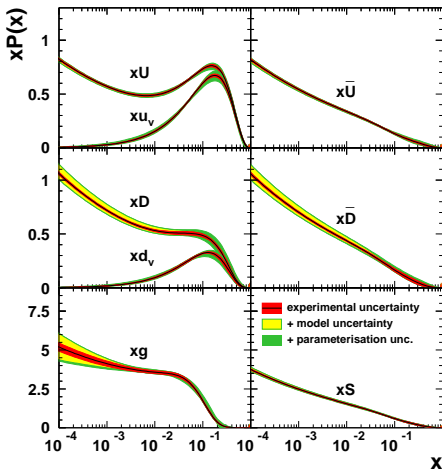
$$\frac{\partial g_i\left(\frac{x}{z}, \mu^2\right)}{\partial \ln \mu^2} = \frac{\alpha_s(\mu^2)}{2\pi} \int_x^1 \frac{dz}{z} \left(\sum_j P_{g q_j} \cdot q_j\left(\frac{x}{z}, \mu^2\right) + P_{g g} \cdot g\left(\frac{x}{z}, \mu^2\right) \right)$$

The DGLAP equations tell us the PDF(Q^2, x) given PDF(Q_0^2, x)

In addition a new PDF fit to the combined data (HERAPDF) has been made.



H1PDF 2009, $Q^2 = 4 \text{ GeV}^2$



New H1 fit^a uses only H1 data:

Data Set		Data Points	χ^2_{unc}
low Q^2	[2]	58	55.9
medium Q^2	this measurement	99	81.5
e^+p NC high Q^2 , 94 – 97	[7]	130	92.6
e^+p CC high Q^2 , 94 – 97	[7]	25	21.2
e^-p NC high Q^2 , 98 – 99	[8]	139	112.1
e^-p CC high Q^2 , 98 – 99	[8]	28	17.3
e^+p NC high Q^2 , 99 – 00	[9]	147	137.4
e^+p CC high Q^2 , 99 – 00	[9]	28	31.1

Fits 5 PDFs : $xu_v, xd_v, xg,$
 $x\bar{U} = \bar{u} + \bar{c}, x\bar{D} = \bar{d} + \bar{s} + \bar{b}$

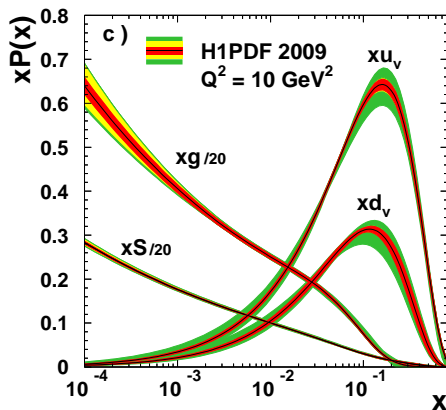
^aDESY-09-005



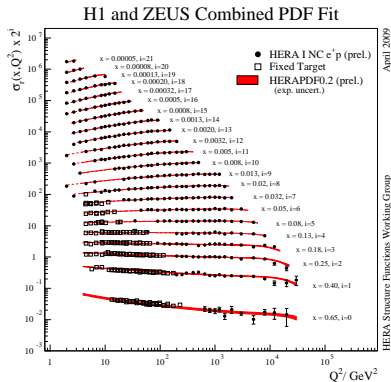
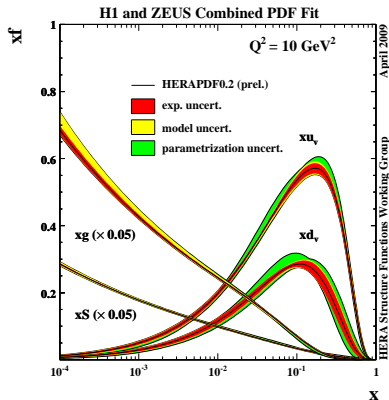
- Good fit to the data
 $\chi^2/n.d.f = 587/644$
- Reduced uncertainty at low- x
w.r.t. H1PDF2000
- Larger (more realistic)
uncertainties at high- x (new
parametrisation uncertainty
dominant)

Parametrisation Uncertainty

New uncertainty determined by using
parametrisations which describe data
well but have unphysical behaviour at
large x



Similar procedure adopted for fit to combined HERA data¹:

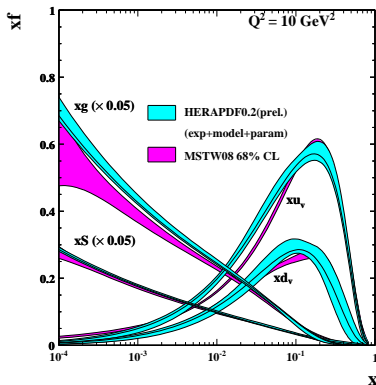
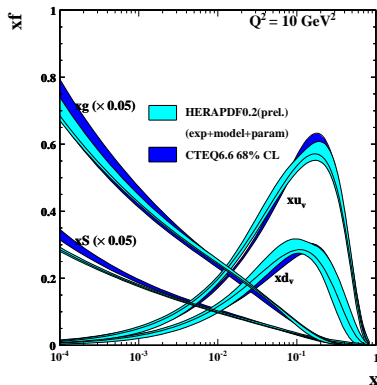


A beautiful fit to the data: $\chi^2/n.d.f. = 576/592$

¹H1prelim-09-045,ZEUS-prel- 09-011



The new combined HERA-I fit compares well with global fits:

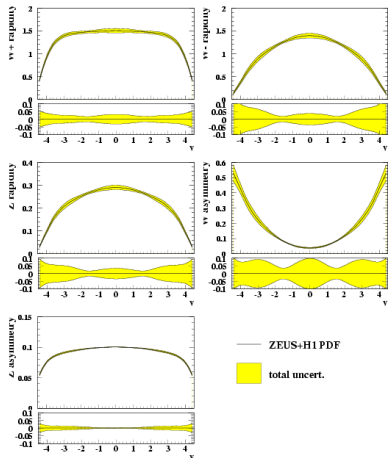


This has implications for the LHC



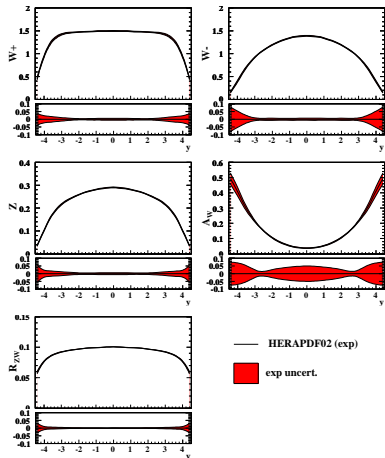
ZEUS-S: ZEUS + H1

W and Z rapidity distributions



HERA PDF

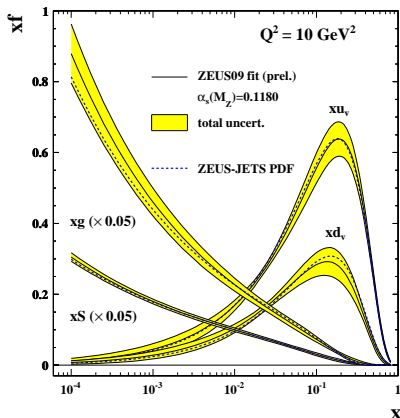
W and Z rapidity distributions



New ZEUS Fit

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ZEUS-prel-09-010

ZEUS-Jets showed that adding jet data constrains the gluon better. New ZEUS fits show areas of improvement with HERA II data. Added data relative to ZEUS-jets:

- High Q^2 e^-p NC
- High Q^2 e^-p CC
- High Q^2 e^+p CC
- F_L measurement

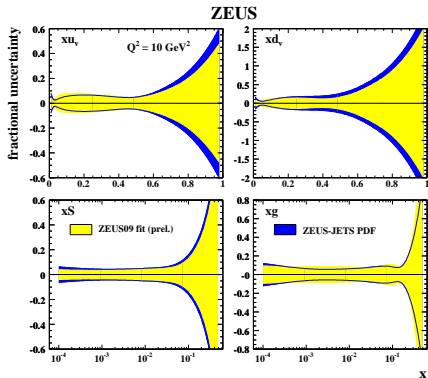
1060 points with $\chi^2/n.d.f. = 0.97$
Polarised data treated separately \rightarrow EW sensitivity



New ZEUS Fit

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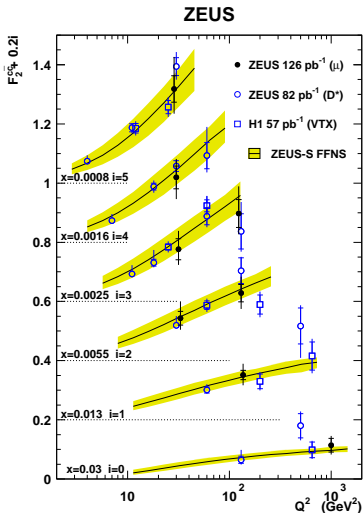
Measuring F_i and PDFs at HERA
 F_2 and $\times F_3$
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Comparison of uncertainties on new fit to ZEUS-JETS shows areas of improvement from adding HERA II data:

- Better u_v at high- x from Highest Q^2 e^-p NC and CC data
- Better d_v at high- x from Highest Q^2 e^+p CC data
- Better g from F_L data





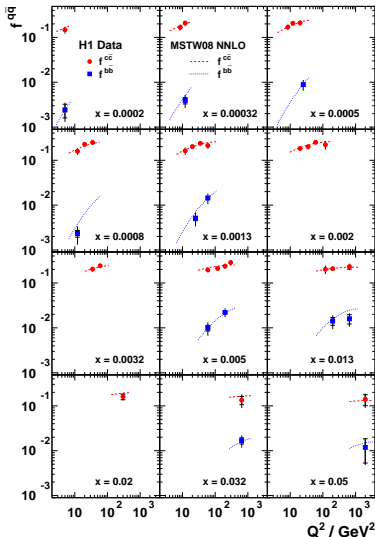
A new measurement^a of $F_2^{c\bar{c}}$ and $F_2^{b\bar{b}}$ using muons to tag events.

- Results for $F_2^{c\bar{c}}$ shown here
- Results agree well with QCD predictions
- Agree well with measurements from D^* events and inclusive impact parameter measurements

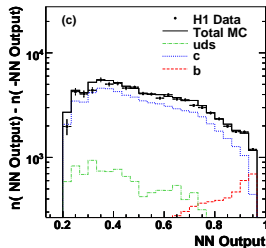
^a DESY-09-056



H1 CHARM AND BEAUTY CROSS SECTION FRACTION



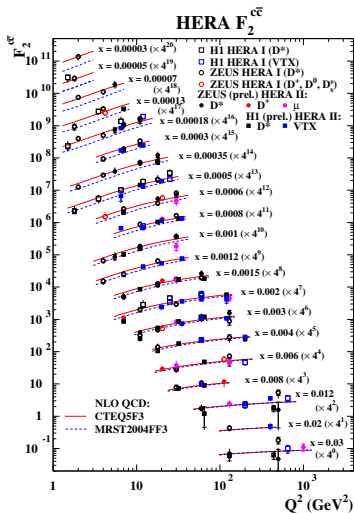
New measurement^a of $F_2^{c\bar{c}}$ and $F_2^{b\bar{b}}$
(inclusive impact parameters)



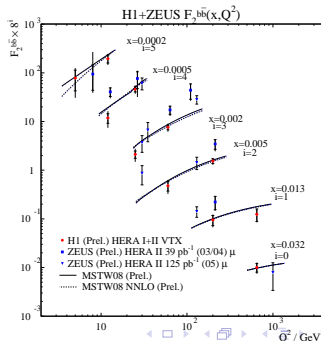
- Smallest extrapolation to $F_2^{Q\bar{Q}}$
- Agrees well with QCD predictions

^a DESY-09-096

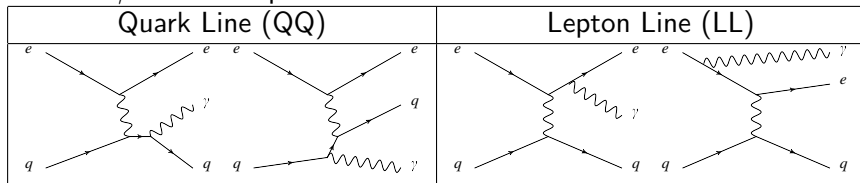




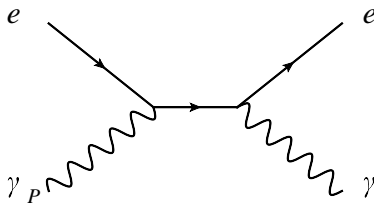
- Detailed, consistent picture of $F_2^{Q\bar{Q}}$ has been built up
- Many independent measurements of $F_2^{c\bar{c}}$
- Still much to learn about $F_2^{b\bar{b}}$



Isolated γ s at HERA produced via:



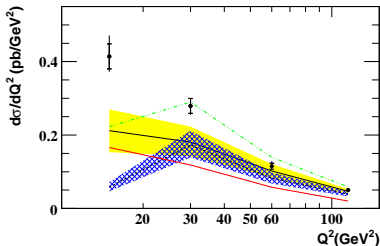
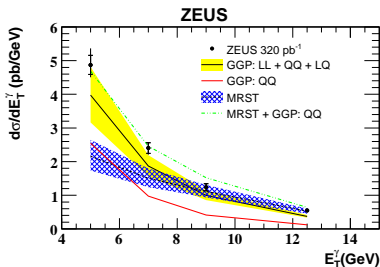
As a consequence of adding QED corrections to the PDFs² a photon component γ_P of the PDFs arises. Giving also $e\gamma_P \rightarrow e\gamma$



- $\gamma_P(Q^2, x)$ important for EW corrections at LHC
- MRST2004 the only PDF with full QED corrections
- Used old ZEUS data to cross check γ_P PDF

²Eur. Phys. J. C39, No. 2. (2005), 155





New measurement of isolated photon production at ZEUS:

- Compared to GGP^a
- Also compared to MRST2004 prediction (LL component only)
- Finally (green line) compared to MRST2004 LL and GGP QQ

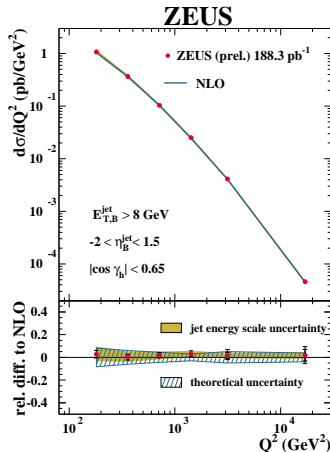
E_T spectrum well described by theories, but problems with Q^2 spectrum. (Similar behaviour w.r.t to GGP previously observed by H1)
MSTW08 with QED corr. in preparation

^a Gehrman-De Ridder et al. - Phys. Rev. Lett.96:132002 (2006)



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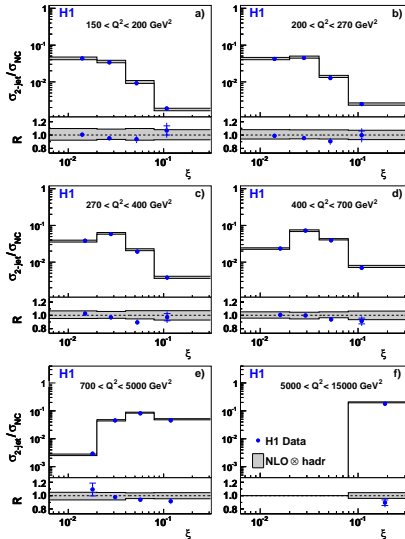
Inclusive jets in High Q^2 NC^a:

- A stringent test of pQCD
- Good description by NLO QCD over large Q^2 range
- Theoretical uncertainty dominates experimental uncertainty at high Q^2
- In some regions PDFs the dominant theoretical uncertainty
→ can constrain the gluon

^aZEUS-prel-09-006



Normalised 2-Jet Cross Section



New H1 inclusive and multijet measurement ^a:

- momentum fraction carried by incoming parton:

$$\zeta = x_{Bj}(1 + \frac{M_{12}^2}{Q^2})$$

- Normalised dijet cross sections as a function of ζ
- NLO cross sections describe data well
- Theory error (Higher orders) significantly larger than exp.

^a DESY-09-032



Measurements of α_s

Introduction
PDFs
Jets
Summary

Jet Production in DIS
Measurements of α_s
Jet Substructure

From H1 multijet paper:

Extraction of α_s

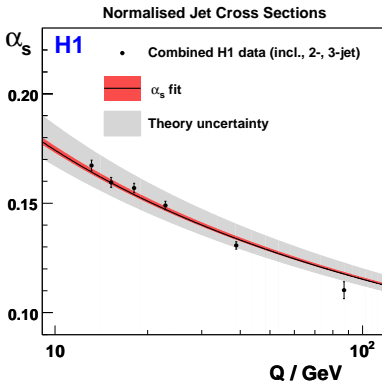
- QCD predictions were fitted using a χ^2 method
- Values of α_s were extracted by fitting the individual normalized inclusive, 2-jet, 3-jet cross sections and their combination

Fit quality $\chi^2/n.d.f. = 65/53$

DESY-09-032

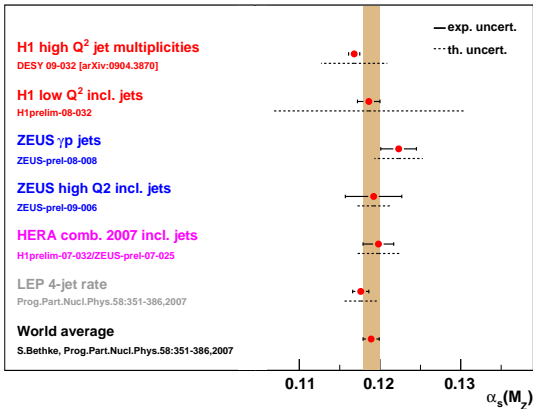
See the poster by A.

Baghdasaryan



Observed running of α_s as expected from QCD





- Extracted values of α_s compatible with world average
- Comparable precision to e^+e^- measurements
- Different measurements, environments and processes consistent

Great success of QCD!
More HERA jet measurements to be seen in K. Hatakeyama's talk



Jet substructure can be studied by re-running the k_T algorithm with smaller values of the resolution parameter y_{cut}

Subjet distributions can be used to study:

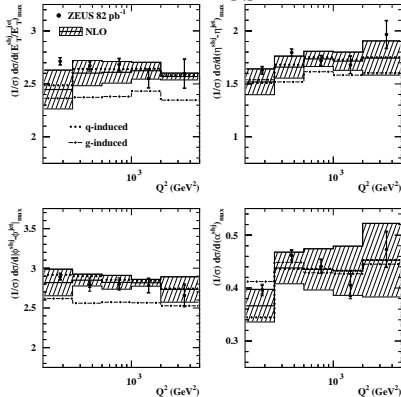
- Pattern of radiation from the primary parton
 - Direct test of the splitting functions and scale dependence
- Colour coherence
 - soft radiation tends to be emitted in the proton direction

As attention at the LHC turns to jet-substructure as tool for boosted-heavy particle reconstruction³ it is very interesting to see theory confront real data on jet substructure.

³Phys.Rev.Lett.100:242001,2008



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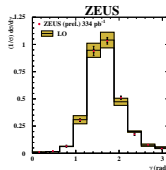
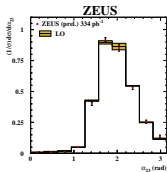
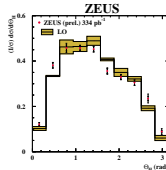
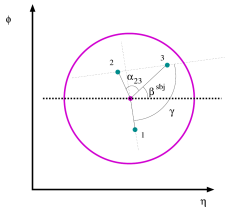


Study of jets with exactly two subjets for $y_{cut} = 0.05^a$

- Normalised cross sections well described by pQCD predictions
- Scale dependence of radiation from partons well described by pQCD

^aDESY-08-178





Subject distributions for jets with 3 subjects for $y_{\text{cut}} = 0.03$

- θ_H - angle between planes determined by the highest E_T subject and the beam and the two lowest E_T subjects
- α_{23} - The angle between the highest E_T subject and the vector difference of the two lowest E_T subjects as seen from the jet center in the $\eta - \phi$ plane
- γ - The angle between the highest E_T subject and the vector difference of the two lowest E_T subjects

pQCD predictions give an adequate description of the data

ZEUS-prel-09-007



- 1 Introduction
- 2 Structure Functions and Parton Distribution Functions
- 3 Jets
- 4 Summary**



HERA continues to produce important QCD measurements:

- World leading proton structure determination:
 - New data at highest Q^2 will help constrain valence PDFs
 - $F_2^{Q\bar{Q}}$ with increasing precision
 - Potential to measure photon component of the proton
 - New combined data even more precise than using separate results
- Precise measurements of α_S
- Excellent determination of jet cross sections:
 - Theoretical uncertainties often larger than experimental
 - Potential to constrain the gluon PDF



Back-Up Slides

EW results
Combination and PDF fits

Back-Up Slides begin here



5 EW results

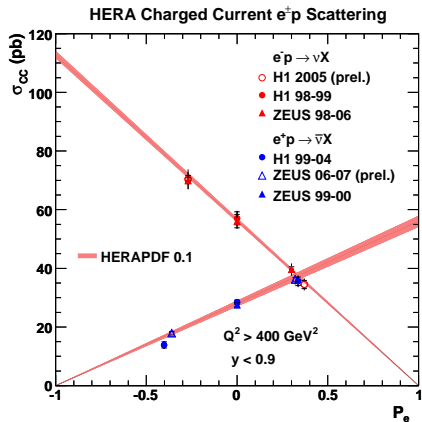
6 Combination and PDF fits



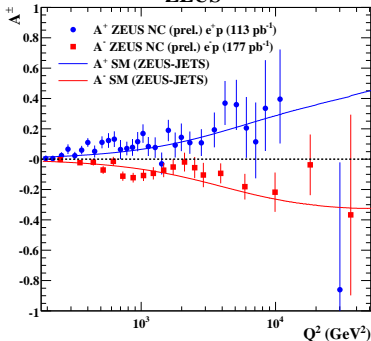
Total CC Cross section

EW results
Combination and PDF fits

CC Cross Section
EW Fit results



ZEUS



ZEUS-prel-07-012
ZEUS-prel-08-005

With polarised e^\pm we now have access to Polarisation asymmetries:

$$A^\pm = \frac{2}{\mathcal{P}_R - \mathcal{P}_L} \cdot \frac{\sigma^\pm(\mathcal{P}_R) - \sigma^\pm(\mathcal{P}_L)}{\sigma^\pm(\mathcal{P}_R) + \sigma^\pm(\mathcal{P}_L)}$$

to a good approximation:

$$A^\pm \simeq \mp k a_e \frac{F_2^{\gamma Z}}{F_2}$$

at large Bjorken- x

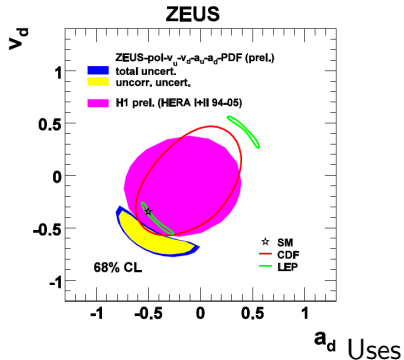
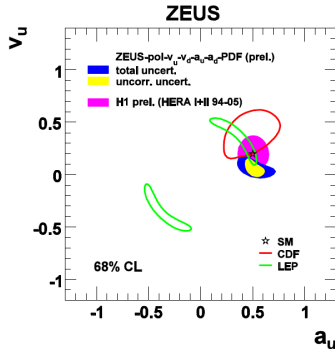
$$A^\pm \simeq \mp -k \frac{1+d_v/u_v}{4+d_v/u_v}$$



EW Fit Results

EW results
Combination and PDF fits

CC Cross Section
EW Fit results



only the preliminary version of the new e^-p NC data



5 EW results

6 Combination and PDF fits



Non ZEUS sources:

- F_2 data on $\mu - p$ scattering from BCDMS [39], NMC [40], and E665 [41];
- deuterium-target data from NMC [40] and E665 [41]. These were included in order to have \bar{u} , \bar{d} flavour separation;
- NMC data on the ratio F_2^D/F_2^p [42]. These determine the ratio of the d to u valence shapes;
- the CCFR [43] xF_3 data, from (anti-)neutrino interactions on an iron target. These give the strongest constraint on high- x valence PDFs. They are used only in the x range $0.1 \leq x \leq 0.65$ in order to minimize dependence on the heavy-target corrections. The latter were performed according to the prescription of MRST [31]. These xF_3 data are unaffected by the recent re-analysis of CCFR F_2 data [44,45].

