

# Jets and $\alpha_s$ Measurements at HERA

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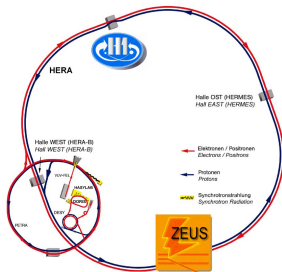
On Behalf of the H1 and ZEUS Collaborations  
The 2009 Europhysics Conference on High Energy Physics  
Krakow, July 2009



## Outline:

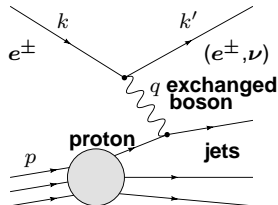
- 1 Jet Production at HERA and Technicalities
- 2 Inclusive Jets in Photoproduction
- 3 Inclusive Jets at Low  $Q^2$
- 4 Inclusive- and Multi-Jets at High  $Q^2$
- 5 Summary

# HERA



## Electron-Proton Collisions at HERA:

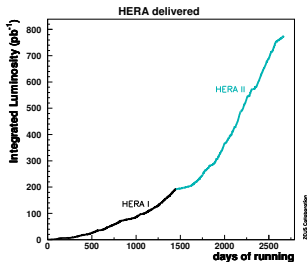
$\sqrt{s} = 318 \text{ GeV}$  ← center of mass energy



## Kinematic Variables:

- $Q^2 = -(\mathbf{k} - \mathbf{k}')^2$  ← virtuality of exchanged boson
- $x = \frac{Q^2}{p \cdot q}$  ← Bjorken scaling variable
- $y = \frac{Q^2}{s \cdot x}$  ← inelasticity parameter

$$Q^2 = s \cdot x \cdot y$$



# Jet Production at HERA

## Kinematic Regimes:

- 1 photoproduction ( $\gamma p$ ):  $Q^2 \approx 0 \text{ GeV}^2$
- 2 deep inelastic scattering (**DIS**):  $Q^2 > 1 \text{ GeV}^2$

## Jet cross section in pQCD: Series expansion in powers of $\alpha_s$

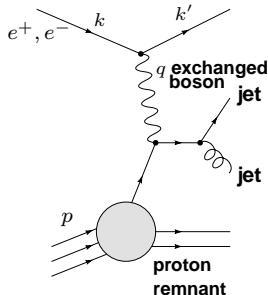
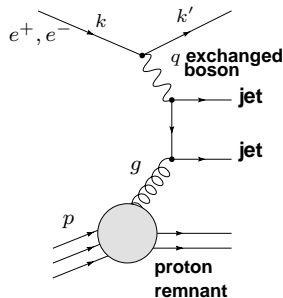
$$\sigma_{\text{jet}} = \sum_m \alpha_s^m(\mu_R) \sum_{a=q,\bar{q},g} f_{a/p}(x, \mu_F) \otimes \hat{\sigma}_{a,m}(x, \mu_R, \mu_F) (1 + \delta_{\text{had}}) \dots$$

## Coefficients are **convolutions** of:

- parton distribution functions (PDFs)  $f_{a/p}$  (and of  $\gamma$ -PDF in case of  $\gamma p$ )
- hard scattering matrix element  $\hat{\sigma}$

## Measurement:

- test concept of pQCD, factorization, universality of strong coupling and PDFs
- using factorization, pQCD  $\rightarrow$  extraction of  $\alpha_s$ , PDFs



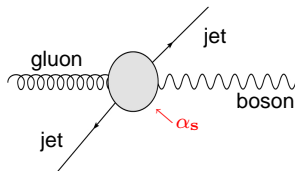
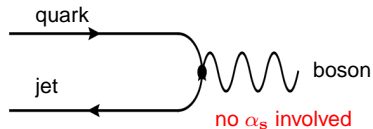
# Technicalities

## The Breit Frame in DIS

the Breit frame is suitable for studying QCD with high  $E_T$  jets

- exchanged boson space-like
- **struck quark in Born level has zero  $E_T$**  (no QCD involved)
- **directly sensitive to hard QCD processes**  $\rightarrow$   $E_T$  can be used for identification
- suppression of beam remnant jet

- **jets are reconstructed in the Breit frame** using the  $k_\perp$  cluster algorithm
  - $\rightarrow$  **infrared and collinear safe**
- data are corrected for detector, QED, electro-weak effects with MC models
- NLO predictions are corrected for parton shower and hadronisation effects



# ZEUS: Inclusive Jets in Photoproduction (1/2)

## Previous Publication:

- data (98-00) with  $82 \text{ pb}^{-1}$  luminosity
- $\alpha_s$  extracted from  $\frac{d\sigma}{dE_T}$ 

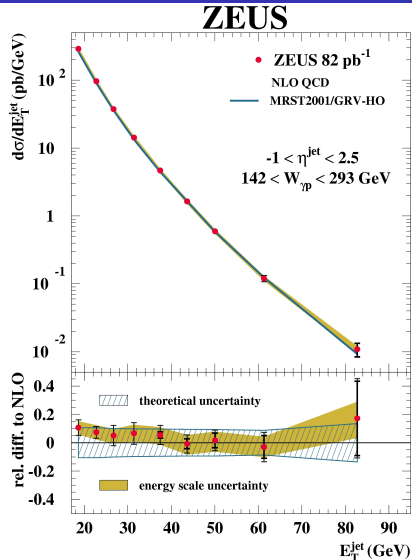
$$\alpha_s(M_Z) = 0.1224 \pm 0.0001 \text{ (stat.)}$$

$$\begin{matrix} +0.0022 \\ -0.0019 \end{matrix} \text{ (exp)}$$

$$\begin{matrix} +0.0054 \\ -0.0043 \end{matrix} \text{ (th)}$$
- **theory error dominates (4.2%)** over experimental error ( $\approx 1.7\%$ )

## $\alpha_s$ from re-analysis (same data):

- **theory:**
  - $O(\alpha_s^2)$ : Klasen, Kleinwort, Kramer
  - **MRST2001** (previously: MRST99)
  - photon PDFs: GRV-HO
  - $\mu_R = \mu_F = E_T^{\text{jet}}$  for each jet
- **new method for  $\mu_R$  variation** (Jones et al.)



- **good data description by NLO prediction!**

# ZEUS: Inclusive Jets in Photoproduction (2/2)

## $\alpha_s$ Extraction:

- pQCD calculations depend on  $\alpha_s$  via the partonic cross section and the PDFs
- NLO calculations using various sets of PDFs with different assumed  $\alpha_s$  were performed
- parametrize  $\alpha_s(M_Z)$  dependence of observable  $d\sigma/dA$  in bin  $i$  according to

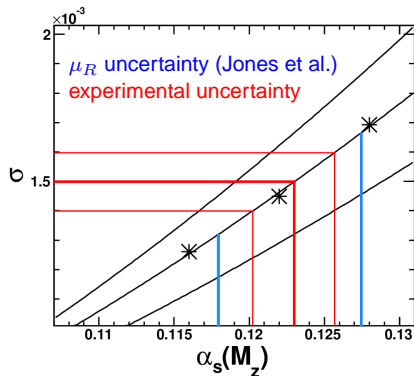
$$\frac{d\sigma_i}{dA} = C_1 \cdot \alpha_s(M_Z) + C_2 \cdot \alpha_s^2(M_Z)$$

- map measured  $d\sigma/dA$  to x-axis and extract  $\alpha_s(M_Z)$

⇒ **complete  $\alpha_s$  dependence of the calculations and the PDFs is preserved!**  
(matrix elements and PDF evolution)

- $\alpha_s(M_Z) = 0.1223 \pm 0.0001(\text{stat.})^{+0.0023}_{-0.0021}(\text{sys.}) \pm 0.0030(\text{th.})$

⇒ **very precise  $\alpha_s$  determination with 3.1% total error!**



# H1: Inclusive Jet Production at Low $Q^2$ (1/3)

## DIS at low $Q^2$ :

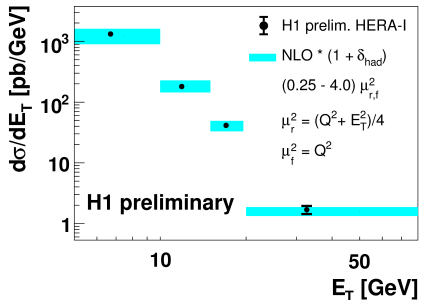
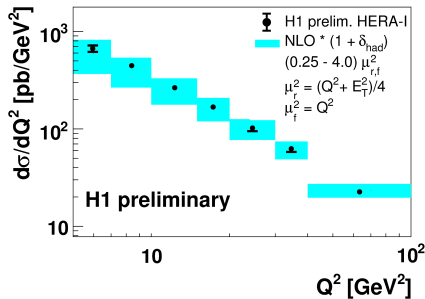
- lots of statistic
- electron in backward region
- ⇒ natural place to look first

- **but:** reliability of pQCD at NLO with decreasing  $Q^2$  or  $E_T$ ?

- used integrated luminosity:  $44 \text{ pb}^{-1}$
- $5 < Q^2/\text{GeV}^2 < 100$
- $E_{T,\text{Breit}}^{\text{jet}} > 5 \text{ GeV}$
- inclusive jet and dijet measurement

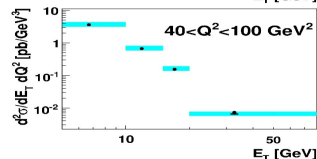
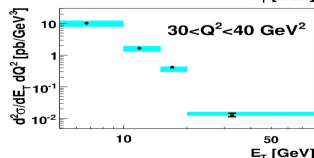
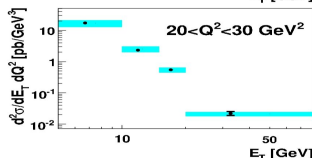
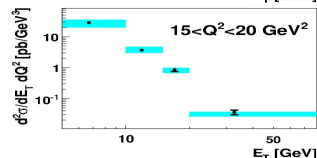
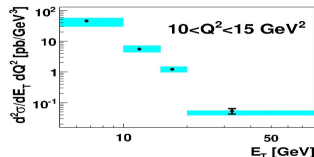
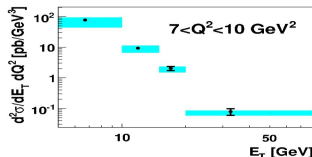
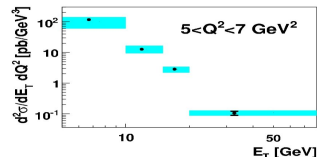
## Main Sources of Experimental Systematical Uncertainties:

- ① hadronic energy scale uncertainty  
→  $\frac{\Delta\sigma}{\sigma} \approx 4 - 10\%$
- ② acceptance correction uncertainty  
→  $\frac{\Delta\sigma}{\sigma} \approx 2 - 15\%$



# H1: Inclusive Jet Production at Low $Q^2$ (2/3)

$$\frac{d^2\sigma}{dQ^2 dE_T}$$



● H1 preliminary HERA-I

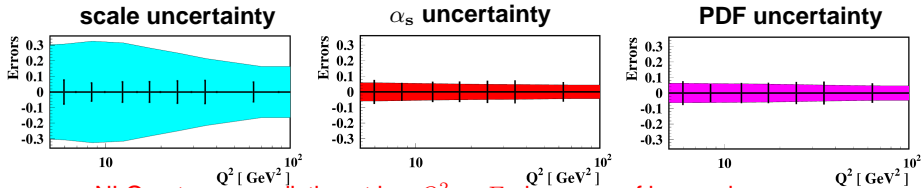
■  $\text{NLO}^*(1 + \delta_{\text{had}})$

$$\mu_r^2 = (Q^2 + E_T^2)/4, \mu_f^2 = Q^2$$

- larger NLO errors compared to data uncertainties
- good data description by NLO predictions within errors!



# H1: Inclusive Jet Production at Low $Q^2$ (3/3)



- **NLO not very predictive at low  $Q^2$  or  $E_T$  because of low scales**

- renormalization scale uncertainty dominates and increases with decreasing  $Q^2$  and at low  $E_{T,\text{Breit}}^{\text{jet}}$

→ **orders beyond NLO are needed in theoretical predictions!**

## $\alpha_s$ Extraction:

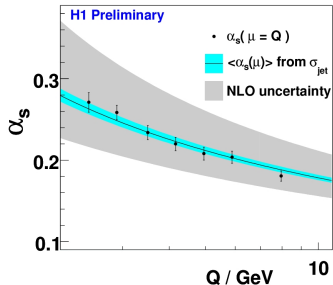
- double differential inclusive jet cross sections

$$\alpha_s(M_Z) = 0.1186 \quad \begin{array}{l} \pm 0.0014 \text{ (exp.)} \\ +0.0132 \text{ (theory)} \\ -0.0101 \text{ (theory)} \\ \pm 0.0021 \text{ (PDF)} \end{array}$$

⇒

- **$\approx 1\%$  exp. uncertainty,  $\approx 10\%$  theoretical error**

$\alpha_s$  from Inclusive Jet Cross Section (HERA-I)



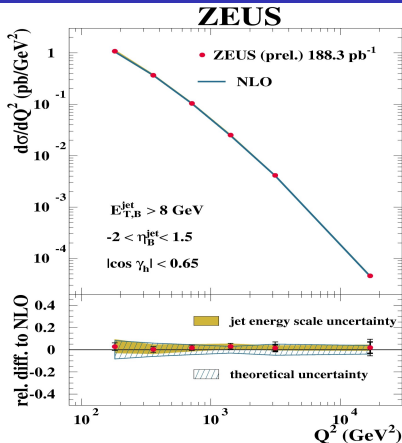
# ZEUS: Inclusive NC Jets at High $Q^2$ (1/4)

- **stringent tests of pQCD calculations at high  $E_T$**
- data taken between 2004 - 2006 were used
- integrated luminosity:  $188 \text{ pb}^{-1}$

→ shown is the single-differential **inclusive jet NC cross section** as a function of  $Q^2 > 125 \text{ GeV}^2$

- *dijet cross sections: see Juan Terron's talk*

- **good description** of data by NLO QCD over many orders of magnitude (for both  $\mu_R = E_{T,B}$  and  $Q$ )
- smaller **theoretical uncertainty** than dijets, but still **dominates** over experimental except at high  $Q^2$

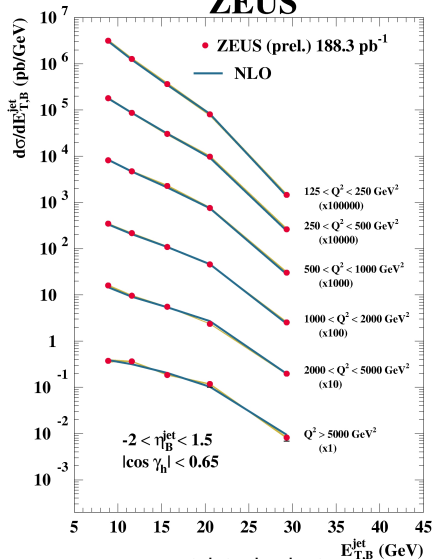


## Main Sources of Exp. Sys. Uncertainties:

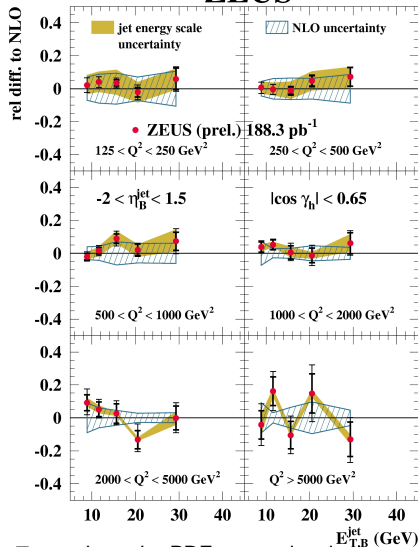
- 1 hadronic energy scale uncertainty  
→  $\frac{\Delta\sigma}{\sigma} \approx 5\%$
- 2 model dependence of acceptance correction  
→  $\frac{\Delta\sigma}{\sigma} \approx 3\%$

# ZEUS: Inclusive NC Jets at High $Q^2$ (2/4)

## ZEUS



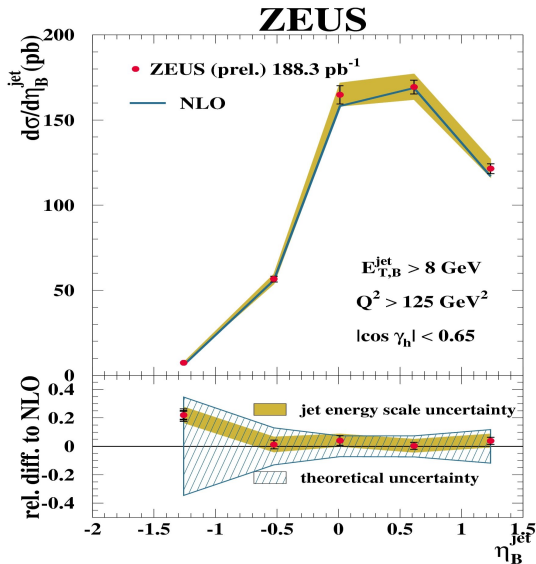
## ZEUS



- $\mu_R$  uncertainty dominates except at high  $E_{T,B}$  where the PDF uncertainty is dominant  $\Rightarrow$  **potential to further constrain the gluon density in the proton**

# ZEUS: Inclusive NC Jets at High $Q^2$ (3/4)

- inclusive jet cross section as a function of  $\eta_{\text{Breit}}$
- $\frac{d\sigma}{d\eta}$  shape is dictated by kinematic constraints
- **good agreement** between data and NLO for  $\frac{d\sigma}{d\eta}$



# ZEUS: Inclusive NC Jets at High $Q^2$ (4/4)

## $\alpha_s$ Extraction:

- extracted from  $\frac{d\sigma}{dQ^2}$  for  $Q^2 > 500 \text{ GeV}^2 \Rightarrow$  yields smaller total  $\alpha_s$  error
- **experimental uncertainties:**
  - $\rightarrow$  largest contribution due to jet energy scale uncertainty ( $\pm 1.9\%$ )
- **theoretical uncertainties:**
  - $\rightarrow$  dominated by terms beyond NLO ( $\pm 1.8\%$ )
  - $\rightarrow$  PDF ( $\pm 0.8\%$ )
  - $\rightarrow$  hadronisation corrections ( $\pm 0.8\%$ )

$$\alpha_s(M_Z) = 0.1192 \pm 0.0009(\text{stat.})_{-0.0032}^{+0.0035}(\text{exp.})_{-0.0021}^{+0.0020}(\text{th.})$$

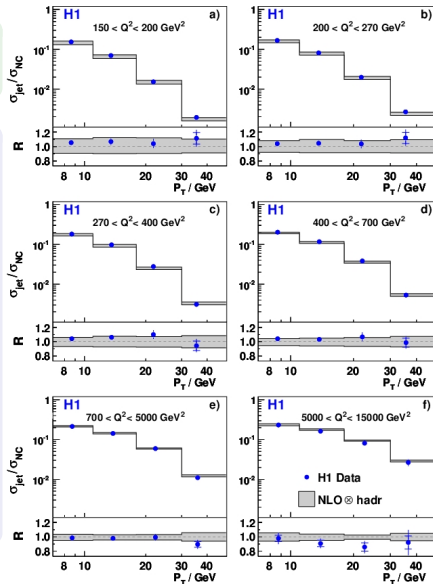
$\Rightarrow$  precise measurement with a total error of about 3.5%!

# H1: Inclusive and Multi-Jet Production at High $Q^2$ (1/2)

data sample with  $395 \text{ pb}^{-1}$   
luminosity

- $150 < Q^2/\text{GeV}^2 < 15000$
- single inclusive, 2- and 3-jet cross sections were measured
- normalization to the inclusive neutral current DIS scattering cross section
  - luminosity uncertainty cancels and energy scale uncertainty reduces in normalized cross sections
- data are well described by NLO predictions!

Normalised Inclusive Jet Cross Section



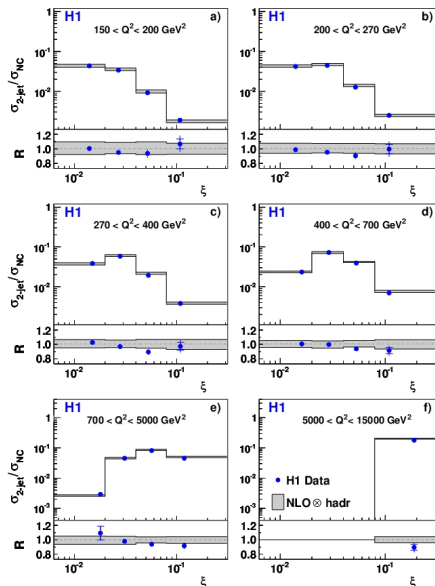
# H1: Inclusive and Multi-Jet Production at High $Q^2$ (2/3)

## Dijet Production:

- momentum fraction carried by the interacting parton:  

$$\xi = x_{Bj} \cdot \left(1 + \frac{M_{12}^2}{Q^2}\right)$$
- normalised dijet cross sections** as a function of  $\xi$  in several regions of  $Q^2$
- NLO predictions provide a **good description of the data** over the whole used phase space
- theory error is significantly larger** than experimental errors in almost all bins
  - $\mu_R$  uncertainty is largest theory error
  - jet energy scale uncertainty dominates experimental uncertainty

## Normalised 2-Jet Cross Section



# H1: Inclusive and Multi-Jet Production at High $Q^2$ (3/3)

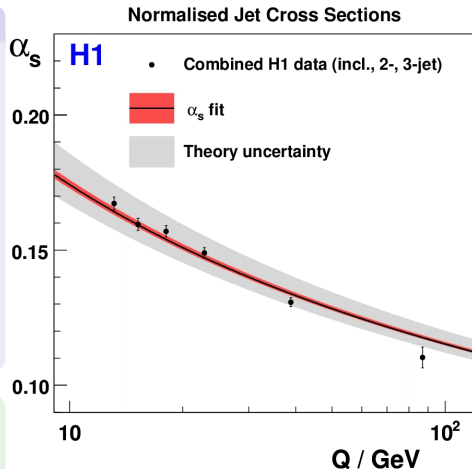
## Extraction of $\alpha_s$

- QCD predictions were fitted using a  $\chi^2$  **method**
  - parameters representing systematic shifts of detector observables are left free in the fit (**Hessian method**)
- values of  $\alpha_s$  were extracted by fitting the individual normalized inclusive, 2-jet, 3-jet cross sections and their combination

### Combined value:

$$\alpha_s(M_Z) = 0.1168 \quad \begin{array}{l} \pm 0.0007 \text{ (exp.)} \\ +0.0046 \text{ (th.)} \\ -0.0030 \text{ (th.)} \\ \pm 0.0016 \text{ (PDF)} \end{array}$$

Fit quality:  $\chi^2/\text{ndf} = 65/53$

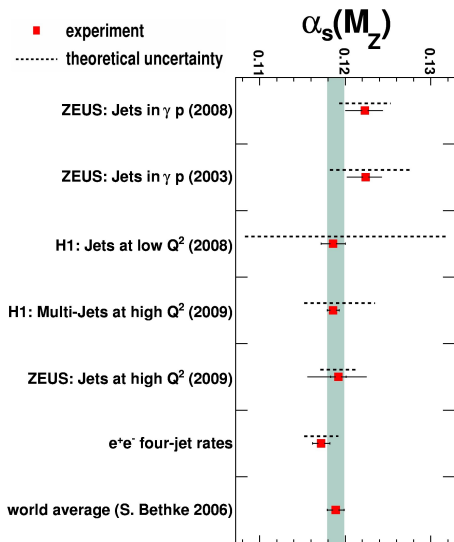


**Observed running agrees with QCD expectation!**



# Summary of $\alpha_s$ Extractions

- **extracted  $\alpha_s$  values are consistent with the world average!**
  - precision is comparable to the values obtained from  $e^+e^-$  interactions
  - HERA competitive!
  - different measurements and environments and processes are consistent
- **great success of QCD!!**



# Summary

## Measurements of jet production at HERA allow detailed tests of QCD dynamics.

- the strong coupling  $\alpha_s$  was extracted using ...
  - inclusive jets in photoproduction
  - inclusive jets at low  $Q^2$
  - inclusive and multi-jets cross sections at high  $Q^2$ .

## Conclusion:

- pQCD calculations describe the data over a wide range of phase space
- theoretical errors are often much larger than experimental uncertainties
- $\alpha_s$  extractions at HERA are competitive!