

# Vector meson production at HERA

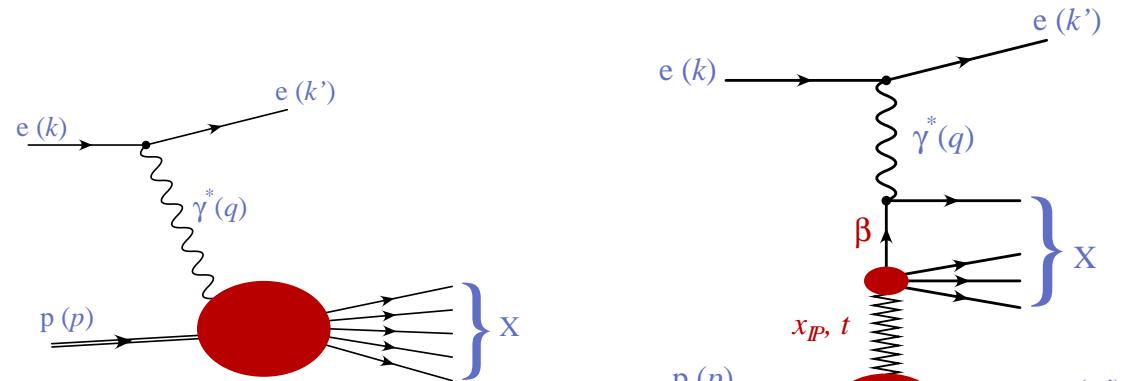
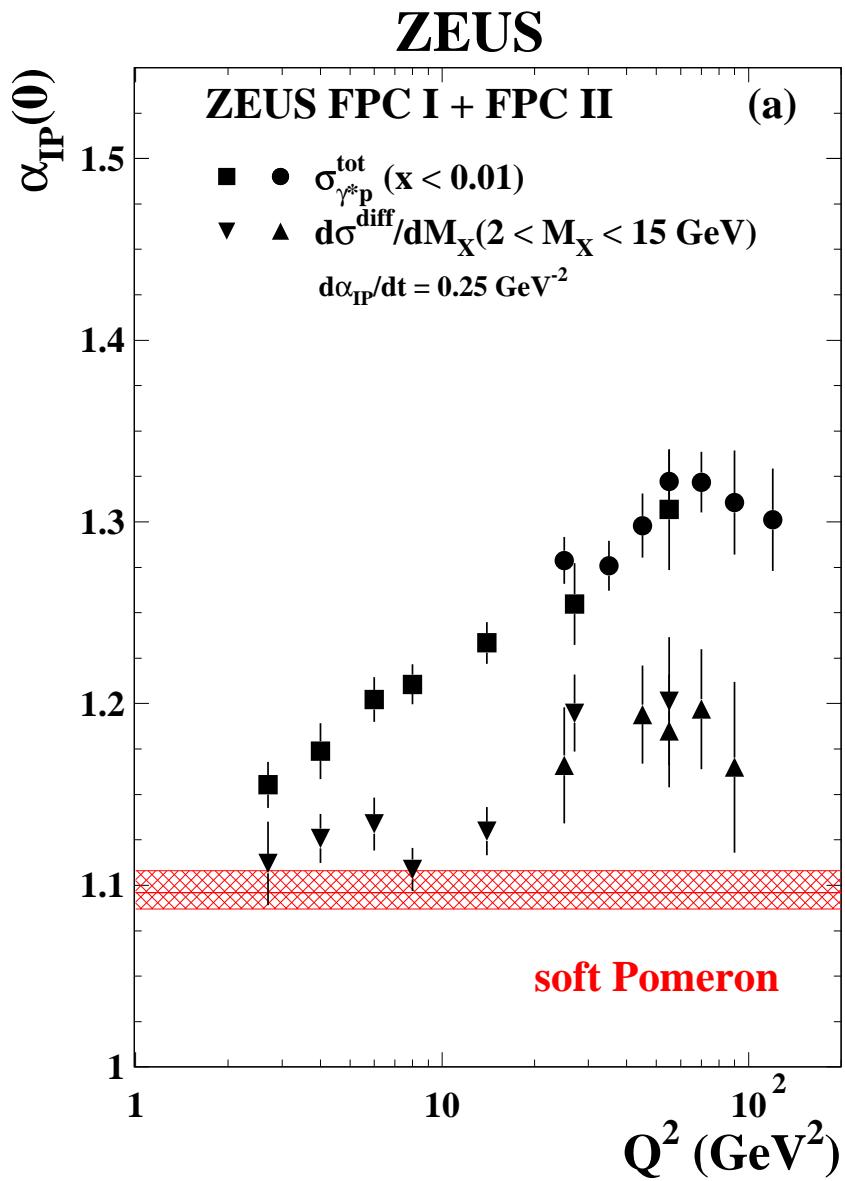
*L. Favart*

I.I.H.E.

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On behalf of H1 and ZEUS

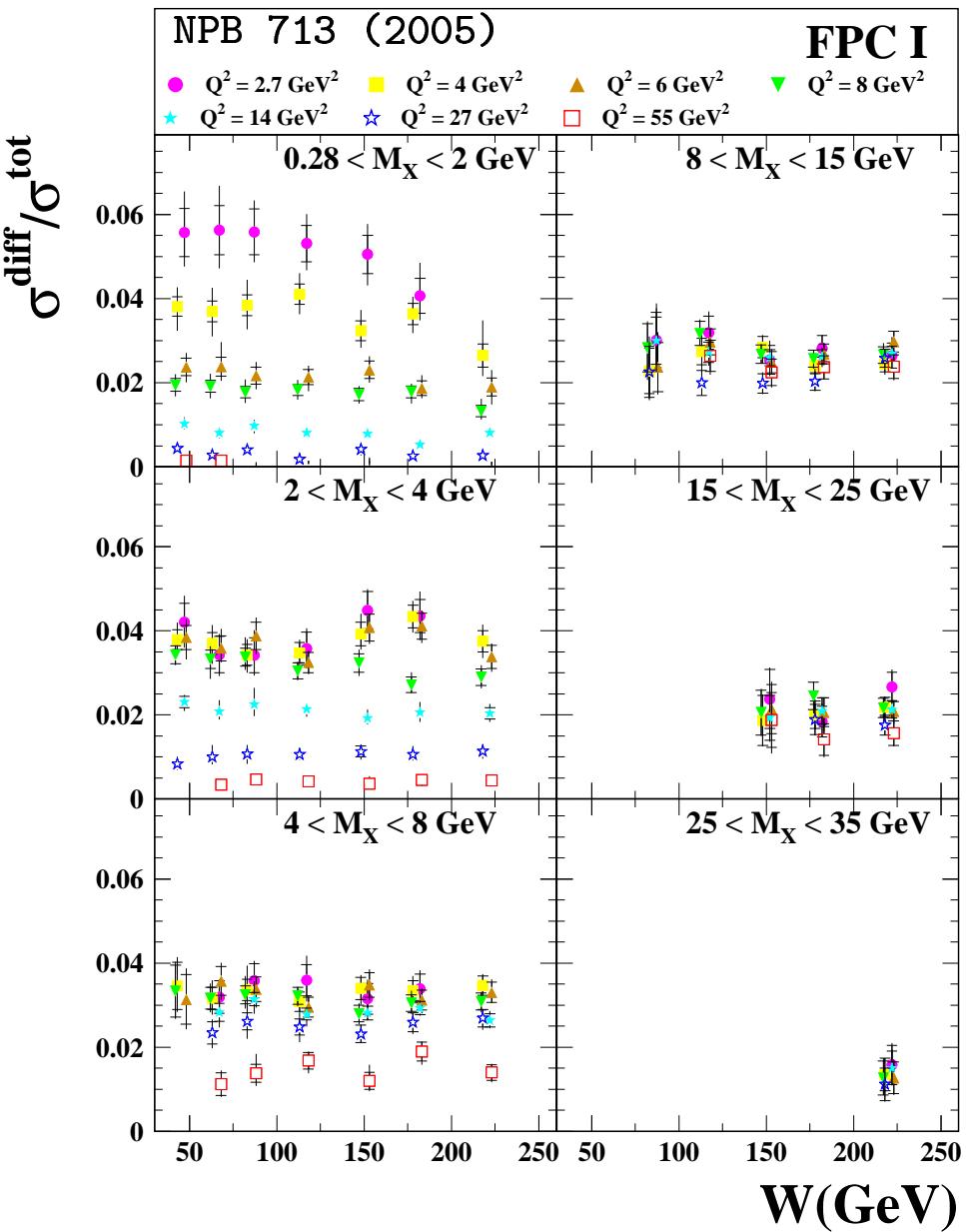
# From inclusive to exclusive diffraction



- Diffraction keeps an important soft contribution up to high  $Q^2$
  - But  $J/\Psi$  or DVCS are well described by pQCD.
- ⇒ How to link inclusive and exclusive diffraction?

# Ratio of Diffractive to inclusive cross-sections

ZEUS

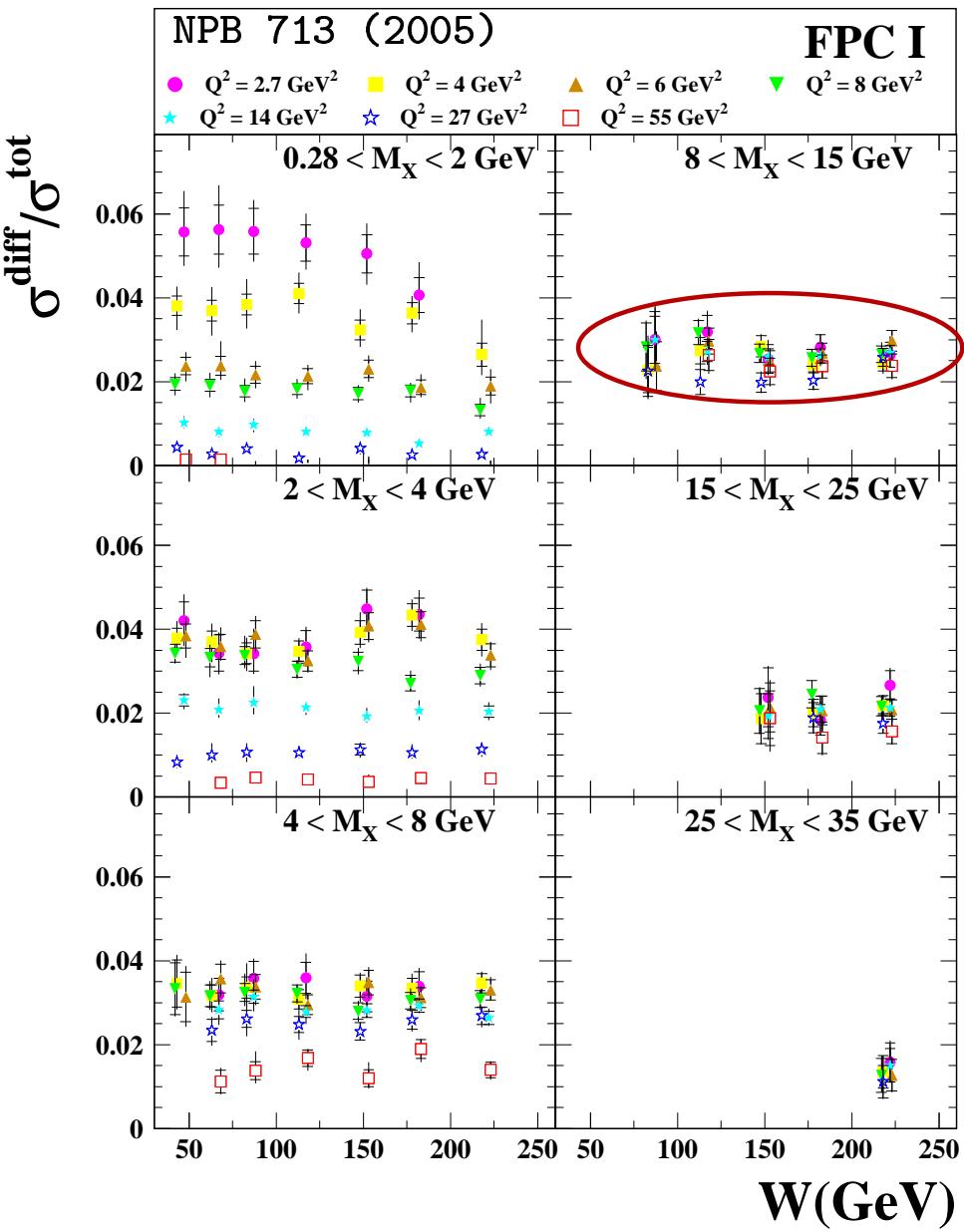


$$W^2 \simeq Q^2/x$$

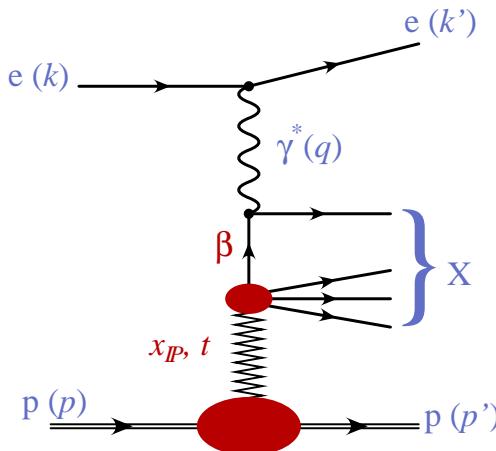
$$\beta \simeq Q^2/(Q^2 + M_X^2)$$

# Ratio of Diffractive to inclusive cross-sections

ZEUS

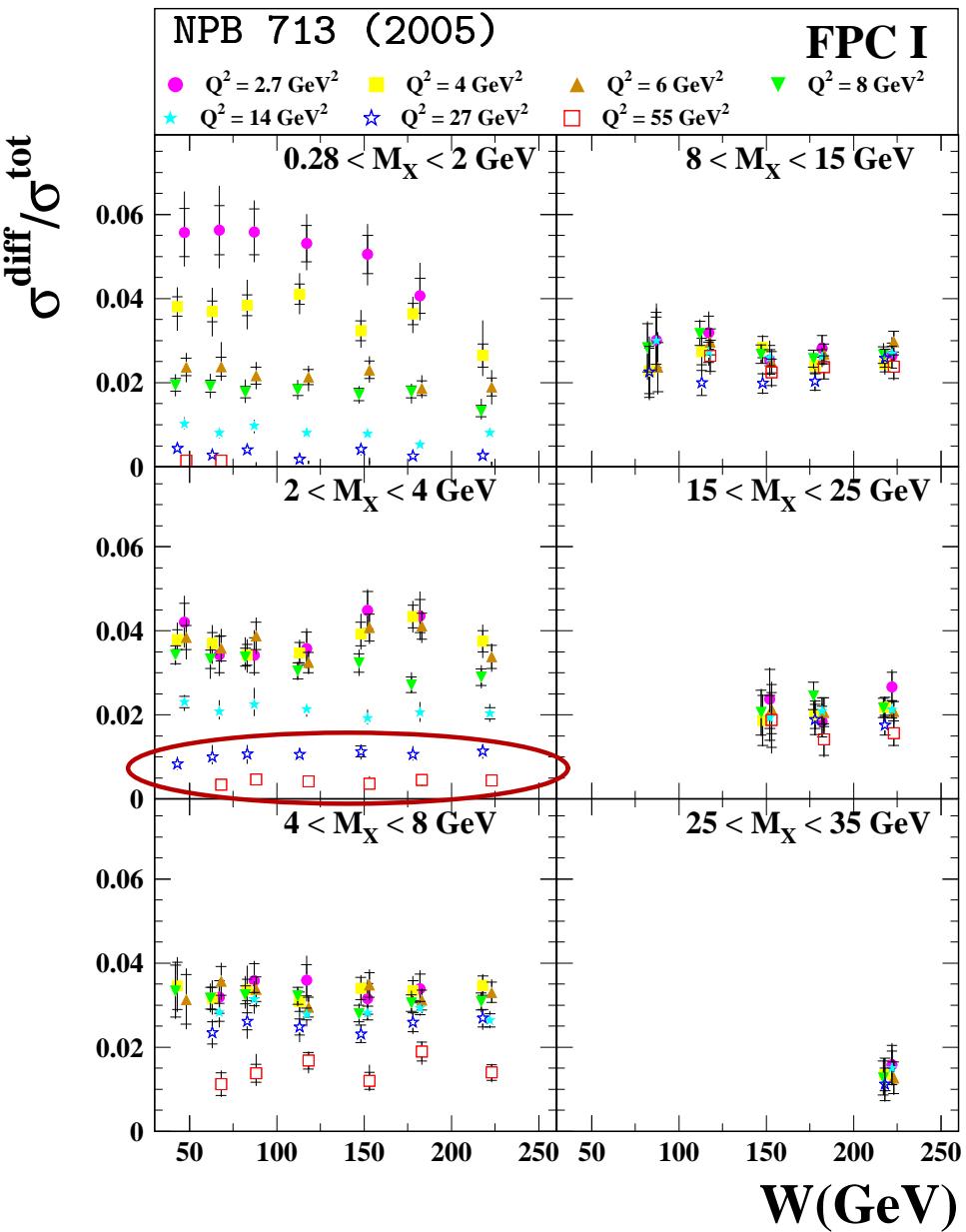


- $M_X > 8 \text{ GeV}:$ 
  - same  $W$  dependence as  $\sigma_{\text{tot}}$
  - no  $Q^2$  dependence
  - same DGLAP evolution
  - $\gamma^*$  sees: 1 parton that can radiate  
no distinction between DIS and DDIS!



# Ratio of Diffractive to inclusive cross-sections

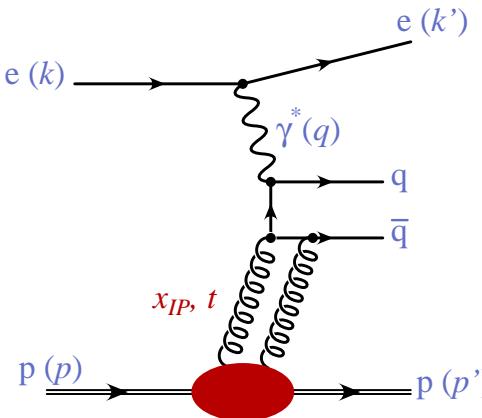
ZEUS



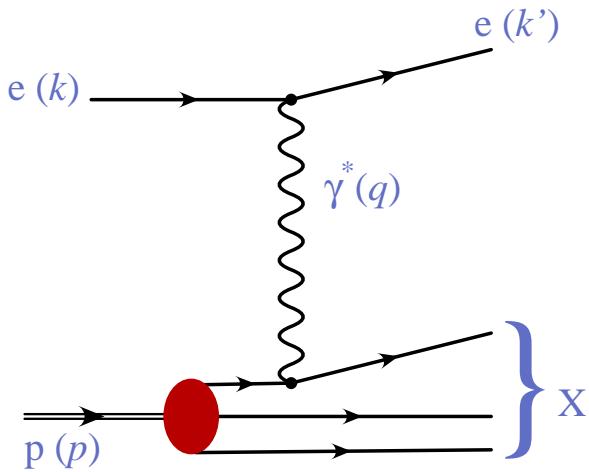
$$W^2 \simeq Q^2/x$$

$$\beta \simeq Q^2/(Q^2 + M_X^2)$$

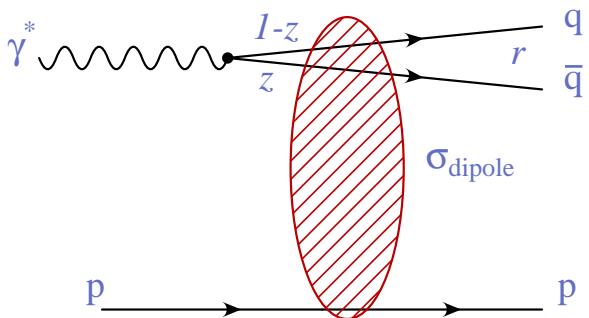
- If  $M_X \searrow, \beta \nearrow \rightarrow \gamma^*$ : more and more of the exchanged object (2 g)
  - large  $\beta$ :  $M_X \ll Q^2$ 
    - contribution of Vector Meson
    - no g radiation allowed
    - "closed" gluon object
- should increase with  $W$  but does not!



# What scale should we use ?



**DIS:** direct  $\gamma - q$  interaction  
 $\Rightarrow$  scale:  $\mu^2 = Q^2$



**DDIS:** hadron-hadron interaction  $\Rightarrow \gamma \rightarrow q\bar{q}$

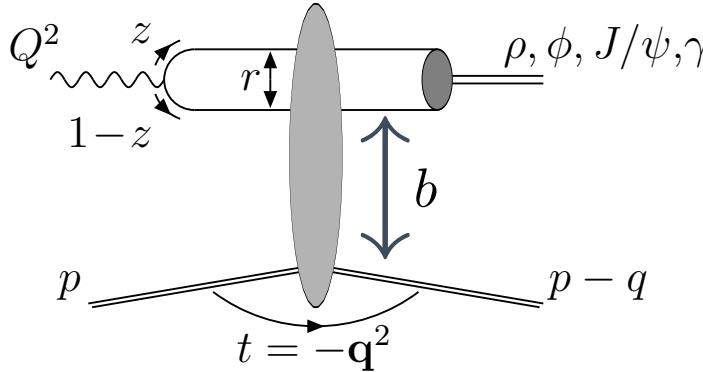
$$\mu^2 \simeq \frac{Q^2 + M_X^2}{4}$$

$\Rightarrow$  We should not compare directly DIS en DDIS at using the same scale

when  $M_X^2$  of DDIS is large,  $\mu^2$  gets closer to the scale used for DIS in previous plot  
 $\Rightarrow$  better agreement.

# Vector meson production: QCD factorisation

at large energy, for  $\mathcal{A}_L$  (large  $Q^2$ ) or heavy quarks:



1.  $\gamma$  fluctuates in  $q\bar{q}$  dipole: QED  $\gamma$  wave function  $\Psi_\gamma$
  2. dipole-proton interaction: universal  $\sigma_{dip}(r, z, b)$
  3.  $q\bar{q}$  recombination into VM
- The scanning radius  $r$  is expected to decrease with increasing  $Q^2$  or  $M_V$
- $\Rightarrow$  universal scale:  $\mu^2 = z(1-z)(Q^2 + M_V^2)$
- for  $\mathcal{A}_L$  (large  $Q^2$ ) or heavy quarks:  $z \simeq 1/2 \Rightarrow \mu^2 \simeq (Q^2 + M_V^2)/4$
- for light quarks,  $\mathcal{A}_T$ : contrib. from end points  $z = 0, 1 \Rightarrow \mu^2$  can be small even for large  $Q^2 \Rightarrow$  soft contributions

# $W$ , $t$ and $M_Y$ dependences

## $W$ dependence

- $\sigma \sim W^\delta \sim |x g(x, \mu^2)| \Rightarrow$  hard  $W$  dependence: signature of a hard scale  
 $\Rightarrow \delta = 4(\alpha(t) - 1) = 4(\alpha(0) + \alpha't - 1)$  larger than soft

$\Rightarrow$  Hard scale:  $\delta, \alpha(0)$  : universal with  $\frac{Q^2 + M_X^2}{4}$

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## $t$ dependence

- $d\sigma/dt \sim e^{-b|t|}$

$$b = b_{dip} \oplus b_{exch} \oplus b_Y$$

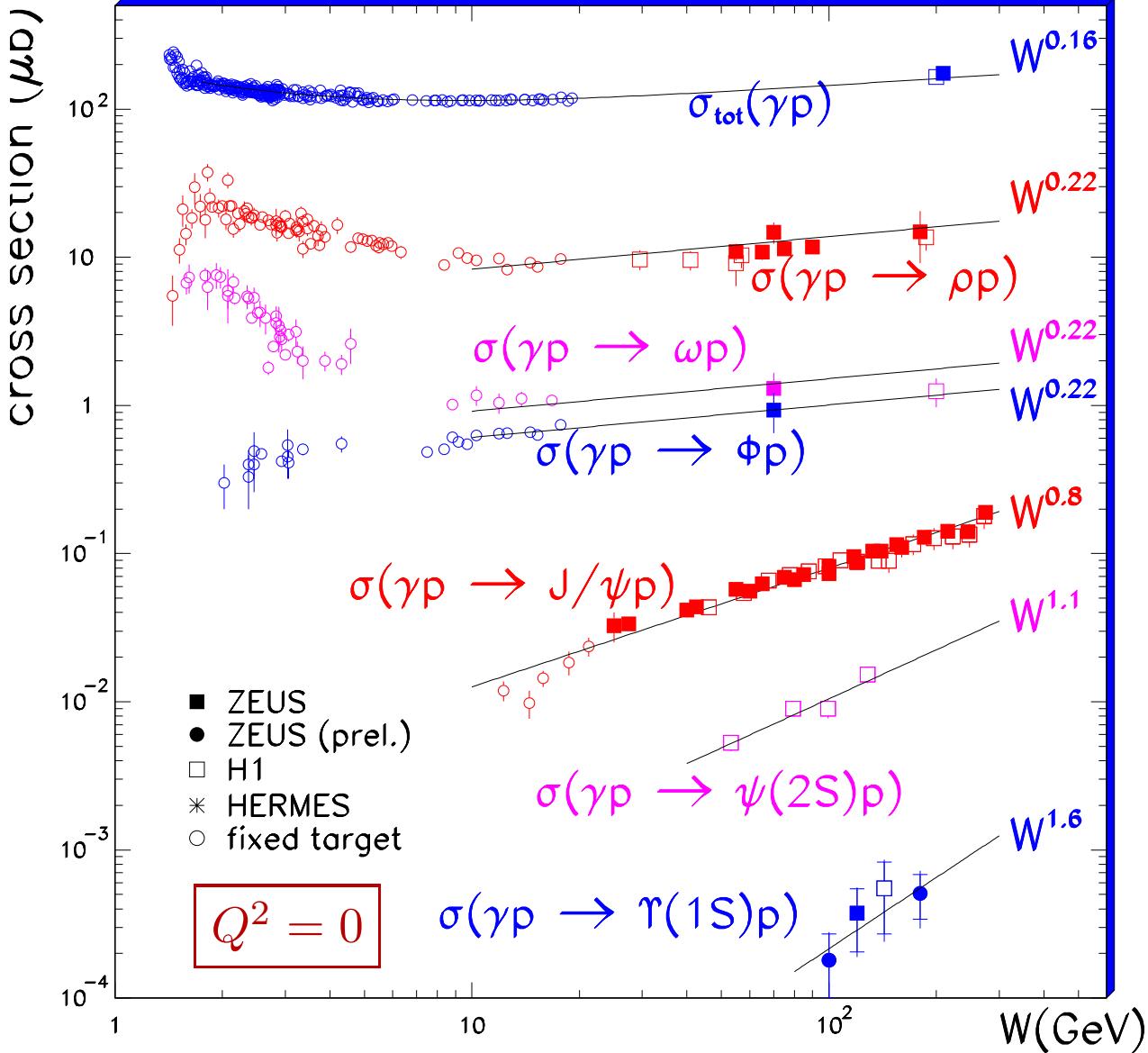
$\Rightarrow$  Hard scale:  $b$ : universal with  $\frac{Q^2 + M_X^2}{4}$

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## $M_Y$ dependence

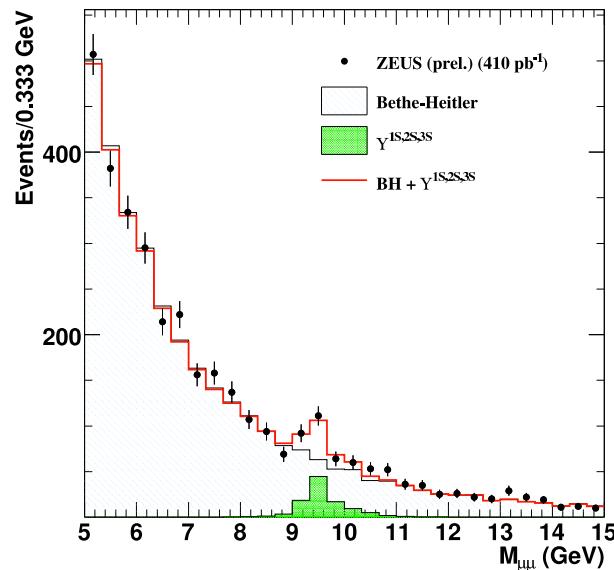
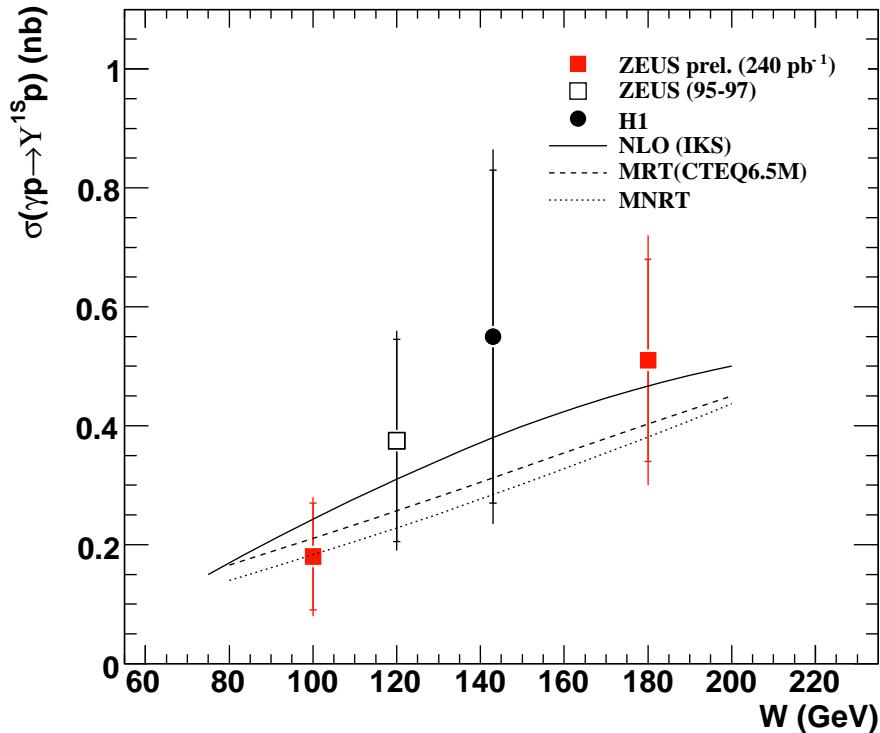
- elastic- proton dissociation universality for  $Q^2$ ,  $W$  and helicity amplitudes.

# Soft to hard transition: mass



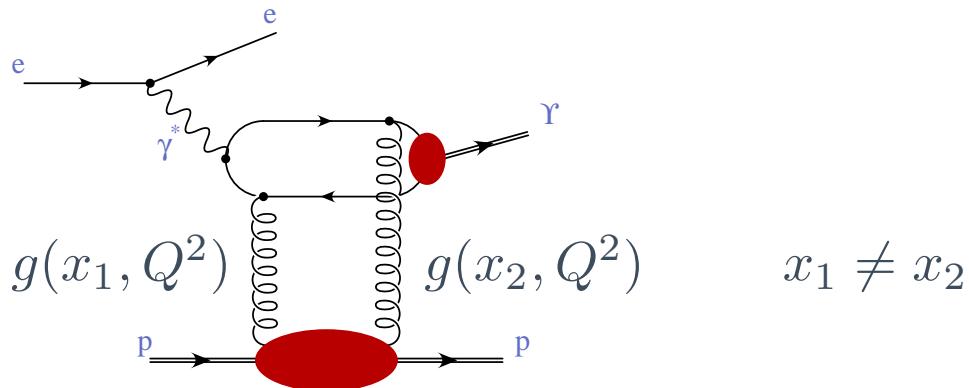
- Low mass ( $\rho, \phi, \omega; M_V^2 \simeq 1 \text{ GeV}^2$ ): no pert. scale  
→ weak energy dep. (soft regime)
- High mass ( $J/\psi, \psi$ ): pert. scale → strong energy dep. (hard regime)
- Large mass ( $\Upsilon$ ) important skewing effect

# Upsilon

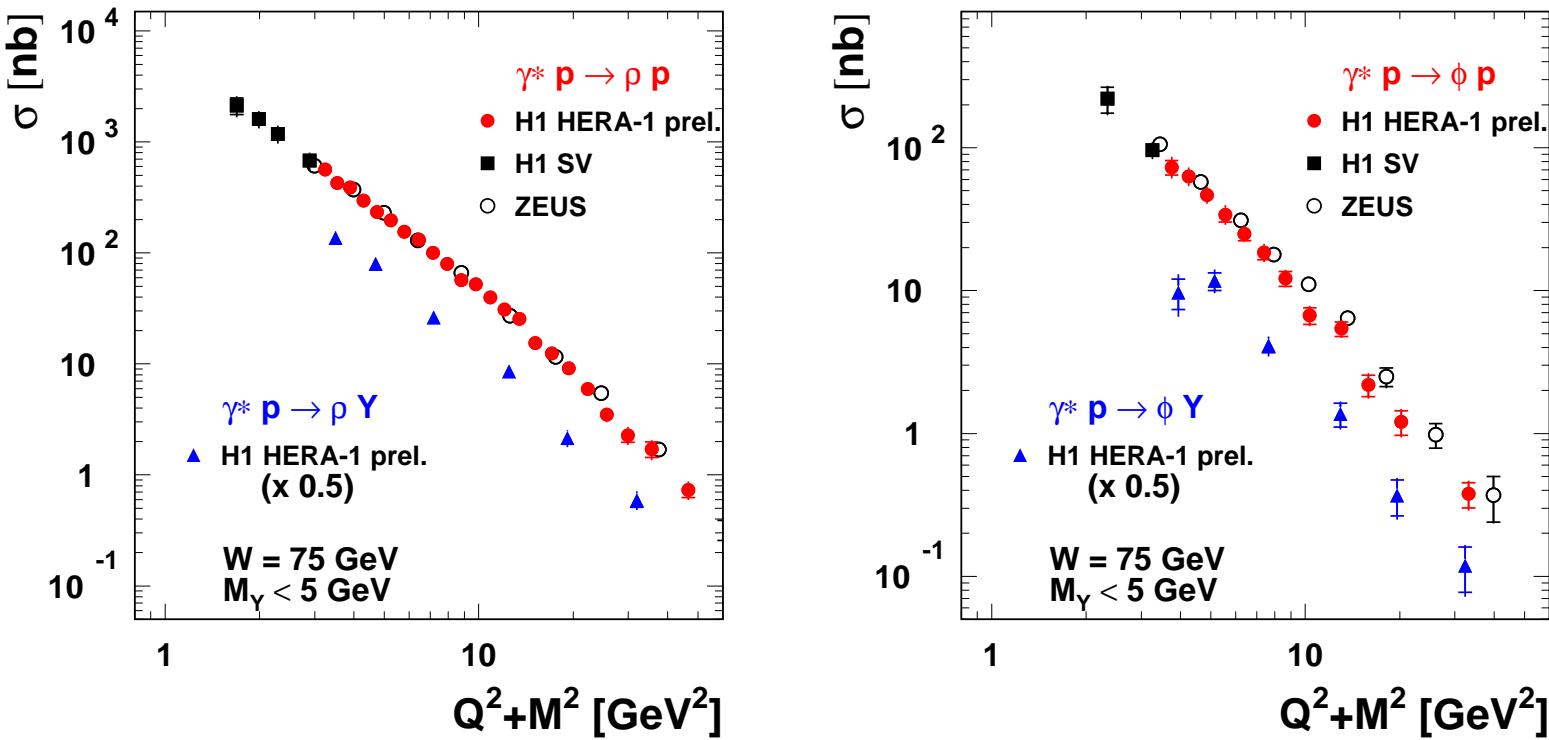


ZEUS (HERA I+II):  $104 \pm 21$  events candidates

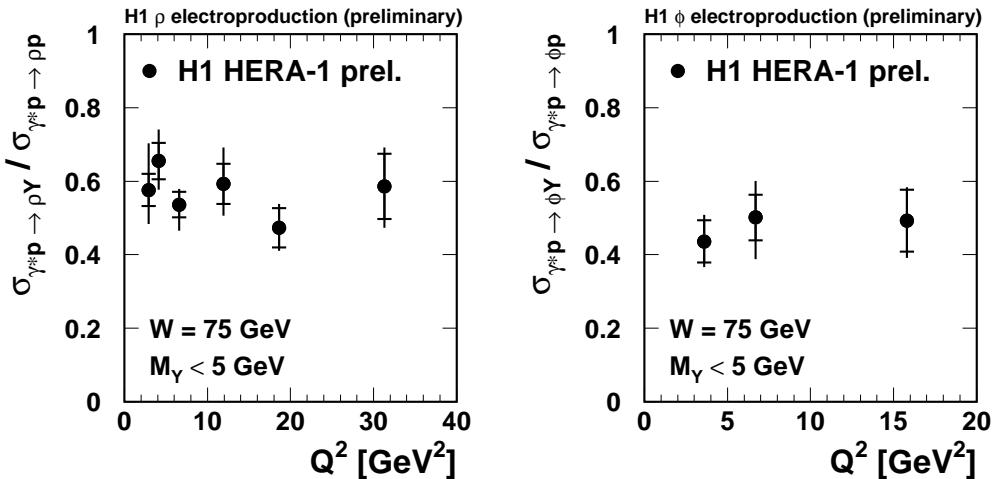
In agreement with NLO predictions including skewing and real part of the amplitude



# Light VM Cross-sections versus $Q^2$

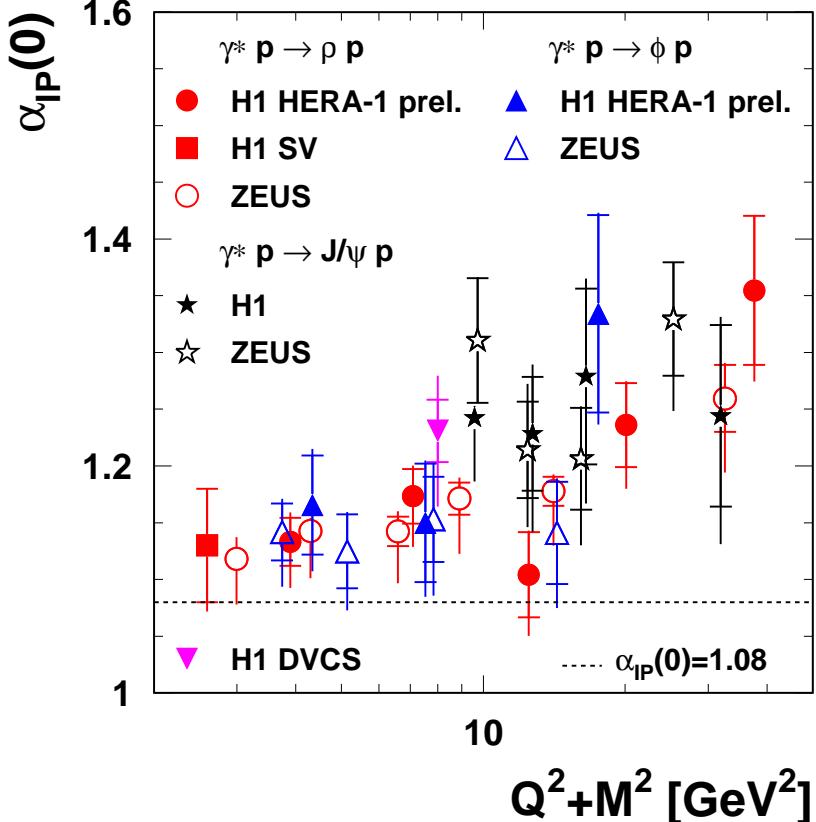
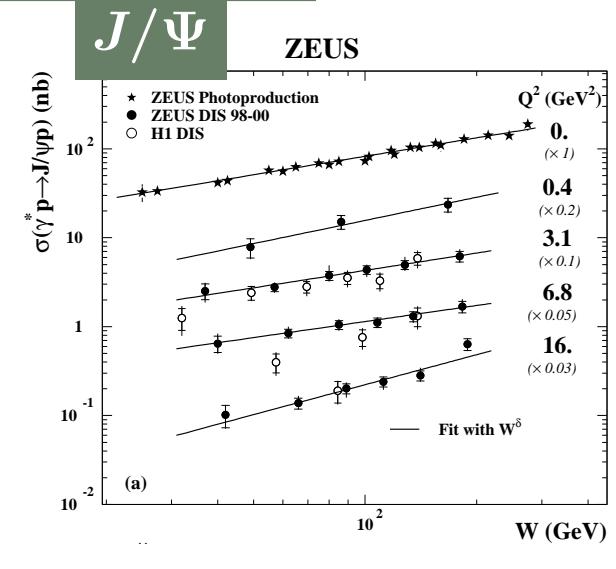
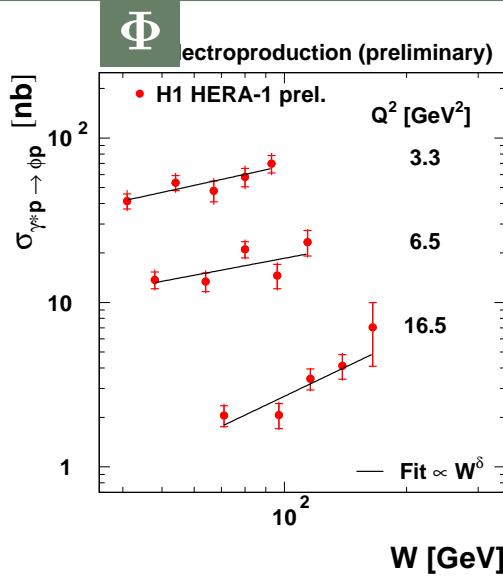
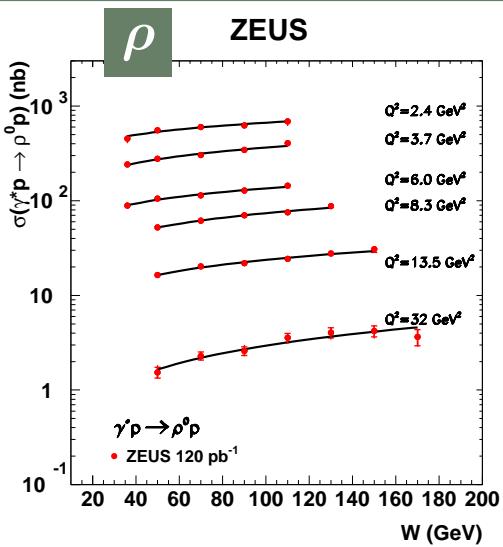


- High precision for elastic cross-sections; First  $\phi$  p-diss. cross-section



- p.diss/el: no  $Q^2$  dep.  
*i.e.* vertex factorisation

# $W$ dependences



$$\alpha_{IP}(0) = 1 + \delta/4 + \alpha'_{IP}/\langle |t| \rangle$$

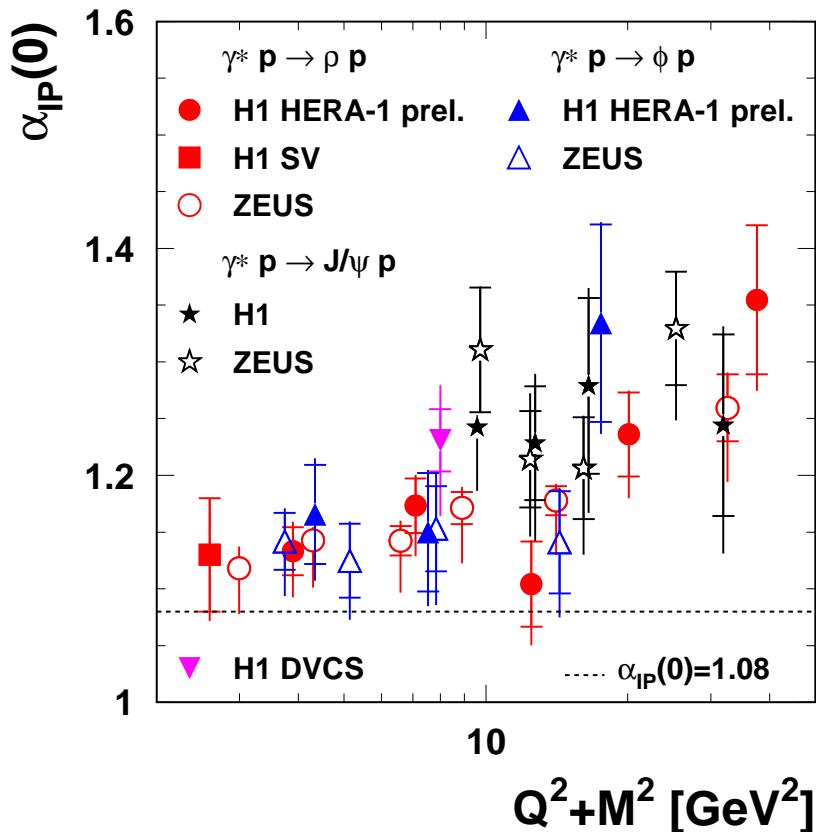
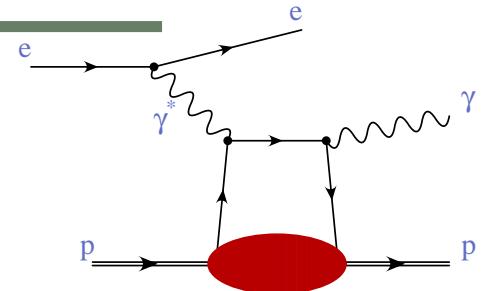
$$\alpha'_{IP} = 0 - 0.25 \text{ GeV}^{-2}$$

- Common hardening of  $\alpha_{IP}(0)$  with  $Q^2 + M^2$  for all VM and DVCS

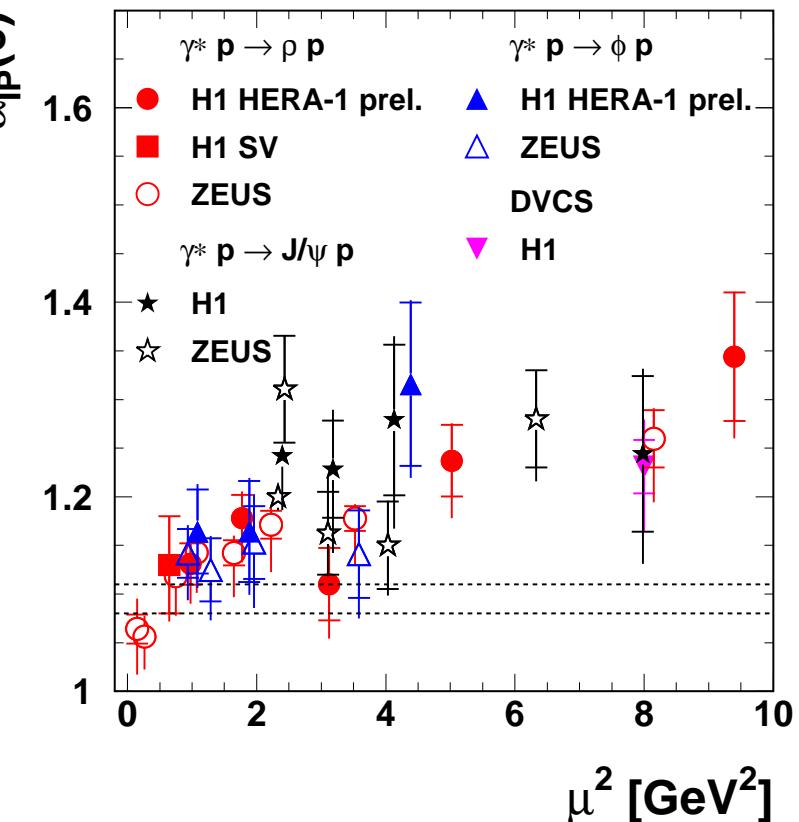
⇒ Transition from soft to hard regime with  $Q^2 + M^2$

# Note on the scale

DVCS is like DIS, the photon (at LO) interacts directly with a resolved quark.

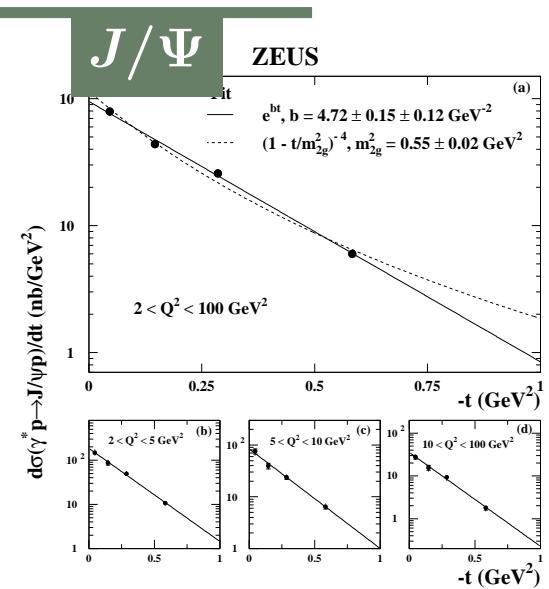
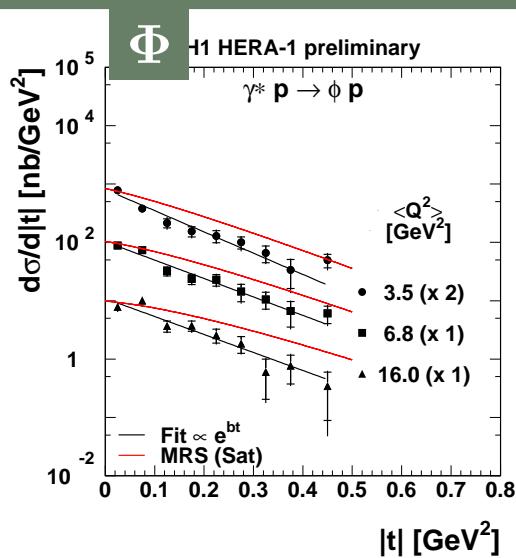
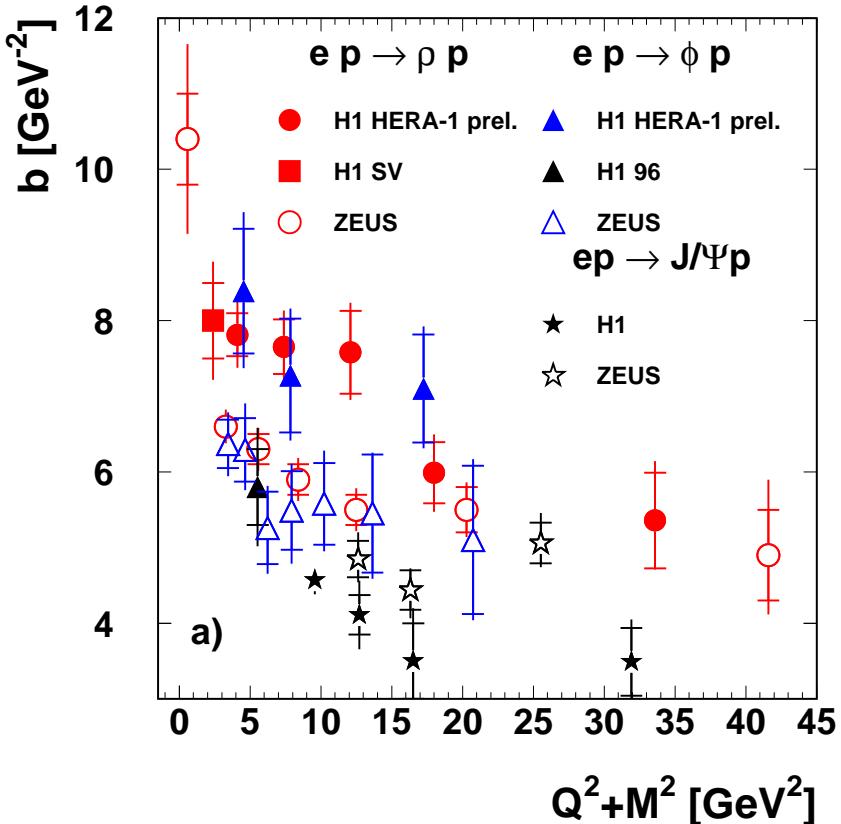


for all:  $\mu^2 = Q^2 + M_X^2$



for VM:  $\mu^2 = \frac{Q^2 + M_X^2}{4}$   
 for DVCS :  $\mu^2 = Q^2$

# $t$ dependences

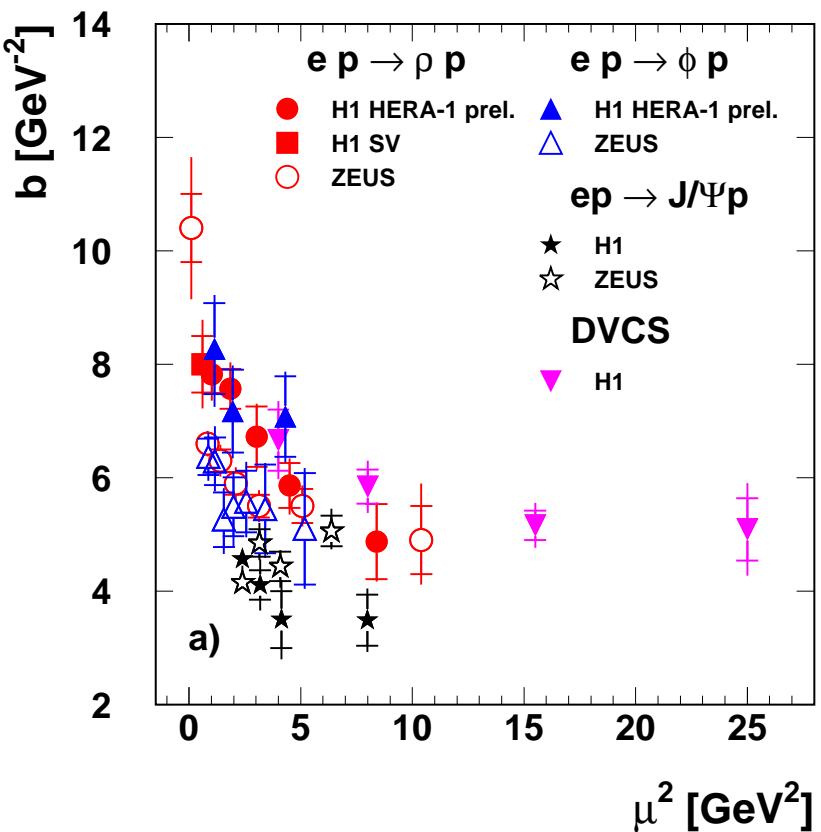
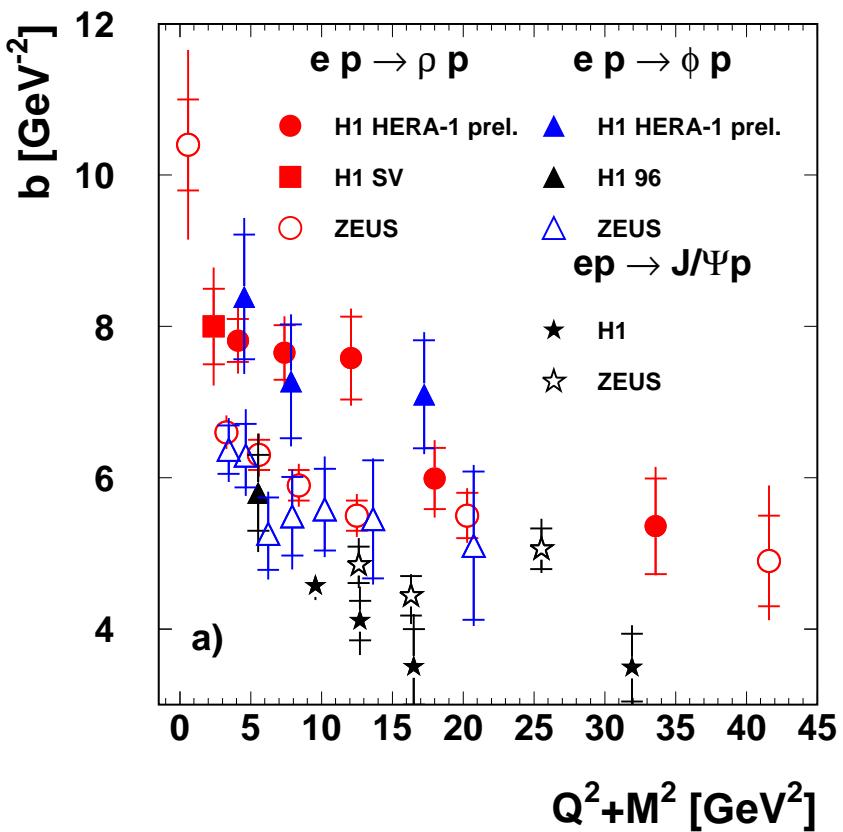


fit of  $e^{-b|t|}$

- $t$  slope hardening with  $Q^2 + M^2$  for all VM and DVCS

⇒ Transition from soft to hard regime with  $Q^2 + M^2$

# Note on the scale



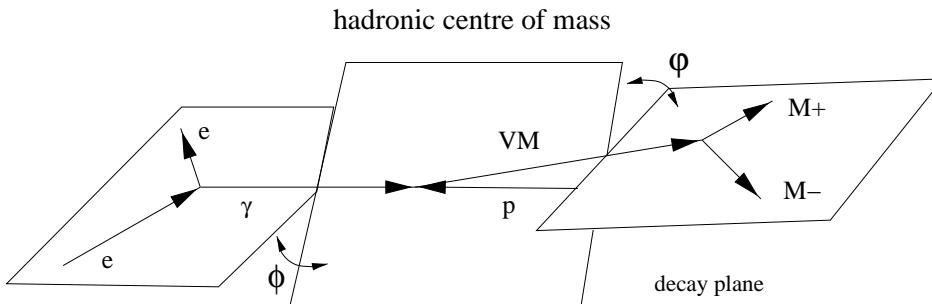
for all:  $\mu^2 = Q^2 + M_X^2$

for VM:  $\mu^2 = \frac{Q^2 + M_X^2}{4}$   
 for DVCS :  $\mu^2 = Q^2$

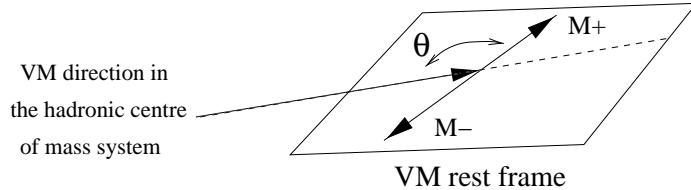
# SPIN DENSITY MATRIX ELEMENTS

$$\theta^*, \Phi, \varphi \iff 15 \text{ SDMEs} : r_{kl}^{ij} \propto T_{\lambda'_\rho \lambda'_\gamma} T_{\lambda_\rho \lambda_\gamma}$$

$T_{\lambda_\rho \lambda_\gamma}$  : helicity amplitudes



electron scattering plane      production plane



VM direction in  
the hadronic centre  
of mass system

No helicity flip:  $T_{00} : \gamma_L \rightarrow \rho_L$

$T_{11} : \gamma_T \rightarrow \rho_T$

Single flip:  $T_{01} : \gamma_T \rightarrow \rho_L$

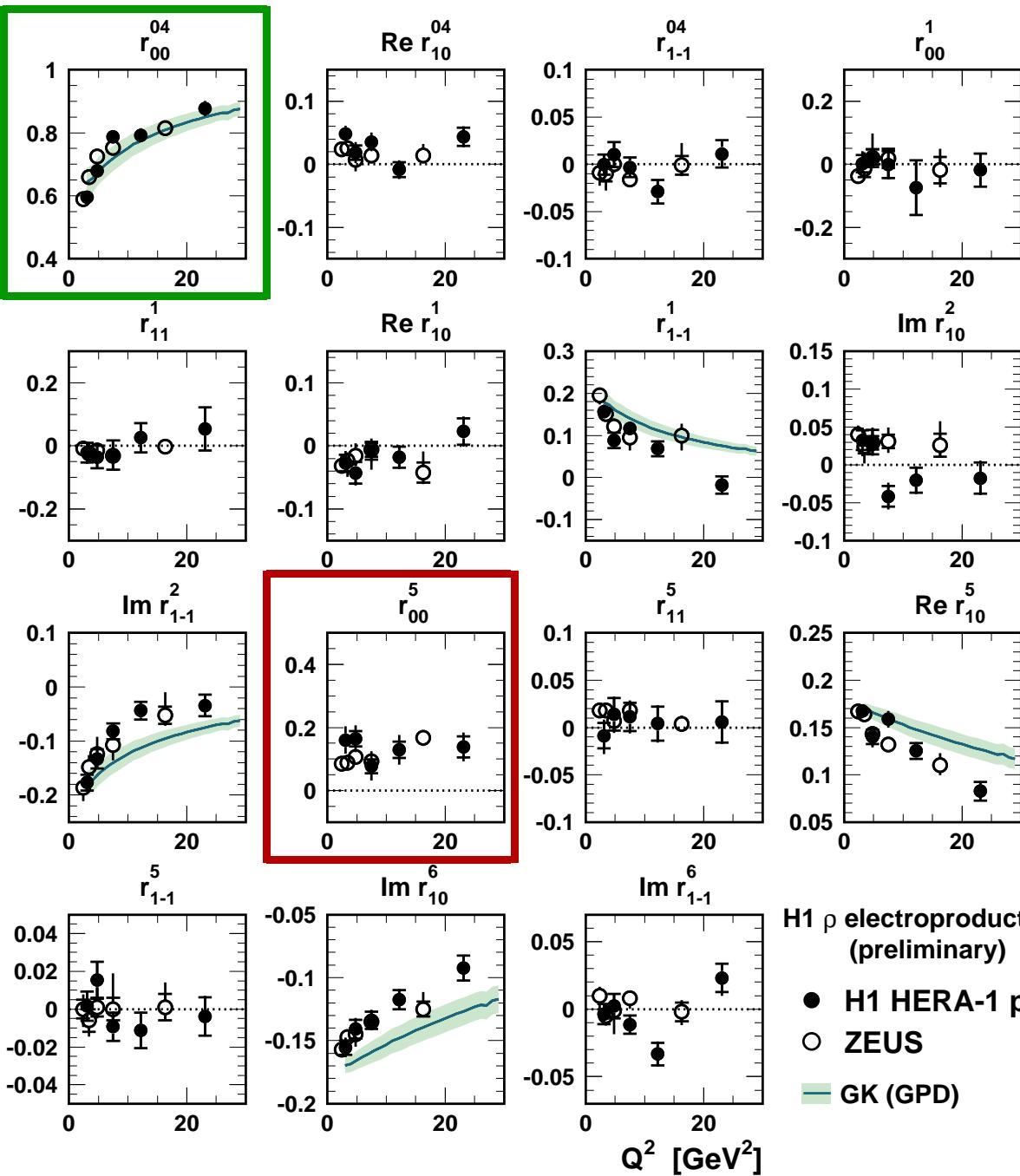
$T_{10} : \gamma_L \rightarrow \rho_T$

Double flip:  $T_{1-1} : \gamma_T \rightarrow \rho_T$

*s*-Channel Helicity Conservation (SCHC):  $T_{01} = T_{10} = T_{1-1} = 0$

- SCHC violation ( single flip  $\propto \sqrt{|t|}$ , double  $\propto |t|$  )
- pQCD Hierarchy ( $|t| < Q^2$ ):  $|T_{00}| > |T_{11}| > |T_{01}| > |T_{10}| > |T_{1-1}|$

# $\rho$ Polarisation - SDMEs vs. $Q^2$



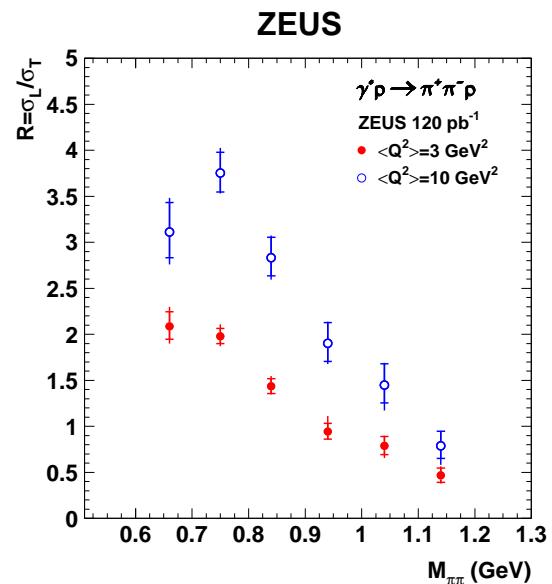
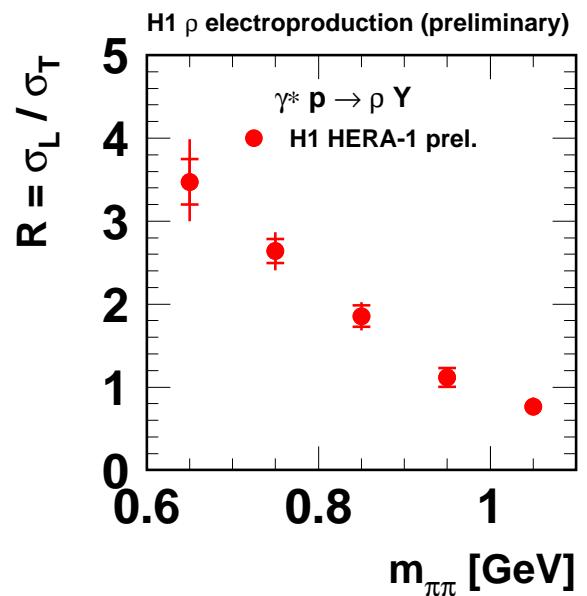
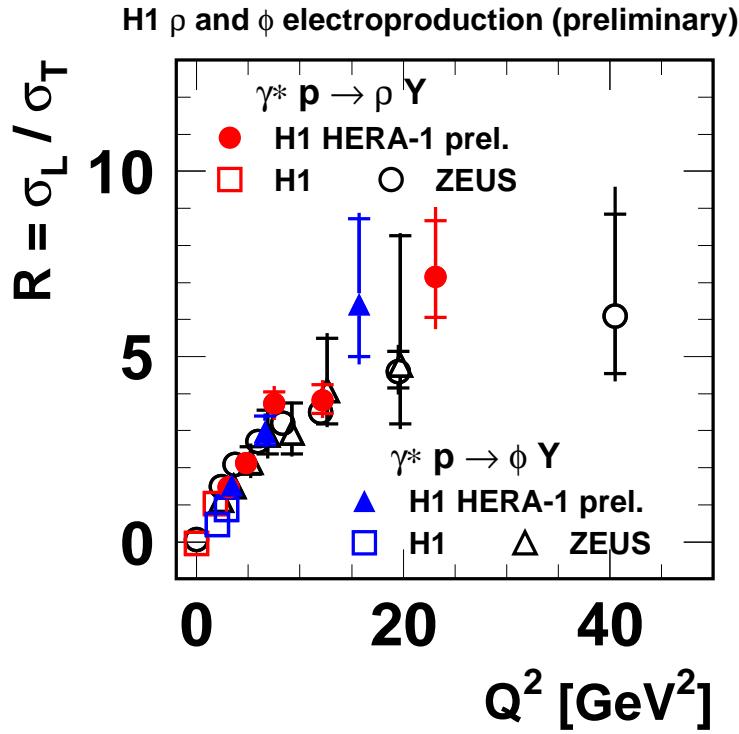
- $r_{00}^{04}$  increases with  $Q^2$
- ↔ similar effects for  $r_{1-1}^1$ ,  $\text{Im } r_{1-1}^2$ ,  $\text{Re } r_{10}^5$  and  $\text{Im } r_{10}^6$  (in SCHC)
- ↔ Fair description by Goloskokov-Kroll (GPD) model
- $r_{00}^5$  violates SCHC (flip)
- Other SDME  $\simeq 0$

H1  $\rho$  electroproduction (preliminary)

- H1 HERA-1 prel.
- ZEUS
- GK (GPD)

# Polarisation - $R = \sigma_L / \sigma_T$

$$R_{SCHC} = \frac{1}{\epsilon} \frac{r_{00}^{04}}{1 - \epsilon r_{00}^{04}} = \frac{|T_{00}|^2}{|T_{11}|^2}$$



- Naive  $R \propto Q^2/M^2$  - modified at high  $Q^2$
- Similar  $R$  for  $\phi$  and  $\rho$
- Strong invariant mass dependence in  $\rho$  case

# Polarisation - Amplitude ratios vs. $Q^2$

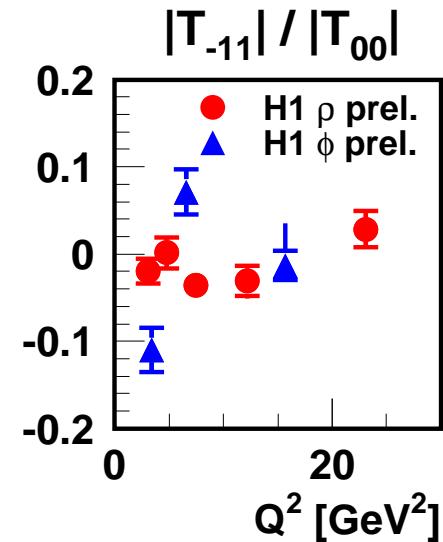
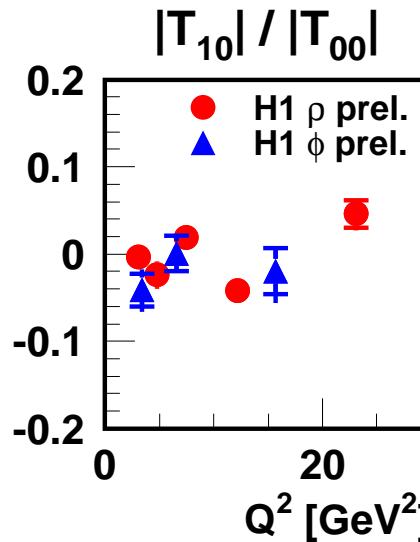
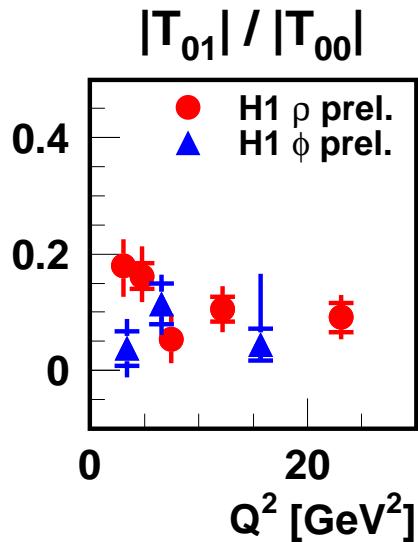
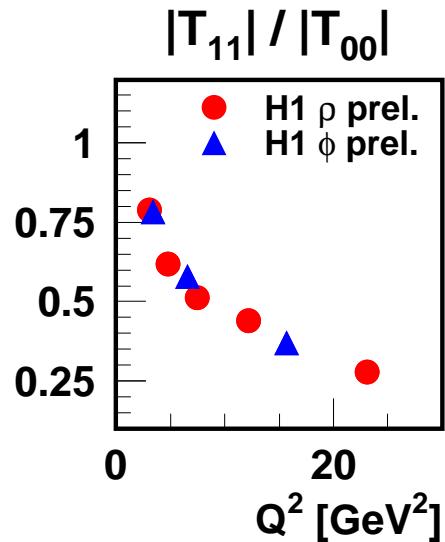
pQCD :

- $|T_{11}|/|T_{00}| \sim \frac{M}{Q} \frac{1+\gamma}{\gamma}$

- $|T_{01}|/|T_{00}| \sim \frac{\sqrt{|t|}}{Q} \frac{1}{\sqrt{2}\gamma}$

- $|T_{10}|/|T_{00}| \sim -\frac{M}{Q^2} \frac{\sqrt{|t|}}{\gamma} \frac{\sqrt{2}}{\gamma}$

$\gamma$  : gluon anomalous dim.



- $|T_{11}|/|T_{00}|$  decreases with  $Q^2 \leftrightarrow \sigma_L/\sigma_T$  increases with  $Q^2$
- $|T_{01}|/|T_{00}| > 0 \leftrightarrow$  SCHC violation
- $|T_{10}|/|T_{00}|$  and  $|T_{-11}|/|T_{00}|$  are small
- ⇒  $|T_{00}| > |T_{11}| > |T_{01}| > |T_{10}|, |T_{-11}| \leftrightarrow$  hierarchy observed

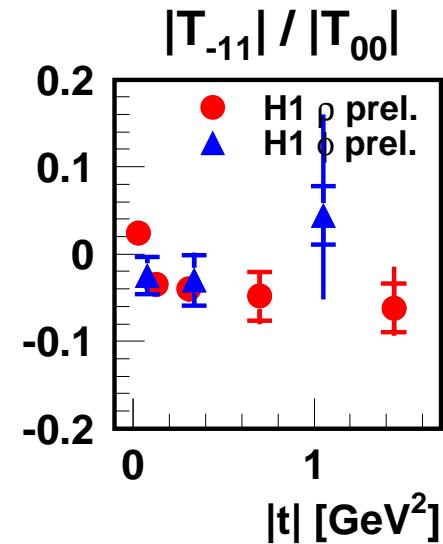
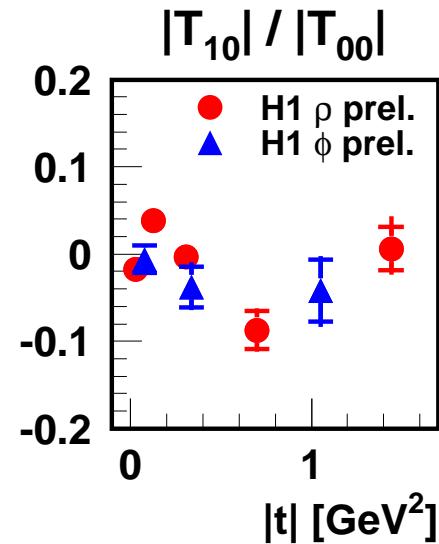
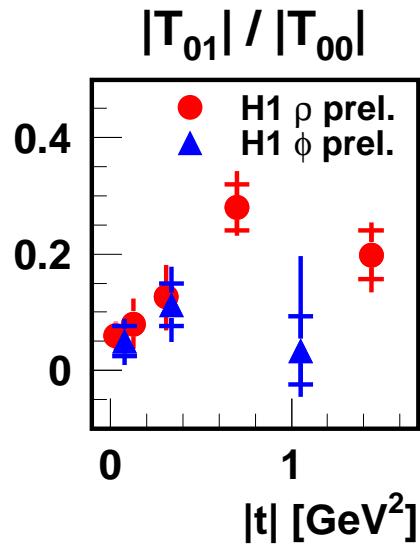
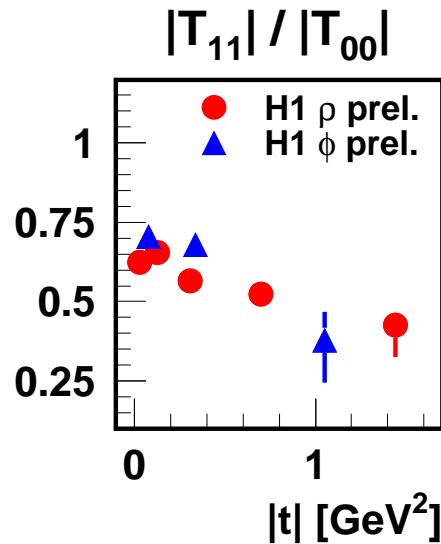
# Polarisation - Amplitude ratios vs. $|t|$

pQCD:

- $|T_{11}|/|T_{00}| \sim \frac{M}{Q} \frac{1+\gamma}{\gamma}$
- $|T_{01}|/|T_{00}| \sim \frac{\sqrt{|t|}}{Q} \frac{1}{\sqrt{2}\gamma}$

$$\bullet |T_{10}|/|T_{00}| \sim -\frac{M}{Q^2} \frac{\sqrt{|t|}}{\gamma} \frac{\sqrt{2}}{\gamma}$$

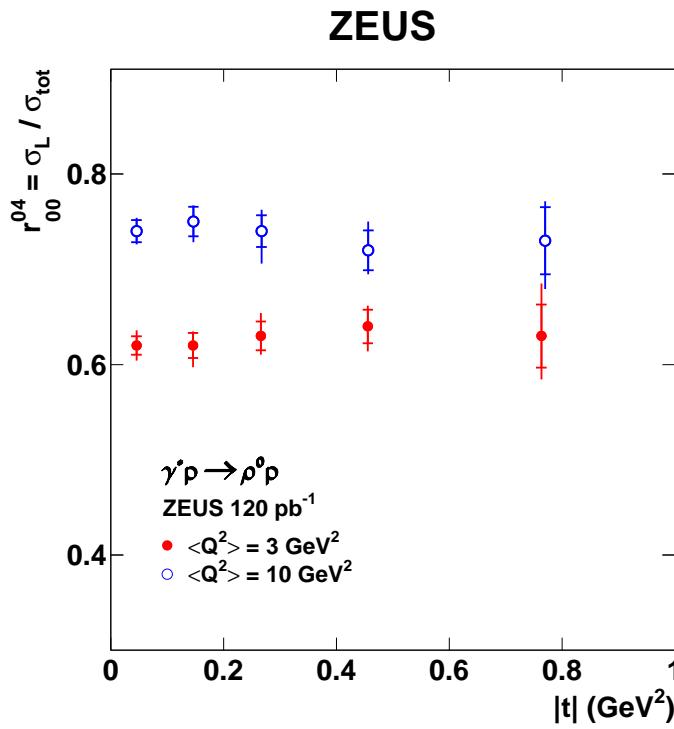
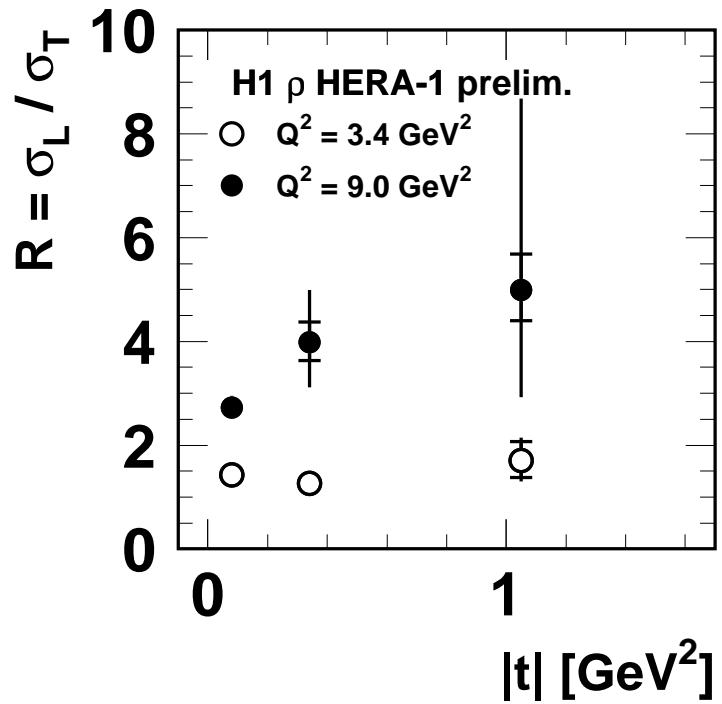
$\gamma$  : gluon anomalous dim.



- $|T_{11}|/|T_{00}|$  decreases with  $|t|$
- $|T_{01}|/|T_{00}|$  increases with  $|t| \leftrightarrow$  SCHC violation increases with  $|t|$
- $|T_{10}|/|T_{00}|$  and  $|T_{-11}|/|T_{00}|$  are small but some  $|t|$  dependence
- $|T_{11}|/|T_{00}|$  decrease partially compensated by  $|T_{01}|/|T_{00}|$  increase  
 $\Rightarrow \sigma_L/\sigma_T$  is the result of partial compensations

# Polarisation - $R = \sigma_L/\sigma_T$ versus $t$

$$R_{SCHC+T_{01}} = \frac{|T_{00}|^2}{|T_{11}+T_{01}|^2}$$



- H1:  $R$  depends on  $t$  for large  $Q^2 \Rightarrow b_L < b_T$  !!! ( $\sigma_L$  more pert. than  $\sigma_T$ )
- Not seen by ZEUS
- due to different  $\rho'$  background treatment

# Conclusions

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Important progresses in precision of VM measurements and understanding of underlaying dynamics.

- $\rho, \phi, J/\psi, \Upsilon, \gamma$
- in  $Q^2, W, t$ , helicity amplitudes, p-diss/el
- precision in the soft to hard transition: scales, and  $L/T$  separation
- many models: GPD, BFKL, dipole, saturation,...  
with semi-qualitative understanding  
but many quantitative desription still lacking

# Back-up Slides

# Polarisation - Retrieving Amplitude ratios

Assume purely imaginary amplitudes  $\rightarrow$  phase =  $\pm 1$  !

$\rightarrow$  Extract  $|T_{11}|/|T_{00}|$ ,  $|T_{01}|/|T_{00}|$ ,  $|T_{10}|/|T_{00}|$  and  $|T_{-11}|/|T_{00}|$  from fit to the 15 SDMEs:

$$r_{00}^{04} = B (\varepsilon + \beta^2)$$

$$\text{Re } r_{10}^{04} = B/2 (2\varepsilon\delta + \beta\alpha - \beta\eta)$$

$$r_{1-1}^{04} = B (\alpha\eta - \varepsilon\delta^2)$$

$$r_{00}^1 = -B \beta^2$$

$$r_{11}^1 = B \alpha\eta$$

$$\text{Re } r_{10}^1 = B/2 \beta(\eta - \alpha)$$

$$r_{1-1}^1 = B/2 (\alpha^2 + \eta^2)$$

$$\text{Im } r_{10}^2 = B/2 \beta(\alpha + \eta)$$

$$\text{Im } r_{1-1}^2 = B/2 (\eta^2 - \alpha^2)$$

$$r_{00}^5 = \sqrt{2}B \beta$$

$$r_{11}^5 = B/\sqrt{2} \delta(\alpha - \eta)$$

$$\text{Re } r_{10}^5 = B/(2\sqrt{2}) (2\beta\delta + \alpha - \eta)$$

$$r_{1-1}^5 = B/\sqrt{2} \delta(\eta - \alpha)$$

$$\text{Im } r_{10}^6 = -B/(2\sqrt{2}) (\alpha + \eta)$$

$$\text{Im } r_{1-1}^6 = B/\sqrt{2} \delta(\alpha + \eta)$$

$$\alpha = |T_{11}|/|T_{00}|$$

$$\beta = |T_{01}|/|T_{00}|$$

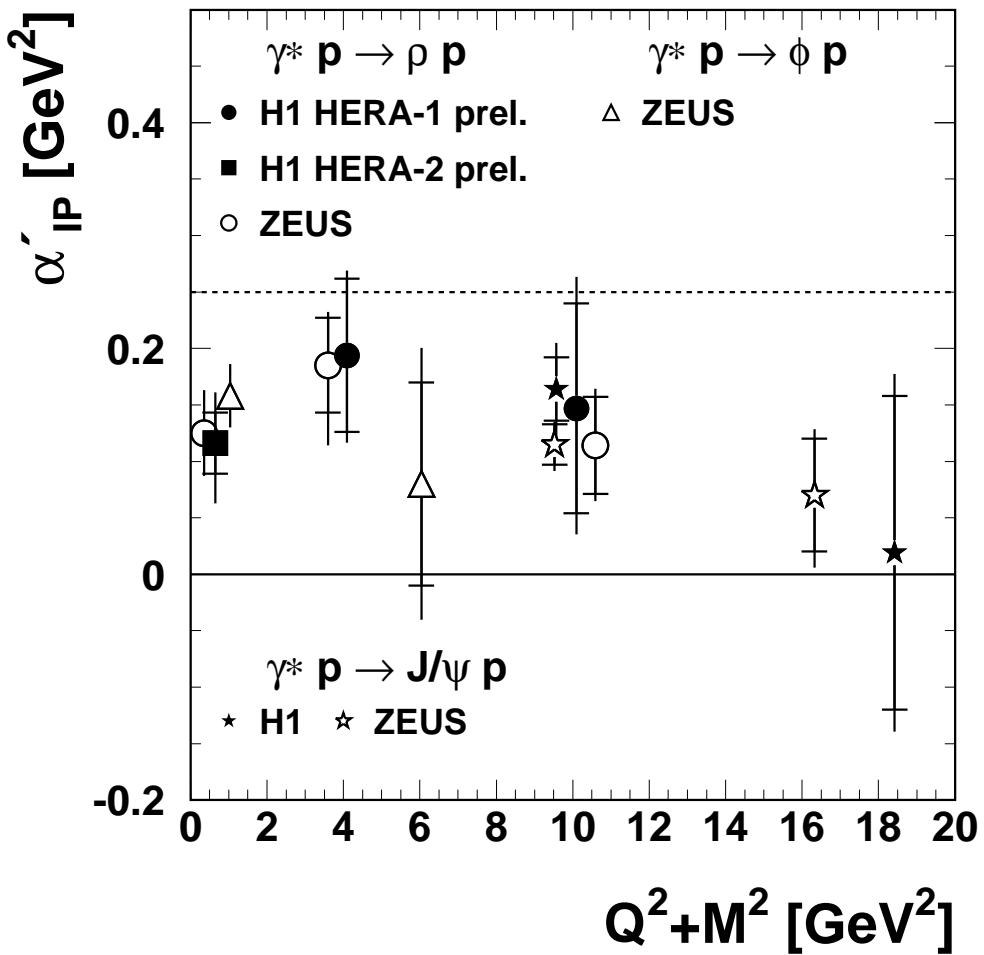
$$\delta = |T_{10}|/|T_{00}|$$

$$\eta = |T_{-11}|/|T_{00}|$$

$$B = \frac{1}{N_T + \varepsilon N_L} = \frac{R}{1 + \varepsilon R}$$

$$N_T = \alpha^2 + \beta^2 + \eta^2$$

$$N_L = 1 + 2\delta^2$$

$\alpha'$ 

# Rho mass

ZEUS

