



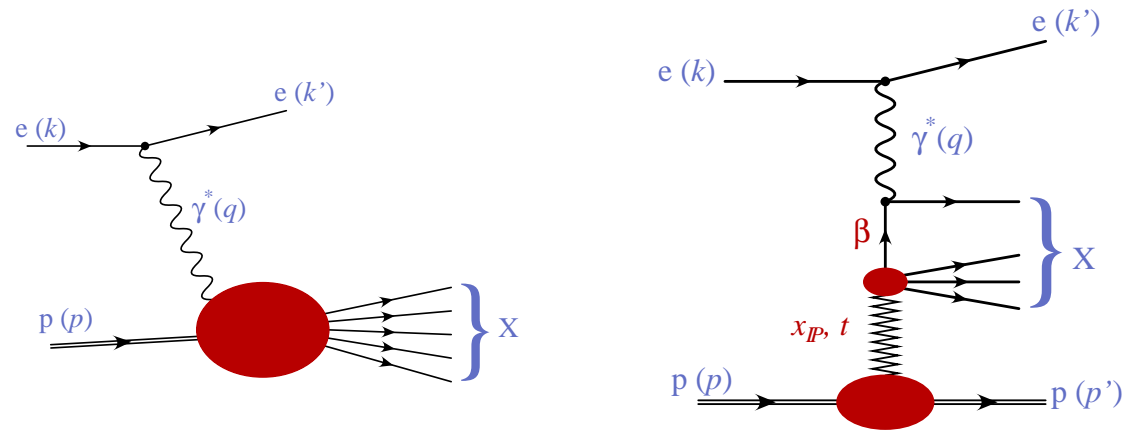
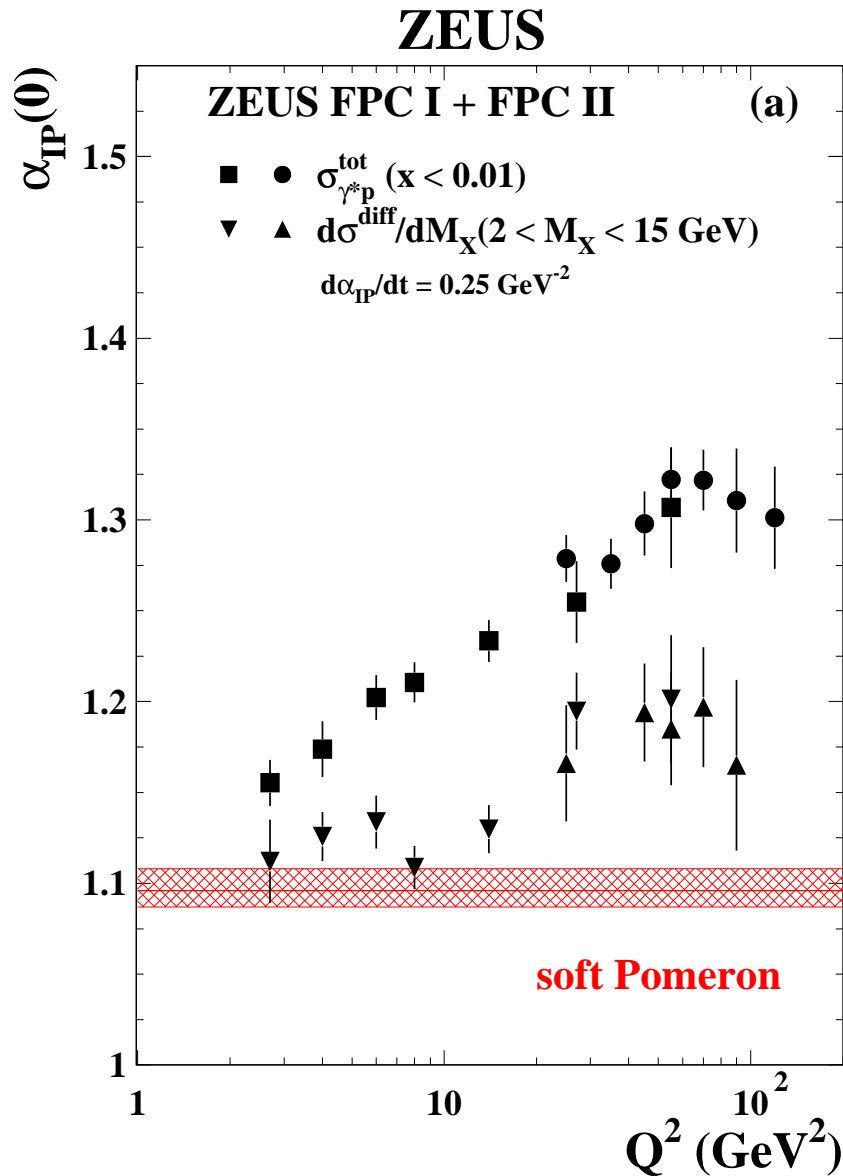
# Vector meson production at HERA

*L. Favart*

I.I.H.E.  
Université Libre de Bruxelles.

On behalf of H1 and ZEUS

# From inclusive to exclusive diffraction

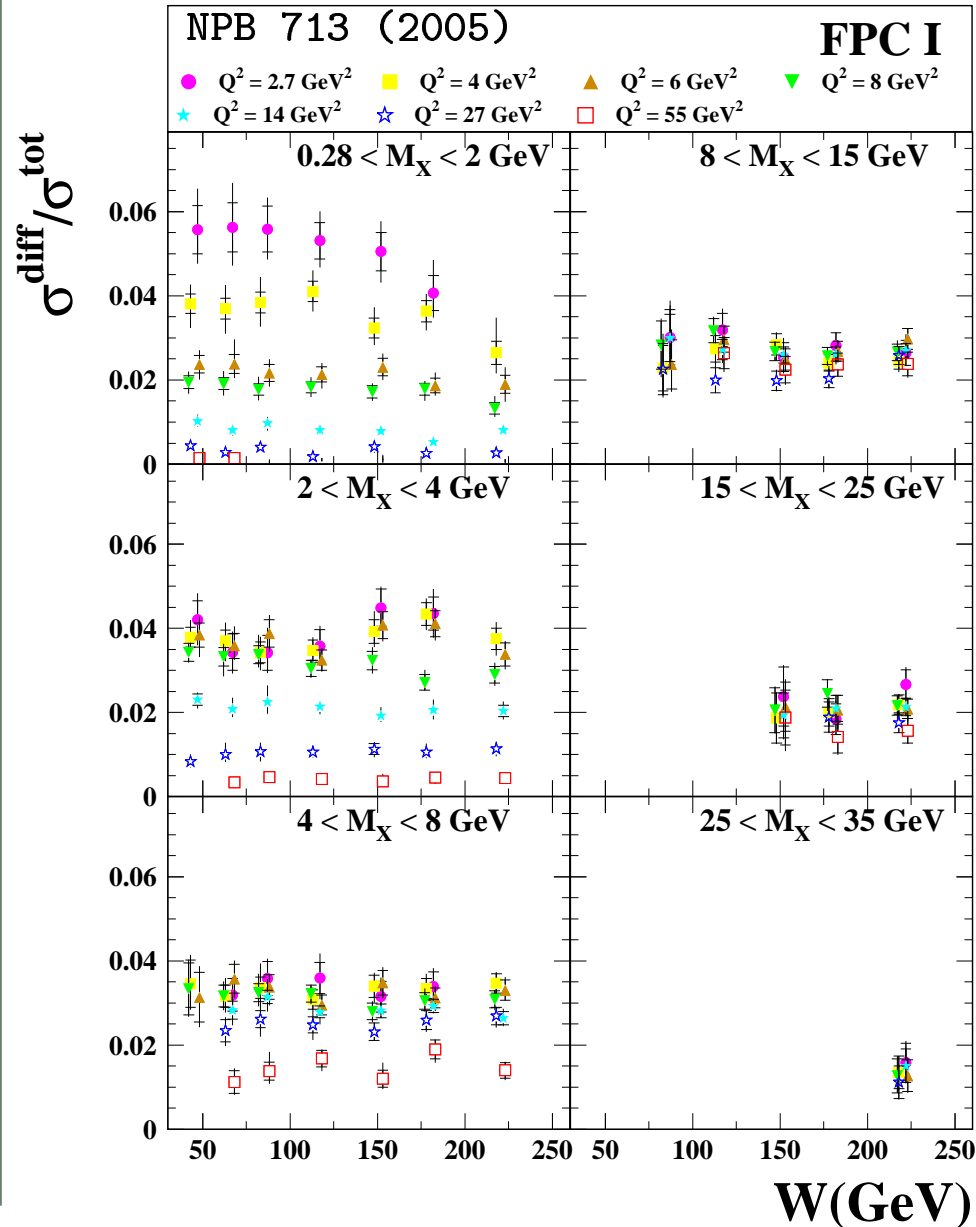


- Diffraction keeps an important soft contribution up to high  $Q^2$
- But  $J/\Psi$  or DVCS are well described by pQCD.

$\Rightarrow$  How to link inclusive and exclusive diffraction?

# Ratio of Diffractive to inclusive cross-sections

## ZEUS

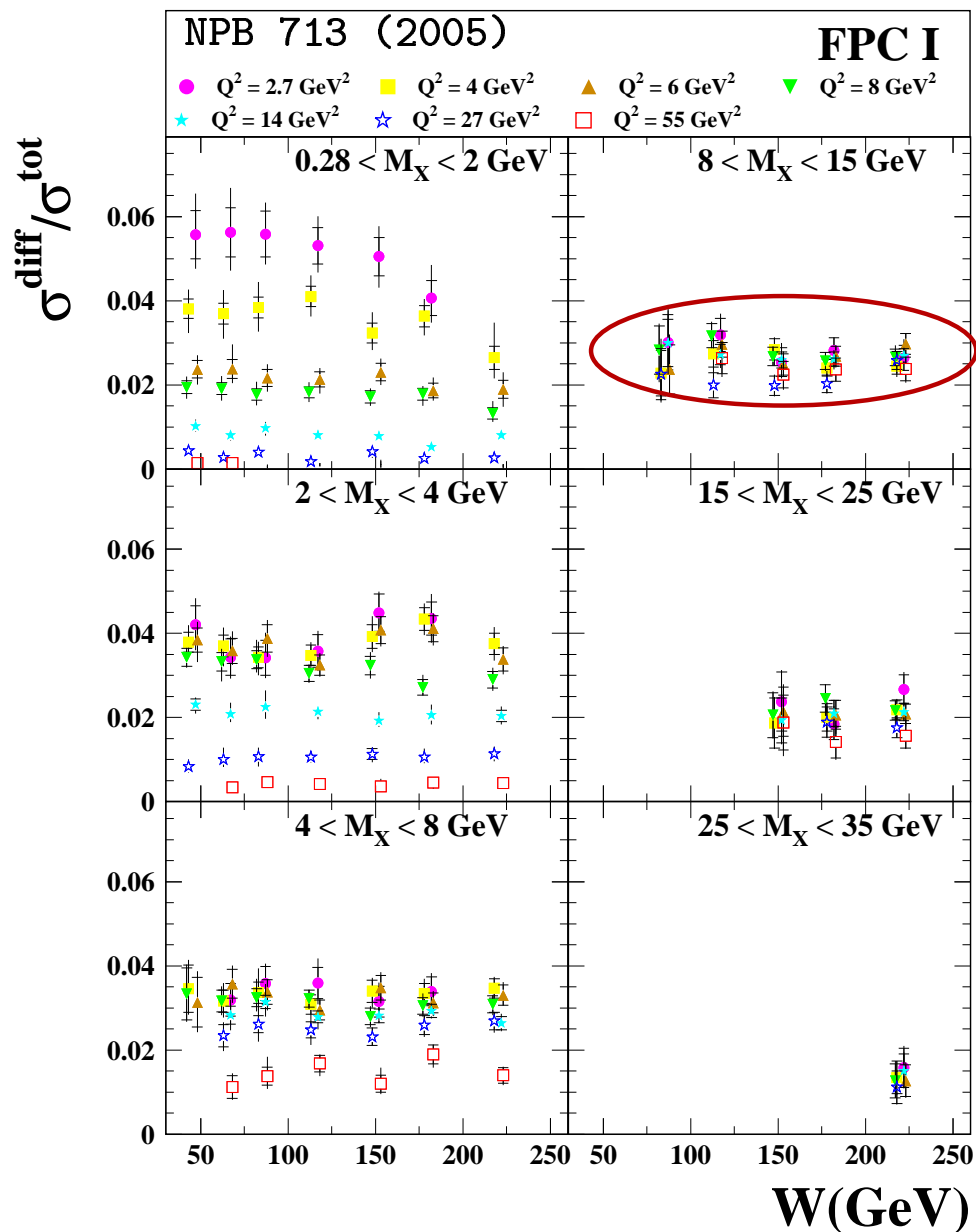


$$W^2 \simeq Q^2/x$$

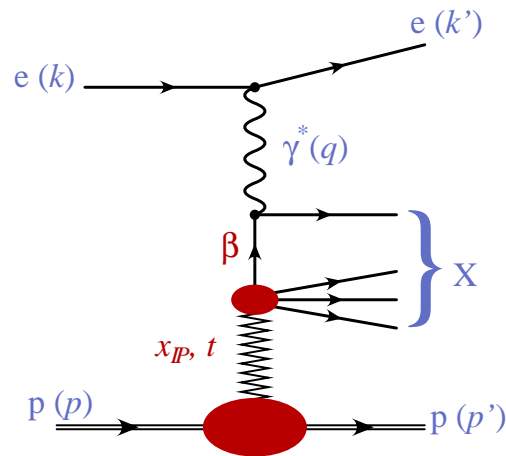
$$\beta \simeq Q^2/(Q^2 + M_X^2)$$

# Ratio of Diffractive to inclusive cross-sections

## ZEUS



- $M_X > 8 \text{ GeV}$ :
    - same  $W$  dependence as  $\sigma_{tot}$
    - no  $Q^2$  dependence
    - same DGLAP evolution
    - $\gamma^*$  sees: 1 parton that can radiate
- no distinction between DIS and DDIS!

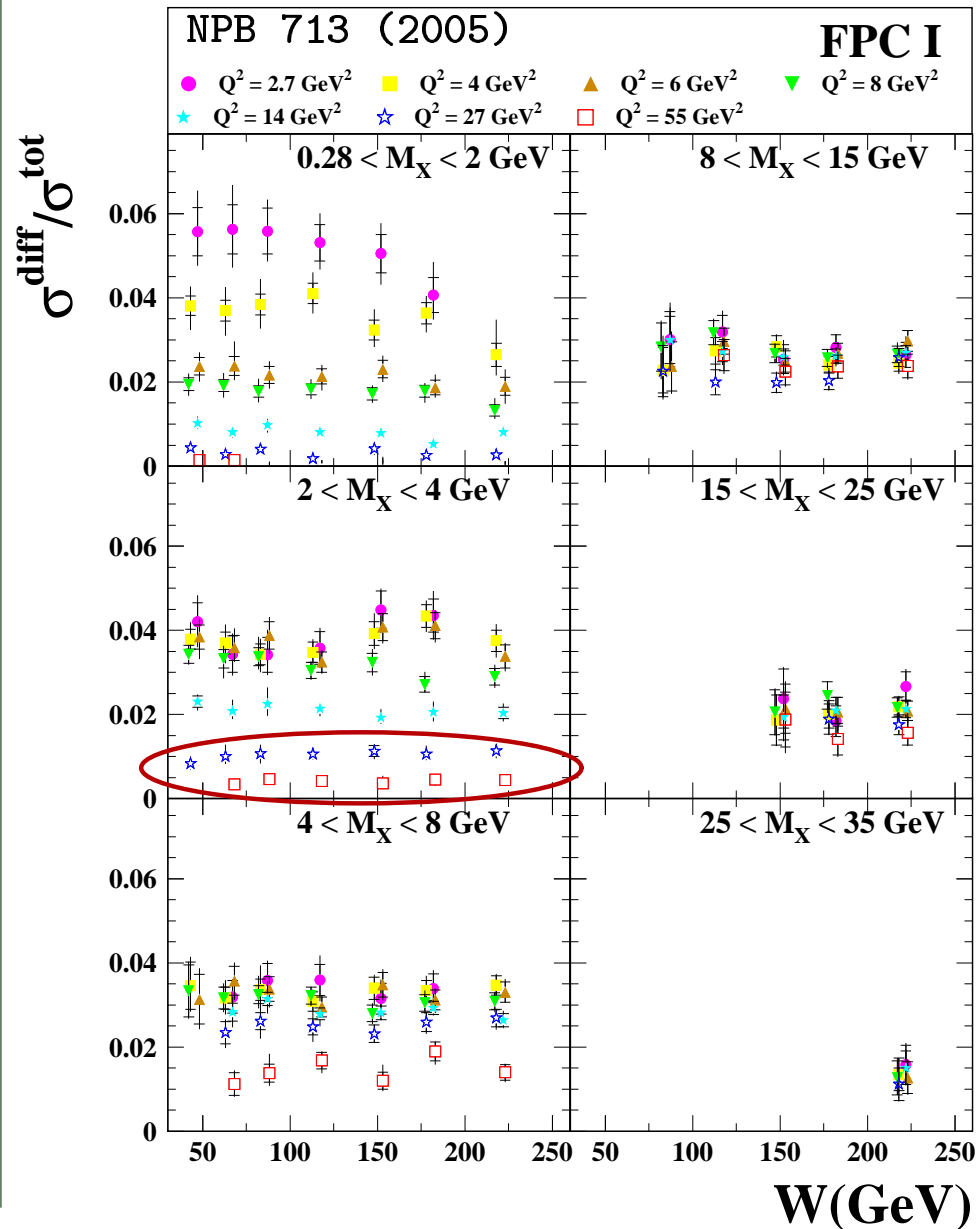


$$W^2 \simeq Q^2/x$$

$$\beta \simeq Q^2 / (Q^2 + M_X^2)$$

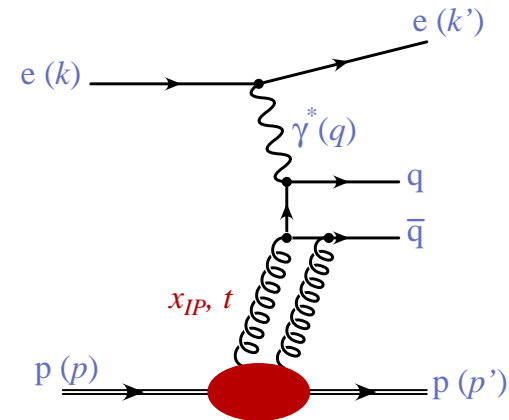
# Ratio of Diffractive to inclusive cross-sections

## ZEUS



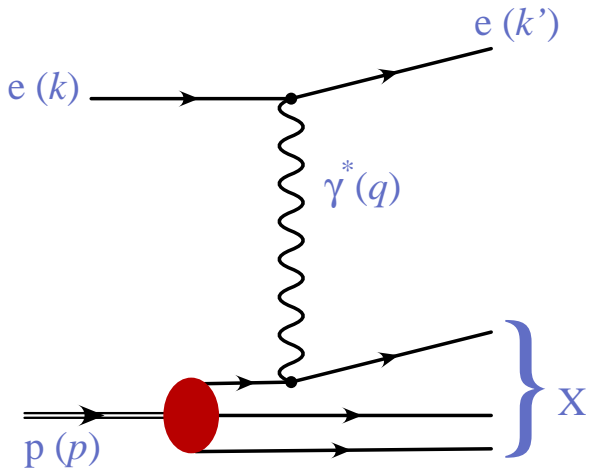
- If  $M_X \searrow, \beta \nearrow \rightarrow \gamma^*$ : more and more of the exchanged object (2 g)
- large  $\beta$ :  $M_X \ll Q^2$ 
  - $\rightarrow$  contribution of Vector Meson
  - $\rightarrow$  no g radiation allowed
  - $\rightarrow$  "closed" gluon object

should increase with  $W$  but does not!

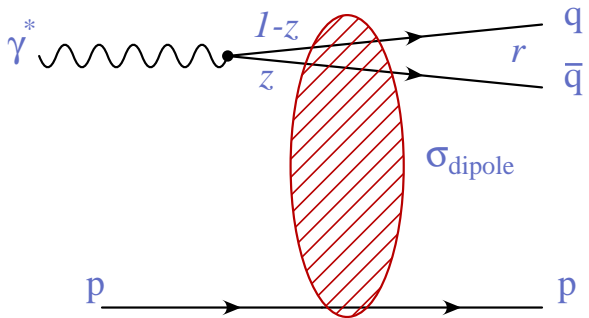


$$W^2 \simeq Q^2/x \quad \beta \simeq Q^2/(Q^2 + M_X^2)$$

# What scale should we use ?



**DIS:** direct  $\gamma - q$  interaction  
 $\Rightarrow$  scale:  $\mu^2 = Q^2$



**DDIS:** hadron-hadron interaction  $\Rightarrow \gamma \rightarrow q\bar{q}$

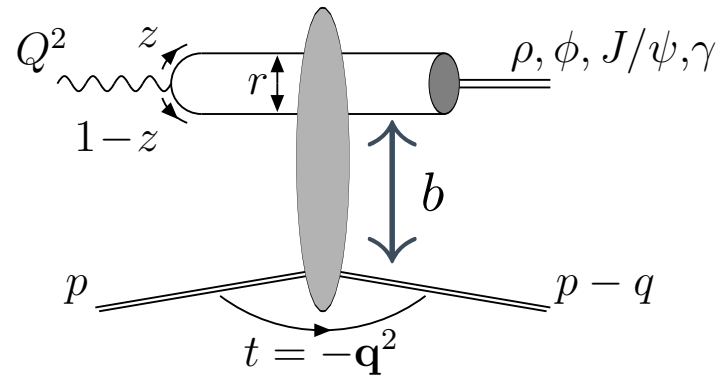
$$\mu^2 \simeq \frac{Q^2 + M_X^2}{4}$$

$\Rightarrow$  We should not compare directly DIS en DDIS at using the same scale

when  $M_X^2$  of DDIS is large,  $\mu^2$  gets closer to the scale used for DIS in previous plot  
 $\Rightarrow$  beter agreement.

# Vector meson production: QCD factorisation

at large energy, for  $\mathcal{A}_L$  (large  $Q^2$ ) or heavy quarks:



1.  $\gamma$  fluctuates in  $q\bar{q}$  dipole: QED  $\gamma$  wave function  $\Psi_\gamma$
2. dipole-proton interaction: universal  $\sigma_{dip}(r, z, b)$
3.  $q\bar{q}$  recombination into VM

- The scanning radius  $r$  is expected to decrease with increasing  $Q^2$  or  $M_V$

$\Rightarrow$  **universal scale**:  $\mu^2 = z(1-z)(Q^2 + M_V^2)$

- for  $\mathcal{A}_L$  (large  $Q^2$ ) or heavy quarks:  $z \simeq 1/2 \Rightarrow \mu^2 \simeq (Q^2 + M_V^2)/4$

- for light quarks,  $\mathcal{A}_T$ : contrib. from end points  $z = 0, 1 \Rightarrow \mu^2$  can be small even for large  $Q^2 \Rightarrow$  **soft contributions**

# $W$ , $t$ and $M_Y$ dependences

## $W$ dependence

-  $\sigma \sim W^\delta \sim |x g(x, \mu^2)| \Rightarrow$  hard  $W$  dependence: signature of a hard scale

$\Rightarrow \delta = 4(\alpha(t) - 1) = 4(\alpha(0) + \alpha' t - 1)$  larger than soft

$\Rightarrow$  Hard scale:  $\delta, \alpha(0)$  : universal with  $\frac{Q^2 + M_X^2}{4}$

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## $t$ dependence

-  $d\sigma/dt \sim e^{-b|t|}$

$b = b_{dip} \oplus b_{exch} \oplus b_Y$

$\Rightarrow$  Hard scale:  $b$ : universal with  $\frac{Q^2 + M_X^2}{4}$

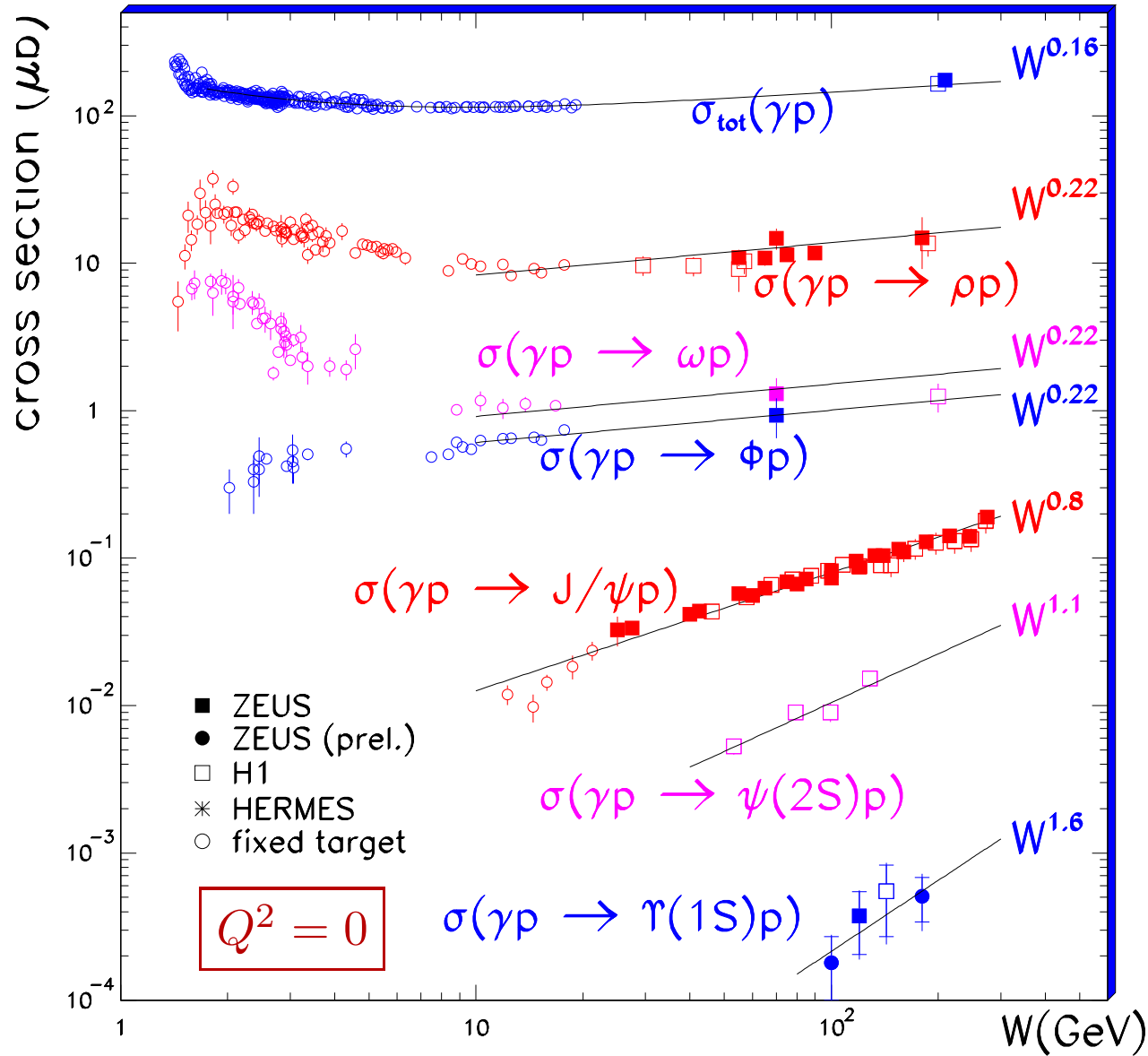
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## $M_Y$ dependence

- elastic- proton dissociation universality for  $Q^2$ ,  $W$  and helicity amplitudes.

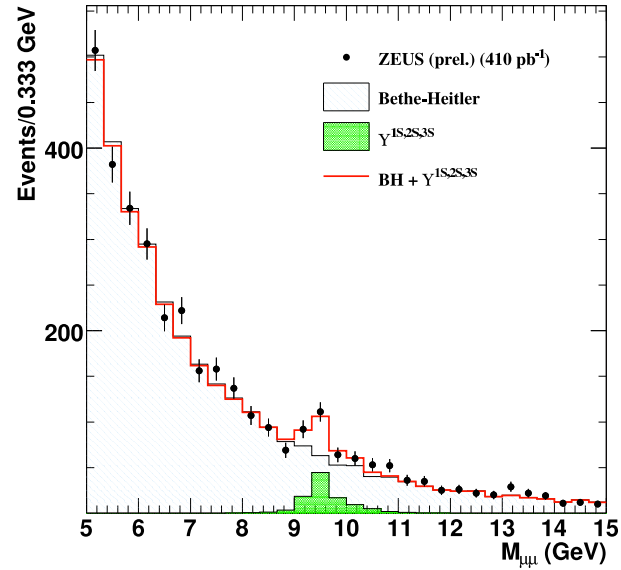
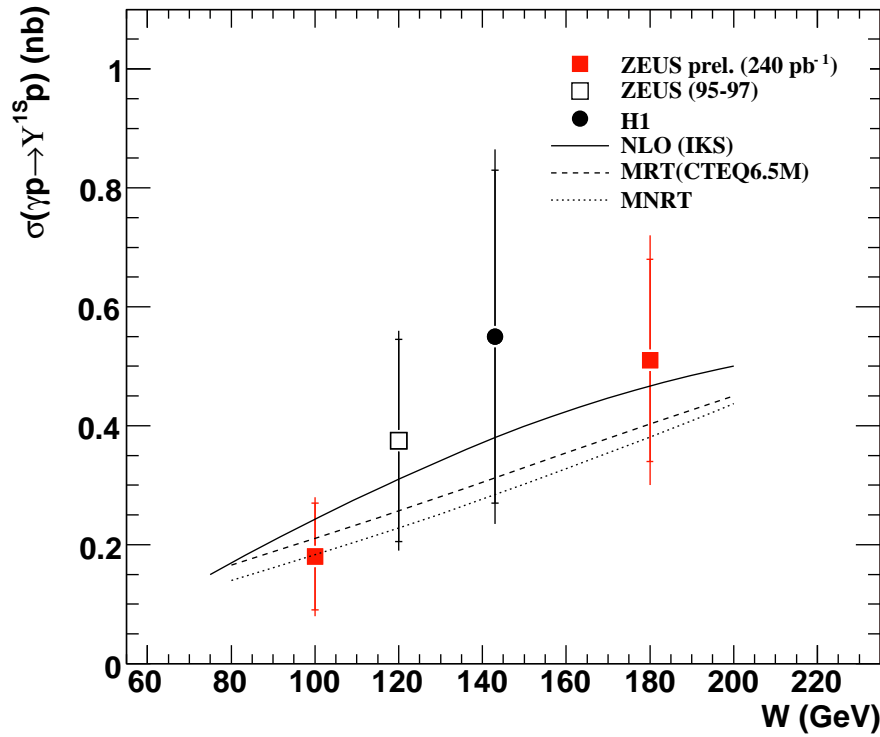


# Soft to hard transition: mass



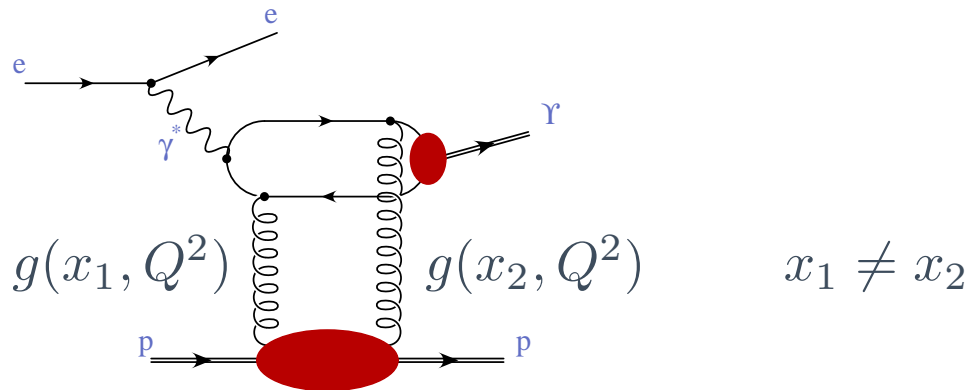
- Low mass ( $\rho, \phi, \omega; M_V^2 \simeq 1 \text{ GeV}^2$ ): no pert. scale  
 → weak energy dep. (soft regime)
- High mass ( $J/\psi, \psi$ ): pert. scale → strong energy dep. (hard regime)
- Large mass ( $\Upsilon$ ) important skewing effect

# Upsilon

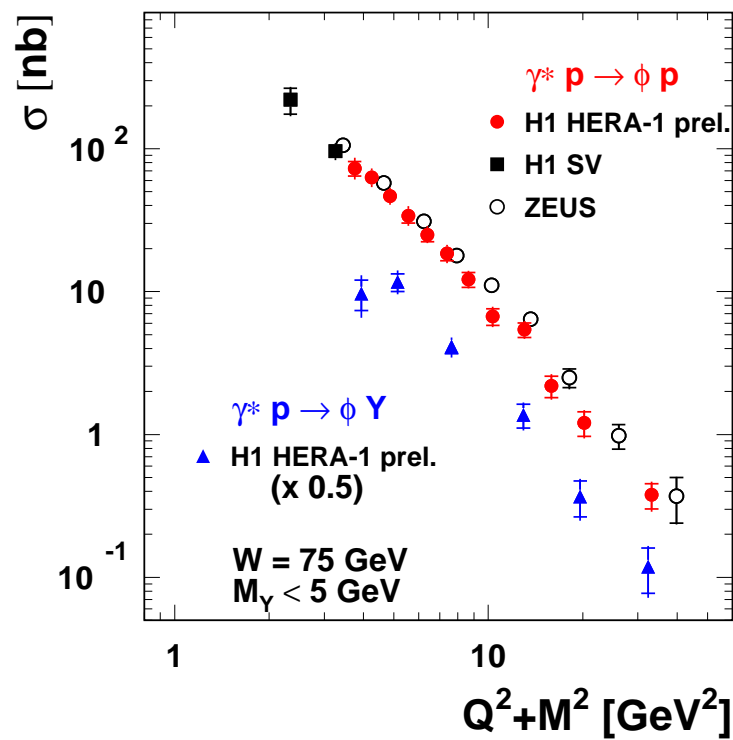
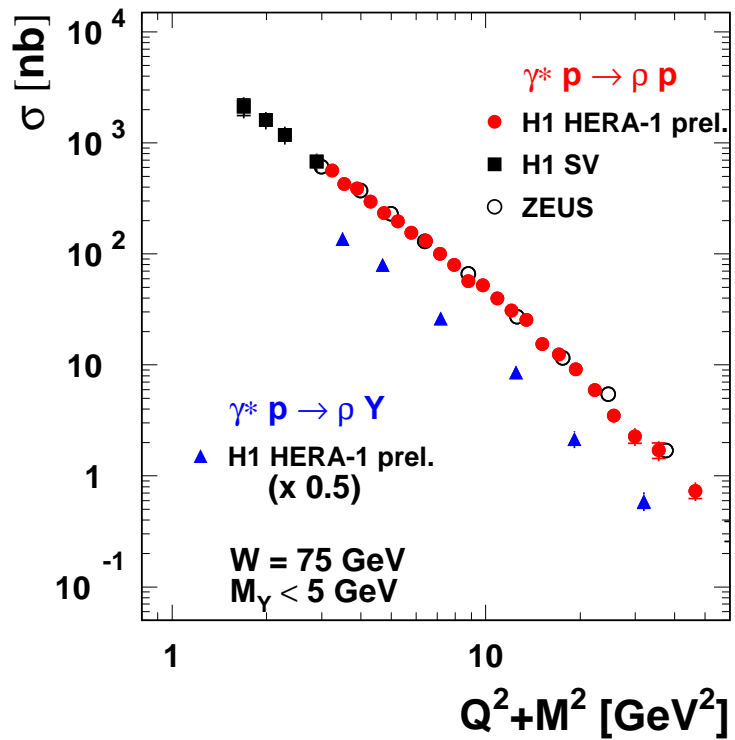


ZEUS (HERA I+II):  $104 \pm 21$  events candidates

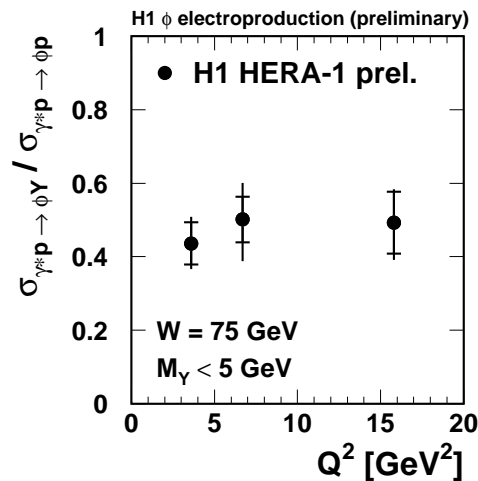
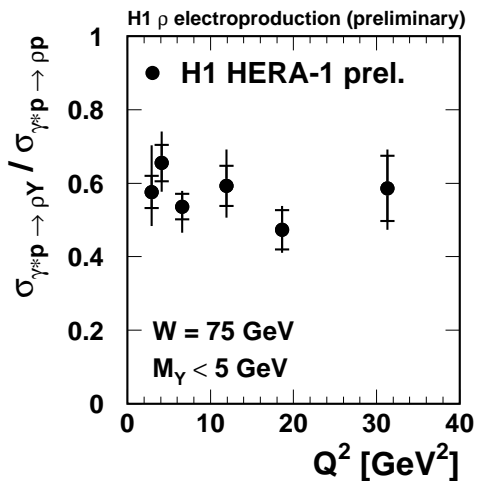
In agreement with NLO predictions including skewing and real part of the amplitude



# Light VM Cross-sections versus $Q^2$

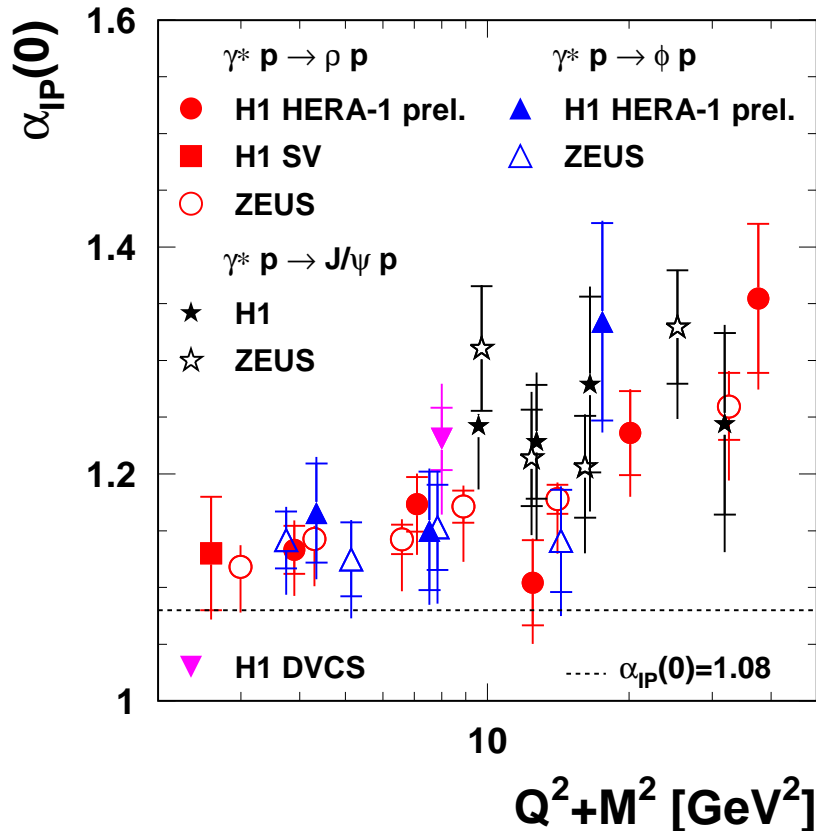
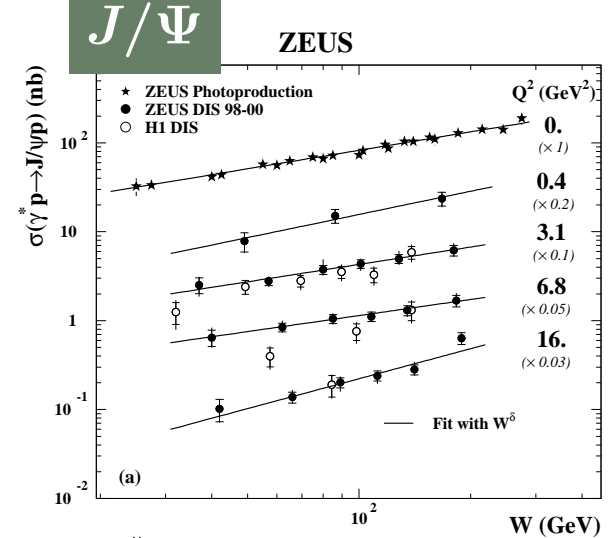
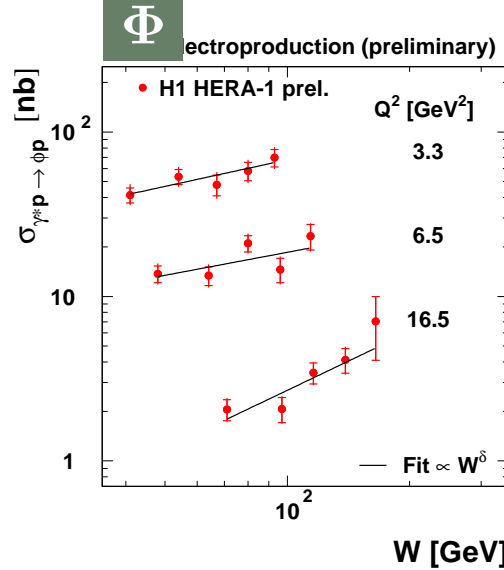
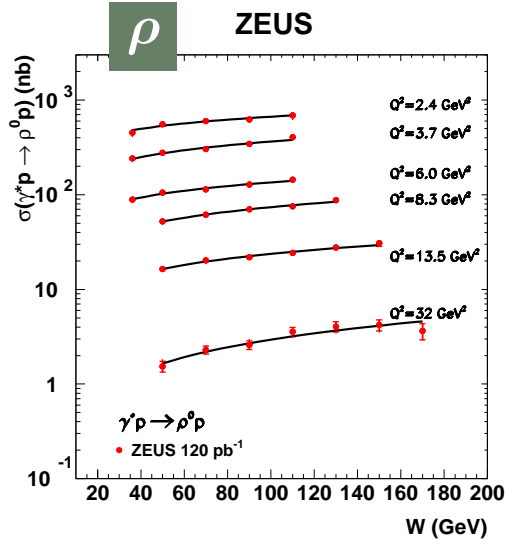


- High precision for elastic cross-sections; First  $\phi$  p-diss. cross-section



- p.diss/el: no  $Q^2$  dep.  
*i.e.* vertex factorisation

# W dependences



$$\alpha_P(0) = 1 + \delta/4 + \alpha'_P / \langle |t| \rangle$$

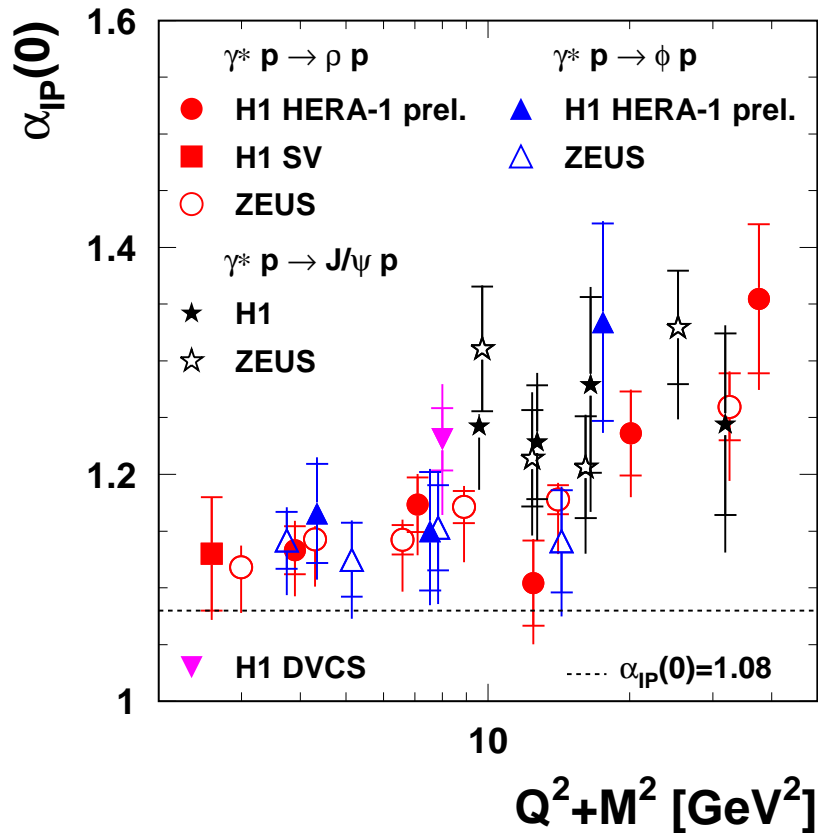
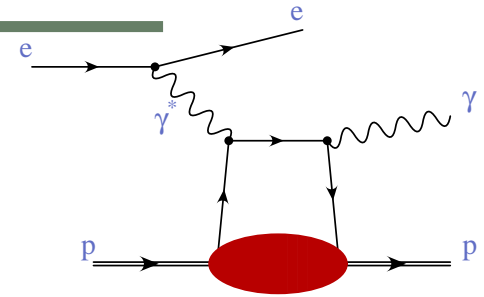
$$\alpha'_P = 0 - 0.25 \text{ GeV}^{-2}$$

- Common hardening of  $\alpha_P(0)$  with  $Q^2 + M^2$  for all VM and DVCS

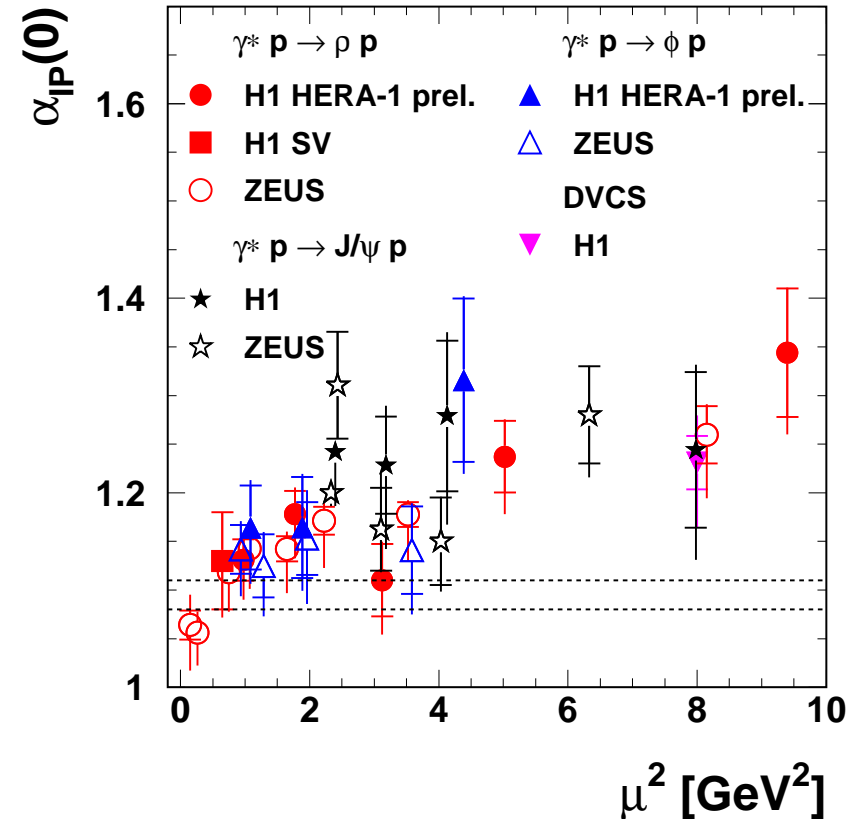
⇒ Transition from soft to hard regime with  $Q^2 + M^2$

# Note on the scale

DVCS is like DIS, the photon (at LO) interacts directly with a resolved quark.



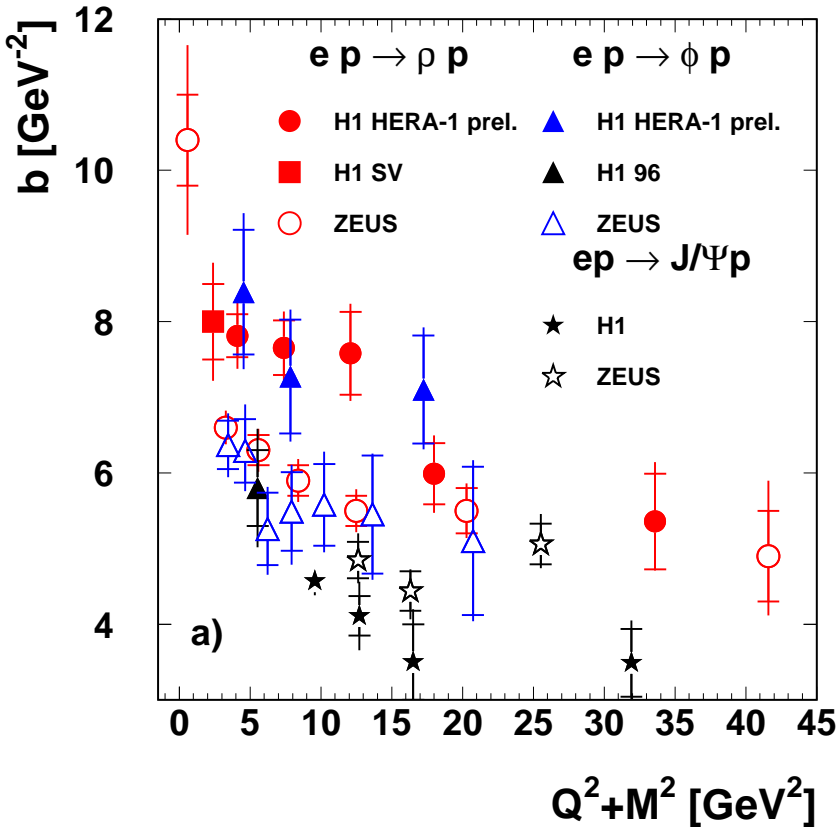
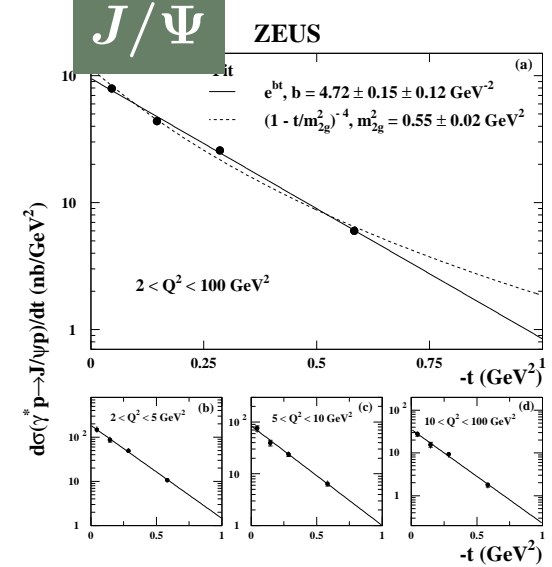
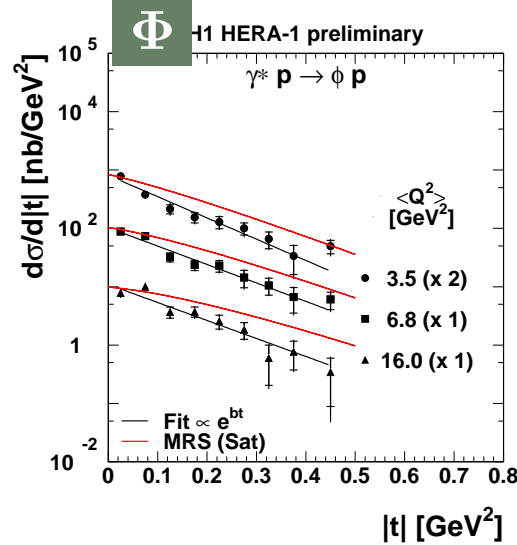
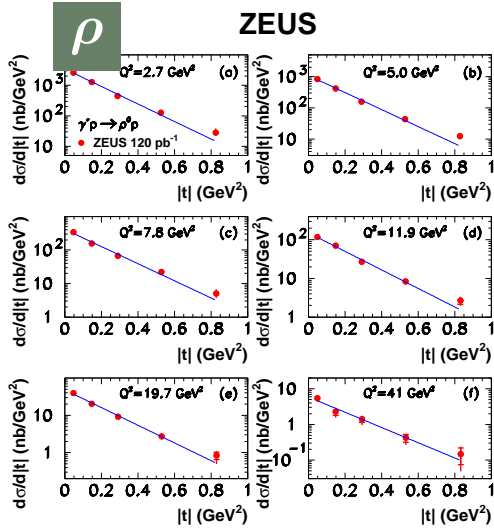
for all:  $\mu^2 = Q^2 + M_X^2$



for VM:  $\mu^2 = \frac{Q^2 + M_X^2}{4}$

for DVCS :  $\mu^2 = Q^2$

# $t$ dependences

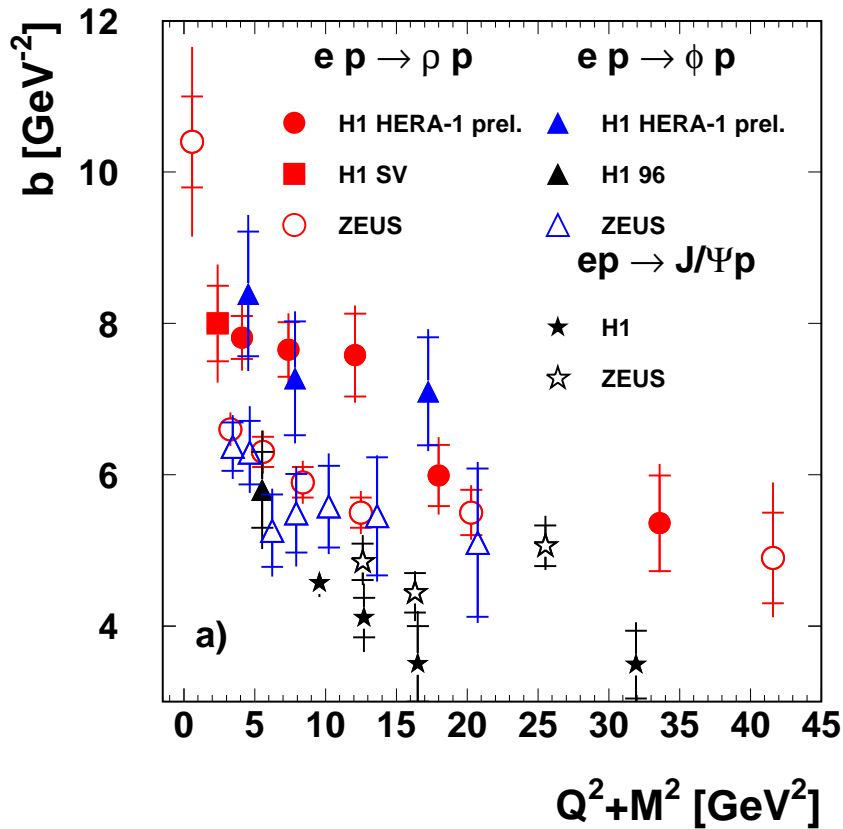


fit of  $e^{-b|t|}$

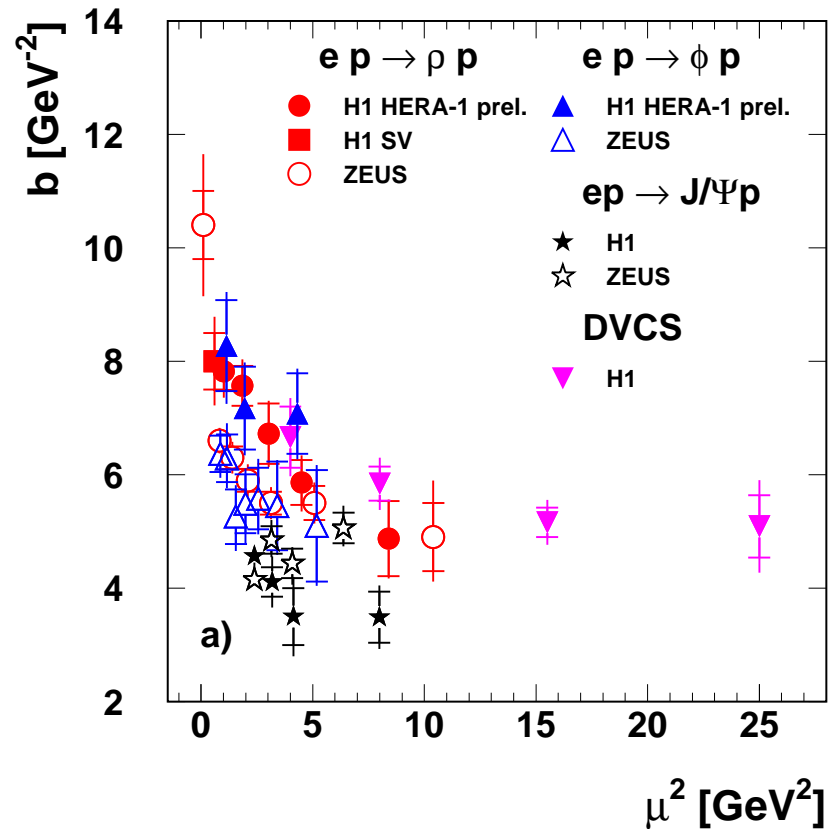
●  $t$  slope hardening with  $Q^2 + M^2$  for all VM and DVCS

⇒ Transition from soft to hard regime with  $Q^2 + M^2$

# Note on the scale



for all:  $\mu^2 = Q^2 + M_X^2$

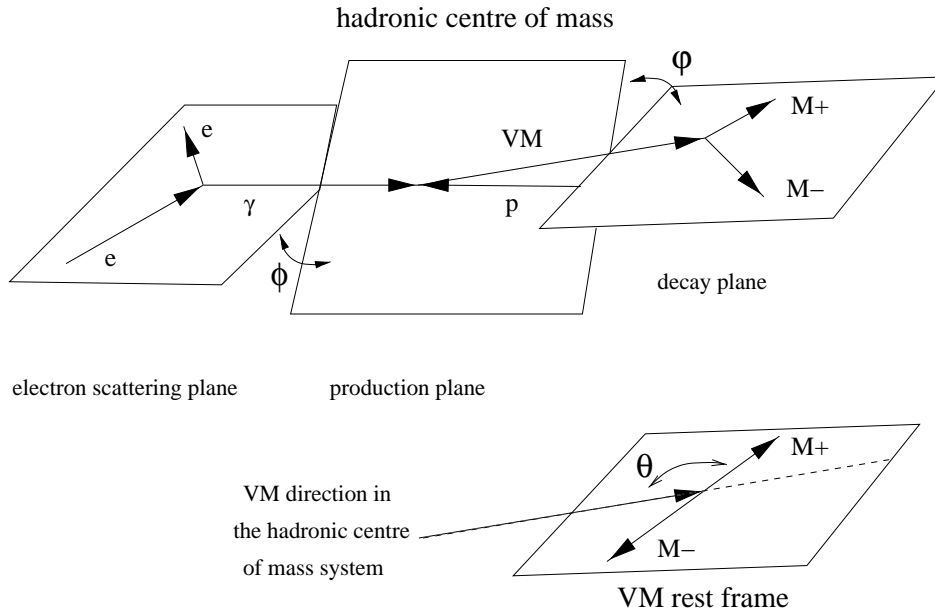


for VM:  $\mu^2 = \frac{Q^2 + M_X^2}{4}$   
 for DVCS :  $\mu^2 = Q^2$

# SPIN DENSITY MATRIX ELEMENTS

$$\theta^* , \Phi , \varphi \iff 15 \text{ SDMEs} : r_{kl}^{ij} \propto T_{\lambda'_\rho \lambda'_\gamma} T_{\lambda_\rho \lambda_\gamma}$$

$T_{\lambda_\rho \lambda_\gamma}$  : helicity amplitudes



No helicity flip:  $T_{00} : \gamma_L \rightarrow \rho_L$

$T_{11} : \gamma_T \rightarrow \rho_T$

Single flip:  $T_{01} : \gamma_T \rightarrow \rho_L$

$T_{10} : \gamma_L \rightarrow \rho_T$

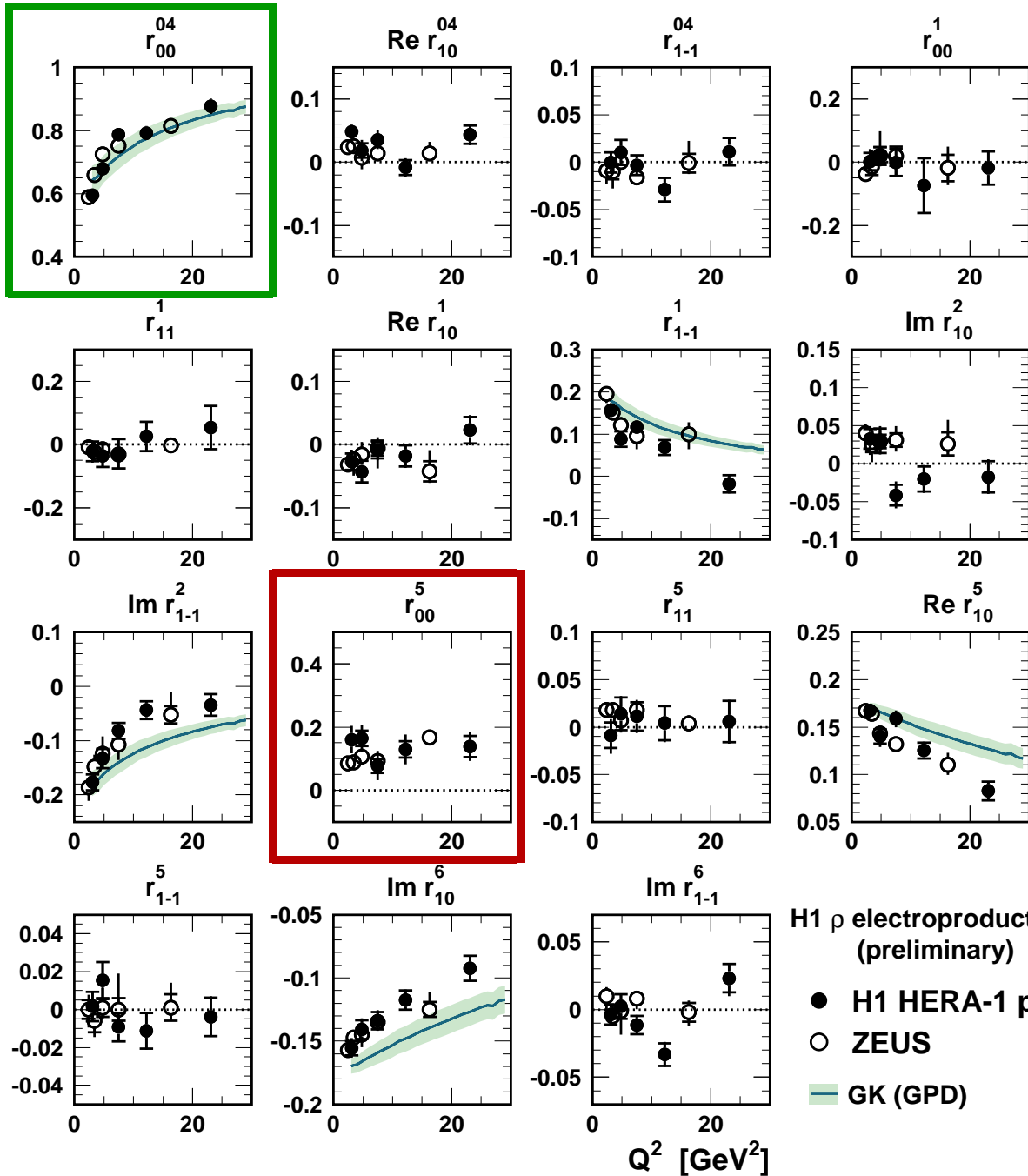
Double flip:  $T_{1-1} : \gamma_T \rightarrow \rho_T$

**s-Channel Helicity Conservation (SCHC):**  $T_{01} = T_{10} = T_{1-1} = 0$

- SCHC violation ( single flip  $\propto \sqrt{|t|}$ , double  $\propto |t|$  )
- pQCD Hierarchy ( $|t| < Q^2$ ):  $|T_{00}| > |T_{11}| > |T_{01}| > |T_{10}| > |T_{1-1}|$



# $\rho$ Polarisation - SDMEs vs. $Q^2$



- $r_{00}^{04}$  increases with  $Q^2$
- ↔ similar effects for  $r_{1-1}^1$ ,  
 $\text{Im } r_{1-1}^2$ ,  $\text{Re } r_{10}^5$  and  
 $\text{Im } r_{10}^6$  (in SCHC)
- ↔ Fair description  
 by Goloskokov-Kroll  
 (GPD) model
- $r_{00}^5$  violates SCHC (flip)
- Other SDME  $\simeq 0$

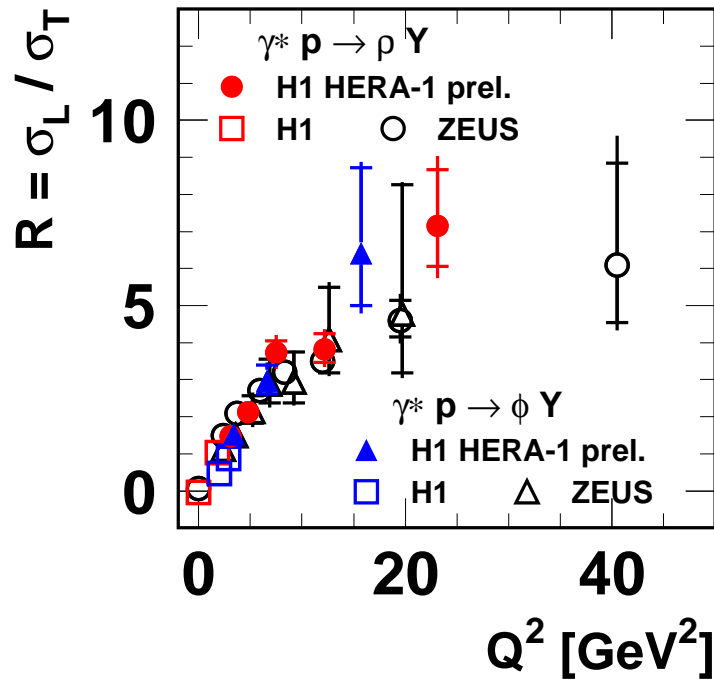
H1  $\rho$  electroproduction  
(preliminary)

- H1 HERA-1 prel.
- ZEUS
- GK (GPD)

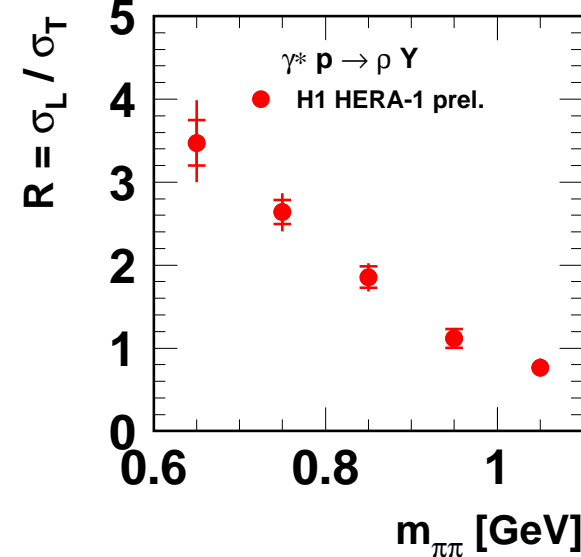
# Polarisation - $R = \sigma_L / \sigma_T$

$$R_{SCHC} = \frac{1}{\epsilon} \frac{r_{00}^{04}}{1 - \epsilon r_{00}^{04}} = \frac{|T_{00}|^2}{|T_{11}|^2}$$

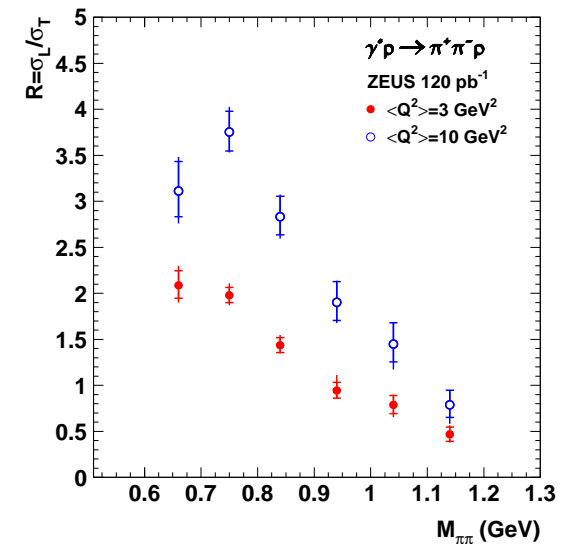
H1  $\rho$  and  $\phi$  electroproduction (preliminary)



H1  $\rho$  electroproduction (preliminary)



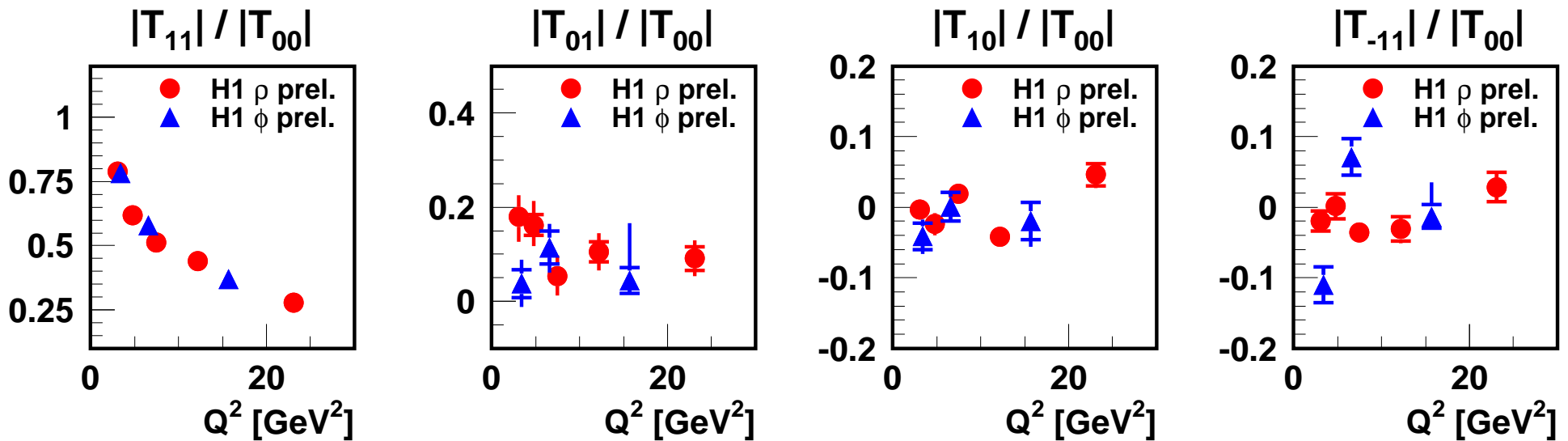
ZEUS



- Naive  $R \propto Q^2 / M^2$  - modified at high  $Q^2$
- Similar  $R$  for  $\phi$  and  $\rho$
- Strong invariant mass dependence in  $\rho$  case

# Polarisation - Amplitude ratios vs. $Q^2$

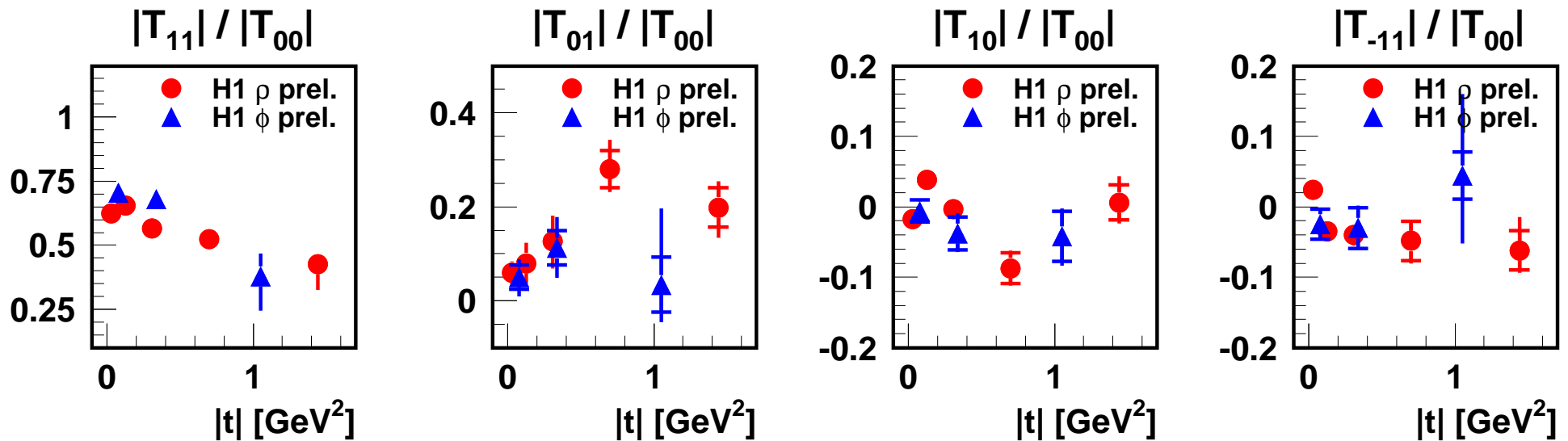
- pQCD :
- $|T_{11}|/|T_{00}| \sim \frac{M}{Q} \frac{1+\gamma}{\gamma}$
  - $|T_{10}|/|T_{00}| \sim -\frac{M}{Q^2} \frac{\sqrt{|t|}}{\gamma} \frac{\sqrt{2}}{\gamma}$
  - $|T_{01}|/|T_{00}| \sim \frac{\sqrt{|t|}}{Q} \frac{1}{\sqrt{2}\gamma}$
- $\gamma$  : gluon anomalous dim.



- $|T_{11}|/|T_{00}|$  decreases with  $Q^2 \leftrightarrow \sigma_L/\sigma_T$  increases with  $Q^2$
  - $|T_{01}|/|T_{00}| > 0 \leftrightarrow$  SCHC violation
  - $|T_{10}|/|T_{00}|$  and  $|T_{-11}|/|T_{00}|$  are small
- $\Rightarrow |T_{00}| > |T_{11}| > |T_{01}| > |T_{10}|, |T_{-11}| \leftrightarrow$  hierarchy observed

# Polarisation - Amplitude ratios vs. $|t|$

- pQCD:
- $|T_{11}|/|T_{00}| \sim \frac{M}{Q} \frac{1+\gamma}{\gamma}$
  - $|T_{10}|/|T_{00}| \sim -\frac{M}{Q^2} \frac{\sqrt{|t|}}{\gamma} \frac{\sqrt{2}}{\gamma}$
  - $|T_{01}|/|T_{00}| \sim \frac{\sqrt{|t|}}{Q} \frac{1}{\sqrt{2}\gamma}$
- $\gamma$  : gluon anomalous dim.

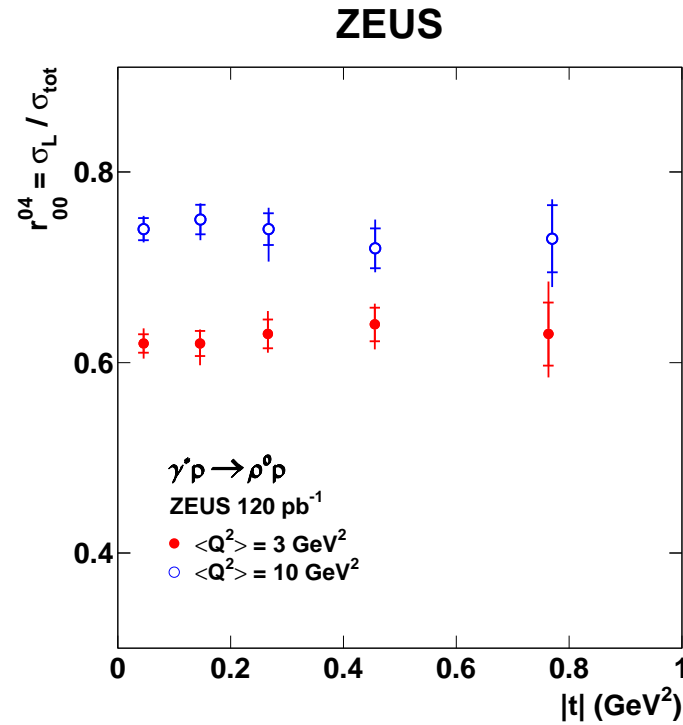
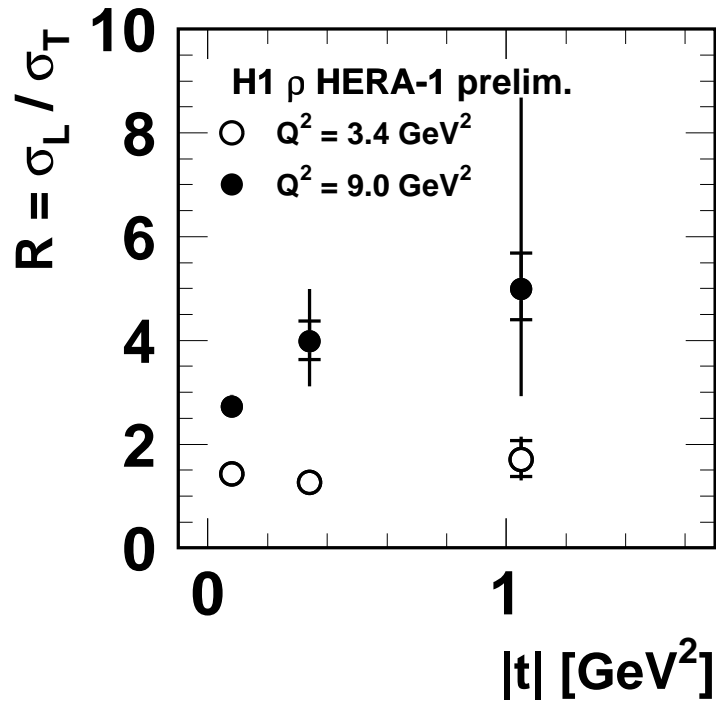


- $|T_{11}|/|T_{00}|$  decreases with  $|t|$
- $|T_{01}|/|T_{00}|$  increases with  $|t| \leftrightarrow$  SCHC violation increases with  $|t|$
- $|T_{10}|/|T_{00}|$  and  $|T_{-11}|/|T_{00}|$  are small but some  $|t|$  dependence
- $|T_{11}|/|T_{00}|$  decrease partially compensated by  $|T_{01}|/|T_{00}|$  increase

$\Rightarrow \sigma_L/\sigma_T$  is the result of partial compensations

# Polarisation - $R = \sigma_L / \sigma_T$ versus $t$

$$R_{SCHC+T_{01}} = \frac{|T_{00}|^2}{|T_{11}+T_{01}|^2}$$



- H1:  $R$  depends on  $t$  for large  $Q^2 \Rightarrow b_L < b_T$  !!! ( $\sigma_L$  more pert. than  $\sigma_T$ )
- Not seen by ZEUS
- due to different  $\rho'$  background treatment

# Conclusions

Important progresses in precision of VM measurements and understanding of underlying dynamics.

- $\rho, \phi, J/\psi, \Upsilon, \gamma$
- in  $Q^2, W, t$ , helicity amplitudes, p-diss/el
- precision in the soft to hard transition: scales, and  $L/T$  separation
- many models: GPD, BFKL, dipole, saturation,...  
with semi-qualitative understanding  
but many quantitative description still lacking

# Back-up Slides

# Polarisation - Retrieving Amplitude ratios

Assume purely imaginary amplitudes  $\longrightarrow$  phase =  $\pm 1$  !

$\longrightarrow$  Extract  $|T_{11}|/|T_{00}|$ ,  $|T_{01}|/|T_{00}|$ ,  $|T_{10}|/|T_{00}|$  and  $|T_{-11}|/|T_{00}|$   
from fit to the 15 SDMEs:

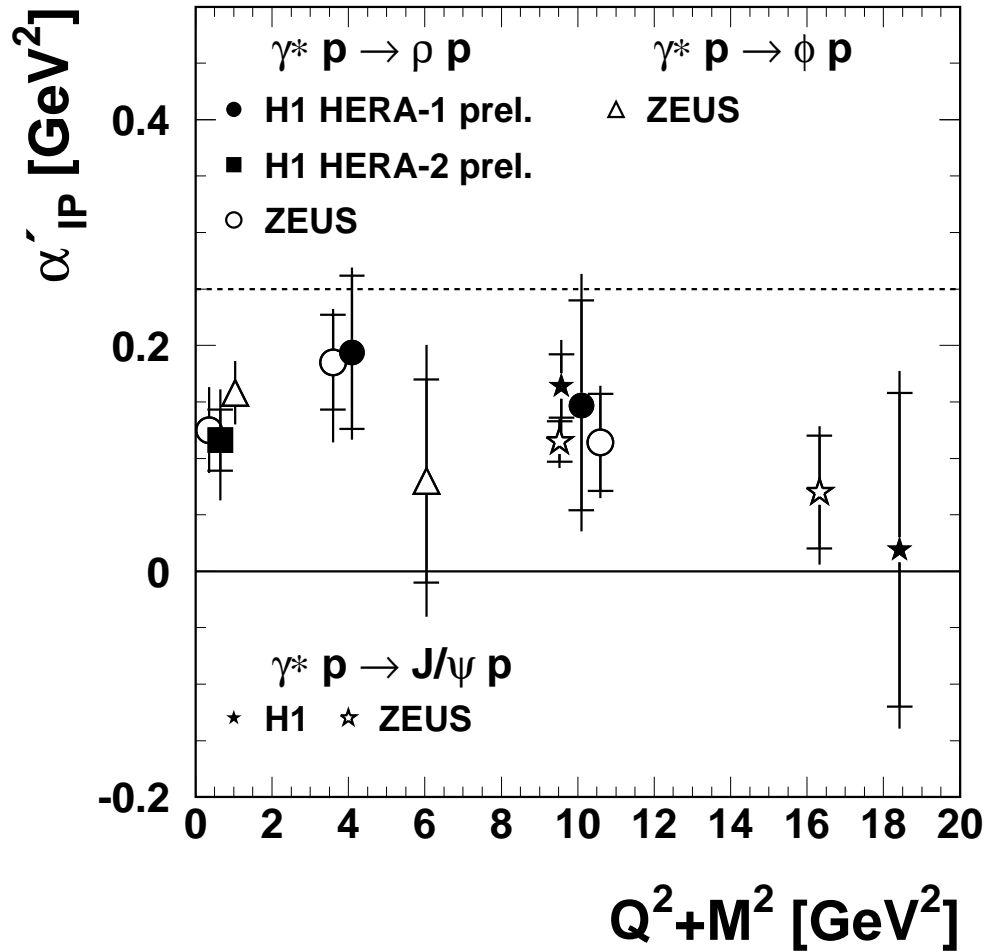
$$\begin{aligned}
 r_{00}^{04} &= B (\varepsilon + \beta^2) \\
 \text{Re } r_{10}^{04} &= B/2 (2\varepsilon\delta + \beta\alpha - \beta\eta) \\
 r_{1-1}^{04} &= B (\alpha\eta - \varepsilon\delta^2) \\
 r_{00}^1 &= -B \beta^2 \\
 r_{11}^1 &= B \alpha\eta \\
 \text{Re } r_{10}^1 &= B/2 \beta(\eta - \alpha) \\
 r_{1-1}^1 &= B/2 (\alpha^2 + \eta^2) \\
 \text{Im } r_{10}^2 &= B/2 \beta(\alpha + \eta) \\
 \text{Im } r_{1-1}^2 &= B/2 (\eta^2 - \alpha^2) \\
 r_{00}^5 &= \sqrt{2}B \beta \\
 r_{11}^5 &= B/\sqrt{2} \delta(\alpha - \eta) \\
 \text{Re } r_{10}^5 &= B/(2\sqrt{2}) (2\beta\delta + \alpha - \eta) \\
 r_{1-1}^5 &= B/\sqrt{2} \delta(\eta - \alpha) \\
 \text{Im } r_{10}^6 &= -B/(2\sqrt{2}) (\alpha + \eta) \\
 \text{Im } r_{1-1}^6 &= B/\sqrt{2} \delta(\alpha + \eta)
 \end{aligned}$$

$$\begin{aligned}
 \alpha &= |T_{11}|/|T_{00}| \\
 \beta &= |T_{01}|/|T_{00}| \\
 \delta &= |T_{10}|/|T_{00}| \\
 \eta &= |T_{-11}|/|T_{00}|
 \end{aligned}$$

$$\begin{aligned}
 B &= \frac{1}{N_T + \varepsilon N_L} = \frac{R}{1 + \varepsilon R} \\
 N_T &= \alpha^2 + \beta^2 + \eta^2 \\
 N_L &= 1 + 2\delta^2
 \end{aligned}$$



$\alpha'$



# Rho mass

**ZEUS**

