High Q² Cross Sections and Electroweak Studies at HERA

Lake Louis Winter Institute 2007

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On behalf of the HI and ZEUS collaborations

HERA



HERA



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Luminosity and Polarisation



Deep Inelastic Scattering

$$egin{aligned} Q^2 &= -q^2 \ x &= Q^2/2(P\cdot q) \ y &= (P\cdot q)/(P\cdot k) \ Q^2 &= x\,y\,s \end{aligned}$$



Neutral and Charged Currents



Charged Current Cross Section vs Pe

Standard Model weak interaction left-handed

– only LH particles (RH anti-particles) interact

Polarisation is asymmetry of the helicity states

$$P_e = \frac{N_R - N_L}{N_R + N_L}$$

CC cross section modified by P_e:

$$\sigma_{CC}^{e^{\pm}p}(P_e) = (1 \pm P_e) \cdot \sigma_{CC}^{e^{\pm}p}(P_e = 0)$$

- Measurement shows the expected linear dependence on P_{e}
- Extrapolation to $P_{e_{-}} = +1$, $P_{e^{+}} = -1$ absence of RH charged currents
- $M(W_R) \gtrsim 200 \text{ GeV}$ @ 95% CL



 e_{R}

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Neutral Current Cross Section

$$F_{2} = F_{2}^{em} + \frac{Q^{2}}{Q^{2} + M_{Z}^{2}} F_{2}^{\gamma Z} + \left[\frac{Q^{2}}{Q^{2} + M_{Z}^{2}}\right]^{2} F_{2}^{Z} \propto \sum_{q=u...b} (q + \overline{q})$$

$$xF_{3} = \frac{Q^{2}}{Q^{2} + M_{Z}^{2}} xF_{3}^{\gamma Z} + \left[\frac{Q^{2}}{Q^{2} + M_{Z}^{2}}\right]^{2} xF_{3}^{Z} \propto \sum_{q=u...b} (q - \overline{q})$$

Neutral Current Cross Section

$$\frac{d^{2}\sigma^{NC}(e^{\pm}p)}{dxdQ^{2}} = \frac{2\pi\alpha^{2}}{xQ^{4}}Y_{+}\left[F_{2} - \frac{y^{2}}{Y_{+}}F_{L} \mp \frac{Y_{-}}{Y_{+}}xF_{3}\right] \qquad Y_{\pm} = 1 \pm (1-y)^{2}$$
Dominant contribution
Sizeable only at high y
Contribution only important at high Q²

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$$(F_2, F_2^{\gamma Z}, F_2^Z) = x \sum (e_q^2, 2e_q v_q, v_q^2 + a_q^2)(q + \bar{q})$$

$$(xF_3^{\gamma Z}, xF_3^Z) = 2x \sum (e_q a_q, v_q a_q)(q - \bar{q})$$

Polarisation Asymmetry in Neutral Current Cross Section

$$A^{\pm} = \frac{2}{P_R - P_L} \cdot \frac{\sigma^{\pm}(P_R) - \sigma^{\pm}(P_L)}{\sigma^{\pm}(P_R) + \sigma^{\pm}(P_L)}$$

$$A^{\pm} \simeq \mp k a_e \frac{F_2^{\gamma Z}}{F_2} \propto a_e v_q$$

- $\delta A = A^+ A^-$, only significant at high Q^2
- probability for $\delta A = 0$ at $Q^2 > 5000 \text{ GeV}^2$ is 3.1×10^{-3}
- Clear evidence of Parity Violation in NC interactions at distances < 10⁻¹⁸m



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xF₃ Structure Function Neutral Current



- γZ^0 interference term flips sign when $e^+ \rightarrow e^-$
- Constrains x dependence of the valence quarks



Extraction of Parton Density Functions

(From HERA I Data)

10⁴

 YZ^0

 Q^2 (GeV²)



medium x gluon constrained by jet data

Extraction of Parton Density Functions

(From HERA I Data)

Fits of Electroweak Parameters

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- Sensitivity to a_q, v_q couplings of the light quarks to Z⁰ allows for a combined QCD-EW
- HI performs fit using unpolarised HERA I data
- ZEUS provides preliminary results including HERA II data, with its polarisation giving improved sensitivity to v_q

Summary

- DIS at HERA provides the possibility for testing the Standard Model and the measurement of electroweak parameters over a broad range of phase space
- The large sample of $e^{\pm}p$ data has allowed for the determination of the structure functions xF_3 and $xF_3^{\gamma Z}$, further increasing knowledge of the proton at lower x
- New longitudinal polarised lepton data has been able to demonstrate
 - the absence of RH Charged Currents
 - clear evidence of parity violation in Neutral Current interactions
 - improvement on the combined QCD+EW fit using HERA I data, especially for the light quark weak couplings to the Z⁰
- Still more data to analyse, and yet more still to come, increasing reach and precision

Polarised NC and CC cross Section Formulas

$$\begin{split} \tilde{\sigma}^{\pm} &= \frac{d^2 \sigma^{\pm}}{dx dQ^2} \frac{Q^4 x}{2\pi \alpha^2 Y_+} = \tilde{F}_2^{\pm} \mp \frac{Y_-}{Y_+} x \tilde{F}_3^{\pm} - \frac{y^2}{Y_+} \tilde{F}_L^{\pm} \\ \tilde{F}_2^{\pm} &= F_2 + k (-v_e \mp P a_e) F_2^{\gamma Z} + k^2 (v_e^2 + a_e^2 \pm 2P v_e a_e) F_2^Z \\ x \tilde{F}_3^{\pm} &= k (-a_e \mp P v_e) x F_3^{\gamma Z} + k^2 (2v_e a_e \pm P (v_e^2 + a_e^2)) x F_3^Z \\ \tilde{\sigma}^- - \tilde{\sigma}^+ &= 2 \frac{Y_-}{Y_+} (-a_e \cdot k x F_3^{\gamma Z} + 2v_e a_e \cdot k^2 x F_3^Z) \\ &- 2k Y_- a_e x F_3^{\gamma Z} / Y_+ \end{split}$$

$$F_{2} = \sum_{q=u...b} \left(e_{q}^{2} - 2e_{q}v_{q}v_{e}P_{Z} + (v_{e}^{2} + a_{e}^{2})(v_{q}^{2} + a_{q}^{2})P_{Z}^{2} \right) \cdot x(q + \overline{q})$$

$$xF_{3} = \sum_{q=u...b} \left(-2e_{q}a_{q}a_{e}P_{Z} + 4a_{q}v_{q}v_{e}a_{e}P_{Z}^{2} \right) \cdot x(q - \overline{q})$$

Remember that $P_Z >> P_Z^2$ and $v_e \sim 0.04$

$$P_Z = \frac{1}{\sin^2 \theta_W} \frac{Q^2}{Q^2 + M_Z^2}$$

- \rightarrow xF₃ γ -Z⁰ interference term is largest
- → Expect axial coupling of u-quark to be best constrained

Improvements to Parton Density Functions

- ZEUS performed a new fit incorporating HERA II e⁻ p data
- further improved on the previous HERA I fit especially for u_v (d_v) at large x

