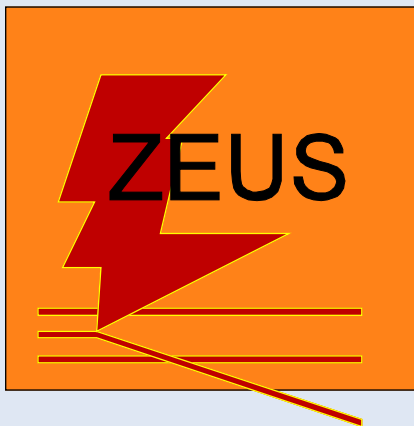
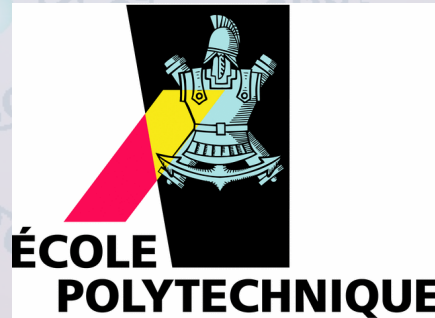


QCD at HERA

V. Boudry

Laboratoire Leprince-Ringuet,
École polytechnique,
Palaiseau, France

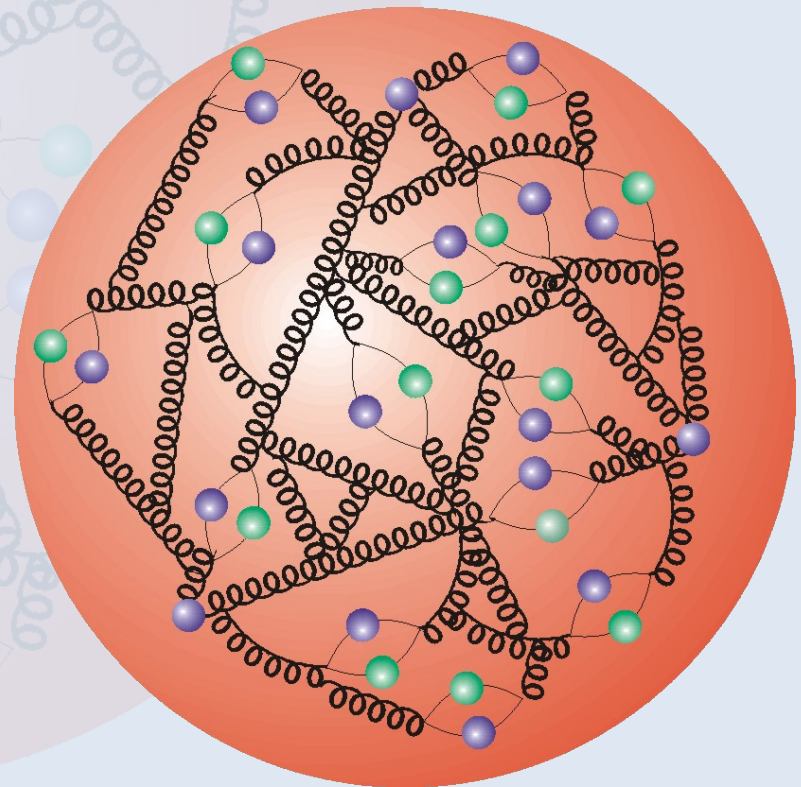
LM



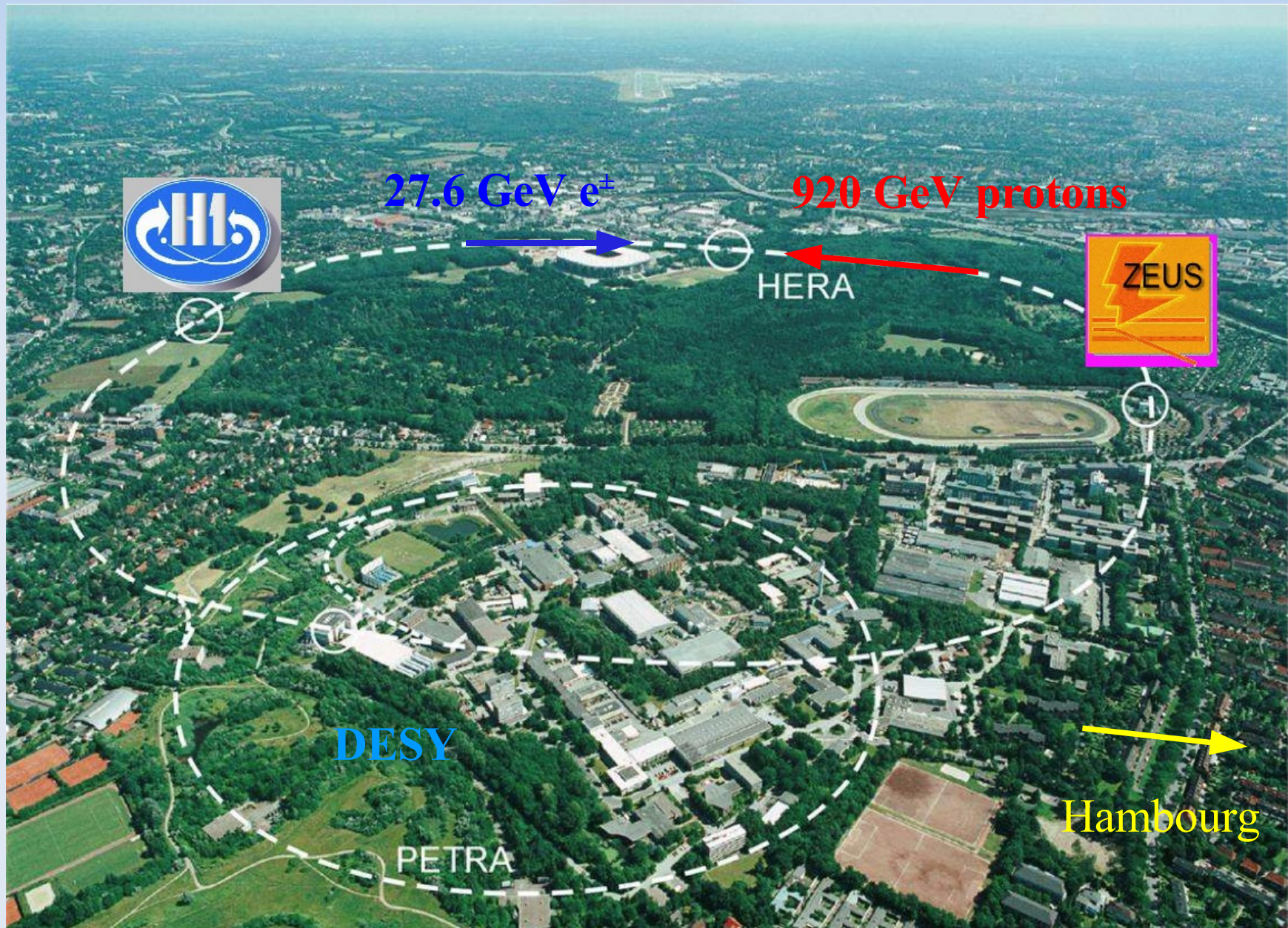
Introduction

- 15 years of ep scattering at high energy
- Main goal: study of proton structure
 - substructures ?
higher 4-momentum transfert \rightarrow smaller distance
 $Q^2 \sim 10^5 \text{ GeV}^2 \rightarrow 10^{-18} \text{ m}$ (1/1000 of the size of the p)
 - understanding of confinement ?
low x \rightarrow screening
- 2 most striking results of HERA from QCD:
 - Strong rise of F_2 at low x
 - Size of diffractive contributions in DIS
- Entering precision measurements:
 - Parton distribution function in the proton
 - α_s
 - Diffraction models
- \rightarrow Many challenges for pQCD

Rem:
No EW
No BSM
results here

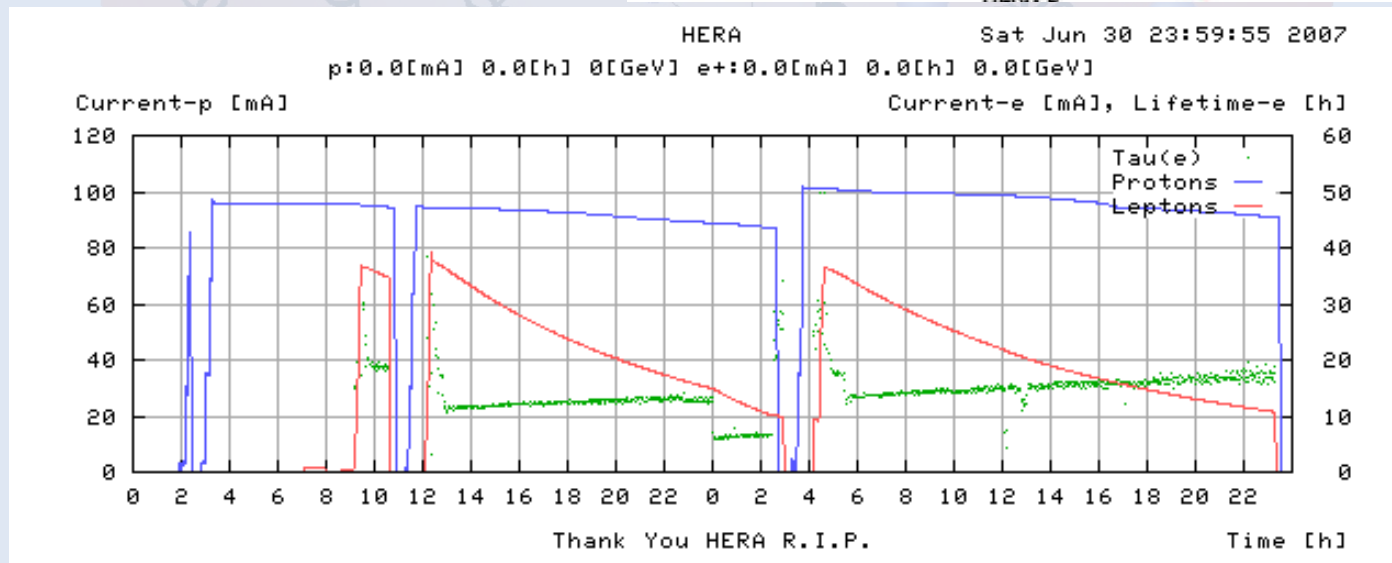
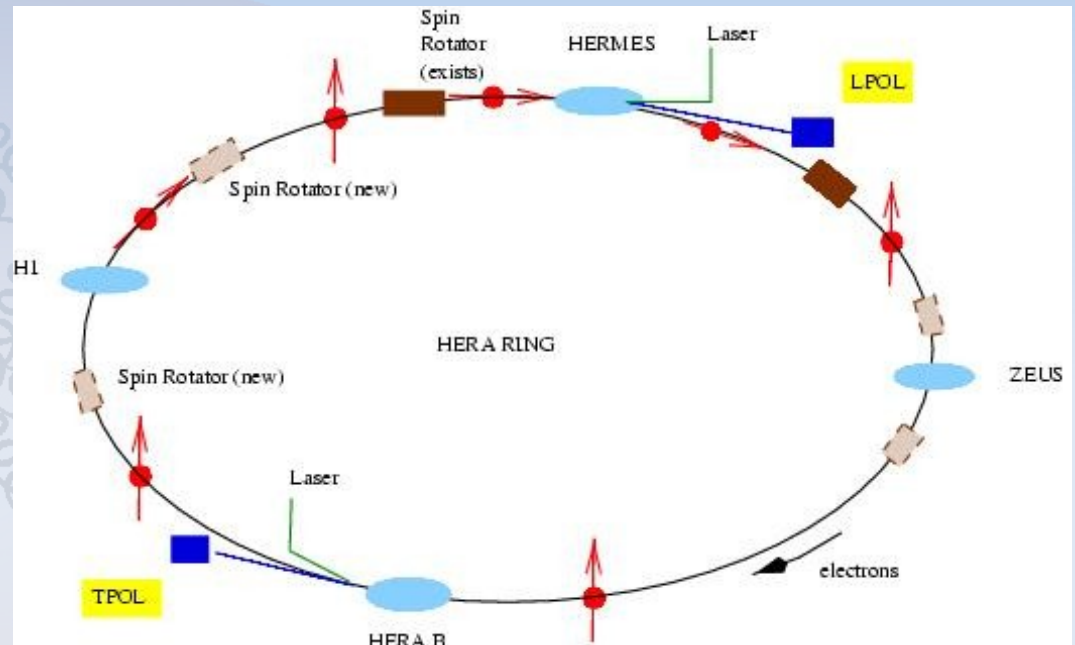


HERA



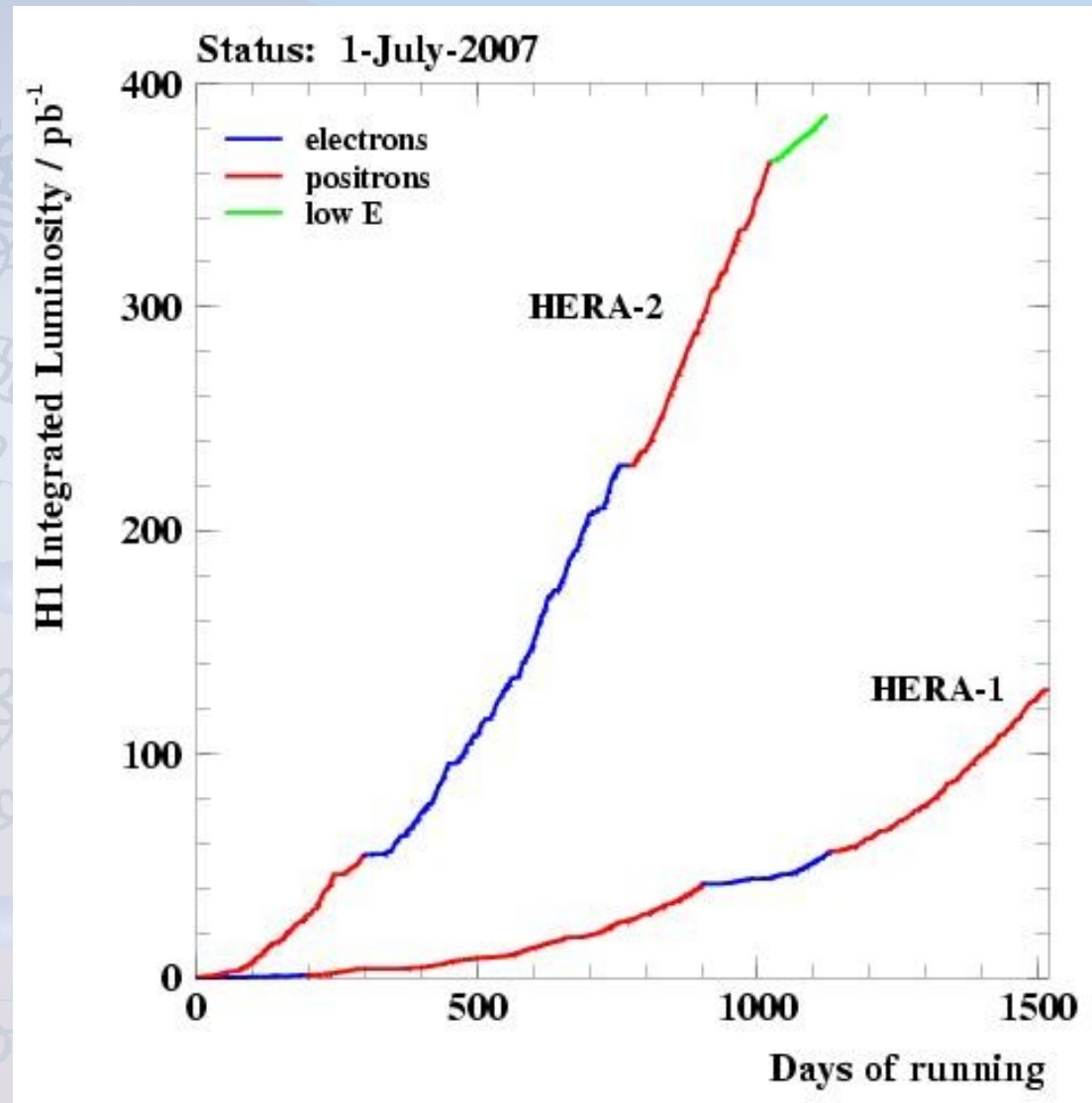
A unique machine

- Only hybrid ep collider
- Start 1992
- Upgrade 2000-2002
 - improved beam focusing
 - longitudinal polarization → H1 & ZEUS
- end 1/7/2007 (-few mins)



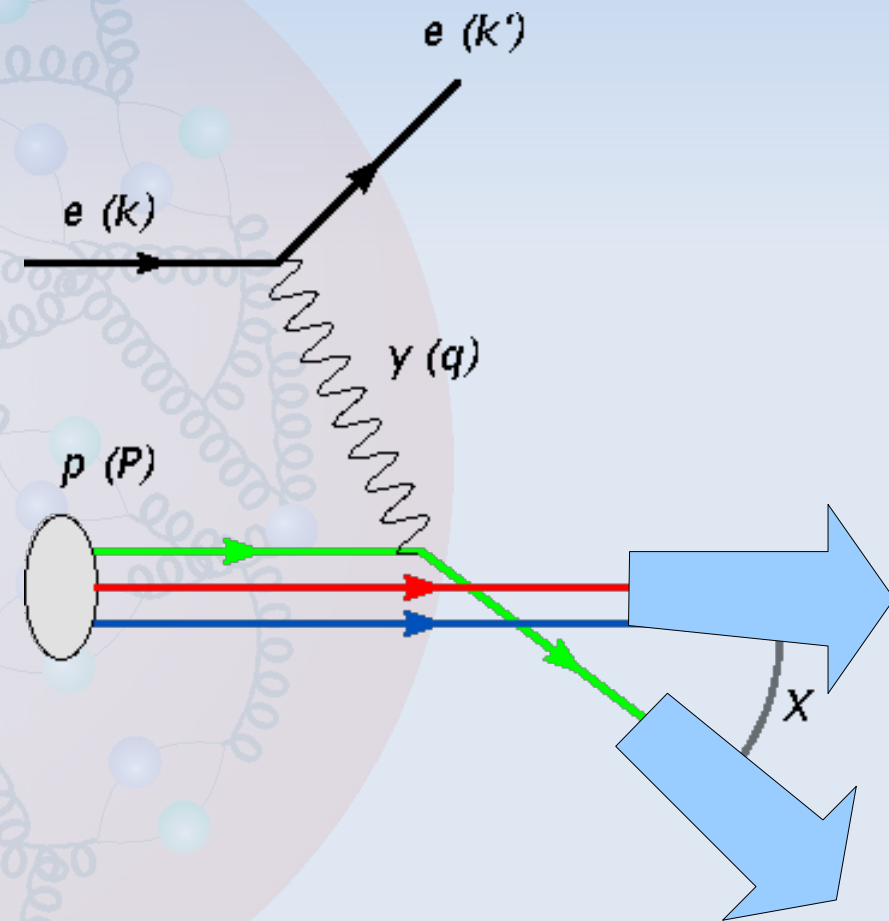
Collected luminosity

- High Energy Running ($\sqrt{s}=300\text{--}320$ GeV)
 - 1992 \rightarrow March 20th, 2007
 - 758 pb^{-1} delivered by HERA
 - ~ 478 pb^{-1} for H1 physics
 - ~ 504 pb^{-1} for ZEUS physics
- Low Energy Running ($E_p = 460$ GeV, $\sqrt{s} = 225$ GeV)
 - 16 pb^{-1} delivered
- Intermediate: ($E_p = 575$ GeV, $\sqrt{s} = 252$ GeV)
 - 8.4 pb^{-1} delivered



DIS kinematics

- $Q^2 = -q^2$
 γ virtuality
- $x = Q^2/2 P \cdot q$
fraction of momentum struck quark
- $y = P \cdot q/P \cdot k = Q^2/xs$
inelasticity (fraction of energy deposited in p rest frame)
- $W = (q+p)^2$
cms energy of the γp system
- 2 indep^t variables inclusive measurement

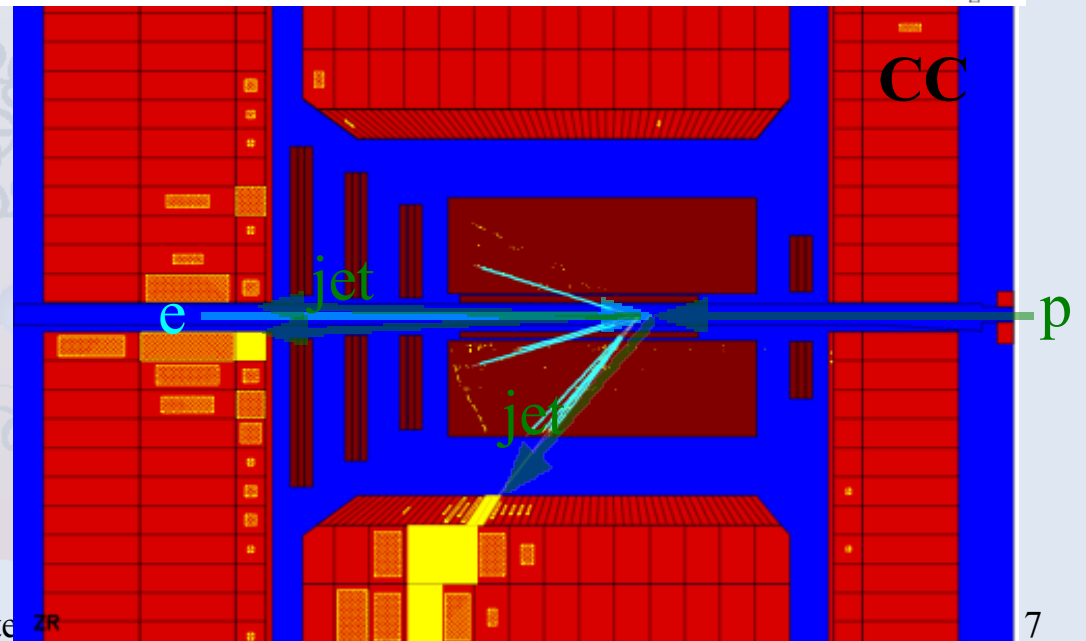
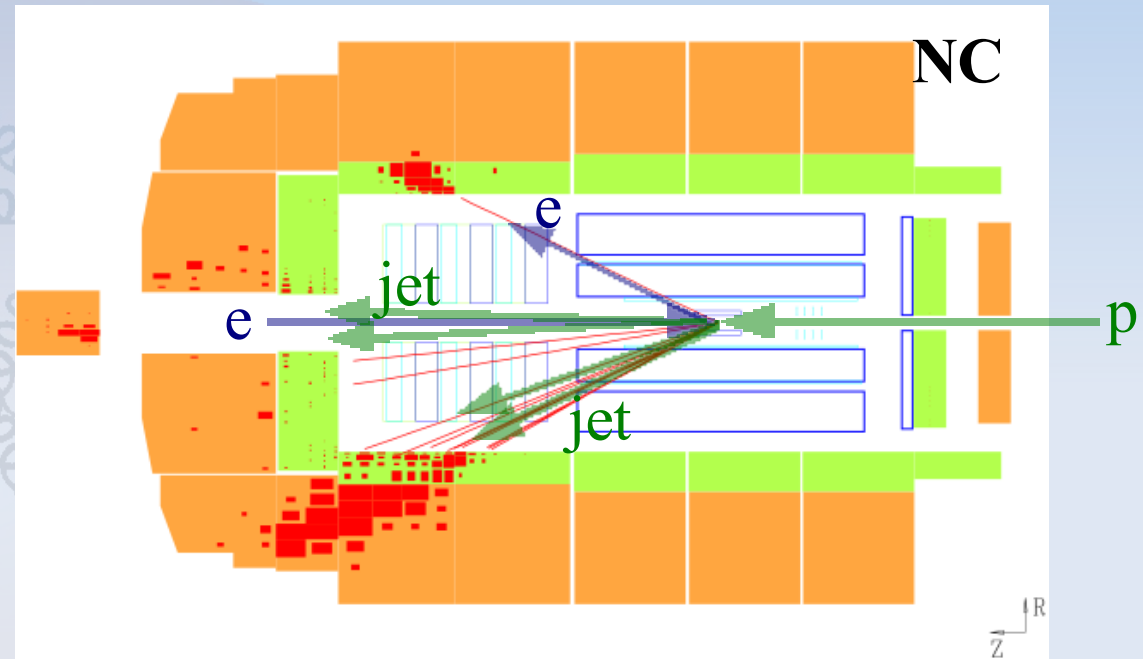


Deep Inelastic Scattering

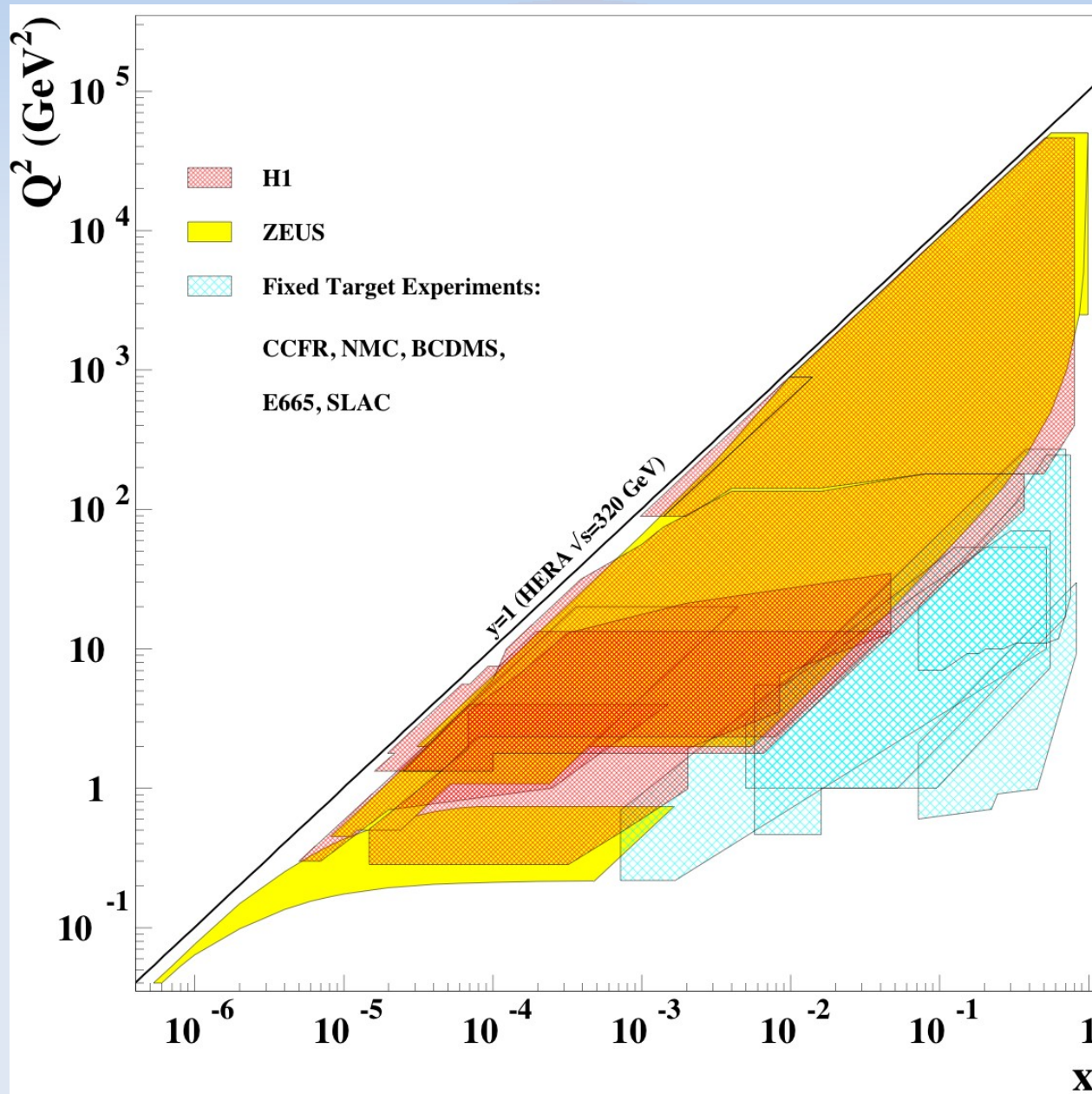
- Main study of HERA
- → inclusive DIS NC & CC

$$\frac{d^2 \sigma(e^\pm p)}{dx dQ^2}$$

- (x, Q^2) from
 - electron (E_e, θ_e)
 - hadrons $((E-Pz)_h, \gamma_h)$
 - combination



Kinematics domain



Proton Structure Functions

$$\frac{d^2\sigma(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[Y_+ F_2(x, Q^2) - y^2 F_L(x, Q^2) \mp Y_- xF_3(x, Q^2) \right] (1 + \delta_r); \quad Y_\pm = 1 \pm (1-y)^2$$

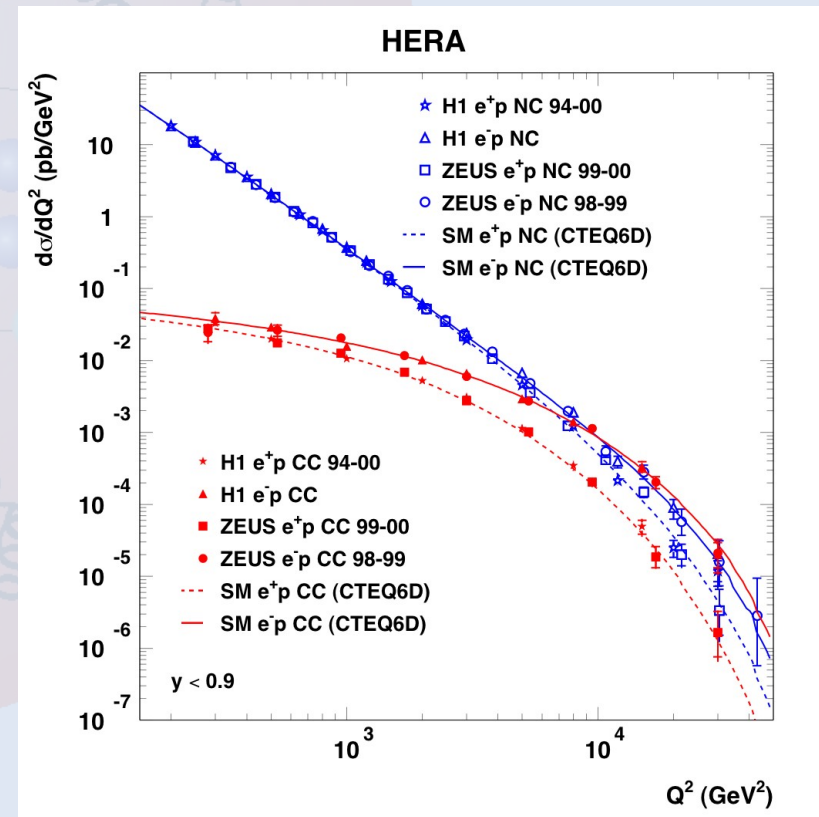
Spin effect

Longitudinal structure function

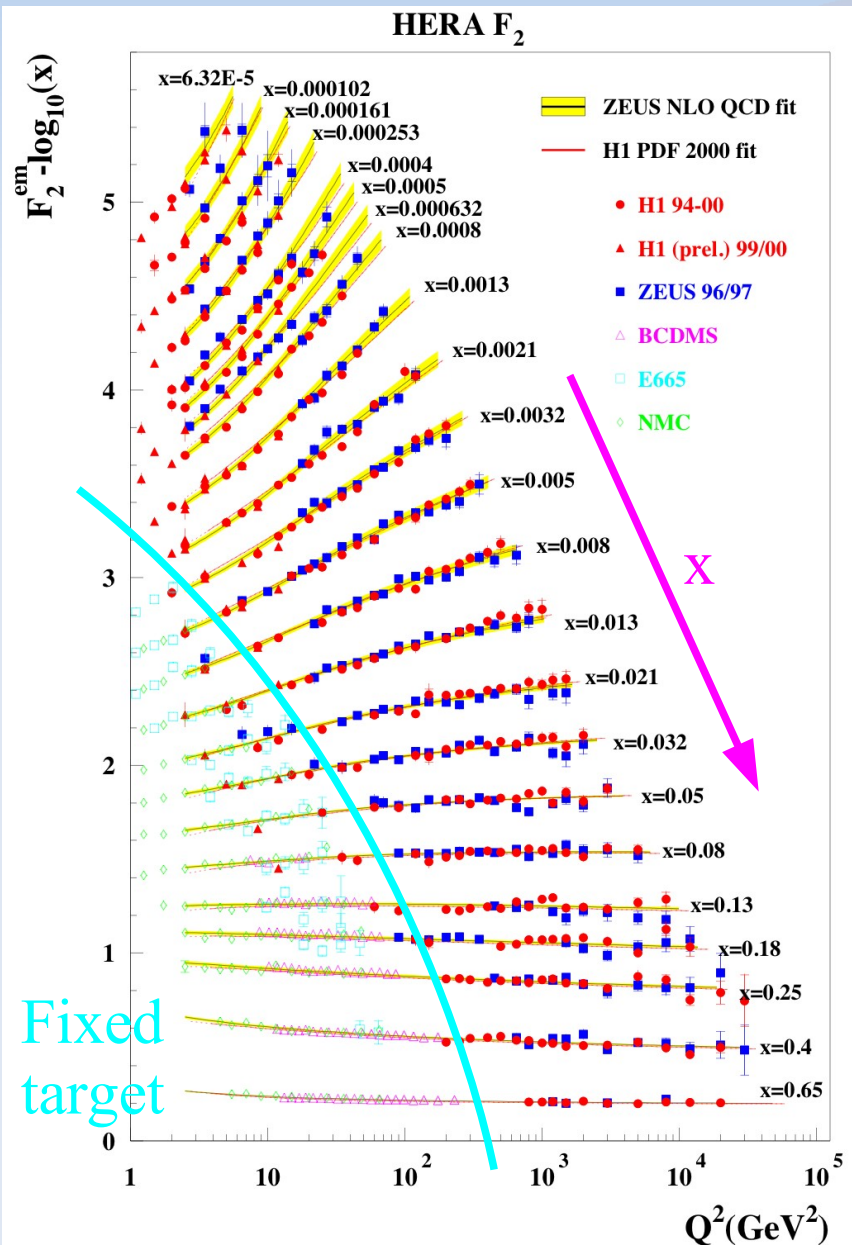
EW contributions

Radiative corrections

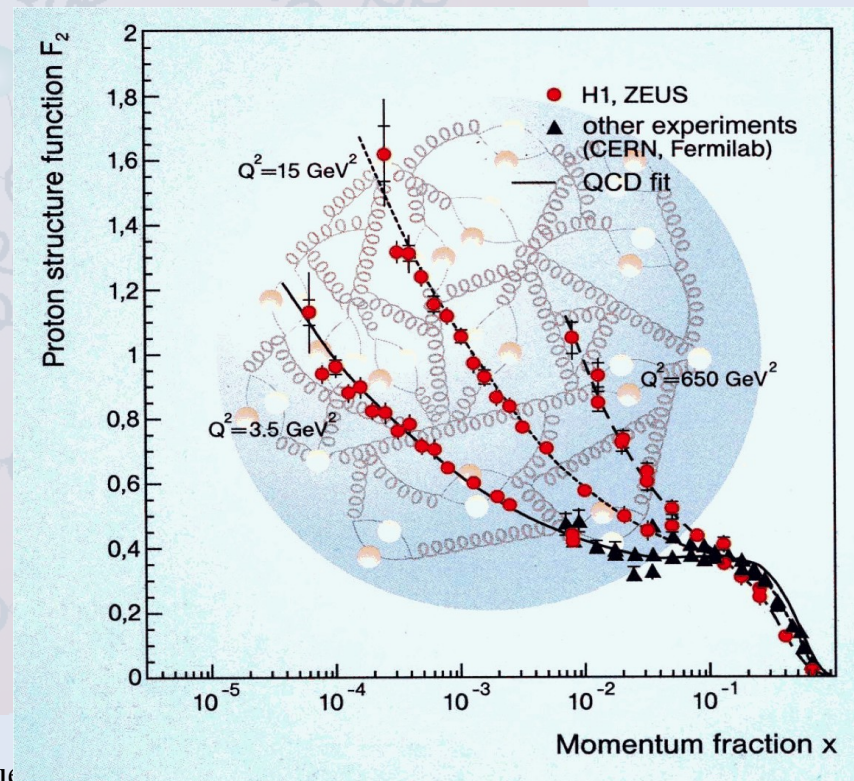
- F_2 dominates in most phase space (esp. pure em coupling)
- F_L contributes at high y
- $F_3 \sim \gamma Z$ interference \rightarrow High Q^2



SF evolution

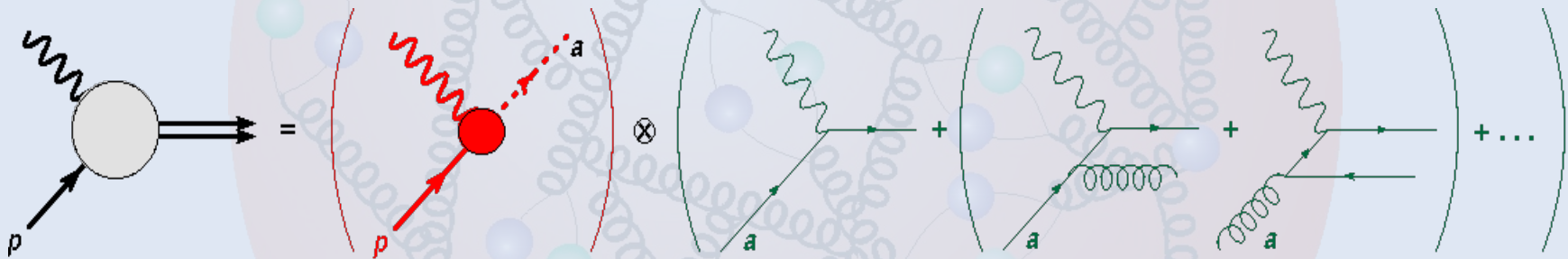


- In the Quark-Parton Model,
 - no Q^2 dependance
- with gluons (& sea quarks):
 - More partons @ High Q^2
 - $\log Q^2$ scaling violation
- The opacity of the proton increases @ low x



Factorization:

- In the Quark-Parton Model: pdf $f_a(x, Q^2) = a(x)$ = probability to find a parton "a" with a fraction x for the proton, at a scale Q^2
 $a = q, \bar{q} (u, d, s, \dots), g$
 - For the pure e.m. part: $F_2(x) = x \sum e_q^2 (q(x) + \bar{q}(x))$
- With QCD:



universal, scale dependent
 Q^2 evolution by DGLAP eqs.

process dependent coeff.
 pQCD in power series of $\alpha_s(Q^2)$

$$F_i(x, Q^2) = \sum_{a=q, \bar{q}, g} f_a(x, Q^2) \otimes C_i^a(x, Q^2)$$

Determination of PDF at HERA

Procedure:

- Parametrization of $a(x)$ at starting scale Q_0^2 : valence q , sea \bar{q} , g with all the constraints (sum rules)
- Evolution of $a(x) \rightarrow f_a(x, Q^2)$ using NL DGLAP equations
- Convolution with pQCD predicted coefficients $\rightarrow \sigma$
- Fit to data (\supset all systematics)

$$\begin{aligned} F_2 &= x \sum e_q^2 (q(x) + \bar{q}(x)) \\ xF_3 &= x \sum 2e_q a_q (q(x) - \bar{q}(x)) \\ \sigma_{e^+p}^{CC} &\sim x(\bar{u} + \bar{c}) + x(1-y)^2(d + s) \\ \sigma_{e^-p}^{CC} &\sim x(u + c) + x(1-y)^2(\bar{d} + \bar{s}) \end{aligned}$$

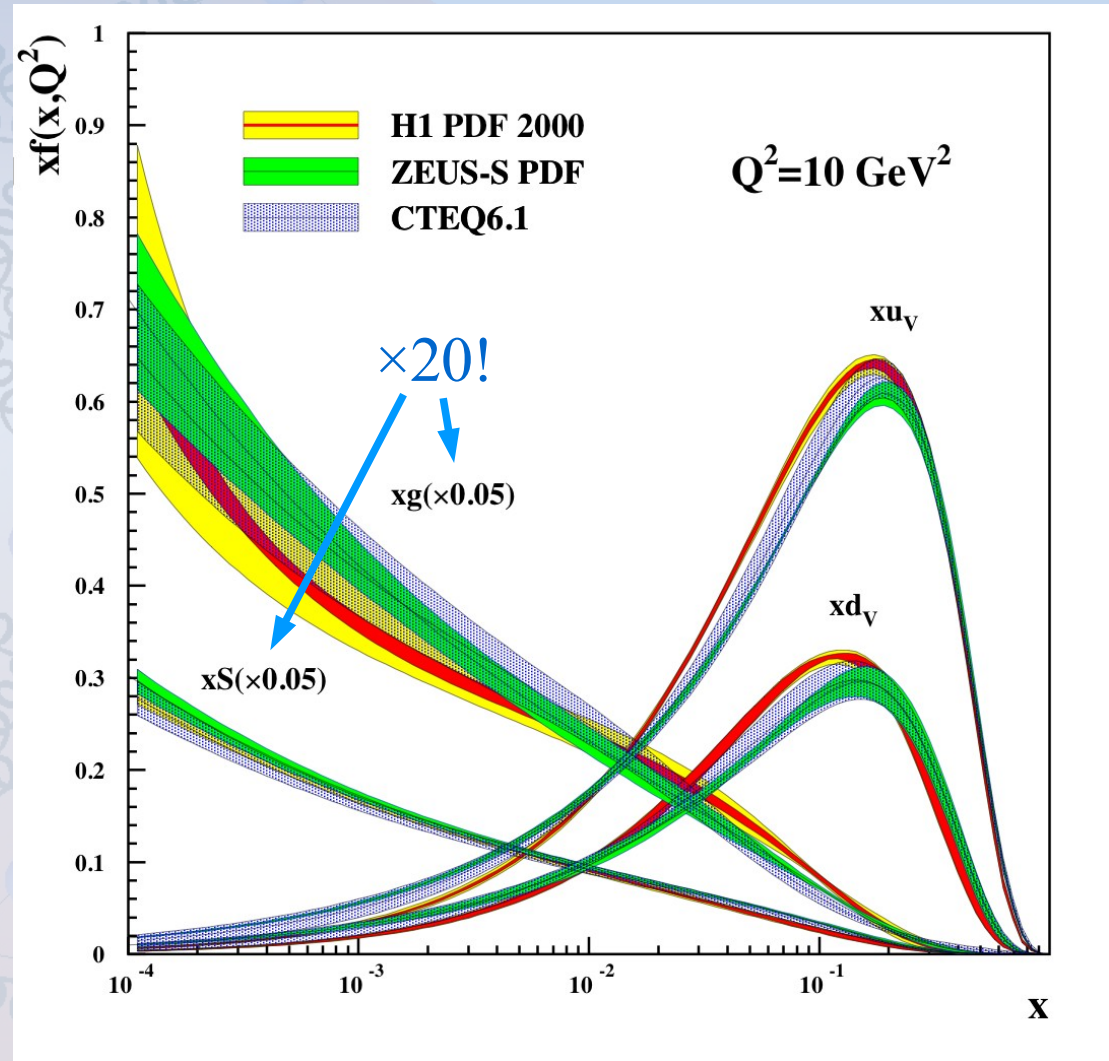
Analyses:

- low Q^2 inclusive NC \rightarrow low x sea and g (indirect from scaling)
- High Q^2 NC & CC inclusive DIS \rightarrow valence quarks density
- Jets production data $\rightarrow g$ at mid x

PDF from NLO Fits

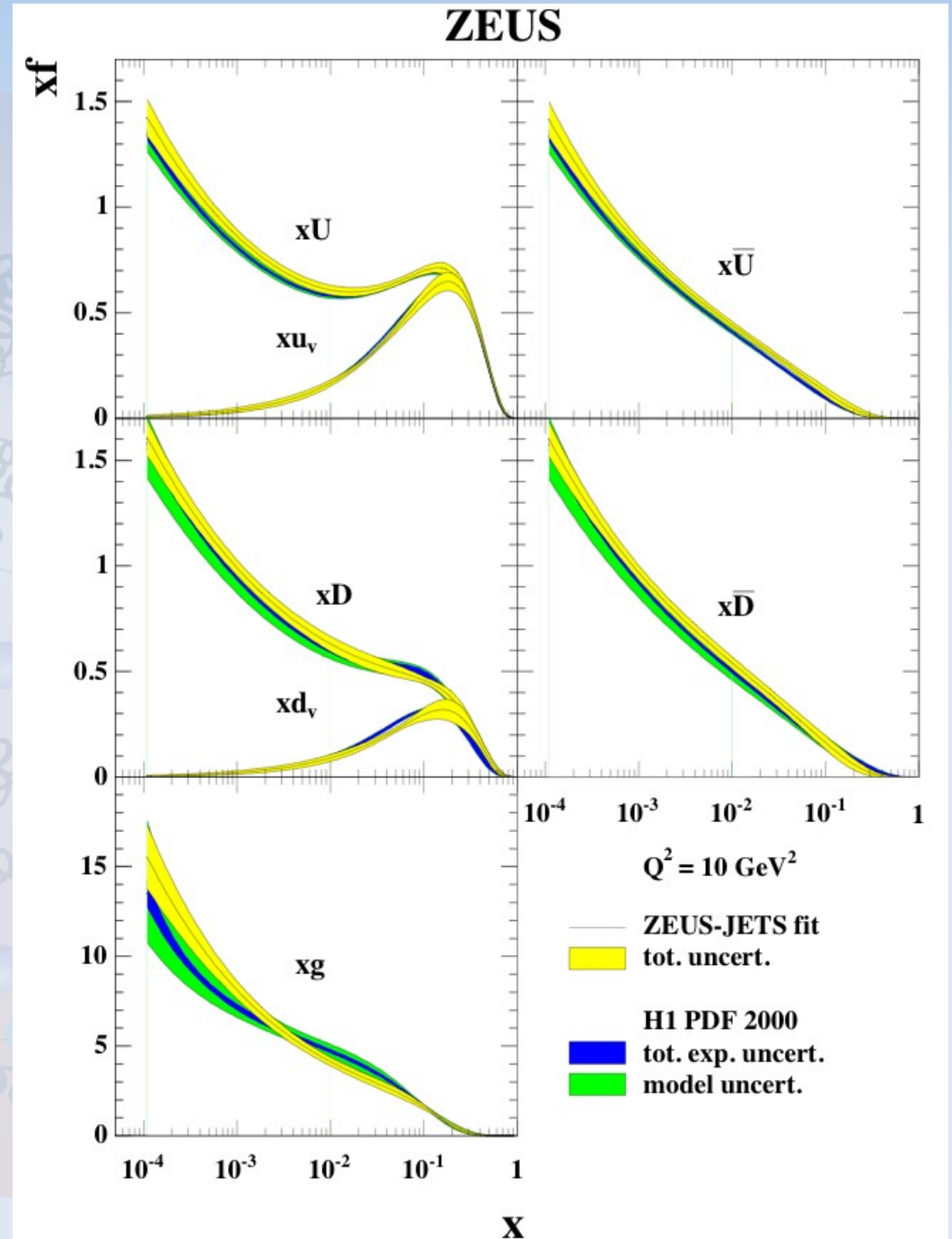
- From F2 data (H1 & ZEUS)
 - HERA-I data
 - well described by fits
 - 1.5–3% precision
- \supset fixed target (ZEUS)
- CC data
 - for valence quark at high x

- Good agreement
- low x dominated by gluons
- LHC ~ gg collider
- expects much improved precision from
- HERA-II data ($e^+p \times 3$, $e^-p \times 10$)
 - \rightarrow 1 – 2% precision
- Combined DIS cross-sections



ZEUS-Jets Fits

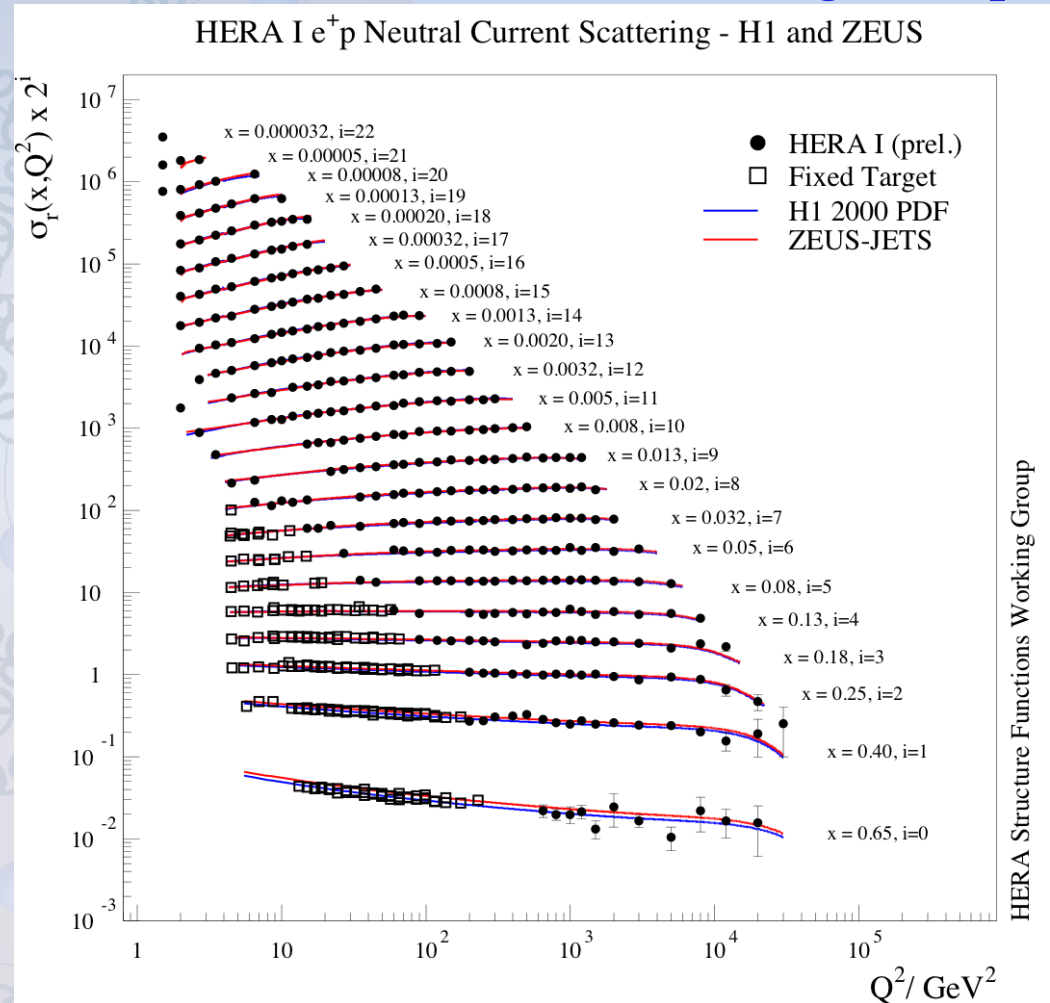
- HERA-I data
- Simultaneous pdf's + α_s
- DIS NC data + jets
 - inclusive jets in DIS
 - dijets in photoproduction
 - $\sim 2\times$ precision on gluons at mid x ($0.01 < x < 0.2$)
- $xU = x(u+c)$; $xD = x(d+s)$



Combined DIS cross-section (H1 & ZEUS)

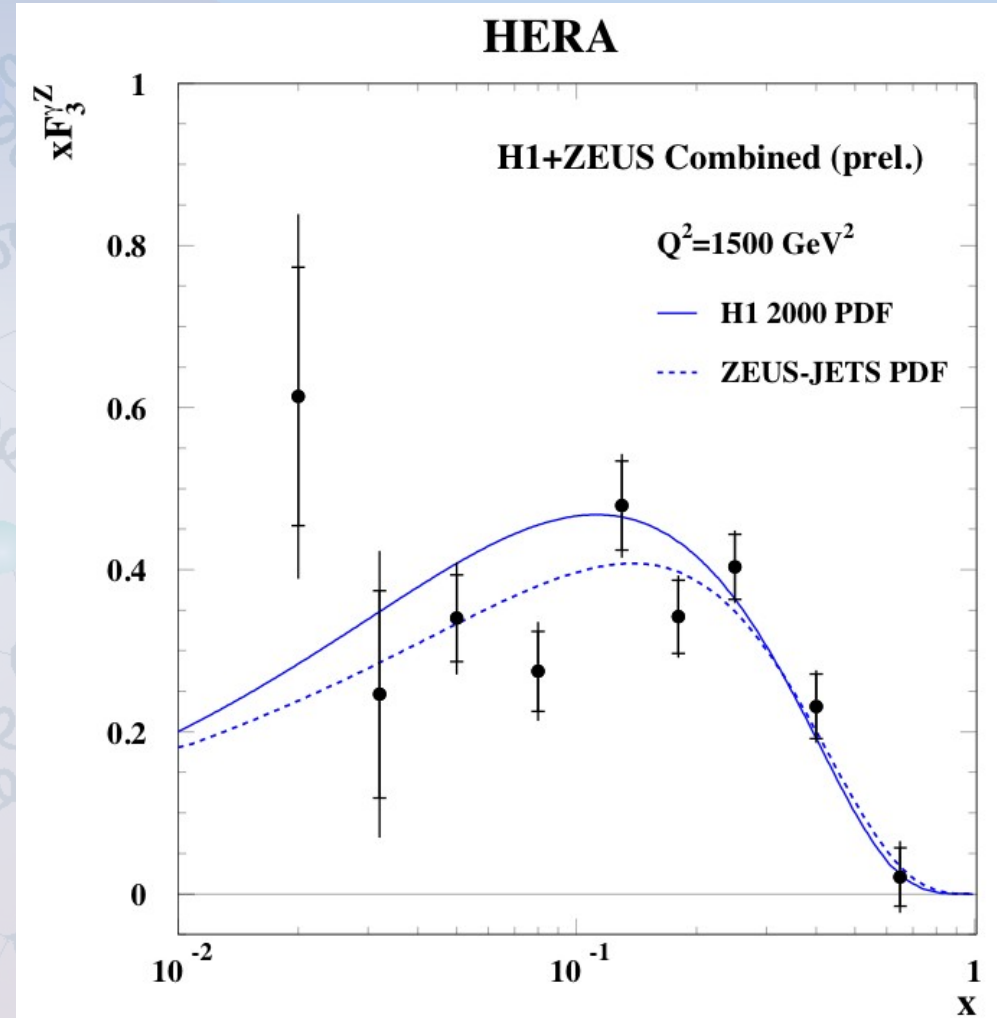
- From HERA-I (1996-2000) published data
- $Q^2 > 1.5 \text{ GeV}^2$
- Coherent approach of syst. error correlation
- Constraint due to X-calibration
→ Precision gain > pure stat. :
×2 (not $\sqrt{2}$)
- First step to more combinations
 - inclusion of HERA-II
 - pdf, QCD fits, ...

HERA Structure Functions Working Group



Combined xF_3

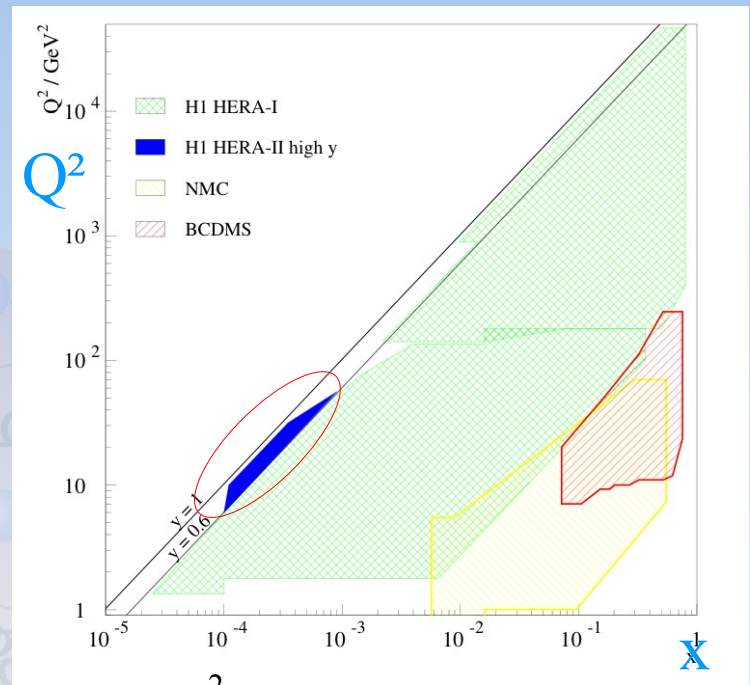
- First combined SF
Combination of H1+ZEUS DIS
NC cross-sections
- $xF_3 \propto \sigma(e-p) - \sigma(e+p) \propto 2u_v + d_v$
→ measure of valence quarks
- $200 < Q^2 < 30000 \text{ GeV}^2$
- $\mathcal{L} = 478.8 \text{ pb}^{-1}$
(HERA-I H1+ZEUS)
- Good agreement with pdf
 - esp. no increase at low x
(sea q contributions ~ 0)



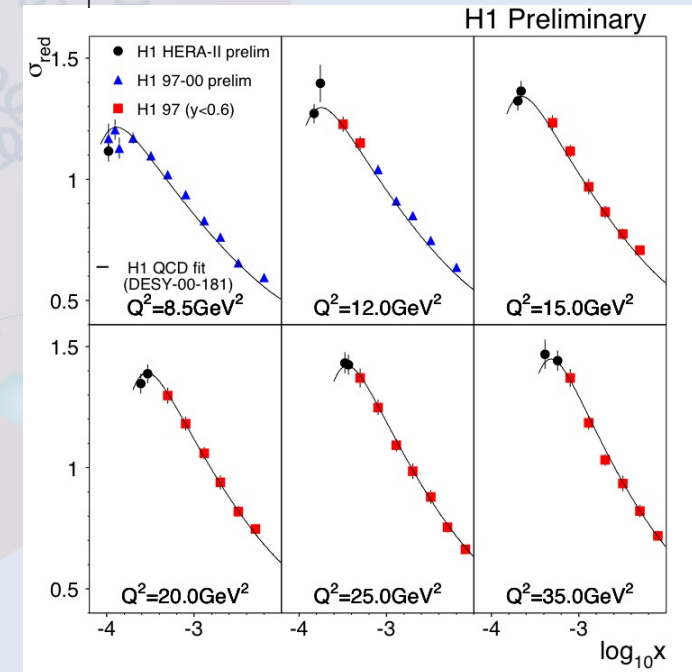
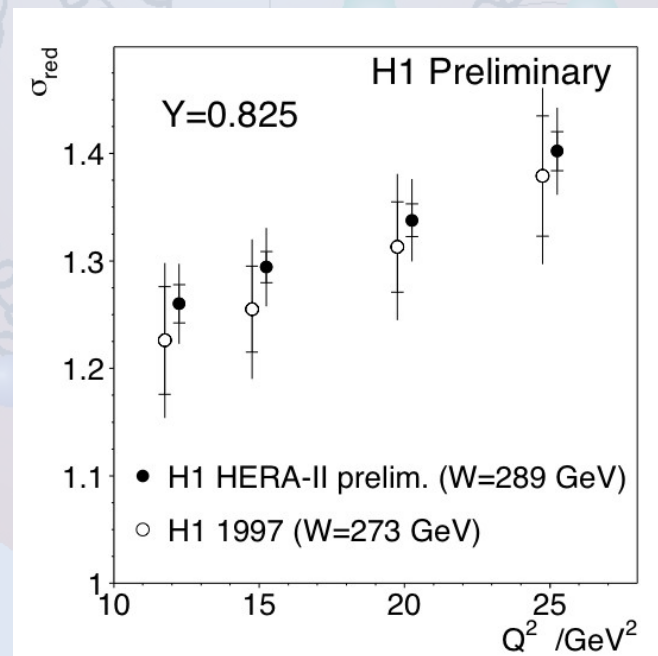
High y

- 2003-2006 data ($e^{\pm}p$ data)
 - $\mathcal{L} = 96 \text{ pb}^{-1}$
- $12 \text{ GeV}^2 < Q^2 < 150 \text{ GeV}^2$
- $0.75 < y < 0.9$
- High Sensitivity to F_L
 - \rightarrow constrains on DGLAP
 - $F_L \sim xg$

- $2\times$ precision wrt previous data
- \rightarrow prepares for low E F_L determination



$$\sigma_{\text{red.}} = F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2)$$

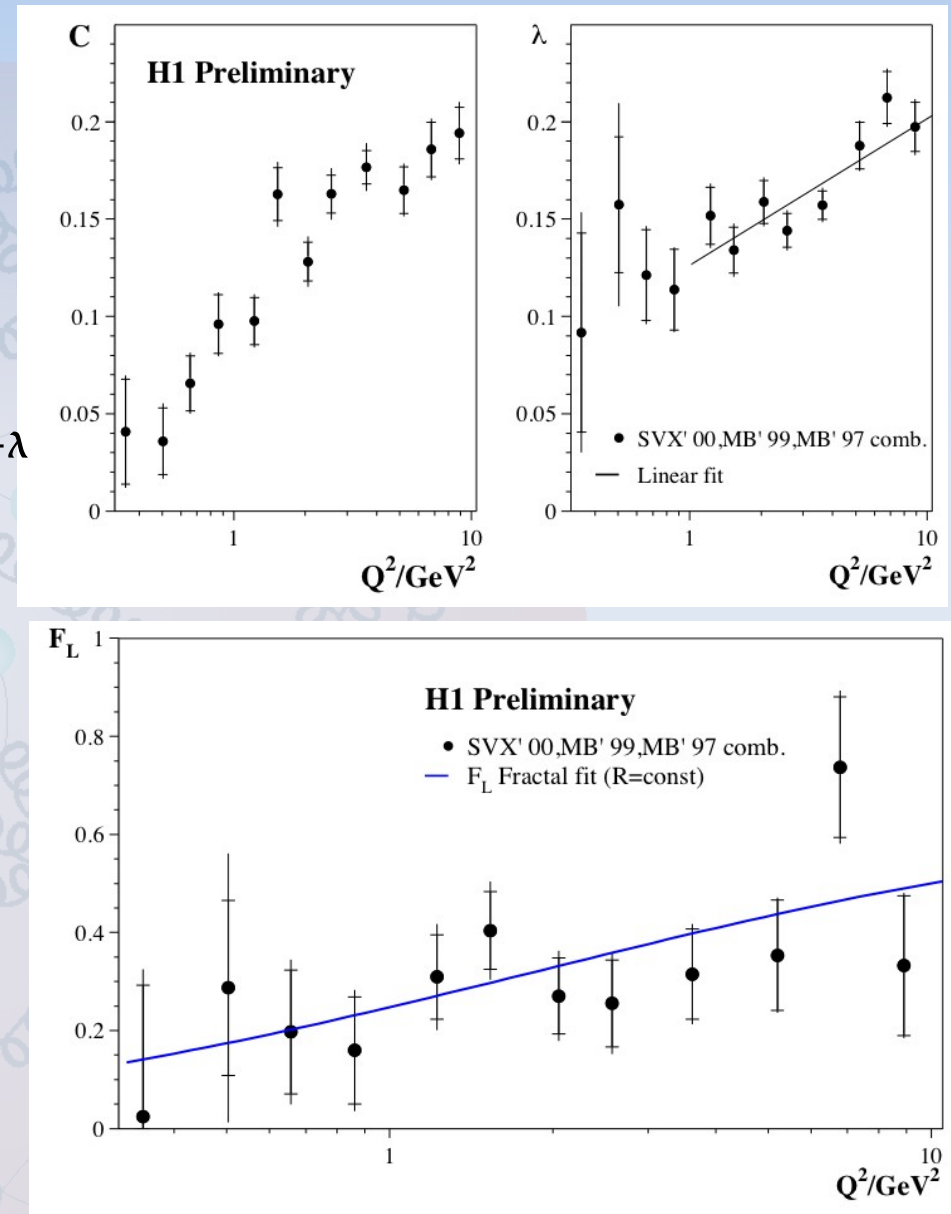


low x , low Q^2 measurement

- High precision from special run in 99/00
 - shifted vertex \rightarrow lower θ_e
 - minimum bias trigger
- $0.2 < Q^2 < 12 \text{ GeV}^2$
- $4 \cdot 10^{-6} < x < 0.02$
 - \supset data with $y < 0.85$
 - \rightarrow sensitivity to F_L
- 2-3% precision

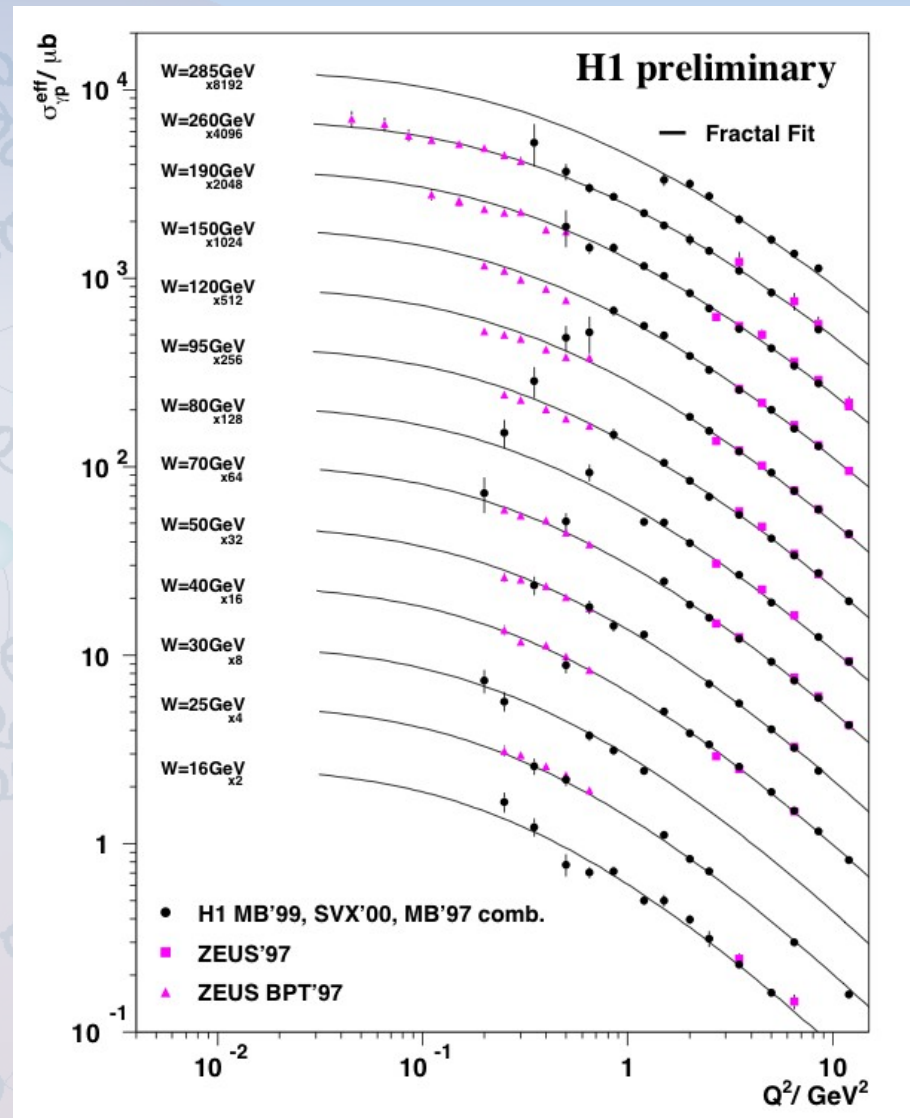
$$F_2 \propto C x^{-\lambda}$$

- Extended kin. domain (lower Q^2 , larger x) by use of radiative correction
- \rightarrow transition to the soft QCD
 - empirical predication: fractal fits, power laws



low Q^2 measurements

- At low Q^2 ,
 - $F_2 \sim \sigma_T + \sigma_L$
 - $F_L \sim \sigma_L$
- New preliminary measurement of $\sigma_{\text{eff.}} = \sigma_T + [1 - y^2 / (1 + (1 - y)^2)] \sigma_L$
- Fill the gap to photoproduction



Measures of $\alpha_s(M_Z)$

- Many methods:

- Scaling violations $\left(\frac{\partial F_2}{\partial \ln Q^2}\right) \propto \alpha_s [P \otimes g + P \otimes F_2]$

- exclusive states (jets cross-sections, jet properties)

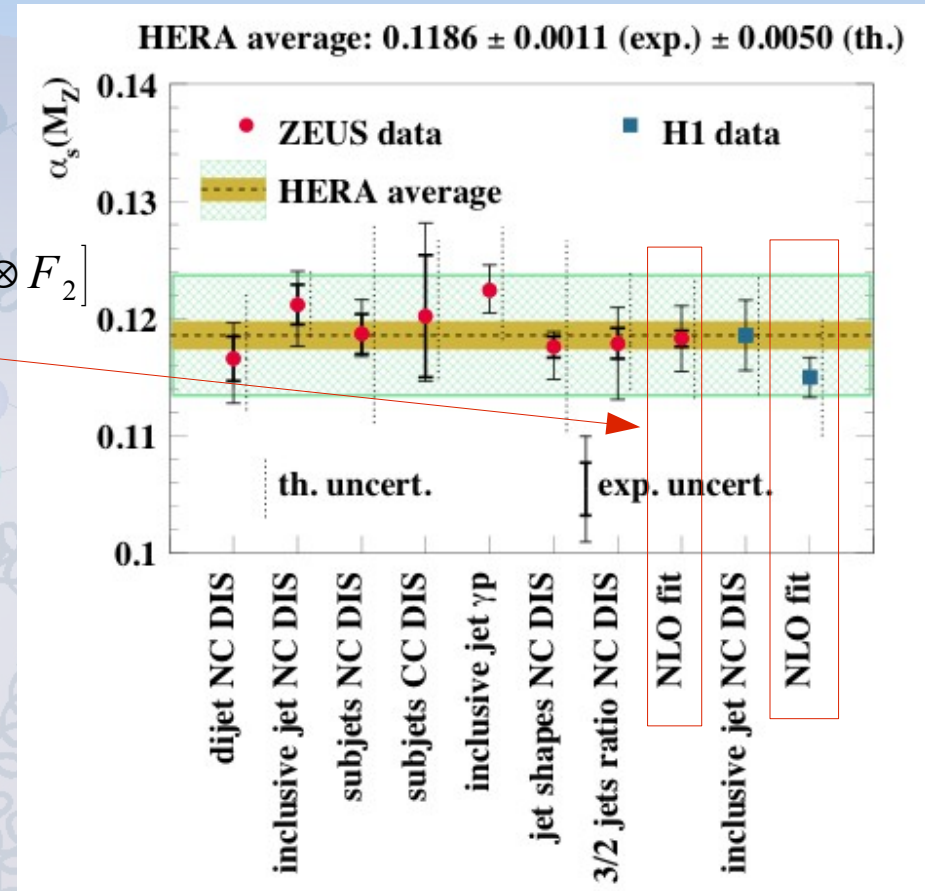
- combined values to NLO

- All in good agreement

- Dominated by th. errors

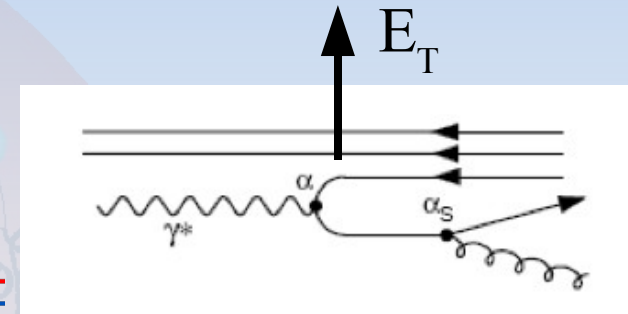
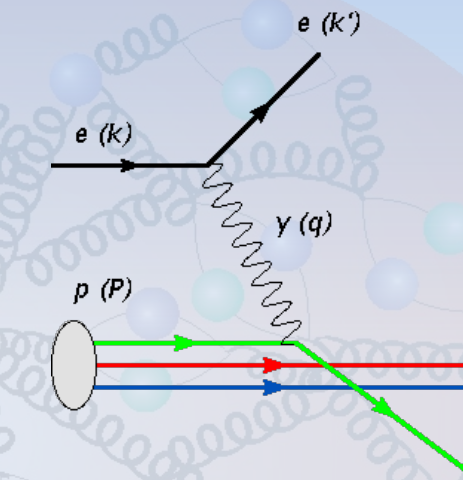
$$\alpha_s(M_Z) = 0.1186 \pm 0.0011 \text{ (exp)} \pm 0.005 \text{ (th)} \text{ (H1 + ZEUS)}$$

$$\rightarrow \alpha_s(M_Z) = 0.1189 \pm 0.0010 \text{ (world average, Bethke 2006)}$$



α_s from Inclusive jets X-sections in NC DIS

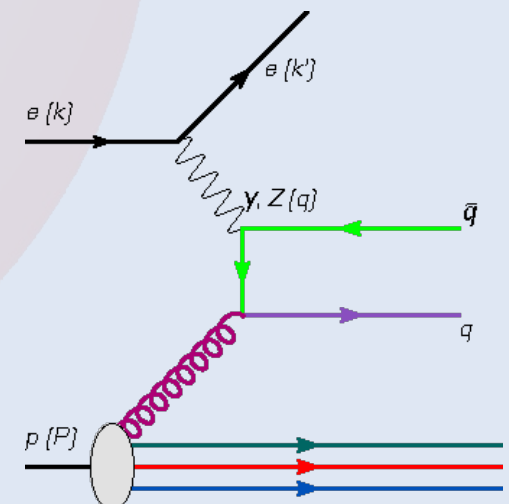
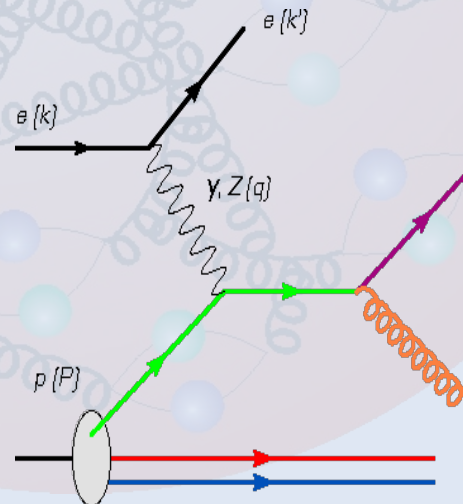
- High E_T jets
 - low experimental uncertainty
 - calc. in pQCD
- In the Breit frame (γ -p cms):
 - suppr. direct DIS (Born process)
 - suppr. of p remnants
- longitudinally inv. k_T jet algorithm
 - IR safe,
 - parton / hadron equi.
- Inclusive jets (\neq di-jets)
 - reduced th. uncertainties
 - IR safe
- NLO calc
 - low theoretical uncertainty



Leading Order:

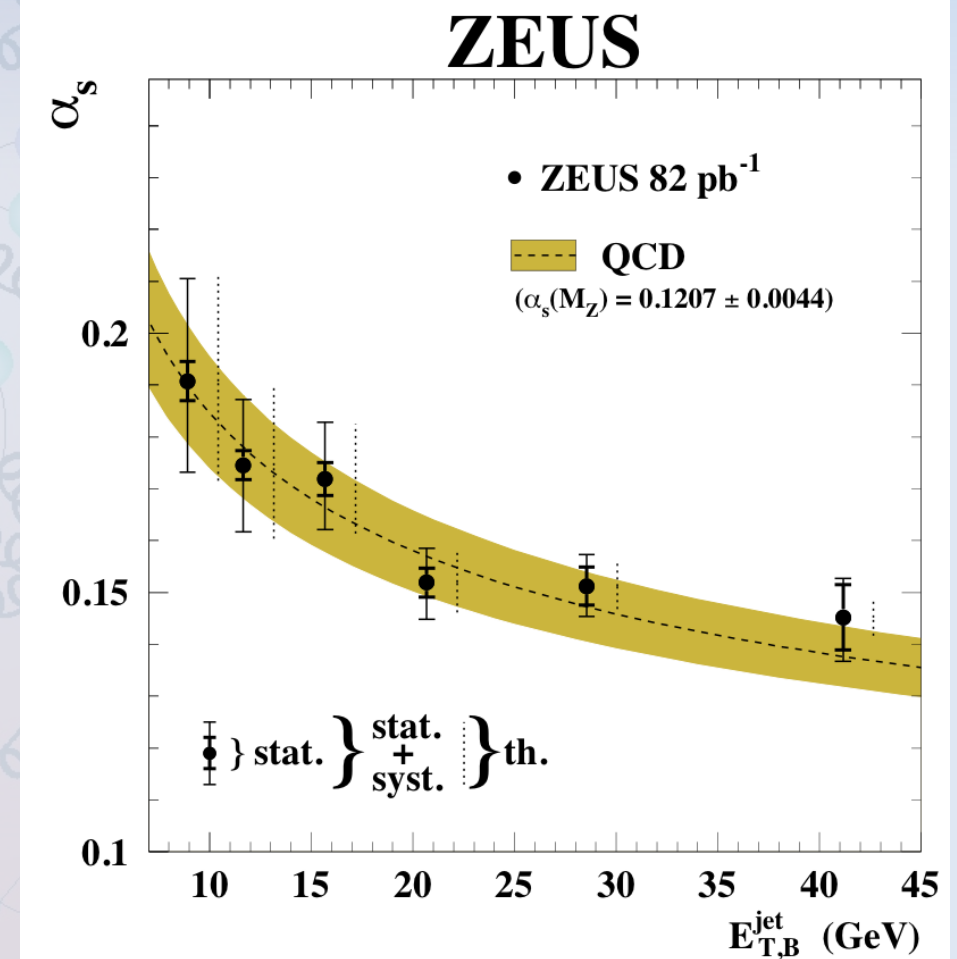
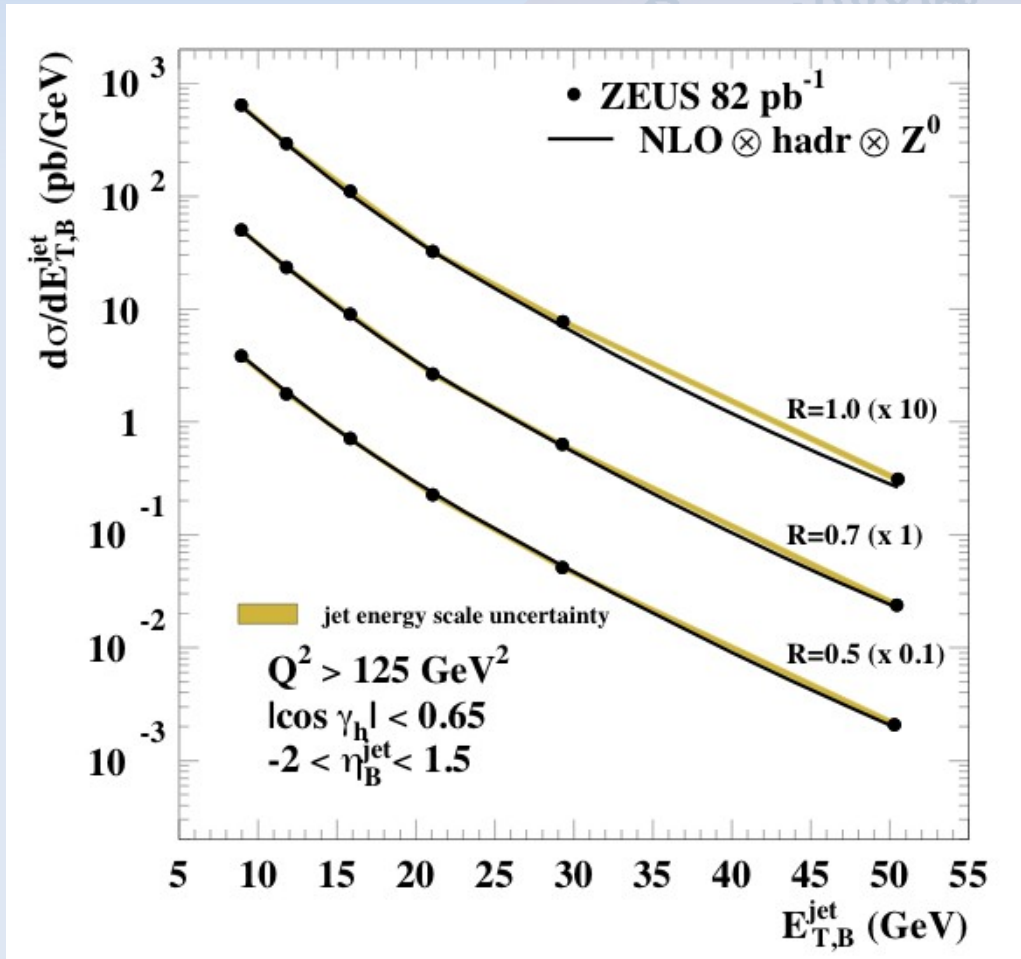
QCD Compton

Boson-Gluon Fusion



Jets inclusive in NC DIS (ZEUS)

- Agreement for different jet Radius R
- E_t^{jet} = running scale for α_s

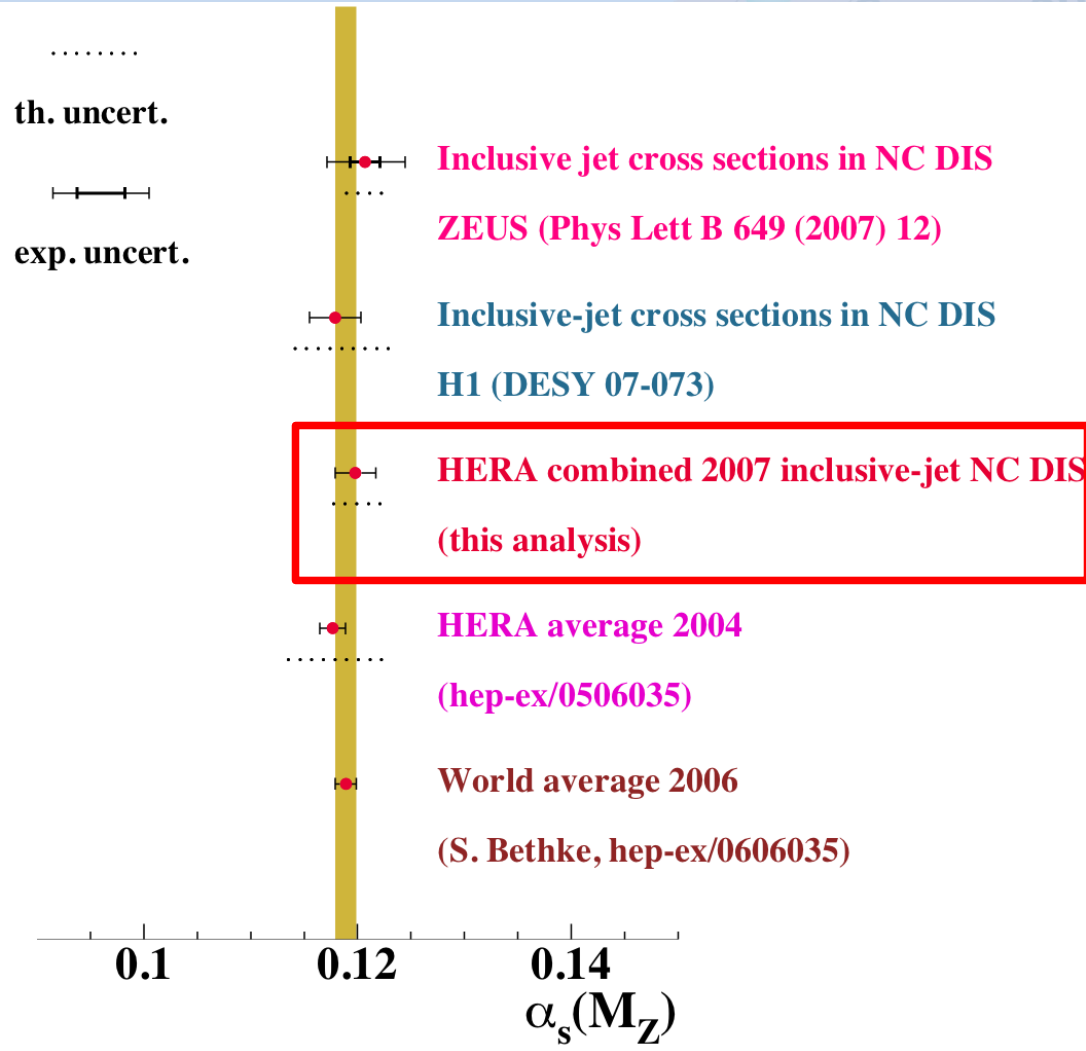


HERA 2007 combined α_s



HERA α_s Working Group

**H1 and ZEUS
Collaborations**



Combine *data* of

DIS NC inclusive jets from

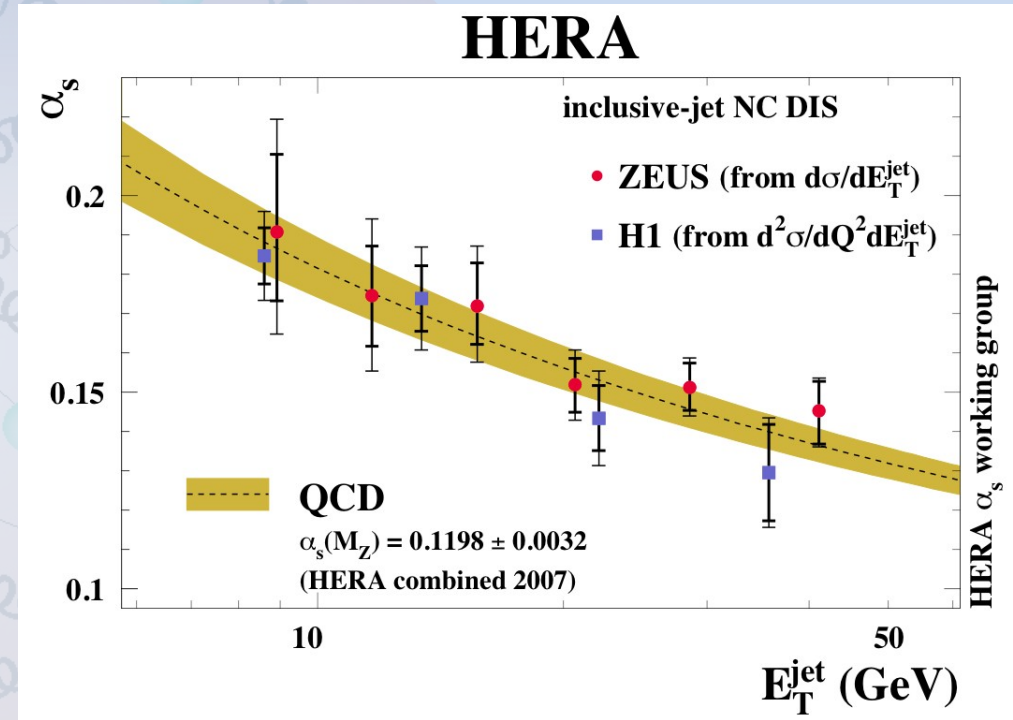
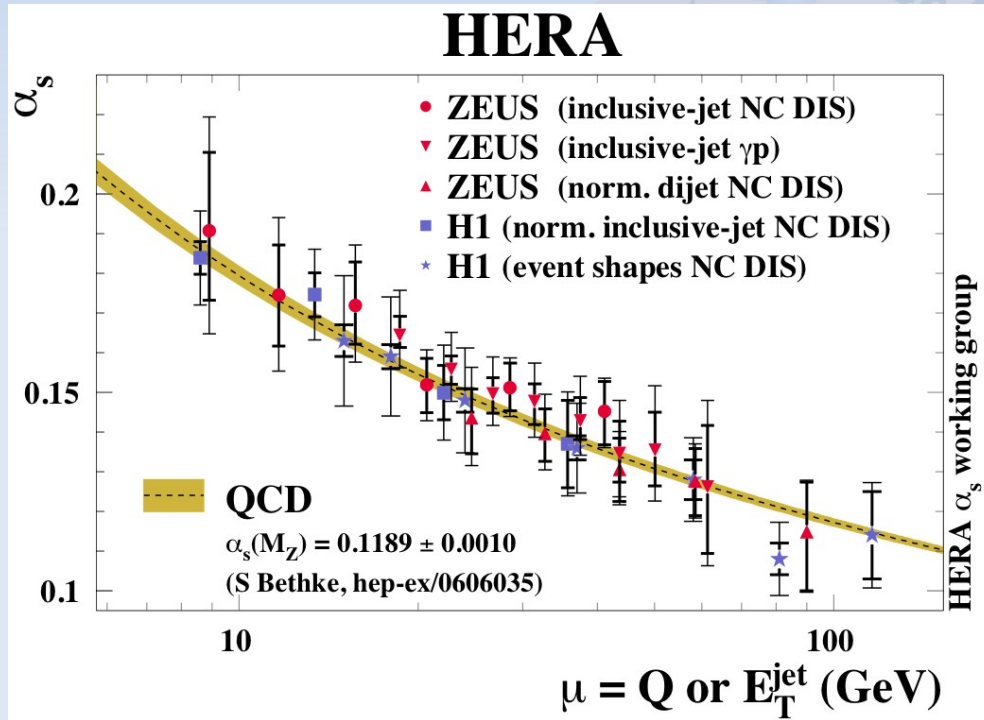
- ZEUS [Phys. Lett. B649(2007)12]
- H1 [hep-ex/0706.3722]

Consistent measurement

- **$0.1198 \pm 0.0019(\text{exp}) \pm 0.0026(\text{th})$**
- $0.1186 \pm 0.0011(\text{exp}) \pm 0.0050(\text{th})$
- 0.1189 ± 0.0010

Running of α_s ...

... from HERA data alone



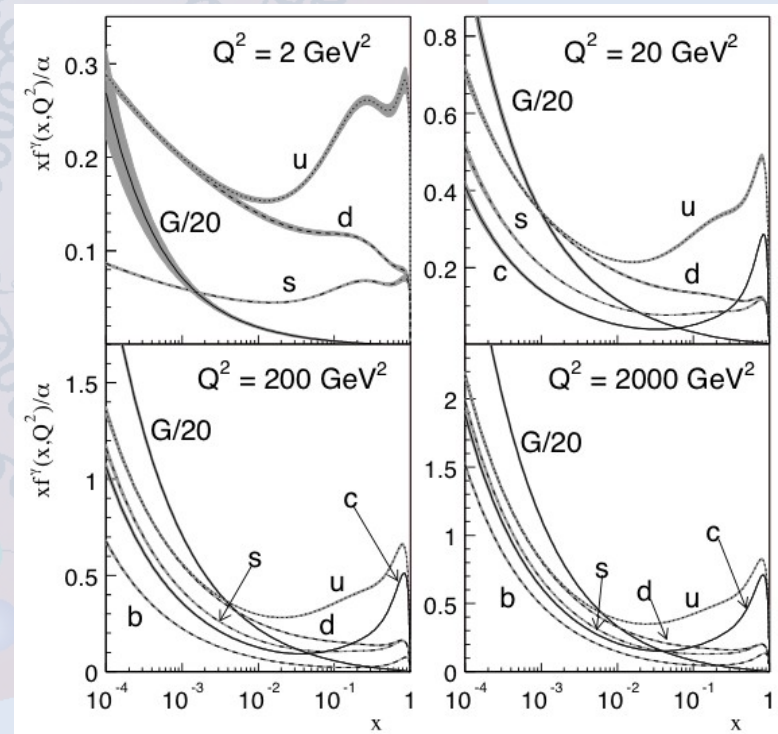
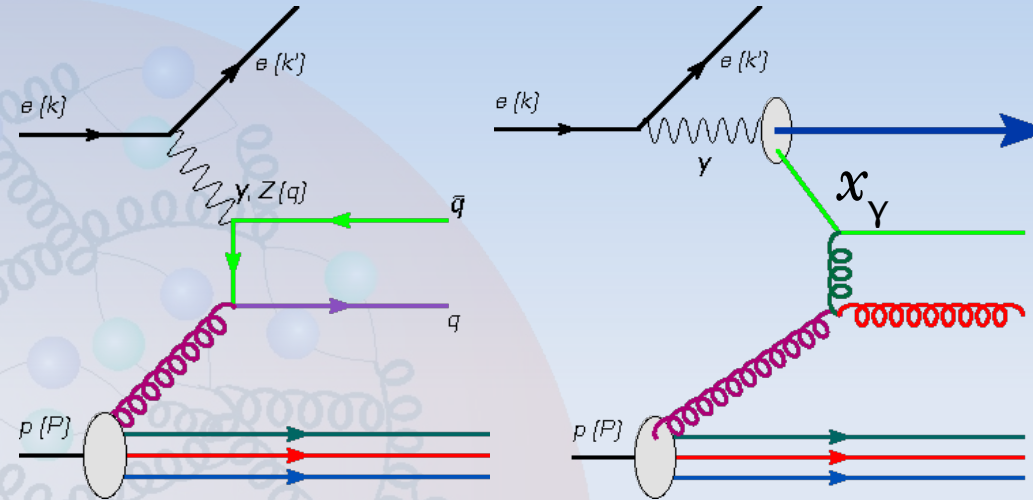
High E_T jets in photoproduction ($Q^2 \sim 0$)

- parton density in the photon
- Gluon in the protons

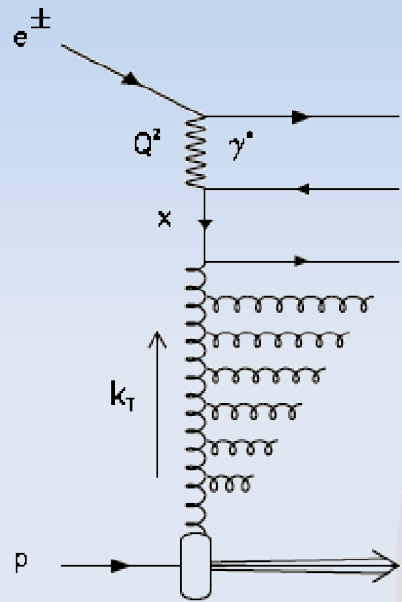
- kin:
 - $Q^2 < 1 \text{ GeV}^2$
 - $142 < W_{\gamma p} < 293 \text{ GeV}$
 - $E_{\text{jet } 1(2)} > 20 \text{ (15) GeV}$
 - $-1 < \eta_{\text{jet}} < 3$ and $-1 < \eta_{\text{jet}} < 2.5$
- 82 pb⁻¹ (98-00 data)

- High E_T 2j with
 - $\gamma\gamma^* \rightarrow \text{hadrons (ee)}$,
 - low- x $\gamma^*p \rightarrow \text{hadrons}$

→ pdf in photons



BFKL vs DGLAP

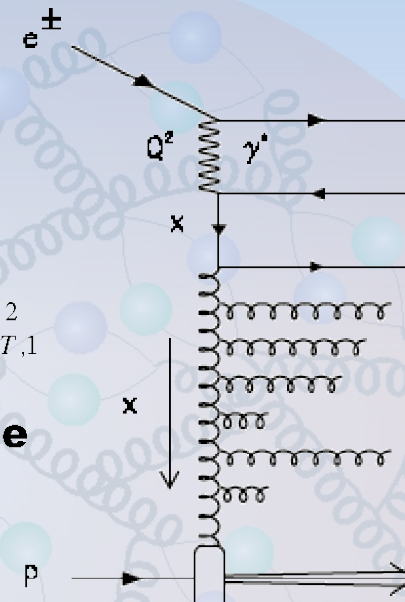


DGLAP

Evolution & resummation
in powers of $\ln Q^2$

$$Q^2 \gg k_{T,n}^2 \gg \dots \gg k_{T,2}^2 \gg k_{T,1}^2$$

**The DGLAP gluon cascade
is strongly ordered in k_T
and ordered in x**



BFKL

Evolution & resummation
in powers of $\ln(1/x)$

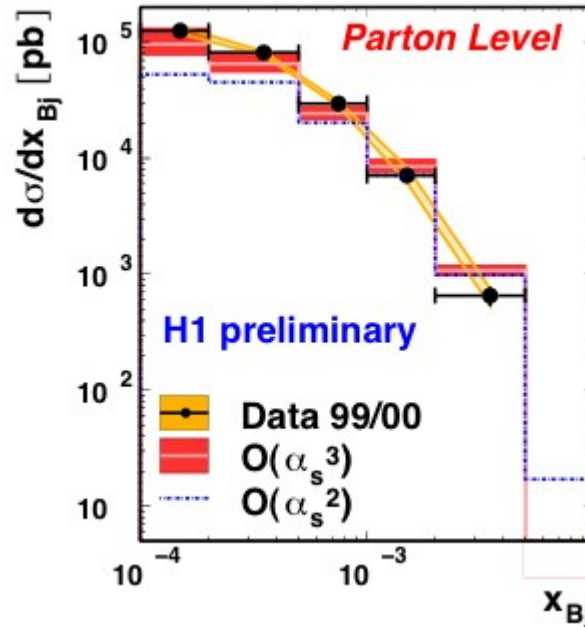
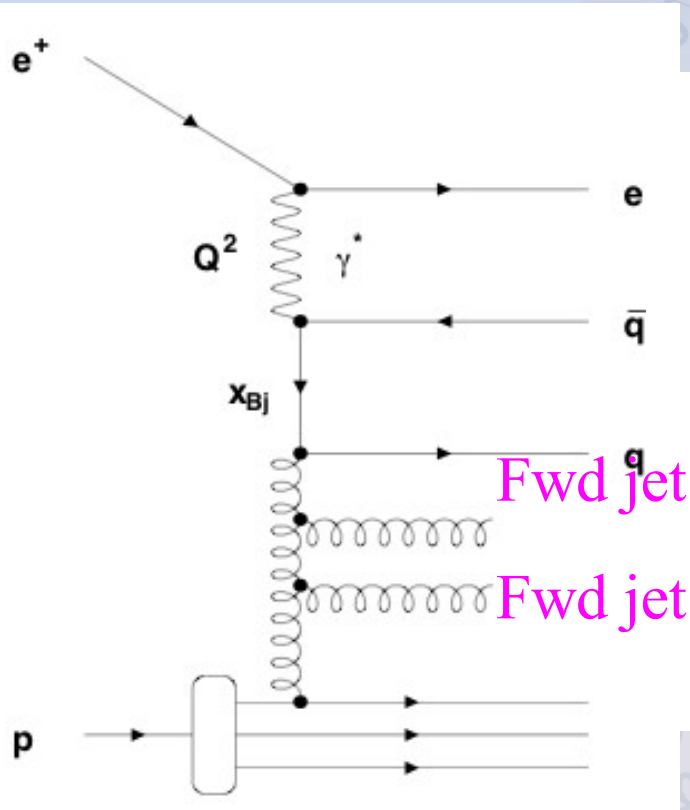
$$x_1 \gg x_2 \gg \dots \gg x_n \gg x$$

**The BFKL is only
strongly ordered in x**

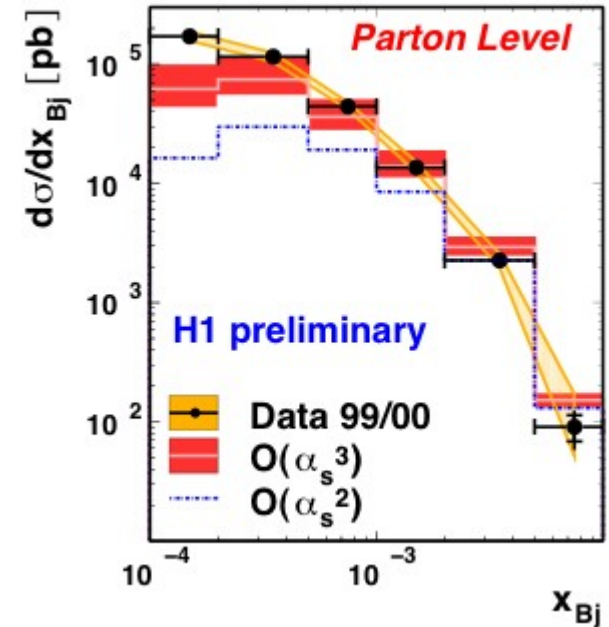
- **DGLAP** (Dokshitzer-Gribov-Lipatov-Altarelli-Parisi) is expected to break down at low x and Q^2 region
- **BFKL** (Balitsky-Fadin-Kuraev-Lipatov) can be applicable at low x
- **CCFM** (Ciafaloni-Catani-Fiorani-Marchesini) describes an evolution in both Q^2 and x and approaches BFKL at low x and DGLAP at high Q^2 ; angular ordering

First hints of a breakdown of DGLAP

- 3 jets dynamic at low x and low Q^2



2 central jets

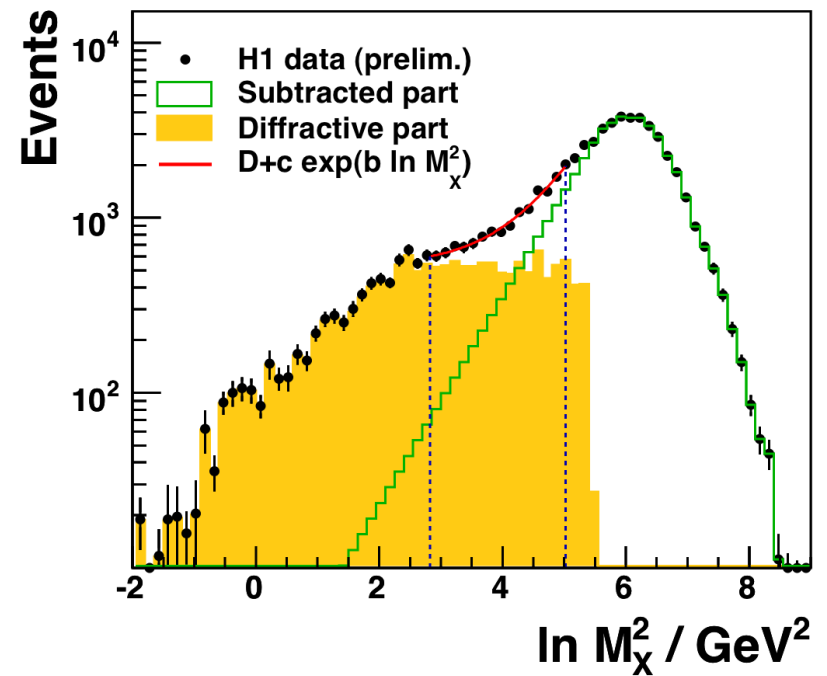
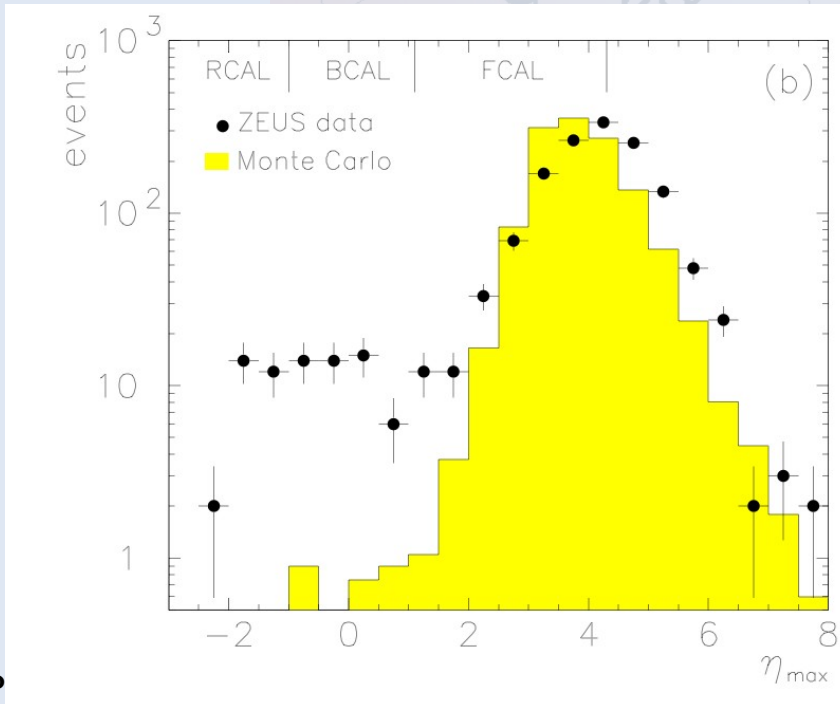
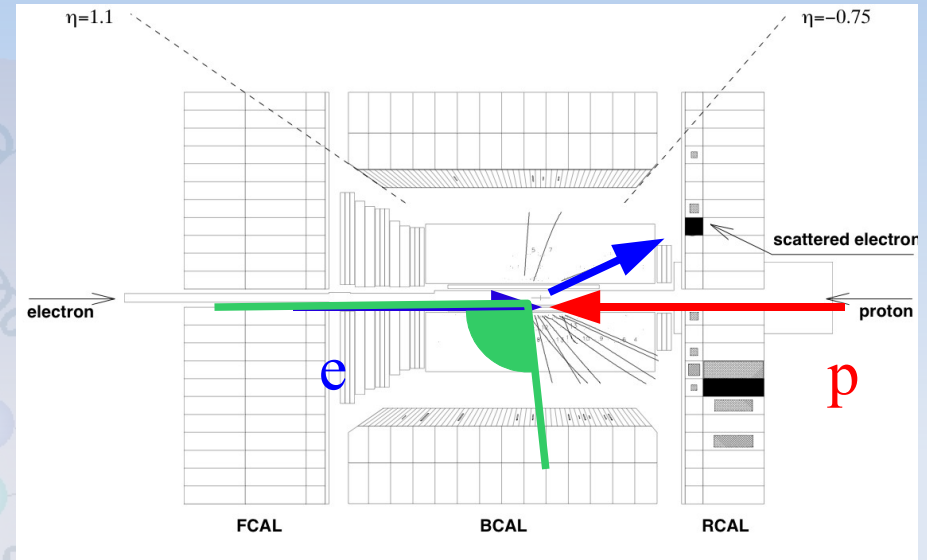


2 forward jets

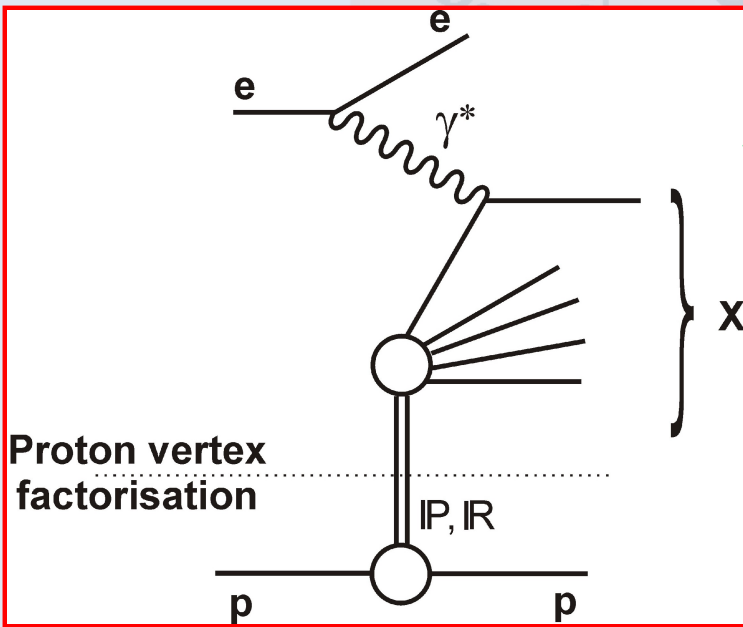
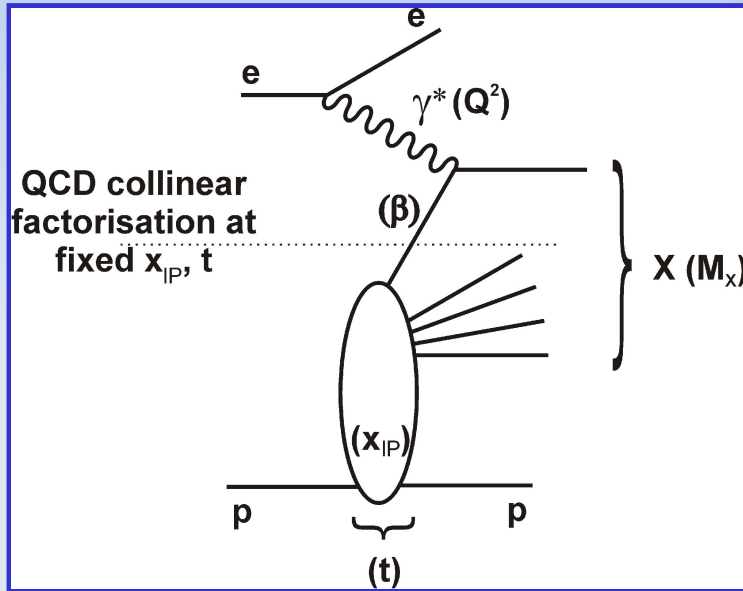
- fwd in the direction of the proton → unordered k_T gluons emission ?
 - fwd jet = $\theta_{jet} < 20^\circ$ and $x_{jet} = E_{jet}^* / E_P > 0.035$ typically BKFL
- in γ^*p cms*

Diffraction re-discovery

- re-discovery by ZEUS in 93: 1/10 of DIS events present a large rapidity gap
- $ep \rightarrow eXp$,
 $\rightarrow p$ barely touched
 - 1% of long. momentum exchanged
 $P_T \sim 100$ MeV.
- \rightarrow Regge theory (“Vaccum exchange”)



Regge Factorization



- DIS:

$$F_2(x, Q^2) = \sum_{a=q, \bar{q}, g} f_a \otimes C_2^a$$

- Diffractive DIS:

$$F_2^{D(3)}(x_{IP}, \beta, Q^2) = \sum_{a=q, \bar{q}, g} f_a^D \otimes C_i^a$$

- if Regge factorization holds:

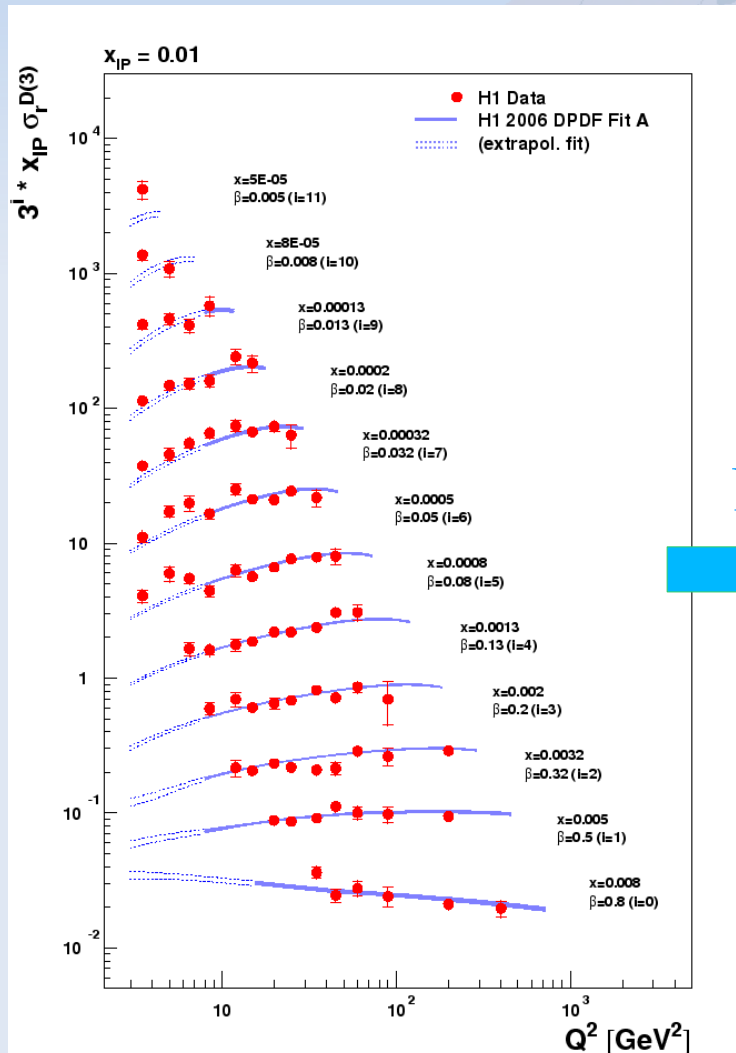
$$f_a^D(x_{IP}, \beta, Q^2) = \text{Flux}(x_{IP}) f_a^{IP}(\beta, Q^2)$$

t = squared 4-mom. transfer to proton
 x_{IP} (or ξ) = fractional proton mom. loss
 (mom. frac. IP/p)

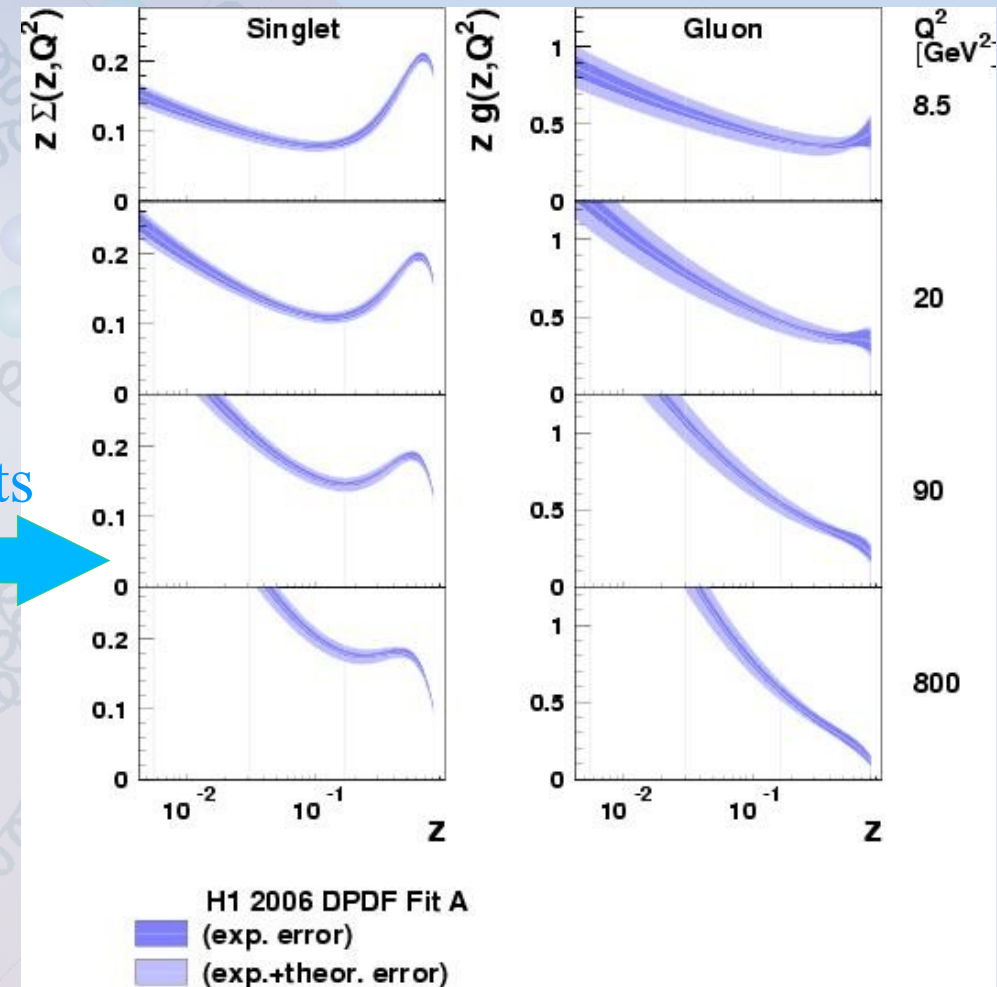
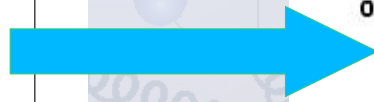
β (or z_{IP}) = fraction of total exchanged
 mom. entering hard scatter
 (mom. frac. q / IP or g / IP)

Hard Diffraction: PDF's

- If factorisation holds : Hard Diff \rightarrow IP PDF's

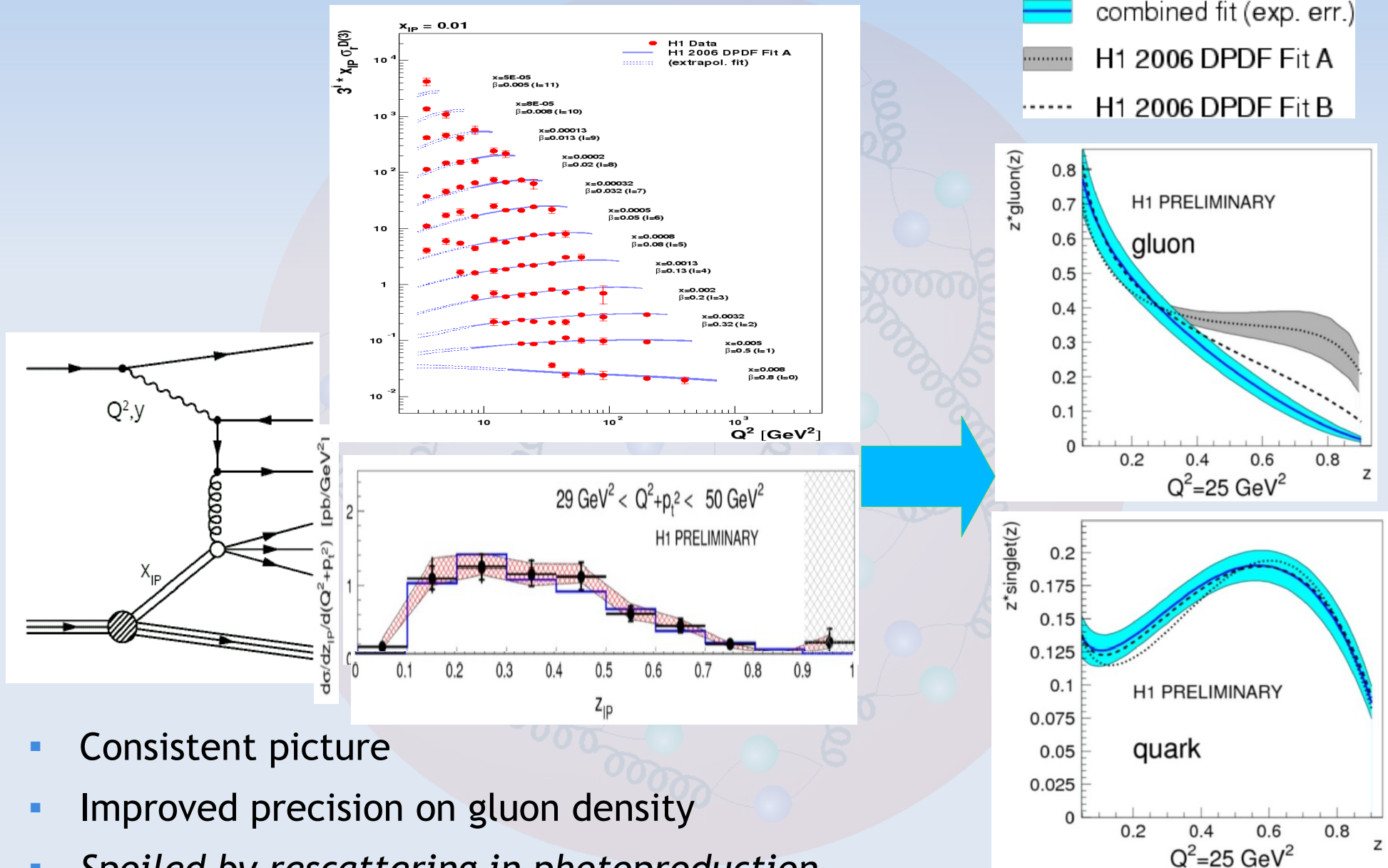


NLO fits



$\sim 70\%$ gluons
Integrated over z

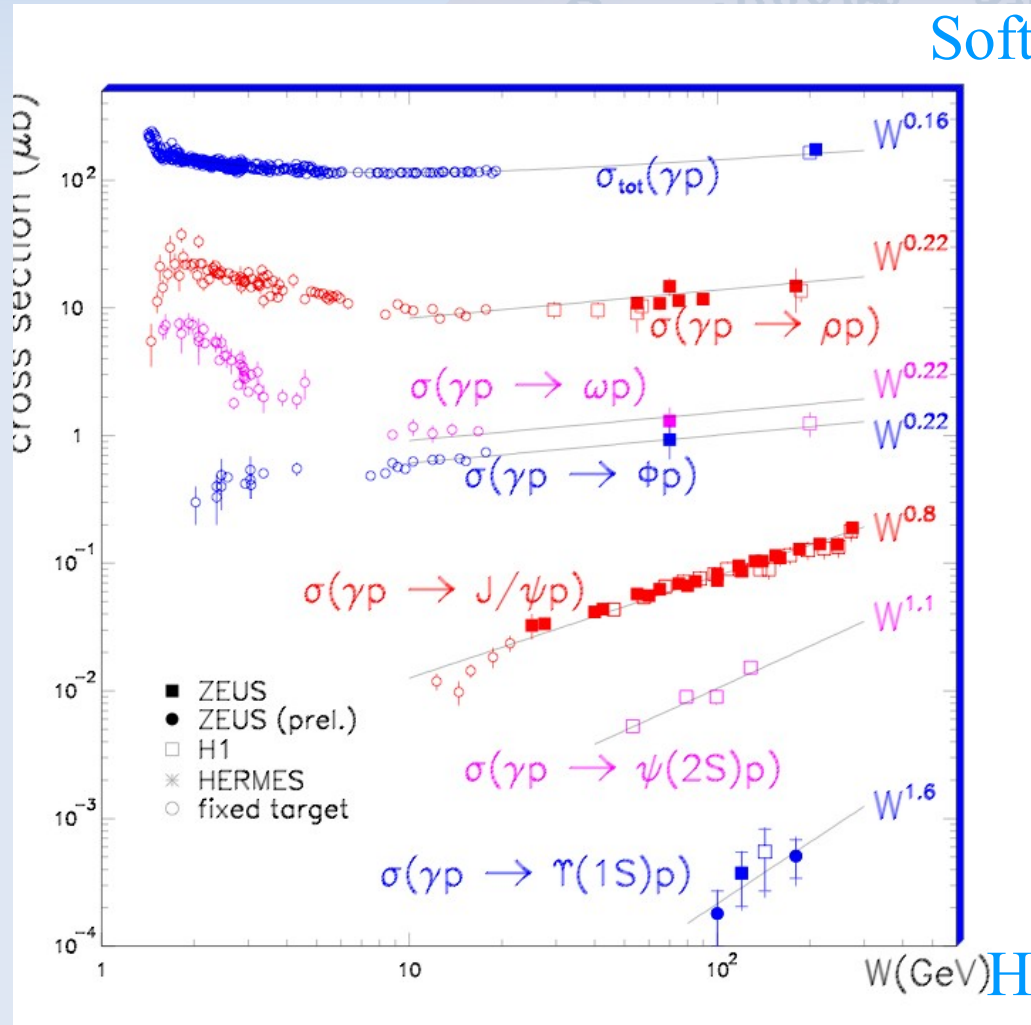
Diffractive PDF's (inclusive +2jets)



- Consistent picture
- Improved precision on gluon density
- Spoiled by rescattering in photoproduction*

VM production

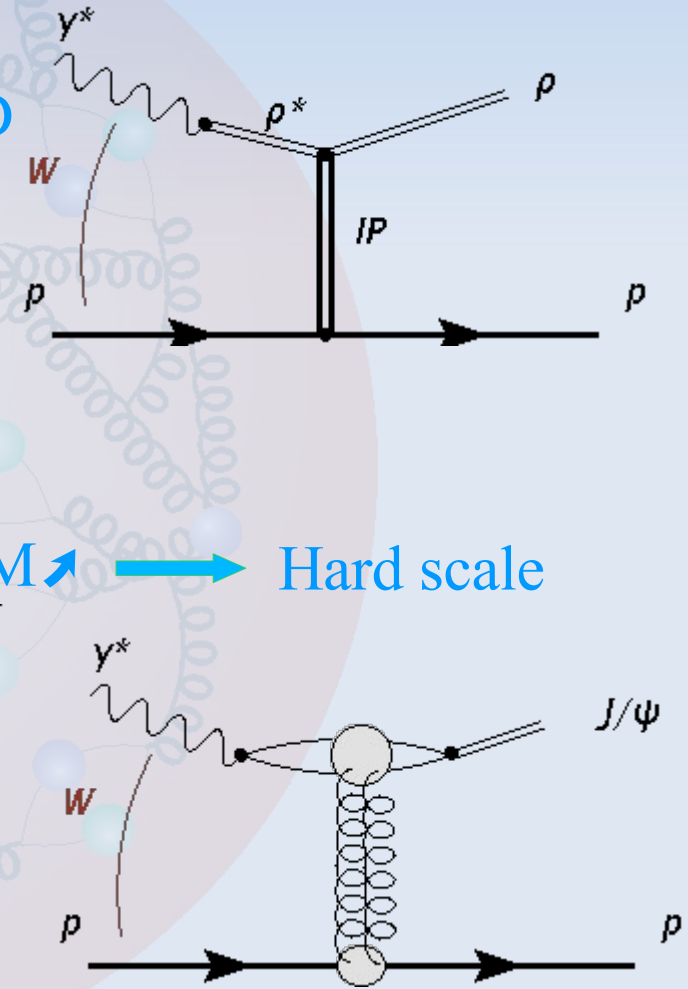
- Vector Mesons: (γ) , ρ^0 , ω , Φ , J/Ψ , Υ
 - γ^* fluctuate in VM + hadronic scattering



Soft QCD

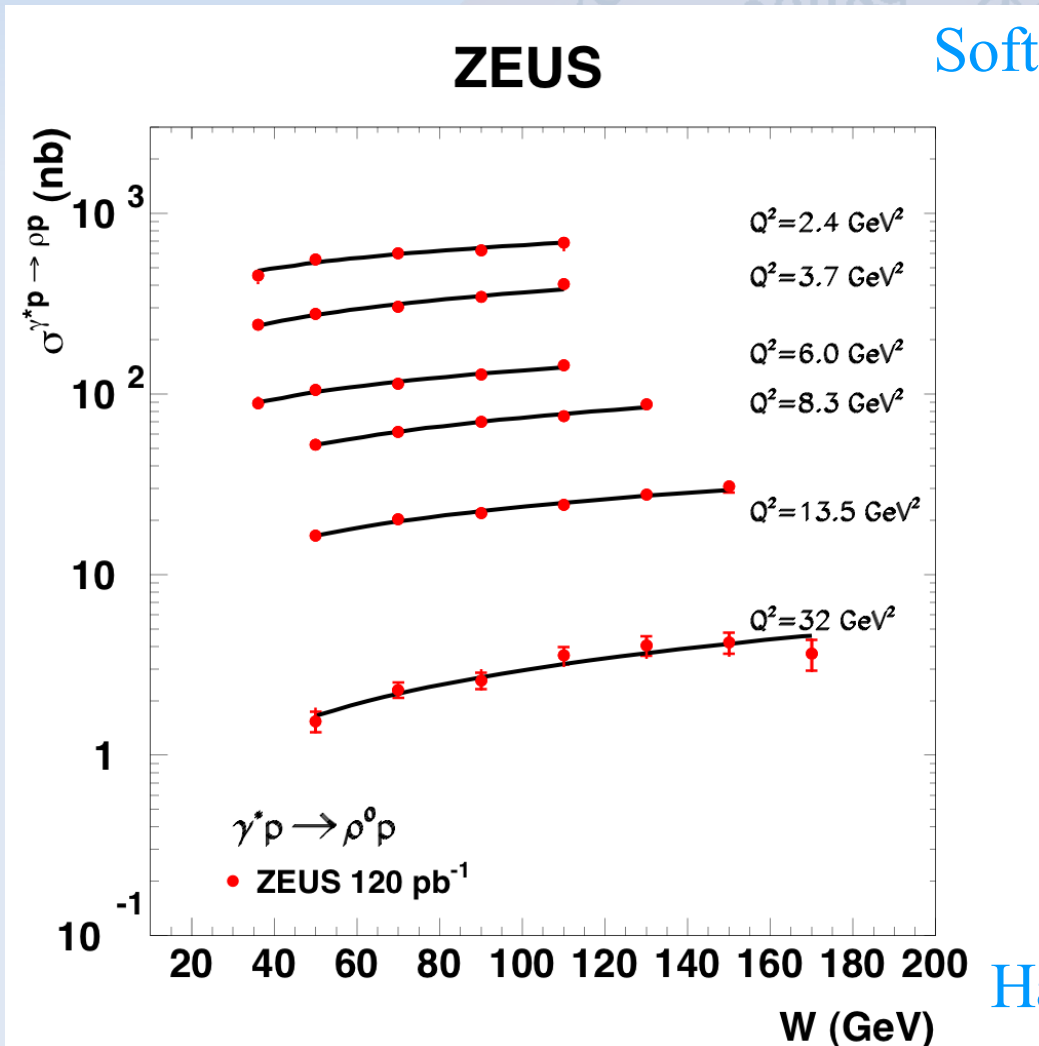
$M \nearrow$ \longrightarrow Hard scale

Hard QCD

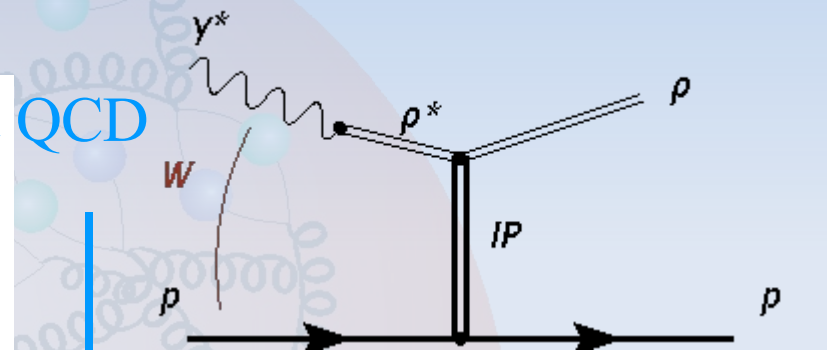


VM production

- Vector Mesons: (γ), ρ^0 , ω , Φ , J/Ψ , Υ
 - γ^* fluctuate in VM + hadronic scattering

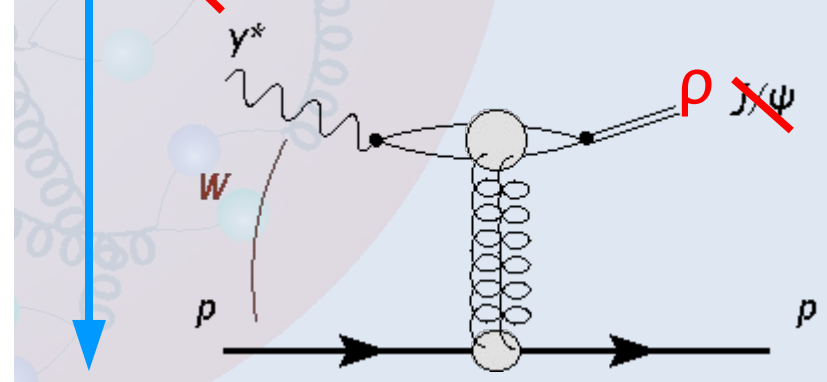


Soft QCD



Q^2 \nearrow
 M \nearrow \rightarrow Hard scale

Hard QCD

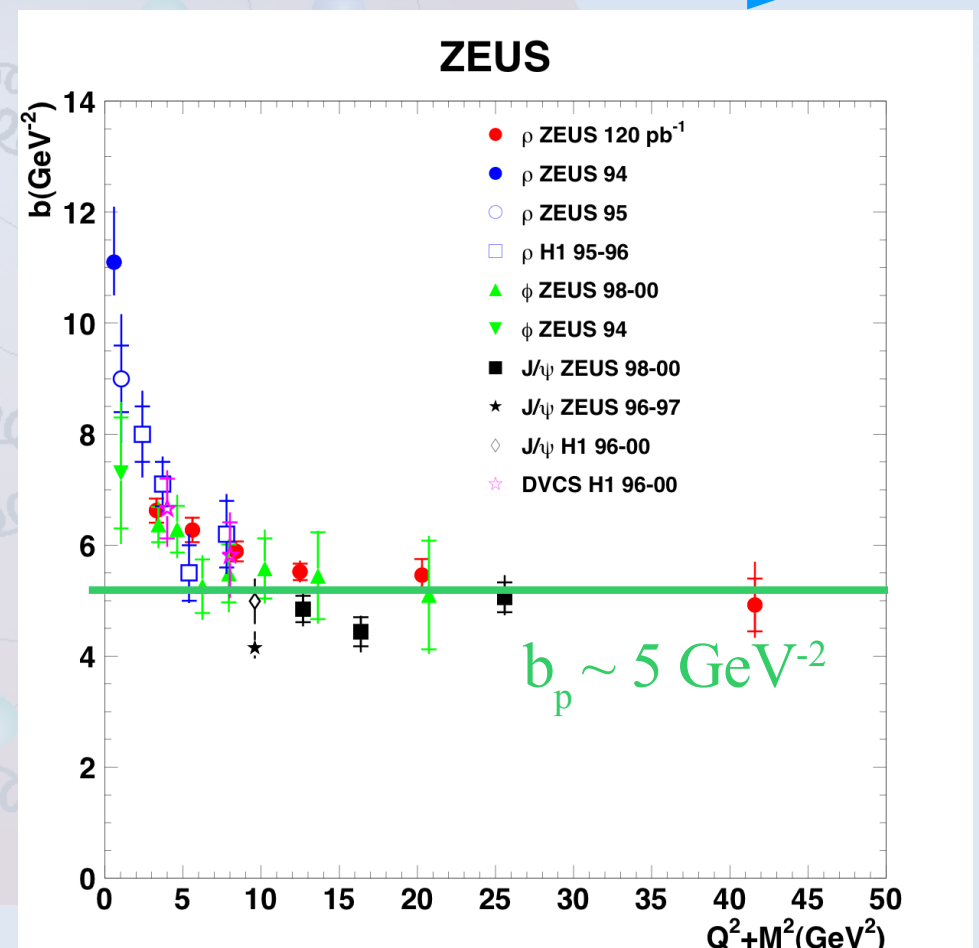
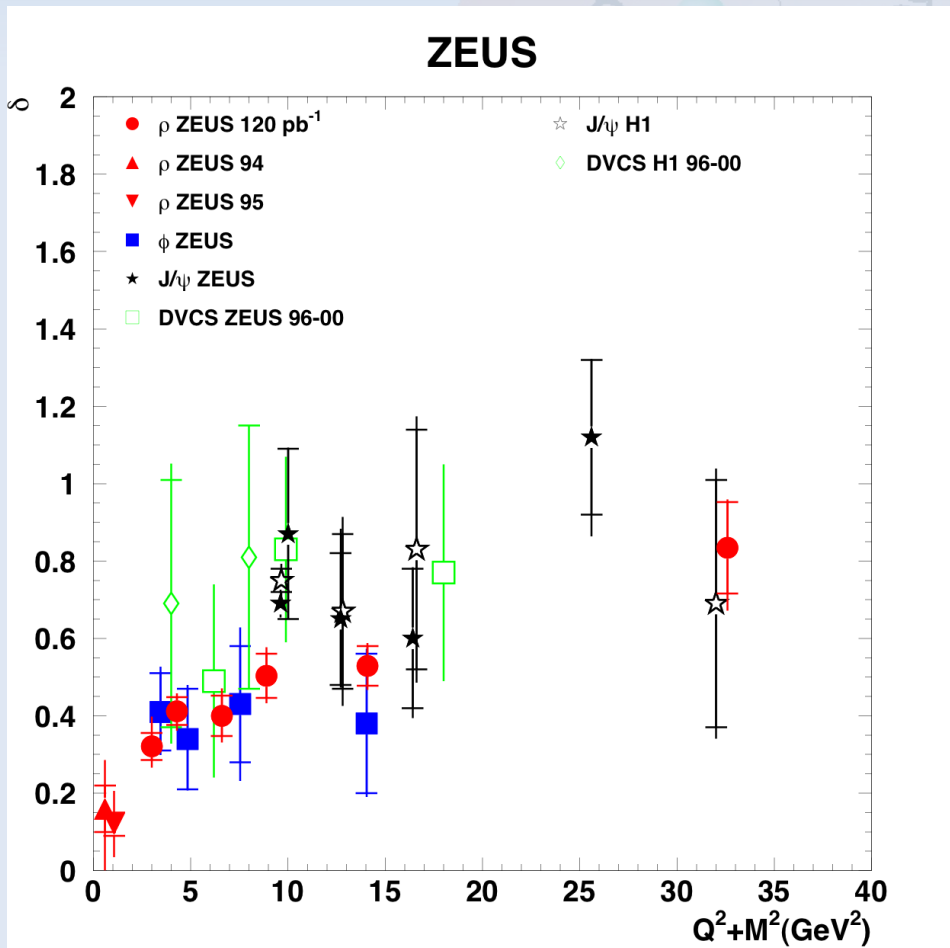
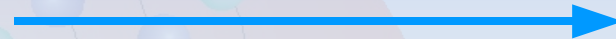


VM production vs hard scale

- Study at moderate Q^2
- $\sigma \sim W^\delta$

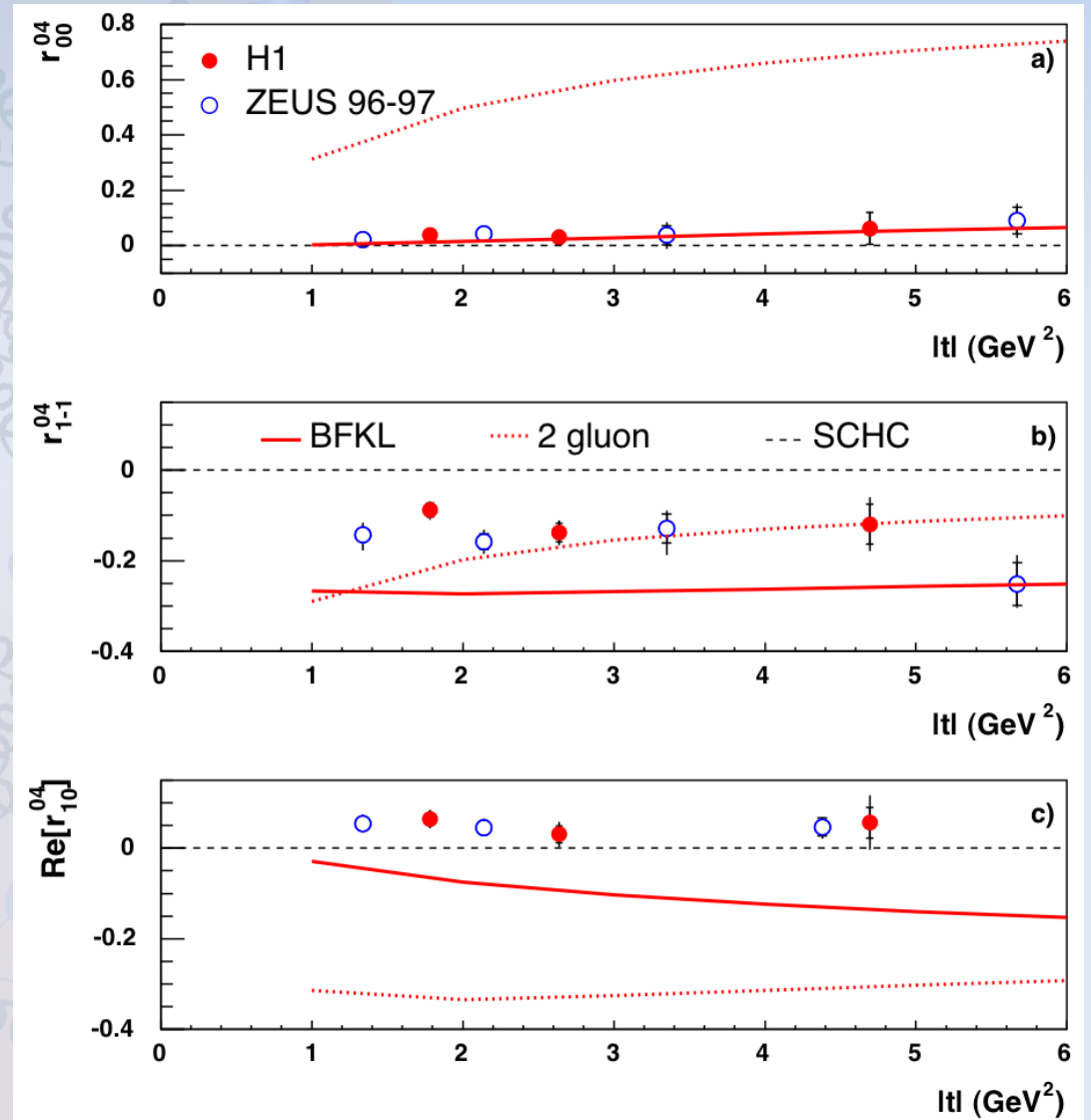
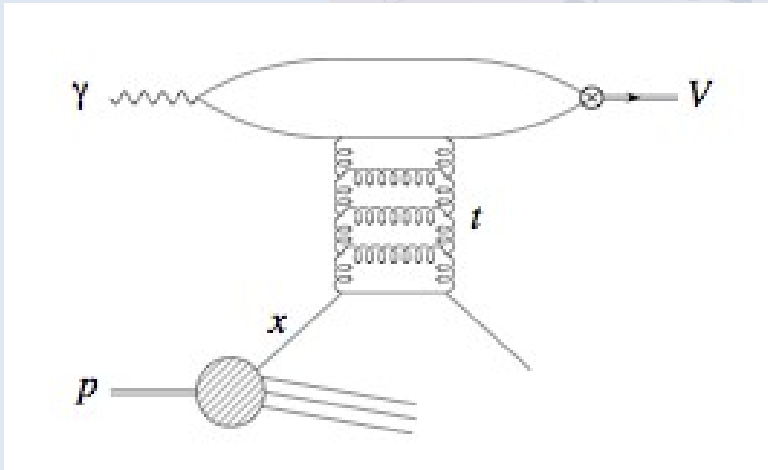
$$\delta = \delta_0 + 0.25 \ln(Q^2 + M^2)$$

- $d\sigma/dt \sim e^{bt}$ at low $|t|$
- $b = b_v + b_p$
- $b_v \sim 1/(Q^2 + M^2)$
qqbar pair size



VM test of QCD dynamics

- $ep \rightarrow epp^0$ @ high $|t|$ (H1)
- spin analysis
- BFKL model
 - vs 2 gluons
 - vs Regge Model (helicity conservation)



Conclusions & Outlook

- Many “unmissable” topics uncovered
 - DVCS, Heavy Quarks, many many analysis...
- Huge progress on p structure function precision
 - extended precision in all of the kin.
→ low & high x, low & high Q^2 , high y
- ... and in the QCD basis of diffraction
- Still a lot of work
 - combine H1 & ZEUS data started
 - HERA-II data “barely” touched
→ improvement of precision $\times \sim 2$ expected
- and many new results to come,
 - direct measurements of $F_L \sim \alpha_s xg(x)$ from low energy runs
 - inclusion of charm and beauty data (F2cc and F2bb) in QCD fit
 - NNLO QCD fits
 - ...