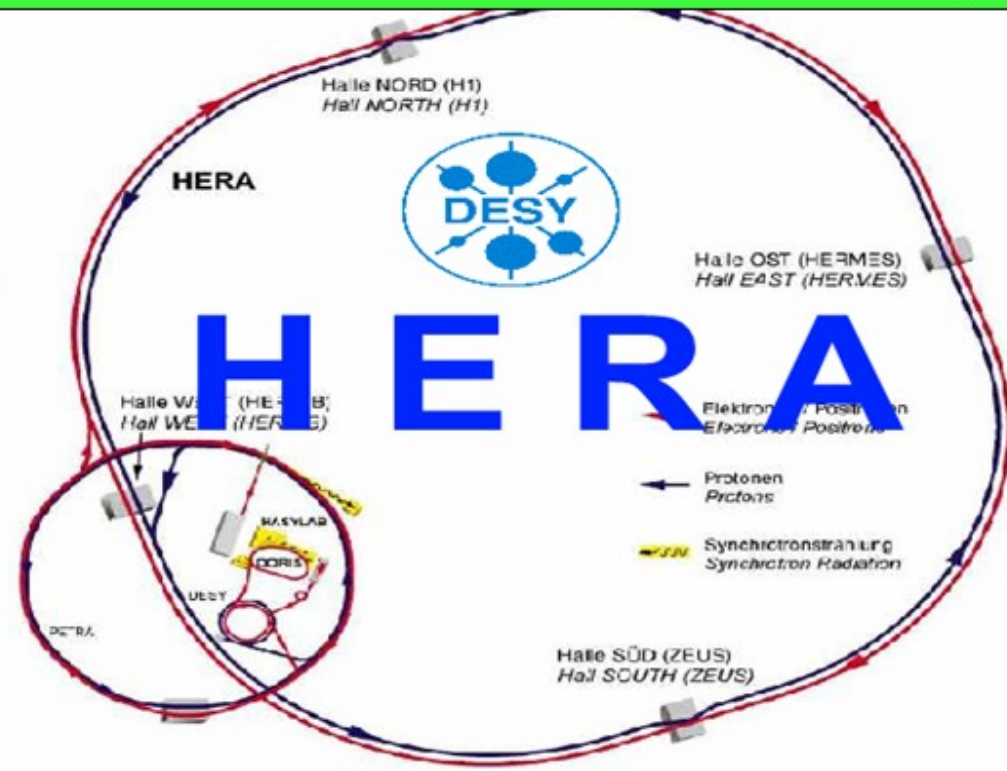
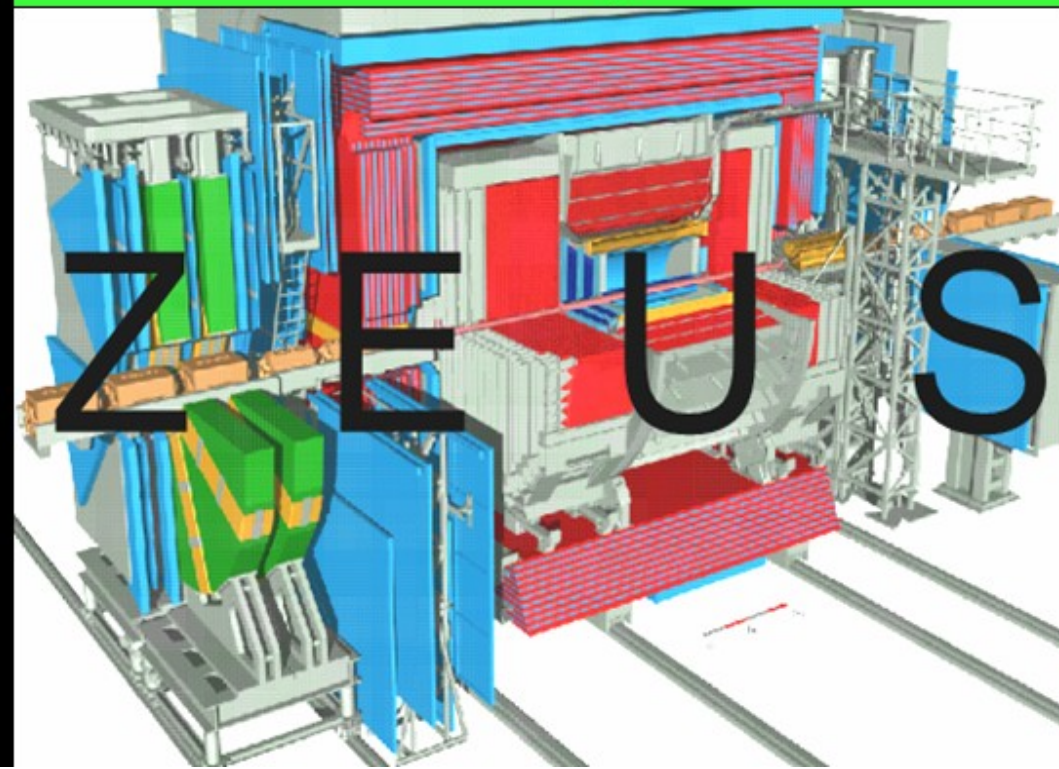


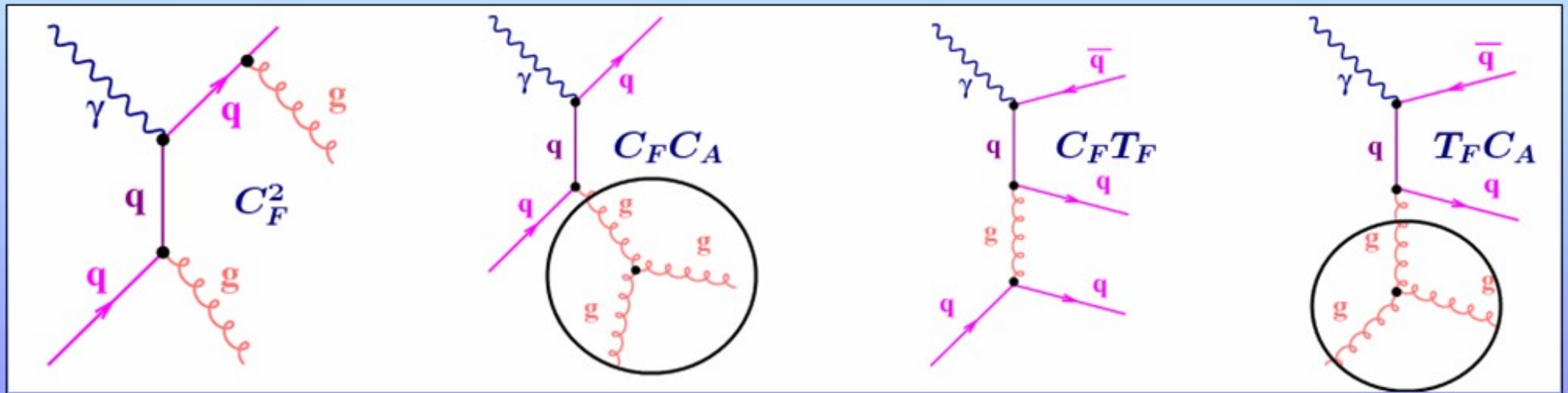
Subjet distributions

Angular correlations in three-jet events

Elías Ron (Universidad autónoma de Madrid)



- Three jet events arising from hard interactions at HERA allow the study of the underlying gauge structure of QCD.
- The **dynamics** of a gauge theory such as **QCD** is determined by the colour factors C_F , C_A and T_F .



- At leading order in α_s , the **3-jet cross section** in **NC DIS** can be expressed as:

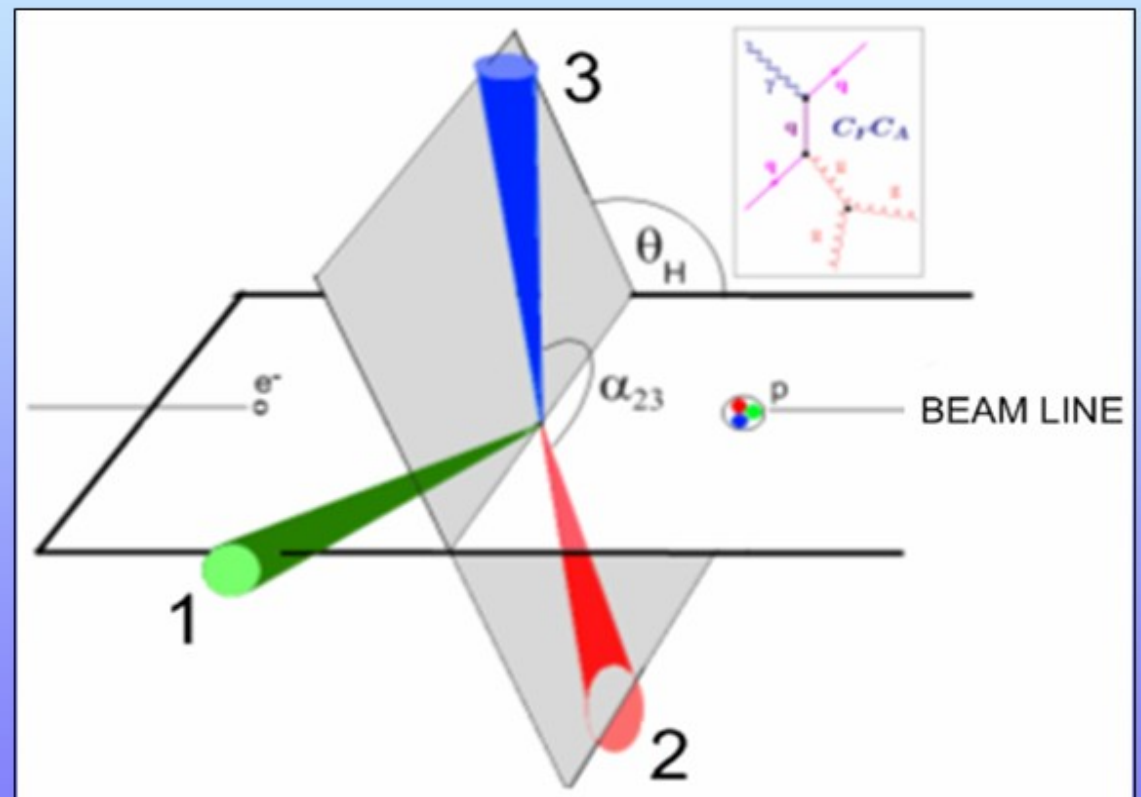
$$\sigma_{ep \rightarrow 3\text{jets}} = C_F^2 \cdot \sigma_A + C_F C_A \cdot \sigma_B + C_F T_F \cdot \sigma_C + T_F C_A \cdot \sigma_D$$

- Angular correlations between jets can be defined in DIS providing sensitivity to the **different colour configurations**.

θ_H : Angle between the plane determined by the **highest** transverse energy jet (**green**) and the beam line, and the plane determined by the two lowest transverse energy jets (**red** and **blue**)

α_{23} : Angle between the lowest transverse energy jets (**red** and **blue**).

η_{\max}^{jet} : pseudorapidity of the **most forward jet**.



$$\cos(\beta_{KSW}) : \cos \left[\frac{1}{2} (\angle[(\vec{p}_1 \times \vec{p}_3), (\vec{p}_2 \times \vec{p}_B)] + \angle[(\vec{p}_1 \times \vec{p}_B), (\vec{p}_2 \times \vec{p}_3)]) \right]$$

JETS were searched using the **k_T cluster algorithm** in the inclusive mode in the Breit frame.

The kinematic region is:

$$\rightarrow Q^2 > 125 \text{ GeV}^2,$$

$$|\cos\gamma_h| < 0.65$$

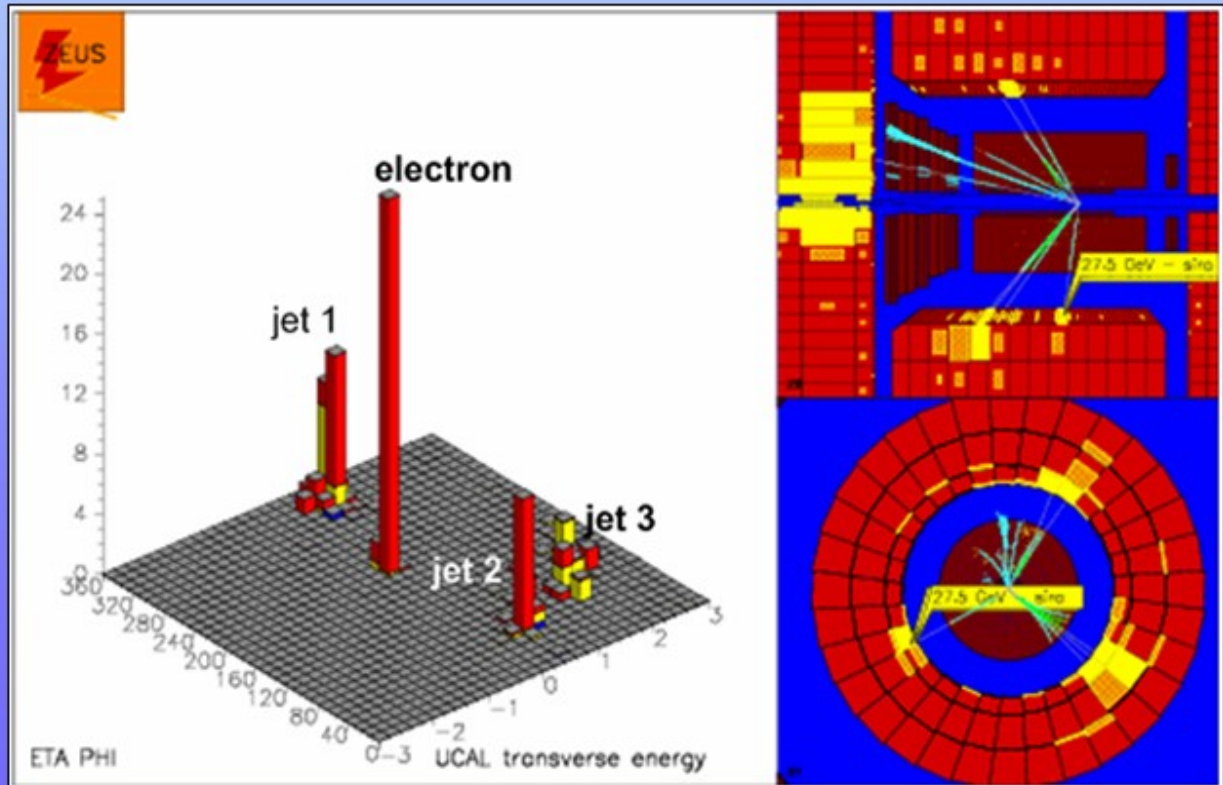
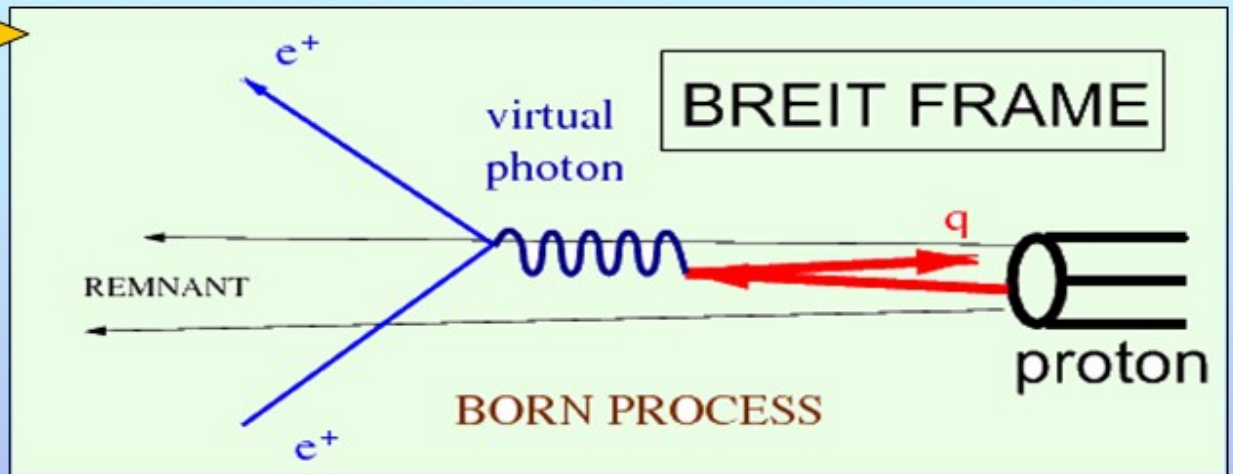
$$-2 < \eta_B^{\text{jet}} < 1.5$$

→ at least 3 jets of $E_{T,B}^{\text{jet}1} > 8 \text{ GeV}$,

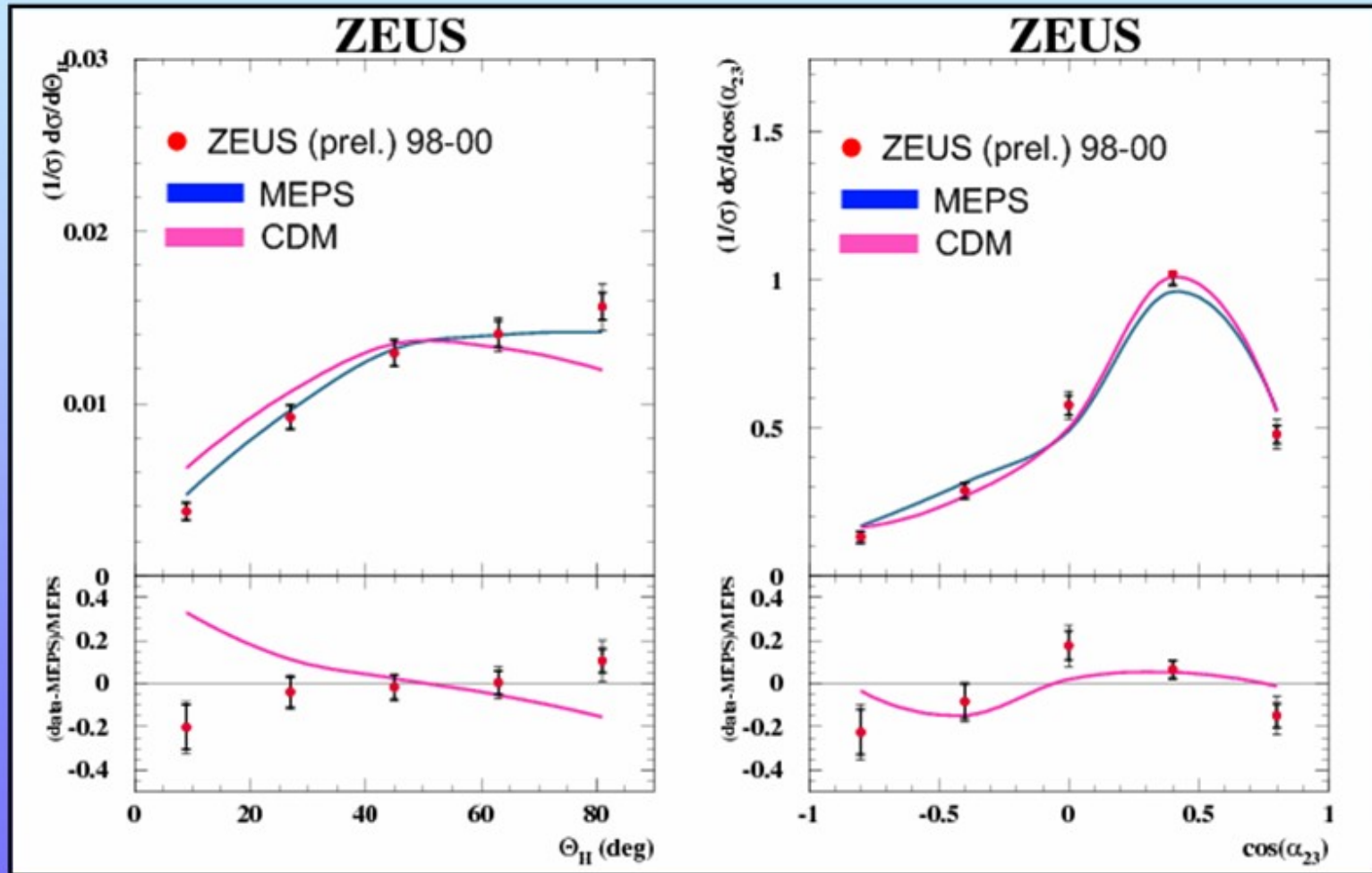
$$E_{T,B}^{\text{jet}2,3} > 5 \text{ GeV}$$

The event sample consists of **1015 jet events** in the range:

$$0.004 < x < 0.2$$



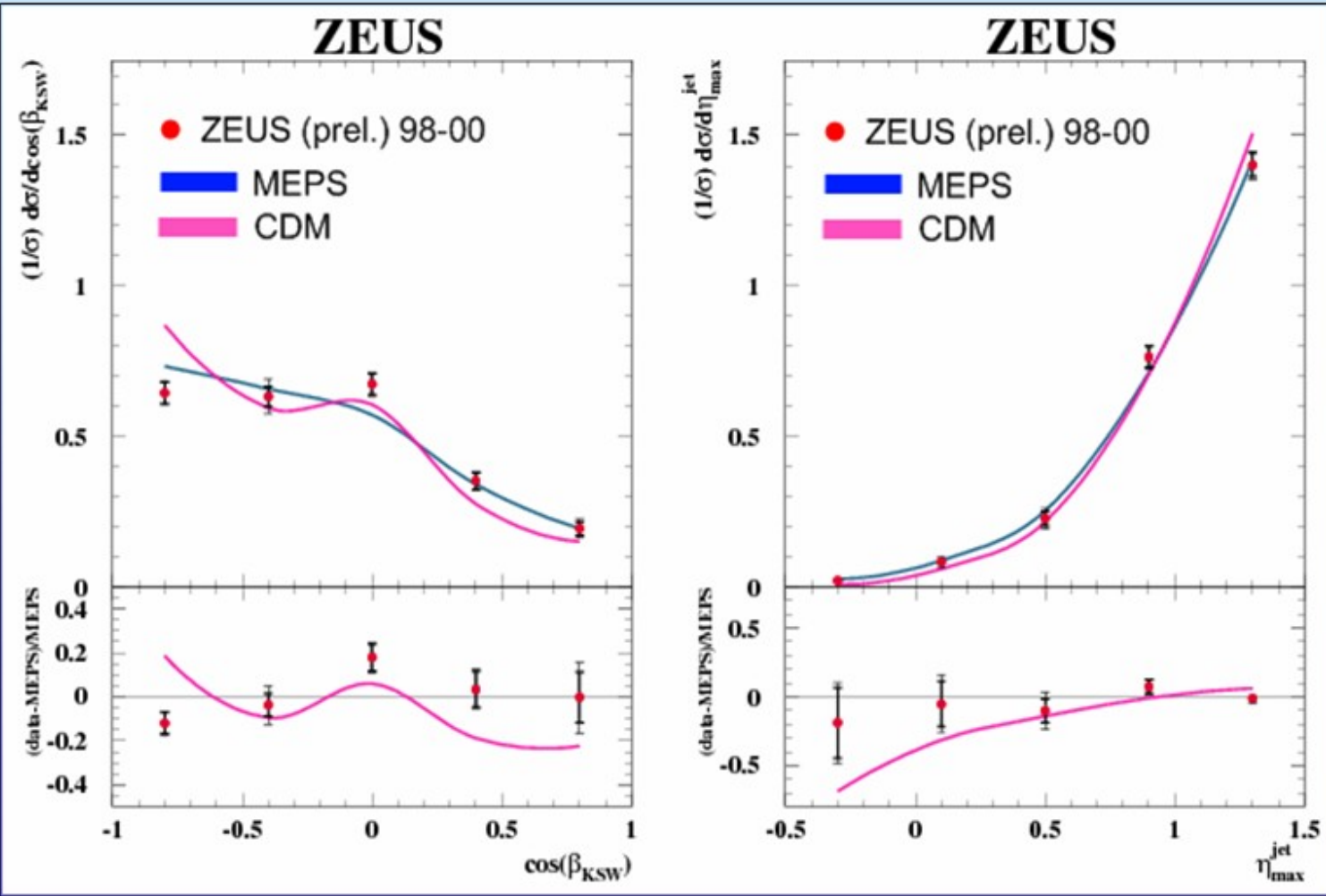
θ_H , α_{23} , β_{KSW} and $\eta_{\text{max}}^{\text{jet}}$ normalised cross sections vs. Color Dipole Model (CDM) and Matrix-element + Parton-shower (MEPS) of LEPTO



Cross sections for θ_H and $\cos(\alpha_{23})$

Good agreement with both Monte Carlo models, **MEPS** does a better description

θ_H , α_{23} , β_{KSW} and η_{max}^{jet} normalised cross sections vs. Color Dipole Model (CDM) and Matrix-element + Parton-shower (MEPS) of LEPTO



Cross sections for $\cos(\beta_{KSW})$ and η_{max}^{jet}

Good agreement with both Monte Carlo models, **MEPS** does a better description

Predictions for the colour components at $O(\alpha_s^2)$ have been calculated with the program **DISENT** with:





-pPDFs: **CTEQ6M1** set

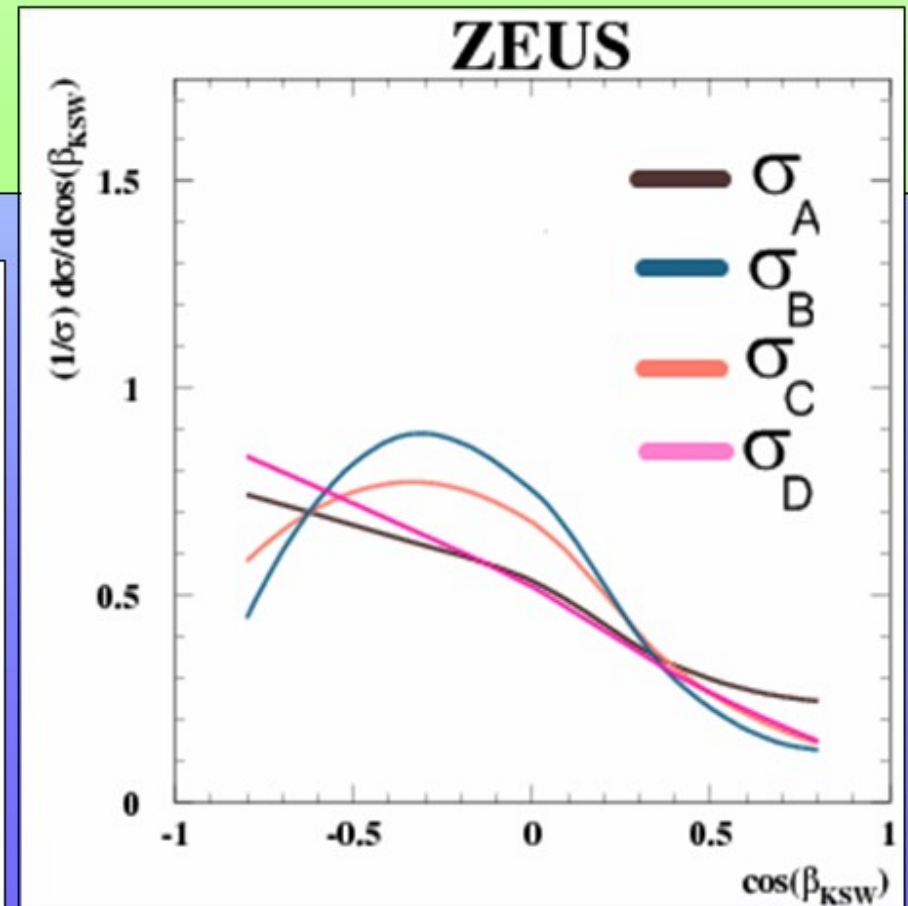
$-\alpha_s$ was calculated at two loops with $\alpha_s(M_Z) = 0.118$

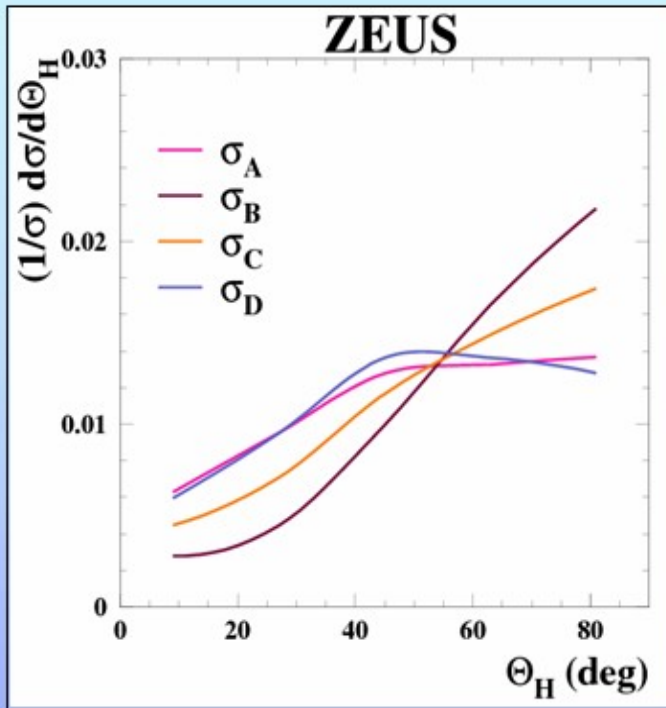
-Renormalization scale $\mu_R = Q$

-Factorisation scale $\mu_F = Q$

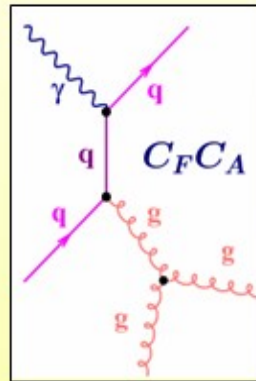
For **SU(3)**, the predicted relative contributions of each colour configuration are:

| | | | |
|---|------------|-----|-----------|
|  | σ_A | 23% | C_F^2 |
|  | σ_B | 13% | $C_F C_A$ |
|  | σ_C | 39% | $C_F T_F$ |
|  | σ_D | 25% | $T_F C_A$ |





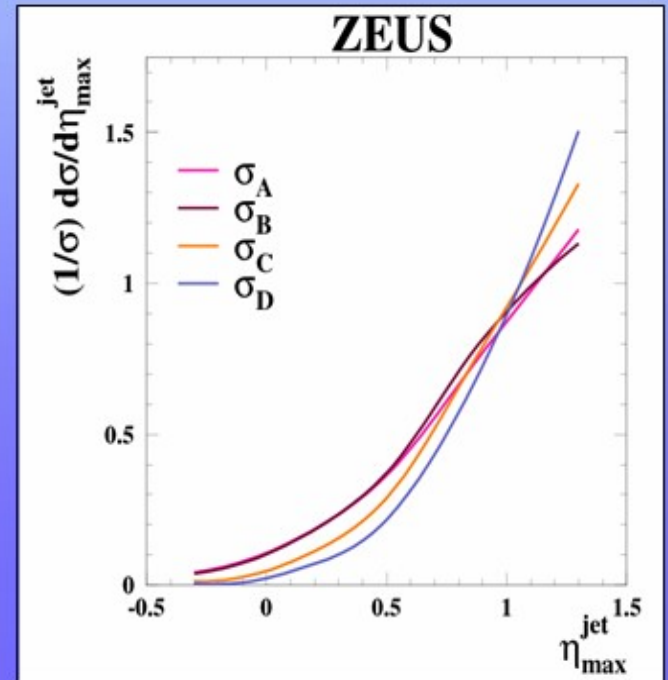
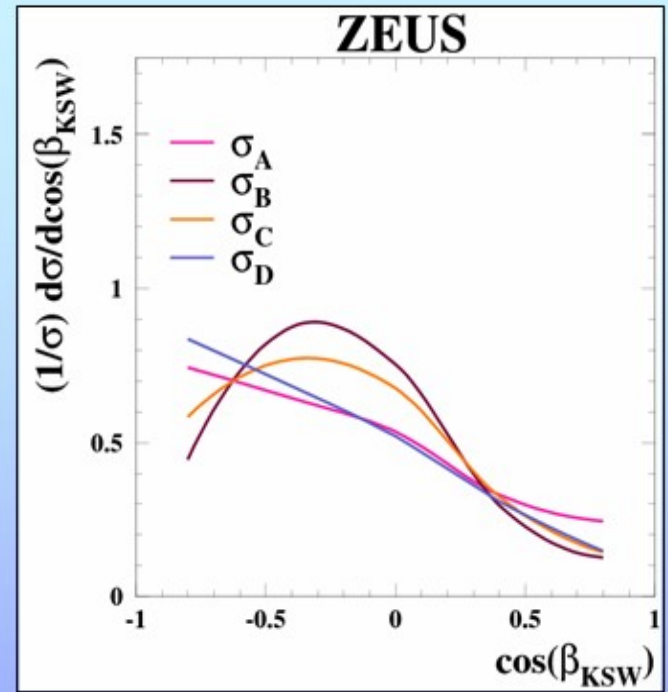
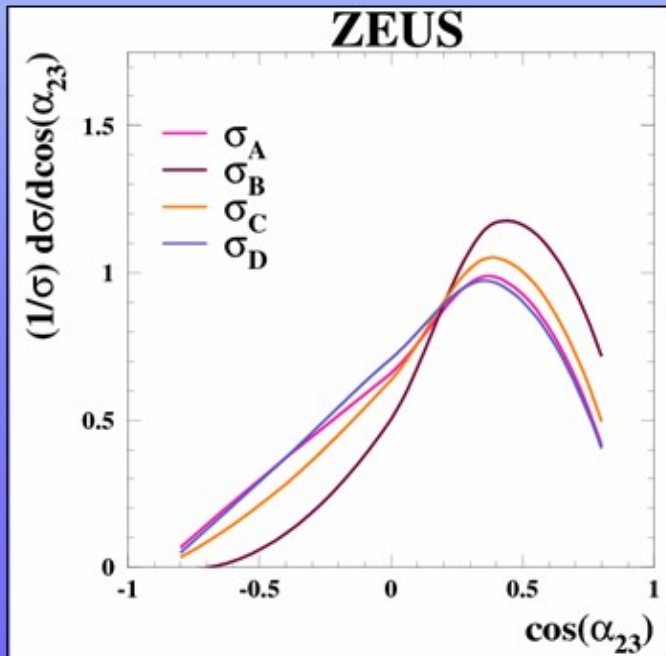
The distributions for σ_B (triple-gluon vertex in quark induced processes) have a very different shape than the others.



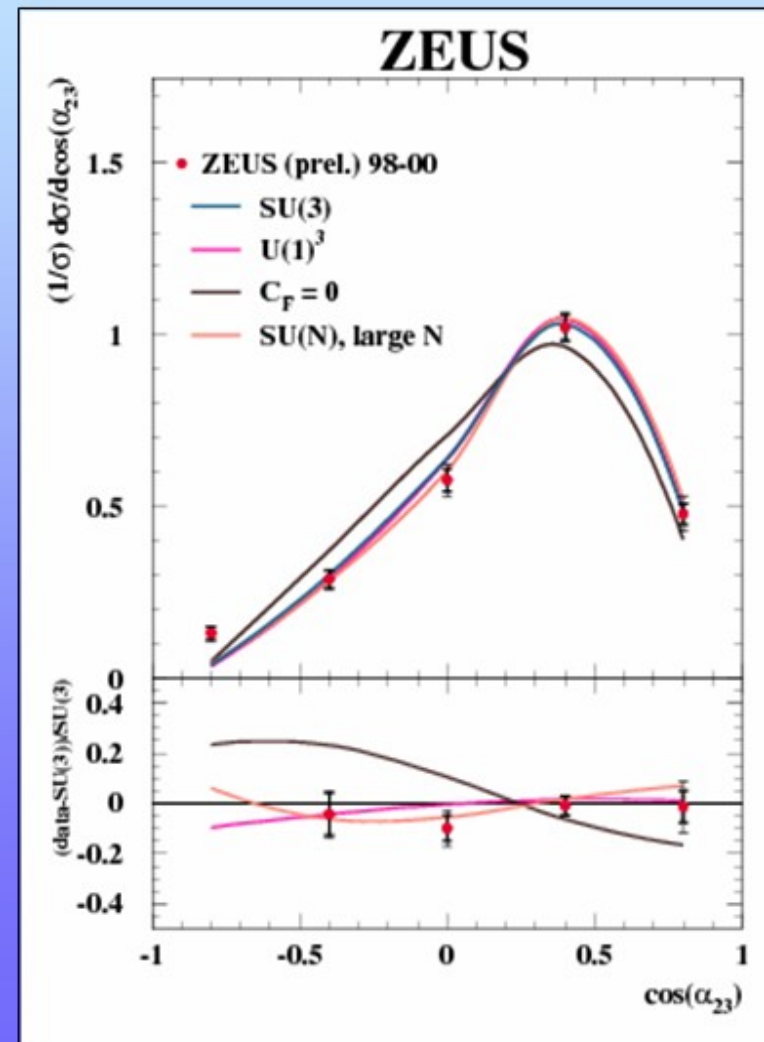
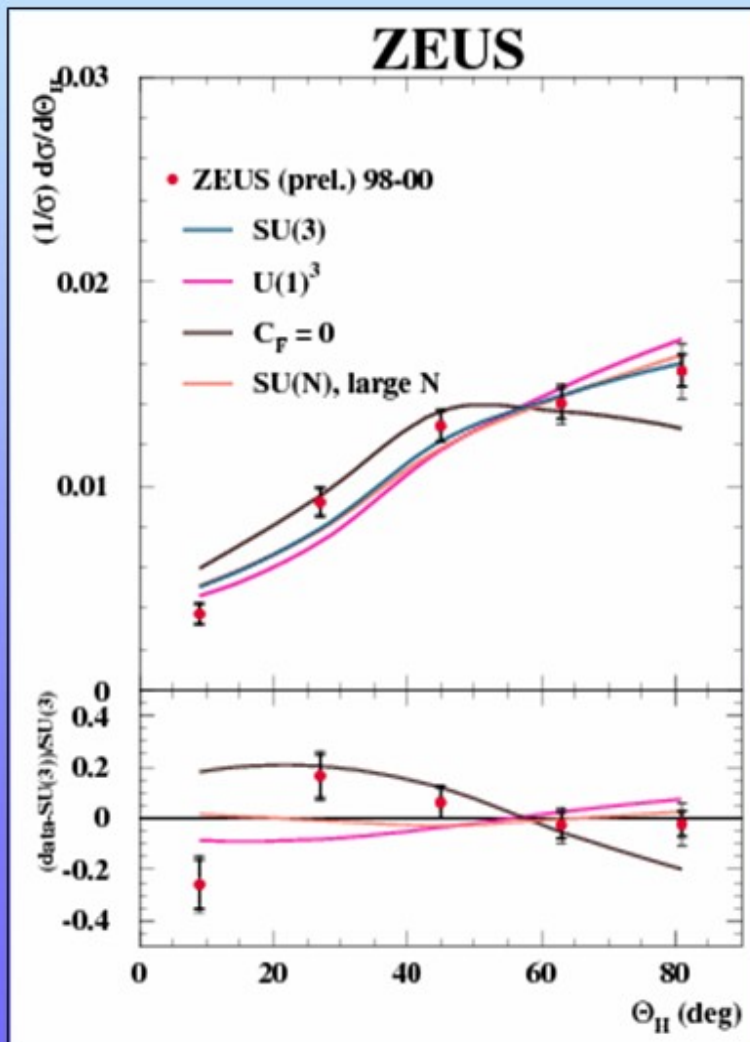
The distribution in

$$\eta_{\max}^{\text{jet}}$$

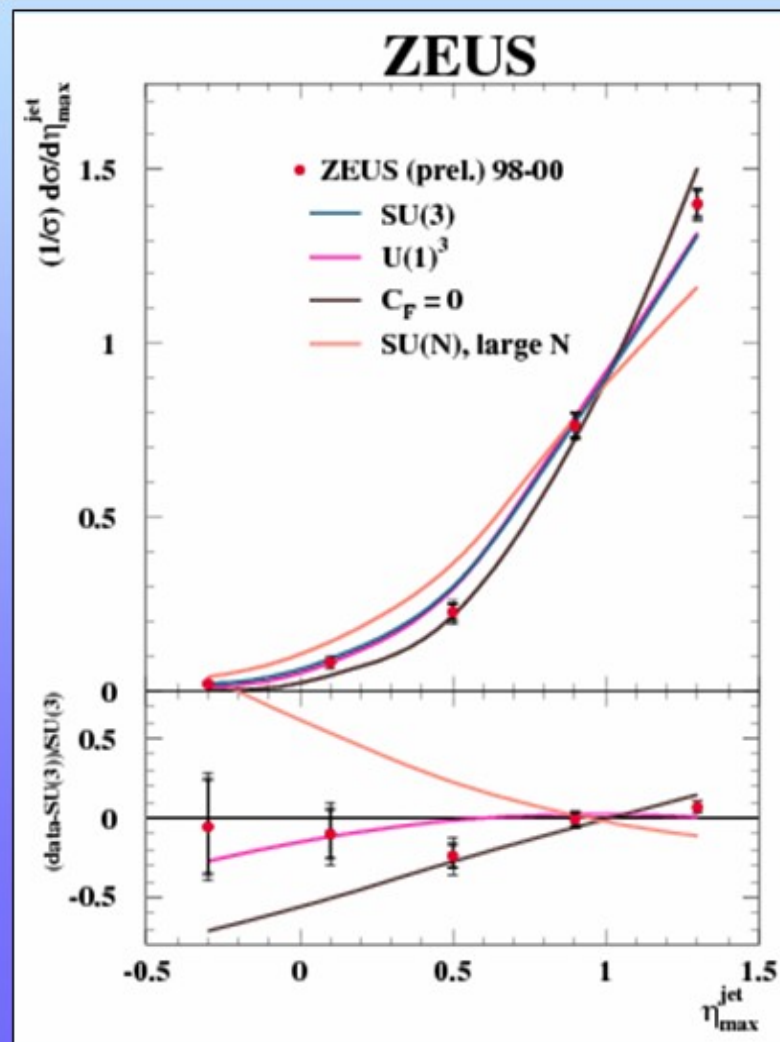
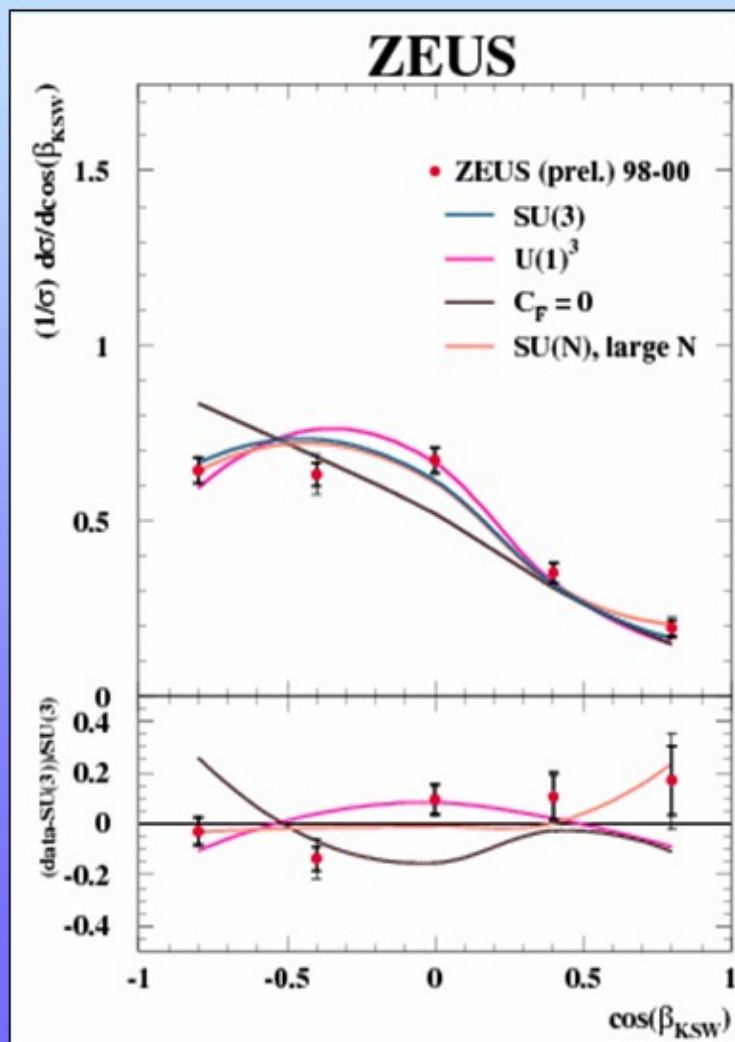
for σ_D (triple-gluon vertex in gluon induced processes) has a different shape than the others



Measured normalised differential cross sections as functions of Θ_H and $\cos(\alpha_{23})$ are compared with the calculations of **DISINT** based on **SU(3)**, **U(1)³**, **SU(N) for large N** and $C_F=0$.



Measured normalised differential cross sections as functions of $\cos(\beta_{KSW})$ and $\eta_{\text{jet,max}}^{\text{jet}}$ compared with the calculations of **DISENT** based on **SU(3)**, **U(1)³**, **SU(N)** for large N and $C_F=0$.

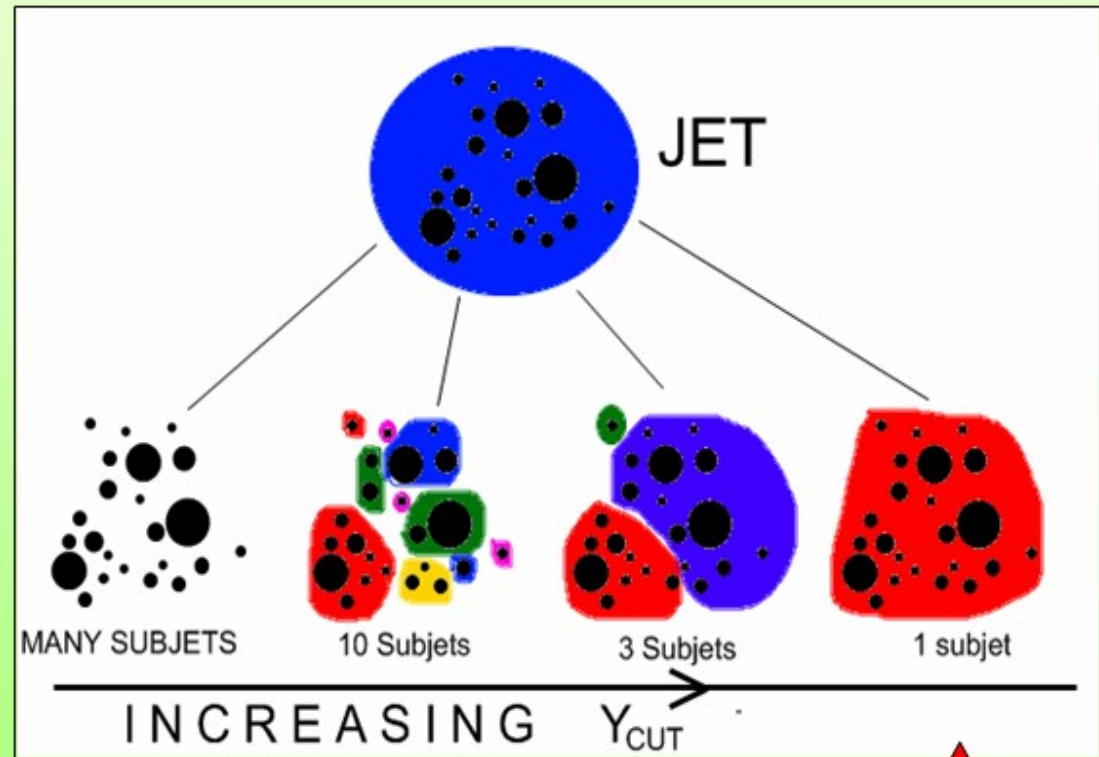


- Angular correlations ($\Theta_H, \alpha_{23}, \beta_{\text{KSW}}, \eta_{\text{max}}^{\text{jet}}$) in three-jet events in **NC DIS** have been measured using **82 pb⁻¹** in the kinematic region defined by $Q^2 > 125 \text{ GeV}^2$ and $|\cos \gamma_h| < 0.65$
- Fixed-order calculations separated according to the **colour configurations** were used to study the sensitivity of the angular distributions to the **underlying gauge structure**:
 - $\Theta_H, \alpha_{23}, \beta_{\text{KSW}}$ distinguish well the contribution from the **triple-gluon vertex in quark-induced processes**
 - $\eta_{\text{max}}^{\text{jet}}$ distinguishes the contribution coming from the **triple-gluon vertex in gluon induced processes**.
- The measurements are consistent with the admixture of color configurations as predicted by **SU(3)**.
- The data disfavour **SU(N) in the limit of large N** and $C_F = 0$.

At high transverse energy the fragmentation effects become negligible and the main contribution to the jet substructure comes **from parton radiation**.

Subjects are resolved within a jet by reapplying the **k_T cluster algorithm** on all the particles belonging to a jet. Subjects are all the particles within a jet which are at a distance bigger than d_{cut} from each other, where d_{cut} is:

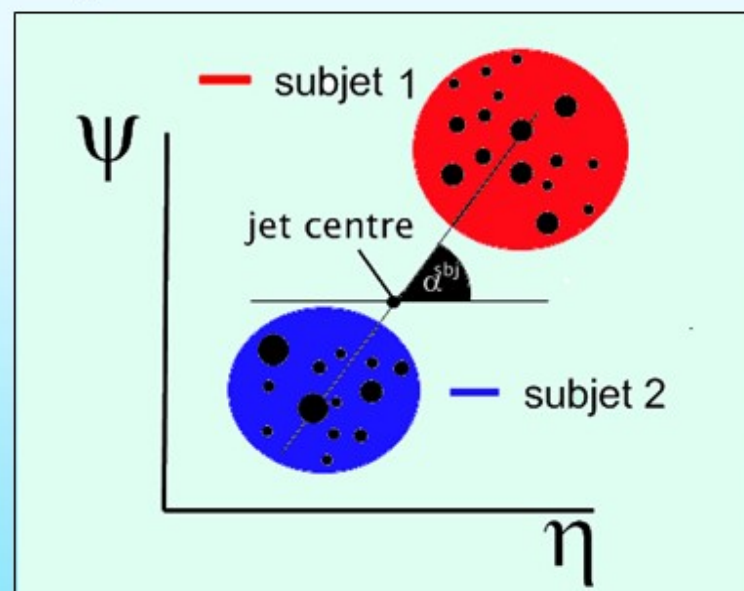
$$d_{cut} = y_{cut} \cdot (E_T^{jet})^2$$



The subject multiplicity depends on the value chosen for the parameter y_{cut}

The pattern of **QCD** radiation has been studied by means of differential cross sections with respect to the variables:

- α^{sbj} , the angle between the highest E_T subjet and the beam line, as seen from the jet axis.
- E_T^{sbj} / E_T^{jet}
- $\eta_{sbj} - \eta_{jet}$
- $|\phi_{sbj} - \phi_{jet}|$

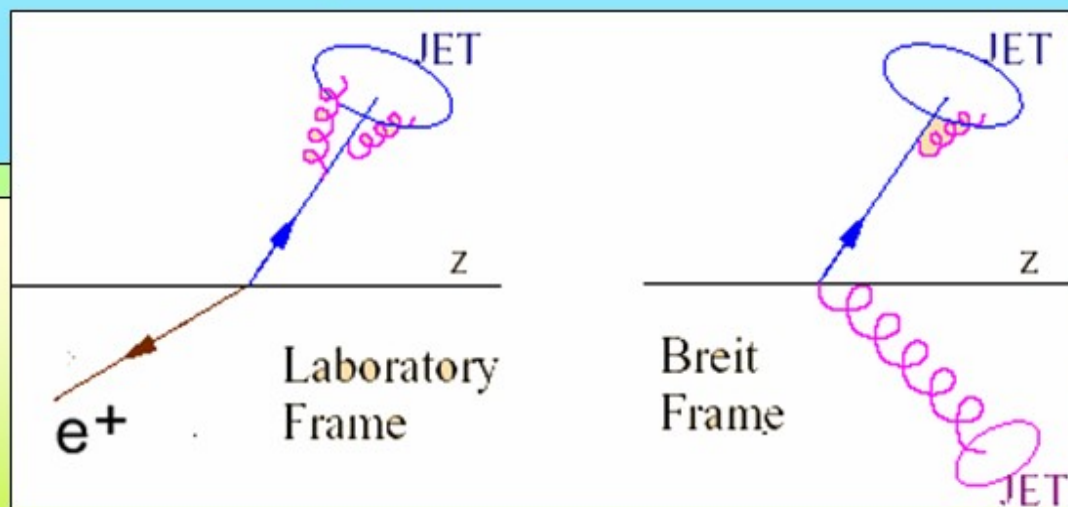


The kinematic range is:

$$Q^2 > 125 \text{ GeV}^2$$

$$E_T^{jet} > 14 \text{ GeV} \quad -1 < \eta^{jet} < 2.5$$

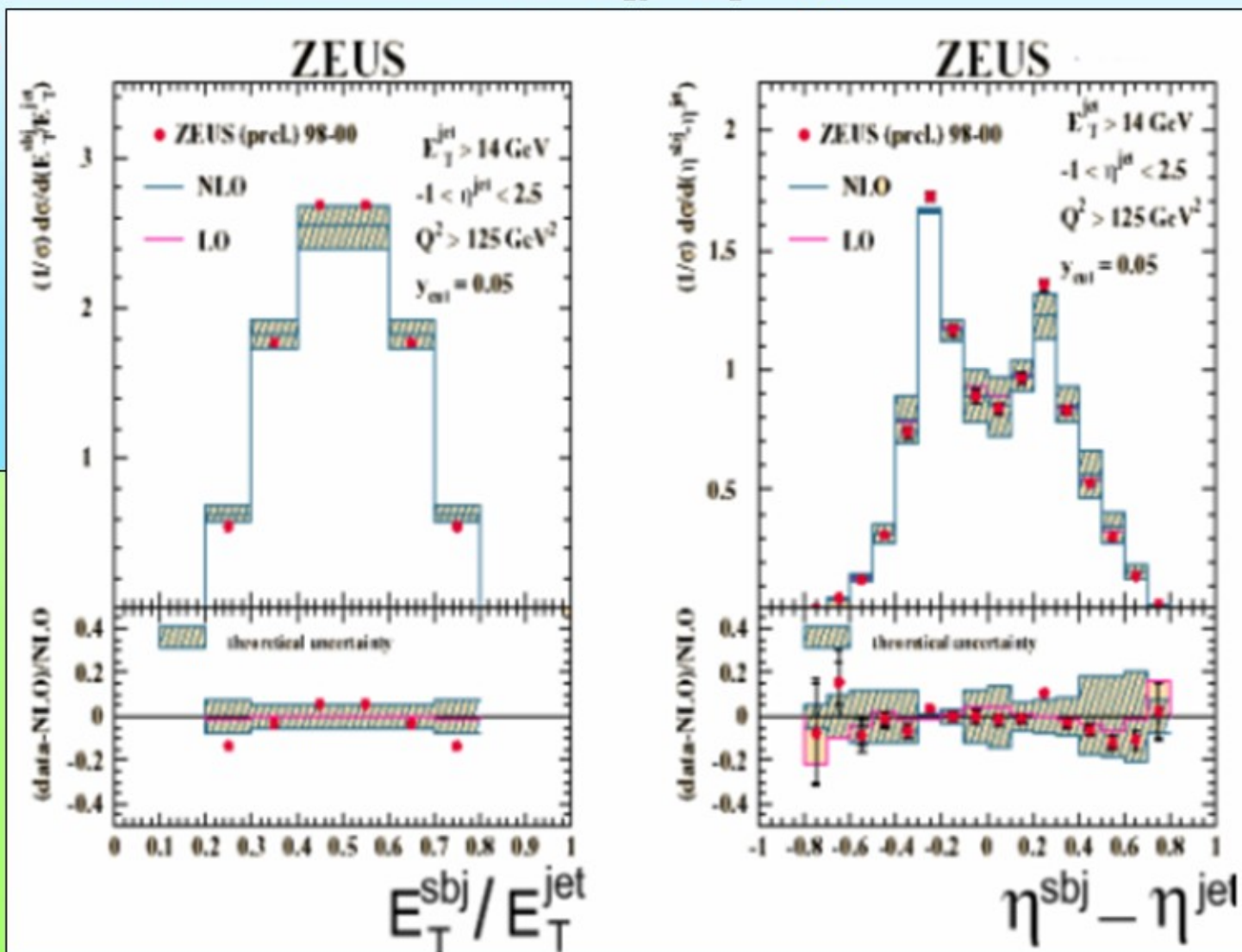
Final Sample: Jets in the lab frame with **exactly 2** subjets at $y_{cut} = 0.05$



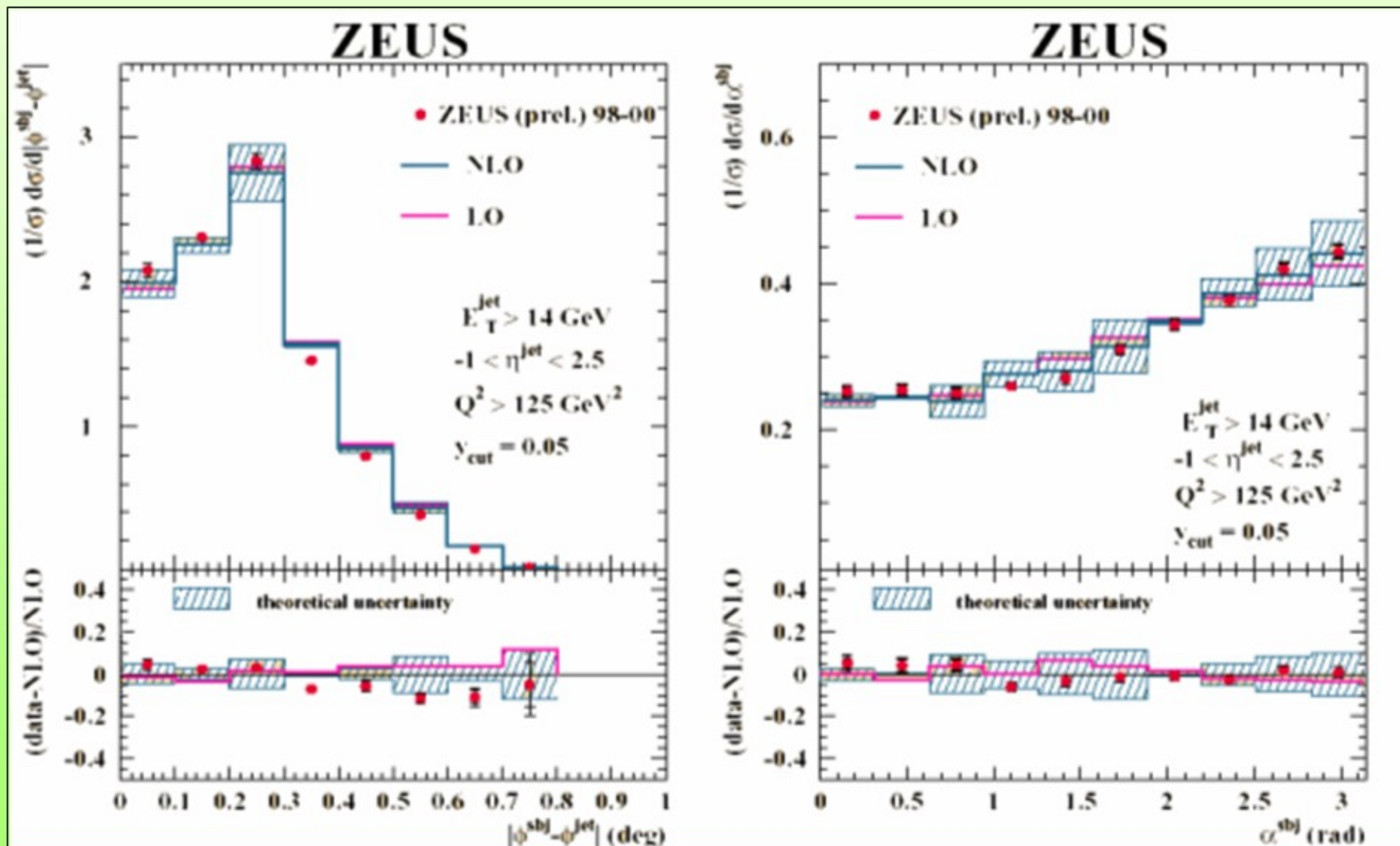
Fixed-order QCD predictions were calculated at LO and NLO using DISENT with:

- α_s was calculated at two loops with $\alpha_s(M_Z) = 0.1175$
- Renormalisation and factorisation scales were: $\mu_R = \mu_F = Q$
- pPDFs: MRST99 sets
- Calculations were corrected to hadron level to compare with the data

NLO predictions describe the data within $\pm 10\%$

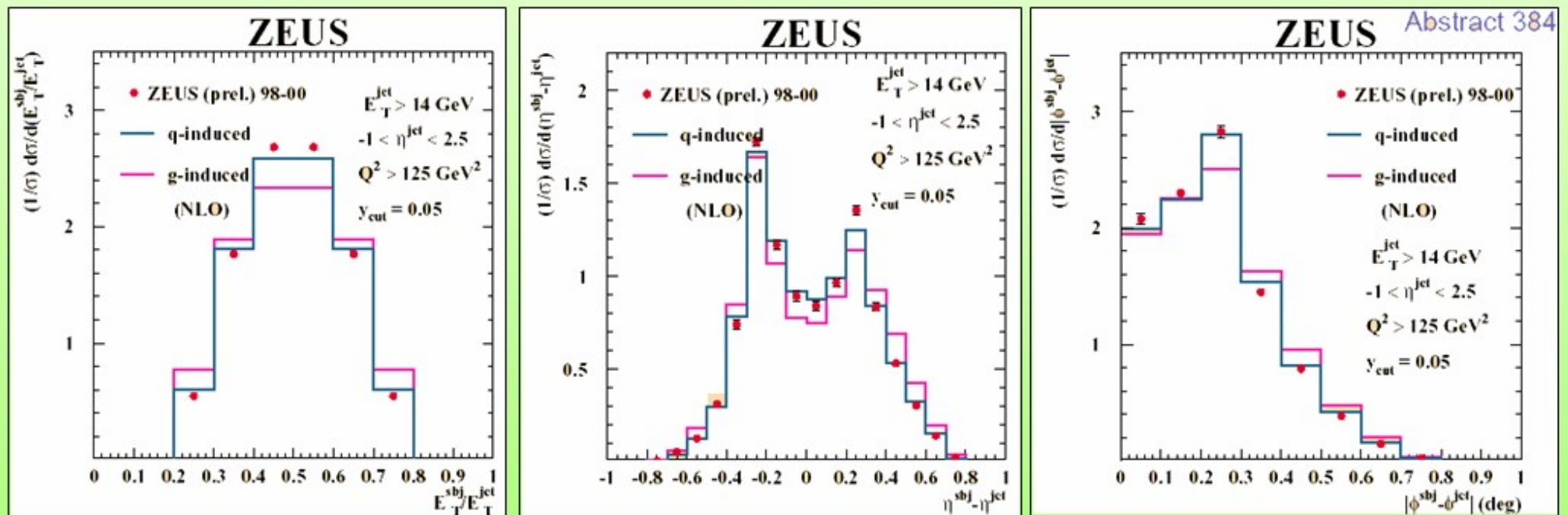


Normalised differential cross sections for α^{sbj} and $|\phi_{sbj} - \phi_{jet}|$

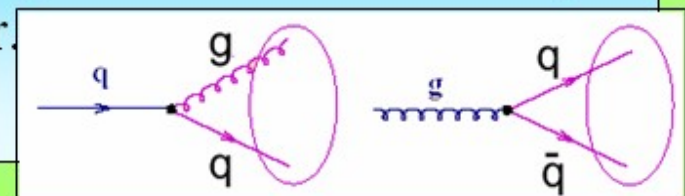


NLO predictions describe the data within $\pm 10\%$

Normalised differential cross sections for $|\phi_{\text{sbj}} - \phi_{\text{jet}}|$, $\eta_{\text{sbj}} - \eta_{\text{jet}}$ and $E_T^{\text{sbj}} / E_T^{\text{jet}}$ are compared with calculations for quark- and gluon-induced processes separately. The prediction of QCD is 82% of **quark-induced processes** and 18% of **gluon induced**.



Comparison shows that the data are better described by the calculations for jets arising from a qg pair than those coming from a $q\bar{q}$ pair.



- Normalised differential subjet cross sections for jets with **exactly** two subjets for $y_{cut}=0.05$ in inclusive-jet NC DIS have been measured using **82 pb⁻¹** in the kinematic region defined by $Q^2 > 125 \text{ GeV}^2$.
- The data show that the two subjets:
 - **tend to have similar transverse energies,**
 - **tend to be close to each other**
 - the highest E_T subjet **tends to be in the rear part** with respect to jet axis.
- Reasonable description of data by fixed-order QCD calculations:
 - The pattern of parton radiation as predicted by QCD **explains the subjet topology in the data.**
 - The data are consistent with the **dominance of quark-induced** processes.