

# Jets, Event Shapes, and Determination of $\alpha_s$ in DIS at HERA

Thorben Theedt  
On Behalf of the H1 and ZEUS Collaborations

## Outlook:

- Inclusive jets (ZEUS/H1)
- Dijets (ZEUS)
- Multijets (H1/ZEUS)
- Event shapes (H1/ZEUS)
- Summary

# Jets: Motivation and basic concepts

Jet cross section in pQCD: Series expansion in powers of  $\alpha_s$

$$d\sigma = \sum_{m=0}^{\infty \text{ or } 2} \alpha_s^m(\mu_R) \sum_{a=q, \bar{q}, g} f_a(\eta, \mu_F) \otimes d\hat{\sigma}(x_{Bj}/\eta, \mu_R, \mu_F) (1 + \delta_{had})$$

pQCD factorization

Coefficients are convolutions of:  $f_a(\eta, \mu_F)$ ...PDFs (proton structure) and  $d\hat{\sigma}(x_{Bj}/\eta, \mu_R, \mu_F)$ ...hard scattering ME

## Measurement:

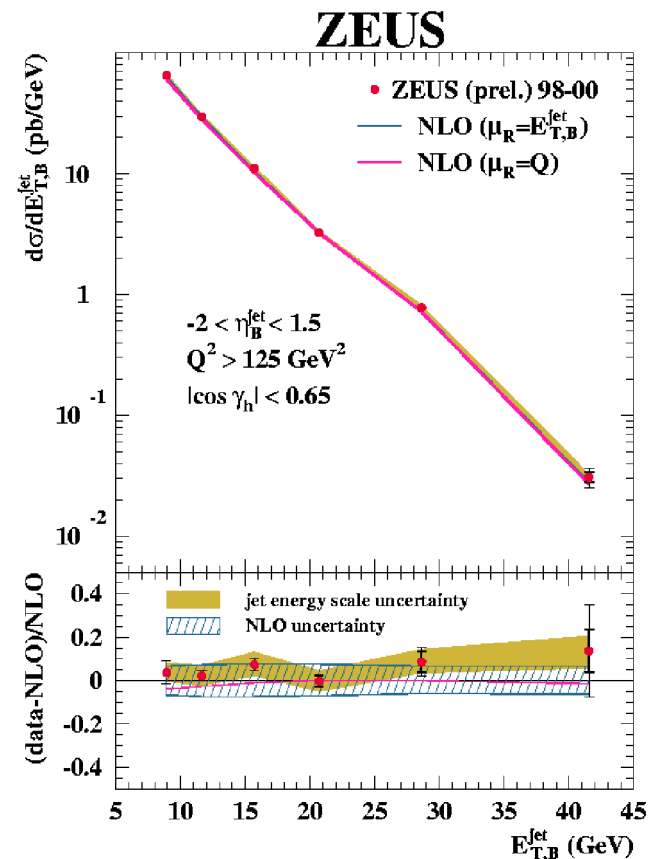
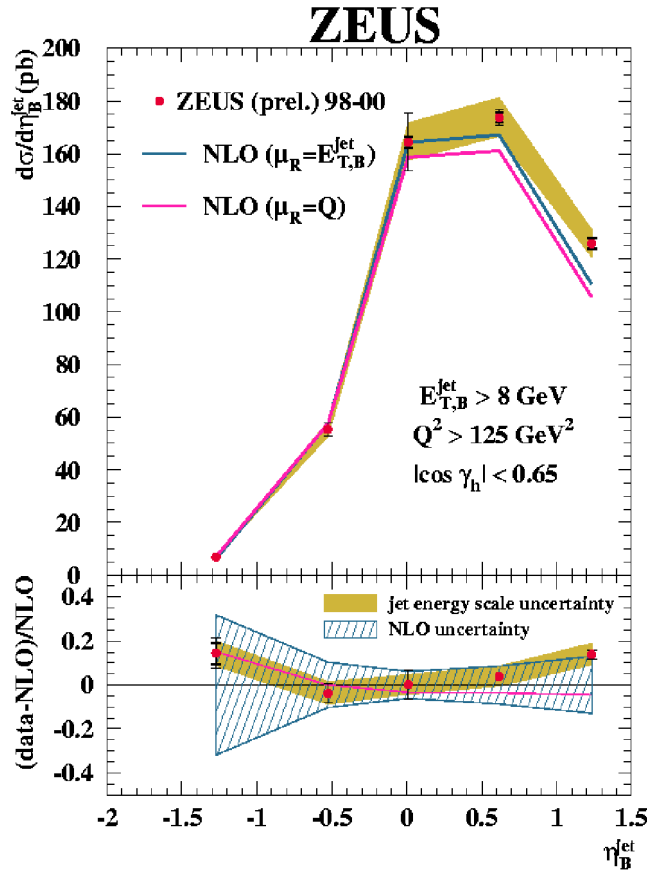
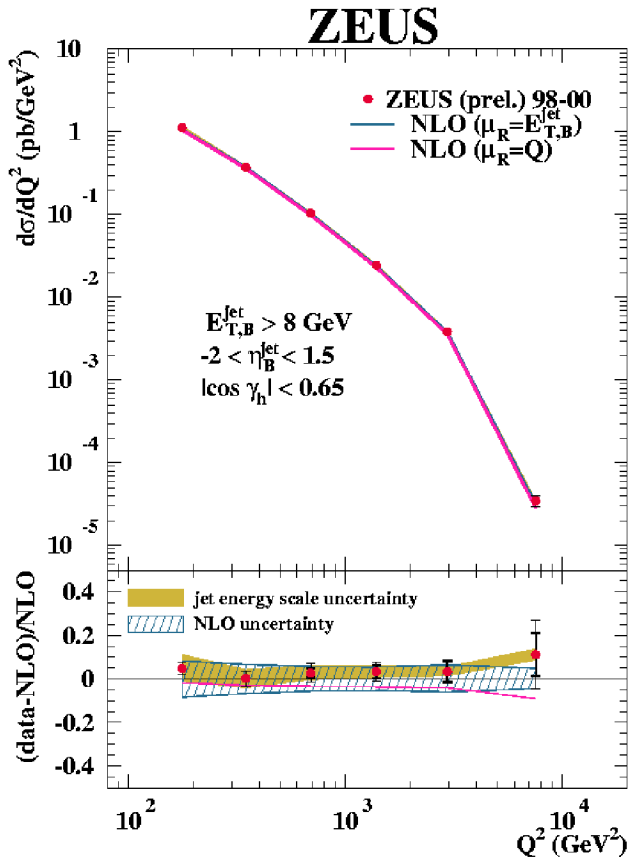
- Test concept of pQCD, factorization, universality of strong coupling and PDFs
- Assume factorization, pQCD ➔ **get  $\alpha_s$ , PDFs (important for LHC)**
- Also access to underlying gauge group, effect of exchanged bosons, parton dynamics in the proton,...

## Tools:

- $k_T$  cluster algorithm on cells or energy flow objects (DIS: in the Breit reference frame)
- Data corrected for detector and QED effects with LO MC models
- NLO corrected to hadron level with LO MC + parton shower +hadronisation models
- Latest PDFs like CTEQ6...
- Excellent understanding of jet energy scale (1-3%) (typically 10 % effect in xsection)

# Inclusive Jets (ZEUS)

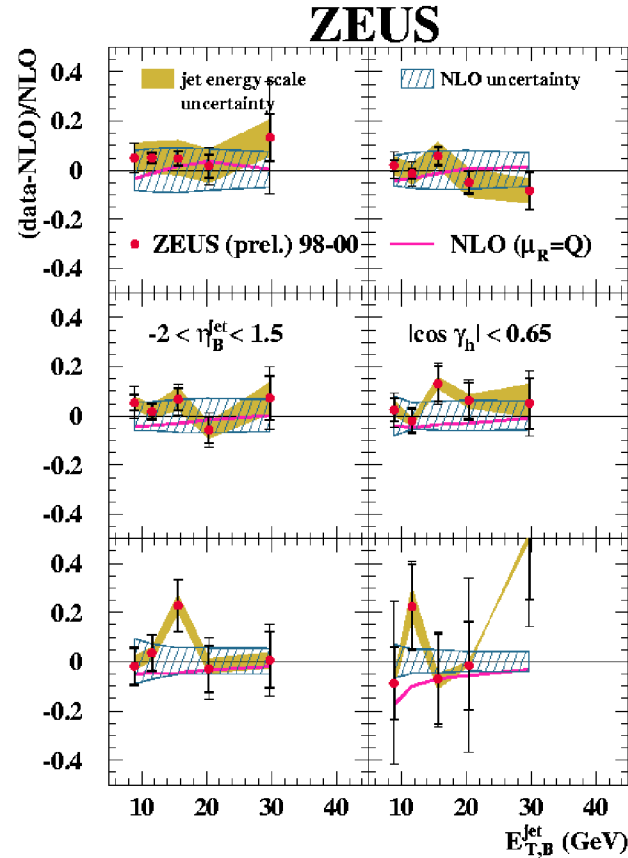
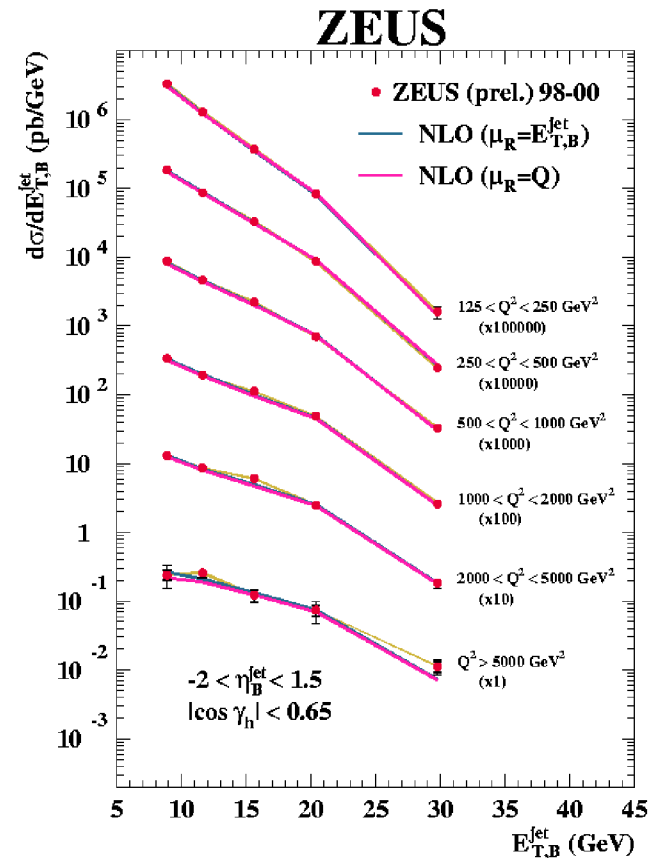
**Data:** 82 pb<sup>-1</sup>(98-00) **Selection:**  $Q^2 > 125 \text{ GeV}^2$ ,  $|\cos(\gamma_{\text{had}})| < 0.65$ ,  $E_{T,B} > 8 \text{ GeV}$ ,  $-2 < \eta_B < 1.5$



Data well described by the NLO (DISENT);  
 Experimental errors dominated by uncertainty on jet energy scale  
 Theoretical errors dominated by scale variation effect (missing higher orders ?)

# Inclusive Jets (ZEUS)

**Double differential:** inclusive jet cross sections in ET in different regions of  $Q^2$



Reminder: 96/97 inclusive jet measurement has been used in QCD fits and helped to reduce the error on gluon density at high  $x$

➔ gain from new analysis with higher statistic and higher  $\sqrt{s}$

- Data well described by NLO;
- $E_T$  and  $Q^2$  dependence ( $E_T$  dependence gets less steep as  $Q^2$  increases) indicates sensitivity to PDFs

# Extraction of $\alpha_s$

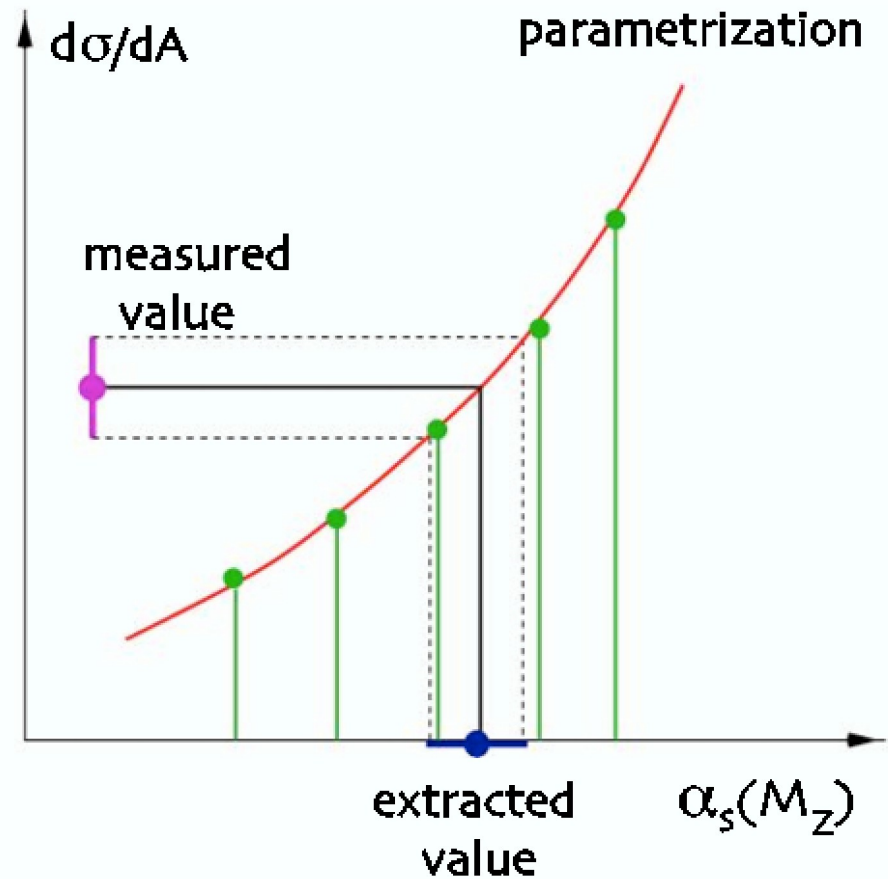
- Perform NLO calculation with different values of  $\alpha_s(M_Z)$

(The values of  $\alpha_s$  used correspond to those used in the different PDFs sets available (incl. jets: MRST99; multijets: CTEQ4A))

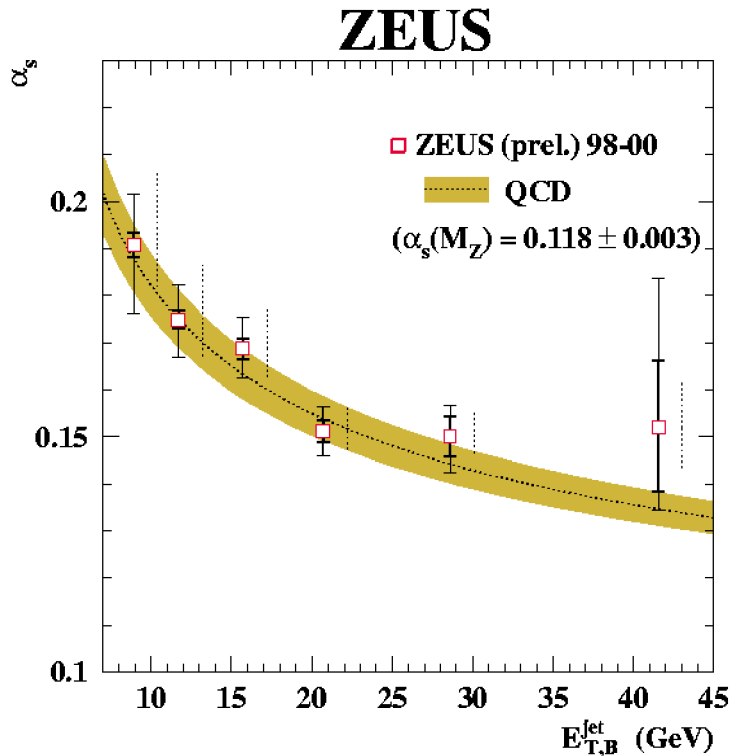
- Parametrize  $\alpha_s(M_Z)$  dependence of observable ( $d\sigma/dA$ ) in bin  $i$  according to

$$\frac{d\sigma_i}{dA} = C_1 \cdot \alpha_s(M_Z) + C_2 \cdot \alpha_s^2(M_Z)$$

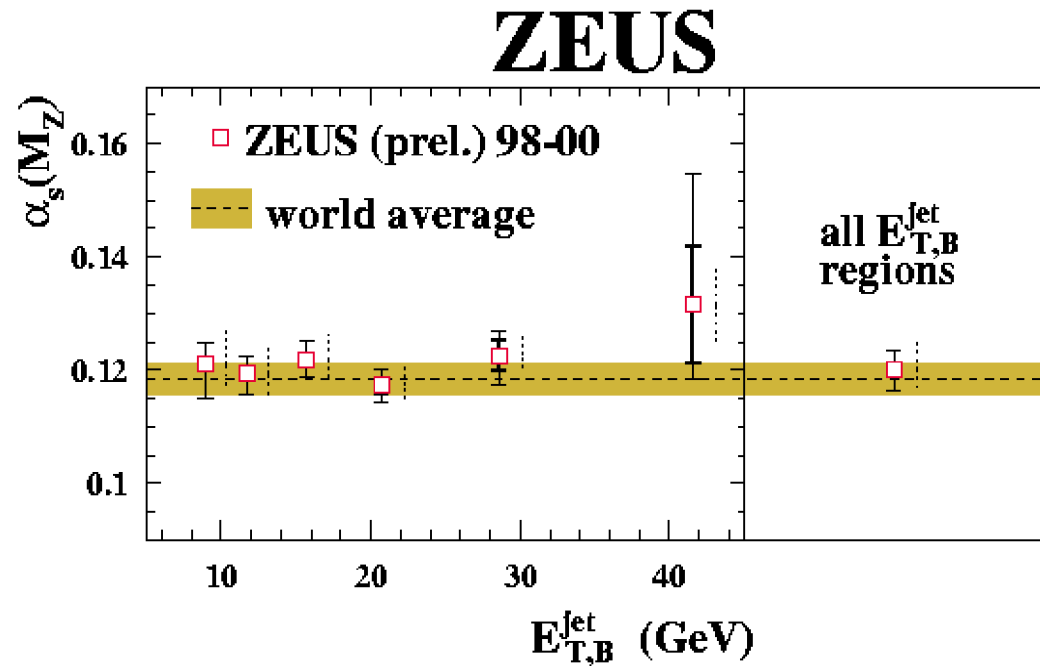
- Map measured  $d\sigma/dA$  to x-axis and extract  $\alpha_s(M_Z)$



# Inclusive Jets (ZEUS)



Demonstration of running coupling



Points compatible with each other and with world average

ZEUS inclusive jets:  $\alpha_s(M_Z) = 0.1196 \pm 0.0025$  (exp)  $\pm 0.0023$  (theo)

World average  $\alpha_s(M_Z) = 0.1187 \pm 0.0020$

H1 inclusive jets:  $\alpha_s(M_Z) = 0.1197 \pm 0.0016$  (exp)  $\pm 0.0047$  (theo)

# Inclusive Jets (H1)

## Data:

61 pb<sup>-1</sup> (99-00)

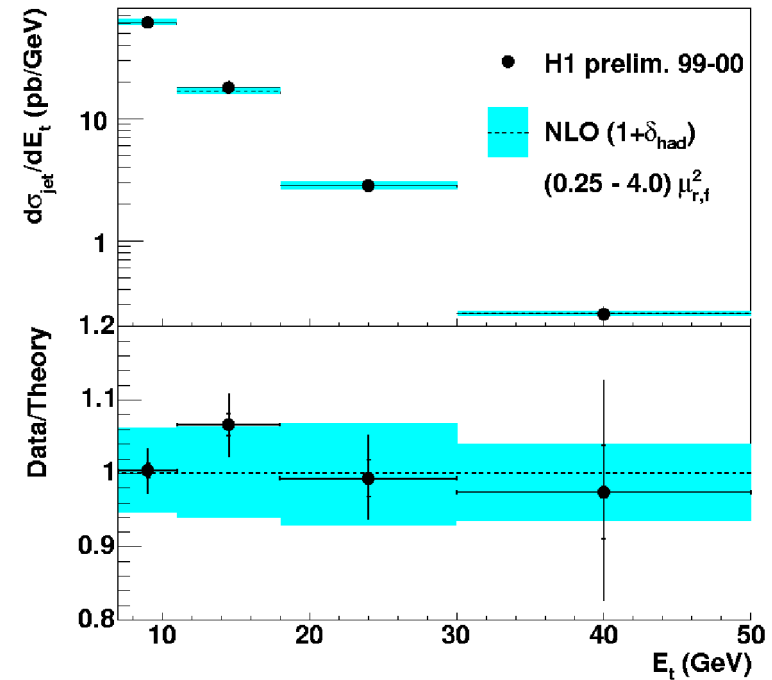
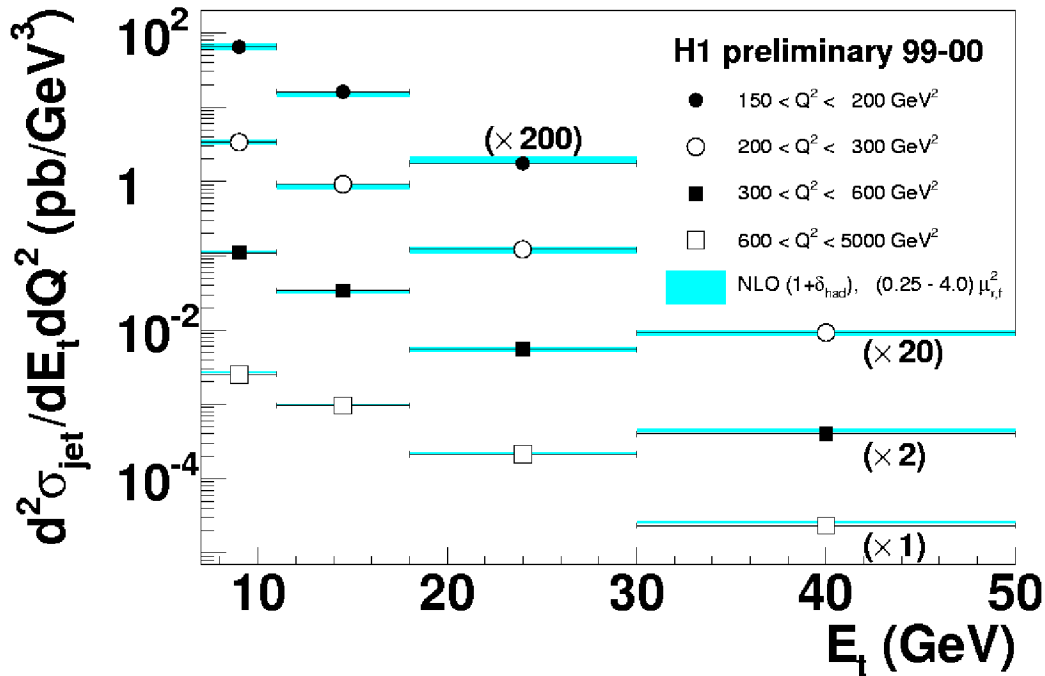
## Selection:

125 < Q<sup>2</sup> < 5000 GeV<sup>2</sup>

0.2 < y < 0.6

E<sub>T,B</sub> > 7 GeV, -1 < η<sub>L</sub> < 2.5

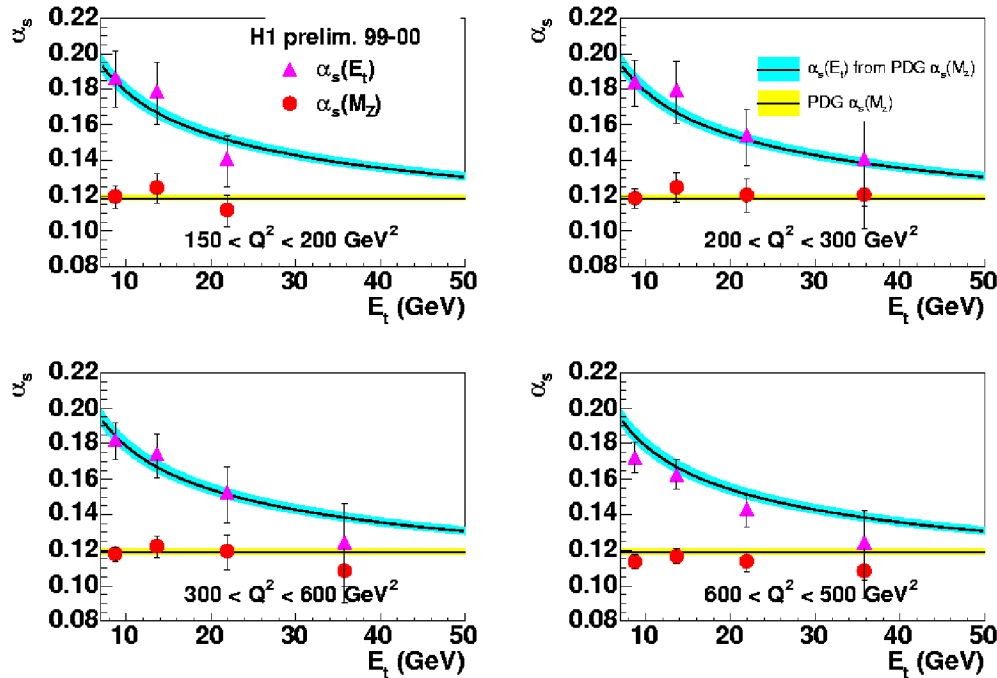
Similar phase space as ZEUS analysis; similar precision



Very good agreement of data and theory (NLOJET++/ CTEQ5M1) within all errors  
 Uncertainty dominated by theory (scale variation effect; missing higher orders!)

# Inclusive Jets (H1)

$\alpha_s(M_Z)$  extracted from double diff. xsections:



- $\alpha_s(M_Z)$  extracted from 15 data points
- All single measurements are consistent
- Combination of all points in one value
- Result consistent with world average and ZEUS inclusive jets
- Small experimental uncertainty
- Theory error dominates (missing higher orders) but remember:  $Q^2 < 5000 \text{ GeV}^2$ ; theoretical errors get smaller at high values of  $Q^2$

H1 inclusive jets:  $\alpha_s(M_Z) = 0.1197 \pm 0.0016(\text{exp}) \pm 0.0047(\text{theo})$

World average  $\alpha_s(M_Z) = 0.1187 \pm 0.0020$

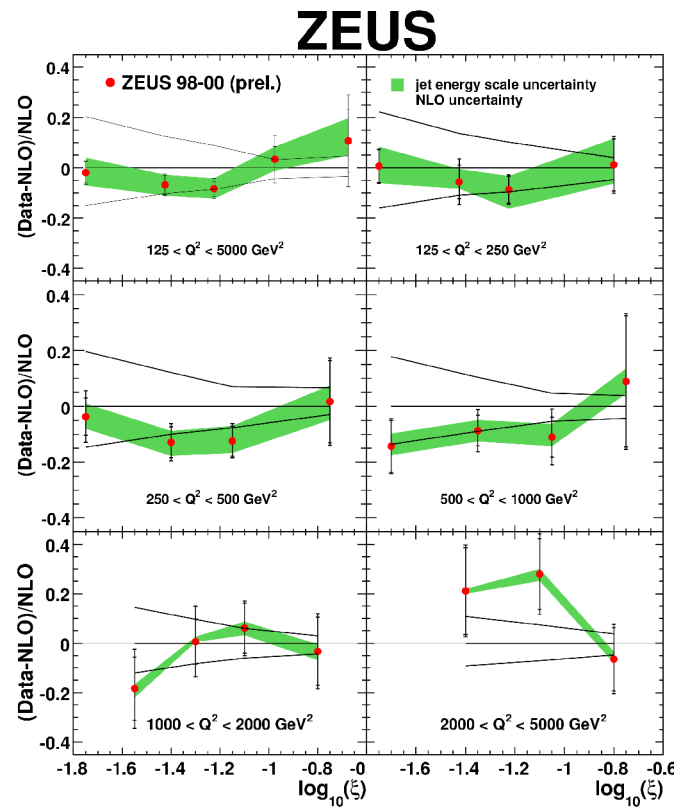
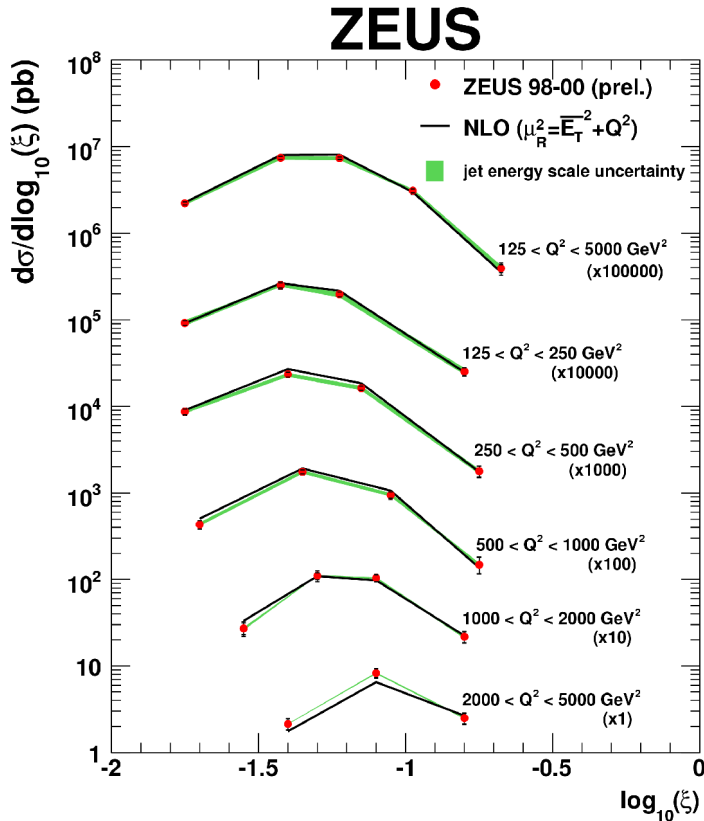
ZEUS inclusive jets:  $\alpha_s(M_Z) = 0.1196 \pm 0.0025(\text{exp}) \pm 0.0023(\text{theo})$



# Dijets (ZEUS)

Data: 82 pb<sup>-1</sup> (98-00)

Selection:  $Q^2 > 125 \text{ GeV}^2$ ,  $|\cos(\gamma_{\text{had}})| < 0.65$ ,  
 $E_{T,B}^{\text{jet}1(2)} > 12(8) \text{ GeV}$ ,  $-2 < \eta_B < 1.5$



**Idea:** PDFs characterized by  $Q^2$  and  $\xi$  → use double diff. Xsections for QCD fits (g at high  $\xi$ )

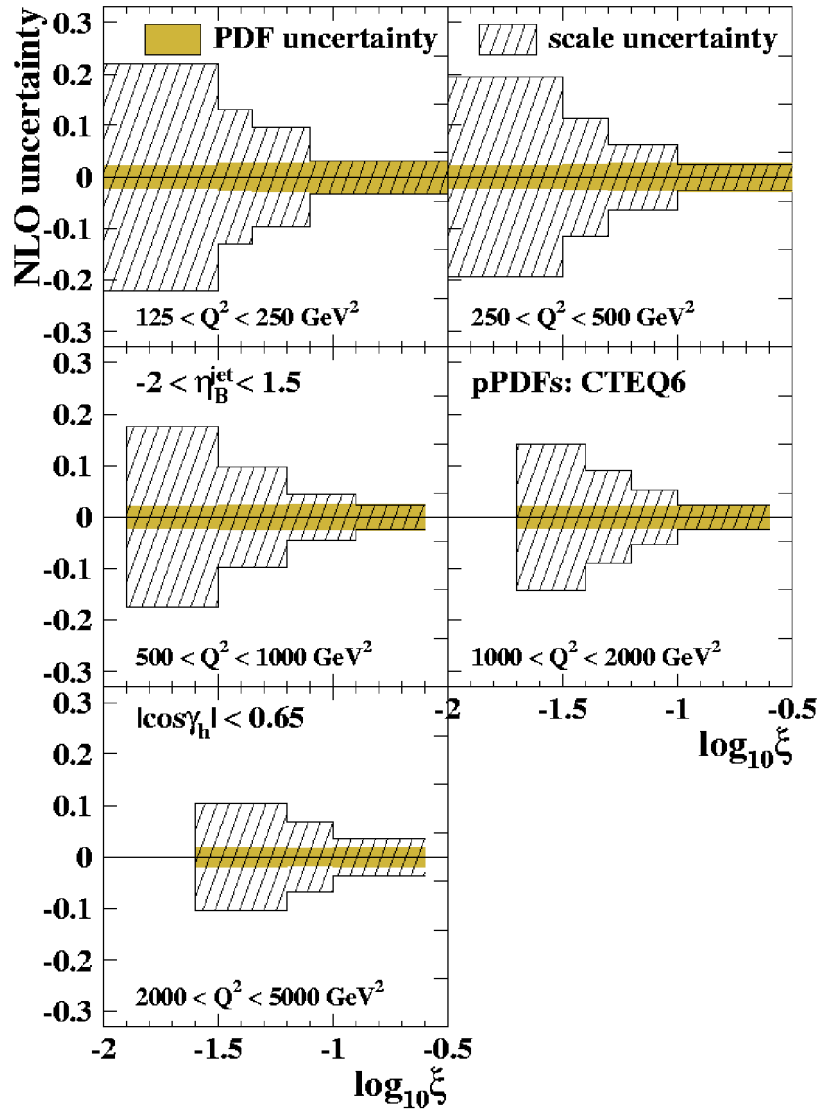
In dijet events:

$$\xi = x_{Bj} \left( 1 + \frac{M_{jj}}{Q^2} \right)$$

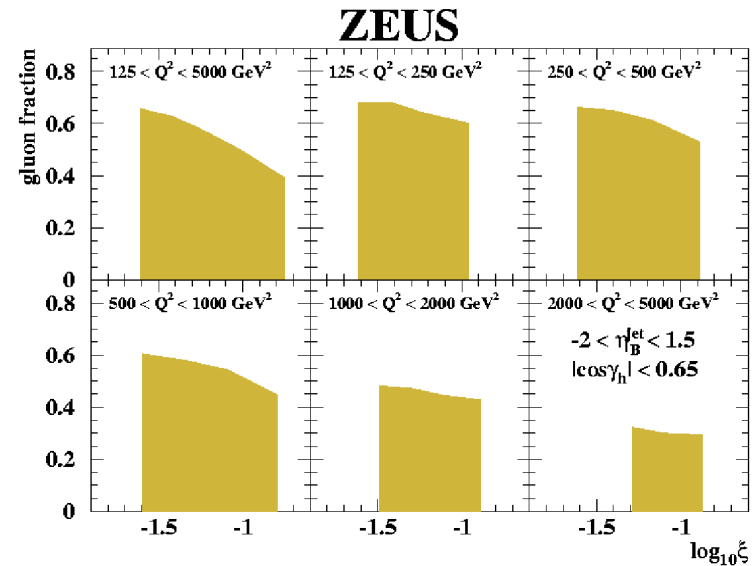
- Data well described by NLO (DISENT/CTEQ6);
- Theoretical errors are dominating in most regions
- At high  $Q^2$  statistic is getting low (important to look at HERA II data!)

# Dijets (ZEUS)

## NLO uncertainty:




## Gluon fraction:



## Theoretical errors:

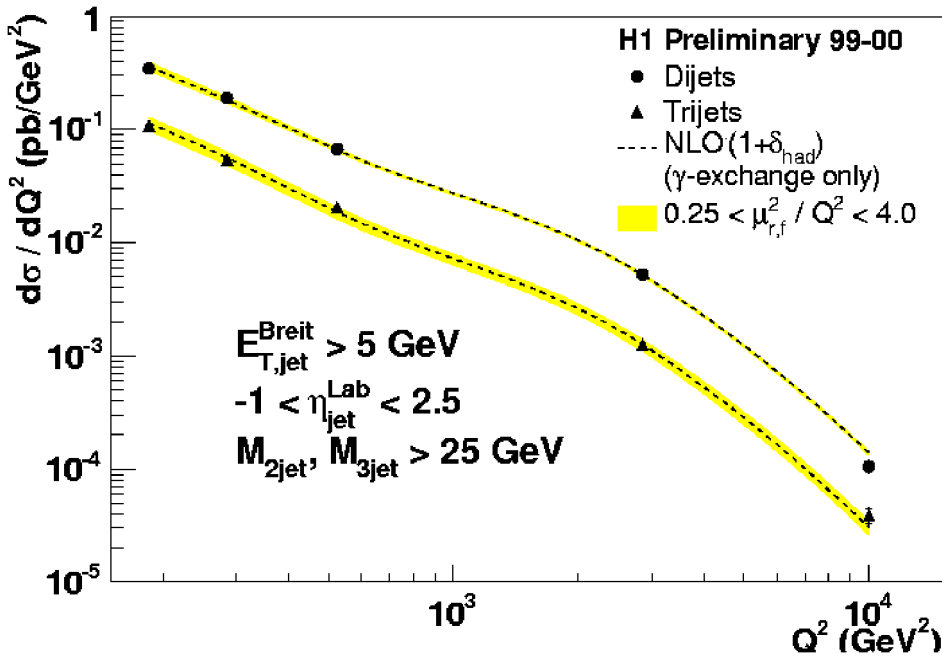
- Scale uncertainty 5-20 %, large at small  $\xi$ ,  $Q^2$
- PDF uncertainties  $\approx 3$  %, significant at high  $\xi$
- Gluon fraction decreases with increasing  $\xi$  and  $Q^2$  but still substantial gluon contribution ( $> 30$  %)
- Also gluon uncertainty sizable (not shown)

 use in NLO QCD fits of PDFs

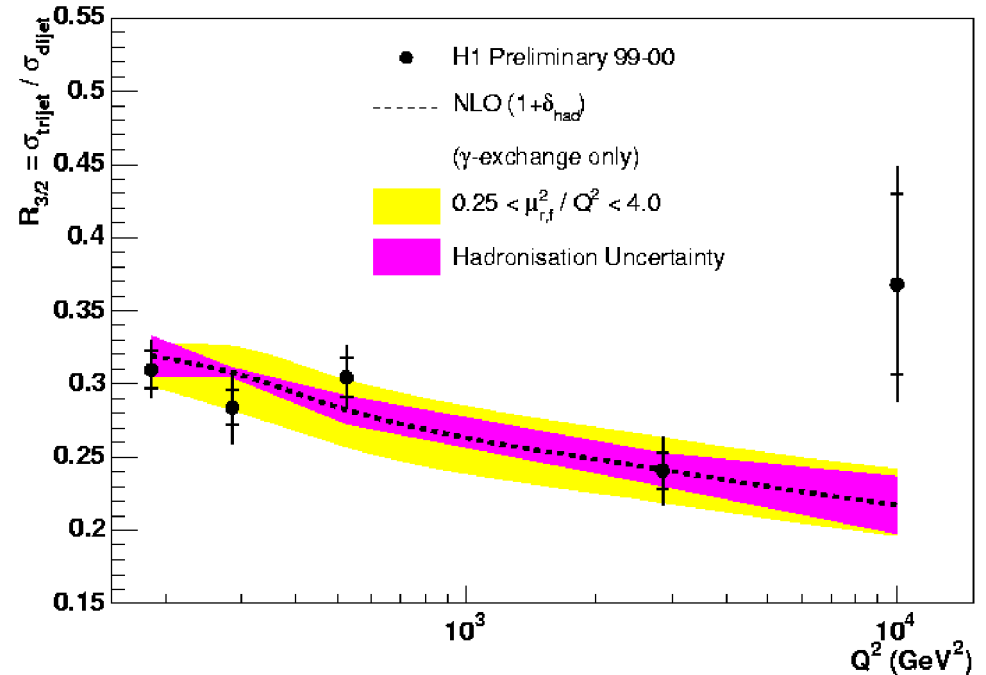
# Multijets (H1)

**Data:**  $65 \text{ pb}^{-1}$  (99-00) **Selection:**  $Q^2 > 125 \text{ GeV}^2$ ,  $0.2 < y < 0.6$ ,  
 $E_{T,B} > 5 \text{ GeV}$ ,  $M_{jj} > 25 \text{ GeV}$ ,  $-1 < \eta_L < 2.5$

## Di -and trijets:



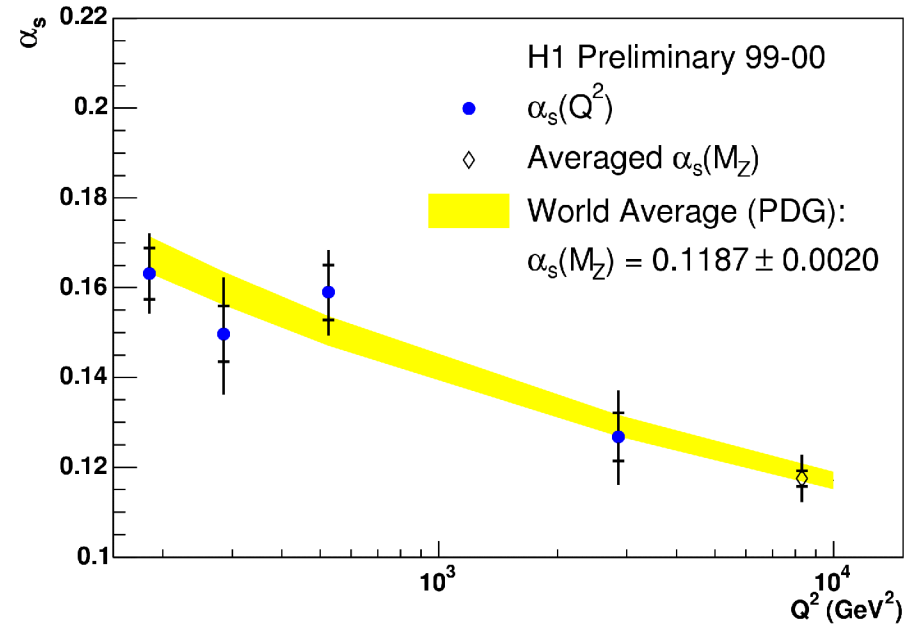
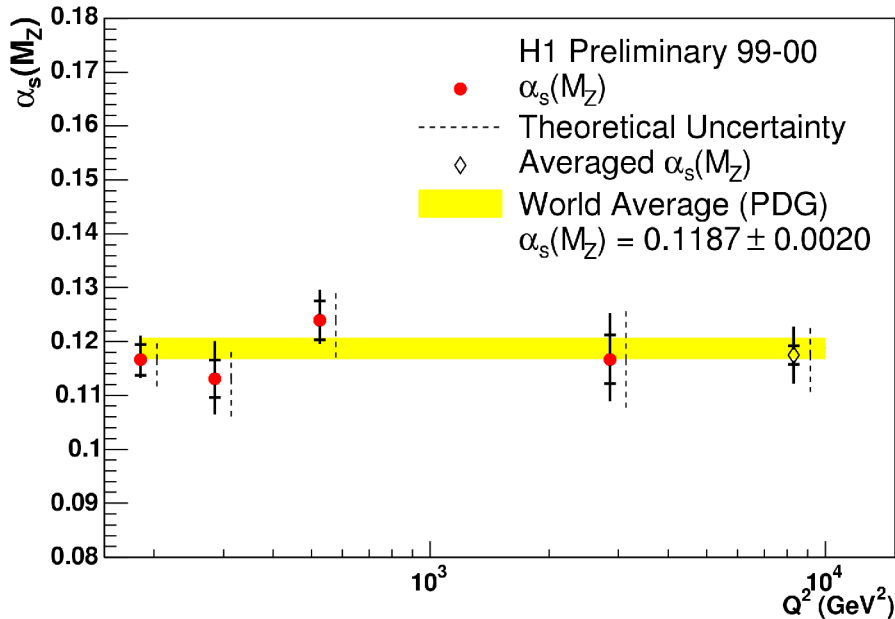
## Ratios:



- NLO QCD (NLOJET++ / CTEQ5M) provides excellent description of di-and trijet data
- Last data point in ratio not described;  $Z^0$  exchange not included in NLO calculation
- In the 3/2-jet ratio some theo. and exp. errors cancel ➡ use this quantity for  $\alpha_s$

# Multijets (H1)

## Strong coupling from 3/2-jet ratio:



- Values are compatible with each other and world average
- Nice demonstration of running coupling

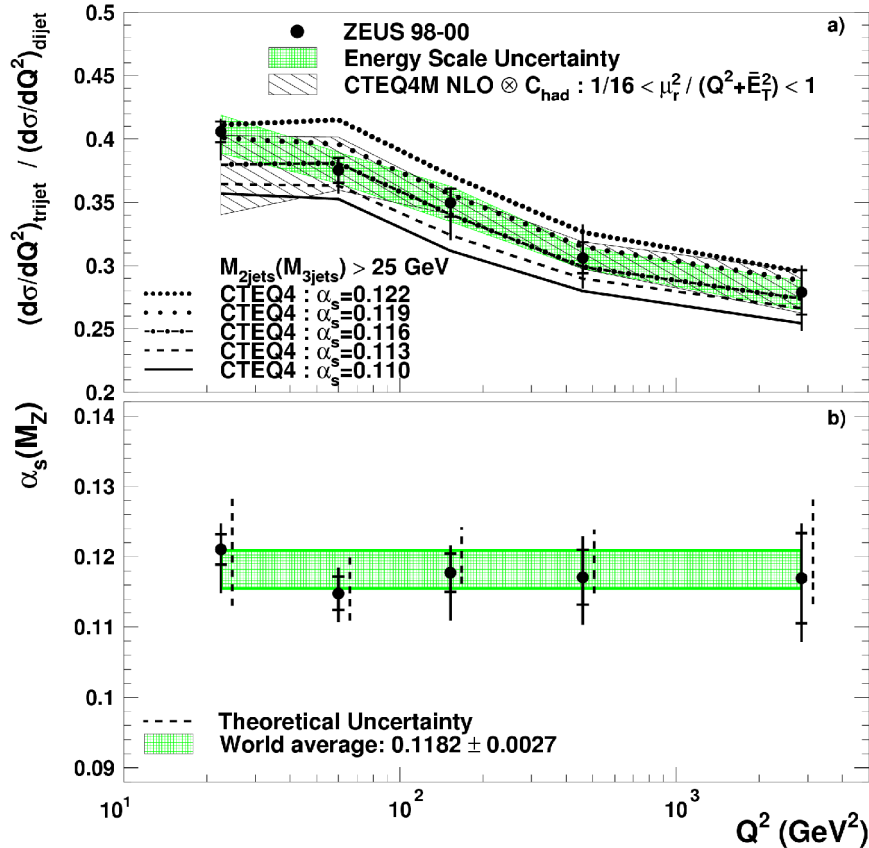
H1 multijets:  $\alpha_s(M_Z) = 0.1175 \pm 0.0017 (stat) \pm 0.0050 (syst) \pm 0.0061 (theo)$

H1 incl. jets:  $\alpha_s(M_Z) = 0.1197 \pm 0.0016 (exp) \pm 0.0047 (theo)$

- Errors significantly larger than for inclusive jets
- Systematic and theoretical errors are of the same size

# Multijets (ZEUS)

## ZEUS



### Data:

82 pb<sup>-1</sup> (98-00)

### Selection:

$10 < Q^2 < 5000 \text{ GeV}^2$ ,  $0.04 < y < 0.6$ ,

$E_{T,B} > 5 \text{ GeV}$ ,  $M_{jj} > 25 \text{ GeV}$ ,  $-1 < \eta_L < 2.5$

Using 3/2-jet ratio  $\rightarrow$  cancellation of errors (theo.) allows extraction of  $\alpha_s$  with good precision down to very low  $Q^2$  ( $Q^2 = 10 \text{ GeV}^2$ )

ZEUS multijets:  $\alpha_s(M_Z) = 0.1179 \pm 0.0013 (stat) \pm 0.0037 (exp) \pm 0.0055 (theo)$

H1 multijets:  $\alpha_s(M_Z) = 0.1175 \pm 0.0017 (stat) \pm 0.0050 (syst) \pm 0.0061 (theo)$

# Event Shapes: Motivation and basic concepts

Alternative approach to non-perturbative hadronisation effects: **Power Corrections (PC)**

PC calculable for inclusive quantities: event shapes

$$\tau = 1 - \frac{\sum_i |\vec{p}_i \cdot \vec{n}|}{\sum_i |\vec{p}_i|}$$

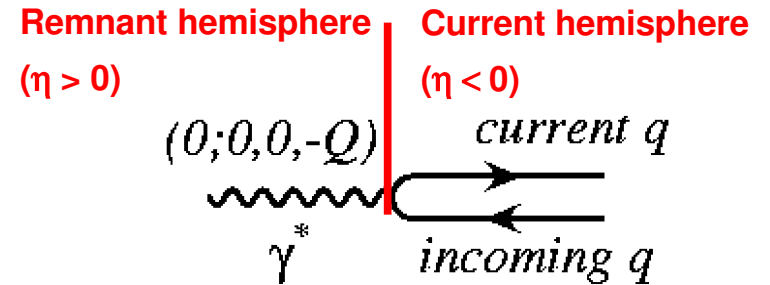
Thrust

$$B = \frac{\sum_i |\vec{p}_i \times \vec{n}|}{\sum_i |\vec{p}_i|}$$

Jet broadening

$$M = \frac{(\sum_i E_i)^2 - |\sum_i \vec{p}_i|^2}{(2 \sum_i |E_i|)^2}$$

Jet invariant mass



PC introduces new parameter:  $\alpha_0(\mu_I) = \frac{1}{\mu_I} \int_0^{\mu_I} \alpha_{eff}(\mu) d\mu$  ... supposed to be universal for all variables

Mean values  
(NLO + PC):

$$\hat{V}(\alpha_s, \alpha_0) = \hat{V}_{PT}(\alpha_s) + \hat{V}_{pow}(\alpha_s, \alpha_0)$$

Differential cross sections  
(NLO+NLL + PC):

$$\frac{d\sigma}{dV}(V) = \frac{d\sigma}{dV_{PT}}(V - \hat{V}_{pow})$$

NLO+NLL: different matching schemes  
Avoid double counting!

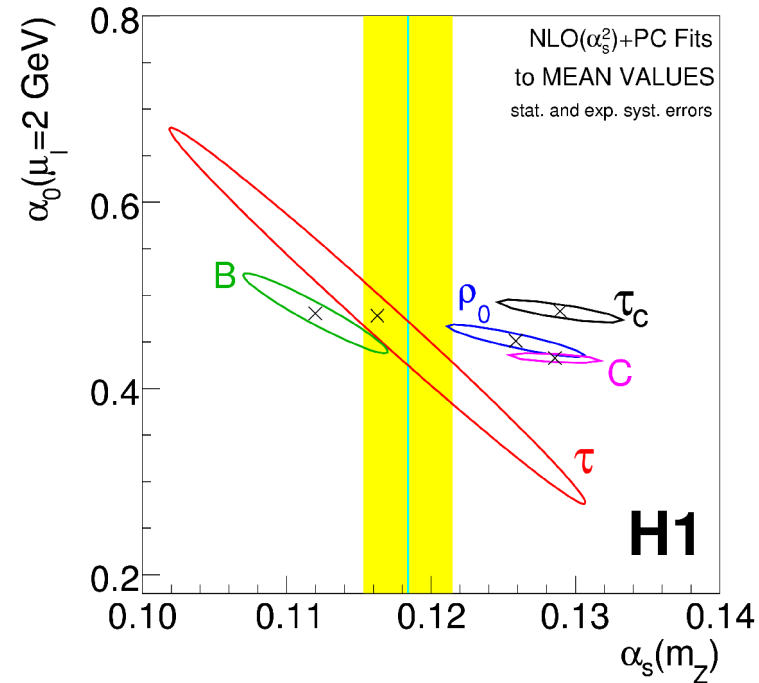
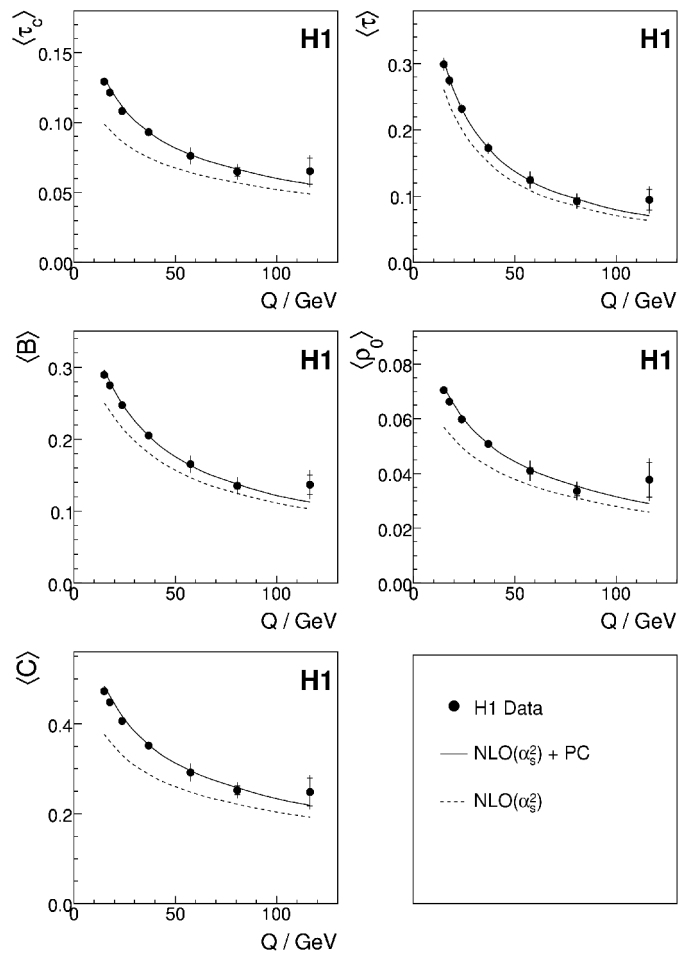
Measurement:

- Test Power Correction ansatz
- Extract  $\alpha_s$  and  $\alpha_0$

# Event Shapes (H1)

**Data:** 106 pb<sup>-1</sup> (95-00)    **Selection:** 196 < Q<sup>2</sup> < 40000 GeV<sup>2</sup>, 0.1 < y < 0.7

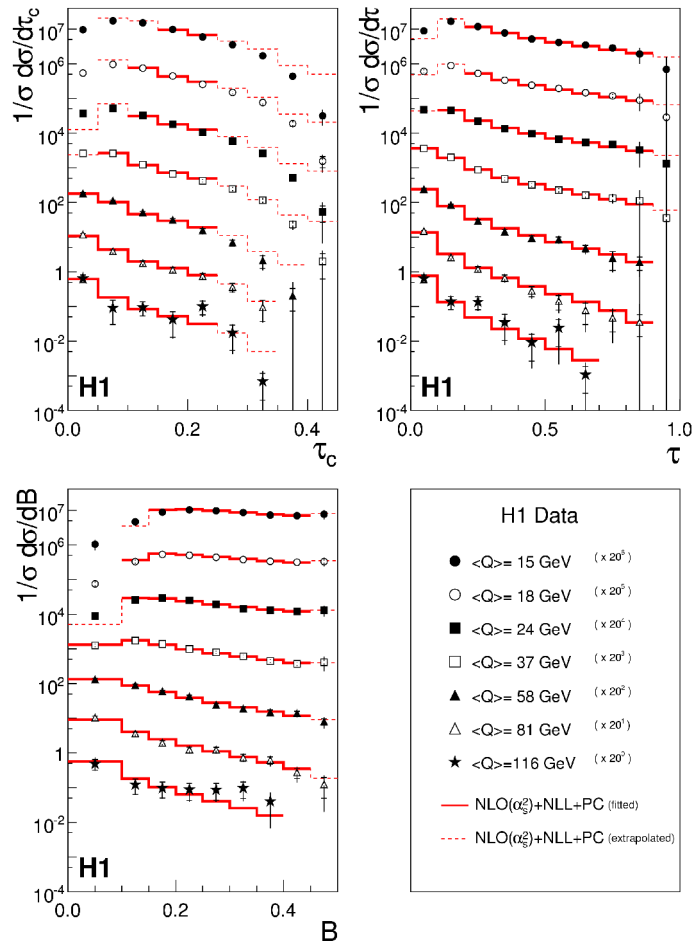
**Mean values compared to NLO QCD fits +PC : nice description of the data**



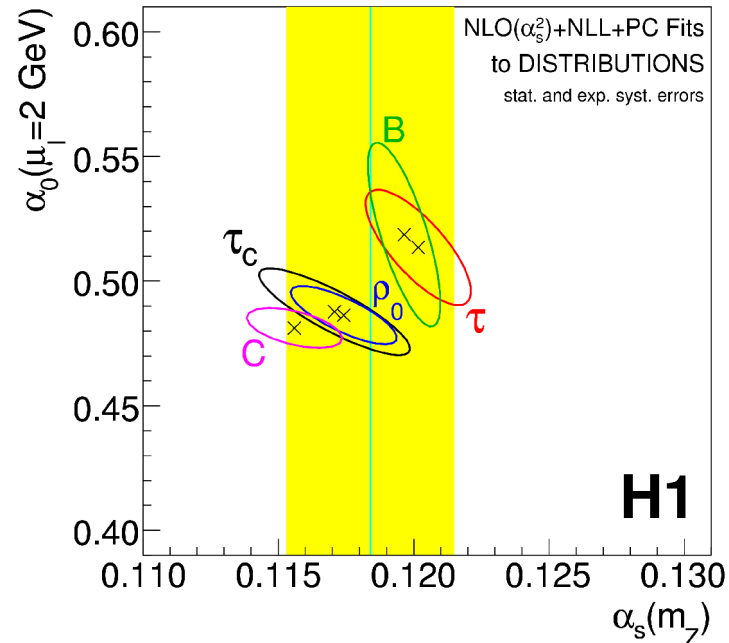
- Extracted  $\alpha_0$  values  $\approx 0.45 - 0.5$  (universality at 10% level)
- Extracted values of  $\alpha_s$  show a rather large spread

# Event Shapes (H1)

## Differential cross sections:



## Extracted $\alpha_0$ and $\alpha_s$ values:



- Consistent values for  $\alpha_0$  and  $\alpha_s$  (maximal difference: two STDV)
- $\alpha_s$  in good agreement with world average
- $\alpha_0 \approx 0.5$  universal within 10%

$$\alpha_s(M_Z) = 0.1198 \pm 0.0013 (\text{exp}) \pm 0.0050 (\text{theo}) \quad (\text{in good agreement with H1. incl jets})$$

$$\alpha_0 = 0.476 \pm 0.008 (\text{exp}) \pm 0.039 (\text{theo})$$

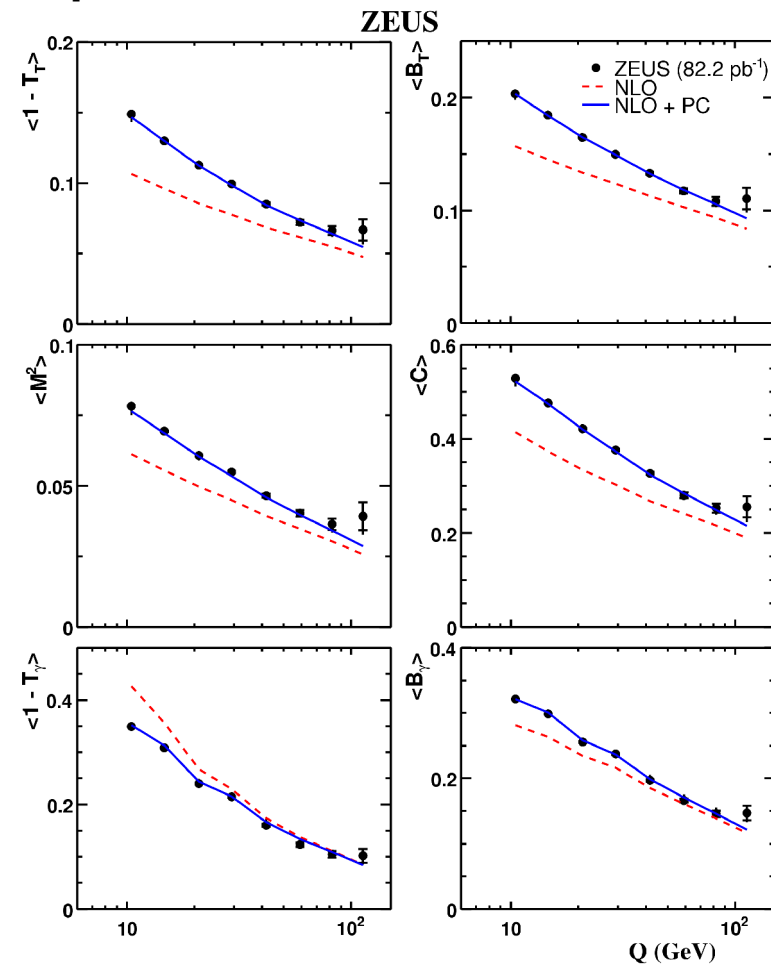
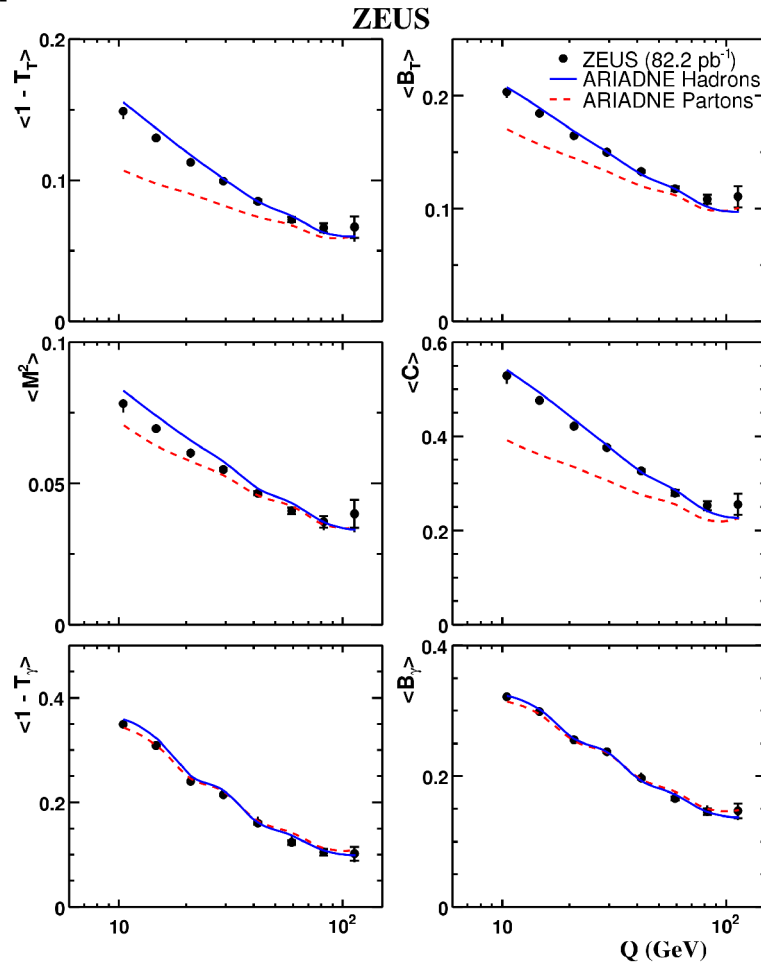


# Event Shapes (ZEUS)

**Data:** 82 pb<sup>-1</sup> (98-00)    **Selection:** 80 < Q<sup>2</sup> < 20480 GeV<sup>2</sup>, 0.0024 < x < 0.6, 0.04 < y < 0.9

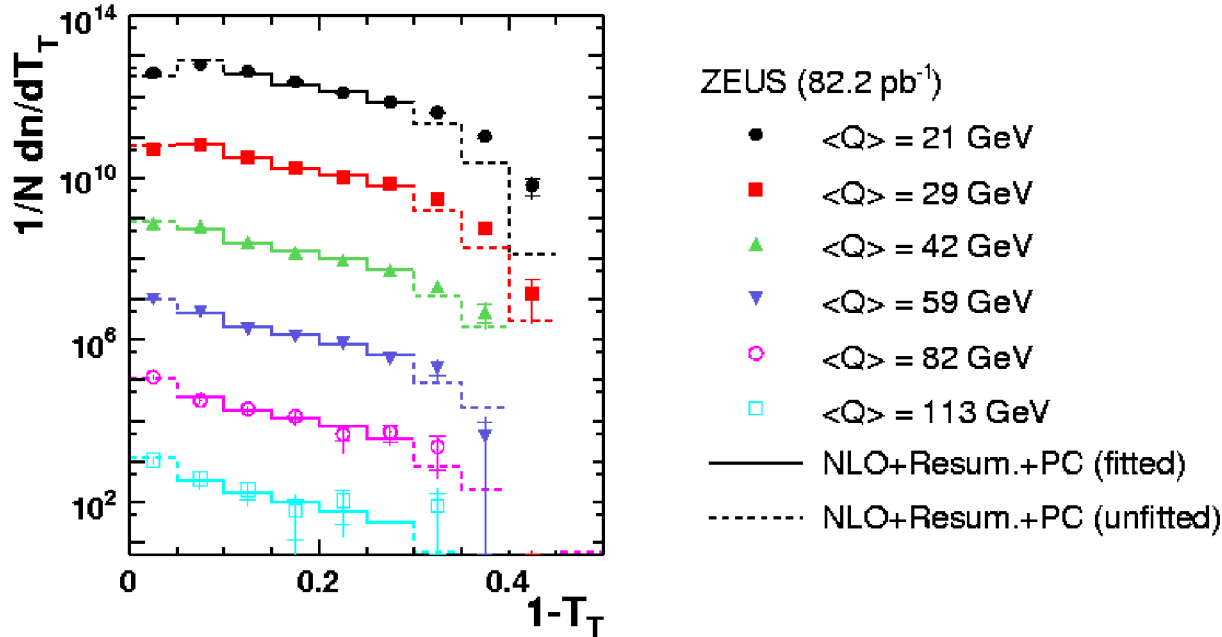
**Comparison of mean values to ARIADNE:**

**Comparison of mean values to NLO+PC:**



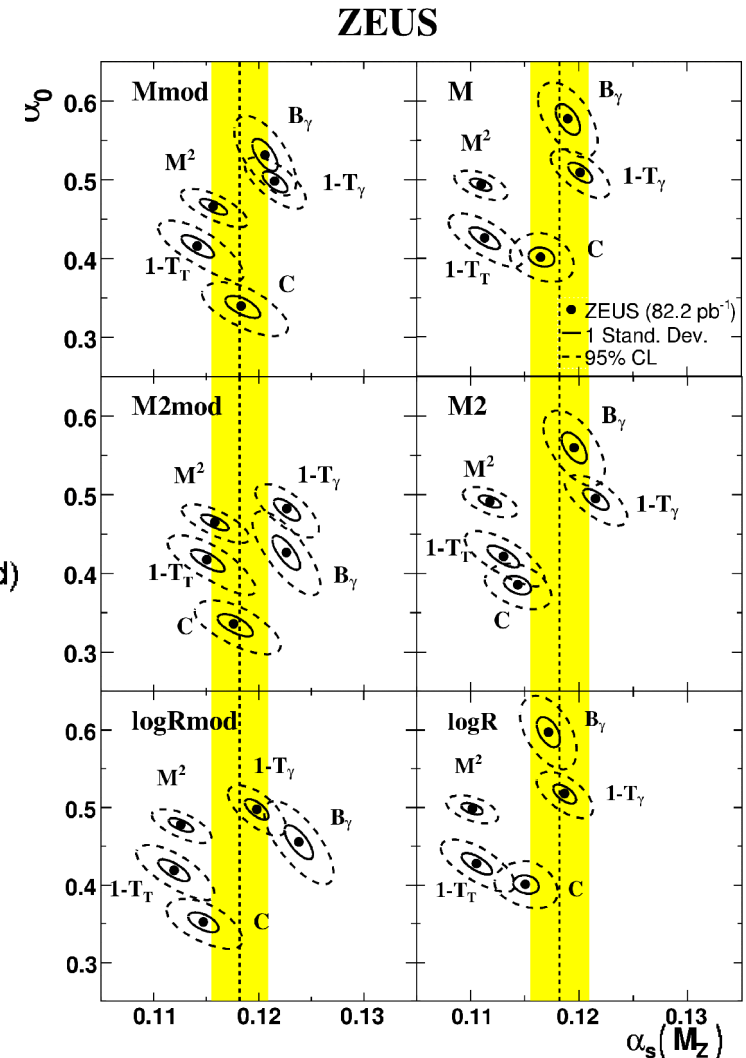
# Event Shapes (ZEUS)

## Differential cross sections:



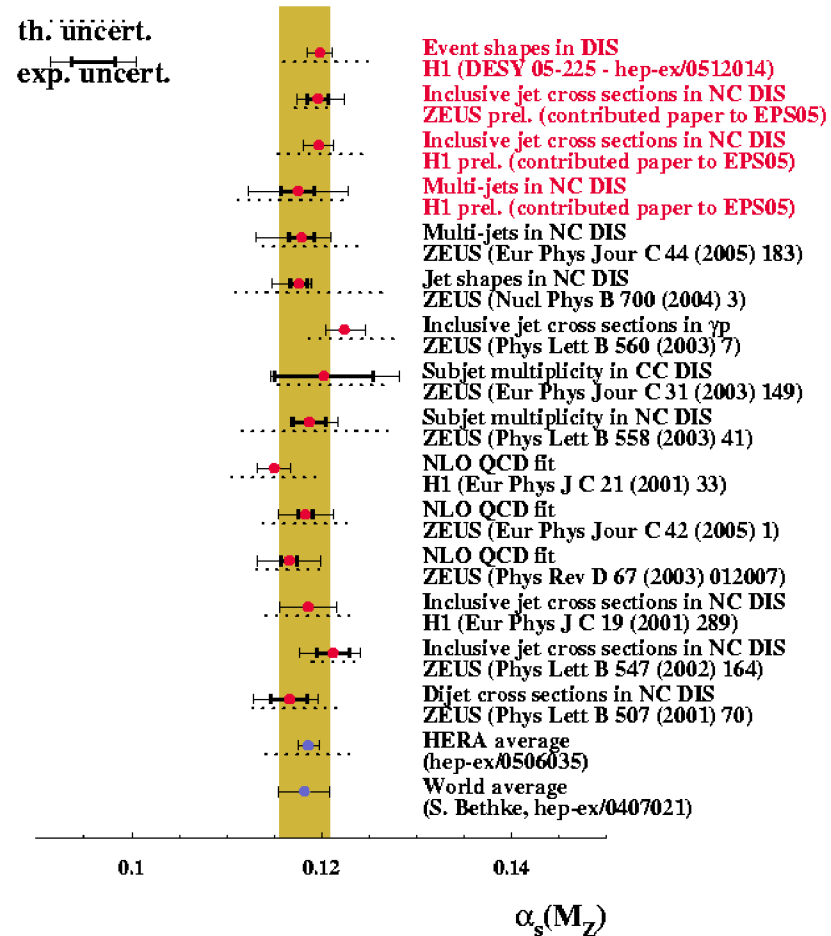
## Extracted values of $\alpha_s$ and $\alpha_0$ for different matching schemes (from differential xsections)

- Results depend on the scheme used.
- Large spread of extracted  $\alpha_0$  (universality?)
- Could indicate problems in theoretical description of the data.



# Summary

- Measurements demonstrate excellent understanding of pQCD; concepts of factorization and PDF universality work very well.
- Power correction gives nice description of mean event shape variables but results depend on matching scheme (could indicate problems with PC)
- Very precise extraction of  $\alpha_s$ ; values are consistent with each other and world average.
- In many regions (low  $Q^2$ ,  $E_T$ ,  $M_{jj}$ ) errors are dominated by scale variation effects; higher orders (NNLO) would really help.
- Correction of NLO is done with LO MC+PS; would be great to have NLO+PS for consistency.
- Analyses shown based on HERA I data: at high  $Q^2$ ,  $E_T$ ,  $M_{jj}$ , and  $\xi$  statistic is getting low (dominating error).
- HERA II already delivered more than  $350 \text{ pb}^{-1}$ : will allow even more precise measurements.



HERA average:  $\alpha_s(M_Z) = 0.1186 \pm 0.0011 (\text{exp}) \pm 0.0050 (\text{theo})$  (June 2005)