



# Multijet Final States at HERA



Results from ZEUS

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- Multijets at low- $x$  in DIS
- Multijets in Photoproduction
- Three-Jet Angular Correlations in DIS

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# Multijets



- Multijet events access parton dynamics at high order pQCD.
- Variables in Multijet systems test different fundamental QCD properties.

Analyses presented:

- Multijets at low-x in DIS
  - DGLAP parton evolution at low- $x_{Bj}$
- Multijets in Photoproduction
  - 3-,4-Jets in PhP
  - First analysis of four-jet events in photoproduction at HERA
  - Test/tune MPI-models
- Three-Jet Angular Correlations in DIS
  - Test underlying gauge symmetry

# Multijets at low- $x$ in DIS

- DGLAP evolution sums over  $\ln(Q^2)$  terms.
  - predicts strong ordering of cascading partons in  $k_T$  and  $x$
  - well tested at medium to high  $Q^2$ .
- Examine QCD evolution at
  - low- $x_{Bj}$  ( $10^{-4} < x_{Bj} < 10^{-2}$ )
  - low- $Q^2$  ( $10 \text{ GeV}^2 < Q^2 < 100 \text{ GeV}^2$ ).
- Study angular correlations between two highest- $E_T$  jets in hadronic-center-of-mass frame

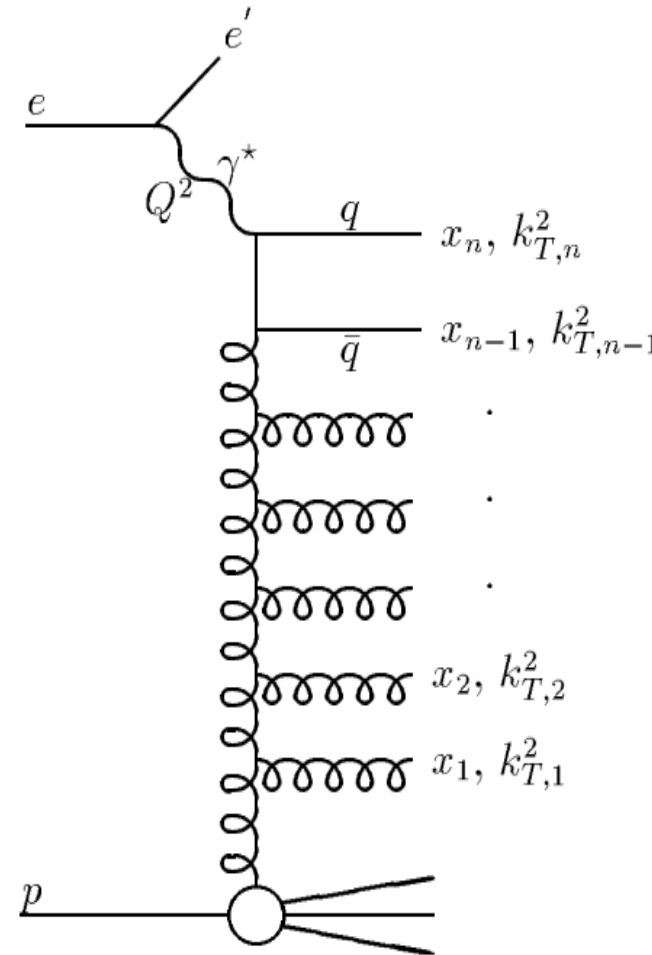
Jet selection:

2(3) jets in HCM frame

- $E_T > 7/5/5 \text{ GeV}$
- $-1.0 < \eta_{\text{jet,lab}} < 2.5$

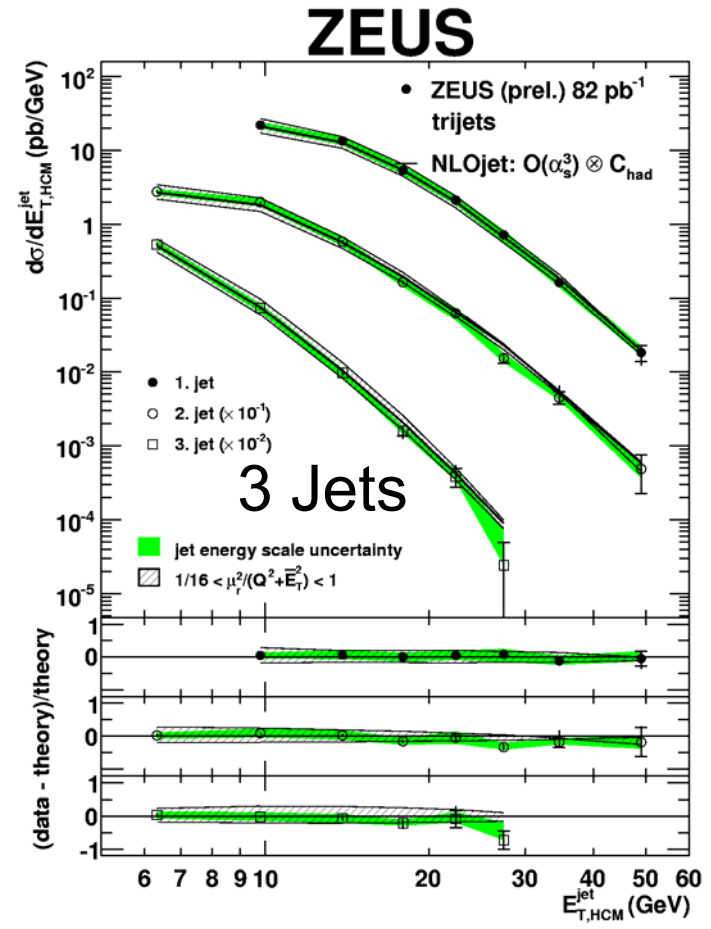
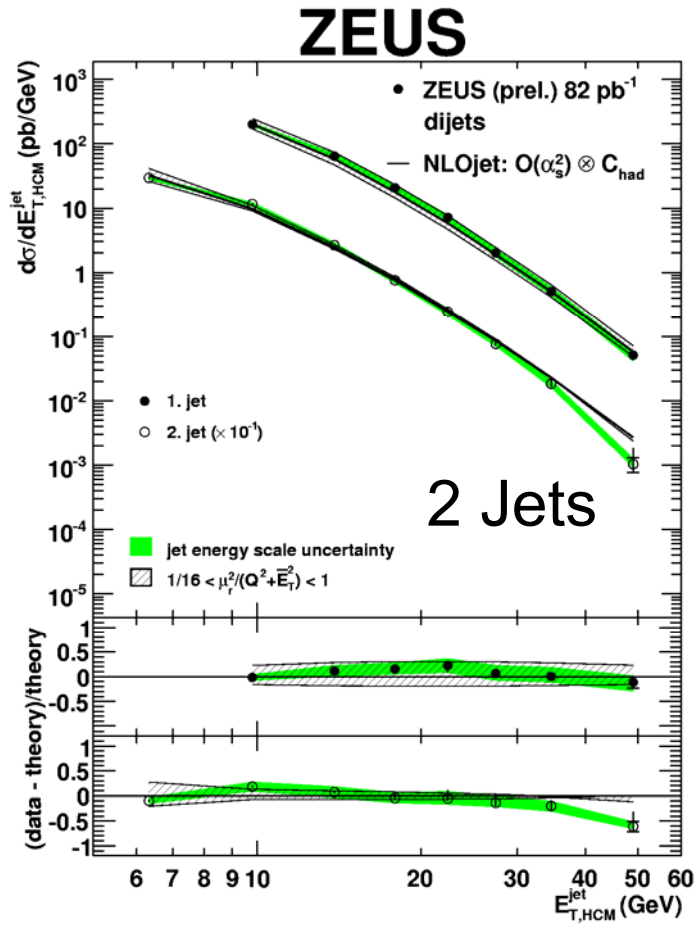
NLO Calculation:

- NLOjet
- $O(\alpha_s^2)$  for Dijets
- $O(\alpha_s^3)$  for Trijets
- $O(\alpha_s^3)$  for Dijets in a restricted phase space



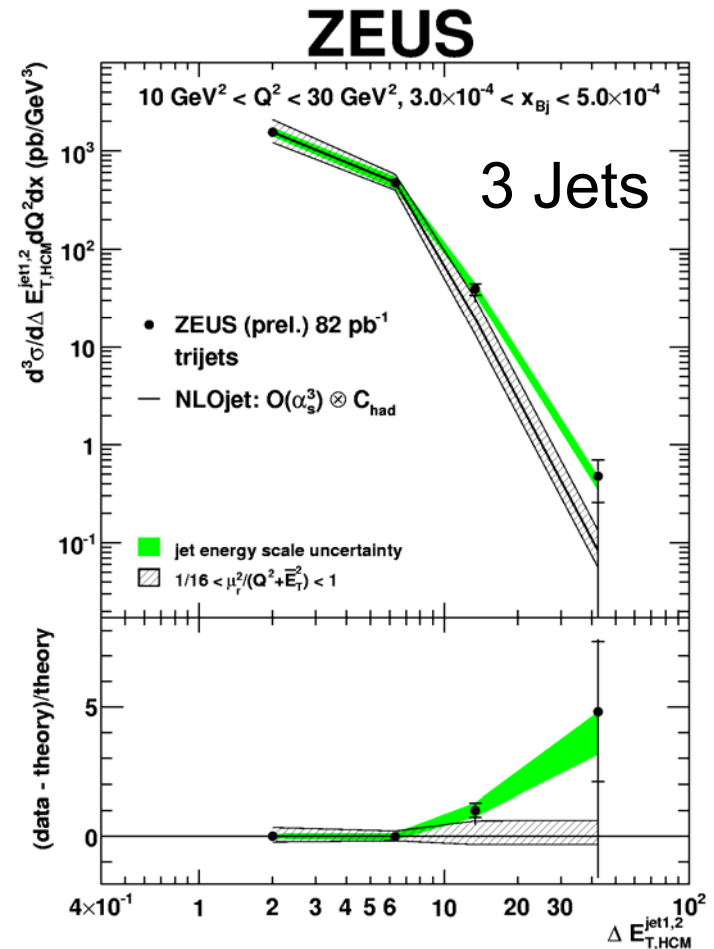
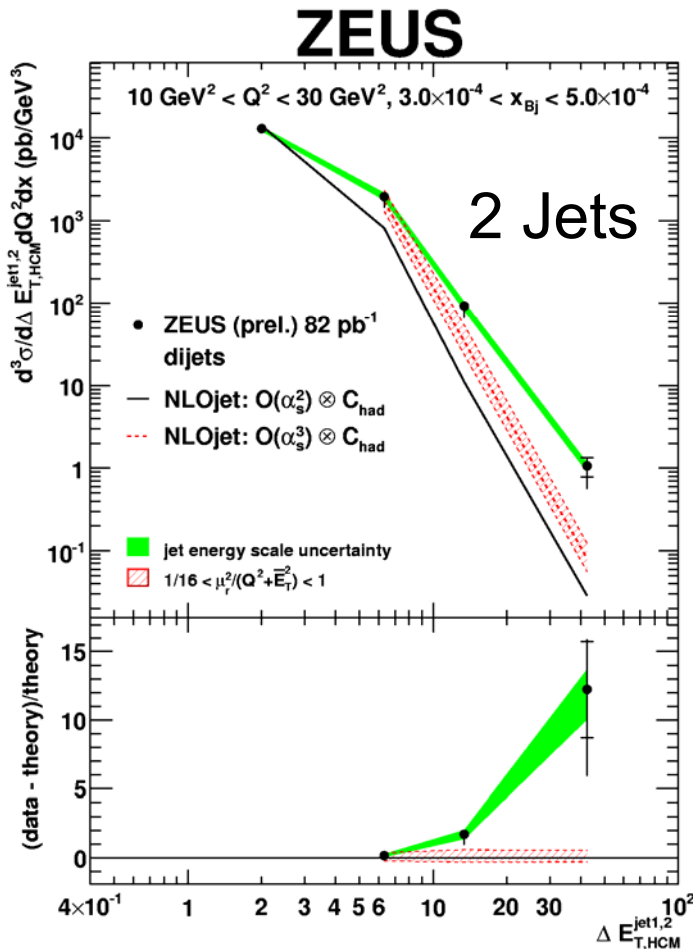


# Di-, Trijet cross sections vs. $\text{Jet-}E_{T, \text{HCM}}^{\text{jet}}$



NLOjet describes data well, except at highest  $E_{T, \text{jet}2(3)}$

# $\Delta E_T^{\text{HCM}}$ btw 2 highest- $E_T$ Jets



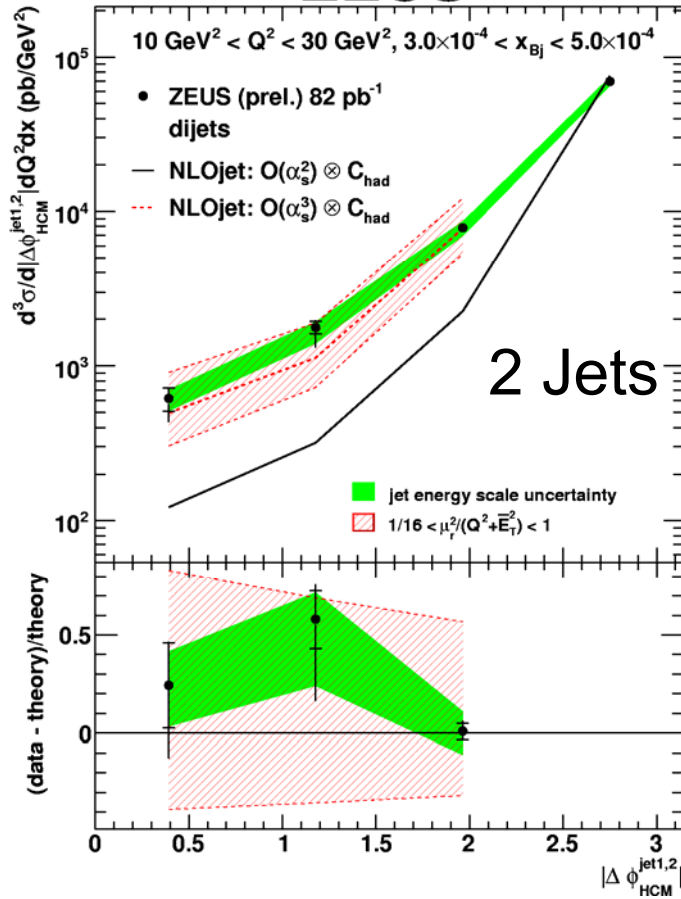
NLOjet at lowest order does not describe  $\Delta E_T$  at high  $\Delta E_T$ ,  
 NLOjet  $O(\alpha_s^3)$  gives slight improvement for dijets.



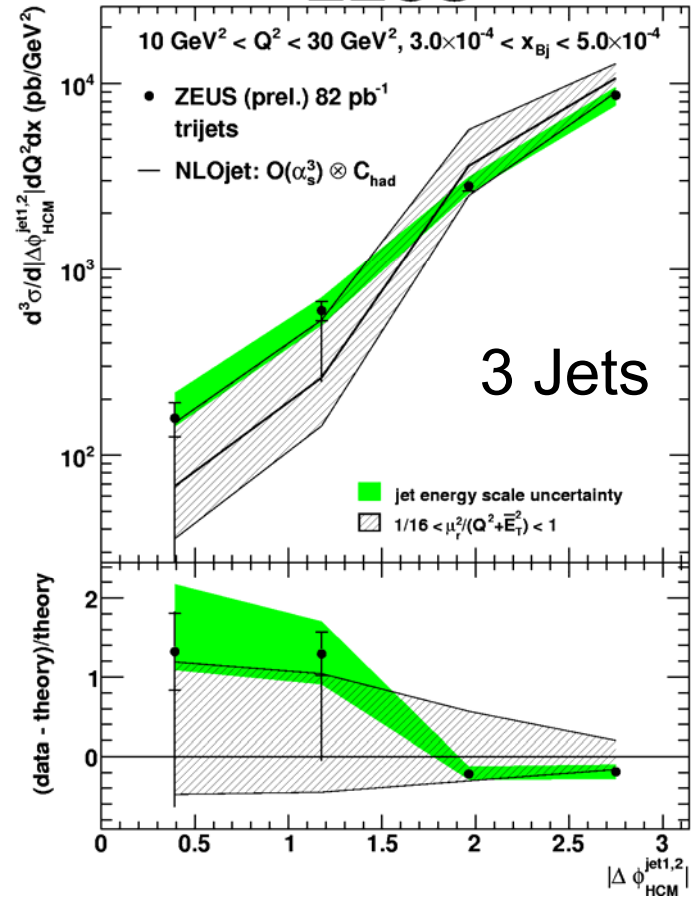
# $|\Delta\Phi^{\text{HCM}}|$ btw 2 highest- $E_T$ Jets



## ZEUS



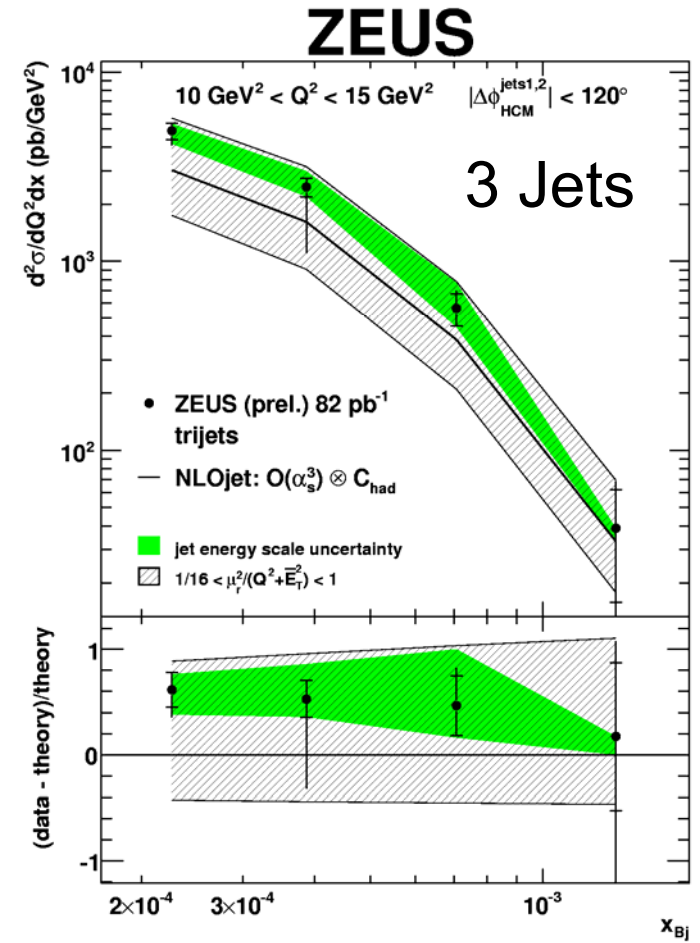
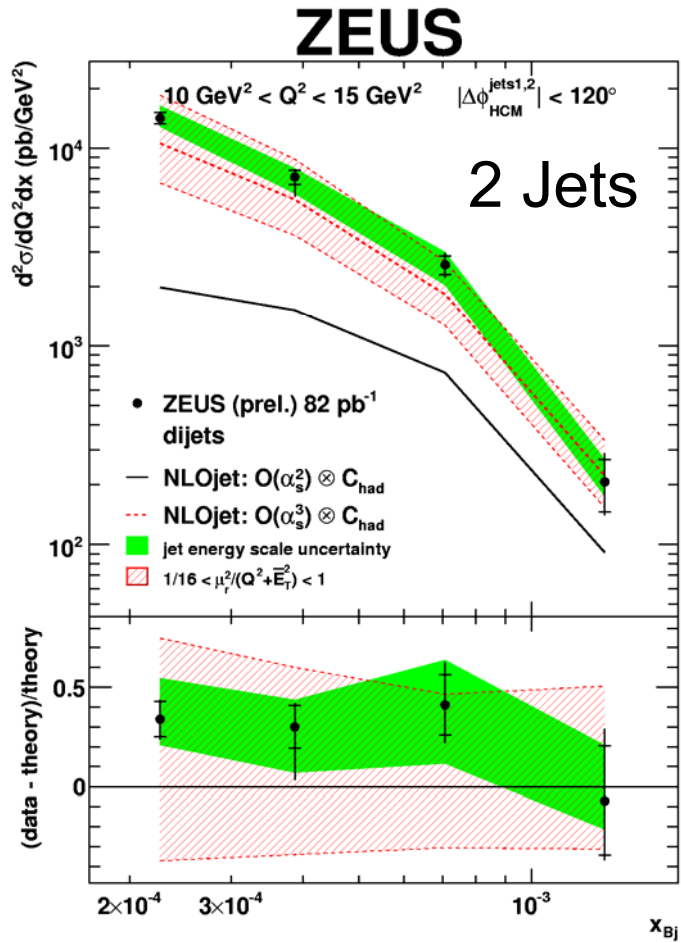
## ZEUS



### NLOjet at O(α<sub>s</sub><sup>3</sup>) describes data

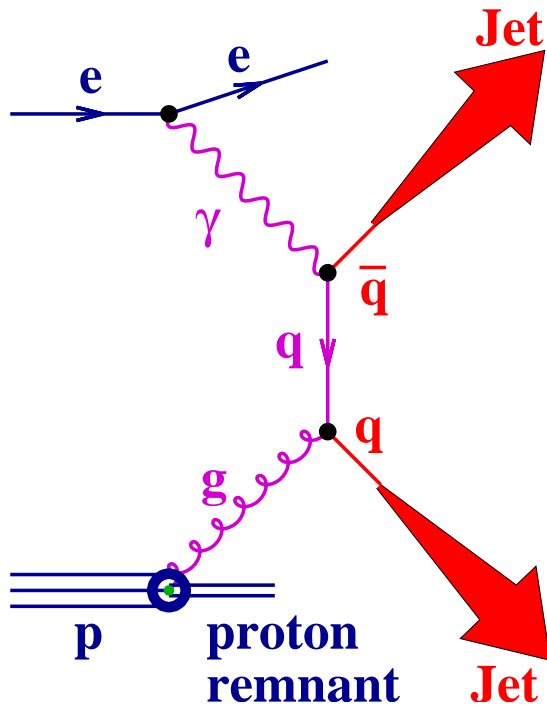


# Di-, Trijets for $|\Delta\Phi^{\text{HCM}}| < 120^\circ$



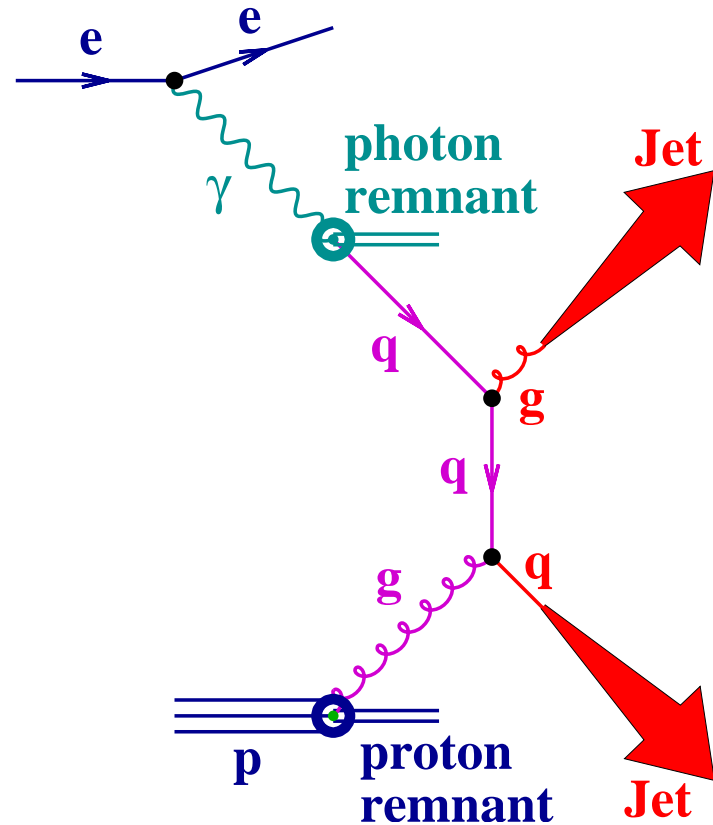
NLOjet at  $O(\alpha_s^3)$  describes data

# Jets in Photoproduction



direct

$$x_{\gamma}^{\text{obs}} \approx 1$$



resolved

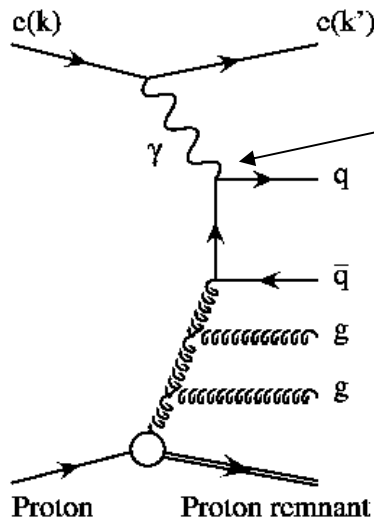
$$x_{\gamma}^{\text{obs}} < 1$$



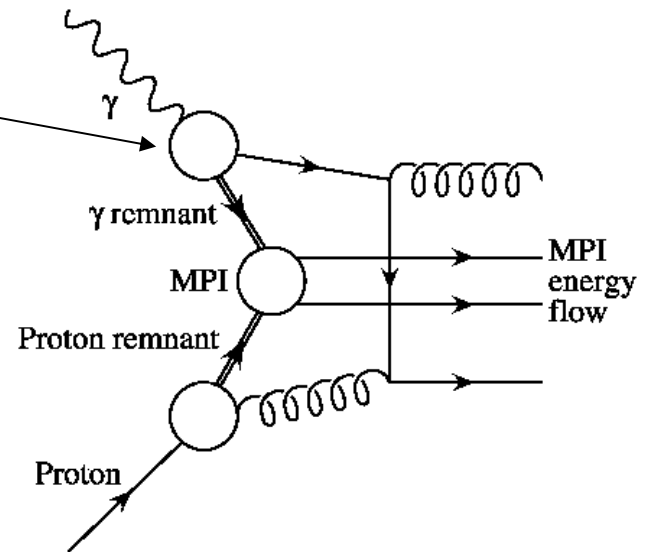
# Multijets in Photoproduction

## 3-,4-Jet production

First Measurement of 4-Jet Events in PHP  
at HERA examines higher order QCD



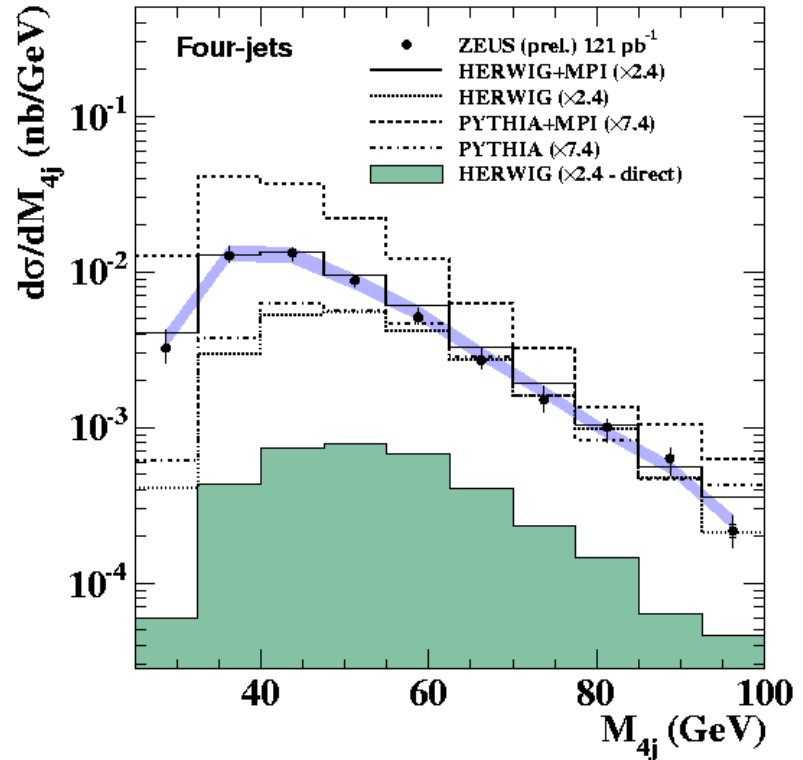
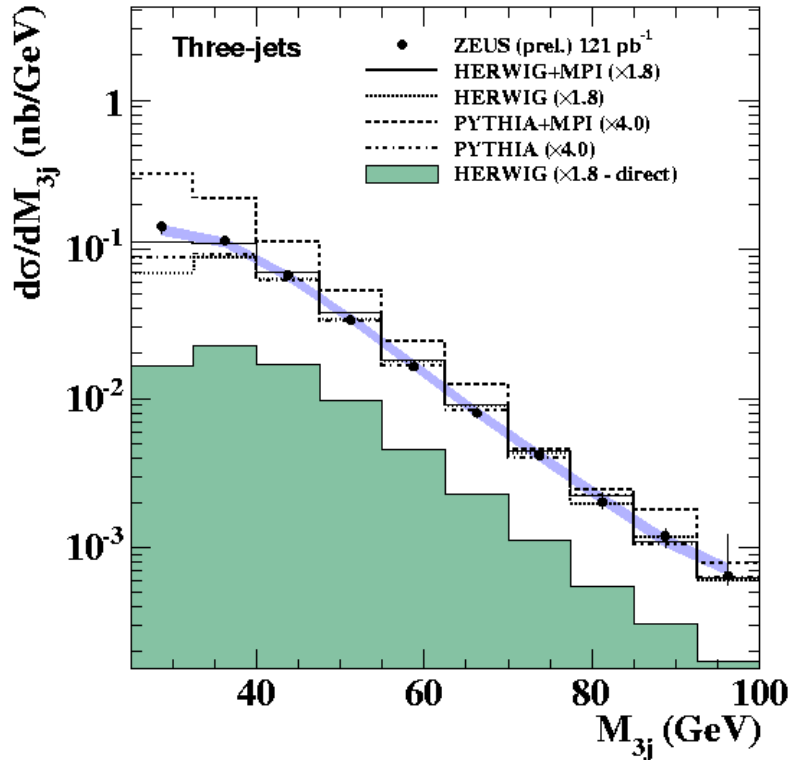
direct resolved  
Photoproduction



lowest order to 4-Jet process  
• access higher orders

MPI contribution to 4-Jet events  
• test of MPI in „clean“ hadronic -  
induced reaction

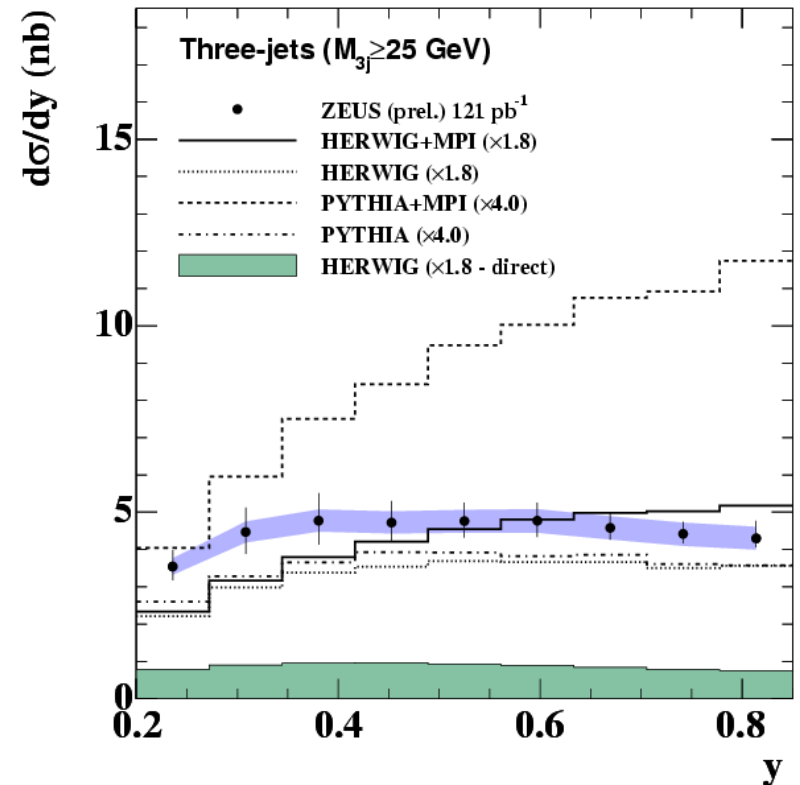
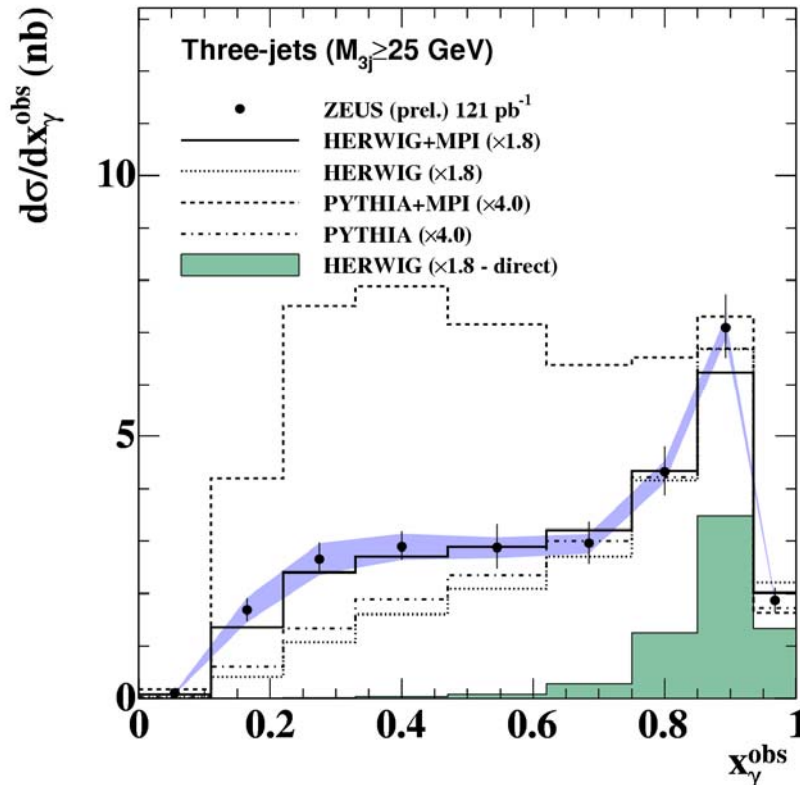
## 3,4-Jet cross section vs. $M_{nj}$



- For  $M_{3j(4j)} > 50(70)$  GeV MCs describe data without MPI
- MC without MPI normalized to data for  $M_{nj} > 70$  GeV
- HERWIG with tuned MPI describes data well
- PYTHIA with MPI overestimates cross section

# Multijets in PHP

## MC and MPI

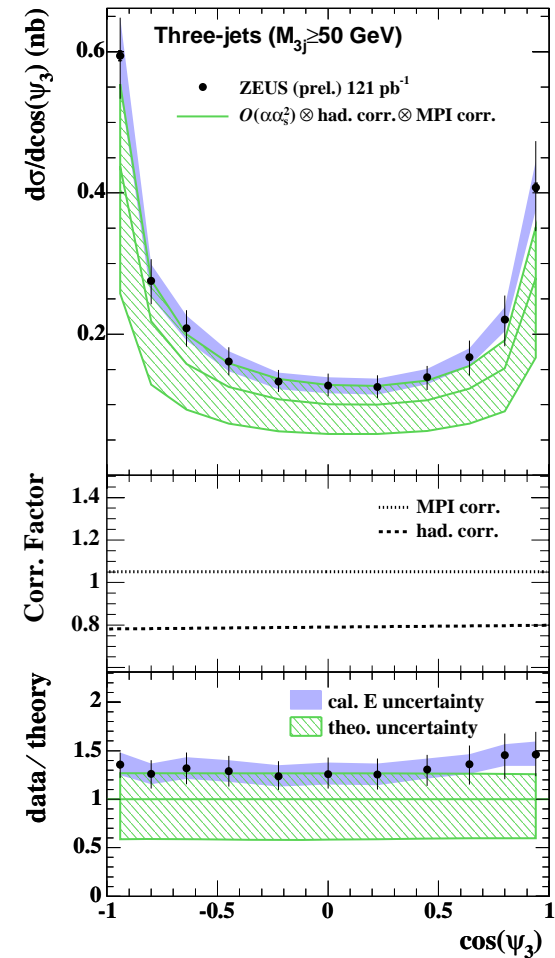
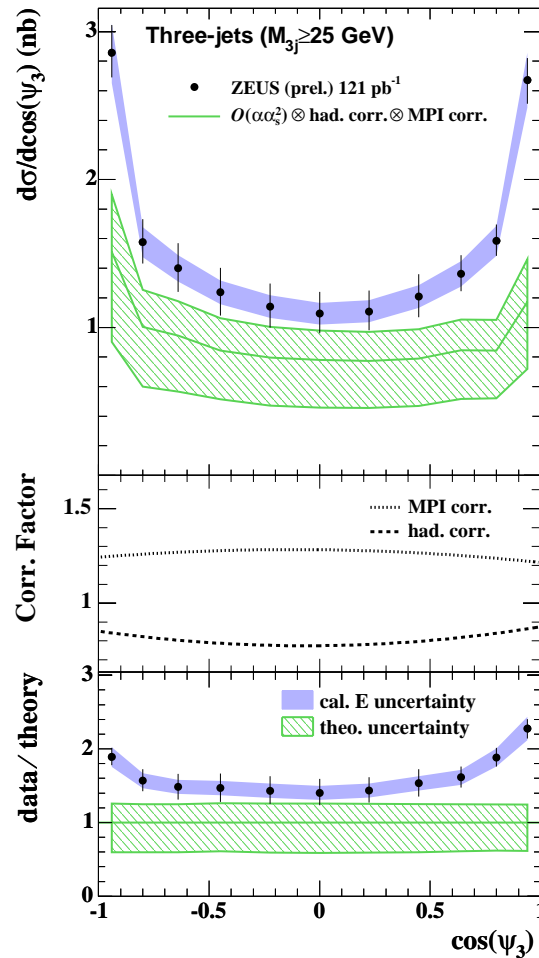


- MCs without MPI describe  $y$ , but fail to describe  $x_{\gamma}^{\text{obs}}$  distribution
- PYTHIA: MPI tuned to generic collider data, HERWIG: MPI tuned to describe  $x_{\gamma}^{\text{obs}}$
- HERWIG+MPI describes  $x_{\gamma}^{\text{obs}}$ ,  $y$  not described anymore
- PYTHIA+MPI does not describe data
- $x_{\gamma}^{\text{obs}}$  and  $y$  distribution: ideal ground for tuning and testing MPI models

# Multijets in PHP

$\cos(\psi_3)$   
reflects orientation of  
lowest energy jet

- directly sensitive to  $O(\alpha_s^2)$

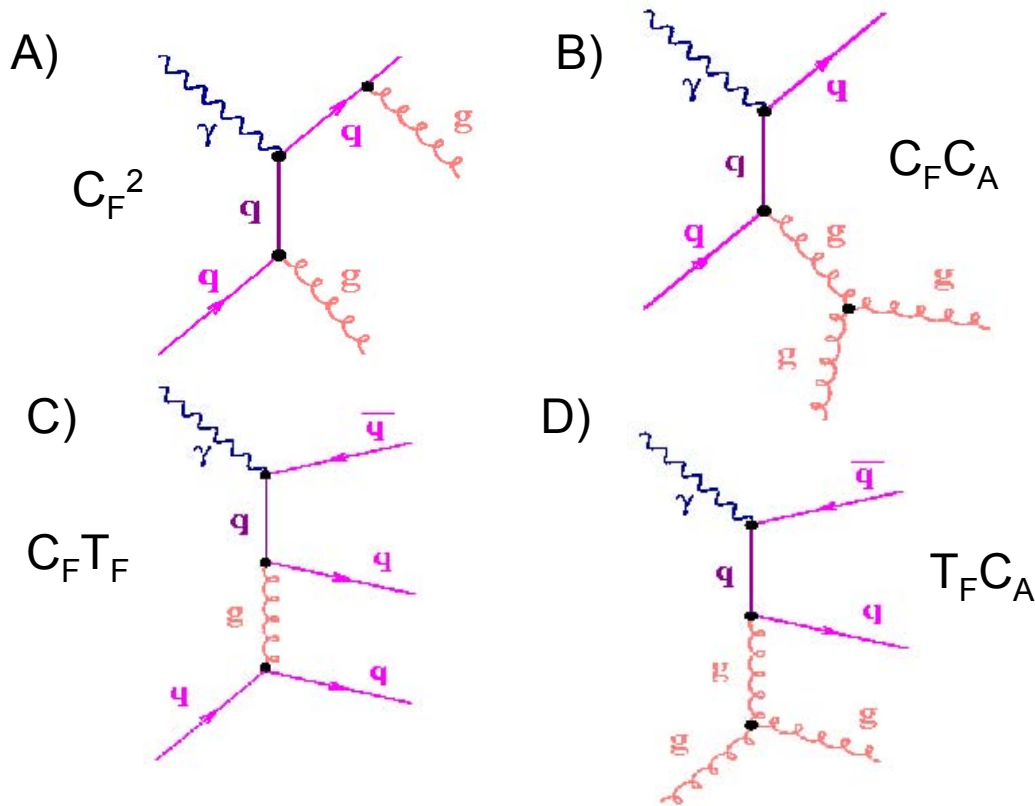


$O(\alpha_s^2)$  pQCD (corrected for hadronization and MPIs) describes high mass region.

# Angular Correlations of 3-Jets in DIS

At  $O(\alpha_s^2)$  calculations of three-jet cross sections the color factors control the rates of these processes:

$$\sigma_{ep \rightarrow 3\text{jets}} = C_F^2 \cdot \sigma_A + C_F C_A \cdot \sigma_B + C_F T_F \cdot \sigma_C + T_F C_A \cdot \sigma_D$$

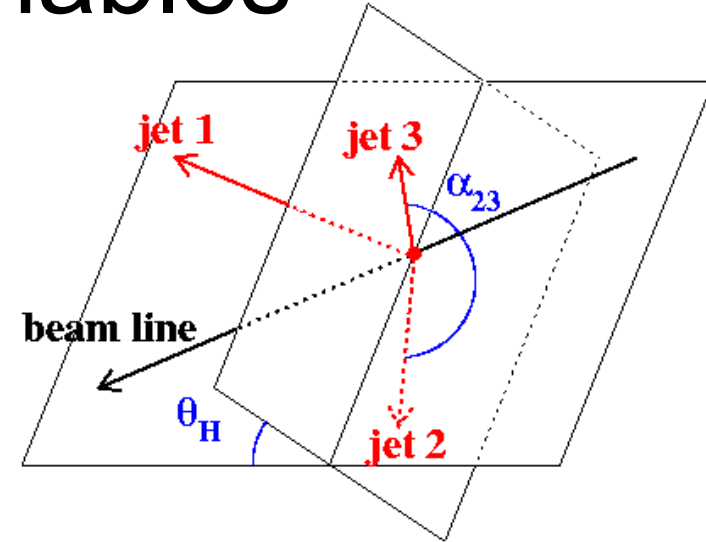


- SU(3) (QCD):  
 $C_A/C_F = 9/4$ ,  $T_F/C_F = 3/8$
- Abelian gluon model based on  $U(1)^3$  (no gluon self-coupling):  
 $C_A/C_F = 0$ ,  $T_F/C_F = 3$
- SO(3):  
 $C_A/C_F = 1$ ,  $T_F/C_F = 1$
- SU(N):  
 $C_A = N_C$ ,  $C_F = \frac{N_C^2 - 1}{2N_C}$ ,  $T_F = 1/2$

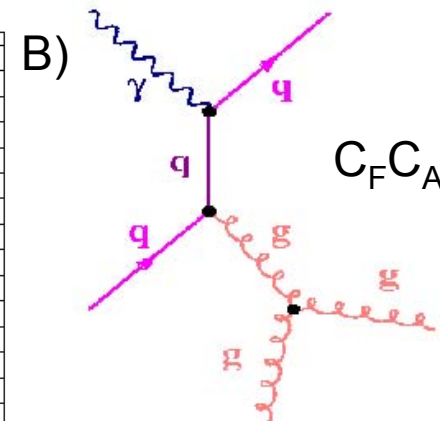
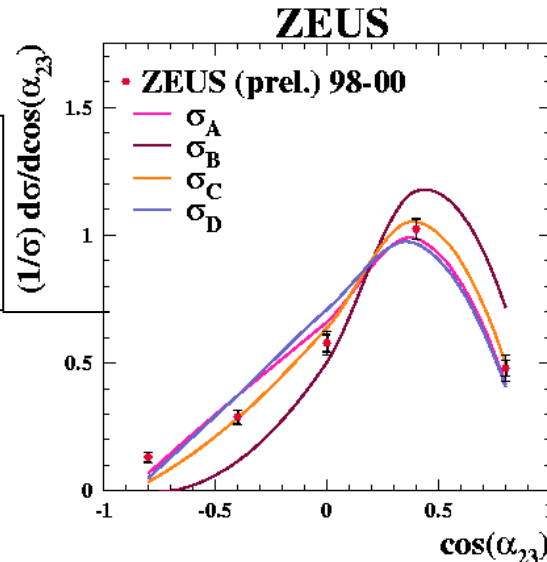
# Angular Correlations

## Definition of Variables

- $\Theta_H$ : angle between the plane determined by the highest- $E_T$  jet and the beam, and the plane of the two lowest- $E_T$  jets
- $\alpha_{23}$ : angle between the lowest- $E_T$  jets
- $\cos(\beta_{KSM})$ :  $\cos\left[\frac{1}{2}(\angle[(\vec{p}_1 \times \vec{p}_3), (\vec{p}_2 \times \vec{p}_B)] + \angle[(\vec{p}_1 \times \vec{p}_B), (\vec{p}_2 \times \vec{p}_3)])\right]$
- $\eta_{\max}^{\text{jet}}$ :  $\eta$  of the most forward jet of the three-jet system in the Breit frame



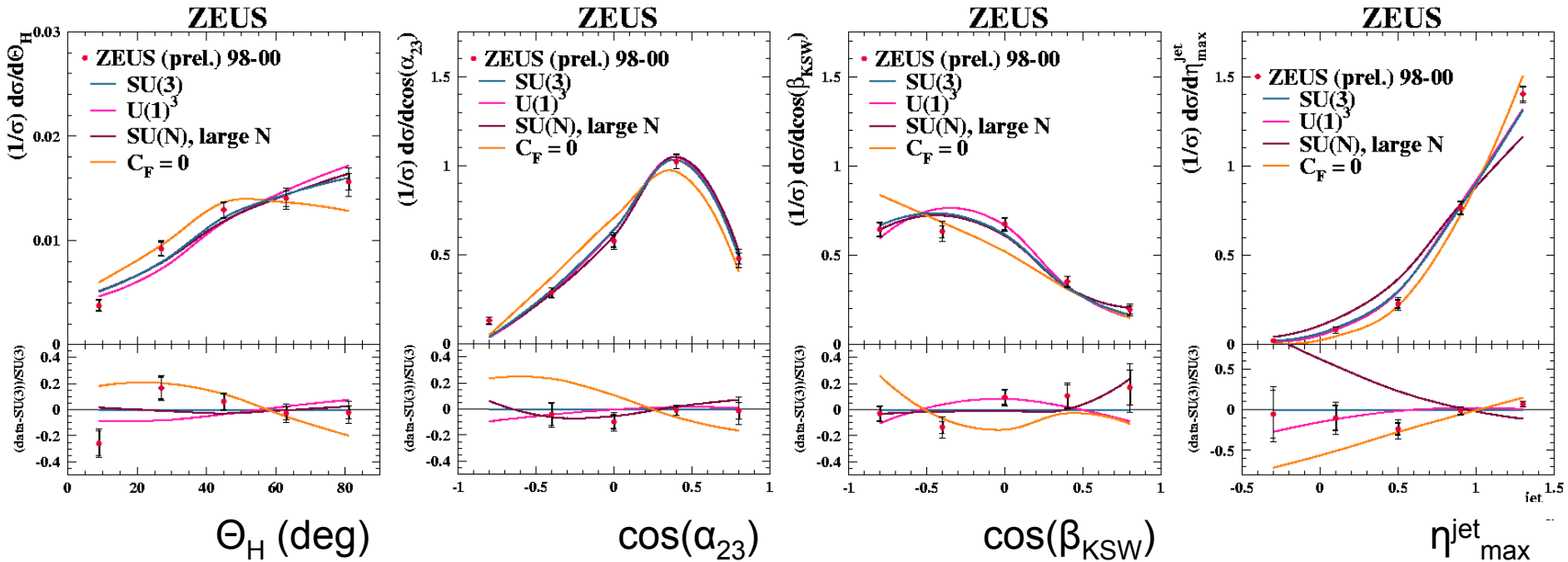
Shapes of different processes contributing to  $\cos(\alpha_{23})$  cross section



Data:  $81.7 \text{ pb}^{-1}$   
 $Q^2 > 125 \text{ GeV}^2$ ,  $|\cos(\gamma_h)| < 0.65$   
 3 Jets in Breit frame with  
 $E_T > 8/5/5 \text{ GeV}$ ,  $-2 < \eta < 1.5$



# Angular Correlations Comparison to theory



- Data reasonably described by SU(3)
- Differences to U(1)<sup>3</sup> are of the order of the statistical error
- Prediction with C<sub>F</sub> = 0 doesn't describe shape of data
- SU(N) in large-N limit ( $\rightarrow T_F/C_F \approx 0$ ) fails to describe  $\eta_{\max}^{\text{jet}}$  distribution



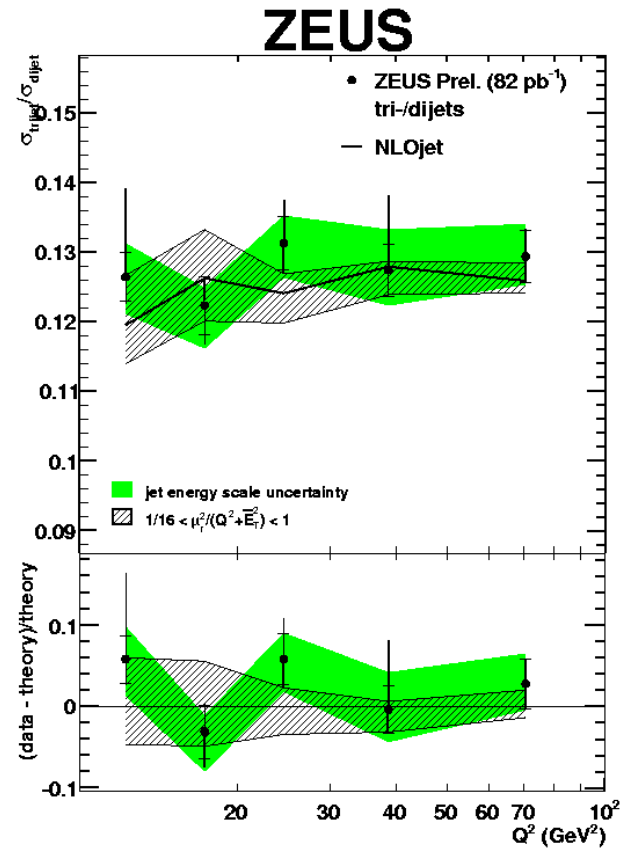
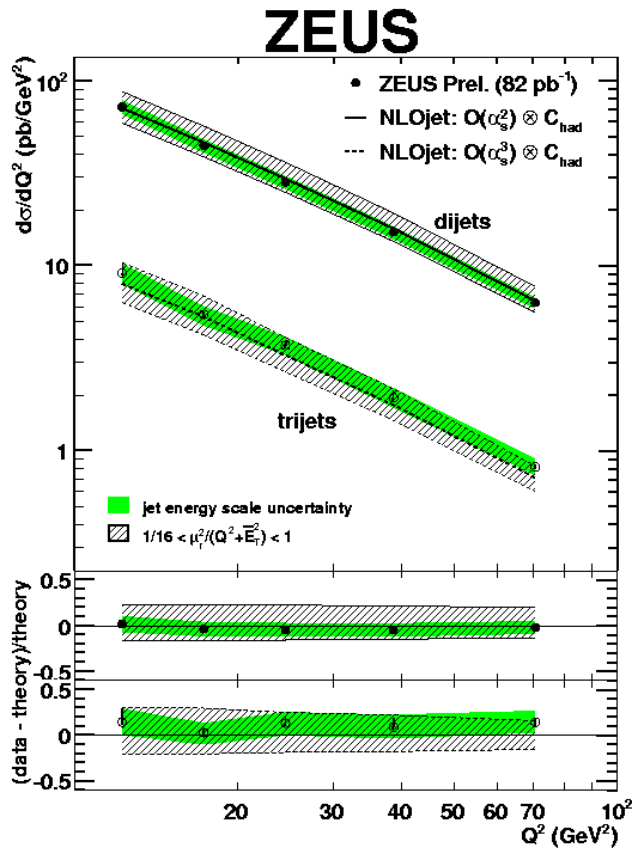
# Summary – ZEUS Multijets



- Multijets at low- $x$  in DIS
  - NLOjet (DGLAP based pQCD) at  $O(\alpha_s^2)$  does not describe dijet cross section with low azimuthal separation
  - Including another order of  $\alpha_s$  improves NLOjet agreement for dijets
  - High- $\Delta E_{T,jets}$  tail of the data is not described for di-, trijets
    - improvement shown with higher order for dijets
- Multijets in Photoproduction
  - First measurement of 4-jets in photoproduction
  - HERWIG+MPIs describes data well
  - $O(\alpha_s^2)$  pQCD describes three-jets for  $M_{3j} > 50$  GeV
- Three-Jet Angular Correlations in DIS
  - Sensitivity to different color components allows access to underlying gauge group
  - SU(3) gives a reasonable description of data
  - Calculations with  $T_F/C_F \approx 0$  or  $C_F = 0$  disfavored

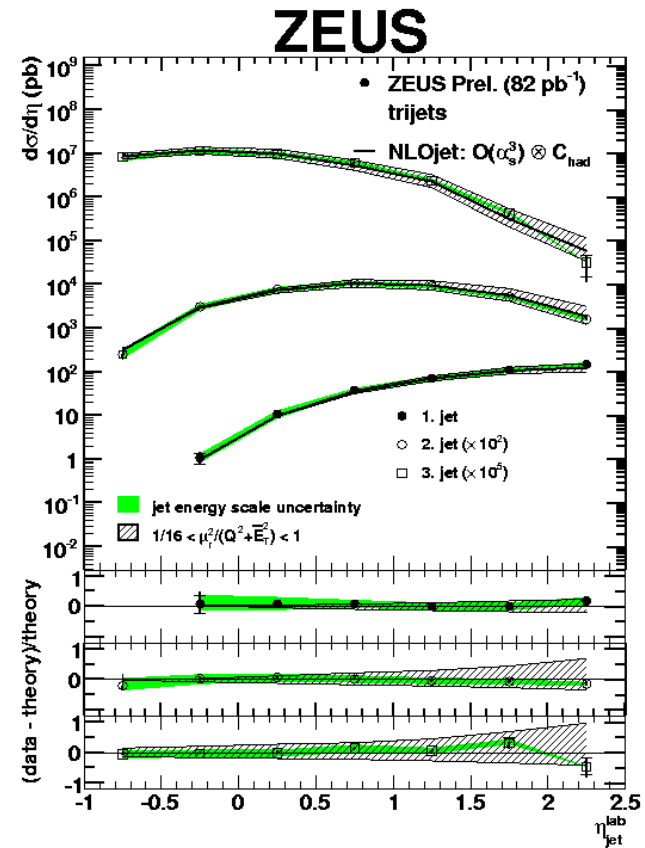
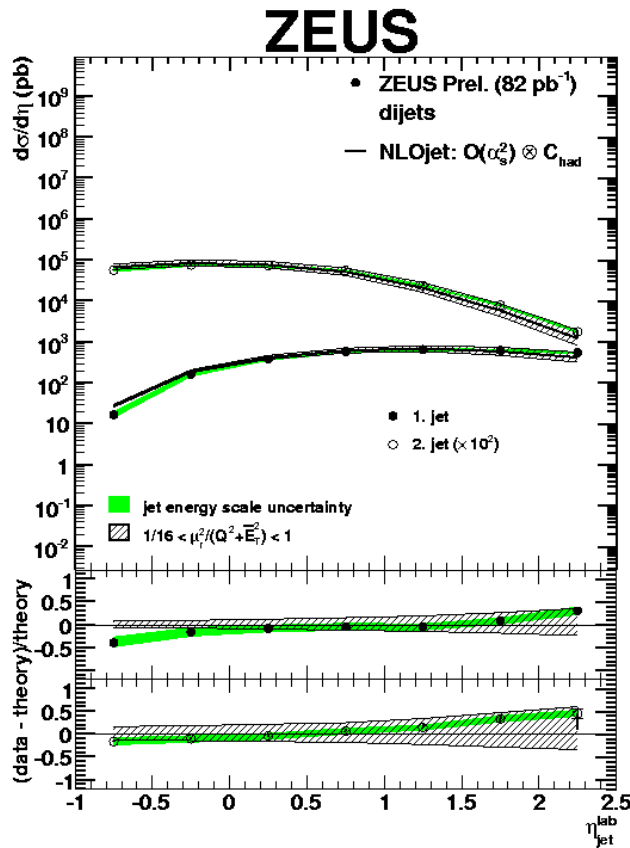


# Di-, Trijet cross sections vs. $Q^2$

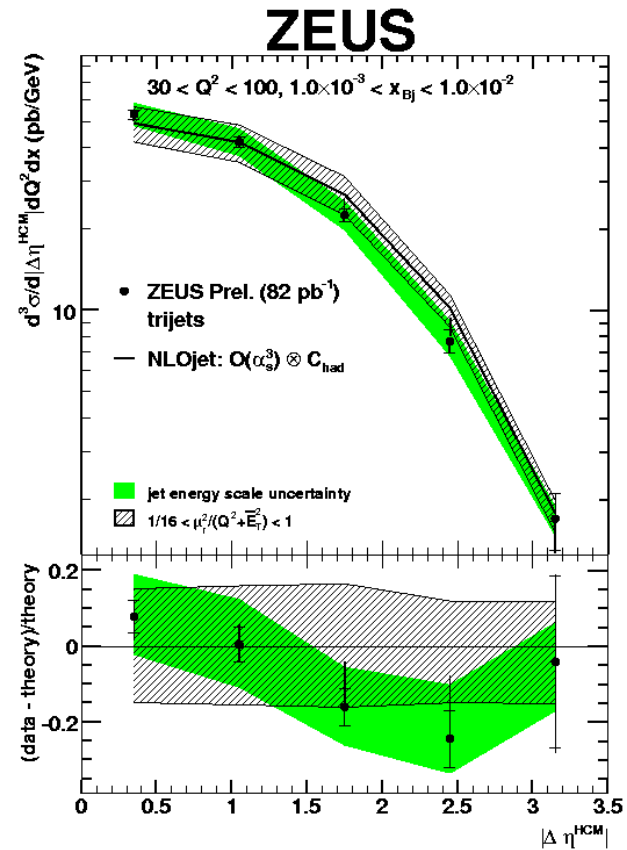
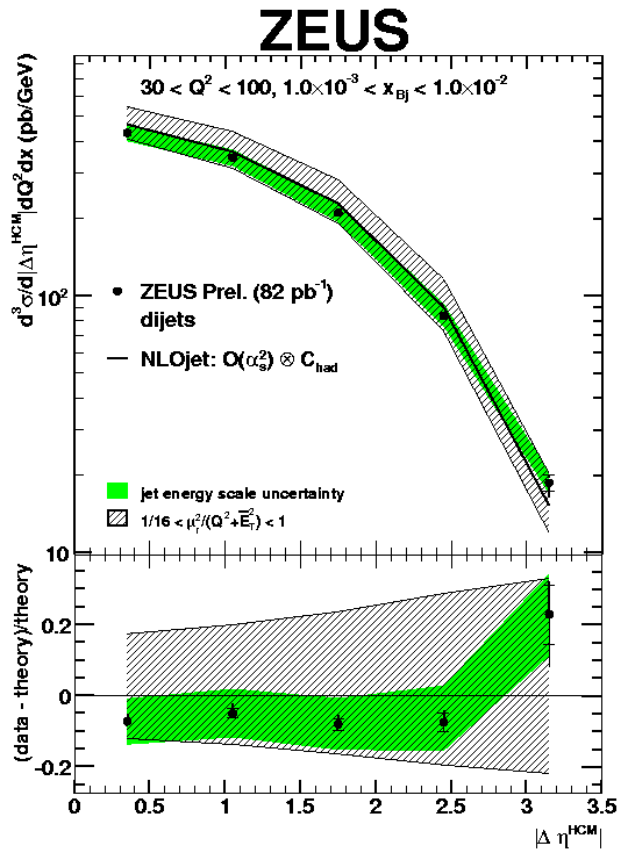


Dijet and Trijet cross sections described by NLOjet within uncertainties.

# Di-, Trijet cross sections vs. Jet- $\eta$

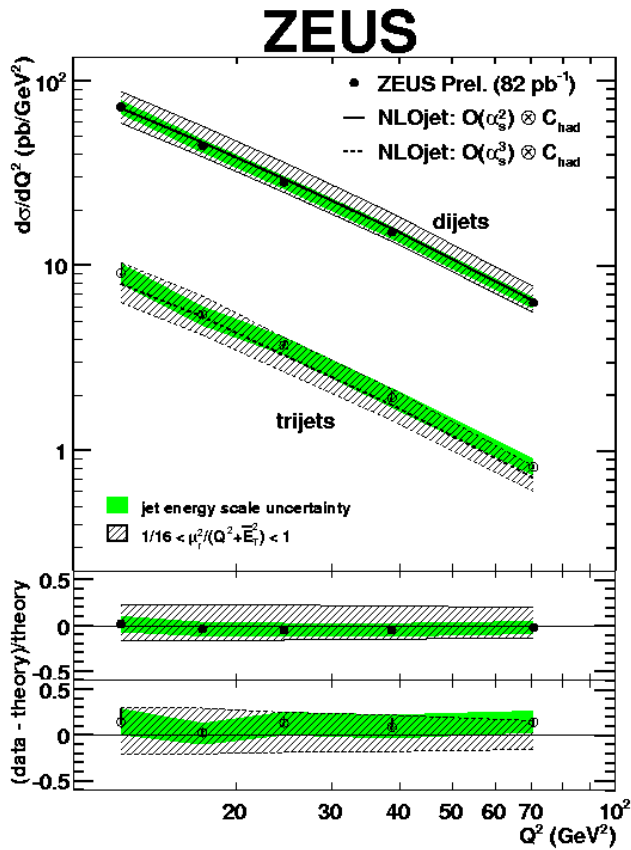


Jet- $\eta$  well described within uncertainties

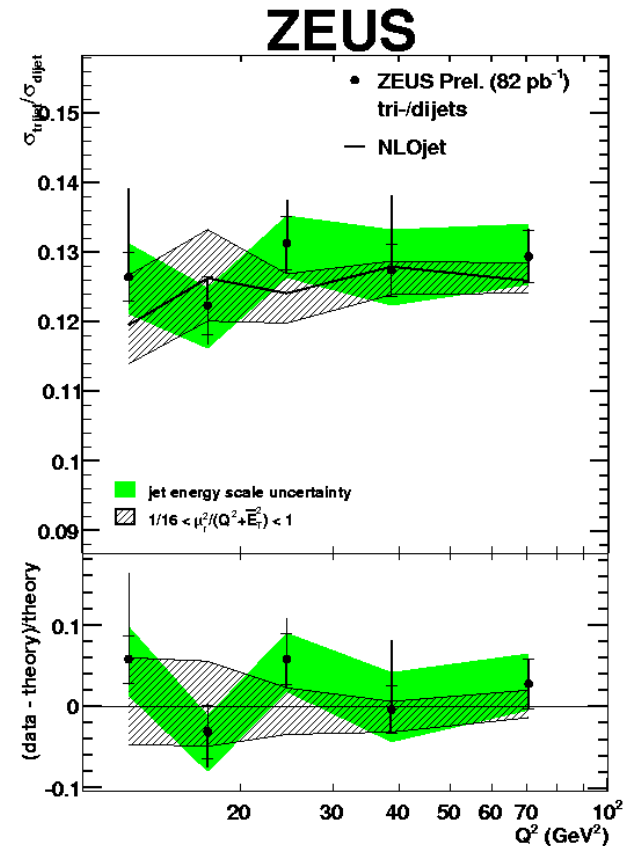


NLOjet consistent within large uncertainties

# Di-, Trijet cross sections vs. $Q^2$



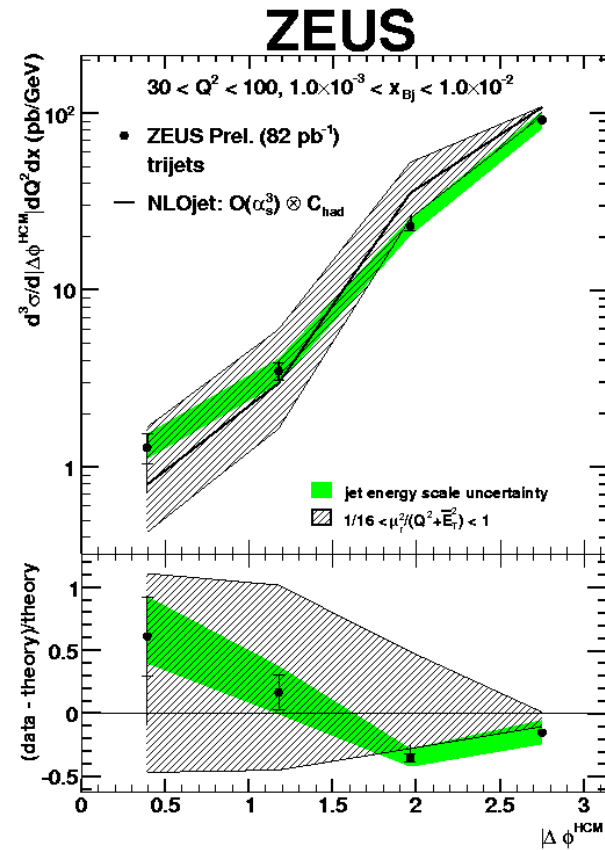
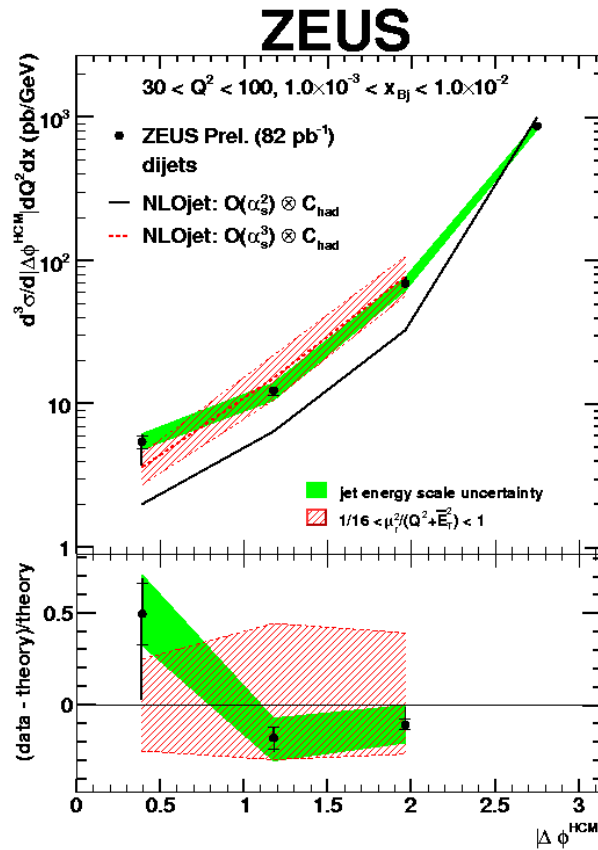
$\frac{data - theory}{theory}$



Dijet and Trijet cross sections described by NLOjet within uncertainties.



# $|\Delta\Phi^{\text{HCM}}|$ btw 2 highest- $E_T$ Jets



NLOjet agreement for dijets using a higher order calculation,  
description for trijets inside the large uncertainties

# Multijets in PHP

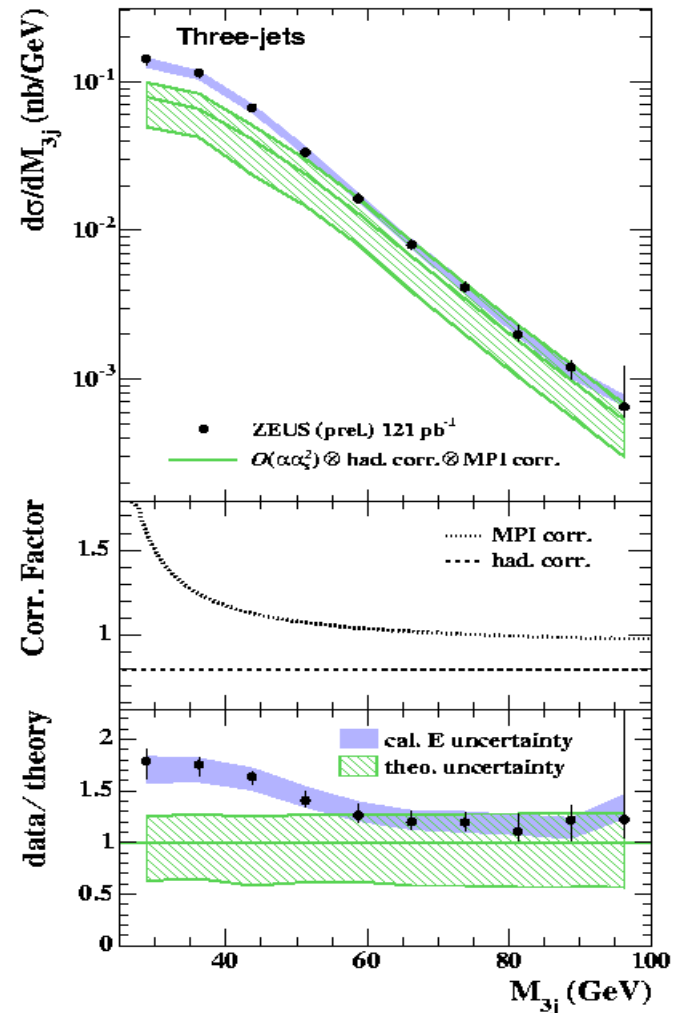
## comparison to pQCD

$O(\alpha_s^2)$  pQCD (Klasen, Kleinwort, Kramer) with MPI correction from HERWIG compared to the data.

There is no calculation to compare to four-jets in PHP yet.

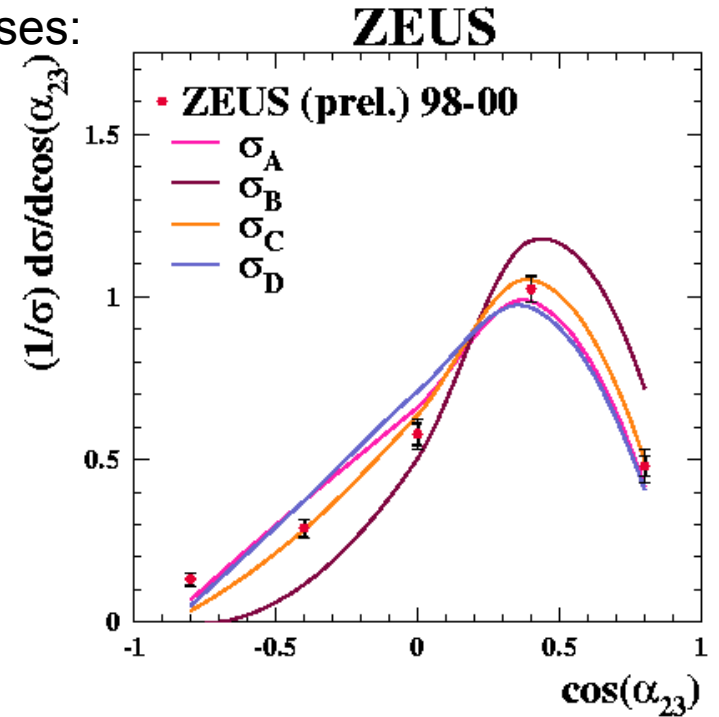
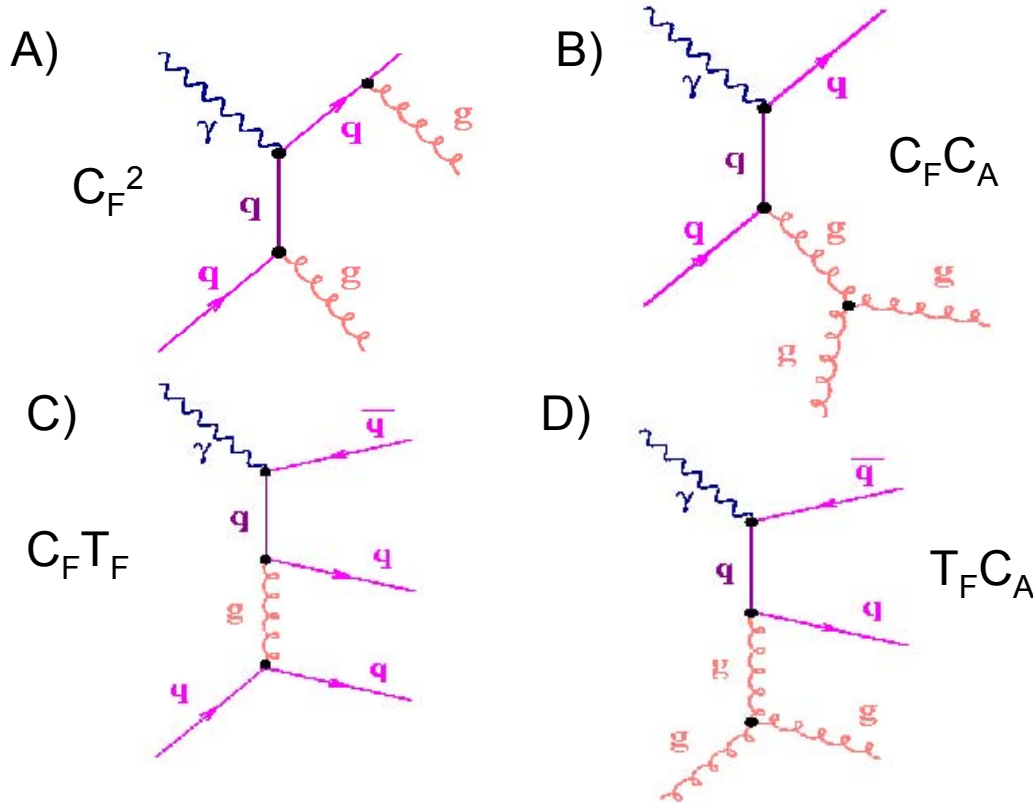
The calculation mostly describes data at high  $M_{3j} > 50$  GeV. For lower  $M_{3j}$  the data get described worse.

Reasons: missing orders or MPI?



In  $O(\alpha_s^2)$  calculations of three-jet cross sections the color factors control the contributions of these processes:

$$\sigma_{ep \rightarrow 3\text{jets}} = C_F^2 \cdot \sigma_A + C_F C_A \cdot \sigma_B + C_F T_F \cdot \sigma_C + T_F C_A \cdot \sigma_D$$



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