

# Review of Power Corrections in DIS

## **FRIF Power Corrections Workshop 06, Paris**

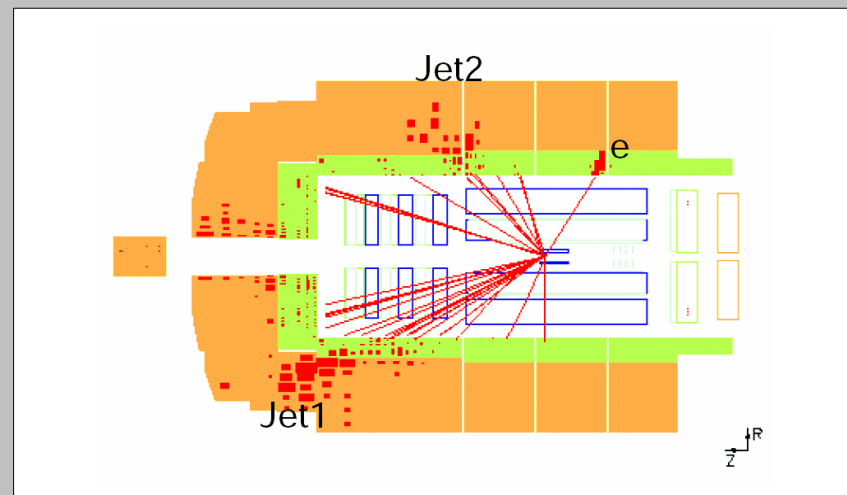
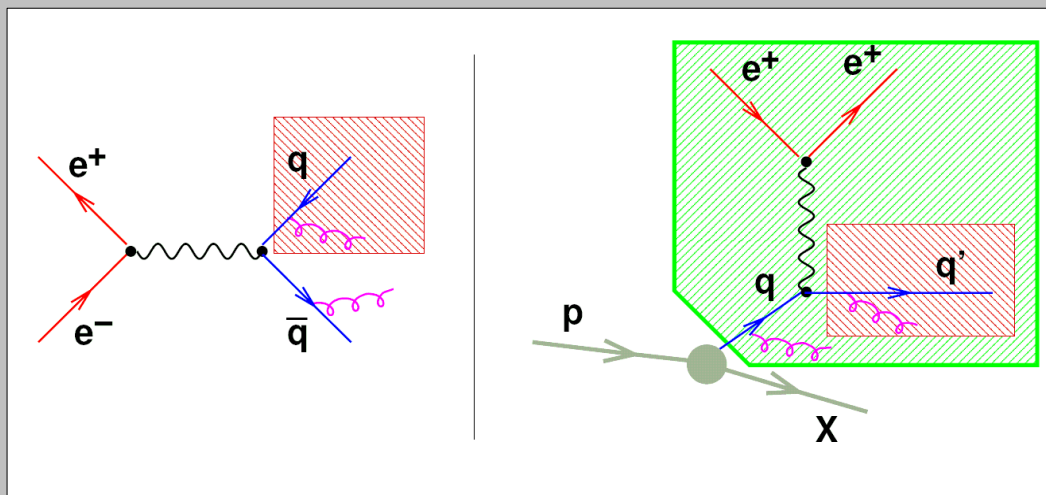
Thomas Kluge, DESY

- ▶ some history
- ▶ peculiarities of event shapes in DIS
- ▶ mean values of 2-jet shapes
- ▶ distributions of 2-jet shapes
- ▶ distributions of 3-jet shapes

# History of Power Corrections in DIS

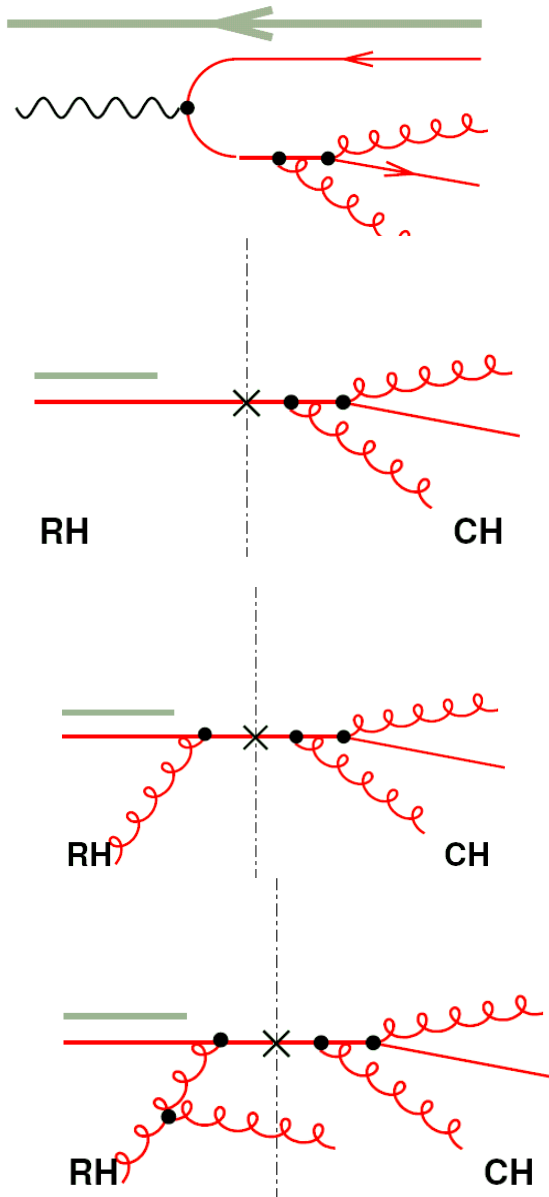
- ▶ **95**: DIS Paris - Brian Webber presents  $\langle F \rangle + PC$  for DIS
- ▶ **96**: DIS Rome - First H1 data  $\langle F \rangle(Q)$ , waiting for pQCD calculation  
MEPJET, DISENT, DISASTER++
- ▶ **97**: H1 publishes  $\langle \tau \rangle, \langle \tau_c \rangle, \langle B \rangle, \langle \rho \rangle$  - universal  $\alpha_0$   
prediction for B not confirmed [PLB406\(1997\)256](#)
- ▶ jet broadening revisited by theory, 2-loop corrections, Milan factor:  
Dokshitzer, Webber, Dasgupta, Salam, ...
- ▶ **99**: H1 publishes mean values- still large spread of  $\alpha_s(m_Z)$ , massless  
observables, first tries with spectra [EPJC14\(2000\)255](#)
- ▶ **01**: HEP Budapest - Mrinal Dasgupta: resummed spectra for DIS
- ▶ **02**: ZEUS results on mean values [EPJC27\(2003\),531](#)
- ▶ **03**: EPS Aachen - prel. H1 spectra, first 3-jet data ( $K_{out}, \chi$ )
- ▶ **04**: HEP Beijing - prel. ZEUS spectra, 3-jet data
- ▶ **12/2005**: H1 results on mean values and distributions, [hep/ex 0512014](#)

# Eventshapes in DIS at HERA



- ▶ t-channel scattering
- ▶  $\sqrt{s} \Leftrightarrow \sqrt{Q^2}$      $Q^2 = sxy$  variable, here:  $Q = 5..115$  GeV
- ▶ initial state: not vacuum, factorise into pdfs
- ▶ outgoing parton  $\pm$ resembles 1/2 of  $e^+e^-$  event
- ▶ separate low momentum proton remnant  $\rightarrow$  Breit frame

# The Breit Frame



- ▶ brick wall frame
- ▶ define hemispheres (CH:  $\eta < 0$ )
- ▶ event shapes defined on particles in current hemisphere
- ▶ emissions in remnant hemisphere
  - some event shapes sensitive through recoil (Global observables)
  - RH partons may leak into CH
- ▶ avoid IR sensitivity due to near empty CH by  $E_{\min}$  requirement, e.g.  $E_{\text{CH}} > 0.1 \cdot Q$
- ▶ jet rates: defined for both hemispheres

# Observables studied

$$T_C = \max_{\vec{n}_T} \frac{\sum |\vec{p}_h \cdot \vec{n}_T|}{\sum |\vec{p}_h|}$$

$$\rho = \frac{(\sum E_h)^2 - (\sum \vec{p}_h)^2}{(2 \sum |\vec{p}_h|)^2}$$

$$C = \frac{3 \sum_{h,i} |\vec{p}_h| |\vec{p}_i| \sin^2 \theta_{hi}}{2 (\sum |\vec{p}_h|)^2}$$

- ▶ defined wrt „own“ axis
- ▶ non-global observables
- ▶ insensitive to pdf

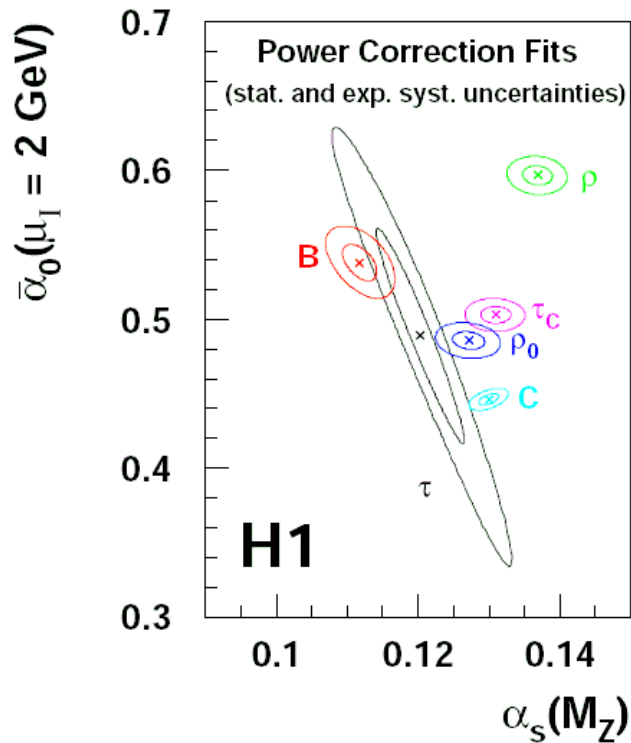
$$T = \frac{\sum |\vec{p}_{z,h}|}{\sum |\vec{p}_h|}$$

$$B = \frac{\sum |\vec{p}_{\perp h}|}{2 \sum |\vec{p}_h|}$$

- ▶ defined wrt virtual boson axis
- ▶ global observables
- ▶ more sensitive to pdf (and evolution)

# Mass effects

1999



- ▶ jet mass defined using E and p
- ▶ dependent on particle masses
- ▶ avoid by using massless scheme
- ▶ substitute E by  $|p|$ ,  $\rho \rightarrow \rho_0$
- ▶ mass effects are substantial
- ▶ residual effect on all variables
- ▶ in the following use  $\rho_0$ , but interesting topic in itself

# Overview of Studies

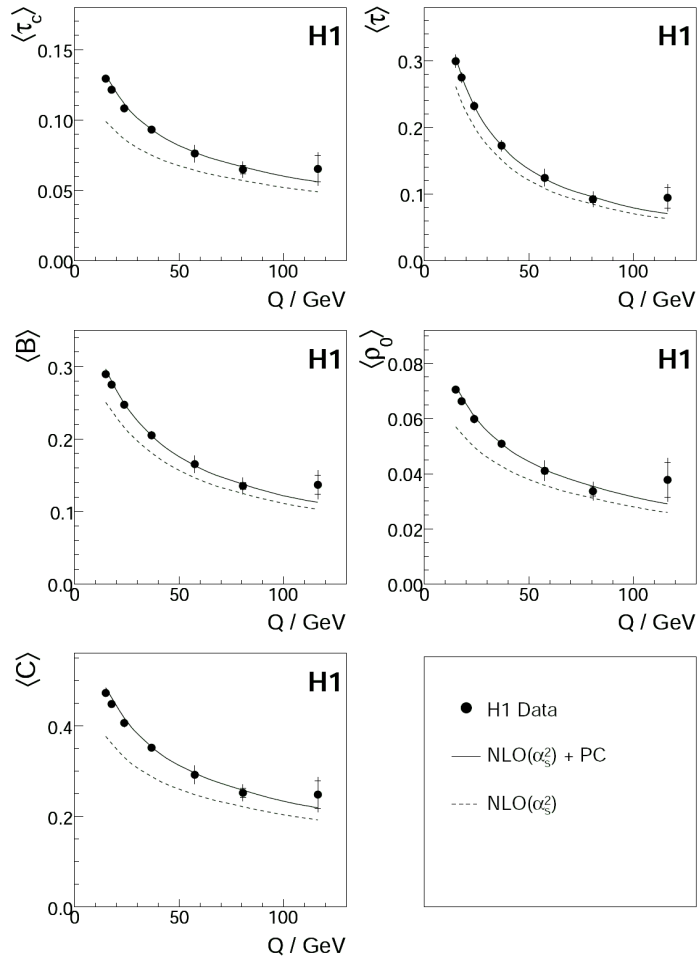
## MEAN VALUES

- ▶ 2-jet event shapes, NLO+PC
- ▶ jet rates, NLO(+PC)

## DISTRIBUTIONS

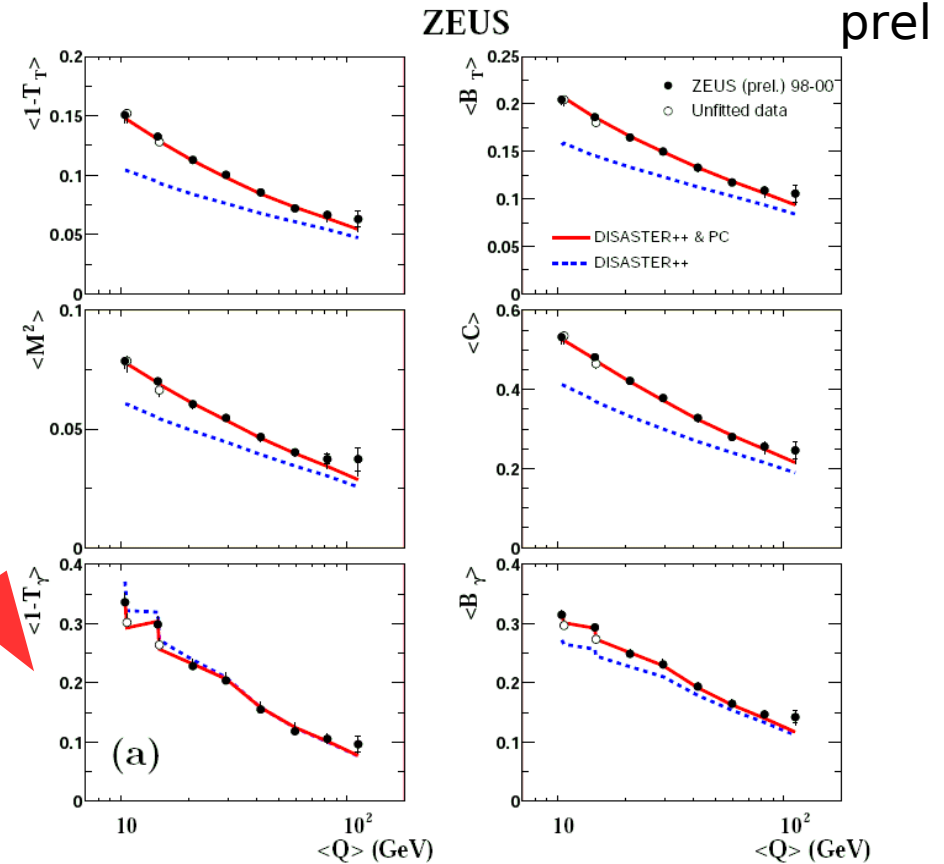
- ▶ 2-jet event shapes, NLO+NLL+PC
- ▶ 3-jet event shapes, LO+NLL+PC
- ▶ jet rates, NLO

# Mean Values



2005

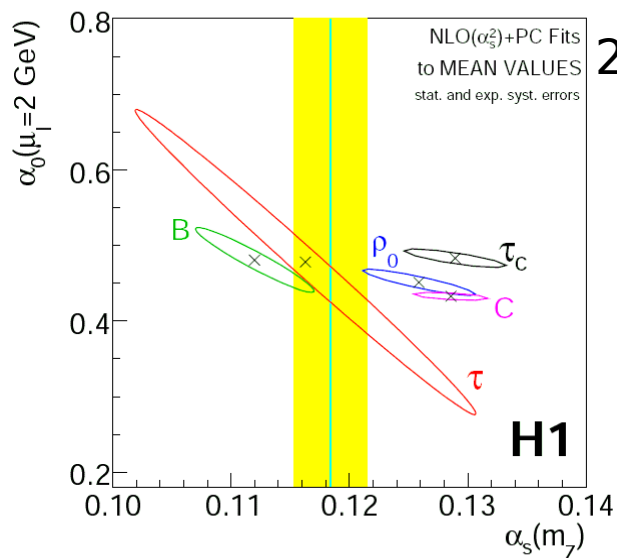
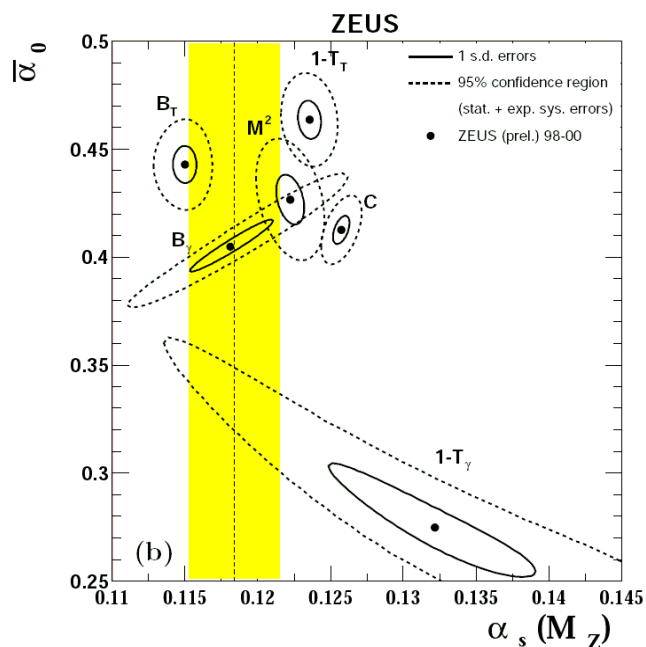
- ▶  $106\text{pb}^{-1}$ ,  $15 < Q < 116$  GeV
- ▶ fit: DISASTER++ with PC
- ▶ power corrections  $> 0$



- ▶  $82\text{pb}^{-1}$ ,  $10 < Q < 113$  GeV
- ▶ fit: DISASTER++ with PC
- ▶ PC for  $\gamma$ -axis variables small,  $\leq 0$  for  $T_\gamma$

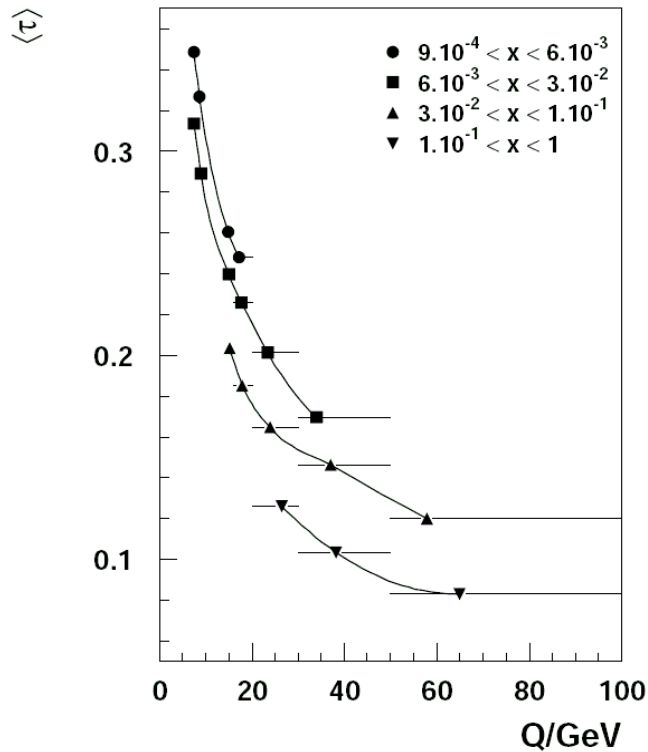


# QCD Fits to Mean Values

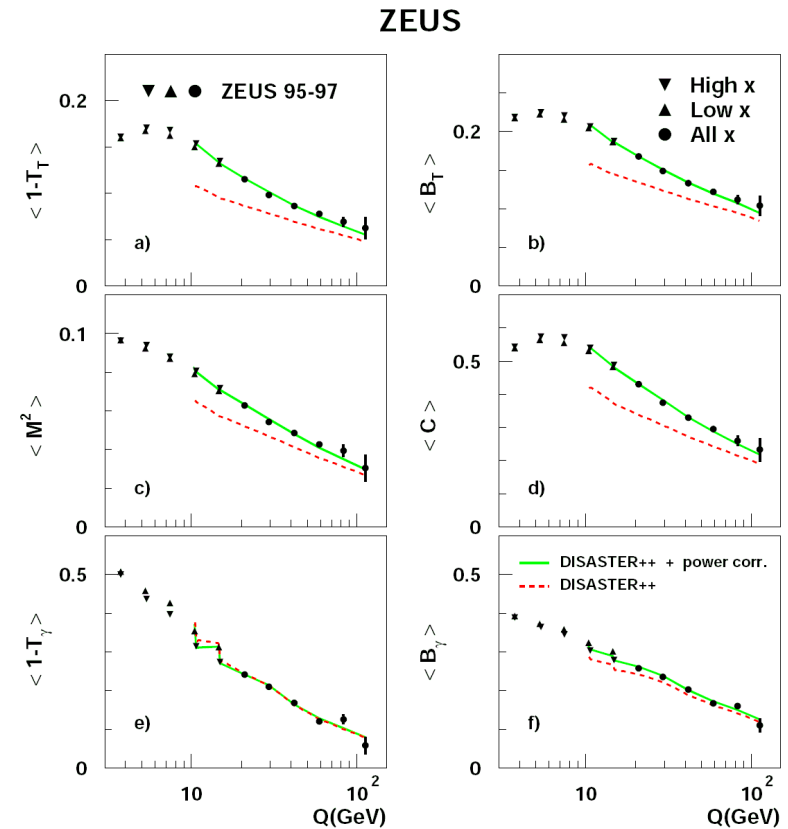


- ▶  $\gamma$ -axis thrust
  - large uncertainties
  - ZEUS: negative correction
- ▶ other: sensible values of  $\alpha_0$ , universality at 10% level, H1  $\sim 10\%$  higher than ZEUS
- ▶ spread in  $\alpha_s$  larger than exp. errors.
  - higher order pQCD needed?
- ▶ results consistent with 95-97 analyses
- ▶ exp. errors small
  - dominating systematic: elm. E-scale due to boost to the Breit system

# x dependence

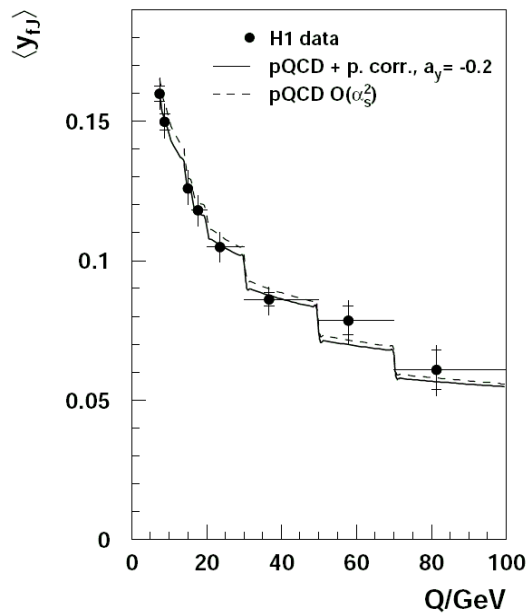


- ▶  $\gamma$ -axis variables: dependence on Bjorken  $x$  due to pdf, largest for thrust
- ▶ H1 integrate over  $Q$  bin
- ▶ ZEUS: split high/low  $x$



- ▶ 95-97:  $x$ -dependence of  $\alpha_0$  seen for some variables
- ▶ not confirmed by new analysis

# Mean Values Jet Rates



▶ jet rates: mean value of resolution  $y$  for  $2+1 \rightarrow 1+1$  jets transition

▶ factorisable JADE  $y_{fj}$

-  $p=1$ ,  $a_f=1$  (PC parameters)

- compatible with pQCD alone

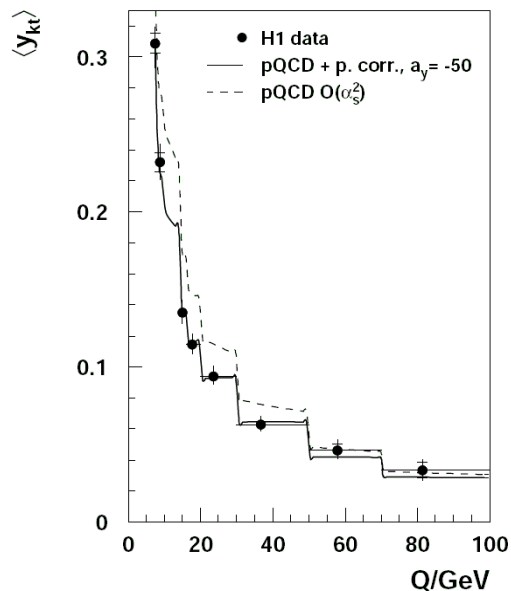
▶ Durham  $k_t$   $y_{kt}$

-  $p=2$ ,  $a_f=?$  (PC parameters)

- fit:  $a_f=-50$

▶ no reasonable fits for  $(\alpha_s, \alpha_0)$

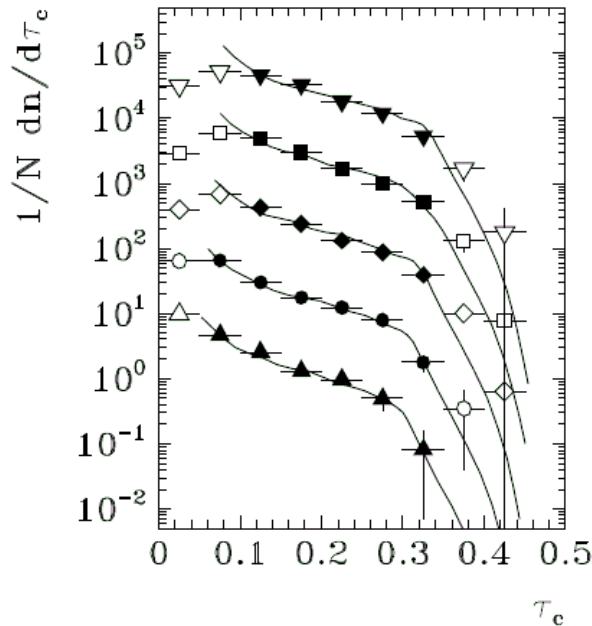
▶ open question...



# Distributions

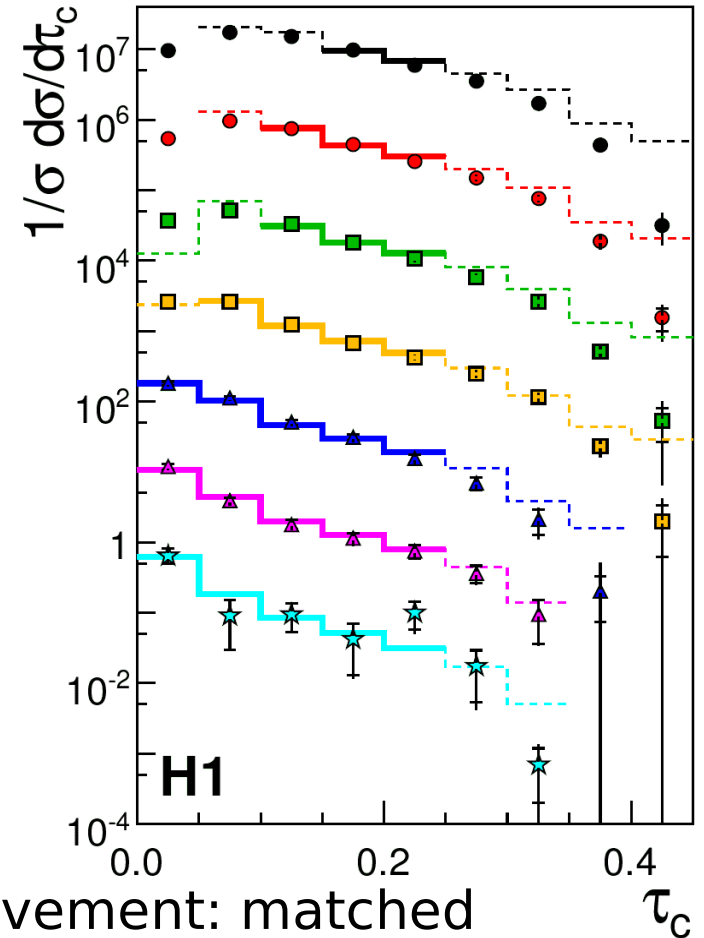
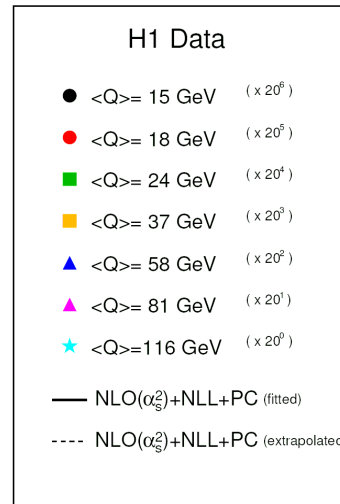
H1 preliminary

1998



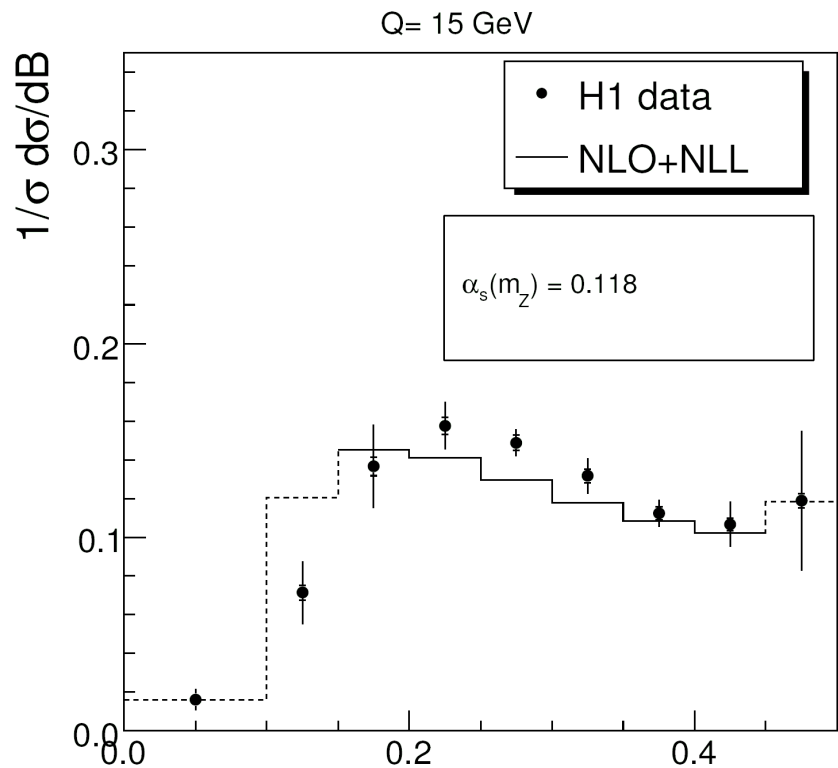
- ▶ no resummation
- ▶ description over limited range
- ▶ large values of  $(\alpha_s, \alpha_0)$  compared to mean values
- ▶ not feasible

2005



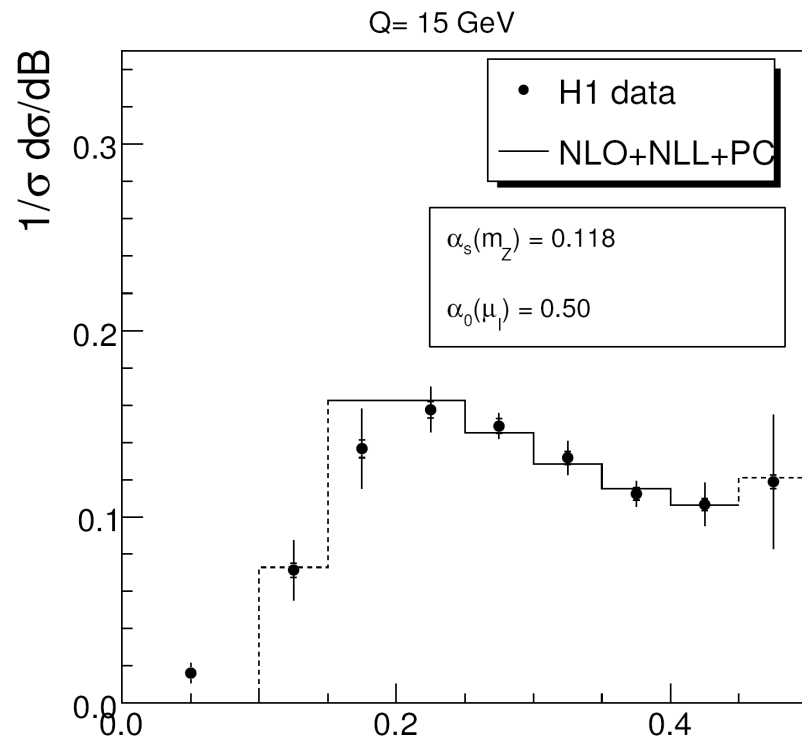
- ▶ key improvement: matched resummation via DISRESUM
- ▶ small errors: stat 1-10%  
syst 2-15%

# Resummed Distributions



B

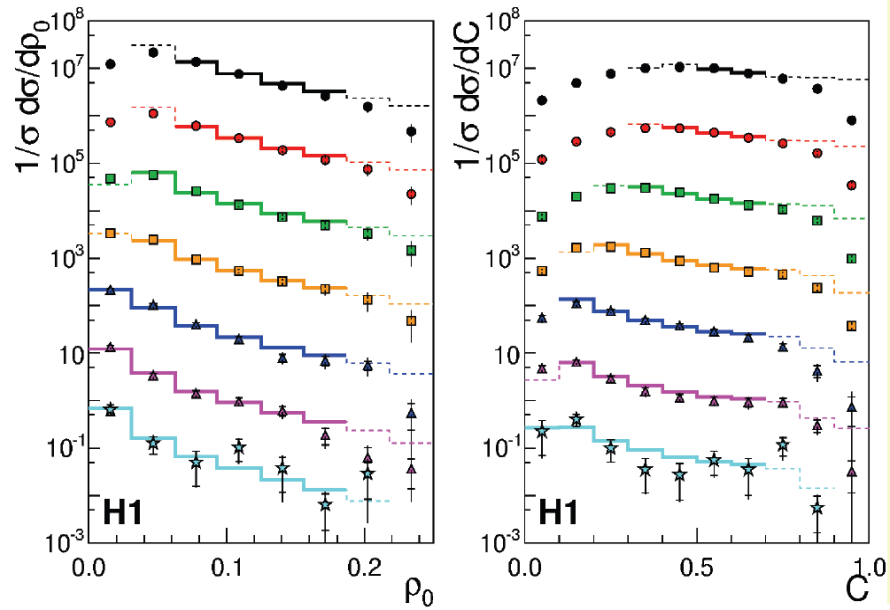
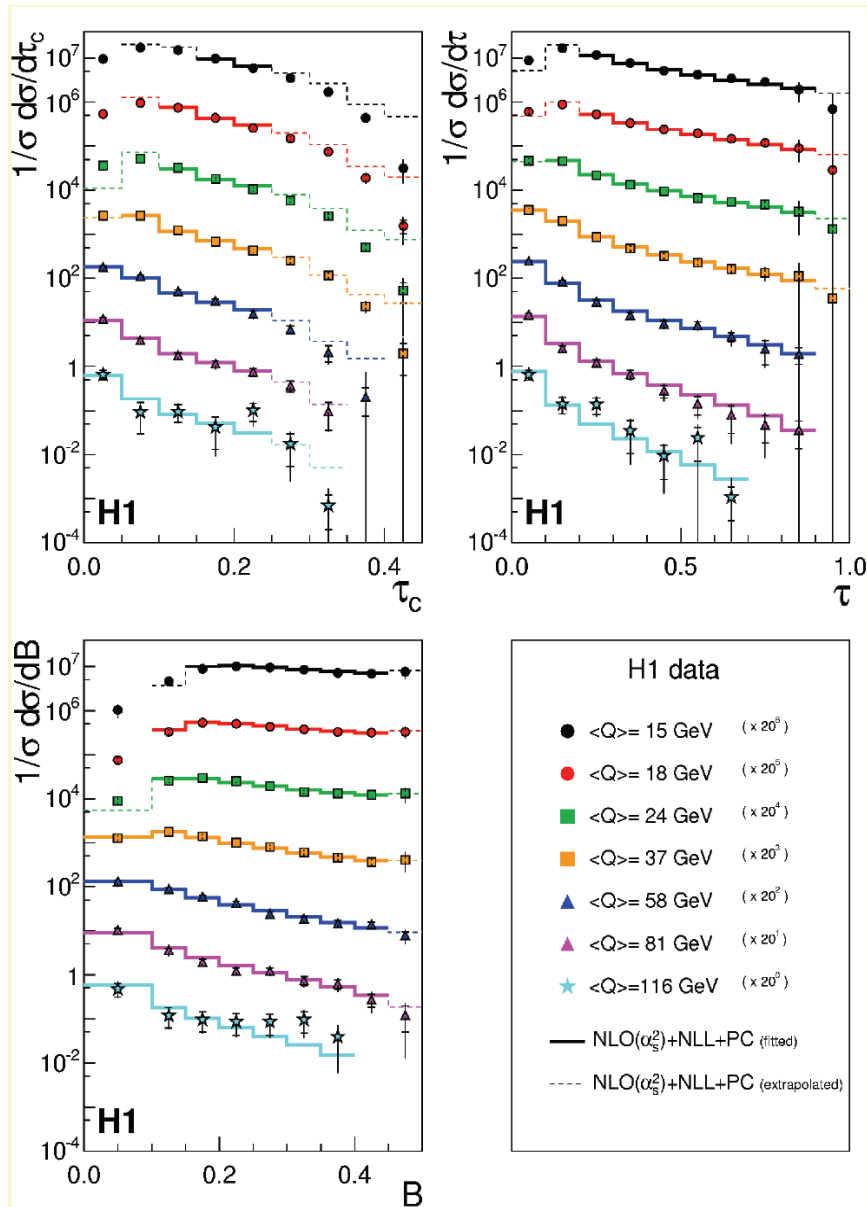
- ▶ pQCD: DISPATCH/DISASTER++
- ▶ matched resummation: DISRESUM



B

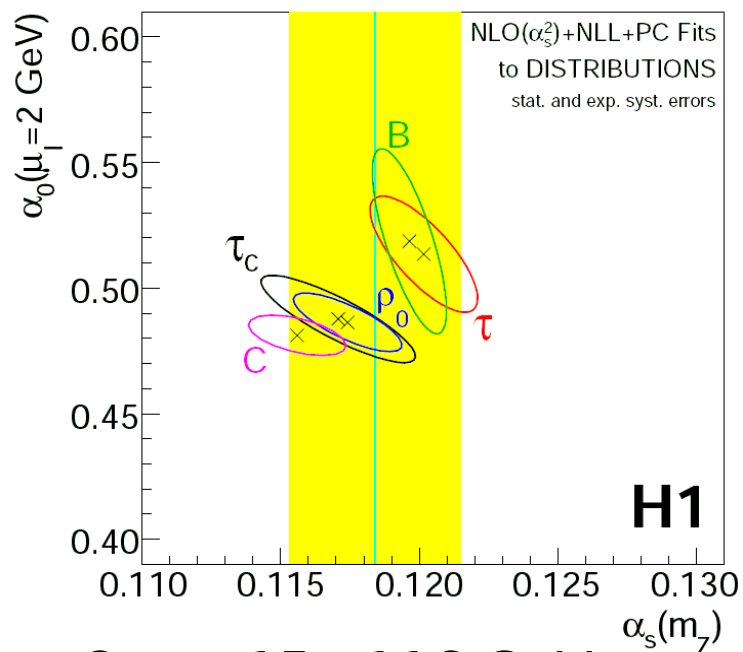
- ▶ + Dokshitzer, Webber power corrections: as implemented in DISRESUM

# Distributions



- ▶ good description over large range!
- ▶ down to  $\langle Q \rangle = 15 \text{ GeV}$

# Fits to Distributions

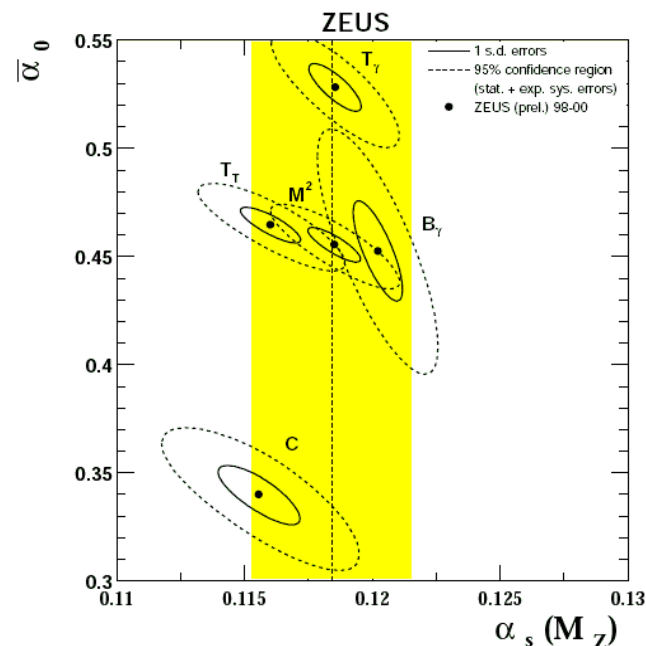


- ▶  $\langle Q \rangle = 15 \dots 116 \text{ GeV}$
- ▶  $\chi^2/\text{dof}: 0.5 \dots 1.4$ ,  $\alpha_0$  around 0.5  
 $\alpha_s$  compatible with world mean
- ▶ grouping:  $\gamma$ -axis / others
- ▶  $\tau$  and C:  $\sim 2.5\sigma$  apart

▶ Average:

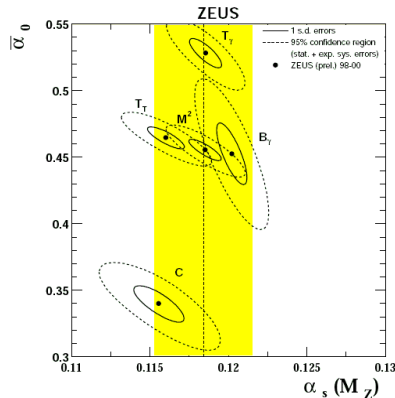
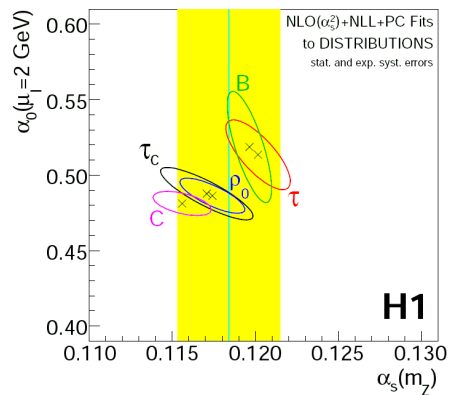
$$\alpha_s(m_Z) = 0.1198 \pm 0.0013 \text{ (exp)} \begin{matrix} +0.0056 \\ -0.0043 \end{matrix} \text{ (theo)}$$

$$\alpha_0 = 0.476 \pm 0.008 \text{ (exp)} \begin{matrix} +0.018 \\ -0.059 \end{matrix} \text{ (theo)}$$



- ▶  $\langle Q \rangle = 21 \dots 113 \text{ GeV}$
- ▶  $\chi^2/\text{dof}: T_\gamma$  and  $B_\gamma \sim 1$ , others 5
- ▶ C-parameter: low value of  $\alpha_0$ , else around 0.5

# Comparison of H1/ZEUS Results



## DISAGREE

### ▶ ZEUS:

- C-par:  $\alpha_0$  low
- overall  $\alpha_0$  lower, except  $T_\gamma$
- $\chi^2/\text{dof}$  large for  $T_t, \rho_0, C$

## AGREE

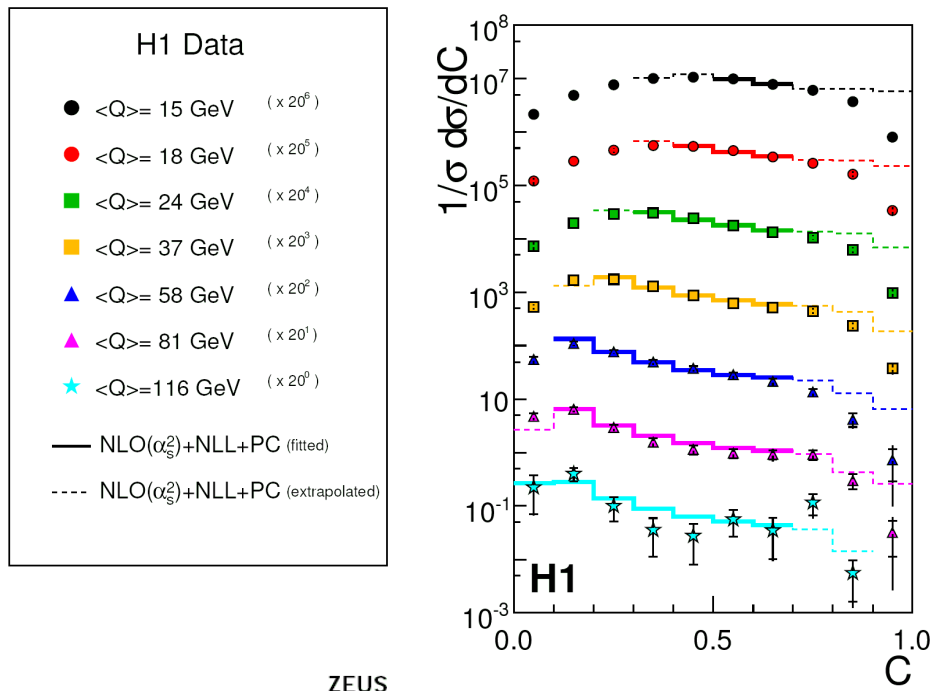
- ▶  $\alpha_s$  compatible with world mean
- ▶  $\alpha_s$  shape-by-shape
- ▶ neg. correlation between  $(\alpha_s, \alpha_0)$
- ▶ C prefers lowest  $(\alpha_s, \alpha_0)$  values
- ▶  $\chi^2/\text{dof}$  best for  $\gamma$ -axis variables

## DIFFERENCES

- ▶ correlations: H1 uses Bayes unfolding, syst. correlations
- ▶ matching scheme:  
H1: mod logR, ZEUS: mod  $M^2$
- ▶ bins used for fitting different



# Fit Ranges



- ▶ H1: more bins at low Q
- ▶ ZEUS: more bins at low F
- ▶ variation of fitted bins and matching schemes included in H1 theory uncertainty

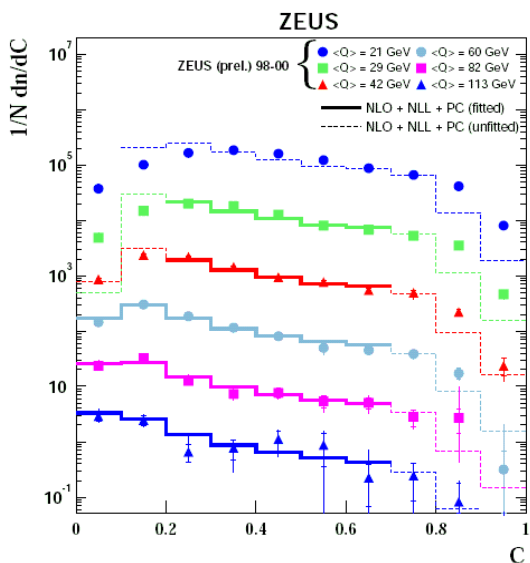
▶  $\gamma$ -axis thrust „ $\tau$ “  
 H1:  $\alpha_0 = 0.51 \pm 0.03 + 0.01 - 0.02$

ZEUS:  $\alpha_0 = 0.53 \pm 0.01$

▶  $\gamma$ -axis broadening „B“  
 H1:  $\alpha_0 = 0.52 \pm 0.04 + 0.03 - 0.01$

ZEUS:  $\alpha_0 = 0.45 \pm 0.02$

uncertainty: only matching, pdf and bins

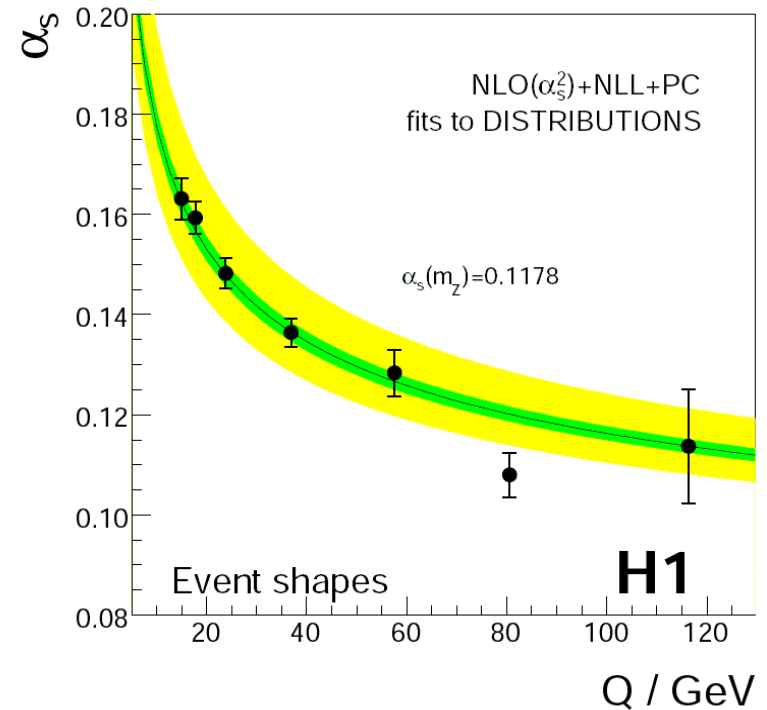


# H1 Distributions

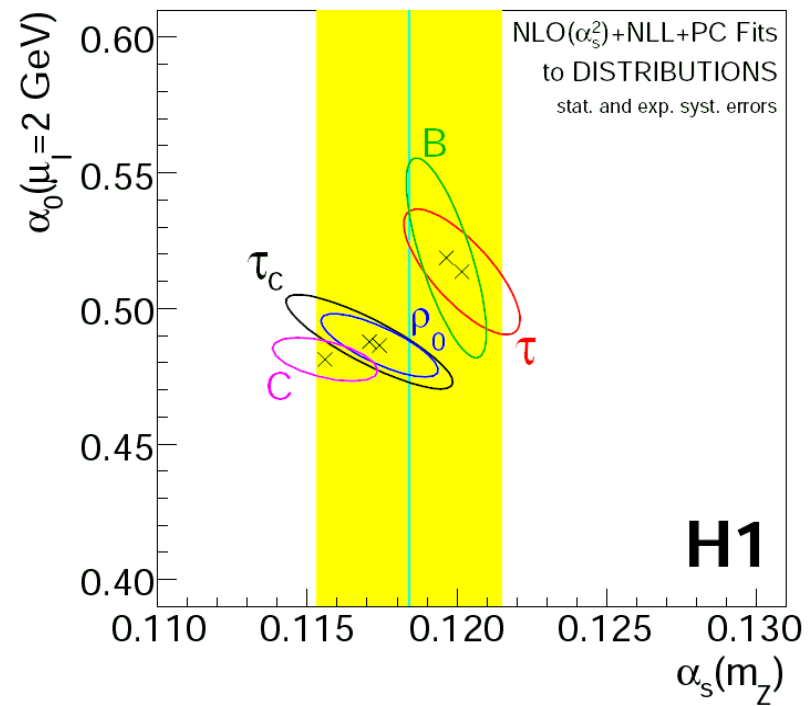
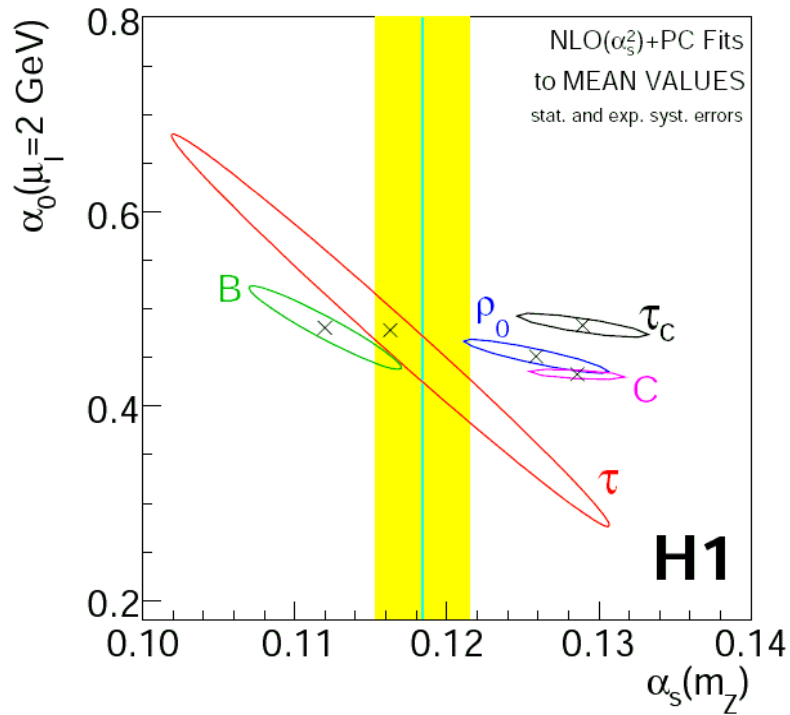
- ▶ now: assume PC valid
- ▶ fit  $\alpha_s(Q)$  with shape specific  $\alpha_0$
- ▶ observe running for all shapes
- ▶ combine, estimate correlations between variables
- ▶ result:

$$\alpha_s(m_Z) = 0.1178 \pm 0.0015 \text{ (exp)} \begin{matrix} +0.0081 \\ -0.0061 \end{matrix} \text{ (theo)}$$

- ▶ determination of  $\alpha_s(Q)$  over large range of scale!
- ▶ sizable renormalisation scale uncertainty

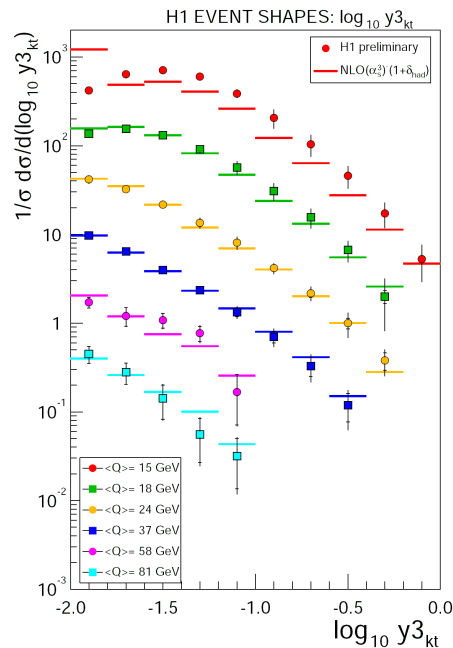
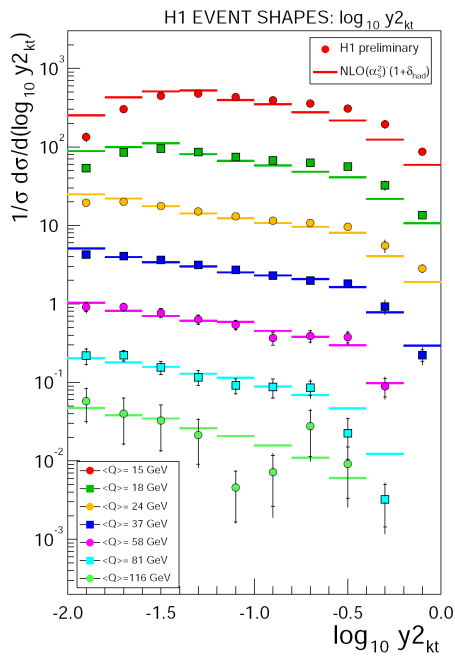


# Means vs Distributions



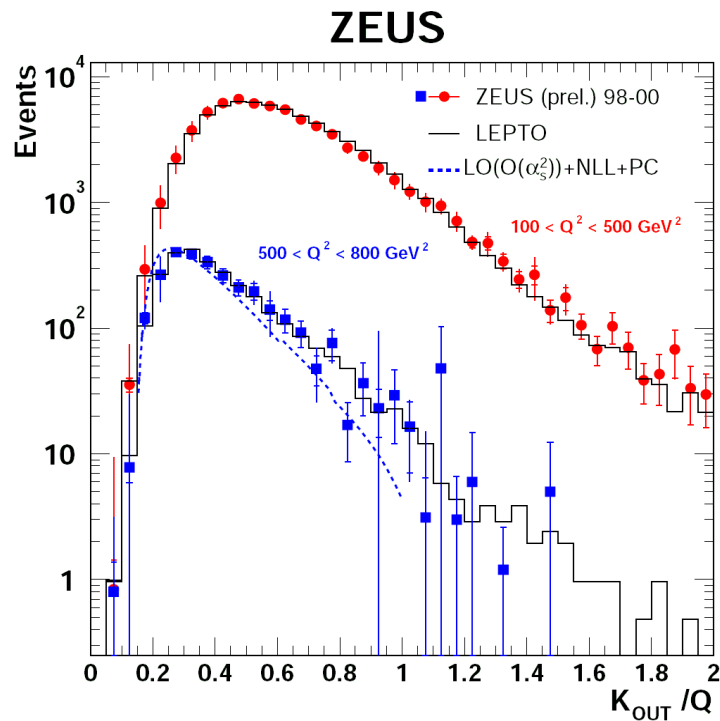
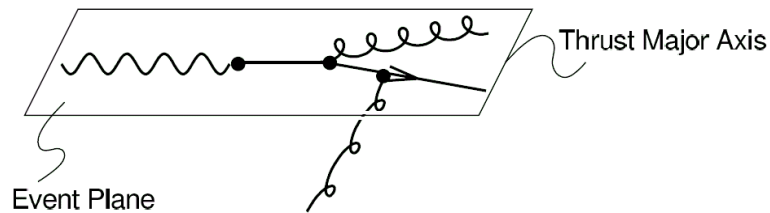
- ▶ Universality of  $\alpha_0$  : already good...
- ▶ ... improvements possible?

# Jet rates Distributions



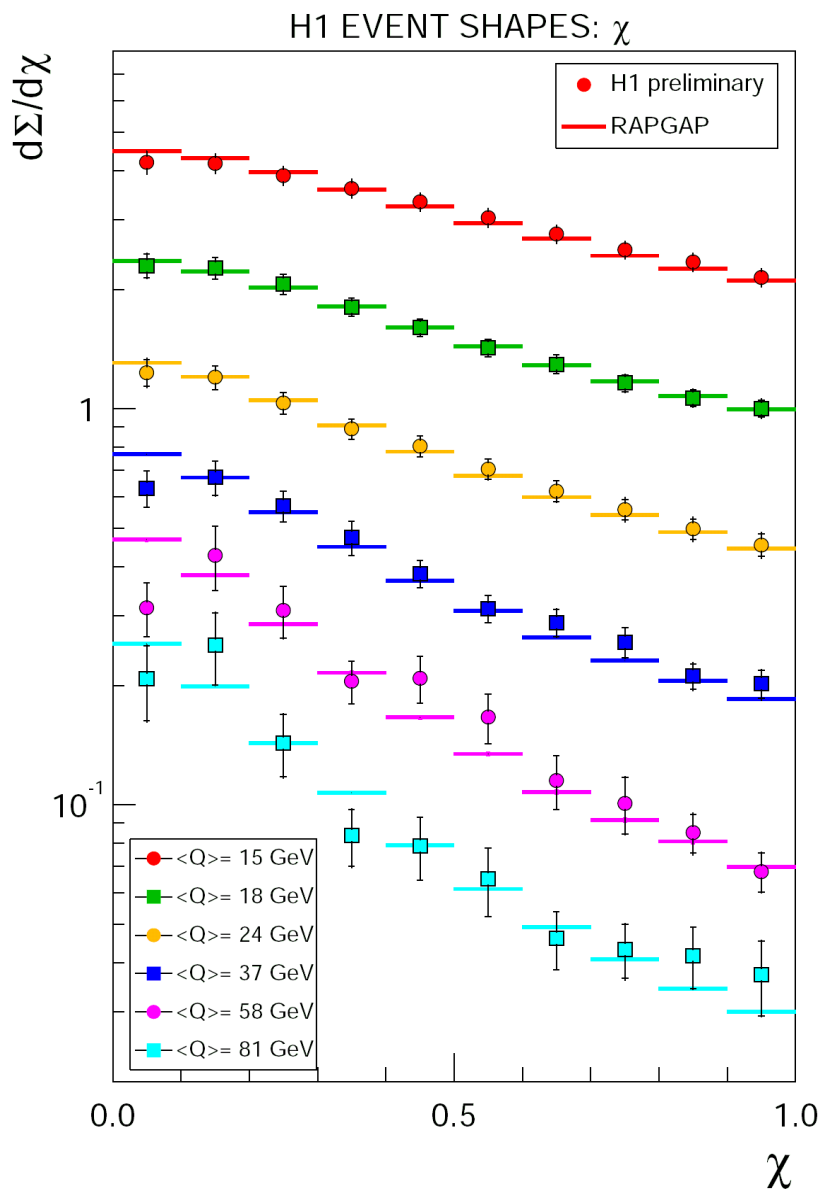
- ▶ distributions of jet rates
- ▶ H1 preliminary data
- ▶ power correction not known
- ▶ high Q  $\rightarrow$  hadronisation small
- ▶ fit of NLO with had. corr. from JETSET failed
- ▶ resummation needed?
- ▶ application for automated resummation (CAESAR)?

# 3-jet Distributions



- ▶  $K_{out}$ : momentum out of event plane
- ▶ sensitive to large angle emissions, in between hard jets
- ▶ extend from current hemisphere ( $\eta < 0$ ) to  $\eta < 3$
- ▶ not so inclusive as 2-jet variables: require  $0.1 < y_2 < 2.5$
- ▶ rather well description by LO+NLL+PC at higher Q, but some shift
- ▶ also prel. H1 data available  
Q: 15...81 GeV

# 3-jet Distributions



- ▶ azimuthal correlation in the event plane:  $\chi$
- ▶ same requirements for  $\eta$  and  $y_2$  as for  $K_{out}$
- ▶ for  $\chi$  and  $K_{out}$  need pQCD at  $\alpha_s^3$
- ▶ NLOJET++ with matched resummation?

# Summary and Conclusion

## STATUS

- ▶ mean values of 2-jet event shapes
  - consistent between H1 and ZEUS
  - universality of  $\alpha_0$ , spread in  $\alpha_s$
- ▶ distributions of 2-jet event shapes
  - recent H1 analysis: consistent  $\alpha_0$  and  $\alpha_s$
  - ZEUS preliminary: larger spread in  $\alpha_0$
- ▶ distributions of 3-jet event shapes
  - preliminary data for  $K_{\text{out}}$  and  $\chi$  available
  - up to now comparison to LO+NLL+PC

## (personal) WISHLIST

- ▶ confirmation for distributions by ZEUS
- ▶ resummed calculation matched with pQCD at  $\alpha_s^3$  for 3-jet distributions
- ▶ power corrections for  $k_t$  jet rate

# Backup

# of $Q$ bin	1	2	3	4	5	6	7
$Q$ Interval/GeV	[14,16]	[16,20]	[20,30]	[30,50]	[50,70]	[70,100]	[100,200]
$\langle Q \rangle$ /GeV	14.9	17.7	23.8	36.9	57.6	80.6	115.6
$\langle x \rangle$	0.00841	0.0118	0.0209	0.0491	0.116	0.199	0.323

strong coupling constant $\alpha_s(m_Z)$					
event shape variable	$\tau_c$	$\tau$	$B$	$\rho_0$	$C$
central value	0.1171	0.1202	0.1196	0.1174	0.1156
uncertainties:					
total	+0.0068 -0.0062	+0.0072 -0.0058	+0.0072 -0.0064	+0.0070 -0.0056	+0.0073 -0.0054
total experimental	$\pm 0.0035$	$\pm 0.0021$	$\pm 0.0014$	$\pm 0.0021$	$\pm 0.0021$
statistical experimental	$\pm 0.0014$	$\pm 0.0006$	$\pm 0.0004$	$\pm 0.0010$	$\pm 0.0009$
systematic experimental	$\pm 0.0033$	$\pm 0.0020$	$\pm 0.0013$	$\pm 0.0019$	$\pm 0.0019$
total theoretical	+0.0058 -0.0051	+0.0068 -0.0054	+0.0071 -0.0063	+0.0067 -0.0052	+0.0069 -0.0049
$\mu_r$ dependence	+0.0054 -0.0048	+0.0058 -0.0043	+0.0056 -0.0044	+0.0064 -0.0050	+0.0069 -0.0048
$\mu_I$ dependence	+0.0002 -0.0002	$<10^{-4}$	$<10^{-4}$	+0.0002 -0.0002	$<10^{-4}$
fit interval	+0.0015 -0.0018	+0.0007 -0.0022	+0.0001 -0.0009	+0.0010 +0.0007	+0.0003 -0.0004
parton density functions	+0.0002 -0.0001	+0.0003 -0.0010	+0.0006 -0.0007	+0.0001 -0.0002	+0.0002 -0.0001
matching scheme	+0.0015 +0.0005	+0.0036 +0.0022	+0.0043 +0.0043	+0.0018 +0.0009	-0.0005 -0.0009

non perturbative coupling $\alpha_0(\mu_I = 2 \text{ GeV})$					
event shape variable	$\tau_c$	$\tau$	$B$	$\rho_0$	$C$
central value	0.488	0.513	0.519	0.486	0.481
uncertainties:					
total	+0.037 -0.035	+0.034 -0.039	+0.059 -0.049	+0.023 -0.035	+0.028 -0.042
total experimental	$\pm 0.021$	$\pm 0.025$	$\pm 0.039$	$\pm 0.014$	$\pm 0.008$
statistical experimental	$\pm 0.009$	$\pm 0.009$	$\pm 0.006$	$\pm 0.006$	$\pm 0.005$
systematic experimental	$\pm 0.019$	$\pm 0.023$	$\pm 0.038$	$\pm 0.013$	$\pm 0.007$
total theoretical	+0.030 -0.027	+0.022 -0.029	+0.044 -0.029	+0.019 -0.032	+0.026 -0.041
$\mu_r$ dependence	+0.020 -0.026	+0.018 -0.027	+0.030 -0.028	+0.017 -0.027	+0.022 -0.038
fit interval	+0.022 -0.007	+0.008 -0.005	+0.030 +0.006	-0.003 -0.016	+0.006 -0.003
parton density functions	+0.001 -0.001	+0.006 +0.004	+0.011 +0.003	+0.001 -0.001	+0.001 -0.002
matching scheme	-0.005 -0.012	-0.009 -0.023	+0.006 -0.010	-0.006 -0.009	-0.014 -0.014

correlation coefficient $\alpha_s, \alpha_0$	-0.85	-0.76	-0.75	-0.78	-0.51
$\chi^2 / \text{d.o.f. (experimental errors)}$	1.13	0.51	0.81	1.40	1.20