

Dijets at low x and low Q^2

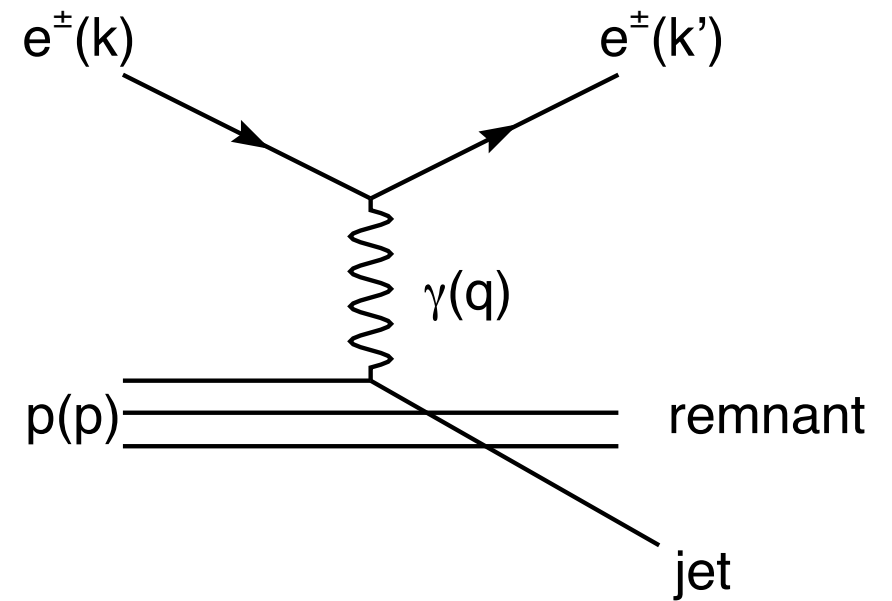
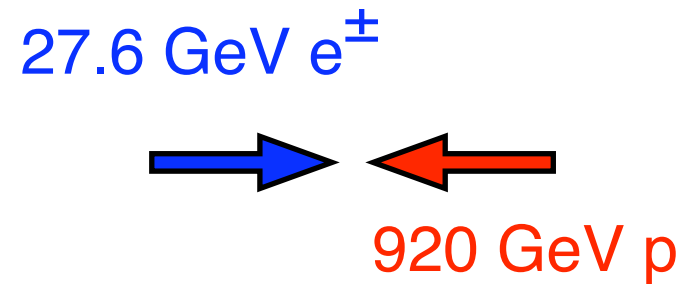
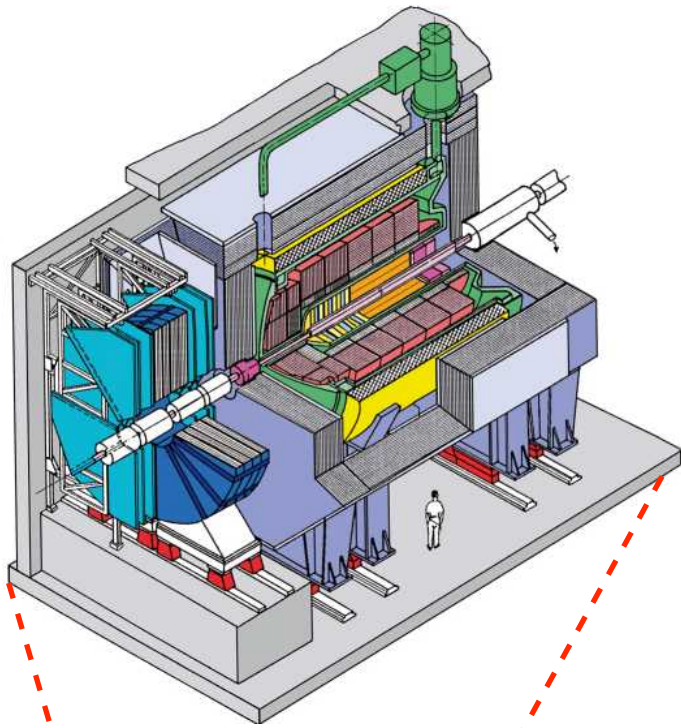
Carsten Niebuhr
DESY



for the H1 Collaboration

EPS2005, Lisbon Portugal

Deep Inelastic Scattering at HERA



Kinematic Variables:

$$Q^2 = -q^2 = -(k - k')^2 \quad \text{Momentum transfer}$$

$$x = \frac{Q^2}{2p \cdot q} \quad \text{Fraction of the proton's momentum that participates in the hard scatter}$$

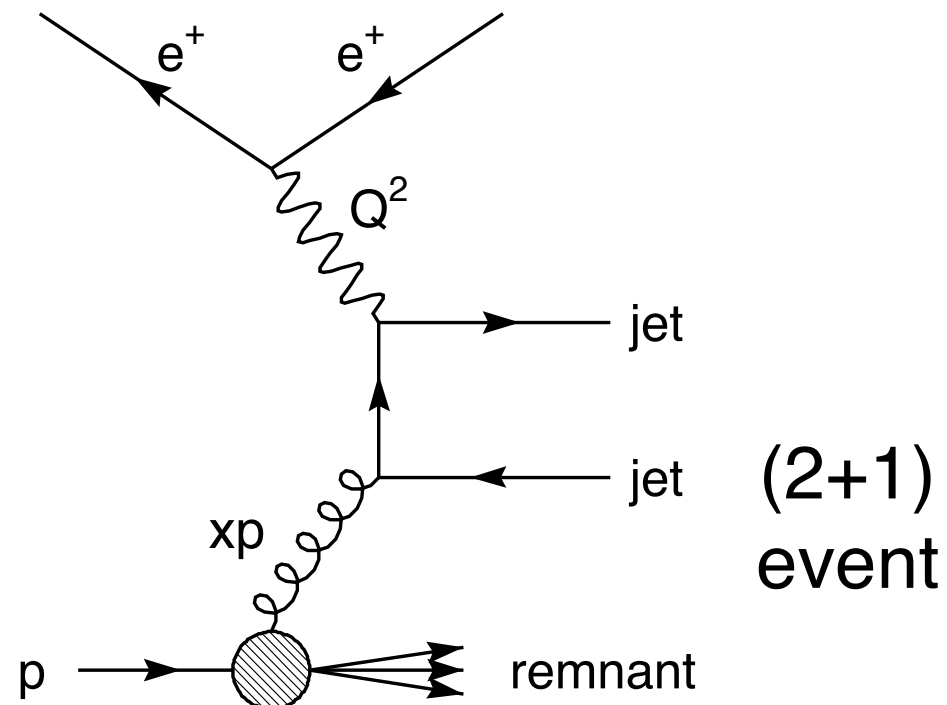
$$y = \frac{p \cdot q}{p \cdot k} \quad \text{Fraction of the electron's energy available in the proton's rest frame}$$

$$Q^2 = sxy \quad \text{s=center of mass energy squared}$$

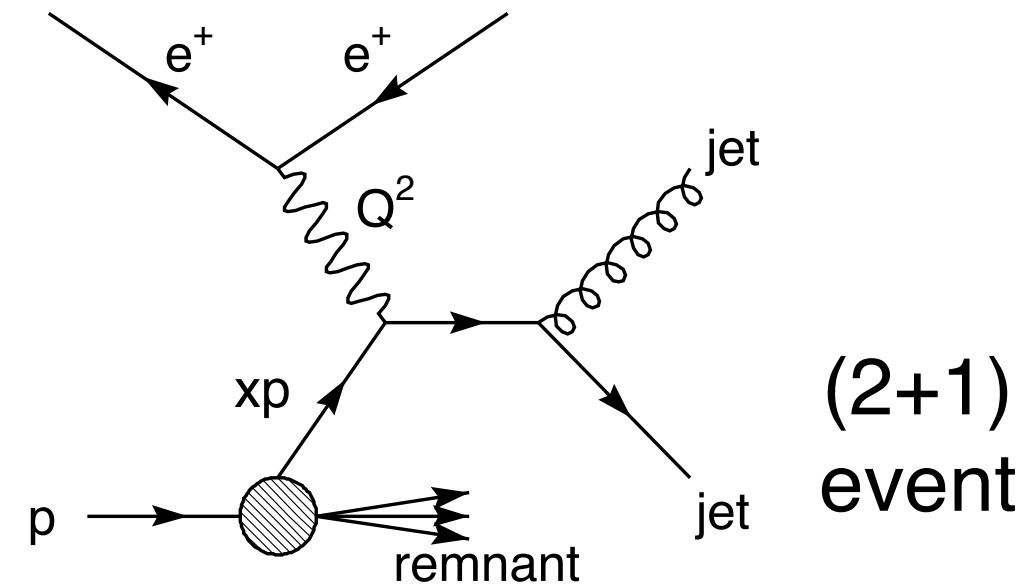


Dijet Production at HERA

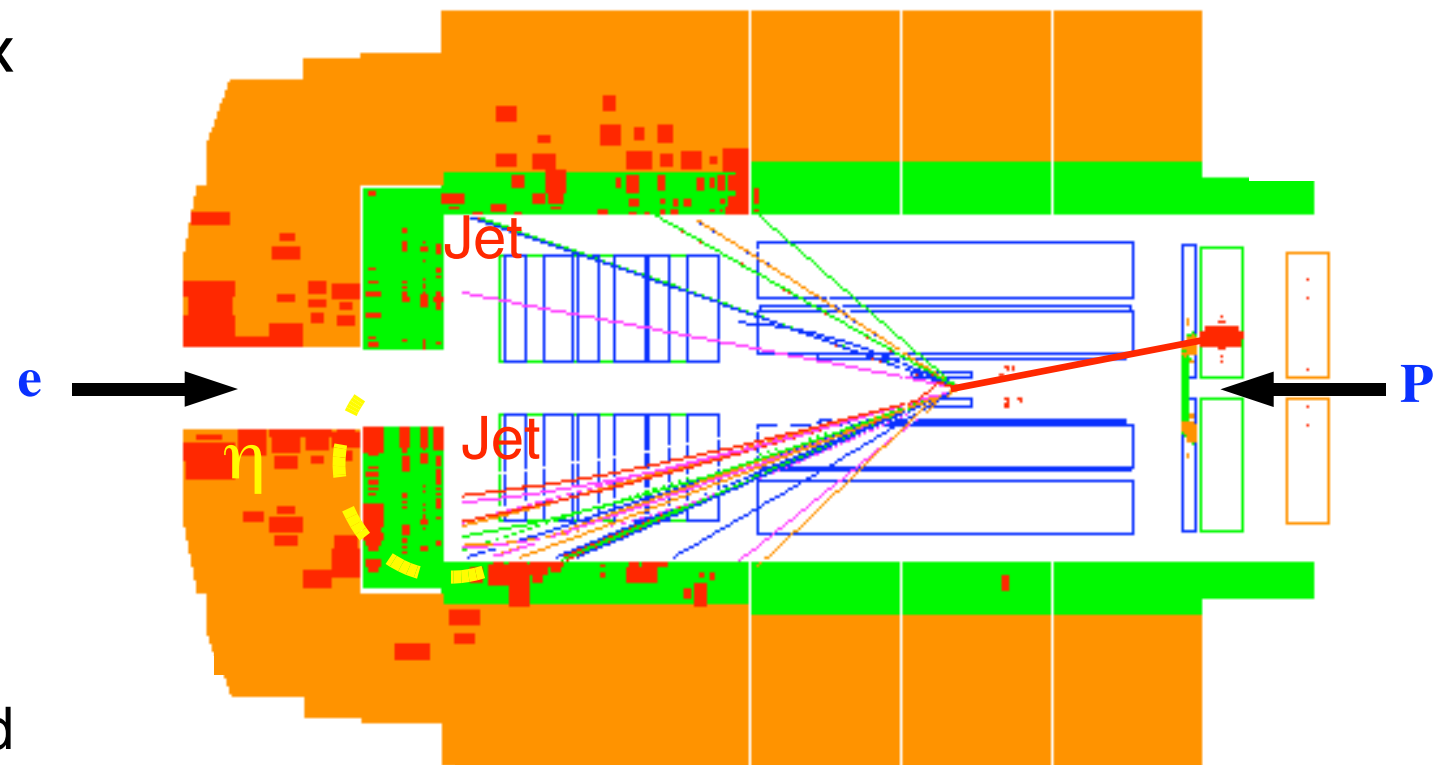
Boson Gluon Fusion



QCD Compton



- Boson Gluon Fusion dominates at low x
- Dijet production provides sensitivity to parton distribution & evolution
- Data presented here are at medium Q^2
 - $2 < Q^2 < 100 \text{ GeV}^2$
 - scattered electron detected in backward calorimeter (SPACAL)



Parton Dynamics in DIS

Different parton evolution schemes exist:

- DGLAP

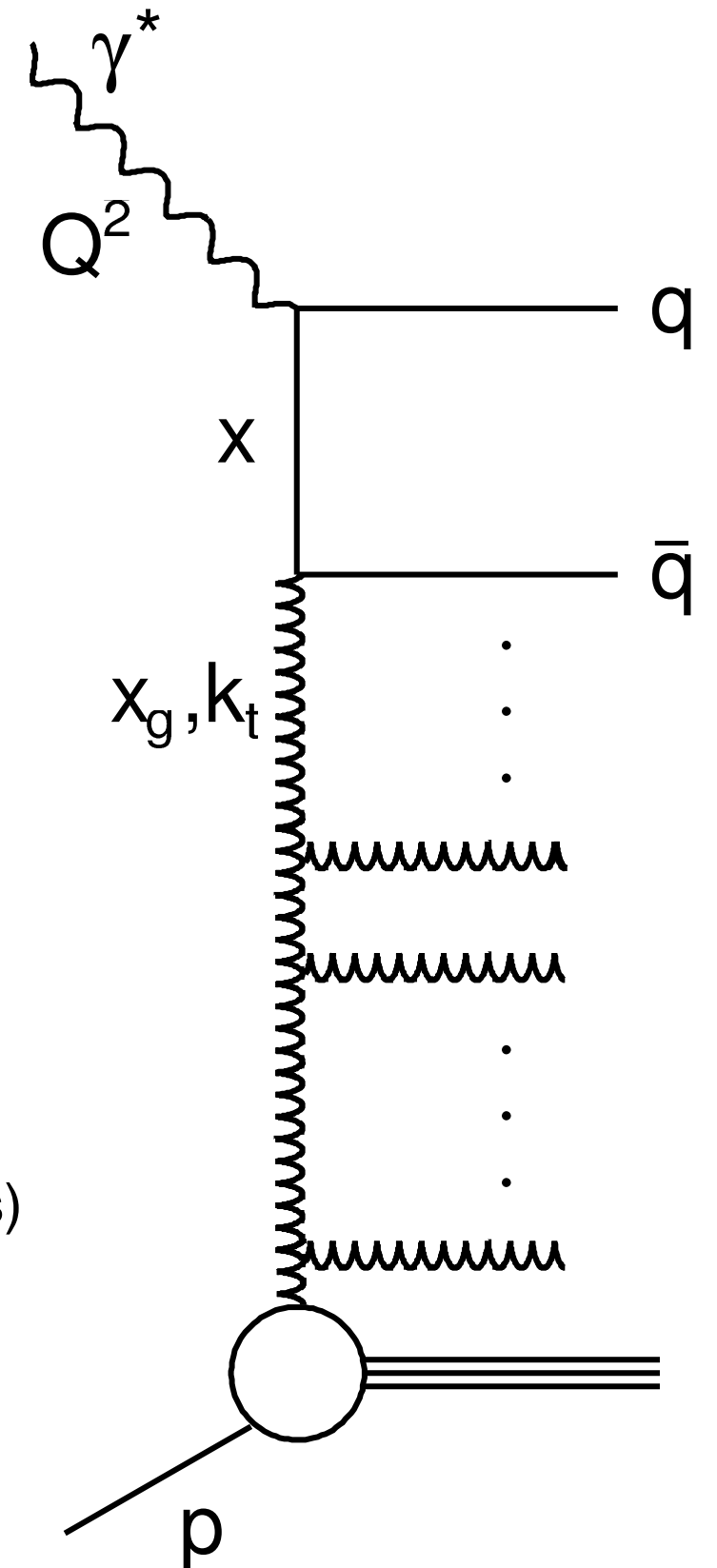
- evolution in Q^2 or k_T^2
- at small x strong k_T ordering: $k_{T,1}^2 \ll \dots \ll k_{T,i}^2 \ll \dots \ll Q^2$
- neglects $\log(1/x)$ terms, expected to break down at very low x

- BFKL

- evolution in $x \Rightarrow$ appropriate at **small x**
- no k_T ordering, instead: $x_1 \ll \dots \ll x_i \ll \dots \ll x$
- successful for forward jets and forward particle production

- CCFM

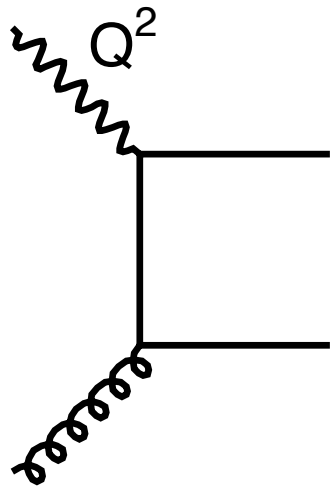
- no k_T ordering, instead angular ordering (gluon coherence effects)
 - for small x : CCFM \rightarrow BFKL
 - for large x : CCFM \rightarrow DGLAP
- MC implementation: CASCADE
- use of unintegrated PDFs



LO and NLO Monte Carlo Programs based on DGLAP

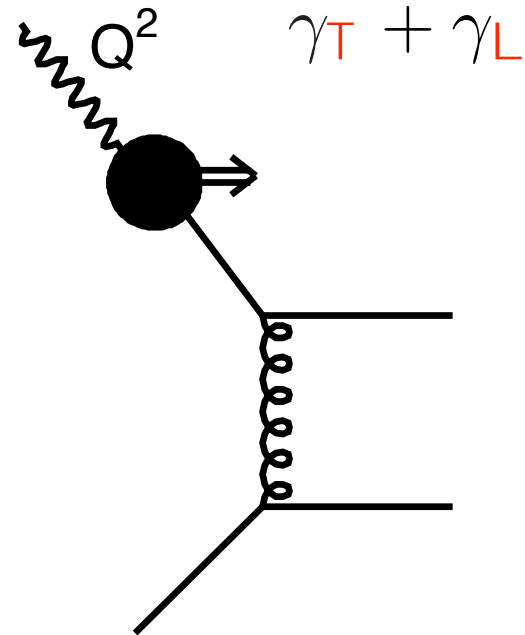
HERWIG

LO direct



+

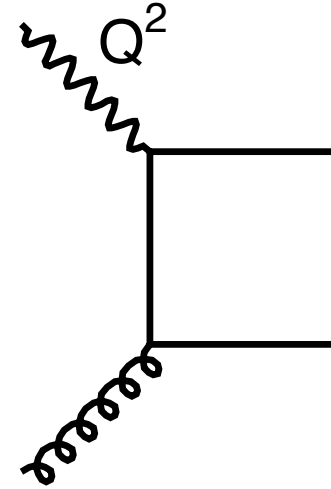
LO resolved



+ parton showers

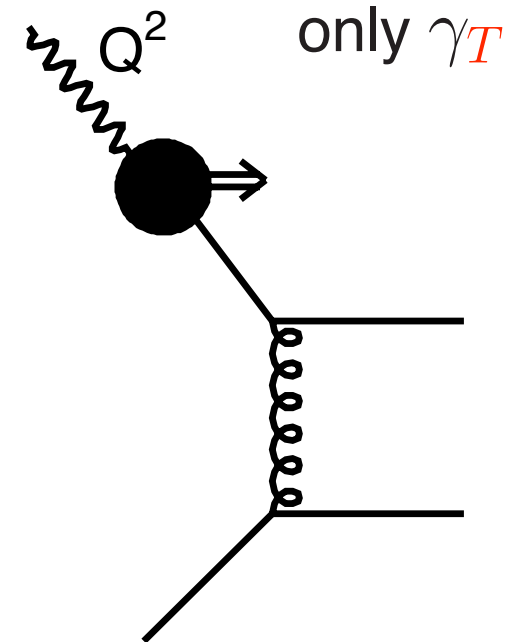
RAPGAP

LO direct



+

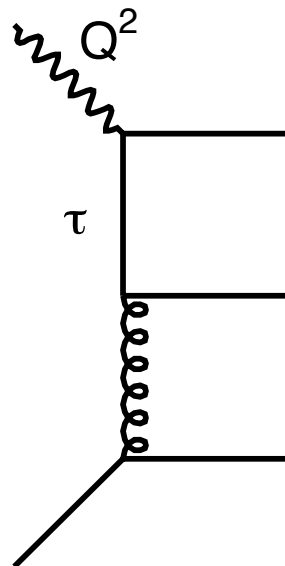
LO resolved



+ parton showers

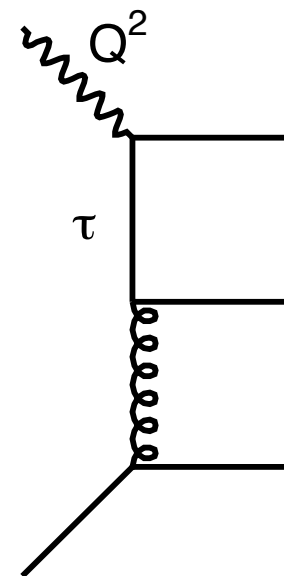
DISENT

NLO direct



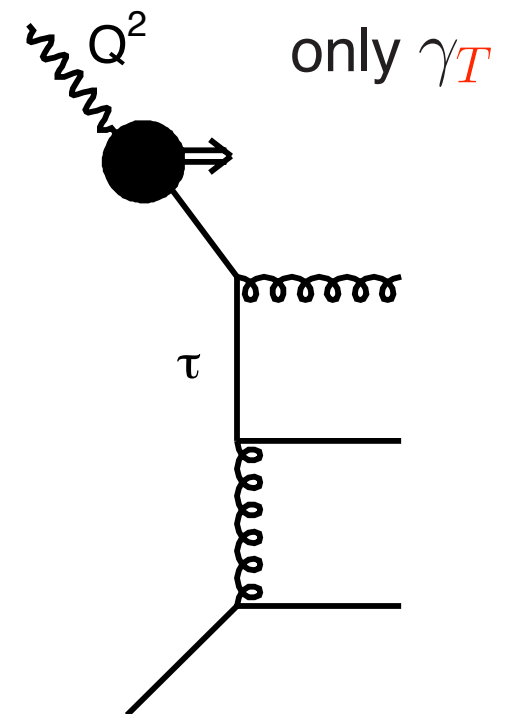
JETVIP

NLO direct



+

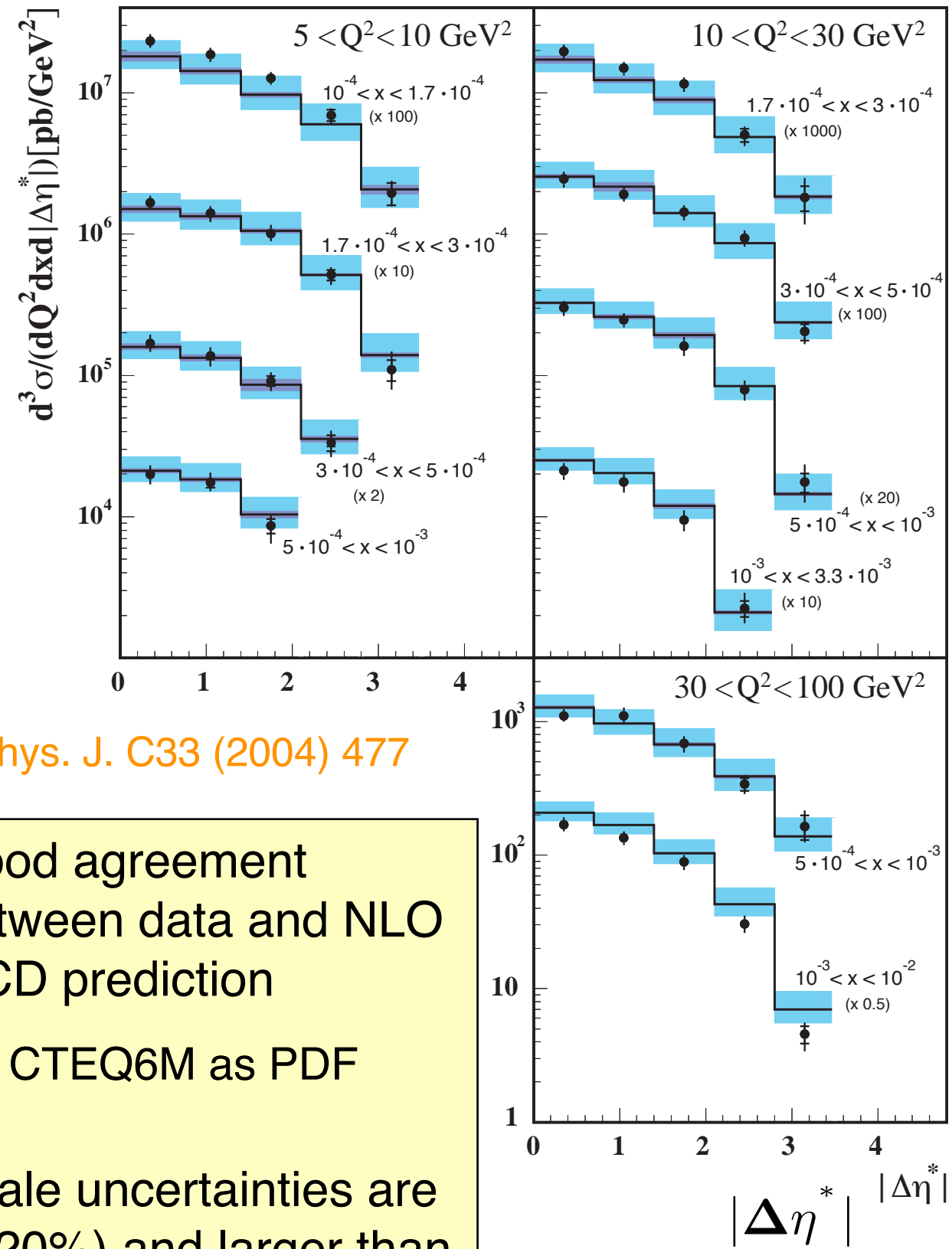
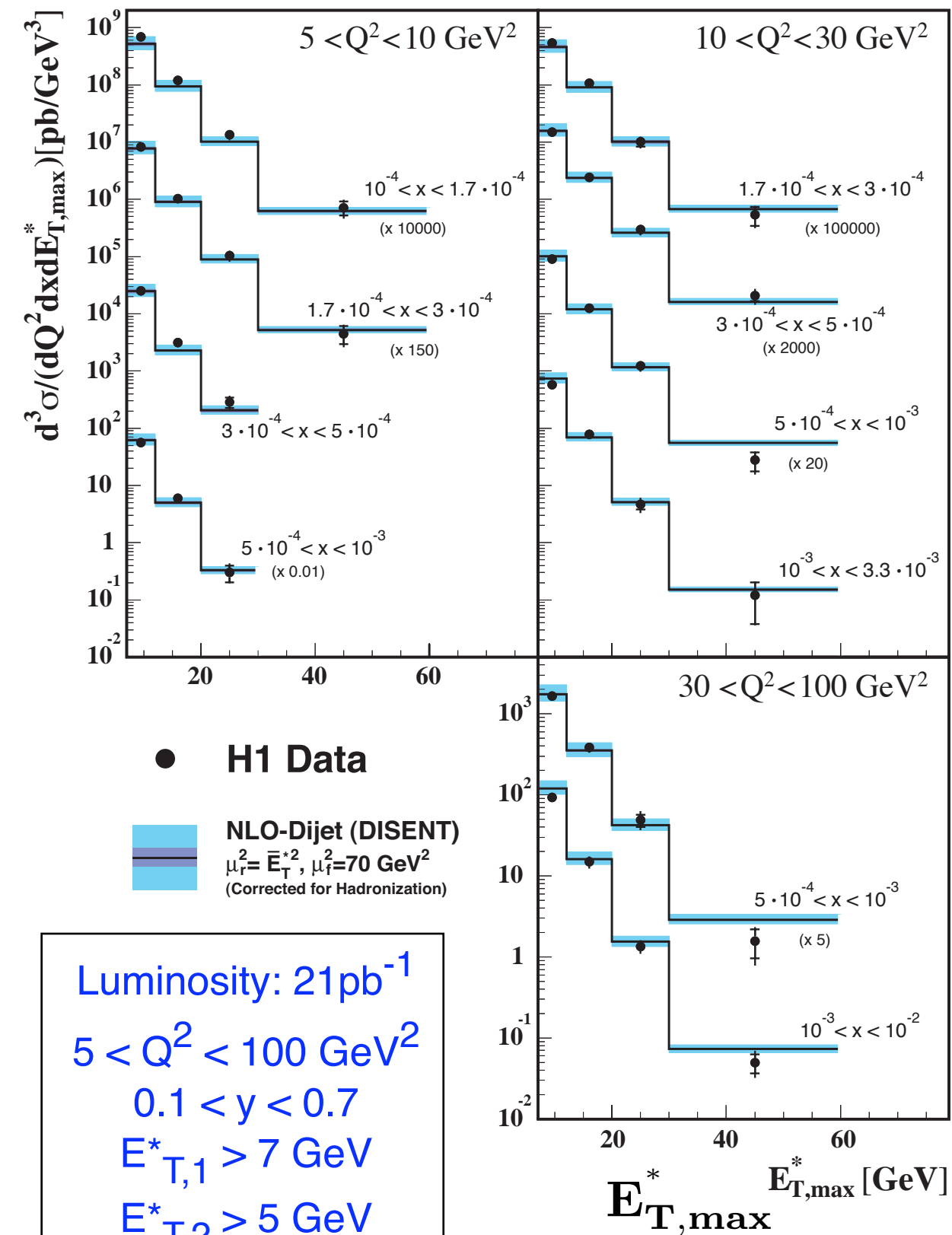
NLO resolved



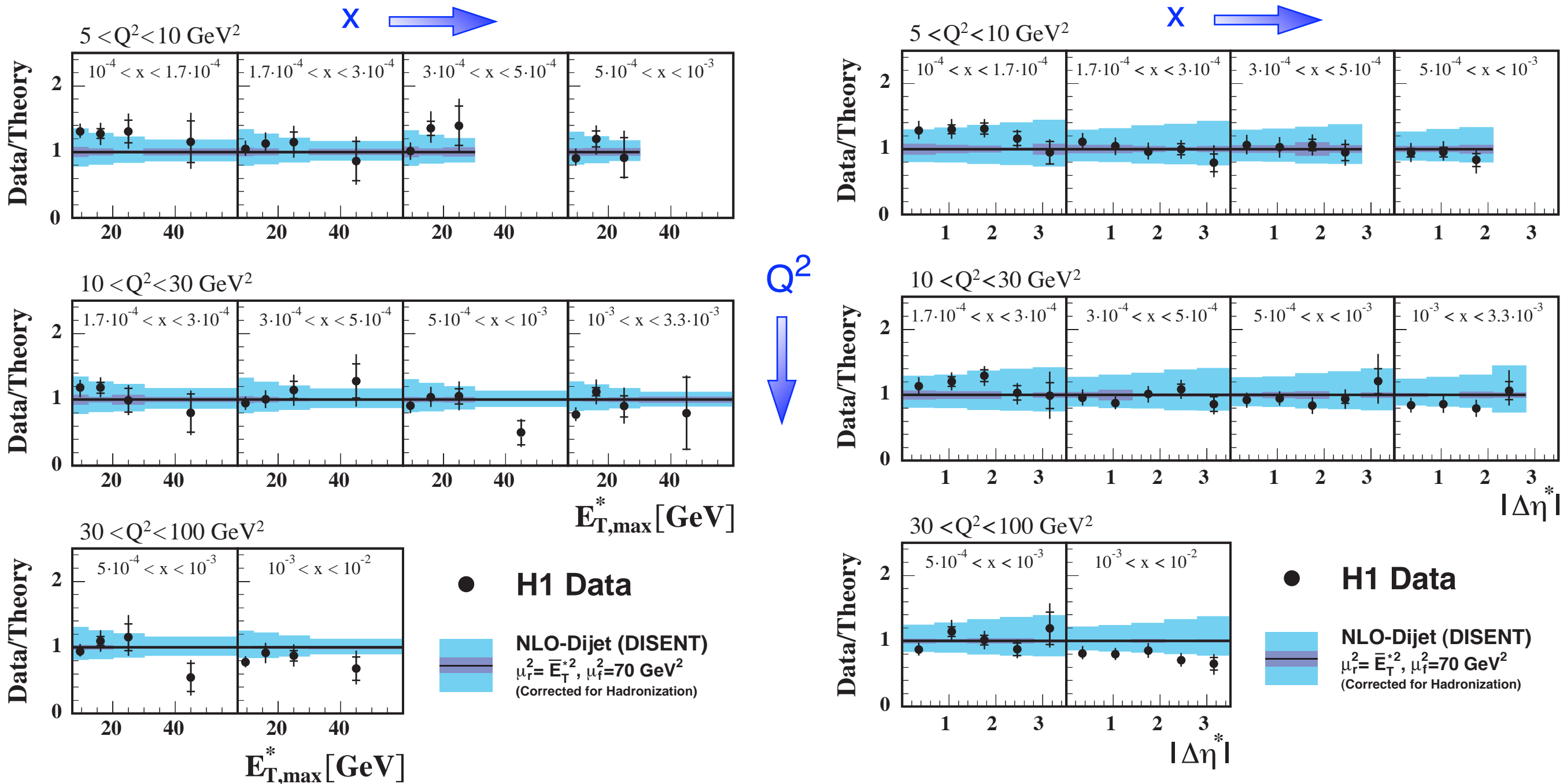
≈ NNLO direct

carsten.niebuhr@desy.de

Triple Differential Dijet Cross Section



Data / NLO for Triple Differential Dijet Cross Section



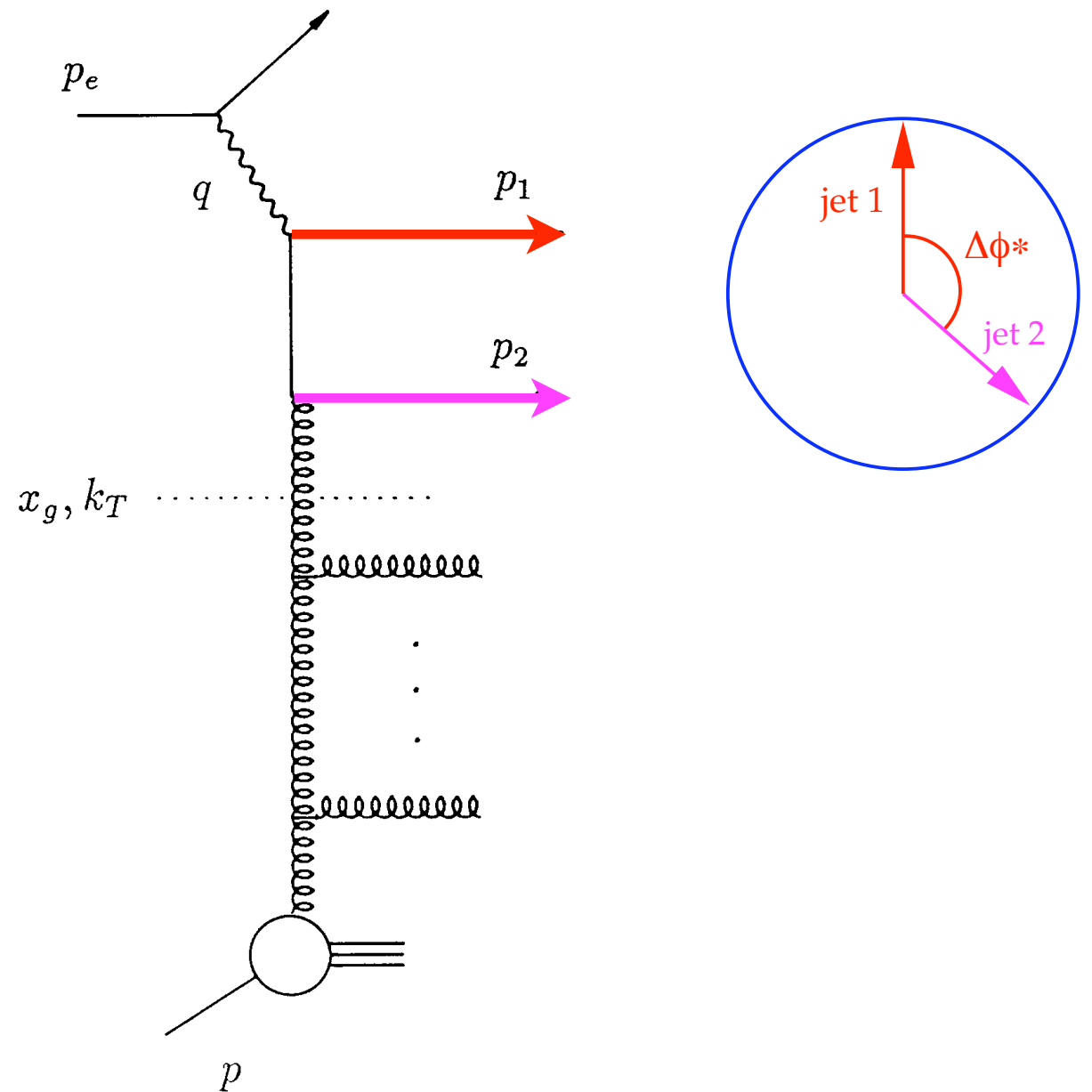
- Effects from low- x dynamics expected to be largest at small $E_{T,max}^*$ and $|\Delta\eta^*|$
- Even in these regions observe good agreement between data and NLO calculations
- To find deviations from DGLAP have to look into more details of final state properties

Dijet Azimuthal Separation

- In LO DGLAP jets are in a back-to-back azimuthal configuration ($k_T \approx 0$)
- Deviations can be due to:
 - higher orders in conventional QCD (NLO, NNLO, ...) and/or
 - alternative parton evolution leading to non-zero k_T
- Study fraction of dijet events for which $\Delta\phi^*$ is significantly smaller than π :

$$S(\alpha) = \frac{\int_0^\alpha N_{Dijet}(\Delta\phi^*, x, Q^2) d\Delta\phi^*}{\int_0^\pi N_{Dijet}(\Delta\phi^*, x, Q^2) d\Delta\phi^*}$$

- choose $\alpha = 2\pi/3$



$$\vec{k}_T = \vec{p}_{T,1} + \vec{p}_{T,2}$$

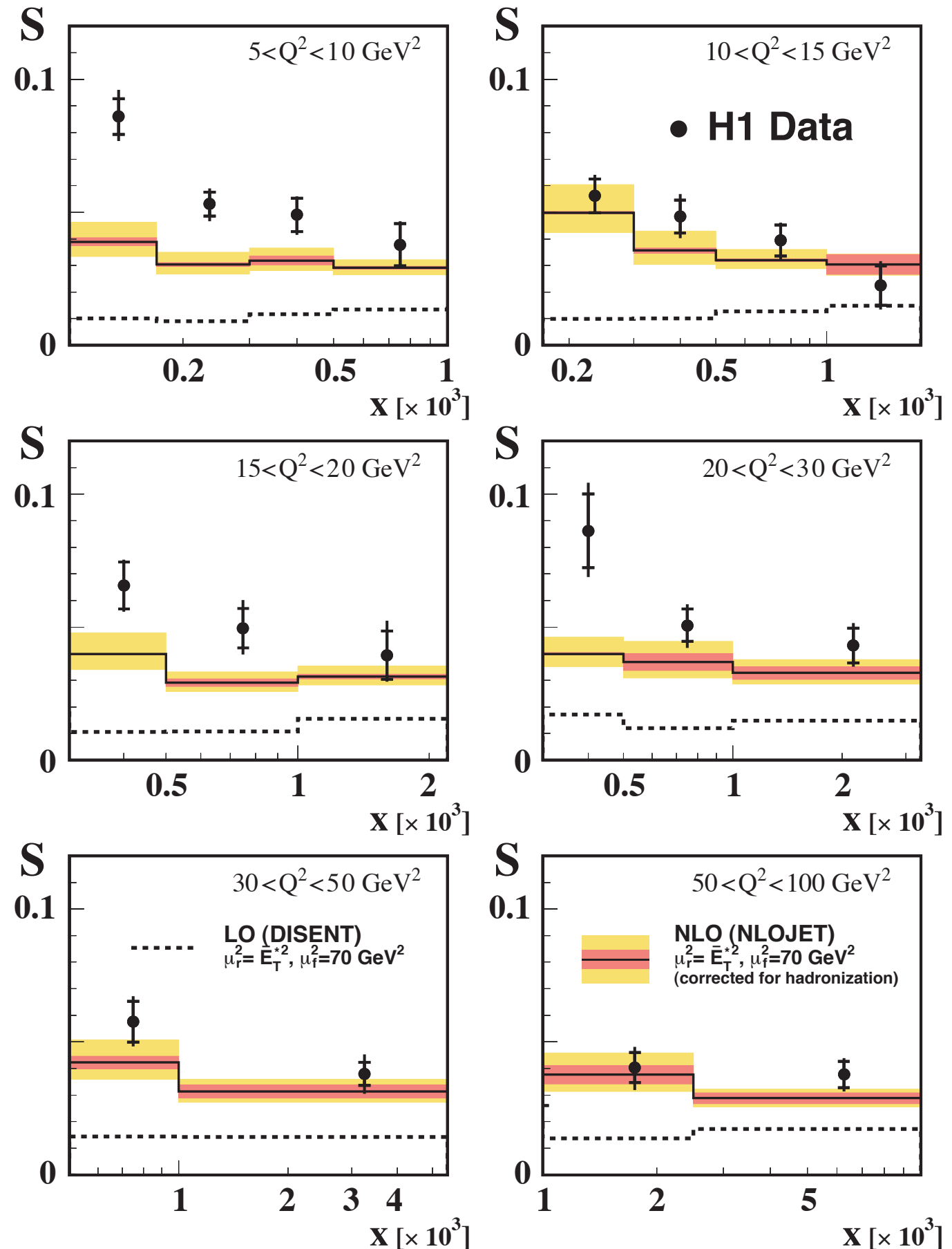
$$k_T^2 = p_{T,1}^2 + p_{T,2}^2 + 2p_{T,1}p_{T,2} \cos \Delta\phi^*$$

\Rightarrow for $k_T \approx 0$ jets are \sim back-to-back

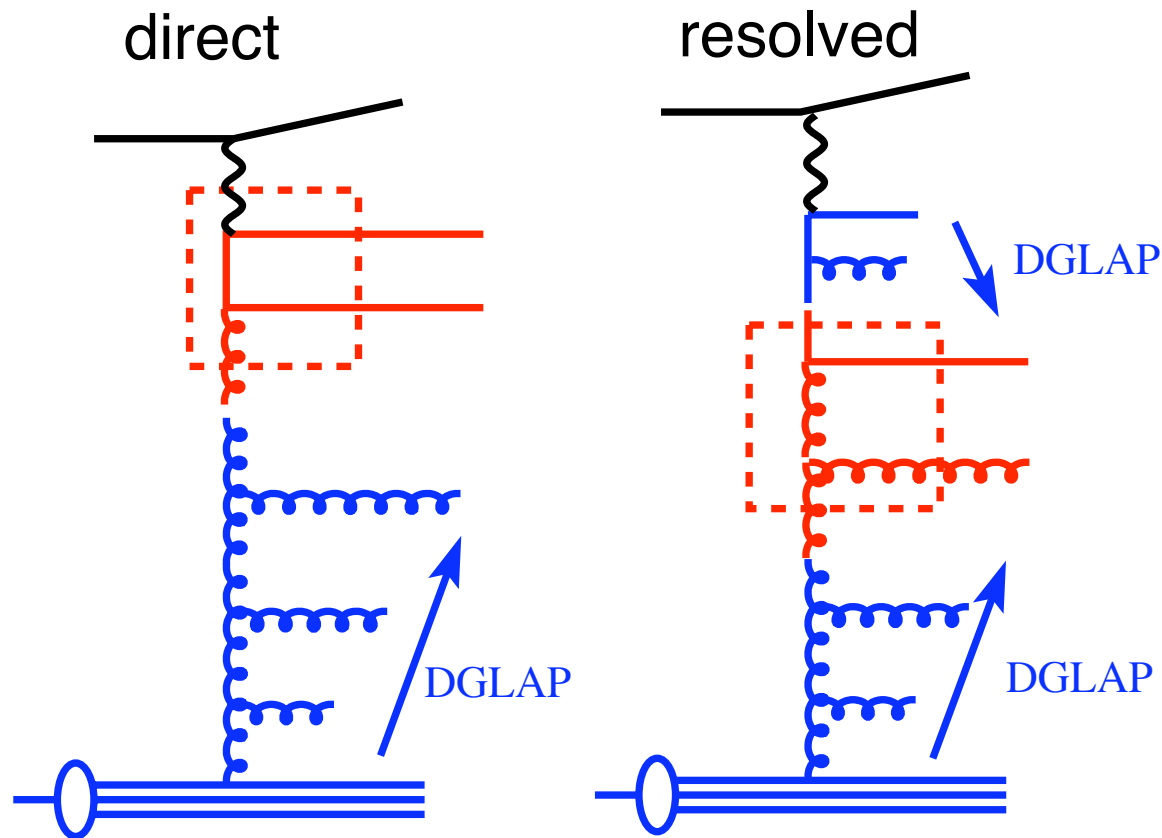
Compare with LO and NLO Calculations

$$S = \frac{\int_0^{2\pi/3} N_{Dijet}(\Delta\phi^*, x, Q^2) d\Delta\phi^*}{\int_0^\pi N_{Dijet}(\Delta\phi^*, x, Q^2) d\Delta\phi^*}$$

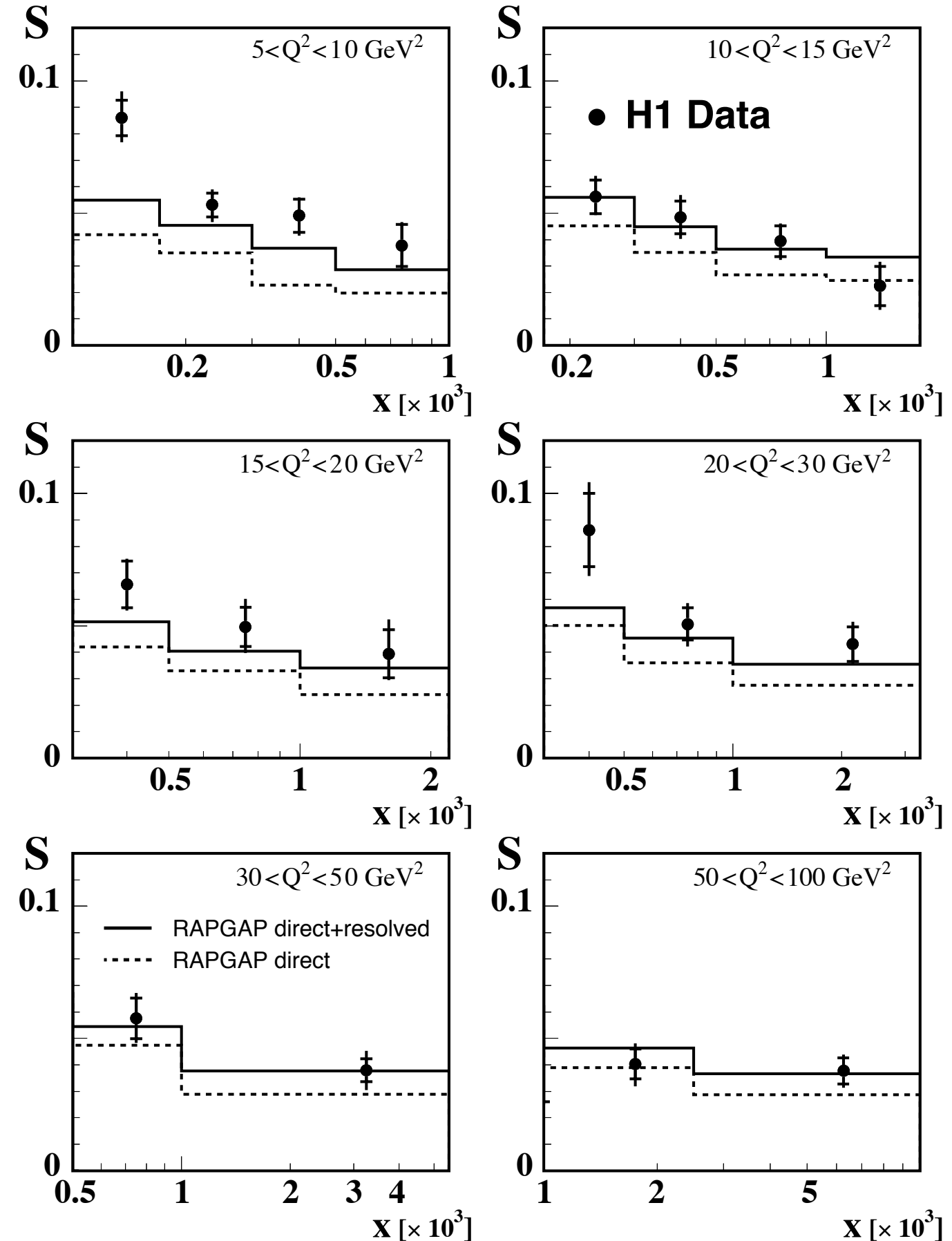
- Data show significant increase towards low x
- Study effect of higher orders:
 - LO predictions [$O(\alpha_s)$]
 - at most 3 jets in final state
 - completely fails to describe data
 - NLO calculations [up to $O(\alpha_s^3)$]
 - 3 or 4 jets in final state
 - reasonable description at large x, Q^2
 - but still too low at small x, Q^2



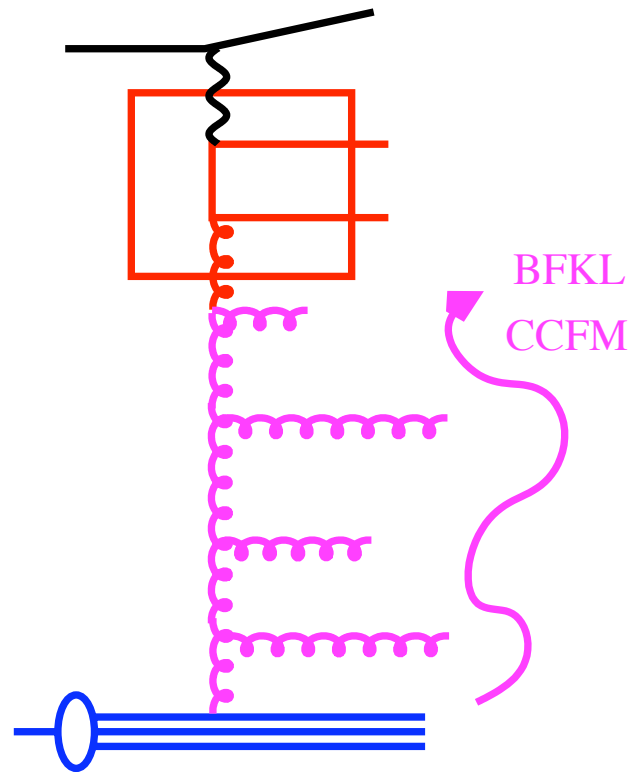
Influence of Resolved Photon Contribution



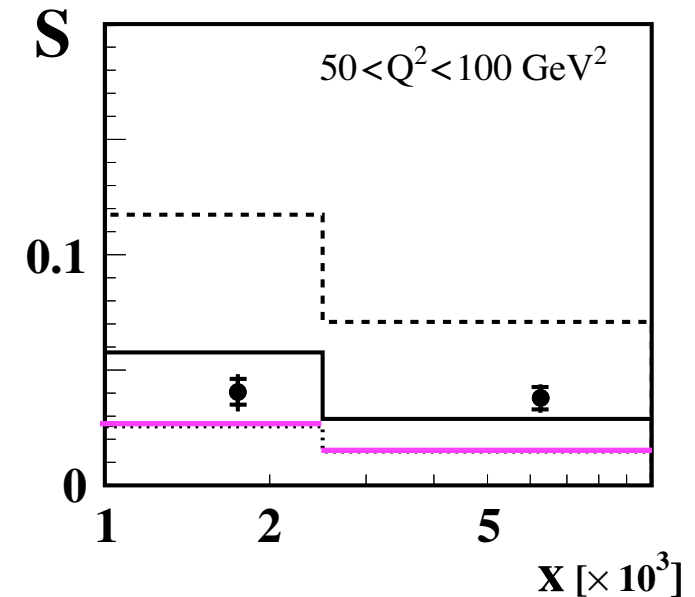
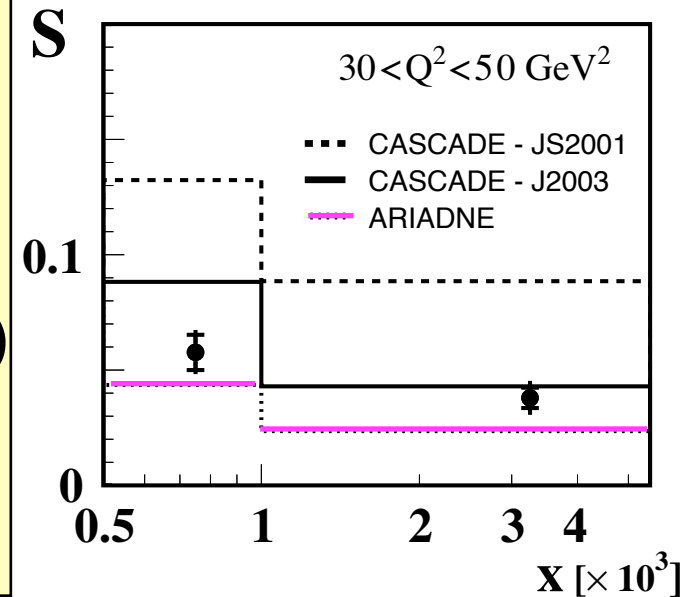
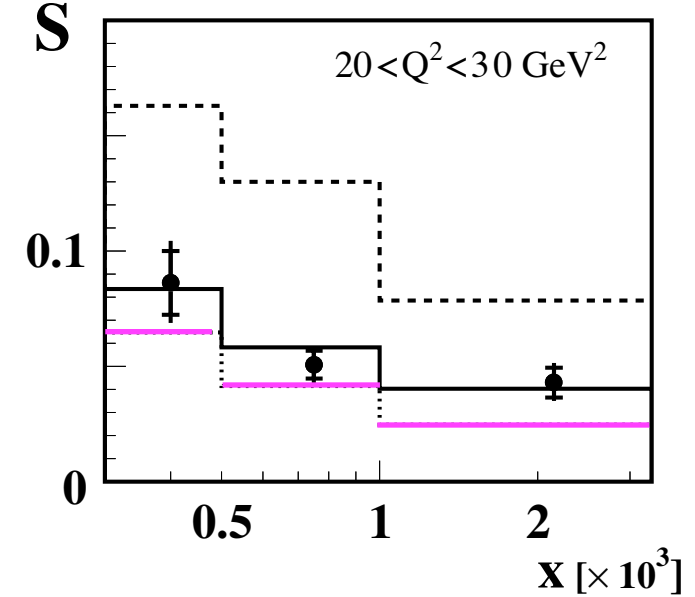
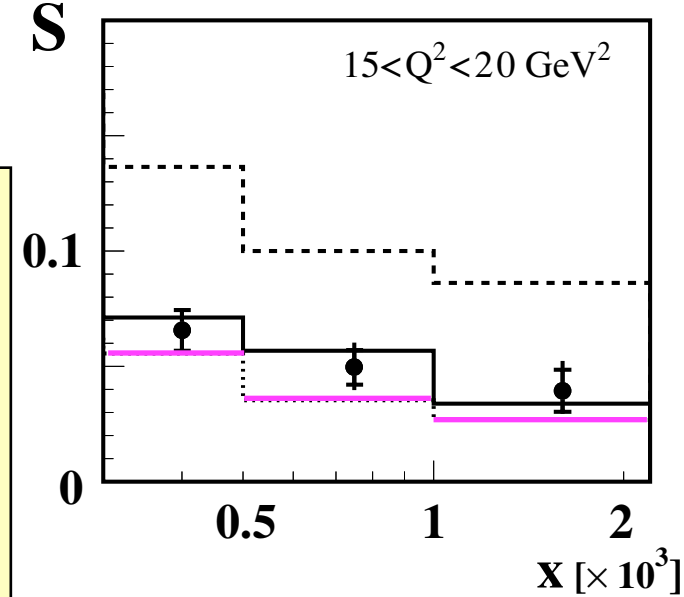
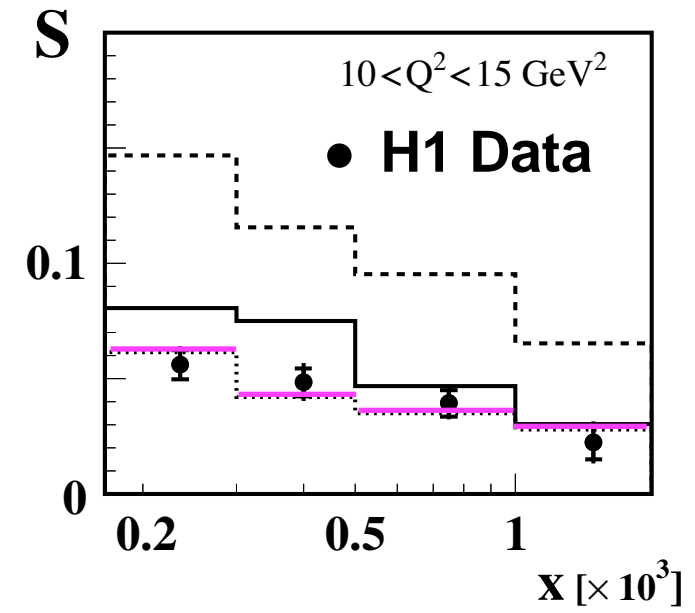
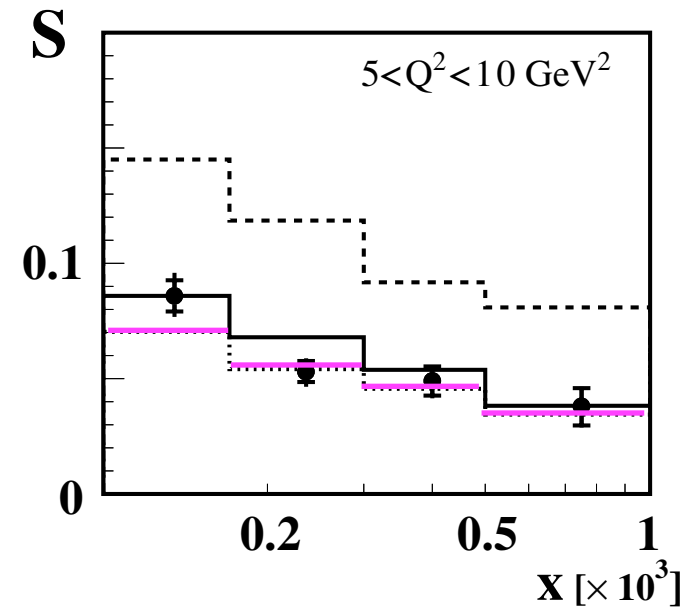
- Resolved photon contribution emulates non- k_T -ordered parton emissions
- Description improves but still falls below the data at small x and Q^2



Alternative Parton Evolutions

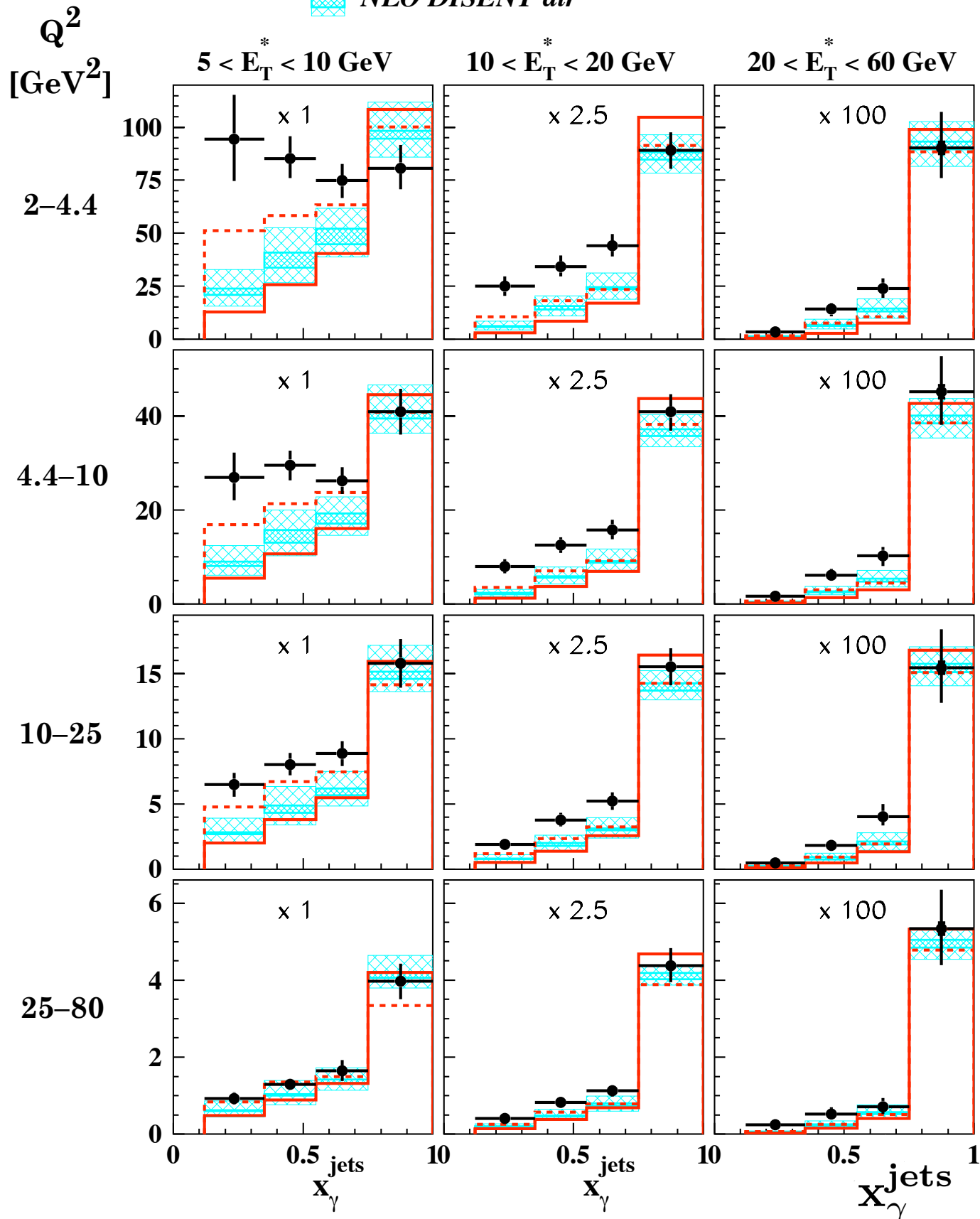


- CASCADE (CCFM evolution) using unintegrated PDFs describes data well
- Data provide sensitivity to choice of unintegrated PDF
 - J2003 much better than JS2001
 - JS2001 only singular terms
 - J2003 full splitting function [set 2 shown]
- ARIADNE (Color Dipole Model: 'BFKL like') also describes the data at low x , Q^2
 - but systematically too low at larger Q^2



Comparison with NLO Calculations $d^3\sigma_{2\text{jet}}/(dQ^2 dE_T^* dx_\gamma^{\text{jets}})$

- *H1 data*
- *NLO JETVIP dir*
- *NLO JETVIP dir+res_T*
- ▨ *NLO DISENT dir*



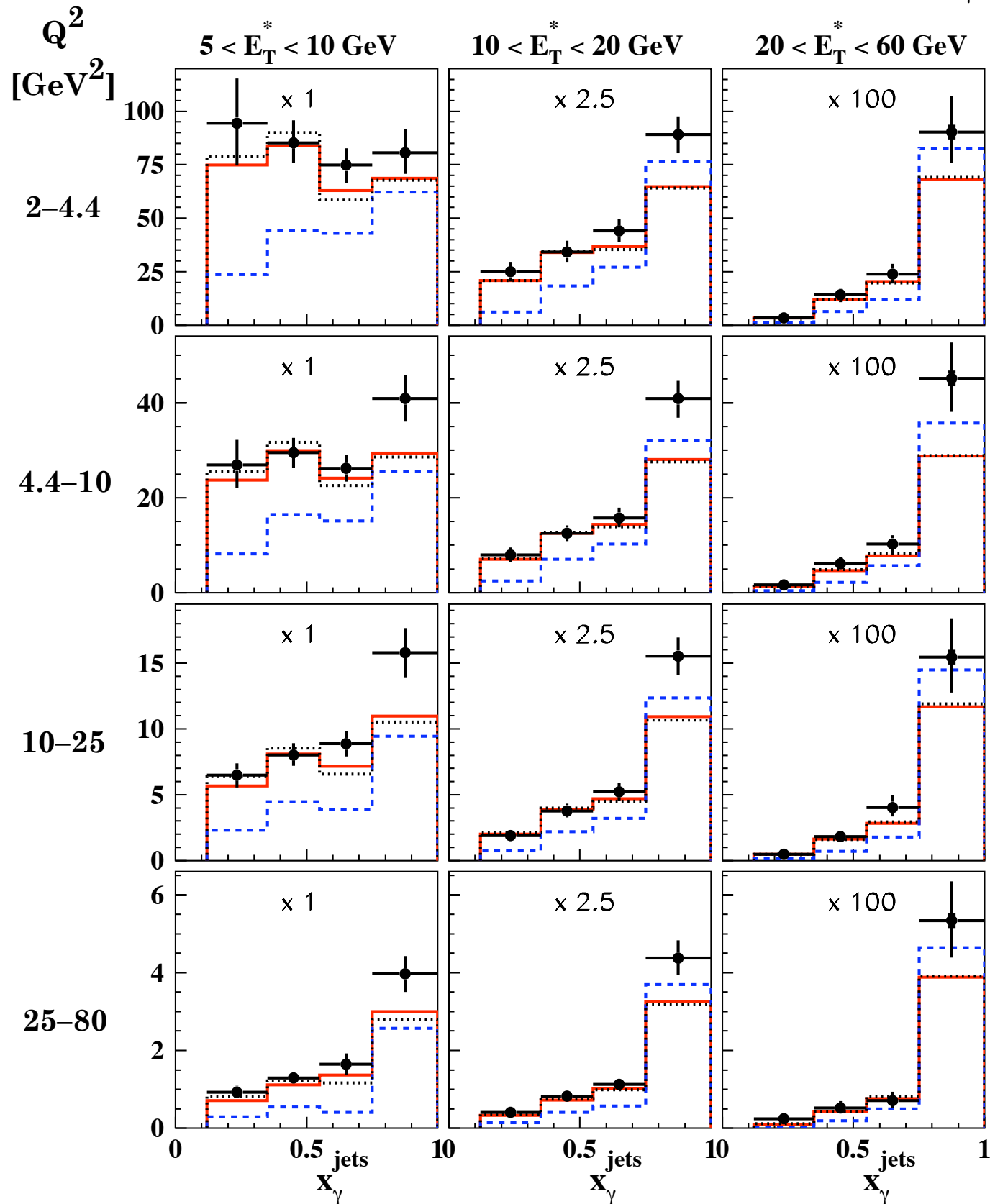
H1	(57 pb ⁻¹ , 1999-2000)
$\sqrt{s} = 318 \text{ GeV}$	
$2 < Q^2 < 80 \text{ GeV}^2$	
$0.1 < y < 0.85$	
$E_{T1}^* > 7 \text{ GeV}$	
$E_{T2}^* > 5 \text{ GeV}$	
$-2.5 < \eta_{1,2}^* < 0$	
longitudinally invariant k_t jet algorithm, $\gamma^* p$ CMS	
Eur. Phys. J. C37 (2004) 141-159	

- Estimate fraction of photon four momentum carried by parton in hard interaction:

$$x_\gamma^{\text{jets}} = \frac{\sum_{j=1,2} (E_j^* - p_{z,j}^*)}{\sum_{\text{hadrons}} (E^* - p_z^*)}$$
 - **direct** part ($x_\gamma^{\text{jets}} > 0.75$) well described
 - **resolved** fraction ($x_\gamma^{\text{jets}} < 0.75$) increases at smaller Q^2
 - data significantly above NLO calculations when using direct photon only
 - excess decreases with increasing Q^2
- JETVIP including γ_T^* improves description but excess for $x_\gamma^{\text{jets}} < 0.75$ remains

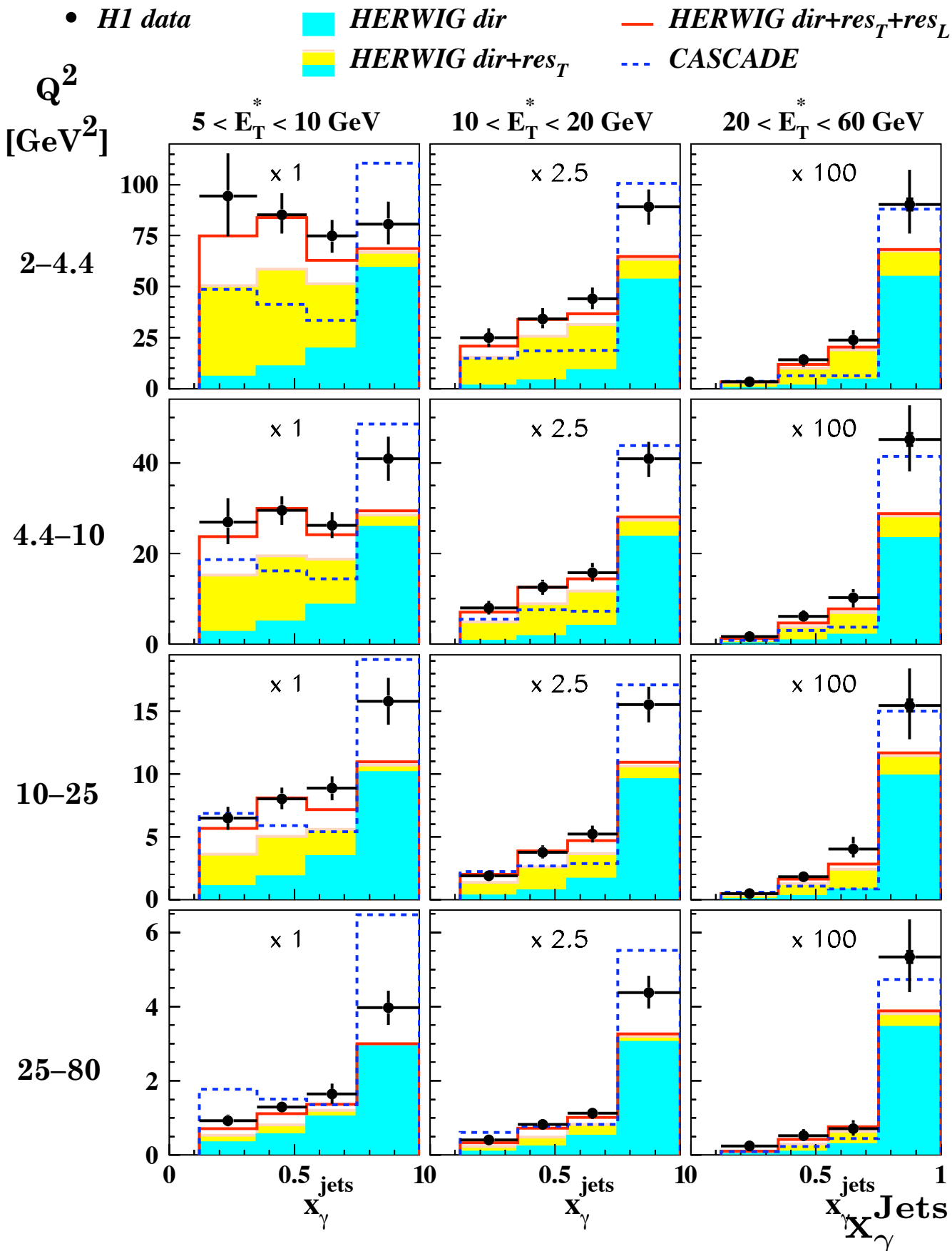
Comparison with LO Monte Carlo including Parton Showers

- *H1 data*
- *HER dir+res_T+res_L (full)*
- *HER dir+res_T+res_L (no hadronisation)*
- - - *HER dir+res_T+res_L (parton level, $D_{i\gamma}^{OED}$)*



- Inclusion of QCD parton showers in HERWIG LO Monte Carlo significantly improves description
 - Hadronisation corrections small
- Some deficit remains in region of high x_{γ}^{jets}
- Best agreement reached when transversely AND longitudinally polarised resolved virtual photons are included (see next slide)

Comparison with Alternative Parton Evolution Schemes



- HERWIG reasonably describes data if transversely and longitudinally polarised resolved photons are included
 - Contribution from resolved photon ladder can be viewed as deviation from k_T - ordering

- CASCADE based on CCFM
 - non- k_T -ordered parton emissions
 - although no explicit virtual photon structure is included can generate sizable contribution at $x_{\gamma}^{\text{jets}} < 0.75$
 - main trends of data described
 - large sensitivity to choice of unintegrated PDF [J2003 set 1 shown]

Summary

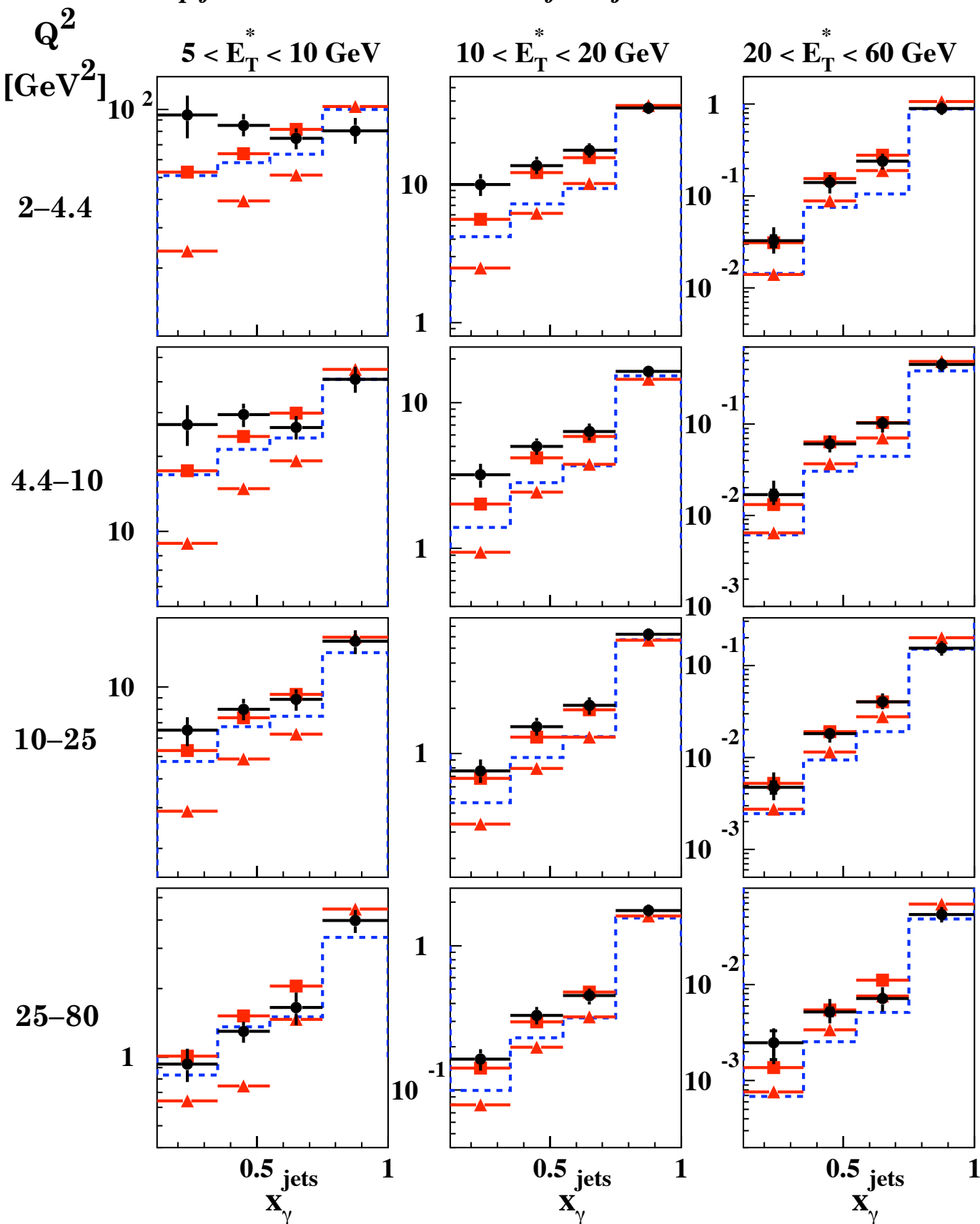
- Dijet production very sensitive tool to study properties of parton distributions and evolution at small x
- HERA data at medium Q^2 [$2 < Q^2 < 100 \text{ GeV}^2$] used to measure triple differential cross sections
 - Eur. Phys. J. C33 (2004) 477
 - Eur. Phys. J. C37 (2004) 14
- Established clear evidence for effects that go beyond the fixed-order NLO QCD calculations
 - NLO calculations do not provide satisfactory agreement at small Q^2 , E_T , x_γ
- LO Monte Carlo predictions give reasonable description if
 - supplemented with [parton showers](#)
 - transversely and [longitudinally](#) polarised resolved photon contribution are included
- CASCADE (based on CCFM) qualitatively describes main features of data

Backup Slides

Comparison with NLOJET++

- *H1 data*
- *NLOJET for 2 jets*
- *NLOJET for 3 jets*

hep-ph/0501065



- NLOJET++ results in 3-jet mode significantly closer to data than those of 2-jet mode
 - have to cut out region $x_\gamma \sim 1$
 - no resolved photon
- largest corrections at small x_γ and Q^2
- remaining gap between data and NLOJET++ 3-jet also most pronounced for small x_γ and low Q^2
 - there is need for further higher order QCD corrections

Triple differential cross section: $d^3\sigma_{2\text{jet}} / (dQ^2 dx_\gamma^{\text{jets}} dy)$

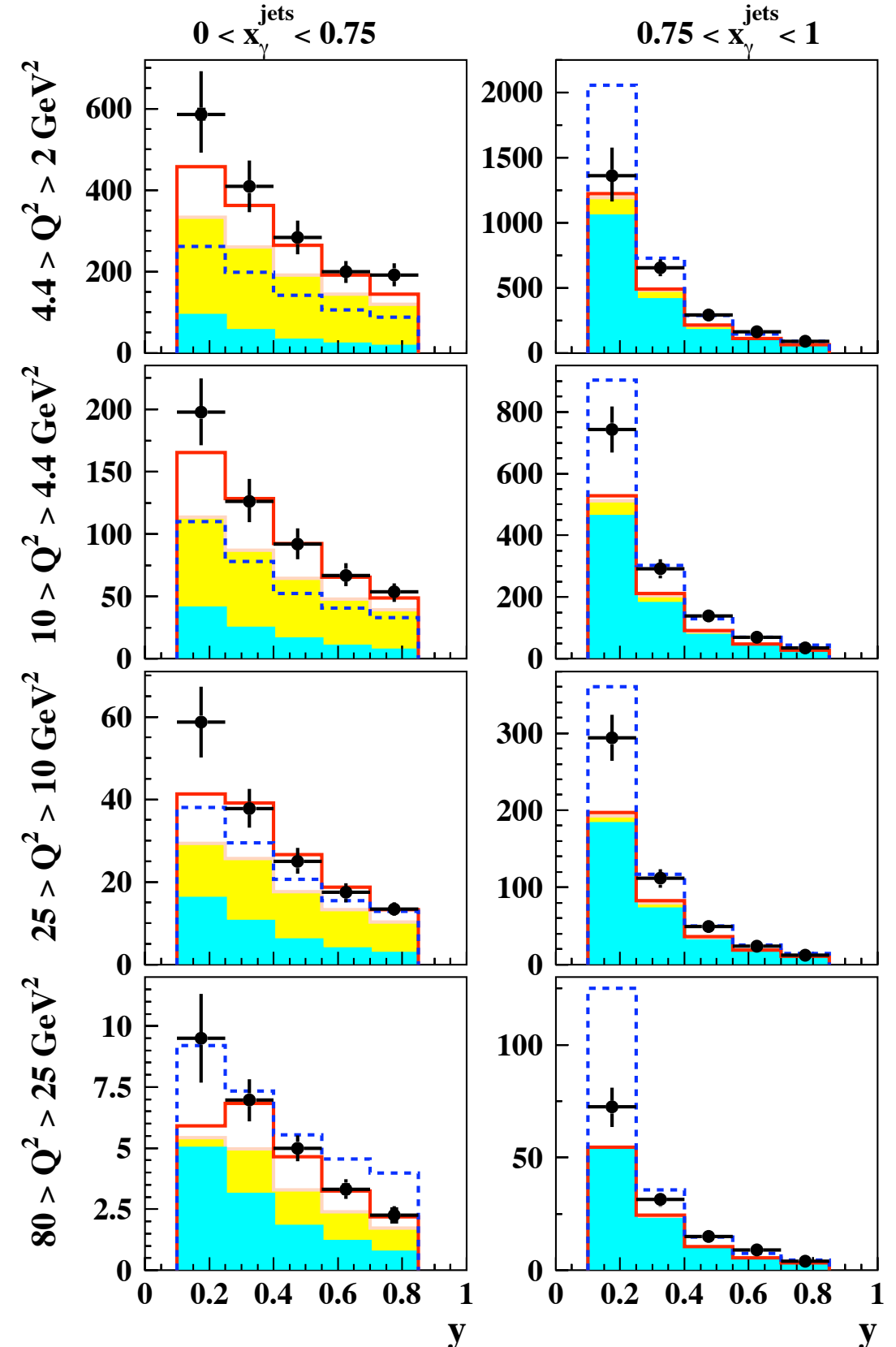
- photon flux is different for transverse and longitudinal photons:

$$f_T(y, Q^2) = \frac{\alpha}{2\pi} \left(\frac{2(1-y) + y^2}{y} \frac{1}{Q^2} - \frac{2m_e^2 y}{Q^4} \right)$$

$$f_L(y, Q^2) = \frac{\alpha}{2\pi} \left(\frac{2(1-y)}{y} \frac{1}{Q^2} \right)$$

- ratio of longitudinally to transversely polarised photons decreases with increasing y

- *H1 data* ■ *HERWIG dir* — *HERWIG dir+res_T+res_L*
■ *HERWIG dir+res_T* - - - *CASCADE*



Triple differential cross section: $d^3\sigma_{2\text{jet}}/(dQ^2 dy d\eta^*)$

- *H1 data*
- *HERWIG dir*
- *HERWIG dir+res_T*
- *HERWIG dir+res_T+res_L*
- *CASCADE*

- Excess observed at low Q^2 and high y
- Most pronounced at $\eta^* \sim 0$ in the forward region of lab frame

