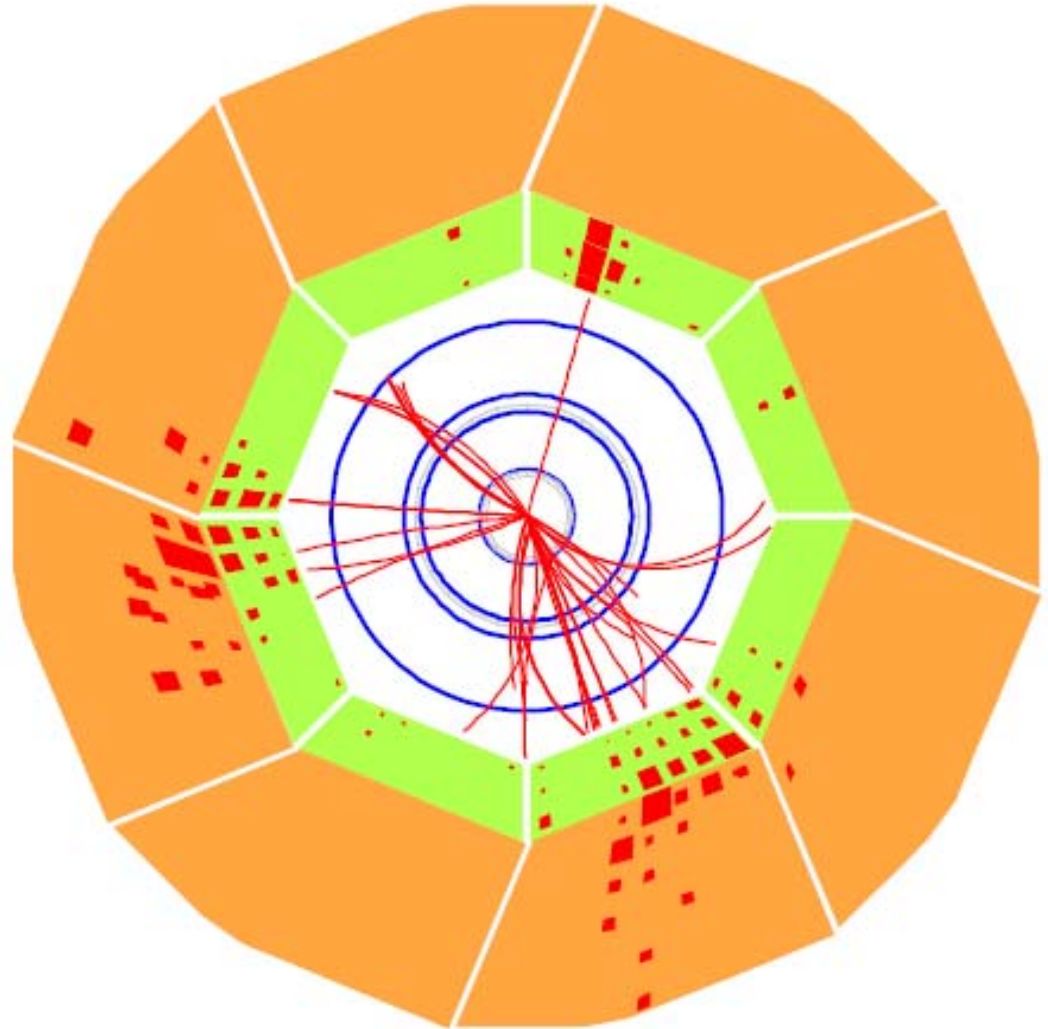


# Tests of the QCD Sector of the Standard Model

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- Structure functions and  $\alpha_s$  in DIS
- Spin physics
- Jets and  $\alpha_s$
- Event shapes
- Fragmentation
- Heavy flavours
- Summary



# Introduction

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- Progress on many fronts in QCD in last few years.
- Nobel prize in physics awarded to Gross, Politzer and Wilczek...



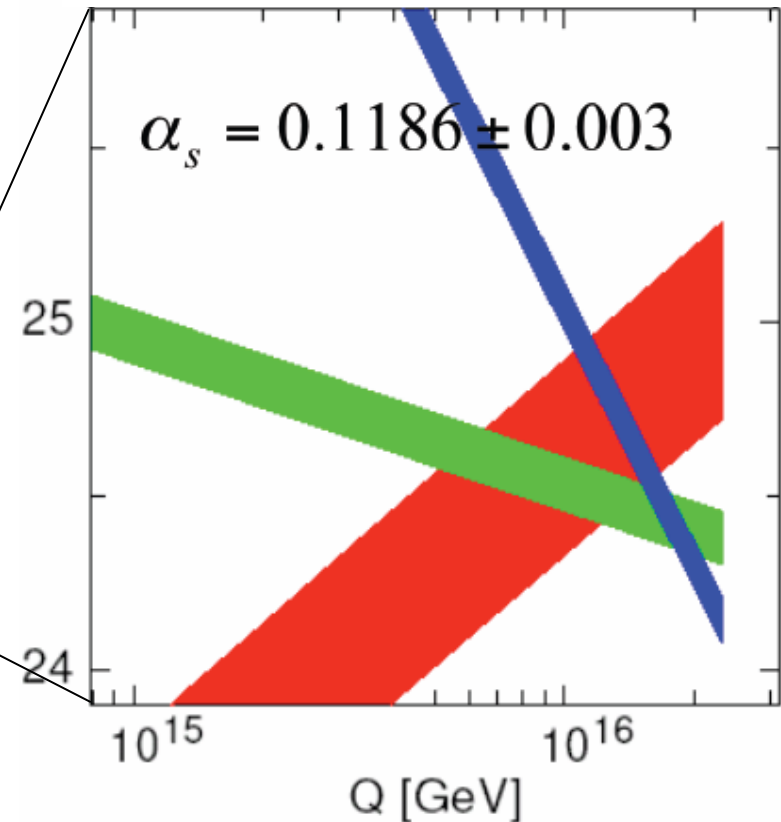
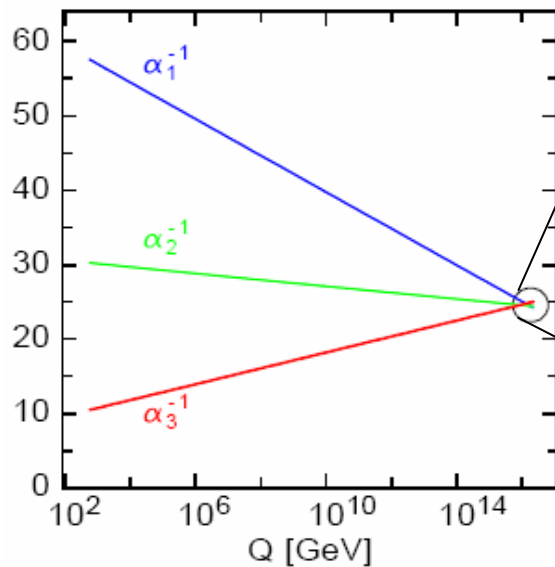
- “...for the discovery of asymptotic freedom in the theory of the strong interaction...”

- It is now official: QCD is the theory of the strong interactions!
- Why then “Tests of the QCD sector of the Standard Model”?
- Because we do not understand how partons are put together to make hadrons...
- ...or how those partons conspire to ensure the proton’s spin is  $\frac{1}{2}$ .
- Because we need to understand future high energy experiments at the LHC...

# Introduction

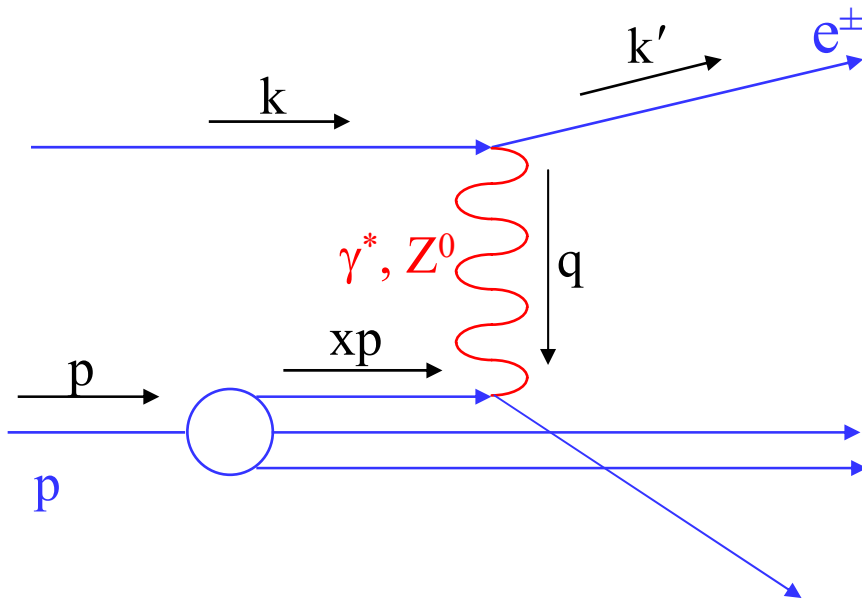
- ...and because  $\alpha_s$  is the least well known of the fundamental constants of nature.
- Increased precision needed to determine if running electromagnetic, weak and strong couplings...

- ...unify at  $\sim 10^{16}$  GeV.



# Structure functions and $\alpha_s$

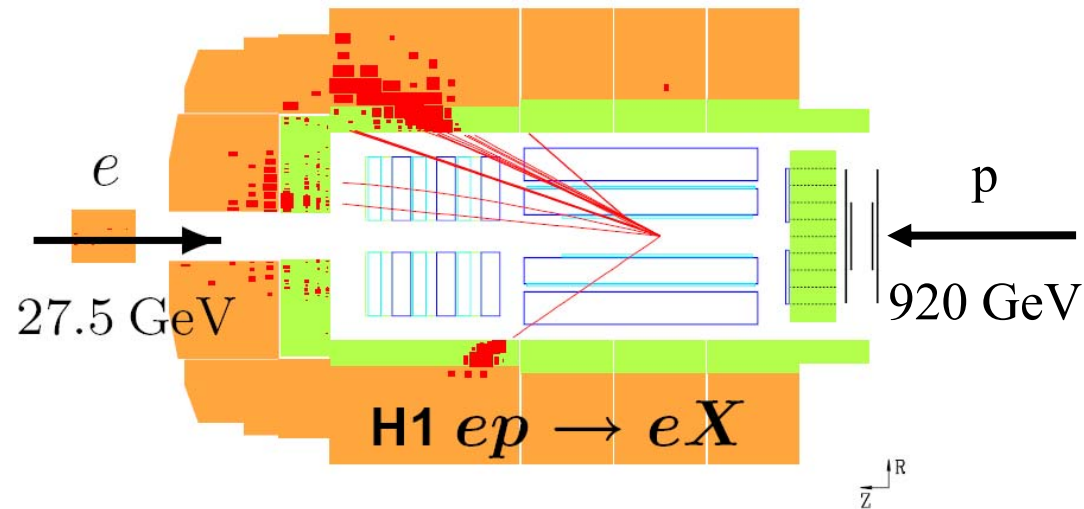
- Measure structure of hadrons in deep-inelastic lepton-nucleon scattering.
- Neutral current DIS:



- Describe in terms of:

$$Q^2 = -q^2, \quad x = \frac{Q^2}{2p \cdot q} \quad \text{and} \quad y = \frac{p \cdot q}{p \cdot k}$$

- HERA is most important source of data on proton structure.



- $0 < Q^2 < 10^5 \text{ GeV}^2$  i.e. sensitive to structure down to  $\sim 10^{-18} \text{ m}$ .
- $10^{-6} < x < 1$ .

# Timescales in DIS

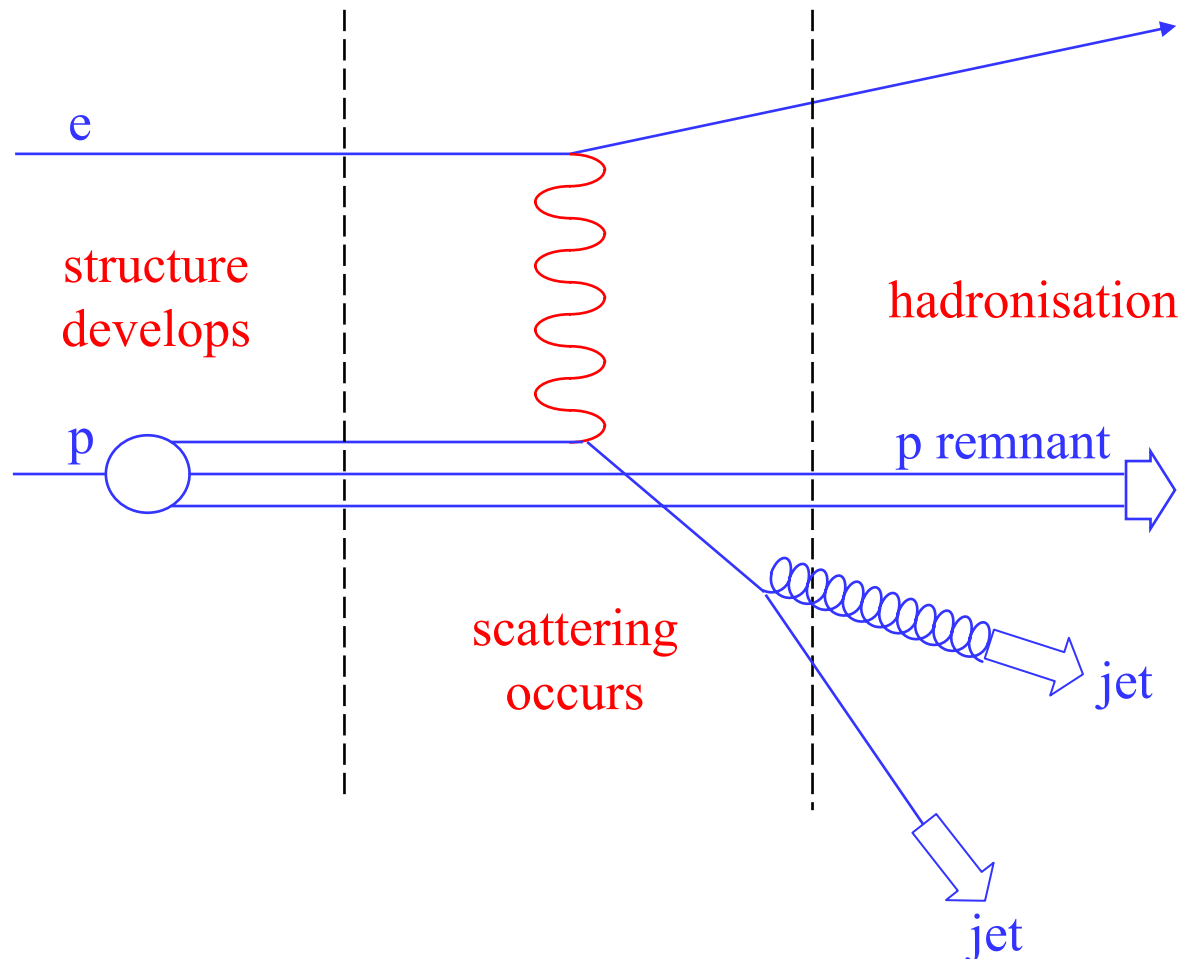
- Time scale for soft interactions

$$\Delta T_{\text{SOFT}} \approx \frac{E}{m} \frac{1}{\Lambda_{\text{QCD}}}$$

- For DIS

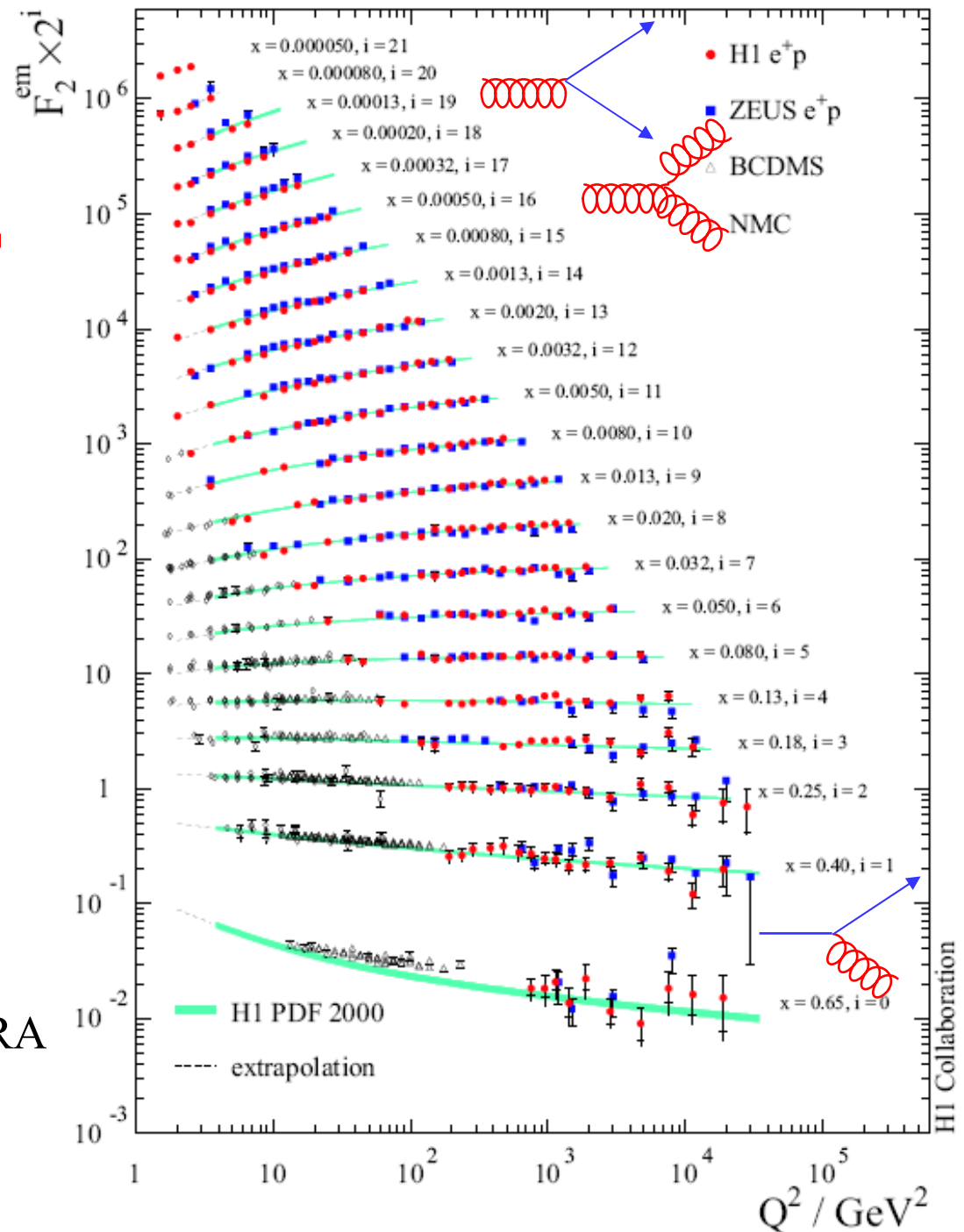
$$\Delta T_{\text{DIS}} \approx \frac{1}{\sqrt{Q^2}}$$

- $\Delta T_{\text{SOFT}} \gg \Delta T_{\text{DIS}}$  so DIS takes snapshot of proton structure.



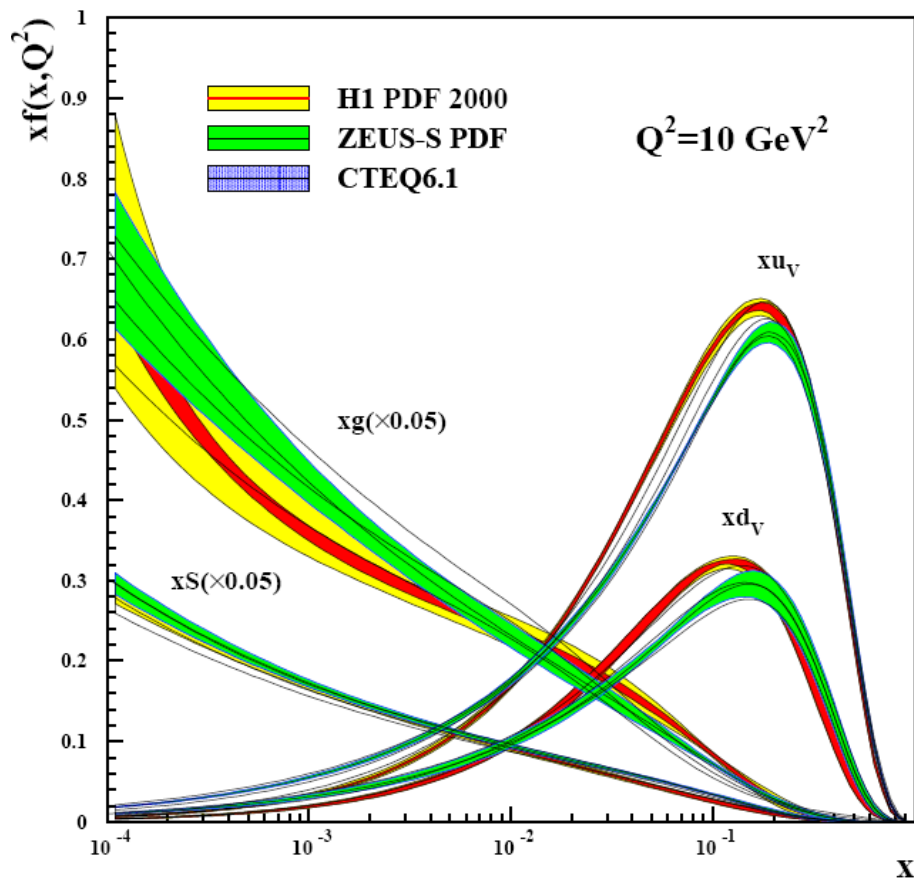
# Neutral current cross section for DIS

- $\frac{d^2\sigma_{NC}(e^\pm)}{dx dQ^2} \sim Y_+ F_2 \mp Y_- xF_3 + y^2 F_L$ .
- $Y_\pm = 1 \pm (1-y)^2$ .
- $F_2 \sim \sum_q x(q(x, Q^2) + \bar{q}(x, Q^2))$ ,  
 $xF_3 \sim \sum_q x(q(x, Q^2) - \bar{q}(x, Q^2))$ ,  
 $F_L \sim \alpha_s(Q^2) x g(x, Q^2)$ .
- $F_2$  dominant for  $Q^2 < m_Z^2$ .
- $xF_3$  measurements require large luminosities.
- Precise  $F_L$  measurement needs HERA running with lower proton beam energies.



# Parton distribution functions

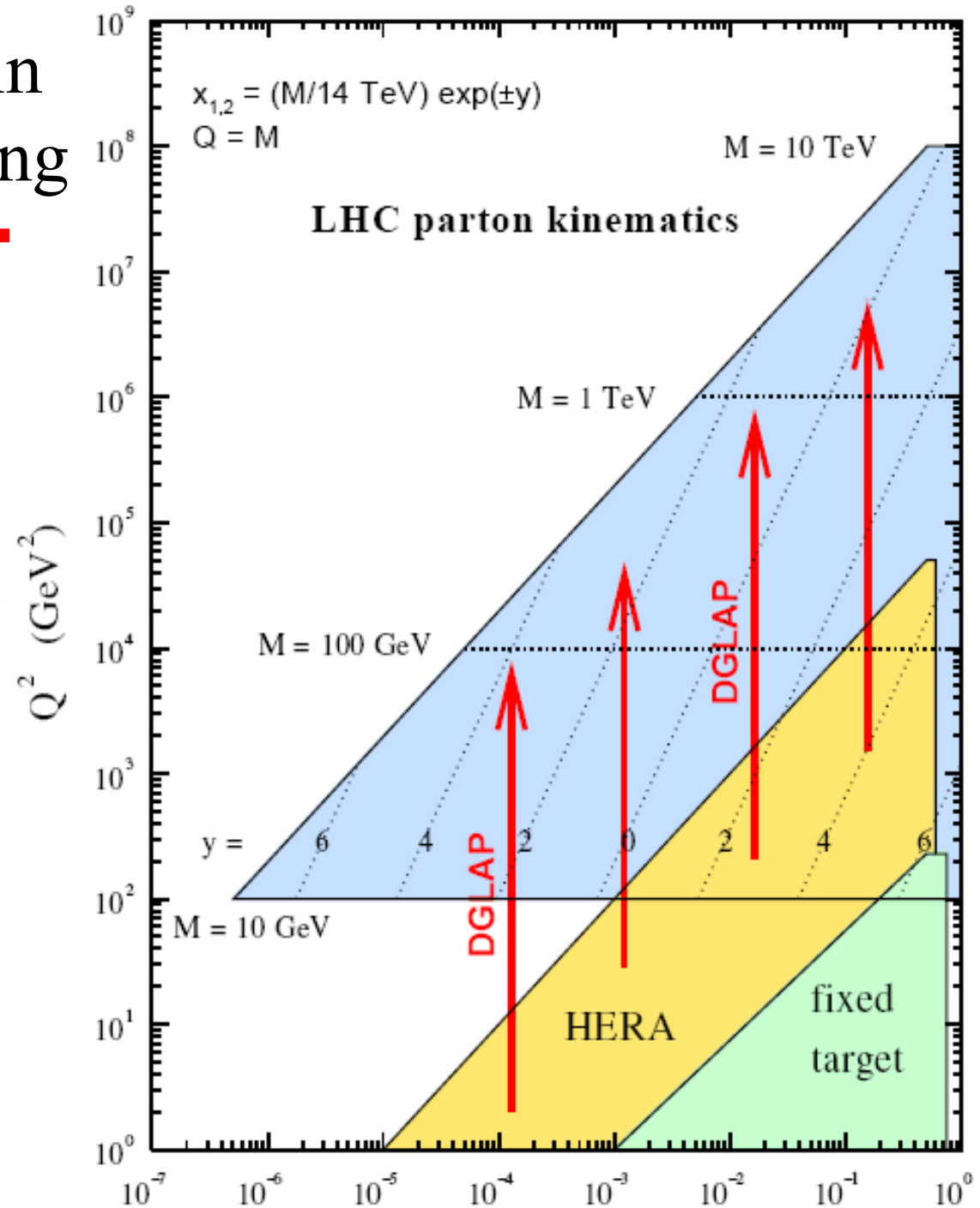
- NLO QCD fits to  $F_2$ ,  $xF_3$ , and CC data allow extraction of the PDFs.



- ...and of  $\alpha_s$ .
- E.g. for ZEUS fit:  
$$\alpha_s(m_Z) = 0.1166 \pm 0.0008(\text{unc}) \pm 0.0032(\text{corr})$$
$$\pm 0.0036(\text{norm}) \pm 0.0018(\text{mod})$$
- Gluon distribution determined from evolution with  $Q^2$ : uncertainties large and gluon distribution correlated with  $\alpha_s(Q^2)$ .

# Recent improvements in theoretical understanding

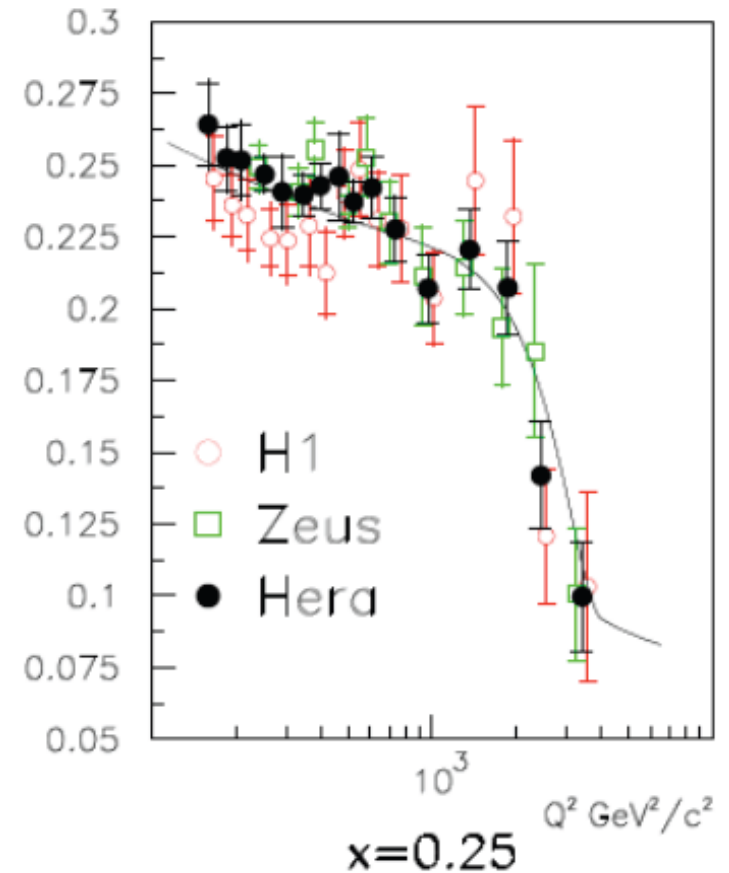
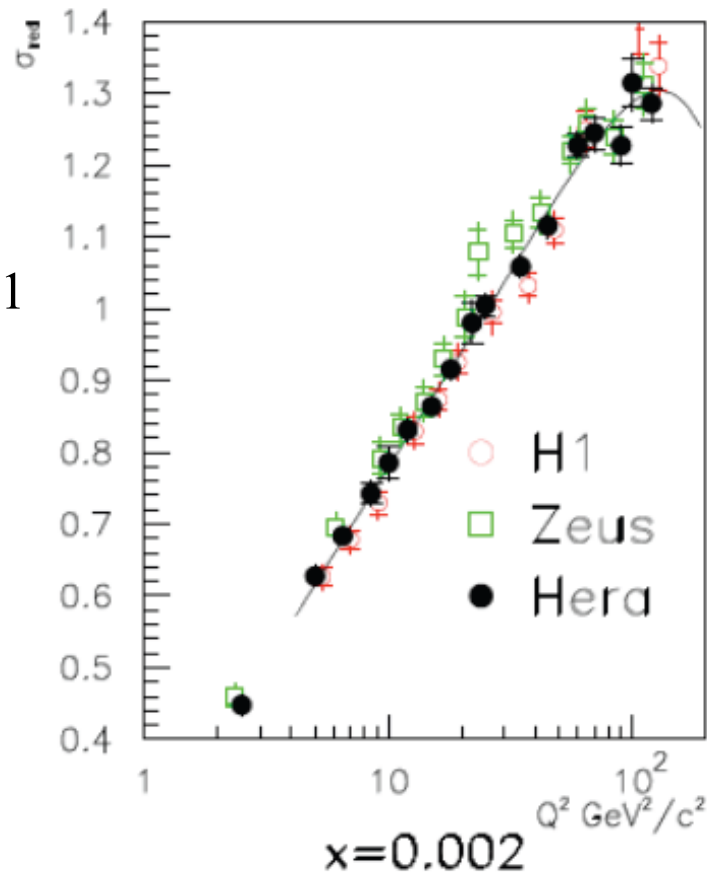
- NNLO DGLAP splitting functions and DIS coefficient functions recently calculated (Moch, Vermaseren, Vogt).
- Will lead to improved precision of PDFs and  $\alpha_s$  – progress shown by Guffanti (Blümlein, Böttcher) and by Alekhin on incorporating DIS and E605 DY data.
- Splitting functions also crucial to extrapolation of PDFs from HERA to TeVatron and the LHC.
- DGLAP appropriate at low  $x$ ?
- NLO MC developments also underway.





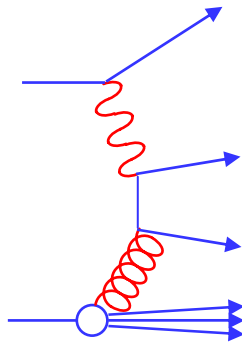
# Experimental progress

- Data taking at high luminosity ongoing (HERA II)
- Techniques for combination of H1 and ZEUS data being studied (HERA-LHC workshop), cross calibration will lead to reduced systematic errors.

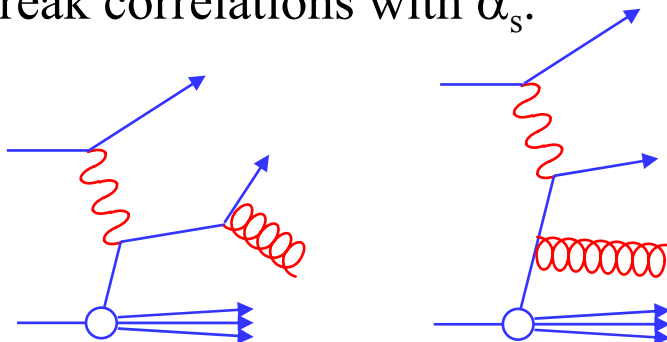


# Add jet data to PDF determinations

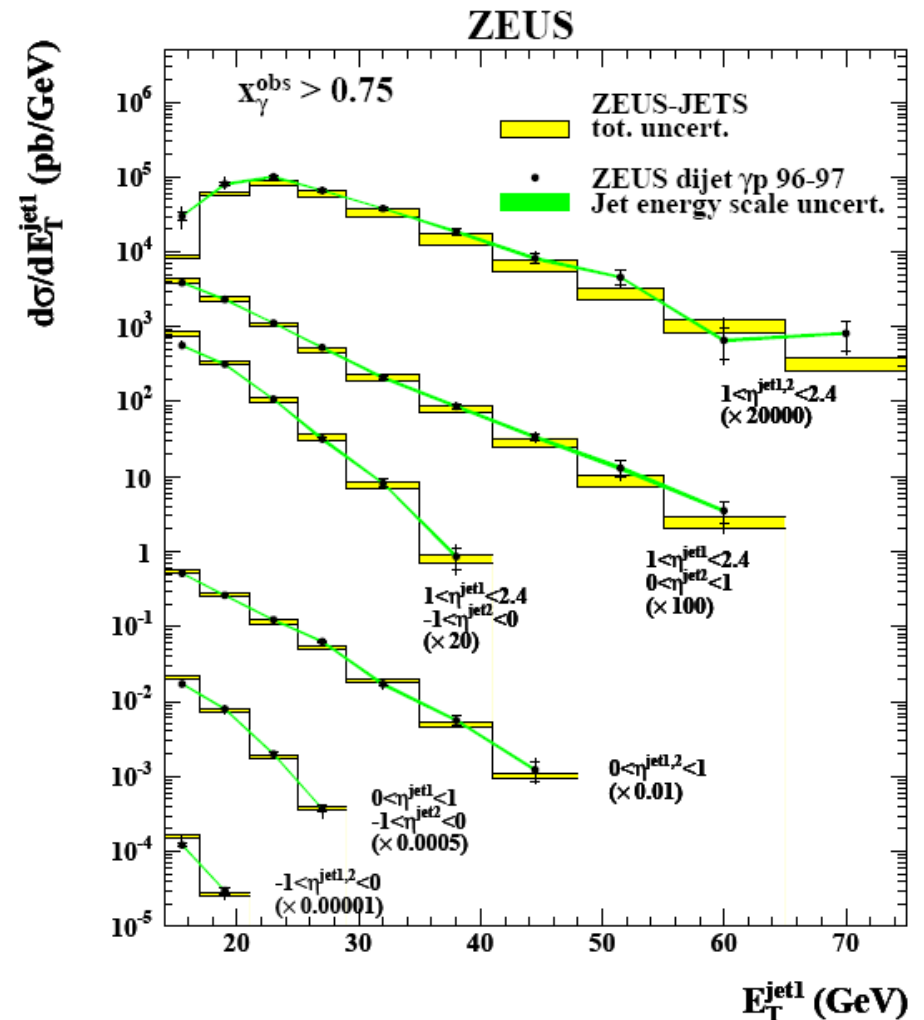
- ZEUS exploit additional constraints provided by DIS and  $\gamma p$  jet data.
- Boson gluon fusion sensitive to gluon distribution.



- Contributions from other diagrams break correlations with  $\alpha_s$ .



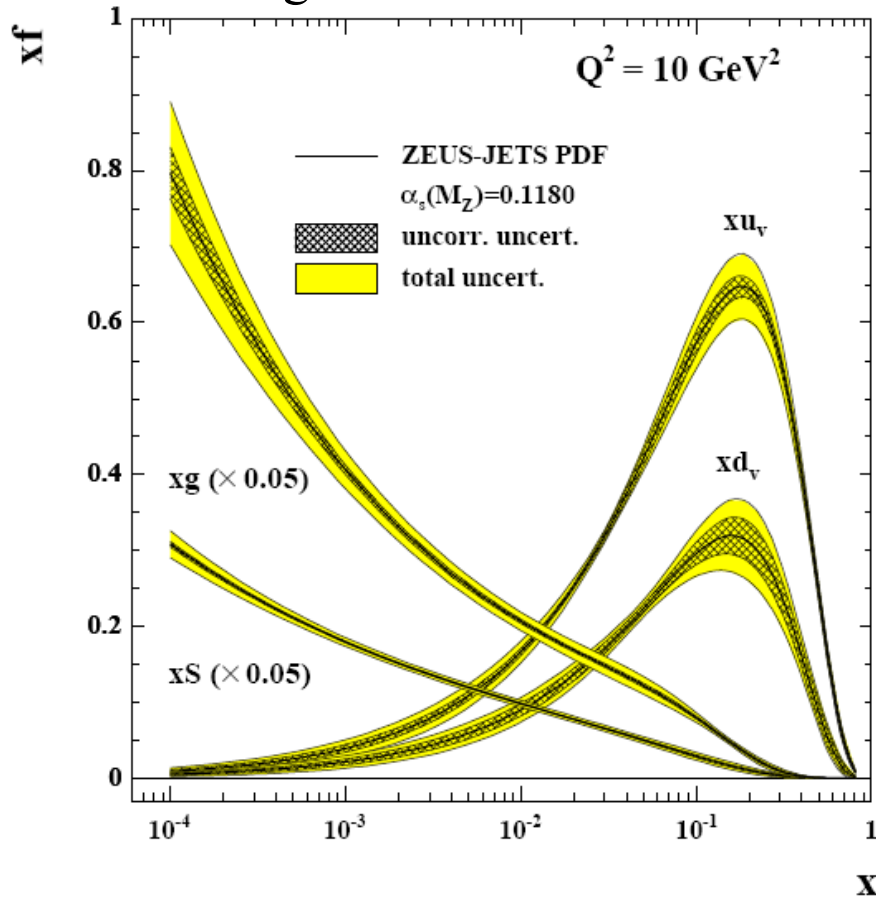
- Dijet cross section, photoproduction:



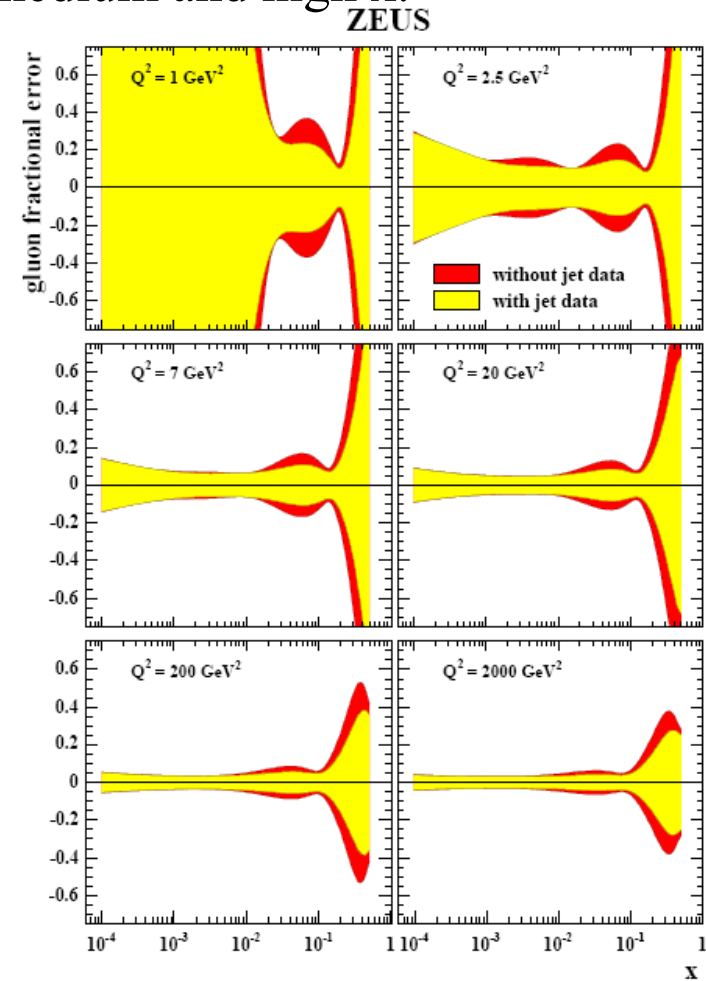
# Using jet data in PDF determinations

- $\alpha_s(m_Z) = 0.1183 \pm 0.0028$  (exp.)  
 $\pm 0.0008$  (mod.)  $\pm 0.005$  (scale).

- Resulting PDFs:

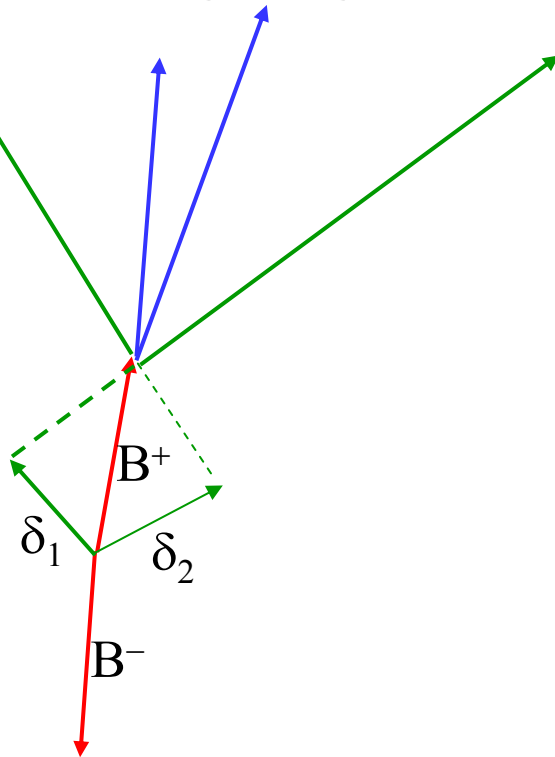


- Improved precision for gluon at medium and high  $x$ .

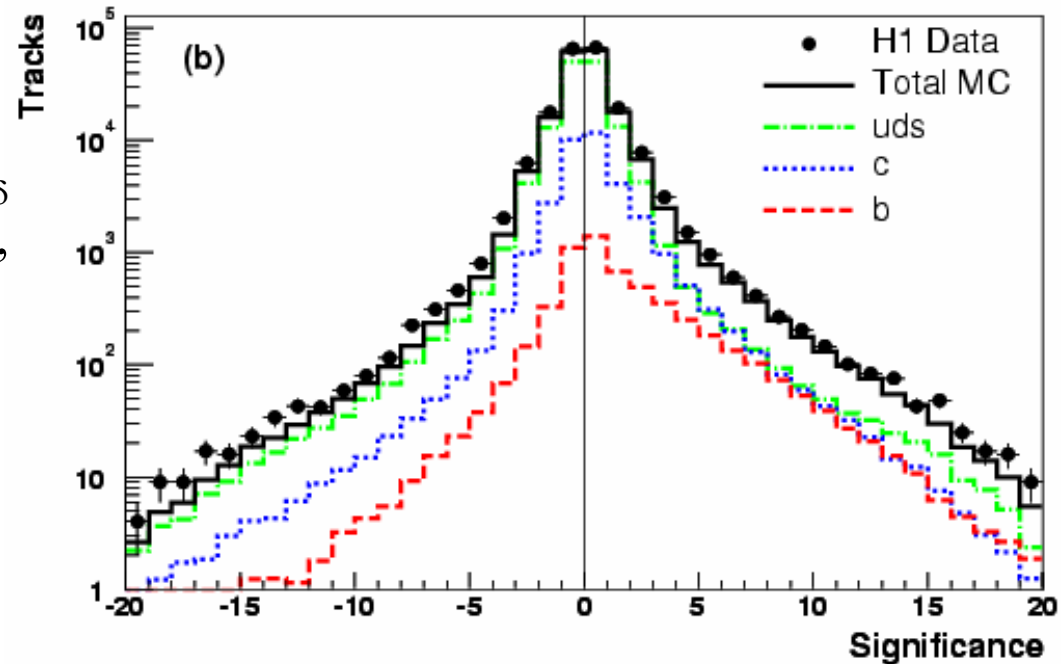


# Charm and beauty in the proton

- Charm and beauty identified using H1 central silicon tracker to measure impact parameter  $\delta$  and its error  $\sigma_\delta$ .
- Flavour discrimination using  $S = \delta/\sigma_\delta$  of tracks with largest significance,  $S_1$ ,  $S_2 \dots$

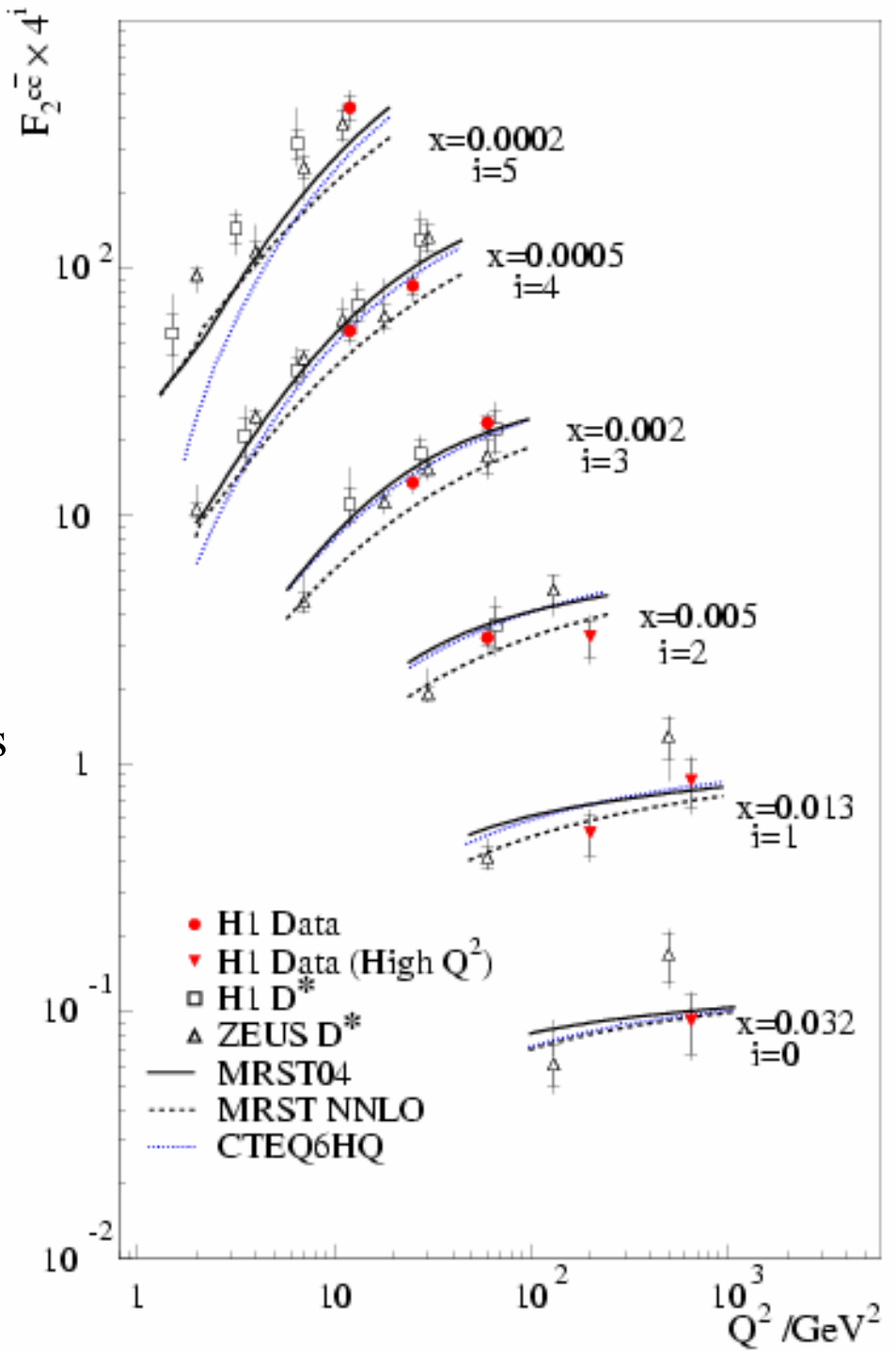


- Significance  $S_1$ .



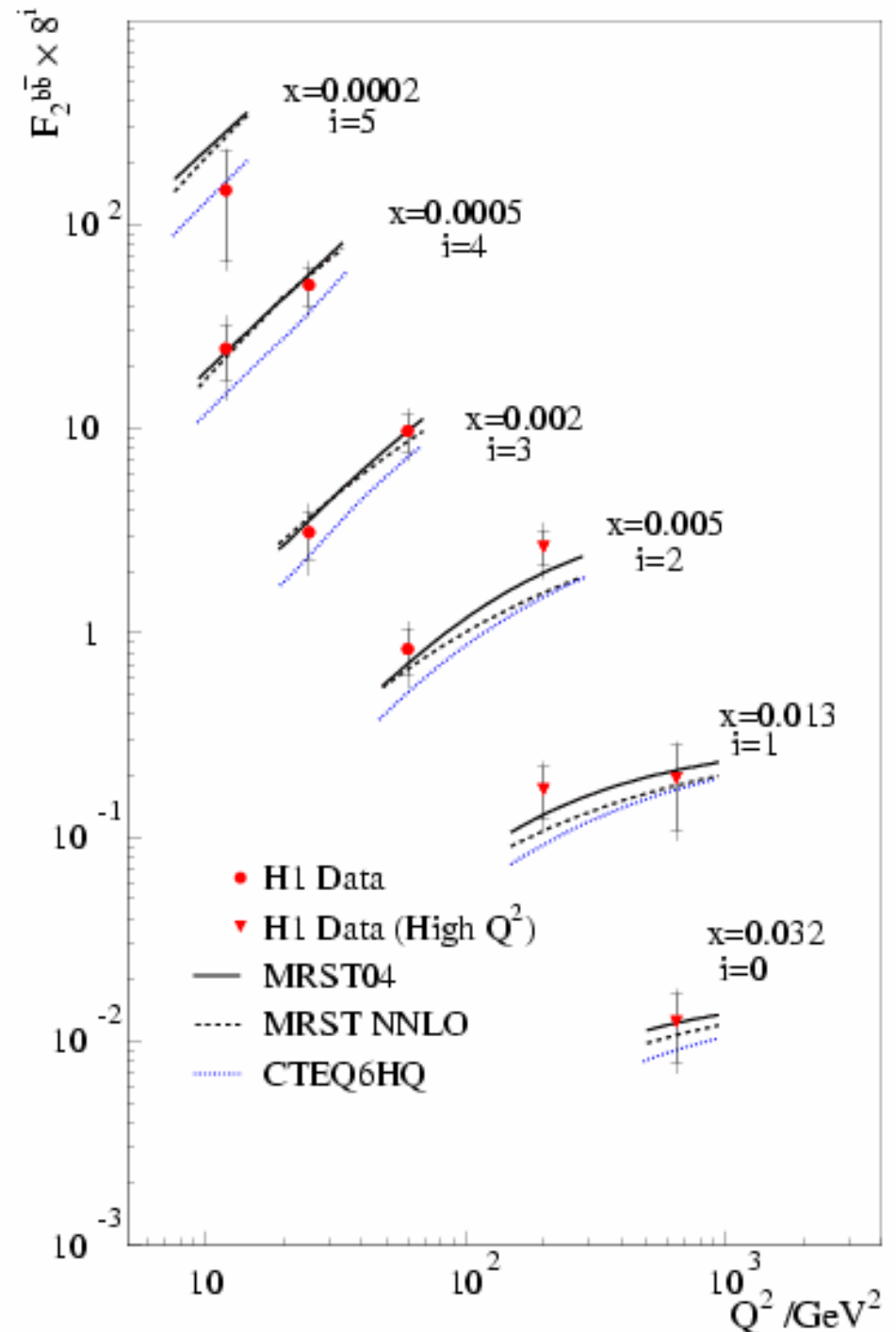
# Charm in proton

- Proportion of c events determined as function of  $x$  and  $Q^2$ ,  $\sim 24\%$  decreasing slightly with  $x$ .
- Hence extract  $F_2^{c\bar{c}}$ .
- Good agreement between “lifetime” and “D\* based” measurements.
- Positive scaling violations increase as  $x$  decreases.
- Well described by higher order QCD calculations.



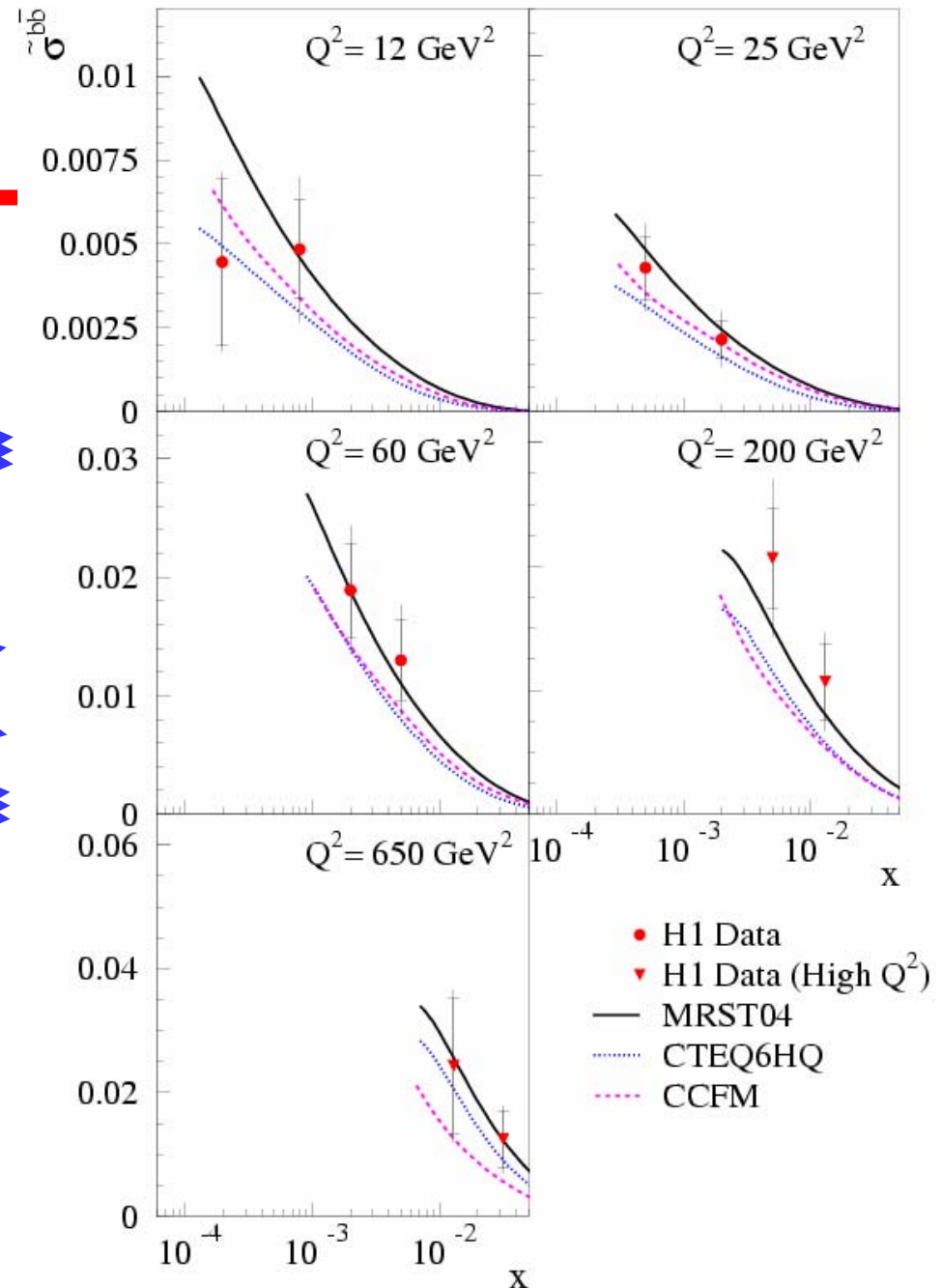
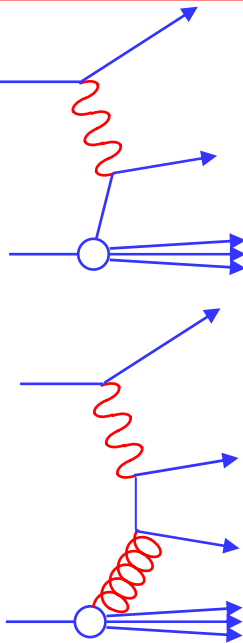
# Beauty in proton

- Proportion of b events found to be 0.3 to 3%, inc. with  $Q^2$ .
- Hence obtain first ever measurements of  $F_2^{b\bar{b}}$ .
- Well described by higher order QCD calculations.
- Of interest to LHC, e.g.  $b\bar{b} \rightarrow H$ .
- $b\bar{b}$  contributes  $\sim 5\%$  to  $pp \rightarrow ZX$ .
- Need better than 20% accuracy on b distribution for 1% Z cross sections at the LHC.



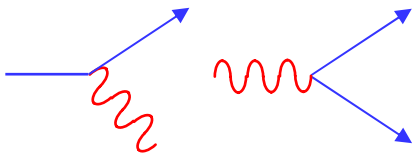
# Two scale problems in QCD and b production

- For  $Q^2 \gg m_Q^2$ , treat Q like uds, i.e. part of structure of proton.
- If  $Q^2 \sim m_Q^2$ , to LO Q produced via boson gluon fusion.
- Careful matching needed to cover entire  $Q^2$  range, “variable flavour number scheme” (ACOT, MRST).
- MRST04 and CTEQ6HQ VFNS, CCFM “massive” calculation.
- More HERA data needed here!



# Contribution of photon to proton structure

- Include photons in evolution.



- u quarks radiate more than d, so fewer u quarks in proton at high x than d quarks in neutron.
- Isospin asymmetry:  $d^p \neq u^n$ ,  $u^p \neq d^n$ .
- Effect is small, but influences NuTeV

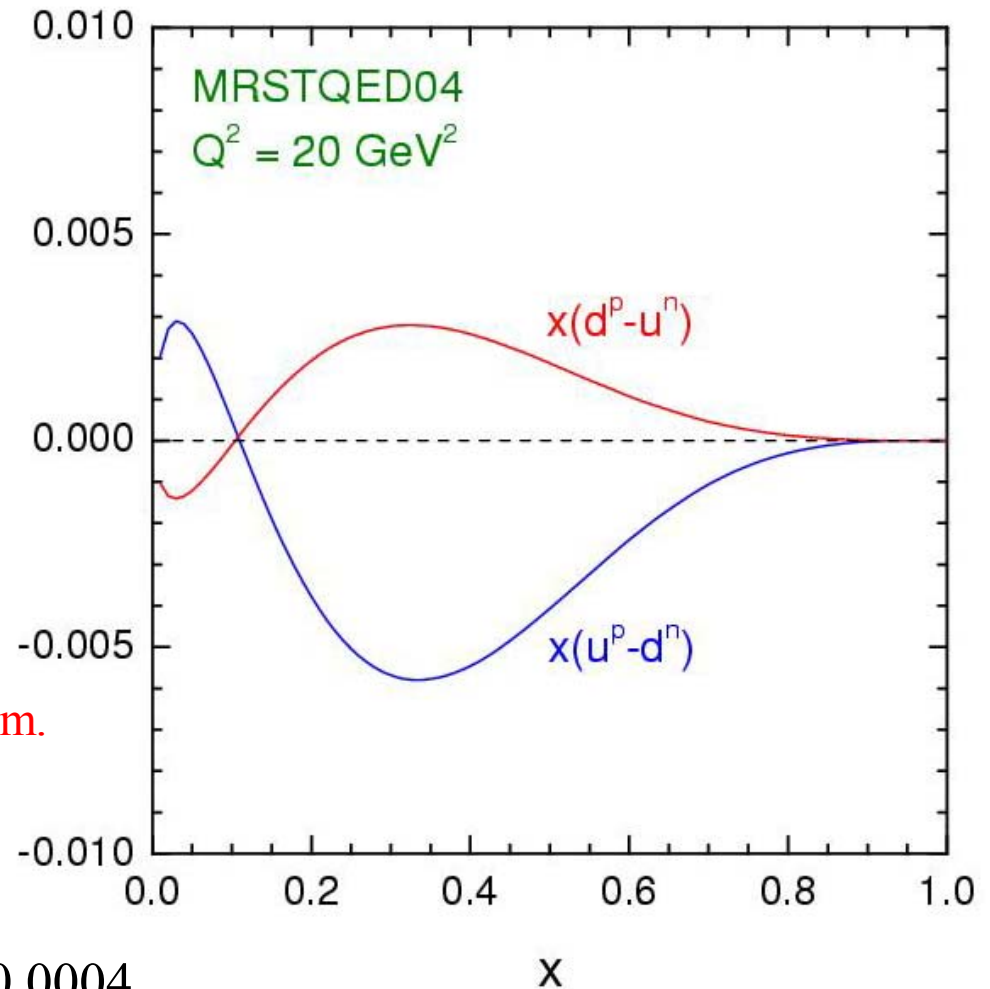
determination of  $\sin^2\theta_W$ :

$$\frac{\sigma_{NC}^{\nu} - \sigma_{NC}^{\bar{\nu}}}{\sigma_{CC}^{\nu} - \sigma_{CC}^{\bar{\nu}}} = \frac{1}{2} - \sin^2\theta_W + \text{isospin viol. term.}$$

- $\sin^2\theta_W = 0.2277 \pm 0.0013 \pm 0.0009$

$\sim -0.002$

- C.f. world average  $\sin^2\theta_W = 0.2227 \pm 0.0004$ .

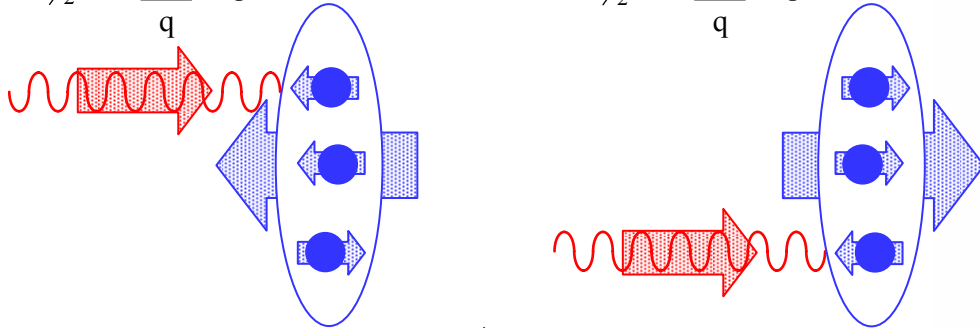




# Spin structure measurements

- $\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + L_z$
- Meas. with pol. target and pol. beam.

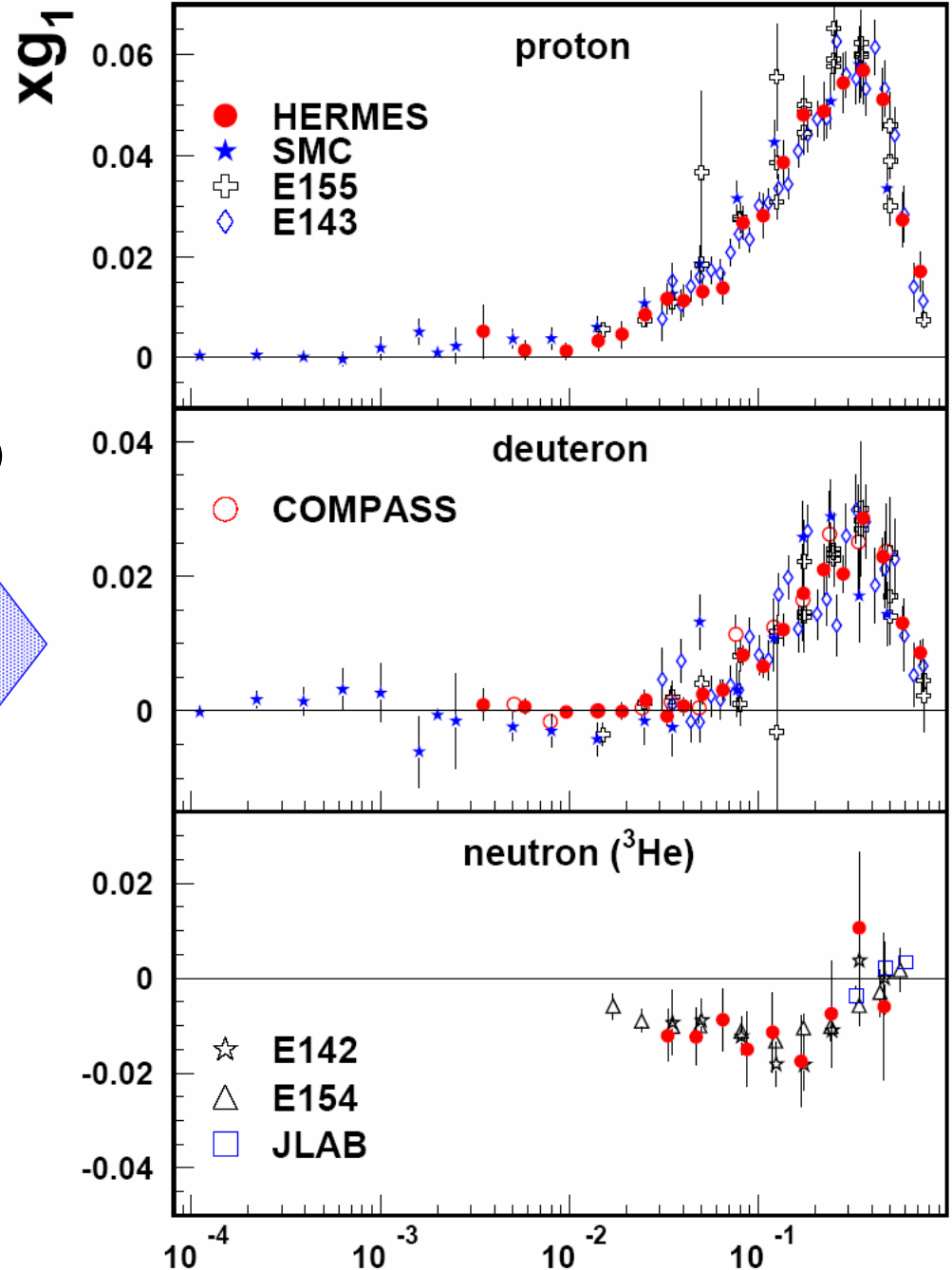
$$\sigma_{\frac{1}{2}} \sim \sum_q e_q^2 q^+(x) \quad \sigma_{\frac{3}{2}} \sim \sum_q e_q^2 q^-(x)$$



- $A = \frac{(\sigma_{\frac{1}{2}} - \sigma_{\frac{3}{2}})}{(\sigma_{\frac{1}{2}} + \sigma_{\frac{3}{2}})}$
- $\sim \frac{\sum e_q^2 (q_+ - q_-)}{\sum e_q^2 (q_+ + q_-)} \sim \frac{g_1(x)}{F_1(x)}$

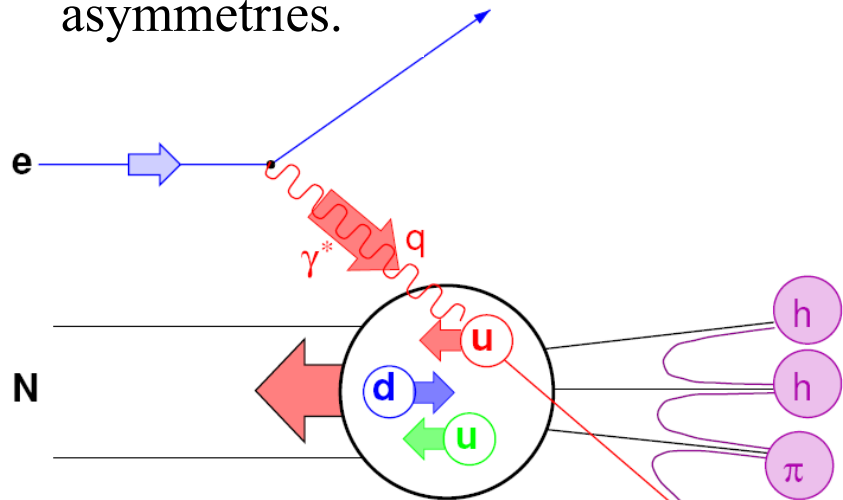
- New data from COMPASS.

- $\Delta\Sigma = 0.202^{+0.042}_{-0.077} \rightarrow 0.237^{+0.024}_{-0.029}$

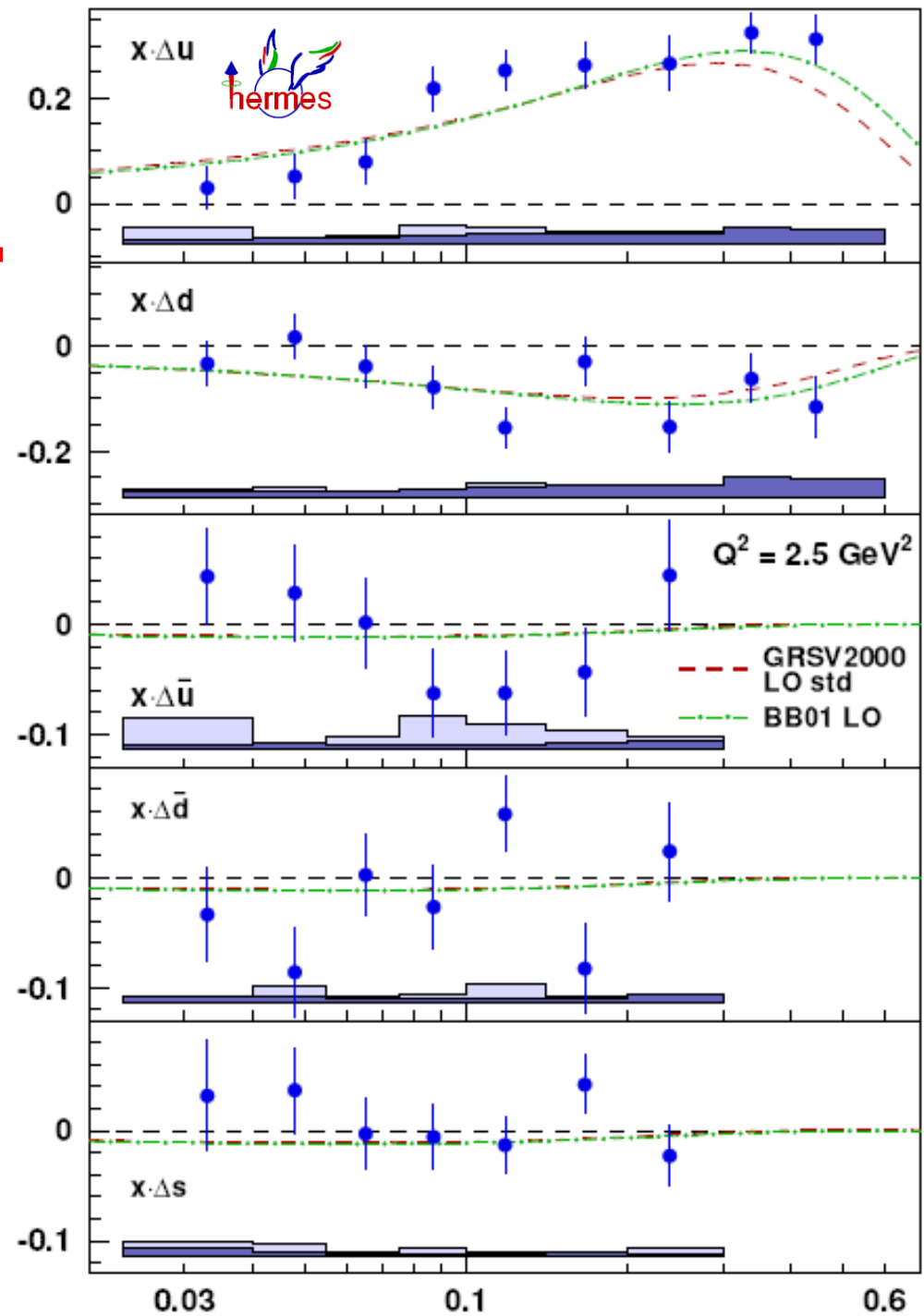


# Spin structure measurements

- Extract contributions of different flavours by measuring semi-inclusive asymmetries.

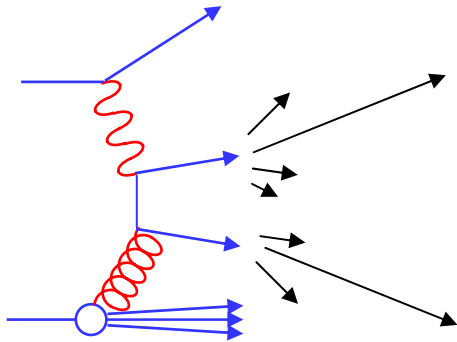


- $\Delta q = q_+ - q_-$
- $\Delta u > 0$  (u spin parallel to p spin)
- $\Delta d < 0$  (d spin anti-parallel to p spin)
- $\Delta \bar{u}$ ,  $\Delta \bar{d}$  and  $\Delta \bar{s}$  all  $\sim 0$ .

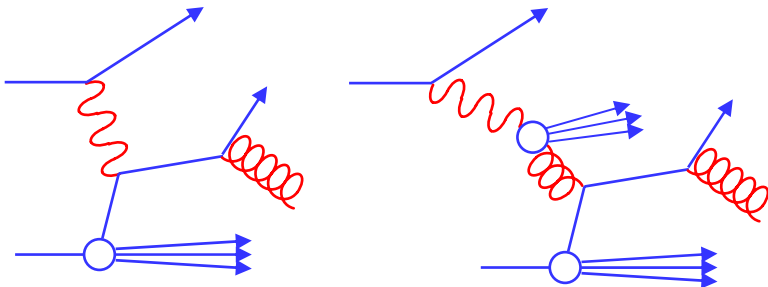


# Spin structure measurements

- Probe gluon spin using photon gluon fusion

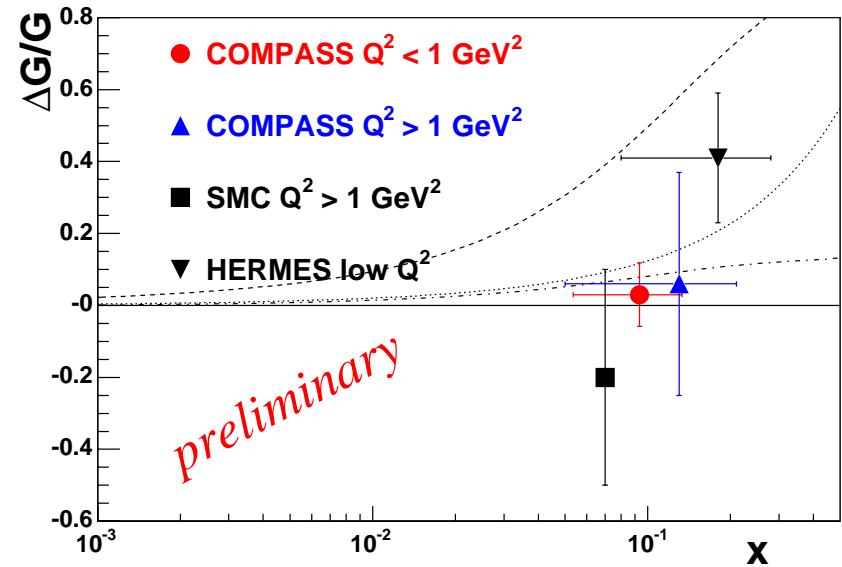


- Demand two high  $p_T$  hadrons in final state.
- Background from QDC and resolved photon events (at low  $Q^2$ ).



- $A - A_{BG} \sim \Delta G/G$

- Resulting measurements

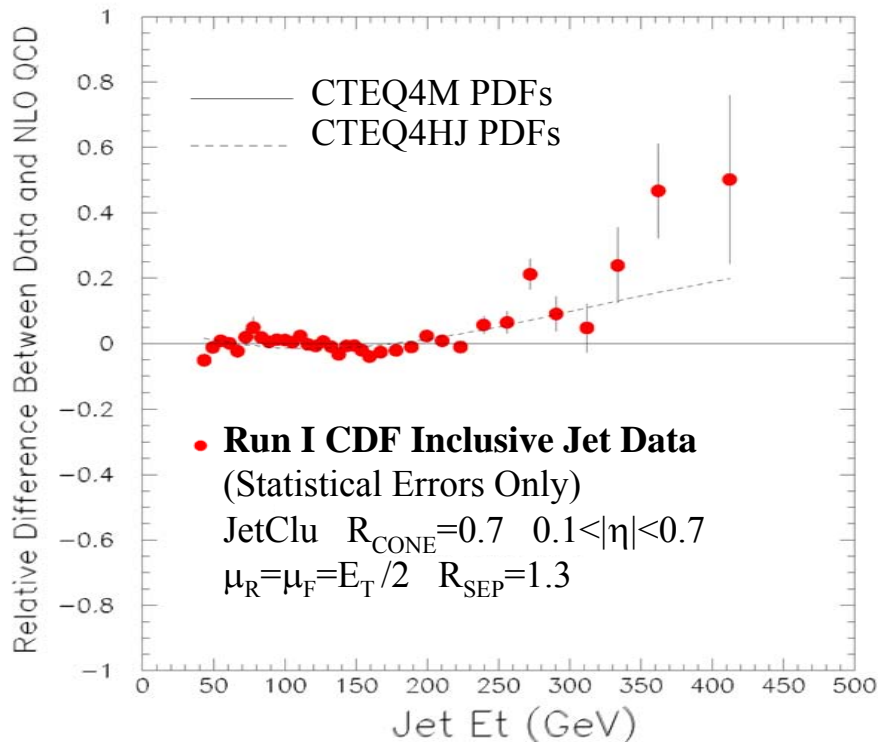


- $\frac{\Delta G}{G} = 0.024 \pm 0.089 \pm 0.057$

- $\Delta G = \int \Delta G(x) dx = 0.2, 0.6, 2.5$   
using GRSV min. standard and max. curves.

# Jets at the TeVatron

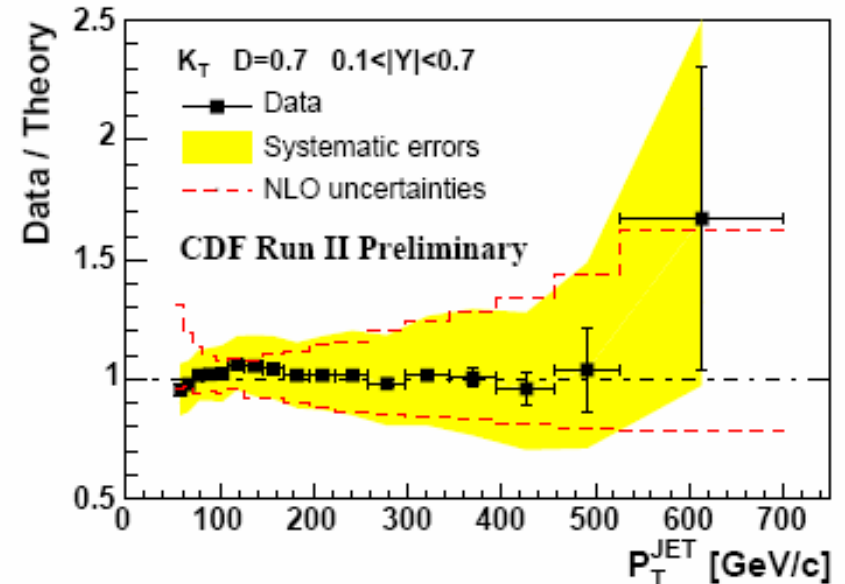
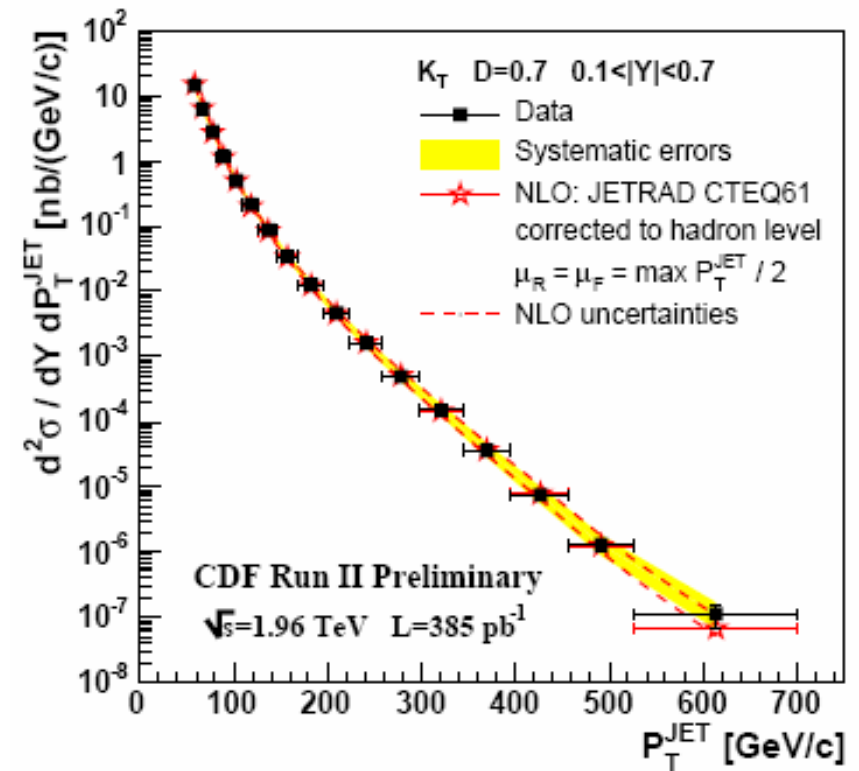
- TeVatron jets test of pQCD over  $\sim 8$  orders of magnitude in  $E_T$ .
- Probe distances down to  $\sim 10^{-19}$  m.
- Excitement when excess observed in Run I jet data.



- Can be explained by increasing gluon distribution at large  $x$ .
- Various problems addressed in Run II jet analyses:
  - ◆ JetClu algorithm not IR or collinear safe.
  - ◆ “Fudge factor”  $R_{\text{sep}}$  introduced to mimic effects of jet algorithm in calculations.
- Move to using “safe” inclusive  $k_T$  and midpoint algorithms.

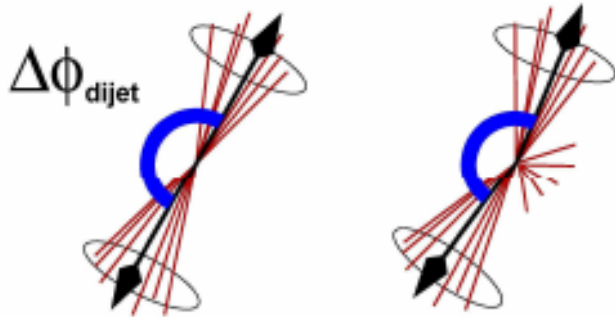
# Jets at the Tevatron

- At Run II, reach in  $p_T$  extended by  $\sim 150$  GeV compared to Run I.
- Experimental uncertainty dominated by energy scale (luminosity uncertainty of 6% not shown on plots).
- NLO QCD corrected to hadron level using Pythia tune A ( $\sim 20\%$  decreasing to  $\sim 0\%$  with  $p_T$ ).
- Theoretical error dominated by uncertainty in gluon at large  $x$ .
- Caution: Moretti, Nolton and Ross recently determined weak corrections to the theory:  $\sim -30\%$  at the highest jet  $E_T$  and  $\sim -12\%$  at  $p_T = 450$  GeV, consequences not yet fully explored.

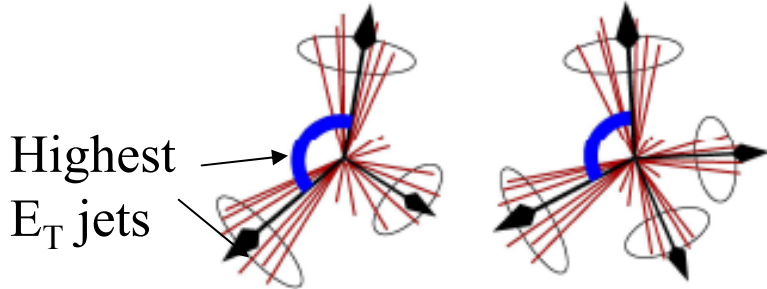


# Dijet azimuthal separation at the TeVatron

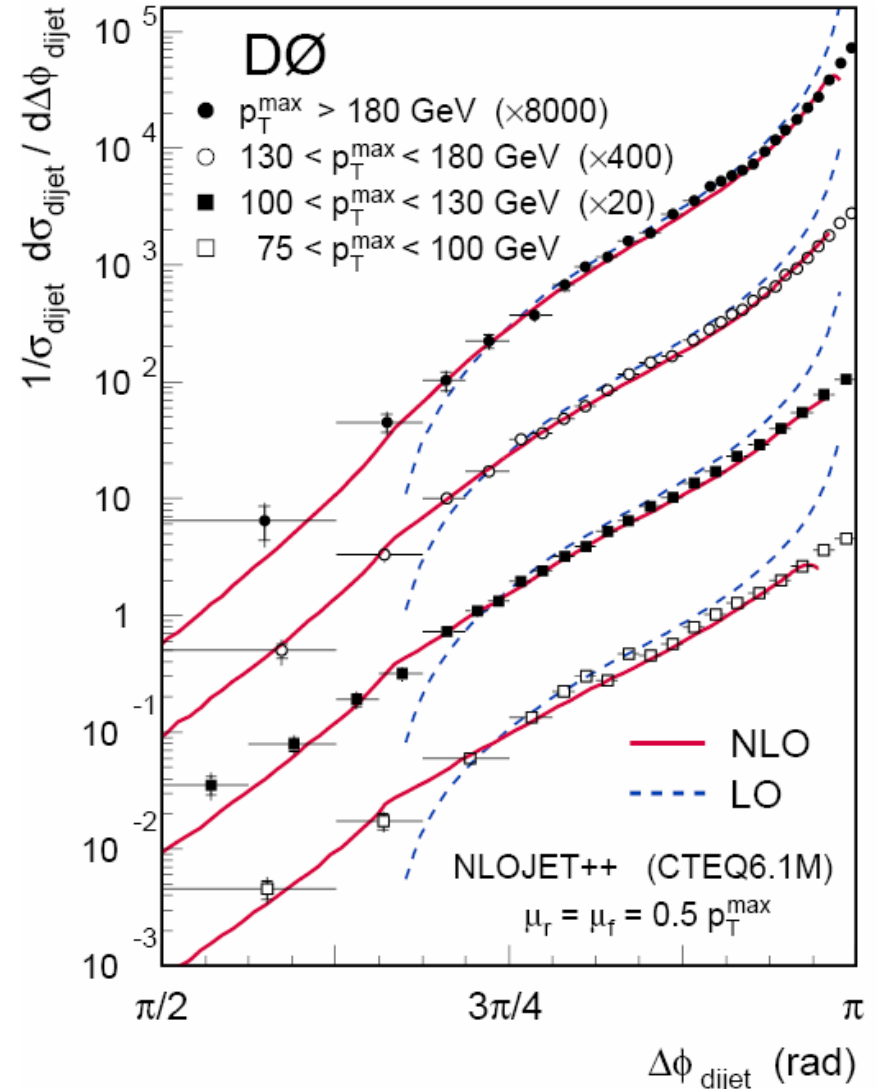
- Two jets back to back in  $\phi$  if only little additional soft radiation.



- If hard radiation,  $\Delta\phi$  can be large.



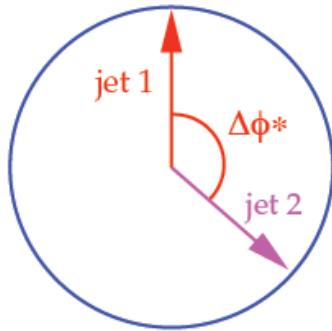
- $\Delta\phi < 2\pi/3$ , four jet region.
- Small and large  $\Delta\phi$  regions poorly described by LO calc, NLO better.



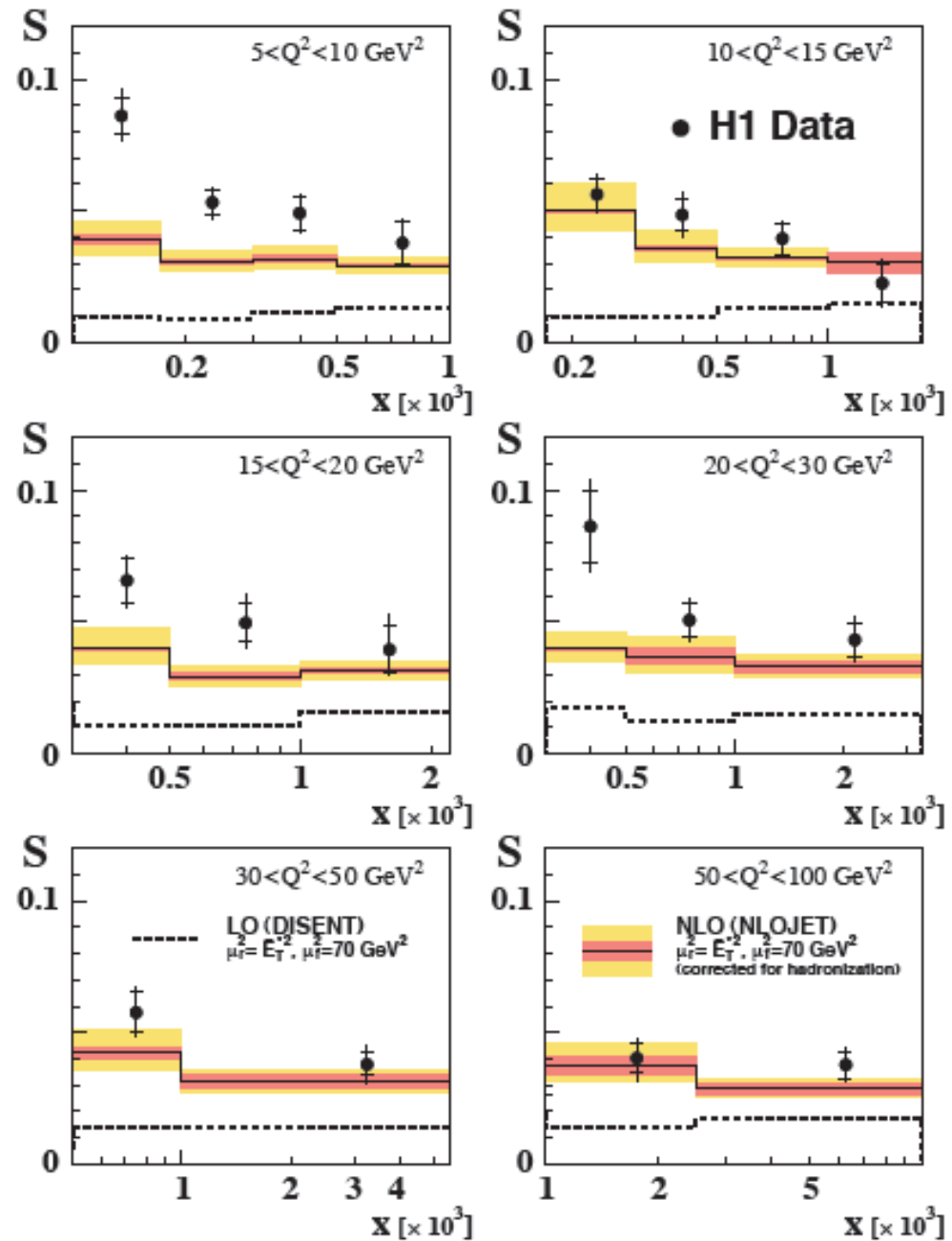
# Dijet azimuthal separation at HERA

- Study frac. of dijets with  $\Delta\phi^* < 2\pi/3$ .

$$S = \frac{\int_0^{2\pi/3} N_{\text{dijet}}(\Delta\phi^*) d\Delta\phi^*}{\int_0^\pi N_{\text{dijet}}(\Delta\phi^*) d\Delta\phi^*}$$

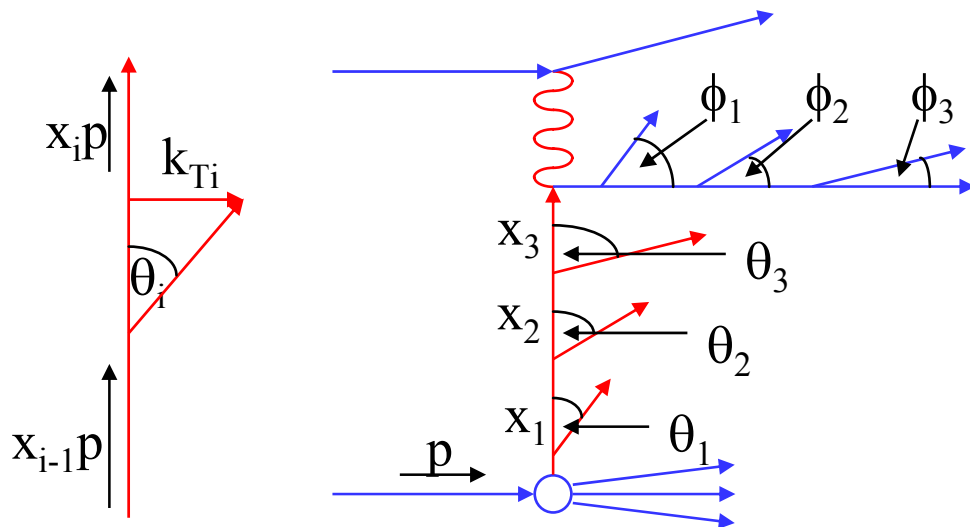


- LO calc [ $O(\alpha_s)$ ], at most 2 jets, fails to describe data.
- NLO calc [ $O(\alpha_s^3)$ ], up to 4 jets, OK at high  $x$ ,  $Q^2$ , but fails at low  $x$  and  $Q^2$ !



# Evolution schemes

- Look again at multiple parton emissions in evolution of p structure.



- QCD interference effects give rise to angular ordering of partons.
- DGLAP approximation, large  $Q^2$ :  
 $\theta_1 < \theta_2 < \theta_3 \dots$

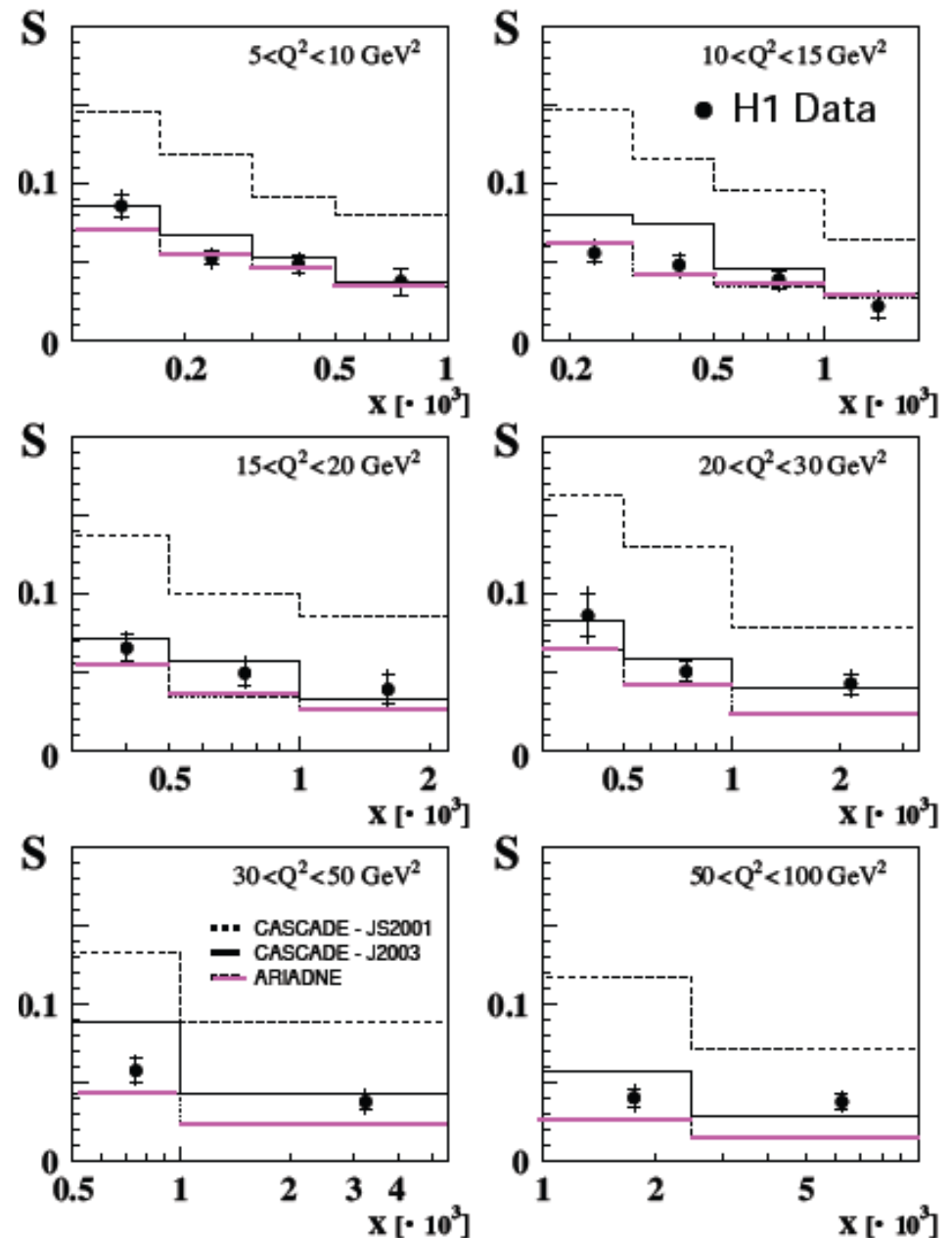
$$\rightarrow k_{T1} < k_{T2} < k_{T3} \dots$$

- In small x regime inappropriate: ignores terms  $\sim \ln(1/x)$ .
- BFKL evolution equation, small x:  
 $\theta_1 < \theta_2 < \theta_3 \dots$   
 $\rightarrow x_1 > x_2 > x_3 \dots$   
 $k_T$  not ordered, sums  $\ln(1/x)$  terms.
- CCFM equation implements angular ordering, applicable at all x and  $Q^2$ .
- Do multiple emissions give measured separation at low x and  $Q^2$ ?
- Check using CASCADE Monte Carlo, based on CCFM equations.



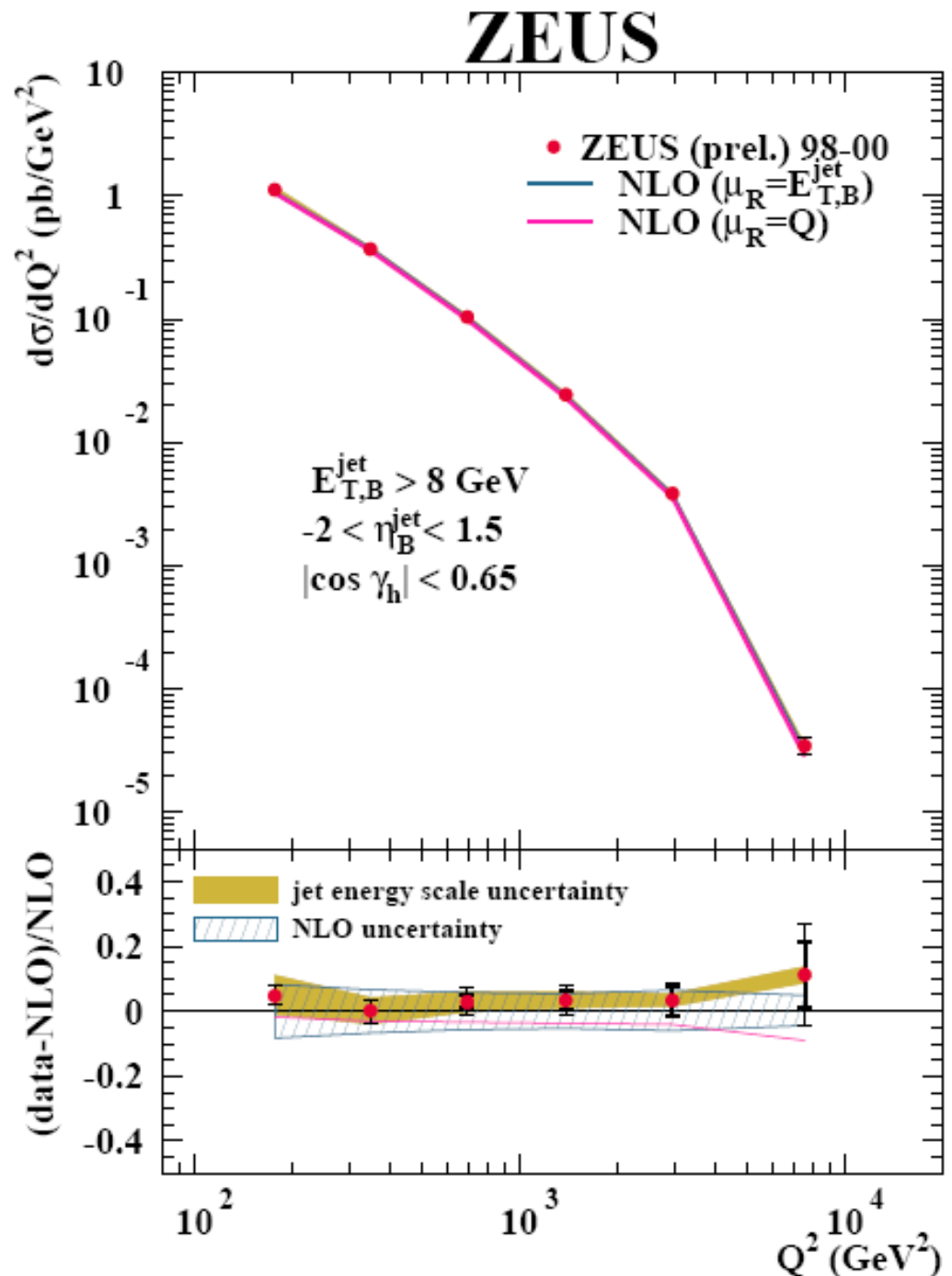
# Jet separation and CCFM evolution

- CASCADE describes data well, using unintegrated PDF.
- J2003 inc. full splitting function much better than JS2001 (singular terms only).
- ARIADNE ( $k_T$  not ordered) also describes data in low  $x$  and  $Q^2$  regime, but fails at high  $x$  and  $Q^2$ .



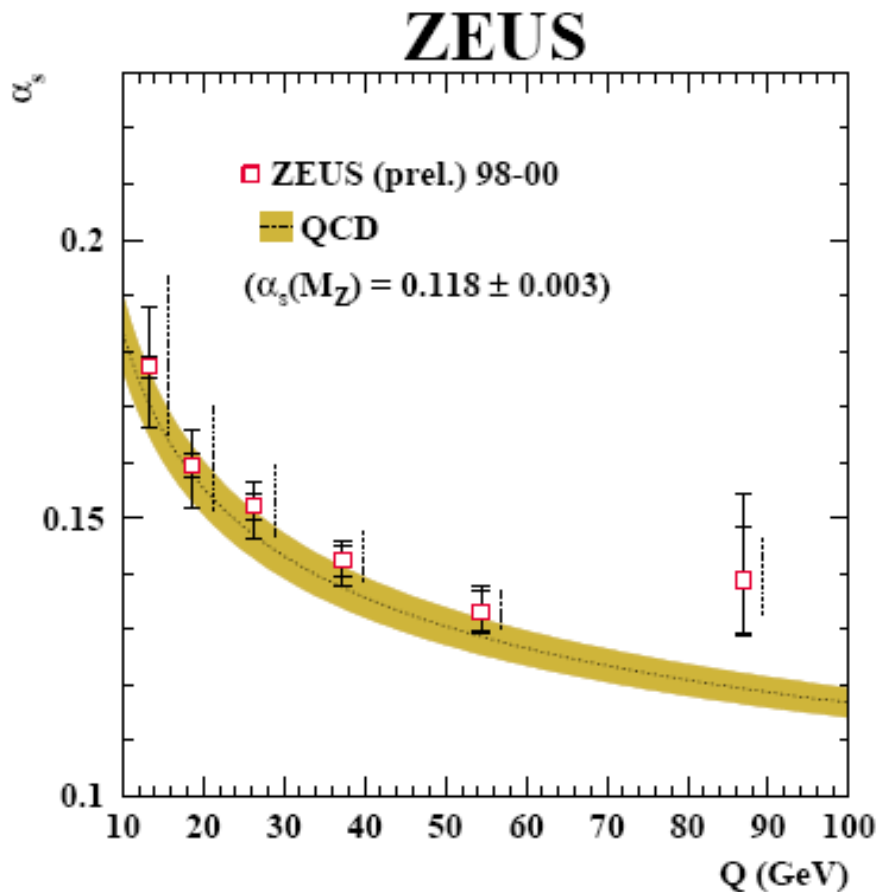
# Jet production and $\alpha_s$ measurements

- Complementary measurements of  $\alpha_s$  to inclusive fits possible using jets.
- Use longitudinally invariant  $k_T$  jet algorithm in the Breit Frame:
  - ◆ Iterative clustering
 
$$d_{i,j} = \min(E_{T,i}^2, E_{T,j}^2) \times \left( (\eta_i - \eta_j)^2 + (\phi_i - \phi_j)^2 \right)$$
  - ◆ Gives n jets with  $d_{i,j} > R_0 = 1$ .
  - ◆ Collinear and IR safe.
- Comparison with DISENT.



# Jet production and $\alpha_s$ measurements

- $\alpha_s$  from inclusive jet cross section.

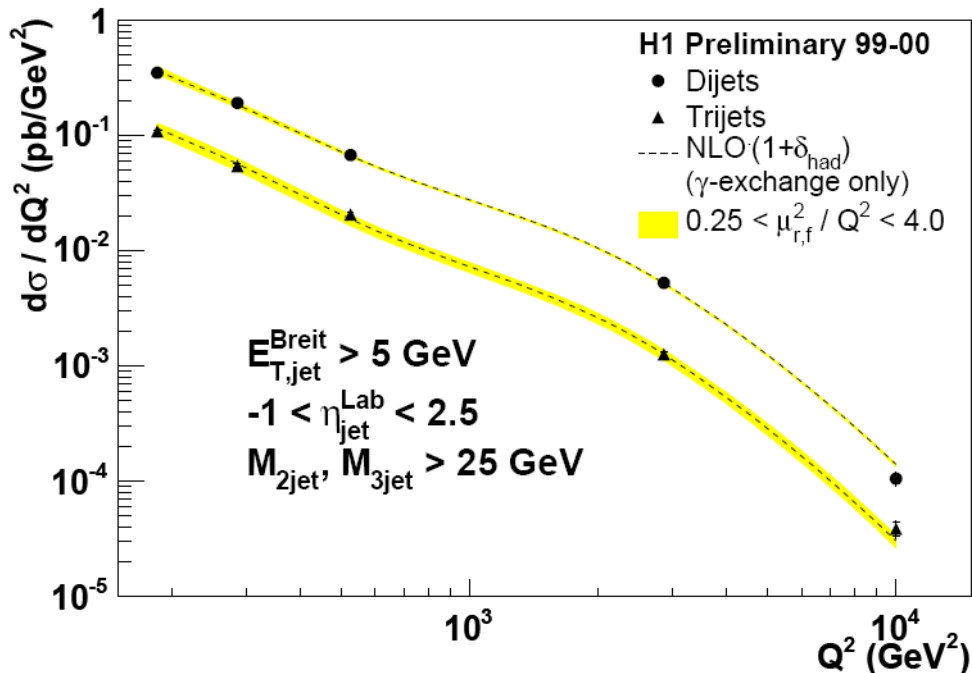


- $\alpha_s(m_Z) = 0.1196 \pm 0.0011(\text{stat})$   
 $+0.0019$  (exp)  $+0.0029$  (theory)  
 $-0.0025$  (exp)  $-0.0017$  (theory)

- Dominant experimental systematic error hadronic energy scale.
- Theory error largely due to renormalisation and factorisation scale uncertainties.

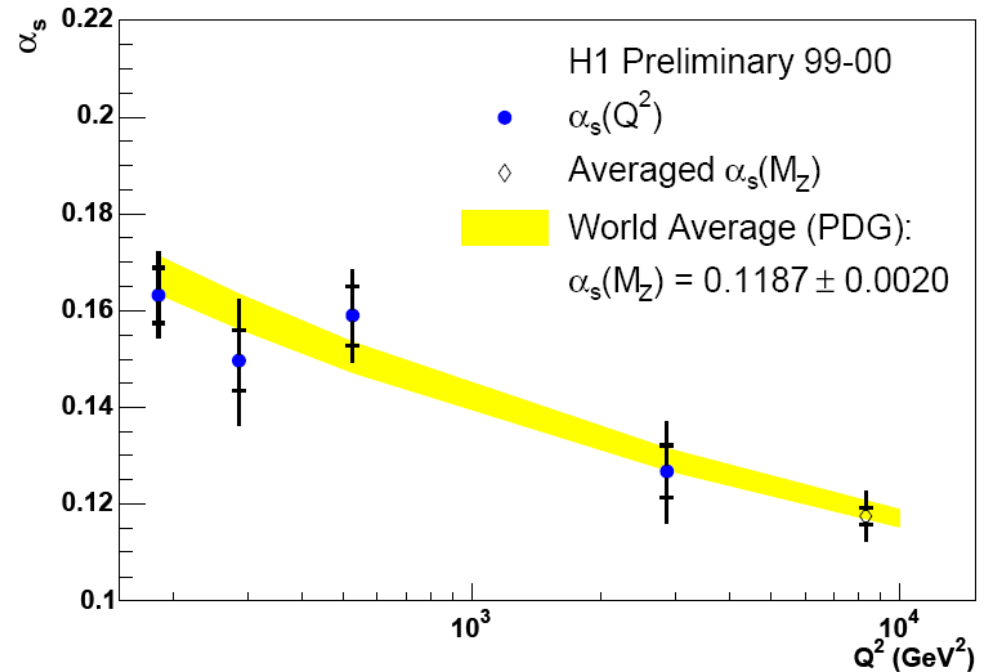
# Jet production and $\alpha_s$ measurements

- Ratio of cross sections for 2 and 3 jet production also sensitive to  $\alpha_s$ .



- Good agreement with NLOJET calculations ( $\gamma$  exchange) except where EW effects significant.

- Resulting  $\alpha_s$  measurement:



- $\alpha_s(m_Z) = 0.1175 \pm 0.0017(\text{stat.})$

$$\pm 0.0050(\text{exp.}) \begin{matrix} +0.0054 \\ -0.0068 \end{matrix} (\text{th.})$$

# Event shapes

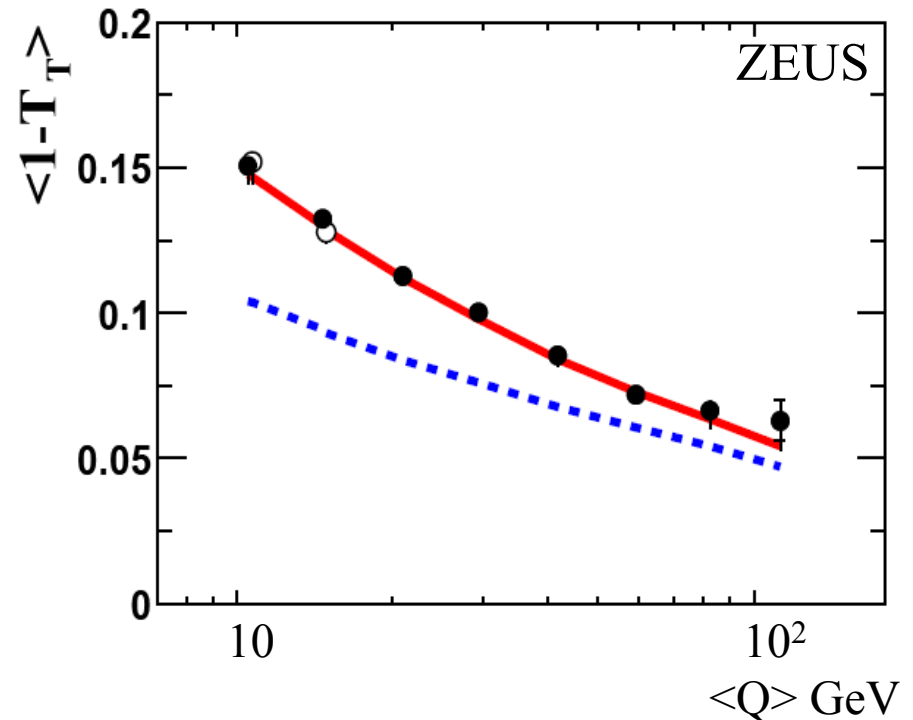
- Study of event shapes allows tests of pQCD and ideas beyond pQCD.

- E.g. thrust,  $T_T = \max_{\hat{n}} \left( \frac{\sum |\vec{p}_i \cdot \hat{n}|}{\sum |\vec{p}_i|} \right)$ .

- Describe  $\langle 1 - T_T \rangle$  using pQCD plus “power corrections” (Dokshitzer, Webber...) which decrease with  $1/Q$   
 $\langle 1 - T_T \rangle = \langle 1 - T_T \rangle_{\text{PC}} + \langle 1 - T_T \rangle_{\text{pQCD}}$

- Introduces universal parameter  $\bar{\alpha}_0$ .
- Fit also T distributions; “pQCD” then re-summed NLL calculations matched to NLO (Dasgupta, Salam) as convergence of pert. series poor for small T.

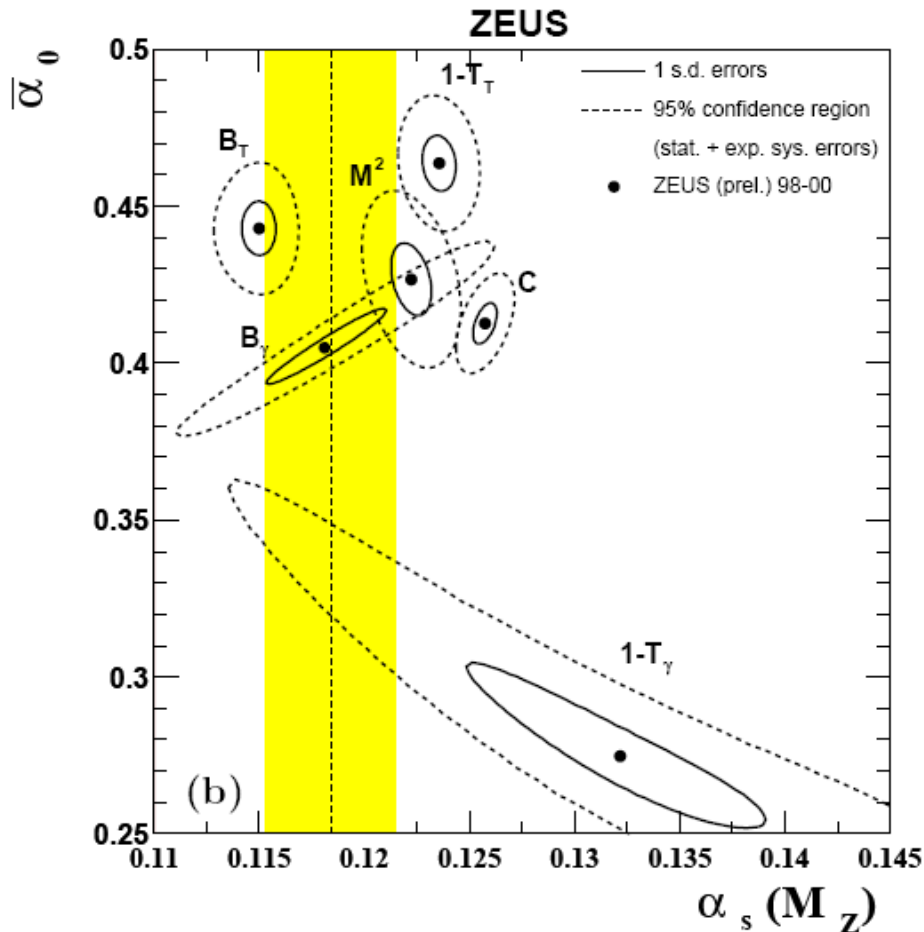
- Measurements in Breit Frame.



- Obtain values of  $\bar{\alpha}_0$  and  $\alpha_s(M_Z)$  from event shape means and distributions.

# Event shapes

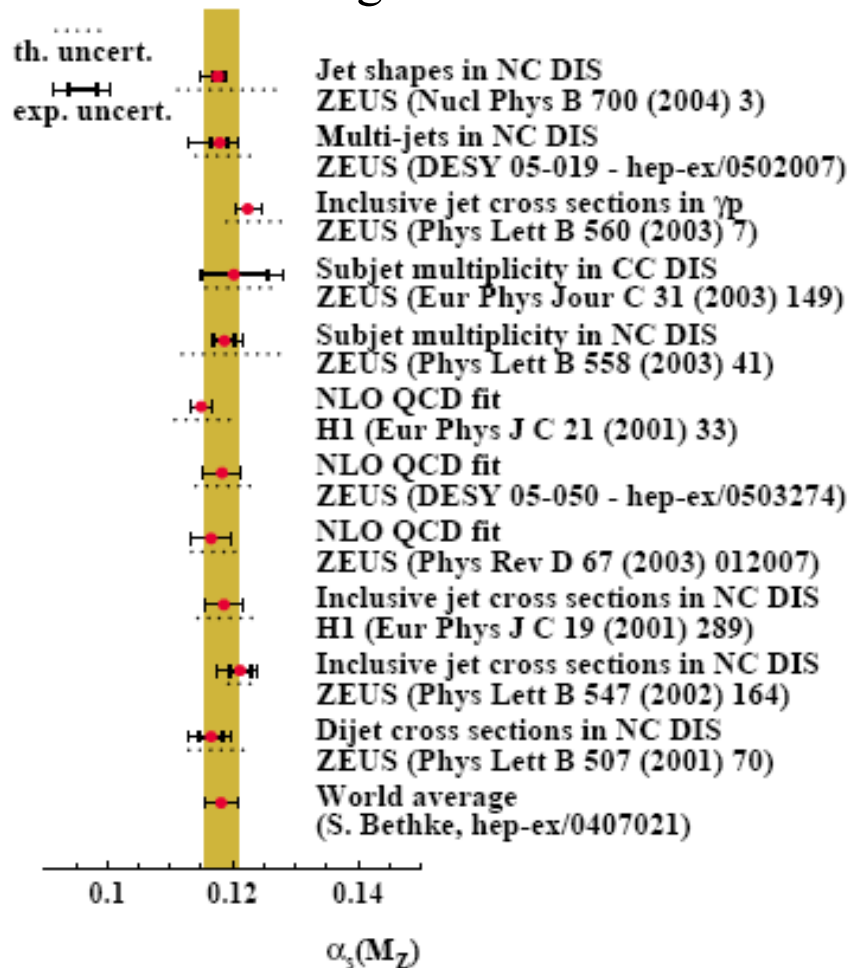
- From means:



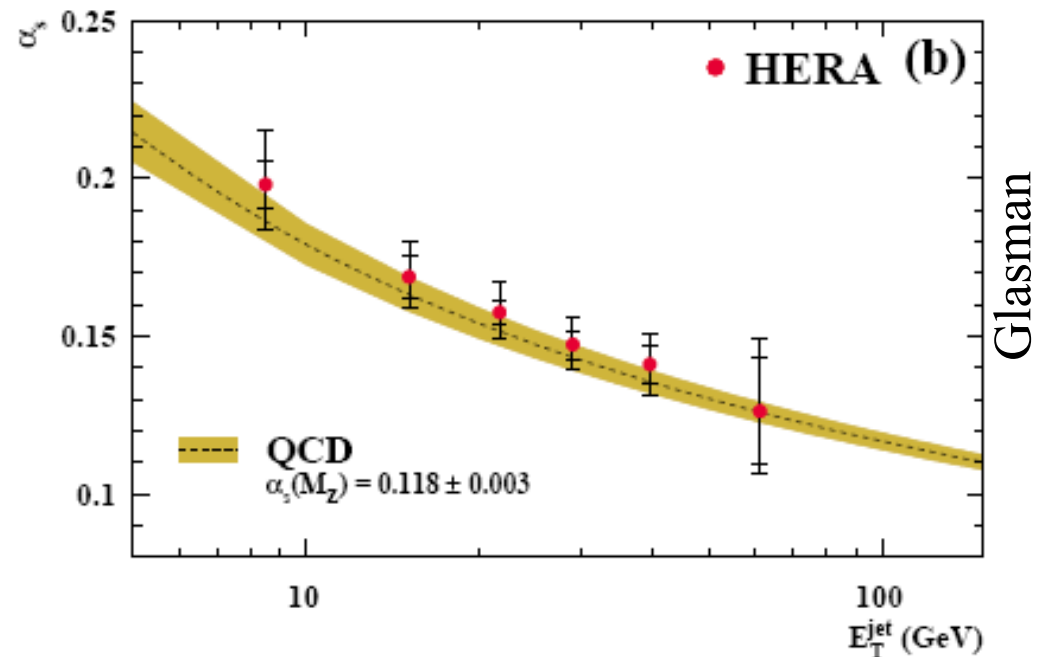
- Results from distributions qualitatively similar.
- $\bar{\alpha}_0 = 0.45 \pm 10\%$  for all variables except  $T_g$  and  $C$ .
- Values of  $\alpha_s(m_Z)$  extracted from means consistent within 5%.
- $\alpha_s(m_Z)$  from distributions consistent with world average.
- Dispersion of  $(\alpha_s(m_Z), \bar{\alpha}_0)$  values indicative of need for higher order calculations?

# HERA $\alpha_s$ summary

- C.f. HERA  $\alpha_s$  measurements and world average:

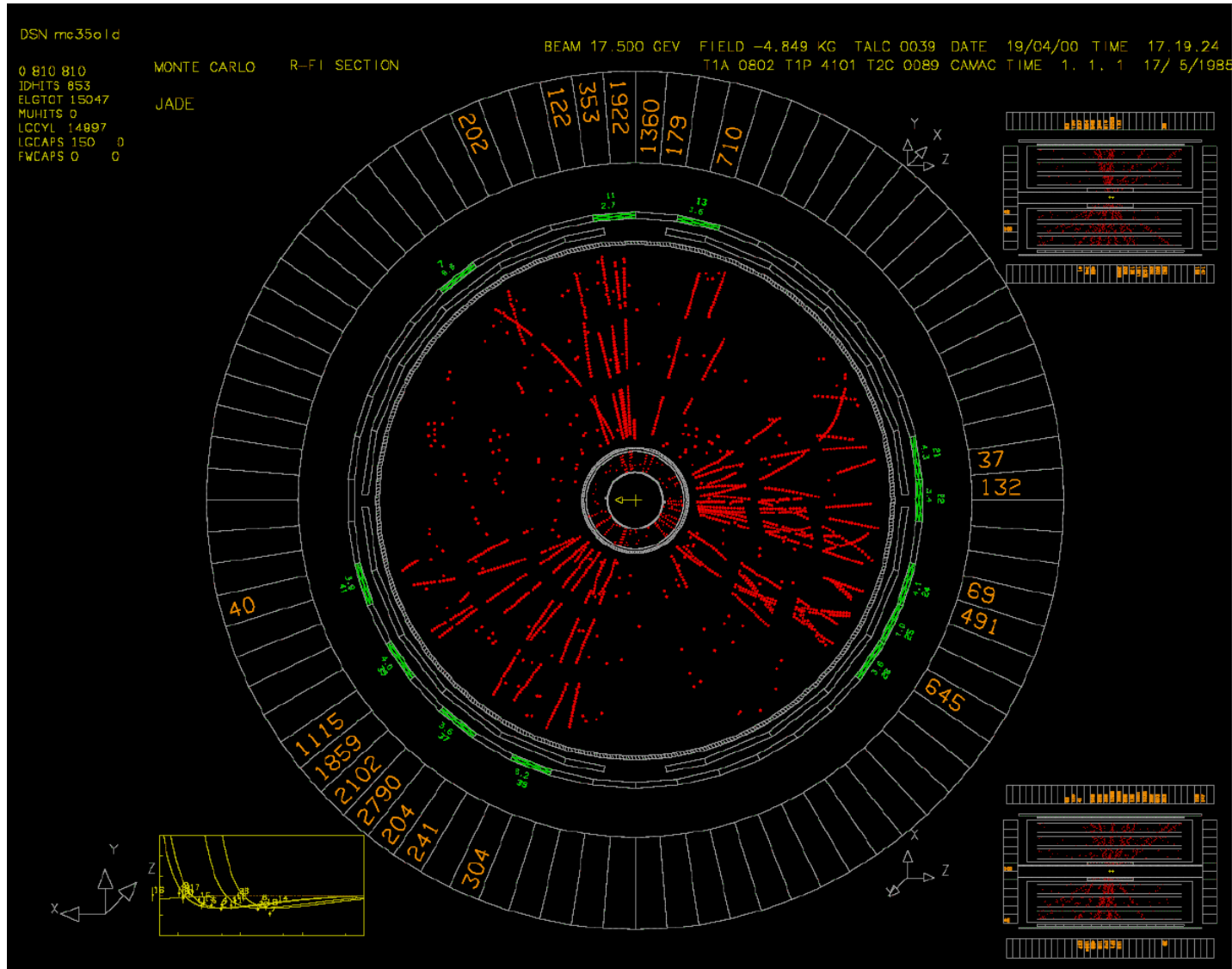


- $\alpha_s$  measurements from jets.



- Preliminary HERA average:  
 $\alpha_s(m_Z^2) = 0.1186 \pm 0.0011(\text{exp.})$   
 $\pm 0.0050(\text{th.})$

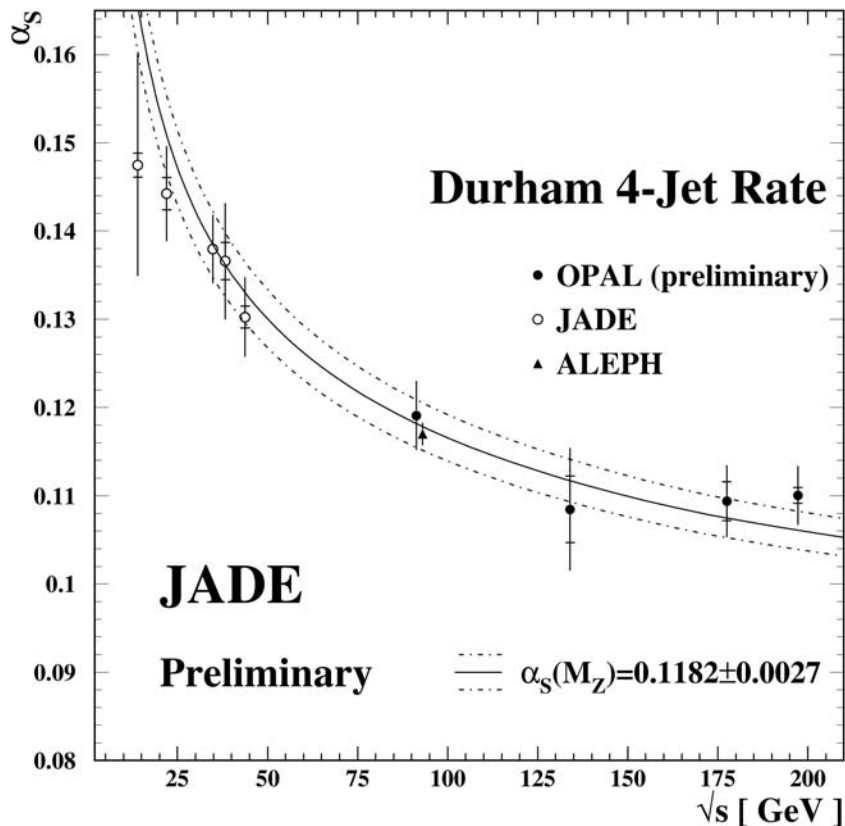
# Back to PETRA where the gluon was discovered



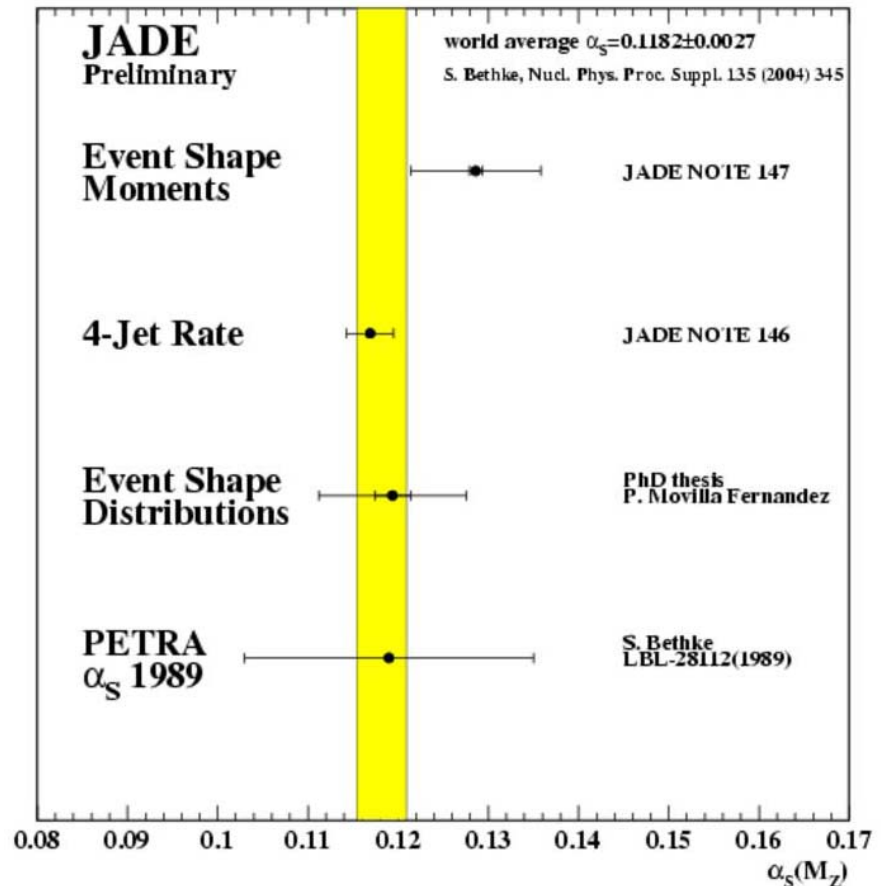


# Reanalysis of JADE data

- Study 4 jet rate using modern Monte Carlos to make hadronisation and detector corrections, c.f. NLO + NLL calculations.

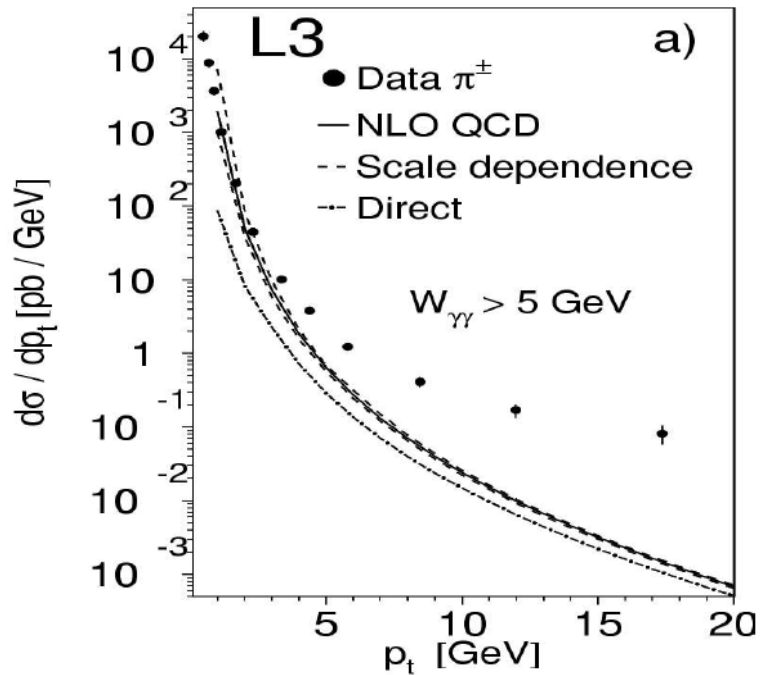


- Significant progress in determination of  $\alpha_s(m_Z)$  in last ~15 years!

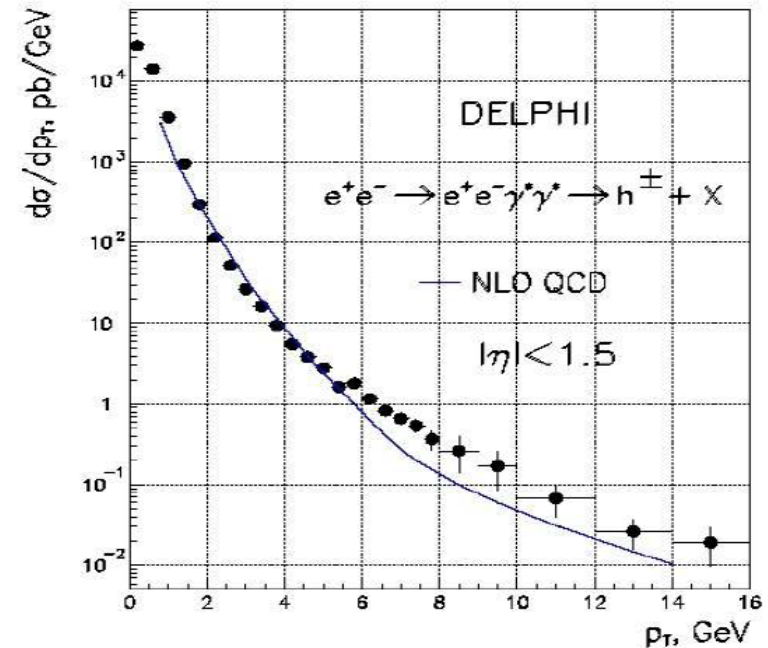


# Hadron production in $\gamma\gamma$ collisions

- Large disagreement with NLO QCD observed by L3 in  $\gamma^*\gamma^* \rightarrow hX$



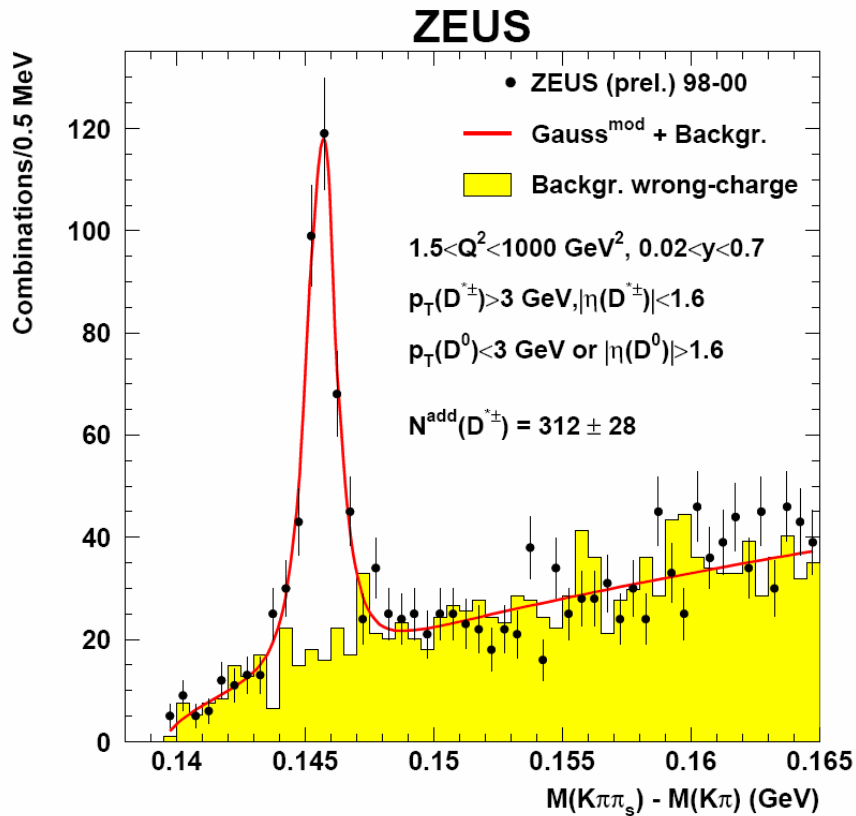
- New measurements by DELPHI show significantly better agreement.



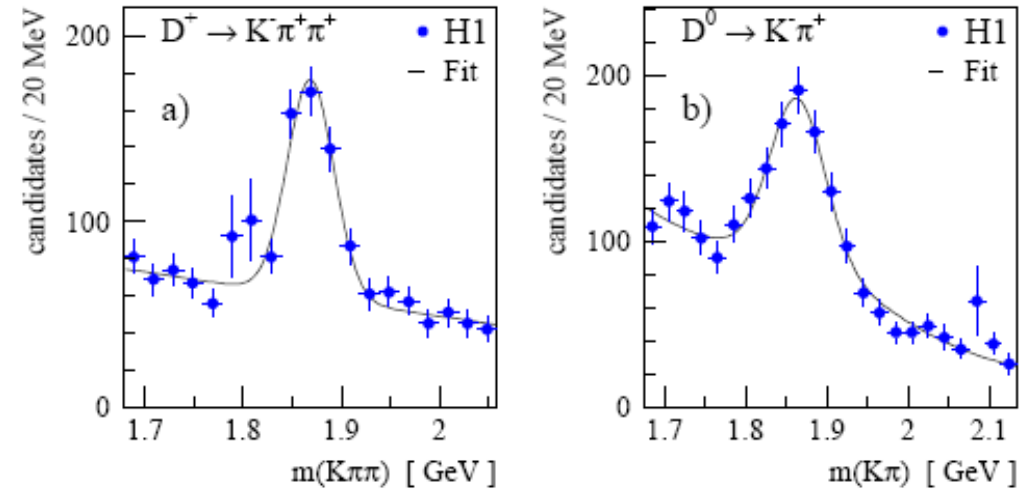
- DELPHI report using L3 cuts allows  $e^+e^- \rightarrow q\bar{q}$  background into event sample at large  $p_T$ .

# Charm fragmentation

- Inclusive cross sections for  $D^*$ ...



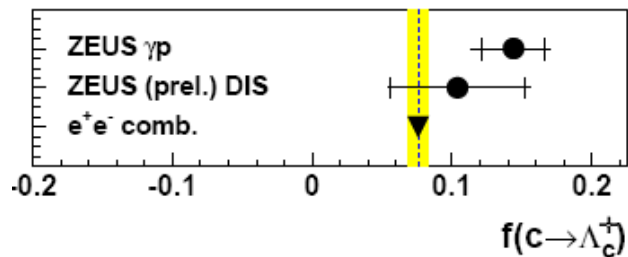
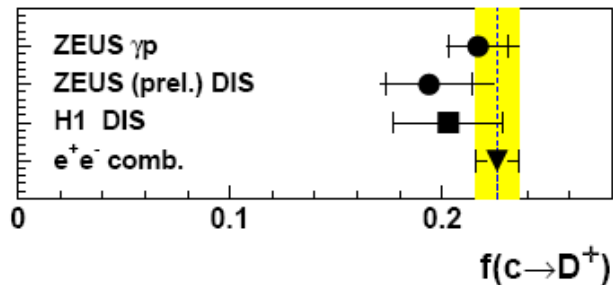
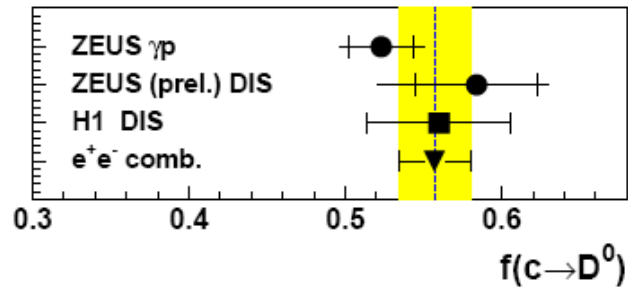
- ...  $D^+$ ,  $D^0$ ...



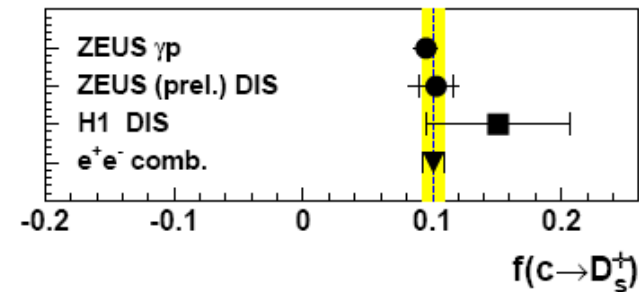
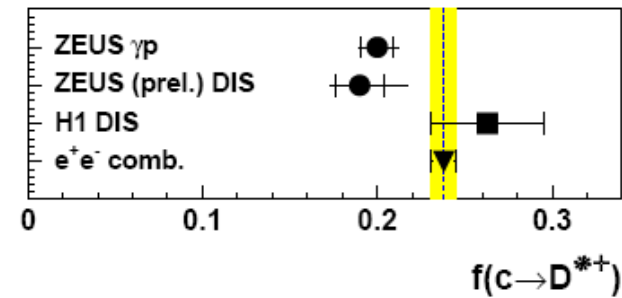
- ...  $D_s^+$  and  $\Lambda_c$  measured by HERA experiments.

# Charm fragmentation

- Hence fragmentation fractions determined:

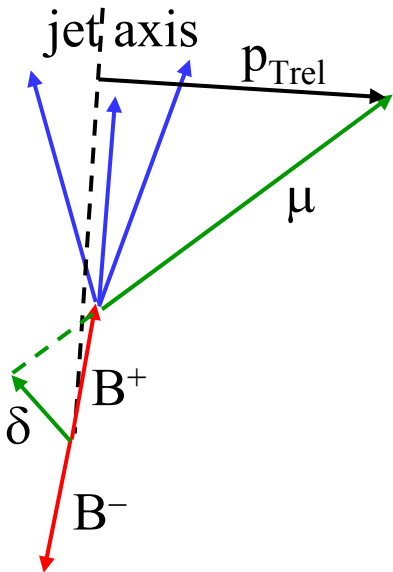
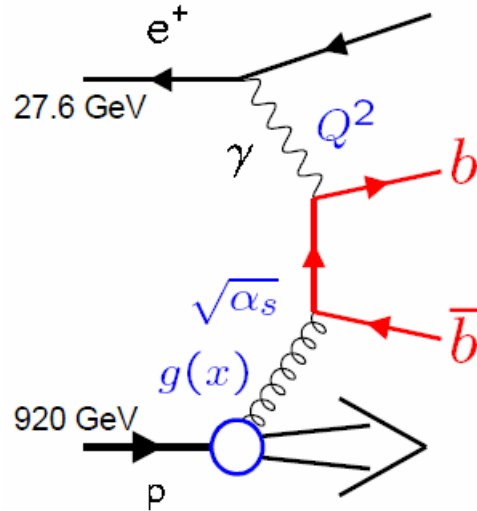


- All fragmentation fractions are consistent with world average and support assumption of universality.



# Beauty in DIS events

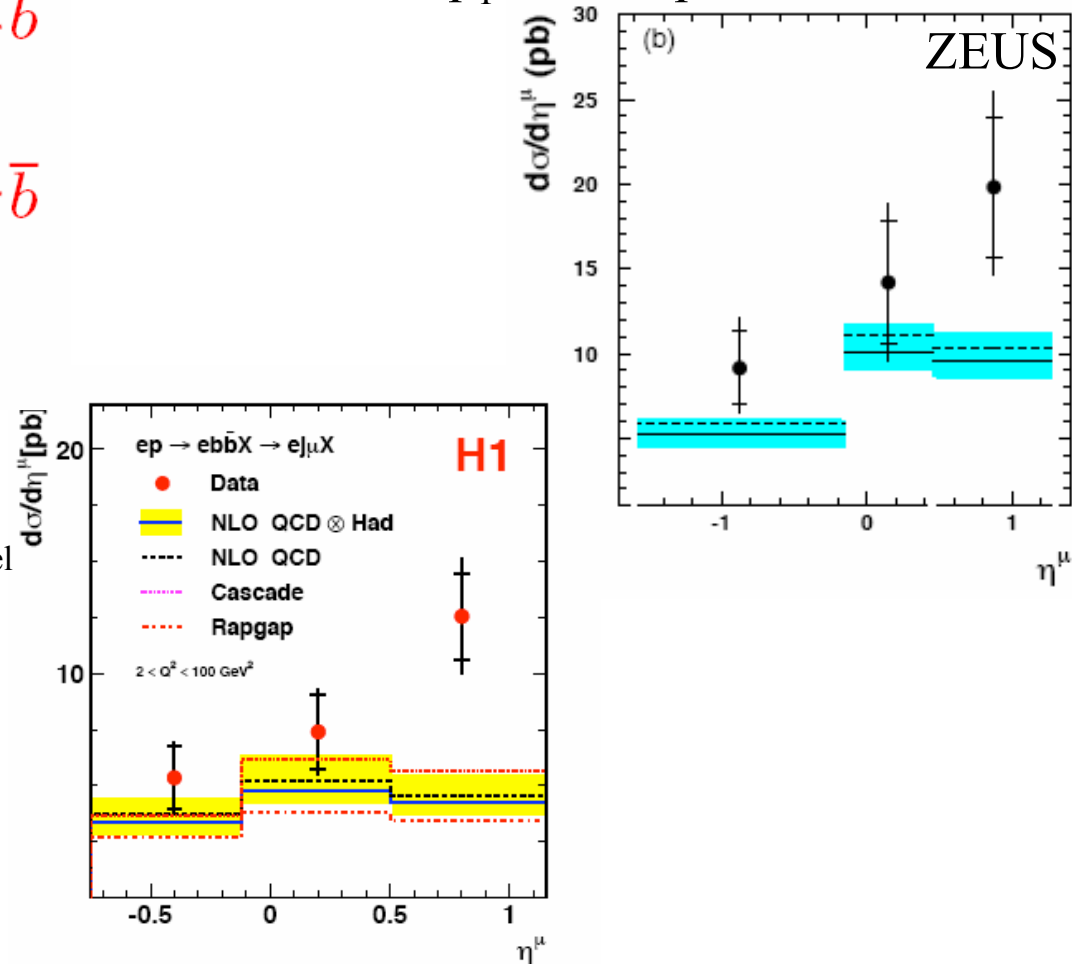
- Main production mechanism in DIS



- Identify semi-muonic beauty decays via  $p_{Trel}$  and impact parameter  $\delta$  of muon (H1) or  $\delta$  (ZEUS).

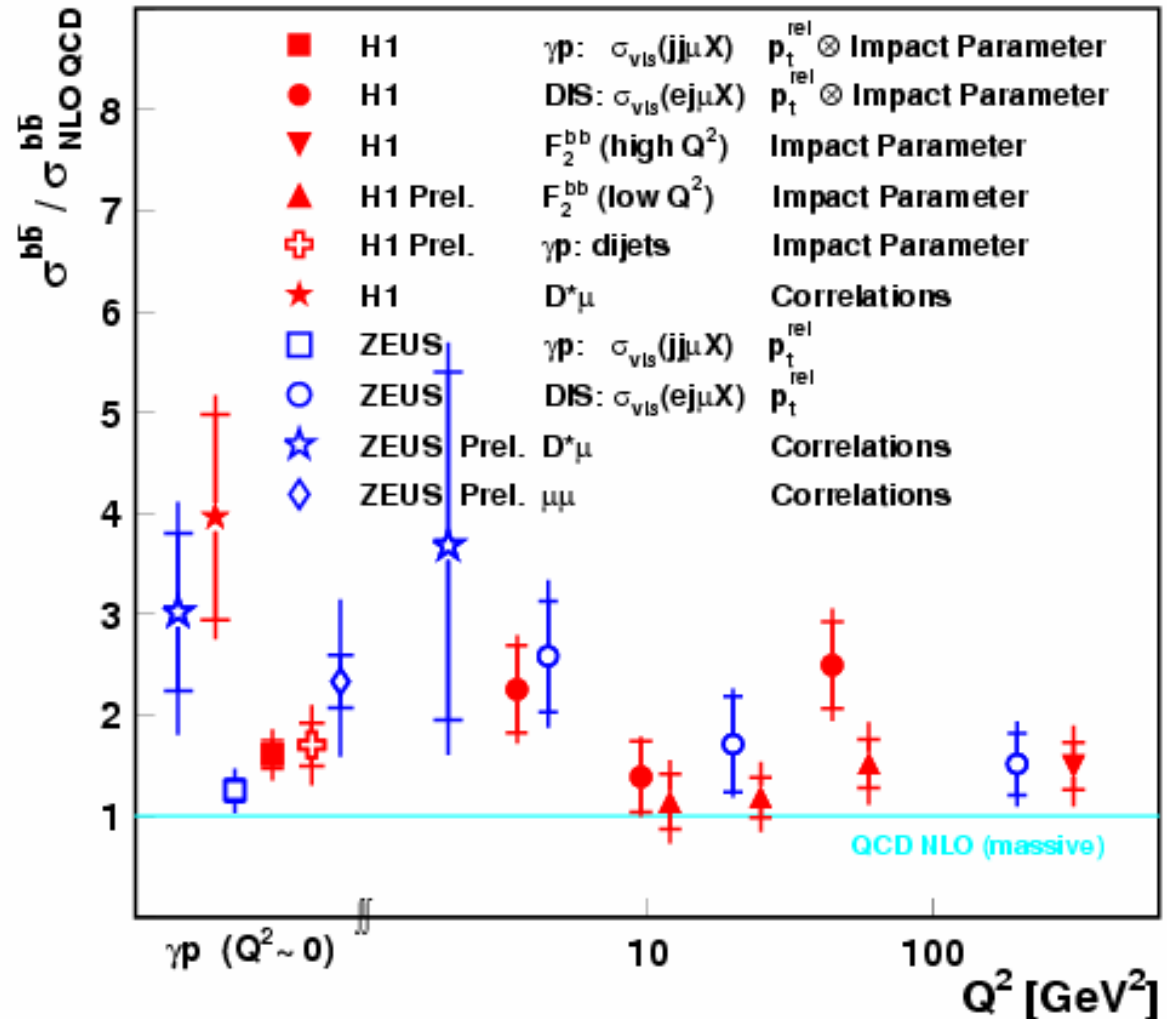
- Measure cross section for  $ep \rightarrow eb\bar{b}Y \rightarrow ejet\mu X$

- NLO QCD below both H1 and ZEUS data at small  $p_{T\mu}$  and in p direction.



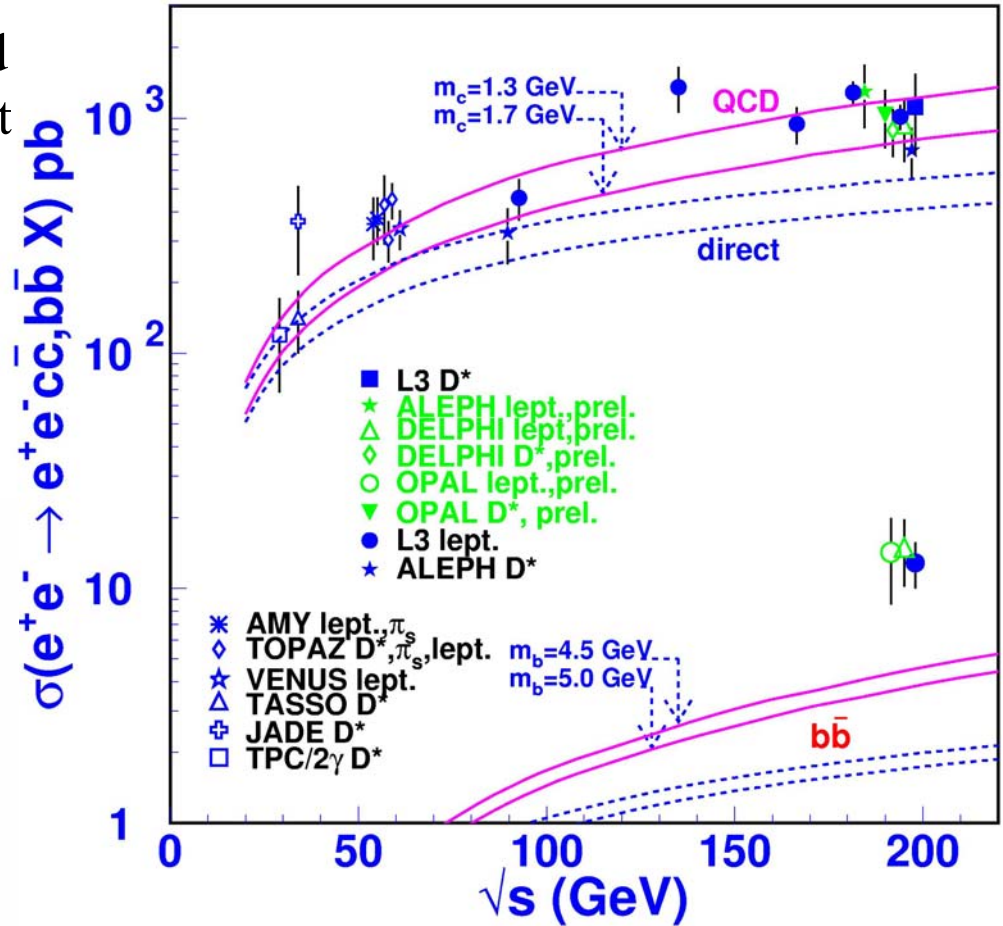
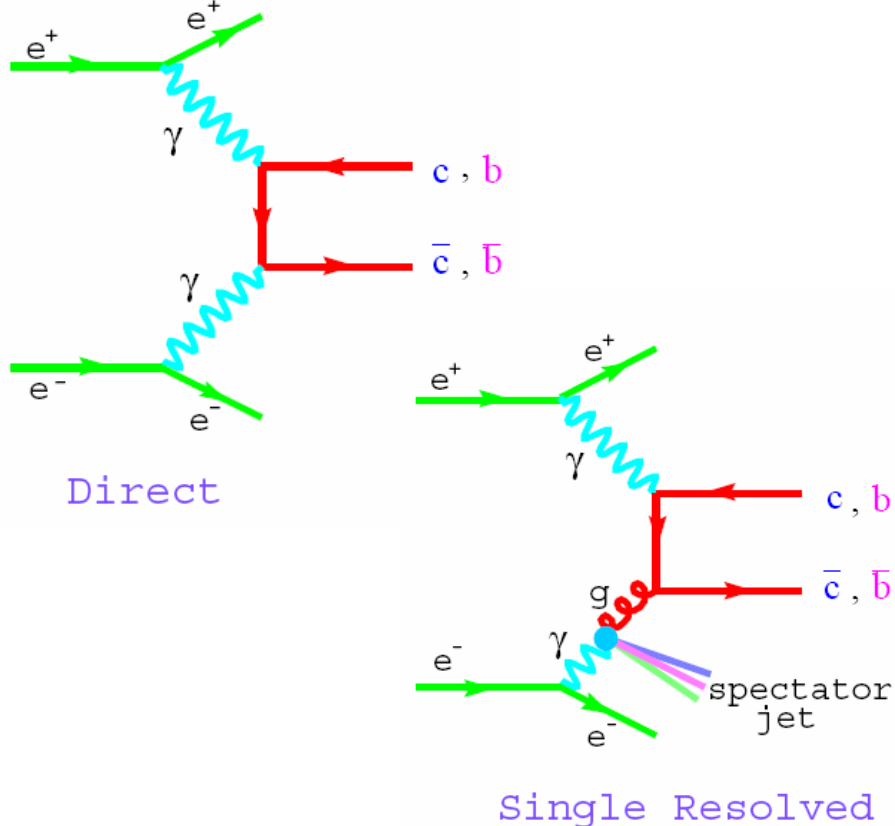
# Summary of beauty measurements at HERA.

- Many measurements of beauty production now available.
- “Massive” NLO calcs tend to lie somewhat below the data (FMNR in photoproduction, HVQDIS for higher  $Q^2$ ).
- Evidence that shapes of distributions poorly described in some places (e.g. in  $e\mu X$  at low muon  $p_T$  and in proton direction).
- “Double tag” analyses with no jet requirement started, aim is to study production of  $b\bar{b}$  with low  $p_T$ .



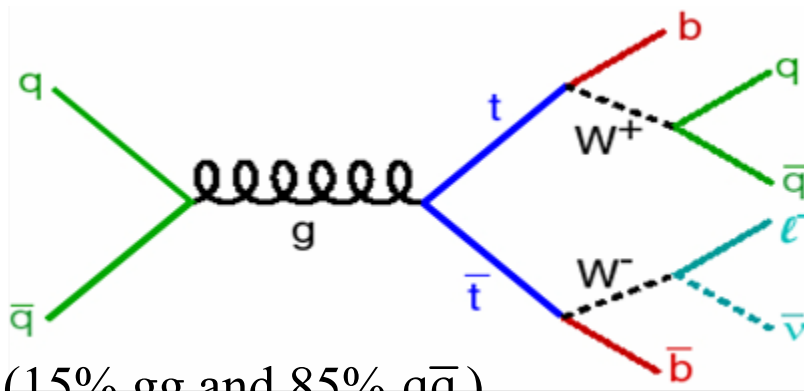
# Heavy flavours in $\gamma\gamma$ scattering

- Recent measurements of heavy flavour production by L3 show good agreement with NLO QCD for c, but lie above expectations for b.



# Top quark production at the TeVatron

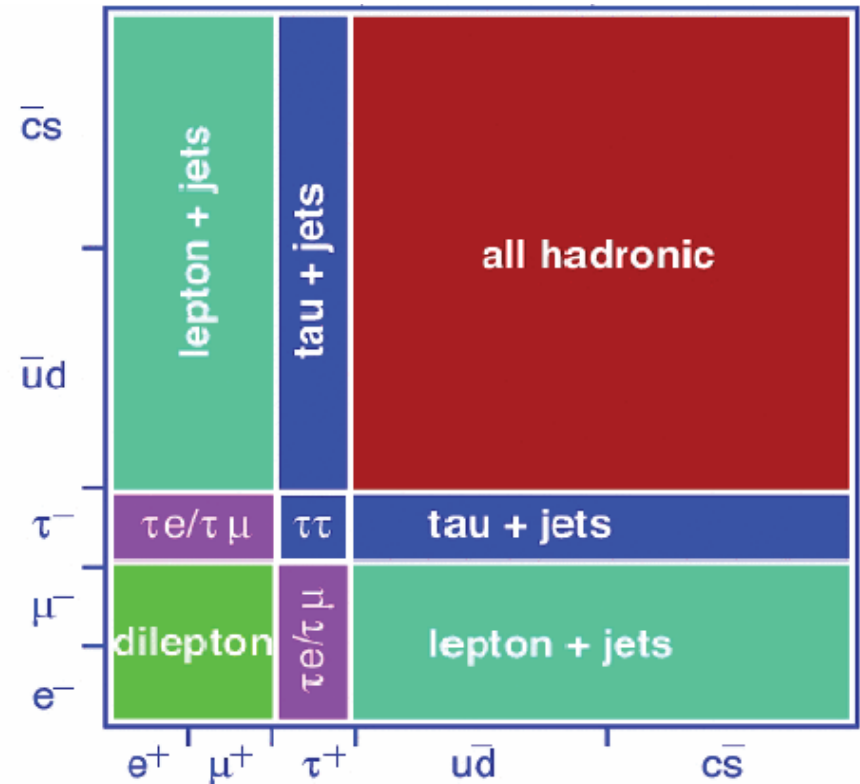
- Production mechanism:



(15%  $gg$  and 85%  $q\bar{q}$ )

- Dominant theory errors are renormalisation and factorisation scale dependence (5%) and PDFs (7%).
- Study all hadronic, lepton + jets, tau + jets (CDF) and dilepton decay modes of Ws.

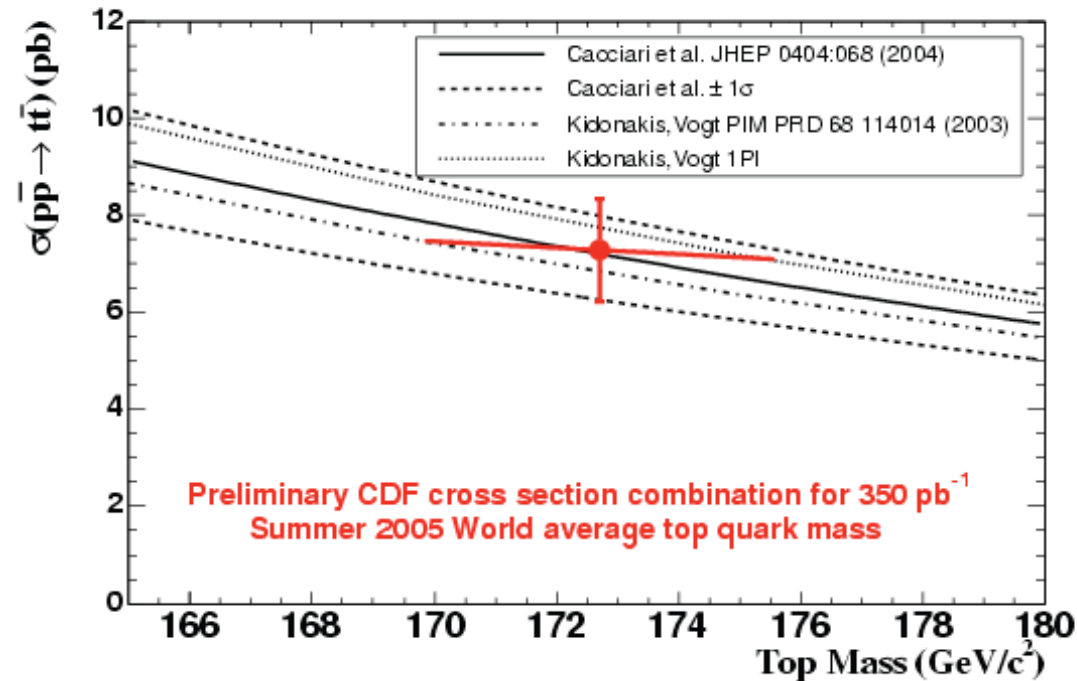
- Decays of Ws in top pair events, BR  $\sim$  area:





# Top quark production at the TeVatron

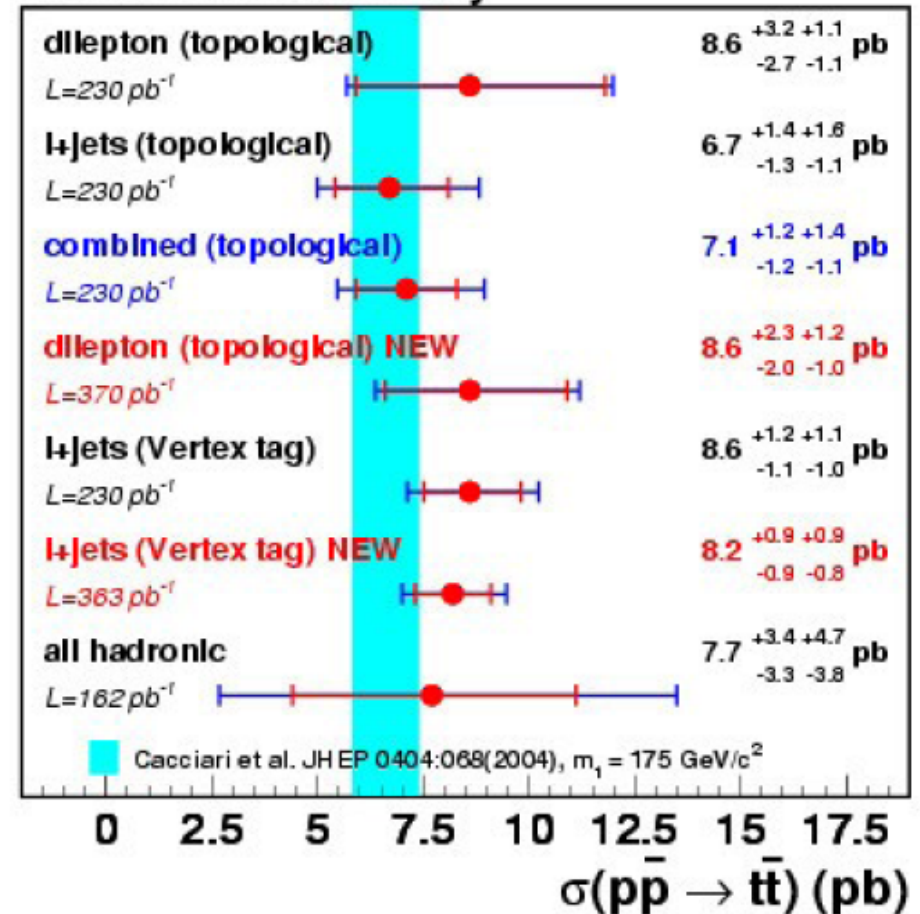
## ■ Combined CDF measurement.



- So far  $\sim 300 \text{ pb}^{-1}$  analysed. experiments have  $\sim 1 \text{ fb}^{-1}$  on tape.
- No evidence yet for single top production.

## ■ Summary of D0 results.

### D0 Run II Preliminary



# Summary

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Thanks to all the speakers in the Hard QCD session, and apologies to those whose work could not be mentioned in this summary!

- QCD is the theory of strong interactions, but developing a complete understanding of its implications remains a challenge.
- Theoretical progress is being made, e.g. in the area of NNLO calculations and in the development of NLO Monte Carlo programs.
- Experiments are increasing the precision and range of data used in structure function and  $\alpha_s$  determinations.
- Further increasing the precision of nucleon PDFs requires more data, new data, and good ideas; some of which are available, or will be soon.
- Surprises continue to appear, such as the effect of the photonic component of proton structure and the size of weak corrections at the TeVatron.
- New and improved jet results coming from the TeVatron and a new round of jet measurements from HERA., studying both jet structure and jet rates.
- Some areas where need for more than DGLAP apparent.
- Inclusive heavy flavour production measurements well described, but still some areas where specific cross sections poorly described.