

# ZEUS $F_2^D$ results

XIII International Workshop on Deep Inelastic Scattering  
Madison, Wisconsin U.S.A., Apr. 27-May 1, 2005

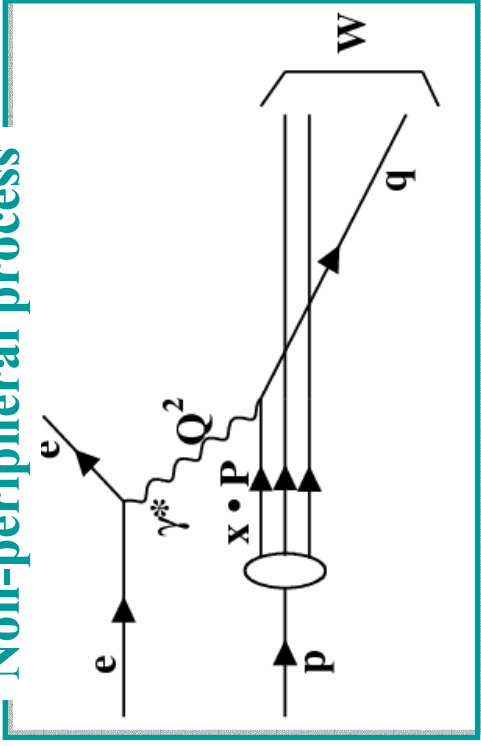
*Heuijin Lim (DESY)*

on behalf of the ZEUS Collaboration

- Introduction
- Diffractive measurement with  **$M_x$  method**
  - ➔ hep-ex/0501060 (Accepted by Nucl. Phys. B.)
- Diffractive measurement with **a leading proton**
  - ➔ Eur. Phys. J. C **38**, 43 (2004) and also hep-ex/0408009
- Summary

# Inclusive Diffraction in Deep Inelastic Scattering

## Non-peripheral process



## Kinematics of $ep \rightarrow eXp$

$$Q^2 = -(k - k')^2 \quad x = Q^2 / (2q \cdot p)$$

$$W = \sqrt{(p + q)^2} \quad M_X^2 = (k - k' + p - p')^2$$

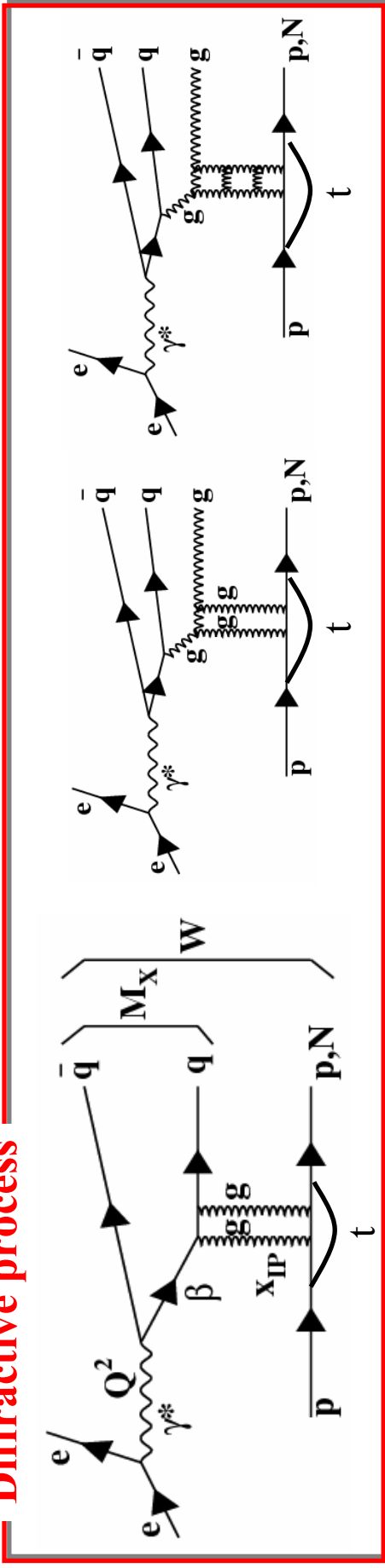
$$x_{IP} \approx \frac{Q^2 + M_X^2}{Q^2 + W^2} \quad \beta \approx \frac{Q^2}{M_X^2 + Q^2} = \frac{x}{x_{IP}}$$

$$t = (p - p')^2 \quad x_L = p'_z / E_p = 1 - x_{IP}$$

## Present diffractive measurement in terms of

$\rightarrow d\sigma(M_X, W, Q^2)/dM_X$  and  $x_{IP} F_2^{D(3)}(\beta, x_{IP}, Q^2)$

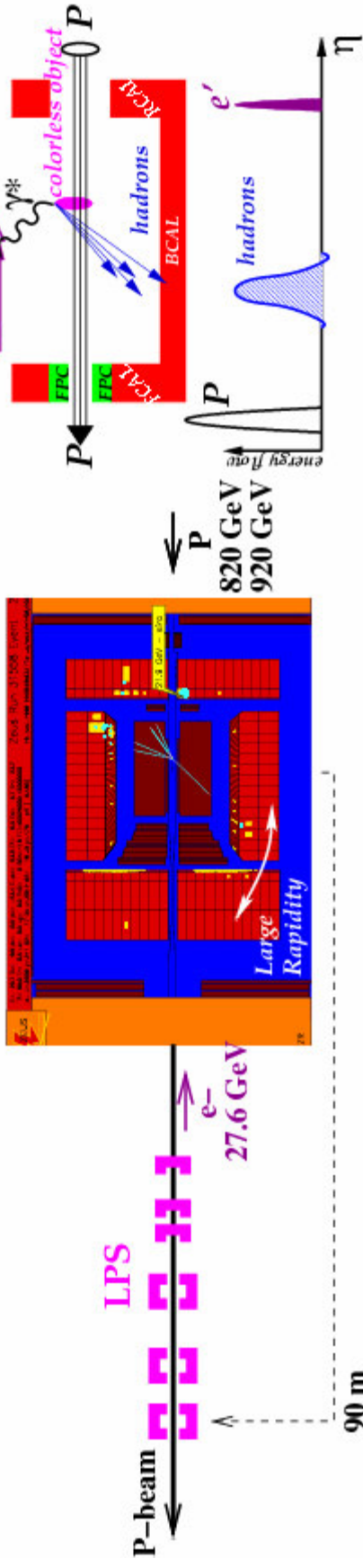
## Diffractive process



# Event Topologies ( ep → eXp )

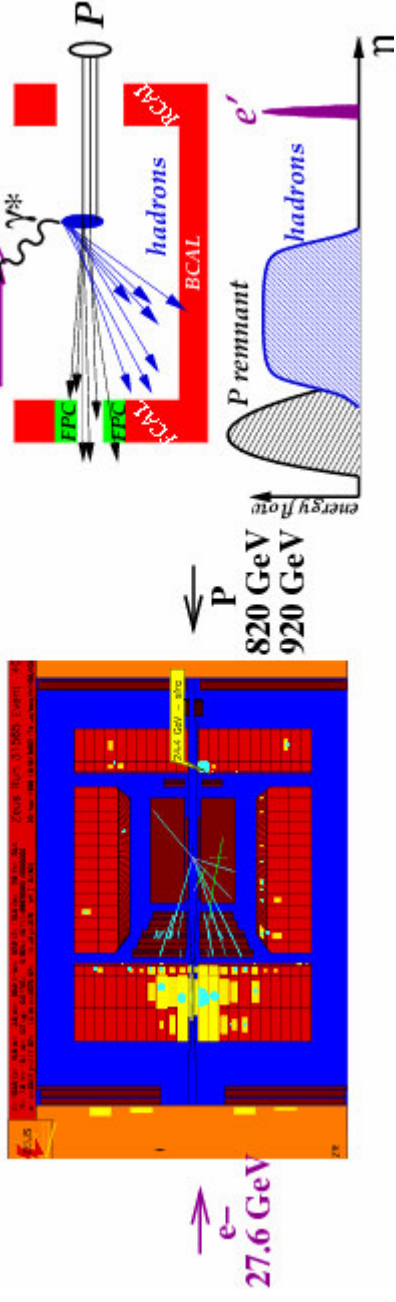
**Diffractive scattering**

( $M_X = 5 \text{ GeV}$ ,  $Q^2 = 19 \text{ GeV}^2$ ,  $W = 123 \text{ GeV}$ )

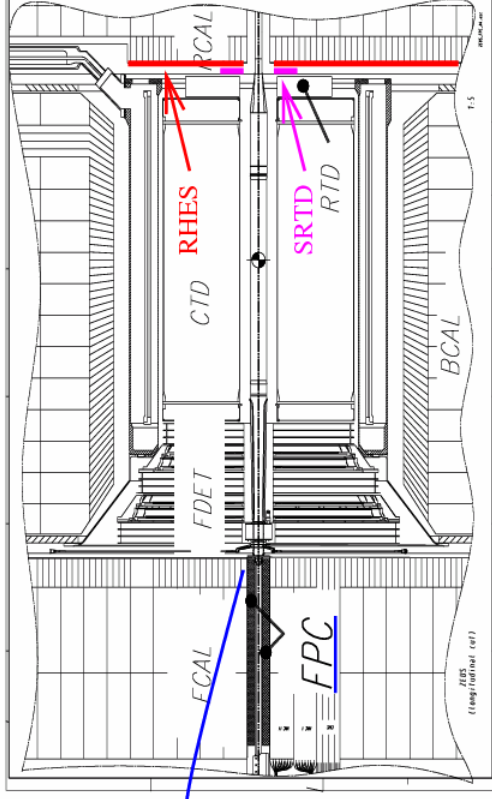
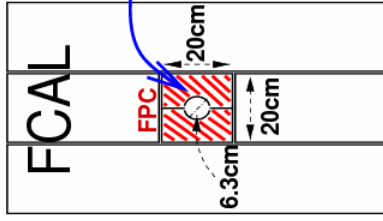


**Non-peripheral scattering**

( $M_X = 45 \text{ GeV}$ ,  $Q^2 = 13 \text{ GeV}^2$ ,  $W = 93 \text{ GeV}$ )



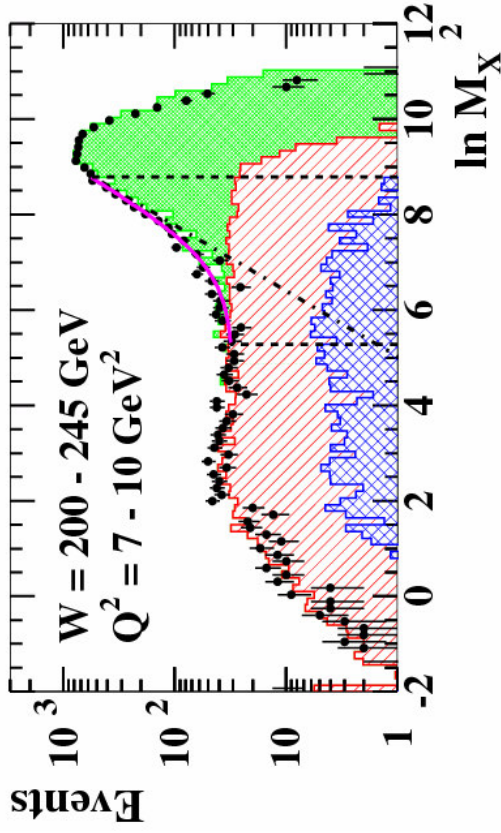
# $M_X$ method using Forward Plug Calorimeter



## Forward Plug Calorimeter

- ✓ Increase the accessible  $M_X$  range by a factor of 1.7.
- ✓ If  $M_N > 2.3$  GeV deposits  $E_{FPC} > 1$  GeV,   
 → recognized and rejected

- Fit( $c \exp(b \ln M_X^2)$ )
- DJANGOH ▨ SATRAP+ZEUSVM ▨ SANG( $M_N < 2.3$  GeV)
- (ZEUS 98-99)-PYTHIA-SANG( $M_N > 2.3$  GeV)



$$\frac{dN}{d \ln M_X^2} = \underbrace{D}_{\text{Diffraction}} + \underbrace{c \cdot \exp(b \cdot \ln M_X^2)}_{\text{Non-diffraction}}$$

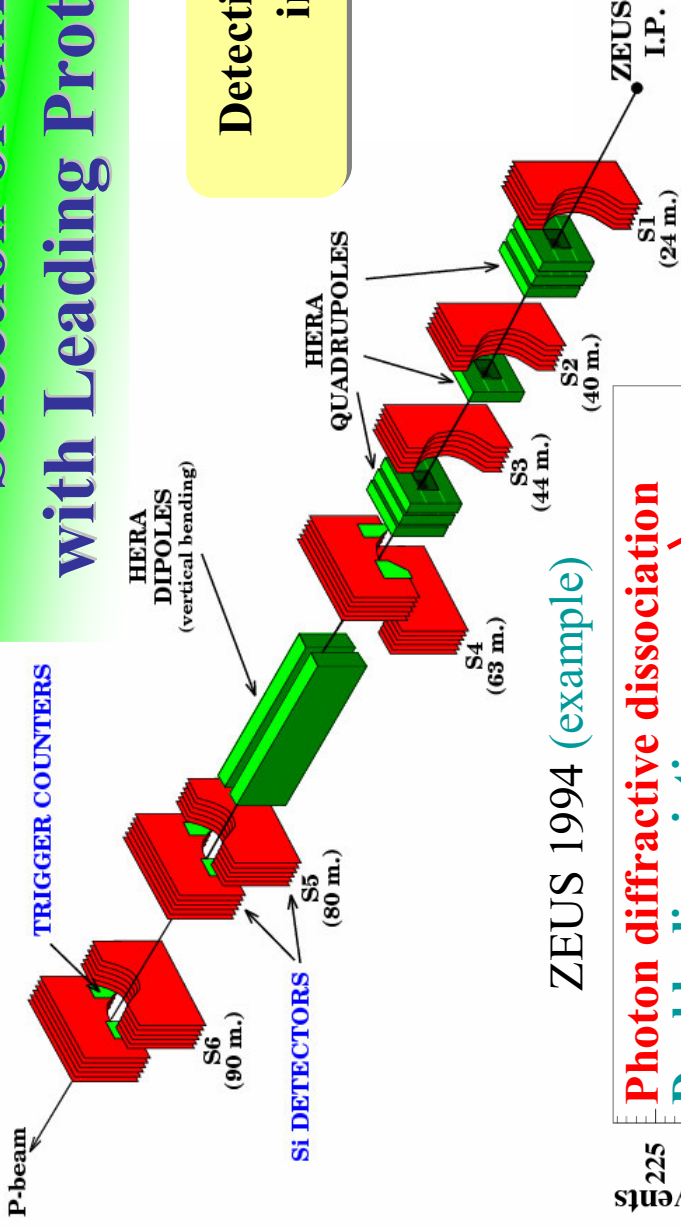
with free parameters,  $D$ ,  $b$  and  $c$  from fit.

$$d\sigma_{\gamma^* p \rightarrow XN}^{\text{diff}}/dM_X, M_N < 2.3 \text{ GeV}$$

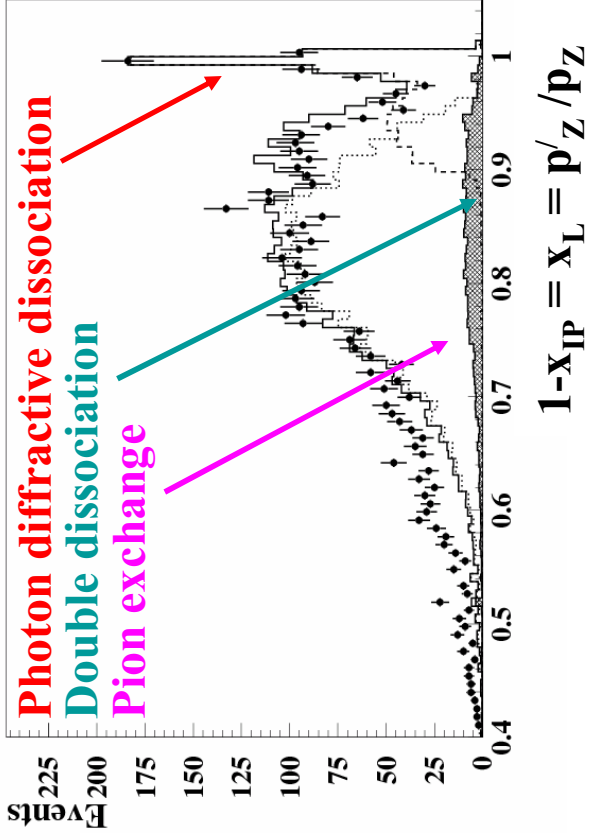
- $2.2 < Q^2 < 80 \text{ GeV}^2$
- $37 < W < 245 \text{ GeV}$
- $0.28 < M_X < 35 \text{ GeV}$

Using 98-99 data  
with 4.2 pb<sup>-1</sup>

# Selection of diffractive events with Leading Proton Spectrometer



ZEUS 1994 (example)



Detection of the scattered proton  
in LPS with  $x_L > 0.9$ .

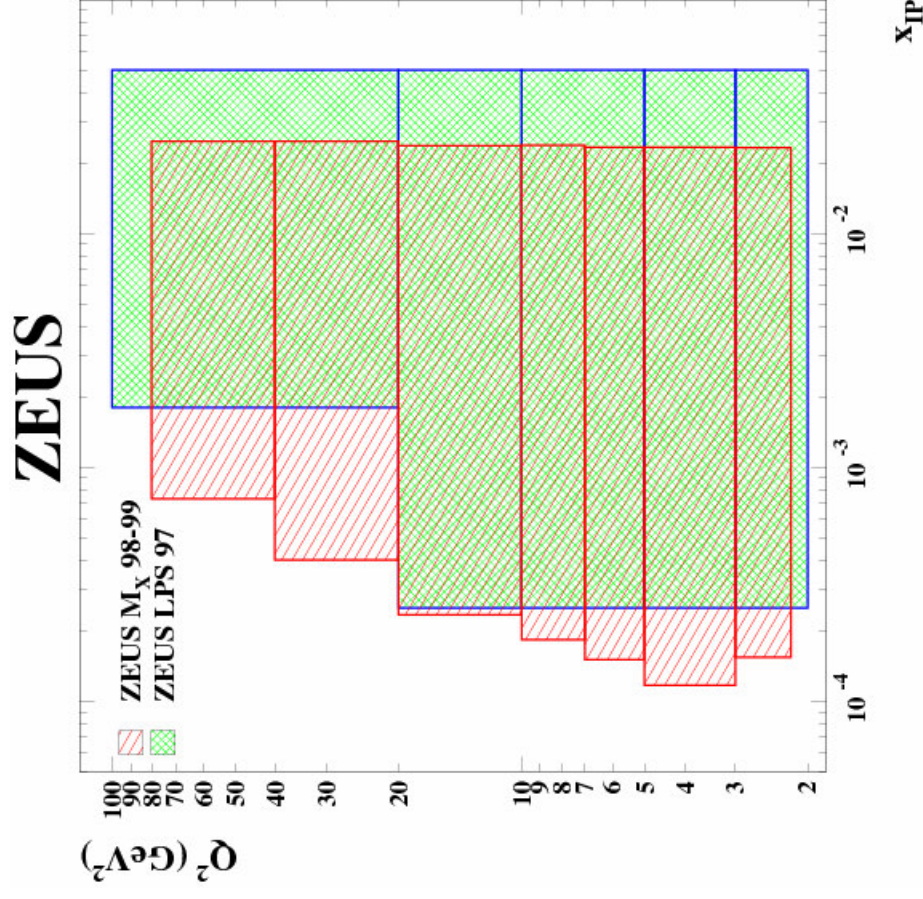
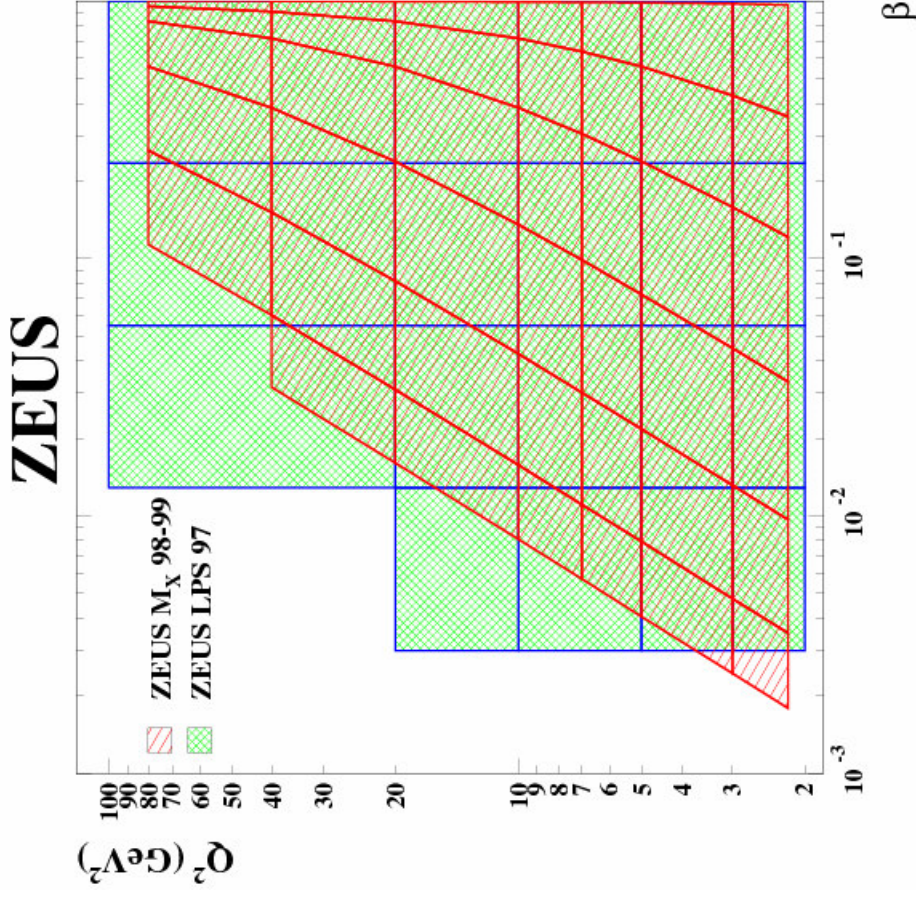
- ✓ No background from proton dissociation.
- ✓ Limited statistics due to geometrical acceptance.

$$d\sigma_{\gamma^* p \rightarrow XN}^{\text{diff}} / dM_X dt$$

Using 97 data

- $0.03 < Q^2 < 0.60 \text{ GeV}^2 \rightarrow 3.6 \text{ pb}^{-1}$
- $2 < Q^2 < 100 \text{ GeV}^2 \rightarrow 12.8 \text{ pb}^{-1}$
- $2.5 < W < 280 \text{ GeV}$
- $1.5 < M_X < 70 \text{ GeV}$
- $0 < |t| < 1 \text{ GeV}^2$

# Kinematical ranges



- **$M_X$  method** : Lower  $M_X$  region ( $\sim$  higher  $\beta$  region) and lower  $x_{IP}$  region.
- **LPS method** : Higher  $x_{IP}$  region

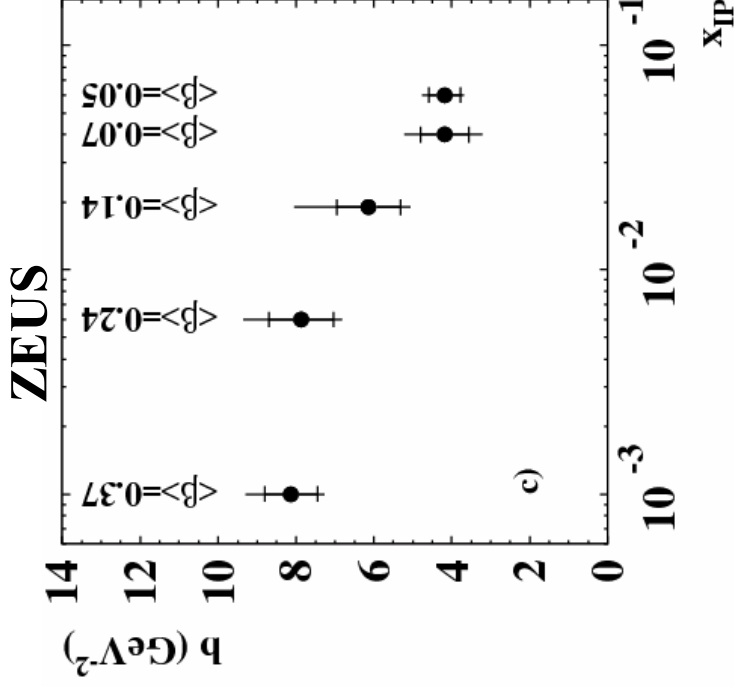
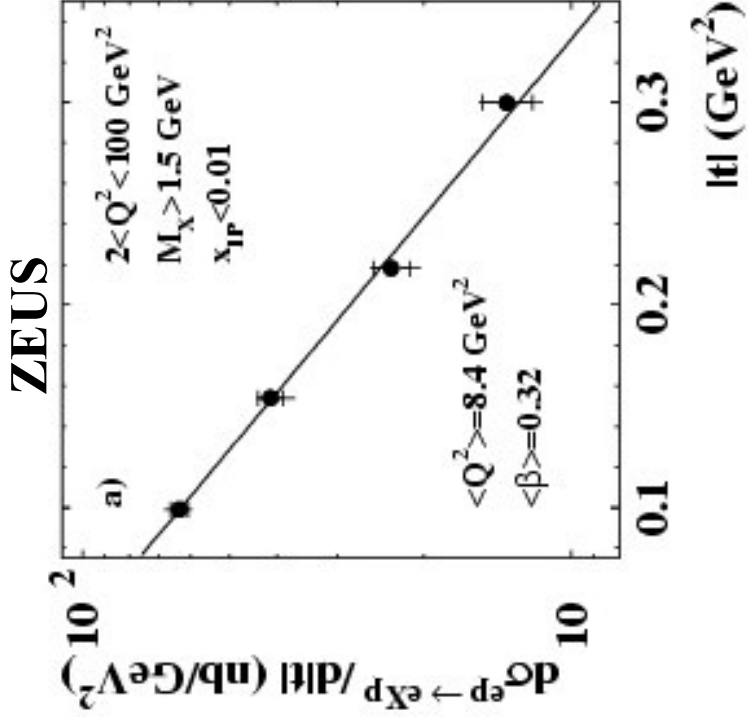
## Diffractive Cross Section

- **t dependence**
- **W dependence**  
→  $\alpha_{\text{IP}}^{\text{diff}}(0)$
- **$M_X$  dependence**
- $\sigma^{\text{diff}}/\sigma^{\text{tot}}$

## Diffractive Structure Function

- **$x_{\text{IP}}$  dependence**  
→  **$Q^2$  dependence**
- **Comparison with theory**
- **$\beta$  dependence**

# t dependence of Diffractive Cross Section (LPS)



• Fit  $t$  distribution to  $d\sigma/d|t| \propto \exp(-b|t|)$

$$b = 7.9 \pm 0.5 \text{ (stat.)}_{-0.5}^{+0.9} \text{ (syst.) GeV}^{-2}$$

→  $d\sigma/d|t|$  shows steep fall-off with  $t$  as in elastic hadron-hadron scattering.

- Regge phenomenology predicts “shrinkage” of the diffractive peak:

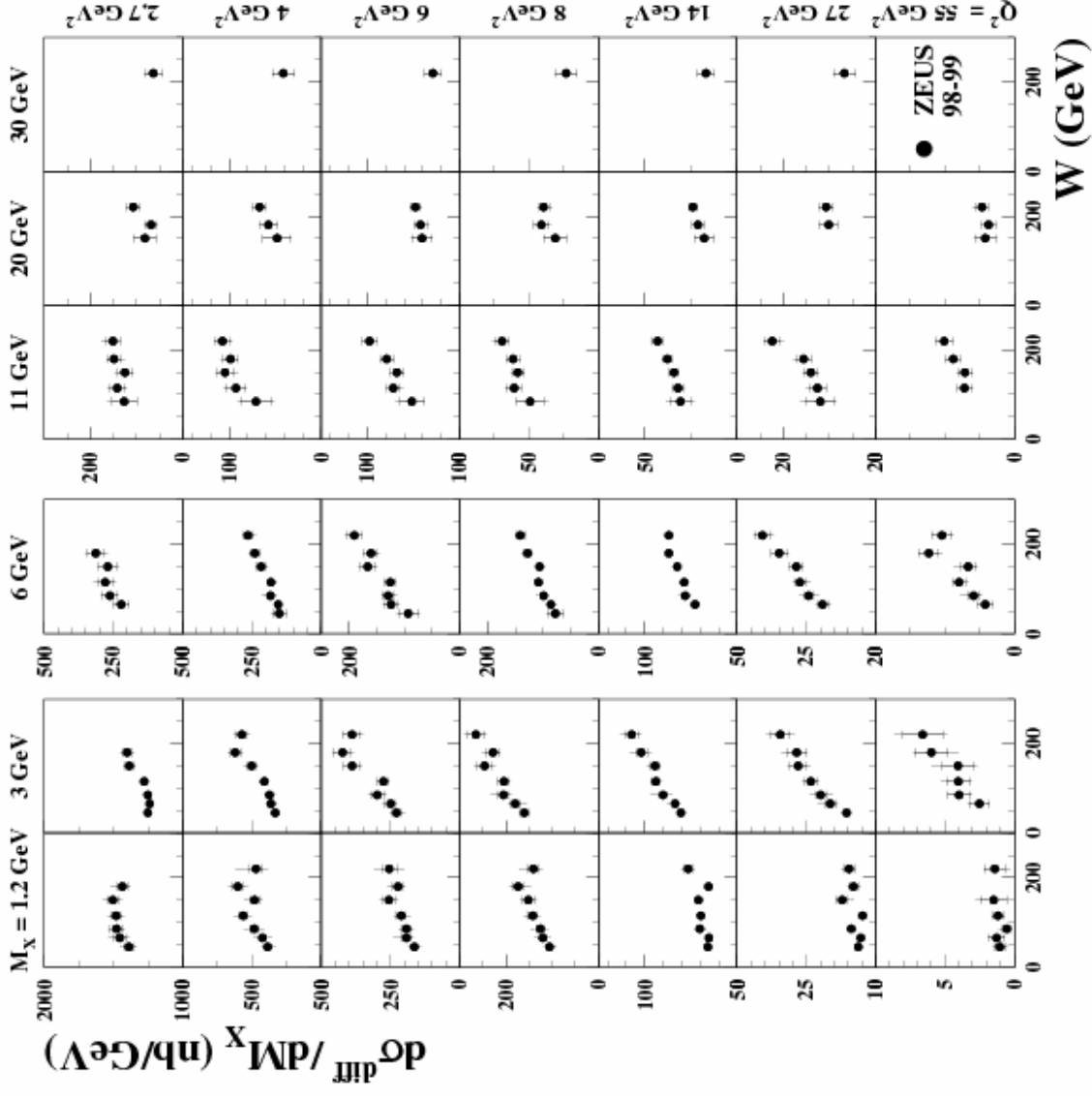
$$b = b_0 + 2\alpha' \ln \frac{W^2}{M_X^2} \approx b_0 + 2\alpha' \ln \frac{1}{x_{IP}}$$

- Additional  $\beta$  dependence expected in models.



# Diffractive Cross Section ( $M_X$ )

**ZEUS**



$$d\sigma_{\gamma^* p \rightarrow XN}^{\text{diff}}/dM_X, M_N < 2.3 \text{ GeV}$$

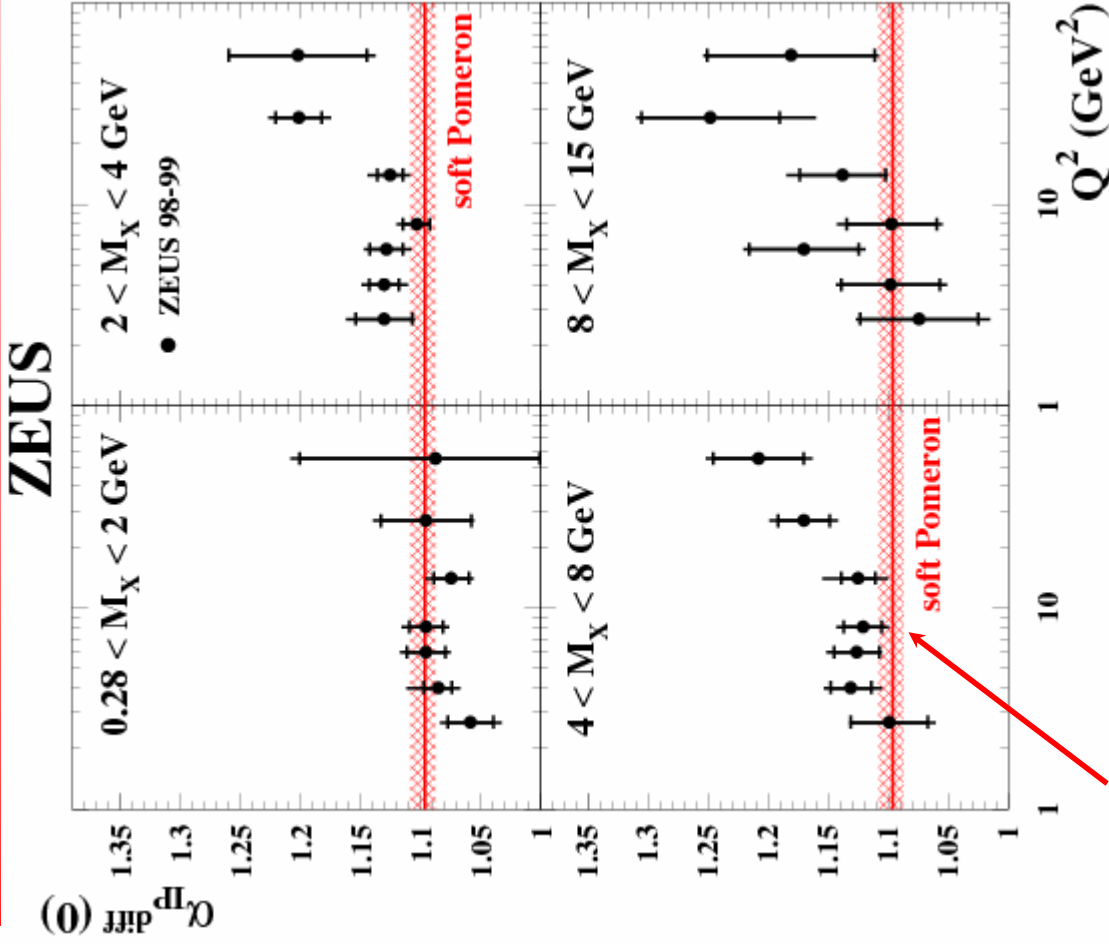
- For  $M_X < 2 \text{ GeV}$ ,

$d\sigma/dM_X$  depends weakly on  $W$ .

- For  $M_X > 2 \text{ GeV}$ ,

$d\sigma/dM_X$  rises rapidly with  $W$ .

# W dependence of Diffractive Cross Section



$\alpha_{IP}^{soft}(0) = 1.096_{-0.009}^{+0.012}$  from had-had scattering

- Fit to the diffractive cross section :

$$\frac{d\sigma_{\gamma p \rightarrow XN}^{diff}}{dM_X} = h \cdot W^{a^{diff}} \sim (W^2)^{(2\alpha_{IP}^{diff}-2)}$$

(h,  $a^{diff}$  free parameters)

Assuming  $d\sigma/dt \propto e^{b \cdot t}$  and

$$\alpha_{IP}(t) = \alpha_{IP}(0) + \alpha'_{IP} \cdot t$$

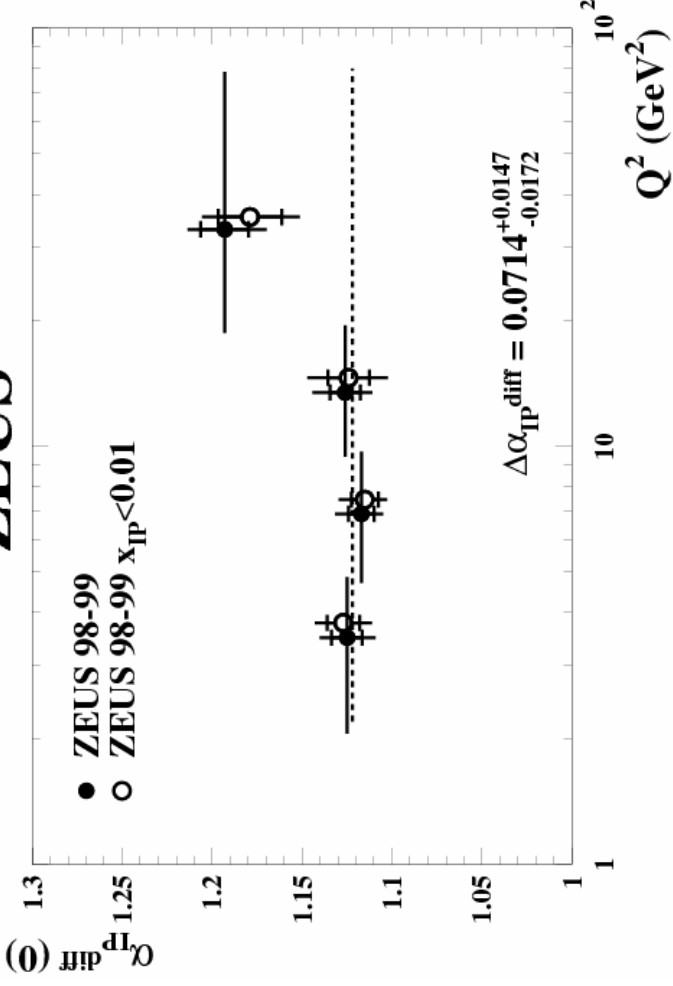
$$\therefore \alpha_{IP}(0) = \overline{\alpha_{IP}} + \alpha'_{IP}/b \approx (a^{diff}/4 + 1) + 0.03$$

from LPS  $\rightarrow$

- For  $M_X < 2 \text{ GeV}$ 
  - $\rightarrow \alpha_{IP}^{diff}(0)$  compatible with the soft Pomeron.
- For larger  $M_X$  and  $Q^2 > 20 \text{ GeV}^2$ 
  - $\rightarrow \alpha_{IP}^{diff}(0)$  lies above the results expected from soft Pomeron and increases with  $Q^2$ .

# Q<sup>2</sup> dependence of $\alpha_{\text{IP}}^{\text{diff}}(0)$

## ZEUS



- Fit to data with  $2 < M_X < 15 \text{ GeV}$

$$\Delta\alpha_{\text{IP}}^{\text{diff}} \equiv \alpha_{\text{IP}}^{\text{diff}}(0; 2.7 < Q^2 < 20 \text{ GeV}^2)$$

$$- \alpha_{\text{IP}}^{\text{diff}}(0; 20 < Q^2 < 80 \text{ GeV}^2)$$

$$= 0.0714 \pm 0.0140(\text{stat.})_{-0.0100}^{+0.0047}(\text{syst.})$$

- ✓  $\alpha_{\text{IP}}^{\text{diff}}(0)$  is rising with  $Q^2$ , with a significance of 4.2 s.d.
- ✓ Assuming single Pomeron exchange, this observation contradicts Regge factorisation.

- Fit to data with  $2 < M_X < 15 \text{ GeV}$  and  $x_{\text{IP}} < 0.01$

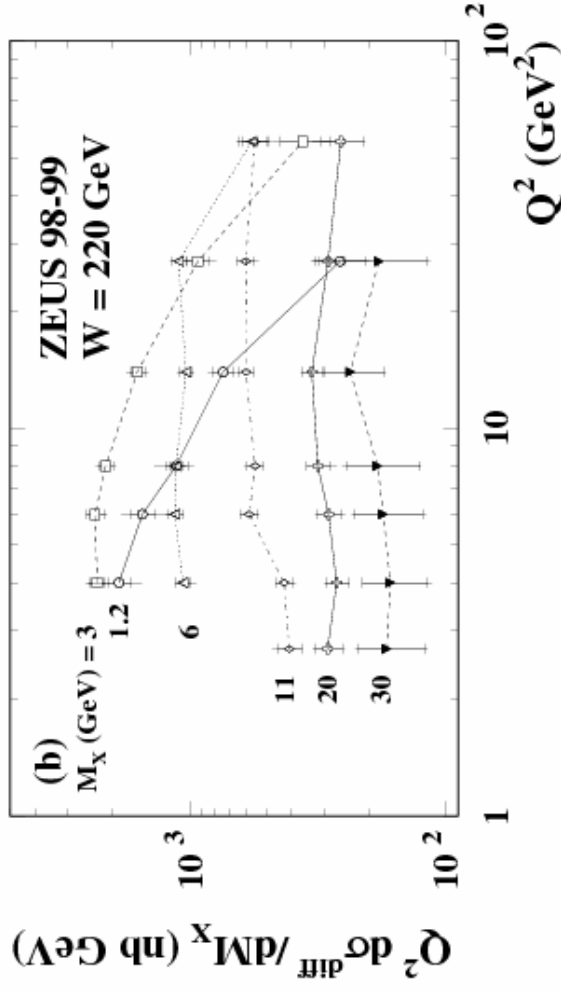
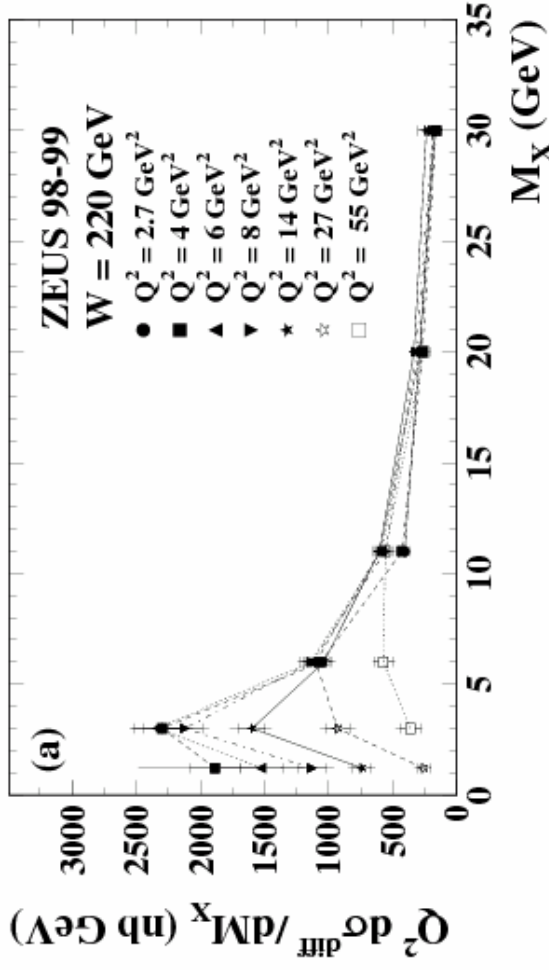
$$\alpha_{\text{IP}}^{\text{diff}}(0; 2.7 < Q^2 < 20 \text{ GeV}^2) = 1.1209 \pm 0.0051(\text{stat.})_{-0.0122}^{+0.0136}(\text{syst.})$$

$$\Delta\alpha_{\text{IP}}^{\text{diff}} \equiv 0.0578 \pm 0.0178(\text{stat.})_{-0.0118}^{+0.0081}(\text{syst.}) \leftarrow \text{Affected from the limited } x_{\text{IP}} \text{ range.}$$

$$\rightarrow \text{Consistent with LPS } \alpha_{\text{IP}}^{\text{diff}}(0; 0.03 < Q^2 < 39 \text{ GeV}^2) = 1.16 \pm 0.02(\text{stat.}) \pm 0.02(\text{syst.})$$

# $M_X$ dependence of diffractive cross section

## ZEUS



$$Q^2 \cdot \frac{d\sigma^{\text{diff}}}{dM_X} \text{ vs. } M_X \text{ at } W = 220 \text{ GeV}$$

- For  $M_X < 4 \text{ GeV}$ ,

rapid decrease with  $Q^2$ .

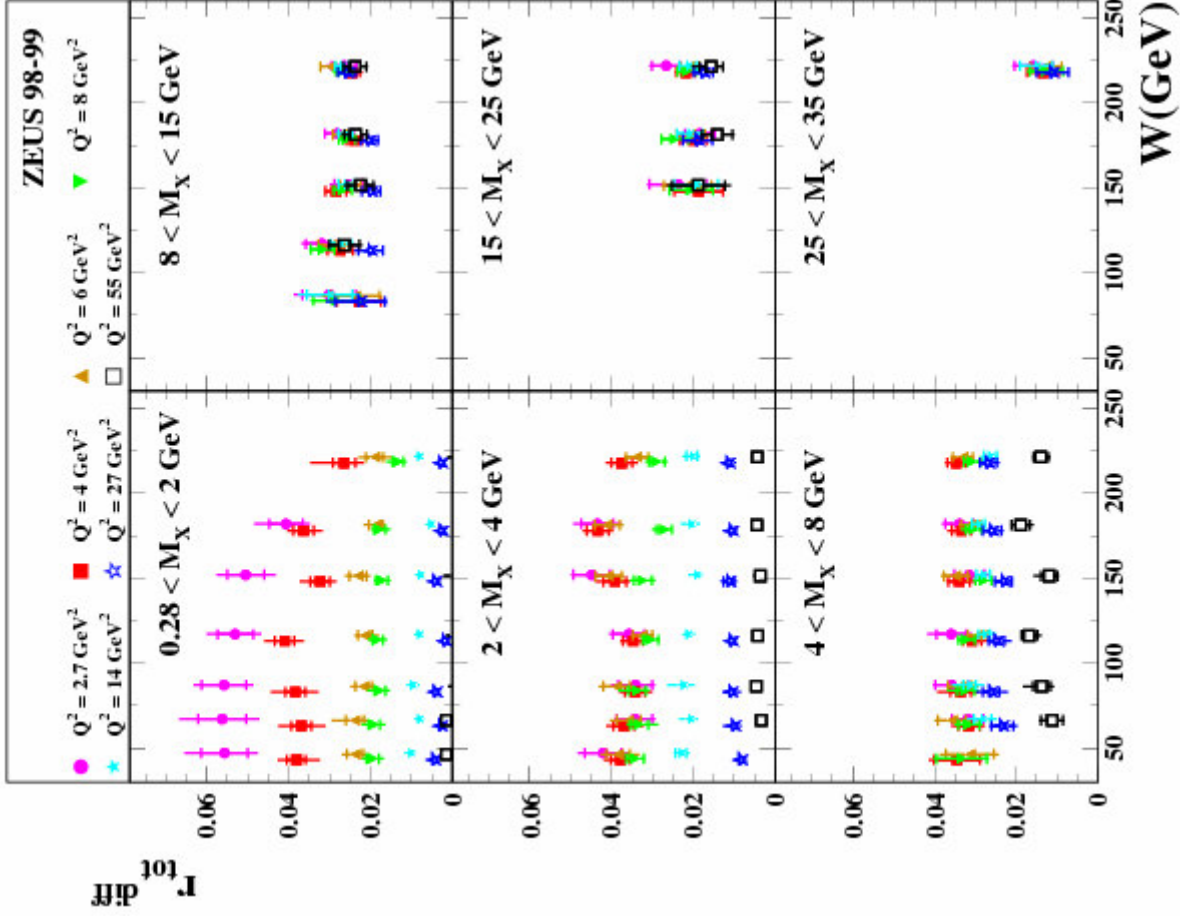
→ predominantly higher twist.

- For  $M_X > 10 \text{ GeV}$ ,

constant or slow rise with  $Q^2$

→ leading twist.

# Diffraction contribution of the total cross section



$$r_{\text{tot}}^{\text{diff}} = \frac{\int_{M_a}^{M_b} dM_X d\sigma_{\gamma p \rightarrow \text{XN}, M_N < 2.3 \text{ GeV}}^{\text{diff}}}{\sigma_{\gamma p}^{\text{tot}}}$$

- For  $M_X < 2 \text{ GeV}$ , falling with  $W$ .
- For  $M_X > 2 \text{ GeV}$ , constant with  $W$ .
- For  $M_X < 2 \text{ GeV}$ , decreasing with rising  $Q^2$ .
- For  $M_X > 8 \text{ GeV}$ , no  $Q^2$  dependence.

→ For larger  $M_X$ ,  $\sigma^{\text{diff}}$  has the similar  $W$  and  $Q^2$  dependences as  $\sigma^{\text{tot}}$ .

- For the highest  $W$  bin ( $200 < W < 245 \text{ GeV}$ ),  $\sigma^{\text{diff}} (0.28 < M_X < 35 \text{ GeV}, M_N < 2.3 \text{ GeV}) / \sigma^{\text{tot}}$   
 $15.8_{-1.0}^{+1.2} \%$  at  $Q^2 = 4 \text{ GeV}^2$   
 $9.6_{-0.7}^{+0.7} \%$  at  $Q^2 = 27 \text{ GeV}^2$

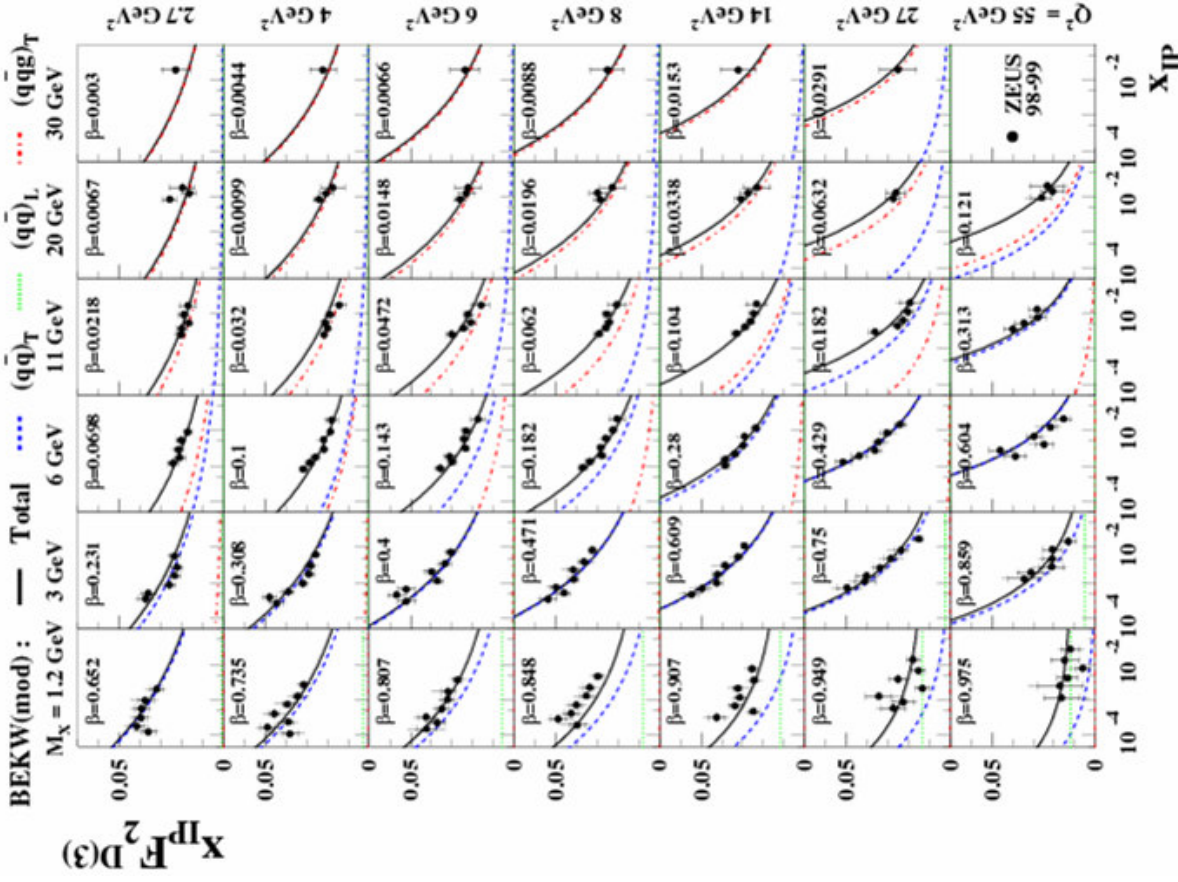
## Diffractive Cross Section

- **t dependence**
- **W dependence**  
→  $\alpha_{\text{IP}}^{\text{diff}}(0)$
- **$M_X$  dependence**
- $\sigma^{\text{diff}}/\sigma^{\text{tot}}$

## Diffractive Structure Function

- **$x_{\text{IP}}$  dependence**  
→  **$Q^2$  dependence**
- **Comparison with theory**
- **$\beta$  dependence**

# Diffractive structure function of the proton



- For  $M_X < 2 \text{ GeV}$ ,  $x_{\text{IP}} F_2^{D(3)}$  is constant with  $x_{\text{IP}}$ .
- For  $M_X > 2 \text{ GeV}$ , rapid increase as  $x_{\text{IP}} \rightarrow 0$ .

- Data are compared with the color dipole model in BEKW parametrisation.

(Bartels, Ellis, Kowalski and Wüsthoff)

$$x_{\text{IP}} F_2^{D(3)} = c_T \cdot F_{q\bar{q}}^T + c_L \cdot F_{q\bar{q}}^L + c_g \cdot F_{q\bar{q}g}^T$$

$$F_{q\bar{q}}^T \propto \beta(1 - \beta)$$

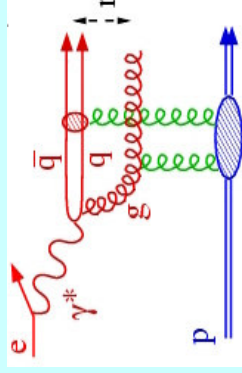
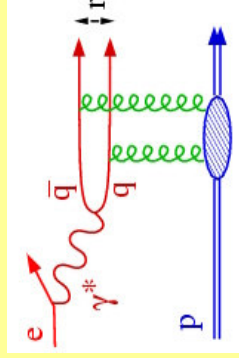
**dominates at  $\beta > 0.15$**

$$F_{q\bar{q}}^L \propto \beta^3(1 - 2\beta)^2$$

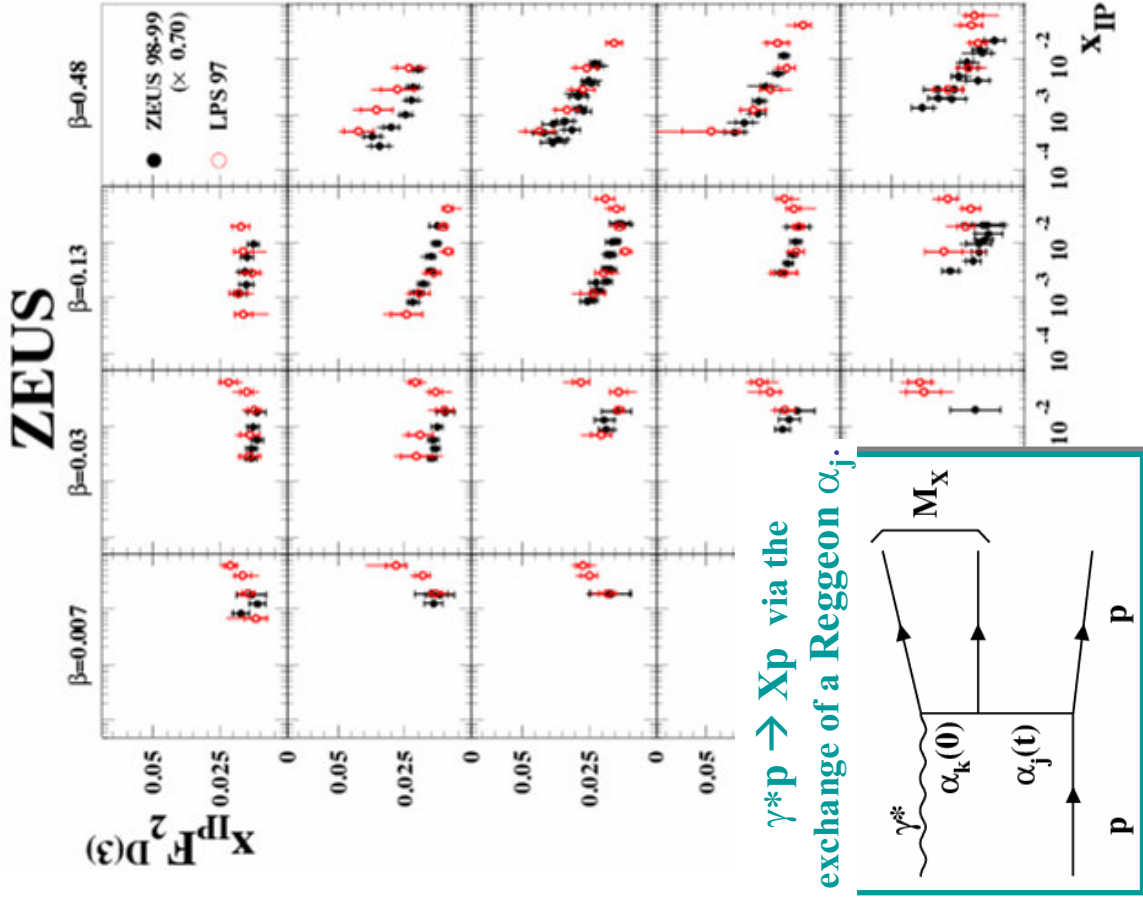
**substantial at large  $\beta$**

$$F_{q\bar{q}g}^T \propto (1 - \beta)^\gamma$$

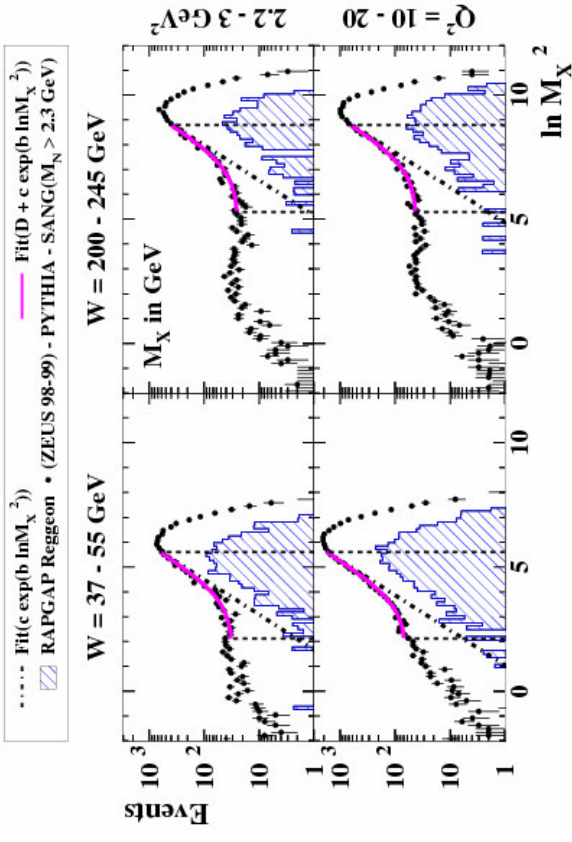
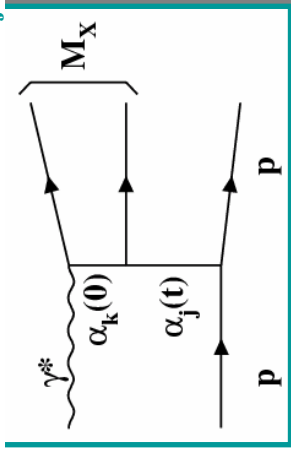
**dominates at small  $\beta$**



# Comparison of LPS and $M_X$ method



$\gamma^* p \rightarrow Xp$  via the exchange of a Reggeon  $\alpha_j$ .



$$\frac{d\sigma_{\text{Reggeon}}^*}{d \ln M_X^2} \propto \exp(1 + \alpha_k(0) - 2\bar{\alpha}_j) \cdot \ln M_X^2$$

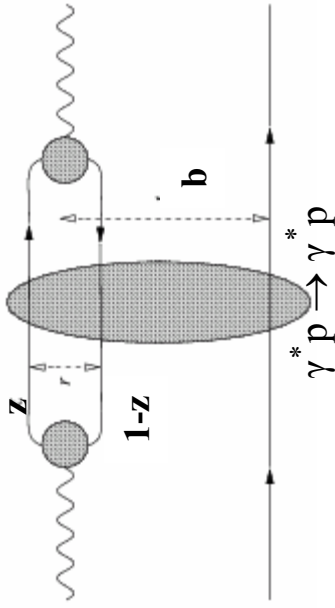
$$\propto \exp(b_{\text{IR}} \cdot \ln M_X^2) \text{ with } b_{\text{IR}} = 1$$

•  $M_X$  method suppresses the Reggeon contributions.

• Good agreement between LPS and  $M_X$  method ( $\times 0.7$  for  $M_N < 2.3 \text{ GeV}$ ) except for the region of  $x_{IP} > 0.01$  where Reggeon contributions may dominate LPS.



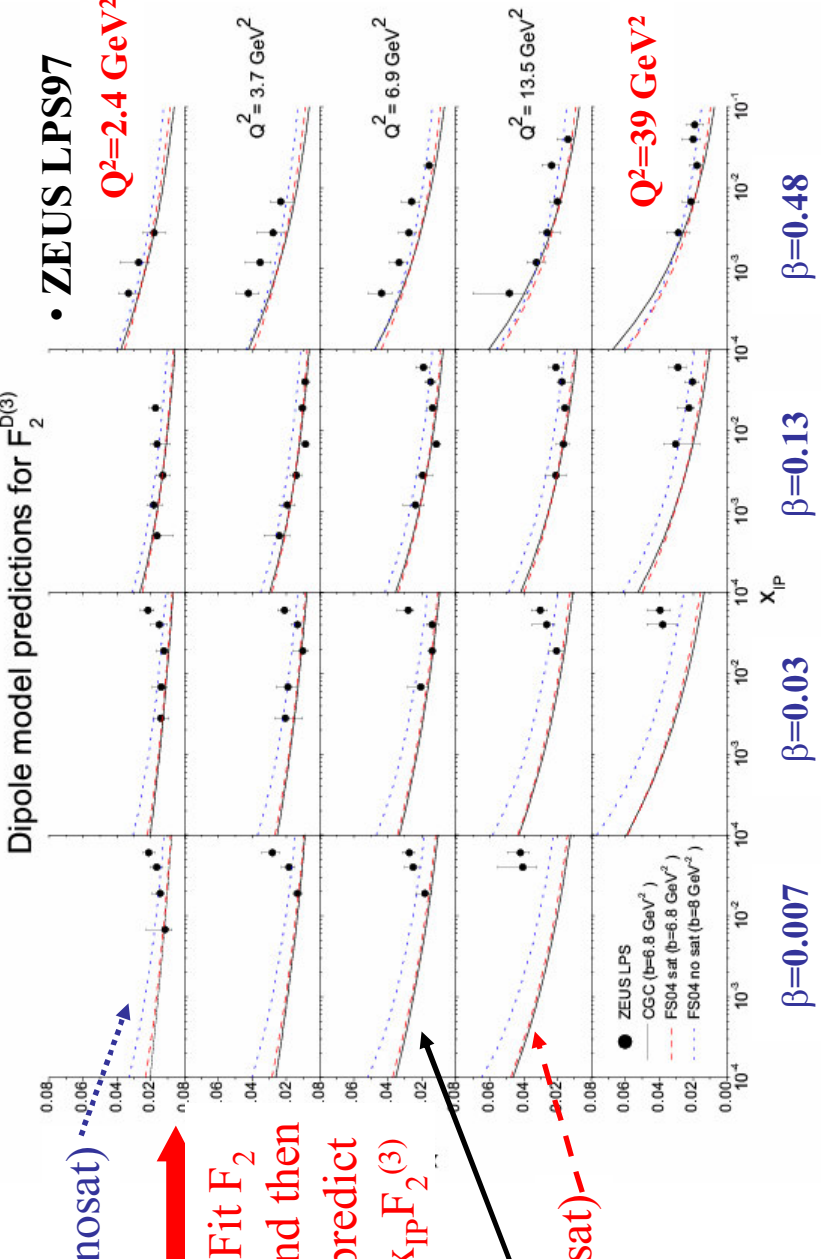
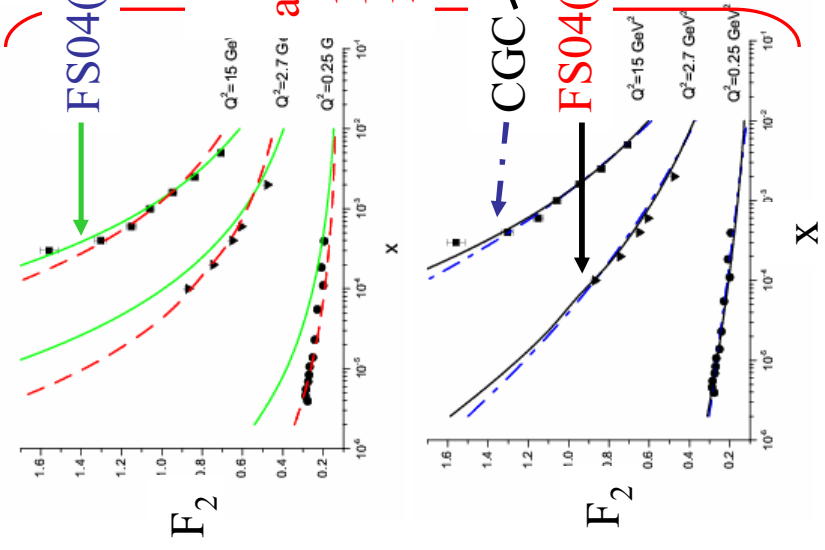
# Comparison with Colour Dipole Model - I



J.D. Bjorken, M. Mistry, J. Kogut, D. Soper, N.N. Nikolaev, B.G.Zakharov, M. Genovese, M. Bertini, A.H. Mueller, K. Golec-Biernat, M. Wüsthoff, H. Kowalski, A. Stasto, J. R. Forshaw, G. Kerley, G. Shaw, E. Iancu, K. Itakura, S. Munier .....

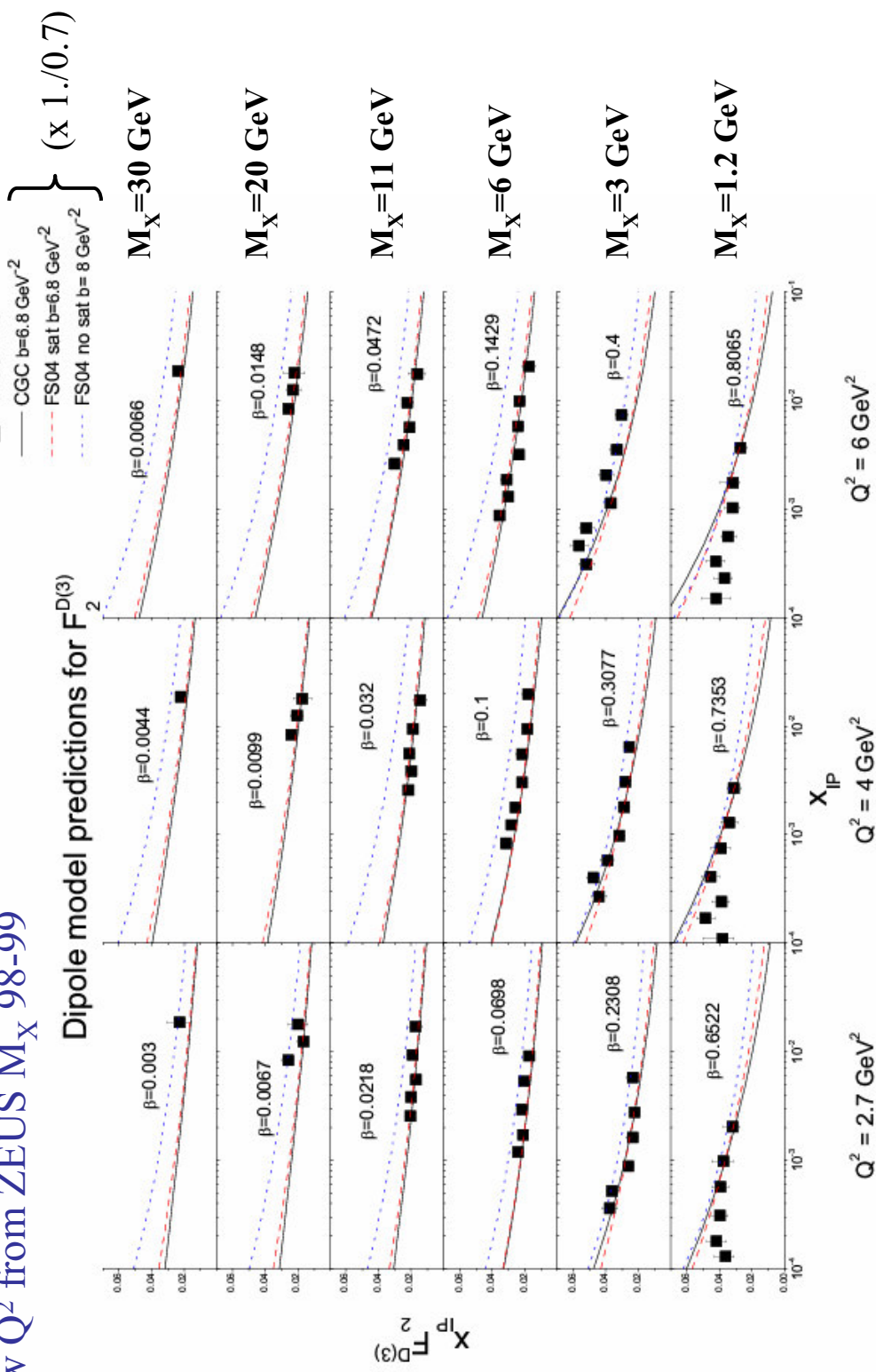
**Comparison with FS04(Forshaw & Shaw) Regge dipole model with/without saturation and CGC(Colour Glass Condensate) model → Refer to hep-ph/0411337.**

*Thanks to J. Forshaw.*



# Comparison with Colour Dipole Model - II

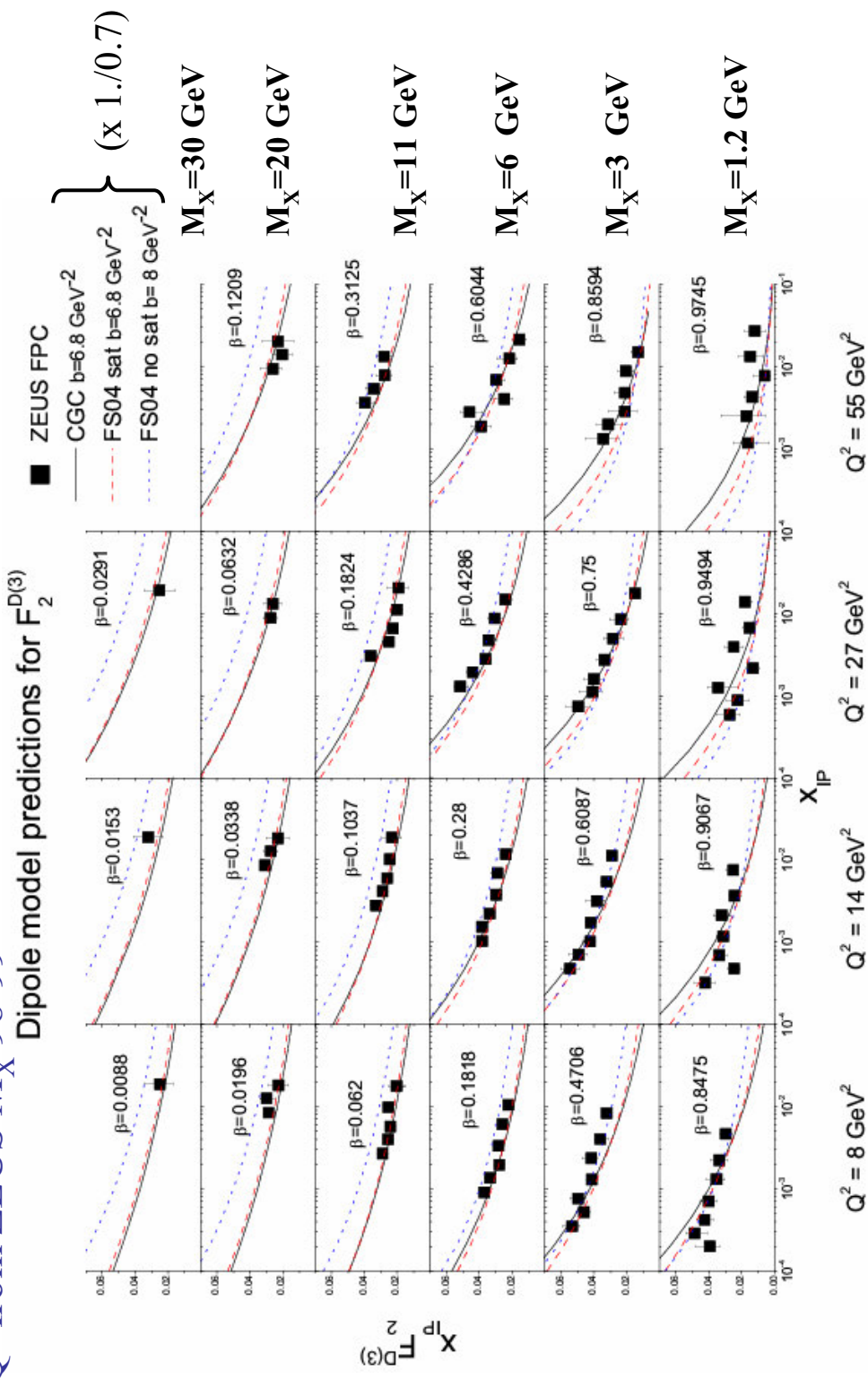
Low  $Q^2$  from ZEUS  $M_X$  98-99



→ Predictions of model are corrected by  $1/0.7$  for the  $M_N < 2.3 \text{ GeV}$  of ZEUS  $M_X$  method.

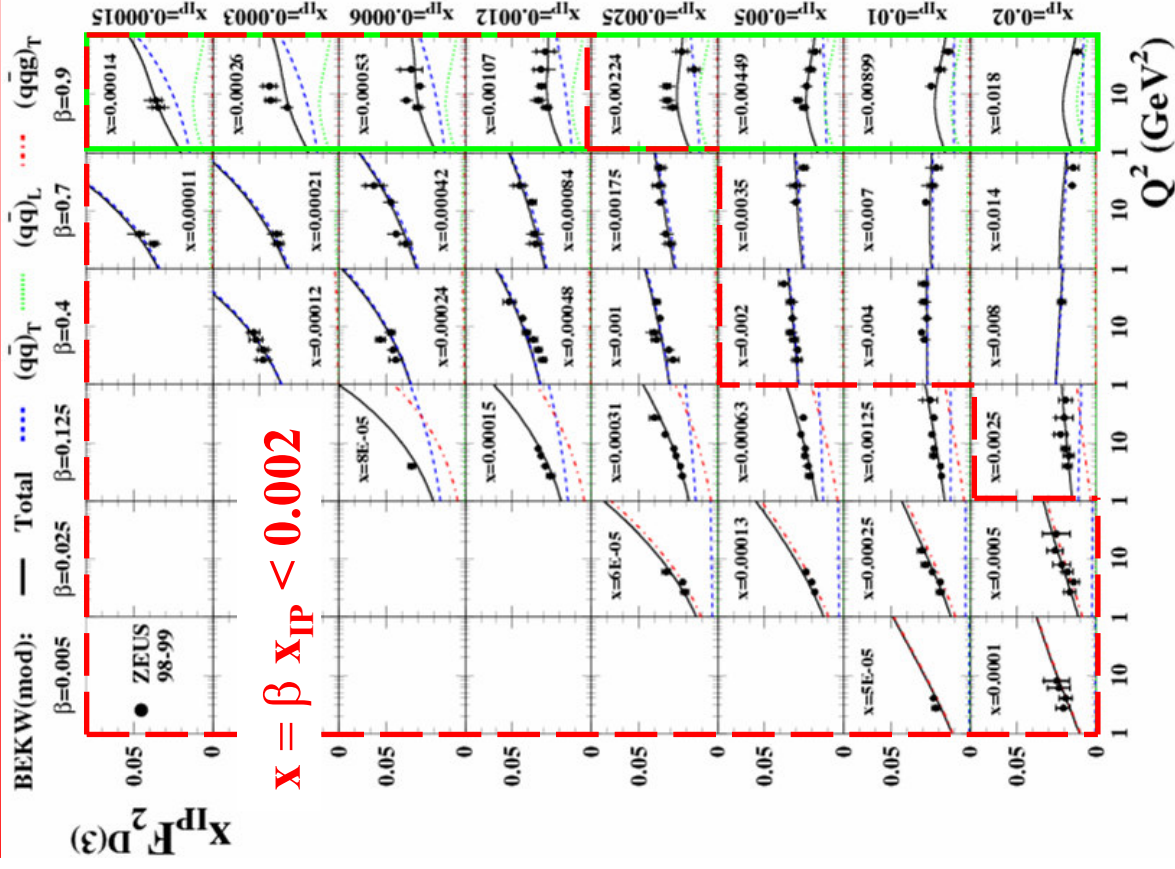
# Comparison with Colour Dipole Model - III

High  $Q^2$  from ZEUS  $M_X$  98-99



- CGC and FS04(sat) are able simultaneously to describe  $F_2$  and  $x_{IP}F_2D^{(3)}$ .
- Forshaw & Shaw have not been able to find a good fit which does not invoke saturation.

# $Q^2$ dependence of $x_{\text{IP}} F_2^{\text{D}(3)}$



- For  $\beta=0.9$

(dominated events with  $M_X < 2$  GeV),  
 → Constant or slowly decreasing with  $Q^2$ .  
 Expect higher twist effect from  $(q\bar{q})_L$ .

- For  $\beta \leq 0.7$  and  $x = \beta x_{\text{IP}} < 0.002$ ,  
 $x_{\text{IP}} F_2^{\text{D}(3)}$  increases with increasing  $Q^2$ .

→ **Positive scaling violations.**

Suggest perturbative effects such as  
 gluon emission

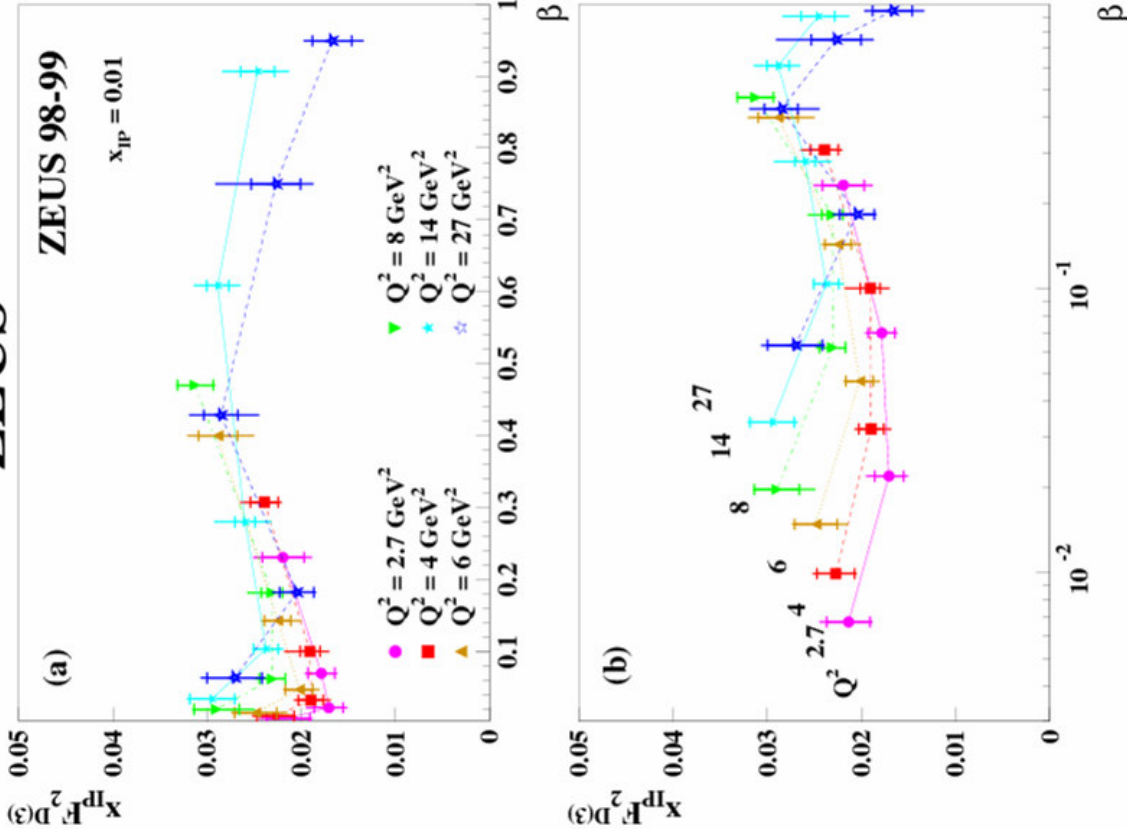
- For fixed  $\beta$ ,

$Q^2$  dependence of  $x_{\text{IP}} F_2^{\text{D}(3)}$  changes with  $x_{\text{IP}}$ .

→ **Inconsistent with the Regge factorisation hypothesis**

# $\beta$ dependence of $x_{\text{IP}} F_2^{D(3)}$ at $x_{\text{IP}}=0.01$

## ZEUS



- $x_{\text{IP}} F_2^{D(3)}$  for  $x_{\text{IP}}=x_0=0.01$   
 $\rightarrow$  expect this to represent the structure function of Pomeron, up to a normalisation constant.

- **For  $\beta > 0.1$**

- $x_{\text{IP}} F_2^{D(3)}$  has a maximum around  $\beta=0.5$ .  
 $\rightarrow$  The  $\beta(1-\beta)$  dependence observed is expected in dipole models of diffraction by  $\gamma^* \rightarrow q\bar{q}$  splitting and two gluon exchange.

- **For  $\beta < 0.1$**

- $x_{\text{IP}} F_2^{D(3)}$  rises as  $\beta \rightarrow 0$  and the rise accelerates with growing  $Q^2$ .  
 $\rightarrow$  Similar to the **logarithmic scaling violation of  $F_2$  at low  $x$**  due to QCD evolution.

# Summary

## • The measurements of diffraction in DIS with $M_X$ method and with a leading proton show :

- ✓ Slope of  $d\sigma/d|t|$  is compatible with soft interaction at the proton vertex.
- ✓ Indication for **Regge factorisation breaking** seen in
  - $Q^2$  dependence of  $\alpha_{\text{IP}}^{\text{diff}}(0)$
  - $Q^2$  dependence of  $x_{\text{IP}} F_2^{D(3)}$  for fixed  $\beta$  and fixed  $x_{\text{IP}}$
- ✓ Diffractive contribution of the total cross section

|  |   |   |
|--|---|---|
| $\sigma^{\text{diff}}/\sigma^{\text{tot}}$       | $M_X < 2 \text{ GeV}$<br><i>Decreasing with <math>W</math></i>    | <b>Higher <math>M_X</math></b><br><i>Constant with <math>W</math></i> |
| $\leftarrow \alpha_{\text{IP}}^{\text{diff}}(0)$ | No $Q^2$ dependence<br>Soft Pomeron                               | $Q^2$ dependence<br>Breaking of single Pomeron exchange               |
| $\sigma^{\text{diff}}/\sigma^{\text{tot}}$       | <i>Decreasing with <math>Q^2</math></i><br>Higher twist behaviour | <i>Constant with <math>Q^2</math></i><br>Leading twist behaviour      |
| $\leftarrow Q^2 \sigma^{\text{diff}}$            |   |   |

- ✓ Diffraction shows evidence for **pQCD evolution with  $Q^2$  as  $x_{\text{IP}} \rightarrow 0$  or  $\beta \rightarrow 0$** .
- ✓ Data can be described by color dipole model (BEKW, GBW, FS04, CGC .....).

## • Expect new diffractive results with high statistics for an extended kinematic range (especially $Q^2 < 500 \text{ GeV}^2$ ) soon.