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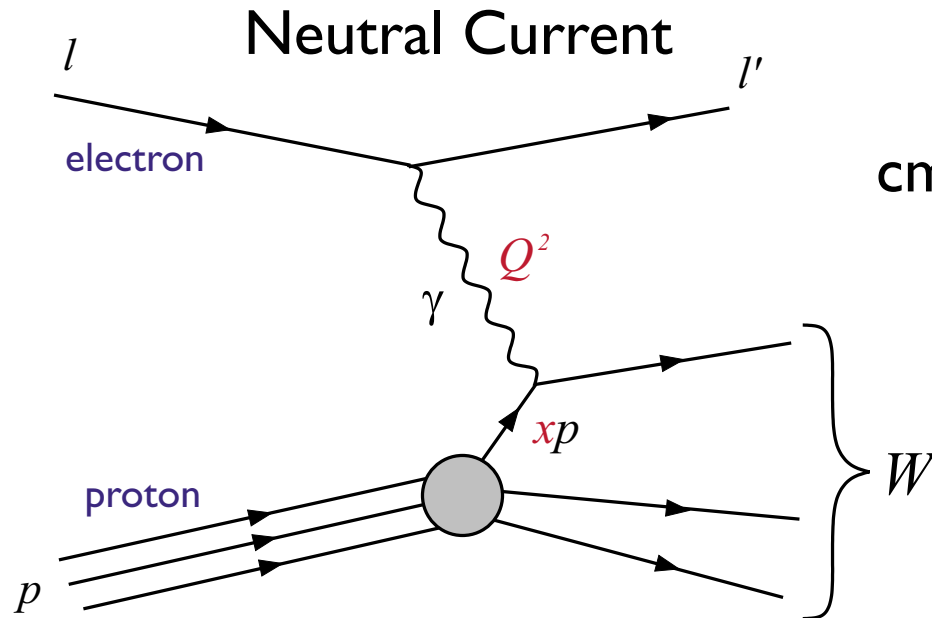
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HI Collaboration

## Measurements of Proton Structure Functions at Low $Q^2$ at HERA

- Deep Inelastic Scattering at HERA
- Measurements of  $F_2$  in Shifted Vertex and Radiative Events
- Extraction of  $F_L$

**LOW-X**  
Prague, 15.09.04

# Deep Inelastic Scattering



cms energy  $\sqrt{s} = \sqrt{(l + p)^2} \approx 300 \text{ GeV}$

photon virtuality  $Q^2 = -(l - l')^2$

Bjorken variable  $x = \frac{Q^2}{2p \cdot (l - l')}$

Inelasticity  $y \approx \frac{Q^2}{xs}$

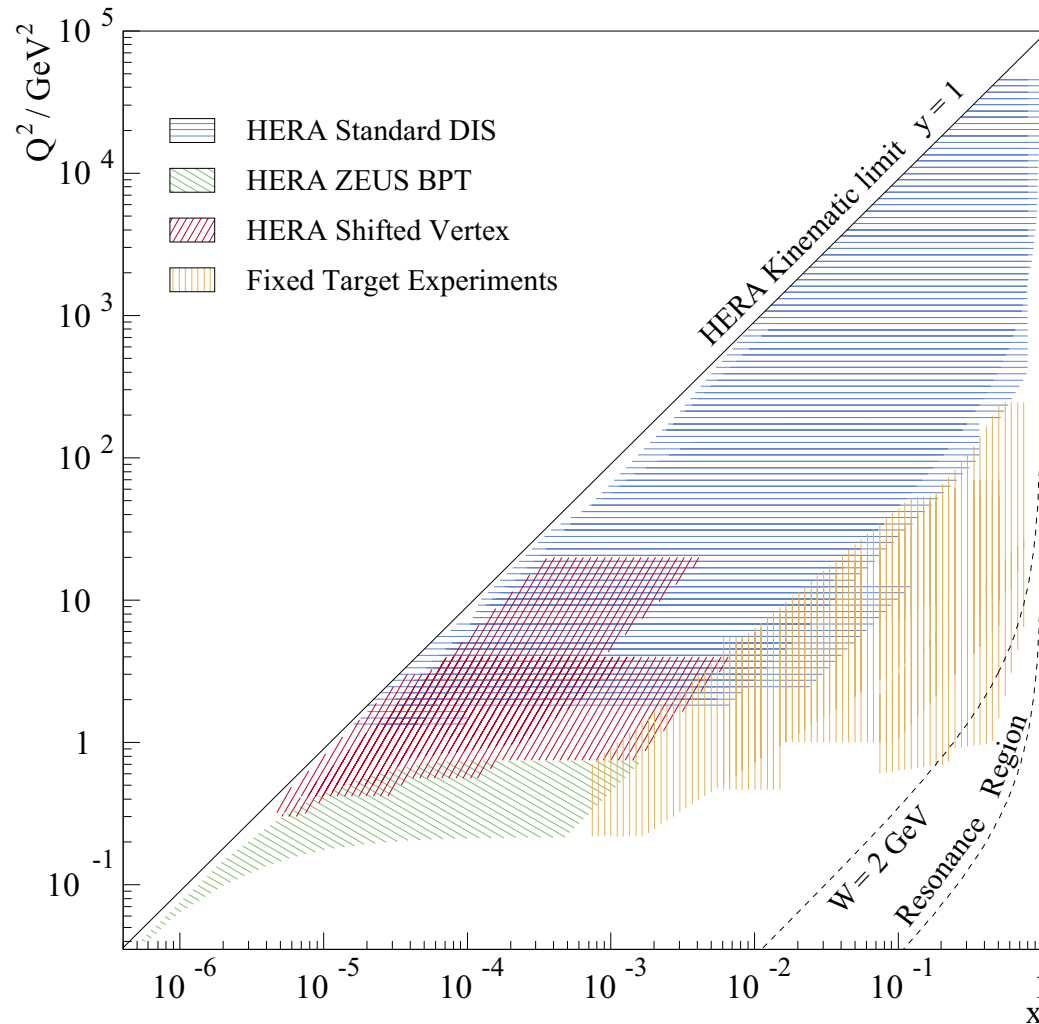
Invariant mass of the  $W = \sqrt{Q^2 \frac{1-x}{x} + m_p^2}$

# Structure Functions in DIS

$$\frac{d^2\sigma}{dx dQ^2} = \frac{2\pi\alpha^2}{Q^4 x} (Y_+ F_2(x, Q^2) - y^2 \cdot F_L(x, Q^2)) \quad Y_+ = 1 + (1-y)^2$$

- $F_2(x, Q^2) = x \sum_i e_i^2 [q_i(x, Q^2) + \bar{q}_i(x, Q^2)]$ 
  - dominant contribution
  - sensitive to quark content  
[indirect sensitivity to gluon density via scaling violation]
- $F_L(x, Q^2)$ 
  - contributes significantly only at high  $y$
  - QPM:  $F_L = 0$
  - QCD:  $F_L \propto \alpha_S g$
  - directly sensitive to gluon density

# Accessible Phase Space



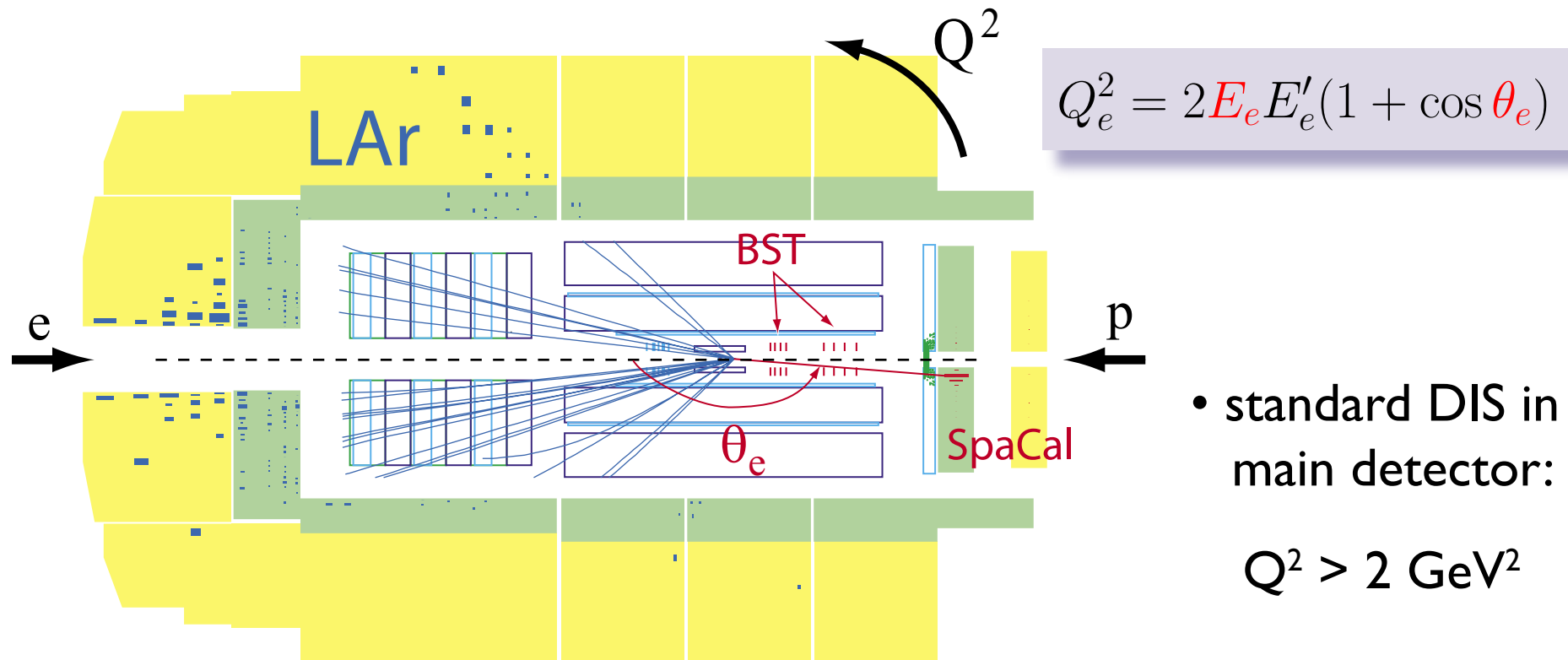
## Medium-high $Q^2$ :

- asymptotic freedom
- perturbative QCD

## Low $Q^2$ :

- transition to soft hadronic physics
- $\alpha_s(Q^2)$  becomes large
- phenomenological models

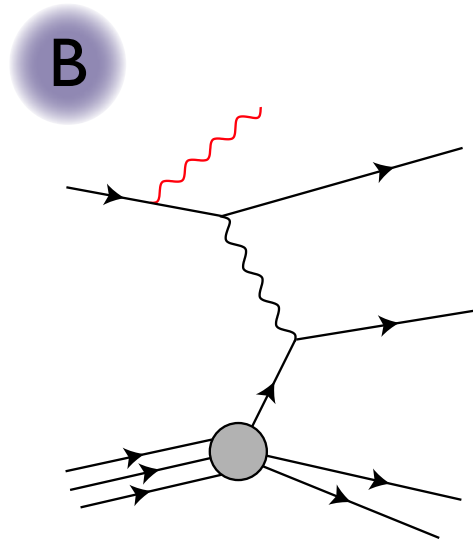
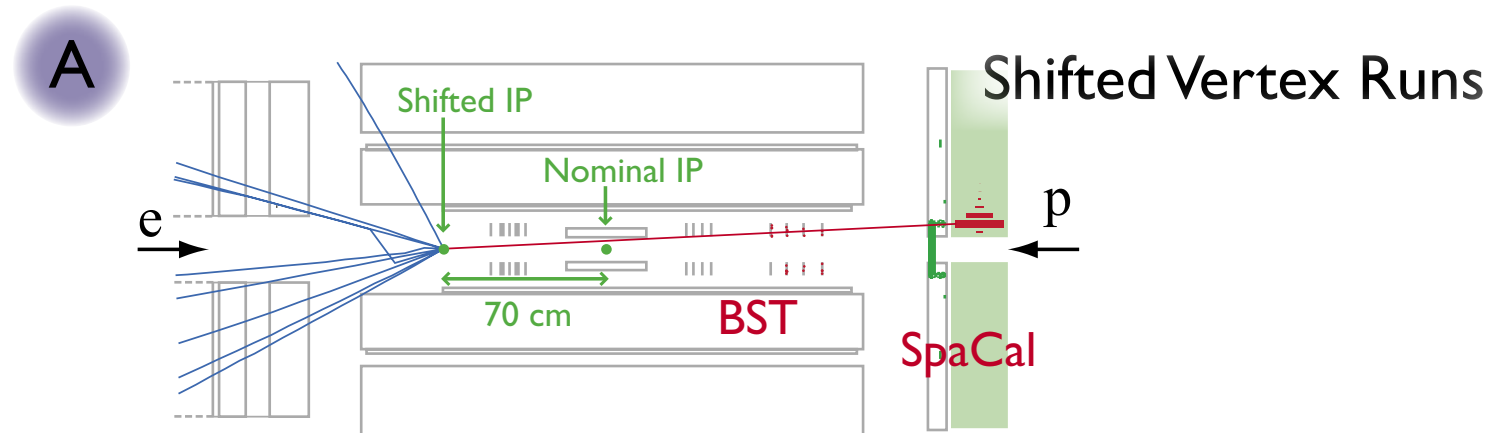
# Experimental Techniques at Low $Q^2$



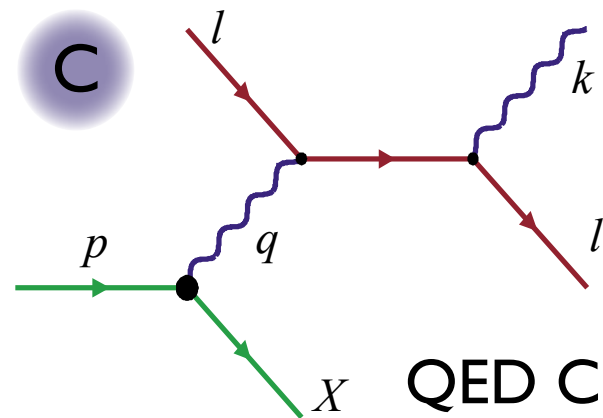
*Possibilities to access lower  $Q^2$ :*

- larger polar angles
- lower initial electron energy

# Experimental Techniques at Low $Q^2$

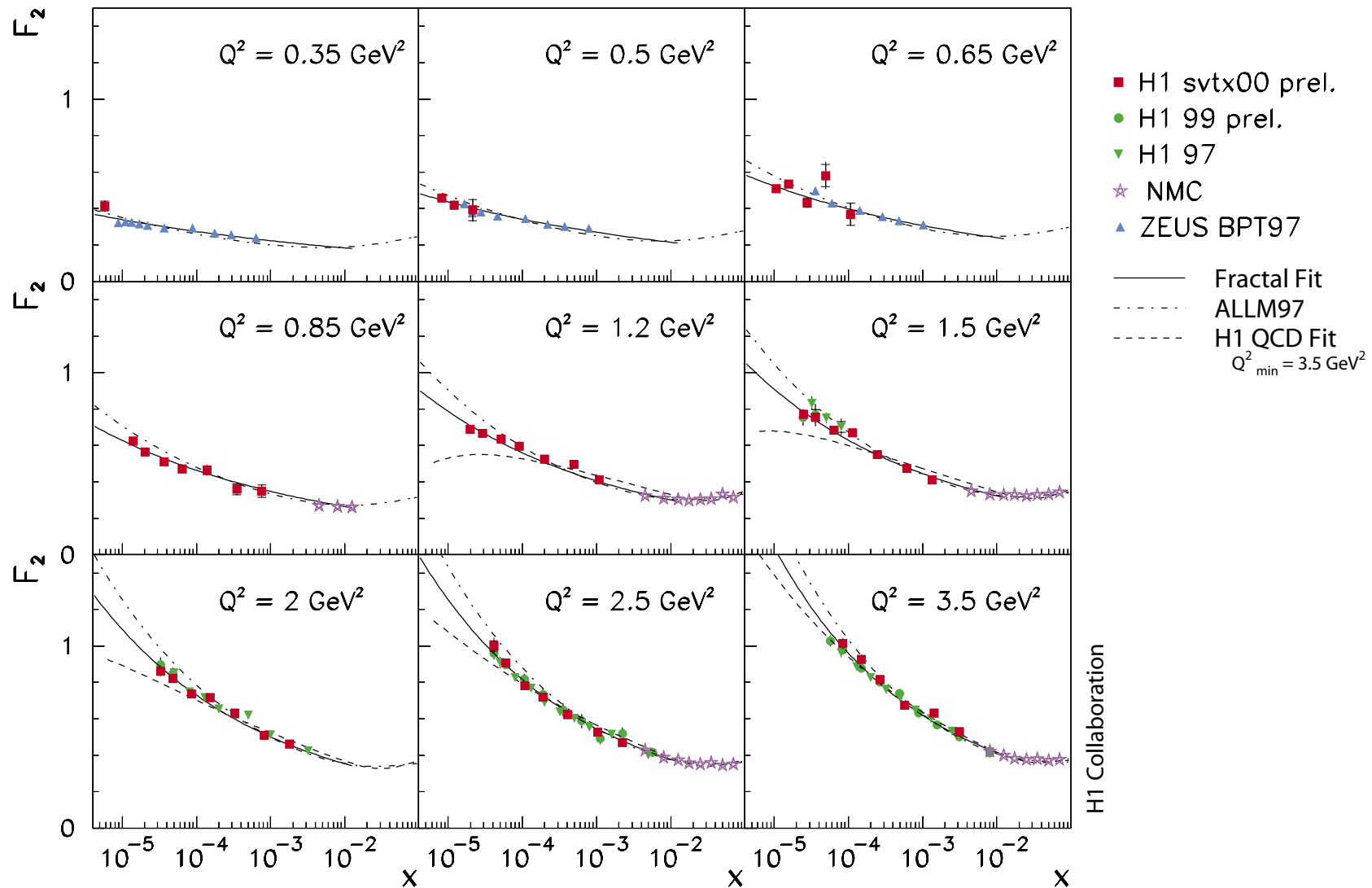


Initial State Radiation (ISR)

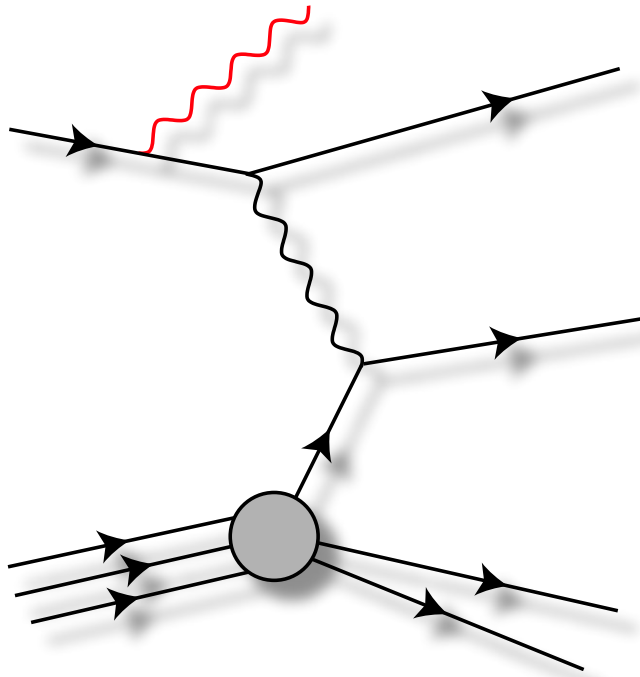


QED Compton (QEDC)

# Shifted Vertex and Previous Results at low $Q^2$



# Initial State Radiation (ISR)



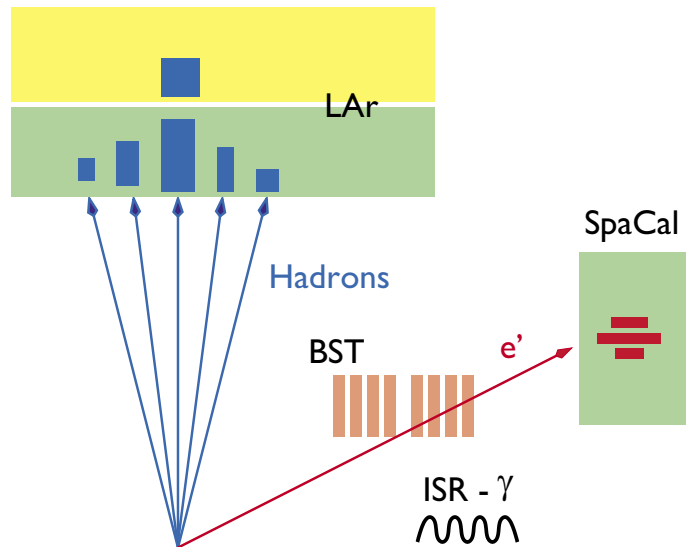
- $\gamma$  is radiated from incoming e
- equivalent to inclusive DIS at reduced  $s = 4E_e E_p$
- $Q^2 = sxy$   
 $\Rightarrow$  higher x at fixed  $Q^2$

*Previous measurements:*

- $\gamma$  directly detected



# Untagged ISR in Shifted Vertex (HI)

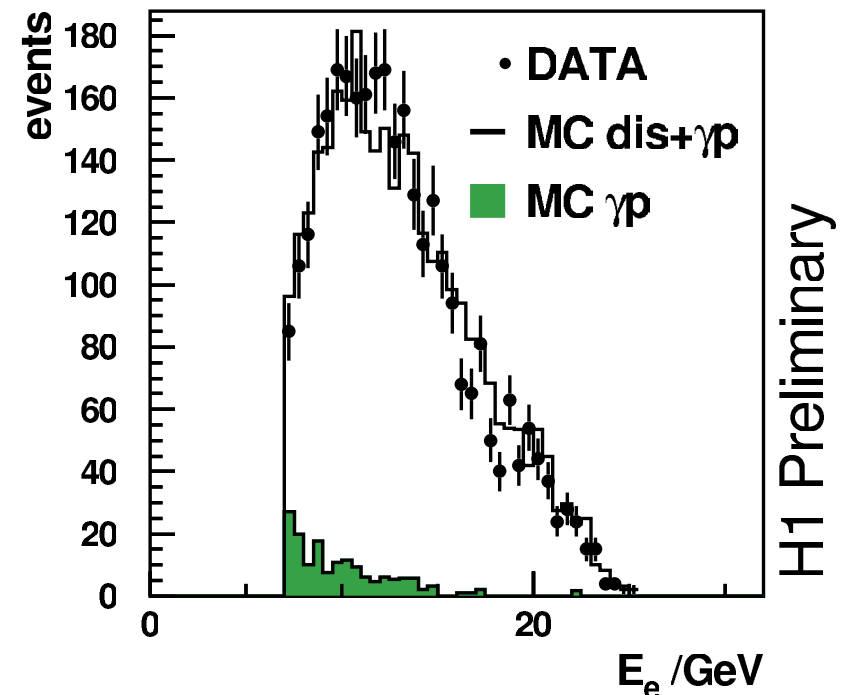


- $\gamma$  is undetected
- $\gamma p$  background rejected by BST

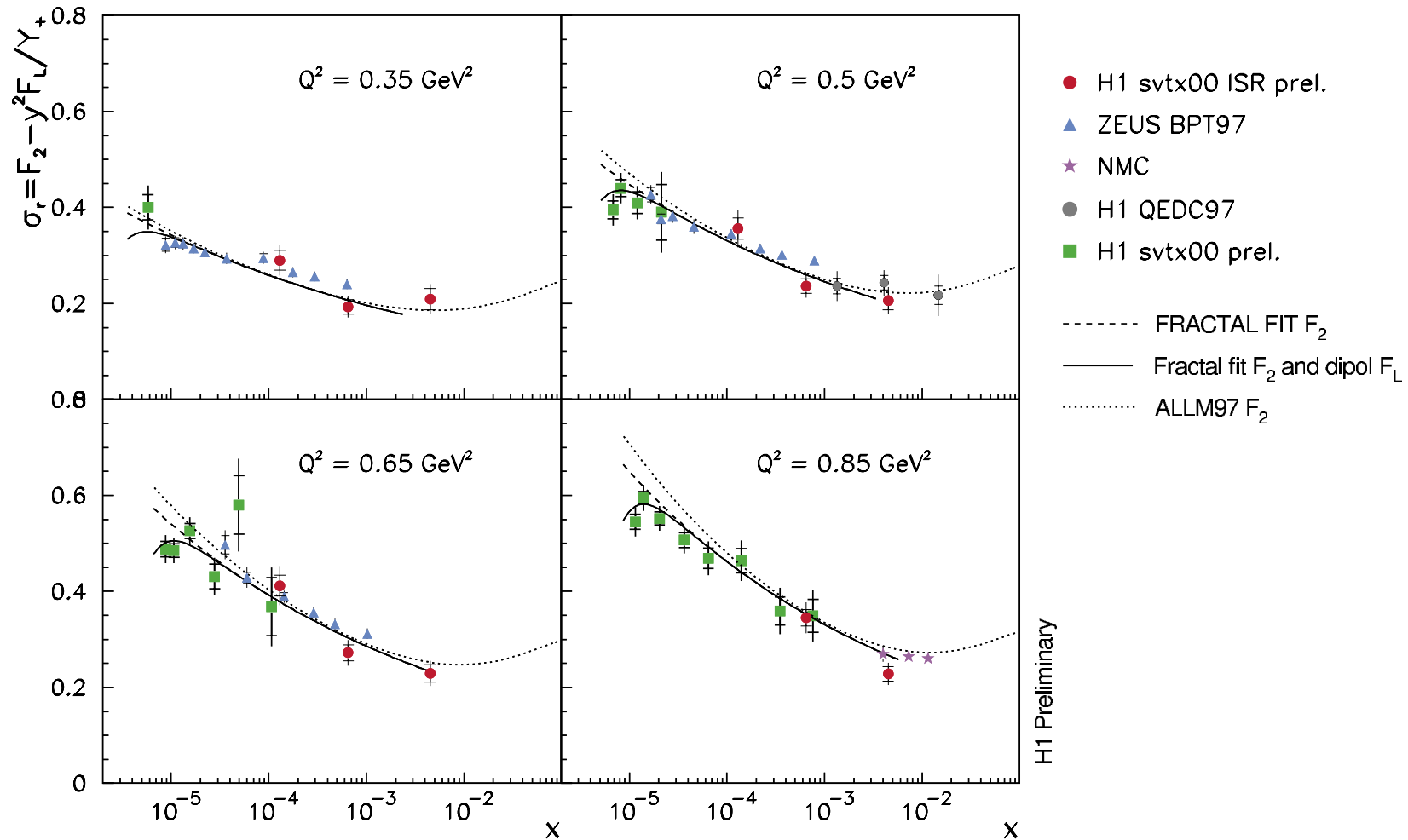
## Kinematics:

- $E - p_z$  is used to determine initial electron energy

$$2E_e = (E - p_z)_{had} + (E - p_z)_{e'}$$

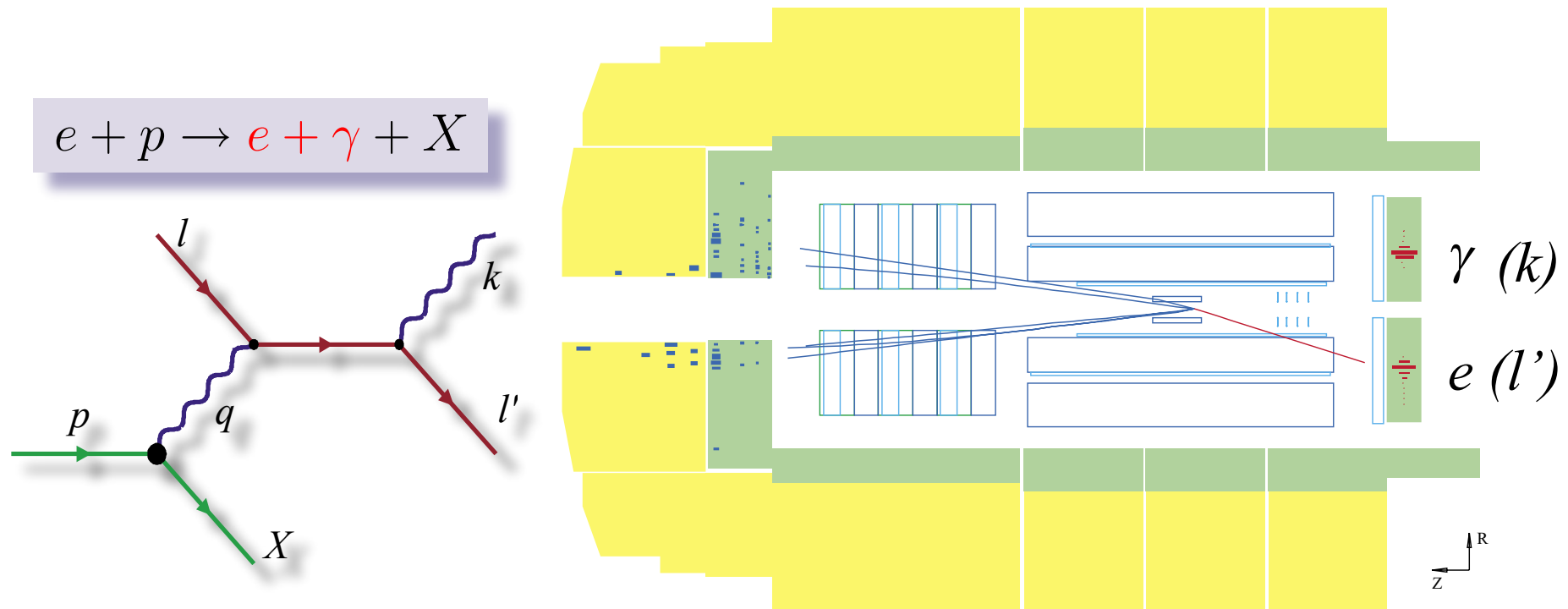


# $F_2$ in Shifted Vertex ISR



⇒ shifted vertex measurement extended to higher  $x$

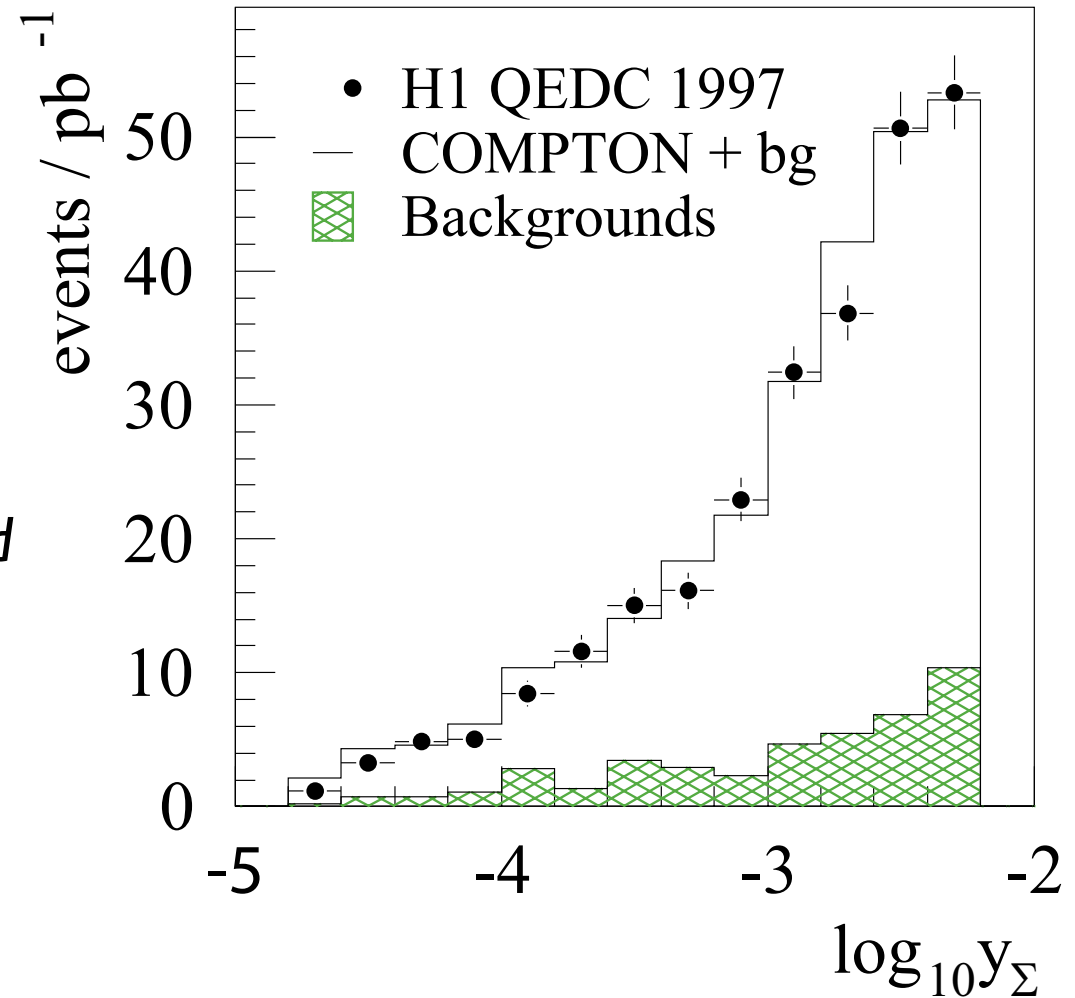
# Inelastic QED Compton Events



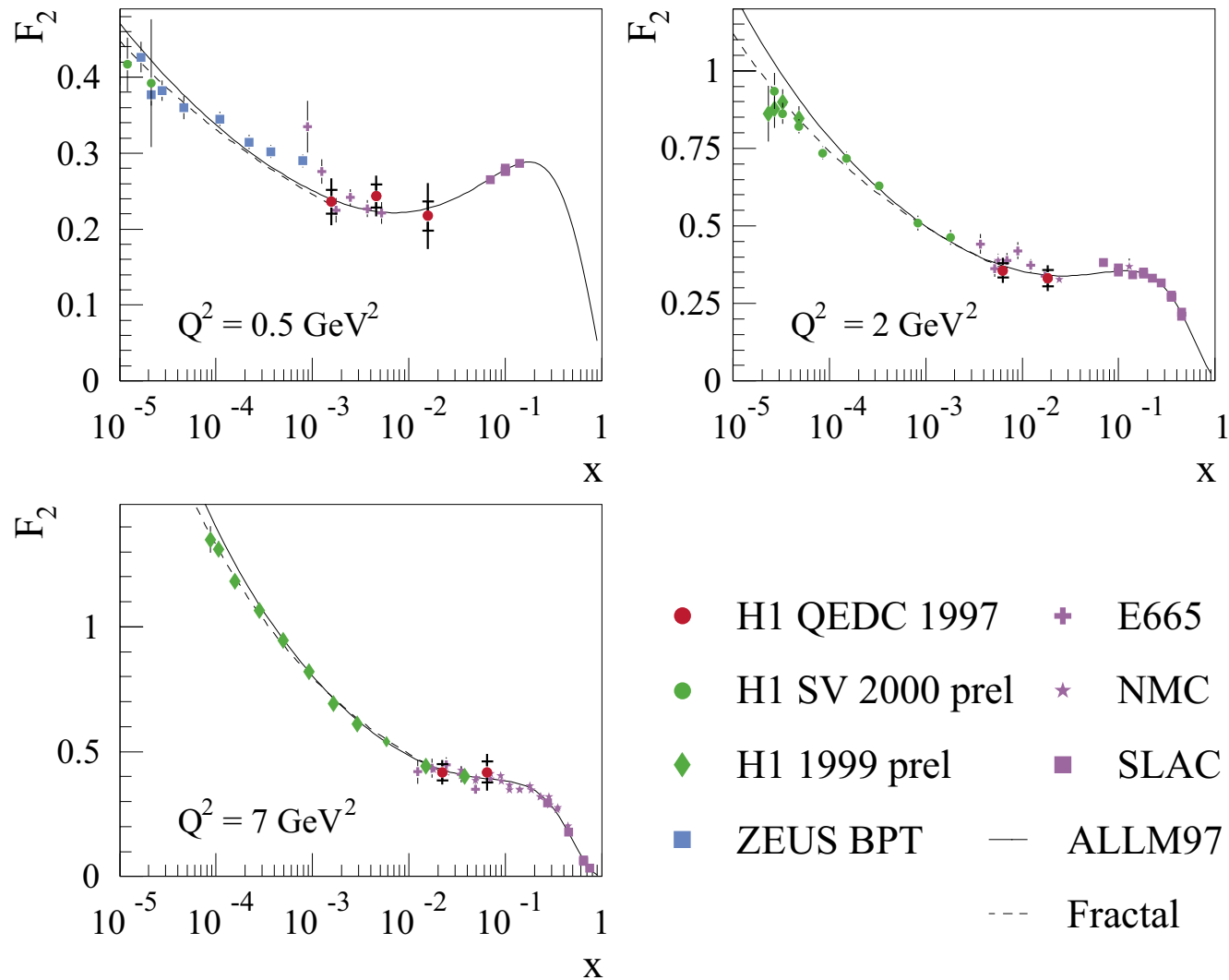
- low virtuality of the exchanged photon  $\Rightarrow$  access to low  $Q^2$
- high virtuality of the exchanged electron
- DIS background: -  $\pi^0$  fakes QEDC  $\gamma$   
- dominates QEDC signature at low  $x$

# Inelastic QED Compton Events

- Medium - high  $x$  are measured*
- understanding of hadronic final state at low  $W$
  - use of SOPHIA Monte Carlo model

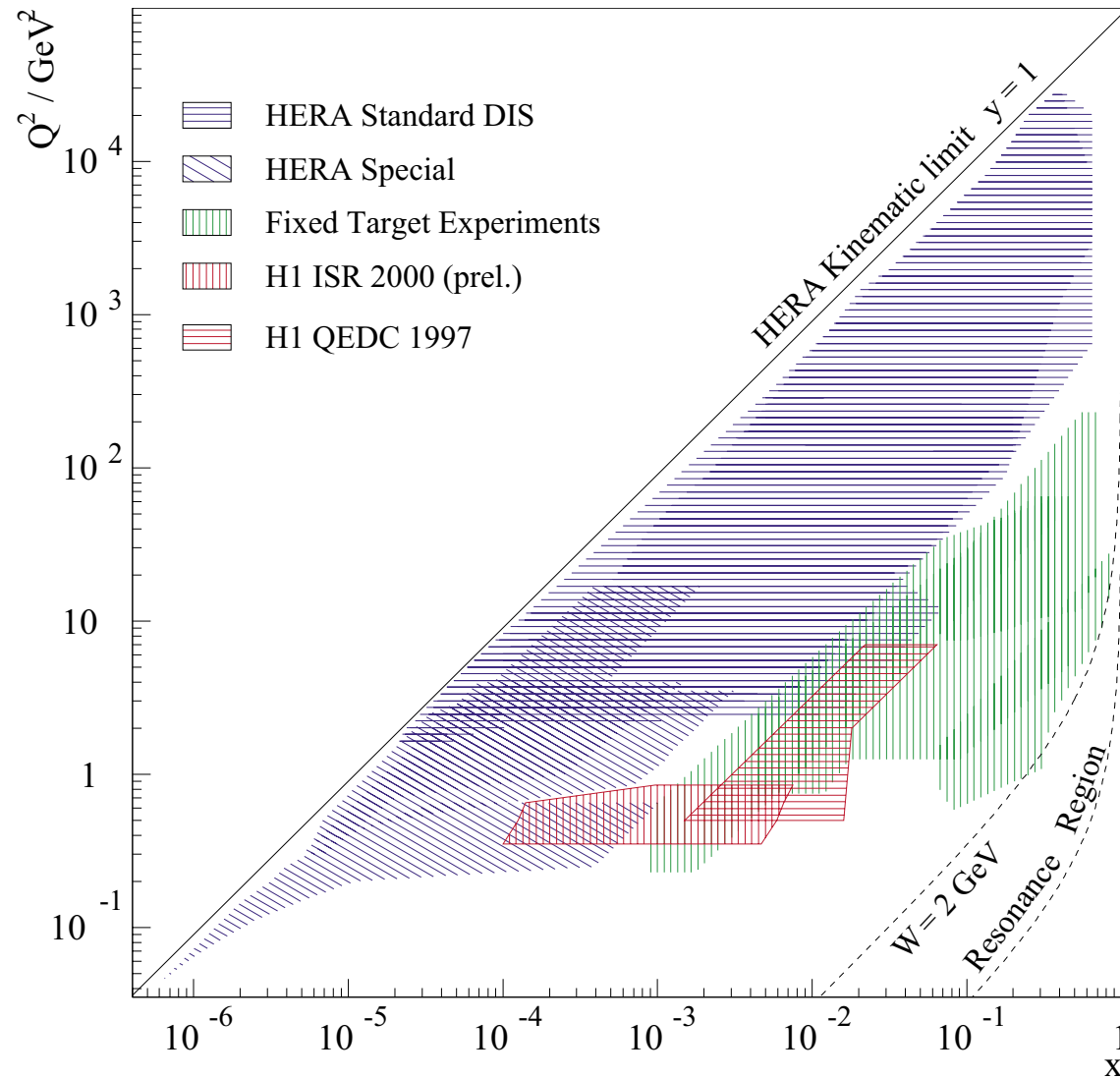


# $F_2$ Measurement with QEDC Events



- good agreement with fixed target experiments

# Overview $F_2$



- **QEDC:**

$$0.5 < Q^2 < 7 \text{ GeV}^2$$

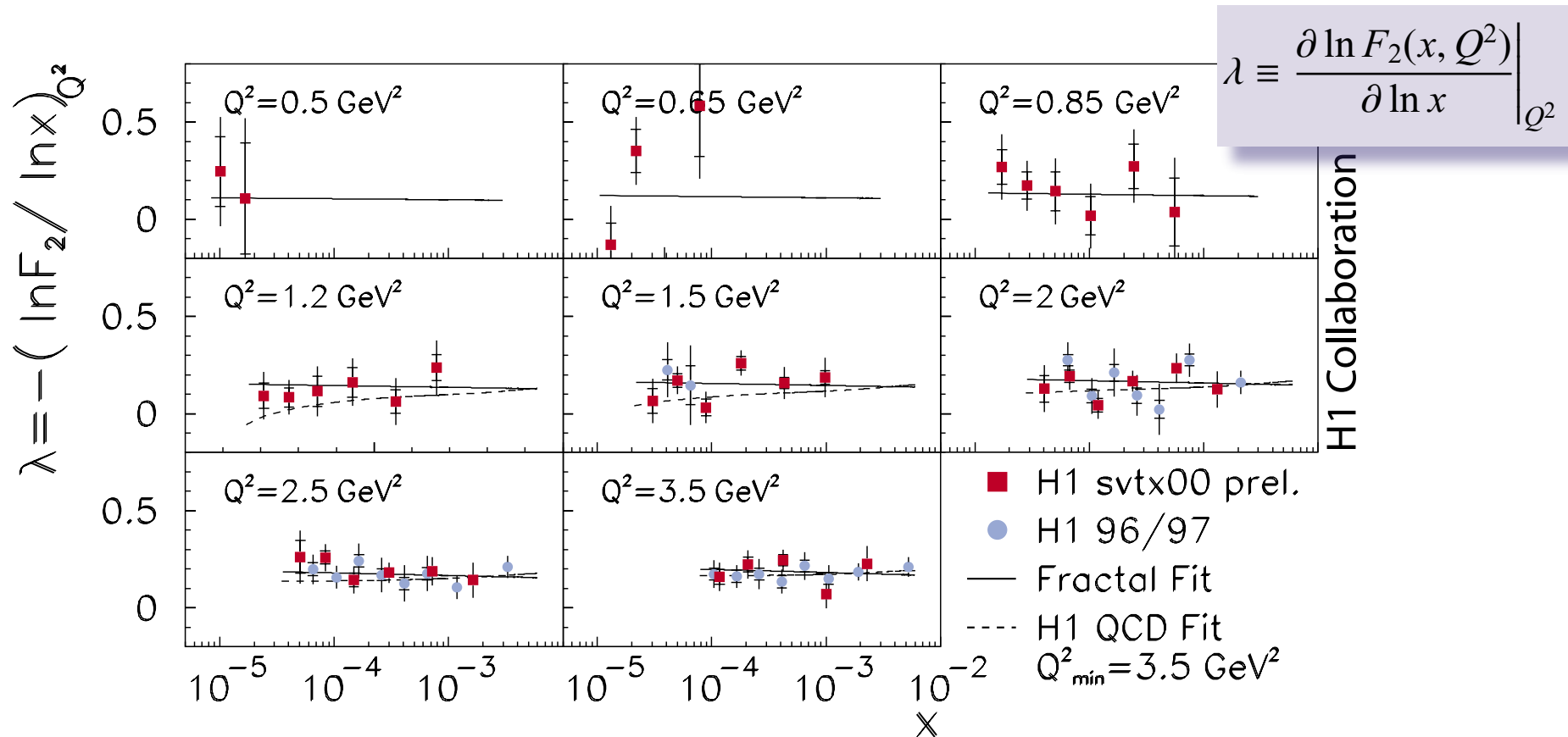
$$2 \cdot 10^{-3} \lesssim x \lesssim 0.1$$

- **shifted vertex ISR:**

$$0.35 < Q^2 < 0.85 \text{ GeV}^2$$

$$10^{-4} \lesssim x \lesssim 5 \cdot 10^{-3}$$

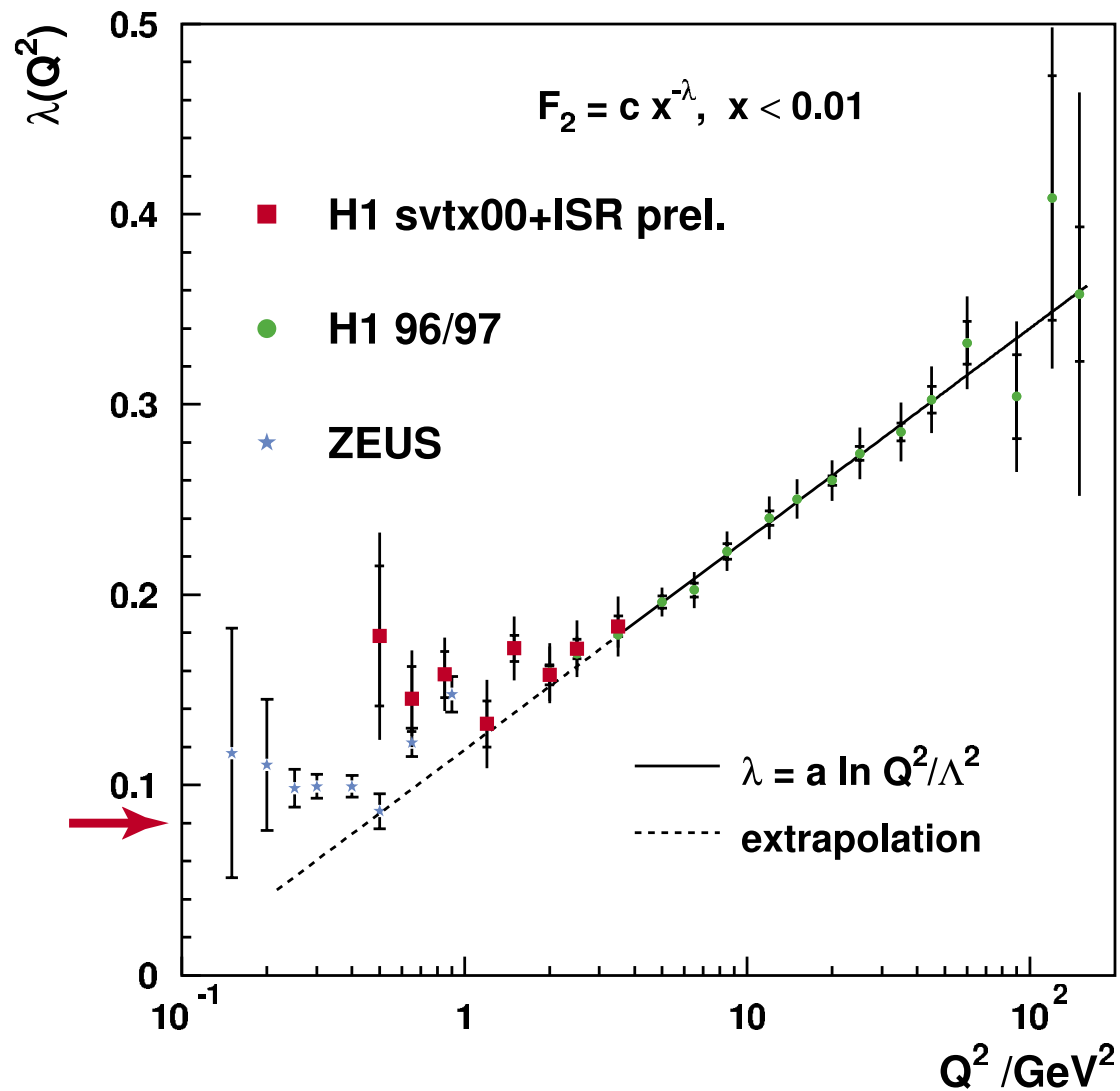
# Rise of $F_2$ at Low $x$



- derivative independent of  $x$  for  $x < 0.01$
- rise of  $F_2$  well parameterised by

$$F_2(x, Q^2) = c(Q^2)x^{-\lambda(Q^2)}$$

# Improved Extraction of $\lambda(Q^2)$



- at  $Q^2 \gtrsim 3 \text{ GeV}^2$ :

$$\lambda \propto \ln Q^2, c \approx \text{const}$$

partonic degrees of freedom

- at  $Q^2 \lesssim 1 \text{ GeV}^2$ :

$$\lambda(Q^2) \rightarrow 0.08$$

transition to hadronic degrees of freedom



# Extraction of $F_L$

$$\sigma_r = \frac{Q^4 x}{2\pi\alpha^2 Y_+} \cdot \frac{d^2\sigma}{dx dQ^2} = F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2) \quad Y_+ = 1 + (1-y)^2$$

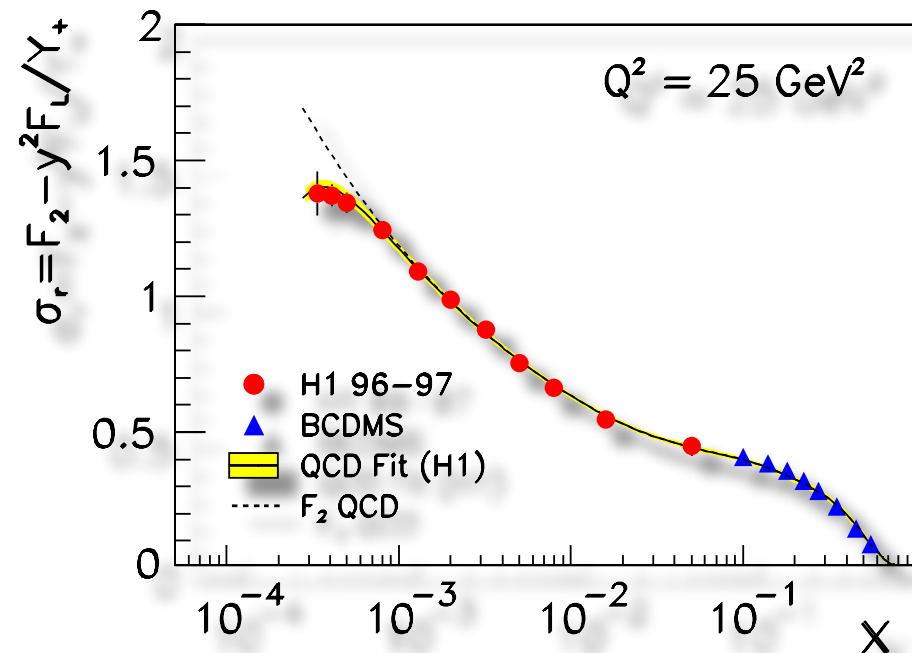
- data sensitive at highest  $y$  only
- direct measurement requires data at different  $s$

*Indirect determination:*

extrapolation of  $F_2$  to higher  $y$ :

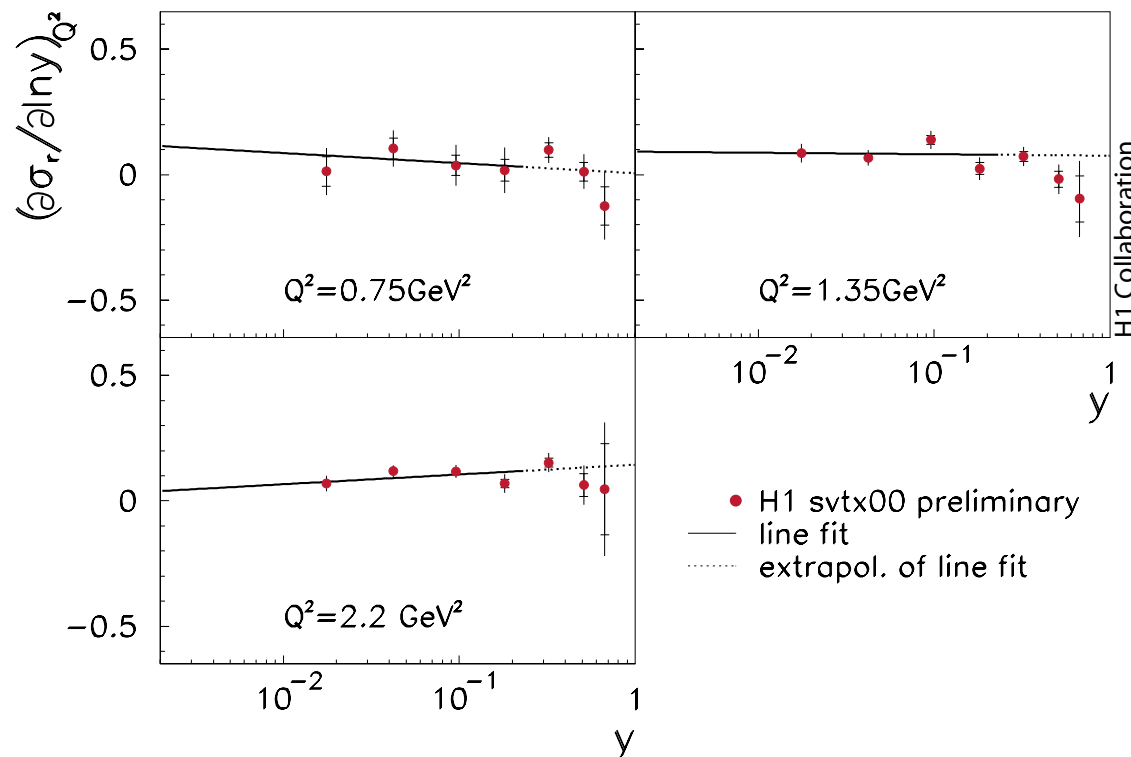
$$F_L \propto F_2 - \sigma_r$$

- derivative method
- shape method



# $F_L$ extraction: Derivative Method

$$\left. \frac{\partial \sigma_r}{\partial \ln y} \right|_{Q^2} = \left. \frac{\partial F_2}{\partial \ln y} \right|_{Q^2} - \frac{2y^2(2-y)}{Y_+^2} F_L$$



- already shown:

$$F_2 \propto x^{-\lambda} \text{ for } x < 0.01$$

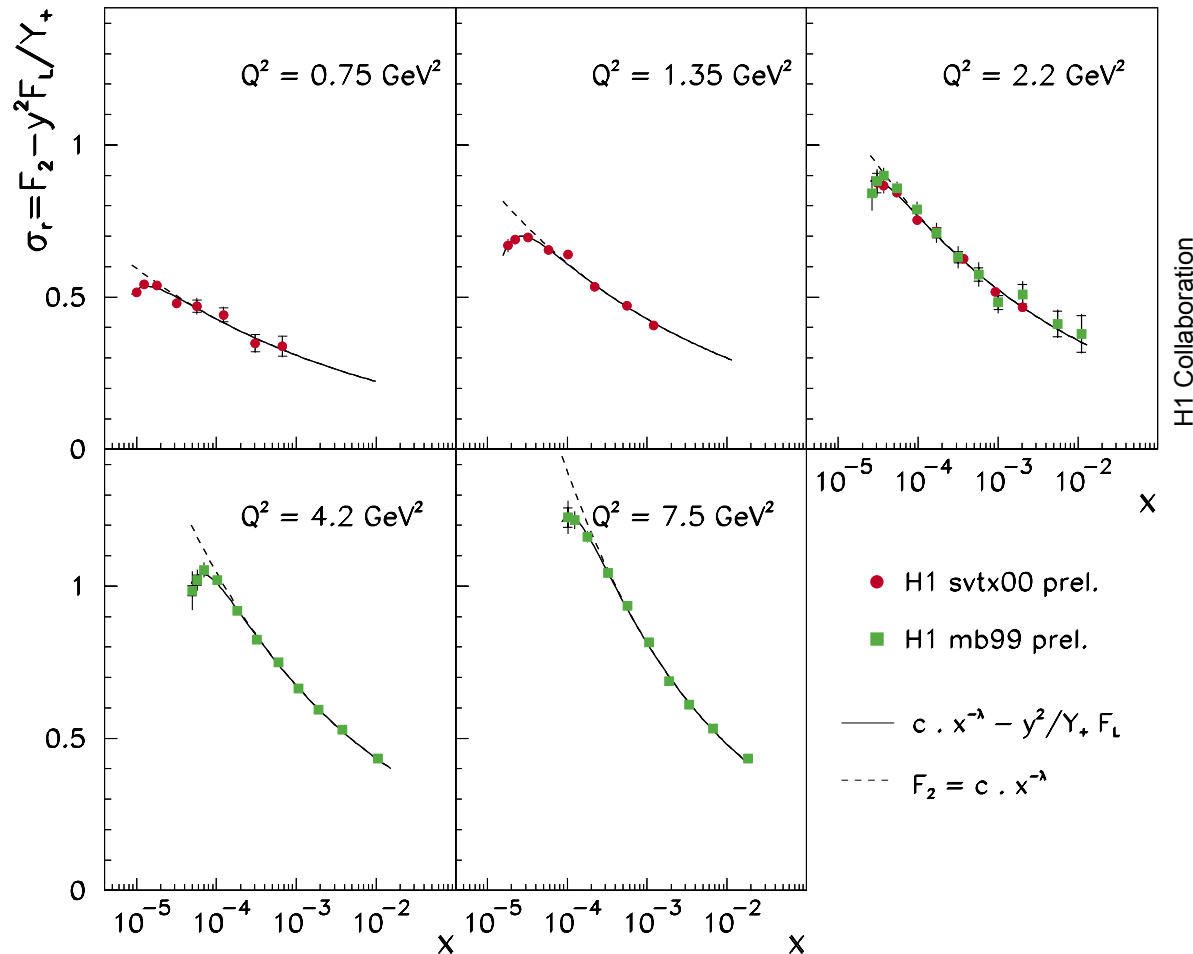
- for  $\lambda \ll 1$  it follows:

$$\frac{\partial F_2}{\partial \ln y} \text{ linear in } \ln y$$

$\Rightarrow F_2$  can be extrapolated from a straight line fit for  $y < 0.2$

$\Rightarrow$  deviation from linear behaviour is attributed to  $F_L$

# $F_L$ extraction: Shape Method



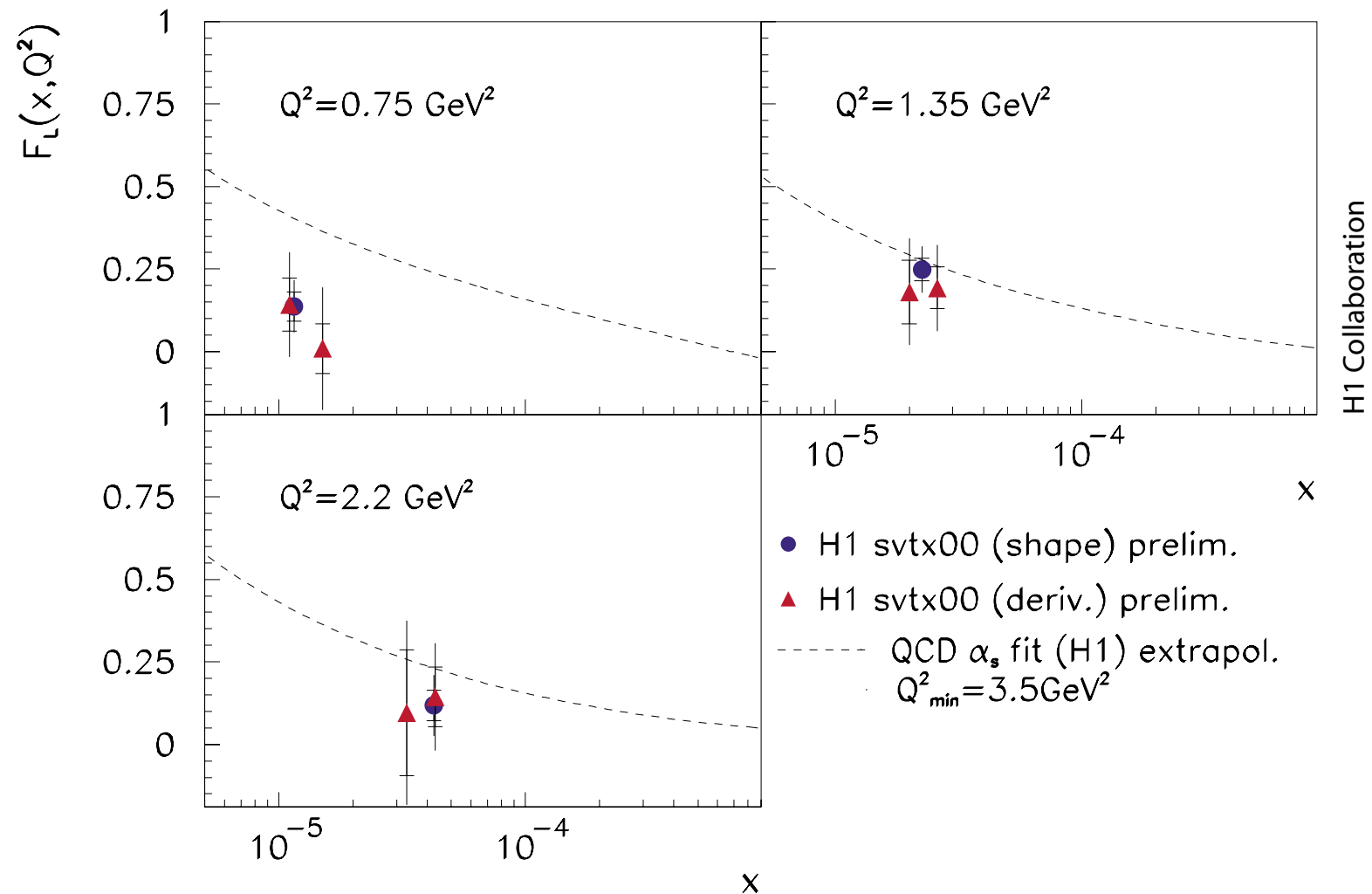
$F_L$  is extracted by fitting  $\sigma_r$ :

$$\sigma_r = c x^{-\lambda} - \frac{y^2}{Y_+} F_L$$

- $c$ ,  $\lambda$  and  $F_L$  free parameters
- turn-over driven by  $y^2 / Y_+$
- $F_L = F_L(Q^2)$

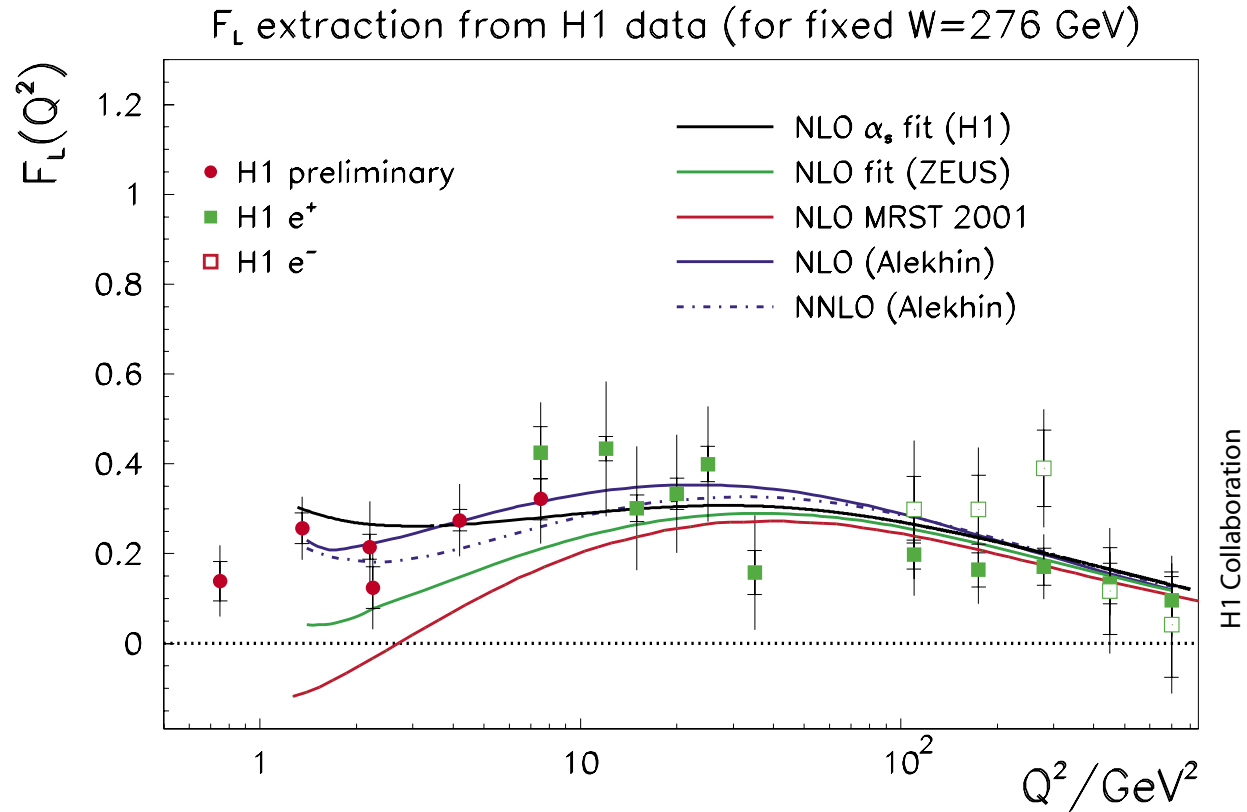
- good description of cross section in full kinematic range

# Shape Method vs. Derivative Method



- shape method provides higher precision

# $F_L(Q^2)$ at fixed $y = 0.75$



possible at HERA only with  
lowered ep cms energy

additional constraint on gluon [positive  $F_L$  at low  $Q^2$ ]  
 direct  $F_L$  measurement important [HERA/LHC workshop]

# Summary

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New structure function measurements at low  $Q^2$

$F_2$ : phase space extended towards **higher  $x$**

**untagged ISR** in shifted vertex

$$0.35 < Q^2 < 0.85 \text{ GeV}^2$$

$$10^{-4} \lesssim x \lesssim 5 \cdot 10^{-3}$$

inelastic **QEDC scattering**

$$0.5 < Q^2 < 7 \text{ GeV}^2$$

$$2 \cdot 10^{-3} \lesssim x \lesssim 0.1$$

$F_L$ : positive for  $Q^2 > 0.75 \text{ GeV}^2$