

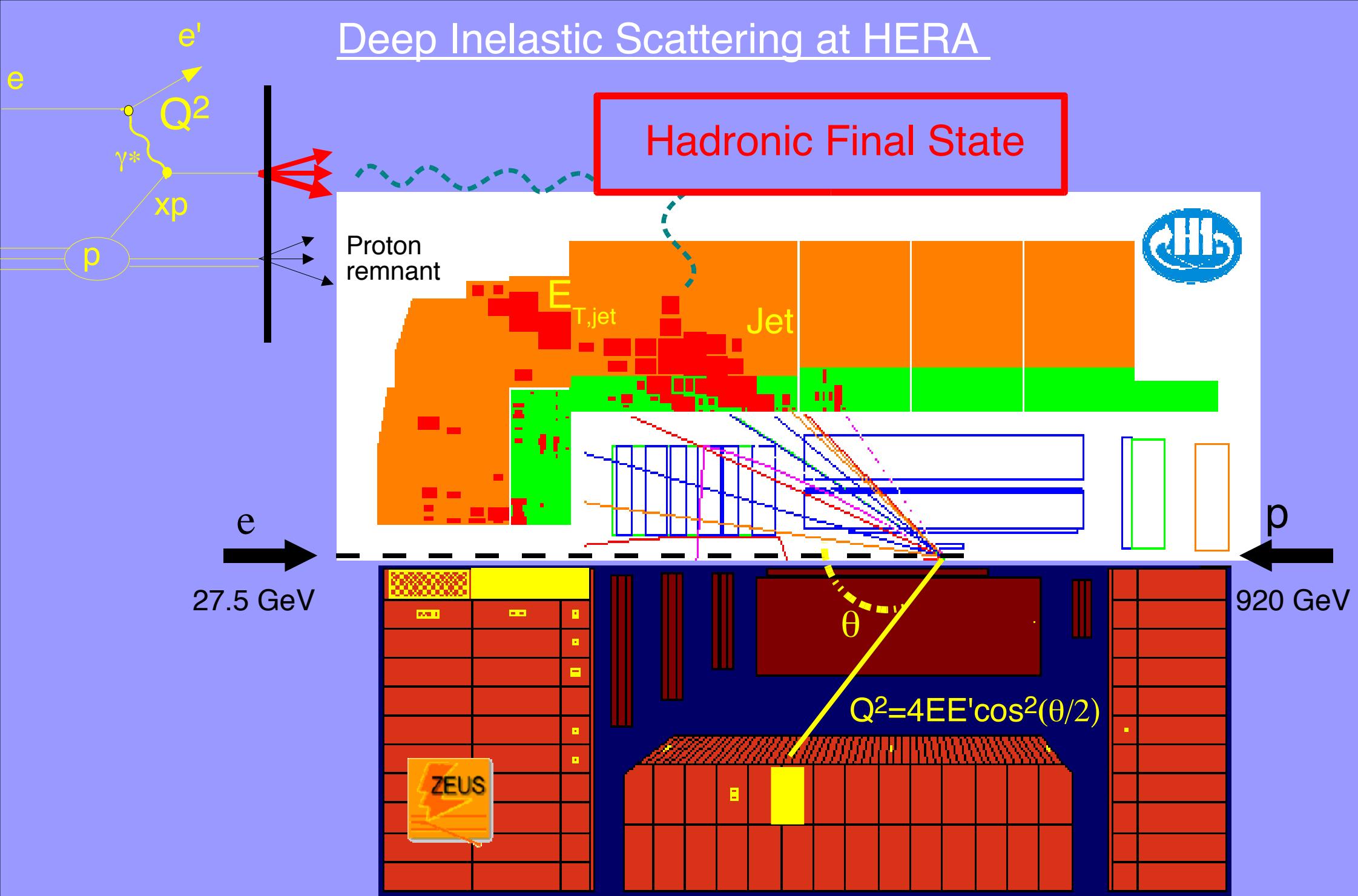
# Jets in Deep Inelastic Scattering at HERA and Measurement of $\alpha_s$

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DESY Hamburg



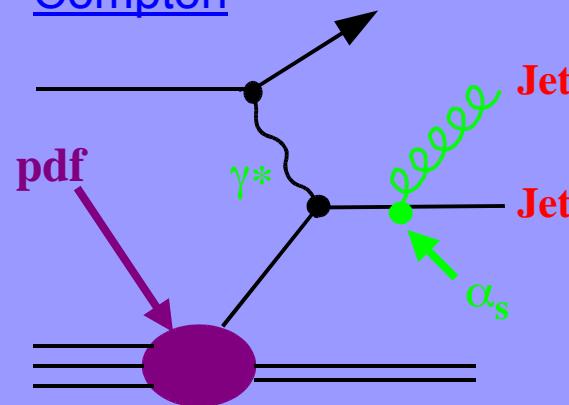
Lake Louise Winter Institute February 2004

# Deep Inelastic Scattering at HERA

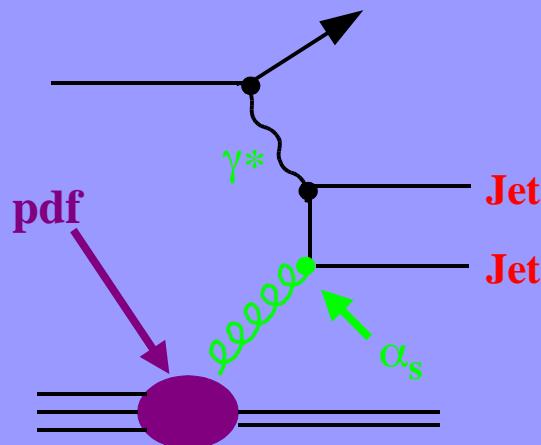


# Jet Cross Sections in DIS

## QCD-Compton



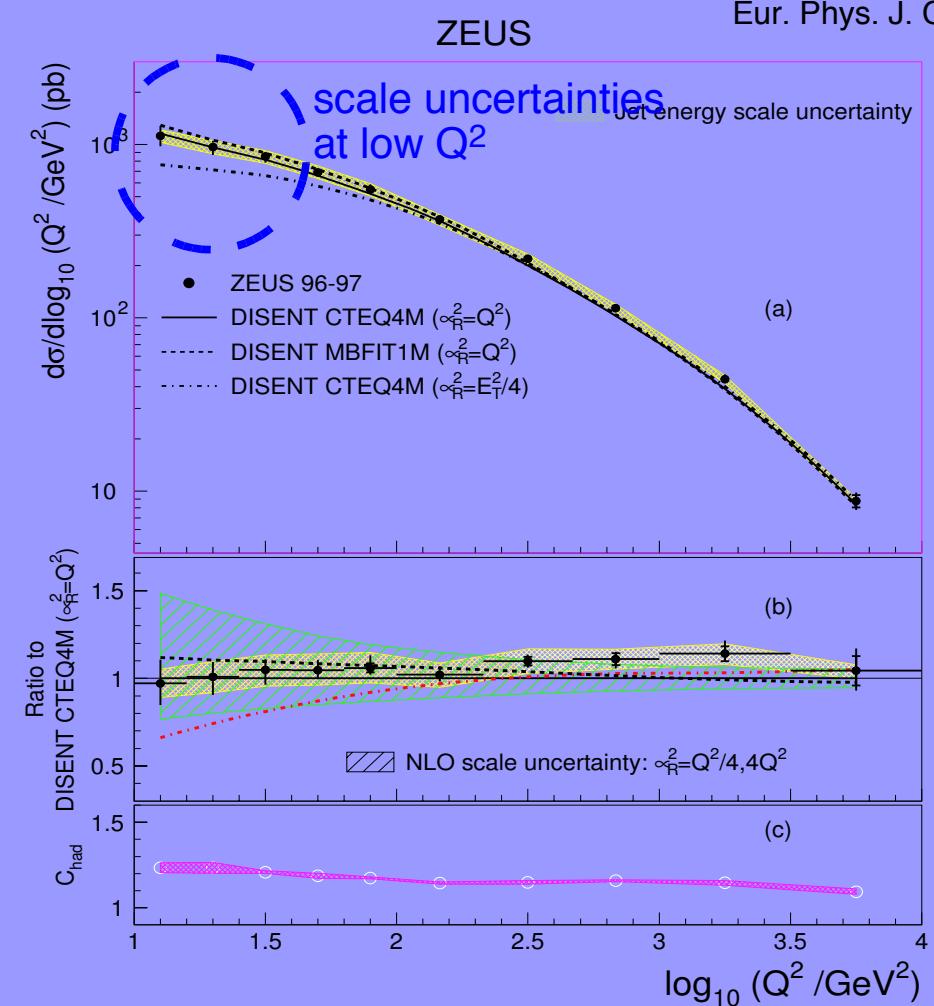
## Boson Gluon Fusion



$$\sigma_{jet} = \sum_n \alpha_s^n(\mu_r) \sum_{i=G,q} \hat{\sigma}_{jet}(\mu_r, \mu_f) \otimes \text{pdf}(\mu_r, \mu_f)$$

## Dijet Cross Section

Eur. Phys. J. C C23 (2002) 1



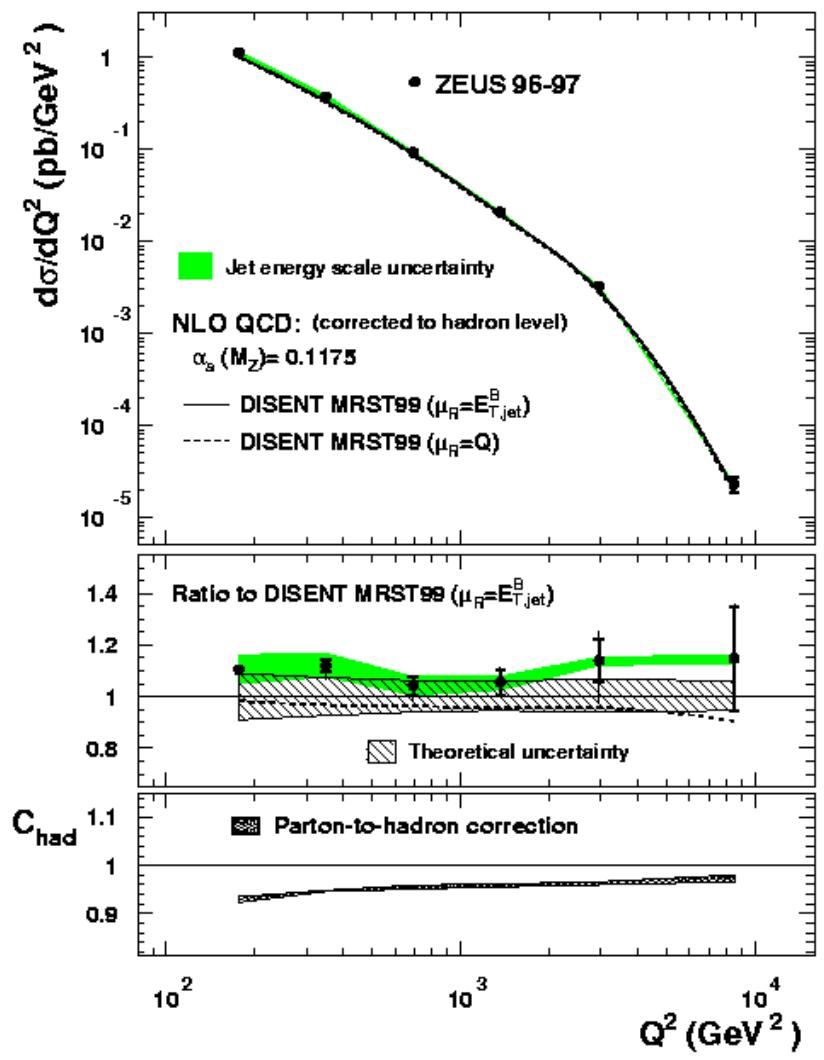
Description of data by NLO-QCD [ $\mathcal{O}(\alpha_s^2)$ ] if  $Q^2 > 150 \text{ GeV}^2$  with small scale uncertainties

# Inclusive Jet Cross Sections

## Theoretical and experimental advantages

Phys. Lett. B 547 (2002) 164

**ZEUS**



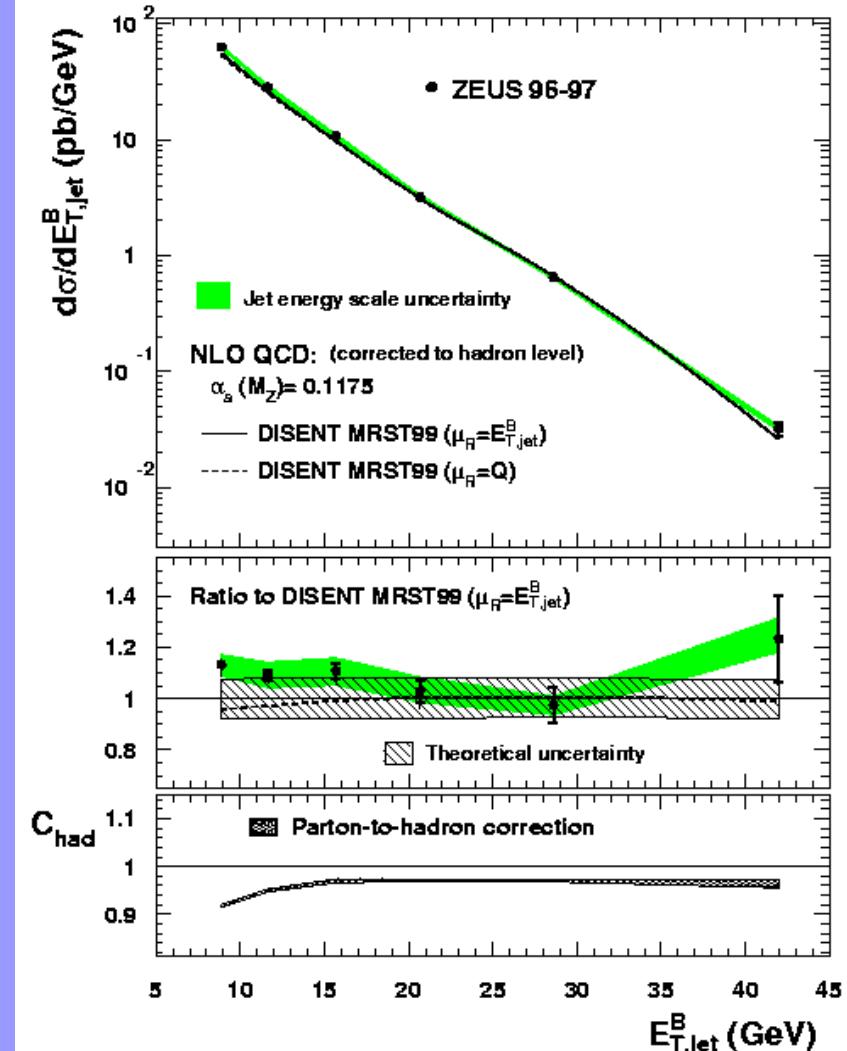
Experimental  
and  
theoretical  
uncertainties  
 $O(7\%)$

Best agreement  
between data  
and theory at large  
 $Q^2, E_T$

Small hadronisation  
corrections  
at large  $Q^2, E_T$

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**ZEUS**



Extraction of  $\alpha_s$  possible at large values of  $Q^2$  and  $E_T$

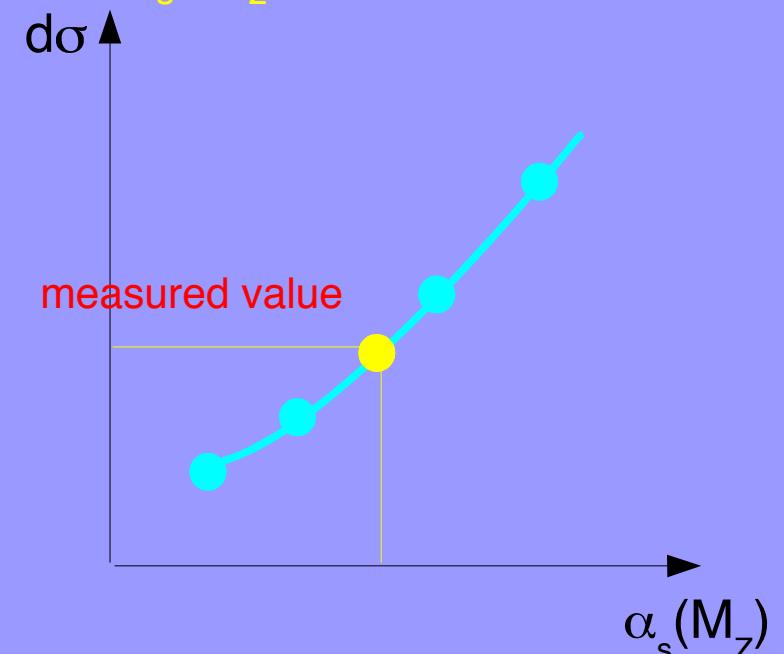
## Determination of $\alpha_s$

- Parameterize jet cross section as power series of  $\alpha_s(M_z)$

$$d\sigma \sim A \cdot \alpha_s + B \cdot \alpha_s^2$$

Based on NLO-QCD predictions which employing different values of  $\alpha_s(M_z)$

- Extract from measured cross section 'true' value of  $\alpha_s$
- Result from inclusive cross section  $d\sigma/dQ^2$   
 $Q^2 > 500 \text{ GeV}^2$



$$\alpha_s(M_z) = 0.1212 \quad +0.0017 \quad \leftarrow \text{Stat.}$$

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$$+0.0023 \quad \leftarrow \text{Exp.: Jet Energy Scale}$$
$$-0.0031 \quad \leftarrow$$

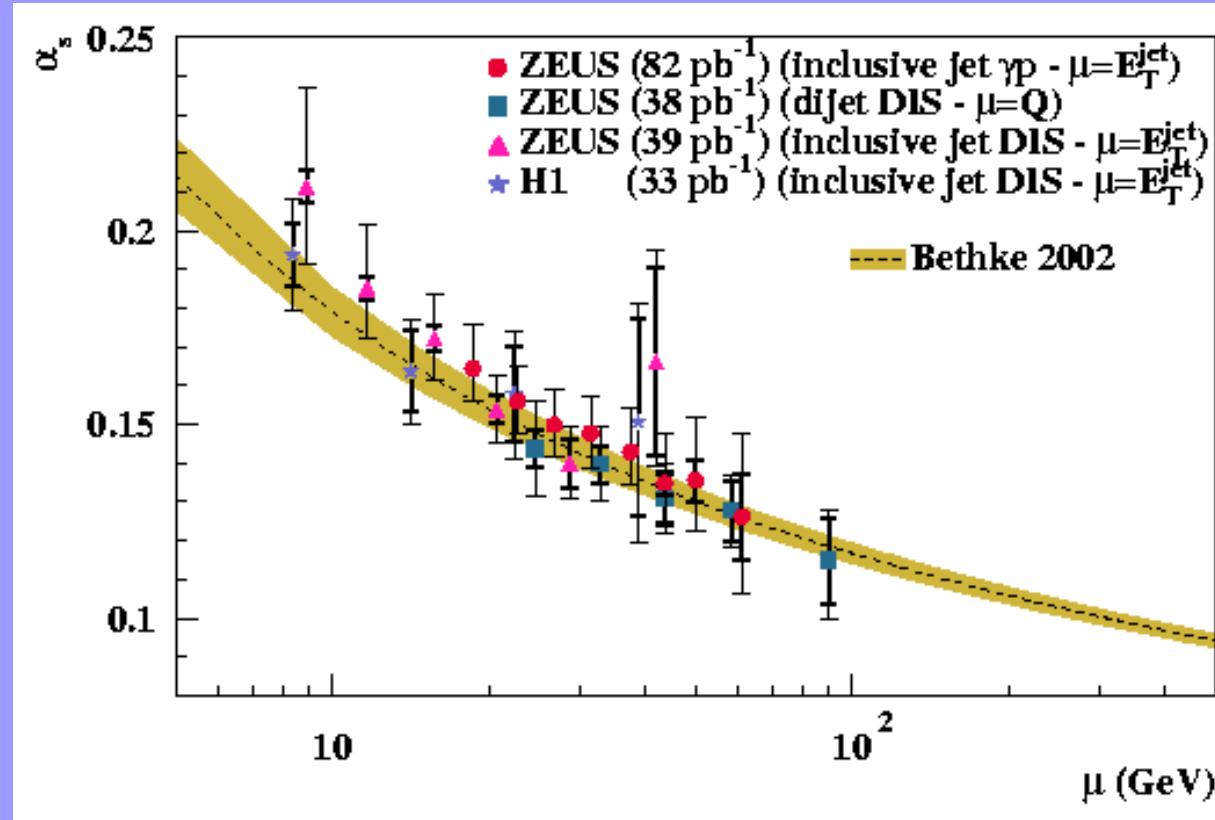
$$+0.0028 \quad \leftarrow \text{Theory: Terms beyond NLO 3\%}$$
$$-0.0027 \quad \leftarrow \text{Parton PDFs 1\%}$$

Hadronisation corrections 0.2%

Precise Determination of  $\alpha_s$  !

# $\alpha_s$ from inclusive Jet and Dijet Cross Sections

Extraction of  $\alpha_s$  at different energy scales  $\mu$   
→ Running of  $\alpha_s$  with energy  
(Basic QCD prediction)

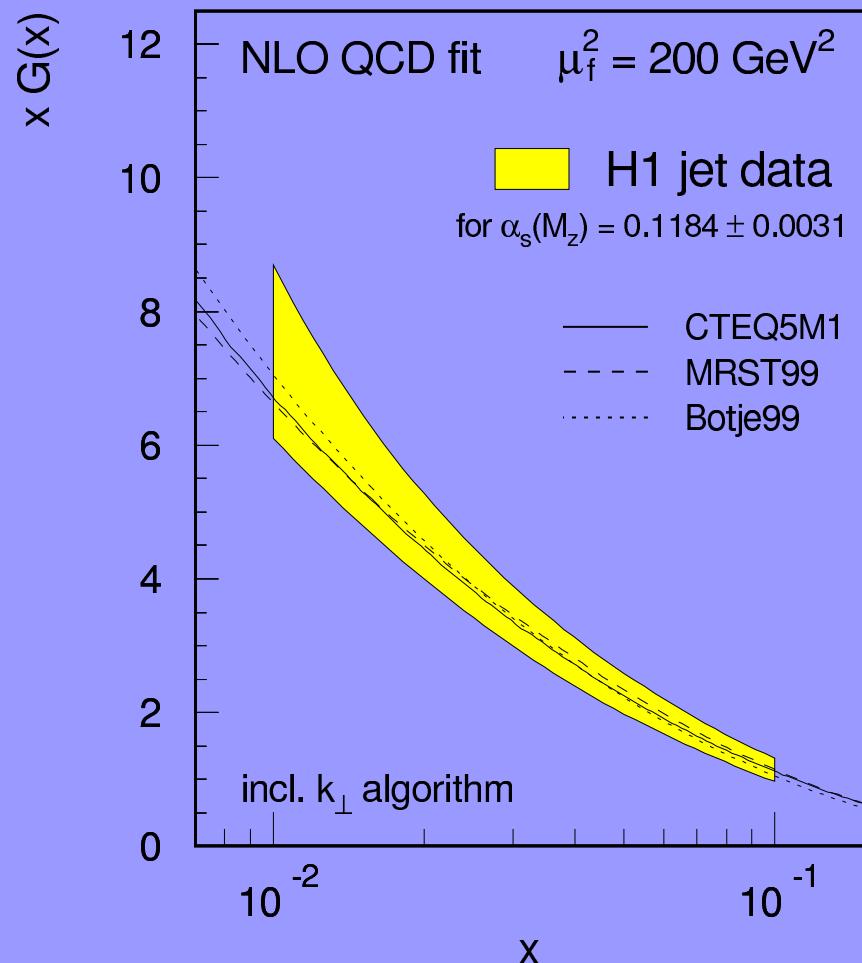
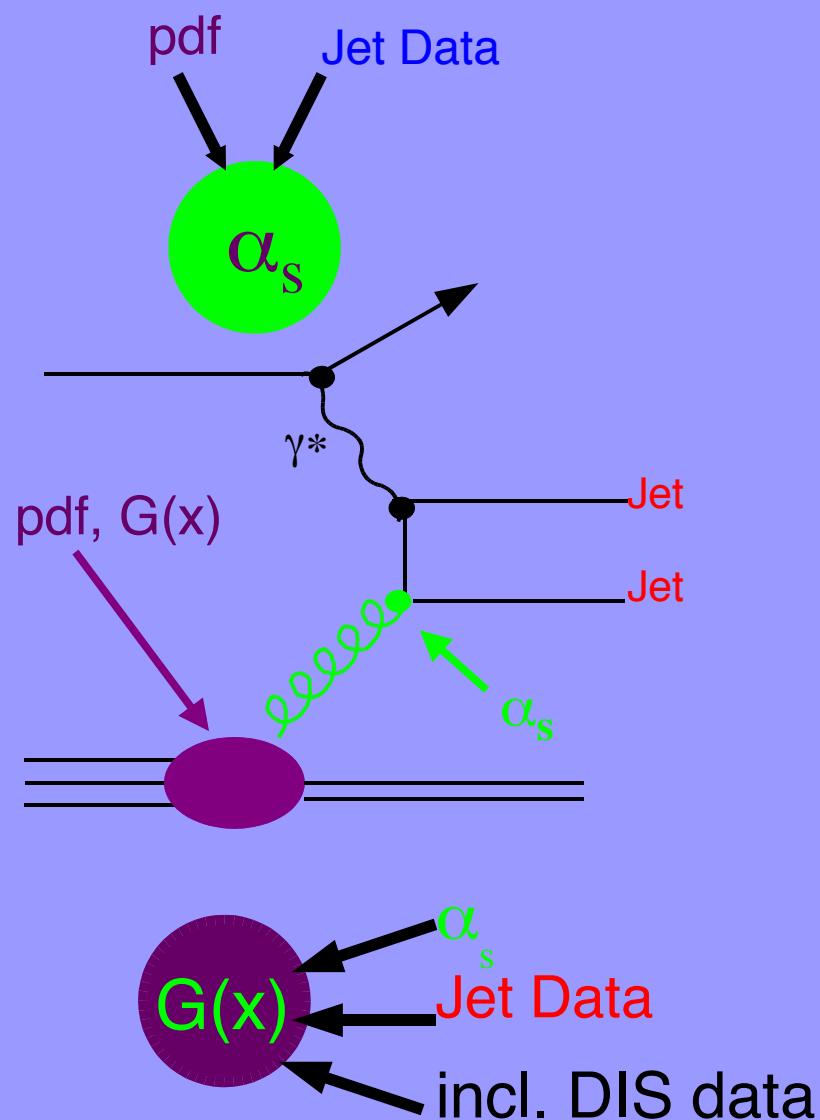


- Phys. Lett. B 570 (2003) 7  
Phys. Lett. B 507 (2001) 70  
Phys. Lett. B 547 (2002) 164  
Eur. Phys. J. C 19 (2001) 289

Results show clearly the running of  $\alpha_s$  over wide range of  $\mu$   
Consistency with global fits

# Determination of the Gluon Density with Jets

Eur. Phys. J. C 19 (2001) 289



$$\int_{0.01}^{0.1} dx xG(x, \mu_f = 200 \text{ GeV}^2) = 0.229$$

Direct determination of gluon density  
with jets consistent with result from global fits

Universality of gluon density !

# Simultaneous fit of $\alpha_s$ and the gluon density $xG(x)$

Eur. Phys. J. C 19 (2001) 289

Basic idea:

Use three different cross sections to determine unknowns  $\alpha_s$ ,  $G(x)$ ,  $q(x)$

$$\sigma_{DIS} \sim q(x)$$

$$\sigma_{jet} \sim \alpha_s \cdot (c_G G(x) + c_q q(x))$$

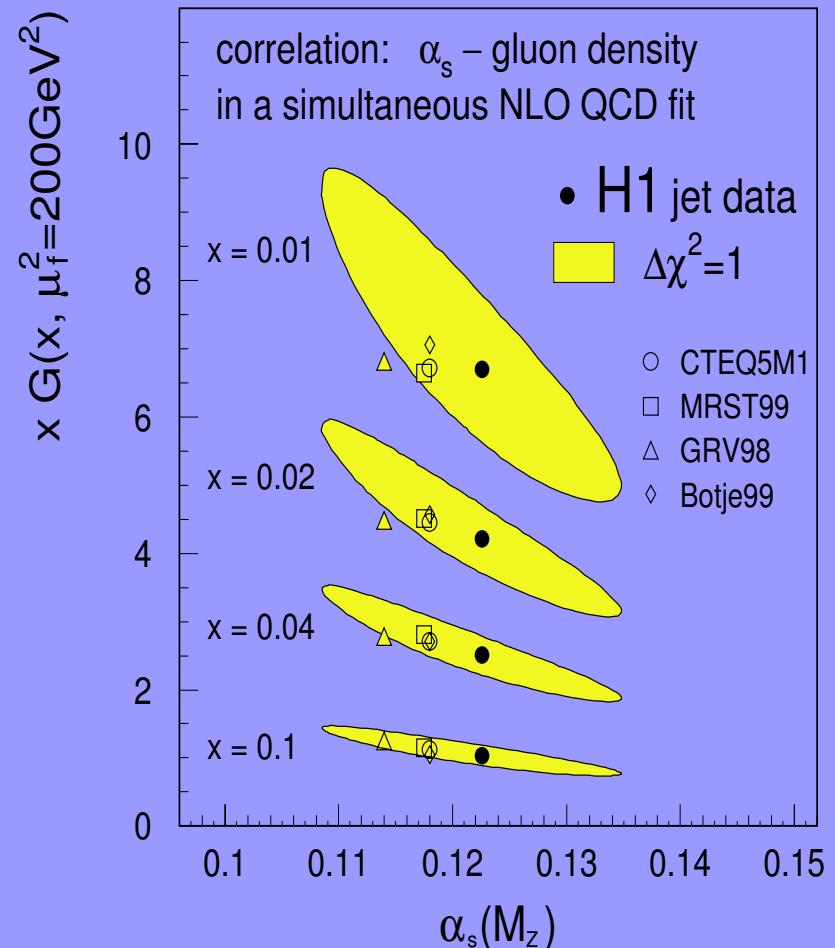
$$\sigma_{2jet} \sim \alpha_s \cdot (c'_G G(x) + c'_q q(x))$$

Kinematic range:

- DIS x-section:  $150 < Q^2 < 1000 \text{ GeV}^2$
- Jet x-section:  $150 < Q^2 < 5000 \text{ GeV}^2$

Fit:

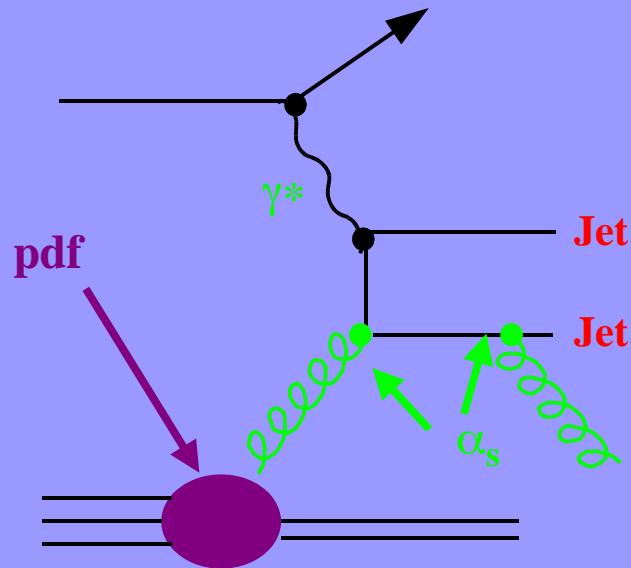
- fixed factorization scale  $\mu_f$
- put experimental, scale and hadronization uncertainties into systematics



Large anti-correlation between  $G(x)$  and  $\alpha_s$   
Result consistent with global fits

Improvement by higher statistic @ large ET

# Three Jet Cross Sections in DIS

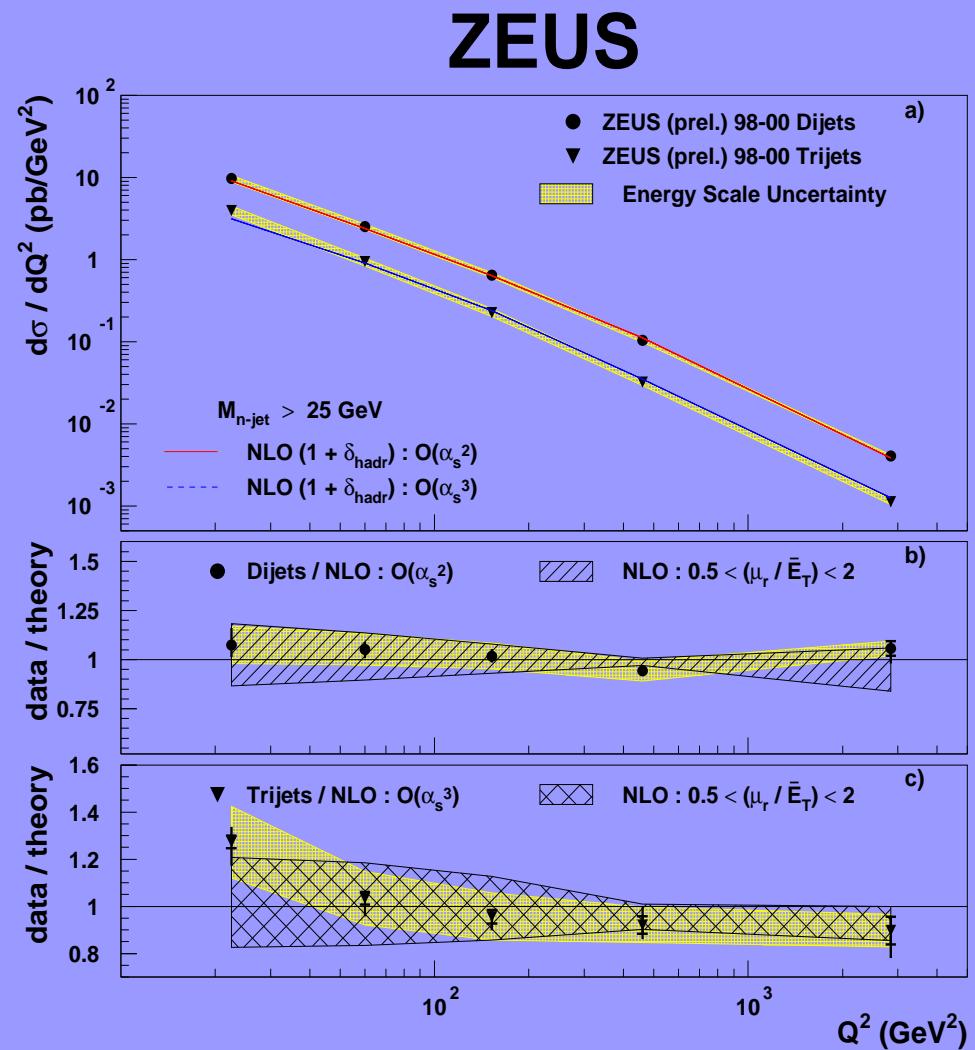


LO process proportional to  
 $\alpha_s^2$   
 $\Rightarrow$  High sensitivity to  $\alpha_s$

Contributed Paper to EPS '03

Dijet and three-jet cross sections  
 well described by NLO QCD  
 calculations  
 (up to  $\alpha_s^3$  for three jets)

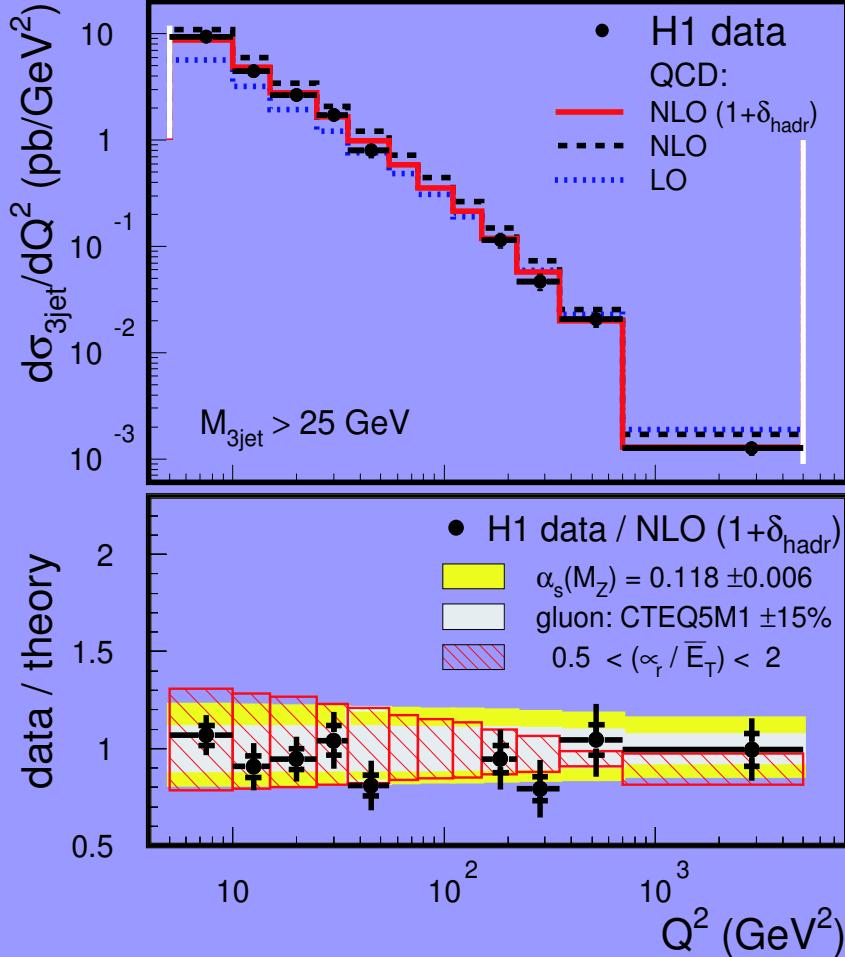
Potential for extraction of  $\alpha_s$  !?



# $\alpha_s$ measurement employing three jet cross sections

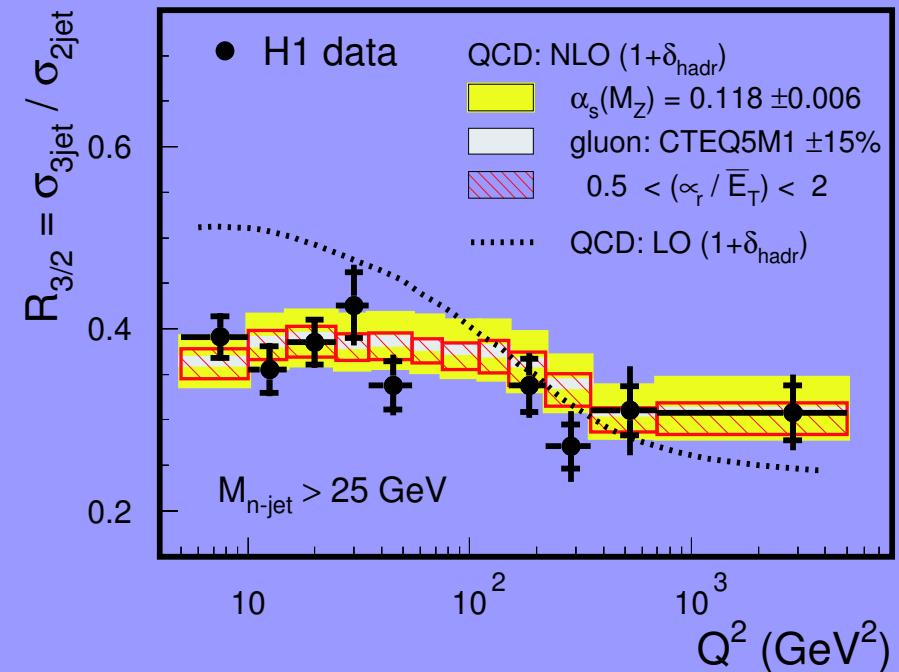
## Three jet cross section

Phys. Lett. B 515 (2001) 17



$$R_{3/2} = \sigma_{3\text{jet}} / \sigma_{2\text{jet}}$$

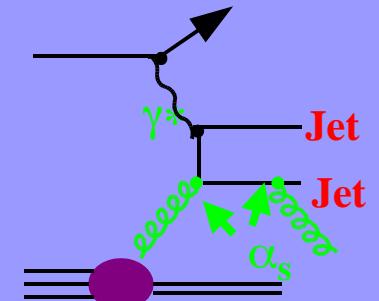
Phys. Lett. B 515 (2001) 17



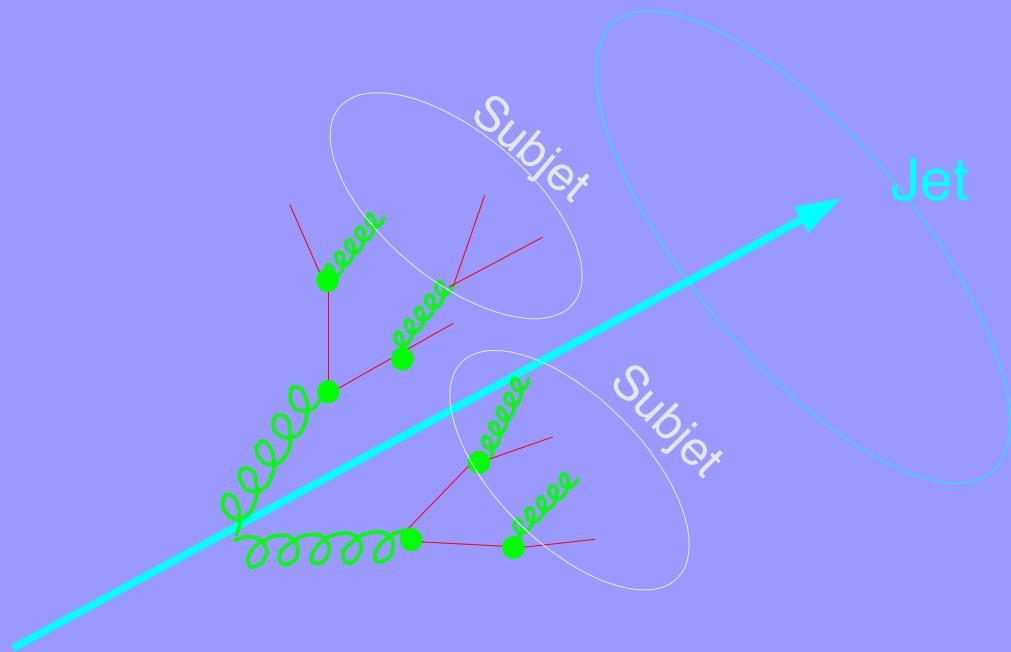
Reduced sensitivity to gluon density by ratio

Sizeable sensitivity on gluon density

Large sensitivity to small variations of  $\alpha_s$



## Jet Substructure



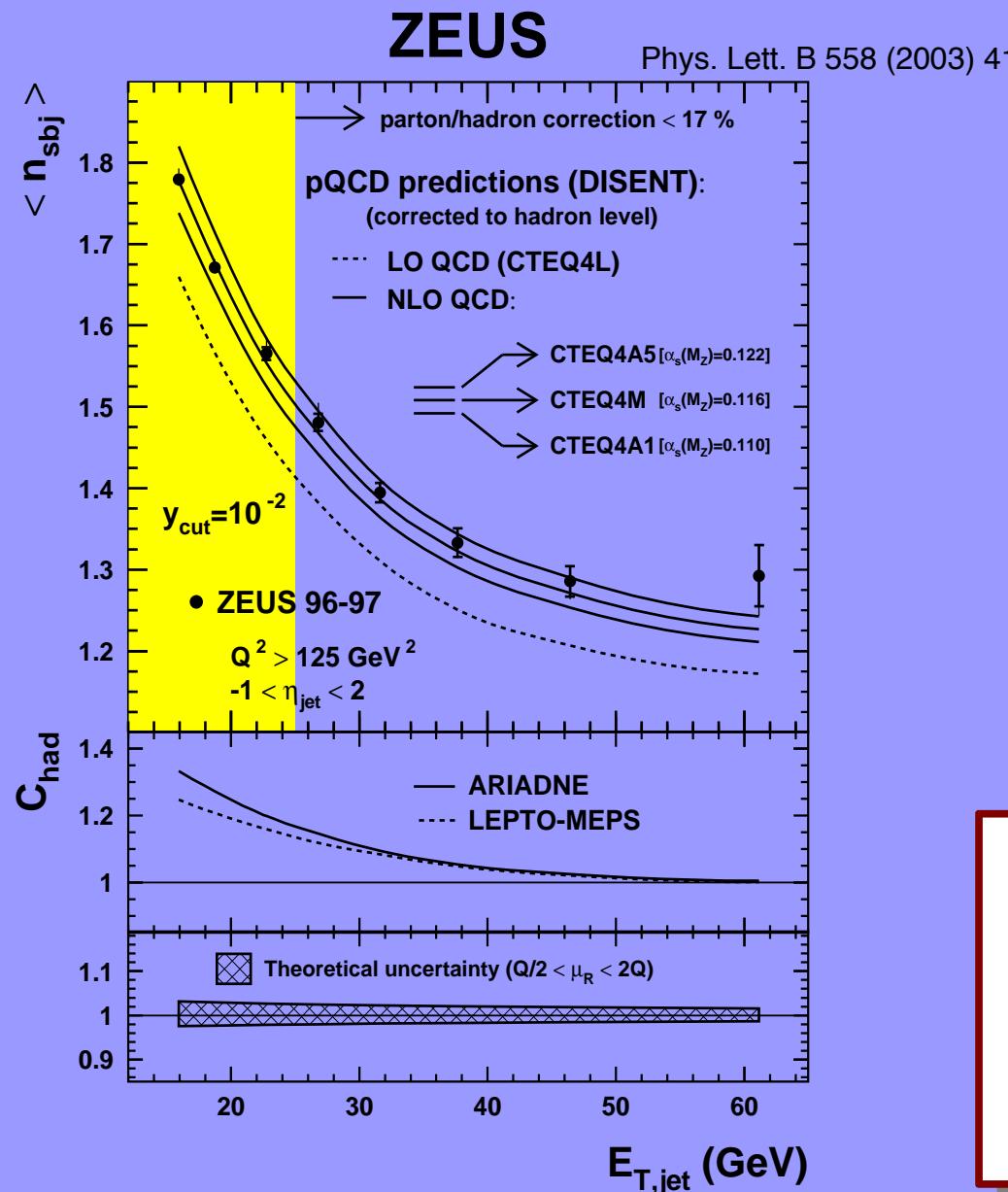
A jet can be decomposed  
into subjets

Formation of partons → subjets is driven by QCD

Subjet-Multiplicity sensitive to  $\alpha_s$

# Subjet Multiplicity and Determination of $\alpha_s$

Measurement in Lab. Frame



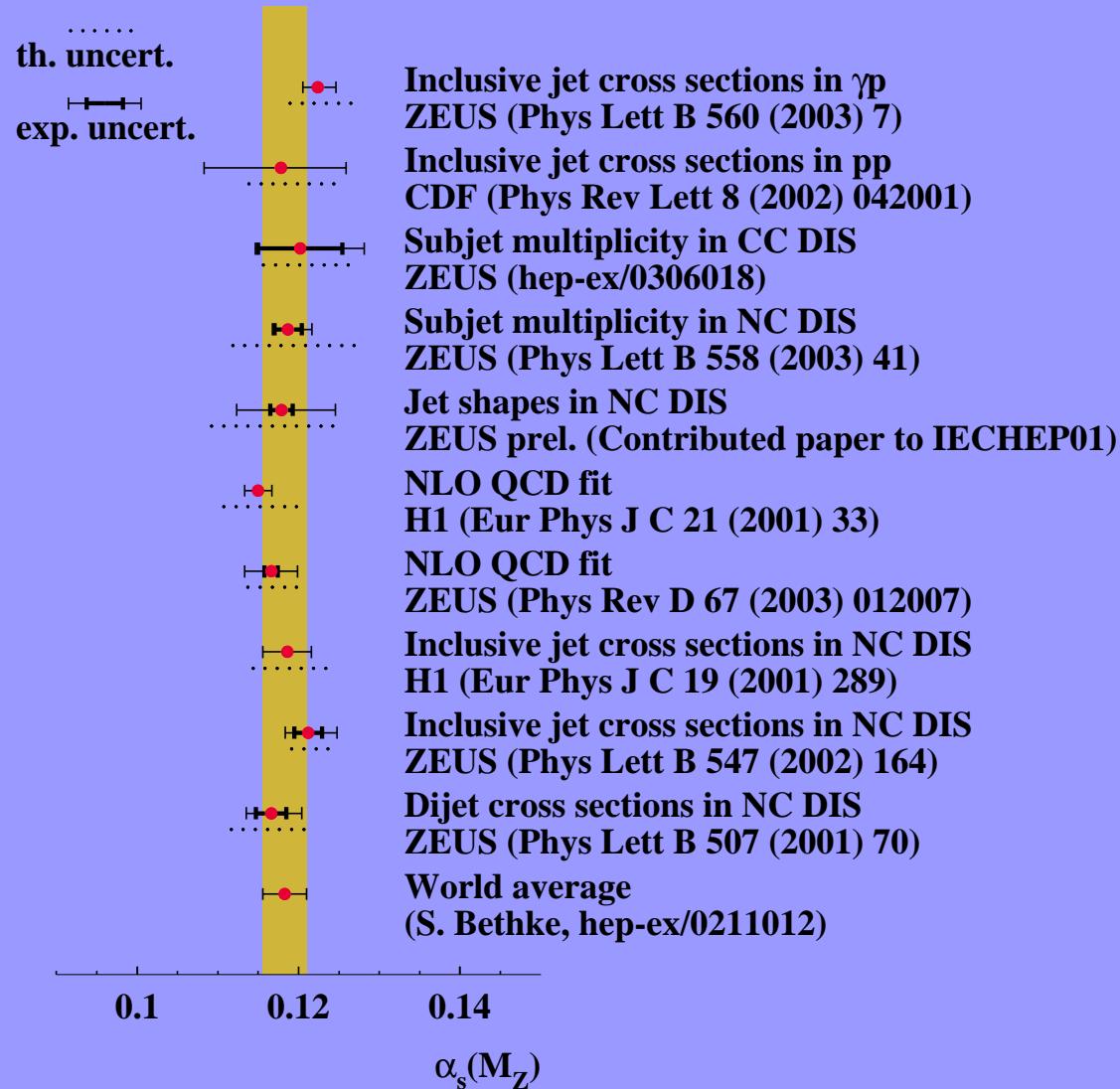
- Number of subjets decreases as  $E_T$  of jet increases
  - NLO QCD calculations describe data
  - Predictions based on different  $\alpha_s$  'oscillate' around data
- Determination of  $\alpha_s$

$\alpha_s(M_Z) = 0.1187 \quad +0.0017 \quad \text{Stat.}$

Phys. Lett. B 558 (2003) 41       $+0.0024$   
 $-0.0009 \quad \text{Exp.}$

$+0.0093 \quad \text{Theory}$   
 $-0.0076$

# Conclusions



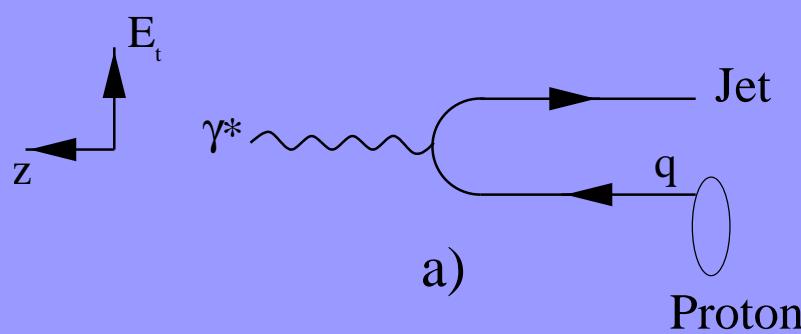
- Multijet production in DIS at HERA allow for stringent test of QCD
- Precise determination of  $\alpha_s$  by various jet observables
- Consistent results
- Significant impact on world average of  $\alpha_s$

## The Breit Frame

In ep lab-frame outgoing hadrons have to balance  $E_T$  of scattered e

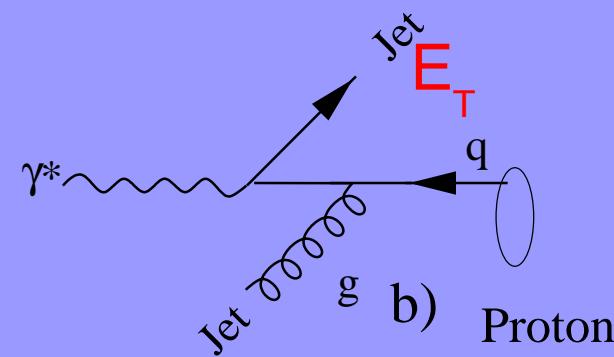
Choose frame where transverse energy is solely produced by interesting hard scatter  
Frame where proton and photon collide head on

QPM



a)

QPM + QCD



b)

$$2x \vec{P}_{proton} + \vec{q}_\gamma = 0$$

No transverse energy  
in naive QPM

Transverse energy  $E_T$   
by QCD process