

## JETS IN DEEP-INELASTIC SCATTERING AT HERA AND DETERMINATIONS OF $\alpha_s$ \*

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Several methods to extract the strong coupling constant  $\alpha_s$  by means of highly energetic jets in Deep-Inelastic Scattering are presented. The results from the various methods agree with one another and with the world average. The errors are competitive to those achieved in  $\alpha_s$  determinations in other processes such as proton-anti-proton scattering.

### 1. Introduction

Measurements of the hadronic final state in deeply inelastic  $ep$  scattering (DIS) provide precision tests of quantum chromodynamics (QCD). At HERA data are collected over a wide range of the negative four-momentum-transfer  $Q^2$ , and the transverse energy  $E_T$  of hadronic final state jets. As sketched in Eq. 1 the jet cross section can be expressed as a power series of  $\alpha_s$  combined with a convolution of the hard matrix element,  $\hat{\sigma}_{jet}$ , and appropriate parton distribution functions of the proton.

$$\sigma_{jet} = \sum \alpha_s^n(\mu_r) \sum \hat{\sigma}_{jet}(\mu_r, \mu_f) \otimes \text{pdf}(\mu_f, \dots), \quad (1)$$

with  $\mu_r$  and  $\mu_f$  being mass scales.

Fig. 1 shows diagrams of the leading order, here  $O(\alpha_s)$ , processes for dijet-production in DIS.

The accurate measurement of jet production, hence, allows for a precise determination of  $\alpha_s$ .

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\*Talk given on behalf of the H1 and ZEUS collaborations at the Lake Louise Winter Institute 15-21 Feb. 2004, Lake Louise, Canada

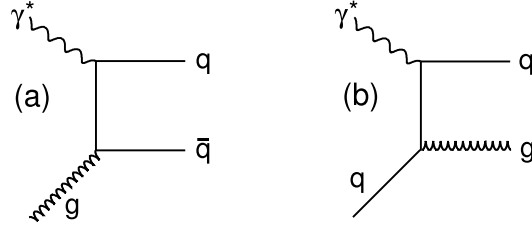


Figure 1. Leading order diagrams for dijet production in  $ep$  scattering. (a) photon-gluon fusion and (b) QCD-Compton process.

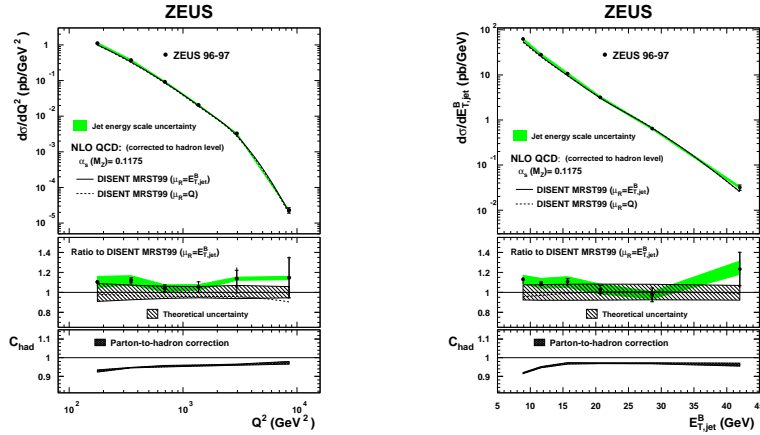


Figure 2. Single inclusive jet cross section as a function of  $Q^2$  (left) and  $E_{T,jet}^B$  (right) compared with NLO QCD predictions.

## 2. Single Inclusive Jet Cross Section

For this analysis it is required to identify at least one jet above a given transverse energy. Fig. 2 shows the measured single inclusive jet cross section as a function of  $Q^2$  and the transverse energy of the jet as measured in the Breit-Frame compared with NLO-QCD calculations <sup>1</sup>.

The data have a typical experimental uncertainty of 7 % and are well reproduced by the theoretical predictions at large values of  $E_T$  and  $Q^2$ . The NLO-QCD calculations, currently only available at the parton level, are corrected for hadronisation effects using LO models. These corrections are expected to be small at large  $E_T$  and  $Q^2$ .

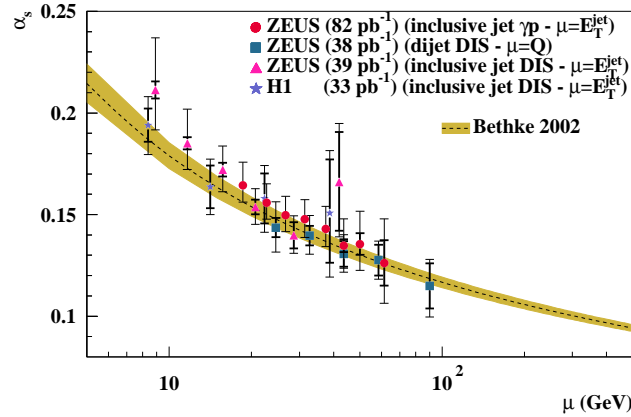


Figure 3. Various results on  $\alpha_s$  measurements in DIS as a function of a mass scale  $\mu$  compared with results from global fits.

### 2.1. Determination of $\alpha_s$

The dependency of a generic jet cross section on  $\alpha_s(M_Z)$  is parameterized in the corresponding analysis bins with the help of suitable NLO-QCD predictions featuring slightly different values of  $\alpha_s(M_Z)$ . By comparison of the parameterized cross section with the measured cross section the values for  $\alpha_s$  are obtained. The resulting  $\alpha_s(M_Z)$  from *e.g.* the single inclusive jet cross section for  $Q^2 > 500$  GeV is found in the ZEUS analysis to be

$$\alpha_s(M_Z) = 0.1212 \pm 0.0017(\text{stat.})_{-0.0031}^{+0.0023}(\text{exp.})_{-0.0027}^{+0.0028}(\text{theor.}).$$

The experimental error (exp.) is dominated by the uncertainty on the energy scale for the jet measurement. The largest contribution to the theoretical uncertainty (theor.) is given by a residual dependency on the renormalization scale  $\mu_r$  which corresponds to uncertainties due to the contributions of terms beyond next-to-leading order.

In Figure 3 the result is displayed as a function of a mass scale  $\mu$  together with other values of  $\alpha_s$  extracted from DIS-jet data <sup>2</sup>.

The expected running of  $\alpha_s$  as a function of  $\mu$  is clearly visible. In addition the figure demonstrates the compatibility of the resulting  $\alpha_s$  values with those obtained in global fits <sup>3</sup>.

### 3. Jet Substructure and Determination of $\alpha_s$

Jets appear as a collimated spray of particles which are combined to by dedicated algorithms. These particles are the end point of a cascade of successive particle emissions from the hard interaction to the hadronic final state.

The development of the cascade is governed by the strong coupling constant  $\alpha_s$ . An attempt is made to resolve subjets using dedicated algorithms within the identified jets<sup>4</sup>. The amount of subjets is expected to depend on  $\alpha_s$ . Fig. 4 shows the number of subjets as a function of the jet- $E_T$  measured in the laboratory frame. The number of subjets decreases as the transverse energy of the jet increases. The transverse energy of the jet sets the scale for  $\alpha_s$ . Thus, the probability to radiate partons is small at large transverse energies. The data are well described by NLO-QCD calculations employing different parton pdfs featuring slightly different values of  $\alpha_s(M_Z)$ . For  $E_T$  larger than 30 GeV the hadronization corrections become small allowing for a QCD analysis to determine  $\alpha_s$  from subjet multiplicites. The resulting value

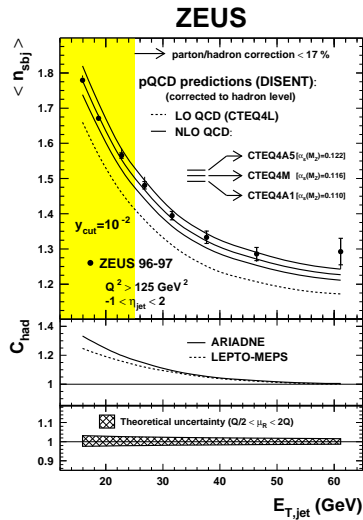


Figure 4. Subjet multiplicites for different transverse energies of jets. Jets were identified in the laboratory frame.

is found by ZEUS to be

$$\alpha_s(M_Z) = 0.1187 \pm 0.0017(\text{stat.})_{-0.0009}^{+0.0024}(\text{exp.})_{-0.0076}^{+0.0093}(\text{theor.}).$$

### 4. 3-jet Cross Sections

3-jet cross sections are well suited for an extraction of  $\alpha_s$  because the lowest order contribution to this event class is proportional to  $\alpha_s^2$ . The sensitivity to uncertainties due to proton pdf's can be reduced by building the ratio  $R_{3/2}$ , *i.e.* the ratio of 3-jet to dijet cross sections. A measurement of this observable is shown in Fig. 5. While a minor sensitivity to variations of the pdf's is observed the ratio is very sensitive to small variations of  $\alpha_s$  which underlines the potential of this observable for future determinations of  $\alpha_s$ .

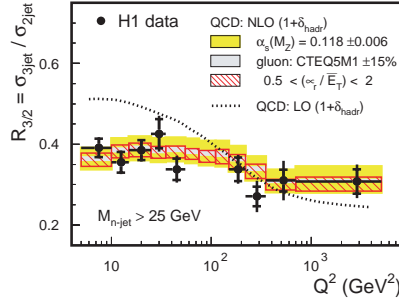


Figure 5. The observable  $R_{3/2}$  as a function of  $Q^2$  compared with NLO-QCD predictions.

### 5. Conclusion and Outlook

The analysis of jet events in DIS allows for precise measurements of the strong coupling constant  $\alpha_s$ . A compilation of results is given in Fig. 6. They have a major impact on the current world average value of  $\alpha_s$ . Ongoing analysis of HERA I <sup>6</sup> data as well as new data expected from HERA II open the possibility for  $\alpha_s$  determinations including 3-jet cross sections.

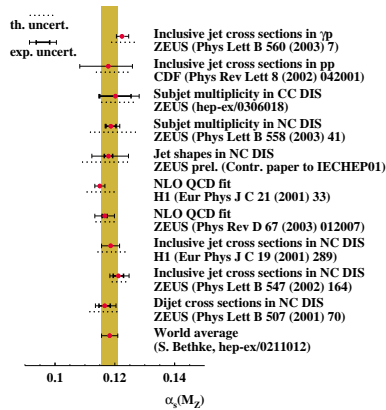


Figure 6.  $\alpha_s(M_Z)$  values obtained in DIS together with results from  $p\bar{p}$ -collisions and the world average.

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