



Hadron Structure 2004  
Smolenice Castle, Slovakia

# Measurements of proton structure at low $Q^2$

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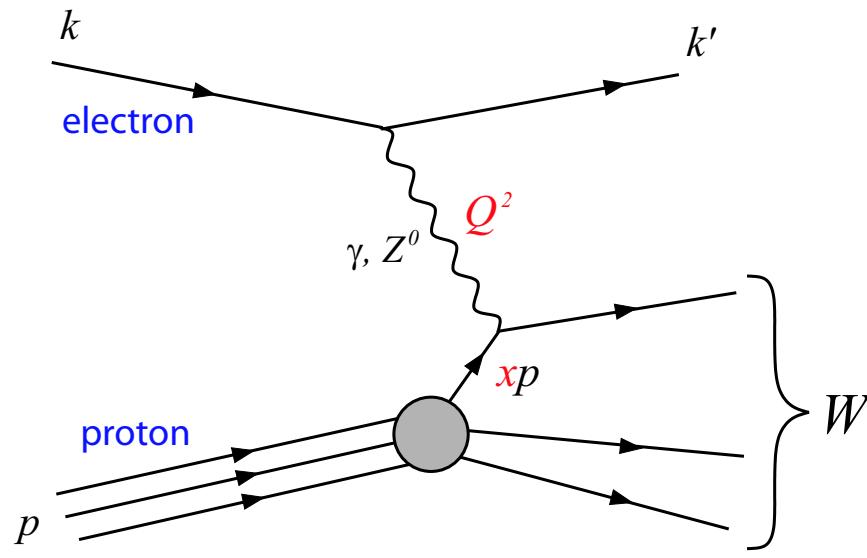
University of Dortmund



- ◆ Introduction
- ◆  $F_2$  Measurement at large  $x$
- ◆  $F_L$  Determination
- ◆ Summary

# Deep Inelastic Scattering

**Neutral Current:**  $e + p \rightarrow e + X$



◆ kinematic variables:

$$s = (p + q)^2 \quad \text{cms energy}$$

$$Q^2 = -(p - k)^2 \quad \text{momentum transfer}$$

$$x = \frac{Q^2}{2p \cdot q} \quad \text{Bjorken-variable}$$

◆ additional information

$$y \simeq \frac{Q^2}{sx} \quad \text{Inelasticity}$$

$$W^2 = Q^2 \frac{1-x}{x} + m_p^2 \quad \begin{matrix} \text{cms energy in} \\ \gamma^* p \text{ system} \end{matrix}$$

# Structure functions in DIS

Measuring the cross section:

$$\frac{d^2\sigma}{dxdQ^2} = \frac{2\pi\alpha^2}{Q^4x} \left( Y_+ F_2(x, Q^2) - y^2 F_L(x, Q^2) \right) \quad Y_+ = 1 + (1 - y)^2$$

$F_2$  is measured,  $F_L$  is extracted

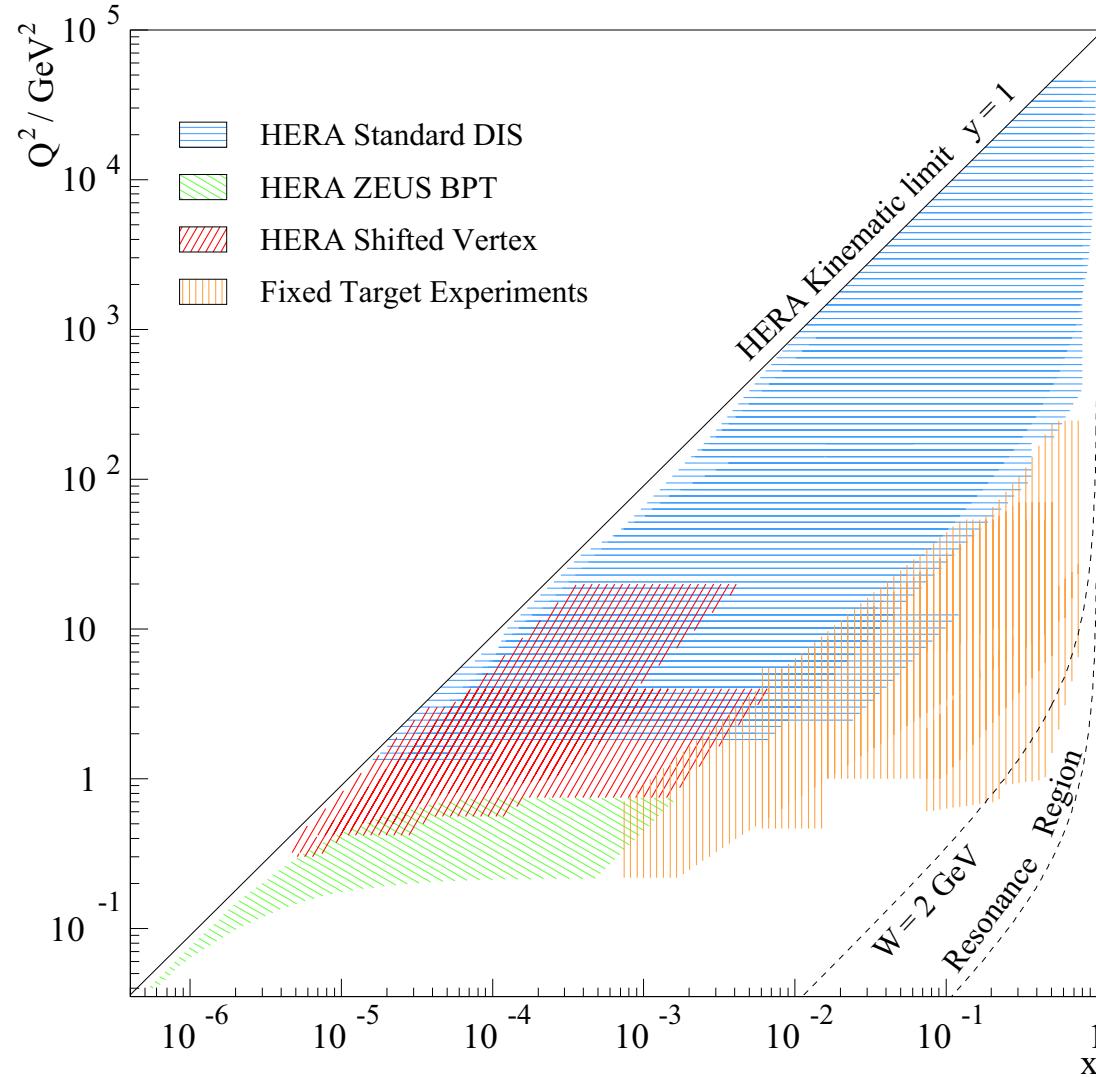
- ◆  $F_2(x, Q^2) = x \sum_i e_i^2 [q_i(x, Q^2) + \bar{q}_i(x, Q^2)]$

- ▶ Dominates the low  $y$  region
- ▶ Sensitive to quark content

- ◆  $F_L(x, Q^2)$

- ▶ Contributes only at high  $y$
- ▶ QPM:  $F_L = 0$
- QCD:  $F_L \neq 0$  (gluon emission)

# Kinematic Plane



*Medium-High  $Q^2$*

*asymptotic freedom*  
*perturbative QCD*

*Low  $Q^2$*

*Transition to  $\gamma p$*

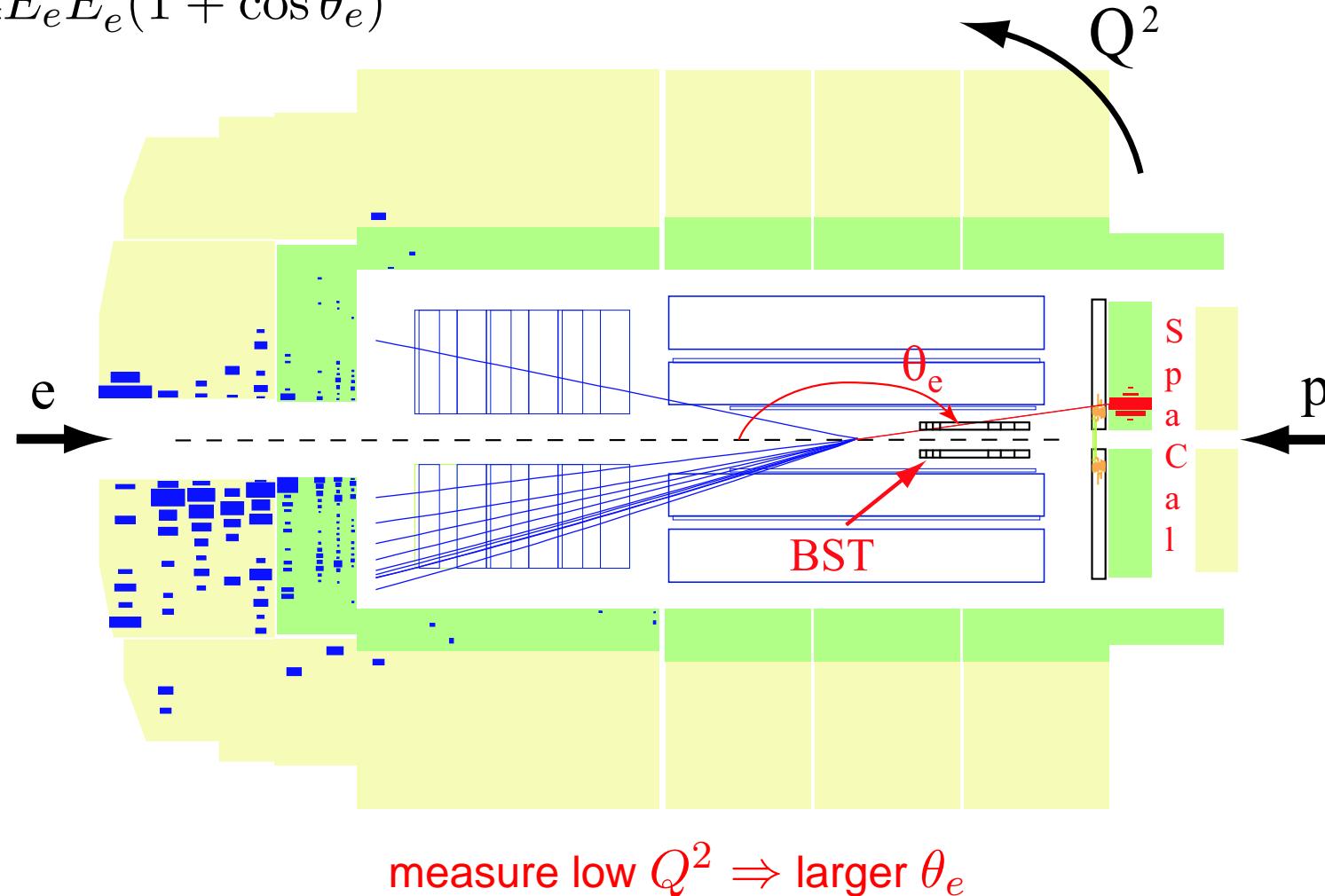
*$\alpha_s(Q^2)$  large:*

*Phenomenological models*

# Experimental techniques at low $Q^2$

Standard DIS measurement:  $Q^2 \geq 2\text{GeV}^2$

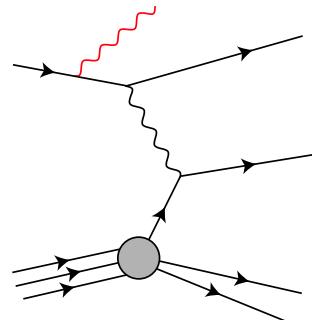
$$Q^2 = 4E_e E'_e (1 + \cos \theta_e)$$



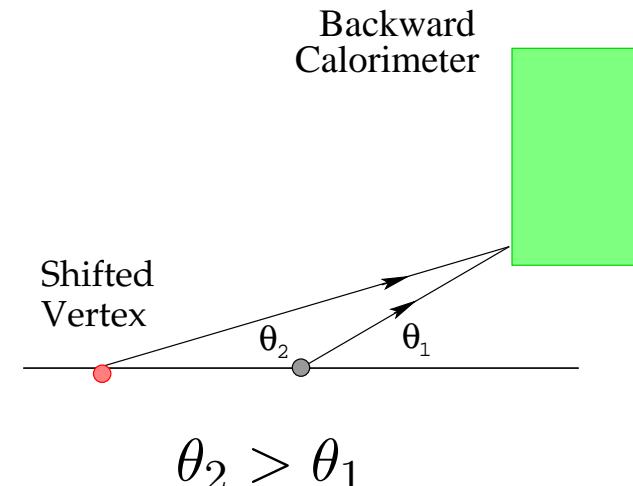
# Experimental techniques at low $Q^2$

Measuring **large** scattering angles  $\Rightarrow$

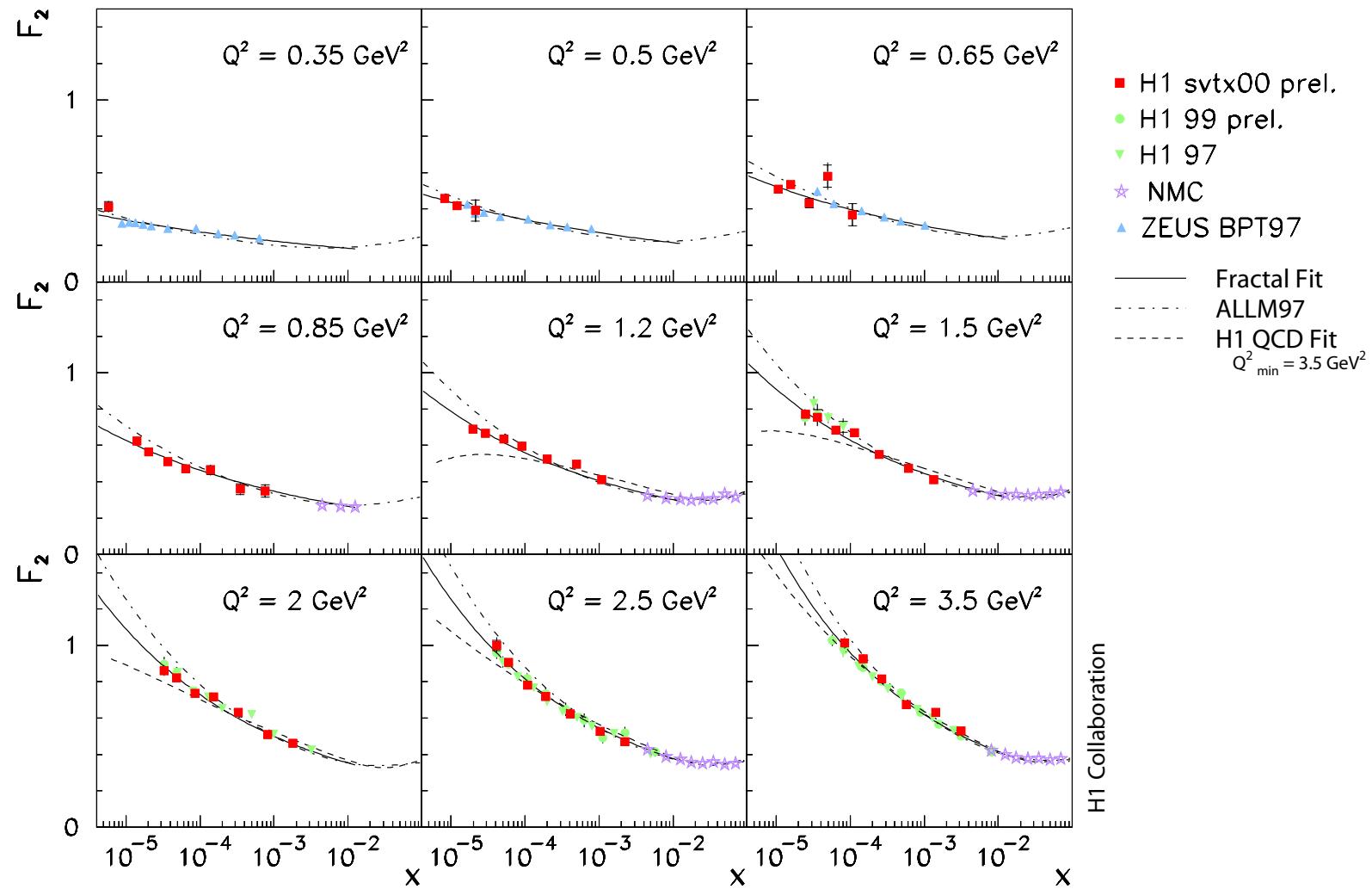
- ◆ Detectors close to the beam pipe (ZEUS BPC/BPT)
- ◆ Radiative events



- ◆ Shifted vertex runs

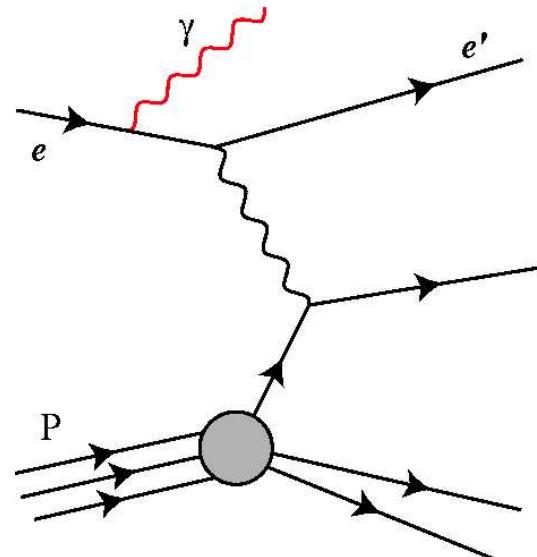


# Shifted Vertex $F_2$ Measurements



# ISR Measurement Method

*Signature:*

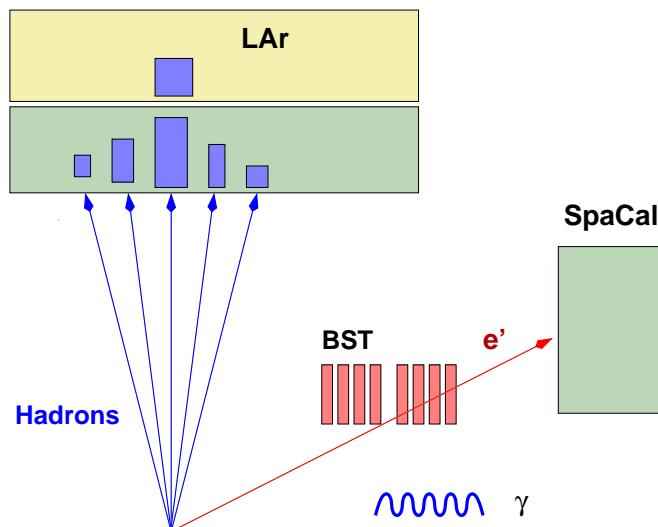


$\gamma$  emitted from incoming  $e$ :

- ◆ cms is reduced  $\Rightarrow$  accessing the **high  $x$**  region is possible!
- ◆ Alternative ISR  $F_2$  analysis:  
 *$\gamma$  explicitly detected*

*New method:*

- ◆  $\gamma$  is undetected
- ◆  $x, Q^2, E_e$  reconstructed:
  - ★ final state
  - ★ energy momentum conservation



# ISR Measurement in Shifted Vertex run

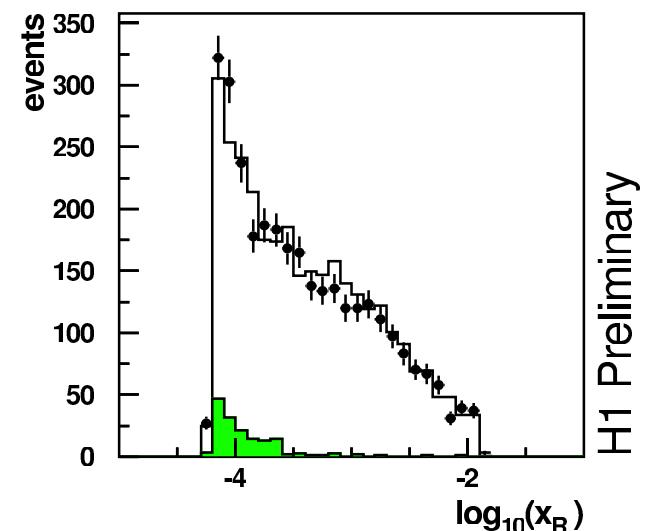
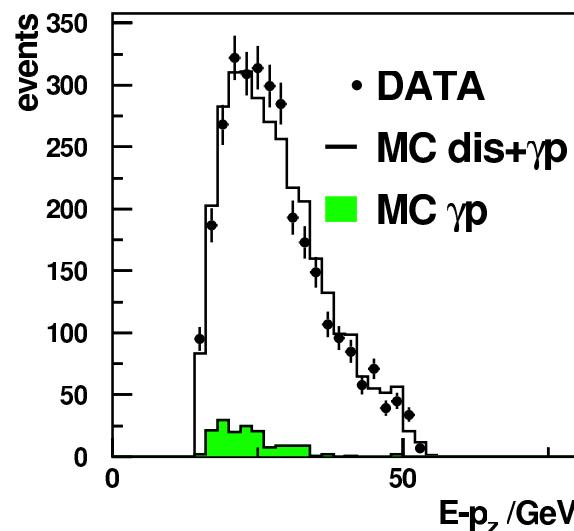
Reminder:  $\Sigma$ —method

- ◆ Incoming energy:

$$2E_e = (E - P_z)_{tot}$$

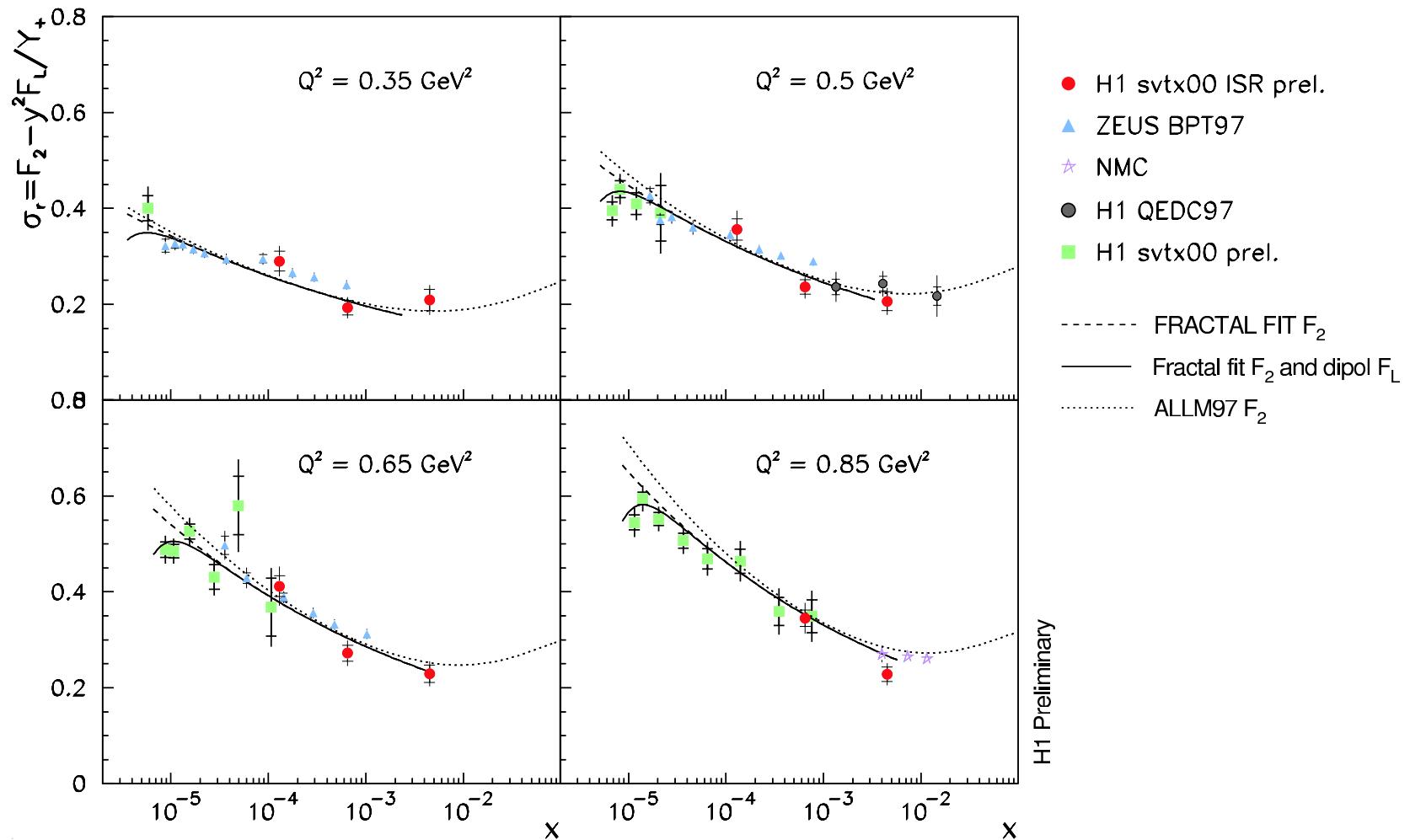
- ◆ Kinematic:

$$X_R = \frac{Q_\Sigma^2}{4E_e E_p}$$



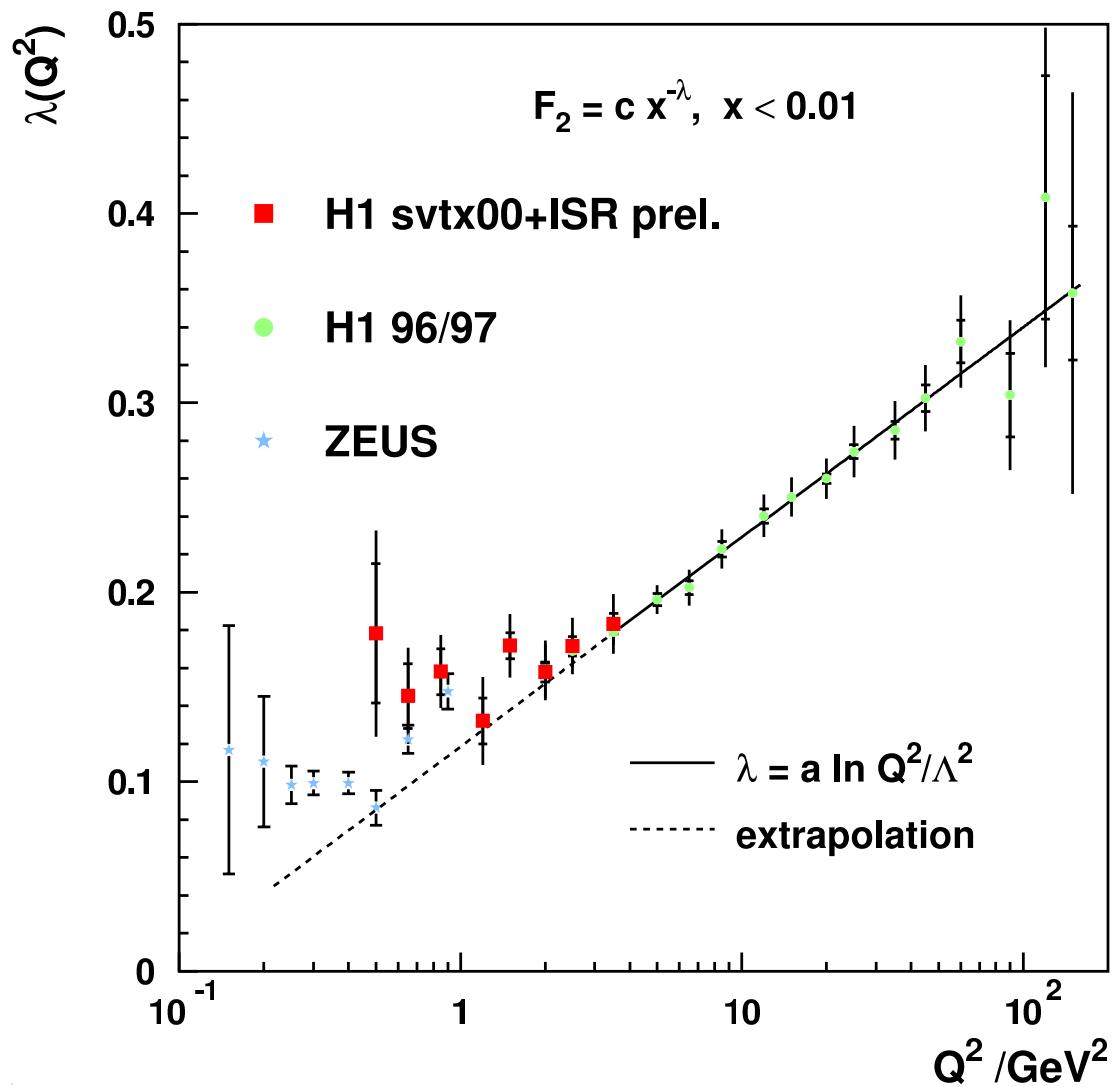
**BST  $\Rightarrow$  suppression of  $\gamma p$  background**

# Cross Section Measurement using ISR events



high  $x$  at low  $Q^2$  is accessed

## Improved extractions of $\lambda$



$$\lambda = \left( \frac{\partial \ln F_2}{\partial \ln x} \right)_{Q^2}$$

► Rise of  $F_2$  at  $x < 10^{-2}$

well parametrized by

$$F_2 = c(Q^2)x^{-\lambda(Q^2)}$$

► At  $Q^2 \geq 3 \text{ GeV}^2$ :

$$\lambda \approx \ln Q^2 \quad c \approx \text{const}$$

*Partonic degrees of freedom*

► At  $Q^2 \leq 2 \text{ GeV}^2$ :

$$\lambda \rightarrow 0.08$$

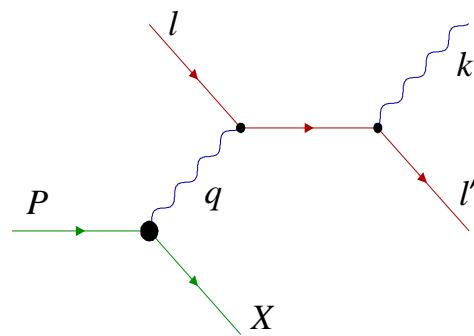
*Transition to hadronic degrees  
of freedom*

# Inelastic QED-Compton events

Signature:

- ★  $e + p \rightarrow e + \gamma + X$

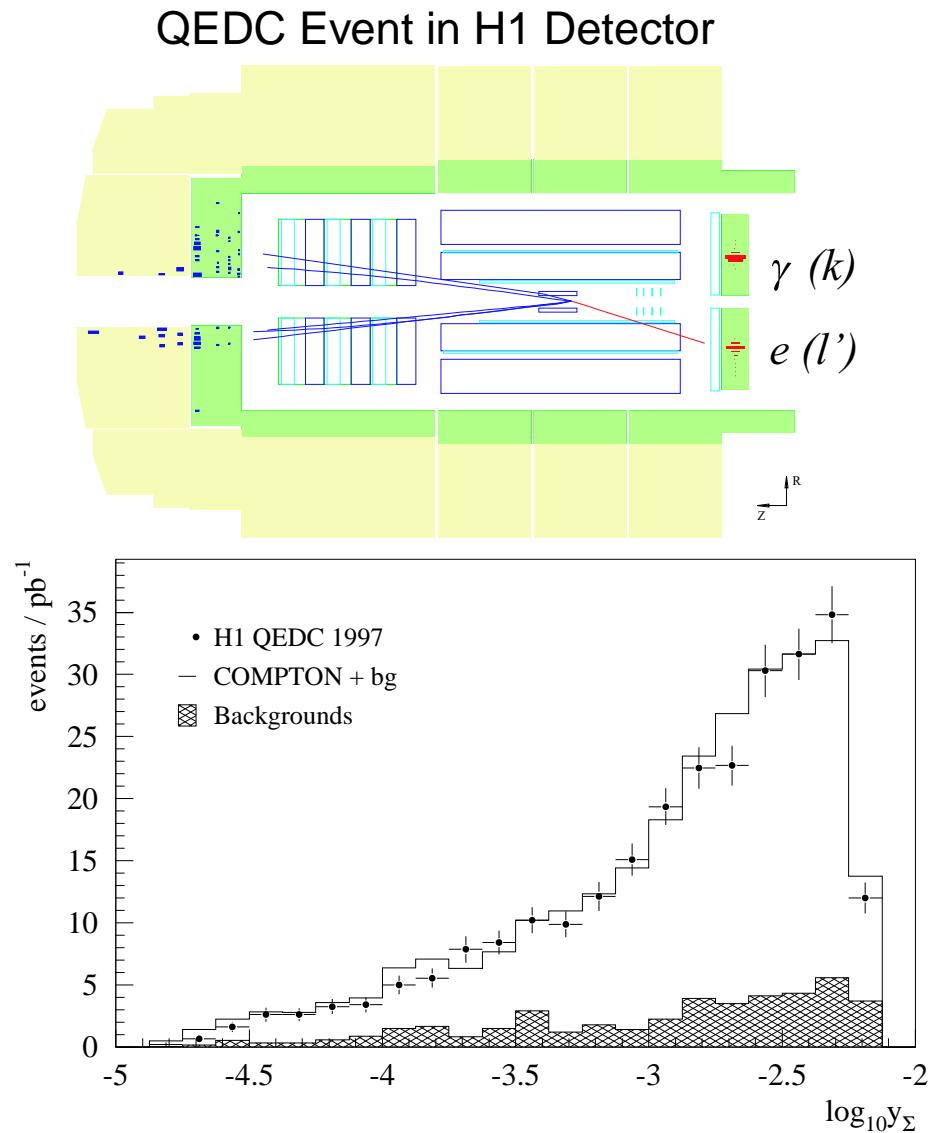
- ★  $\vec{q} \parallel \vec{l}$



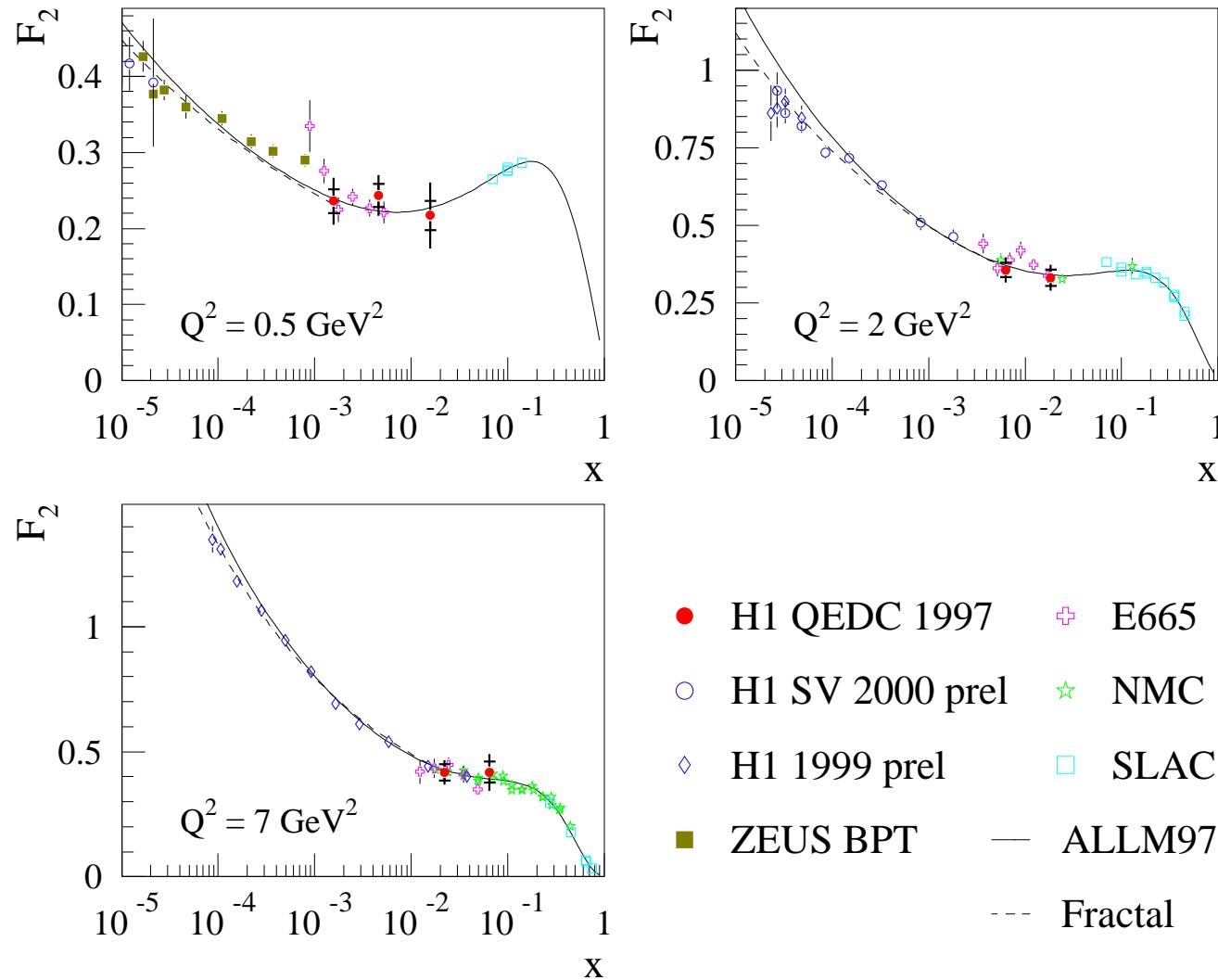
*Medium-High  $x$  is measured*

$$x\epsilon(0.001 - 0.06)$$

- ▶ understanding of HFS at low  $W$
- ▶ Use SOPHIA MC model



# $F_2$ measurement with QED-Compton events

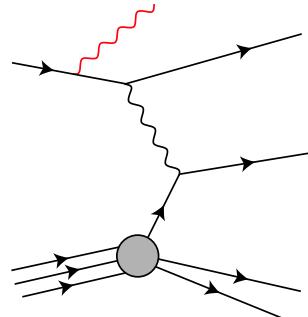


Good agreement with fixed target experiments

## Measurement of $F_L$

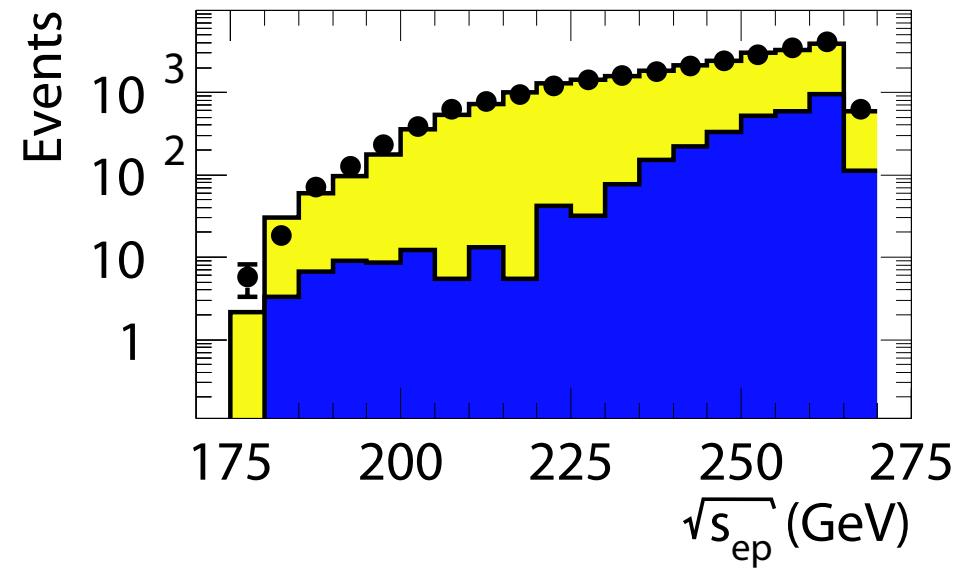
$$\frac{d^2\sigma}{dxdQ^2} = \frac{2\pi\alpha^2}{Q^4x} \left\{ \left[ 1 + (1-y)^2 \right] F_2(x, Q^2) - y^2 F_L(x, Q^2) \right\}$$

- ▶  $F_L$ : contribution to  $\sigma$  only at high  $y$
- ▶ Direct measurement requires data at different  $s$
- ▶ Using ISR events:

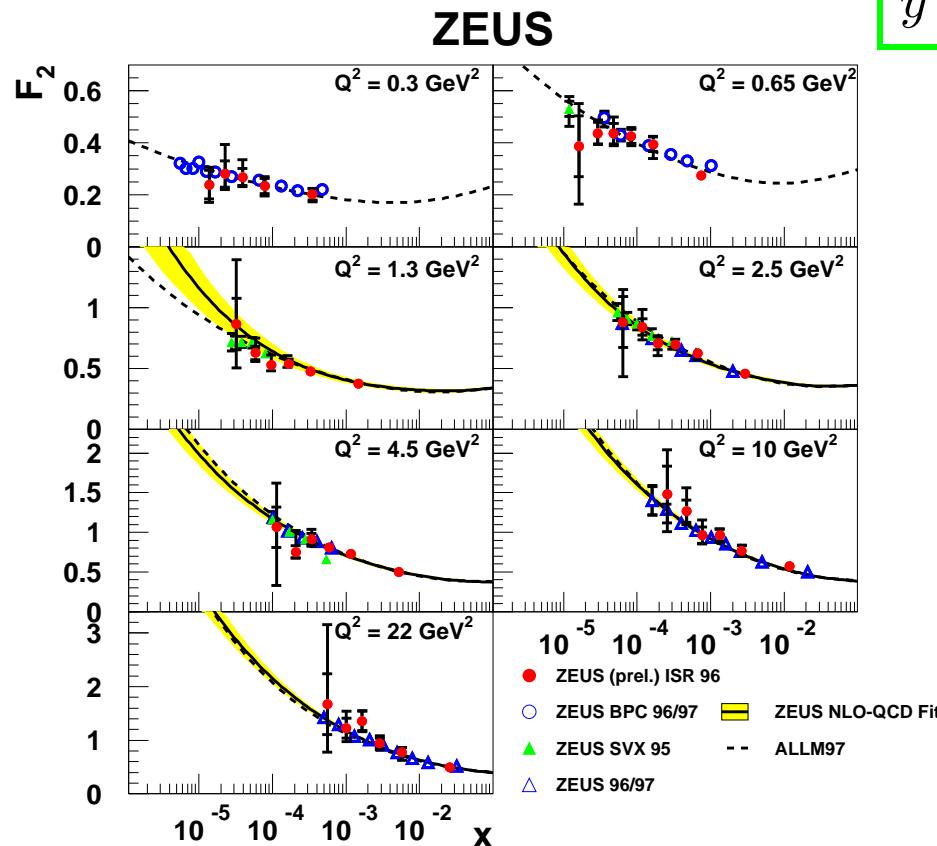


At fixed  $Q^2, x$

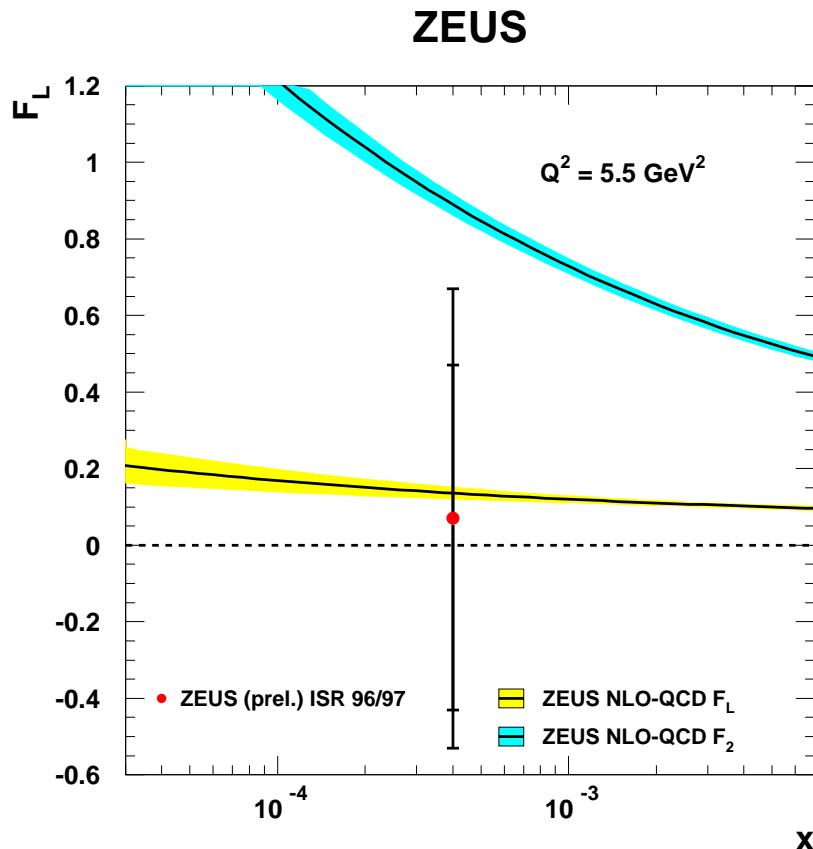
*varying  $s \Rightarrow y$  vary*



# Measurement of $F_L$



$$y = 0.11 - 0.23 \quad Q^2 = 1 - 30 \text{ GeV}^2$$



- Ratio  $N_{data}/N_{MC}(F_L = 0)$  is analysed  $\Rightarrow F_L$

First **direct** determination of  $F_L$  from ISR  
result is consistent with QCD

## Extraction of $F_L$

$$\frac{d^2\sigma}{dxdQ^2} = \frac{2\pi\alpha^2Y_+}{Q^4x} \sigma_r \quad \sigma_r = F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2)$$

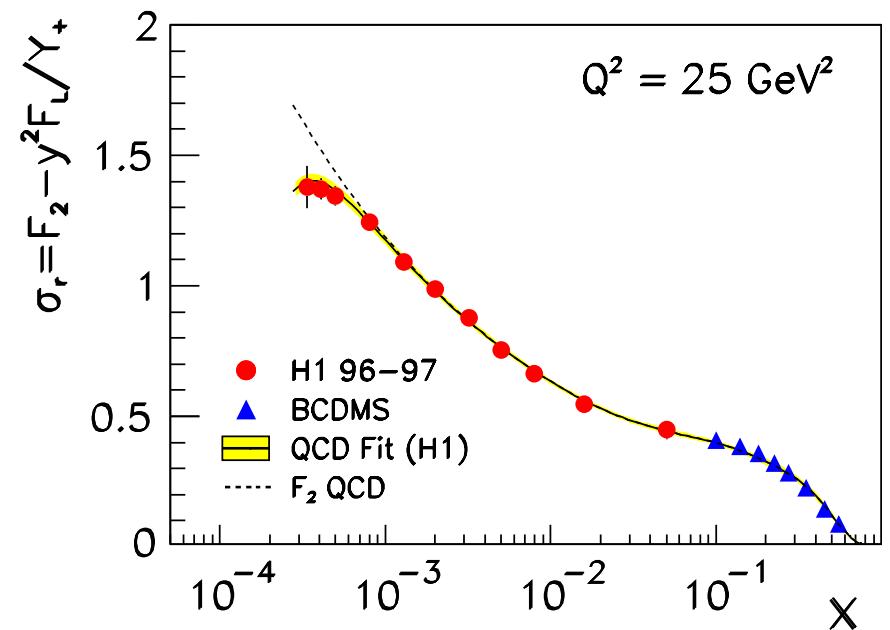
► Indirect determination:

*extrapolating  $F_2$  to higher  $y$*

$$F_L \propto F_2 - \sigma_r$$

→ Derivative method

→ Shape method

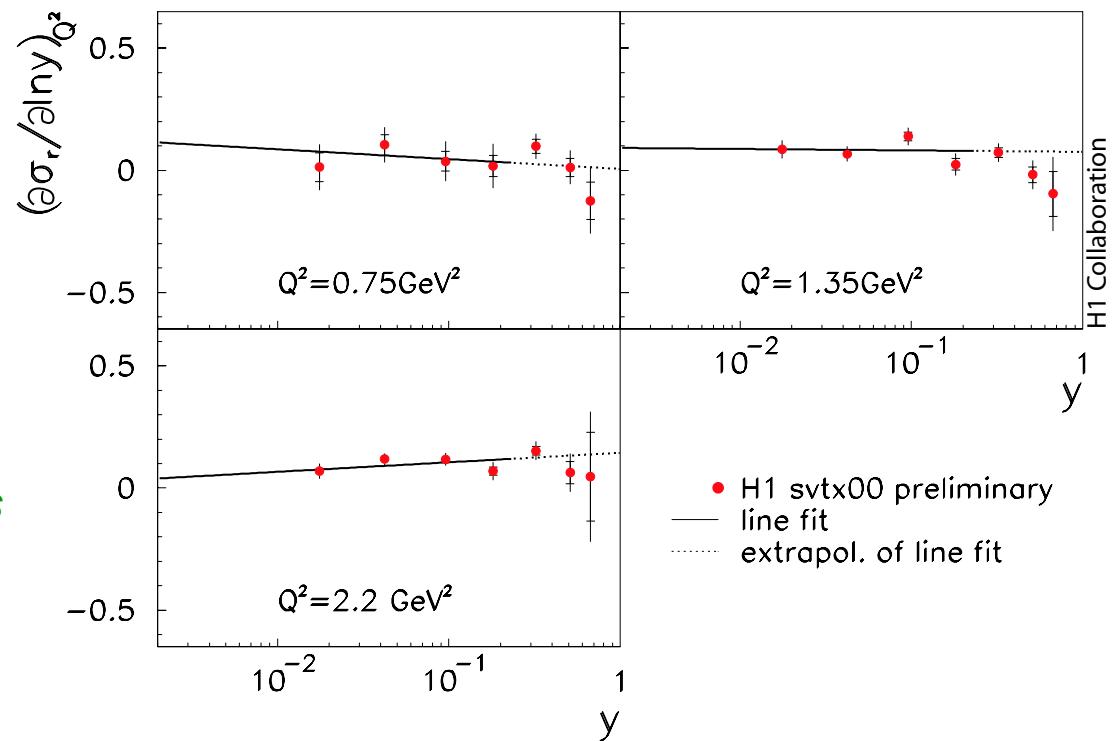


## $F_L$ extraction: Derivative method

$$\left( \frac{\partial \sigma_r}{\partial \ln y} \right)_{Q^2} = \left( \frac{\partial F_2}{\partial \ln y} \right)_{Q^2} - \frac{2y^2(2-y)}{1+(1-y)^2} F_L$$

- ◆ straight line fits:  
low  $y < 0.2$  points
- ◆ linear behaviour of  $F_2$  at high  $y$

$F_L$ : deviation of measured points  
from linear behaviour at high  $y$



## $F_L$ extraction: Shape method

$$\sigma_{fit} = cx^{-\lambda} - \frac{y^2}{1+(1-y)^2} F_L$$

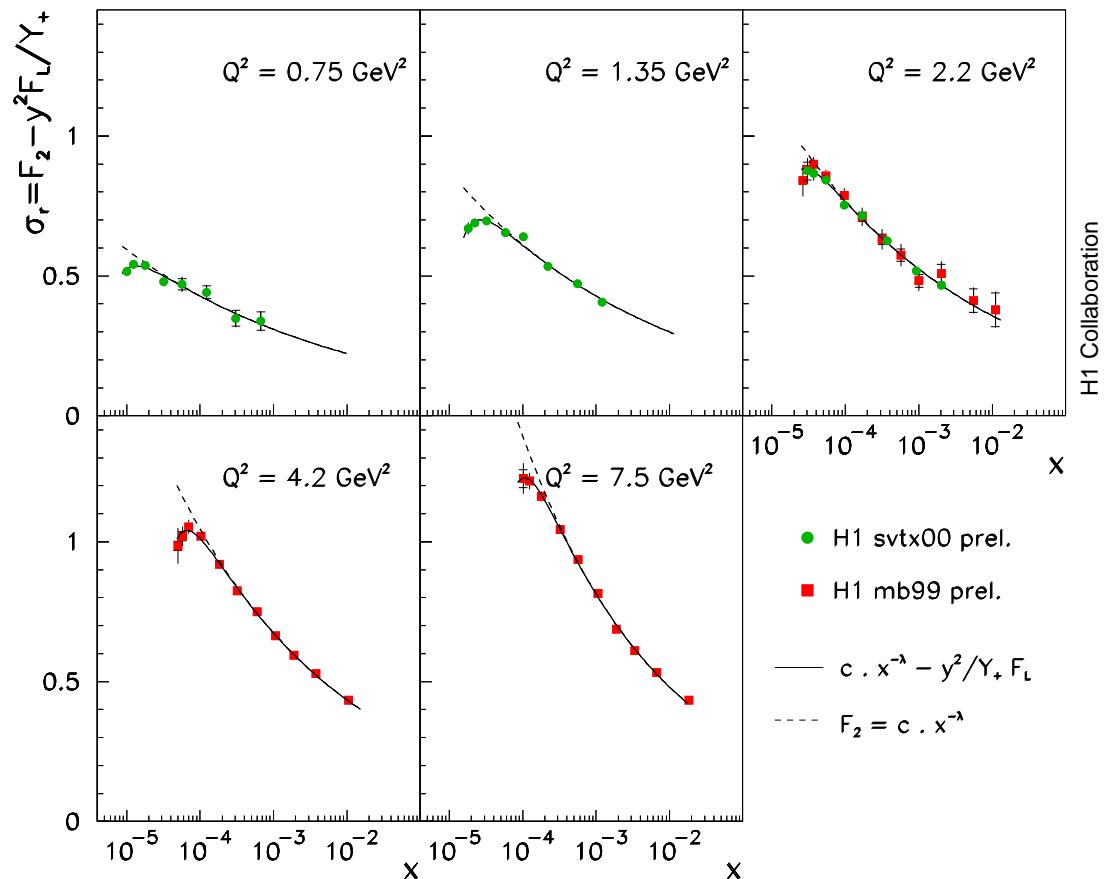
◆ at high  $y$ :

$$\frac{y^2}{1+(1-y)^2}$$

dominates the shape of  $\sigma_r$

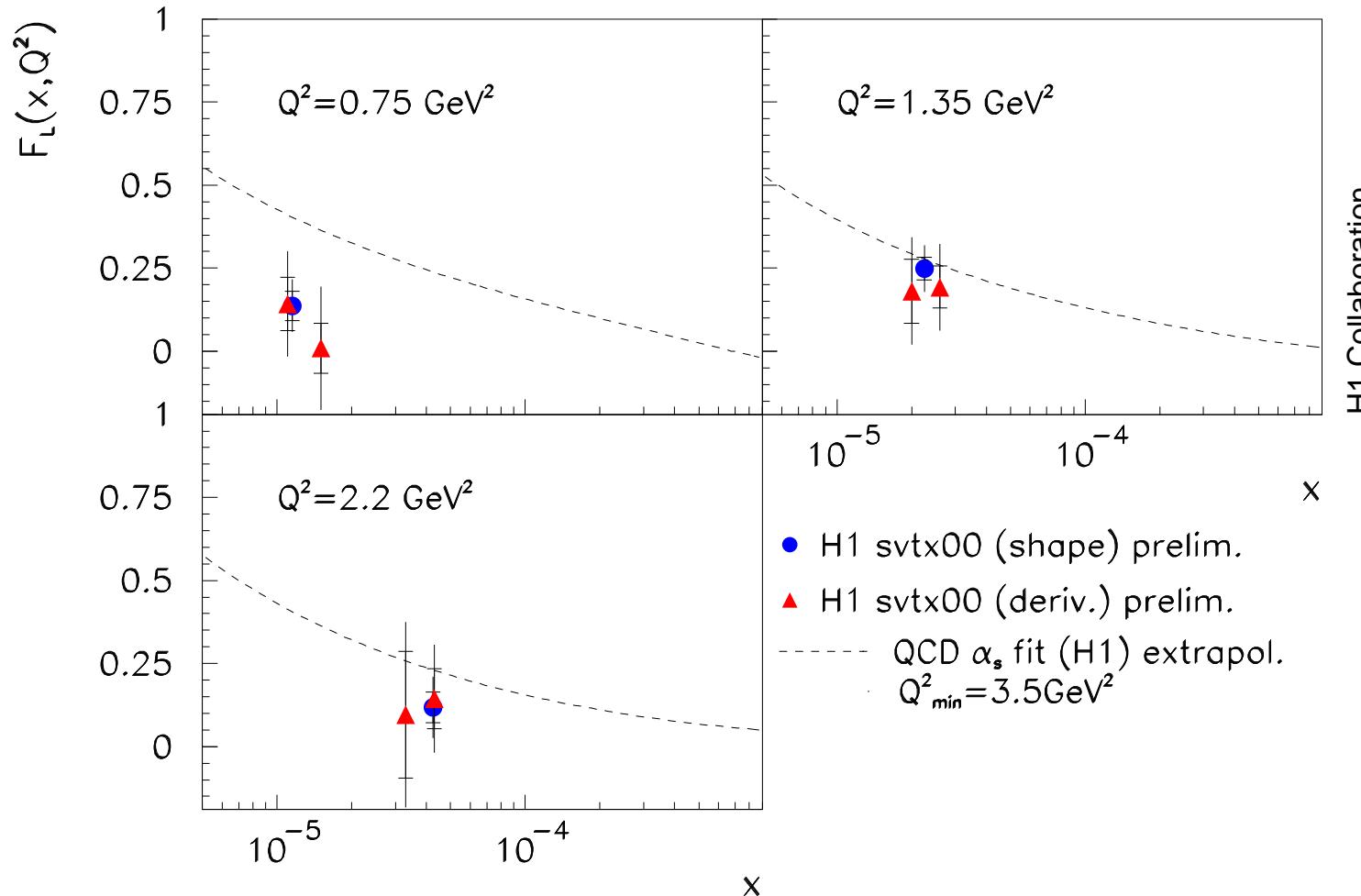
◆  $F_L = F_L(Q^2)$

$F_L$ : extracted from  $\sigma_{fit}$



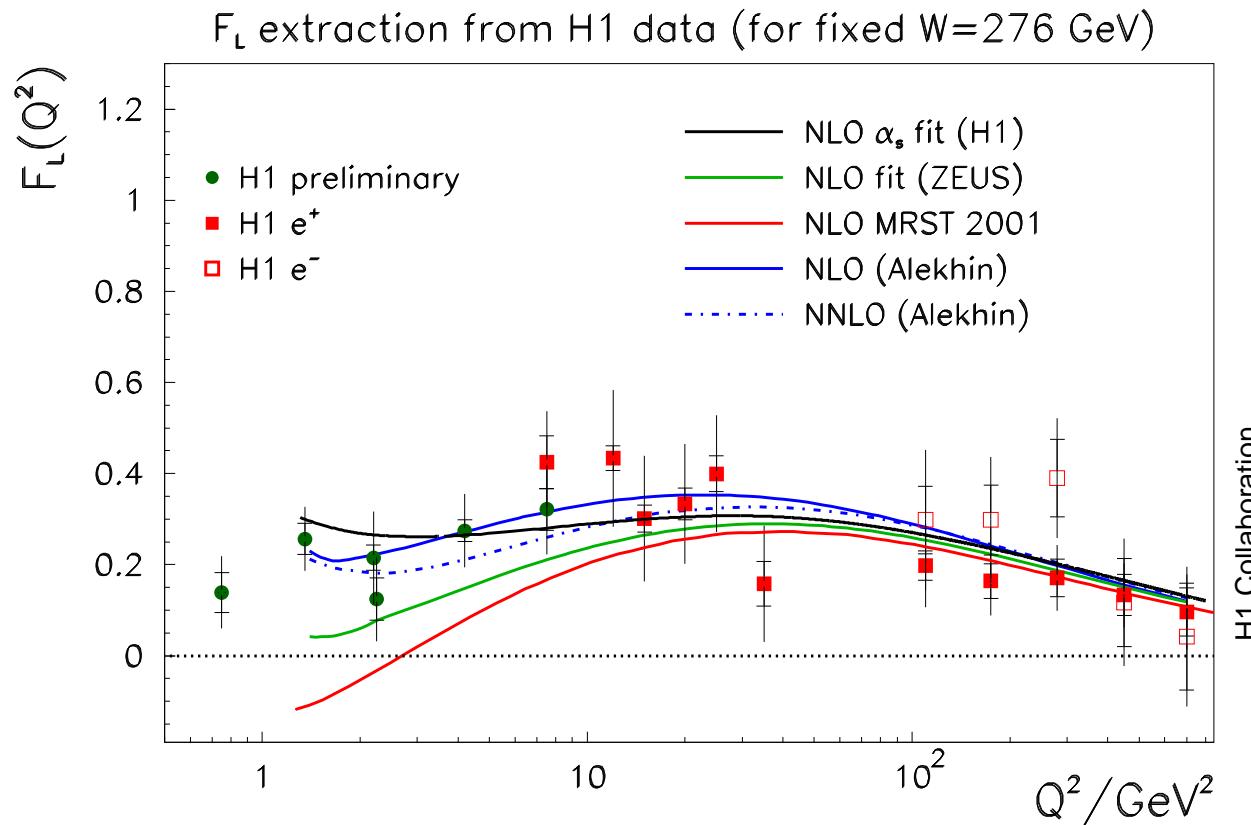
*good agreement with measured cross section*

## Shape method vs. Derivative method



Shape method: more precise

# $F_L(Q^2)$ at Fixed $y = 0.75$



- ◆ New constrains from low  $Q^2$  data
- ◆ Agreement with NLO pQCD fits
- ◆ H1 non-negligible positive  $F_L$  at low  $Q^2 \Rightarrow$  positive  $g$

# Summary

- ◆  $F_2$  is measured with *two new methods*

- ◆ *QECD:*

$$Q^2 \rightarrow 0.1 \text{ GeV}^2 \quad 0.001 \leq x \leq 0.1$$

- ◆ *ISR:*

$$0.35 \leq Q^2 \leq 0.85 \text{ GeV}^2 \quad 10^{-4} \leq x \leq 5 \cdot 10^{-3}$$

- ◆ *Structure function  $F_L$*

- ◆ *Measured with ISR*

- ◆ *Extracted with Derivative and Shape method*

- ◆  $F_L(Q^2)$  at  $W = 276 \text{ GeV}$

→ *non-negligible positive  $F_L$  at low  $Q^2$*